

# Enhancing solar energy harvesting with quantum-dot monolayer on a photonic crystal

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Sandia  
National  
Laboratories

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# Outline

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- Motivation
- PV paradigms
- Photonic crystal
  
- Photonics: Radiative control
  - Solar photovoltaic
  - Solar thermal photovoltaic
  - Near-field thermal photovoltaic

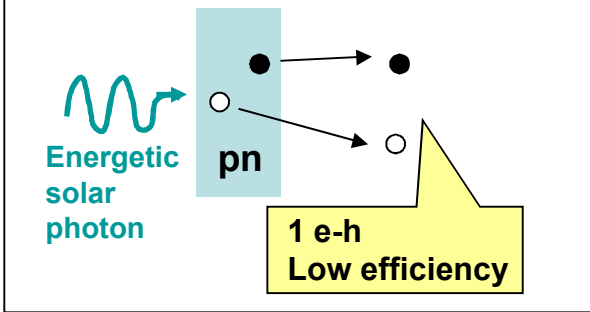
**Explore photonic density of states control  
for  
solar energy applications**

# PV cell paradigms

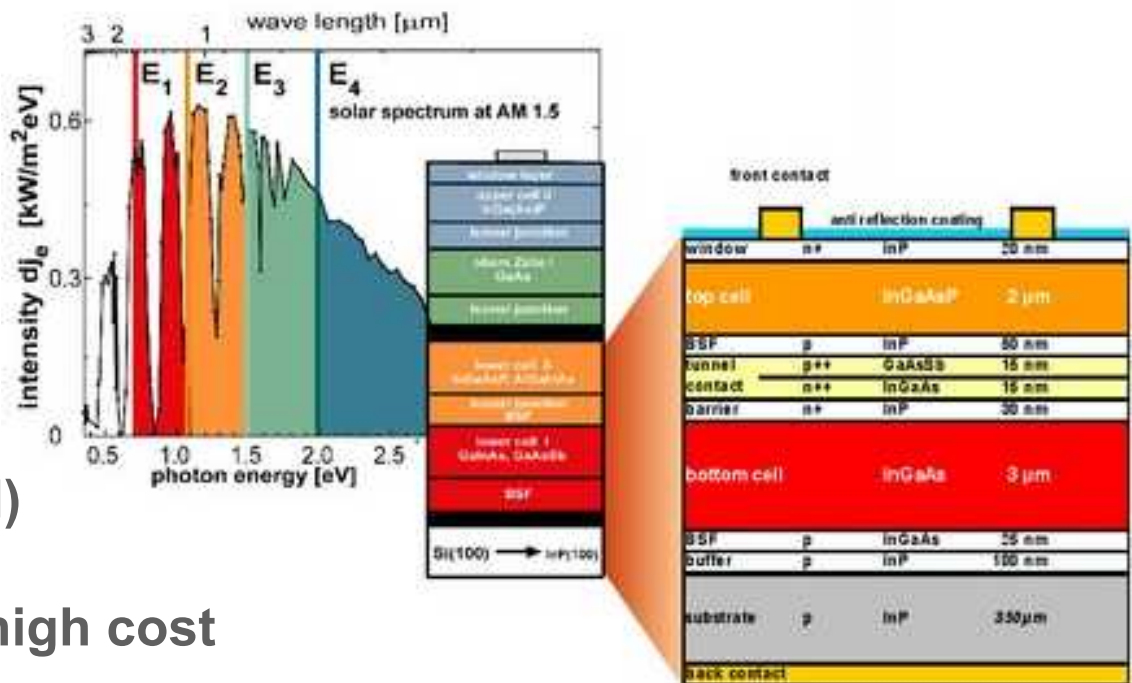
- Holy grail of photovoltaic cell is high performance and low cost

[Third generation photovoltaics by Martin Green, Springer 2003]

One photon, one e-h pair



- 1 photon produces 1 e-h pair
- Efficiency tops at 32% for single junction

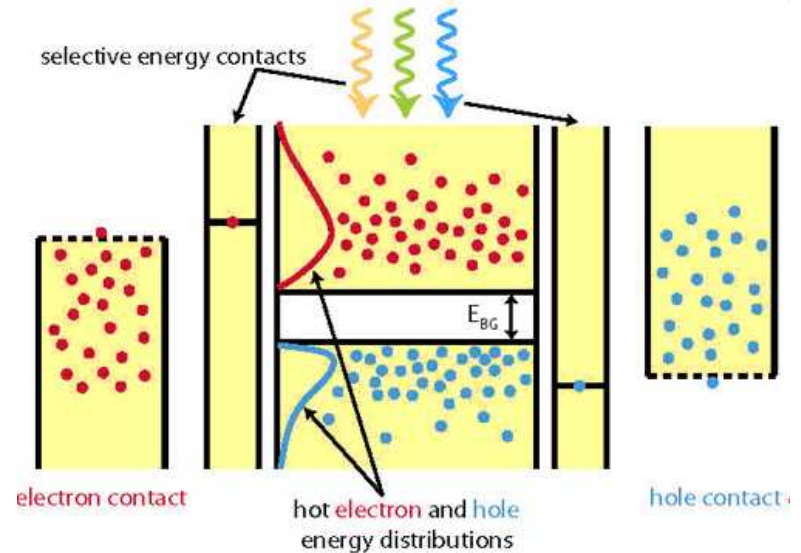


- Tandem cells (multi-energy-threshold)
- >40% efficiency
- high performance and high cost

# PV cell paradigms

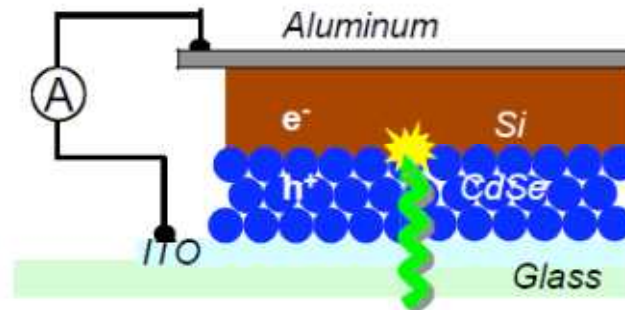
- Hot carriers harvesting
- Use quantum mechanical resonant tunneling structures

Martin Green



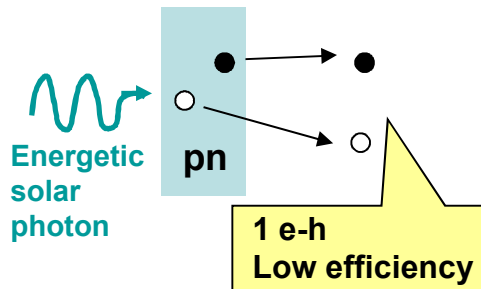
- Quantum dot based solar cell
- Low cost potential

Klimov



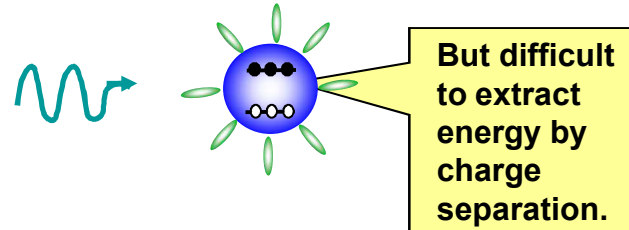
# Photonic crystal solution to the energy extraction problem from quantum dots

