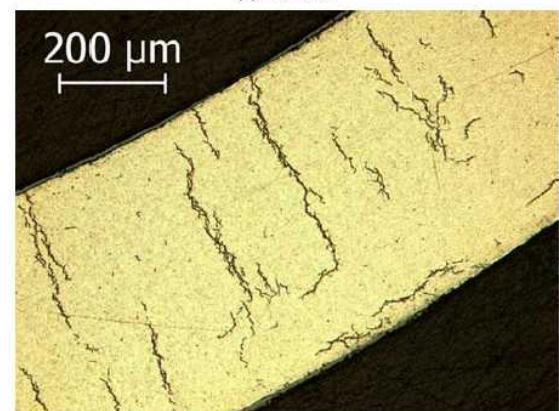
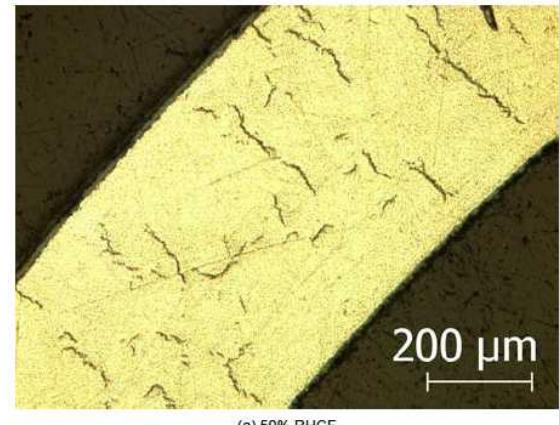


Hydride modeling approach for assessing the hydride behavior in high burnup fuels

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Hydride modeling approach for assessing the hydride behavior in high burnup fuels

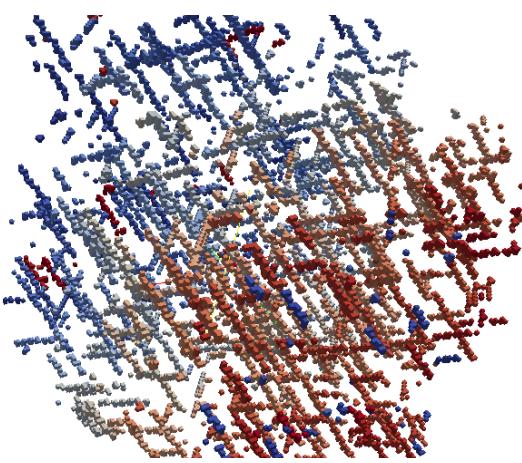
Model objective: to simulate $\delta\text{-ZrH}_{1.5}$ formation at this microstructural scale.

Accomplishments: Developed a basic model to simulate precipitation and growth of $\delta\text{-ZrH}_{1.5}$ precipitates in the $\alpha\text{-Zr}$ matrix

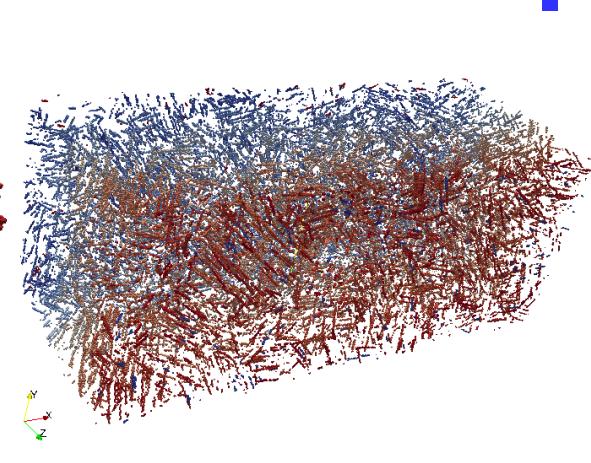
- In a Zircaloy-4 with correct grain and crystallographic texture
- Correct thermodynamic driving forces for the two phases
- With kinetic capability for nucleation and growth of precipitates.



Bradbrook et al, JNM 1972



Precipitates in single crystal



Precipitates in polycrystalline

Hybrid Potts-Phase Field Model

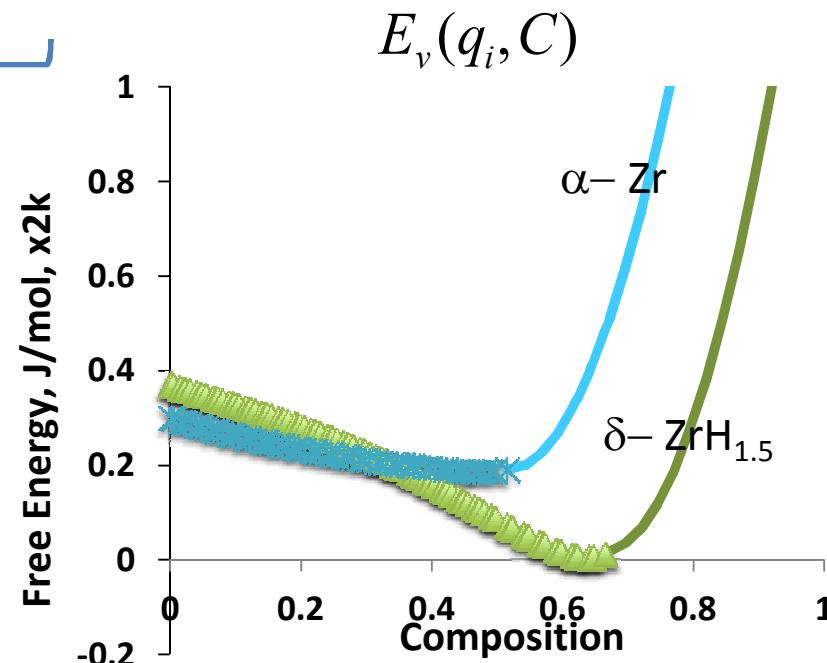
Equation of State (Thermodynamics)

- Combines elements of Potts and phase-field models to treat microstructure and composition evolution.
- EOS is a hybrid of volume free and interfacial energies obtained from both models.

$$E_{hyb} = \sum_{i=1}^N \left(\underbrace{E_v(q_i, C)}_{\text{Volume free energy}} + \underbrace{\frac{1}{2} \sum_{j=1}^n J(q_i, q_j)}_{\text{Interfacial free energy}} \right) + E_{dC}$$

