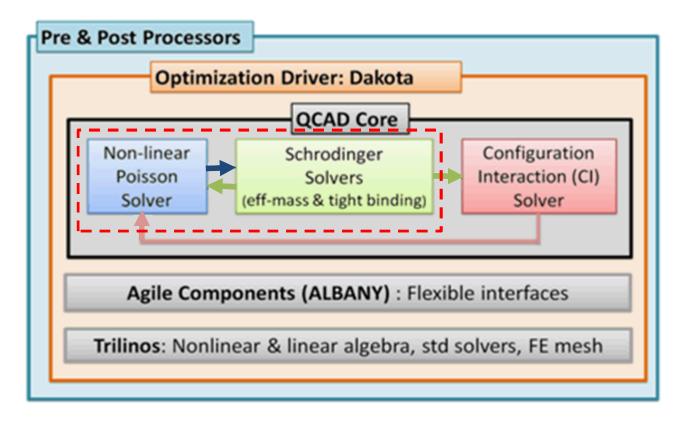


Xujiao (Suzey) Gao, Erik Nielsen, Richard Muller, Ralph Young, Andrew Salinger, Irina Kalashnikova October 2, 2012



## QCAD Framework



**QCAD core** has **nonlinear Poisson**, **Schrodinger**, and **CI solvers**, which can run **individually** or are **combined self-consistently**.

Erik's talk will cover some aspects of the optimization and the pre & post processors and their powerful applications to complex quantum dots devices.



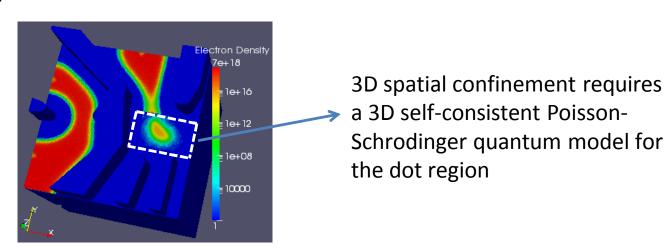
### Motivation

Rick has given some motivations for the QCAD project in his morning talk. Here I will illustrate on two specific motivations.

Commercial TCAD cannot solve nonlinear Poisson equation at cryogenic temperatures, where quantum dot qubits operate at.

Commercial TCAD solves 
$$\begin{cases} -\nabla(\varepsilon_s \nabla \phi) = q(p-n+C) = q \left[ n_i \exp\left(\frac{E_i - E_F}{k_B T}\right) - n_i \exp\left(\frac{E_F - E_i}{k_B T}\right) + C \right] \\ n_i = \sqrt{N_C N_V} \exp\left(\frac{-E_g}{2k_B T}\right) \rightarrow 0 \text{ as temperature T} \rightarrow 0 \end{cases}$$

**Commercial TCAD do not have 3D quantum models,** which are essential for accurately modeling quantum dot devices.





# **QCAD Approach**

**Nonlinear Poisson Solver** – recast the equation <sup>[1]</sup> using well-defined quantities and carefully address the blowup issue of  $exp(a/k_BT)$  function near 0 K

$$-\nabla(\varepsilon_s \nabla \phi) = q(p-n+C) = q \left[ N_V F_{1/2} \left( \frac{E_V - E_F}{k_B T} \right) - N_C F_{1/2} \left( \frac{E_F - E_C}{k_B T} \right) + C \right]$$

$$F_{1/2}(x) = \frac{2}{\sqrt{\pi}} \int_0^\infty \frac{\sqrt{\varepsilon} d\varepsilon}{1 + \exp(\varepsilon - x)}$$
 Fermi-Dirac integral of 1/2 order

#### Self-Consistent Poisson-Schrodinger (P-S) Solver [1]

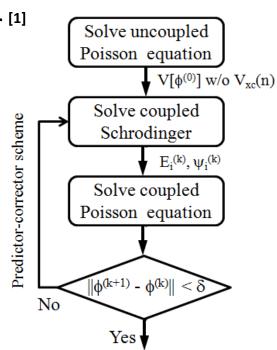
Coupled nonlinear Poisson equation:

$$-\nabla(\varepsilon_s \nabla \phi) = q[p(\phi) - \underline{n(\phi, E_i, \psi_i)} + C(\phi)]$$

