



# **Peridigm: A New Paradigm in Computational Peridynamics**

**Workshop on Nonlocal Damage and Failure  
Peridynamics and Other Nonlocal Models**

**March 11, 2013**

**Michael Parks, Dave Littlewood, John Mitchell, Stewart Silling**

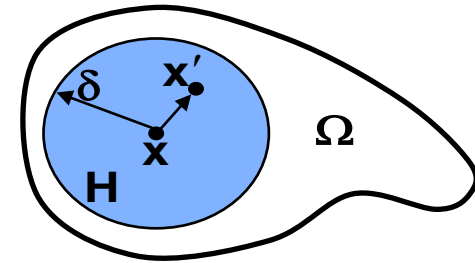
Computing Research Center  
Sandia National Laboratories  
Albuquerque, New Mexico

# What is Peridynamics?

- ❑ Peridynamics is a nonlocal extension of classical solid mechanics that permits discontinuous solutions
- ❑ Peridynamic equation of motion (**integral, nonlocal**)

$$\rho \ddot{u}(\mathbf{x}, t) = \int_H \left( \mathbf{T}[\mathbf{x}, t] \langle \mathbf{x}' - \mathbf{x} \rangle - \mathbf{T}[\mathbf{x}', t] \langle \mathbf{x} - \mathbf{x}' \rangle \right) dV_{\mathbf{x}'} + \mathbf{b}(\mathbf{x}, t)$$

- ❑ Replace PDEs with integral equations
  - ❑ Utilize same equation everywhere; nothing “special” about cracks
  - ❑ No assumption of differentiable fields (admits fracture)
  - ❑ Damage incurred when deformation criteria satisfied (critical stretch, etc.)
  - ❑ No obstacle to integrating nonsmooth functions
  - ❑ Integrand is “force” function; contains constitutive model
  - ❑ Integrand = 0 for points  $\mathbf{x}, \mathbf{x}'$  more than  $\delta$  apart (like cutoff radius in MD!)
  - ❑ PD is “continuum form of molecular dynamics”
- ❑ Impact
    - ❑ Nonlocality
    - ❑ Larger solution space than corresponding classical PDE-based models (fracture)
    - ❑ Account for material behavior at small & large length scales (**multiscale material model**)



Point  $\mathbf{x}$  interacts directly with all points  $\mathbf{x}'$  within  $H$

“It can be said that all physical phenomena are nonlocal. Locality is a fiction invented by idealists.”



A. Cemal Eringen



## Part I

Brief Overview of Peridynamics

## Part II

Demonstration Computations

## Part III

Peridigm: A Computational Peridynamics Code

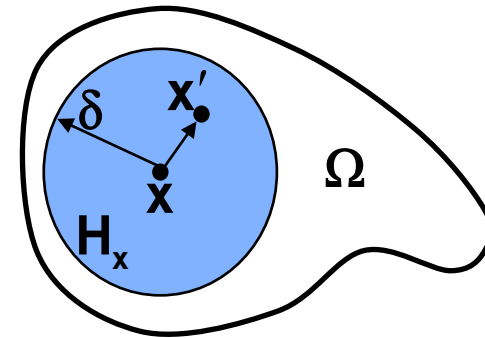
## Part IV

Peridigm: Tutorial and Example

# Peridynamics: The Basics

## □ Horizon and family

- Point  $\mathbf{x}$  interacts directly with all points with distance  $\delta$  (*horizon*)
- Material within distance  $\delta$  of  $\mathbf{x}$  is denoted  $H_x$  (*family of  $\mathbf{x}$* )



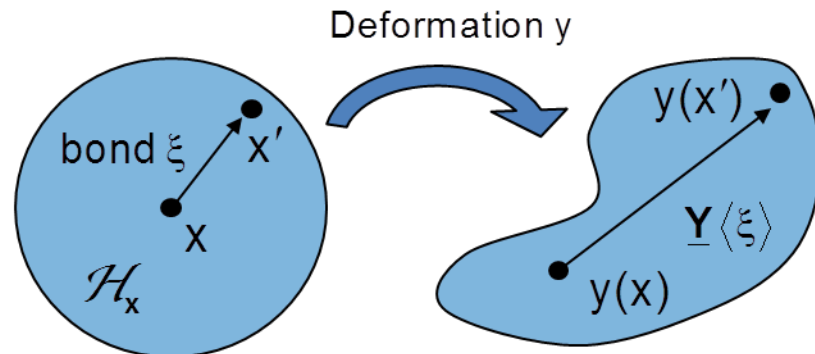
## □ Bonds and bond forces

- Vector between  $\mathbf{x}$  and any point in its family is called a *bond*:  $\xi = \mathbf{x}' - \mathbf{x}$
- Each bond has *pairwise force density vector* applied at both points:  $\mathbf{f}(\mathbf{x}', \mathbf{x}, \mathbf{t})$
- This vector is determined jointly by collective deformation of  $H_x$  and collective deformation of  $H_{x'}$
- Bond forces are antisymmetric:  $\mathbf{f}(\mathbf{x}', \mathbf{x}, \mathbf{t}) = -\mathbf{f}(\mathbf{x}, \mathbf{x}', \mathbf{t})$

## □ Deformation state

- Deformation state operator  $\underline{\mathbf{Y}}$  maps each bond  $\xi$  into its deformed image

$$\underline{\mathbf{Y}}\langle \xi \rangle = \mathbf{y}(\mathbf{x}') - \mathbf{y}(\mathbf{x})$$



Undeformed family of  $x$

Deformed family of  $x$

# Peridynamics: The Basics

## □ Bonds and states

- $\mathbf{f}(\mathbf{x}', \mathbf{x})$  has contributions from material models at both  $\mathbf{x}$  and  $\mathbf{x}'$

$$\mathbf{f}(\mathbf{x}', \mathbf{x}) = \mathbf{T}[\mathbf{x}, \mathbf{t}] \langle \mathbf{x}' - \mathbf{x} \rangle - \mathbf{T}[\mathbf{x}', \mathbf{t}] \langle \mathbf{x} - \mathbf{x}' \rangle$$

