



Simulation of Ionic Aggregation and Ion Dynamics in Ionomers

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January 24, 2013



Sandia
National
Laboratories

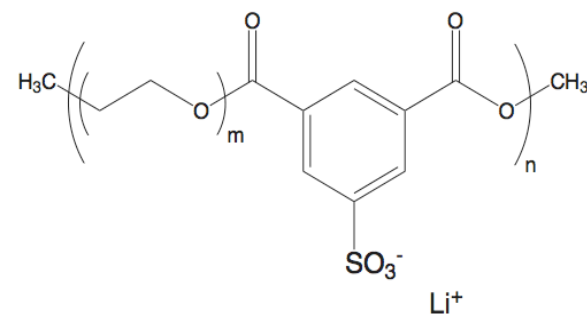
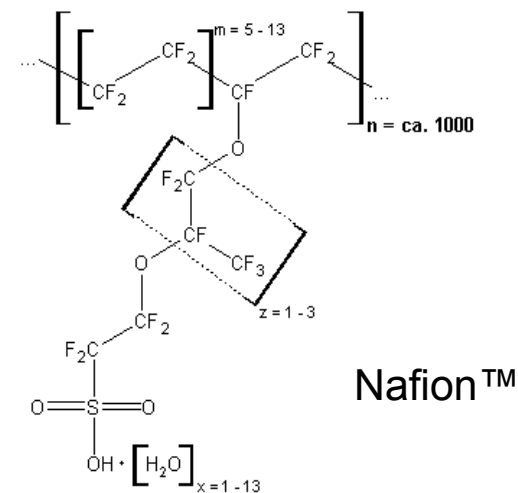
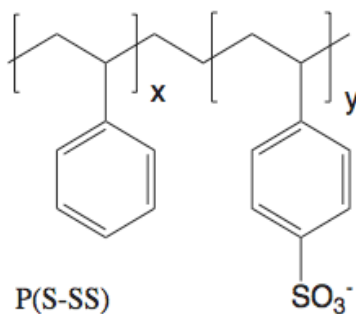
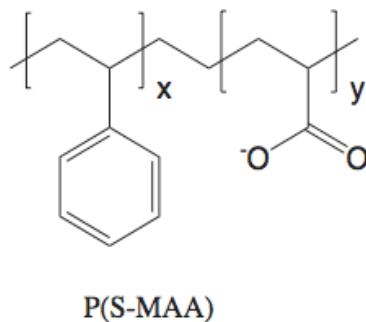
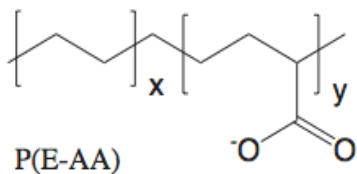
*Exceptional
service
in the
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interest*



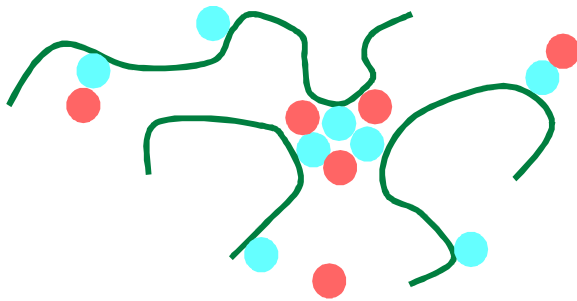
Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

What is an ionomer?

a copolymer
with a small fraction
of covalently-bonded ionic groups



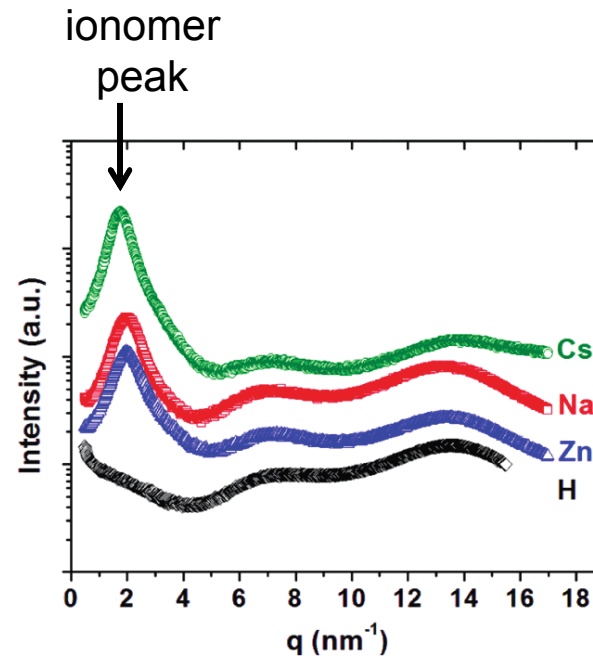
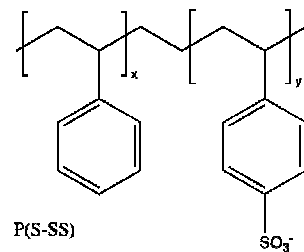
Aggregates in Ionomer Melts



“ionomer peak”

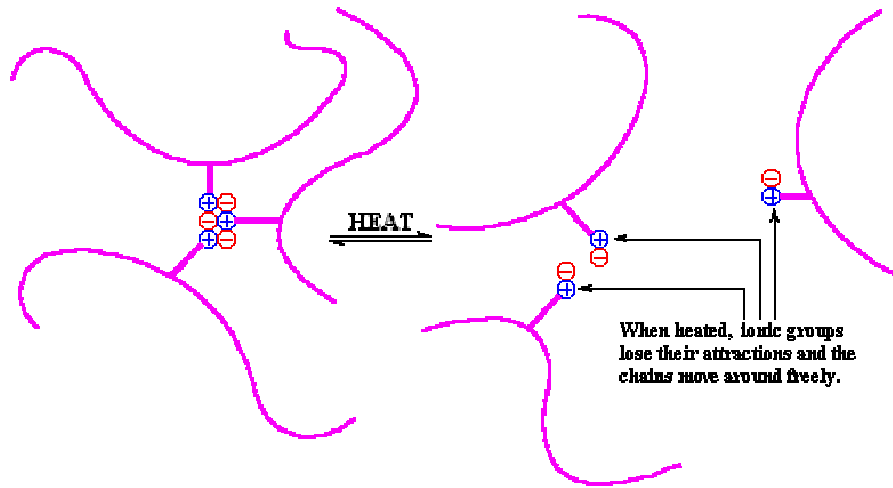
- ubiquitous
- low wavevector peak in scattering
- from inter-aggregate scattering

Coulombic forces favor aggregates
strong pair energy, ≈ 40 kT
polymer entropy limits size



Applications of Ionomers

thermoplastic elastomers



- low T: ionic aggregates behave like crosslinks
 - material is elastic
 - high strength
- high T: ionic aggregates break up
 - material flows (is a liquid)

- golf balls: covers, mantles, intermediate layers, ...
- coatings
- packaging (e.g. foods, cosmetics, ...)
- clear plastic parts
- modifiers in other plastics

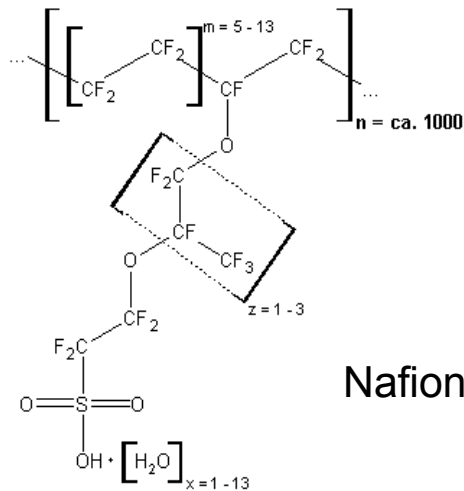
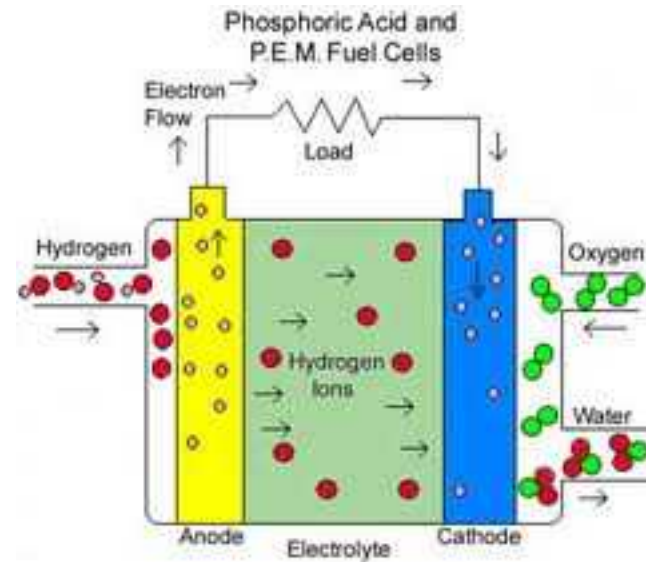


DuPont™ Surlyn®

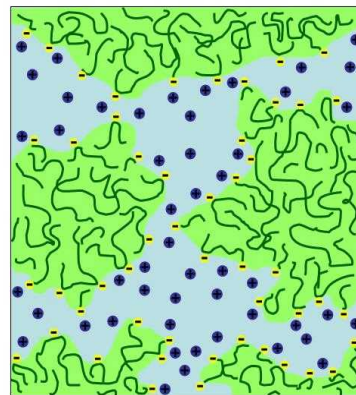
Membranes

ion-selective membranes
typically in water

- water purification
- fuel cells



Nafion™



K. D. Kreuer, 2003

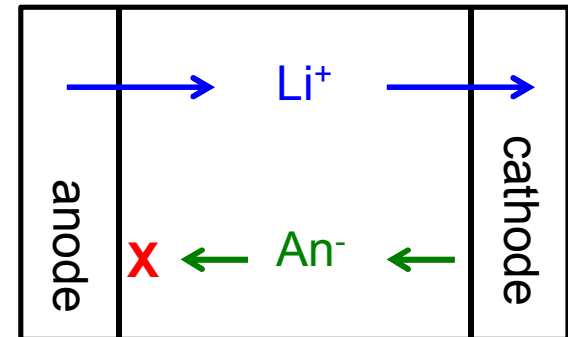
Possible Application: Batteries

Issues with current electrolytes in Li-ion batteries:

- organic solvents
- PEO + lithium salts + solvent
 - need containment
 - flammable!



- solvent free PEO + salt
 - conductivity dominated by anions
 - salt concentration at electrodes
 - extra heating



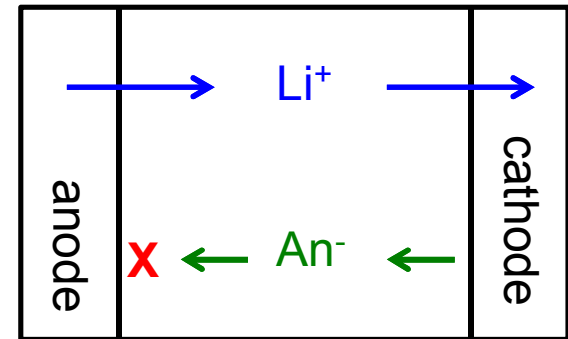
Possible Application: Batteries

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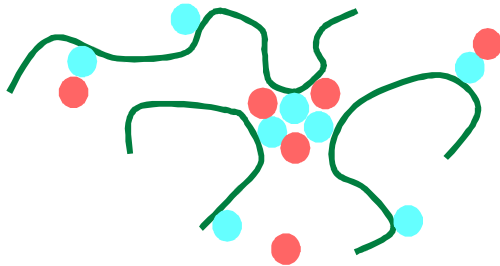
- solvent free PEO + salt
 - conductivity dominated by anions
 - salt concentration at electrodes
 - extra heating



ionomers as next generation electrolytes?

- safer: no solvent
- serve as electrolyte & separator
- less packaging
- improved electrochemical stability
- higher efficiency: single ion conductors

Ionomer Conductivities



- conductivity too low
 - needed for Li-ion batteries: $\geq 10^{-3}$ S/cm
 - Li salt + solvent: $\approx 10^{-2}$ S/cm
 - gel polyelectrolytes: $1-3 \cdot 10^{-3}$ S/cm
 - ionomers: generally $< 10^{-5}$ S/cm
- why?
 - few mobile ions (ion pairs instead)
 - often get ionic aggregates

Need for electrochemical apps:

- relation between molecular architecture & morphology
- effects of morphology on ion transport
- understanding of ion transport mechanisms

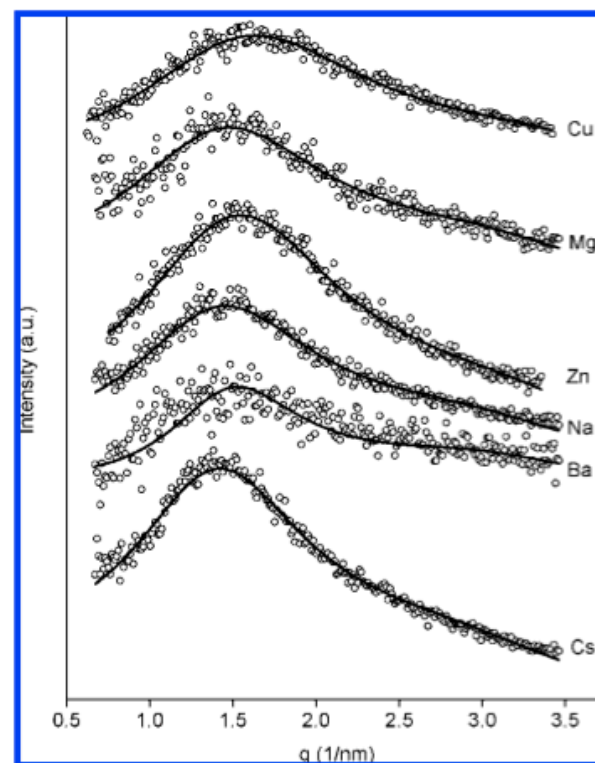
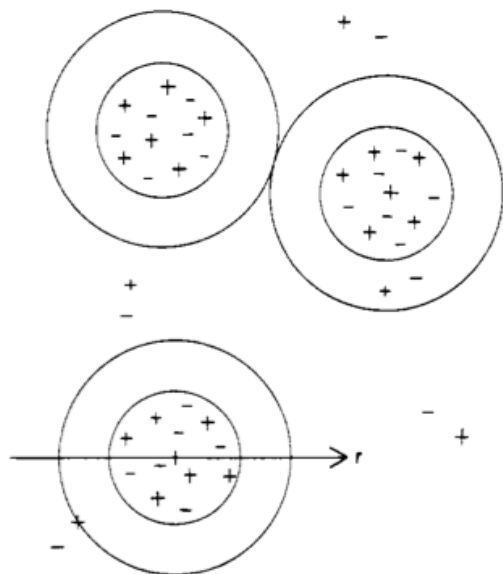
Historical View of Ionomer Melts Sandia National Laboratories

- spherical ion-rich aggregates
- surrounded by ion-poor polymer
- arranged with liquid-like order



“ionomer peak”

- ubiquitous
- low wavevector peak in scattering
- from inter-aggregate scattering