Coupled Schrodinger equation:

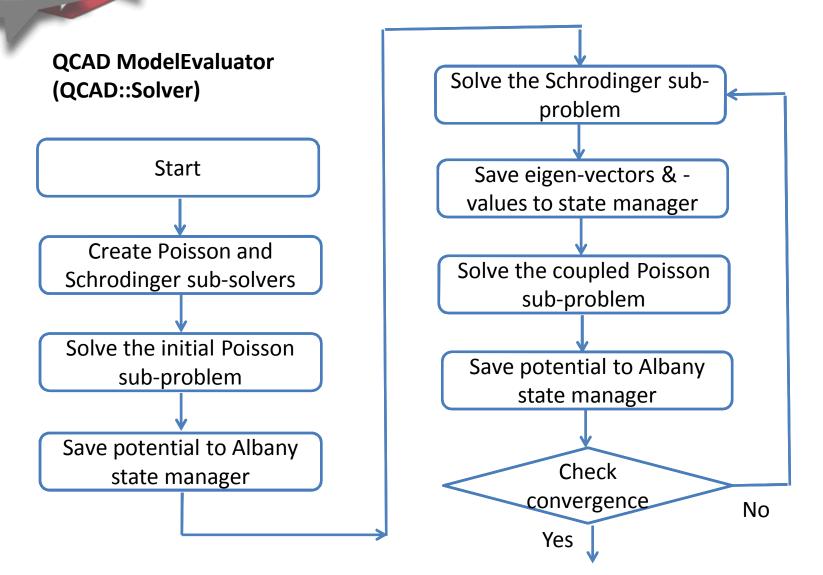
$$\frac{-\hbar^2}{2}\nabla\left(\frac{1}{m^*}\nabla\psi_i\right) + V(\phi, n)\psi_i = E_i\psi_i$$

[1] X. Gao, E. Nielsen, et al., Proceedings of IWCE (submitted).



