

# Multi-Cavity Far Infrared 2D Plasmonic Phenomena with Inhomogeneous Screening

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## Abstract

We have observed coherent interaction of far infrared 2D plasma cavities in a GaAs/AlGaAs HEMT. A generalized transmission line formalism that unifies the screened and unscreened limits into a self-consistent theory describes an evolution of the plasmonic spectrum with increasing electron density modulation from homogeneous to the crystal limit.

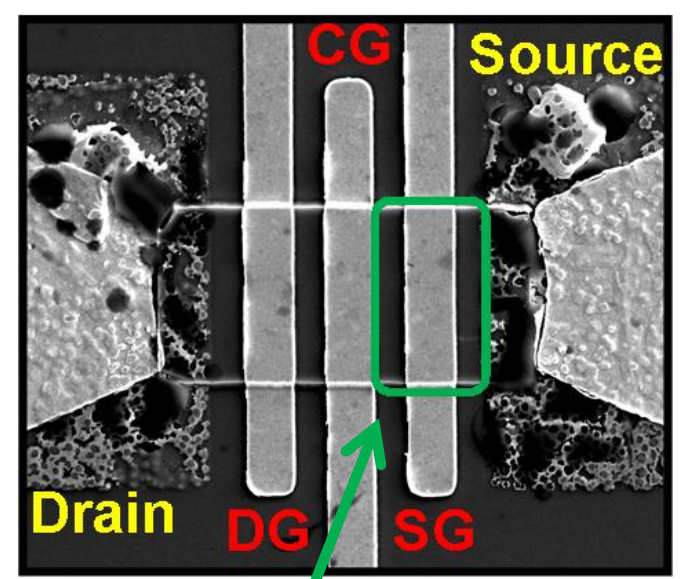
## Antenna Coupled Plasmonic HEMT

A GaAs/AlGaAs high electron mobility transistor (HEMT) is fabricated at the vertex of a broadband log-periodic antenna:

- HEMT channel is 14  $\mu\text{m}$  long by 10  $\mu\text{m}$  wide
- Gates are  $\sim 2 \mu\text{m}$  wide, spaced by  $\sim 2 \mu\text{m}$
- HEMT is reconfigurable 2D plasmonic device consisting of multiple plasmonic cavities**