PSS ionomers

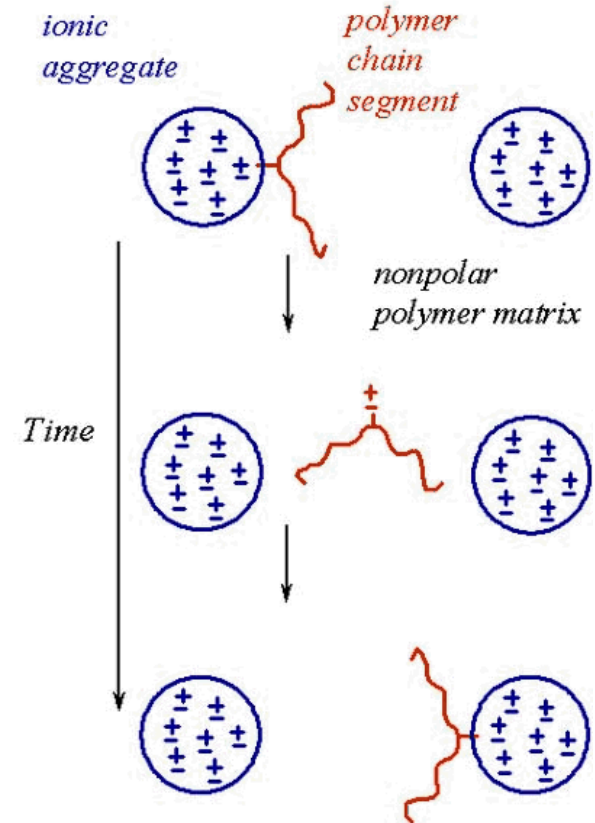
Zhou et al. *Macromolecules* (2008) vol. 41 (16) pp. 6134-6140

D. J. Yarusso; S. L. Cooper; *Polymer* **1985**, 26, 371-378.

Historical View of Dynamics

- requires traversing low dielectric polymer matrix
- large activation energy barrier
- ion **pairs** “hop” between aggregates

this is SLOW

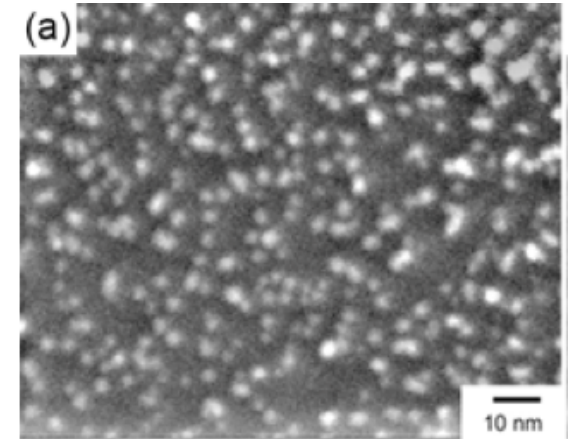


<http://www.princeton.edu/cbe/people/faculty/register/group/research/ionomers/ionomer-melt-rheology-and/>

Outstanding Questions

- What do the aggregates look like, exactly?
 - composition
 - size
 - shape
- What's the dependence on polymer architecture?
 - spacing between charged groups
 - cations
 - anions
- How does ion association affect dynamics?

spherical aggregates

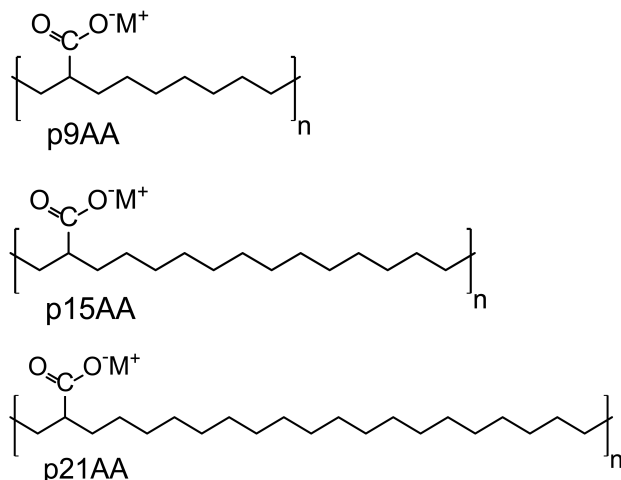


Karen Winey
U Penn

Difficult to measure local
structure experimentally.

Can simulations resolve issue?

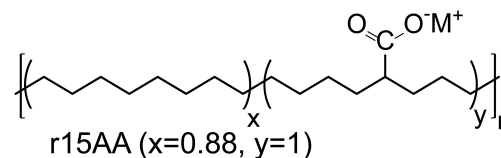
Acyclic Diene Metathesis (ADMET) Precise Copolymer



precise polymers:

- acid group every 9, 15, 21 carbons
- swap H for Zn^{2+} , Li^+ , Na^+ , Cs^+
- nomenclature: $\text{pxAA-y}\% \text{M}$

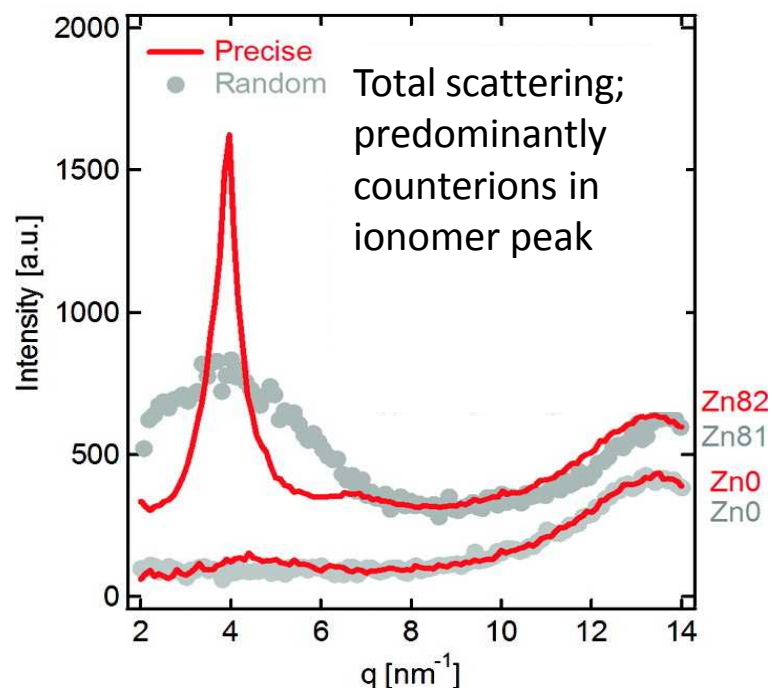
Ring-Opening Metathesis Polymerization (ROMP) Pseudo-Random Copolymer



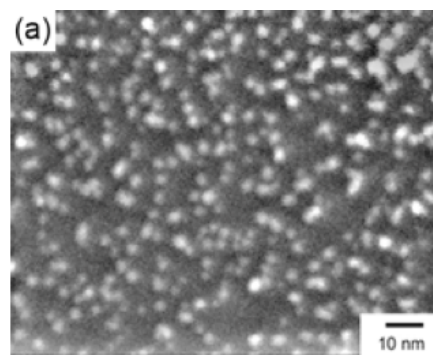
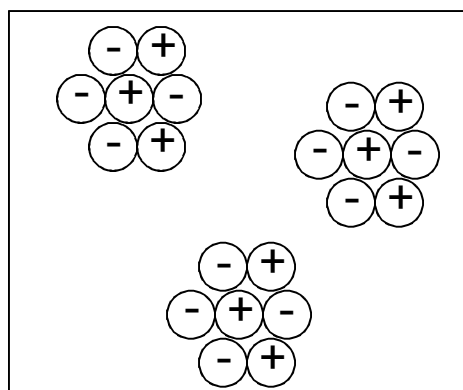
Ken Wagener,
University of Florida

Zn-neutralized Precise Ionomers

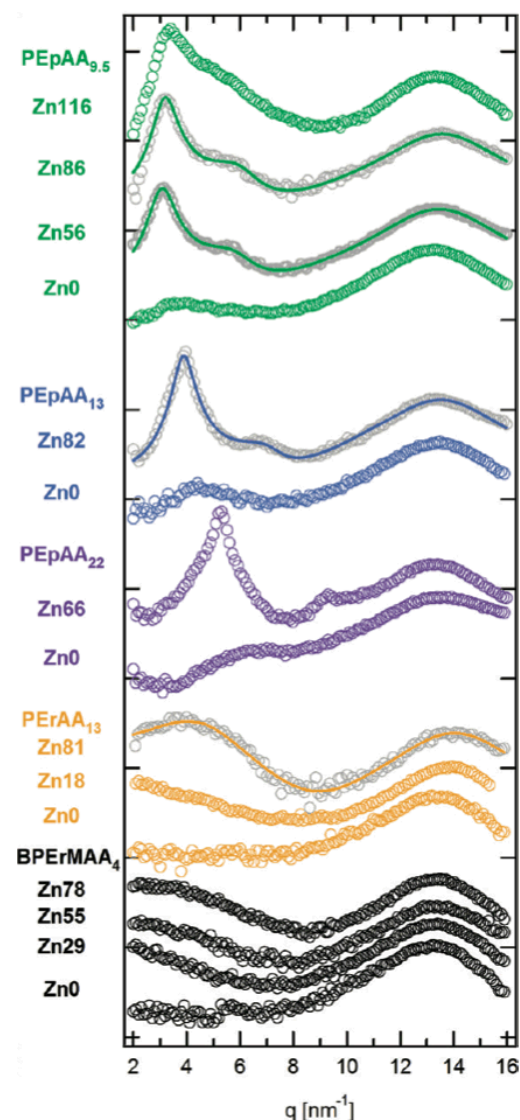
much more defined peak from precise ionomers
ideal for comparison to simulation



modified hard sphere model

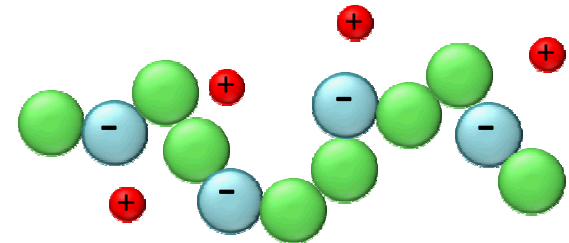
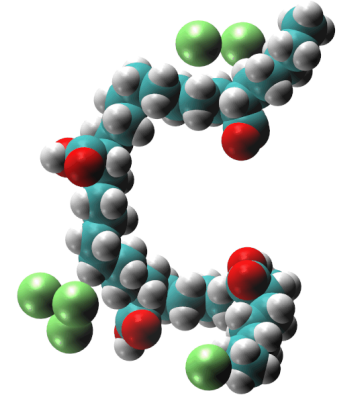


p21AA-56%Zn



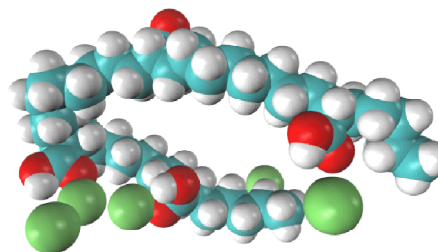
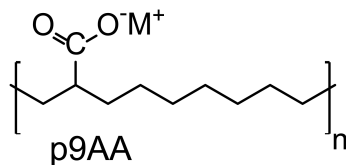
Outline

- atomistic simulations
 - varying cations: Li^+ , Na^+ , Cs^+ , Zn^{2+}
 - varying neutralization
 - compare directly to experiment
 - limited dynamics
- coarse-grained simulations
 - morphology
 - dynamics



Atomistic Ionomer Simulations

- pAA materials:



- Variations in:
 - cation type: M⁺ = Li⁺, Na⁺, Cs⁺, Zn²⁺
 - neutralization level = % COO-M⁺ vs COOH
 - spacing between acid groups
- All atom OPLS force-field
- n = 4 repeat units (4 acid groups)
- ~ 64 Å box, total of ~25,000 atoms
- T = 150 C

Correlation Functions

O-ion – +

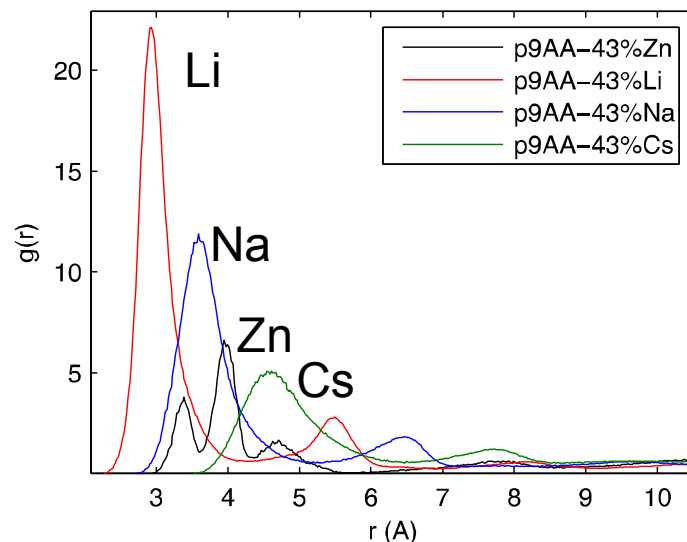
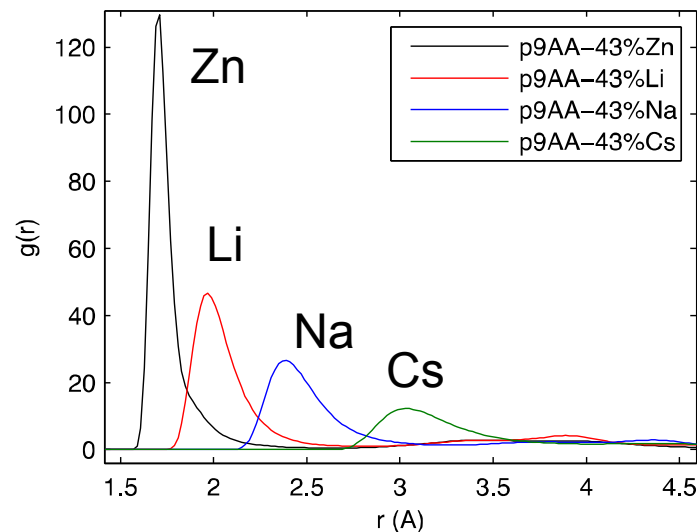
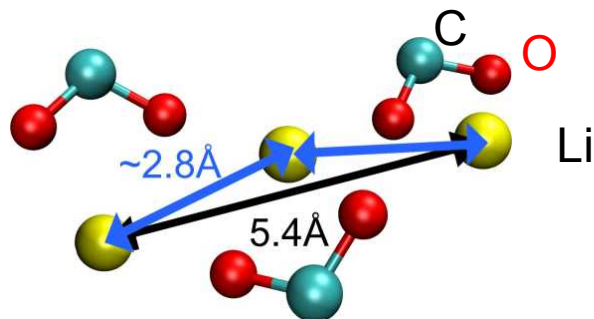
- very large peaks
- peak \sim ion size
- height decreases for larger ions

cluster analysis:

O-ion in same cluster if separation within 1st peak
carbonyl O (OH) in same cluster

ion-ion ++ --

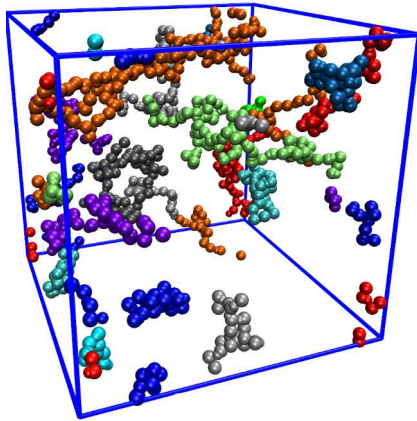
- 1st peak at next-nearest neighbor distance
- secondary peaks visible



