

Albany: A multiphysics application based on Trilinos

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- a parallel, implicit, unstructured-grid finite element code,
- that uses “as many Trilinos packages as possible” in a single code
- to demonstrate advanced engineering analysis capabilities across a wide range of physics applications.

- Albany illustrates how to integrate Trilinos packages in a general way to create a highly-featured parallel application including
 - Discretization services (Intrepid, Shards, STK, Seacas)
 - Linear solvers and preconditioners (Stratimikos, Belos, ML, MueLu)
 - Advanced nonlinear analysis (Piro, NOX, LOCA)
 - Leading edge software construction/engineering capabilities (Phalanx, TBGP, integrated build/test)

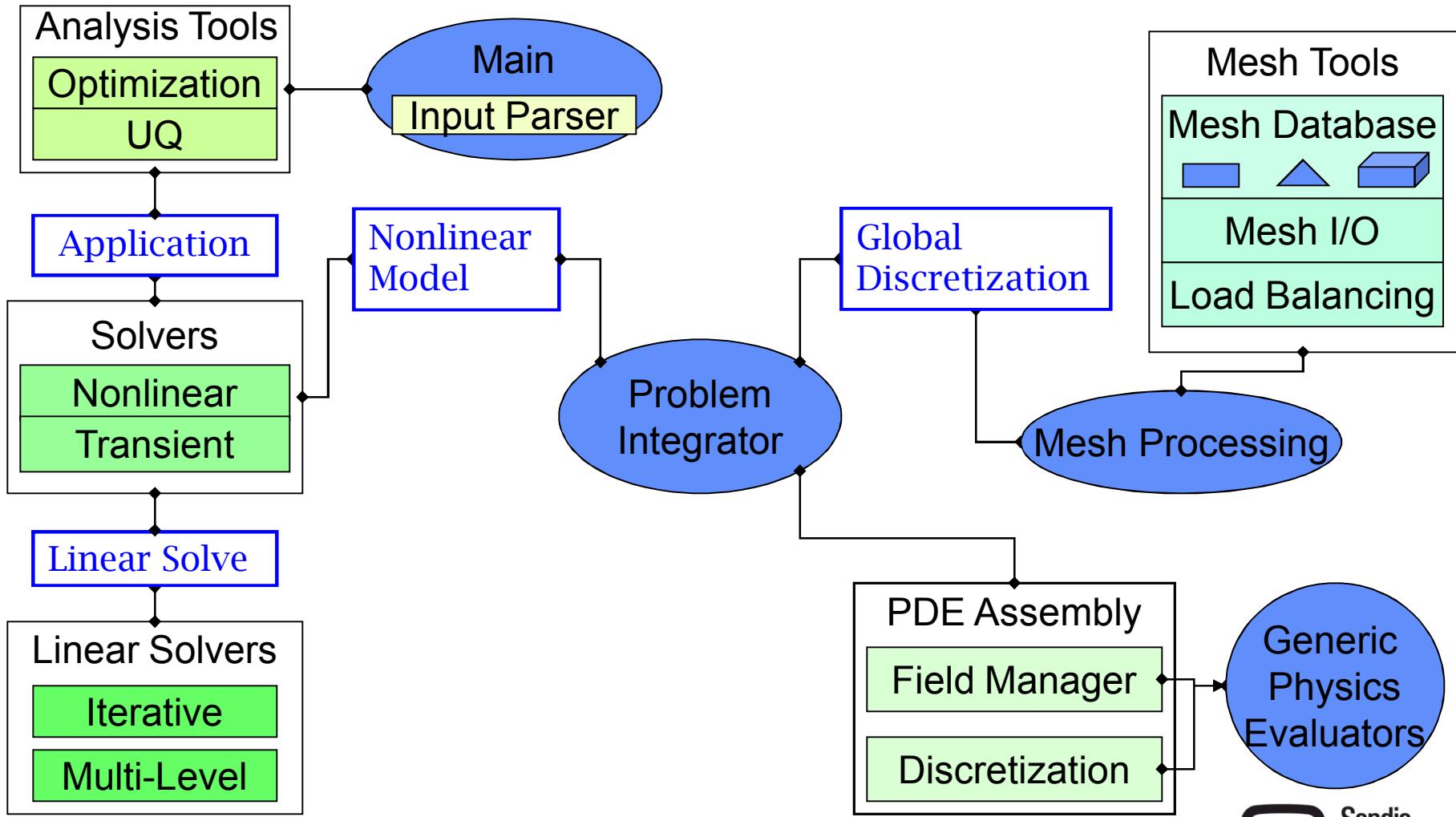


Trilinos packages enabled in AlbanySettings.cmake

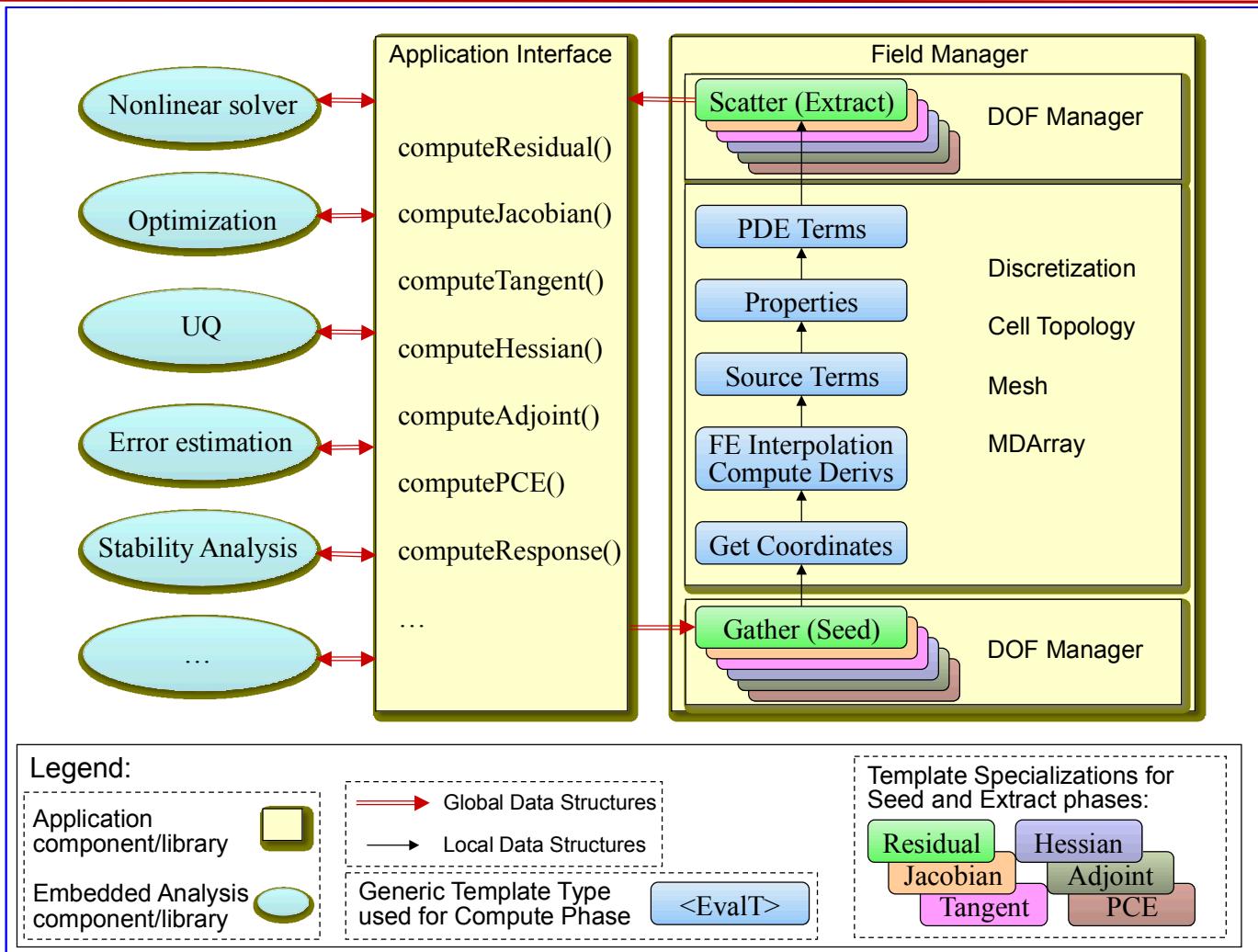
ThyraTpetraAdapters	Amesos	OptiPack
Ifpack2	Anasazi	GlobiPack
MueLu	Belos	Seacas
Teuchos	ML	Stokhos
Shards	Pamgen	Isorropia
Sacado	Phalanx	Piro
Epetra	Intrepid	STK
EpetraExt	NOX	Teko
Ifpack	Stratimikos	Zoltan
AztecOO	Thyra	Rythmos
		MOOCHO



