

Modeling the temperature and excitation dependences of efficiency in InGaN light-emitting diodes

SAND2013-6276P

Weng Chow, Sandia National Laboratories

III-N material system, LEDs and efficiency

Microscopic model

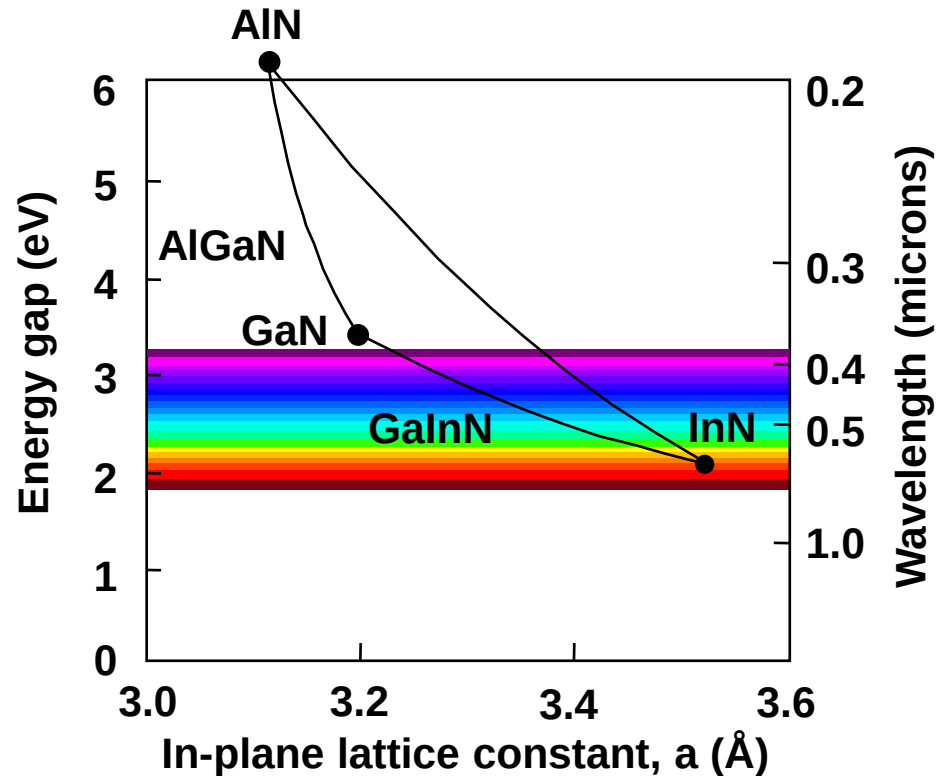
Efficiency versus excitation and temperature

Thanks to:

Sandia's Energy Frontier Research Center (EFRC), DOE, Basic Energy Sciences

Sandia National Laboratories is a multi-program laboratory operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Company, for the United States Department of Energy's National Nuclear Security Administration under Contract DE-AC04-94AL85000

Visible and ultraviolet lasers: wide bandgap Group-III Nitrides

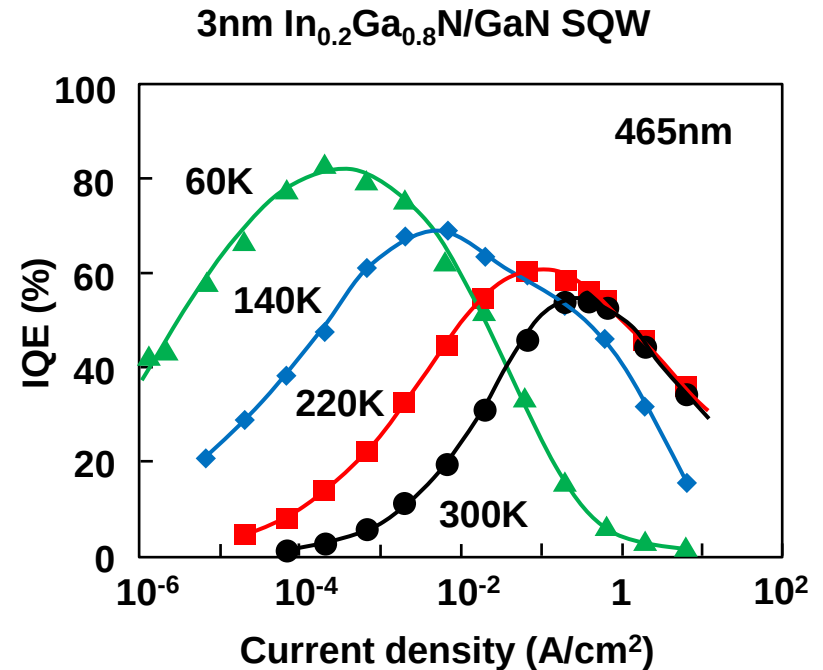
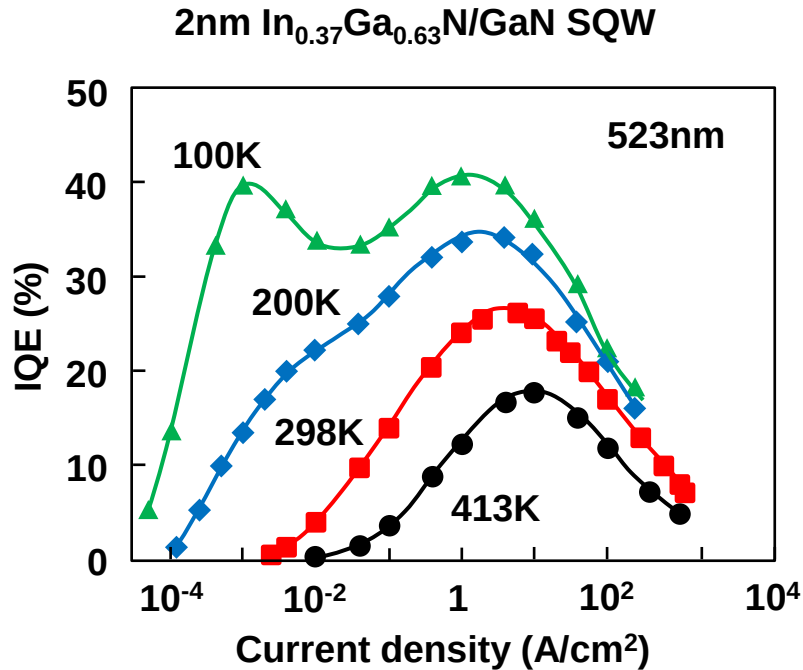


Interesting physics

- High exciton binding energy $\longrightarrow$ Strong many-body Coulomb effects
(23meV for GaN vs. 5meV for GaAs) Chow, Knorr, Koch, Appl. Phys. Lett. 67, 754 (1995)
- Wurtzite crystal symmetry $\longrightarrow$ Strong quantum confined Stark effect