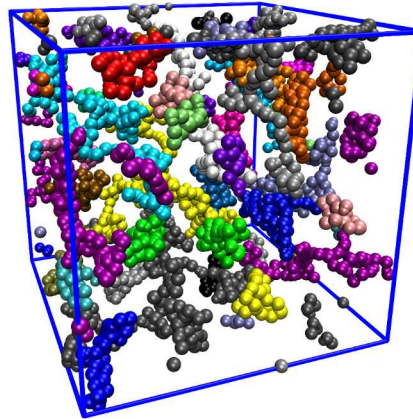
Morphology: Li-neutralized pAA

coloring by cluster

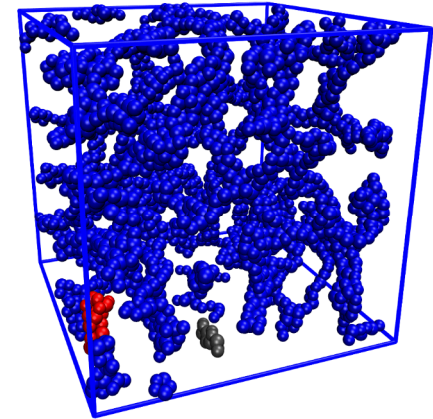
p9AA-10%Li



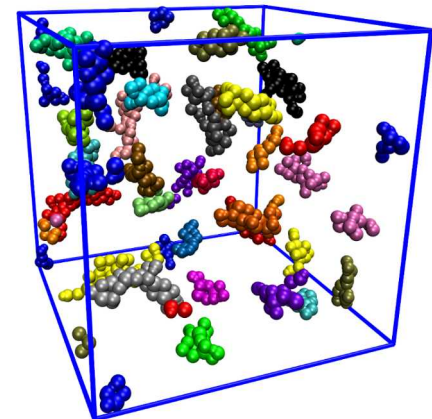
p9AA-43%Li



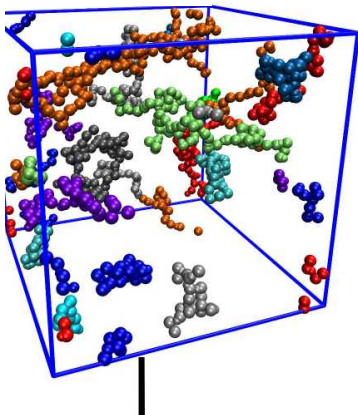
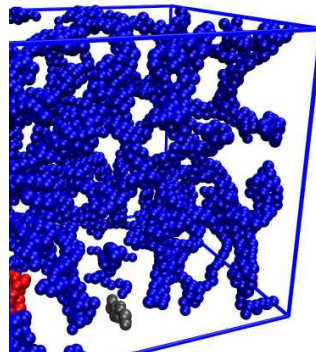
p9AA-100%Li



p21AA-43%Li

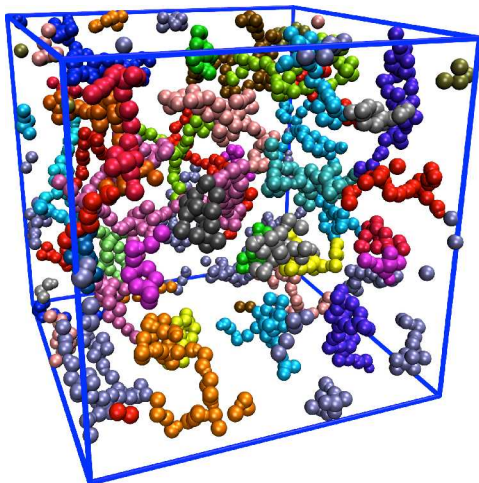


c. p9AA-100%Li
FP

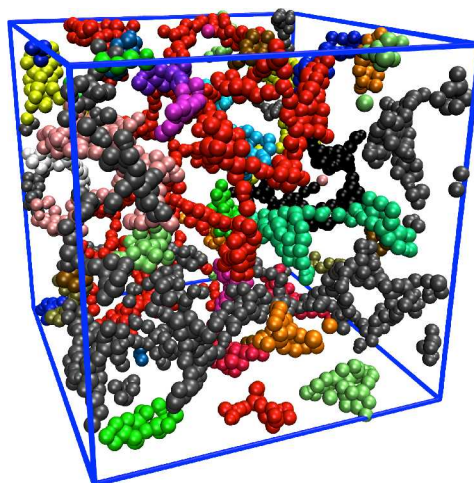


Morphology for Different Cations

Zn²⁺ p9AA-43%M



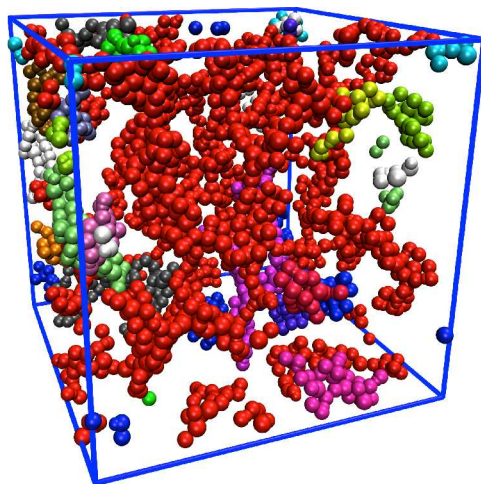
Li⁺



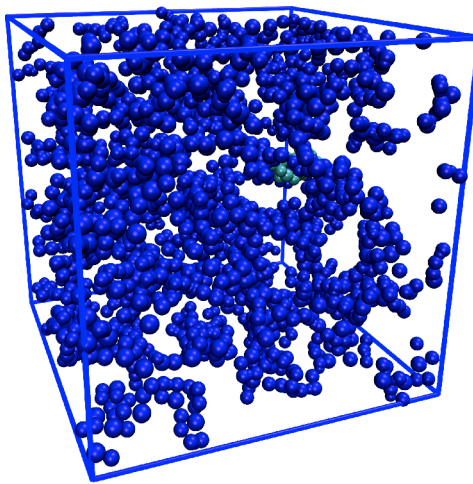
p9AA-y%M

	10%	25%	43%	75%	100%
Zn	LS	LS	SS	SS	SS/CS
Li	SS/LS	LS	LS	LS/PP	PP/FP
Na	SS	SS/LS	PP	FP	FP
Cs	LS	PP	FP	FP	FP

Na⁺



Cs⁺

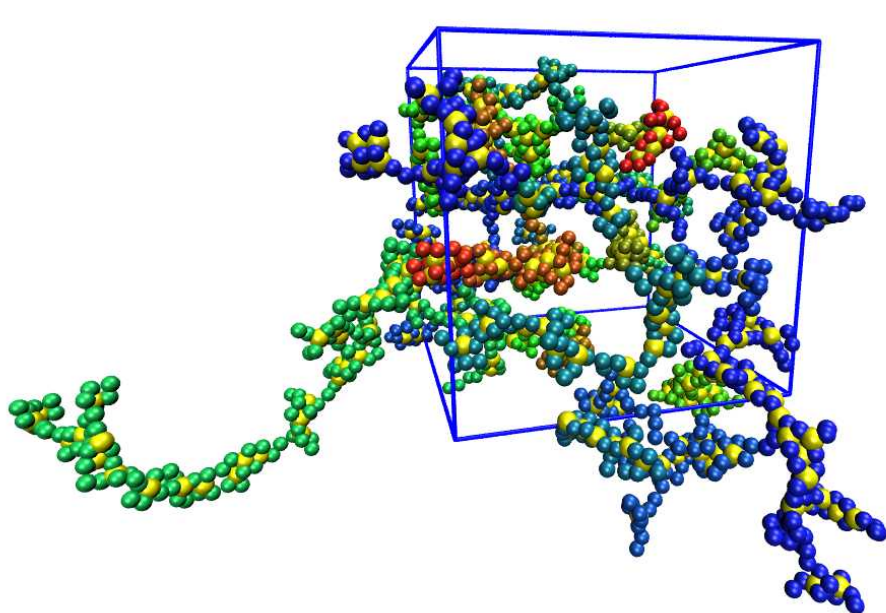


pxAA-43%M

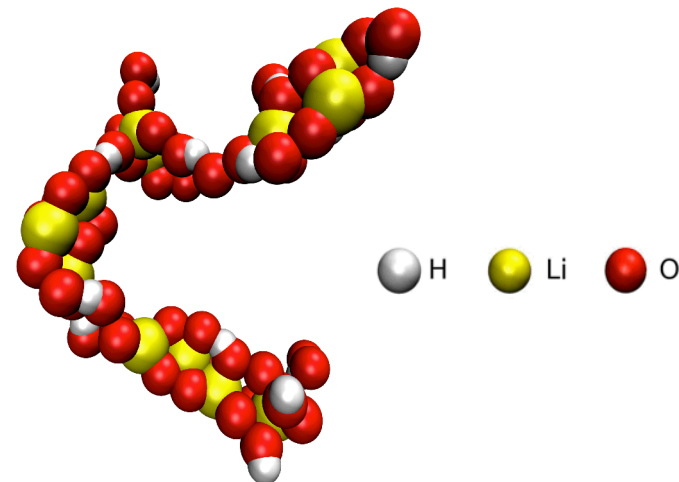
	p9	p15	p21
Zn	SS	SS/CS	CS
Li	LS	SS	SS/CS
Na	PP	SS	SS/CS
Cs	FP	LS/PP	LS/SS

Stringy Aggregates

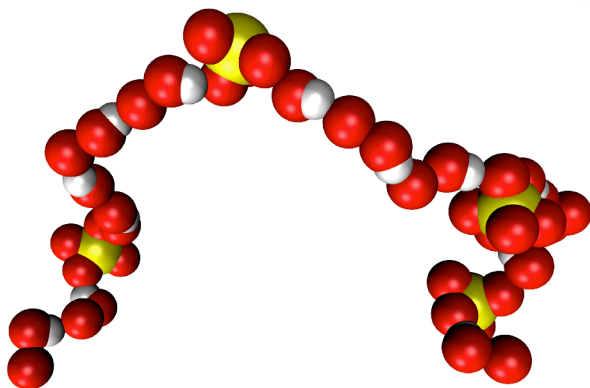
hydrogen bonding contributes to clusters



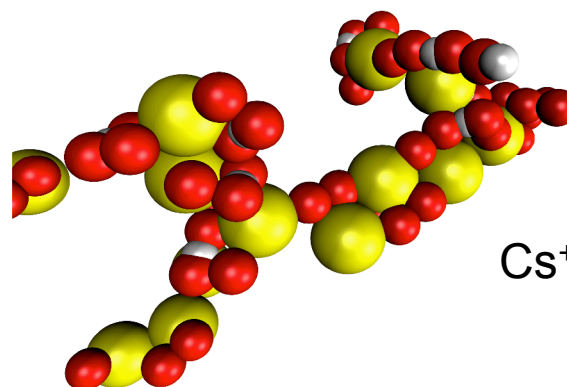
Li^+



Zn^{2+}

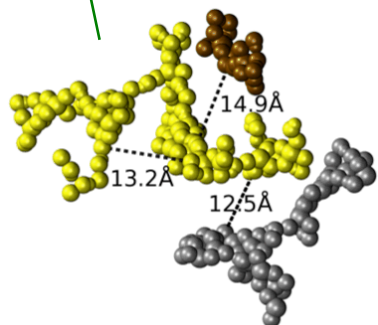
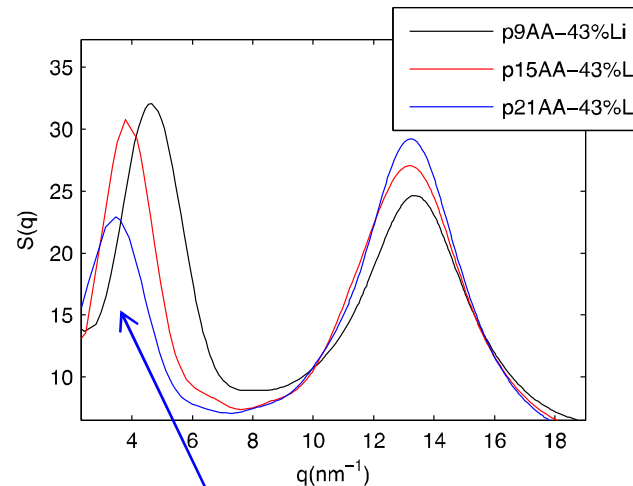
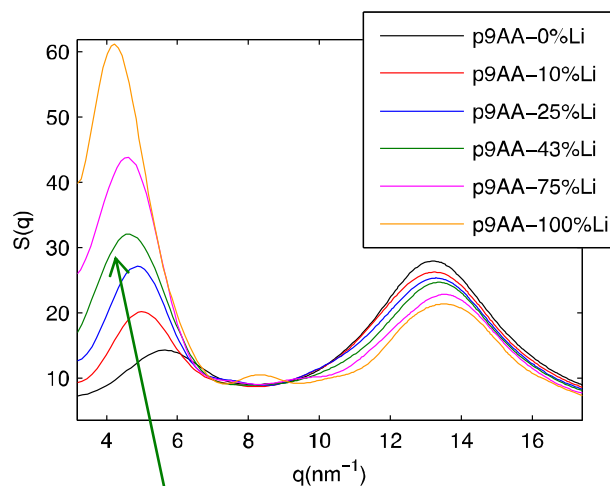


Cs^+

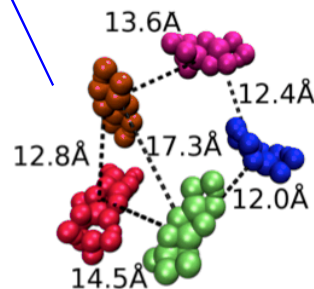


Total Structure Factors for Li-neutralized pAA

$$S(q) = \sum_i c_i f_i^2 + 4\pi\rho \int_0^\infty \frac{\sin(qr)}{qr} r^2 \sum_{i,j} c_i c_j f_i f_j (g_{ij}(r) - 1) dr$$