## One photon, one e-h pair



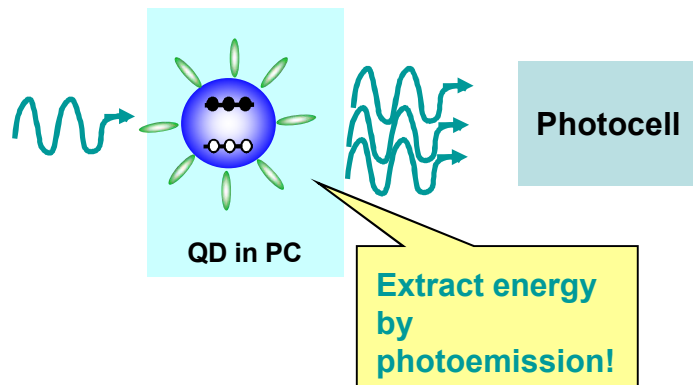
solution

## Multi-exciton generation (MEG)



solution

## Optical stepdown transformer approach



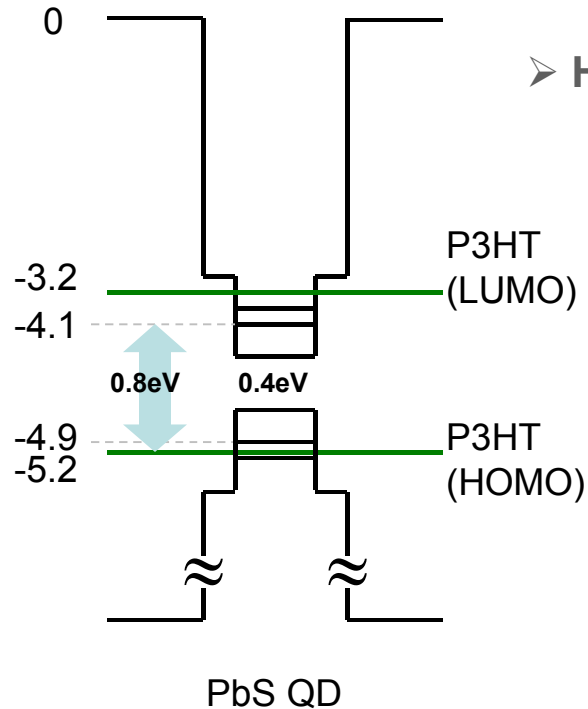
### ➤ Mechanism

Impact ionization, inverse Auger effect, quantum confinement effect of multi-e-h interaction..?

### ➤ Impact to solar cell efficiency: 36-42% for MEG threshold from $3E_g$ to $2E_g$ .

[V. I. Klimov, "Detailed-balance power conversion limits of nanocrystal-quantum-dot solar cells in the presence of carrier multiplication," Applied Physics Letters **89** (12) (2006).]

# Why PbS quantum dots?



➤ Harvest IR part of solar spectrum  
Low exciton energy (0.8eV), size tunable to 0.6eV.

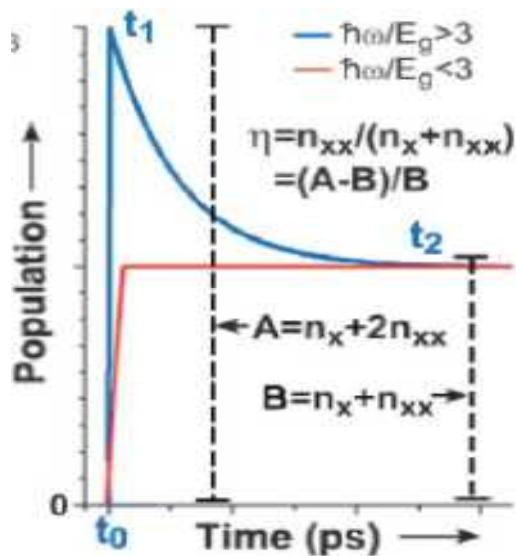
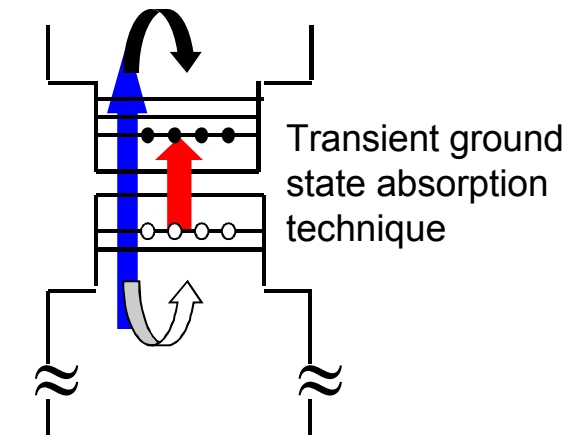
➤ 7 excitons generation reported

➤ Good photonic crystals can be fabricated

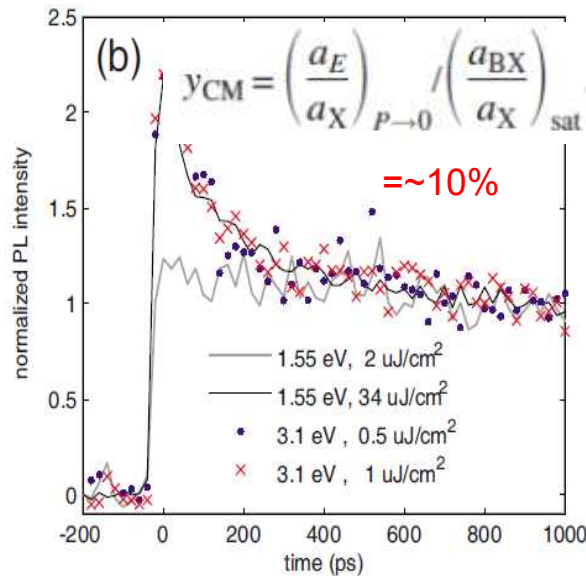
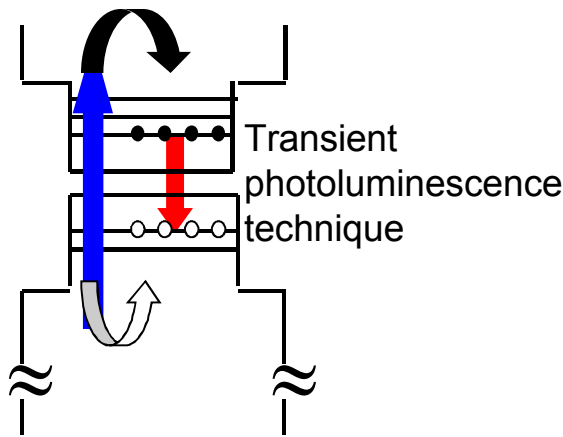
➤ Good potential solar cell candidate



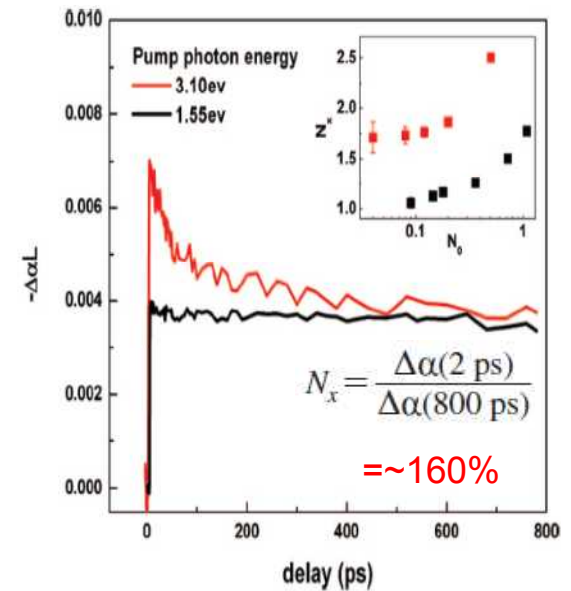
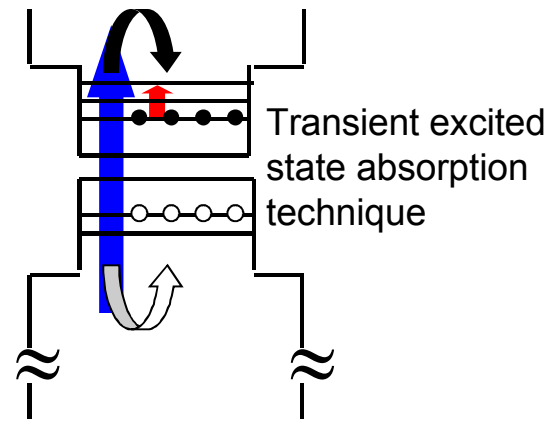
# Is MEG real or not?