Important applications: visible and ultraviolet lasers and LEDs

Experiment



Possible efficiency droop mechanisms

- Auger losses
- Carrier leakage
- Non capture
- Defect
- Junction heating

Considerations for model

- Systematic, unbiased accounting of mechanisms
- Possibility of multiple contributing mechanisms (simultaneous or sequential)
- Possibility of different mechanisms for different experimental configurations
- Minimization of free parameters

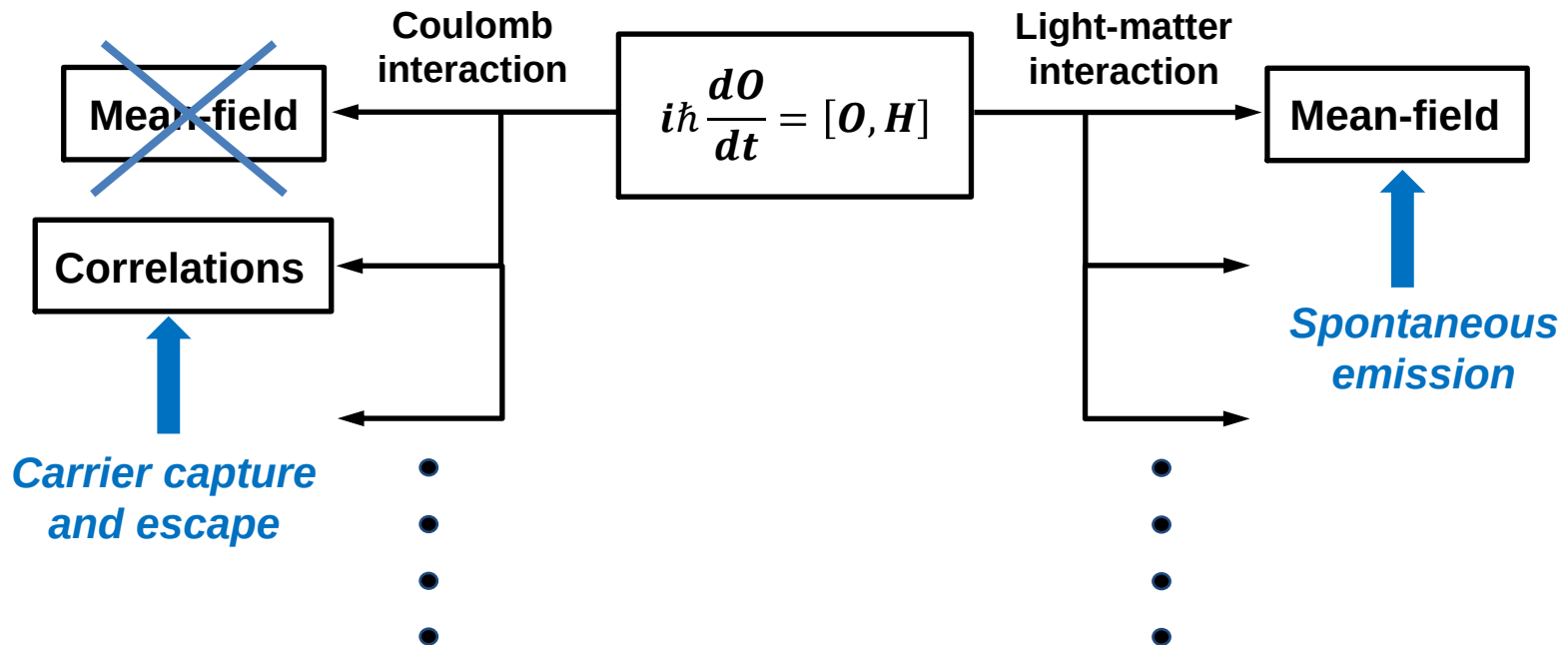
Approach

Hamiltonian

$$H = \underbrace{\sum_i \epsilon_i^e a_i^\dagger a_i + \sum_j \epsilon_j^h b_j^\dagger b_j + \sum_q \hbar \Omega_q c_q^\dagger c_q}_{\text{Single-particle energies}} - \underbrace{\sum_{i,j,q} \wp_{ij} \sqrt{\frac{\hbar \Omega_q}{V \epsilon_b}} (a_i b_j c_q^\dagger + c_q b_j^\dagger a_i^\dagger)}_{\text{Light-matter interaction}}$$

+ Coulomb interaction

Hiesenberg Picture



Model

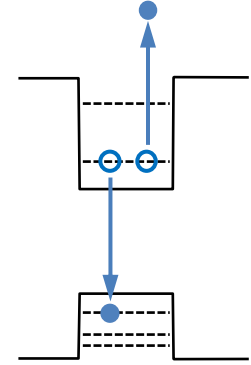
$$\frac{dn_{\sigma,\alpha_{\sigma},k_{\perp}}}{dt} = \overbrace{n_{\sigma,\alpha_{\sigma},k_{\perp}} \sum_{\alpha_{\sigma'}} b_{\alpha_{\sigma},\alpha_{\sigma'},k_{\perp}} n_{\sigma',\alpha_{\sigma'},k_{\perp}}}_{\text{Spontaneous emission (>ns)}} - \overbrace{An_{\sigma,\alpha_{\sigma},k_{\perp}}}_{\text{Defect loss (SRH)}}$$

$$- \gamma_{c-c} [n_{\sigma,\alpha_{\sigma},k_{\perp}} - f(\varepsilon_{\sigma,k_{\perp}}, \mu_{\sigma}, T)]$$

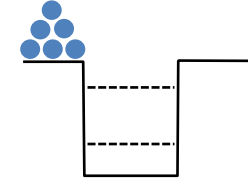
$$- \gamma_{c-p} [n_{\sigma,\alpha_{\sigma},k_{\perp}} - f(\varepsilon_{\sigma,k_{\perp}}, \mu_{\sigma}^L, T_L)]$$

$$- \gamma_{ag} [n_{\sigma,\alpha_{\sigma},k_{\perp}} - f(\varepsilon_{\sigma,k_{\perp}}, \mu_{ag}, T_{ag})]$$

Auger



Carrier injection



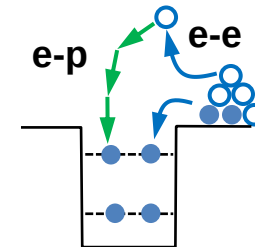
$$\frac{dn_{\sigma,k}^b}{dt} = \overbrace{-b_k n_{e,k}^b n_{h,k}^b}_{\text{Carrier-carrier (100fs)}} + \overbrace{\frac{J}{eN_{\sigma}^p} f(\varepsilon_{\sigma,k}^b, \mu_{\sigma}^p, T_p) (1 - n_{\sigma,k}^b)}_{\text{Carrier injection}} - \overbrace{An_{\sigma,k}^b}_{\text{Defect loss (SRH)}}$$

$$- \gamma_{c-c} [n_{\sigma,k}^b - f(\varepsilon_{\sigma,k}^b, \mu_{\sigma}, T)]$$