- $\underline{\mathbf{I}}[\mathbf{x}]$  is the **force state** – it maps bonds onto bond force densities
- $\underline{\mathbf{I}}[\mathbf{x}]$  is determined by the constitutive model  $\underline{\mathbf{T}} = \hat{\mathbf{T}}(\underline{\mathbf{Y}})$ , where  $\hat{\mathbf{T}}$  maps deformation state to force state
- For elastic materials,  $\underline{\mathbf{I}}[\mathbf{x}] = \mathbf{W}_{\underline{\mathbf{Y}}}$  (Fréchet derivative)

## □ Peridynamics vs. standard equations

- Peridynamic operators and relationships between them are nonlocal analogues of standard theory

Relation	Peridynamic Theory	Standard Theory
Kinematics	$\underline{\mathbf{Y}} \langle \mathbf{x}' - \mathbf{x} \rangle = \mathbf{y}(\mathbf{x}') - \mathbf{y}(\mathbf{x})$	$\mathbf{F} = \frac{\partial \mathbf{y}}{\partial \mathbf{x}}(\mathbf{x})$
Linear Momentum Balance	$\rho \ddot{\mathbf{u}}(\mathbf{x}) = \int_{\mathcal{H}_{\mathbf{x}}} \{ \underline{\mathbf{T}}[\mathbf{x}, \mathbf{t}] \langle \mathbf{x}' - \mathbf{x} \rangle - \underline{\mathbf{T}}[\mathbf{x}', \mathbf{t}] \langle \mathbf{x} - \mathbf{x}' \rangle \} dV_{\mathbf{x}'} + \mathbf{b}(\mathbf{x})$	$\rho \ddot{\mathbf{u}}(\mathbf{x}) = \nabla \cdot \boldsymbol{\sigma}(\mathbf{x}) + \mathbf{b}(\mathbf{x})$
Constitutive Model	$\underline{\mathbf{T}} = \hat{\mathbf{T}}(\underline{\mathbf{Y}})$	$\boldsymbol{\sigma} = \hat{\boldsymbol{\sigma}}(\mathbf{F})$
Angular Momentum Balance	$\int_{\mathcal{H}_{\mathbf{x}}} \{ \underline{\mathbf{Y}} \langle \mathbf{x}' - \mathbf{x} \rangle \times \underline{\mathbf{T}} \langle \mathbf{x}' - \mathbf{x} \rangle \} dV_{\mathbf{x}'} = 0$	$\boldsymbol{\sigma} = \boldsymbol{\sigma}^T$



# Peridynamic Material Modeling

- **Linear Peridynamic Solid (LPS)\***
- Nonlocal analog to linear isotropic elastic solid
- $k$  is bulk modulus,  $\mu$  is shear modulus

$$\rho \ddot{\mathbf{u}}(\mathbf{x}, \mathbf{t}) = \int_{\mathbf{H}} \left( \mathbf{T}[\mathbf{x}, \mathbf{t}] \langle \mathbf{x}' - \mathbf{x} \rangle - \mathbf{T}[\mathbf{x}', \mathbf{t}] \langle \mathbf{x} - \mathbf{x}' \rangle \right) dV_{\mathbf{x}'} + \mathbf{b}(\mathbf{x}, \mathbf{t})$$

$$\mathbf{T}[\mathbf{x}, \mathbf{t}] \langle \mathbf{x}' - \mathbf{x} \rangle = \left( \frac{3k\theta}{m} \underline{\underline{\omega}} \mathbf{x} + \frac{15\mu}{m} \underline{\underline{\omega}} \mathbf{e}^d \right) \frac{\mathbf{x}' - \mathbf{x}}{\|\mathbf{x}' - \mathbf{x}\|}$$

- Many other peridynamic material models available: elastic-plastic, viscoelastic, etc.
- Can wrap classical material models (existing material libraries) in peridynamic “skin”

\*S.A. Silling, M. Epton, O. Weckner, J. Xu, & E. Askari, Peridynamic States and Constitutive Modeling, J. Elasticity, 88, pp. 151-184, 2007.

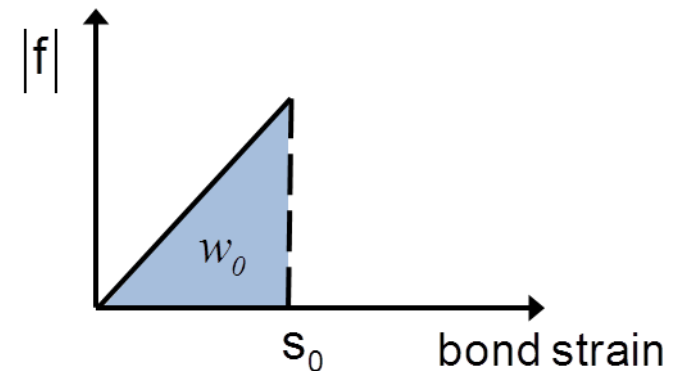
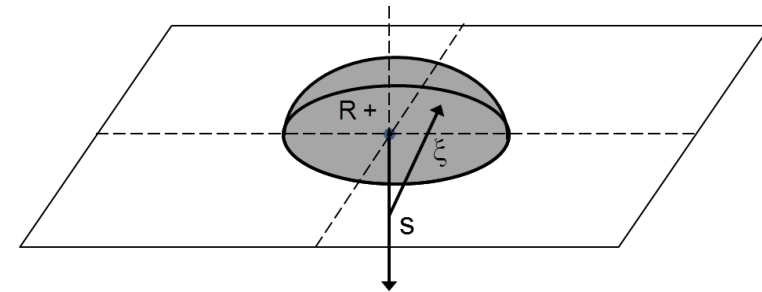
# Peridynamic Fracture Modeling

