



# DSMC Simulations of Transient Gas Flows

**Michael A. Gallis**

Engineering Sciences Center  
Sandia National Laboratories  
Albuquerque, New Mexico, USA

**DSMC: Fundamentals through Advanced Concepts  
Short Course**

***Direct Simulation Monte Carlo: Theory, Methods, and Applications  
Santa Fe, New Mexico; September 13-16, 2009***



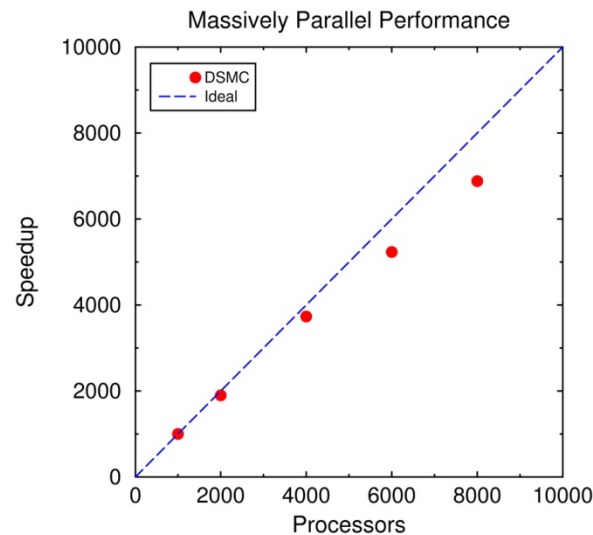
Sandia is a multiprogram laboratory operated by Sandia Corporation, a Lockheed Martin Company, for the United States Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.





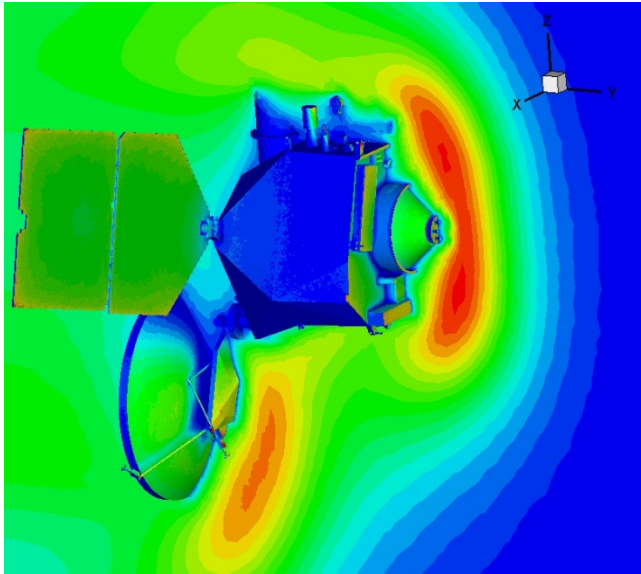
# The Limitations of DSMC

- The computational load increases with the density of the flow
- Statistical error decreases as a function of the *square root* of the number of samples
- DSMC can carry more information than actually needed for some applications
- DSMC is an MP empowered technology

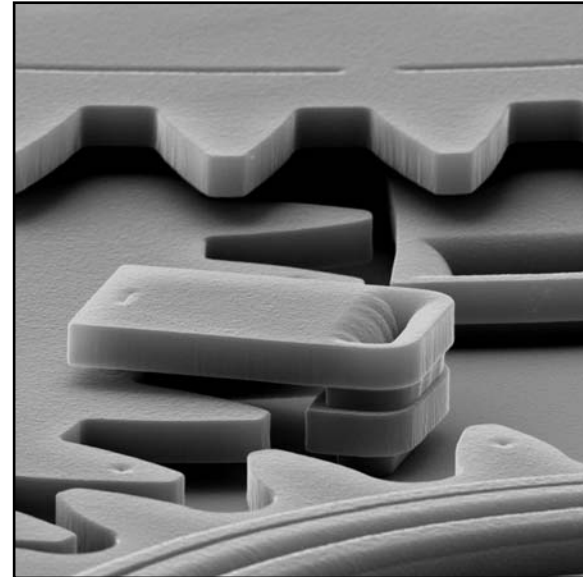




# Can DSMC Compute Transient Microscale Gas Flow?



Traditional DSMC application



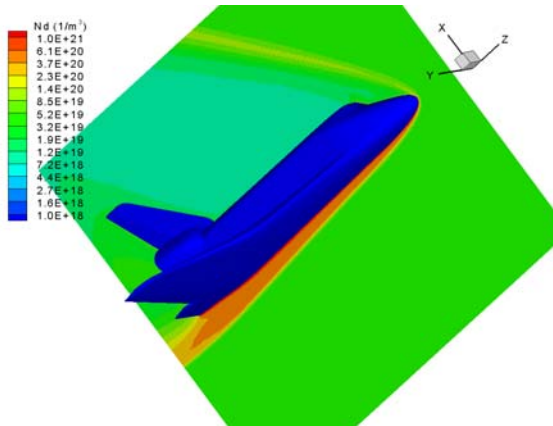
Can DSMC be used?

**Perception: DSMC is a “rough and ready” method, sufficiently accurate for hypersonic flows but not adequate (speed, accuracy) for microscale flows (low-speed, nearly-isothermal)**

**Reality: DSMC can also be used for transient microscale flows if carefully implemented and applied in a massively parallel (MP) environment**



# Why DSMC for Microscale Gas Flows?

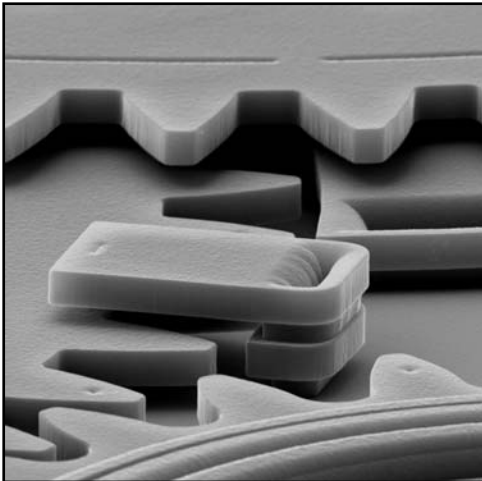


## DSMC is accurate for hypersonic and microscale gas flows

Careful implementation is required – can't “cut corners”  
Pay attention to mesh, time step, number of molecules, statistics

## DSMC has been successfully verified against known results

Low heat fluxes with small molecular mean free path  
Excellent agreement with Chapman-Enskog theory  
Arbitrary heat fluxes with infinite molecular mean free path  
Excellent agreement with well-known solutions



## DSMC can compute regimes that theory cannot predict

High heat fluxes with small molecular mean free path  
Predicts gas state when Chapman-Enskog theory does not apply  
Heat fluxes with molecular mean free path comparable to geometry  
Predicts gas state when wall interactions are significant

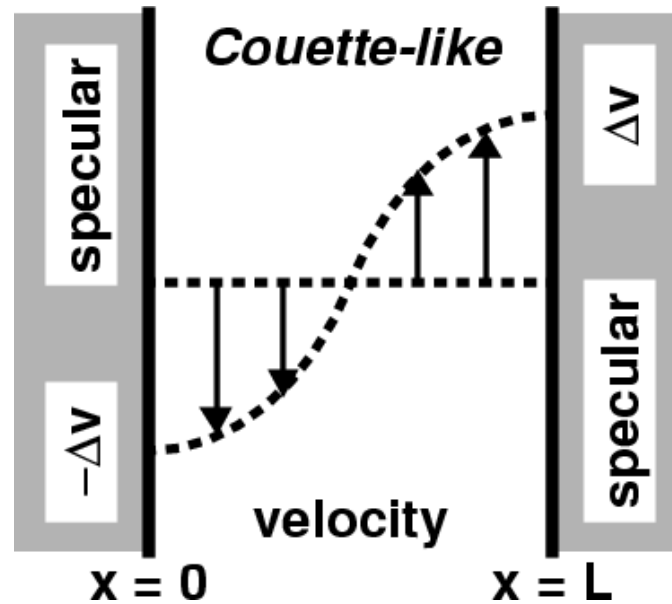


# Convergence of Transient DSMC

- DSMC is standard to judge other noncontinuum methods
  - Investigators starting to do transient DSMC simulations
  - Although inherently transient, only steady flows studied
- How does DSMC converge for transient flows?
- Goal: extract maximum accuracy with minimum effort
  - Identify major parameters controlling DSMC accuracy