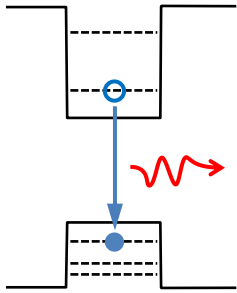
$$- \gamma_{c-p} [n_{\sigma,k}^b - f(\varepsilon_{\sigma,k}^b, \mu_{\sigma}^L, T_L)]$$

$$- \gamma_{ag} [n_{\sigma,k}^b - f(\varepsilon_{\sigma,k}^b, \mu_{ag}, T_{ag})]$$

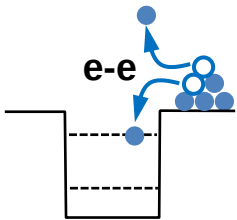
Carrier-phonon (<1ps)



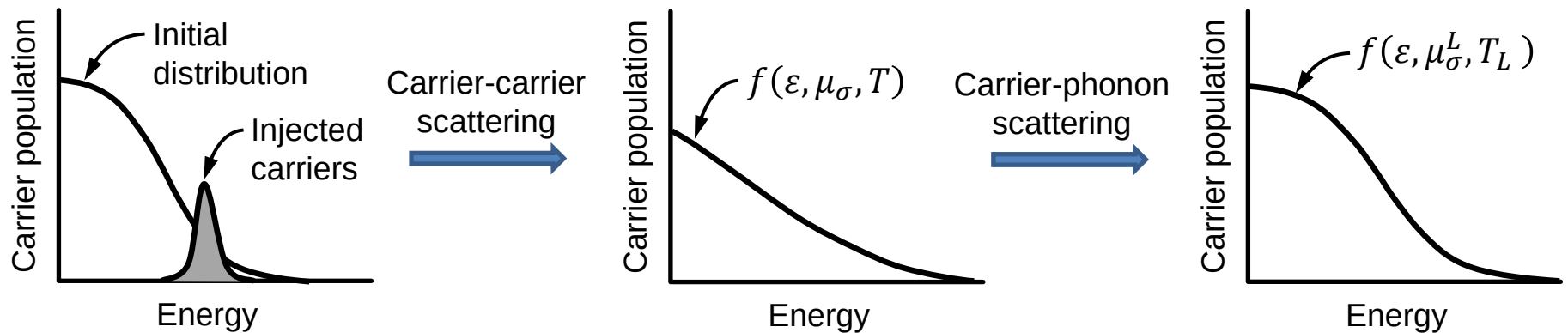
Spontaneous emission (>ns)



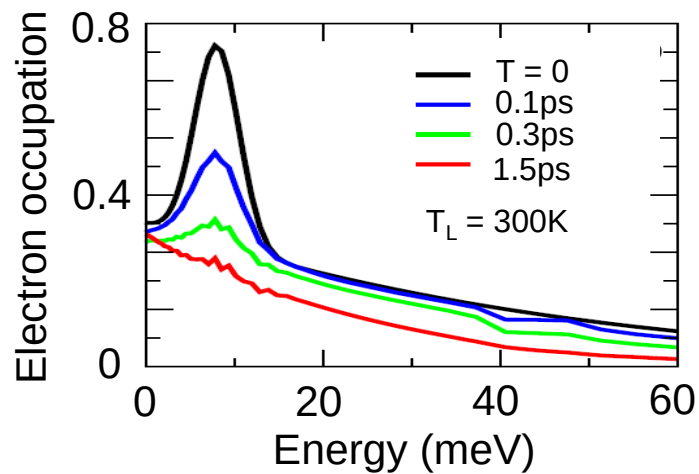
Carrier-carrier (100fs)



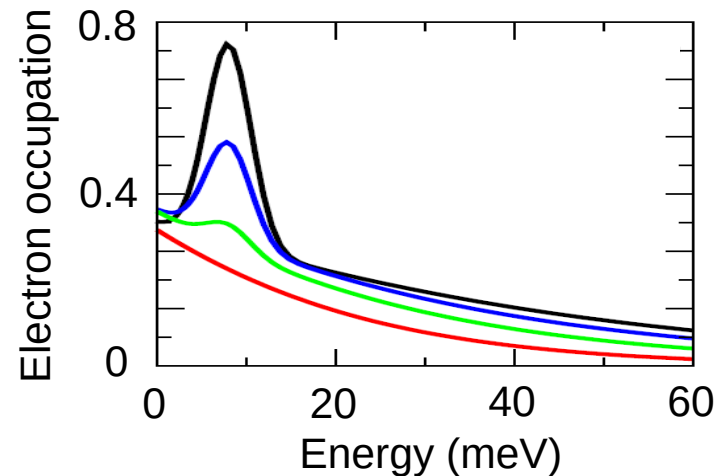
Asymptotic carrier distributions



Quantum kinetic calculation



(Our) rate equation model



Numerical analysis

1

Bandstructure

- a) Solve k·p and Poisson equations for given range of carrier densities
- b) Tabulate energy dispersions and transition matrix elements versus carrier density

