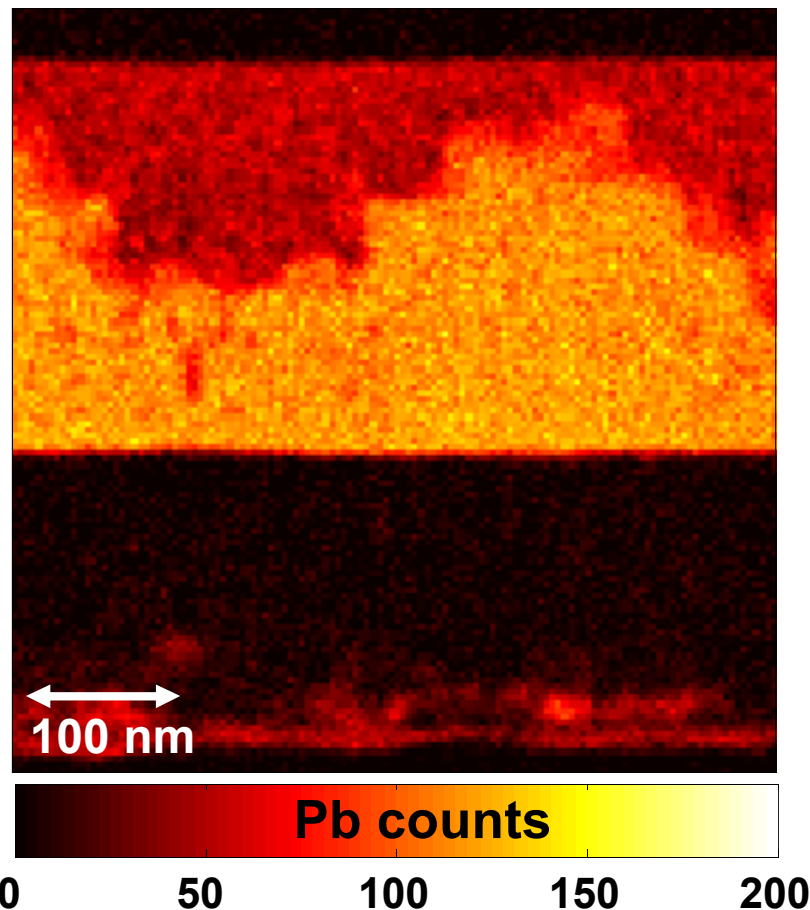


Quantitative X-ray spectrum imaging in $(\text{Pb},\text{La})(\text{Zr},\text{Ti})\text{O}_3$

SAND2008-3713P



Chad Parish

Collaborators:

Geoff Brennecke

Bruce Tuttle

Luke Brewer

Acknowledgements:

Michael Rye

Garry Bryant

Paul Kotula

Joe Michael

Thin-film P(L)ZT ferroelectrics are important for capacitor applications

$\text{Pb}(\text{Zr},\text{Ti})\text{O}_3$ and $(\text{Pb},\text{La})(\text{Zr},\text{Ti})\text{O}_3$:

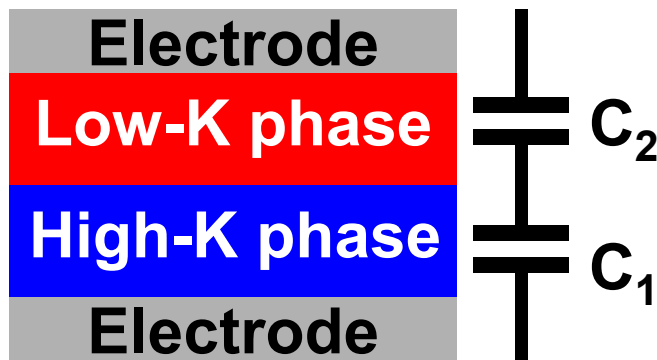
High-dielectric-constant (K) ferroelectrics for multilayer thin films

→ Referred to as PZT and PLZT

Multiple phases can form during processing

Act as series capacitors

→ Loss of overall capacitance of device



$$C_{\text{TOTAL}} \propto \frac{1}{\frac{1}{C_1} + \frac{1}{C_2}}$$

Lowest capacitance value dominates device performance!

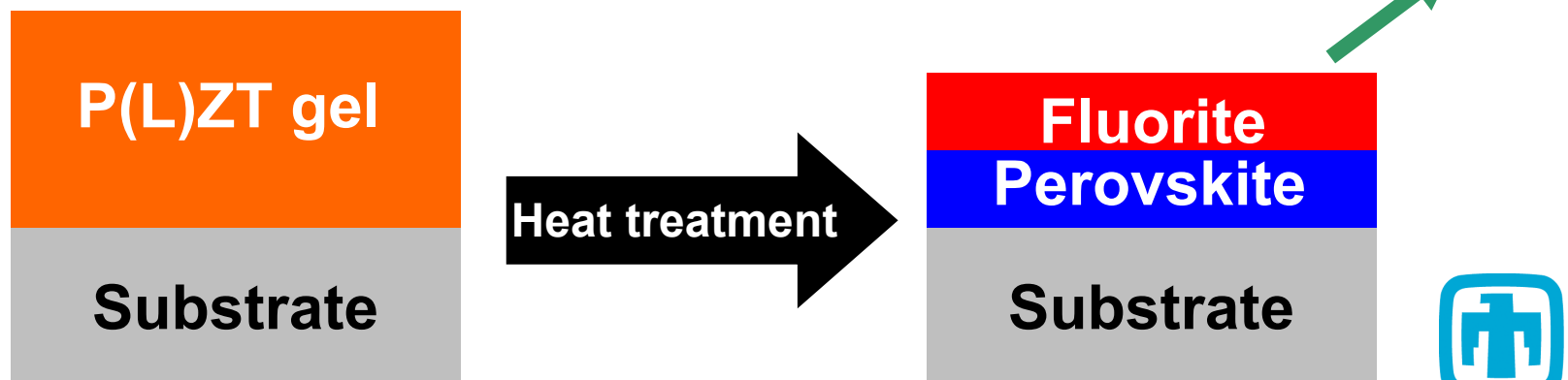
PbO volatility can result in poor film quality

Only the perovskite phase of P(L)ZT has high K

Perovskite is intolerant of Pb non-stoichiometry

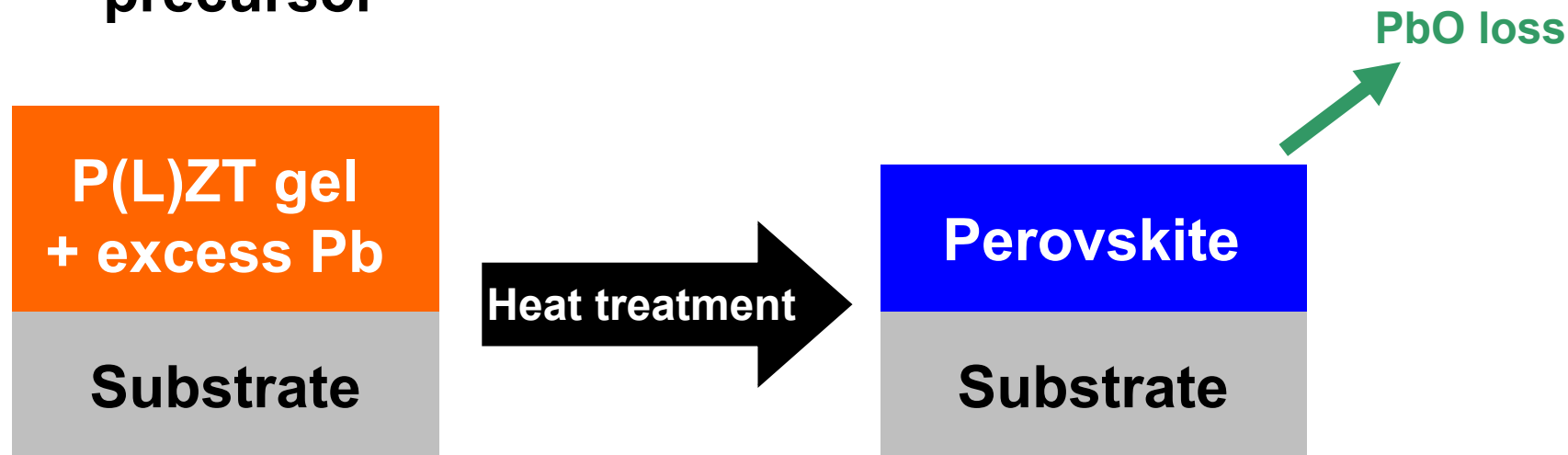
When Pb-deficient, fluorite phase forms, with poor dielectric properties

PbO is volatile → lost during processing
→ mixed-phase films with low K-values



Excess Pb avoids fluorite formation, but has detrimental effects

Typically, 10+% excess Pb is added to the precursor



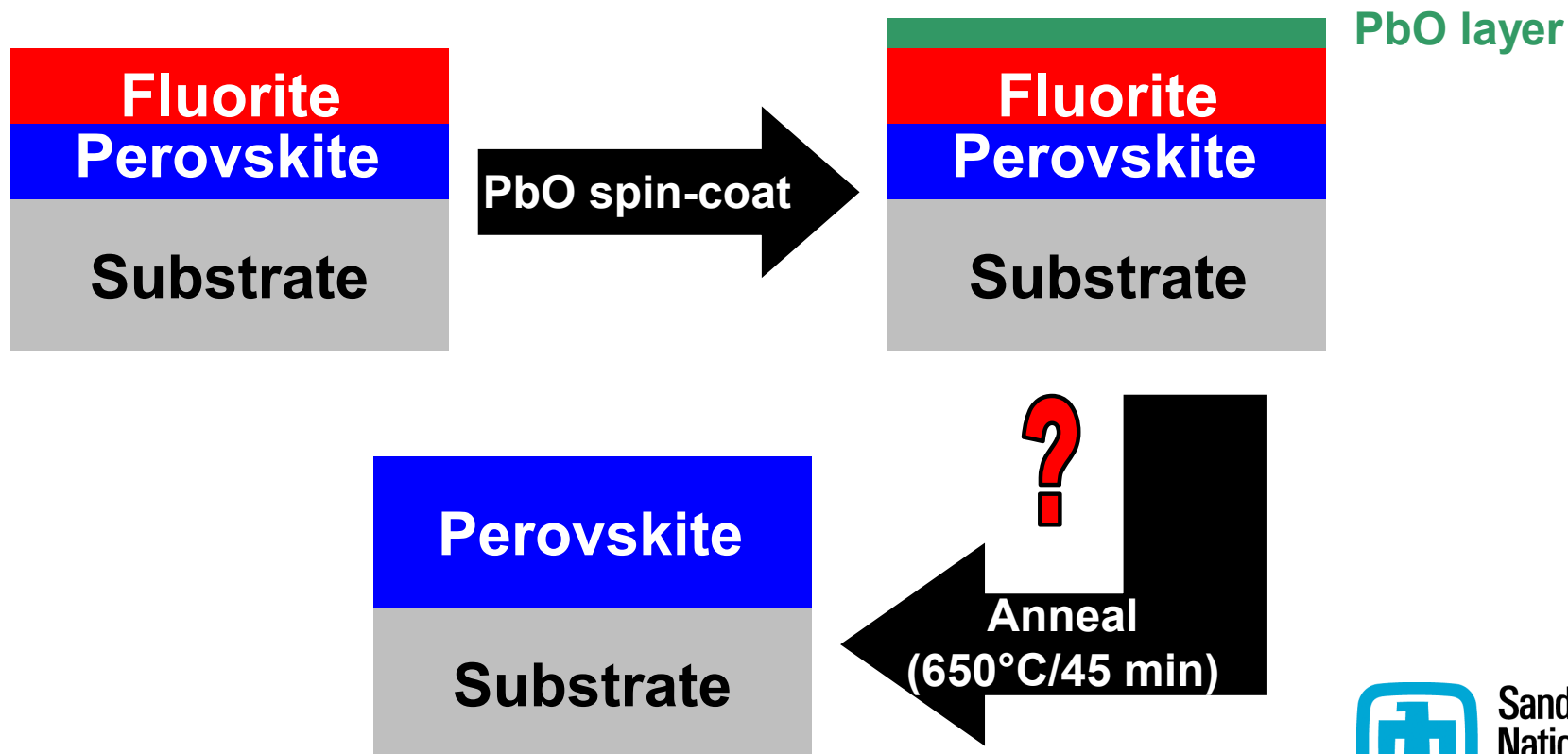
Thinner films require more Pb excess, which interacts with the electrode and substrate

Can we produce single-phase perovskite P(L)ZT without excess Pb?



Will annealing crystallized films under a PbO solution restore the desired phase?

Hypothesis: *If we coat mixed-phase perovskite + fluorite films with PbO solution and anneal, the fluorite will convert to the desired perovskite phase*



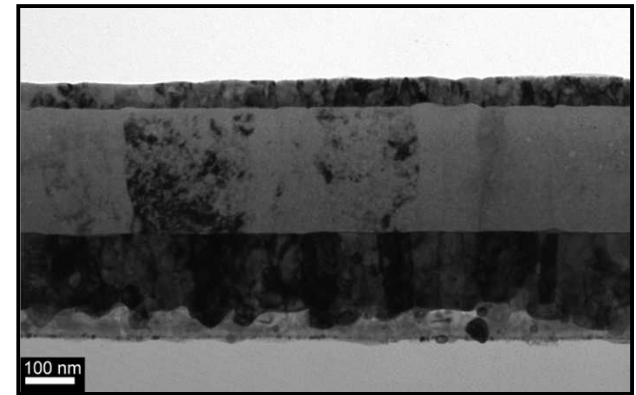
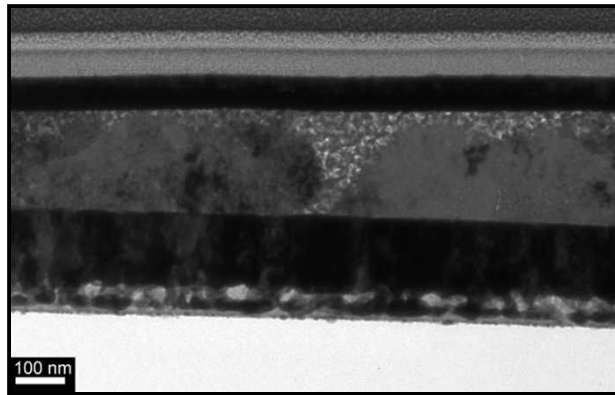


Microscopy shows mixed-phase structures converted to single-phase

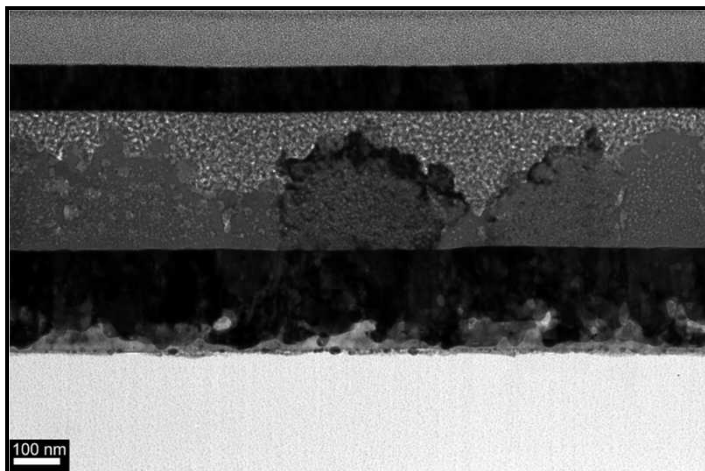
Before overcoat+anneal

After overcoat+anneal

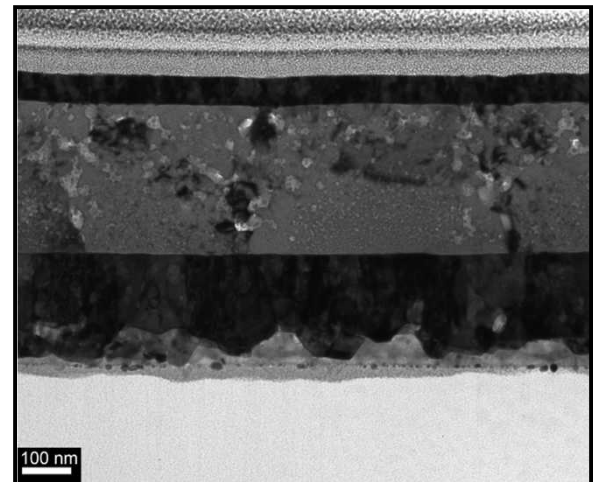
PZT 53/47



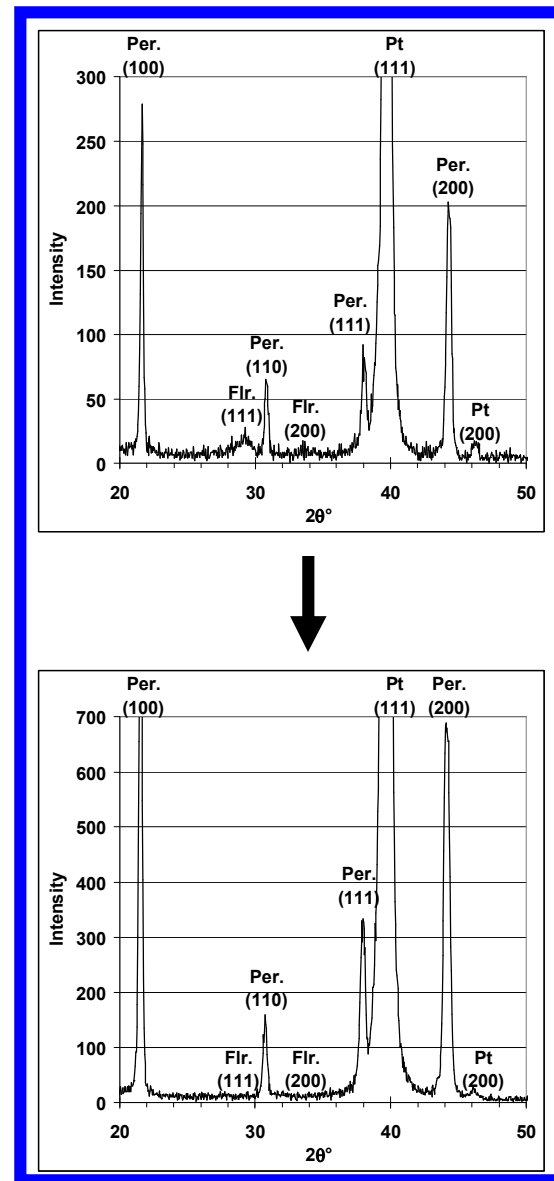
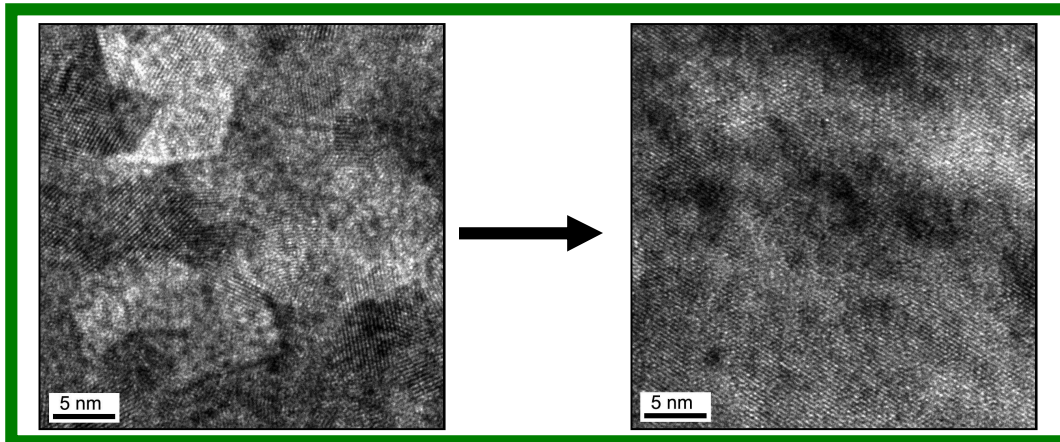
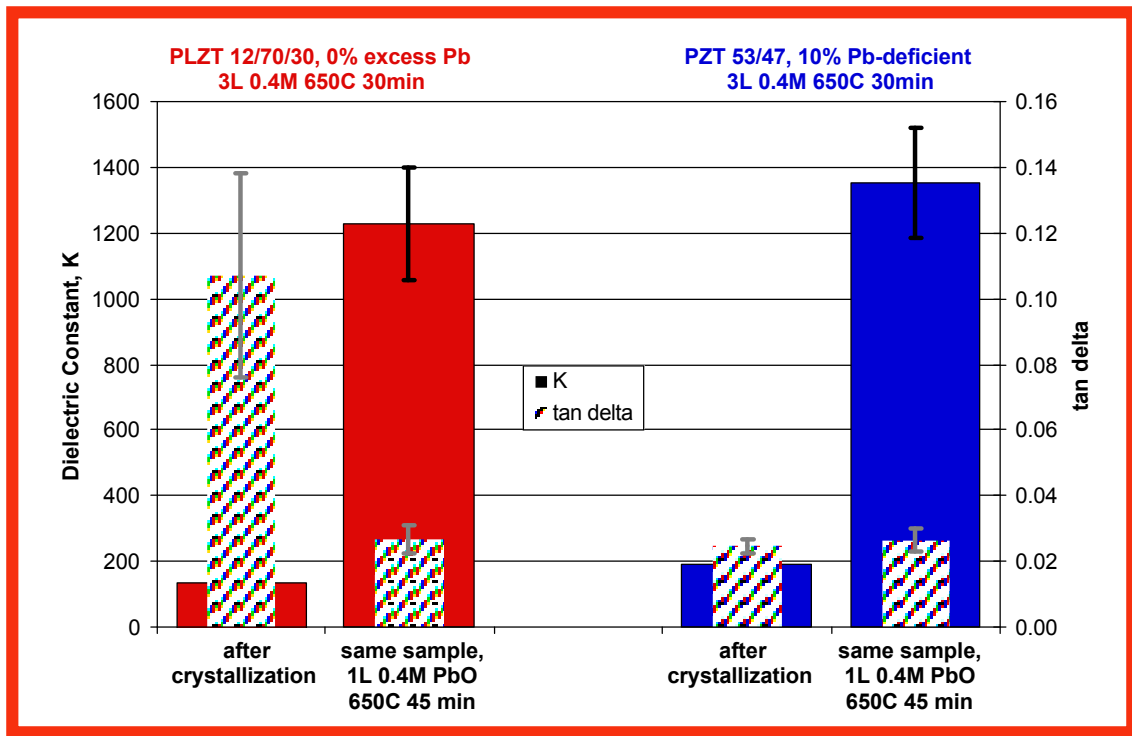
PLZT
12/70/30