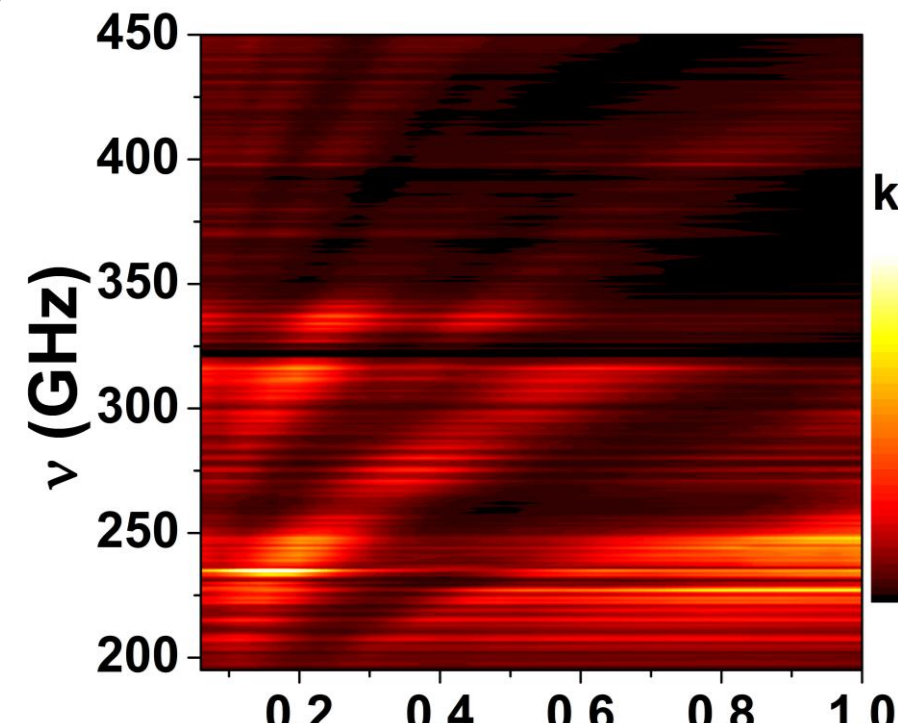


## Frequency Agile THz Detector

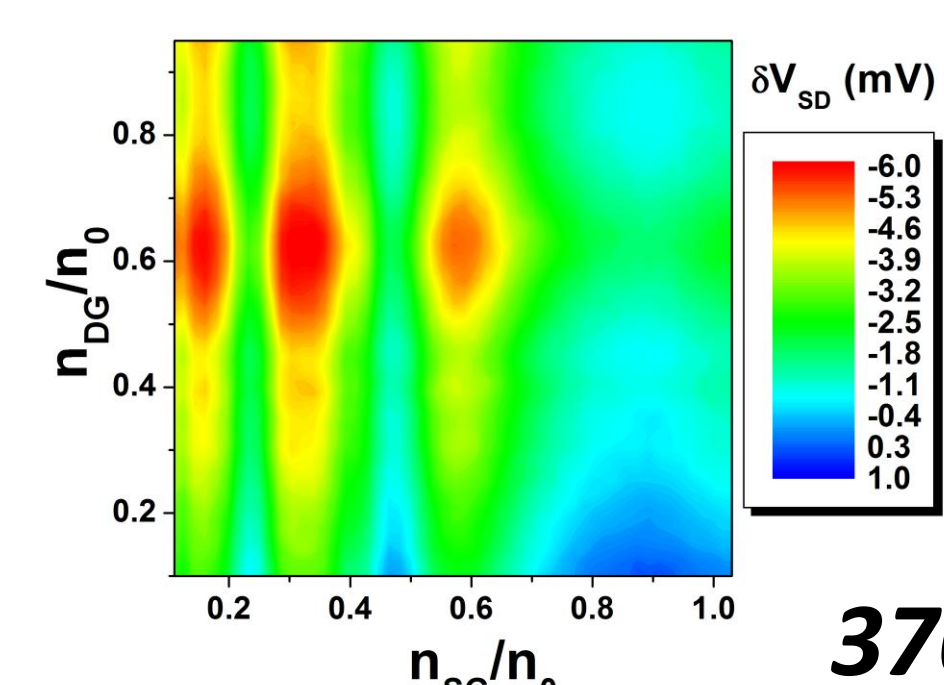