2

Solve for carrier population distributions

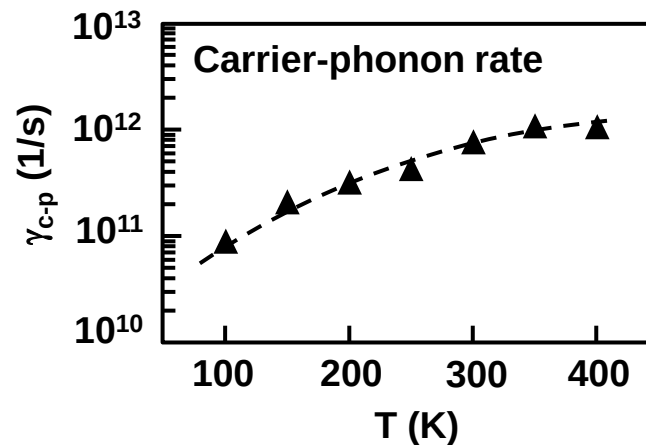
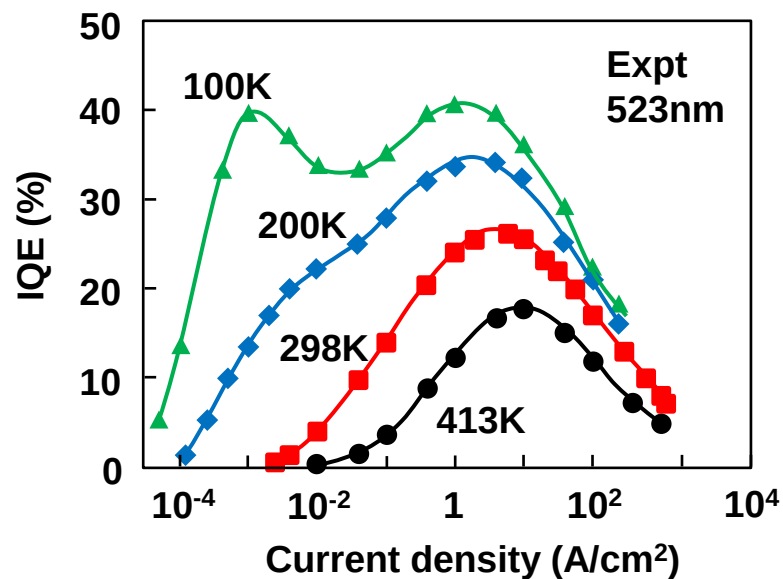
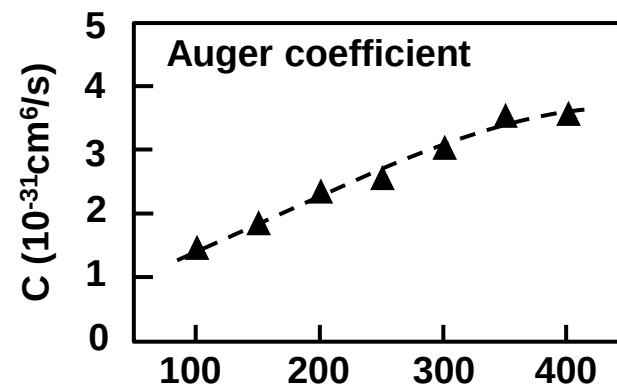
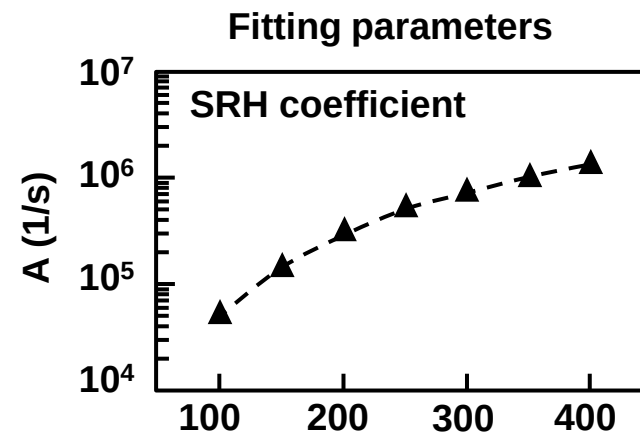
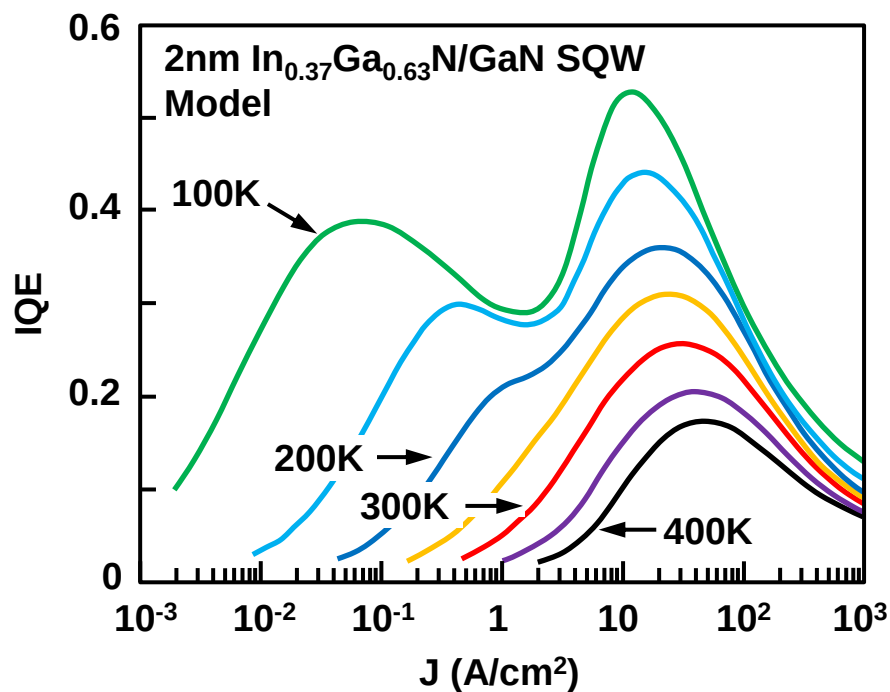
Solve kinetic equations with bandstructure properties and asymptotic Fermi-Dirac distributions updated at each time step