- $E_v(q_i, C)$ is obtained from Thermo Cal
- $E_{dC} = \int 2\kappa_C (\nabla C)^2 dV$

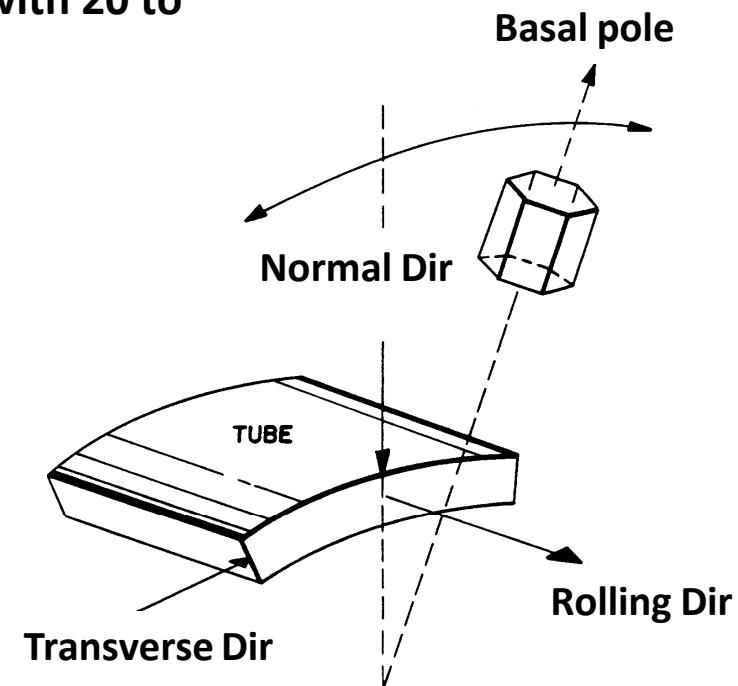
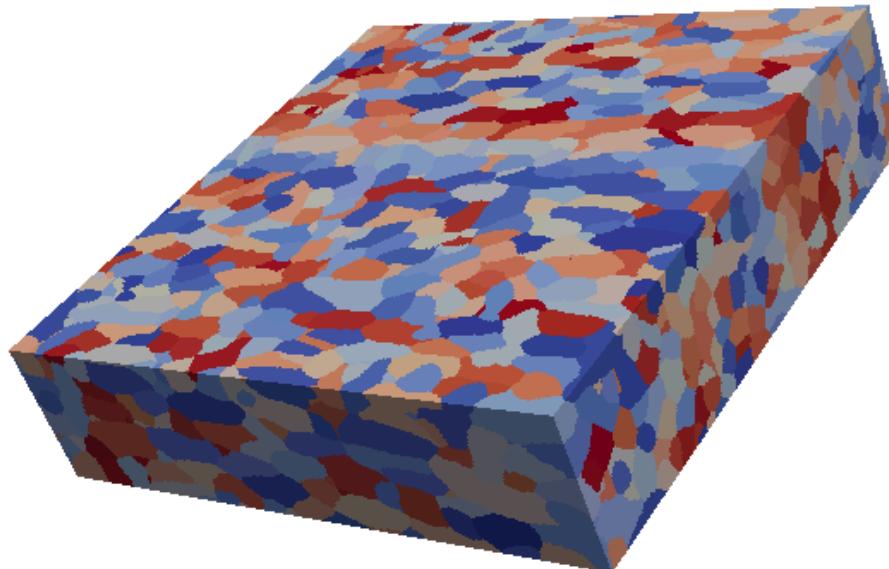
M. Glazov, INL, 2013



Zircaloy-4 and other Zr-based claddings are known to have texture

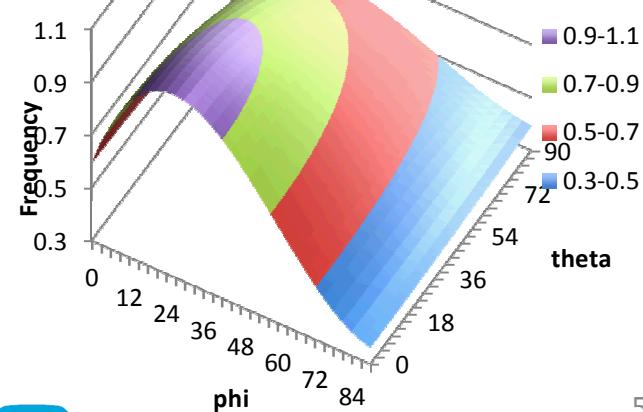
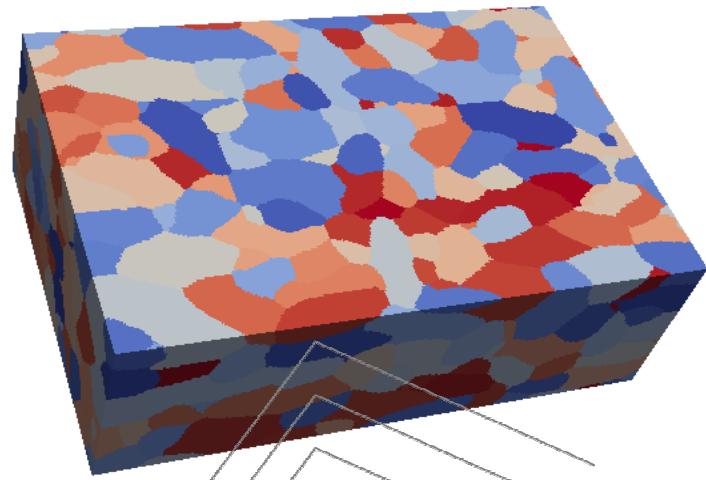
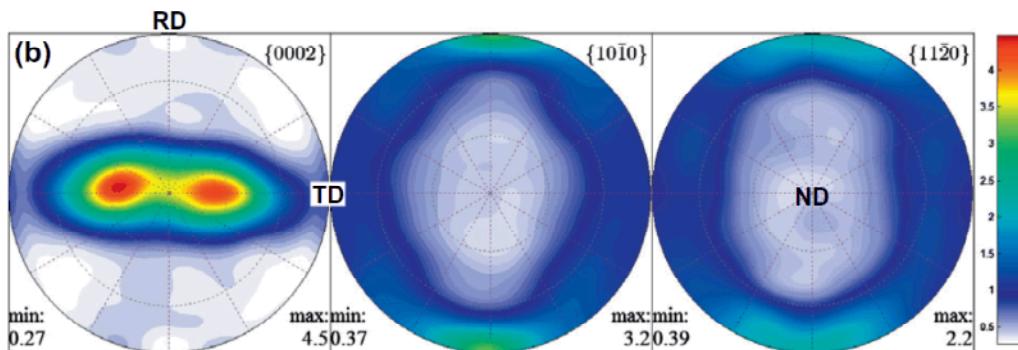
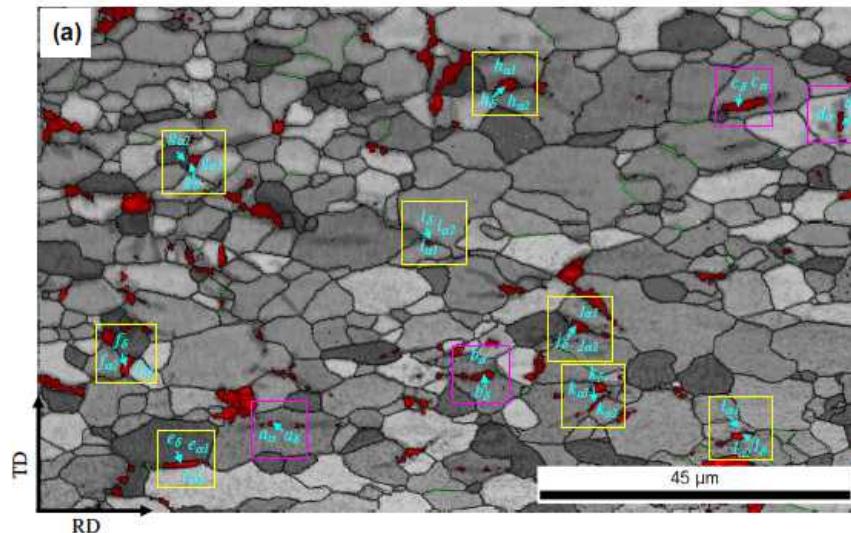
Pilgering process imparts texture