## Couette-like Transient Flow



### Decaying shear flow with slippery walls

- Initial conditions: half-cosine  $v$  velocity; zero  $u$ ,  $w$  velocities; uniform pressure, temperature, density.
- Boundary conditions: specular walls (symmetry)
  - No Knudsen layers, investigate bulk flow behavior
- Long times: motionless; conserve mass, energy



# Couette-like Transient Convergence Study

## Parameters from steady convergence investigations

- Follow Rader, Gallis, Torczynski, and Wagner (2006)
- Domain:  $0 < x < L$ ,  $L = 1$  mm
- Gas: hard-sphere argon (Bird 1994)
- Temperature: 273.15 K

## Quantities varied in simulations

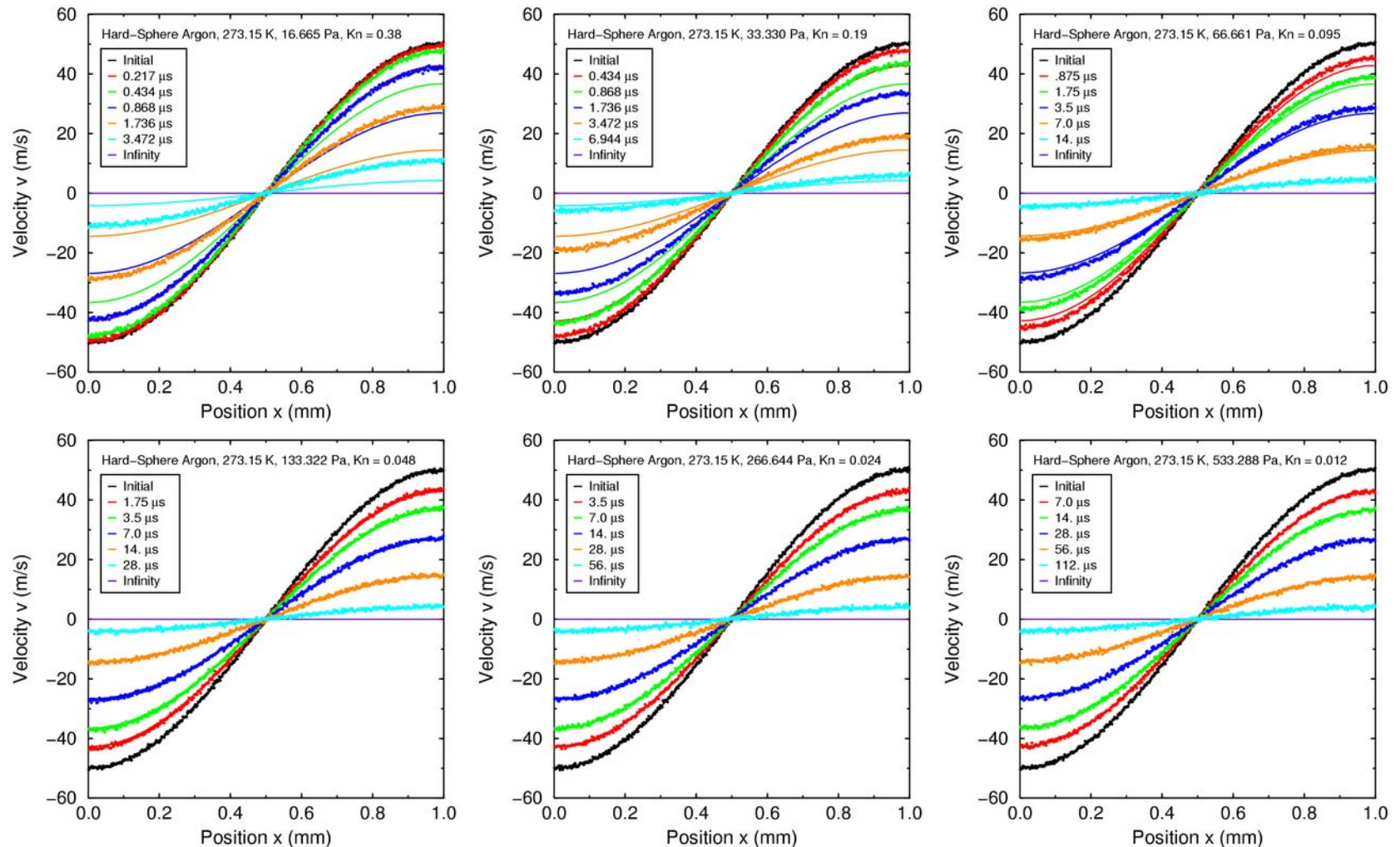
- Velocity:  $v = -\Delta v \cdot \cos[\pi x / L]$ ,  $\Delta v = 50$ -500 m/s,  $c = 381$  m/s
- Pressure:  $p = 4, 2, 1, 0.5, 0.25, 0.125$  torr (focus on 2 torr)  
 $Kn = \lambda/L = 0.012, 0.024, 0.048, 0.095, 0.19, 0.38$
- Cell size:  $0.1 < \Delta x/\lambda < 1$  (MFP at 2 torr,  $\lambda = 0.024$  mm)
- Time step:  $0.1 < \Delta t/t_0 < 1$  (coll. time at 2 torr,  $t_0 = 70$  ns)

## Simulation specifics

- Algorithm: DSMC94, move-sample-collide-sample
- Molecules: 10,000,000 (25,000-250,000 per cell)