### Plasmonic Cavity

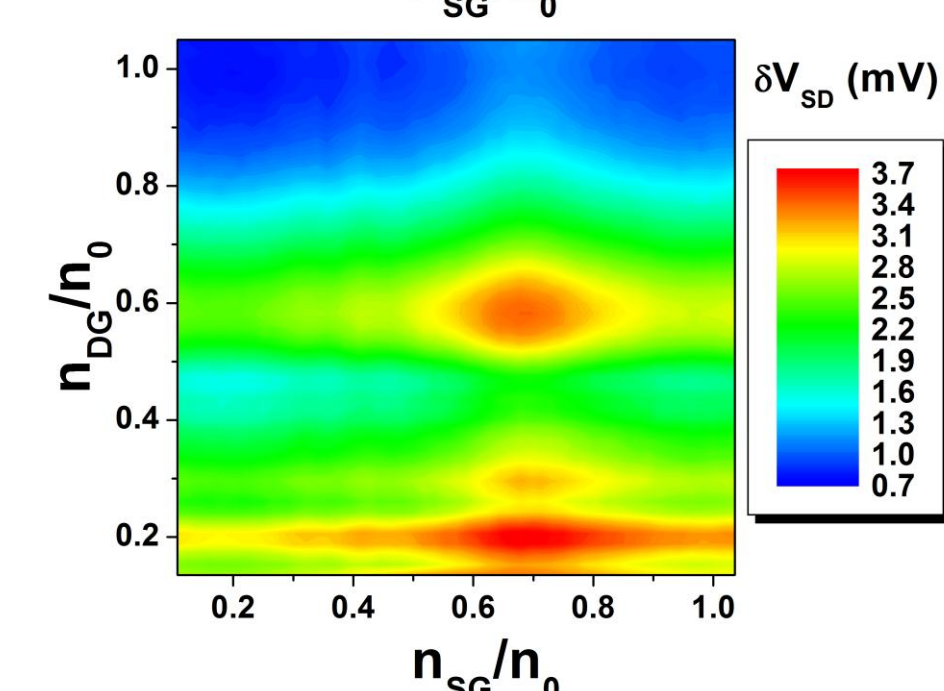
$$n/n_0 = (V_{TH} - V_{SG})/V_{TH} \rightarrow n/n_0$$