## □ Fracture (“Critical Stretch”)

- Break bond if bond stretch  $s$  exceeds critical stretch  $s_0$
- If work to break bond  $\xi$  is  $w_0(\xi)$ , then energy release rate found by summing this work per unit crack area

$$\mathbf{G} = \int_0^\delta \int_{R_+} w_0(\xi) dV_\xi ds$$

- Can then get the critical strain  $s_0$  for bond breakage in terms of  $\mathbf{G}$  (strain energy release rate), an experimentally measurable quantity



## □ Fracture (“Critical Energy”)\*

- Break bond if work done on bond exceeds critical value\*



Part I

Brief Overview of Peridynamics

Part II

Demonstration Computations

Part III

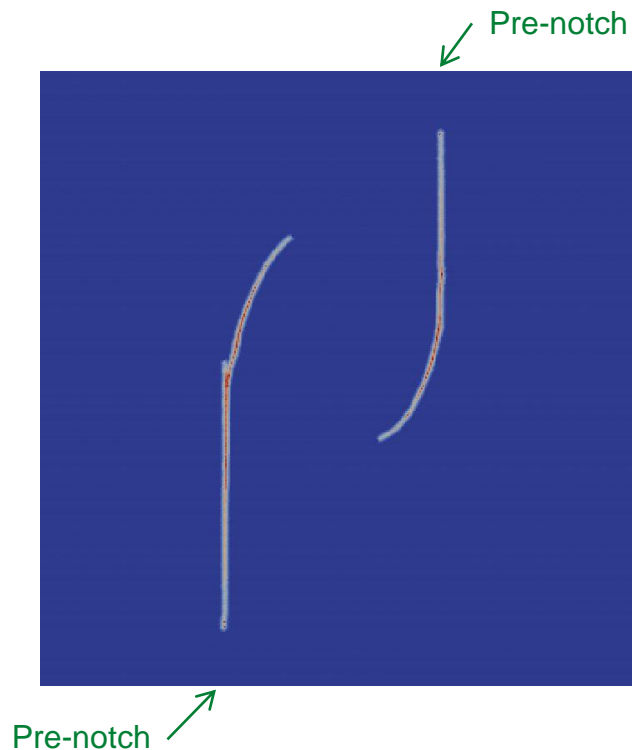
Peridigm: A Computational Peridynamics Code

Part IV

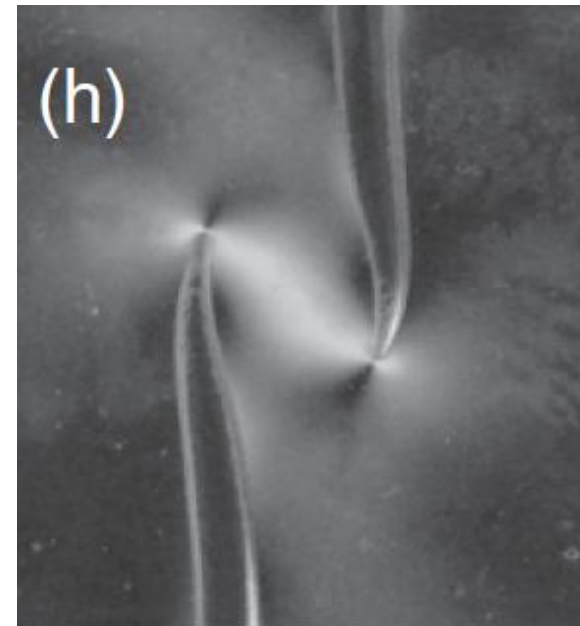
Peridigm: Tutorial and Example

## Two Interacting Cracks

- ❑ Offset notches thin rectangular elastic plate
- ❑ Uniaxial strain applied from sides
- ❑ Approaching cracks produce “en passant” crack pattern



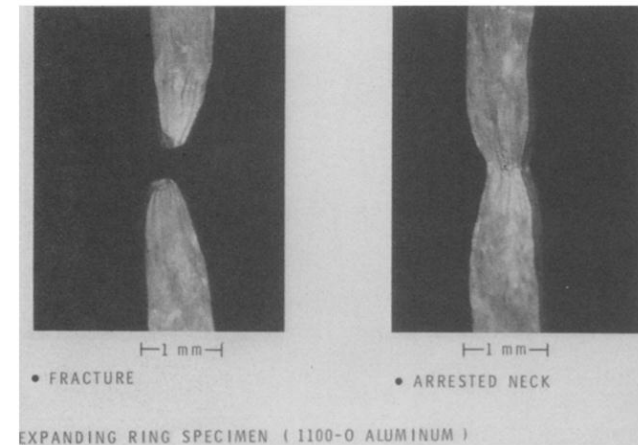
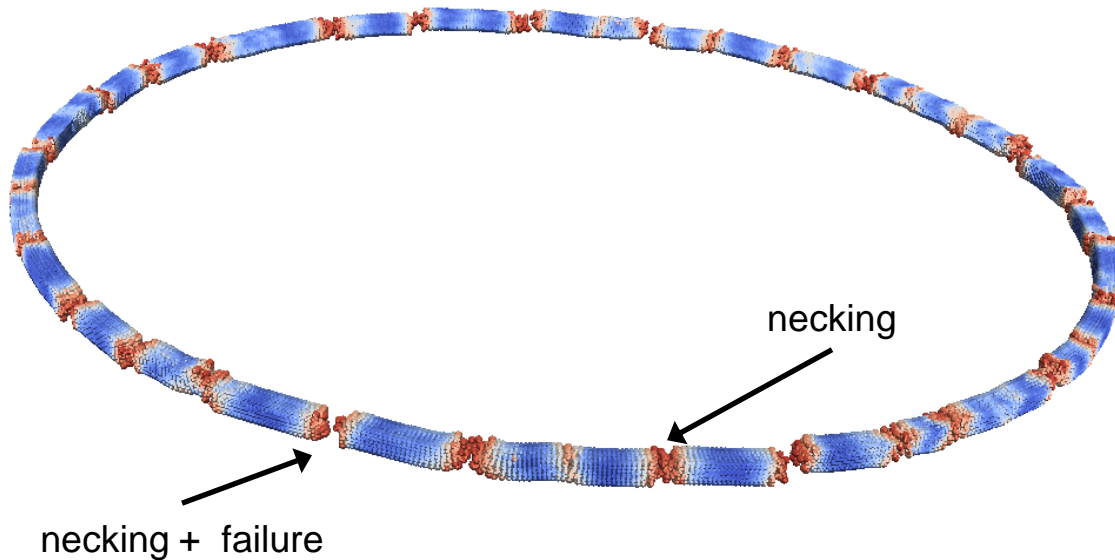
Peridynamics