- Grain shape, elongated ~2x in rolling direction
- Crystallographic, basal plane parallel to ND with 20 to 40° rotation around TD



Generated a Digital Zr-4 Microstructure

from information available in the literature on grain and crystallographic texture

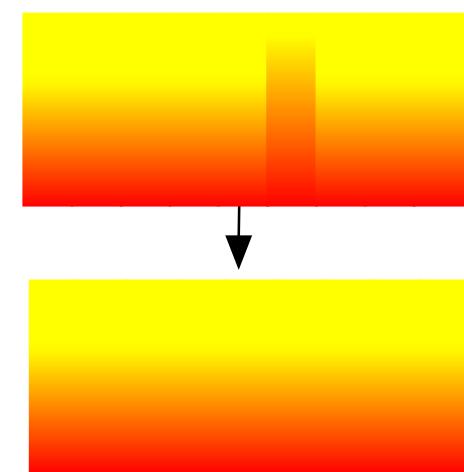
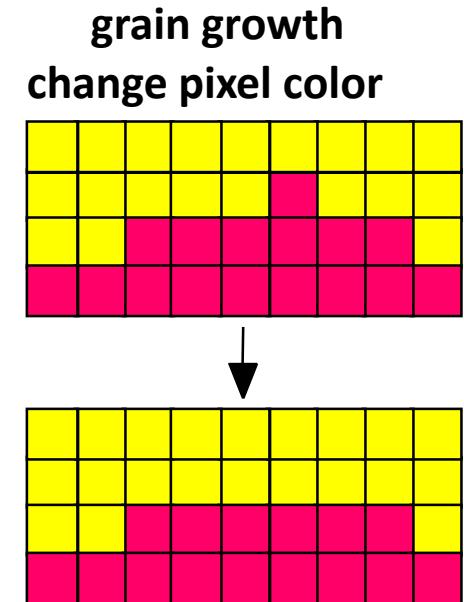


Kinetic of Evolution Hybrid Model

- Microstructure is evolved in the same manner as Potts in response to local free energy using E_{hyb}
 - Metropolis algorithm
- Composition evolved as a phase field parameter.

$$\frac{\partial C}{\partial t} = -M_c \left(\nabla^2 \frac{\partial E_v}{\partial C} - \kappa_c \nabla^4 C \right)$$

- Where E_v is from the hybrid Free Energy



Nucleation and growth of hydride precipitates is simulated by diffusion-controlled kinetics

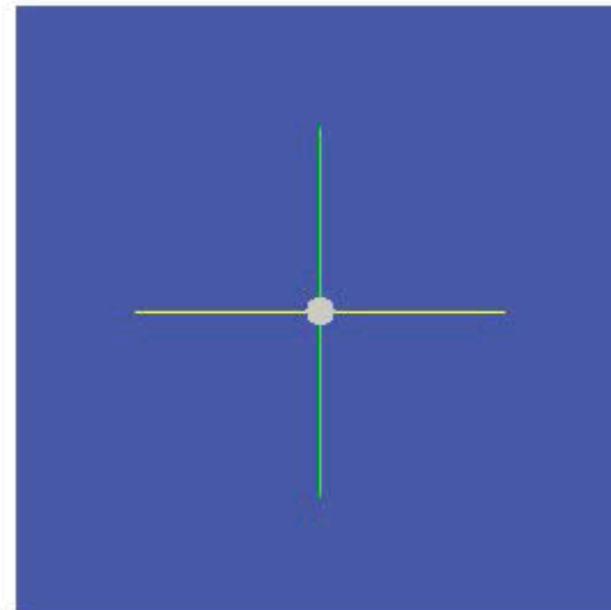
Model:

- Nucleation sites are designated in the single crystal at random locations
- Nucleation rate is constant
- Energetic bias is given to growth direction of the lathes