FIB-Pt
Pt
Film
Pt
Ti
SiO₂

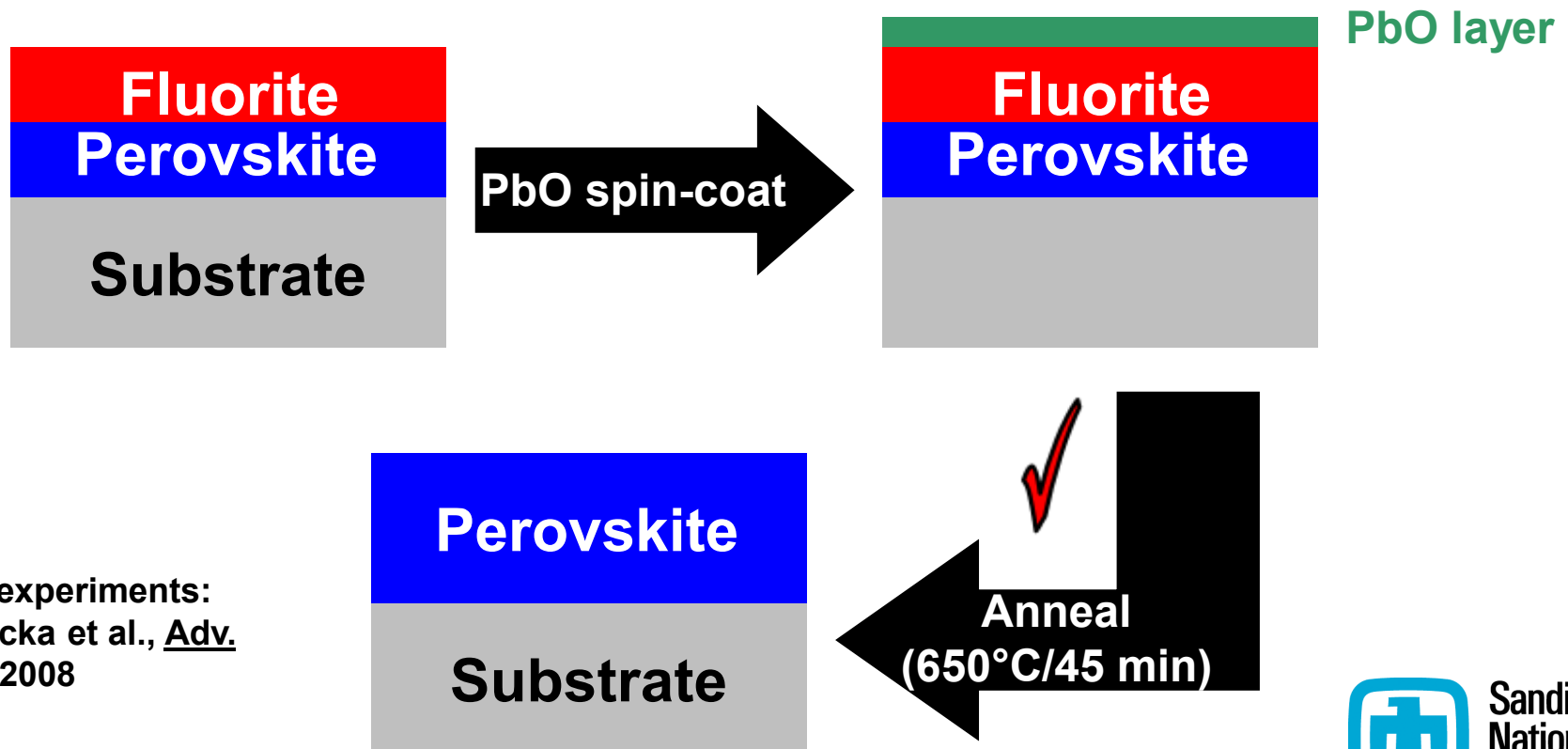


XRD, HREM, and electrical properties confirm the hypothesis



XRD, HREM, and electrical properties confirm the hypothesis

Hypothesis: *If we coat mixed-phase perovskite + fluoride films with PbO solution and anneal, the fluoride will convert to the desired perovskite phase*



Above experiments:
Brennecke et al., Adv. Mater., 2008



We've characterized the structure – but what about the chemistry?

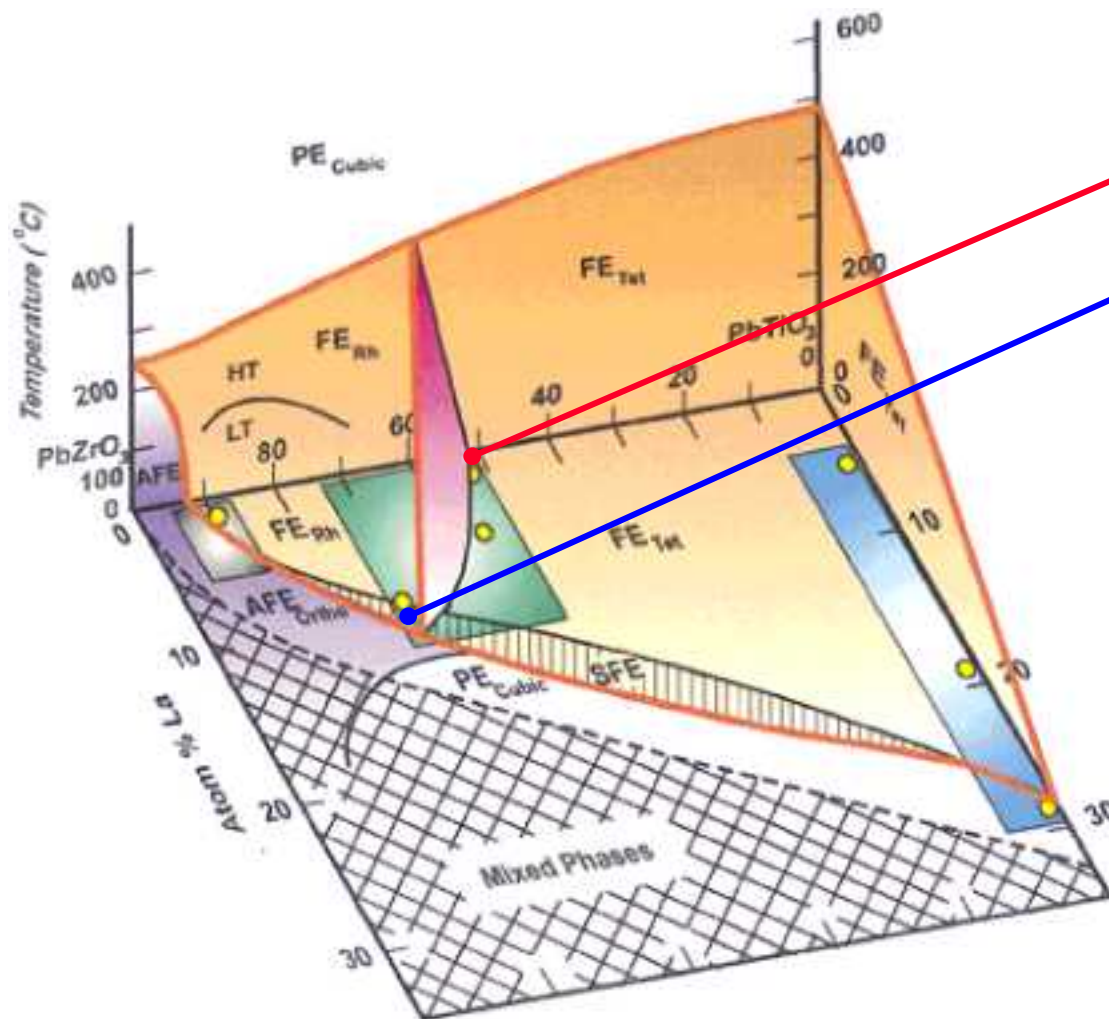
The previous experiments showed us the structural evolution

P(L)ZT film properties are sensitive to local chemistry

- **Pb/B-site ratio**
- **Zr/Ti ratio**
- **La doping**

→ Can we use EDS in STEM to study this local chemistry?

Accurate measurement of cation content is important to interpret properties



PZT 53/47

PLZT 12/70/30

In general, best dielectric properties at phase boundaries

Haertling, J. Am. Ceram. Soc., V82, 1999, P.797

EDS allows us to qualitatively and quantitatively measure chemistry

Scanning TEM (STEM) beam

X-Rays

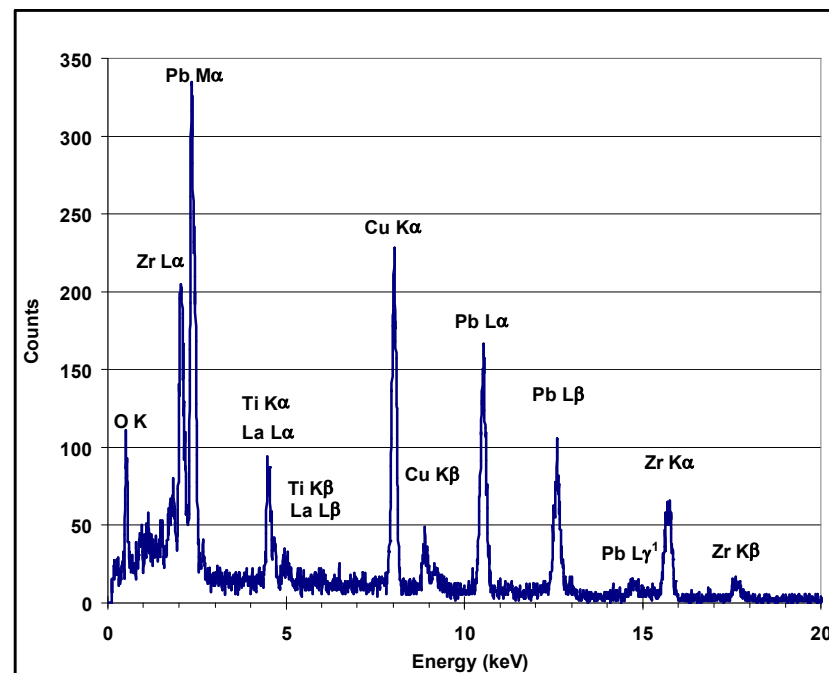
Thin sample
(~100 nm)

To imaging detector

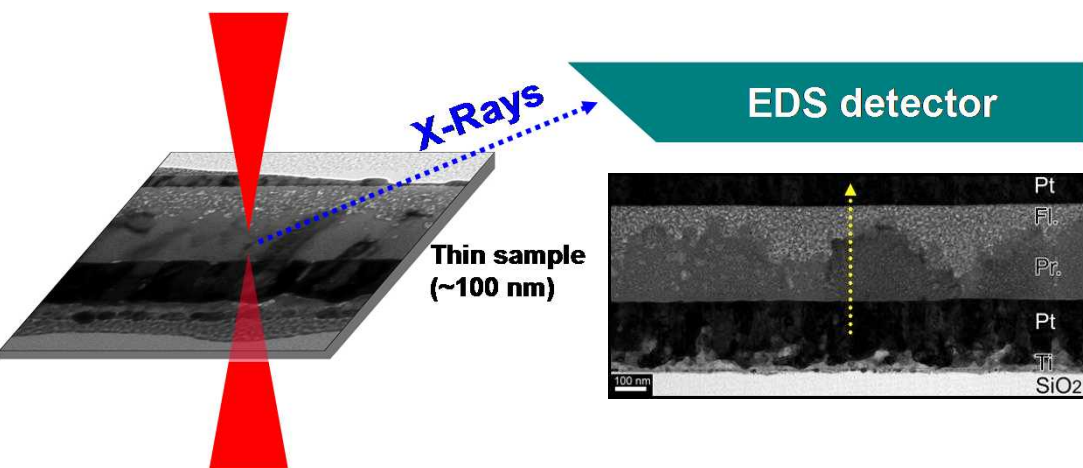
EDS: Energy-dispersive
X-ray spectroscopy

EDS detector

Data

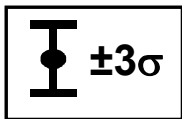
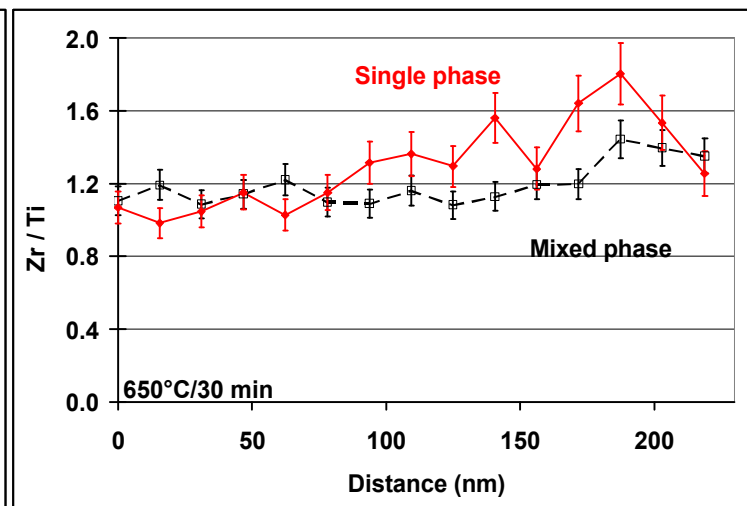
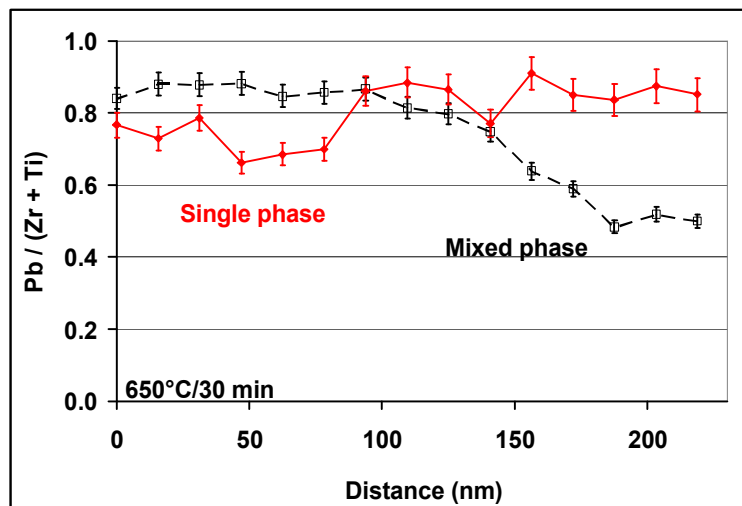


Quantification of linescans time-consuming, but straightforward



$$\frac{C_A}{C_B} = k_{AB} \frac{I_A}{I_B}$$

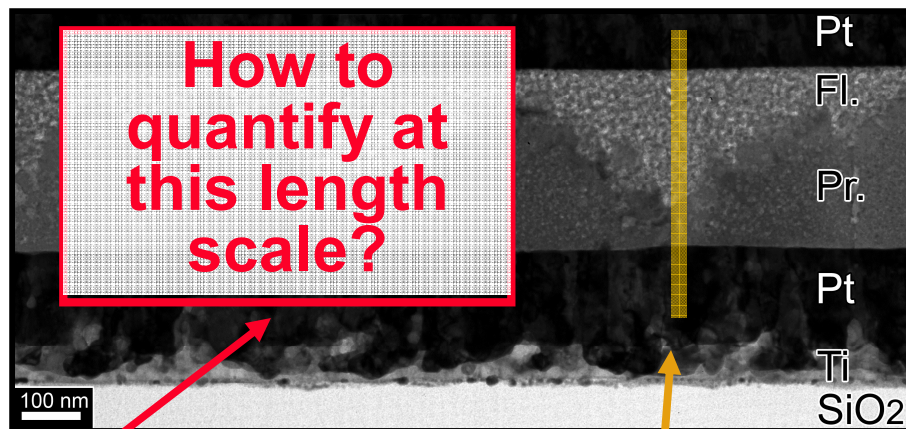
$$\Delta\left(\frac{C_A}{C_B}\right) = \frac{C_A}{C_B} \cdot \sqrt{\left(\frac{\Delta k_{AB}}{k_{AB}}\right)^2 + \left(\frac{\sqrt{I_A}}{I_A}\right)^2 + \left(\frac{\sqrt{I_B}}{I_B}\right)^2}$$



Parish, Brenneka, Tuttle,
and Brewer, J. Mater.
Res., submitted

We need a technique to measure representative cation ratios

SIMS, XPS, AES depth profiling
~several 10s of μm
 $\neq$ feature size



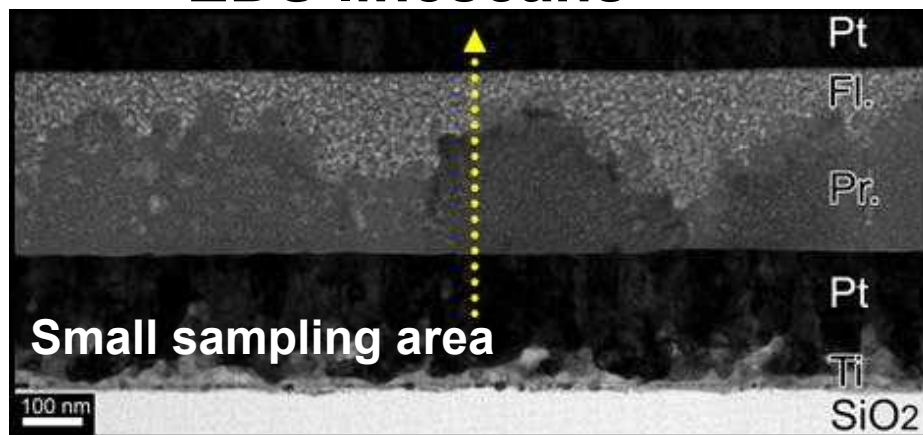
Feature size
~hundreds of nms

EDS linescan sampling
<10 nm
 $\neq$ feature size

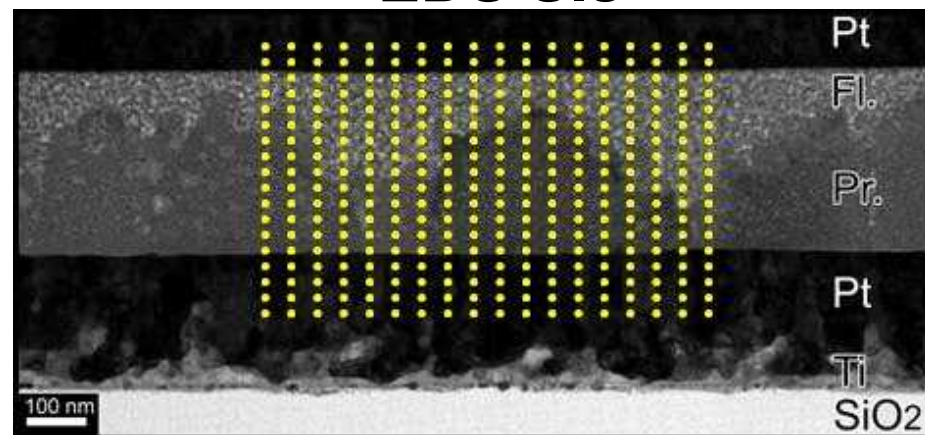


Comparisons: linescans and spectrum images (SIs)