Physical Experiment\*

# Electromagnetically loaded ring

- ❑ 1100-0 aluminum ring (ductile)
- ❑ Motivated by ring fragmentation experiments of Grady & Benson\*
- ❑ Used peridynamic elastic/plastic model\*\*



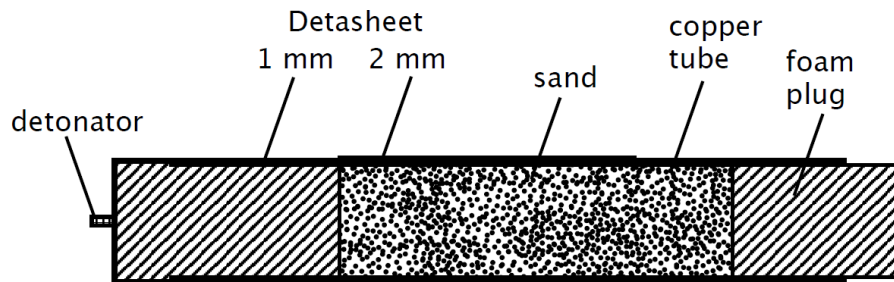
Fracture and arrested neck region  
from dynamic expansion of ring\*

\* D. Grady, D. Benson, Fragmentation of metal rings by electromagnetic loading, *Experimental Mechanics*, 23(4), pp. 393-400, 1983

\*\* J. Mitchell, A Nonlocal, Ordinary, State-Based Plasticity Model for Peridynamics, SAND2011-3166, 2011.

# Explosively Compressed Cylinder\*

- ❑ Motived by experiments of Vogler & Lappo\*
  - ❑ Commonly used for consolidation of powders
  - ❑ Copper cylinders filled with granular material and wrapped with Detasheet explosive
  - ❑ Polyurethane foam plugs used to keep granular sample in tube.
- 
- ❑ Geometry and Material Properties
  - ❑ Copper tubes 305 mm long, ID 50.8 mm, wall thickness of 1.52 mm
  - ❑ PETN based Detasheet with thicknesses of 1, 2, 4, or 6 mm were used, and a
  - ❑ Detonation traveled down length of tube, compressing both tube and sand fill



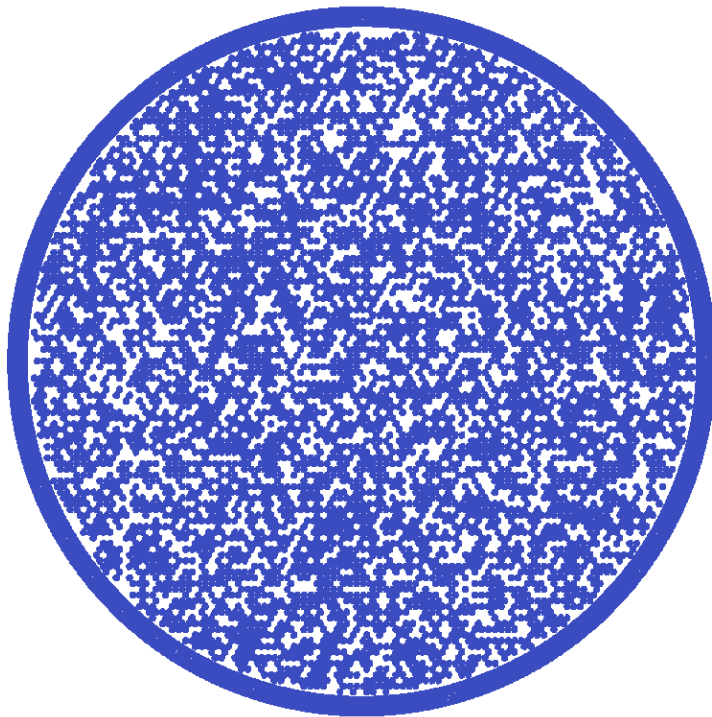
Cylinder schematic



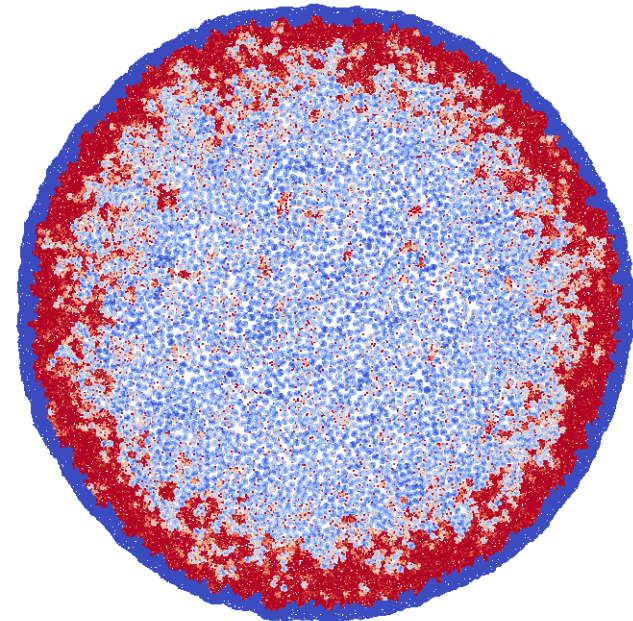
Cylinder after compression

# Explosively Compressed Cylinder

- ❑ Peridigm computational results (with C. Hoffarth (ASU), D. Littlewood (SNL))
  - ❑ Color indicates damage (blue = undamaged, red = damaged)



Before



After

# Tensile Test

- Stainless steel dogbone specimen.
- Apply displacement boundary conditions corresponding to 1% strain.
- Quasistatic solve

before



after



Color proportional to yield.