# Pressure (Knudsen Number) Dependence

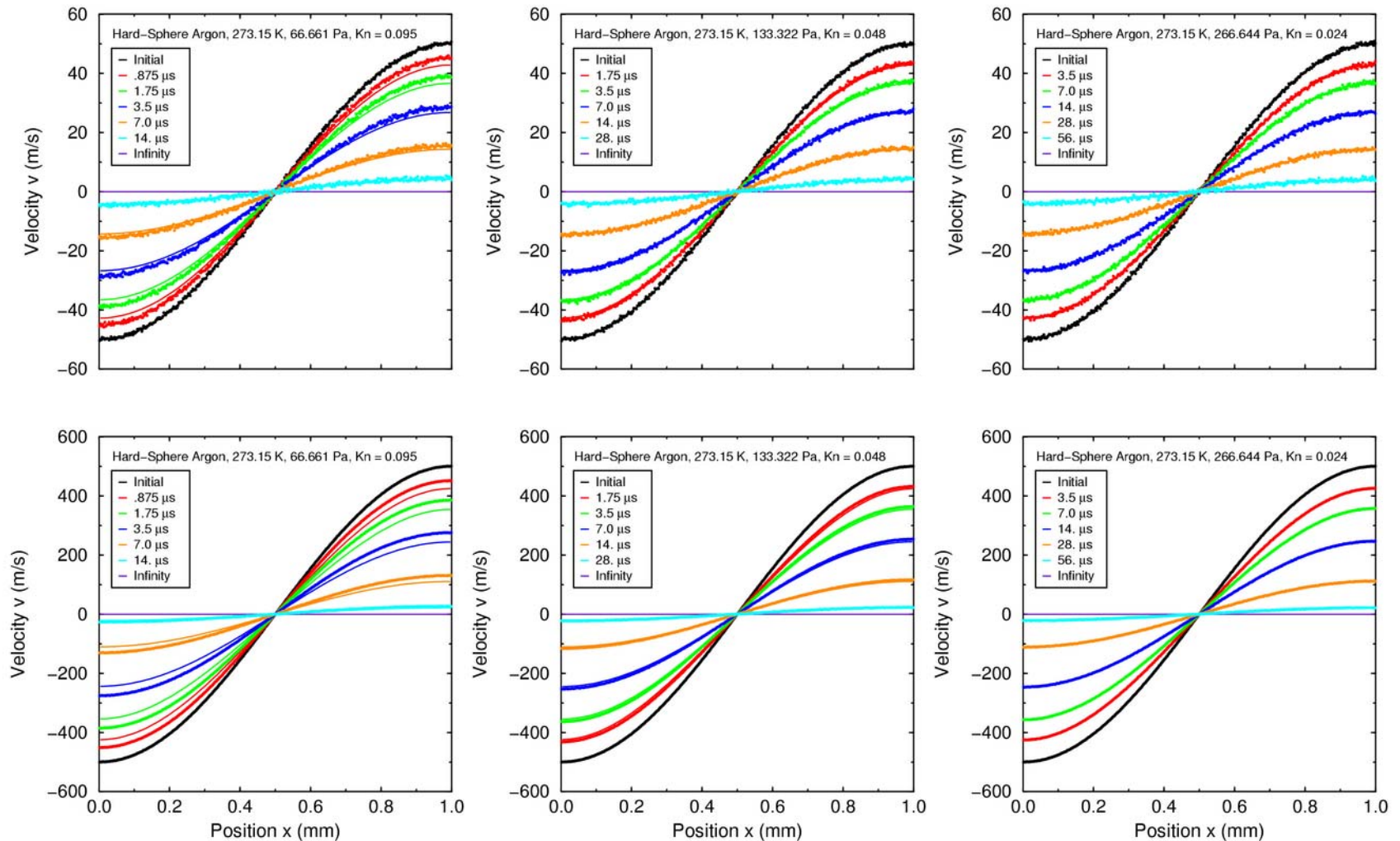


For  $\text{Kn} < 0.03$ , highly resolved DSMC (dots) and continuum (curves) agree closely





# Velocity Dependence



Low-speed (top) and high-speed (bottom) DSMC  
behave similarly in approach to continuum



## DSMC Effective Viscosity

$$v = -\Delta v \cos\left(\frac{\pi x}{L}\right) \exp\left(-\frac{\pi^2 \mu_{\text{eff}} t}{\rho L^2}\right)$$

Find DSMC effective viscosity at particular  $\Delta x$  and  $\Delta t$

- Compare DSMC to continuum analytical solution
  - Appropriate for vanishing Knudsen numbers
  - Appropriate for constant uniform temperature
- Accurate for  $\Delta v = 50$  m/s at 2 torr and 273.15 K
  - Small Knudsen numbers: system, 0.024; shear, 0.006
  - Small temperature rise: 2 K (viscosity increases 0.3%)
- Adjust continuum effective viscosity to match DSMC

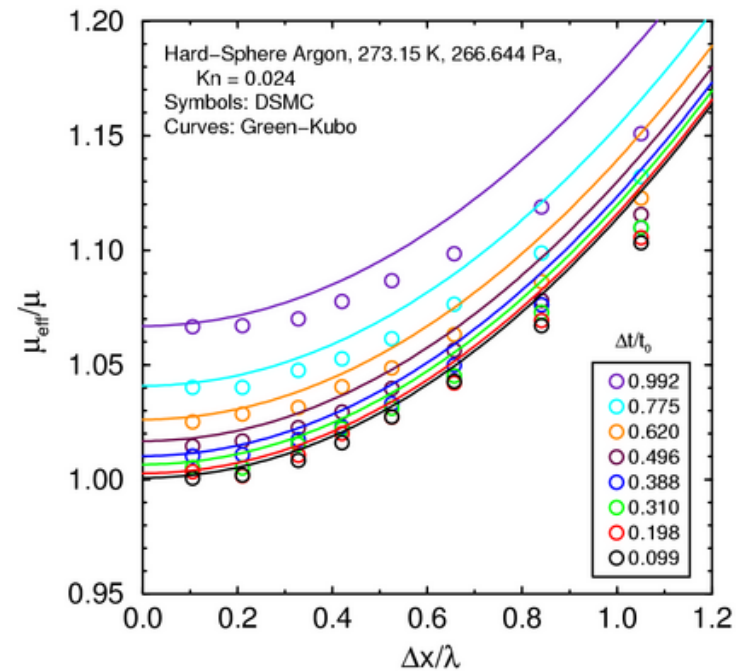
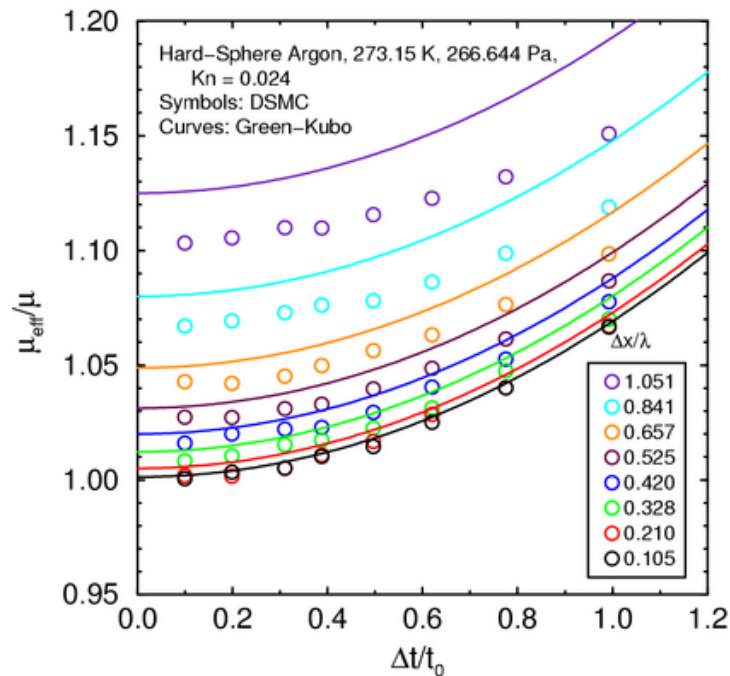
Repeat for many different combinations of  $\Delta x$  and  $\Delta t$

- Compare to predictions of Green-Kubo theory of Garcia & Wagner and Hadjiconstantinou (2000)



# Comparison to Green-Kubo Theory

$$\frac{\mu_{\text{eff}}}{\mu} = 1 + \frac{16}{75\pi} \left( \frac{\Delta t}{t_0} \right)^2 + \frac{16}{45\pi} \left( \frac{\Delta x}{\lambda} \right)^2 = 1 + 0.0679 (\Delta \tilde{t})^2 + 0.1132 (\Delta \tilde{x})^2$$