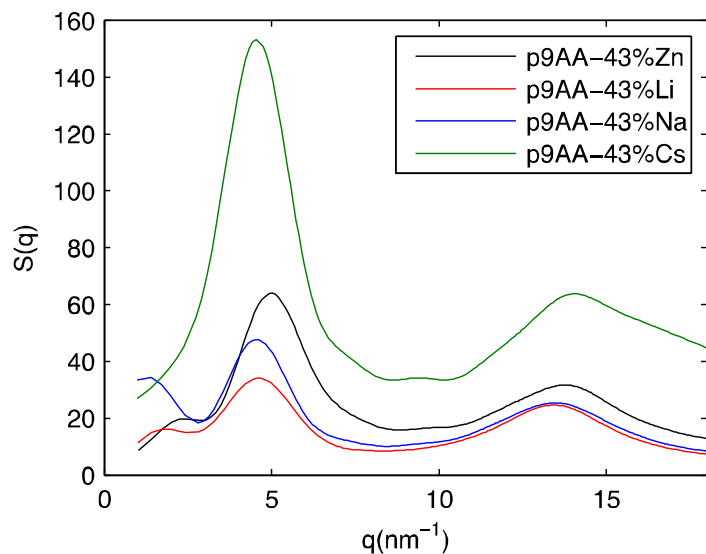
12-17Å
 $q \approx 3.6-5.2/\text{nm}$



ionomer peak from inter-aggregate scattering

Structure Factors vs Cation

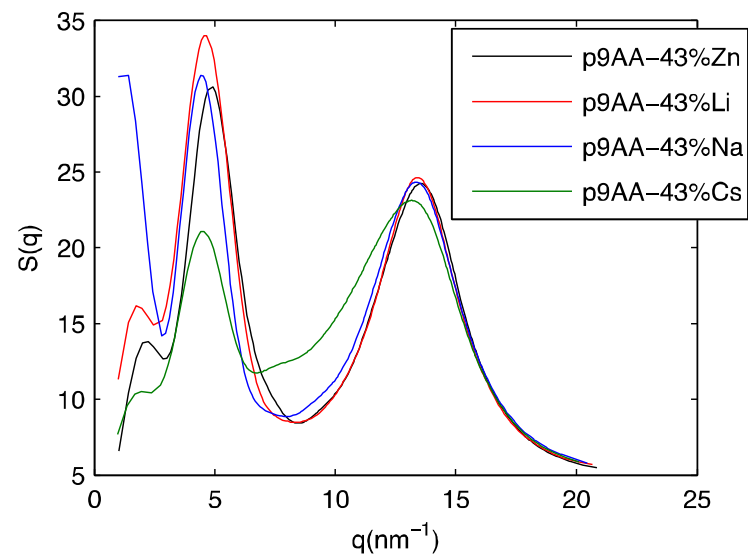
Alchemy



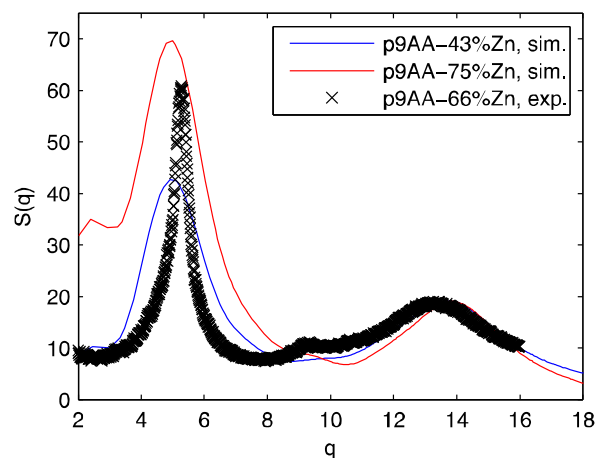
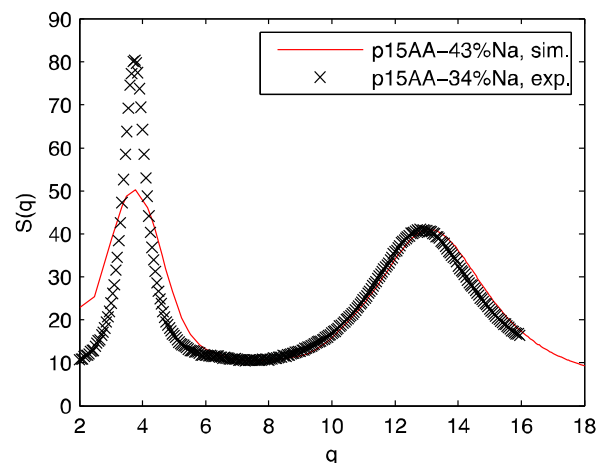
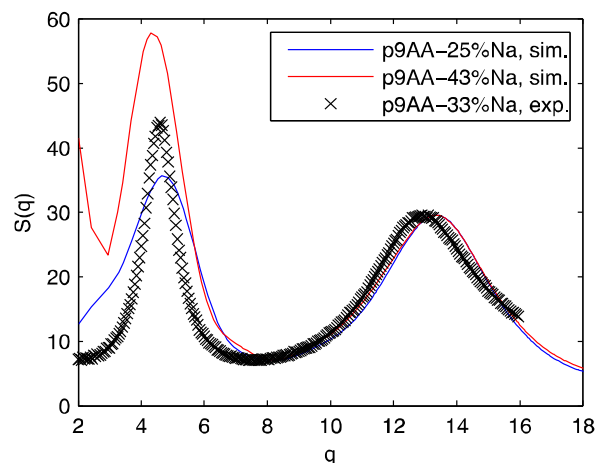
Li^+ form factor
for all ions



$$f_M \rightarrow f_{\text{Li}}$$



Comparison to X-ray Scattering



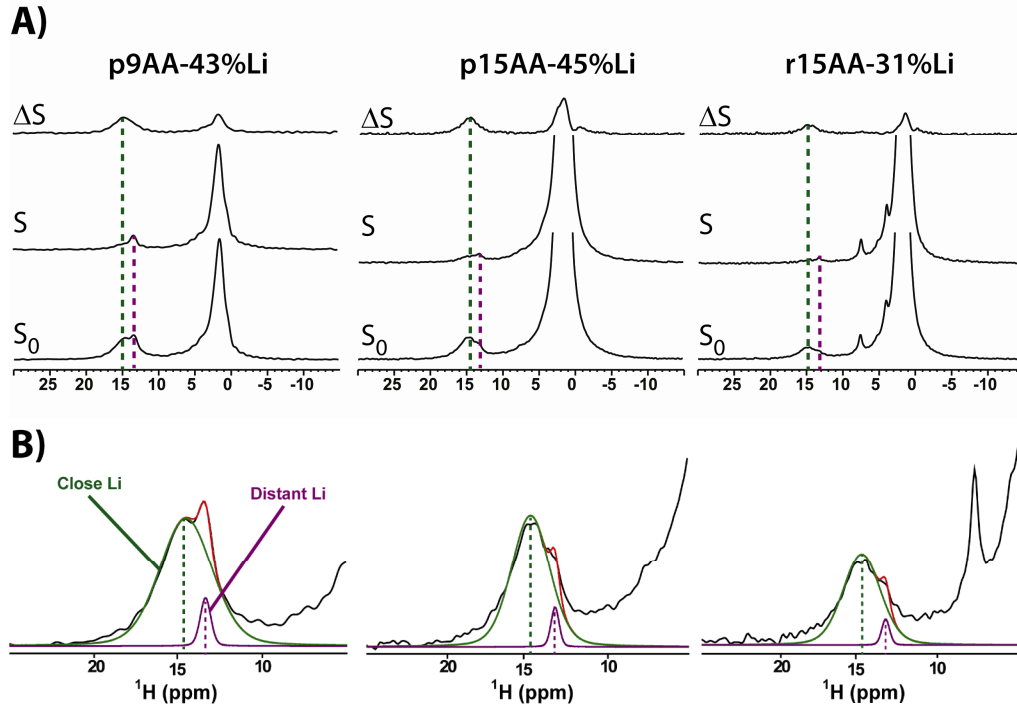
- peaks in correct locations
 - also true for Li, Cs
- x-ray intensity in arbitrary units
 - fit to height of amorphous halo

M. E. Seitz et al., *J. Am. Chem. Soc.* **2010**, 132, 8165

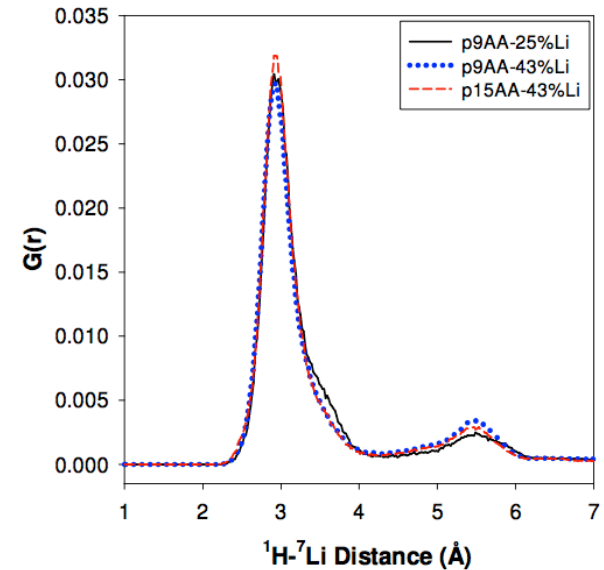
Hall et al., *J. Am. Chem. Soc.* **2012**, 134, 574

Local Li⁺ Environment

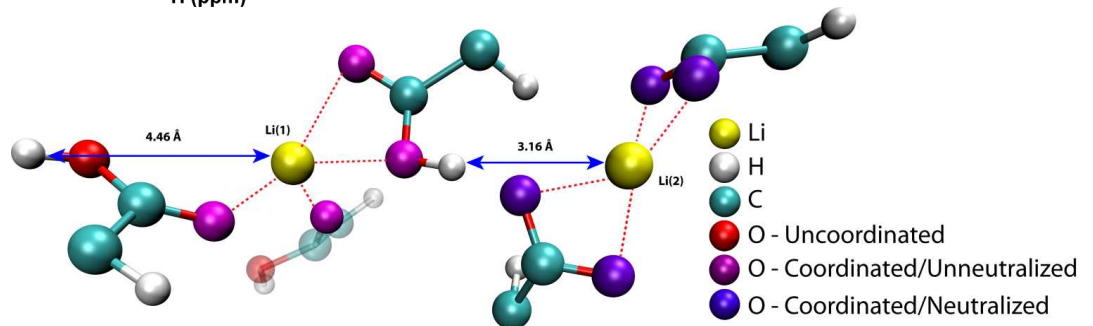
¹H-⁷Li REDOR MAS NMR



atomistic MD



- 2 H-Li distances
- reflects variety of coordination in aggregates

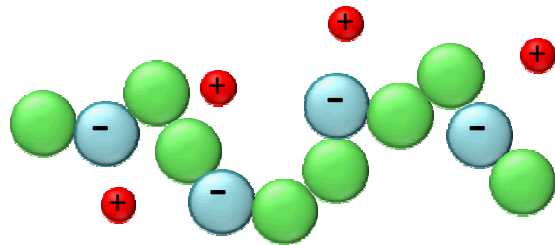


Summary of Atomistic Simulations

- range of morphologies
 - stringy
 - can be percolated
 - not all spherical as previously assumed (except maybe Zn)
 - not well resolved in scattering
 - ionomer peak due to interaggregate scattering
- trends
 - longer aggregates as neutralization increases
 - shorter aggregates as spacer length increases
- hydrogen bonding important in partially neutralized systems
- simulations match experimental $S(q)$ well

Coarse-grained Simulations

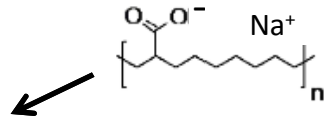
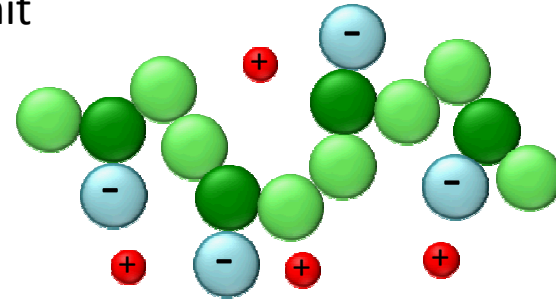
Ions in the polymer backbone:
“**ionenes**”



backbone beads
per repeat unit

$$N_{bb} = 3$$

Ions pendant to the backbone:
“**pendants**”



$$N_{bb} = 3, 5, 7, 9 (11)$$

800 polymers

100% neutralization

bulk dielectric constant = 4

counterion size = $\frac{1}{2}\sigma$

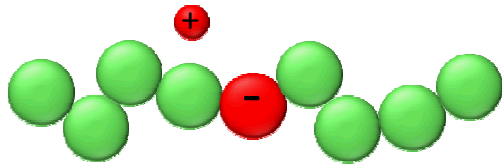
Bjerrum length = 35.7σ

10^8 time steps

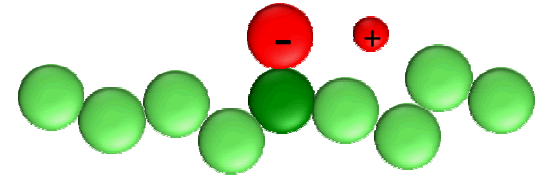
$$\ell_B = \frac{e^2}{4\pi\epsilon_0\epsilon_r kT} = 35.7\sigma$$

$$R_g \approx 3.1 - 3.3\sigma$$

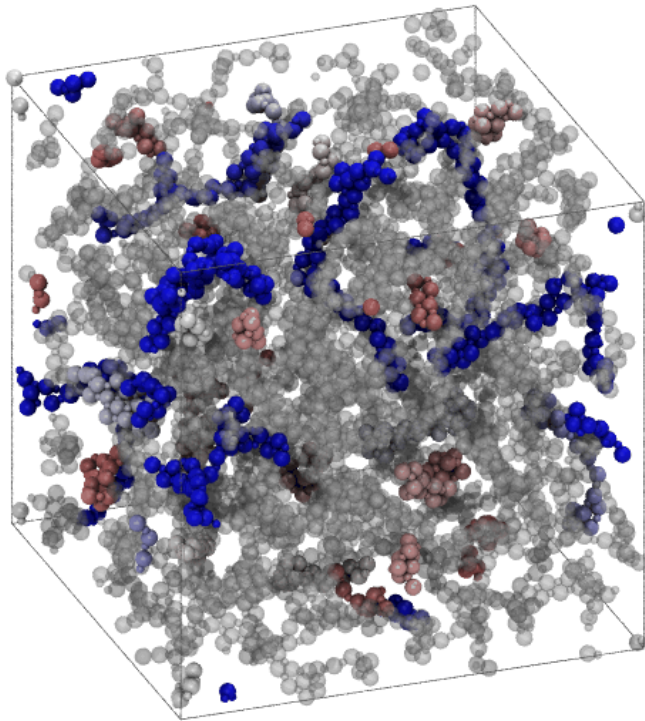
Aggregate Morphology: Architecture Matters



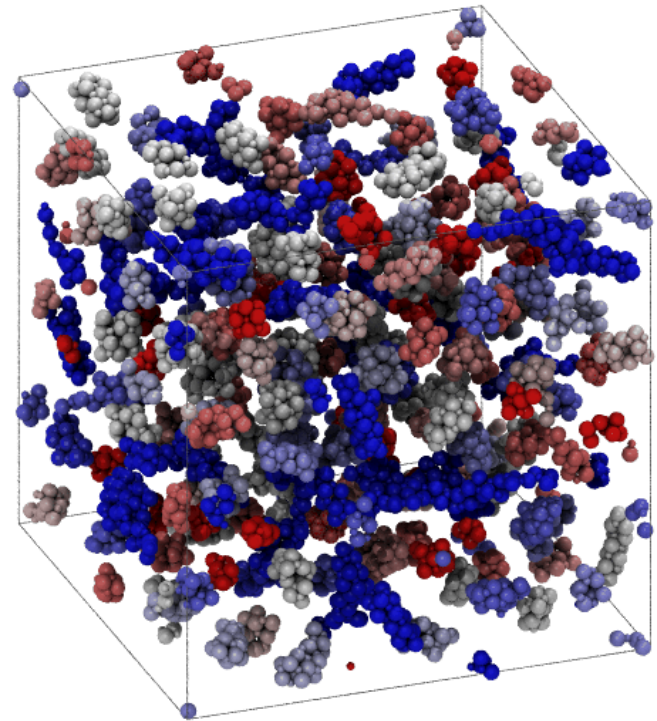
Ionenes: percolated




Pendants: not percolated



$$N_{bb} = 9$$
$$\epsilon_r = 4$$



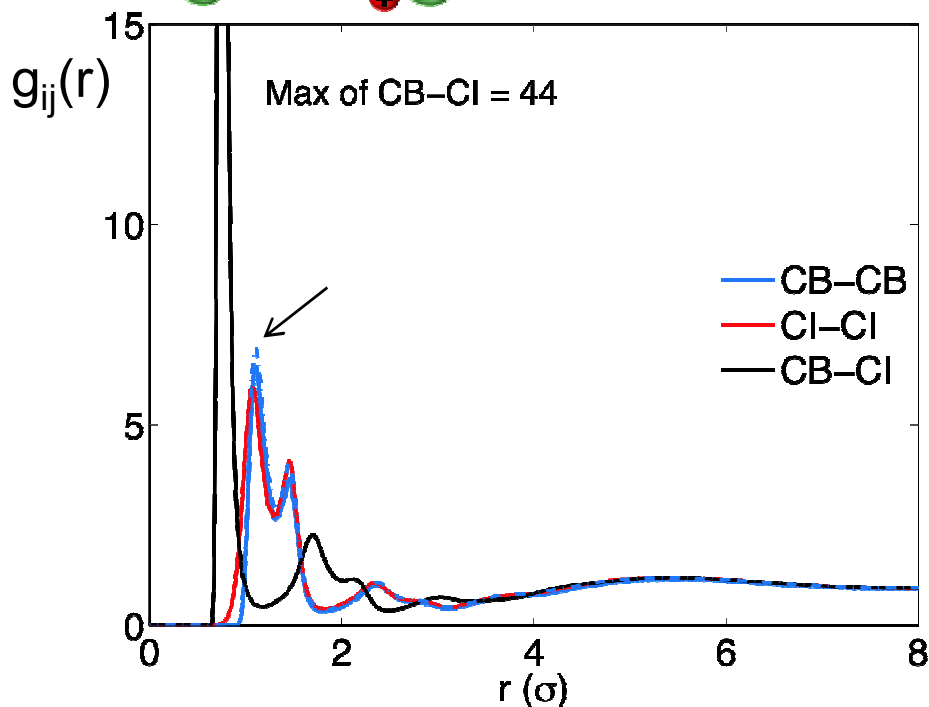
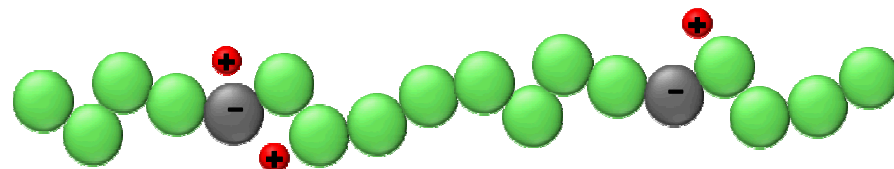
Small clusters  Large clusters