Albany high level design



Albany generic physics interface

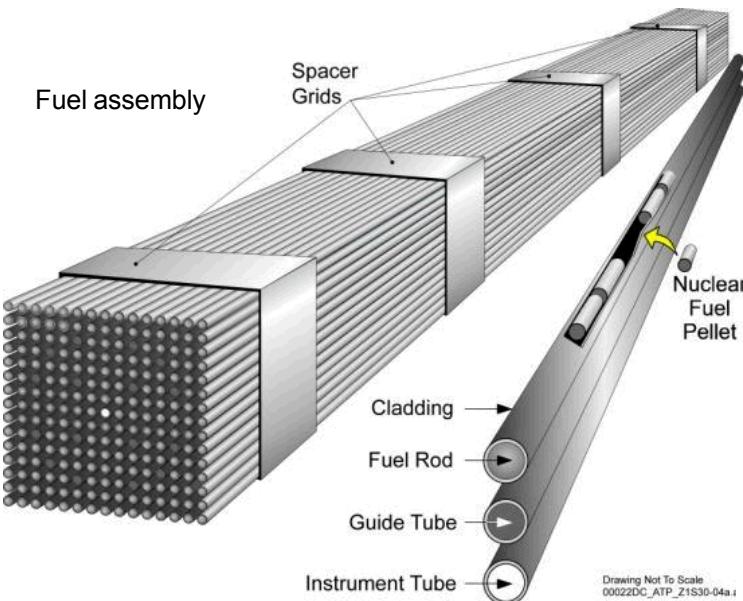


- **Test suite comprised of ~230 problems. Selected examples include:**
- **Computational mechanics**
 - elasticity, J2 plasticity, thermomechanics, unsaturated poroelasticity, thermo-poro-mechanics, diffusion-deformation, cladding Zry4 hydride reorientation, gradient damage, rate independent hardening minus recovery (RIHMR)
- **Fluids**
 - compressible Navier-Stokes, finite element for land ice experiments (FELIX), coupled reactor, vortex shedding, Rayleigh-Bernard
- **Diffusion, misc**
 - heat equation, Poisson Schrodinger, Cahn Hilliard / Elasticity, continuation, load and displacement stepping problems

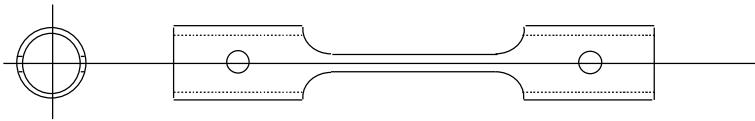


Selected Albany Application Examples

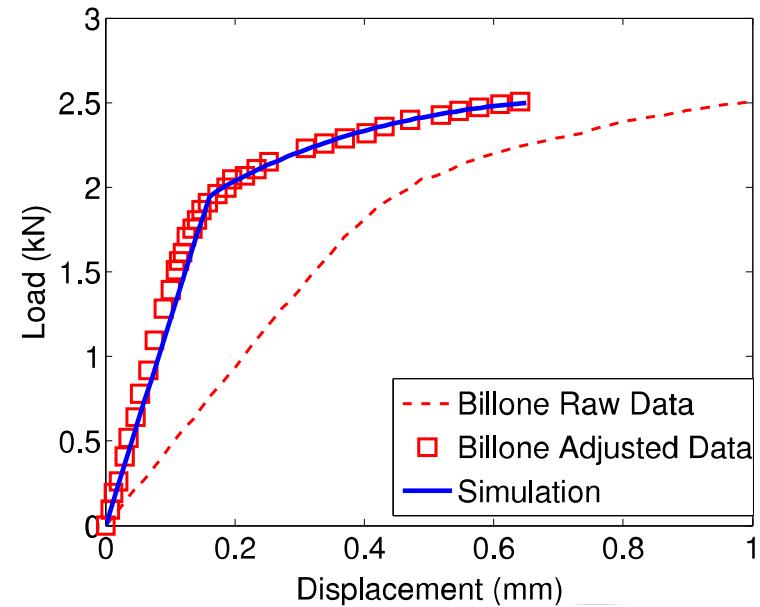
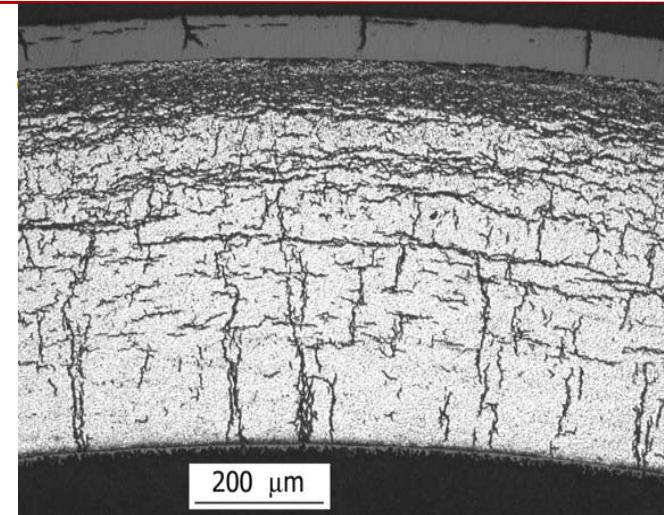
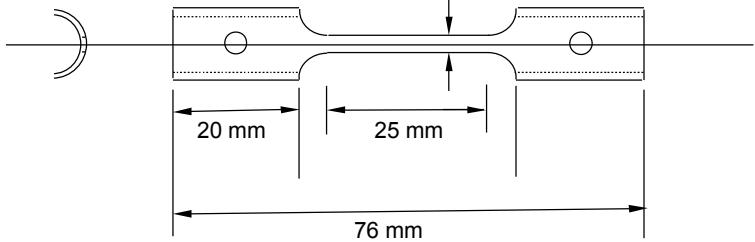
Used reactor fuel handling