Precipitate nucleation and growth



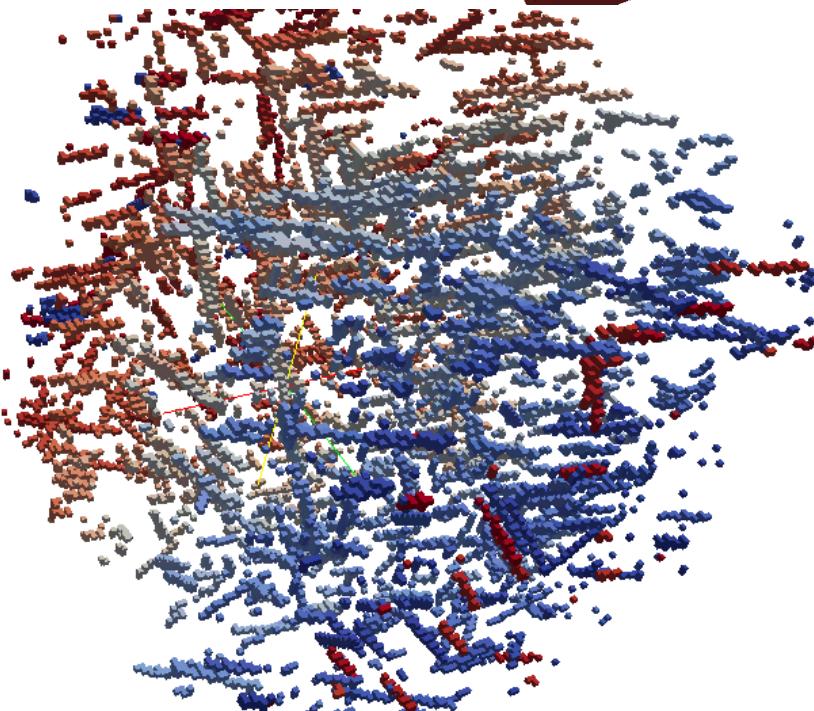
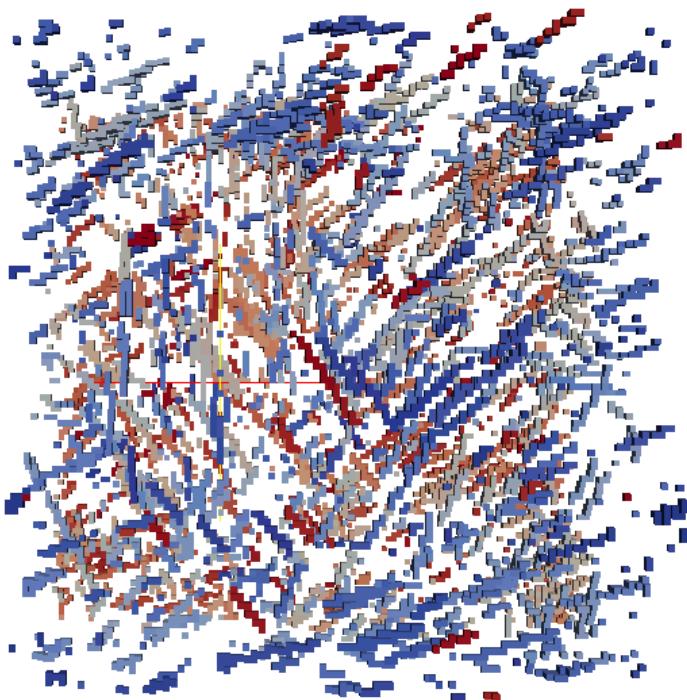
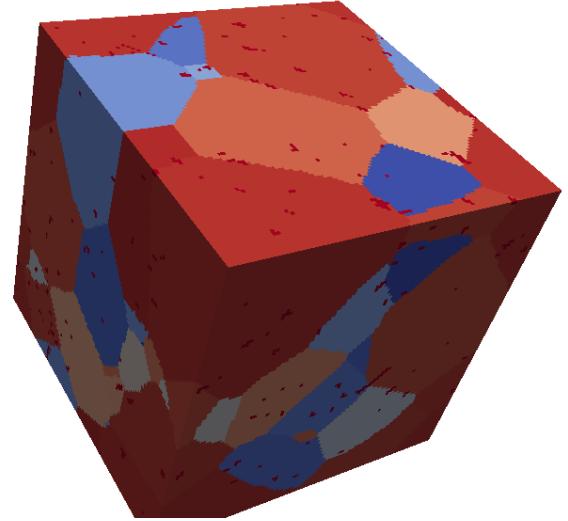
compositional evolution



ZrH_{1.5} Precipitation Polycrystalline Zr

Model:

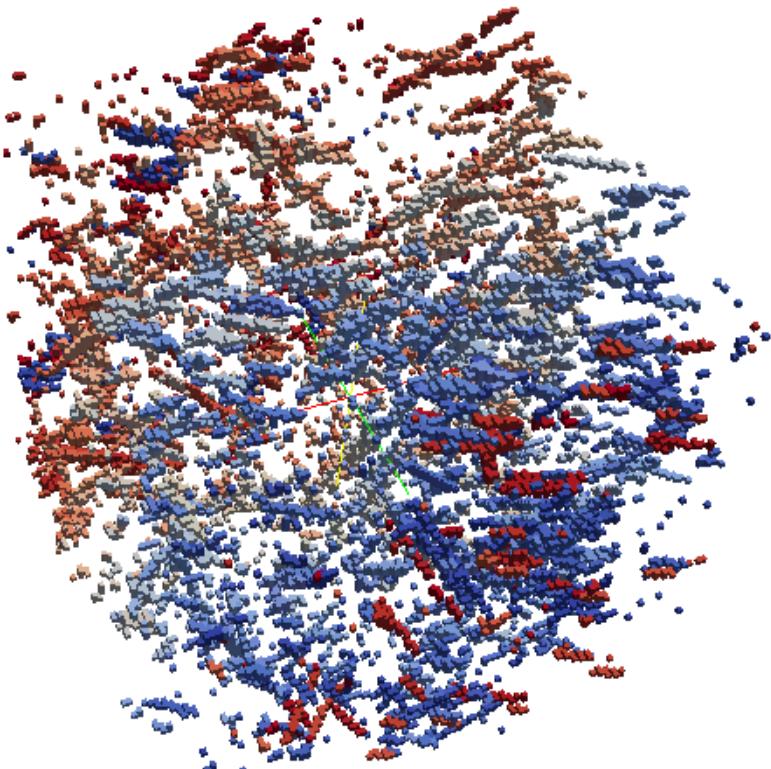
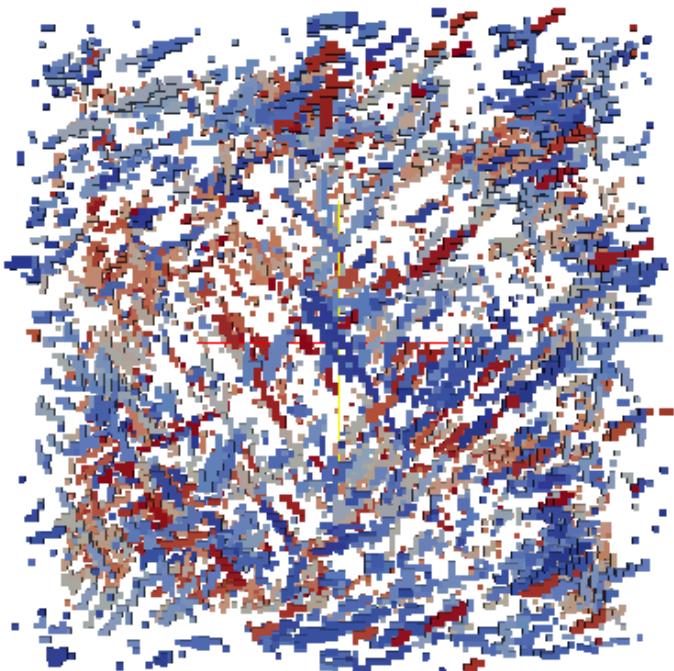
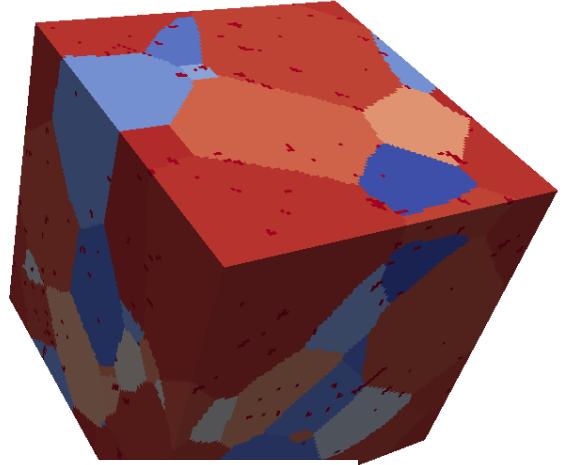
- Nucleation at random locations and nucleation rate is constant
- Energetic bias is given to growth direction of the lathes **with the orientation of the grain**



ZrH_{1.5} Precipitation Uniaxial Stress

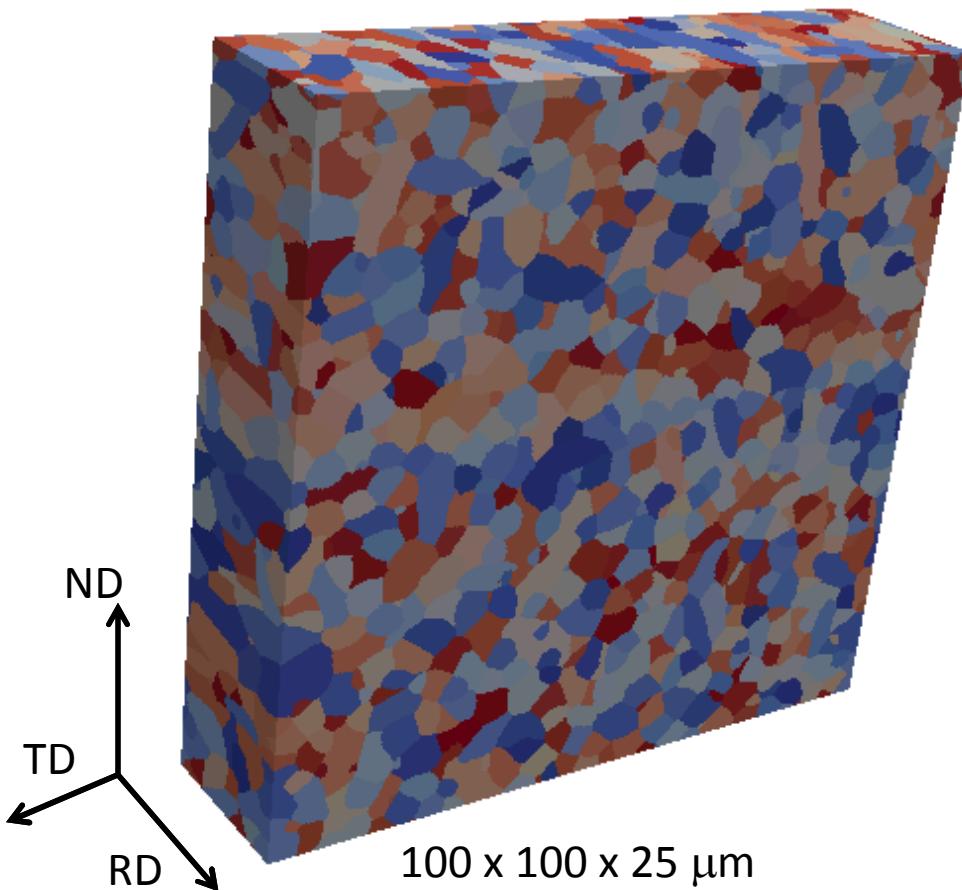
Model:

- Same microstructure
- Energetic bias is given to growth direction of the lathes **with the orientation of the grain and stress direction.**