3

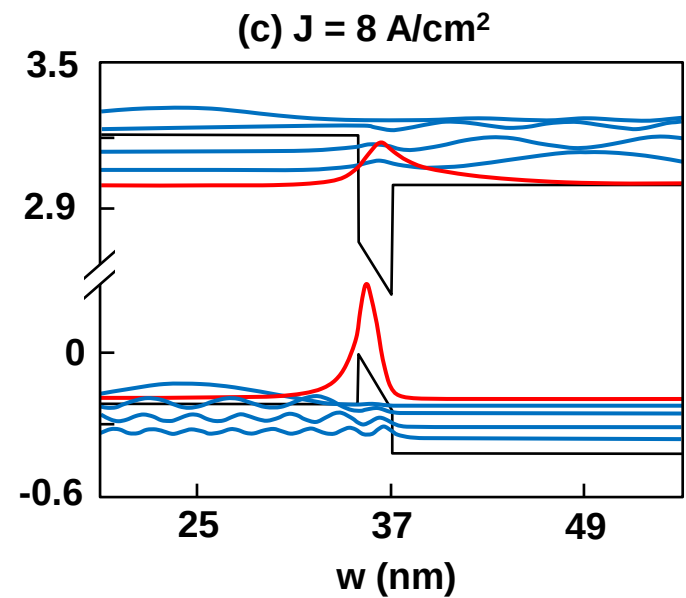
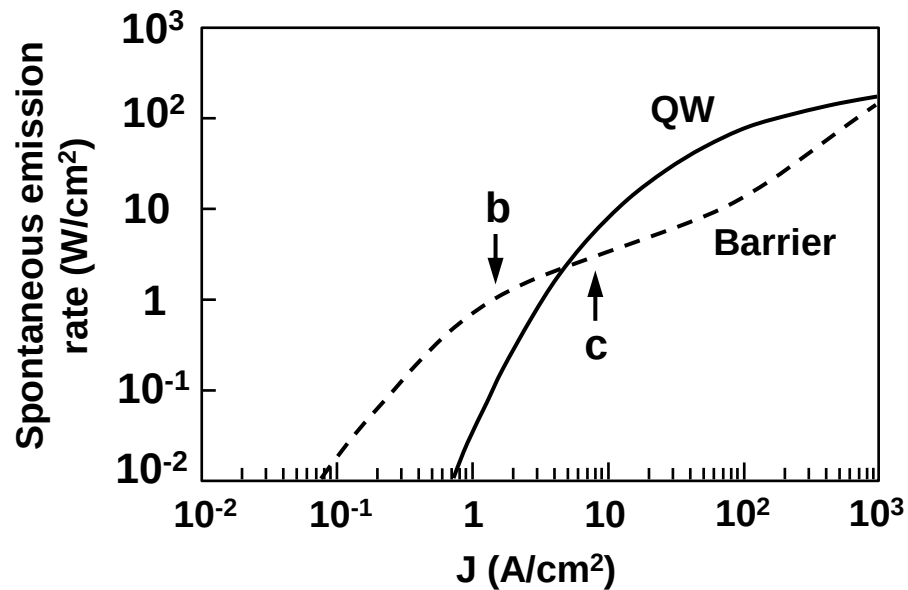
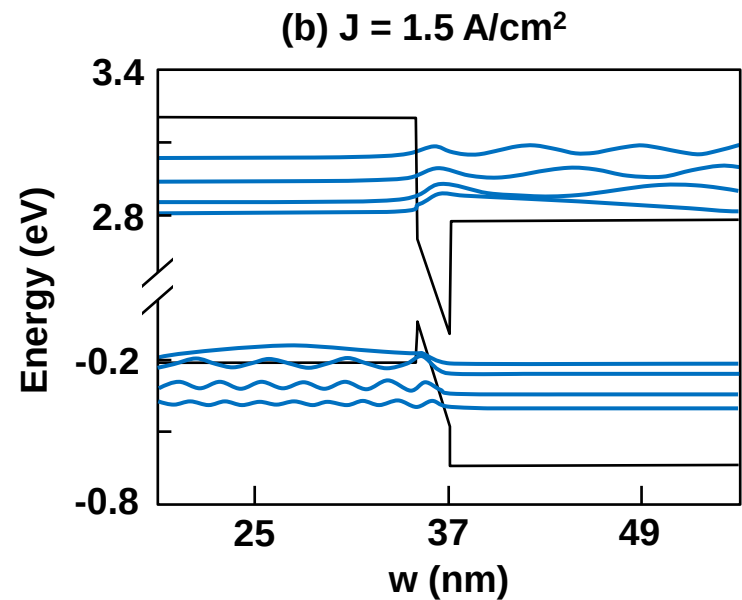
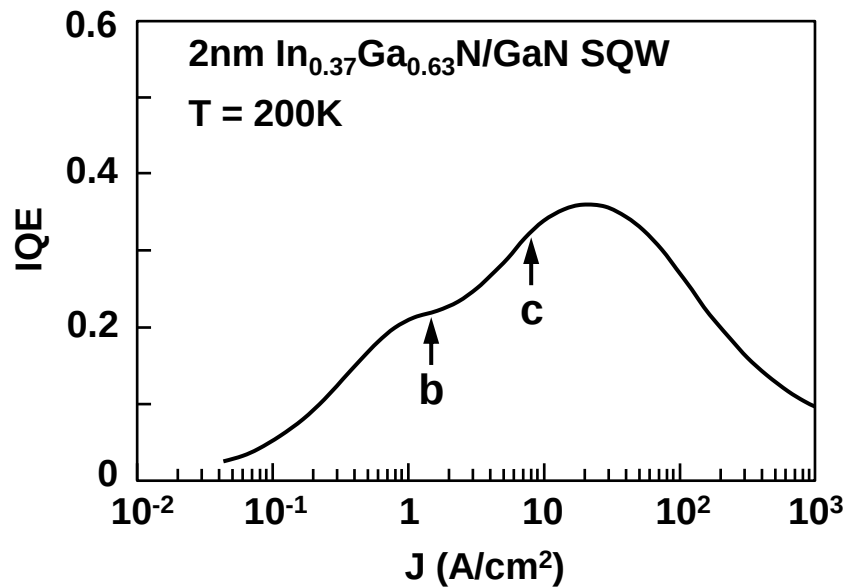
Compute efficiency

$$IQE = \frac{e}{JS} \left(\sum_{\alpha_e, \alpha_h, k_{\perp}} b_{\alpha_e, \alpha_h, k_{\perp}} n_{e, \alpha_e, k_{\perp}} n_{h, \alpha_h, k_{\perp}} + \sum_k b_k n_{e, k}^b n_{h, k}^b \right)$$