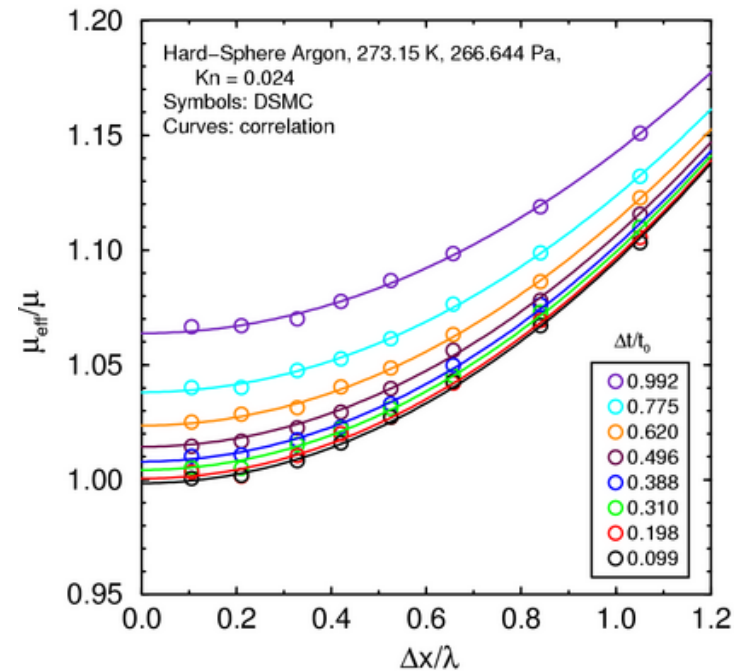
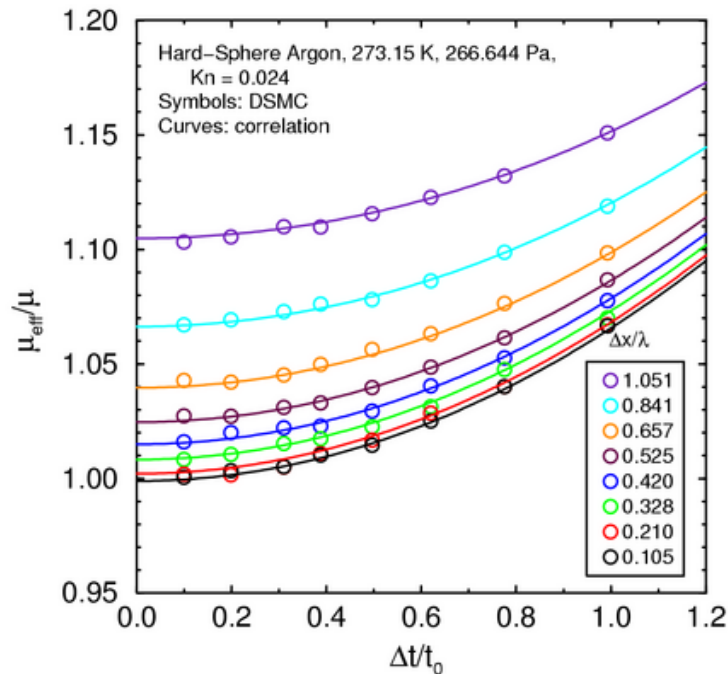


DSMC and Green-Kubo results agree reasonably  
Green-Kubo error estimate is slightly conservative



# Polynomial Correlation

$$\frac{\mu_{\text{eff}}}{\mu} = 0.9978 + 0.0670(\Delta\tilde{t})^2 + 0.0969(\Delta\tilde{x})^2 - 0.0209(\Delta\tilde{t})^2(\Delta\tilde{x})^2 + 0.0025(\Delta\tilde{t})^3(\Delta\tilde{x})^2$$



Viscosity differs by 0.3%, close to thermal variation

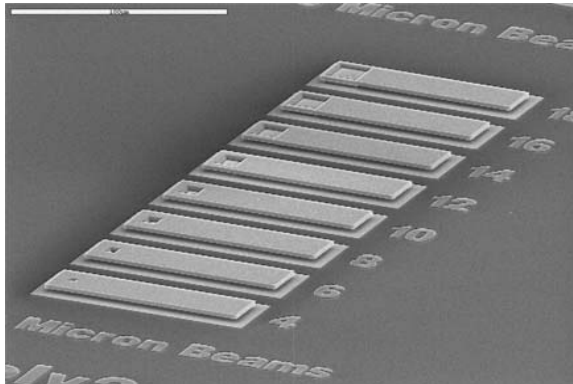
Pure terms agree reasonably with Green-Kubo

Cross terms are required to correlate values



## Quasi-Static Assumption

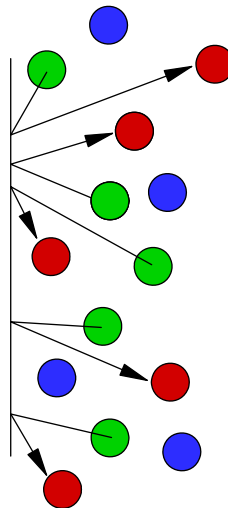
- **The structure movement is quasi-static**
  - *the structure speed is much smaller than the thermal speed of molecules*
  - *the gas is incompressible and isothermal*
- **The moving boundary is replaced by a fixed boundary on which the velocity is applied**





## DSMC Inflow BC

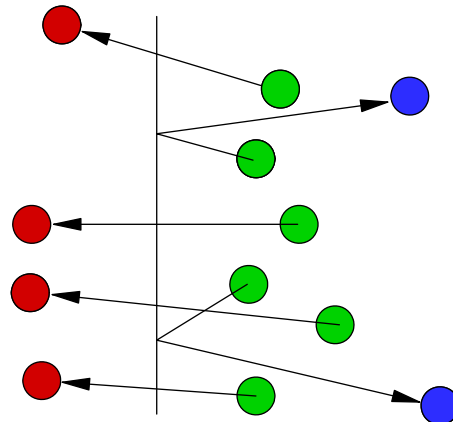
- Molecules that “exit” are reintroduced into the domain with new properties.
- Additional molecules are introduced at a rate that corresponds to the net subsonic inflow.
- Properties of entering molecules selected to produce Maxwellian at prescribed velocity and temperature.





## DSMC Outflow BC

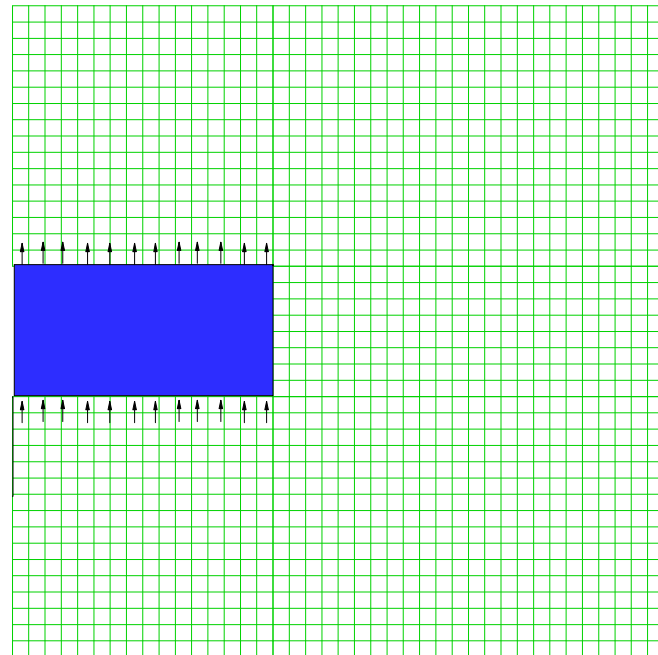
- Molecules that “exit” are deleted at a rate that corresponds to the net subsonic outflow.
- The rest of the molecules that “exit” are reintroduced into the domain with new properties.
- Properties of entering molecules selected to produce Maxwellian at prescribed velocity and temperature.