Nucleation and growth of hydride precipitates

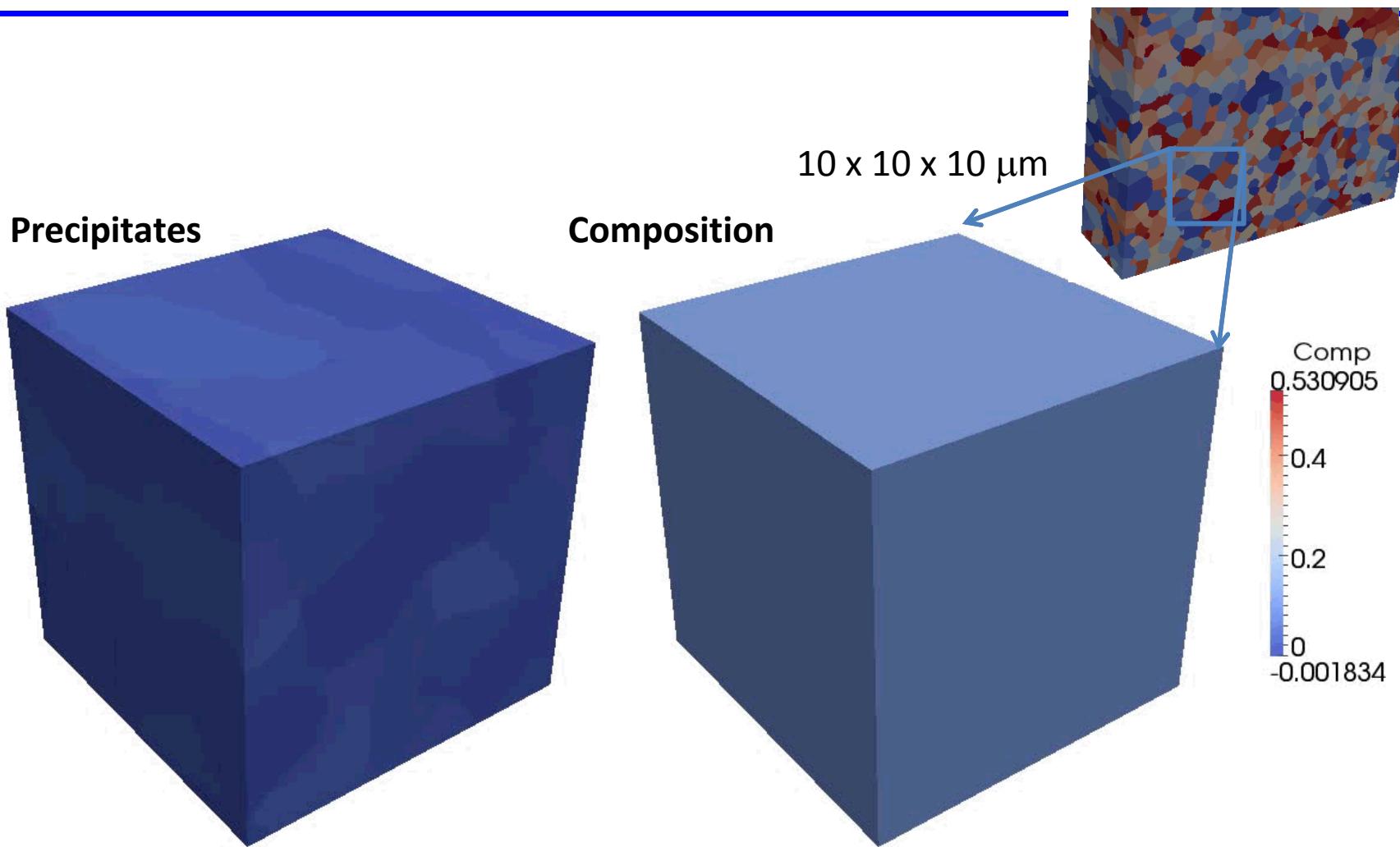
Initial microstructure



Simulation:

- Microstructure as shown
- Basal plane alignment with RD
- 1000 ppm H
- Zr-H thermo
- Nucleation and growth of precipitates
- Diffusion controlled kinetics

Nucleation and growth of hydride precipitates



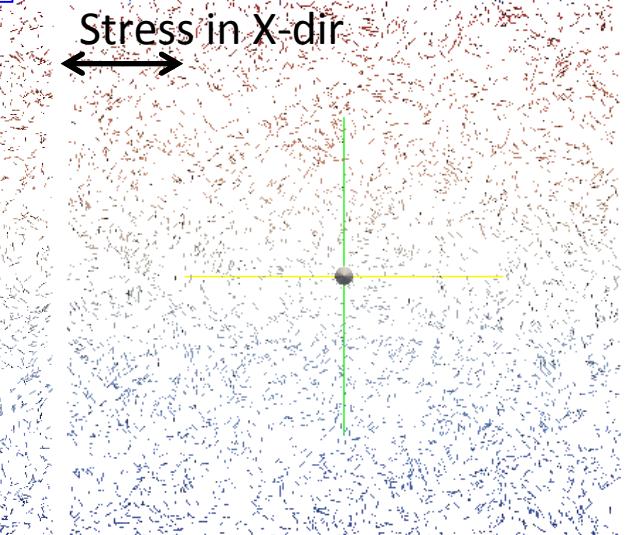
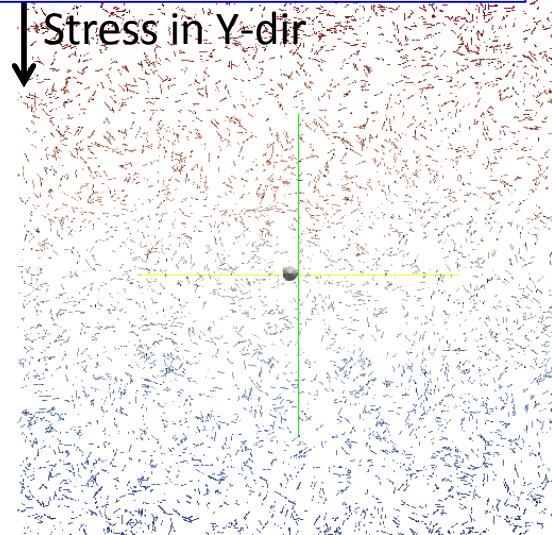
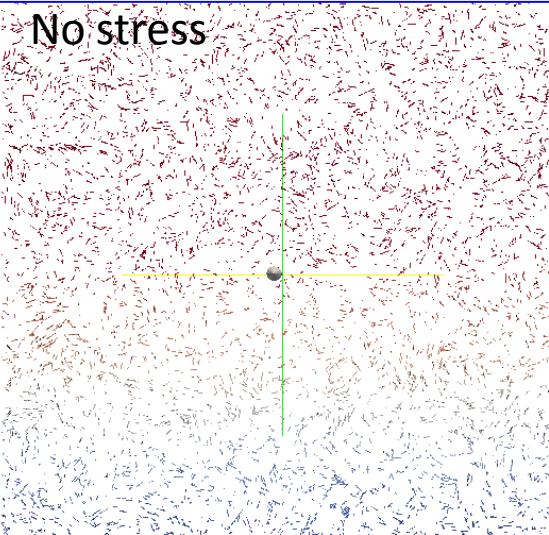
Nucleation and growth of hydrides