R. D. Schaller and V. I. Klimov, "High Efficiency Carrier Multiplication in PbSe Nanocrystals: Implications for Solar Energy Conversion," *Physical Review Letters* **92** (18), 186601 (2004).



G. Nair, S. M. Geyer, L. Y. Chang et al., "Carrier multiplication yields in PbS and PbSe nanocrystals measured by transient photoluminescence," *Physical Review B* **78** (12) (2008).



Minbiao Ji, Sungham Park, Stephen T. Connor et al., "Efficient Multiple Exciton Generation Observed in Colloidal PbSe Quantum Dots with Temporally and Spectrally Resolved Intraband Excitation," *Nano Lett.* **9** (3) (2009).



# Planck radiation law and density of states

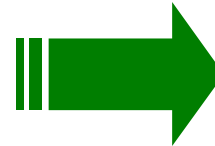
Planck distribution: Mean energy density within  $k$  and  $k+dk$  is

$$u(\omega, T)d\omega = 2\hbar\omega f(k)d^3k = \hbar\omega \frac{\omega^2 d\omega}{\pi^2 c^3} \frac{1}{e^{\hbar\omega/kT} - 1} = \frac{8\pi\hbar c}{\lambda^5} \frac{d\lambda}{e^{hc/\lambda kT} - 1}$$

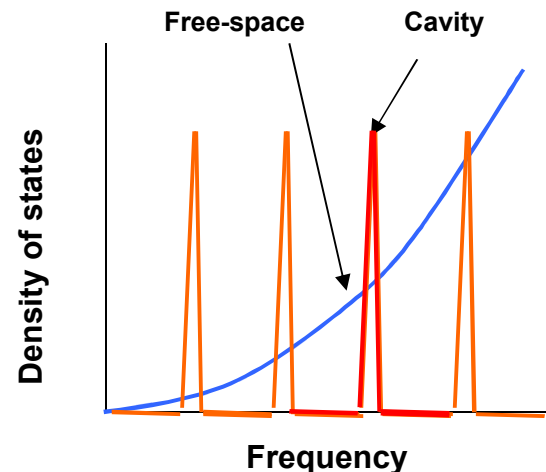
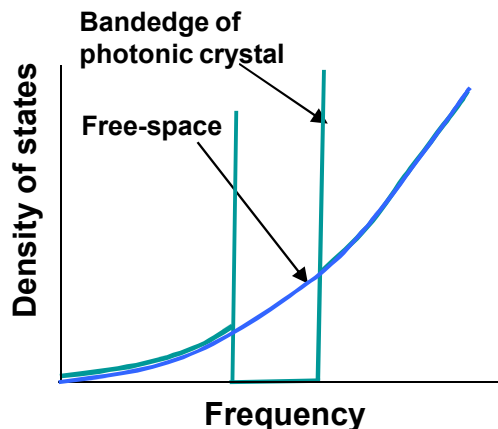
Free space density of states –  
no. of modes per unit frequency  
per unit volume

Mean photon number

*In photonic crystal,  
size of voids are less than the  
characteristic wavelength  
dimension*



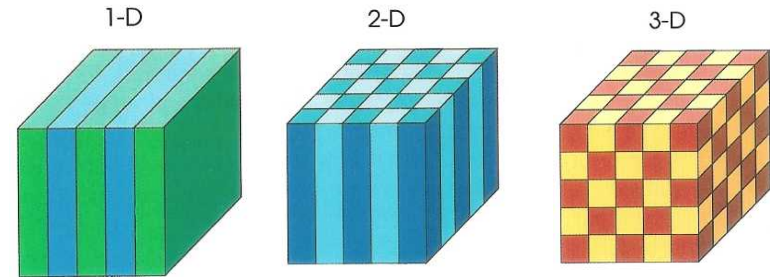
**Non-free-space  
density of states**



# Photonic crystals

**Photonic crystal:** In this context:  $a \sim \lambda$

- A **periodic array of electromagnetic scattering centers** with period comparable to wavelength results in the creation of regions of forbidden propagation commonly termed “**spectral gaps**” or “**band-gaps**”
- Bragg condition alone is insufficient to create an omni-directional bandgap.
- Threshold value of  $\epsilon(r)$  is also needed.



## Principle of PBG Operation:

An electromagnetic wave passing throughout an array of periodic scatterers will undergo destructive interference for certain combinations of wave-vectors at certain frequencies, thus forbidding propagation for such wave-vectors at these frequencies.

$$\left[ \nabla \times \left( \frac{1}{\epsilon(\vec{r})} \nabla \times \right) \right] \vec{H}(\vec{r}) = \left( \frac{\omega}{c} \right)^2 \vec{H}(\vec{r})$$

## Metamaterial:

A metamaterial (or meta-material) is a material which gains its properties from its structure rather than directly from its composition. To distinguish metamaterials from other composite materials, the *metamaterial* label is usually used for a material which has unusual properties.

**In general:  $a \ll \lambda$**

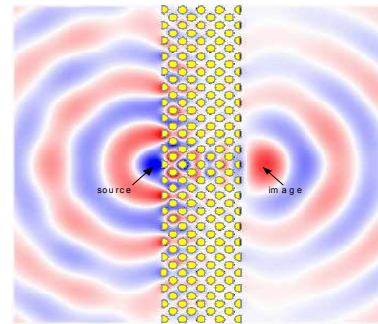
# Photonic crystal bandstructure anatomy

## Bandgap region

- Inhibit spontaneous emission
- Nanocavity
- Waveguides

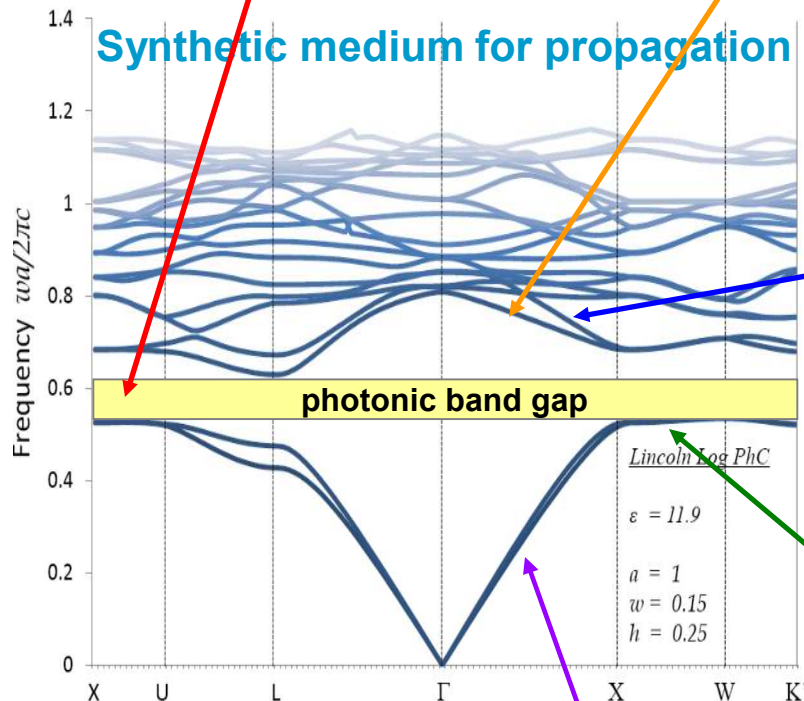
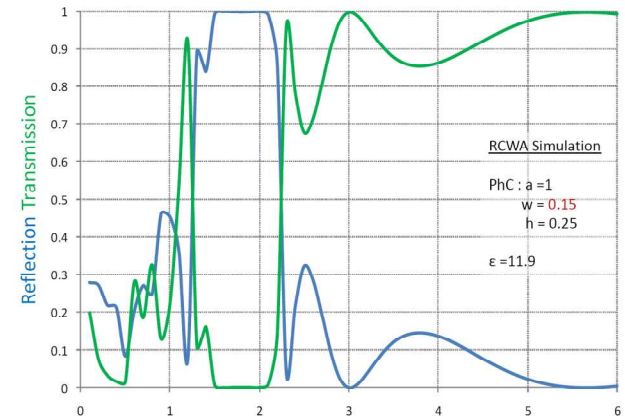
## Backwards slope means