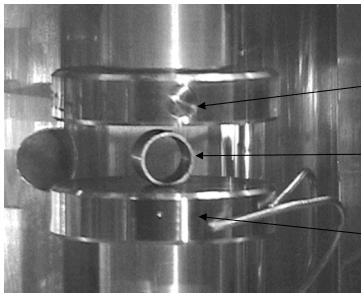
Double Gauge



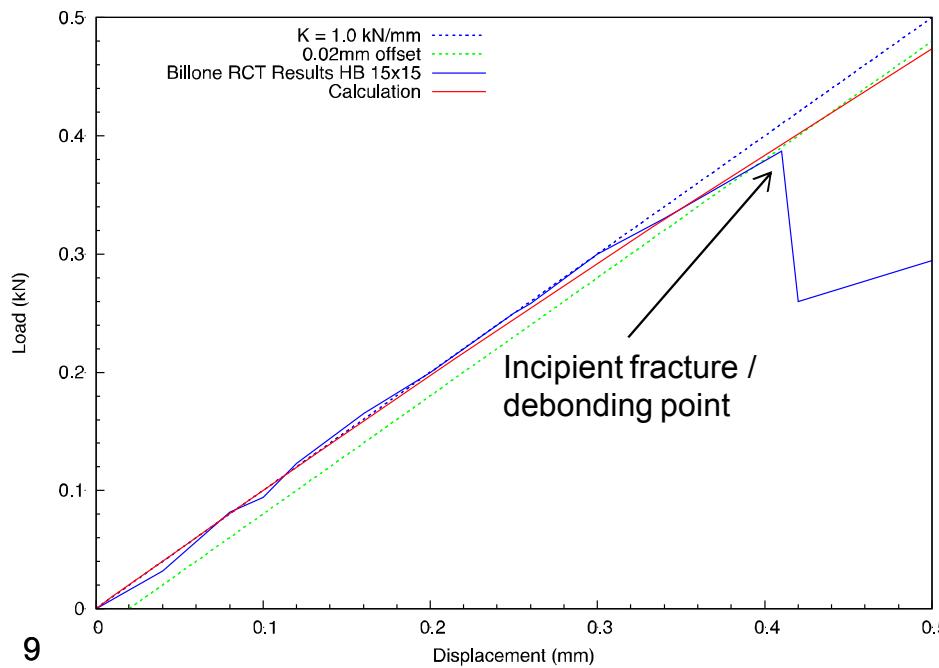
Single Gauge



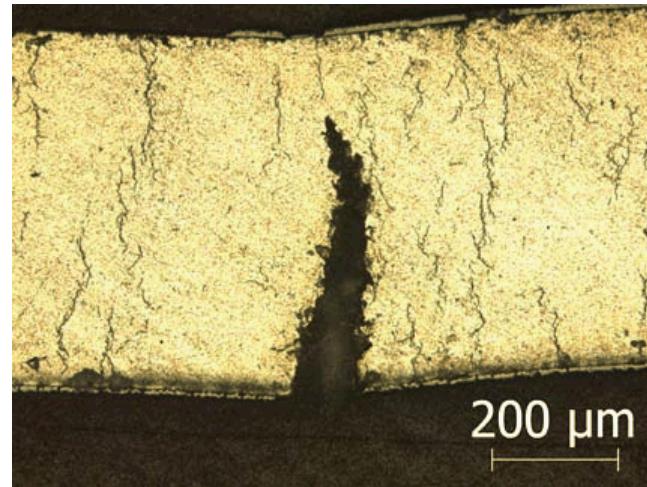
Predict cladding behavior



Ring Compression Test Fixture



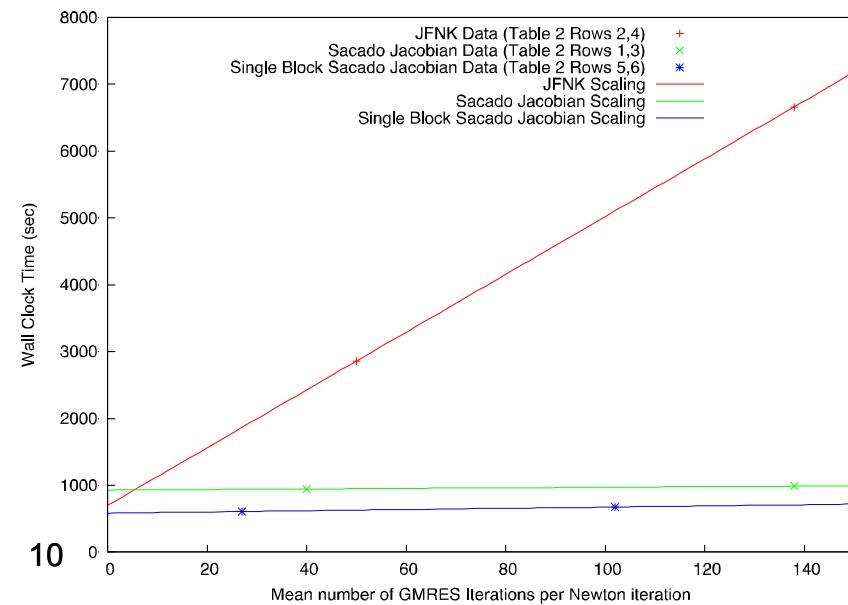
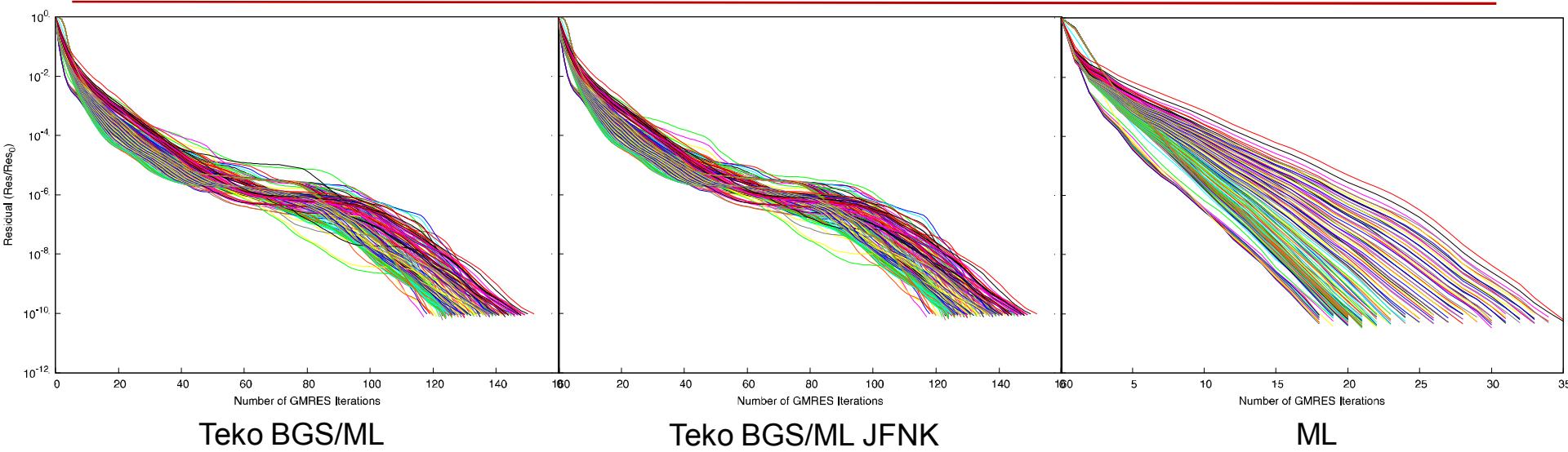
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Billone, et.al. 2012