EDS linescans



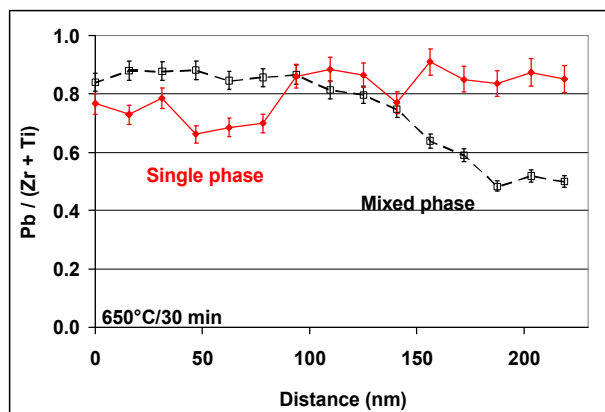
EDS SIs



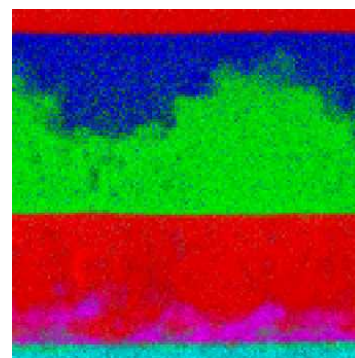
Quantification established in the literature

$$\frac{C_A}{C_B} = k_{AB} \frac{I_A}{I_B}$$

$$\Delta\left(\frac{C_A}{C_B}\right) = \frac{C_A}{C_B} \cdot \sqrt{\left(\frac{\Delta k_{AB}}{k_{AB}}\right)^2 + \left(\frac{\sqrt{I_A}}{I_A}\right)^2 + \left(\frac{\sqrt{I_B}}{I_B}\right)^2}$$

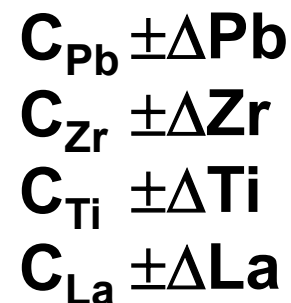
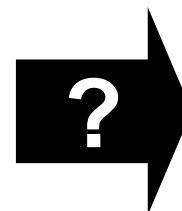
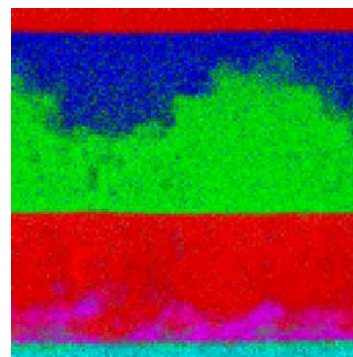
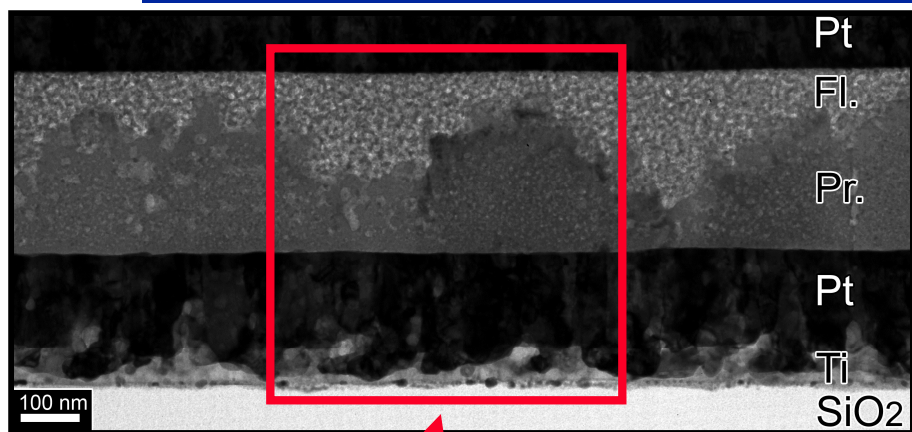


Qualitative analysis we understand, but how to quantify?



$$\begin{aligned} C_{Pb} &\pm \Delta Pb \\ C_{Zr} &\pm \Delta Zr \\ C_{Ti} &\pm \Delta Ti \\ C_{La} &\pm \Delta La \end{aligned}$$

Can we use spectrum imaging?



Feature size $\leftrightarrow$ SI size

Spectrum imaging has the right length scale, but:

- How to get cation fractions

$C_{\text{Pb}}, C_{\text{Zr}}, \dots$?

- How to get statistical uncertainties Δ ?

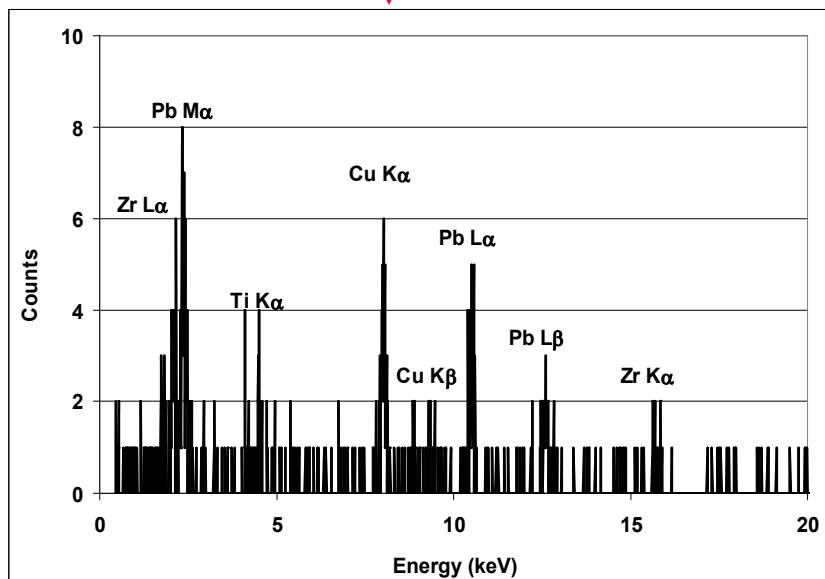
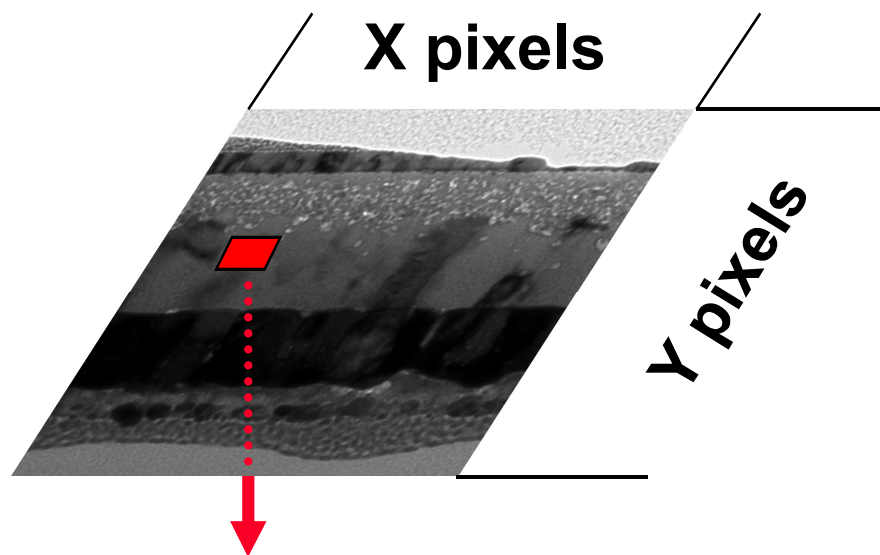
Some literature available

Unable to find any literature



Sandia
National
Laboratories

Spectrum imaging – need to mine the data



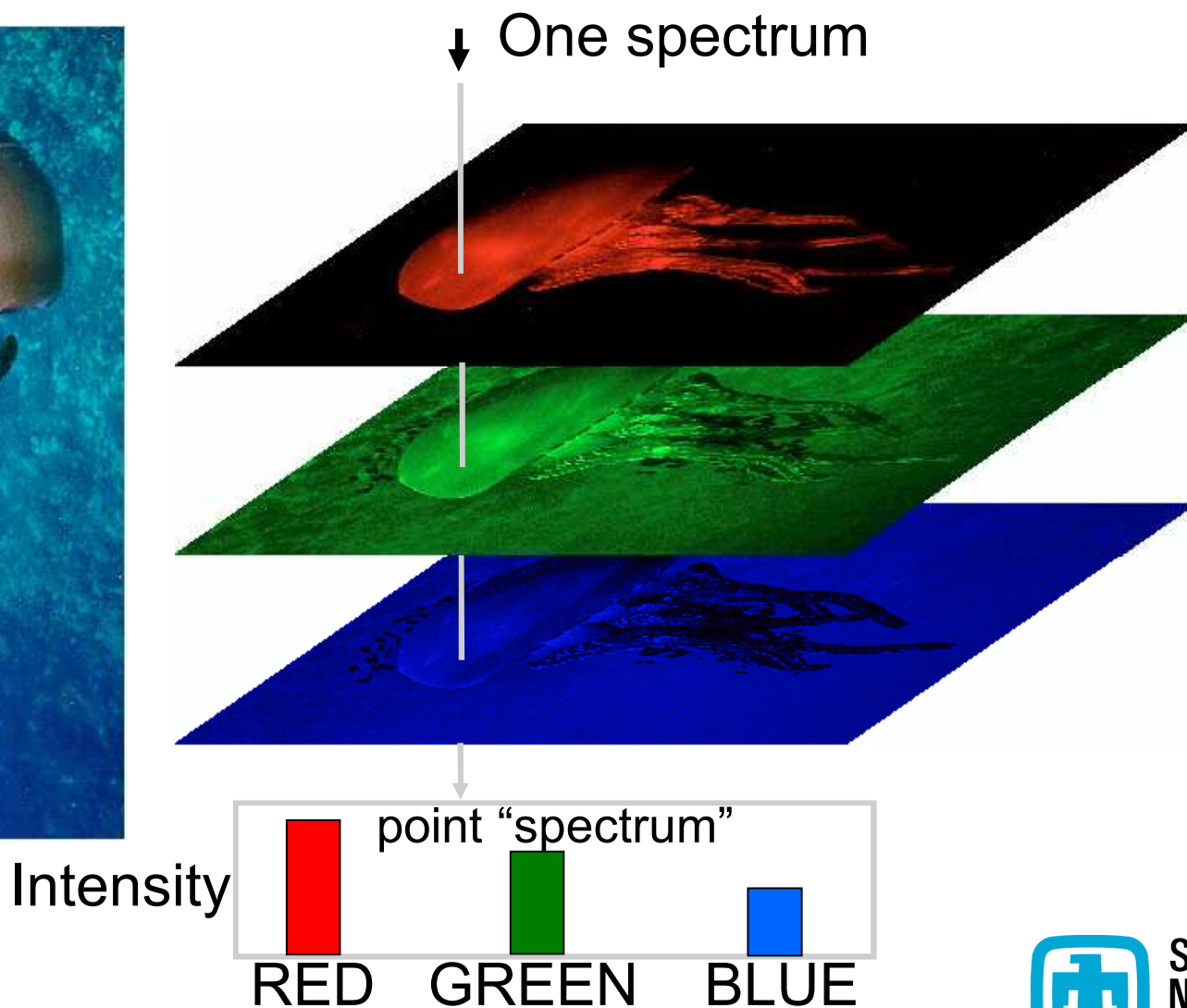
Typical dataset:
128×128 pixels
2048 channels/pix
∴ 34 million datapoints

How to make use of this?
→ Multivariate Statistical Analysis (MSA)

Color image: an example of a 3-channel spectrum image



(Slide courtesy
M. Keenan and
P. Kotula)

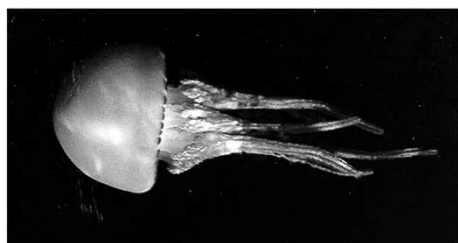


Sandia
National
Laboratories

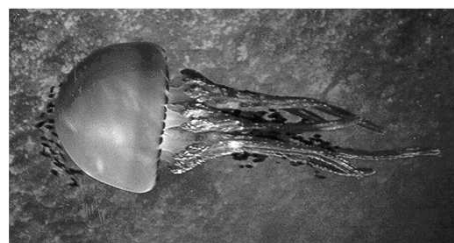
**Spectrum image =
(Concentration) · (Spectral component)^T**



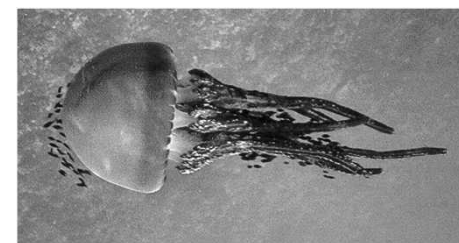
=



x



x



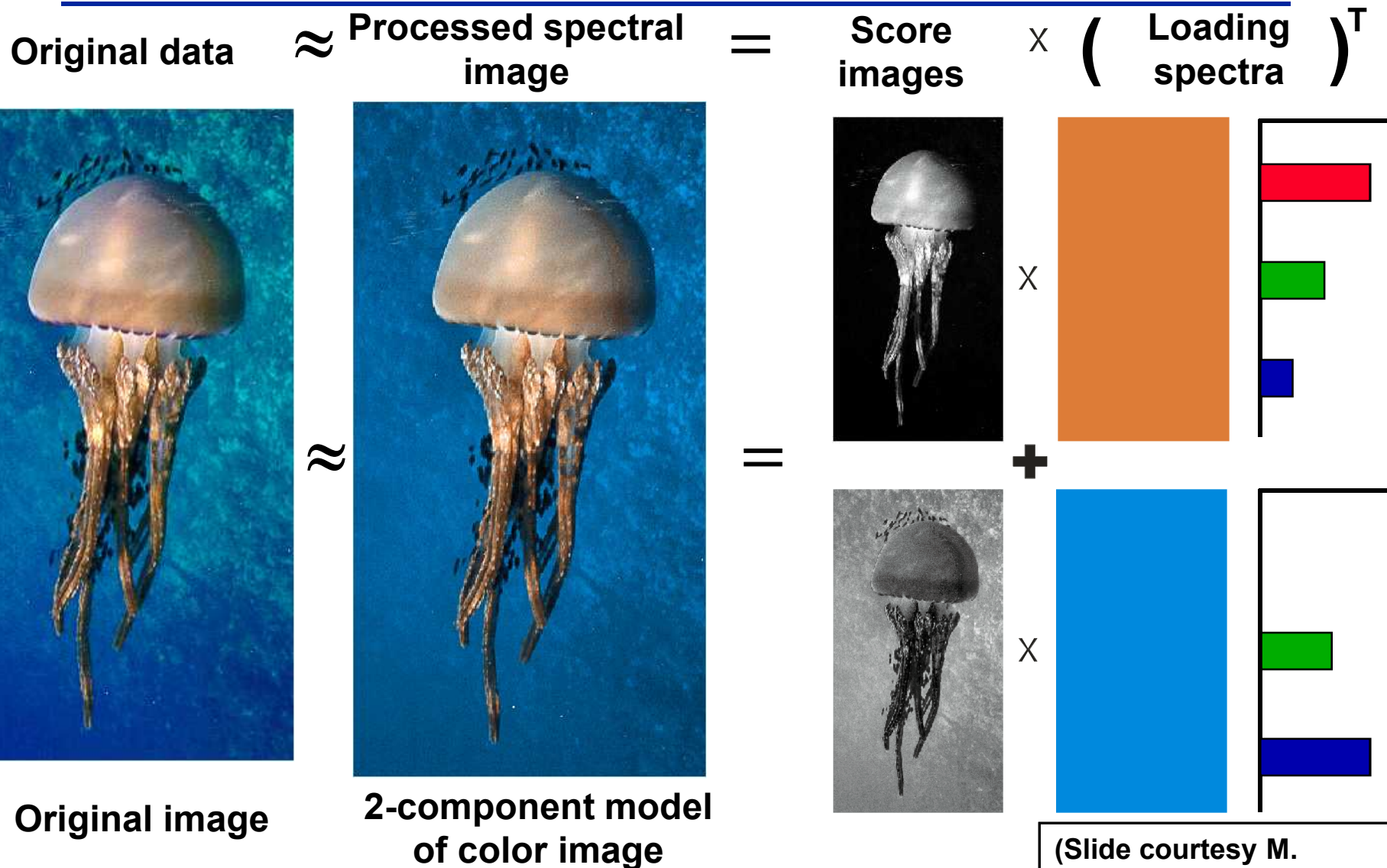
x



note the linearity assumption

(Slide courtesy
M. Keenan and
P. Kotula)

MSA finds the most relevant variations in the data



(Slide courtesy M. Keenan and P. Kotula)

MSA finds the most relevant variations in the data

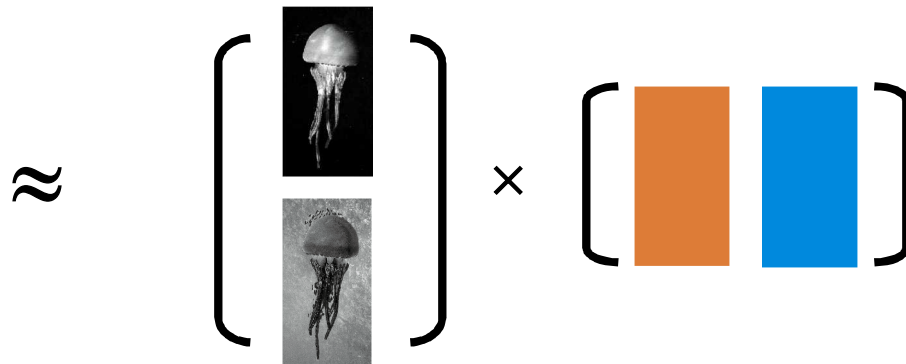
$$\begin{matrix} n \\ m \end{matrix} \boxed{D} \approx \begin{matrix} p \\ m \end{matrix} \boxed{C} \times \begin{matrix} n \\ p \end{matrix} \boxed{S^T}$$

$S = \text{Loading spectra}$

**D = Unfolded
spectral image
matrix**



C = Score images



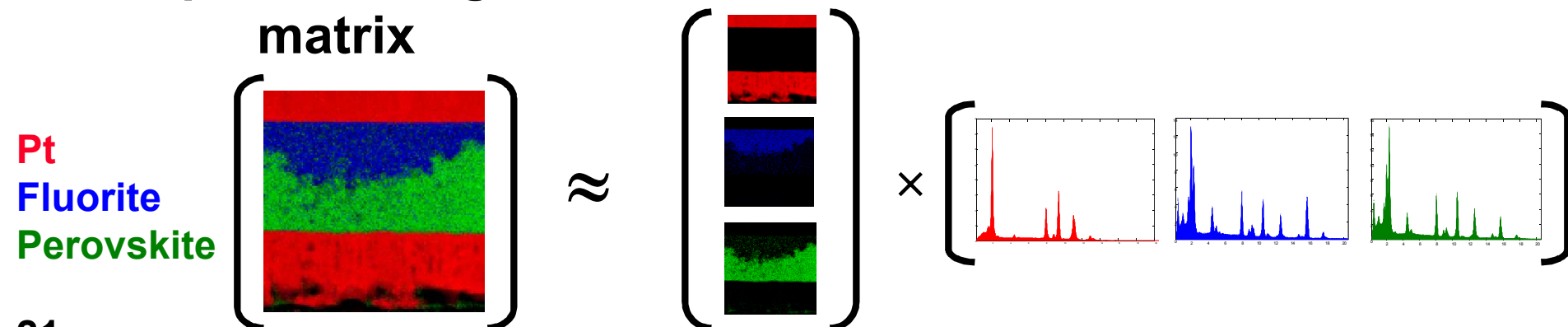
Principal Component Analysis (PCA) used to analyze our EDS spectrum images

$$\begin{array}{c} \textcolor{teal}{n} \\ \textcolor{red}{m} \end{array} \boxed{D} \approx \begin{array}{c} \textcolor{blue}{p} \\ \textcolor{red}{m} \end{array} \boxed{C} \times \begin{array}{c} \textcolor{teal}{n} \\ \textcolor{blue}{p} \end{array} \boxed{S^T}$$