- Negative refraction
- Subwavelength imaging



## Strong curvature:

- Super-prisms
- Dispersion control



## Linear dispersion region

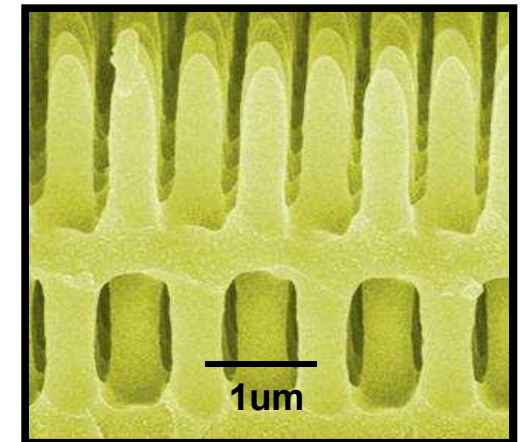
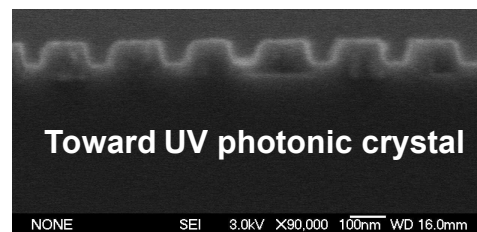
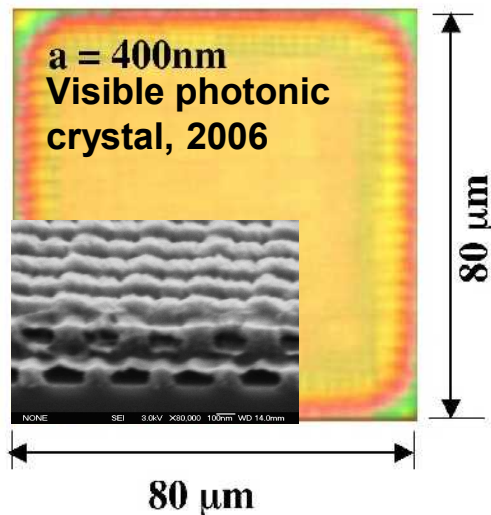
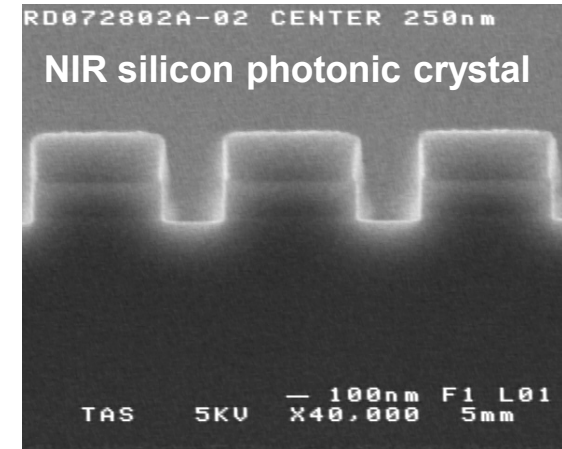
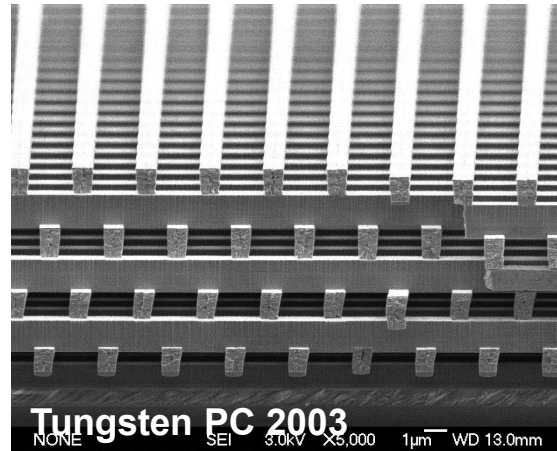
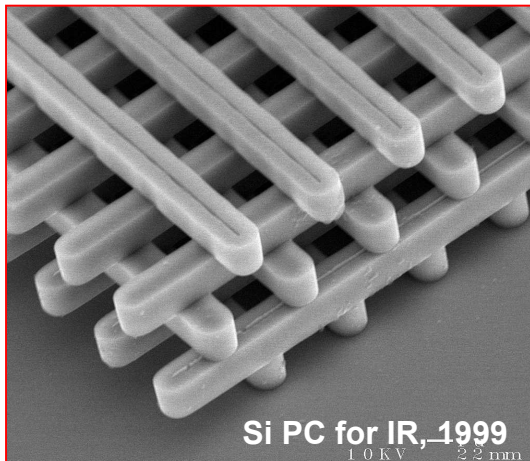
- Optical waveguide and circuits

## $d\omega/dk \rightarrow 0$ :

- Slow light,
- High photon density of states
- Enhance spontaneous emission

# Photonic Crystal Fabrication at SNL

- Enabling fabrication technologies - Low temperature, low stress CMOS compatible and large volume fabrication.



- Other fabrication techniques: proximity field lithography, DXRL, EBL.

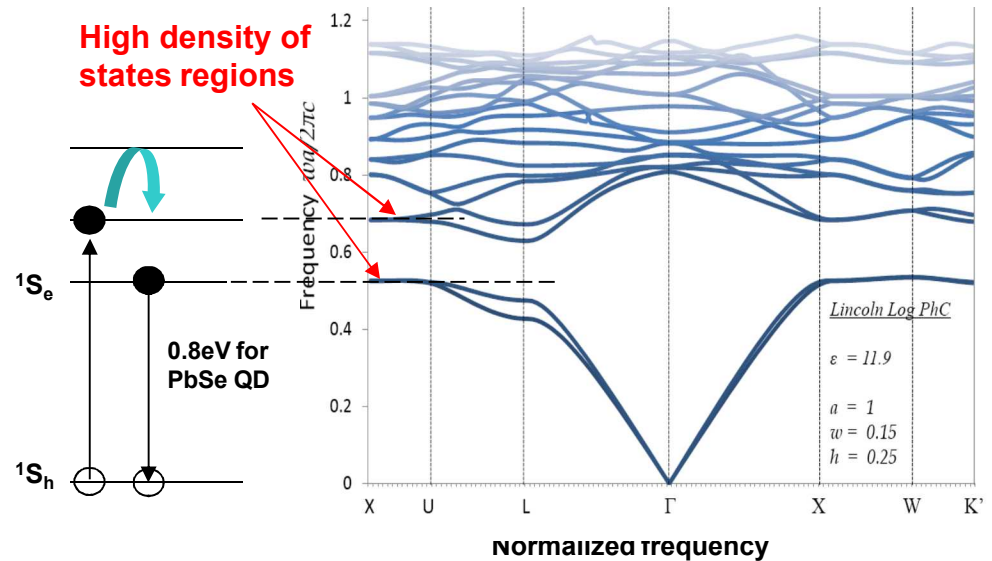


# Radiative properties control by photonic crystals: Band edge effect

## Band edge effect

Slower group velocity means high density of states which increases absorption coefficient.