- Excellent agreement was obtained with experiments on actual fuel samples, up to the point of sample failure

Using state of the art analysis capabilities

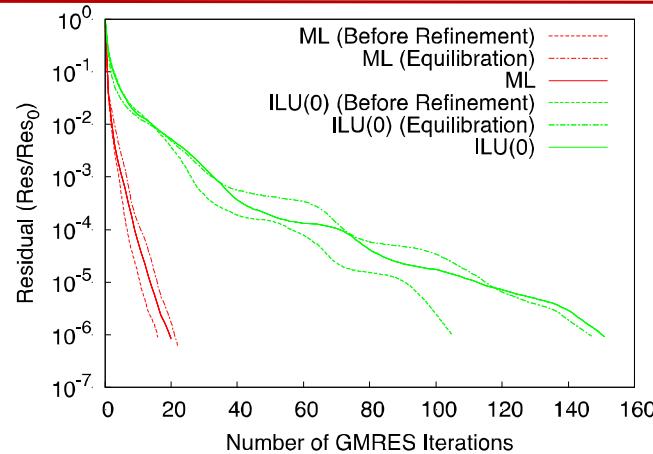


Albany features found most impactful:

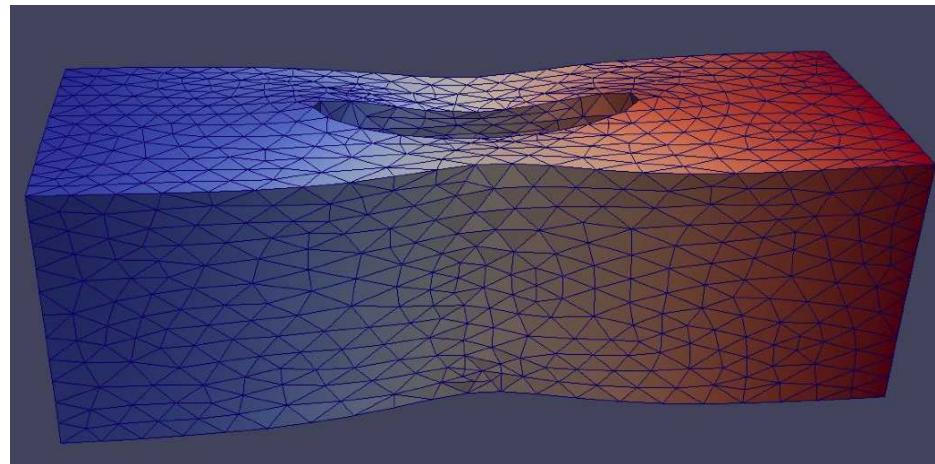
- Rapid model implementation
- Extensive collection of existing physics capabilities that are easily "reused"
- Wide variety of solvers and preconditioners can be brought to bear on the problem
- Everything needed "under one roof": LOCA continuation, parallel load balancing, SA and UQ (TriKota), multiple Jacobian strategies, etc

Adaptive elasticity

- **Elastic deformation of a rectangular bar**
- **Continuation problem: location of right boundary is the continuation parameter**
- **Zienkiewicz-Zhu error indicator drives refinement near hole**
- **Preconditioned Belos (GMRES) solver used inside LOCA**
- **Consider ILU(0) and AMG (SA) – Albany communicates rigid body modes (null space info) to ML**

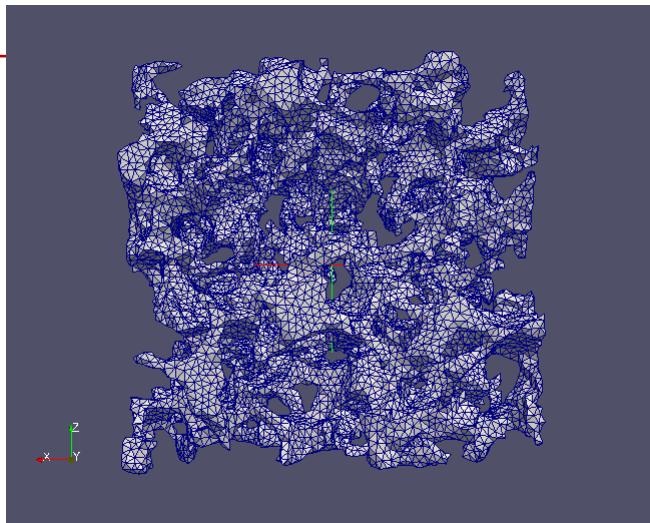


Convergence: Comparing preconditioning options

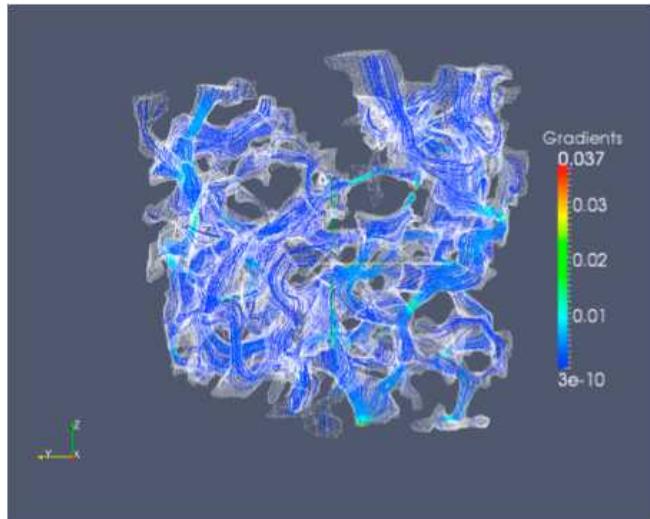


Bar deformation: Mesh adapts to reduce error (ZZ)

LCM: Estimating Effective Thermal Conductivity from Microstructures



Mesh generated from CT images of 12% porosity
Fontainebleau sandstone (from Teng-fong Wong)



Single-phase Thermal Diffusion simulation on
CT Images

- Volume averaging effective thermal conductivity

$$\mathbf{k}_\theta = \phi^f \mathbf{k}_\theta^f + (1 - \phi^f) \mathbf{k}_\theta^s$$

(cf. Preisig & Prevost, IJGGC 2011)

- Homogenized effective conductivity via Eshelby equivalent inclusion method (for spherical inclusions)

$$\mathbf{k}_\theta = \left(\mathbf{k}_\theta^f + \frac{\phi^f (k_\theta^s - k_\theta^f) k_\theta^f}{(k_\theta^s - k_\theta^f) \phi^f + k_\theta^f} \right) \mathbf{I}$$