Simulation results

Precipitates align themselves perpendicular to the applied stress

- No stress, alignment is \sim random along basal plane
- Stress along Y-dir, alignment is perpendicular
- Stress along Z-dir, alignment is *less* perpendicular

However, simulated precipitates are uniformly distributed, individual precipitations do not re-align sufficiently to explain observed behavior



All Zr-based claddings show long-range cooperative formation (Billone et al, ANL UFD report, 2013)

Zirlo™



M5™



Zr-4



There is some missing materials physics in the model

- That gives the long-range ‘communication’ that allows precipitates to form with continuity
- Underlying microstructure is not just textured, but neighboring grains are aligned to give longer precipitate structures?
- Dilatation of ~14% accompanying hydride precipitation favors nucleation of the neighboring precipitates to give continuity?



There is some missing materials physics in the model

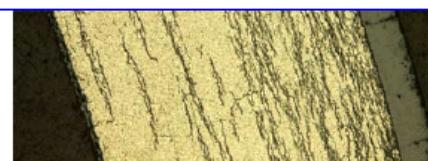
- Add the formation of the complex stress state around the precipitate to test hypothesis. This is much more easily done by modeling than experiments
- The spatial correlation of texture can be probed experimentally.



(c)



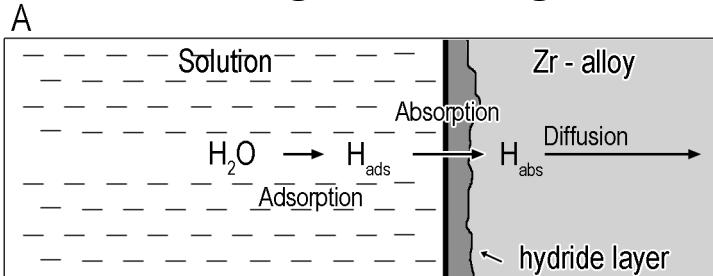
UFD Exp. & Anal. Rev, V. Tikare



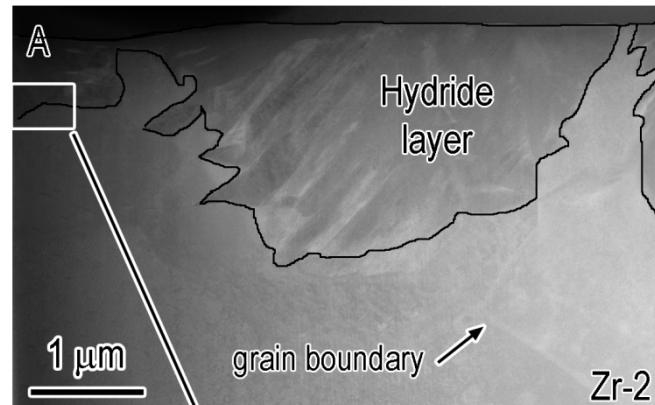
(c)

First V & V Case: Surface Hydride Growth in Zr-Based Claddings (B. Clark et al, SNL, 2013)

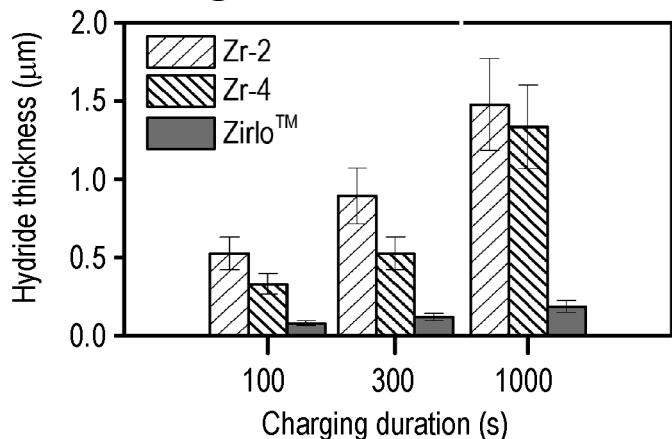
Zr-based cladding were 'charged' with H



Large variation in hydride layer size from grain to grain.