## Out-compete non-radiative process



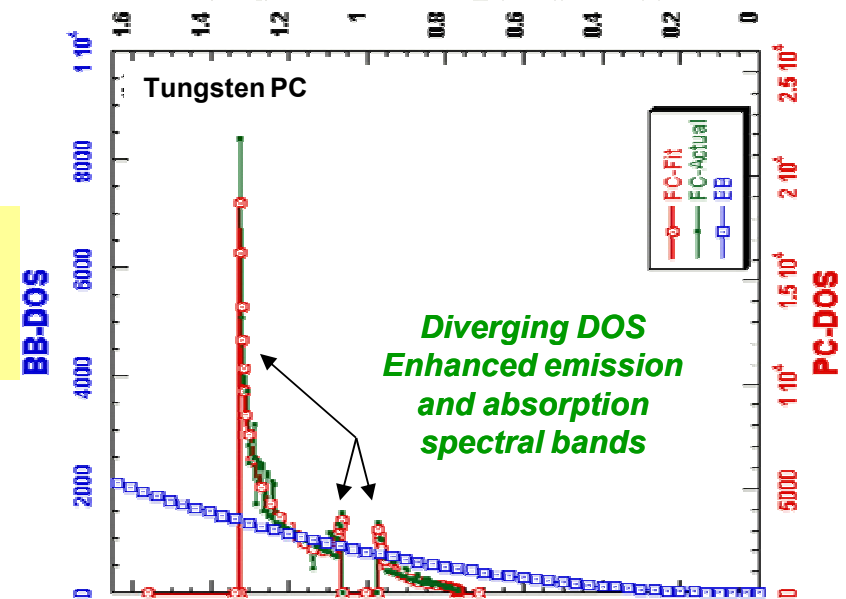
## Radiative transition rate

$$\Gamma_{eg} = \frac{2\pi}{\hbar^2} \sum_{k,n} \left| \langle g, 1_{k,n} | \vec{d} \cdot \vec{E}(\vec{x}_0) | e, vac \rangle \right|^2 \delta(\omega_{k,n} - \omega_0)$$

$$\Gamma_{eg} = \frac{\pi \omega_0 |\vec{d}|^2}{\epsilon_0 \hbar} \rho(\vec{x}_0, \frac{\vec{d}}{|\vec{d}|}, \omega_0)$$

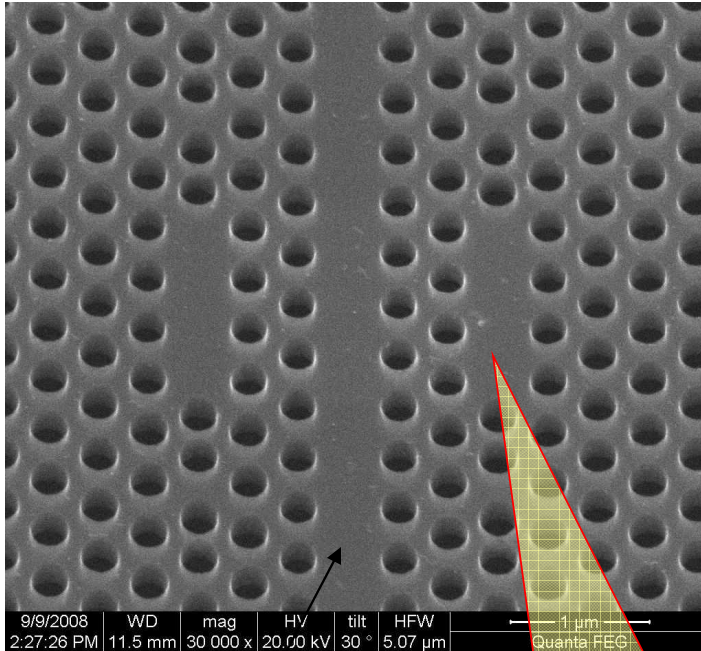
**Photonic density of states engineering**

$$\vec{E}(\vec{x}_0) = \sum_{k,n} \sqrt{\frac{\hbar \omega_{k,n}}{2\epsilon_0 V}} (\vec{E}_{\vec{k},n}(\vec{x}_0) \hat{a}_{\vec{k},n} + h.c.)$$



I. El-Kady et. al. "Emission from an active photonic crystal",  
Phys. Rev. B, vol. 72, 195110 (2005)

# Radiative properties control by photonic crystals: Purcell effect



Waveguide

Purcell enhancement factor

$$P = \frac{3}{4\pi^2} \left( \frac{\lambda}{n} \right)^3 \frac{Q}{V}$$

Spontaneous emission enhancement factor

$$\frac{\tau}{\tau_0} = \left( \frac{3\lambda_C^3 Q}{4\pi^2 n^3 V_m} \right) \times \zeta_r \times \left( \frac{\Delta\lambda_C^2}{\Delta\lambda_C^2 + 4(\lambda_C - \lambda_X)^2} \right) + f,$$