S = Loading spectra

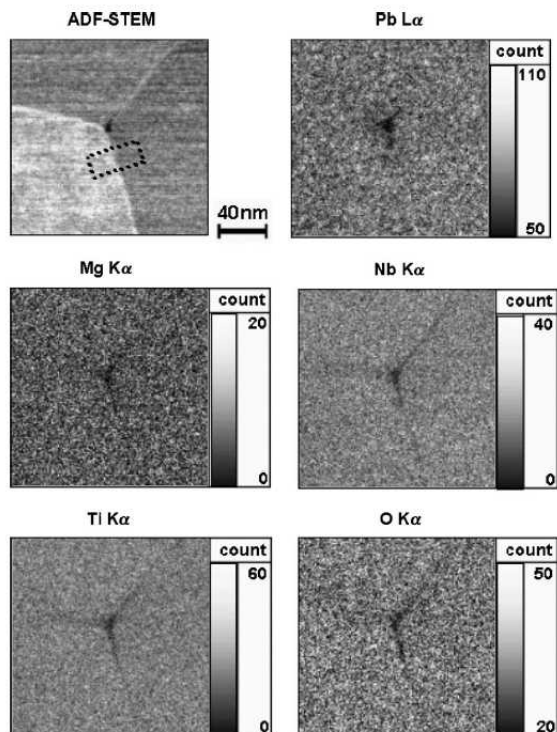
D = Unfolded spectral image matrix

C = Score images



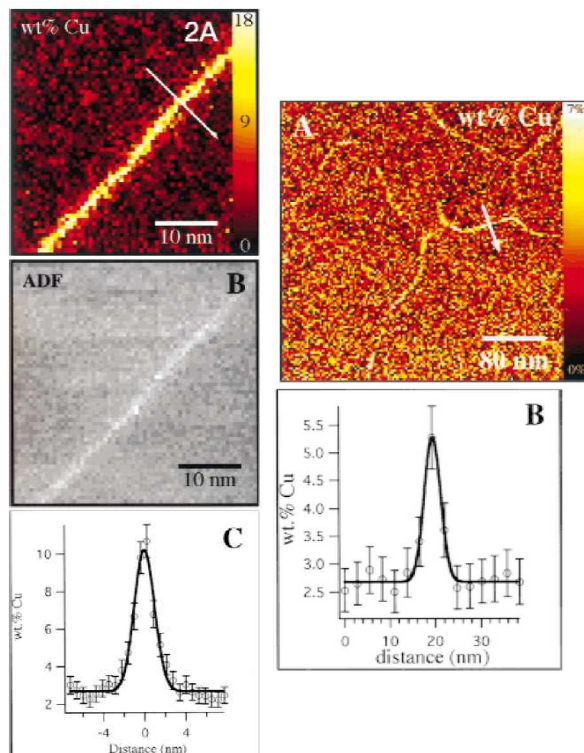
Many papers have quantified from dot maps or SIs (without MSA)

Pb(Mg,Nb)O₃-PbTiO₃



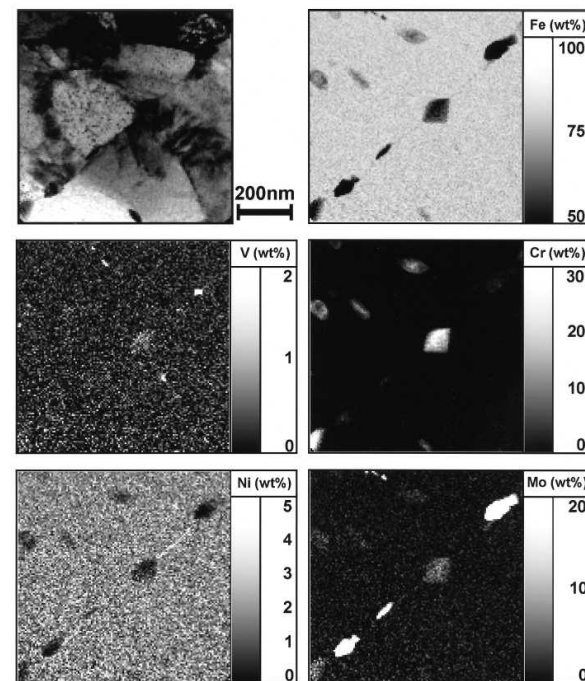
- Gorzkowski et al., J. Mat. Sci., V39, P.6735 (2004)
- (Lehigh Univ. VG STEM)

Al-4% Cu



- Carpenter et al., M&M, V5, P.254 (1999)
- (Lehigh Univ. VG STEM)

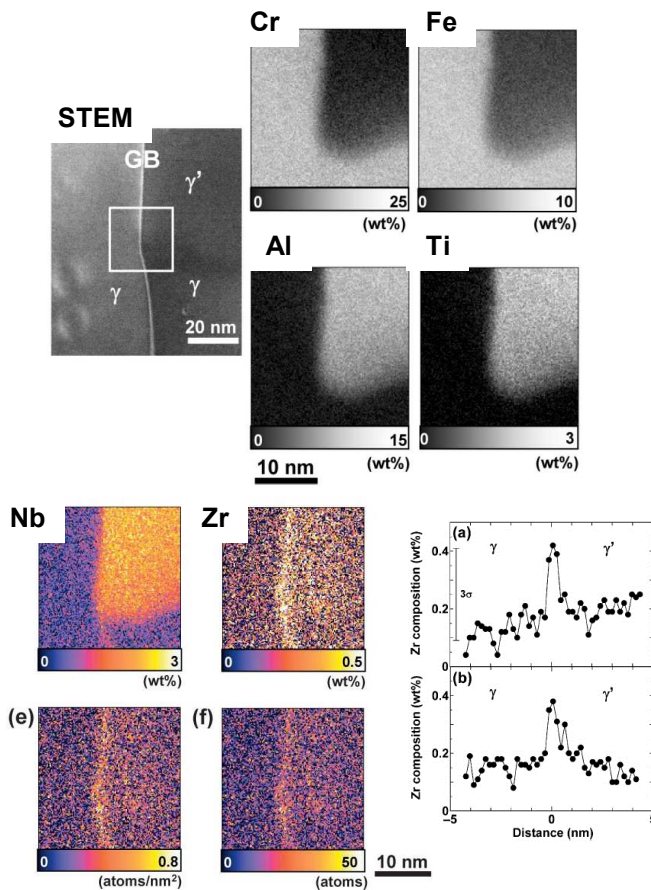
Prior-austenite grain boundary in steel



- Williams et al., J. Elec. Micros., V51(Supp.), P. S113 (2002)
- (Lehigh Univ. VG STEM)

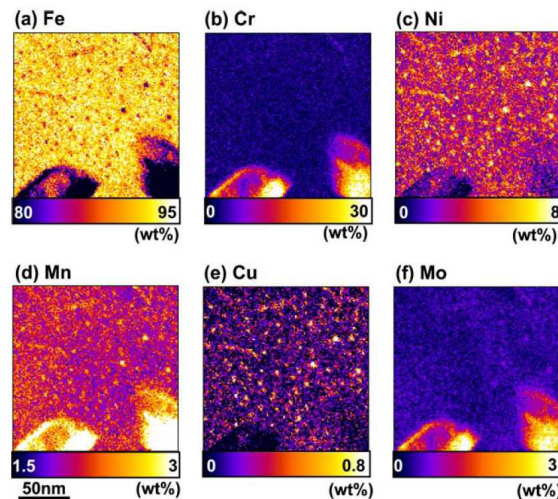
A few papers have quantified with MSA

Ni-based superalloy



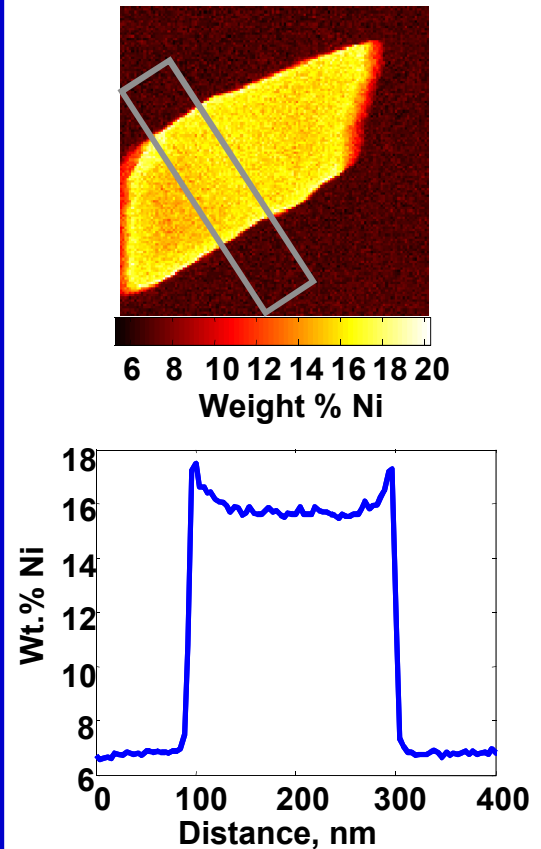
- Watanabe et al., M&M, V12, P.515 (2006)
- Lehigh Univ. VG STEM (C_s corrected)

Irradiated alloy steel



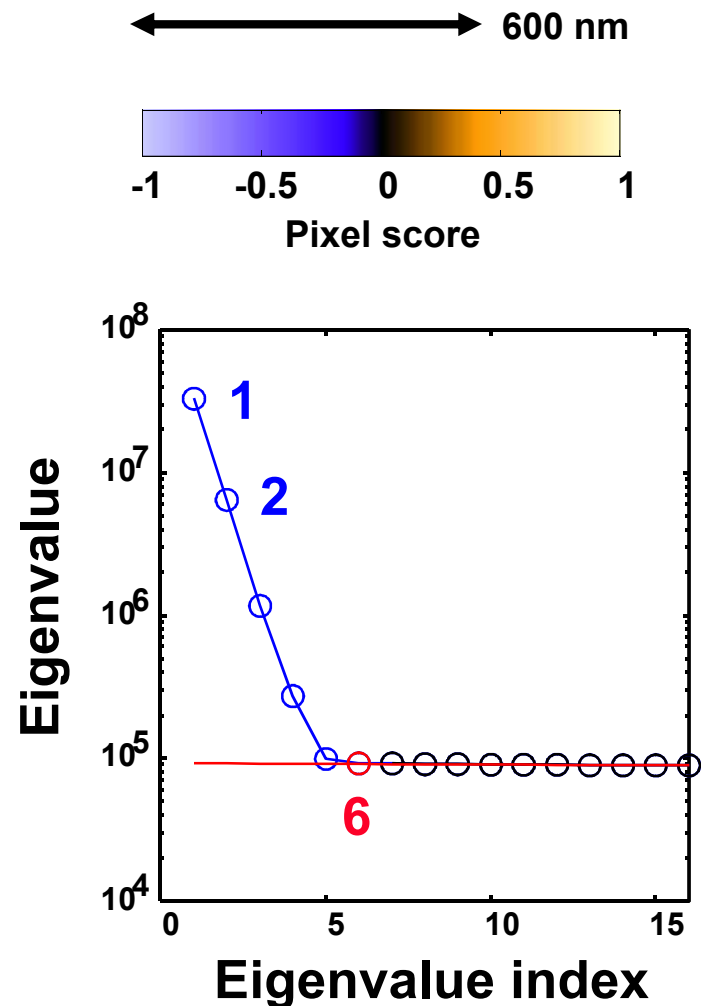
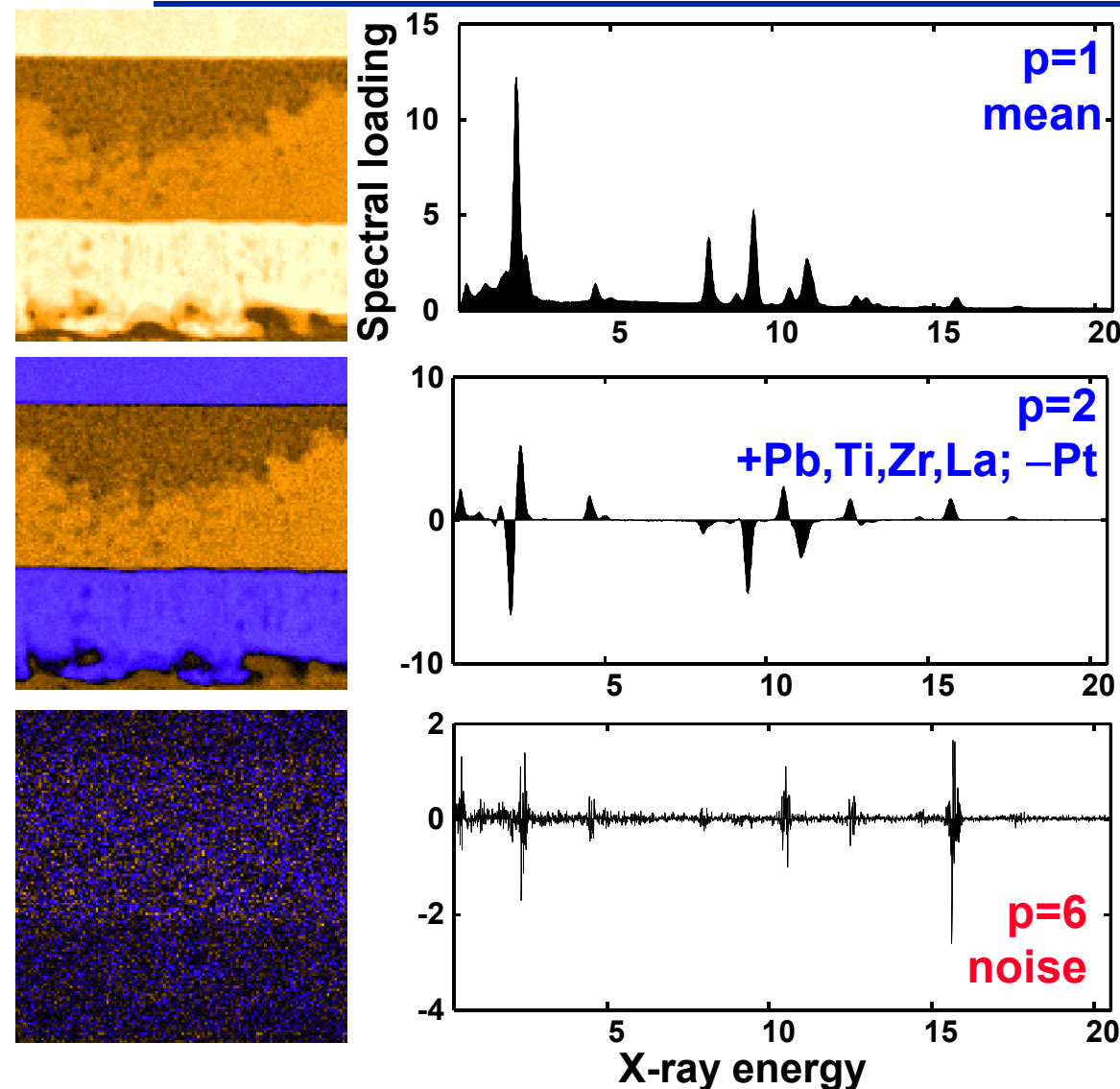
- Burke et al., J. Mat. Sci., V41, P.4512 (2006)
- Lehigh Univ. VG STEM

Fe-Ni meteorite

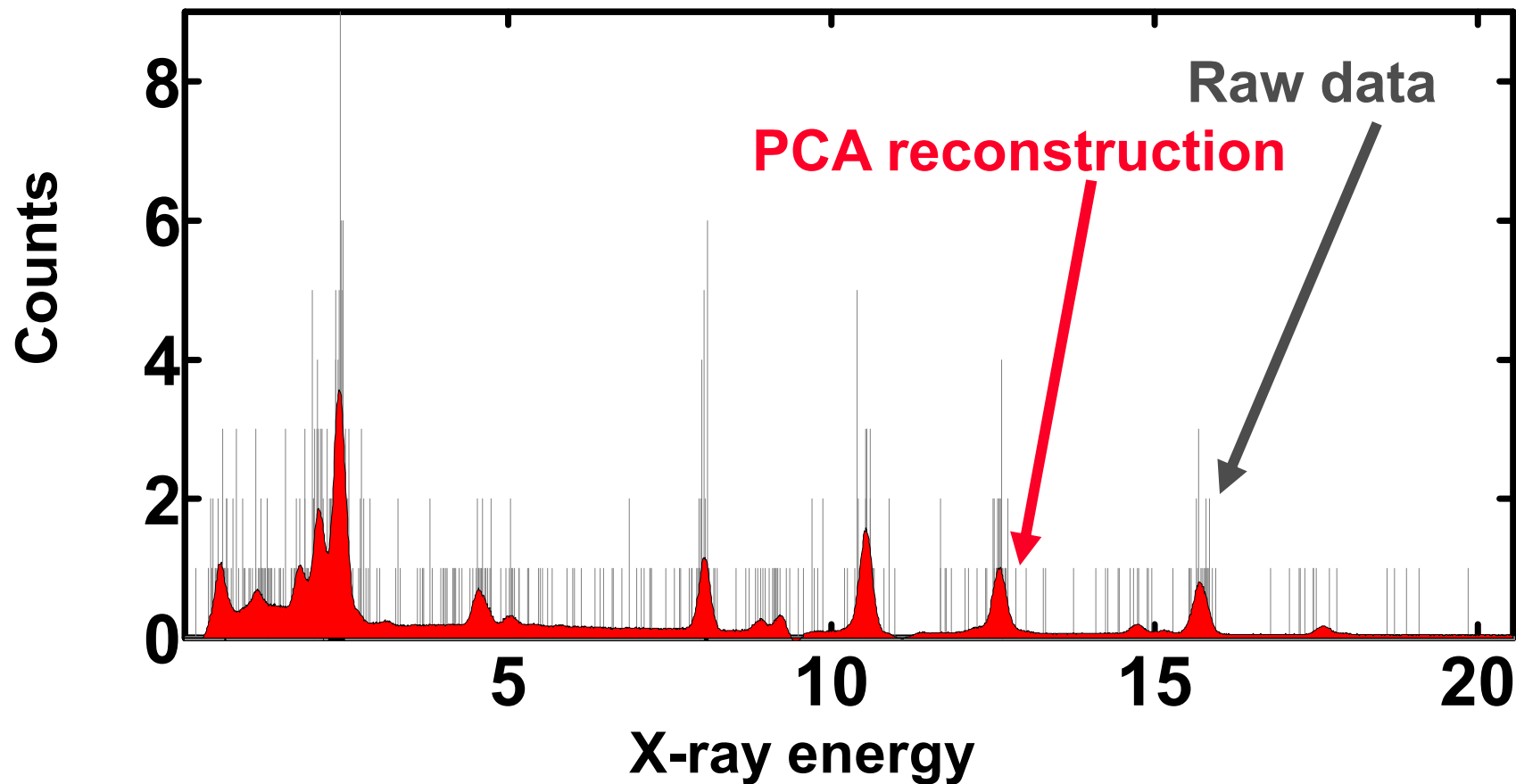


- Goldstein et al., Meteoritics & Planetary Sci., V42, P.913 (2007)
- Sandia Labs Tecnai TEM/STEM