Displacement exaggerated 10×



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Peridigm: Tutorial and Example

# Peridigm

- ❑ **Peridigm** (Open Source, C++)
- ❑ Developers: Parks, Littlewood, Mitchell, Silling
- ❑ <https://software.sandia.gov/trac/peridigm>
- ❑ Intended as Sandia's primary open-source PD code
- ❑ Built upon Sandia's Trilinos Project ([trilinos.sandia.gov](http://trilinos.sandia.gov))
  
- ❑ **Features/Capabilities**
- ❑ Massively parallel, Exodus mesh input, Multiple material blocks
  
- ❑ Only state-based material models
  - ❑ elastic, elastic-plastic, elastic-plastic with hardening, viscoelastic
  
- ❑ Explicit time integration (Velocity-Verlet)
- ❑ Implicit time integration (Newmark-beta method)
- ❑ Quasistatics
- ❑ Nonlinear (Newton/Krylov, nonlinear CG)
- ❑ Linear (preconditioned Krylov subspace methods)
- ❑ Automatic differentiation Jacobians
- ❑ DAKOTA interface for UQ/optimization/calibration, etc. ([dakota.sandia.gov](http://dakota.sandia.gov))



# Peridigm: Peridynamics via Agile Components

Peridigm

## Software Quality Tools



Mailing Lists



Version Control



Build System

Testing (CTest)



Project Management

Issue Tracking

Wiki



UQ

Optimization

Error Estimation

Calibration



Visualization



Service Tools



## Parallelization Tools

Data Structures (Epetra)

Load Balancing (Zoltan)

## Analysis Tools

UQ (Stokhos)

Optimization (MOOCHO)

## Services

Interfaces (Thyra)

Tools (Teuchos, TriUtils)

Field Manager (Phalanx)

DAKOTA Interface (TriKota)

## Solver Tools

Iterative Solvers (Belos)

Direct Solvers (Amesos)

Nonlinear Solvers (NOX)

Eigensolvers (Anasazi)

Preconditioners (IFPack)

Multilevel (ML)

# Peridynamic Codes

- ❑ **EMU** (Export controlled, F90)
  - ❑ Developer: Silling ([www.sandia.gov/emu/emu.htm](http://www.sandia.gov/emu/emu.htm))
  - ❑ Research code
- ❑ **PDLAMMPS (Peridynamics-in-LAMMPS)** (Open source, C++)
  - ❑ Developers: Parks, Seleson, Plimpton, Silling, Lehoucq
  - ❑ Particular discretization of PD has computational structure of molecular dynamics (MD)
  - ❑ LAMMPS: Sandia's open-source massively parallel MD code ([lammps.sandia.gov](http://lammps.sandia.gov))
  - ❑ More info & user guide: [www.sandia.gov/~mlparks](http://www.sandia.gov/~mlparks)
- ❑ **Peridigm** (Open Source, C++)
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  - ❑ Massively parallel, Exodus mesh input, Multiple material blocks
  - ❑ Explicit, implicit time integration
  - ❑ State-based linear elastic, elastic-plasticity, viscoelastic models
  - ❑ DAKOTA interface for UQ/optimization/calibration, etc. ([dakota.sandia.gov](http://dakota.sandia.gov))
- ❑ **Peridynamics in Sierra/SolidMechanics** (Export controlled, C++)
  - ❑ Developer: Littlewood
  - ❑ Sandia engineering analysis code
- ❑ **Peridynamics is a capability that can be added to (almost) any analysis code!**



# Peridigm Material Models

## Linear Peridynamic Solid (LPS)\*

- Nonlocal analog to linear isotropic elastic solid
- $k$  is bulk modulus,  $\mu$  is shear modulus

$$\rho \ddot{\mathbf{u}}(\mathbf{x}, \mathbf{t}) = \int_{\mathbf{H}} \left( \mathbf{T}[\mathbf{x}, \mathbf{t}] \langle \mathbf{x}' - \mathbf{x} \rangle - \mathbf{T}[\mathbf{x}', \mathbf{t}] \langle \mathbf{x} - \mathbf{x}' \rangle \right) dV_{\mathbf{x}'} + \mathbf{b}(\mathbf{x}, \mathbf{t})$$

$$\mathbf{T}[\mathbf{x}, \mathbf{t}] \langle \mathbf{x}' - \mathbf{x} \rangle = \left( \frac{3k\theta}{m} \underline{\underline{\omega}} \mathbf{x} + \frac{15\mu}{m} \underline{\underline{\omega}} \mathbf{e}^d \right) \frac{\mathbf{x}' - \mathbf{x}}{\|\mathbf{x}' - \mathbf{x}\|}$$

- Many other peridynamic material models available:

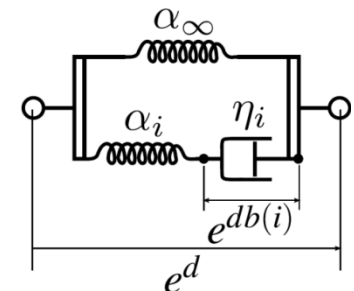
## Elastic-Plastic Model\*\*

- Nonlocal analogue to perfect plasticity model

## Elastic-Plastic Model with Hardening (J. Foster, UTSA)

## Viscoelastic Model\*\*\*

- Nonlocal analog to standard linear solid



\*S.A. Silling, M. Epton, O. Weckner, J. Xu, & E. Askari, Peridynamic States and Constitutive Modeling, J. Elasticity, 88, pp. 151-184, 2007.

\*\*J. Mitchell, A Nonlocal, Ordinary, State-Based Plasticity Model for Peridynamics, SAND2011-3166, 2011.