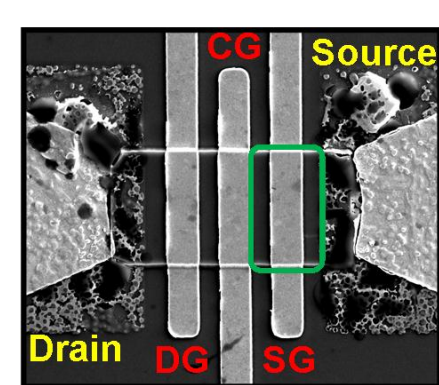
- Center gate (CG) pinched-off to induce bolometric sensor and define plasmonic cavity and +500 nA drain current applied
- Source gate (SG) voltage-tuned & bolometric sensor preferentially detects plasmonic resonances scaling as  $\omega_p \propto \sqrt{n}$  tuned by SG
- R > 100 kV/W & NEP < 50 pW/Hz<sup>1/2</sup> @ T = 11 K**



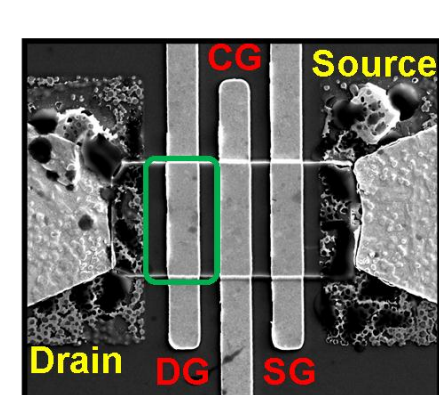
370 GHz



- Reverse of bias polarity changes cavity detected
- Evidence of incoherent inter-cavity coupling



$I = +500 \text{ nA}$



$I = -500 \text{ nA}$

## Plasmonic Transmission Line Model

Plasmons excited in a 2DEG can be treated with a transmission line (TL) model though care must be taken to address the fact that a plasmon is a TM mode:

$$Z_{2DEG} = R_{2DEG} + i\omega L_{2DEG}$$

$$Z_0 = \sqrt{\frac{Z_{2DEG}}{i\omega C(\omega)}}$$

$$iq = \sqrt{i\omega C(\omega)Z_{2DEG}}$$

**from Drude model  $L$  is kinetic inductance**

$$\lim_{qd \rightarrow 0} C(\omega) = \frac{W\epsilon}{d} \quad \lim_{qd \rightarrow \infty} C(\omega) = 2W\epsilon q$$

(fully screened limit) (unscreened limit)

- Gated 2DEG in the screened limit has a gate-channel parallel plate capacitance (Burke *et. al.*, APL (2000))
- Unscreened 2DEG has a circuit capacitance that depends on plasmon wavevector (Rana, IEEE Trans. on Nano. (2008))