(cf. Zhou & Meschke, IJNAMG 2013)

LCM: Optimal Stabilization Parameter Estimation

1D poromechanics governing equation

$$c \frac{\partial^2 \hat{p}}{\partial x^2} = \frac{\partial \hat{p}}{\partial t}, \quad c = \frac{k}{\mu} \frac{M' H}{H + \nu \beta M'}; M' = \frac{M(K + 4G/3)}{K + 4G/3 + B^2 M}$$

Three node stencil (standard Galerkin method)

$$-\hat{p}_{A-1} + 2\hat{p}_A - \hat{p}_{A+1} + \frac{h^2}{6\vartheta c \Delta t} (\hat{p}_{A-1} + 4\hat{p}_A + \hat{p}_{A+1}) = 0$$

Three node stencil (Stabilized Galerkin method)

$$-\hat{p}_{A-1} + 2\hat{p}_A - \hat{p}_{A+1} + \frac{h^2}{12\vartheta c \Delta t} [(2 - \gamma)\hat{p}_{A-1} + (8 + 2\gamma)\hat{p}_A + (2 - \gamma)\hat{p}_{A+1}] = 0$$

Growth/decay rate

$$\cosh \frac{h}{(\sqrt{\vartheta c \Delta t})^h} = \frac{(1 + h^2/\vartheta c \Delta t)(4 + \gamma)/6}{(1 - h^2/\vartheta c \Delta t)(2 - \gamma)/12}$$

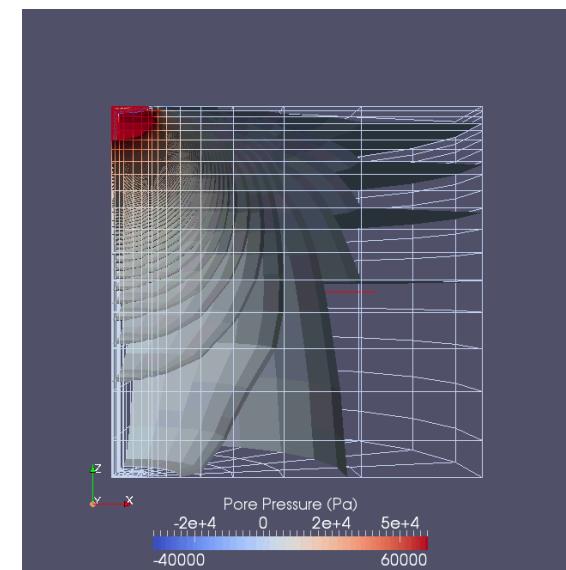
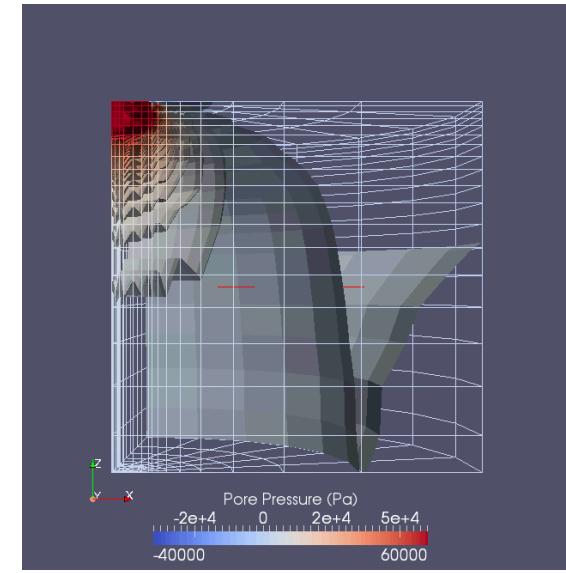
To have real growth/decay rate, we need

$$\gamma > 2 - 12 \frac{\vartheta c \Delta t}{h^2} > 0$$

$$\gamma = (2 - 6 \frac{\vartheta c \Delta t}{h^2}) \left(\frac{1}{2} + \frac{1}{2} \tanh(2 - 12 \frac{\vartheta c \Delta t}{h^2}) \right)$$