\*\*\*J. Mitchell, A Non-local, Ordinary-State-Based Viscoelasticity Model for Peridynamics, SAND2011-8064, 2011.

# Peridigm: Structure & User Interface

- ❑ **Peridigm designed to be user extensible**
  - ❑ User defined material models, compute classes, etc.
- ❑ **Compute class: Compute any user-defined quantity**
  - ❑ Class must declare what data it needs allocated
    - ❑ Examples: per-element or per-node scalar, vector, tensor, etc.
  - ❑ Class must provide routine that computes user-defined quantity
    - ❑ **User writes only serial code -- parallel communication handled “auto-magically”**
- ❑ **Example: Compute Acceleration (for output)**

```
///  
int PeridigmNS::Compute_Acceleration::compute( Teuchos::RCP< std::vector<Block> > blocks ) const {  
    int retval(0);  
  
    Teuchos::RCP<Epetra_Vector> force, acceleration;  
    std::vector<Block>::iterator blockIt;  
    for(blockIt = blocks->begin() ; blockIt != blocks->end() ; blockIt++){  
        force          = blockIt->getData(m_forceDensityFieldId, PeridigmField::STEP_NP1);  
        acceleration   = blockIt->getData(m_accelerationFieldId, PeridigmField::STEP_NP1);  
        *acceleration = *force;  
        double density = blockIt->getMaterialModel()->Density();  
        // Report if any calls to Scale() failed.  
        retval = retval || acceleration->Scale(1.0/density);  
    }  
  
    return retval;  
}
```

- ❑ **Declare “acceleration” as output field in input deck**
  - ❑ Only specified fields are computed



# Peridigm: Structure & User Interface

## ❑ Peridigm material models: Create your own!

```
///  
virtual Teuchos::RCP< std::vector<Field_NS::FieldSpec> > VariableSpecs() const = 0;  
  
///  
virtual void initialize(const double dt,  
                       const int numOwnedPoints,  
                       const int* ownedIDs,  
                       const int* neighborhoodList,  
                       PeridigmNS::DataManager& dataManager) const {}  
  
///  
virtual void computeForce(const double dt,  
                          const int numOwnedPoints,  
                          const int* ownedIDs,  
                          const int* neighborhoodList,  
                          PeridigmNS::DataManager& dataManager) const = 0;  
  
///  
virtual void computeJacobian(const double dt,  
                             const int numOwnedPoints,  
                             const int* ownedIDs,  
                             const int* neighborhoodList,  
                             PeridigmNS::DataManager& dataManager,  
                             PeridigmNS::SerialMatrix& jacobian) const;  
  
// other routines
```



# Peridigm: Recent New Features

## ❑ Surface Correction Factor (SCF): John Mitchell

- ❑ In PD, points close to boundary have fewer bonds than points in bulk
- ❑ This makes the material response different near the boundary
- ❑ Must alter material response near boundary to correct for “missing” bonds
- ❑ This is extremely important for engineering simulations!
- ❑ See John Mitchell’s talk: *On the 'DSF' and the 'Dreaded Surface Effect'*

## ❑ Thermal stress: Dave Littlewood

## ❑ Bond-cutting planes: John Mitchell, Dave Littlewood



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Peridigm: Tutorial and Example

# Fragmenting Cylinder

## ❑ Fragmenting Brittle Cylinder

- ❑ Motivated by tube fragmentation experiments of Winter (1979), Vogler (2003)\*

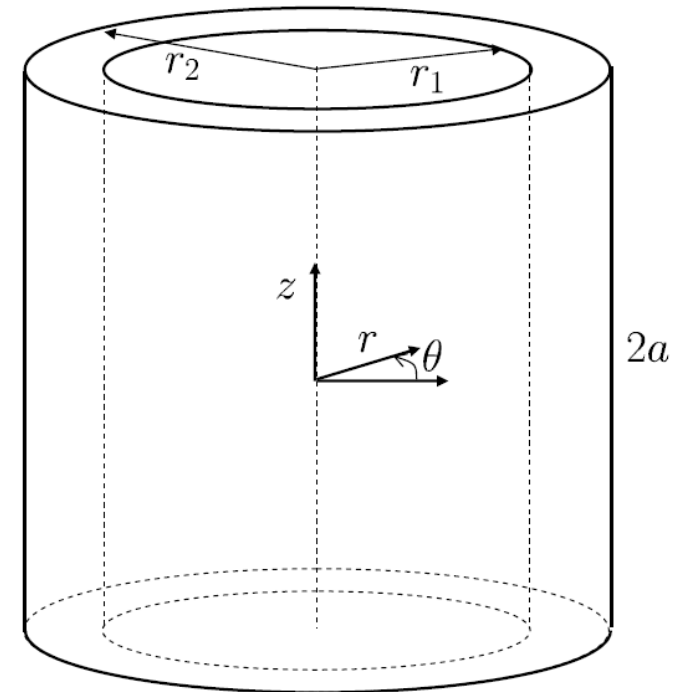
## ❑ Material properties

- ❑ Inner radius  $r_1 = 0.020$  m
- ❑ Outer radius  $r_2 = 0.025$  m
- ❑ Length  $2a = 0.1$  m
- ❑ Density  $\rho = 7800$  kg/m<sup>3</sup>
- ❑ Bulk modulus  $k = 130$  GPa
- ❑ Shear modulus  $\mu = 78$  GPa
- ❑ Yield stress  $Y = 500$  GPa
- ❑ Ultimate stress  $\sigma = 700$  GPa
- ❑ Elongation at failure  $\varepsilon = 0.02$

## ❑ Initial Velocity

- ❑  $v(r) = V_{r0} - V_{r1}(a/z)^2$
- ❑  $v(z) = V_{z0}(a/z)$
- ❑  $v(\theta) = 0$

where  $V_{r0} = 200$  m/s,  $V_{r1} = 50$  m/s,  $V_{z0} = 100$  m/s





# Running Peridigm

## □ Usage:

```
Peridigm Input.xml
```

where Input.xml is a properly formatted input deck using Trilinos/Teuchos XML ParameterList :

```
<ParameterList>
    ... input section here...
</ParameterList>
```