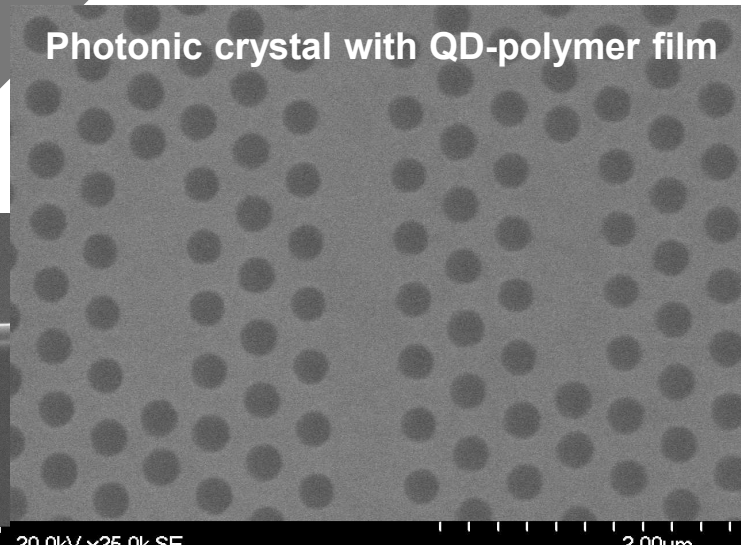
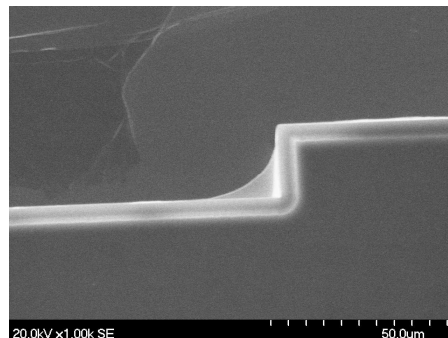
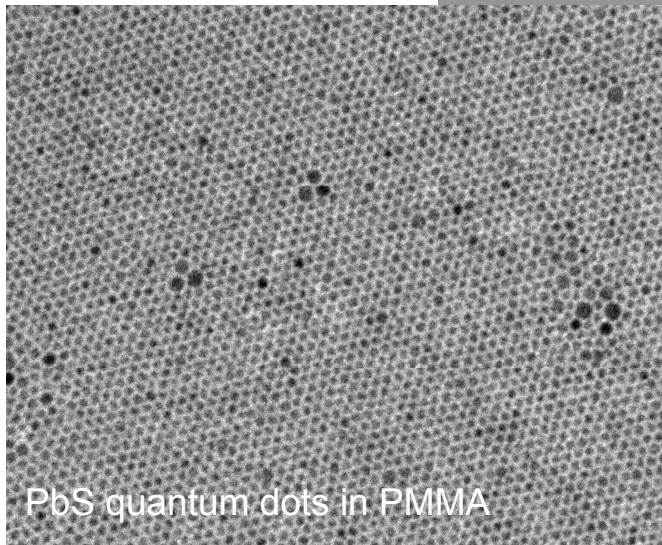
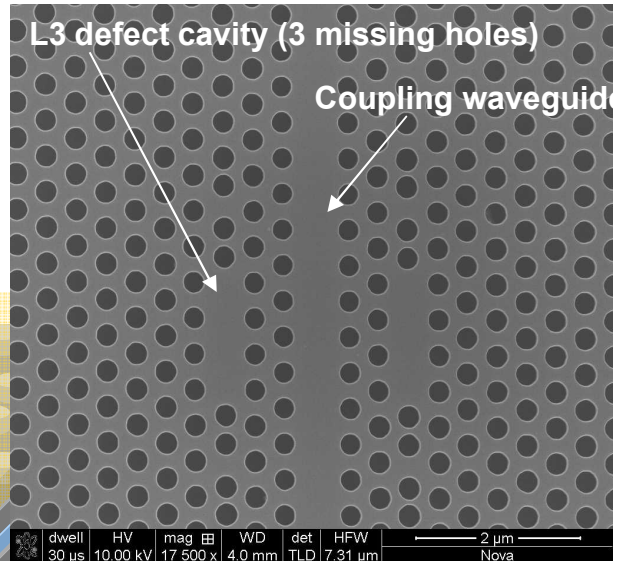
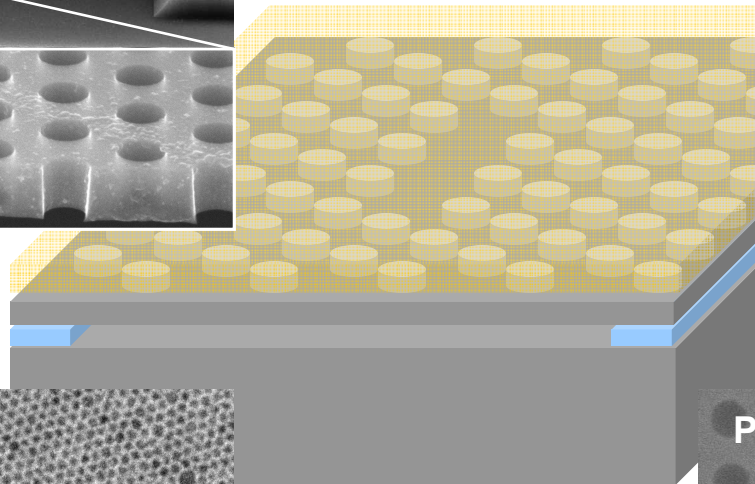
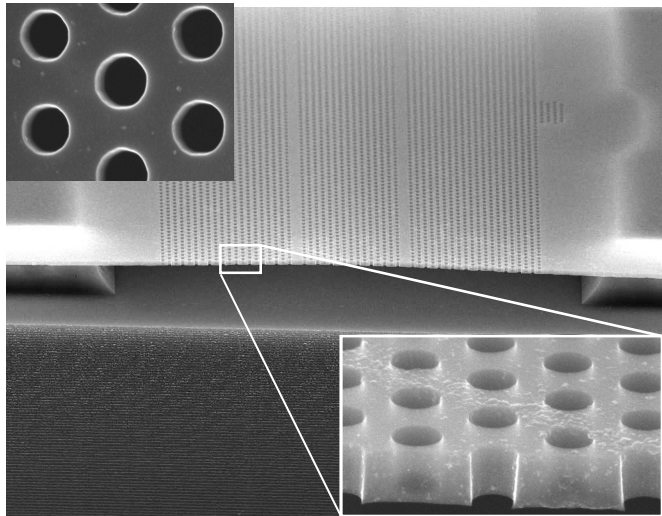
Enhancement factor

Purcell factor  
(interaction strength with vacuum field in a small confined volume)

Cavity resonance effect

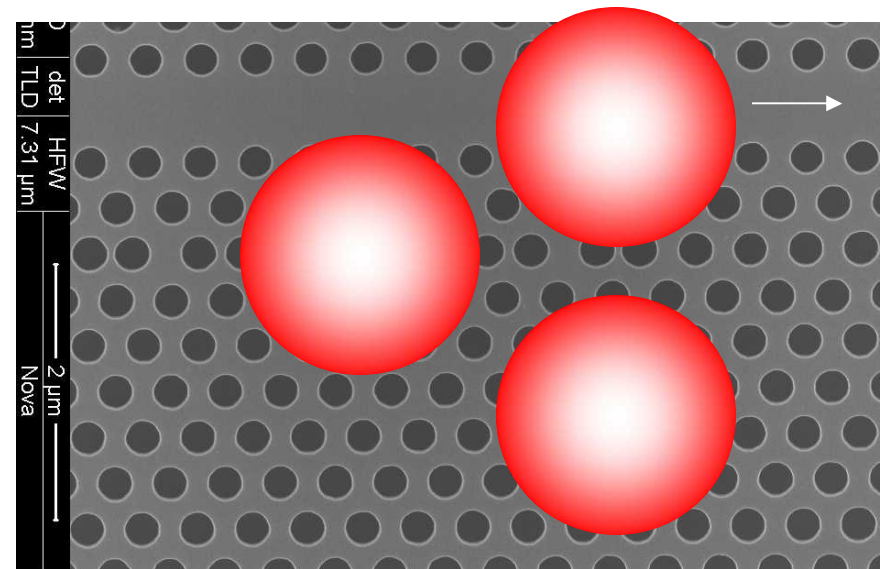
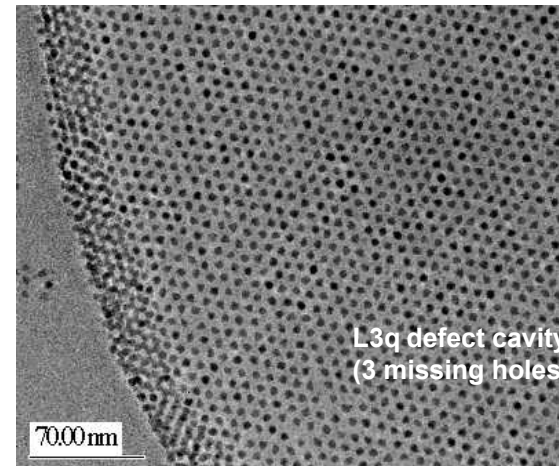
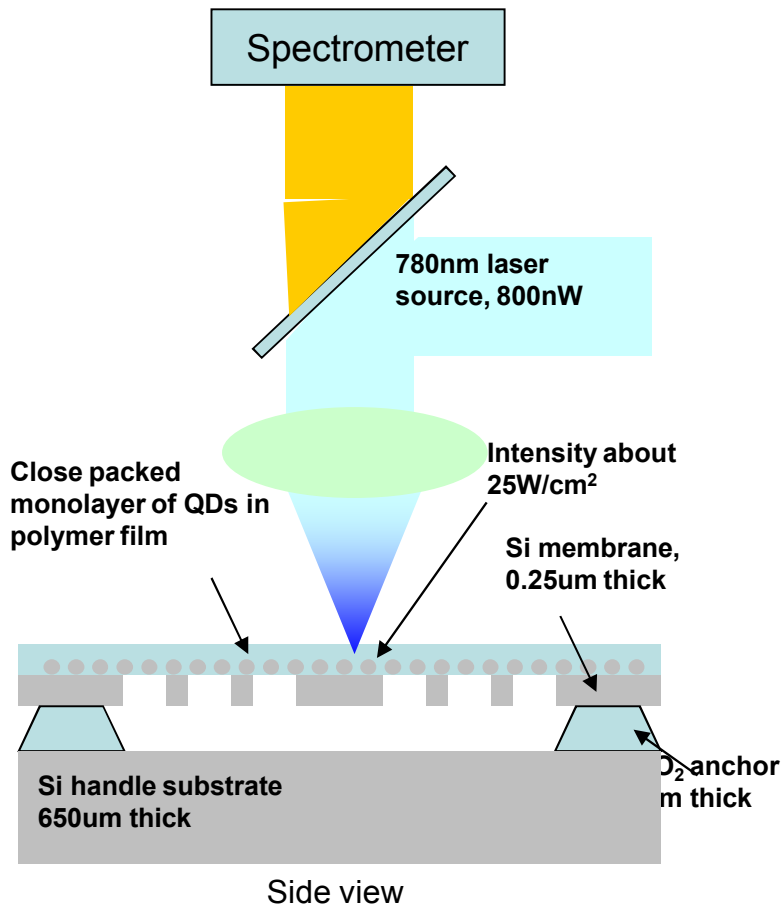
- Mode volume is less than  $(\lambda/n)^3$ .
- $Q = 10^6$  demonstrated.
- $Q$  of  $10^9$  is possible.
- Purcell factor of  $10^5$ .