# Moving Microbeam

- **Geometry**
  - 2D cross-section
  - Half-width: 4 microns
  - Thickness: 2 microns
  - Gap: 4 microns
- **Gas properties**
  - Gas: rarefied nitrogen
  - Pressure: 100 mTorr
  - Temperature: 295 K
- **Flow condition**
  - Velocity: 10 m/s

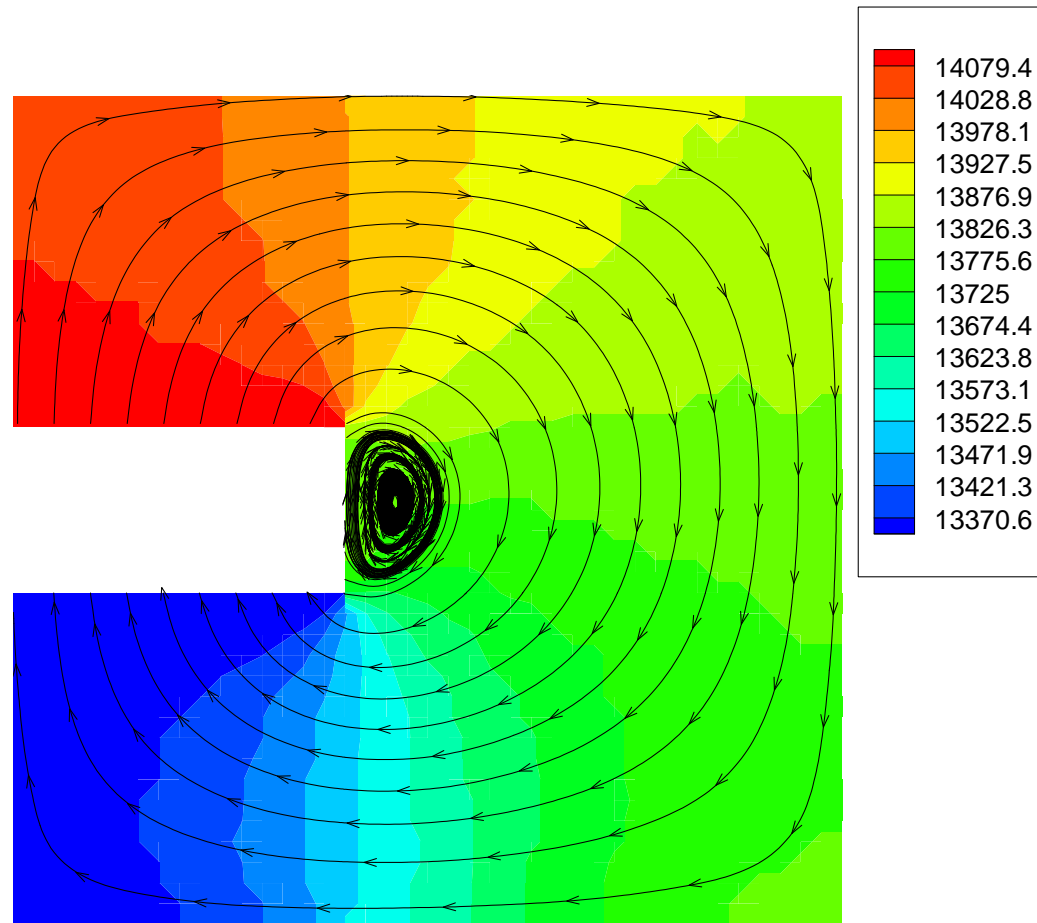






# Moving Microbeam

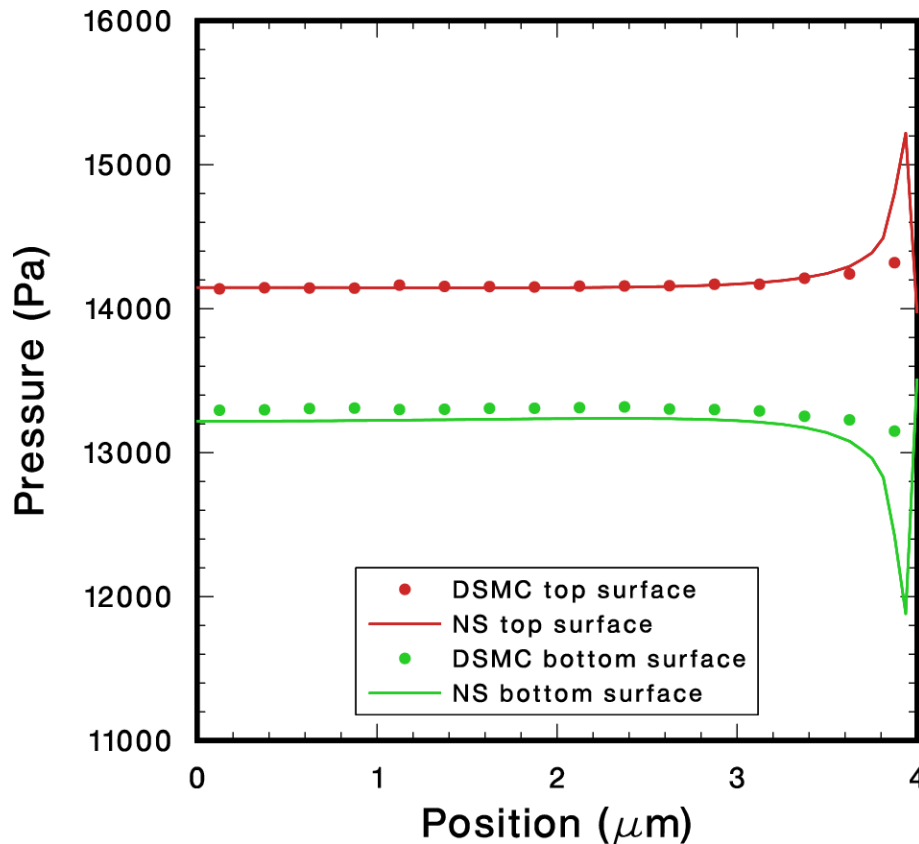
## Pressure Contours and Streamlines





# Moving Microbeam

## DSMC and NS Pressures on the Surfaces



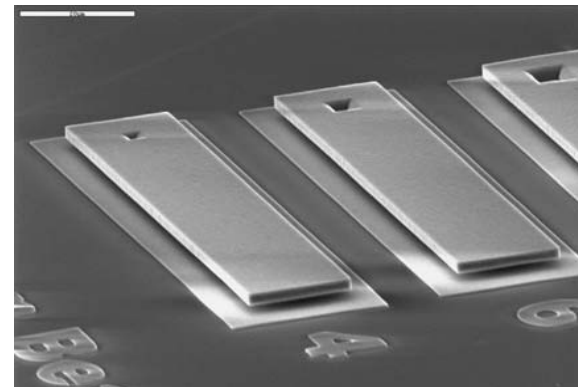
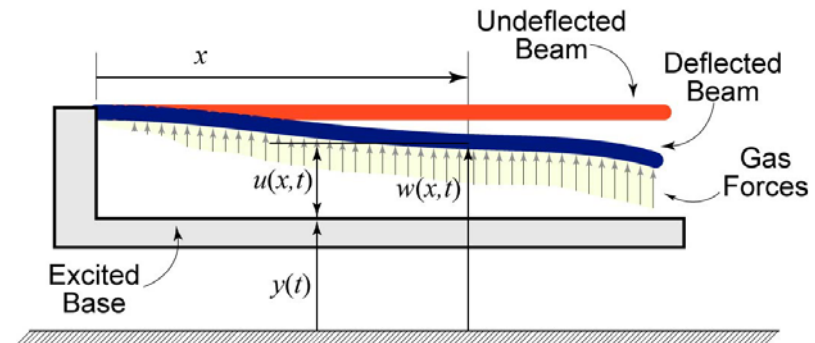
**DSMC:** Icarus