## □ An input deck contains these sections:

```
<ParameterList>
  [Discretization Section]
  [Materials Section]
  [Damage Models Section]
  [Blocks Section]
  [Contact Section]
  [Boundary Conditions Section]
  [Solver Section]
  [Output Sections]
</ParameterList>
```

# Running Peridigm

Refresh  
Example

## Input Deck

```
<ParameterList name="Discretization">
  <Parameter name="Type" type="string" value="PdQuickGrid" />
  <Parameter name="Horizon" type="double" value="0.00417462" />
  <Parameter name="NeighborhoodType" type="string" value="Spherical" />
  <ParameterList name="TensorProductCylinderMeshGenerator">
    <Parameter name="Type" type="string" value="PdQuickGrid" />
    <Parameter name="Inner Radius" type="double" value="0.020" />
    <Parameter name="Outer Radius" type="double" value="0.025" />
    <Parameter name="Cylinder Length" type="double" value="0.100" />
    <Parameter name="Ring Center x" type="double" value="0.0" />
    <Parameter name="Ring Center y" type="double" value="0.0" />
    <Parameter name="Z Origin" type="double" value="0.0" />
    <Parameter name="Number Points Radius" type="int" value="5" />
  </ParameterList>
</ParameterList>
```

Alternative: Read from  
Exodus/Genesis  
mesh generated by  
meshing tool  
(example: CUBIT)

```
<ParameterList name="Materials">
  <ParameterList name="My Linear Elastic Material">
    <Parameter name="Material Model" type="string" value="Elastic"/>
    <Parameter name="Density" type="double" value="7800.0"/>
    <Parameter name="Bulk Modulus" type="double" value="130.0e9"/>
    <Parameter name="Shear Modulus" type="double" value="78.0e9"/>
  </ParameterList>
</ParameterList>
```

Material properties

```
<ParameterList name="Damage Models">
  <ParameterList name="My Critical Stretch Damage Model">
    <Parameter name="Damage Model" type="string" value="Critical Stretch"/>
    <Parameter name="Critical Stretch" type="double" value="0.02"/>
  </ParameterList>
</ParameterList>
```

Damage model  
properties

# Running Peridigm

Used to associate blocks of elements with specific material models

```
<ParameterList name="Blocks">
  <ParameterList name="My Group of Blocks">
    <Parameter name="Block Names" type="string" value="block_1"/>
    <Parameter name="Material" type="string" value="My Linear Elastic Material"/>
    <Parameter name="Damage Model" type="string" value="My Critical Stretch Damage Model"/>
  </ParameterList>
</ParameterList>
```

Function parser: Enter any mathematical function to specify initial velocities or boundary conditions as a function of space & time

```
<ParameterList name="Boundary Conditions">
  <ParameterList name="Initial Velocity X">
    <Parameter name="Type" type="string" value="Initial Velocity"/>
    <Parameter name="Node Set" type="string" value="All"/>
    <Parameter name="Coordinate" type="string" value="x"/>
    <Parameter name="Value" type="string"
      value="(200 - 50*((z/0.05) - 1)^2)*cos(atan2(y,x)) + rnd(5)"/>
  </ParameterList>
  <ParameterList name="Initial Velocity Y">
    <Parameter name="Type" type="string" value="Initial Velocity"/>
    <Parameter name="Node Set" type="string" value="All"/>
    <Parameter name="Coordinate" type="string" value="y"/>
    <Parameter name="Value" type="string"
      value="(200 - 50*((z/0.05) - 1)^2)*sin(atan2(y,x)) + rnd(5)"/>
  </ParameterList>
  <ParameterList name="Initial Velocity Z">
    <Parameter name="Type" type="string" value="Initial Velocity"/>
    <Parameter name="Node Set" type="string" value="All"/>
    <Parameter name="Coordinate" type="string" value="z"/>
    <Parameter name="Value" type="string"
      value="(100*((z/0.05) - 1)) + rnd(5)"/>
  </ParameterList>
</ParameterList>
```

Alternative: Specify nodesets in exodus/genesis database

# Running Peridigm

```
<ParameterList name="Solver">
  <Parameter name="Verbose" type="bool" value="false"/>
  <Parameter name="Initial Time" type="double" value="0.0"/>
  <Parameter name="Final Time" type="double" value="2.5e-4"/>
  <ParameterList name="Verlet">
    <Parameter name="Fixed dt" type="double" value="1.0e-8"/>
  </ParameterList>
</ParameterList>

<ParameterList name="Output">
  <Parameter name="Output File Type" type="string" value="ExodusII"/>
  <Parameter name="Output Format" type="string" value="BINARY"/>
  <Parameter name="Output Filename" type="string" value="fragmenting_cylinder"/>
  <Parameter name="Output Frequency" type="int" value="250"/>
  <Parameter name="Parallel Write" type="bool" value="true"/>
  <ParameterList name="Output Variables">
    <Parameter name="Proc_Num" type="bool" value="true"/>
    <Parameter name="Displacement" type="bool" value="true"/>
    <Parameter name="Velocity" type="bool" value="true"/>
    <Parameter name="Acceleration" type="bool" value="true"/>
    <Parameter name="Force_Density" type="bool" value="true"/>
    <Parameter name="ID" type="bool" value="true"/>
    <Parameter name="Dilatation" type="bool" value="true"/>
    <Parameter name="Damage" type="bool" value="true"/>
    <Parameter name="Weighted_Volume" type="bool" value="true"/>
  </ParameterList>
</ParameterList>
```

Alternative: Implicit time  
integrator (Newmark-Beta) or  
quasistatic solver (damped  
Newton)