IQE versus current density for different lattice temperatures

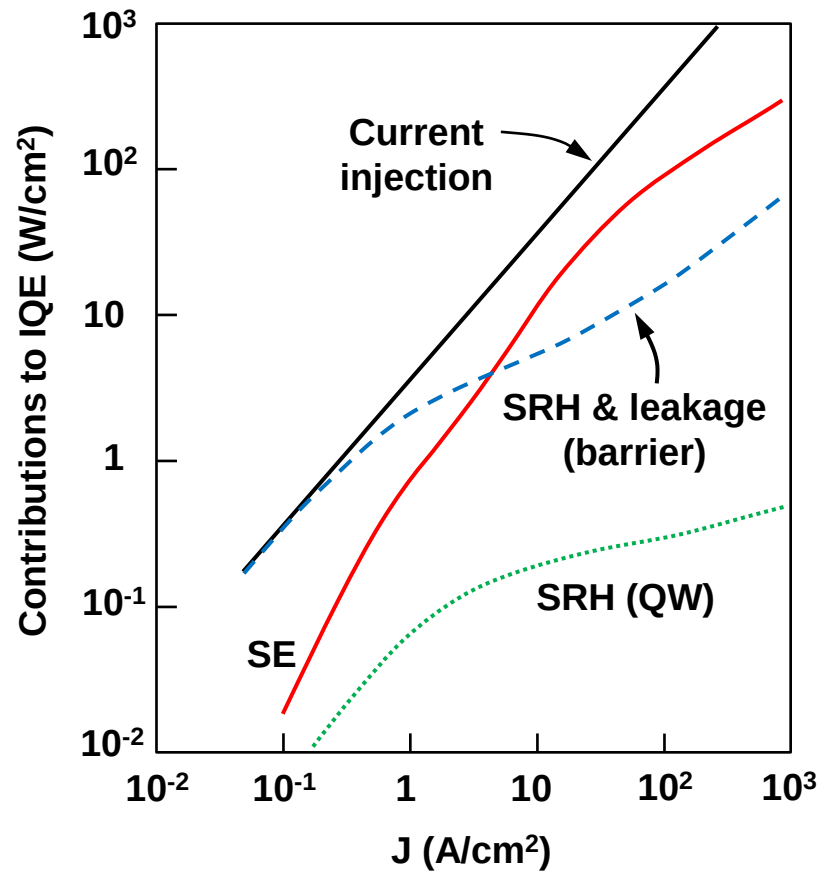


Spontaneous emission from QW and barrier states

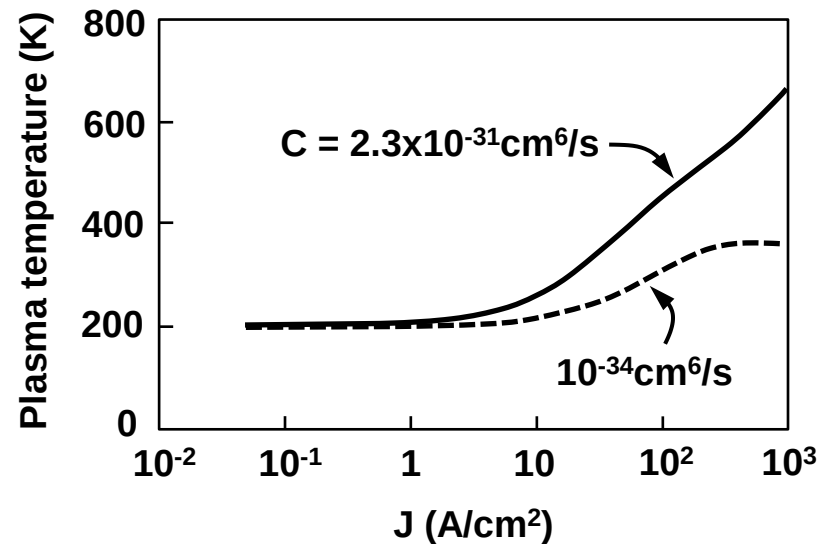
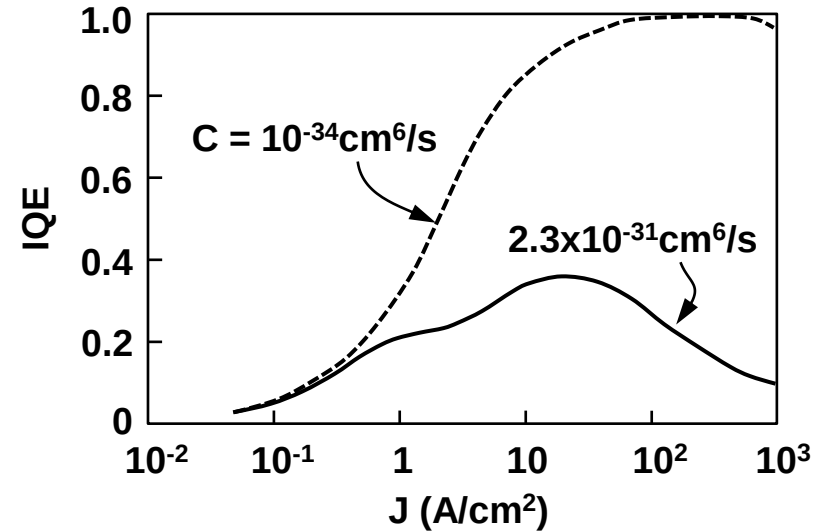