## Generalized Plasmonic TL Model

In general the plasmon is screened and does not satisfy the above limits. A self-consistent plasmonic TL model can be found from electromagnetic theory:



$$\Phi(x, z) = [\Phi_+ e^{-iqx} + \Phi_- e^{iqx}] \begin{cases} \sinh[q(d-z)] e^{-qd}, & z \geq 0 \\ \sinh[qd] e^{q(z-d)}, & z < 0 \end{cases}$$

$$\frac{I(x)}{W} = j(x, z) = \frac{1}{Z_0} [\Phi_+ e^{-iqx} - \Phi_- e^{iqx}] \delta(z)$$

$$C(\omega) = \frac{\Phi(x, z=0)}{\rho(x)} = W\epsilon q (1 + \coth[qd])$$

- Voltage and current are superposition of backward and forward propagating waves consistent with TL

$$P(x) = -\frac{W}{2} \iint E_z H_y dy dz = \frac{1}{2} \Phi(x, 0) I^*(x) \xi^*(\omega, d)$$

$$\xi(\omega, d) = 1 - \frac{q(1 - e^{-2q'd} \cos[2q''d])}{2q'(1 - e^{-2q^*d})} + \frac{q e^{-2q'd} \sin[2q''d]}{2q''(1 - e^{-2q^*d})}$$

$$P(x) \rightarrow \begin{cases} \lim_{qd \rightarrow 0} P(x) = \frac{1}{2} \Phi(x, 0) I^*(x) \\ \lim_{\tau, qd \rightarrow \infty} P(x) = \frac{1}{4} \Phi(x, 0) I^*(x) \end{cases}$$

**The 2D plasmon is in general a TM wave:  $P = \frac{1}{2} VI^*$  is correct only for TEM wave in fully screened limit**

$$\frac{1}{2} \tilde{V}(x) \tilde{I}^*(x) = \frac{1}{2} \Phi(x, 0) I^*(x) \xi^*(\omega, d)$$

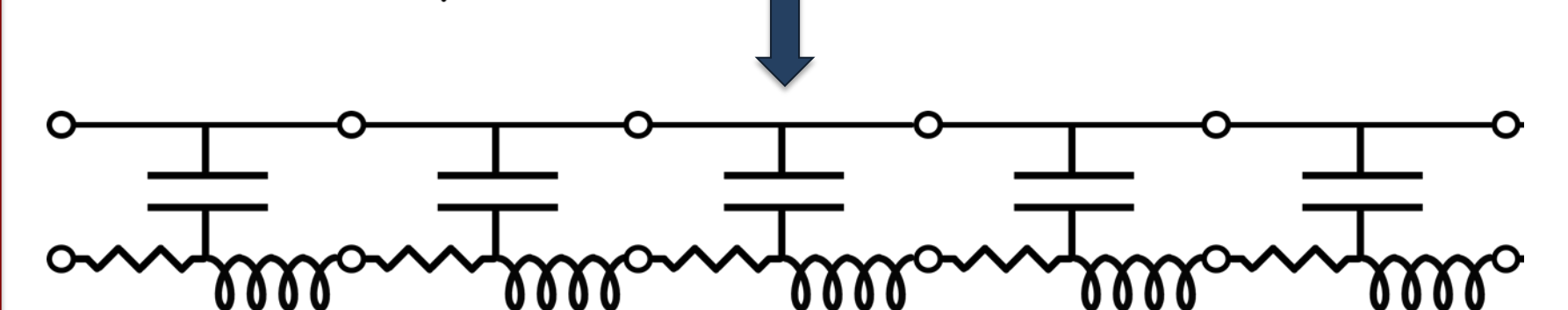
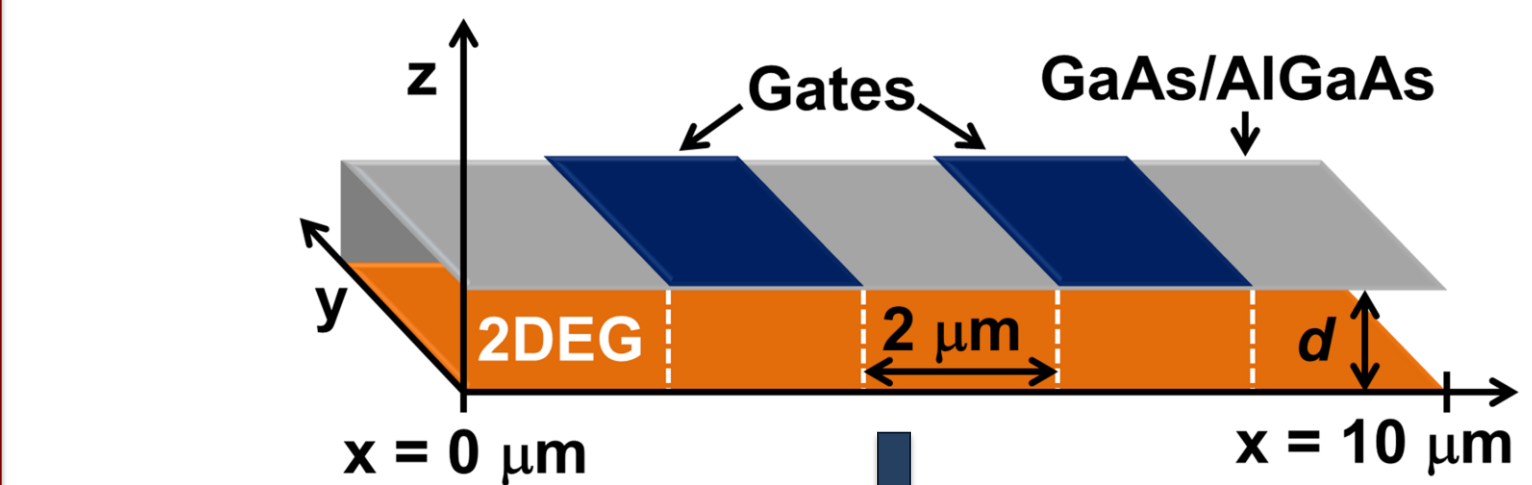
**Defining effective  $V, I$  and  $Z$  for TL maintains continuity of potential and conserves energy.**