Output from compute  
class defined earlier

# The Results...

## ❑ Fragmenting Brittle Cylinder



Before



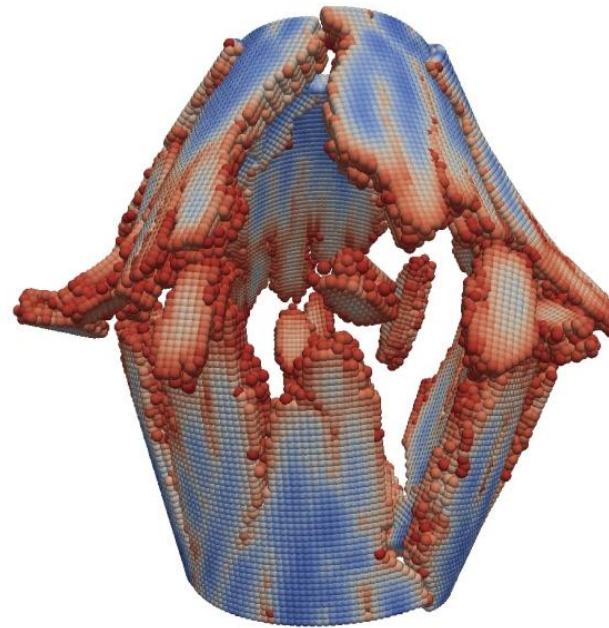
After  
(brittle)

## The Results...

### Fragmenting Brittle Cylinder



Before



After  
(brittle)

### What about ductile failure?

# Running Peridigm

## ❑ Modify the material section and damage model

```
<ParameterList name="Materials">
  <ParameterList name="My Elastic Plastic Material">
    <Parameter name="Material Model" type="string" value="Elastic Plastic"/>
    <Parameter name="Density" type="double" value="7800.0"/>
    <Parameter name="Bulk Modulus" type="double" value="130.0e9"/>
    <Parameter name="Shear Modulus" type="double" value="78.0e9"/>
    <Parameter name="Yield Stress" type="double" value="176.0e6"/>
  </ParameterList>
</ParameterList>
```

Change material type  
and parameters

```
<ParameterList name="Damage Models">
  <ParameterList name="My Critical Stretch Damage Model">
    <Parameter name="Damage Model" type="string" value="Critical Stretch"/>
    <Parameter name="Critical Stretch" type="double" value="0.12"/>
  </ParameterList>
</ParameterList>
```

Increase critical stretch to be consistent with  
elongation at failure for material.

Allows material to yield plastically before failure.

# The Results...

## ❑ Fragmenting Ductile Cylinder



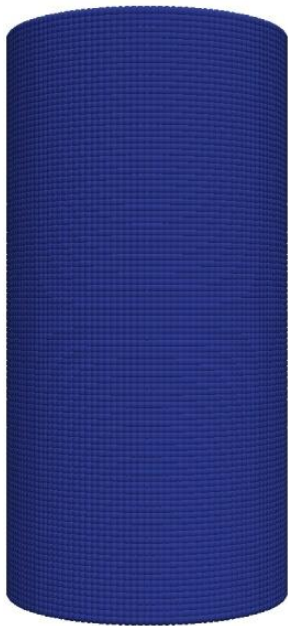
Before



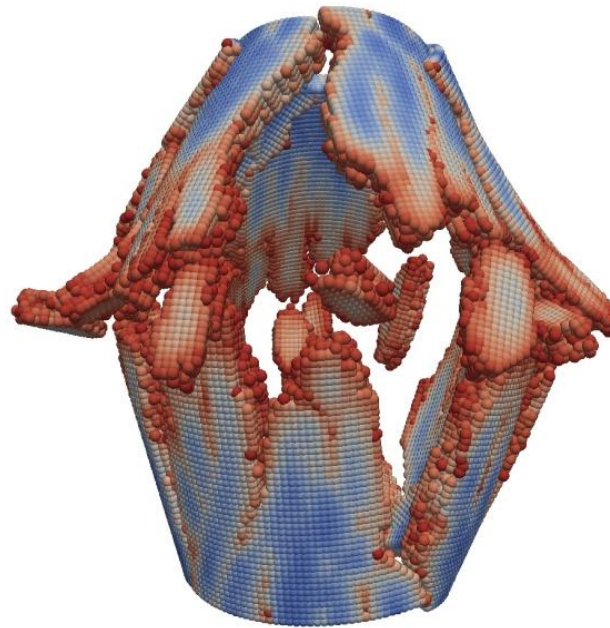
After  
(ductile)

## The Results...

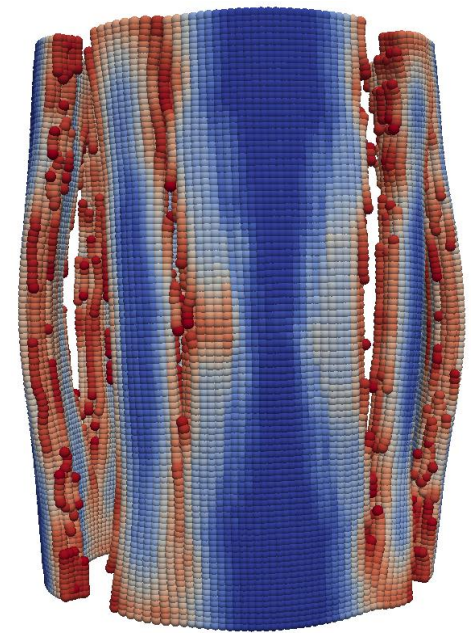
- ❑ Fragmenting Cylinders
  - ❑ Brittle fracture characteristically different from ductile fracture



Before



After  
(brittle)



After  
(ductile)



# Summary

- Peridynamics overview
- Example computations
- Peridigm overview
- Peridigm fragmenting cylinder demonstration
  - Input deck distributed with Peridigm...
  - Other interesting examples (disk impact, tensile test)
  
- Peridigm
  - <https://software.sandia.gov/trac/peridigm>
  
- Contact me for more info: [mlparks@sandia.gov](mailto:mlparks@sandia.gov)
  
- Papers, etc.: [www.sandia.gov/~mlparks](http://www.sandia.gov/~mlparks)
  
- Thank you!