# Photonic crystal fabrication

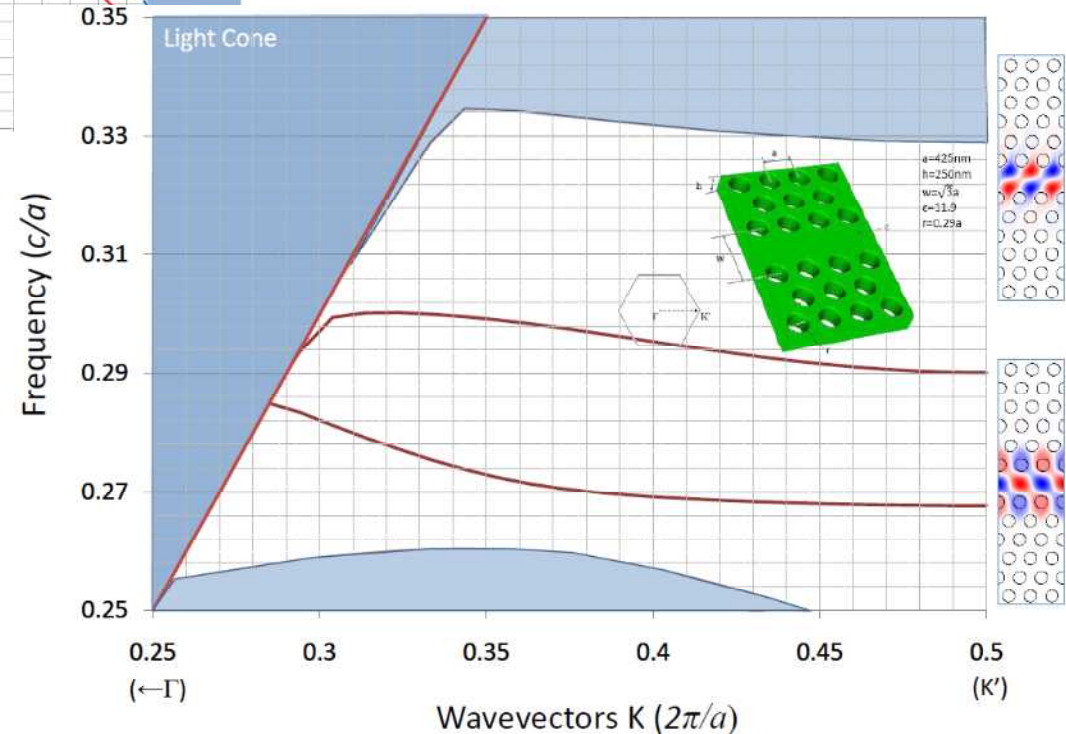
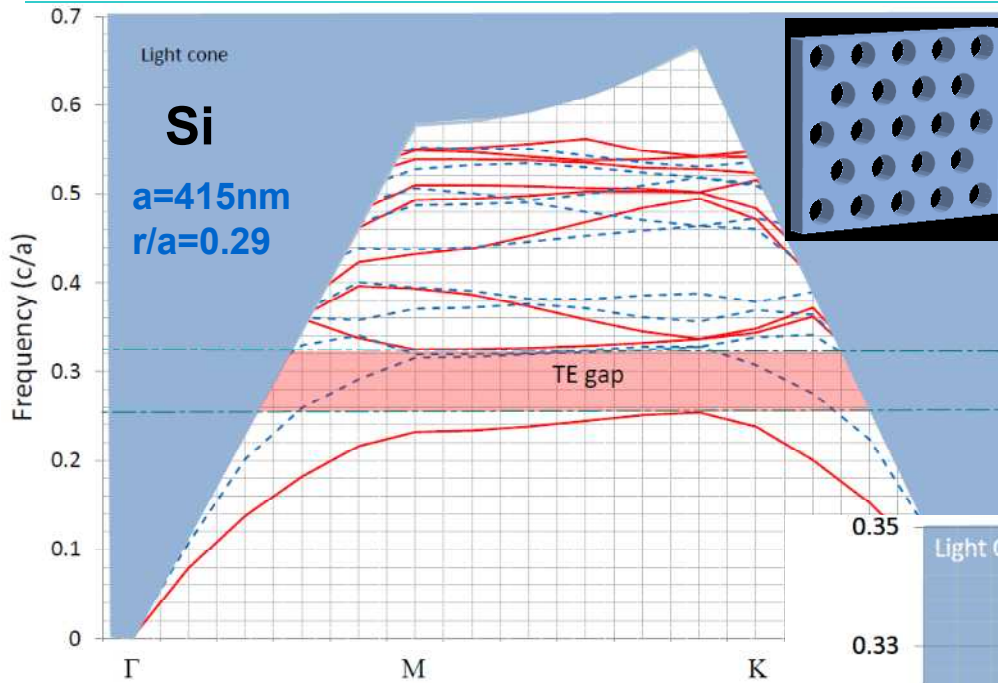




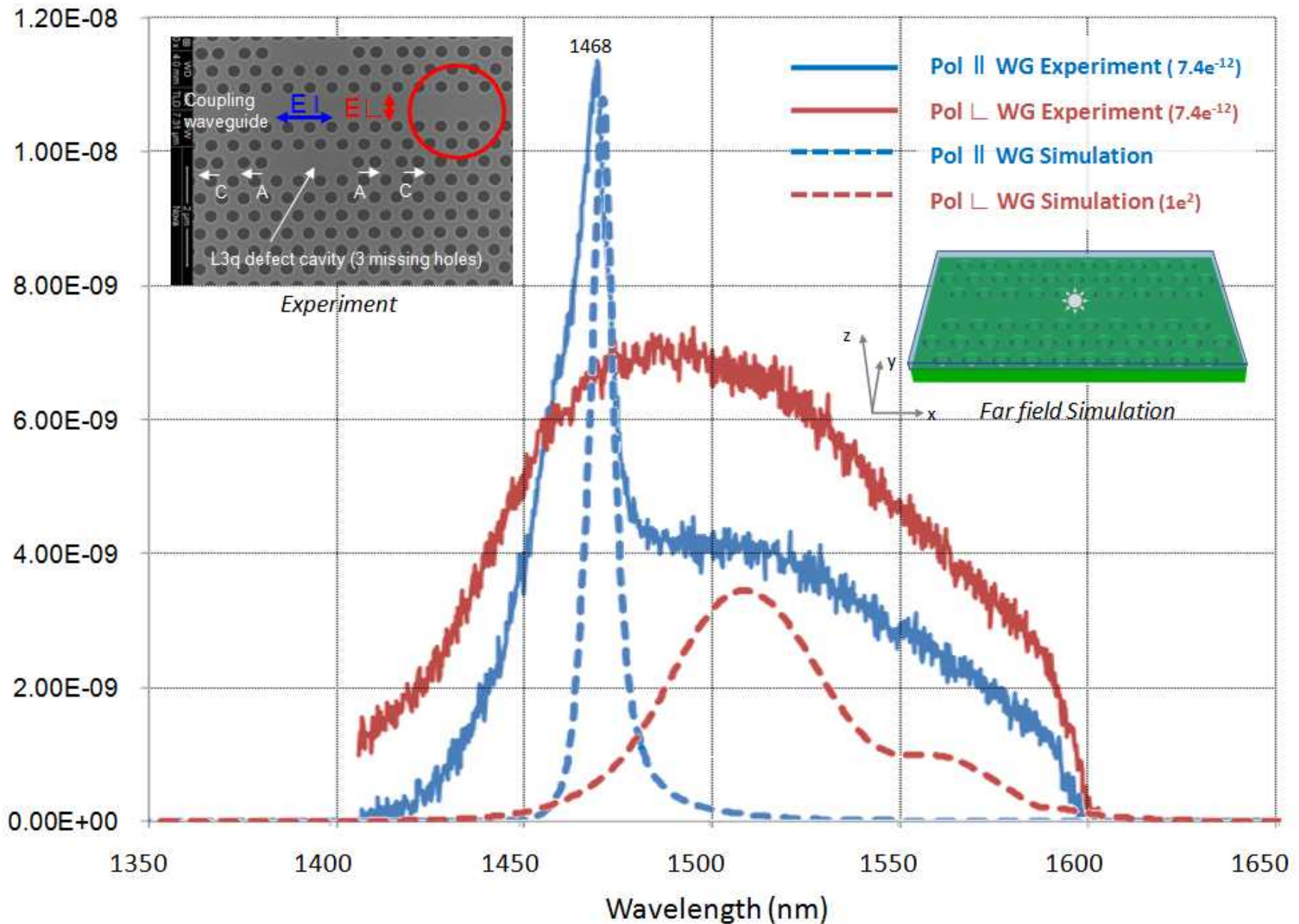
# Photoluminescence experiment from Quantum dots