**NS:** FIDAP (continuum slip, incompressible, isothermal)



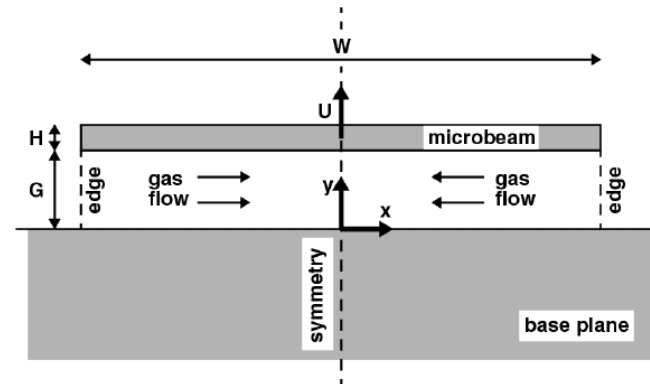
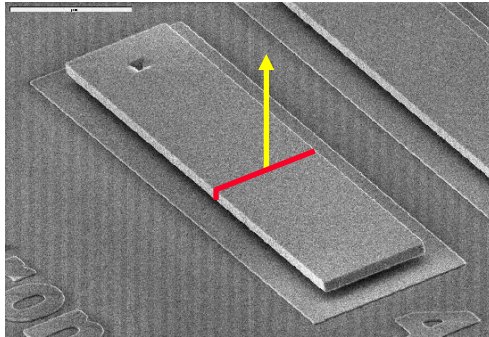
# Cantilevered Microbeams

- “Diving boards for bacteria”
  - Polycrystalline silicon
    - Length: 100 microns
    - Width: 20 microns
    - Thickness: 2 microns
    - Gap height: 2-10 microns
    - Frequency: 10-100 kHz
  - Gas: ambient or rarefied air
- Good candidate for analysis
  - Geometry, properties known
  - Experimentally accessible





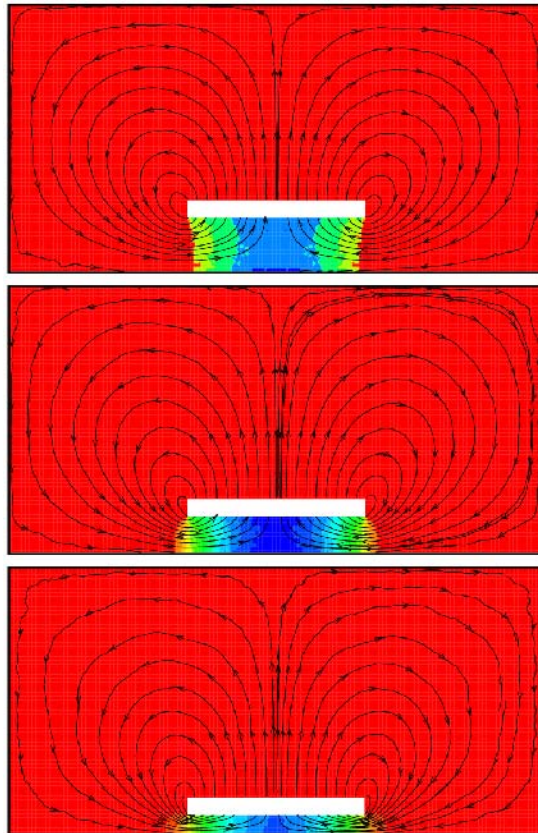
# Microbeam Gas Damping



- DSMC simulation of microbeam gas damping
- Two-dimensional geometry: cross section
- Quasi-static flow:
  - Moving boundary replaced by fixed boundary
  - Velocity applied as boundary condition
- Low velocities, small pressure variations
- Nearly isothermal, nearly incompressible



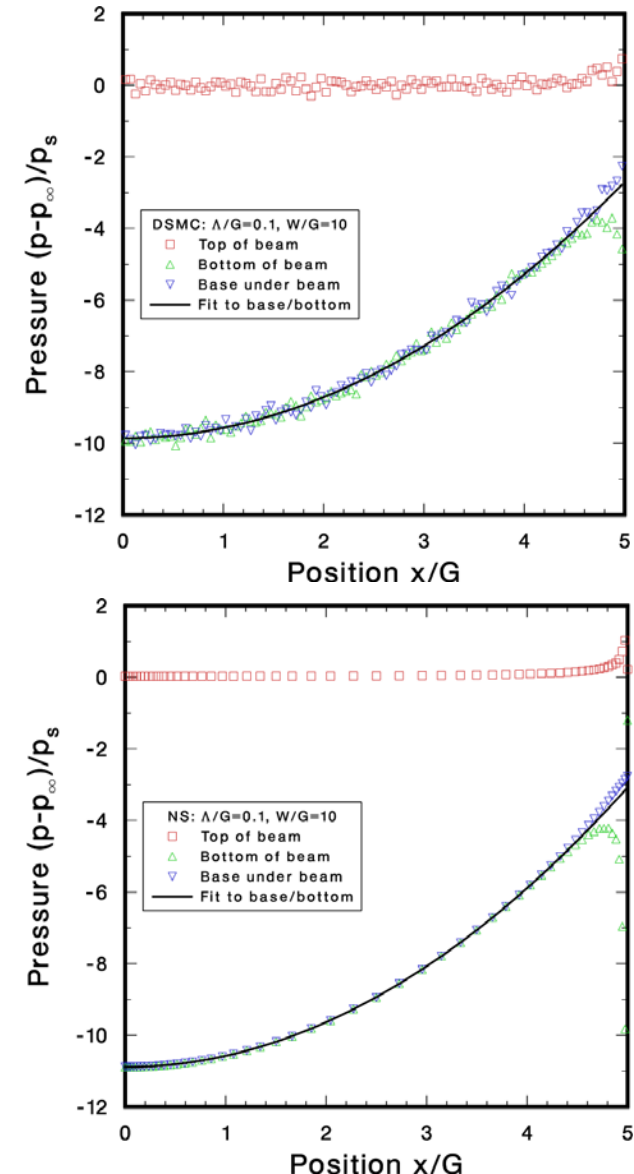
# Quasi-Static DSMC



**DSMC**

**NSSJ**

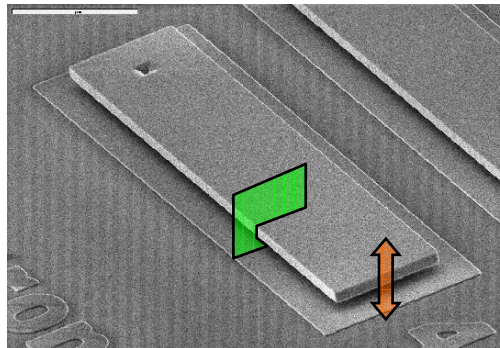
DSMC: 24 hours on 3000 processors (ASCI Red)  
 Sample  $10^{10}$  molecules/cell, ~1 billion time steps  
 Microbeam:  $2 \times 20 \mu\text{m}$ , 1 m/s  
 Gas: **atmospheric** nitrogen





# Transient DSMC Simulation

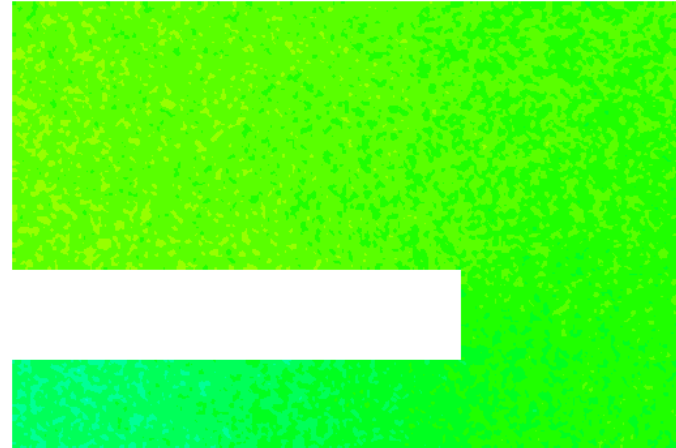
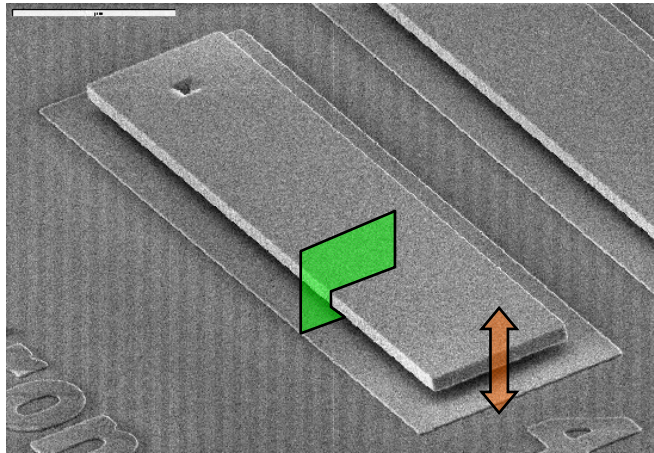
- **Goal: Simulate transient gas flow around a moving microbeam**
- **Microbeam Test Case**
  - Geometry (2-D):  $2 \times 20\text{-}\mu\text{m}$  cross section,  $2\text{-}\mu\text{m}$  gap
  - Gas: **atmospheric** nitrogen
  - Oscillation: 1 MHz with peak speed of 1 m/s
- **DSMC Simulation**
  - Sandia MP implementation (Icarus)
  - Simulation: 24 hours on 8000 processors (ASCI Red, 3 Tflop)
  - Total time simulated:  $3\text{ }\mu\text{s}$  (3 cycles)
  - Computational molecules: 13,000 per cell, ~1 billion total
    - 3 million sampled per cell per frame (uncertainty 50 Pa, 0.2 m/s)