Only charged beads shown

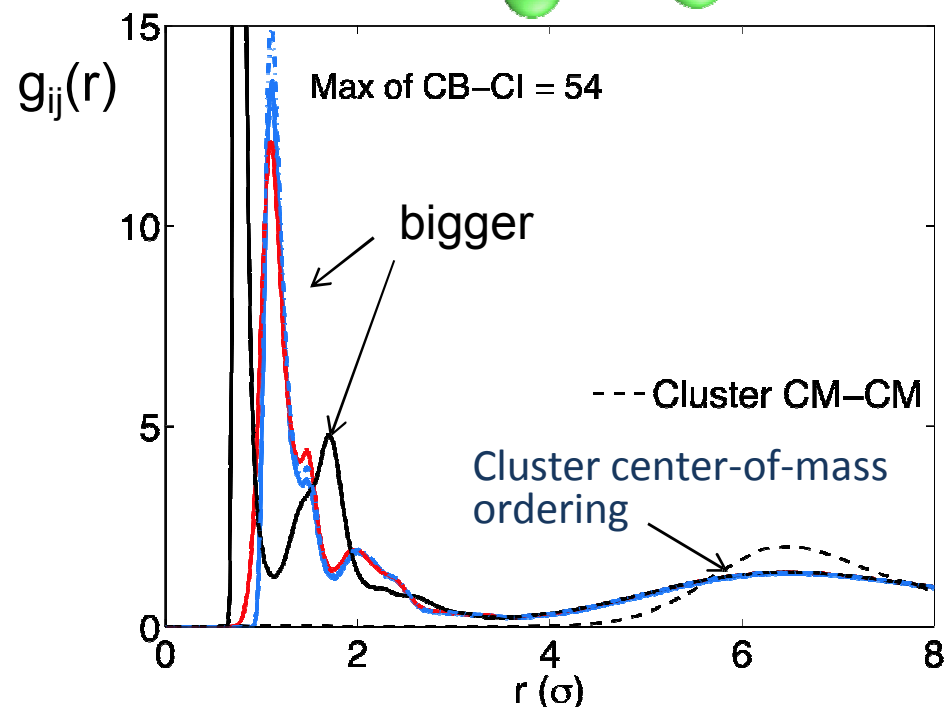
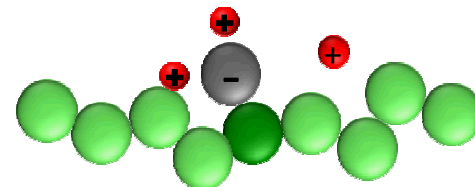
Ion-Ion Pair Correlation Functions

- A clue to difference between ionenes and pendants
- Pendants have larger peaks
- More counterions about pendant charge in polymer

Ionenes

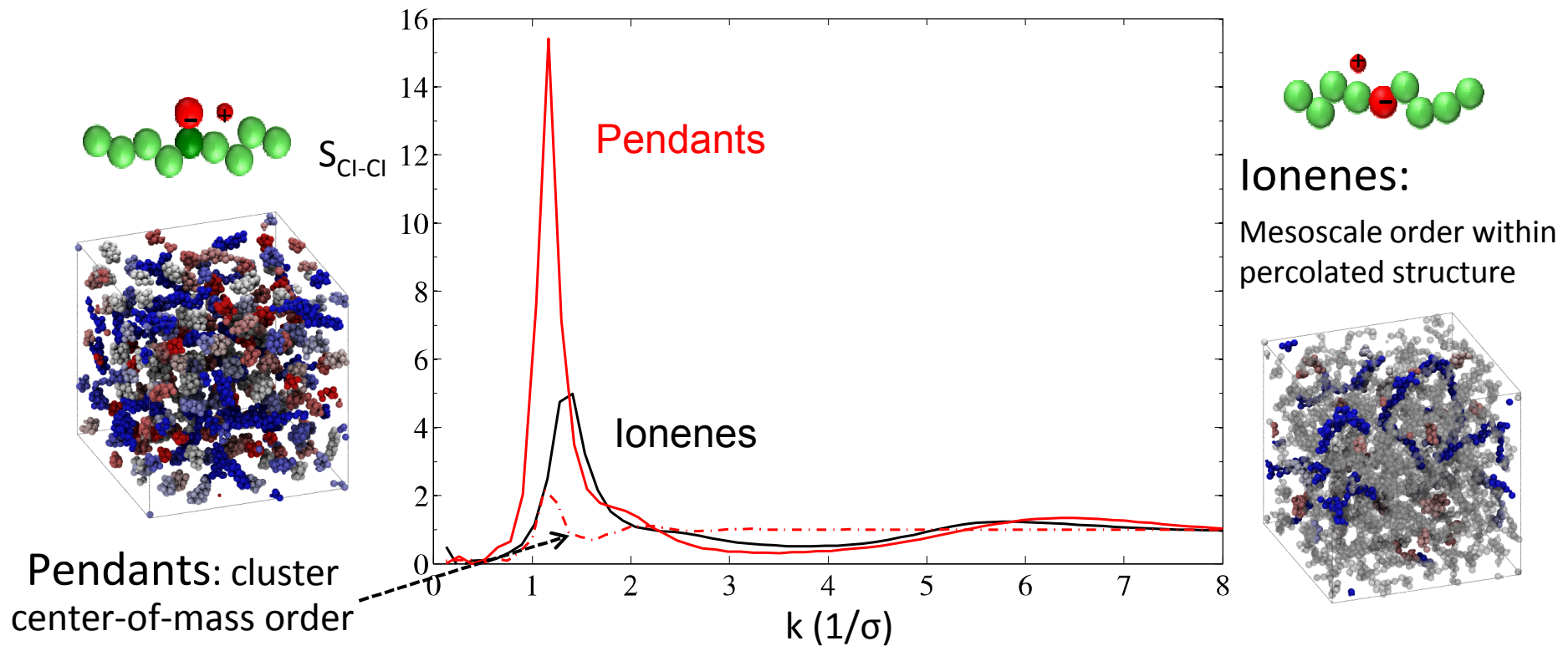


Pendants



Structure Factor (Scattering)

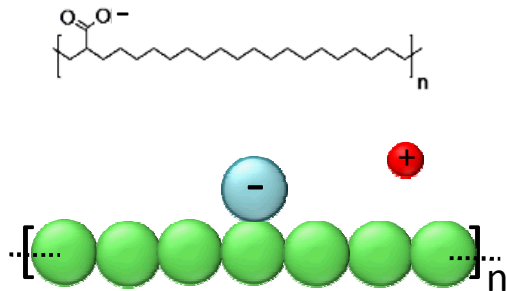
- Ionomer peak for *both* ionenes, pendants
 - Ionene peak: mesoscale order within percolated aggregate
 - Pendant peak: cluster center-of-mass to center-of-mass order
- Experimental peak $\sim 4 \text{ nm}^{-1}$, MD peak $1.2\text{-}1.8 \sigma^{-1} \rightarrow \sim 3\text{-}4 \text{ nm}^{-1}$



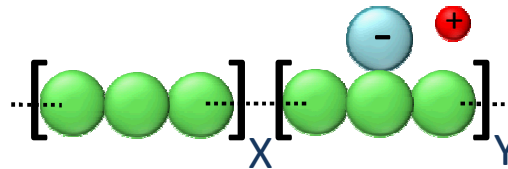
Randomly Spaced Ionomer Model

- random block
 - mimic ROMP
- fully random
 - mimics typical random polymerization

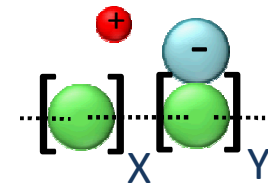
Periodic



Random Block Copolymer



Fully Random Copolymer



connect blocks randomly
vary X/Y

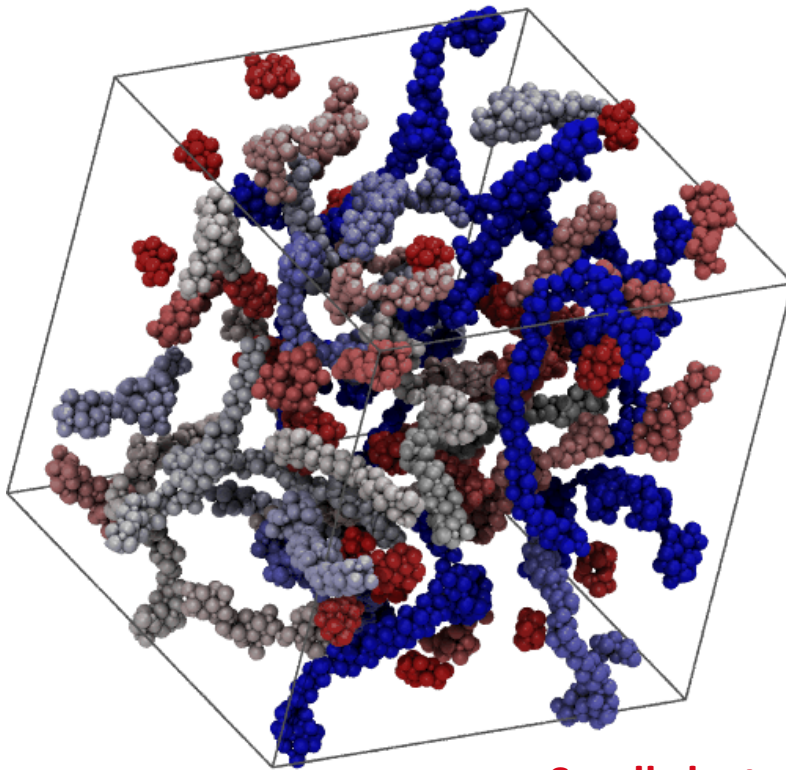
N_{bb} = Number of **b**ackbone **b**eads per charged bead

Aggregate Morphology: Random vs. Periodic

Random Block Copolymer

Pendants: stringy, large clusters

Mean cluster size 87

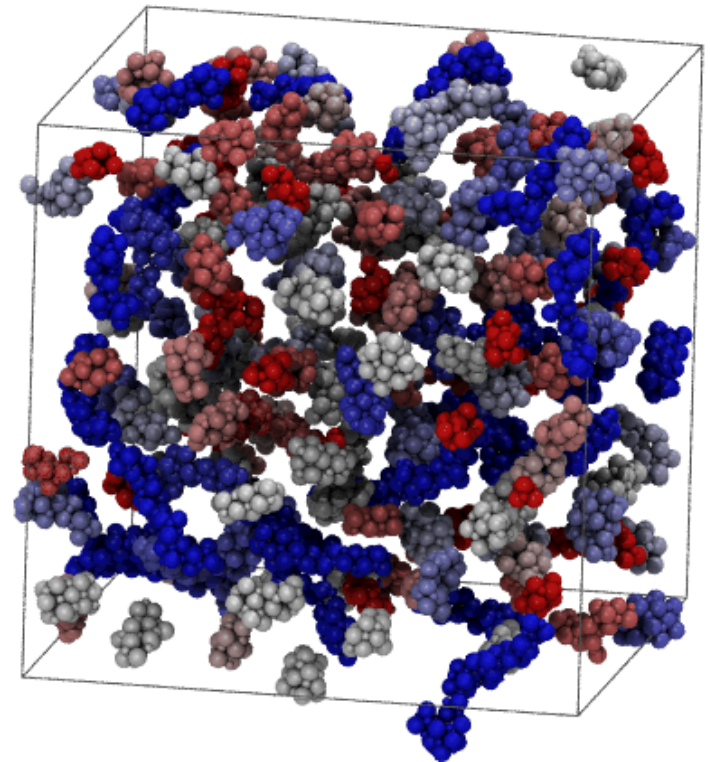


$$\epsilon_r = 4$$
$$N_{bb} = 9$$

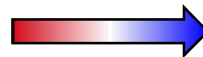
Periodic Pendants:

narrow cluster size distribution

Mean cluster size 31



Small clusters

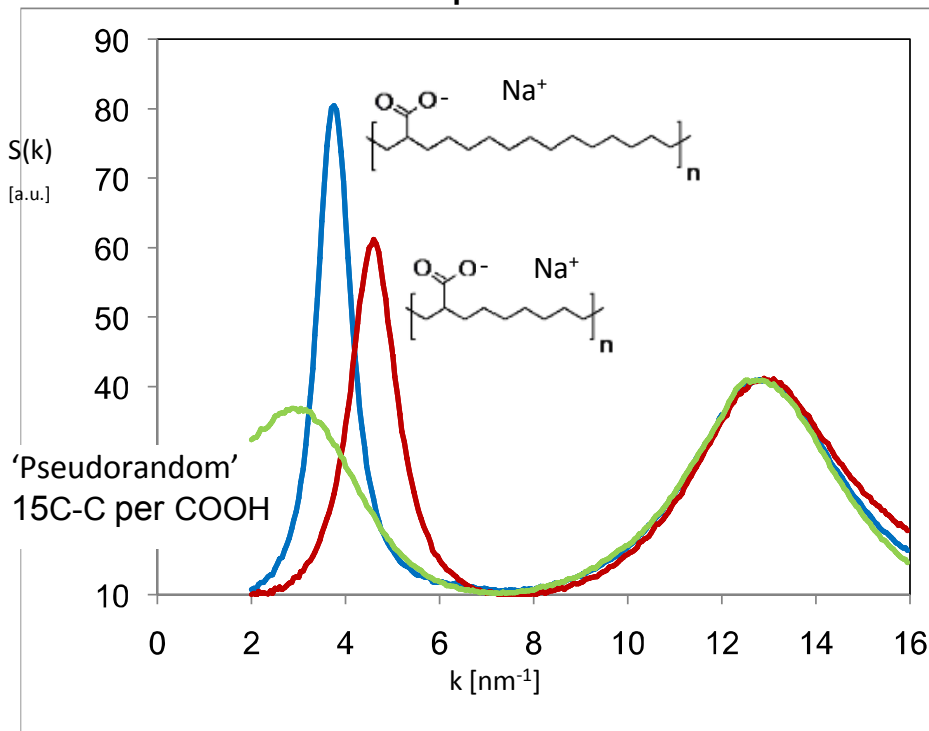


Large clusters

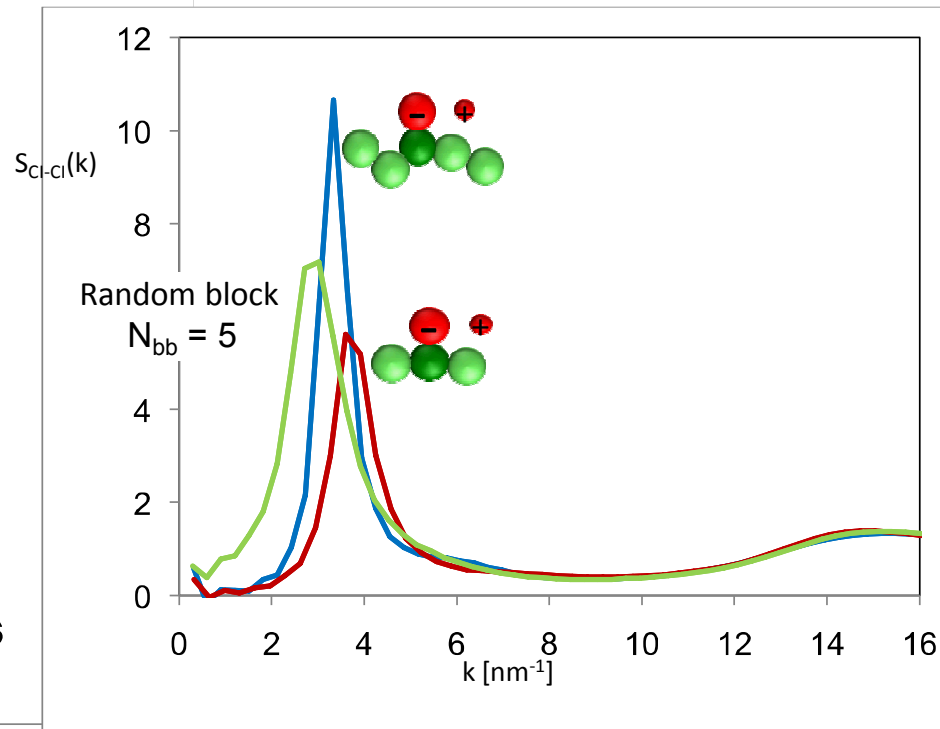
CG MD: Comparison to X-ray Scattering

- Experimental/Simulation Agreement
 - Peak location similar
 - Increasing spacing moves peak to left
 - Random spacing moves and broadens peak