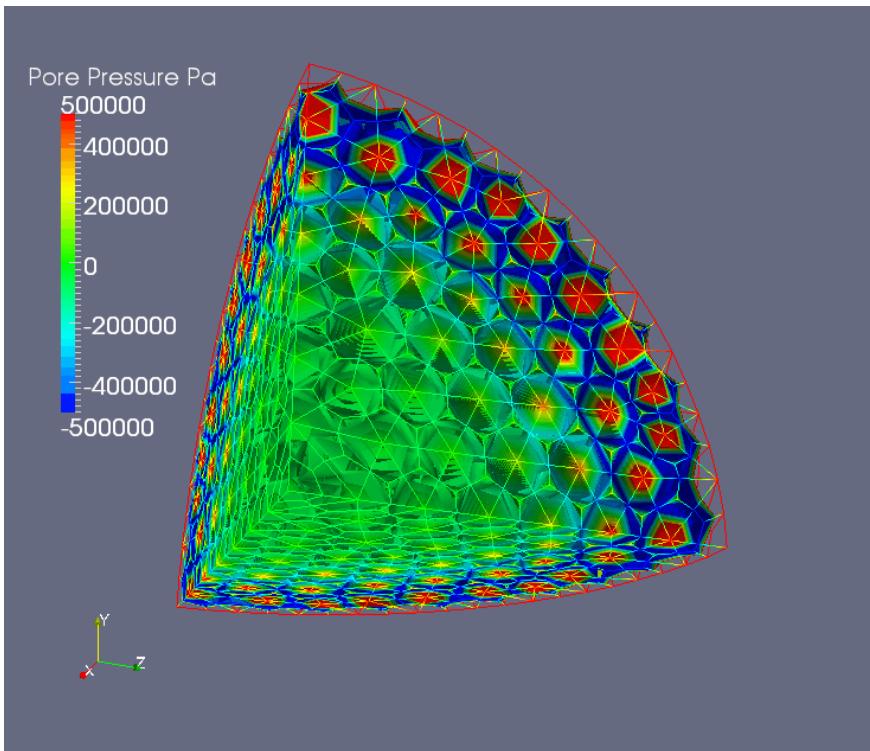
Safety factor

Turn off stabilization without introducing switch



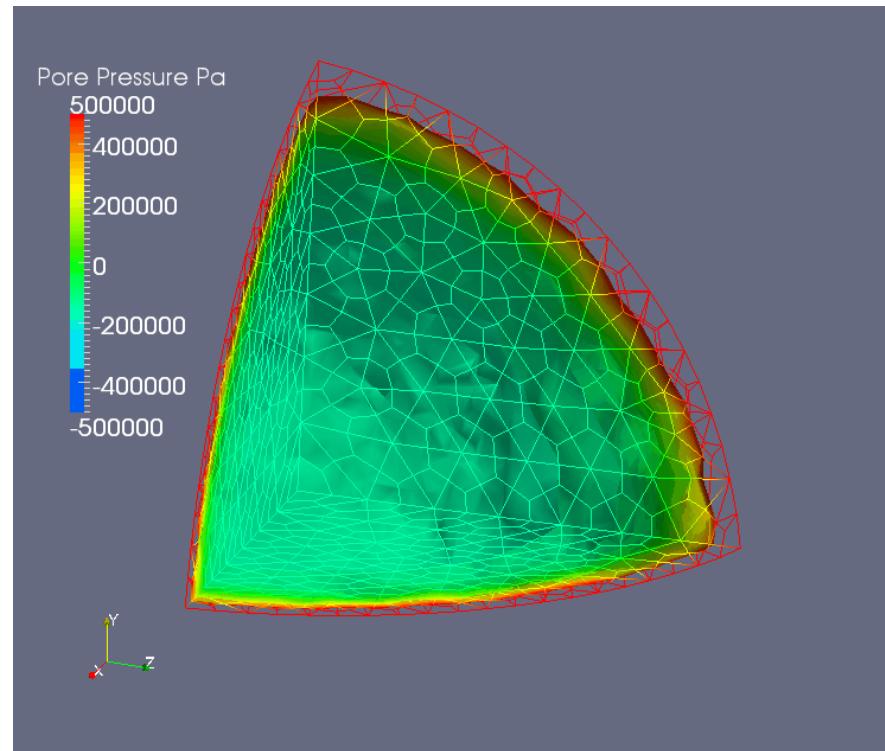
Thermo-hydro-mechanical Responses of Porous Sphere in Thermal Reservoir

Under-diffusion with spurious patterns



Pore Pressure computed with standard Galerkin FEM

Diffusion with estimated optimal stabilization

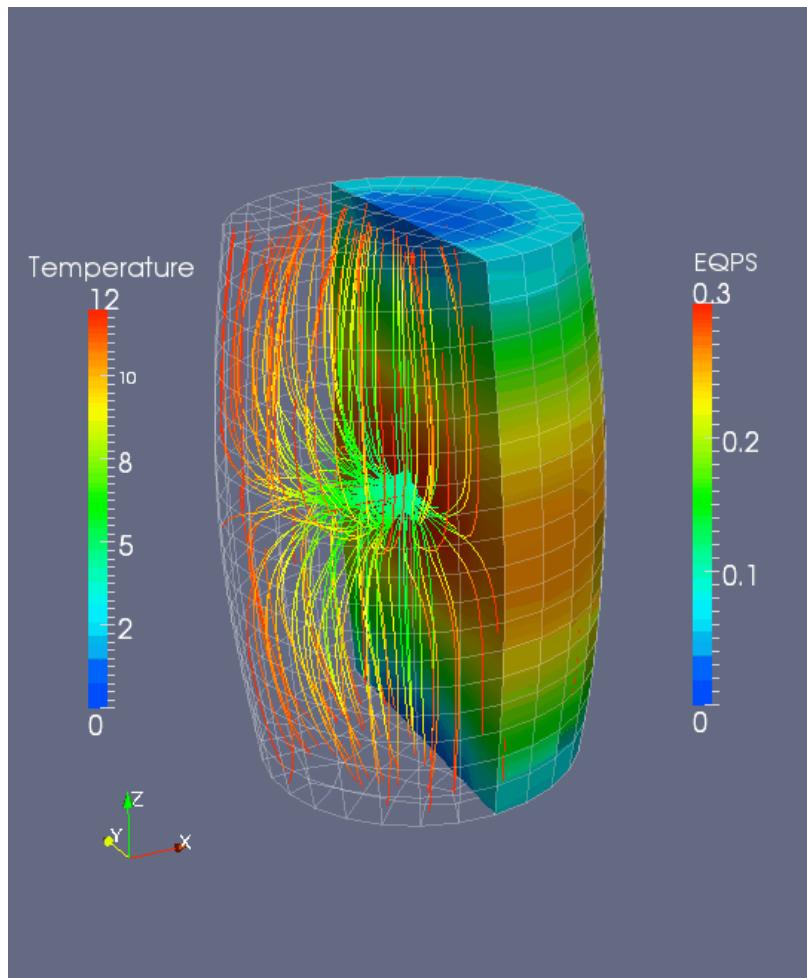


Pore Pressure computed with Stabilized FEM

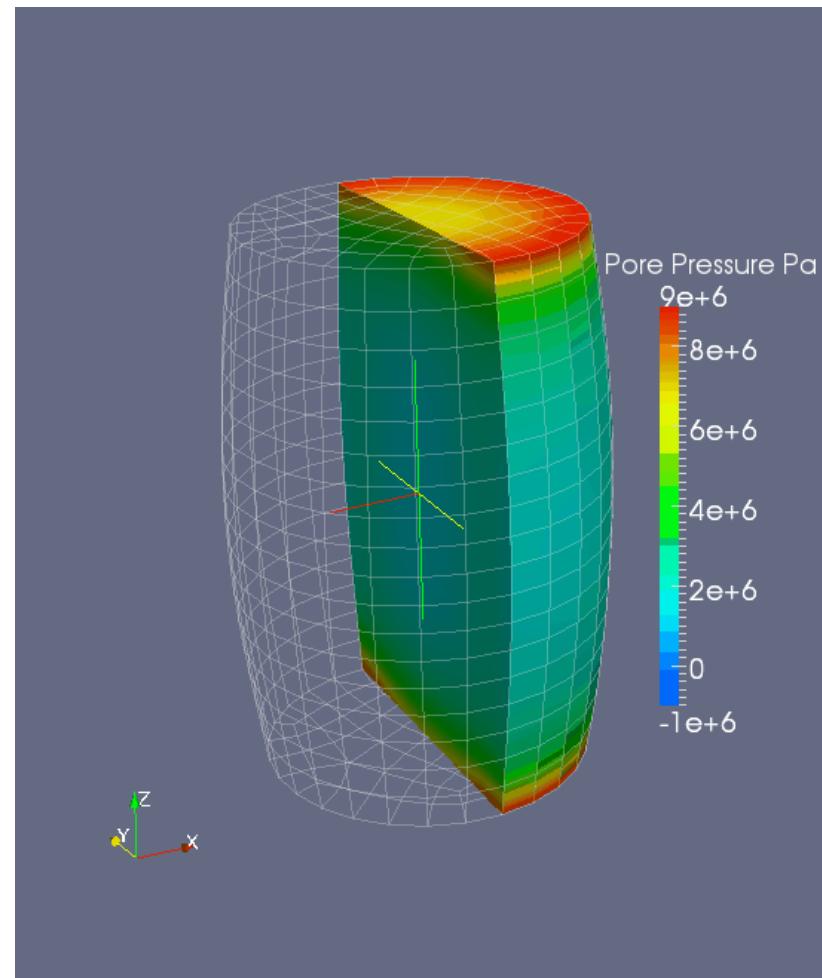
Note: we do not impose shape pore pressure gradient.