PCA finds the chemically relevant variations and rejects noise



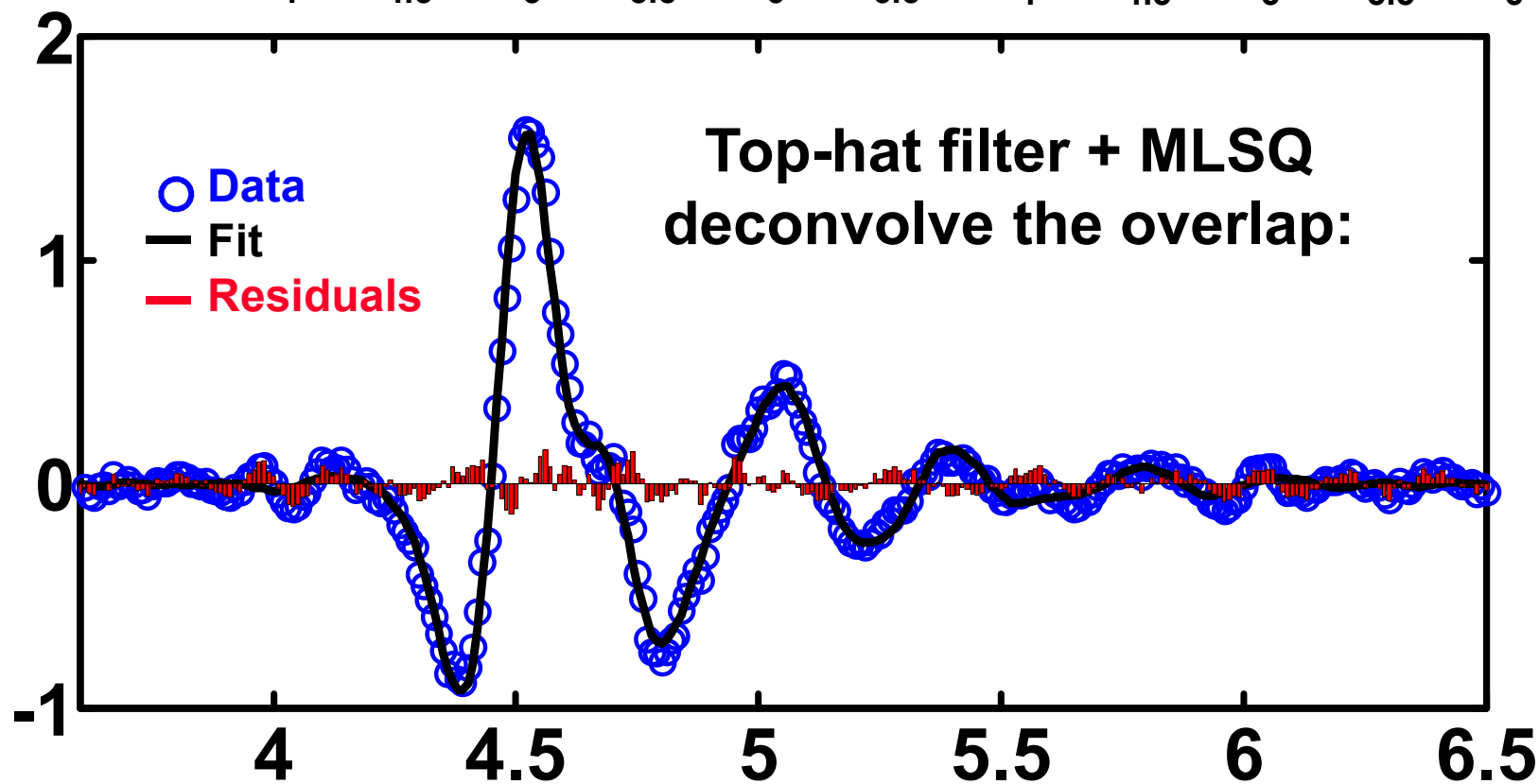
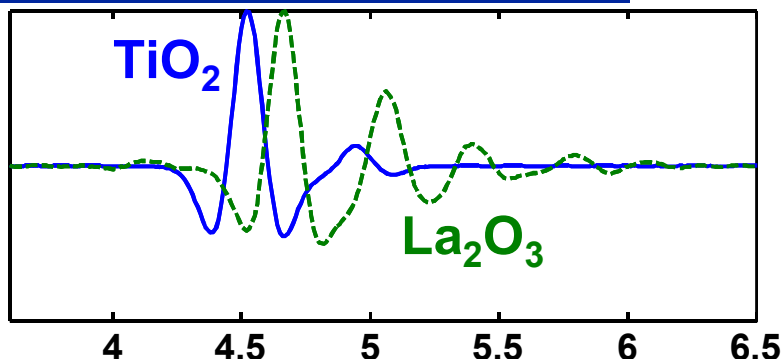
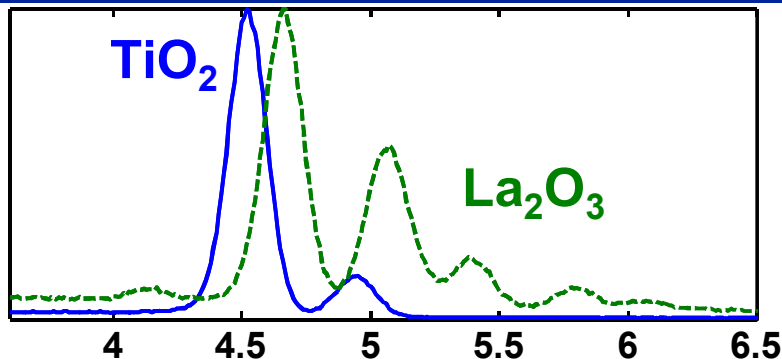
PCA produces a noise-filtered reconstruction of the data at every pixel



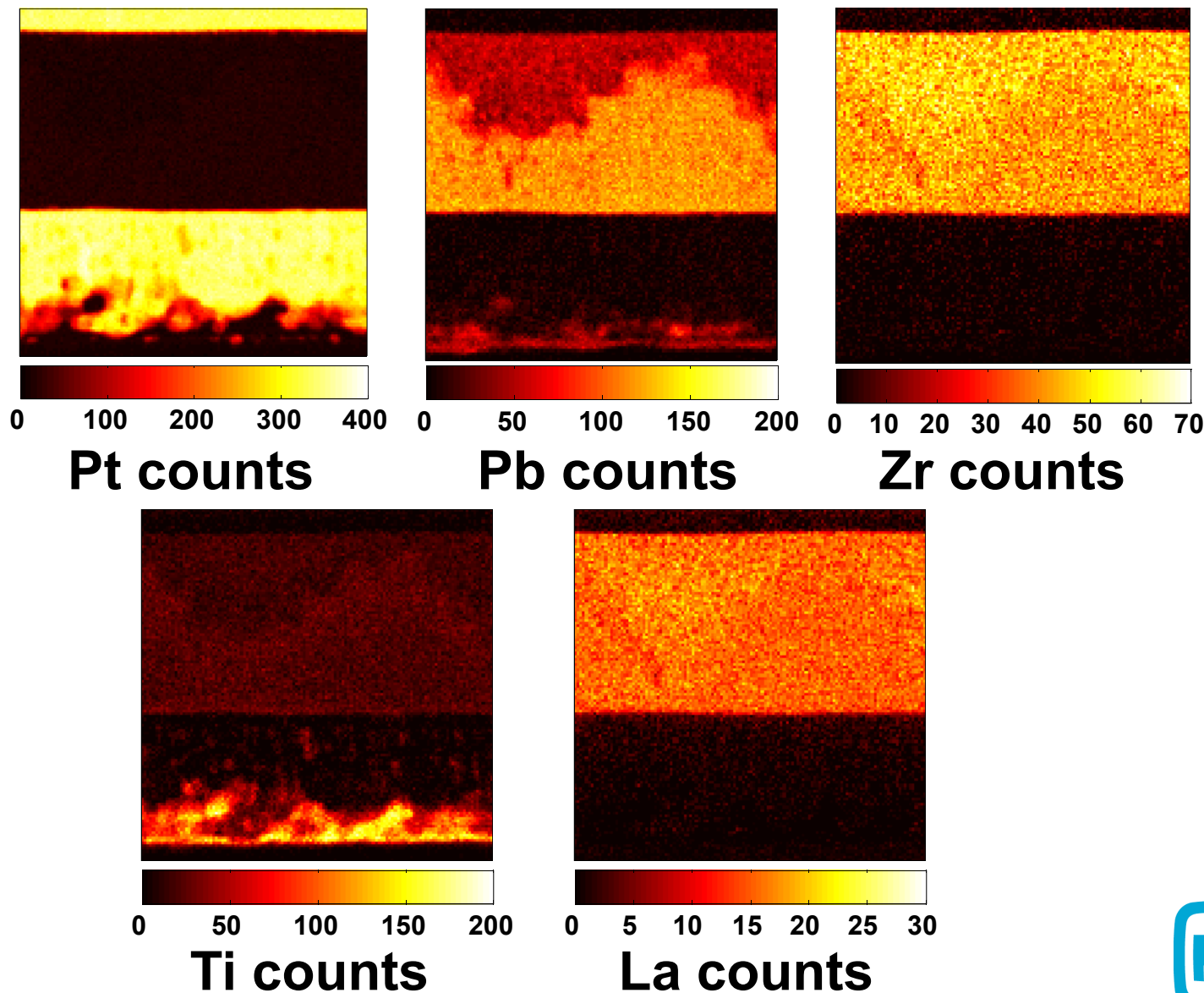


Noise-filtered spectra can be deconvolved and integrated

Ti K and
La L lines
overlap:



Integration and deconvolution at each pixel yields count-maps



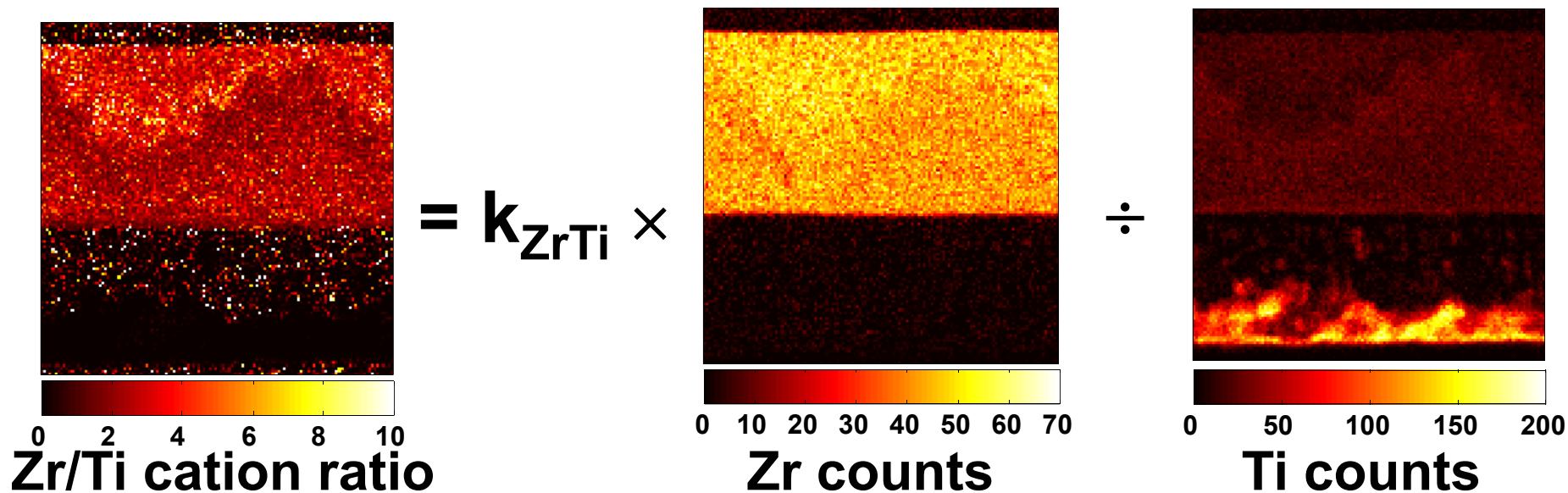
Count maps and the Cliff-Lorimer equation yield quantitative maps

Cliff-Lorimer equation:

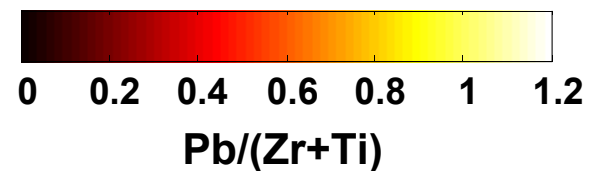
$$\frac{C_{\text{Zr}}}{C_{\text{Ti}}} = k_{\text{ZrTi}} \frac{I_{\text{Zr}}}{I_{\text{Ti}}}$$

J. Microsc., V103(2), 1975, P.203

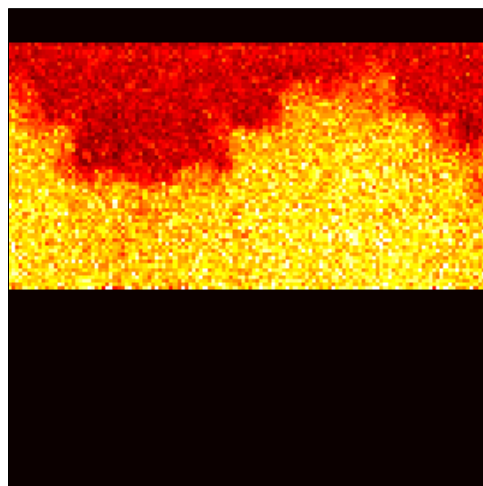
Quantitative mapping:



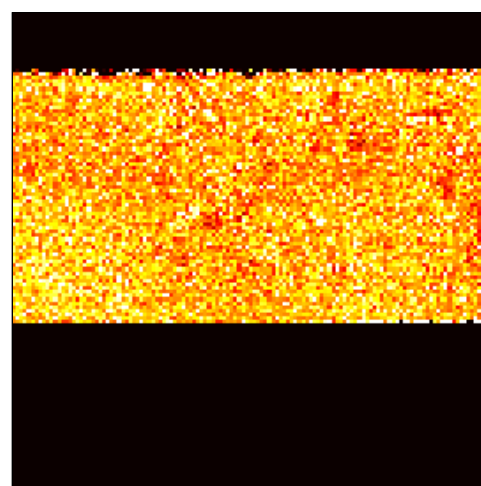
The overcoat+anneal process restores the Pb-stoichiometry



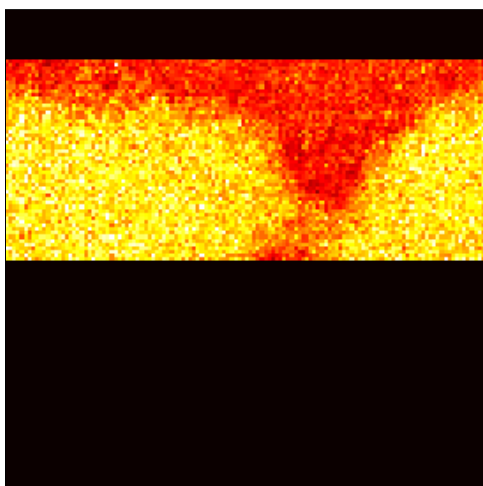
Mixed phase



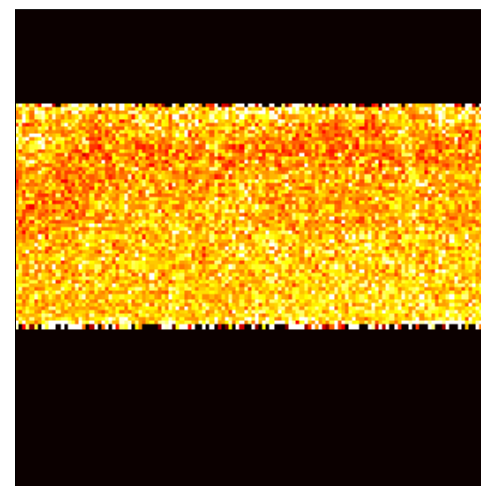
Single phase



PLZT 12/70/30
650°C / 30 min

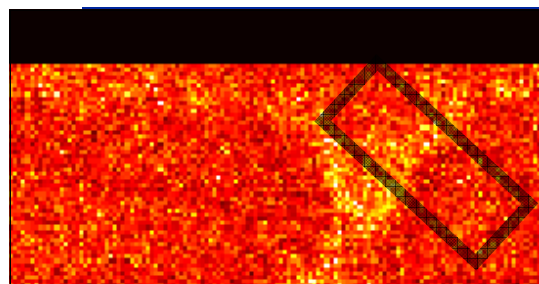


PZT 53/47
650°C / 30 min



↔
200 nm

Zr segregates to the fluorite

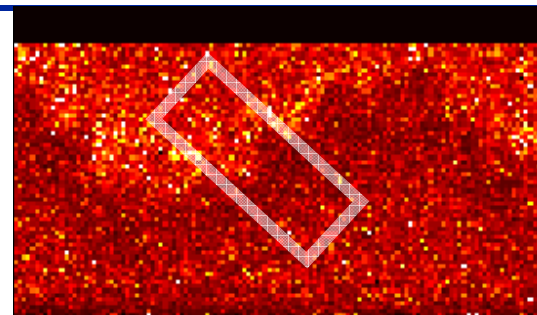
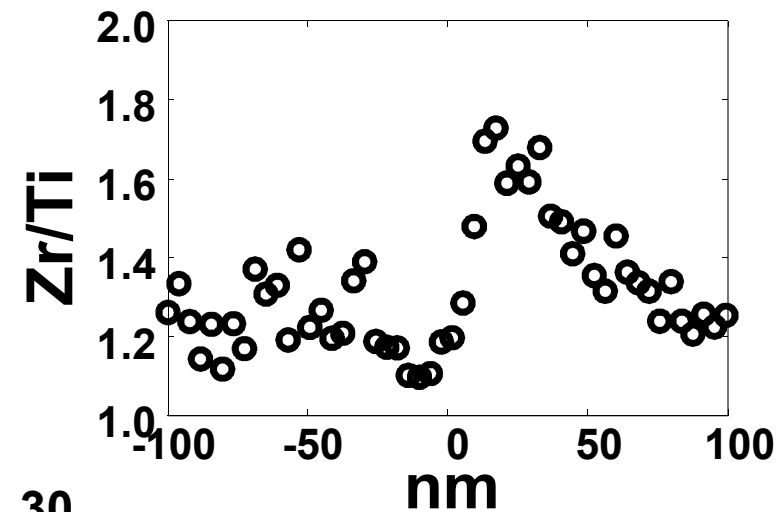


PZT 53/47
650°C/30 min
Mixed-phase



Zr/Ti

0 0.5 1 1.5 2 2.5 3

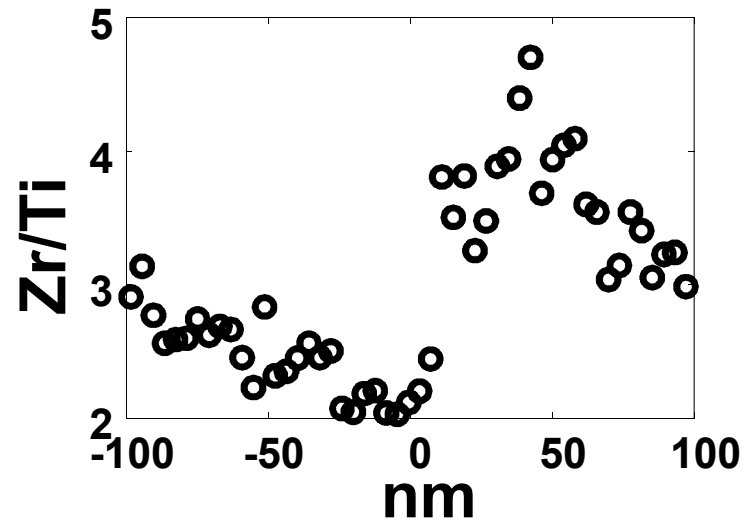


PLZT 12/70/30
650°C/30 min
Mixed-phase

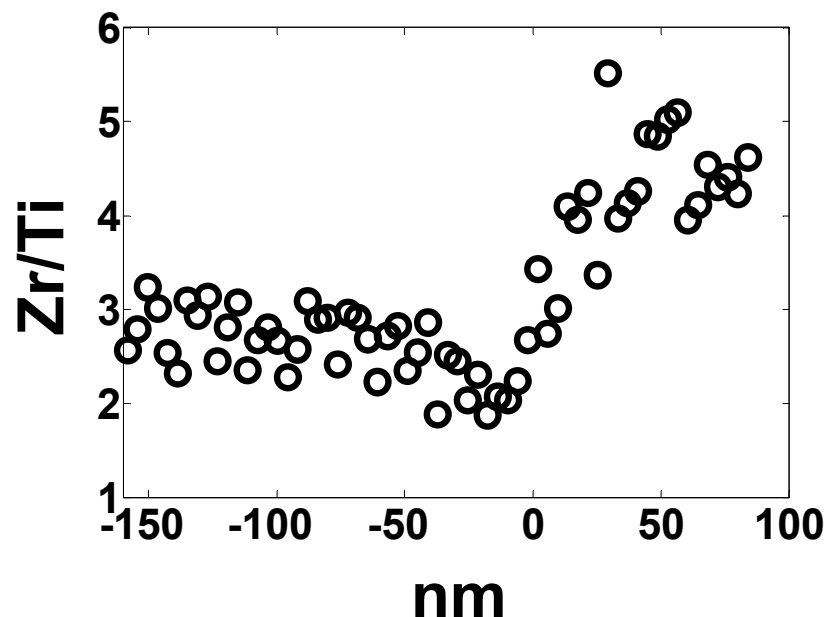
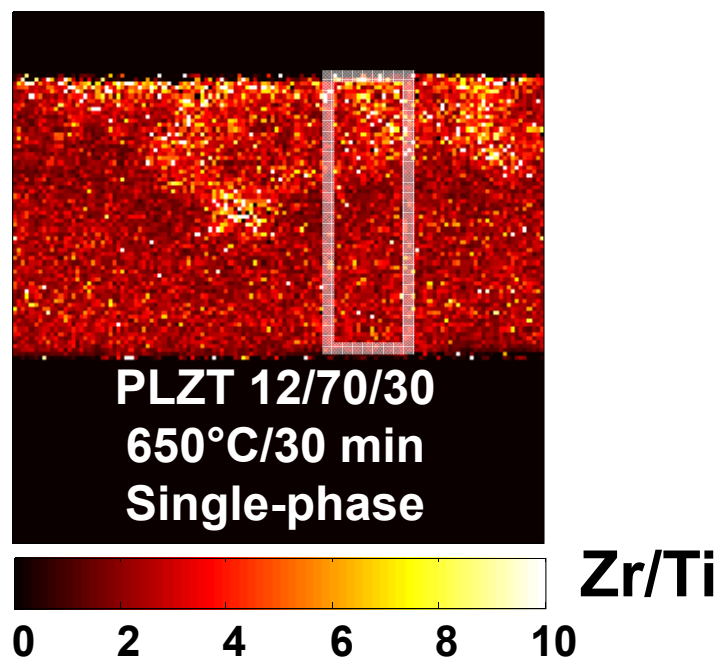