Experiment



Simulation



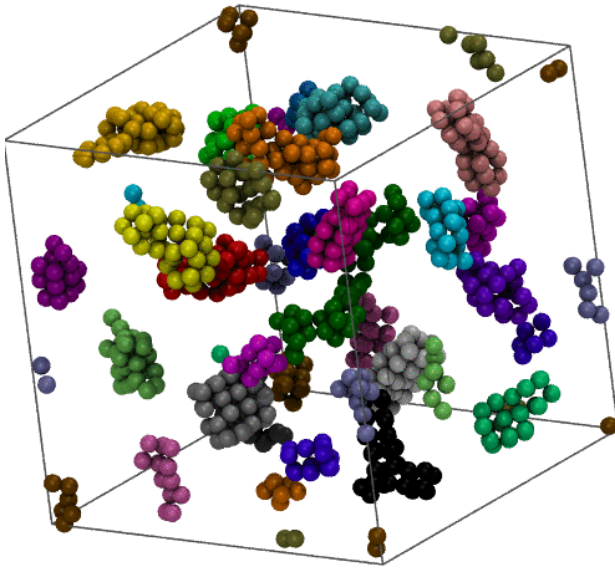
Hall et al., *J. Am Chem. Soc.* (2012)

Cluster Dynamics

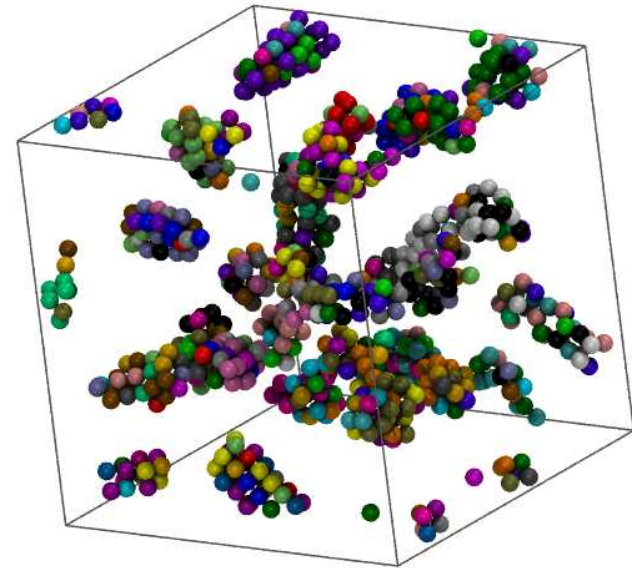
Is there any?

Color distinct clusters by
different color

Start



Finish (10^7 steps later)

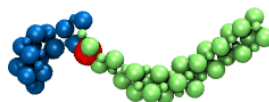
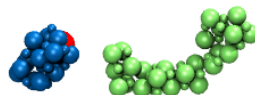


Ions move.

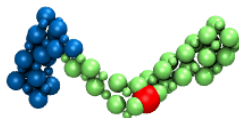
Ion Trajectories

periodic pendants $N_{bb}=9$

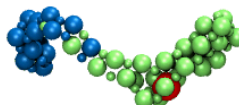
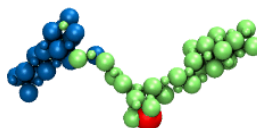
2 separate clusters
Follow one **counterion**



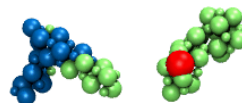
Clusters have collided



Ion has moved to other cluster.
NEVER separated from a cluster.



ions move by cluster
rearrangement/collision



Clusters reform with ion moved

Energies and Cluster Dynamics

+ – pair energy (contact) is 48 kT.

pairs are not likely to separate.

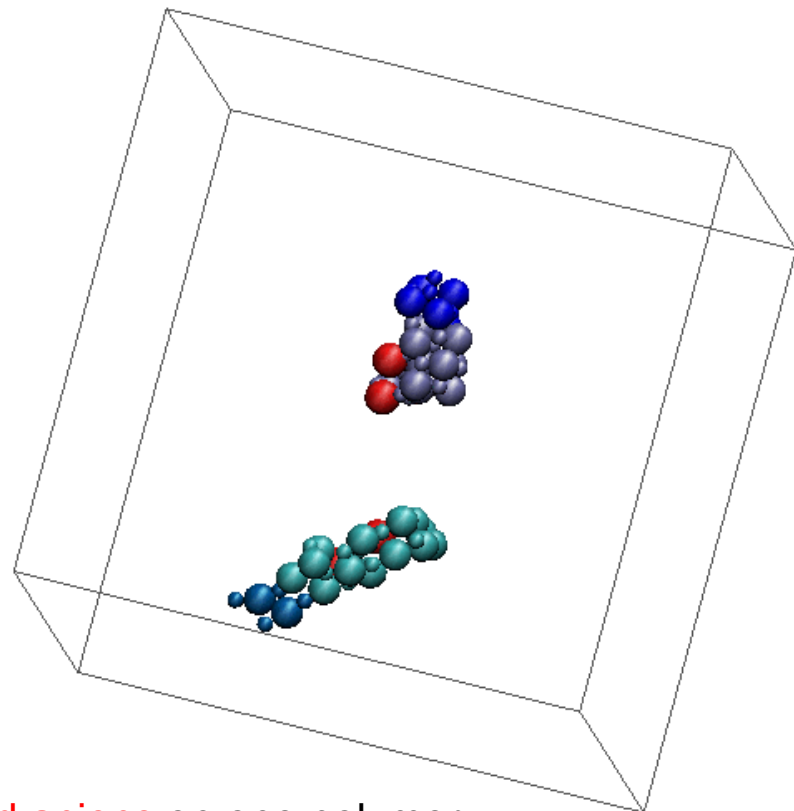
energy to split a cluster is much less
ideal, 2D crystallite has a separation energy of
only 20 kT:



simulations show clusters are flexible (they're
liquids after all) and the energies will be less
than these crystallite calculations.

ions move a lot within a cluster

Pendant (discrete clusters)



Red anions on one polymer.

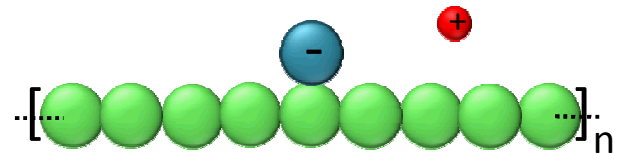
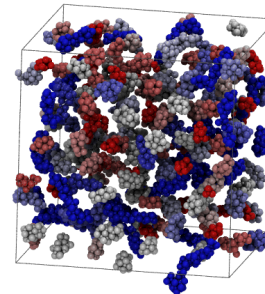
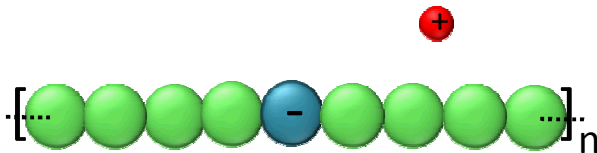
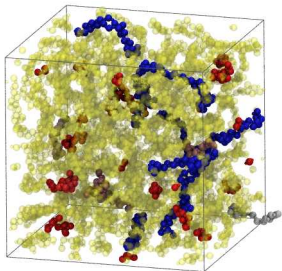
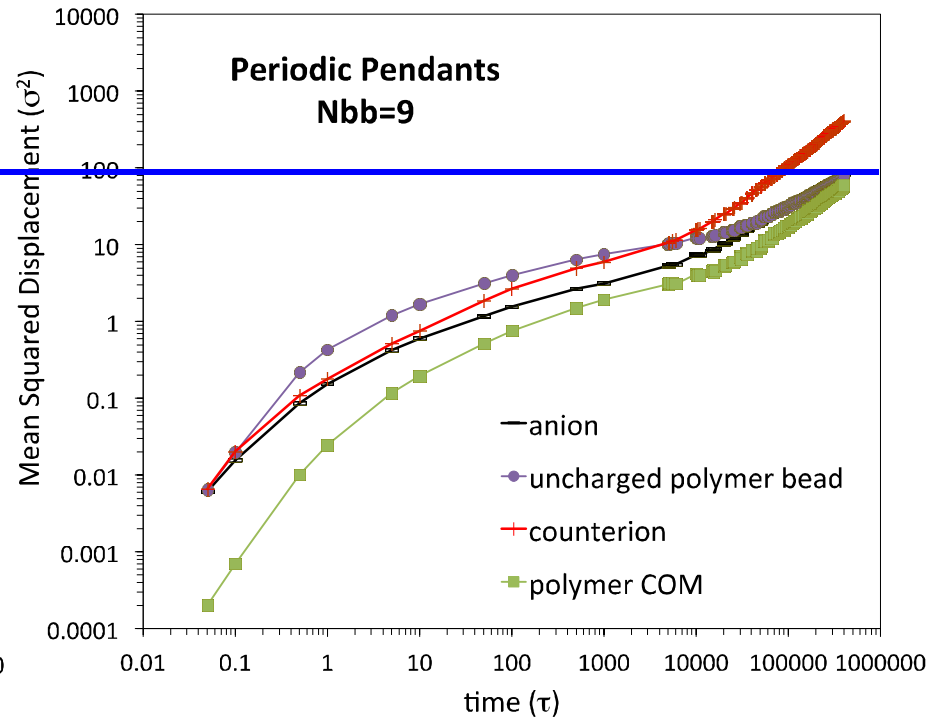
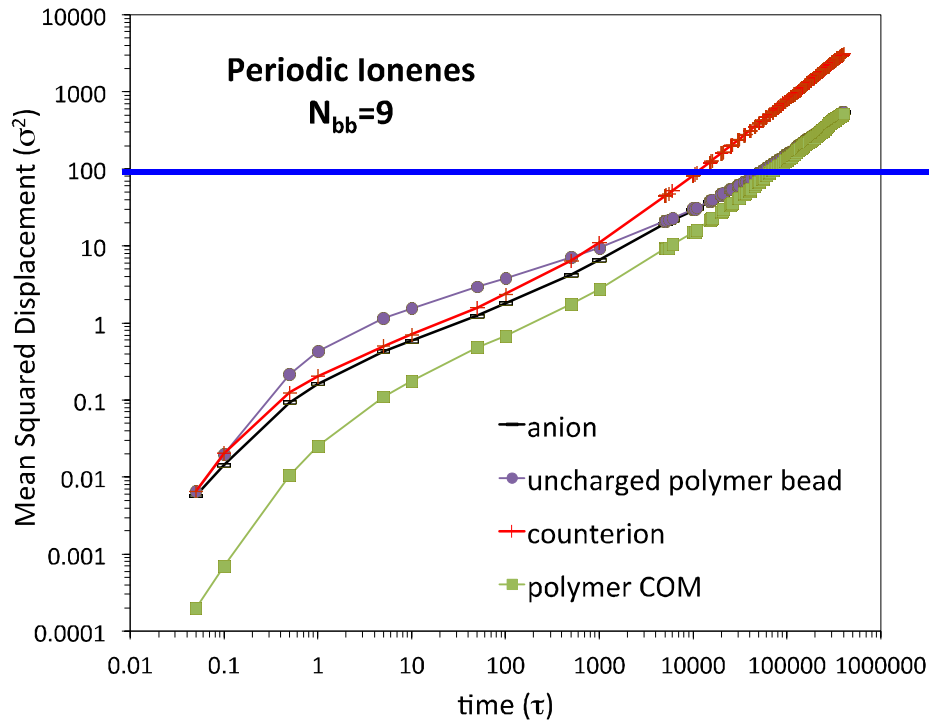
Blue ions initially within 3σ of red anions.

Other ions which temporarily come within 3σ
are transparent.

5000 τ X million time steps

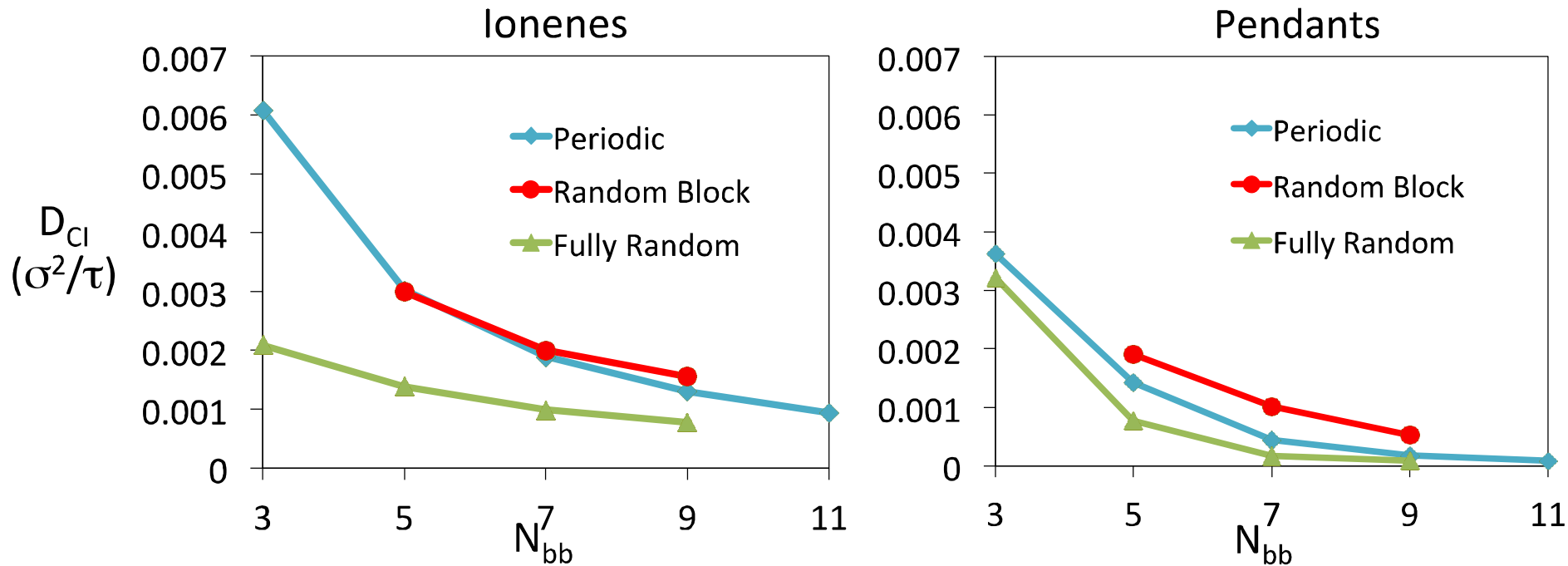
Mean Squared Displacements

- Ionenes, pendants similar at short times
- Pendants slower but qualitatively similar at long times