Contributions to IQE

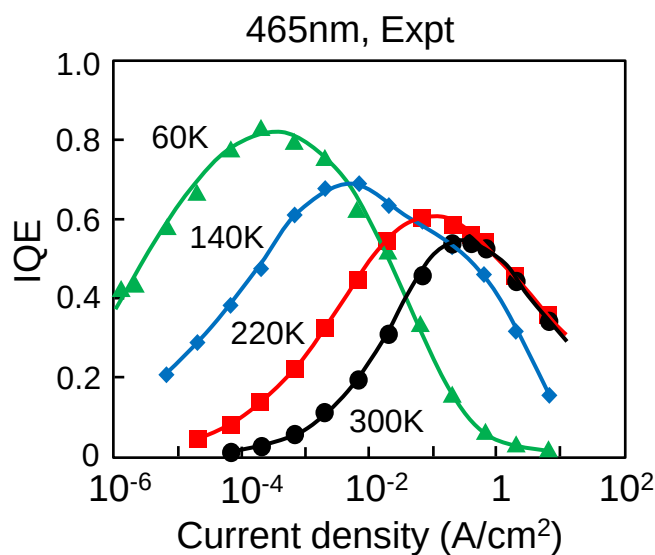
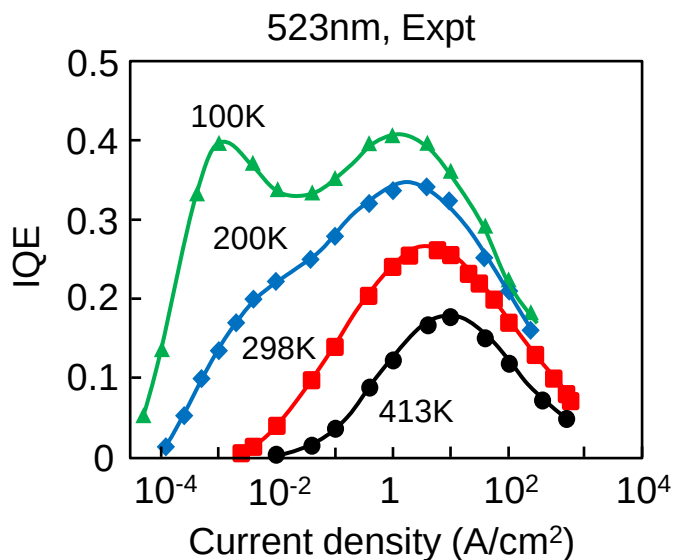
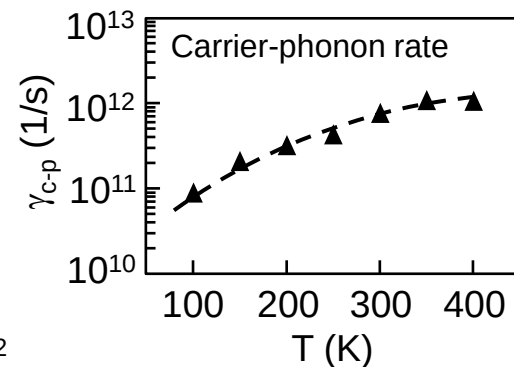
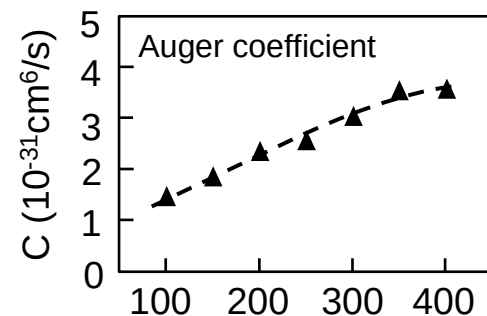
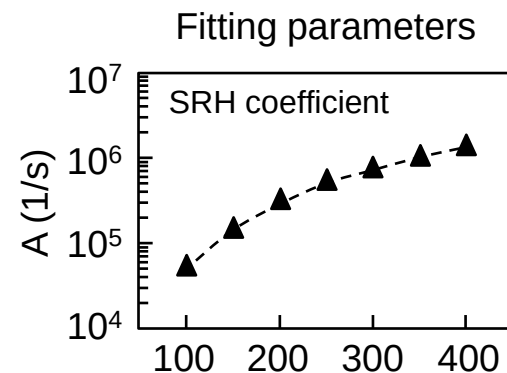
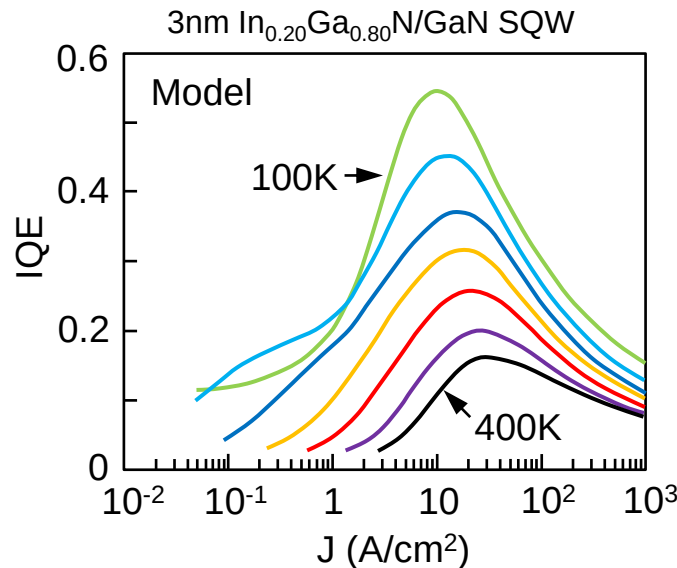
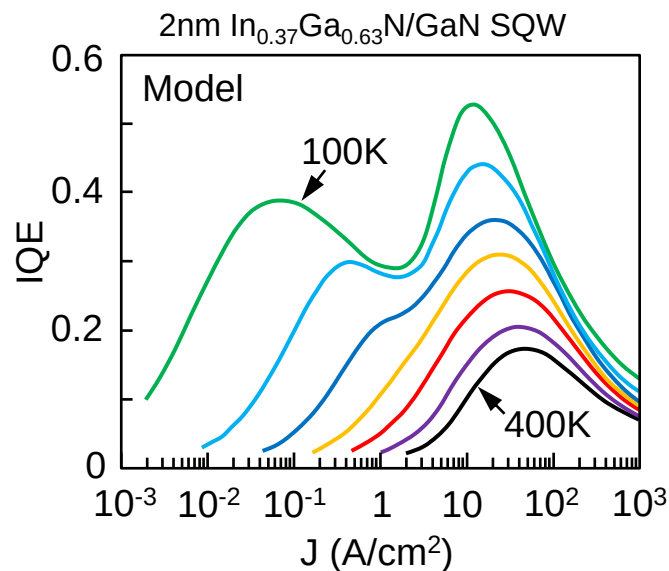
2nm $\text{In}_{0.37}\text{Ga}_{0.63}\text{N}/\text{GaN}$ SQW, $T = 200\text{K}$