Zr/Ti

0 2 4 6 8 10

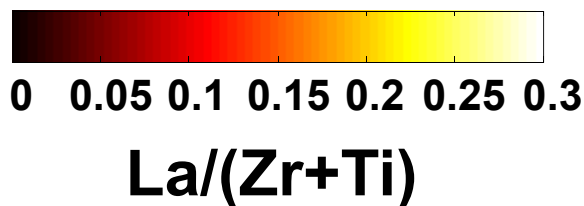
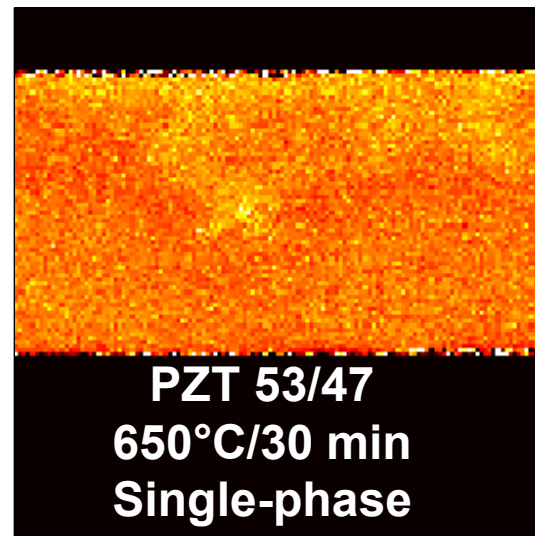
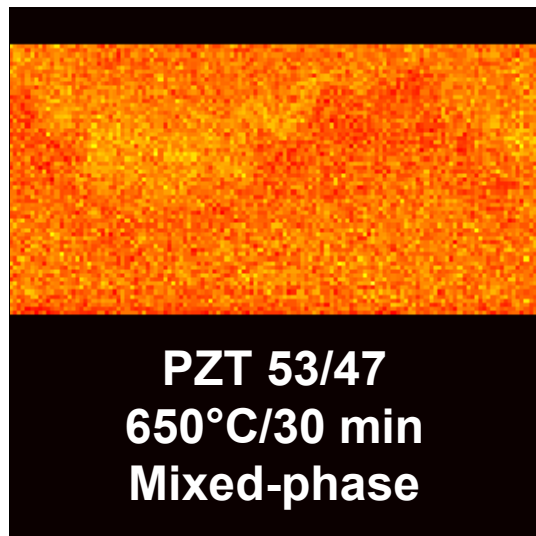


Zr segregation remains after the fluorite → perovskite conversion

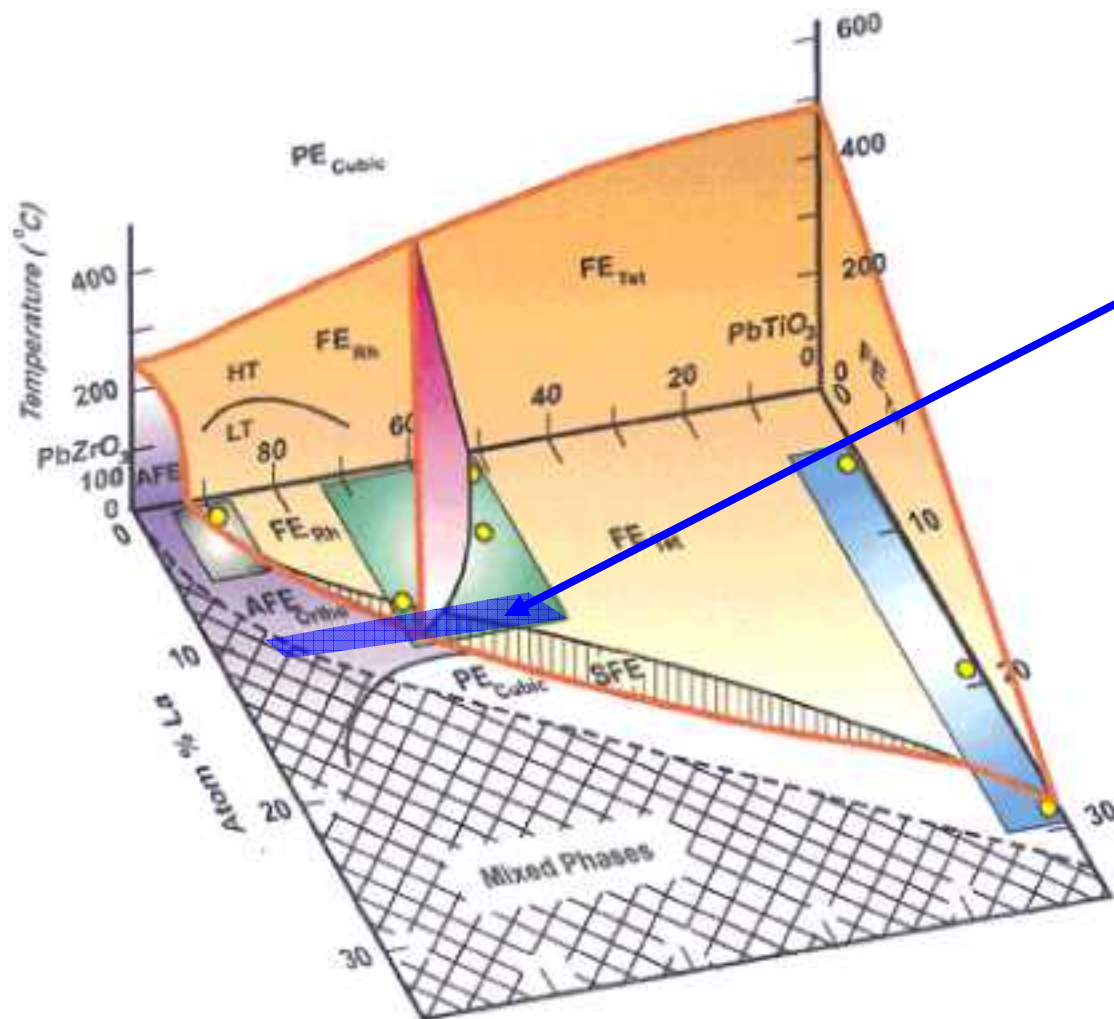


However, little Zr-segregation is seen in the PZT 53/47 material
→ Currently under investigation

La segregation is also present



Accurate measurement of cation content is important to interpret properties



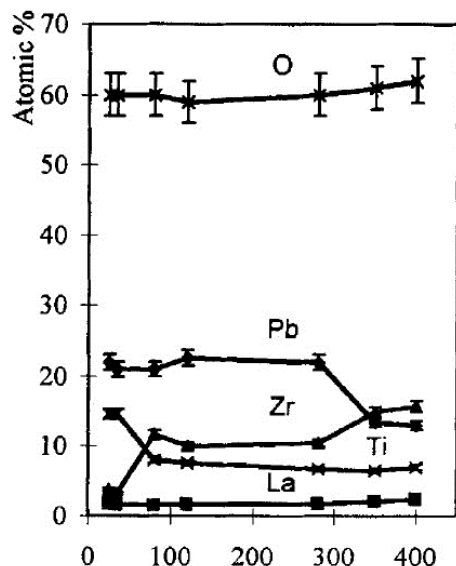
Measured chemistry
crosses phase
boundaries –

This may degrade
properties

Haertling, J. Am. Ceram.
Soc., V82, 1999, P.797

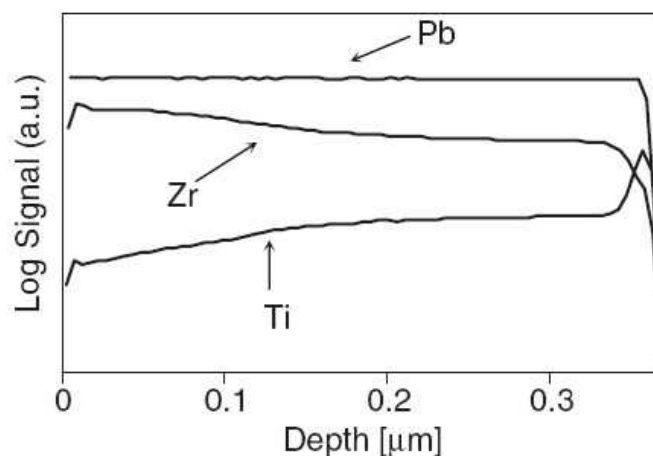
We have succeeded in mapping cations at a length scale $\approx$ feature size

EDS linescan:
Spot size ~ 10 nm



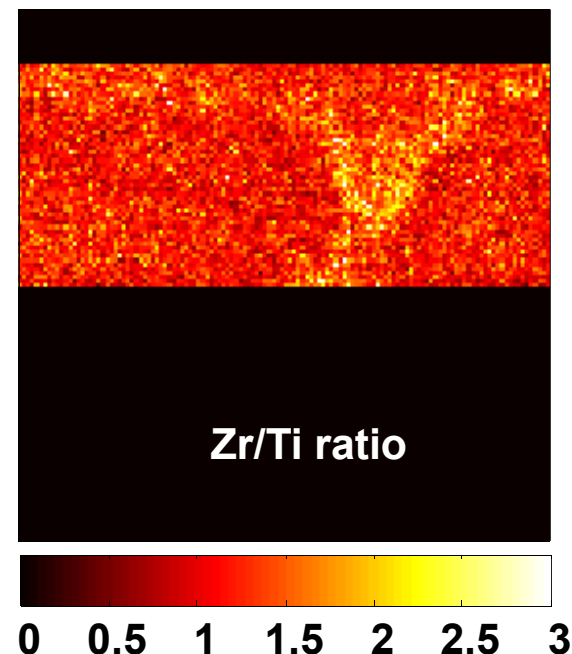
Drazic & Kosec, *Ferroelectrics*,
V201, P.23, 1997

SIMS depth-profile:
Sampled area 40×40 μm



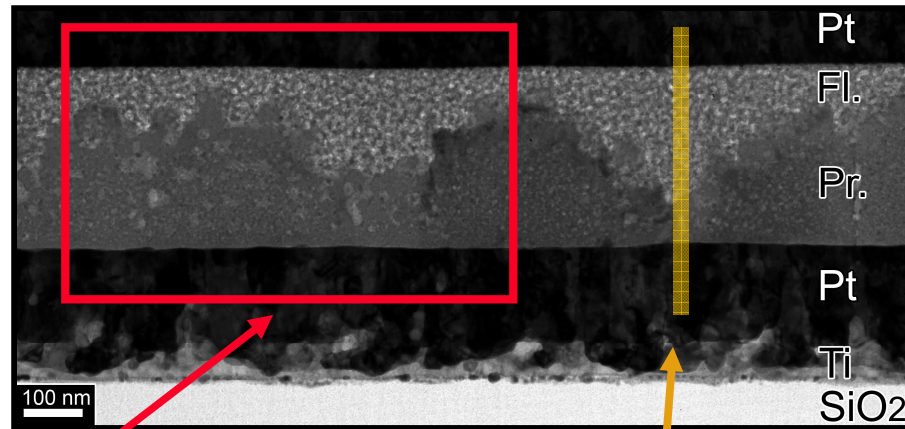
Etin et al., *J. Am. Ceram. Soc.*,
V89, P.2387, 2006

Quantified SI:
 500×250 nm



We have succeeded in mapping cations at a length scale $\approx$ feature size

SIMS, XPS, AES depth profiling
~several 10s of microns
 $\neq$ feature size



Feature size
~hundreds of nms

EDS linescan sampling
~several nanometers
 $\neq$ feature size

Used STEM-EDS SIs
to sample this scale



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We've been able to quantify point-by-point

A novel overcoat+anneal technique allows us to make single-phase perovskite without excess Pb-additions

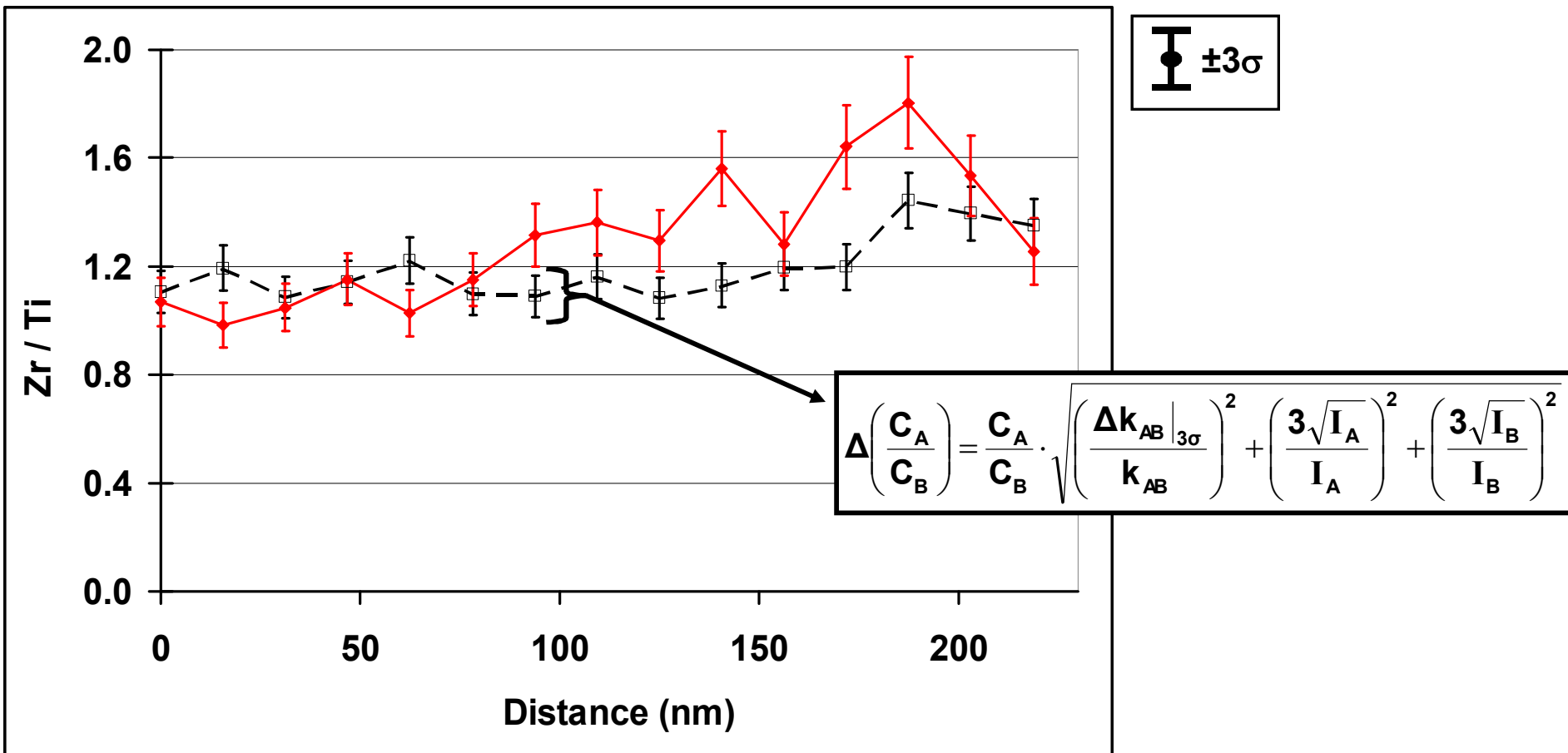
Spectrum images have the proper size scale to study inhomogeneities in PLZT thin films

Severe Zr-segregation found in PLZT but not PZT samples

PCA analysis + Cliff-Lorimer quantification allows mapping of the quantitative cation contents



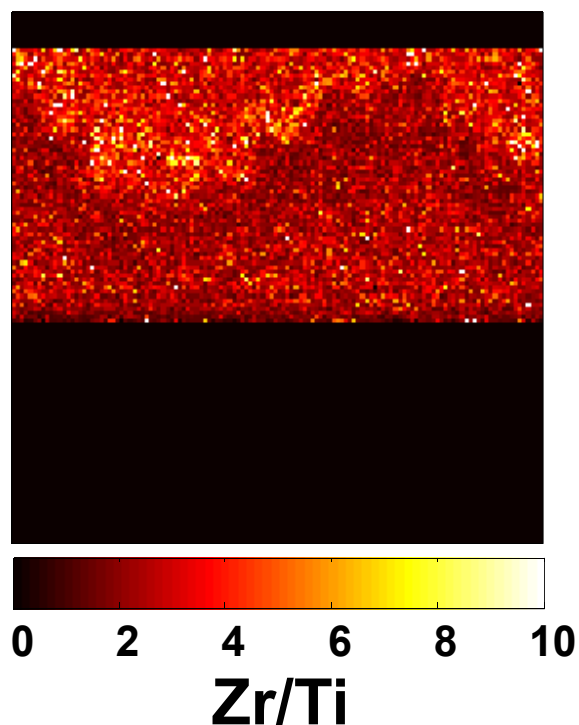
What we're still missing: statistical uncertainty



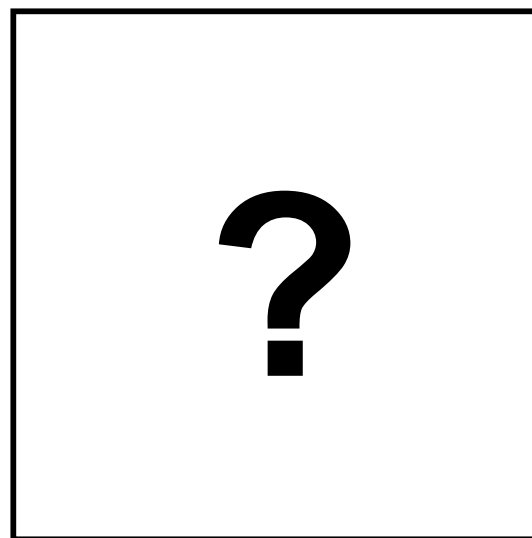
In a traditional EDS point-analysis,
statistical bounds are easily
calculated



What we're still missing: statistical uncertainty

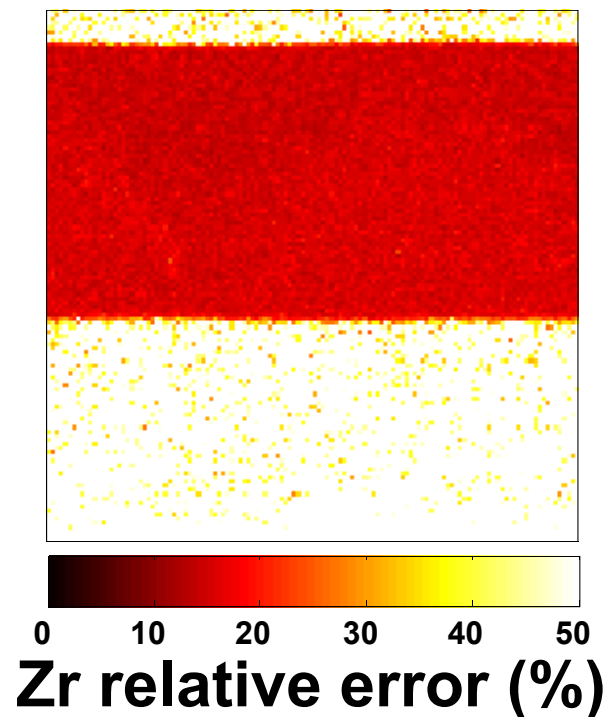
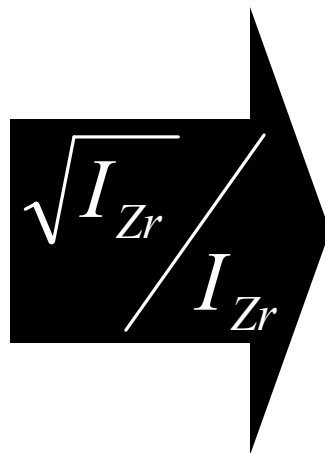
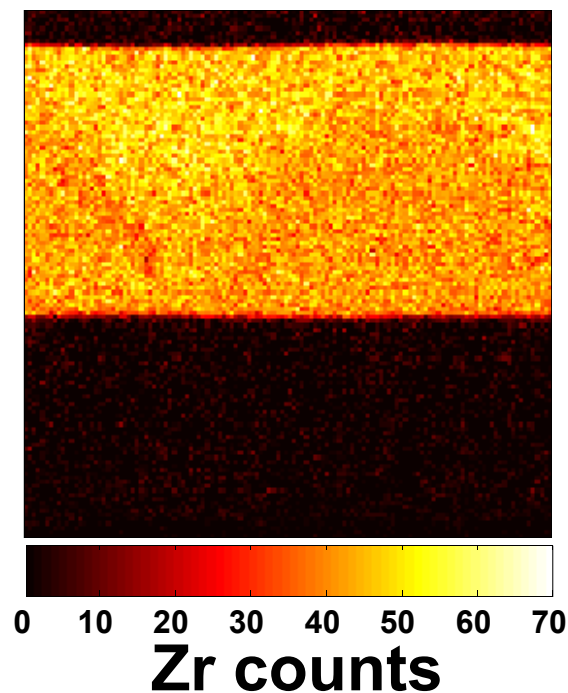