Counterion Diffusion Constants

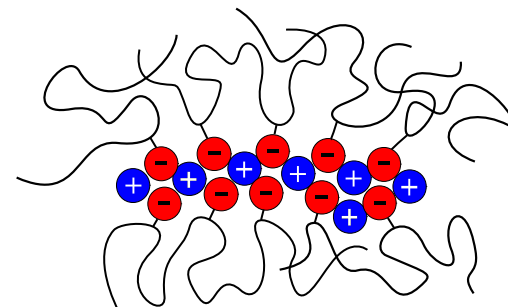
- Ionenes conduct better than pendants
- Greater concentration of ions increases diffusion
- Blocky random copolymerization increases diffusion



$\epsilon_r = 4$

The New Picture

- Aggregates are stringy
 - + – + – ordering
 - polymer backbone constraints
- Counterion influences structure (partial neutralization)
 - Na^+ , Li^+ : medium-sized, stringy aggregates
 - Cs^+ : Percolated network
 - Zn^{2+} : small, isolated clusters
 - Small ion- O^- clusters are bridged by $-\text{OH}$ and $=\text{O}$ groups
- molecular architecture important
 - pendant vs ionene
 - isolated aggregates for pendants or large spacing
 - percolation for ionenes or short spacing
- ion motion by cluster rearrangement
- ions diffuse faster in percolated morphologies



Acknowledgments



Dan Bolintineanu



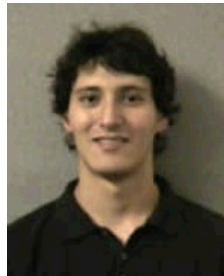
Lisa Hall
(now at OSU)



Mark Stevens



Todd Alam



Karen Winey
Michelle Seitz (now at DSM)
Francisco Buitrago
University of Pennsylvania



Janelle Jenkins

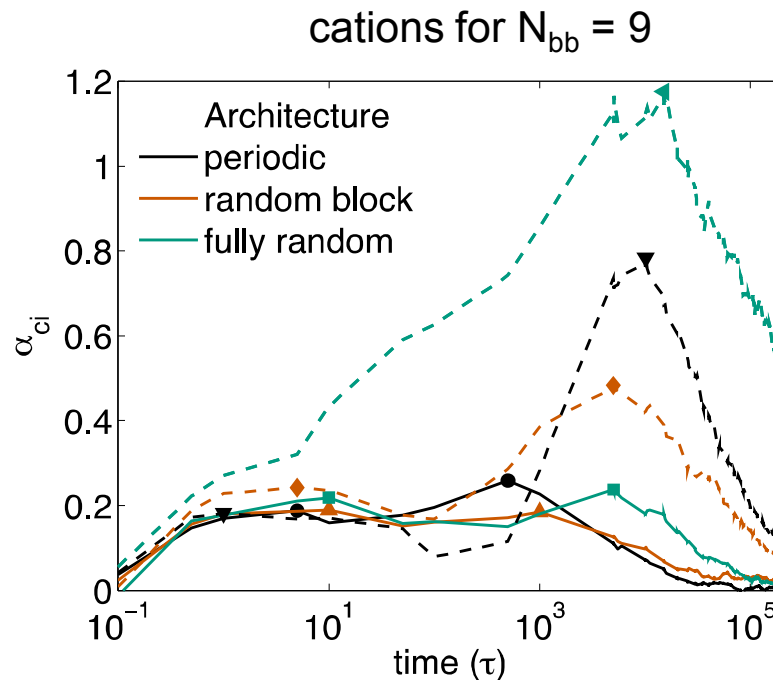
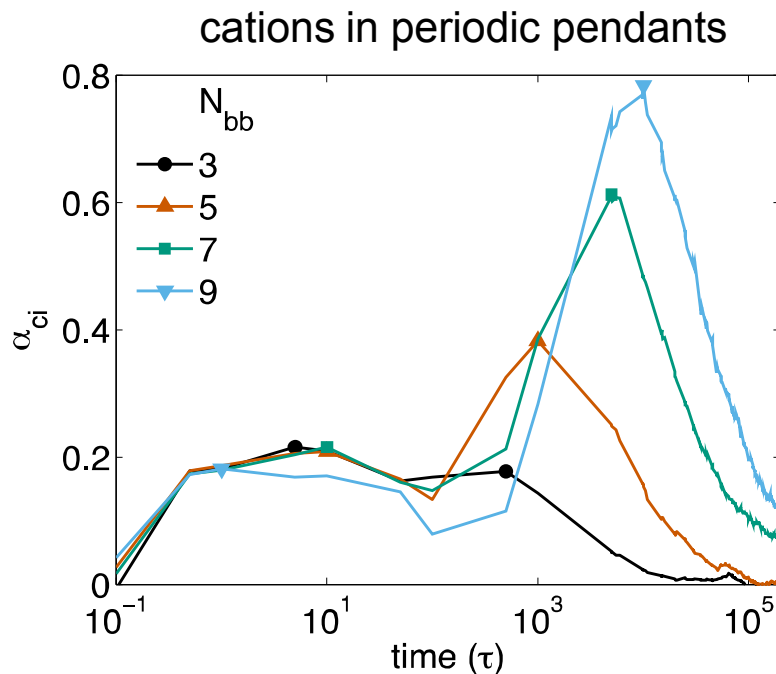


The "Ionomers" LDRD team
Funding: Sandia LDRD Program
CINT
NERSC



Ion Dynamics

non-Gaussian parameter $\alpha(t) = \frac{3 \langle (r(t))^4 \rangle}{5 \langle (r(t))^2 \rangle^2} - 1$



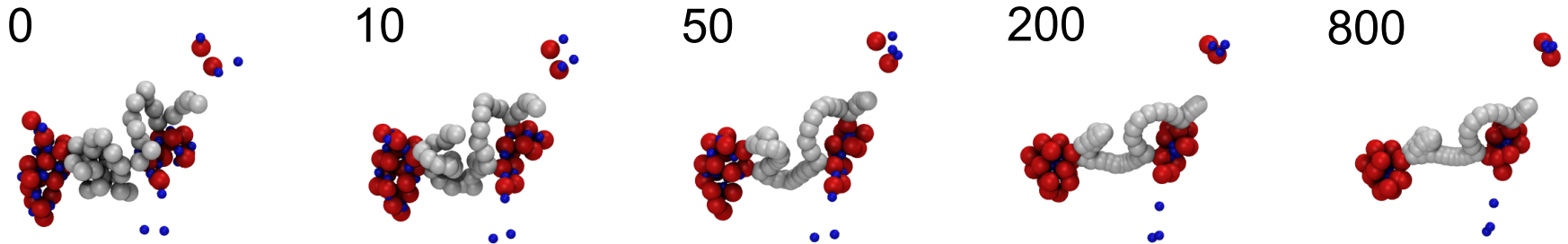
indicative of 2 time scales:

- local motion in clusters
- slower rearrangement between clusters

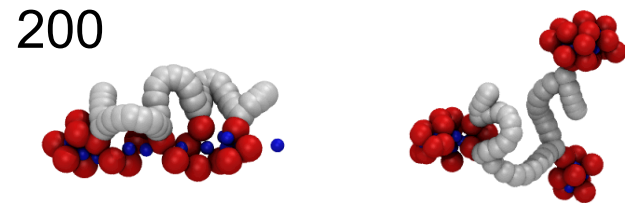
Average Local Structure

one polymer (white, red anions) and nearby ions (red anions, blue counterions)
 $N_{bb}=9$, frames are 1000 steps apart

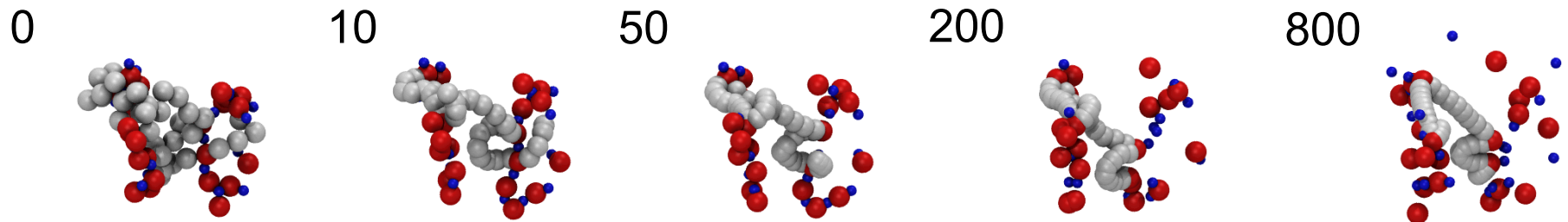
periodic pendant, frames averaged:



other periodic pendant
examples



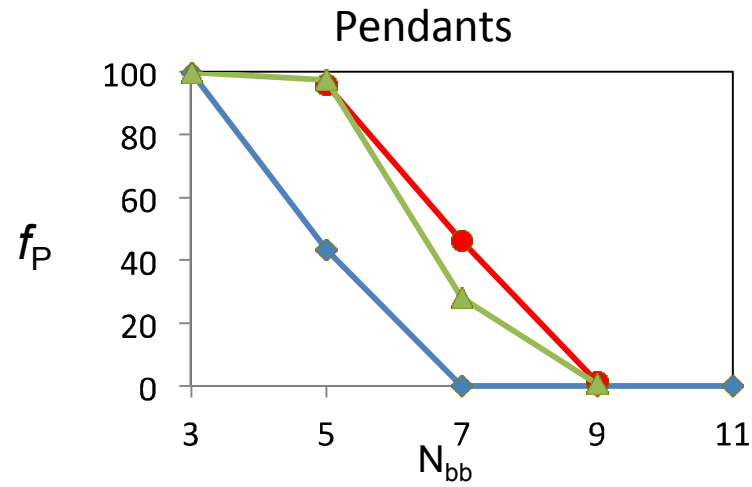
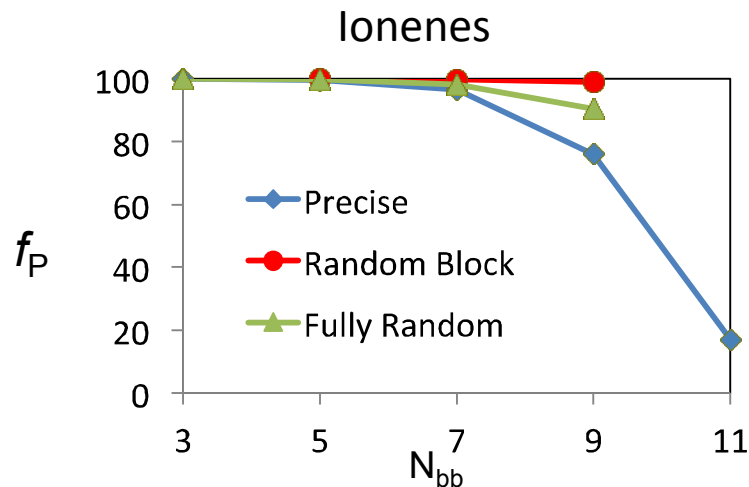
periodic ionene, frames averaged:



Effect of Architecture on Clustering

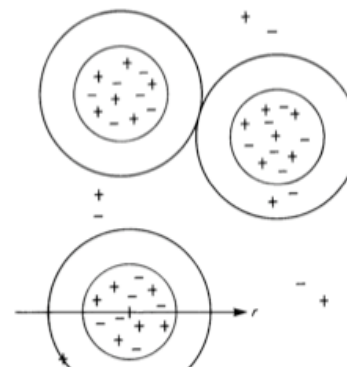
- Ionene architecture, randomness increases percolation
- Randomness usually increases non-percolated cluster size

Fraction in percolated cluster

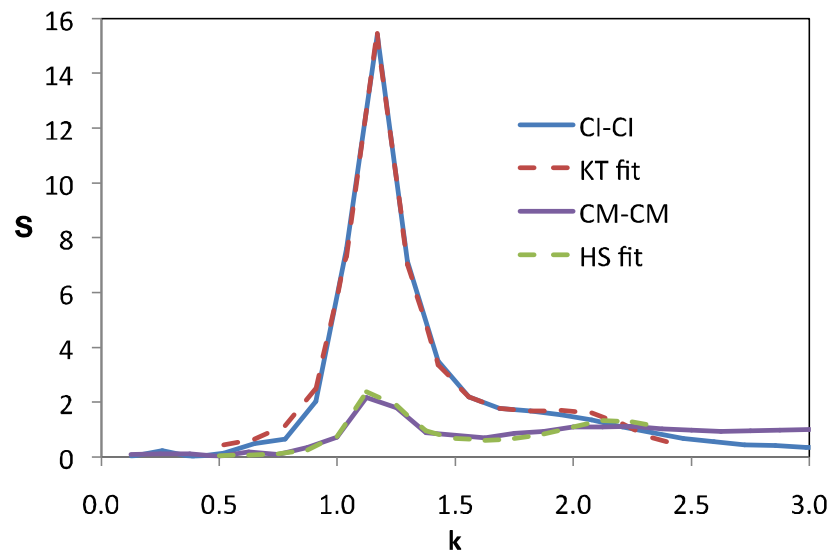


Fit to Scattering

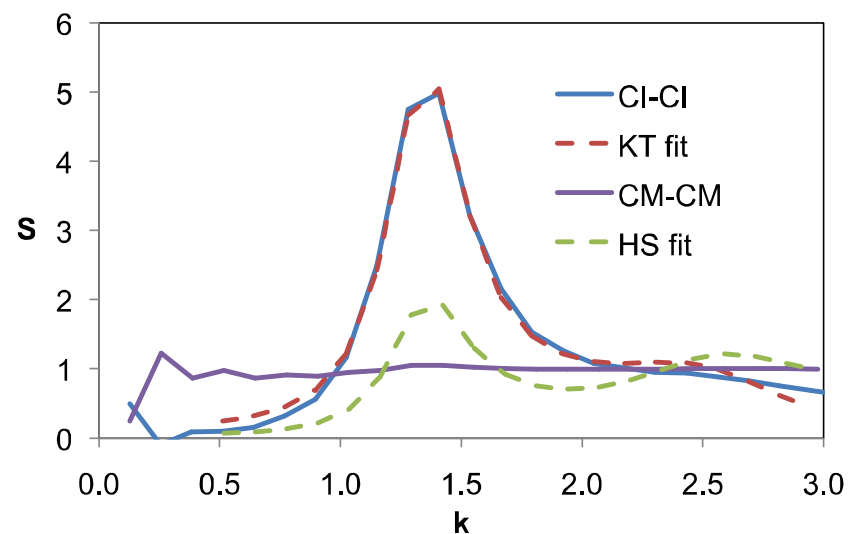
- modified hard sphere model
 - fits pendants well
 - fit parameters match physical meaning
 - fits ionenes well
 - fit parameters don't match