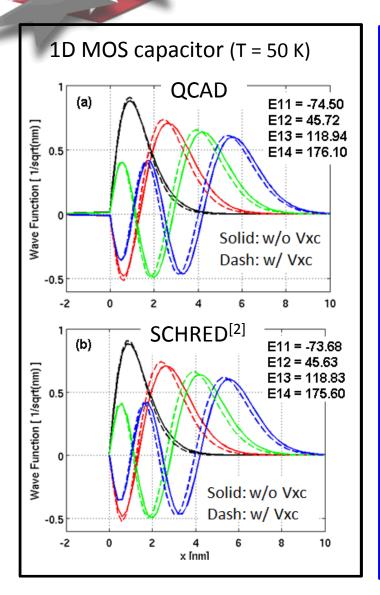


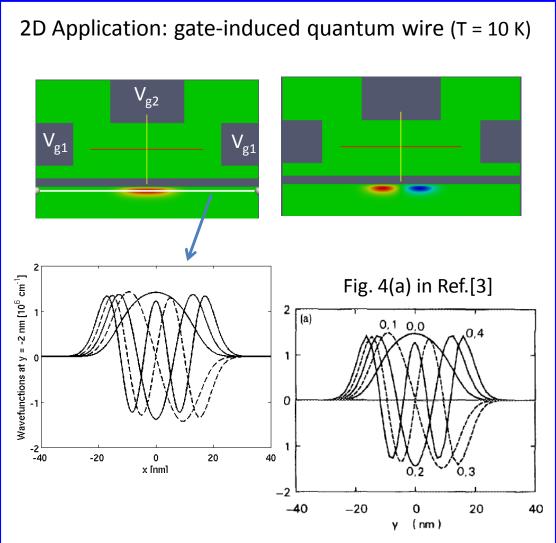
# QCAD P-S Implementation





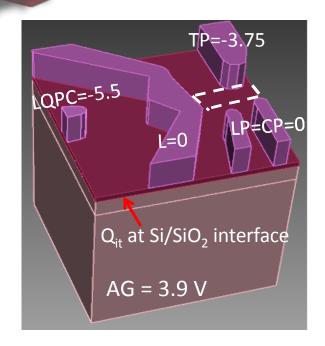
### **Model Validation**

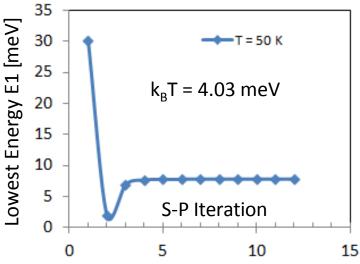




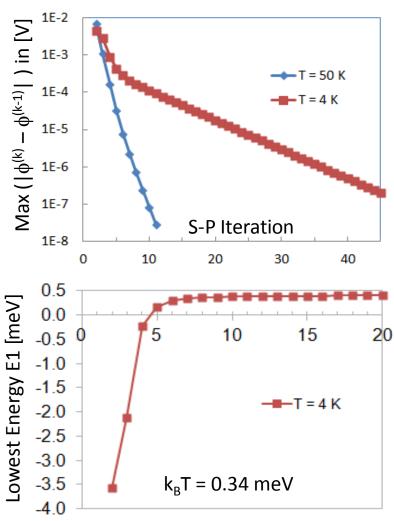


## 3D Quantum Dot - Convergence





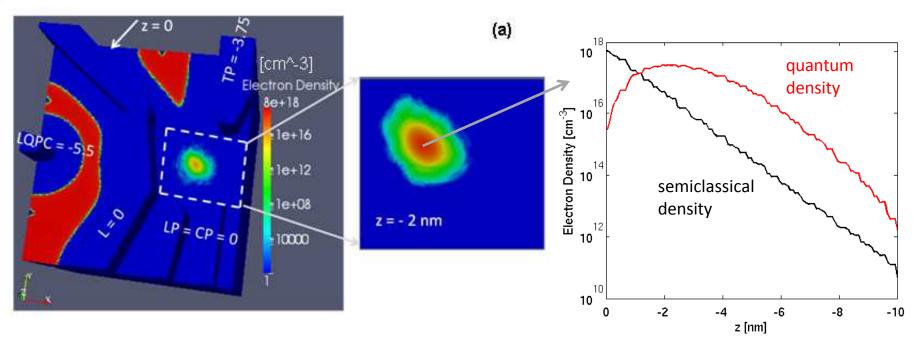
#### Monotonic 3D S-P convergence is observed.



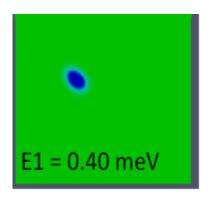


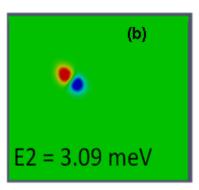
# 3D Quantum Dot – Electron Density

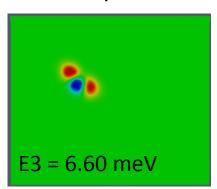
Quantum confinement pushes electrons away from the interface



Lowest three wave functions in the z = -2 nm plane







T = 4 K  

$$Q_{it} = -4.43 \times 10^{11} \text{ cm}^{-2}$$



### Collaborative Teamwork

- The exciting opportunity of working with experts from different areas.
- Irina's work on preconditioners leads to the use of ML preconditioner with Zoltan repartitioning, which gives 2-5x speedup of linear solves in parallel.
- Discussions with Andy and Heidi lead to 2x speedup in QCAD S-P solver by modifying LOCA/Eigensolver interface code to avoid matrix recalculation. 2x is insignificant for small problems, but important for big problems, e.g., 30 hrs -> 15 hrs. Further possible speed improvement is under investigation.