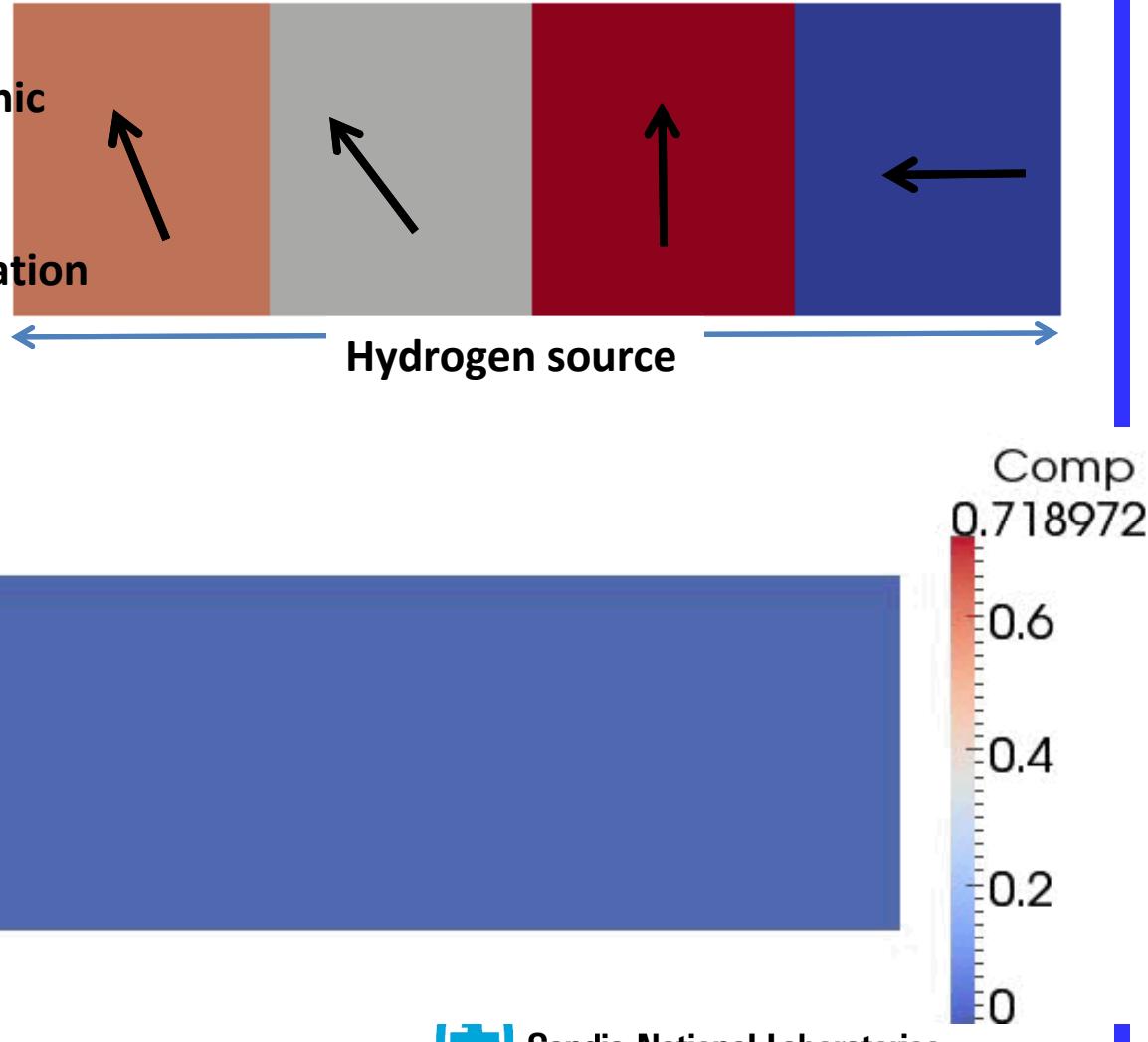
Kinetics suggest diffusion controlled growth, $d \sim t^2$



First V & V Case: Surface Hydride Growth in Zr-Based Claddings (B. Clark et al, 2013)

Simulation:

- Underlying microstructure
- Arrows show crystallographic direction
- H source on surface
- Diffusion controlled, nucleation and growth of precipitates
- Variables
 - D of α -Zr
 - D of δ -ZrH_{1.5}



First V & V Case: Surface Hydride Growth in Zr-Based Claddings (B. Clark et al, 2013)

Interfacial growth of hydride precipitates cannot give the variation with these kinetics.

Which diffusion behaviors can lead to the variation in hydride growth that is grain dependent?

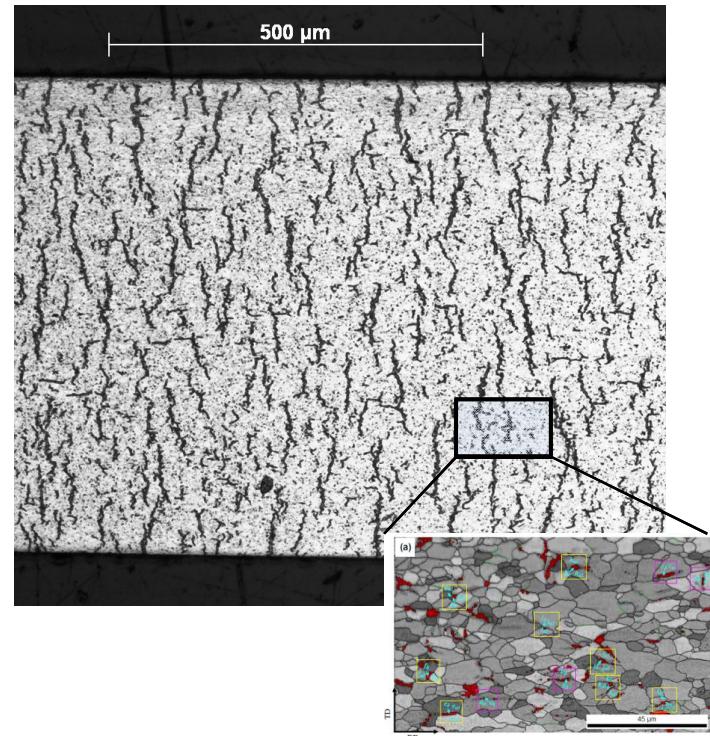
- D is a function of crystallographically direction in α -Zr
- Kearns reported $\sim D_a = 2D_c$, not enough to give variation in precipitate growth.
- Tried $D_a = 100D_c$, still no variation

- D is a function of crystallographically direction in δ -ZrH_{1.5}
- Need $D_a \sim 100D_c$, to get the differential growth.

Kearns, JNM 1972

Experimental Data Needed

- **Microscopy**
 - SEM of the hydrides
 - What are we seeing?
 - How do the individual precipitates align
 - Microstructure of α -Zr
- **Compositional effects**
 - Nb and other alloying elements
 - Free energy calculations



Hydride Roadmap

Where are we and where are we going?

- FY13: demonstrate basic hydride formation in Zr-4 microstructure
- Have a model:
 - Realistic microstructure
 - Reasonably large scale (can simulate 100's of grains.)
 - Actual thermodynamics (free energies)
 - Hydride formation (nucleation and growth)
 - Kinetics are diffusion controlled
 - Can capture radiation effects
 - Nucleation sites and rates
 - Diffusion

Hydride Roadmap

Where are we and where are we going?

- FY14: Further develop the model to simulate hydride formation
 - More complex chemical compositions
 - V&V exercises
 - Incorporating model into MOOSE/BISON/MARMOT
 - Adding temperature effects, both transient and non-isothermal
 - Add micro-mechanical coupling to
 - capture the local stress state around hydride precipitates
 - Influence hydride nucleation and growth

Need the coupling to the micro-mechanical model to address the long-range cooperative hydride precipitate alignment.