$$\tilde{V}(x) \equiv \Phi(x, 0)$$

$$\tilde{I}(x) \equiv I(x) \xi(\omega, d)$$

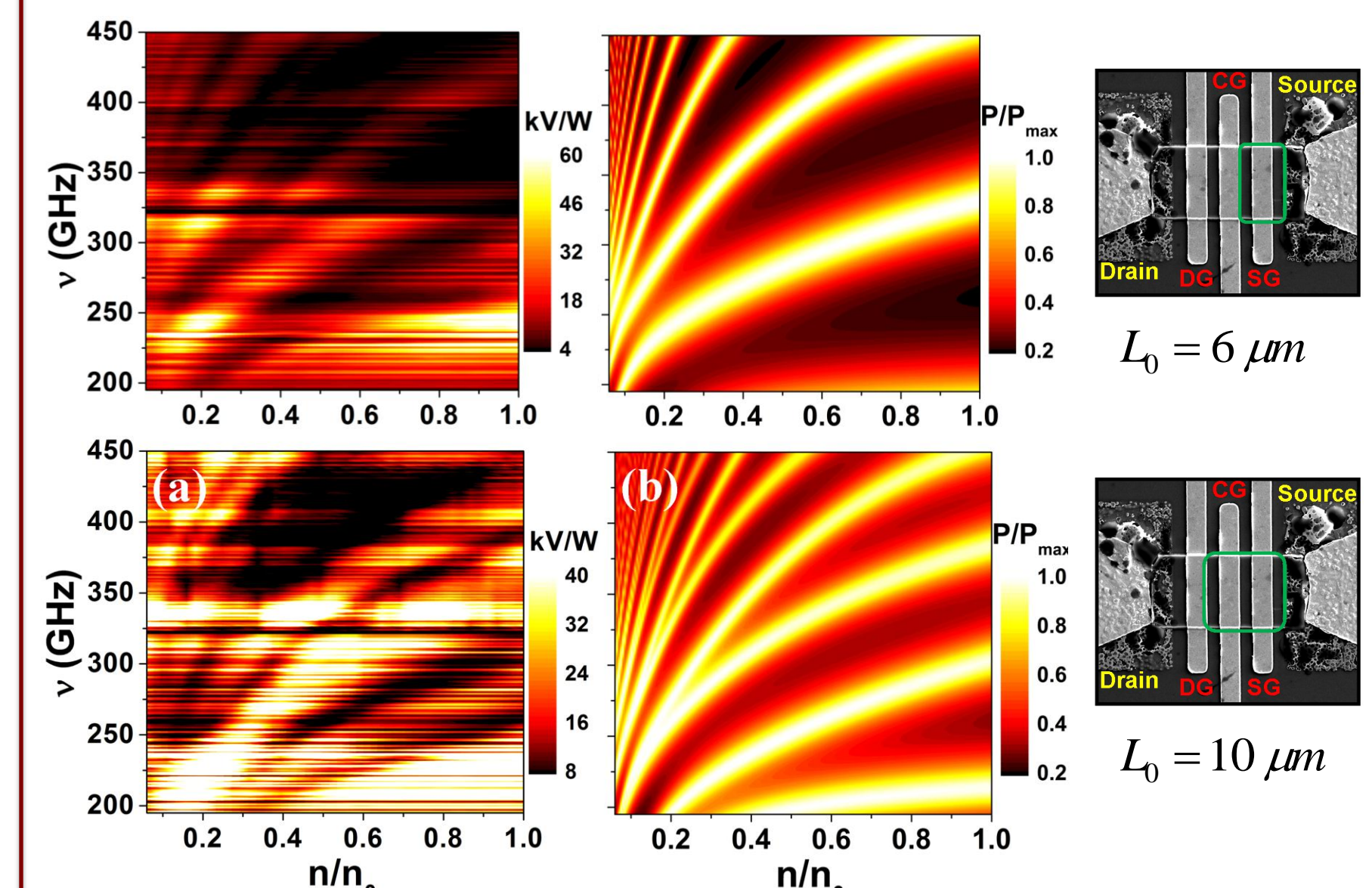
$$\tilde{Z}_0 \equiv \frac{Z_0}{\xi(\omega, d)}$$