# Bandstructure and waveguide defect of air-clad Si photonic crystal

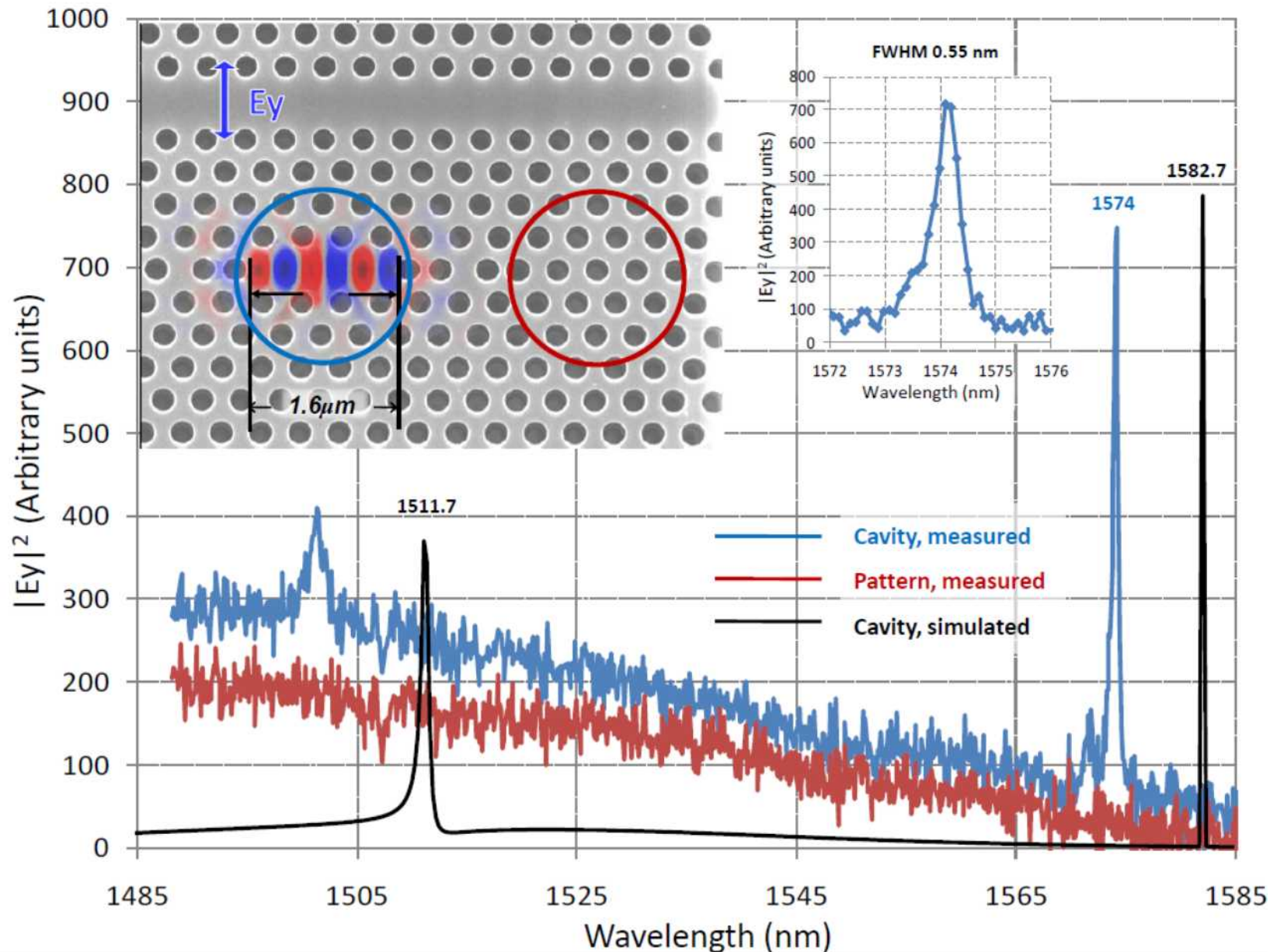


# Enhanced Emission from Quantum dots on photonic crystal waveguide





# Enhanced Emission from Quantum dots on photonic crystal cavity



# Enhanced Factor determination

$$\text{Enhancement factor} = \frac{\text{Emission observed from the cavity at resonant frequency}}{\text{Reference emission}}$$

**What is a good reference?**

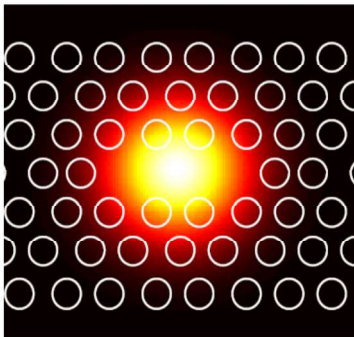
Emission from the pattern surface,  
Emission from the cavity but wrong polarization,

**What about the contributions from dots that are not in the cavity or at the cavity node?**

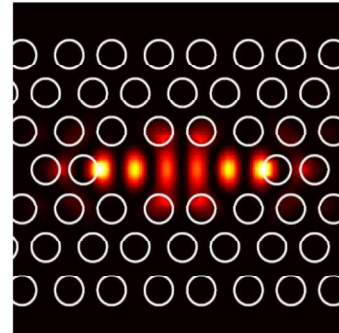
$$\text{Enhancement factor} = \frac{8}{0.157} = 51$$

$$\frac{\Gamma_c}{\Gamma_0} = \frac{Q}{V} \left( \frac{3\lambda^3}{4\pi^2 n^3} \right) \left( \frac{E_{\text{surface}}}{E_{\text{mode}}^{\text{max}}} \right)^2 = 73$$

$$\text{Contributing fraction} = \frac{\int |E_{\text{ex}}(x, y, \text{surface})|^2 |E_{\text{mode}}(x, y, \text{surface})|^2 dx dy}{|E_{\text{mode}}^{\text{max}}(x, y, \text{surface})|^2 \int |E_{\text{ex}}(x, y, \text{surface})|^2 dx dy} = 0.157$$



Excitation field  
Gaussian:  $c = (0 \ 0)$   
 $\sigma = 0.8 \ \mu\text{m}$



Resonance mode :  
Polarization =  $E_y$  ( $|_{-}$ )  
Freq = 0.262  
Wavelength = 1582.7

# Summary

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- We have shown photonic crystal cavity can enhance spontaneous emission of quantum dots significantly.
- We hope to use photonic density of states to control relaxation dynamics of carriers in semiconducting materials.

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Fabrication – Paul Resnick (SNL)

Measurements – Shisheng Xiong (UNM student) and myself



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