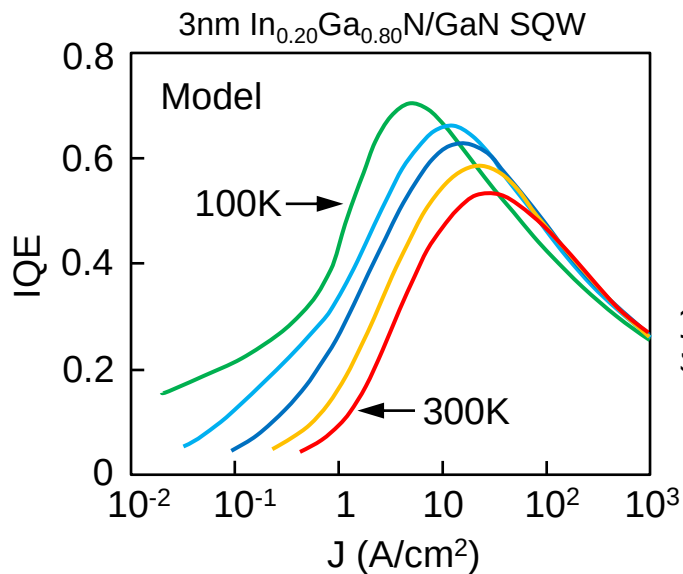
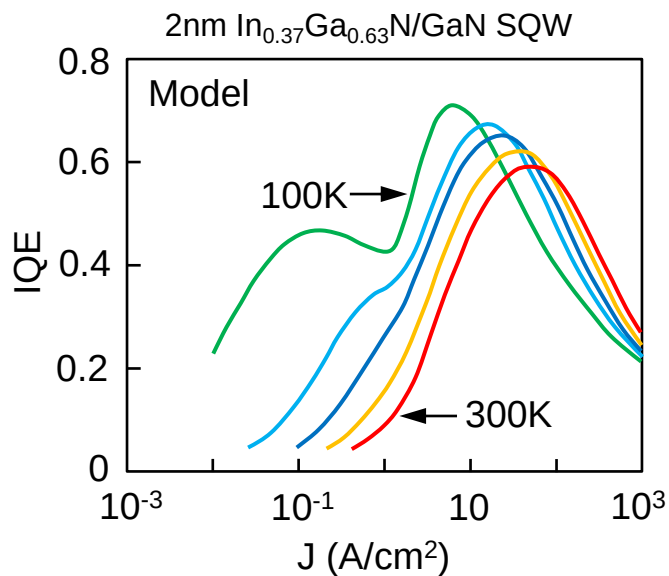
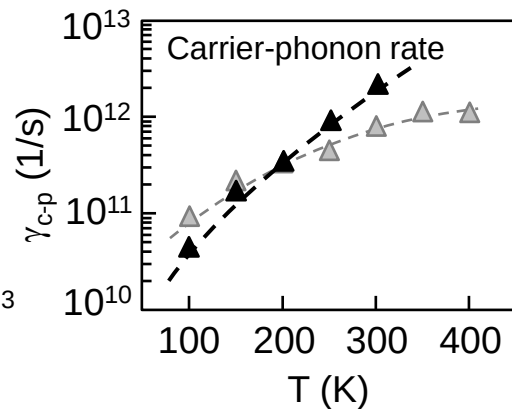
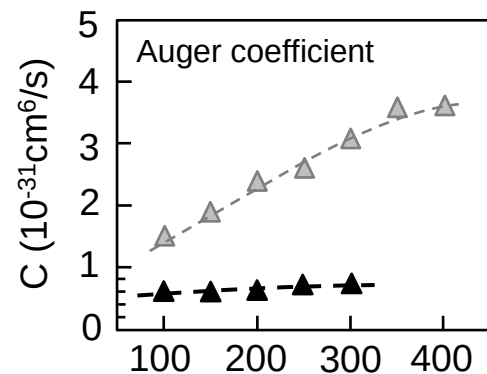
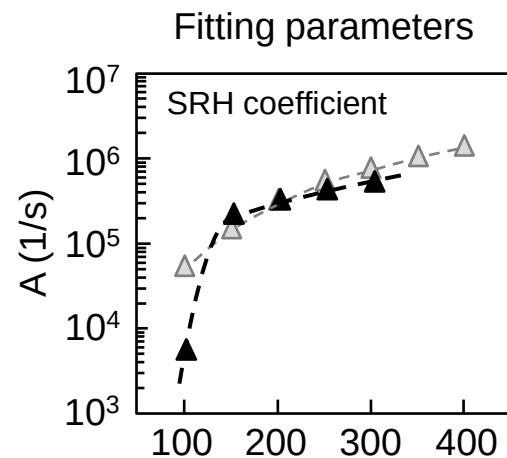
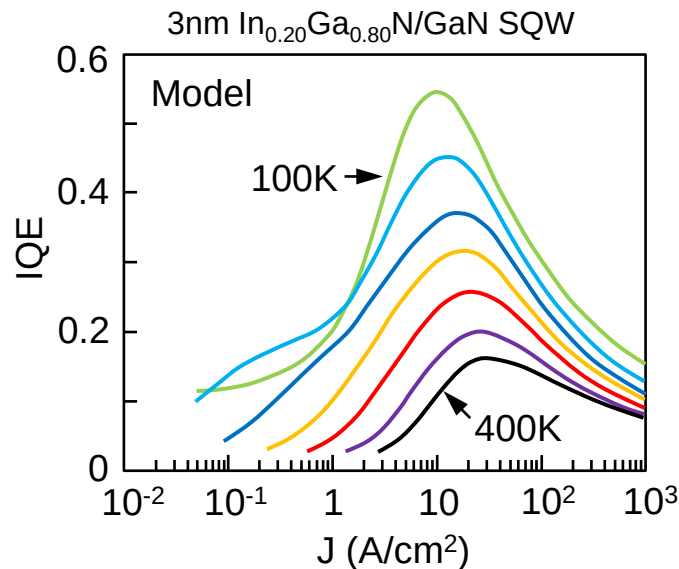
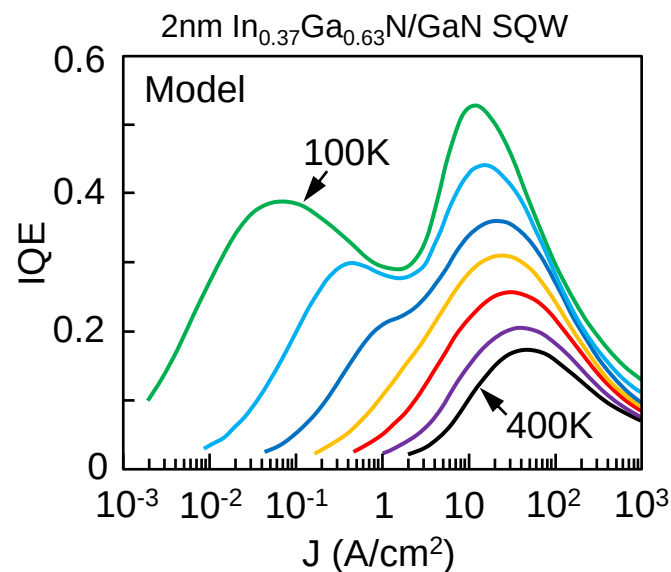
Auger effects



IQE versus current density for different lattice temperatures



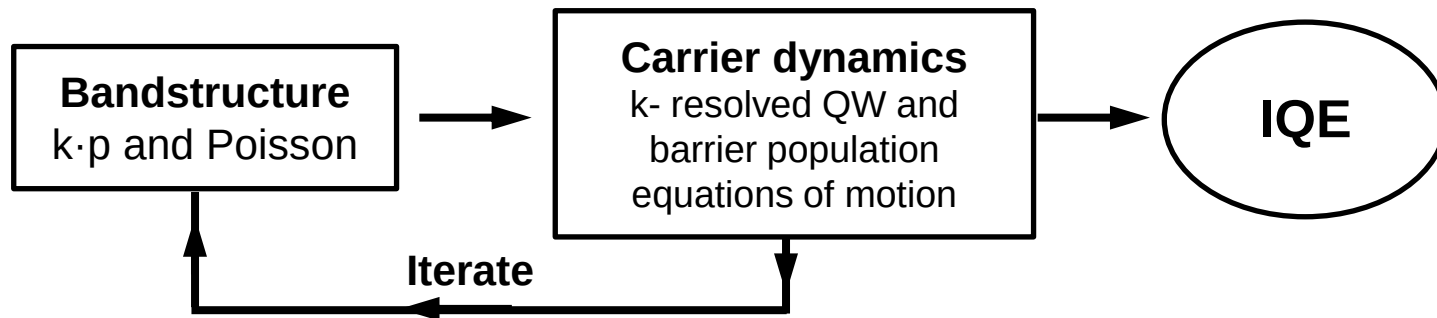
IQE versus current density for different lattice temperatures



Considerations for model

- Systematic, unbiased accounting of physical mechanisms
- Possibility of multiple contributing mechanisms (simultaneous or sequential)
- Possibility of different mechanisms for different experimental configurations
- Minimization of free parameters

Approach (microscopic model)



Possible efficiency droop mechanisms

- Auger losses → C -- carrier-carrier scattering rate
 - Defect → A -- carrier-carrier scattering rate
 - Carrier leakage
 - Non capture
 - Junction heating
- These four mechanisms (Carrier leakage, Non capture, and Junction heating) are grouped by a bracket and point to a common set of parameters: γ_{c-c} -- carrier-carrier scattering rate and γ_{c-p} -- carrier-carrier scattering rate.
- Band structure → k·p and Poisson Eqs → Growth sheet
- Bulk material parameters