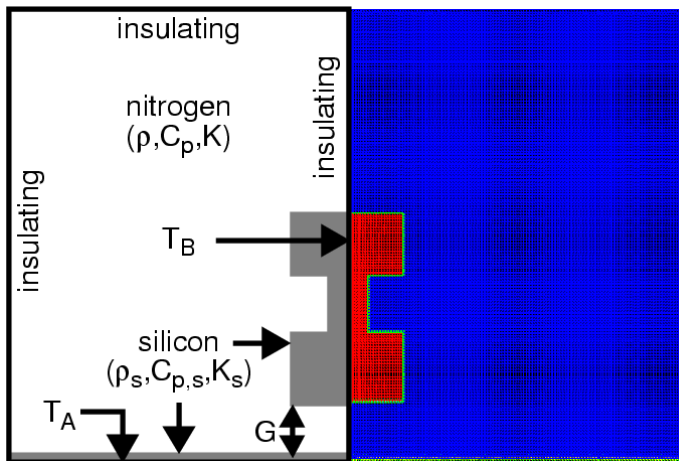
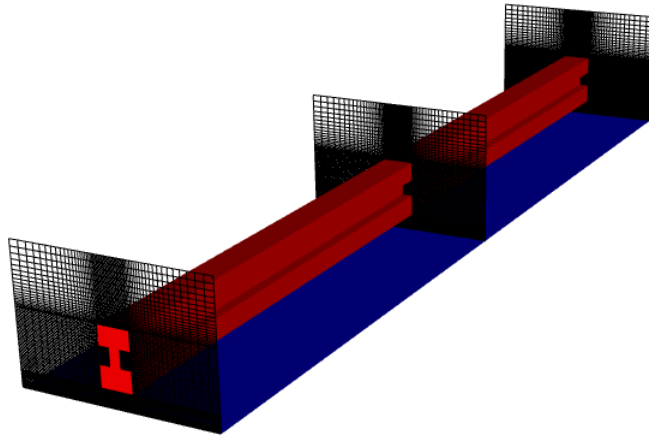
# Oscillating Microbeam Flow Field from DSMC



- Microbeam motion creates pressure variations in gap beneath it
- Pressure on top remains practically unchanged



# Heated Microbeam Near Substrate



## Solid regions: silicon

- Geometry: 2-micron gap
- Beam temperature: ~900 K
- Substrate temperature: ~300 K

## Gas region: nitrogen

- Pressure: atmospheric
- Initial temperature: ~300 K

## NSSJ simulations

- Finite-element (Calore, FIDAP)

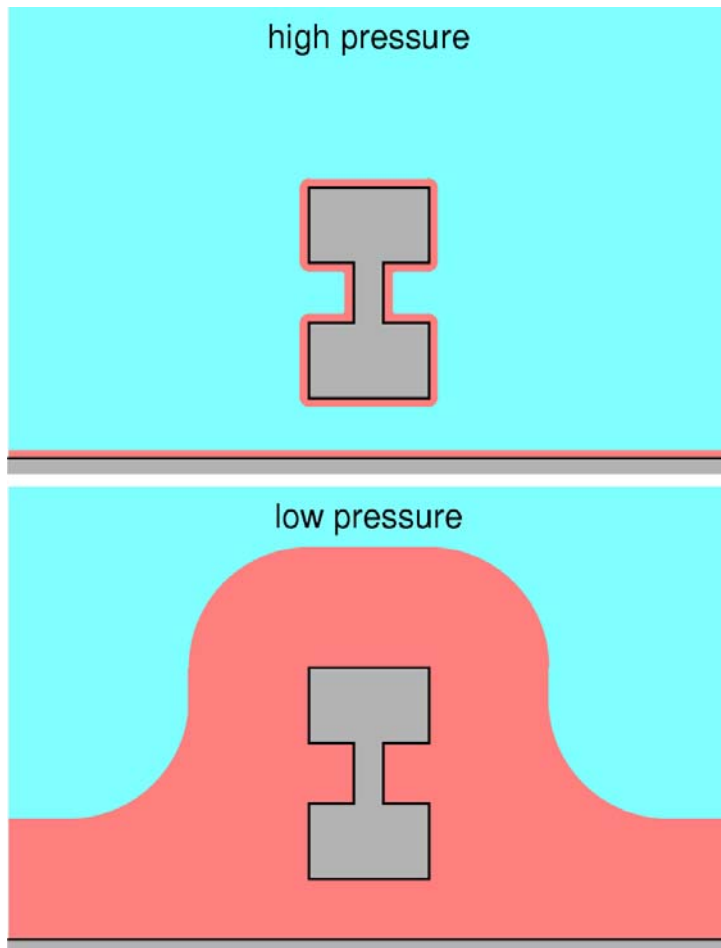
## DSMC simulations

- Two-dimensional, transient
- 100 computational molecules/cell
- 24 hours, 3000 processors, 3 Tflop (ASCI Red)





# Microbeam Noncontinuum Regions



## High pressure

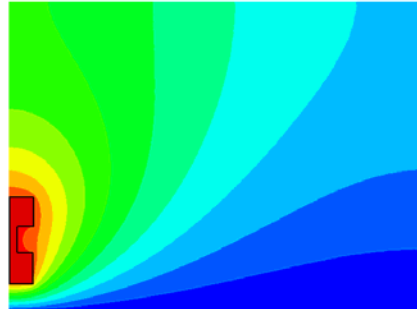
- Thin, isolated, planar Knudsen layers
- Heat transfer = continuum + jumps

## Low pressure

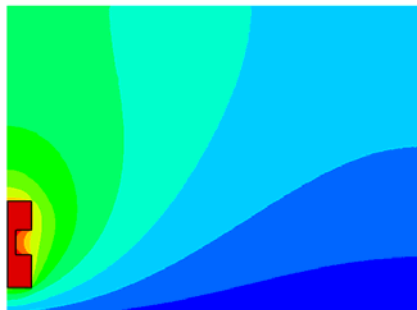
- Thick, merged, convex Knudsen layers
- Heat transfer = free-molecular finite body