$\pm$



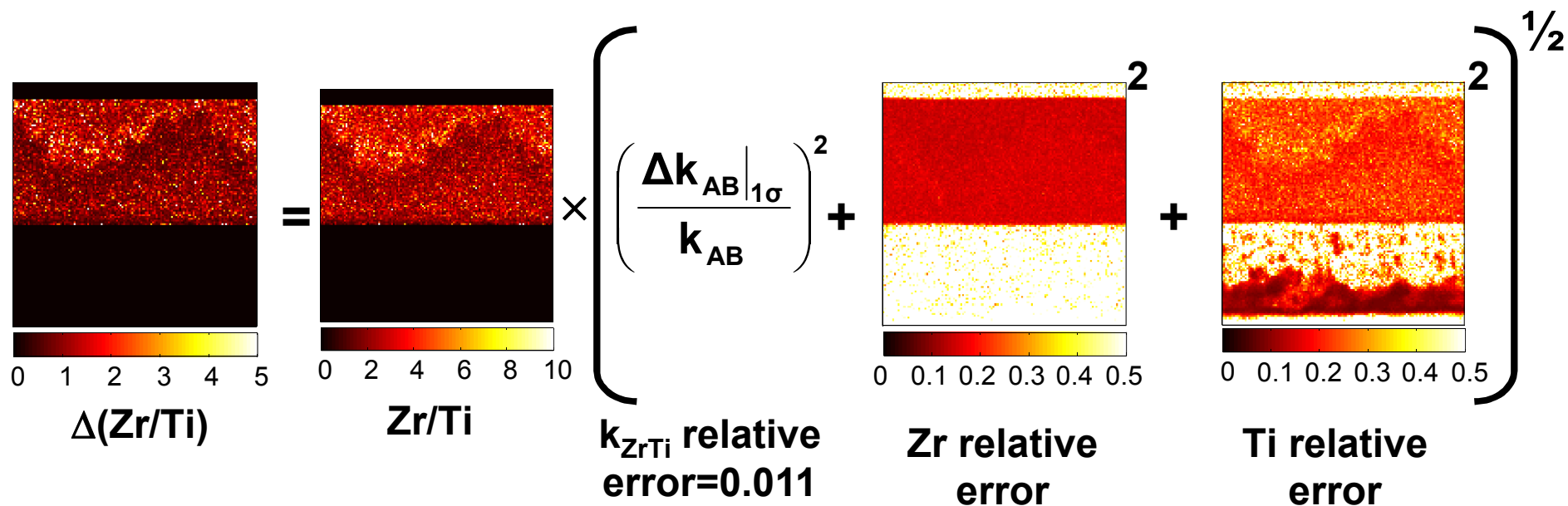
What if we apply our uncertainty equation point-by-point?

$$\Delta \left(\frac{C_A}{C_B} \right) = \frac{C_A}{C_B} \cdot \sqrt{\left(\frac{\Delta k_{AB}|_{1\sigma}}{k_{AB}} \right)^2 + \left(\frac{\sqrt{I_A}}{I_A} \right)^2 + \left(\frac{\sqrt{I_B}}{I_B} \right)^2}$$

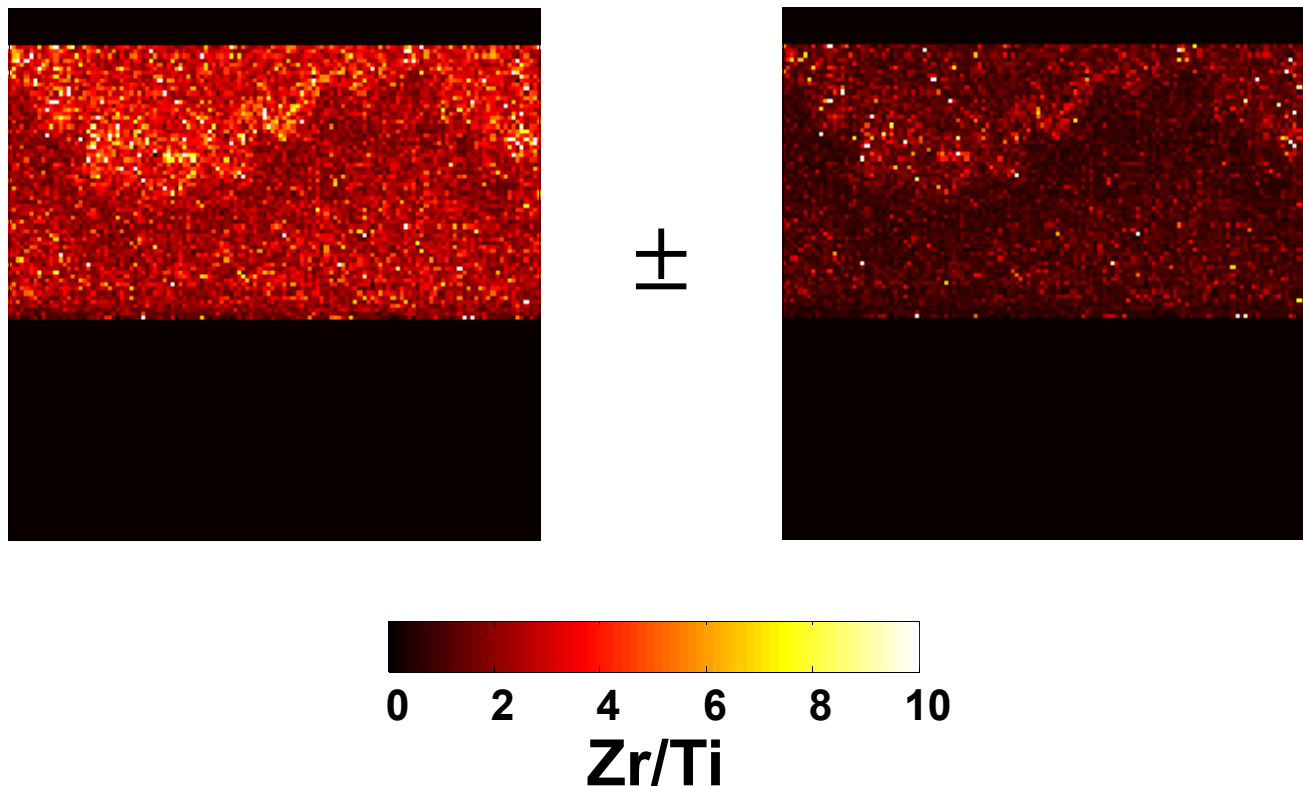


What if we apply our uncertainty equation point-by-point?

$$\Delta\left(\frac{C_A}{C_B}\right) = \frac{C_A}{C_B} \cdot \sqrt{\left(\frac{\Delta k_{AB}|_{1\sigma}}{k_{AB}}\right)^2 + \left(\frac{\sqrt{I_A}}{I_A}\right)^2 + \left(\frac{\sqrt{I_B}}{I_B}\right)^2}$$

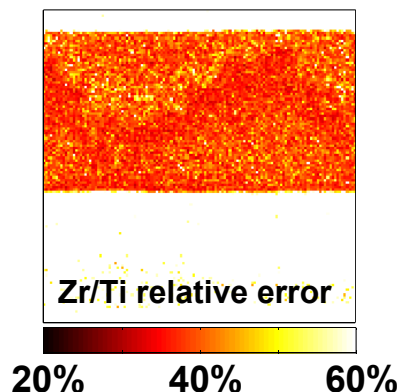


**We thus have cation fraction and
uncertainty with $\leq \approx 10$ nm resolution**

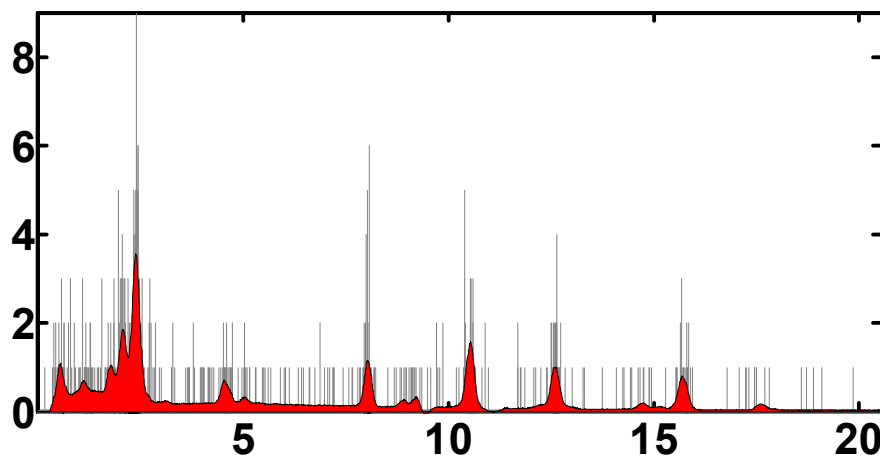


These uncertainties are very large – how to do better?

Uncertainties are $\approx 20\text{-}40\%$ relative:



This is a result of the small # counts/pixel:



How can we use MSA to improve our statistics?



PCA solutions can be mathematically rotated

PCA solution:

$$\mathbf{D} \approx \mathbf{CS}^T$$

$\mathbf{D}$ =data

$\mathbf{C}$ =score images

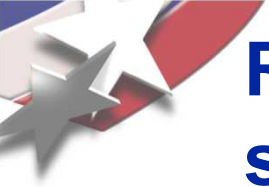
$\mathbf{S}$ =loading spectra

For some rotation $\mathbf{R}$:

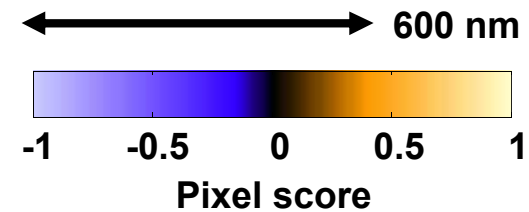
$$\mathbf{D} \approx \tilde{\mathbf{C}}\tilde{\mathbf{S}}^T = (\mathbf{CR})(\mathbf{R}^{-1}\mathbf{S}^T)$$

Choose $\mathbf{R}$ to maximize spatial contrast

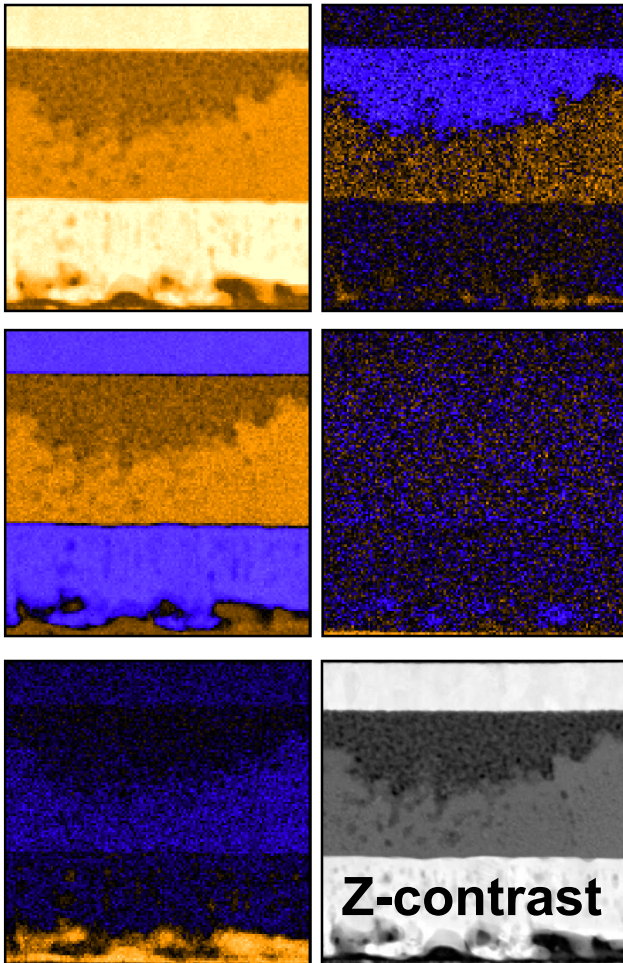




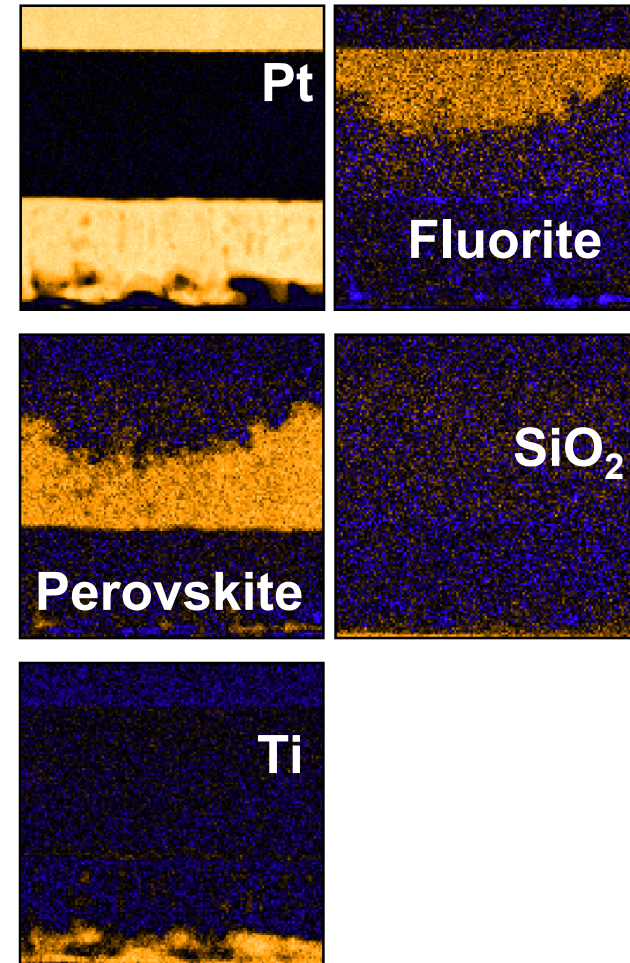
Rotate into a spatially-simple case



Highly mixed
score images



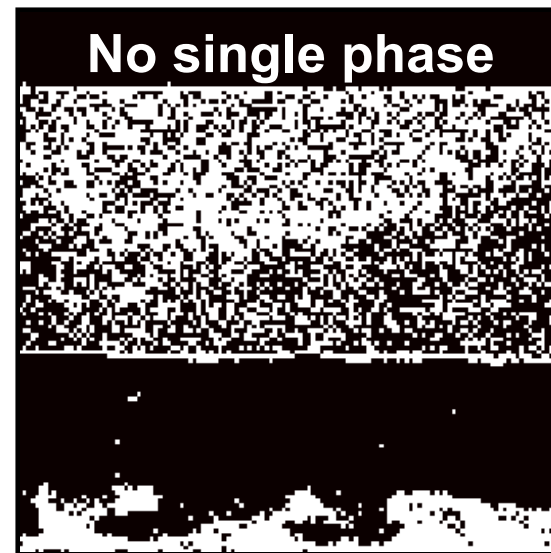
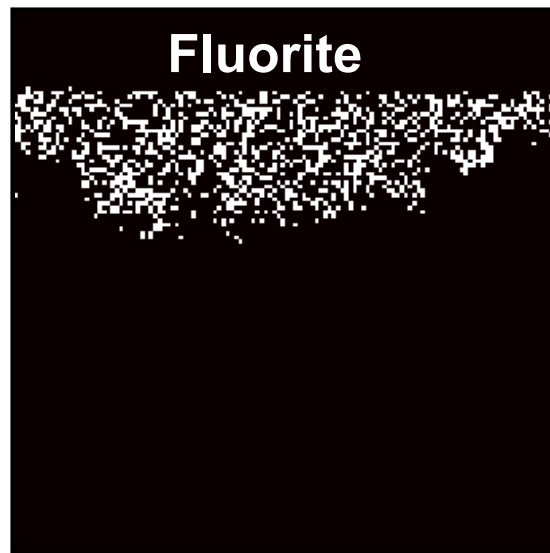
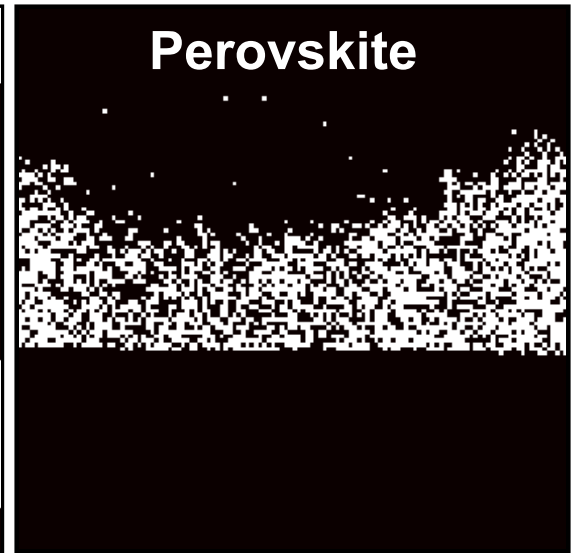
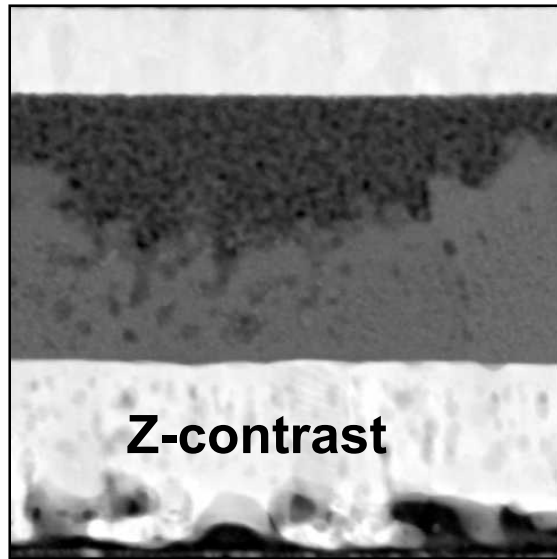
High-contrast
score images



$$C \rightarrow \tilde{C}$$

$$S \rightarrow \tilde{S}$$

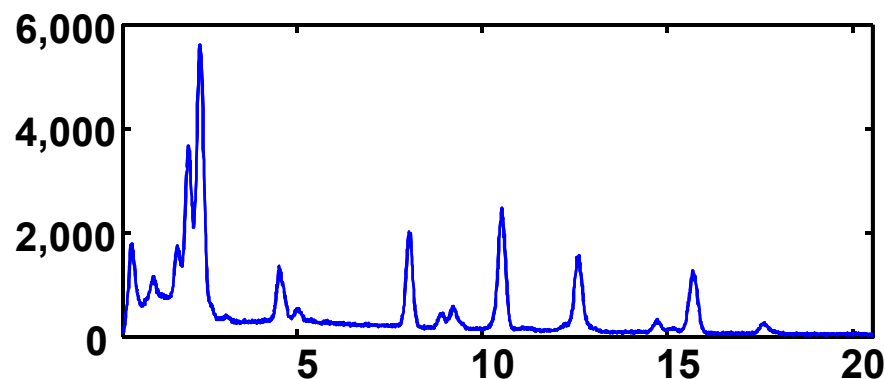
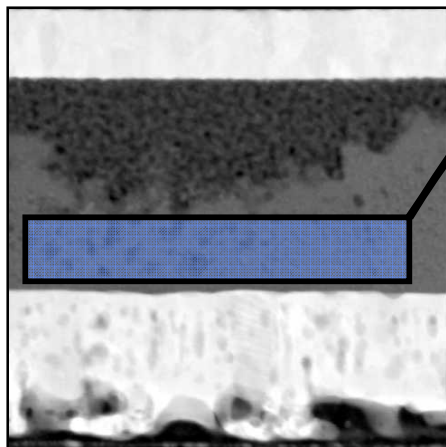
If $\geq 70\%$ of the counts in a pixel are from one PC, define it as single-phase