Unconfined Compression Test of Cold Thermo-sensitive Porous Media at Room Temperature

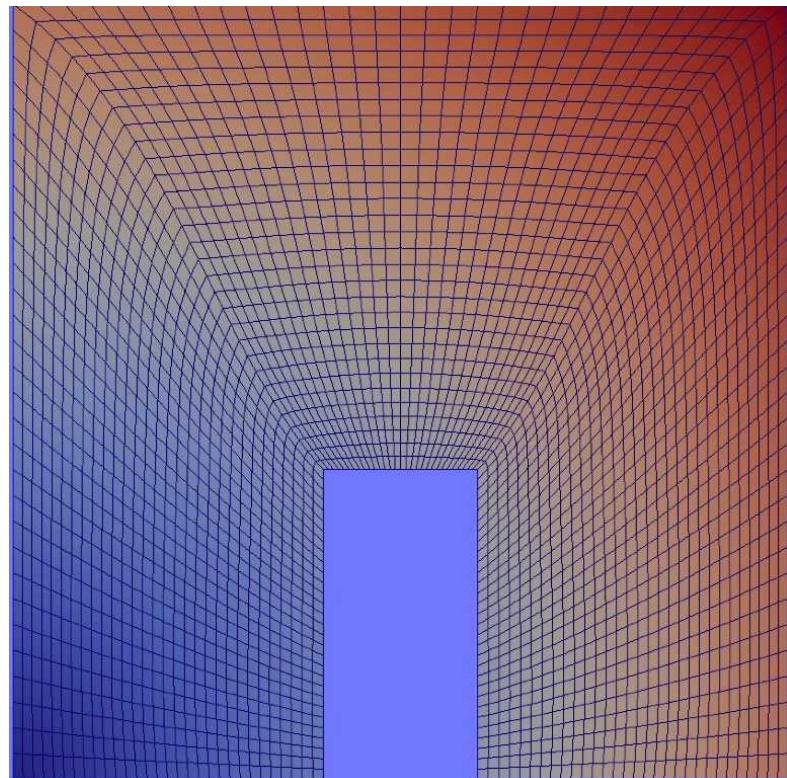
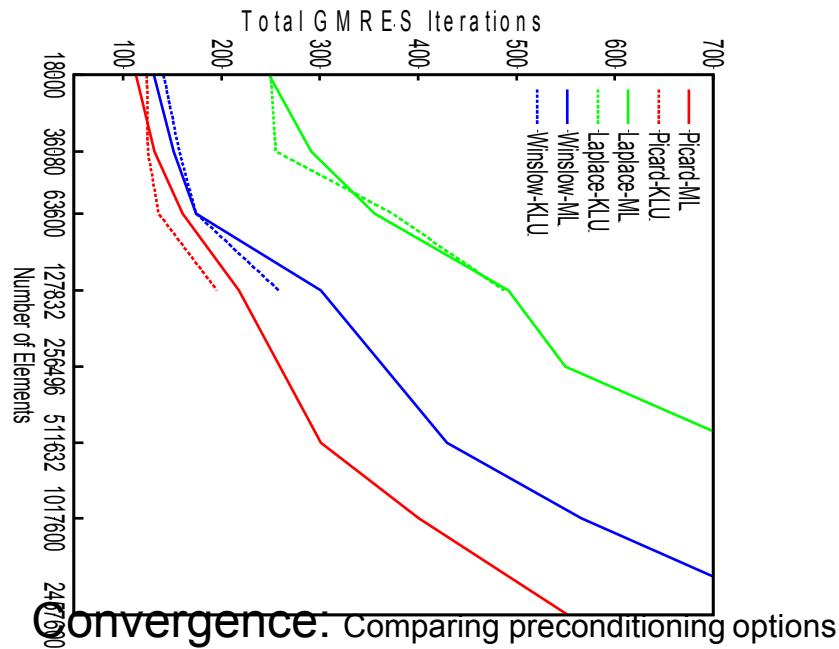
Temperature & equivalent plastic strain



Pore Pressure



- Rapid development of Laplace Beltrami ALE mesh adaptation strategy
- Collection of Trilinos solvers, preconditioners, and continuation strategies supports algorithmic experimentation
- Goal: add FieldManager to Alegra and directly "share" remesh evaluators between Albany and Alegra

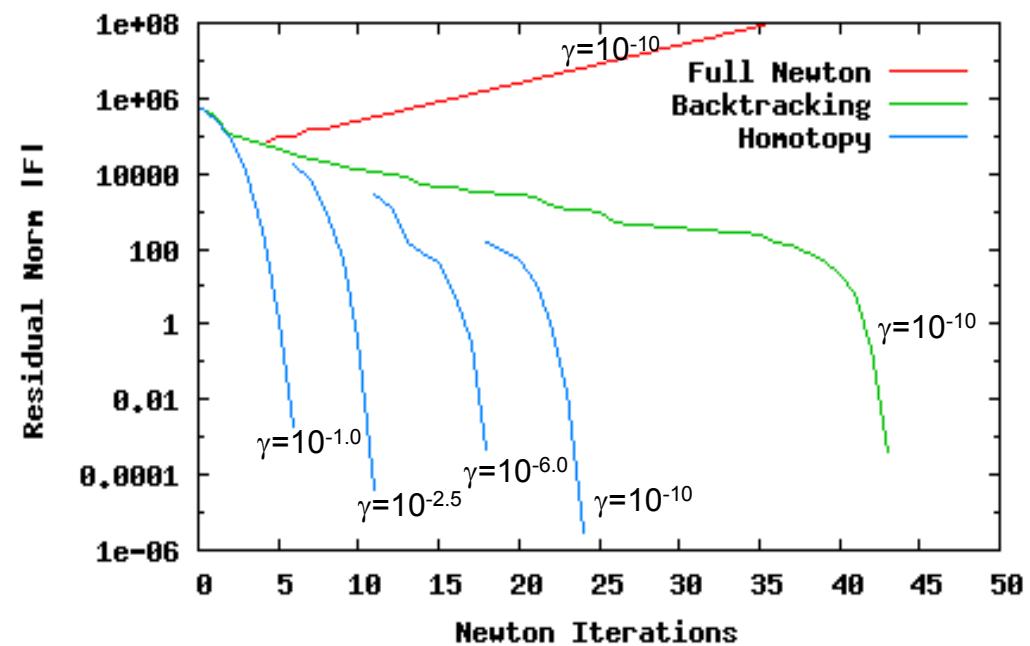
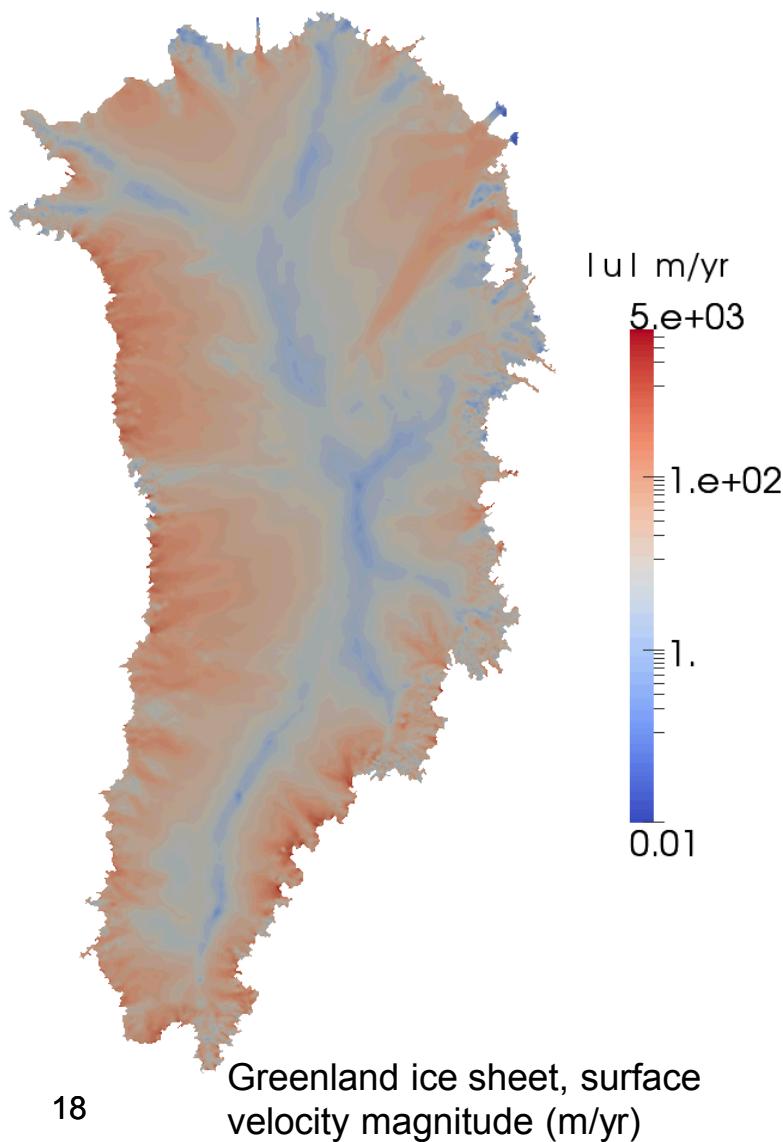