## Finite Plasmonic Crystal



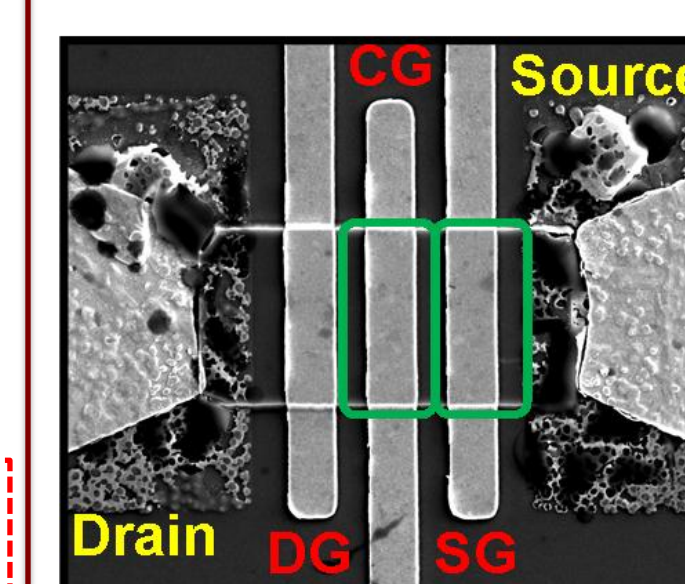
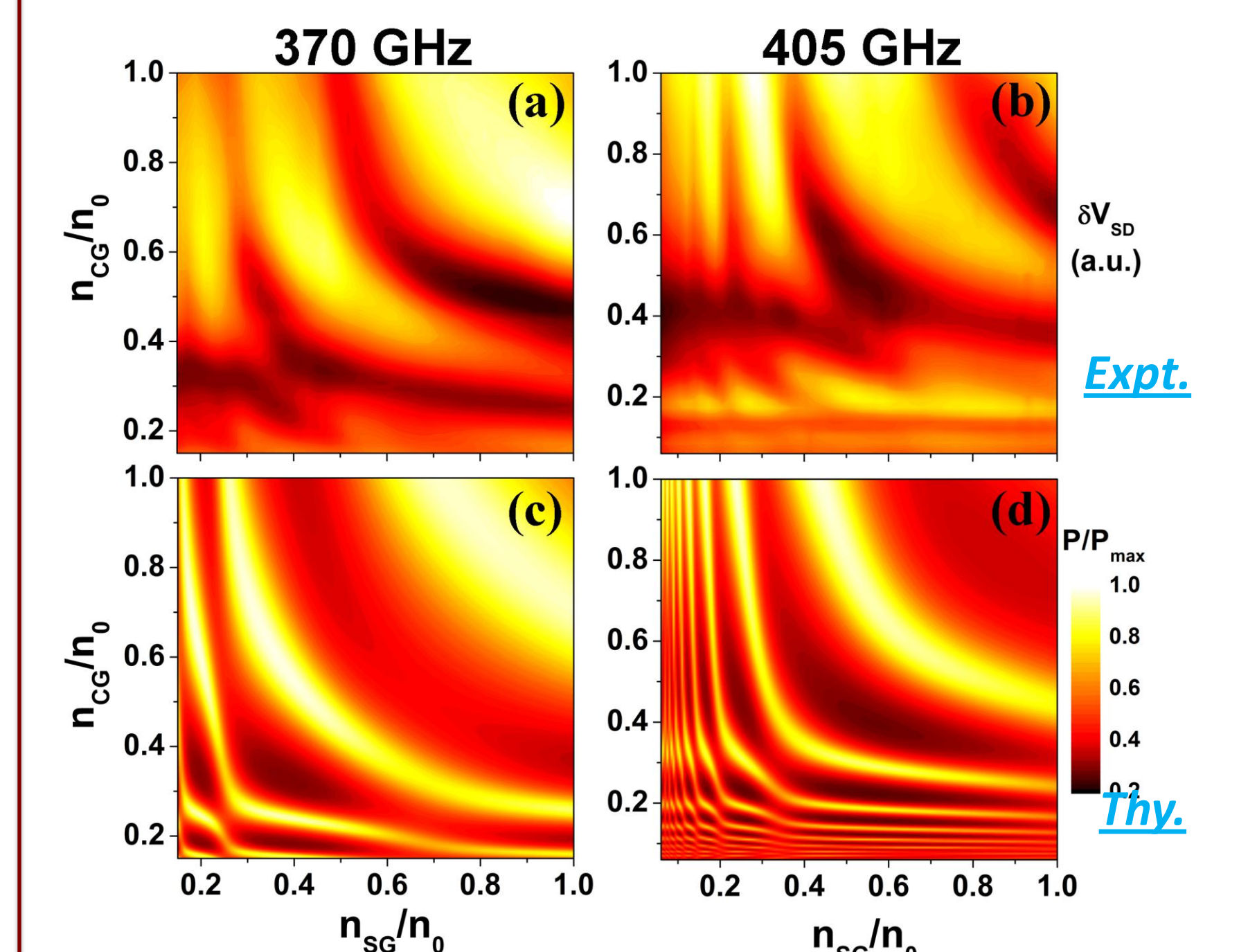
Solution for an inhomogeneous cavity with step-like boundaries between TL elements is reduced to matrix multiplication:

$$\begin{pmatrix} \tilde{V}_m \\ \tilde{I}_m \end{pmatrix} = \left[ \prod_m^n \begin{pmatrix} \cos[q_m a_m] & i\tilde{Z}_m \sin[q_m a_m] \\ i\sin[q_m a_m]/\tilde{Z}_m & \cos[q_m a_m] \end{pmatrix} \right] \begin{pmatrix} \tilde{V}_{n+1} \\ \tilde{I}_{n+1} \end{pmatrix}$$



- Position of gate-induced bolometric sensor (CG vs. DG) determines plasmonic cavity size  $L_0$
- SG and CG tuned identically: plasmonic band structure when 2DEG density modulation is strong

## Coherently Coupled Plasmonic Cavities



Experiment and model show transition from plasmonic spectrum of a homogeneous cavity to coherent interaction of independently tuned sub-cavities below SG & CG

- 2D plasmonic analogue of coupled quantum wells
- Repelled crossings of high order plasmonic eigenmodes in lower left quadrant