This is an unbiased way to perform phase analyses

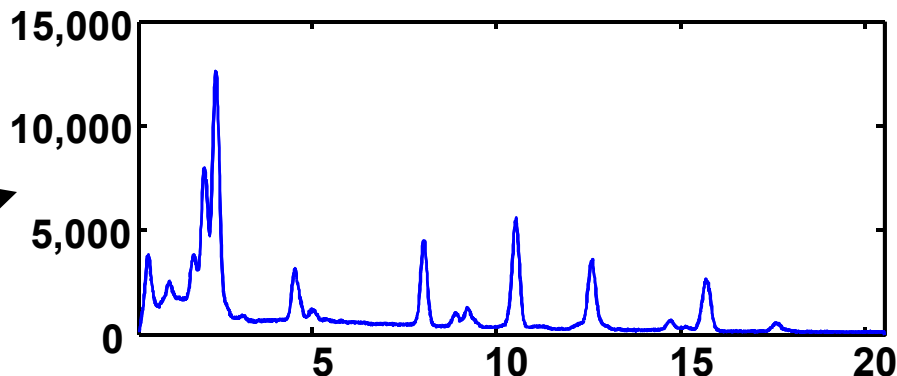
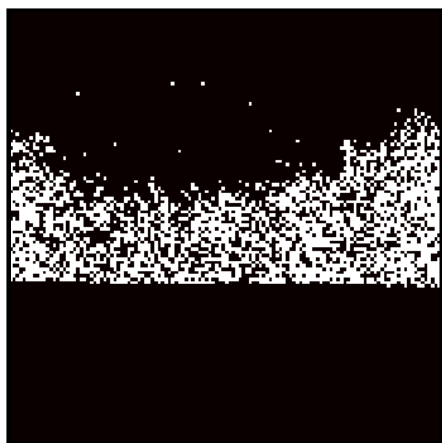
Manual method:

Choose a box with STEM software



This method:

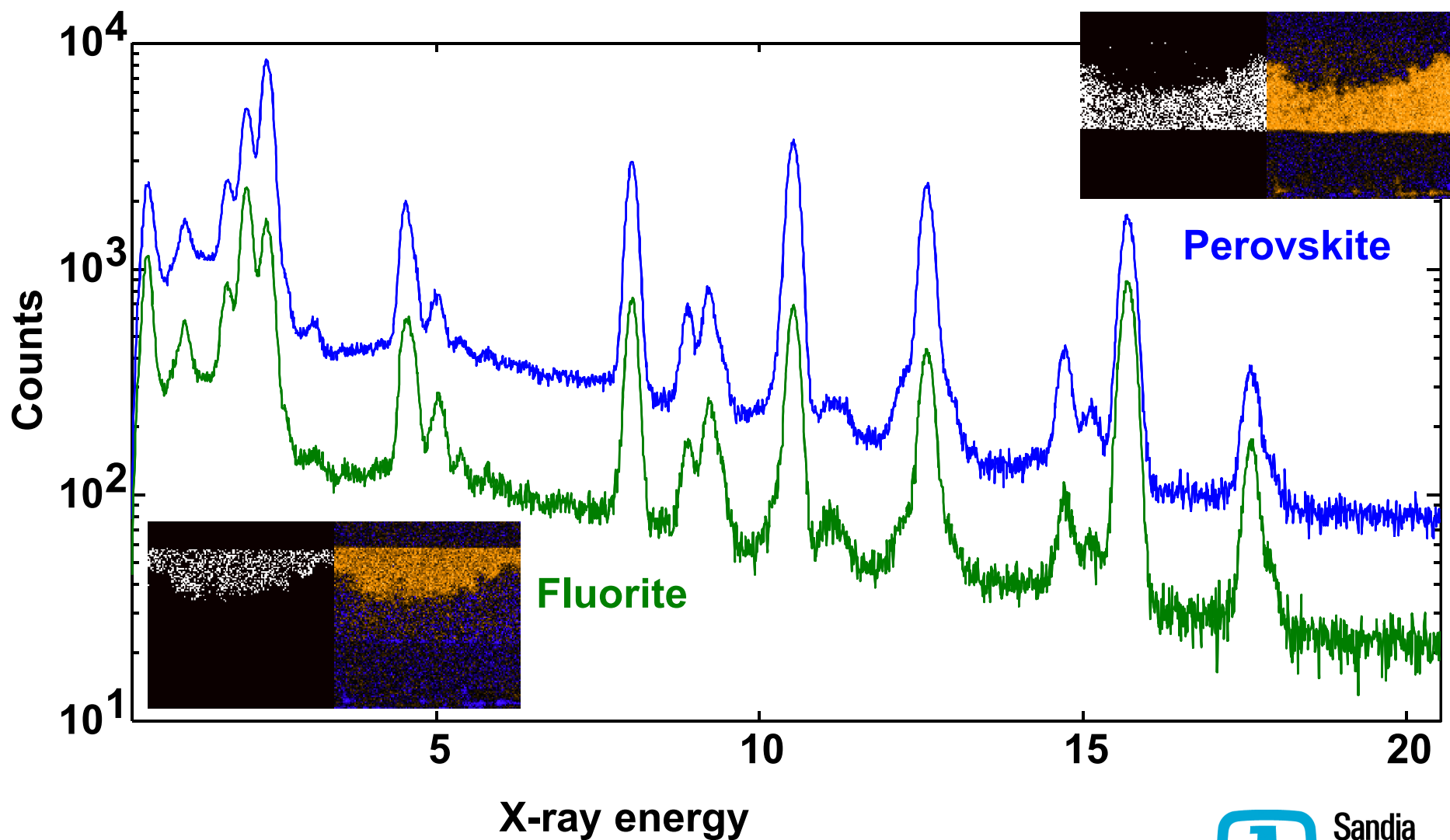
After-the-fact statistical selection



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This is an unbiased way to perform phase analyses





It's possible to use MSA to define phase boundaries for quantification

Single-pixel analysis gave 5-10 nm resolution, but $\approx 30\%$ errors ($\pm 1\sigma$) in cation content

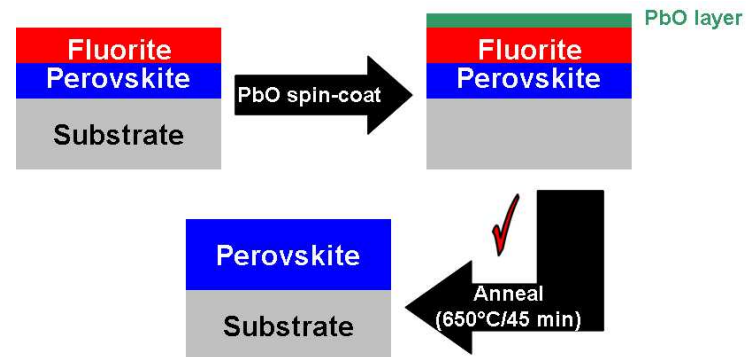
With MSA-defined phases, $<10\%$ error ($\pm 3\sigma$) in quantification:

	Cation fraction ratio								Cation fraction			
	Pb/(Zr+Ti)	Zr/Ti		La/Pb		La/(Zr+Ti)			Pb	Zr	Ti	La
Perovskite	0.86 $\pm$ 0.03	2.09	$\pm$ 0.14	0.18	$\pm$ 0.03	0.16	$\pm$ 0.02		43%	34%	16%	8%
Fluorite	0.34 $\pm$ 0.02	3.85	$\pm$ 0.28	0.52	$\pm$ 0.07	0.18	$\pm$ 0.02		22%	53%	14%	12%

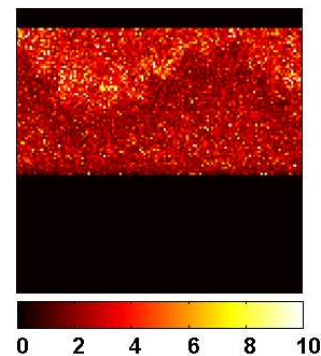
Of course, we can't speak about variations within a phase – we're assuming it's homogenous

We've quantified PLZT chemistry at high resolution, and are studying the statistics

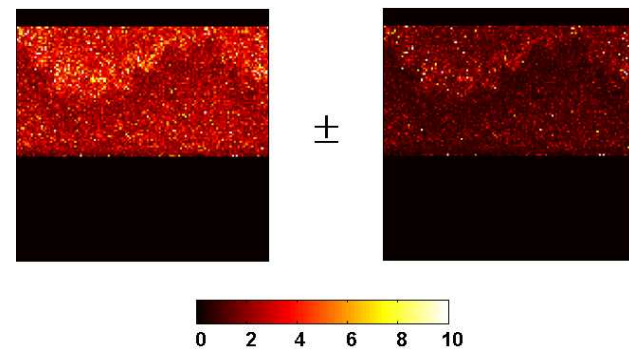
We produced single-phase perovskite without excess Pb-additions



Quantification of spectrum images allowed high-resolution study of segregation



We're exploring statistical error in quantitative SIs

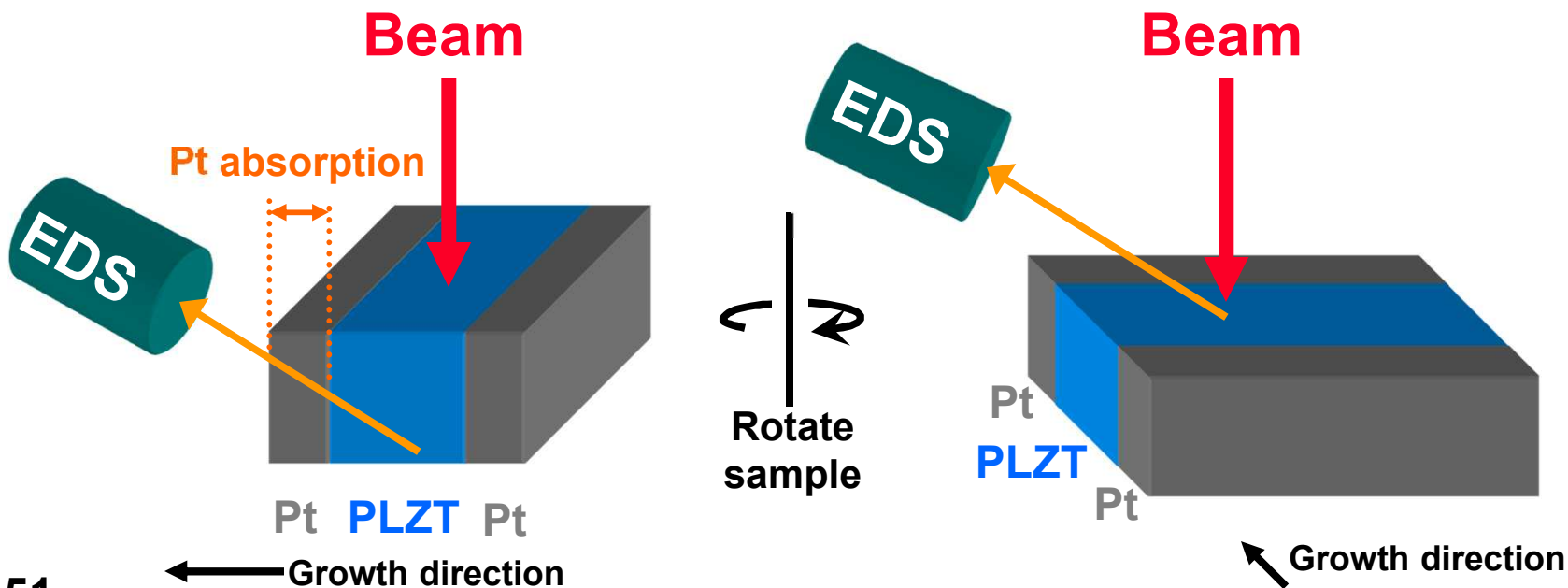


Platinum electrodes must be accommodated for

Platinum electrodes are sputtered above and below the films

Platinum will strongly absorb X-rays of interest

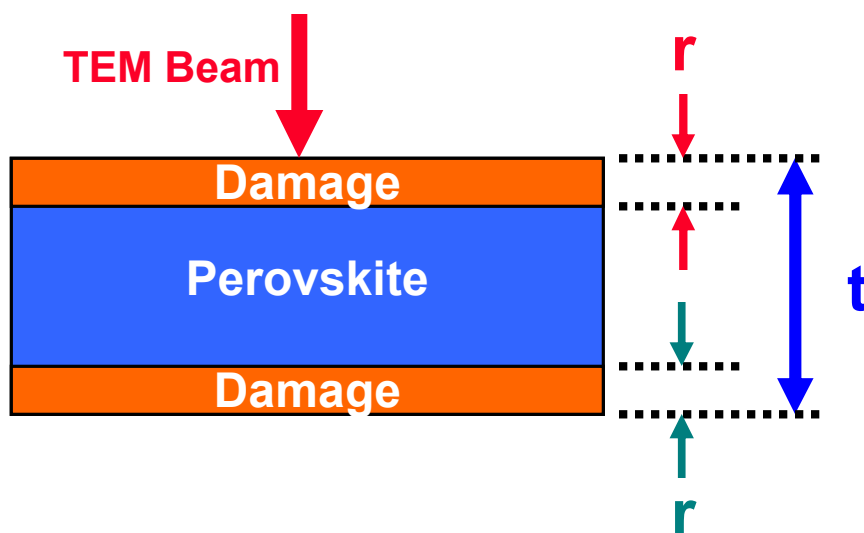
Should use a tilt-rotation holder in TEM to point the interfaces directly at the EDS to avoid absorption



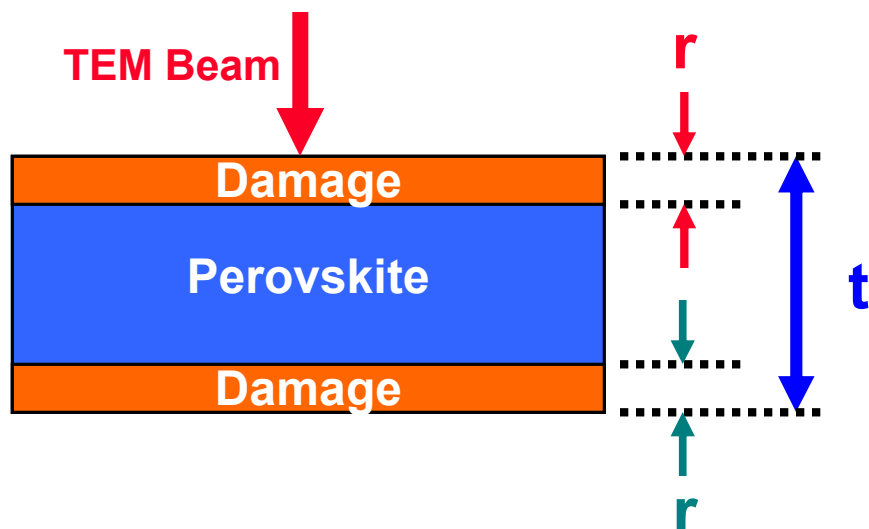
Errors in Pb quantification?

Oddly, the perovskite PZT is measured ~20% Pb deficient
→ Real or artifact? Still under investigation

Theory: Damage from FIB sample preparation



Errors in Pb quantification?



Let's make some assumptions:

$t = 100$ nm

Perovskite is $(t - 2r)$ thick, and has $C_{Pb} = 0.5$

Damaged layers are each r thick, and have $C_{Pb} = 0.25$

EDS measured $C_{Pb} = (0.5 \times (t - 2r)) + (0.25 \times 2r) = 0.4$

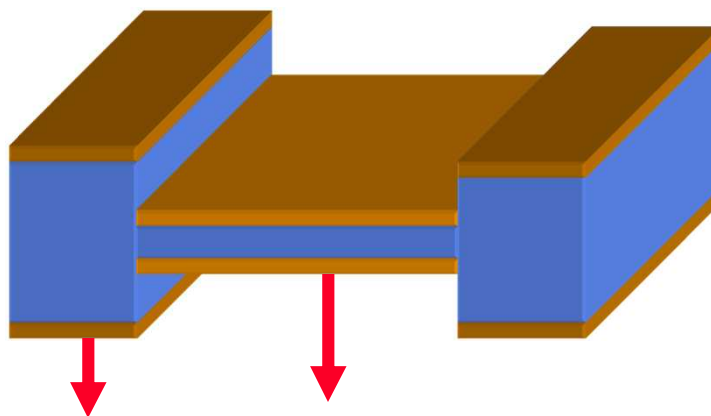
Thus, $r \approx 20$ nm $\leftarrow$ reasonable for FIB-damage



Errors in Pb quantification?

Further analysis:

- FIB-lift out sections are dog-bone shaped
- EDS of different thicknesses → different Pb-fractions



Measured C_{Pb} : ~0.48 ~0.40

- Assume the thick section has $t=300$ nm, $r=20$ nm
- Assume C_{Pb} of 0.50 and 0.25 in thick-section perovskite and damaged layer

Expect to measure $C_{Pb} \sim 0.46$; actually measure $C_{Pb} \sim 0.48$

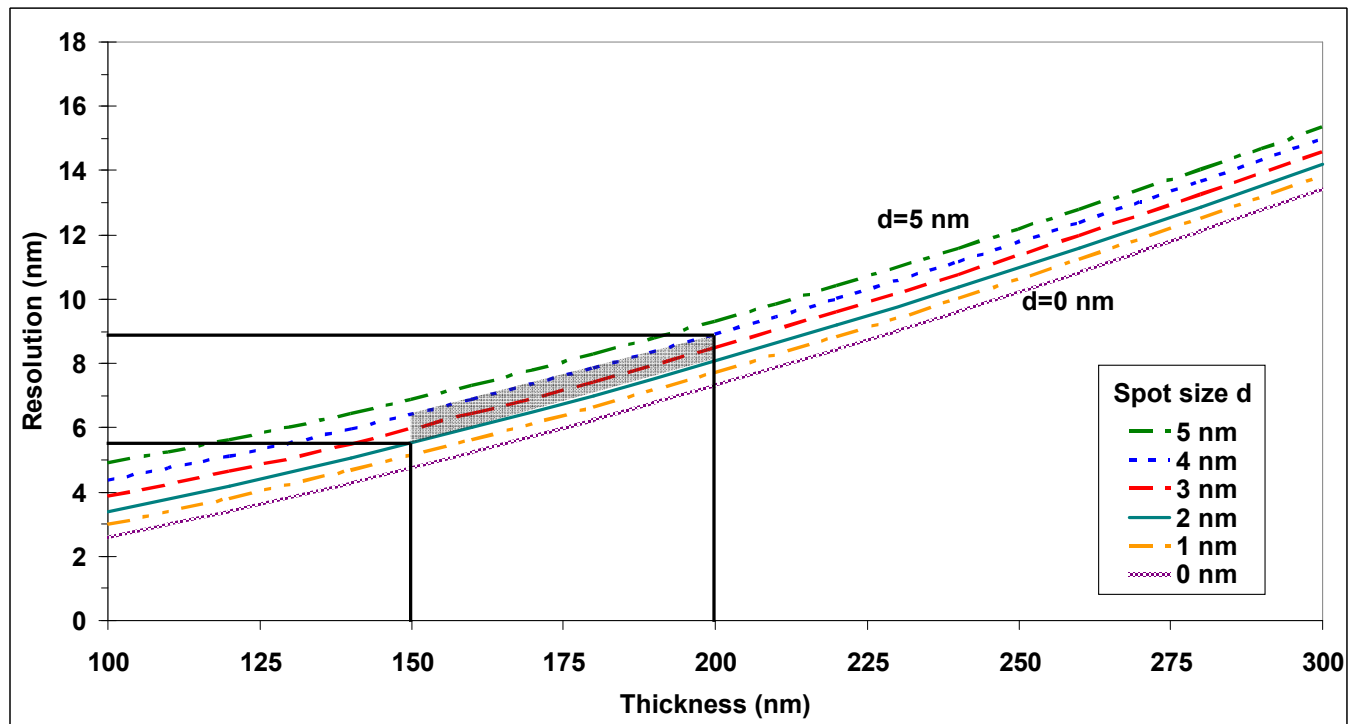
Spatial resolution

$$b = 7.2 \times 10^5 \left(\frac{\langle Z \rangle}{E_0} \right) \left(\frac{\rho}{\langle A \rangle} \right)^{\frac{1}{2}} (t)^{\frac{3}{2}}$$

$$R = \frac{\left[d + (b^2 + d^2)^{\frac{1}{2}} \right]}{2\sqrt{2}}$$

$\langle Z \rangle$ = average atomic number
 $\langle A \rangle$ = average atomic mass [=] g/mol
 E_0 = beam energy [=] eV
 ρ = density [=] g/cm³
 d = spot size [=] cm
 t = thickness [=] cm

Michael et al. J. Microsc., V160, P.41 (1990)
 Reed, Ultramic., V7, P.405 (1982)



Pixel
 size
 3.9 nm