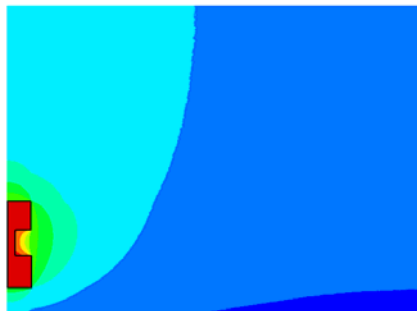
**Steady  
State**



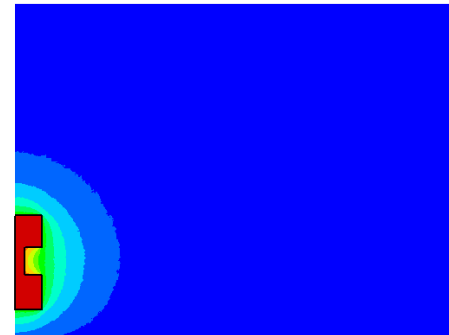
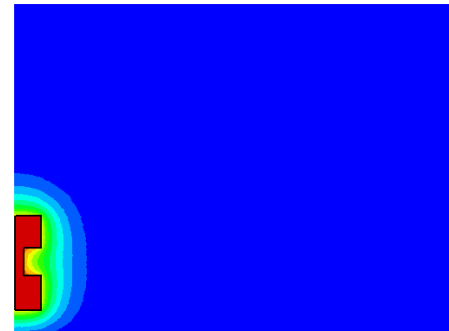
**1 atm**



**0.1 atm**



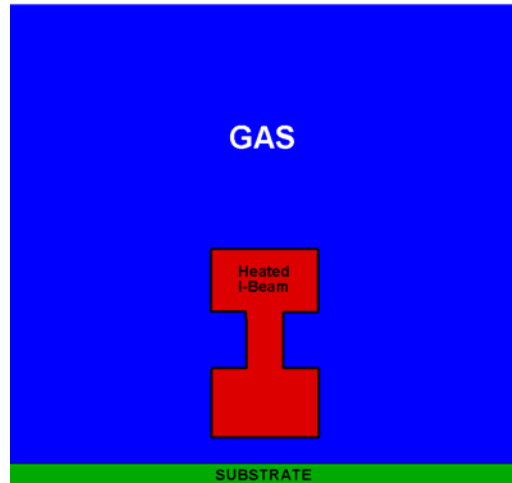
**0.01 atm**



**Transient  
Motion**

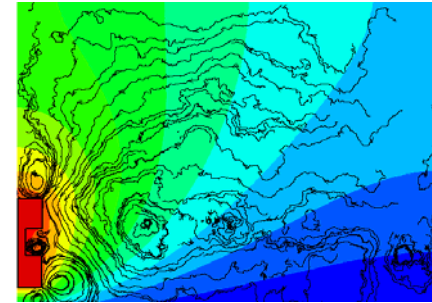


# Heated Microbeam Makes Gas Move

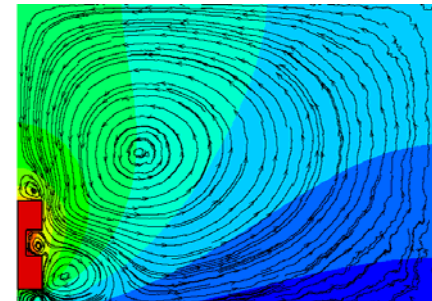


- **DSMC microbeam simulations**
- **Steady gas motion** is induced by temperature differences
  - *Not* buoyancy, *not* transient
- **Noncontinuum effects** cause motion
  - *Not* seen in NSSJ simulations

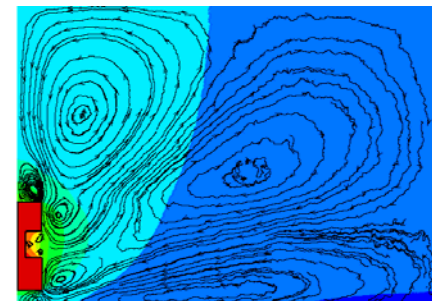
1 atm  
~0.1 m/s



0.1 atm  
~2 m/s



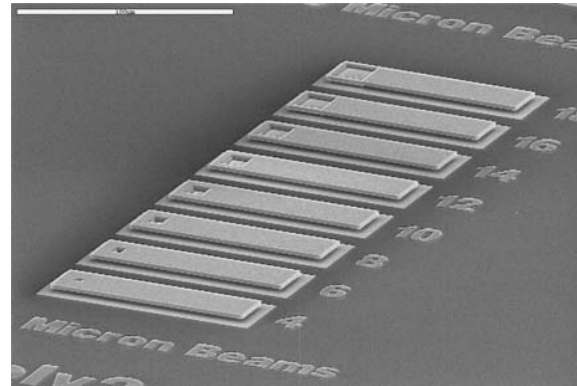
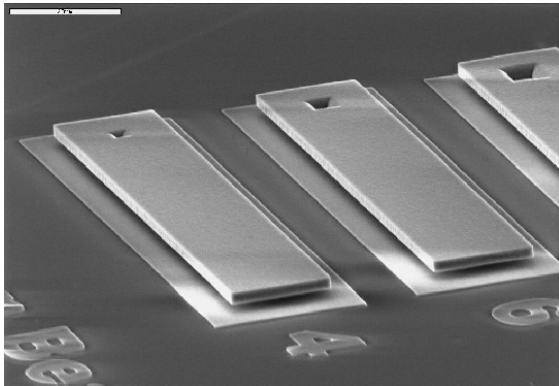
0.01 atm  
~1 m/s





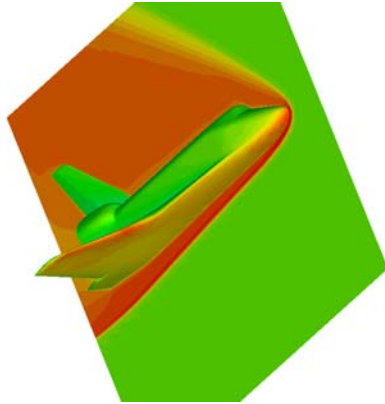
# DSMC for Subsonic Flows

- Massively parallel (MP) implementation is the enabling technology for transient DSMC simulations
- 8000 processors (3 Tflop) for 24 hours is marginally adequate to simulate a few cycles of a 2-D microbeam oscillation
- Simulation of 3-D transient flow is projected to require about  $10^3$  times greater computational power (0.1-10 Pflop)

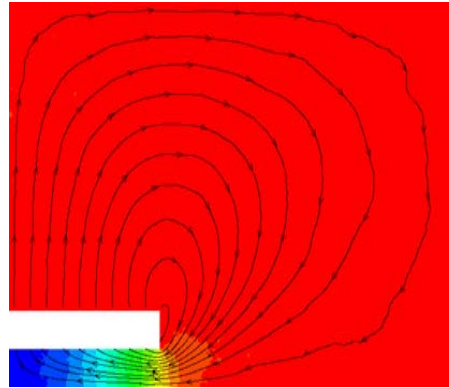




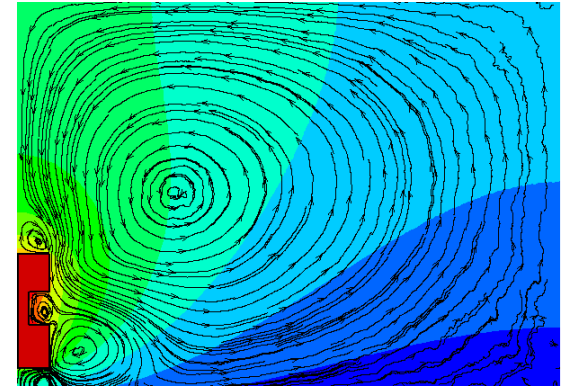
## Summary



Hypersonic Vehicles



Moving microbeam



Heated microbeam

### DSMC for Gas Dynamics

- DSMC can be applied to almost any regime of gas dynamics, including low-pressure, microscale, or hypersonic gas flows.
- DSMC can offer physical insight to processes where physical, chemical, thermal non-equilibrium plays a role.

### DSMC for transient MEMS-type flows

- Possible even with today's computational resources
- Computational effort remains high compared to continuum CFD

### Microscale devices cannot be designed using only macroscale tools

- DSMC reveals true characteristics of microscale flow fields
- DSMC can be used to derive engineering models for designers