

**Parallel Replica Dynamics**  
New LAMMPS features briefs  
LAMMPS Users' Workshop @ CSRI  
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# The PRD Method

Invented by Art Voter:

A. F. Voter, "Parallel replica method for dynamics of infrequent events", *Phys Rev B* **57** 13985 (1998) (146 citations up to Feb 2010)

Core Idea:

- Many atomistic simulations are characterized by long periods of localized vibration within a basin, punctuated by brief transitions between basins
- We assume the transitions between basins occur randomly (Markovian, Poisson process, first-order kinetics.) Then  $t_{ij}$ , the time spent in state  $i$  until a transition to state  $j$ , obeys the following probability law:

$$P(t_{ij} > t) = \exp(-k_{ij}t)$$

- If we run  $R$  independent simulations, the probability law becomes:

$$P(t_{ij}^1, \dots, t_{ij}^R > t) = \prod_{r=1}^R P(t_{ij}^r > t) = \exp(-k_{ij}Rt)$$

- Hence, by running  $R$  independent replicas, the transition kinetics are conserved, but time is rescaled by a factor of  $R$ .
- This only works for first-order kinetics

# The PRD Algorithm

(as implemented in LAMMPS by Mike Brown)

*while (time remains):*

- 1. dephase for  $N_{dephase} * T_{dephase}$  steps*
- 2. until (event occurs on some replica):*
  - run dynamics for  $T_{event}$  steps*
  - quench and check for event on any replica*
- 3. until (no correlated event occurs):*
  - run dynamics for  $T_{correlate}$  steps*
  - quench and check for event on this replica*
- 4. event replica shares state with all replicas*

# PRD in LAMMPS

## Command Syntax

```
prd N t_event n_dephase t_dephase t_corr compute-ID seed
```

E.g.

```
prd 1000000 100 10 10 100 compl 54982
compute          compl all event/displace 0.5
```

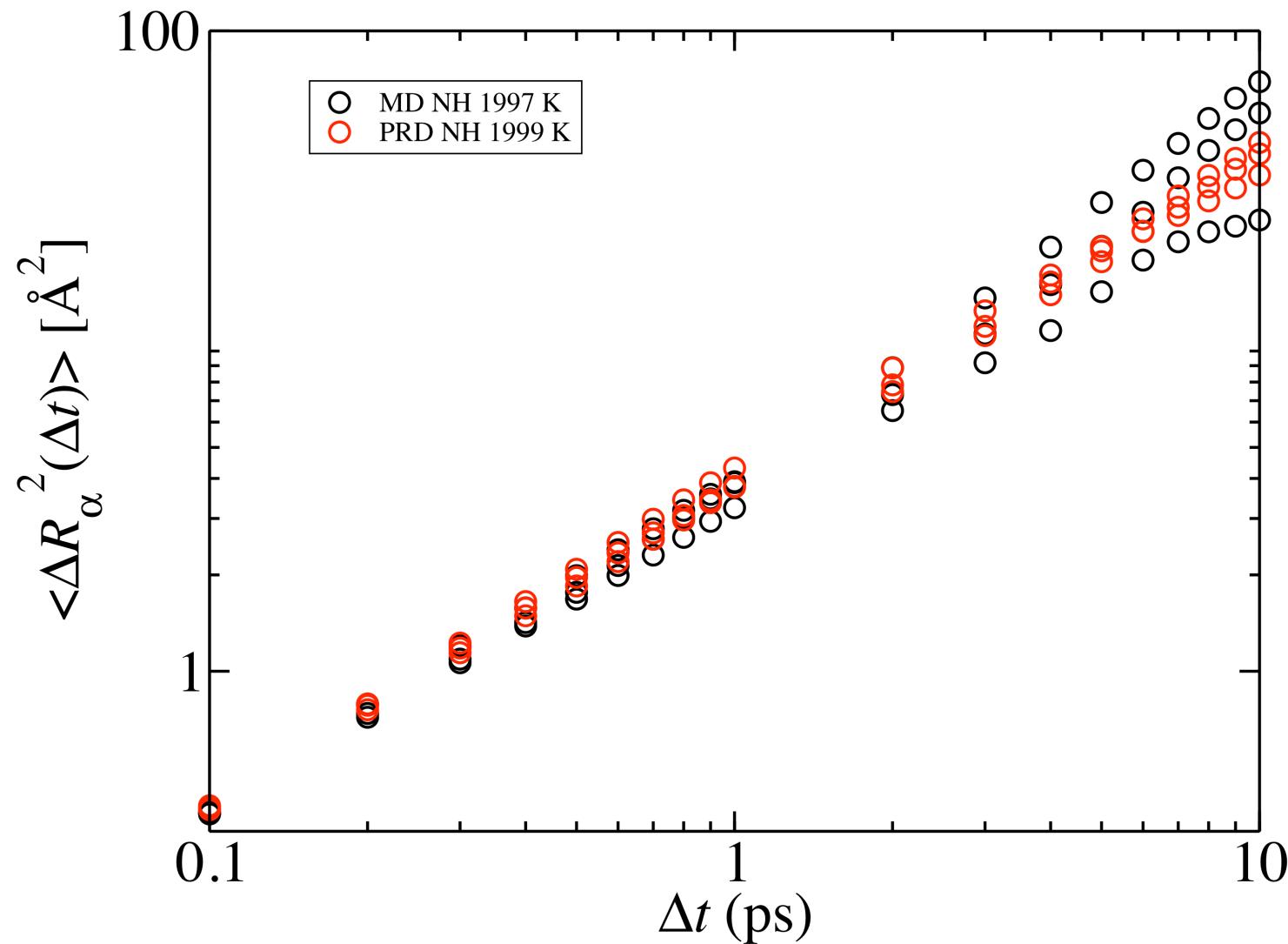
To run 128 replicas:

```
mpiexec -np 128 lmp_tbird -partition 128x1 -in in.si_prd
```

# Test Problem: Vacancy Diffusion

- Created a single vacancy in a 4x4x4x8 Silicon crystal
- Ran 100 ps NVT MD at 2000 K using Stillinger-Weber potential
- Quenched every 0.1 ps and dumped atoms with coordination != 4
- From dump file, obtained  $\mathbf{R}_{vac}(t)$ , the vacancy “center-of-mass” as a function of time
- Ran PRD run style for 1 ns with 1 replica
- Important note: For PRD, the time given in the dump file is the timestep count for 1 replica, which is not a good measure of physical time. This is more accurately represented by the “clock time”, reported for each event in the master log file.

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