- **Navier-Stokes problem**
- **Rythmos time integration: Implicit RK – 1 step Θ (trapezoidal)**
- **Corresponding bifurcation solution (critical velocity 60.254)**

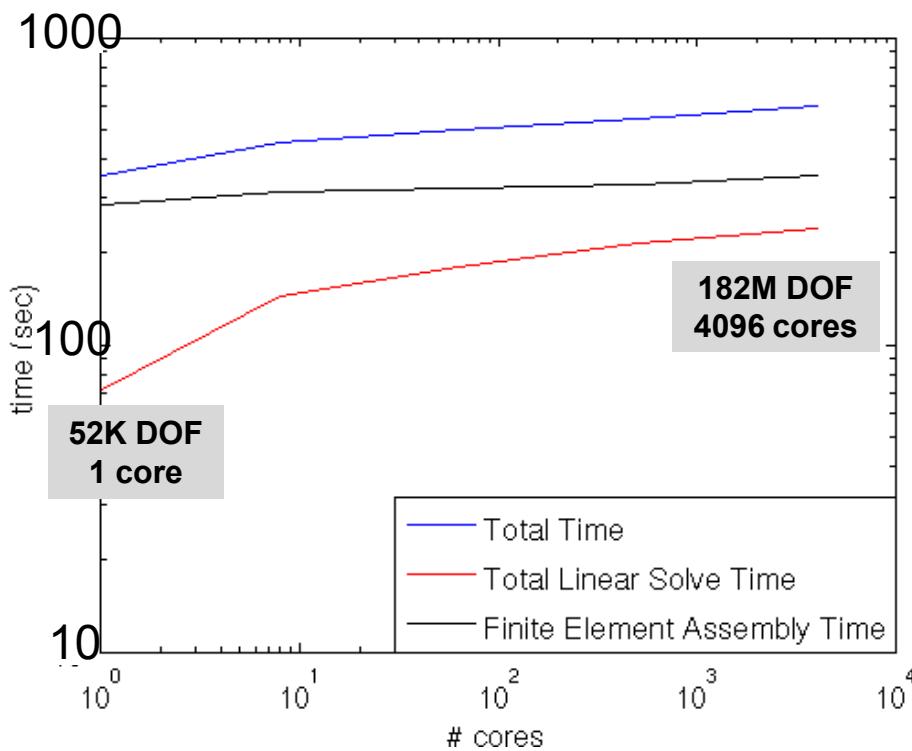


FELIX (Finite Element Land Ice eXperiments)



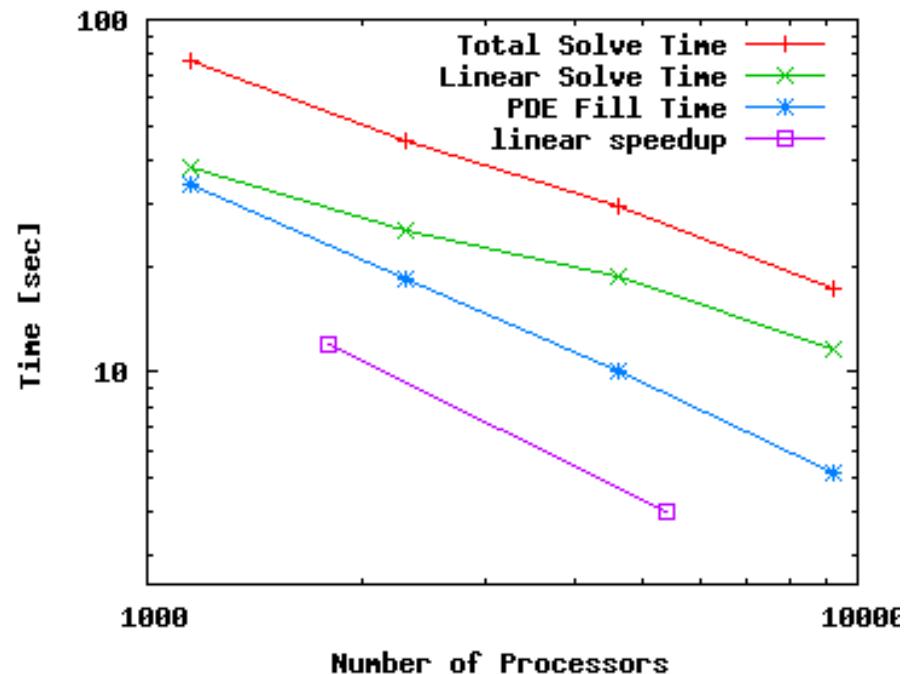
Robustness: Full Newton Method augmented with Homotopy Continuation

Scalability: Initial Data (On Hopper)



Weak Scaling on ISMIP Test problem:

- 60% Efficiency after 4096x scale-up
- Finite Element Assembly nearly constant
- Linear algebra fast but not constant
- Results by: Ray Tuminaro



Strong Scaling on gis2km steady solve:

- 4.5x speed-up on 8x processors
- Absolute times are small
- Setup/PostProcessing cost not shown
- Results by: Pat Worley



Further information

- Albany download web page: <https://software.sandia.gov/albany>
- Albany paper, A. Salinger et. al., "Albany: A Component-Based Partial Differential Equation Code Built on Trilinos," SAND-2013-8430-J (submitted to ACM-TOMS) and references contained therein
- Getting started doc:
<https://software.sandia.gov/albany/gettingStarted.pdf>
- Points of contact: Glen Hansen, gahanse@sandia.gov, Andy Salinger, agsalin@sandia.gov