pendants



ionenes



Equilibration of Simulations

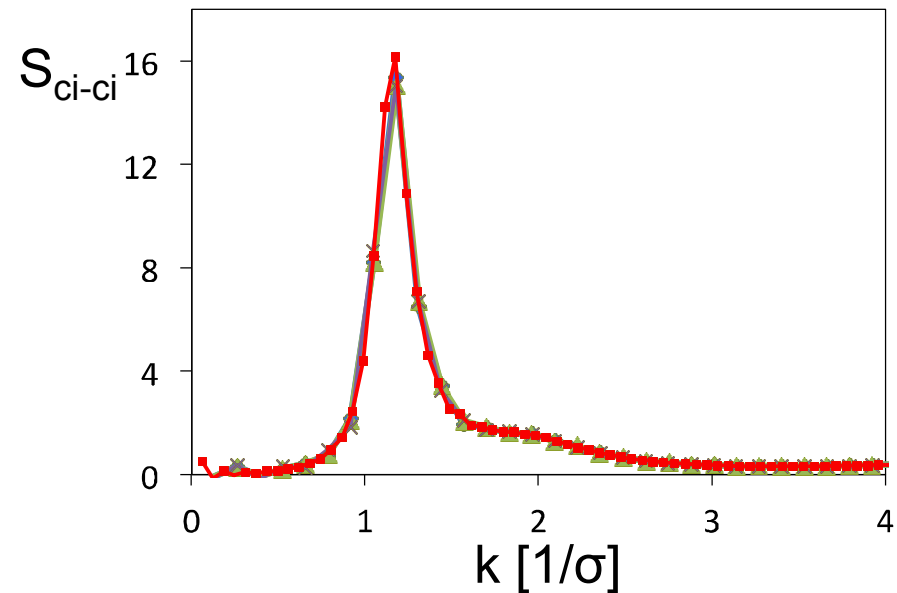
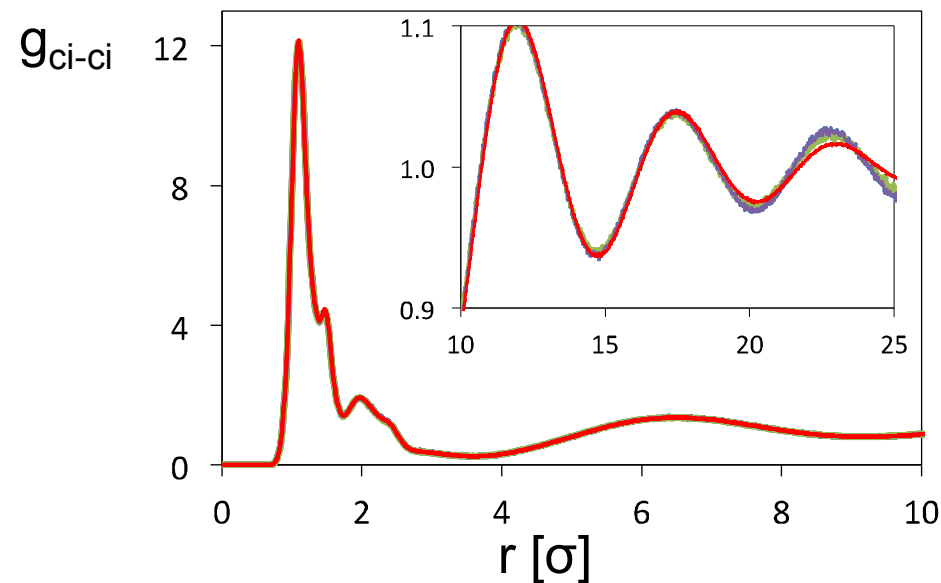
- From random initial configuration, equilibrate for 10^7 steps
- MSD of polymer centers of mass during equilibration $> R_g^2$
- Dynamics data collection start at 3×10^7 steps

$\epsilon_r = 4$, $N_{bb} = 9$ pendants: one of the slowest

no change in structure with:

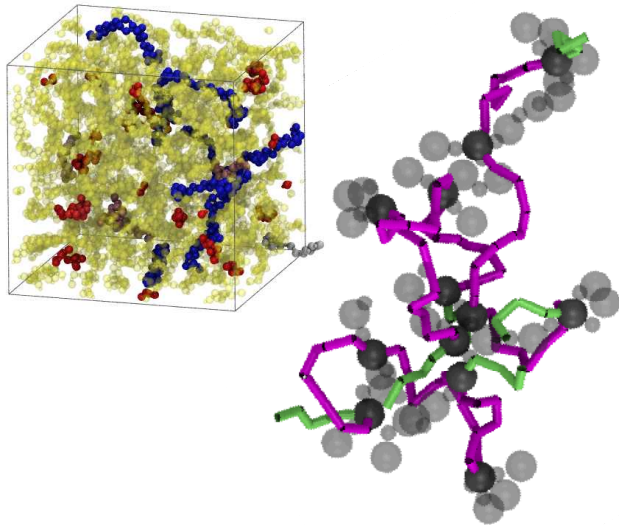
- equilibrating 4 times longer
- using twice the box length
- starting from a different random initial configuration

— Longer equilibration
— Configuration A
— Configuration B
— Larger box



Polymer Morphology

Ionenes



3 nearby polymers

Charged beads

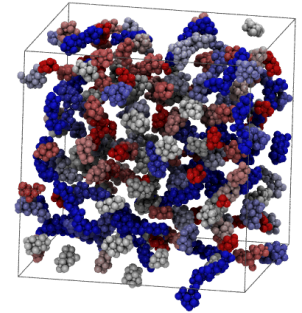
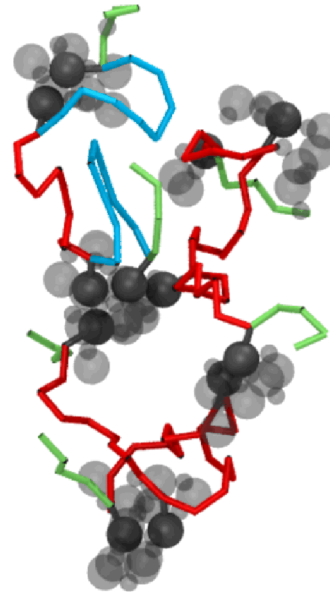
End segments

'Loops'

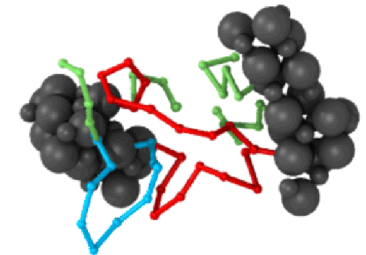
Close loops

Bridges

Pendants



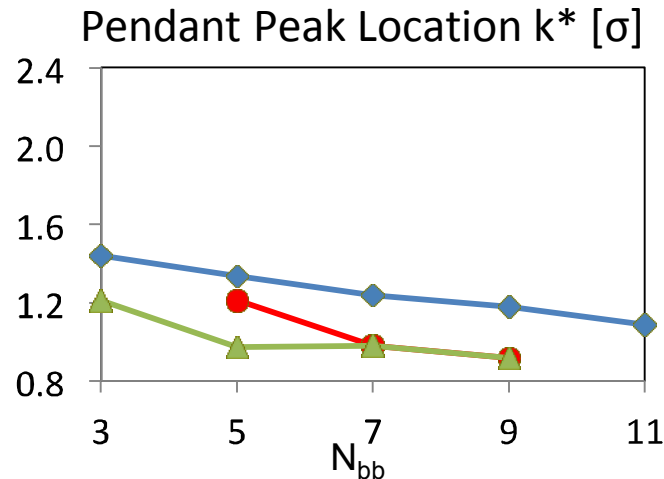
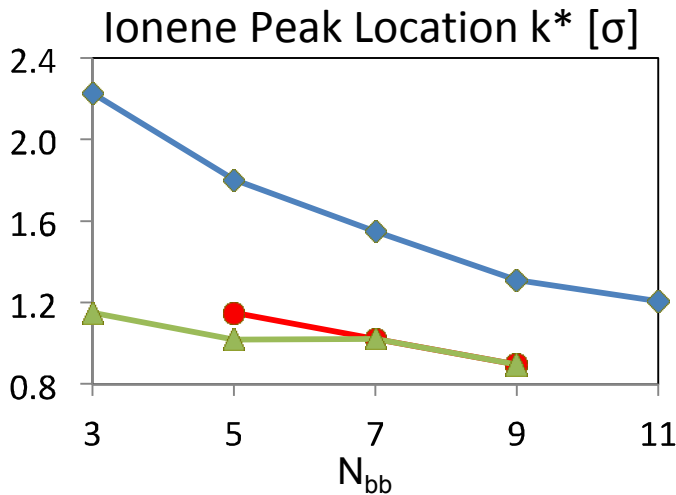
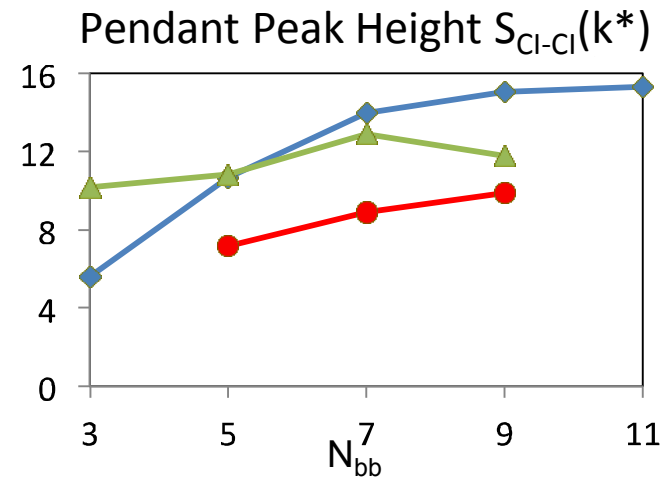
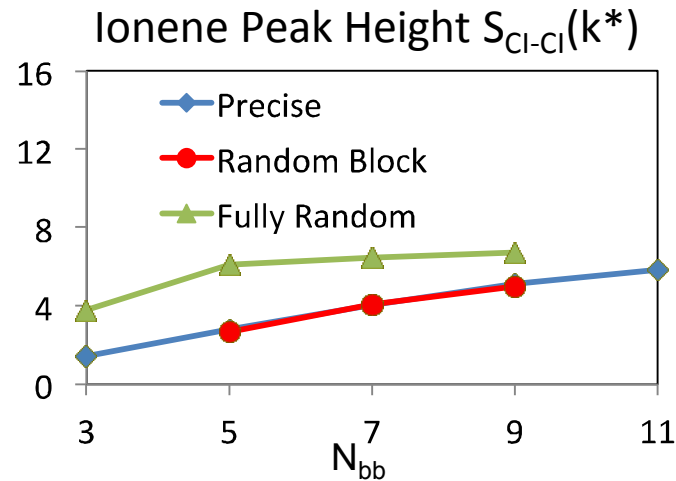
Polymer segments
between 2 clusters



- Architecture determines aggregate morphology
 - Ionenes cannot easily form a compact cluster
 - Pendant backbone more separated from clusters
- Cluster-cluster length scale set by bridges?
 - Pairs of close loops or tails can set similar length scale
 - Decreasing backbone spacing leads to closer aggregates

Effect of Architecture on Ionomer Peak

- Pendants have larger peak than ionenes
- Randomness moves peak to lower wavevector

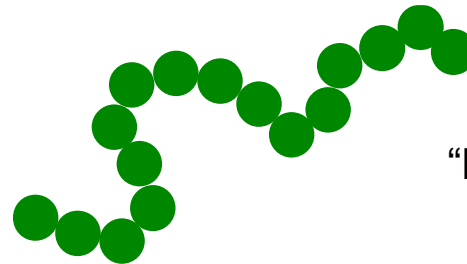


$$\epsilon_r = 4$$

Molecular Dynamics Simulations

- put atoms in a box
- solve $F = ma$ for each atom
- calculate statistical properties (averages) over trajectories

bead-spring polymer model
(Kremer & Grest, 1990)

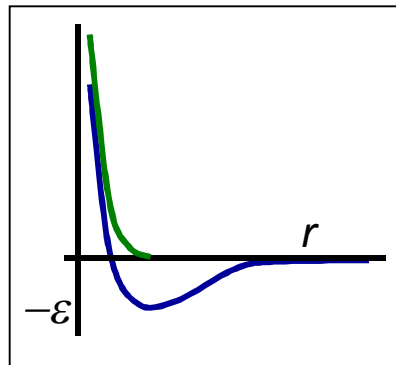


“bead” diameter σ

interactions between all “beads”

Lennard-Jones potential:

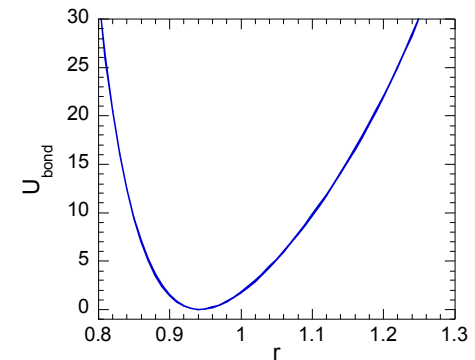
$$u_{LJ} = 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right]$$



interactions between bonded beads

FENE springs $u(r) = -kR_0^2 \ln \left(1 - (r / R_0)^2 \right)$

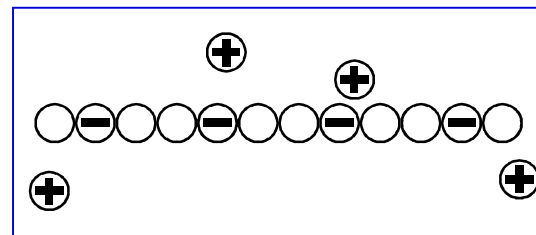
$$U_{\text{bond}} = u_{LJ} + u$$



Ionomer MD Simulations

Coulomb interactions

$$U(r) = \frac{q_1 q_2}{4\pi\epsilon_0\epsilon r}$$



counterions: single beads, size 0.5σ

NVT ensemble: Langevin thermostat

$$f_i = -m_i\Gamma\nu_i + W_i(t)$$

noise W sets temperature

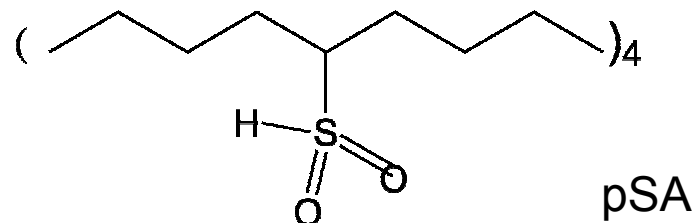
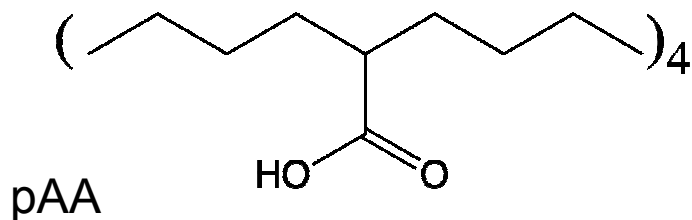
System

- 800 chains of 35-36 beads; 4-12 charges per chain
- 1 counterion per charged bead;
- density $\rho\sigma^3 = 0.7$ (polymer melt)

LAMMPS: open source MD code from Sandia

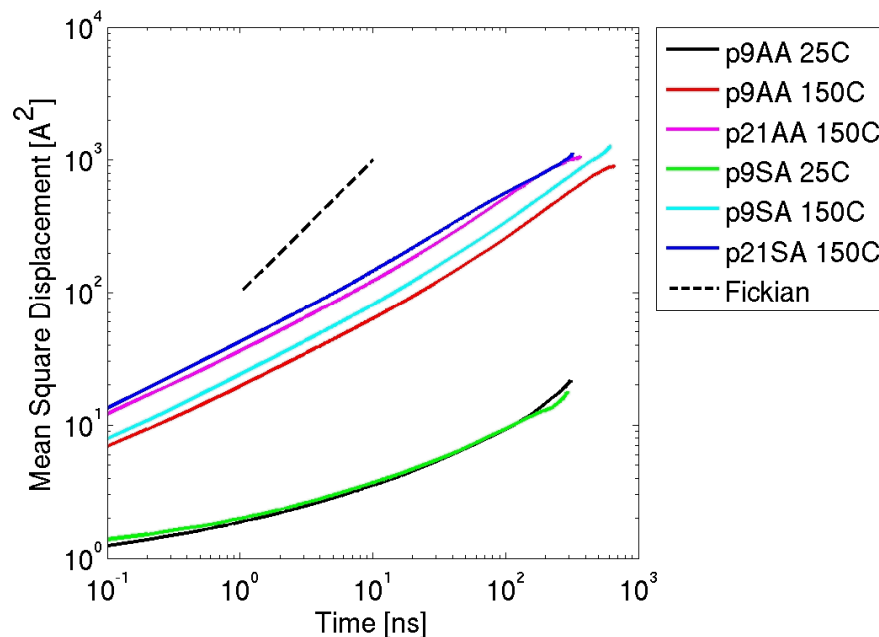
<http://lammps.sandia.gov/>

Acid Copolymer Simulations



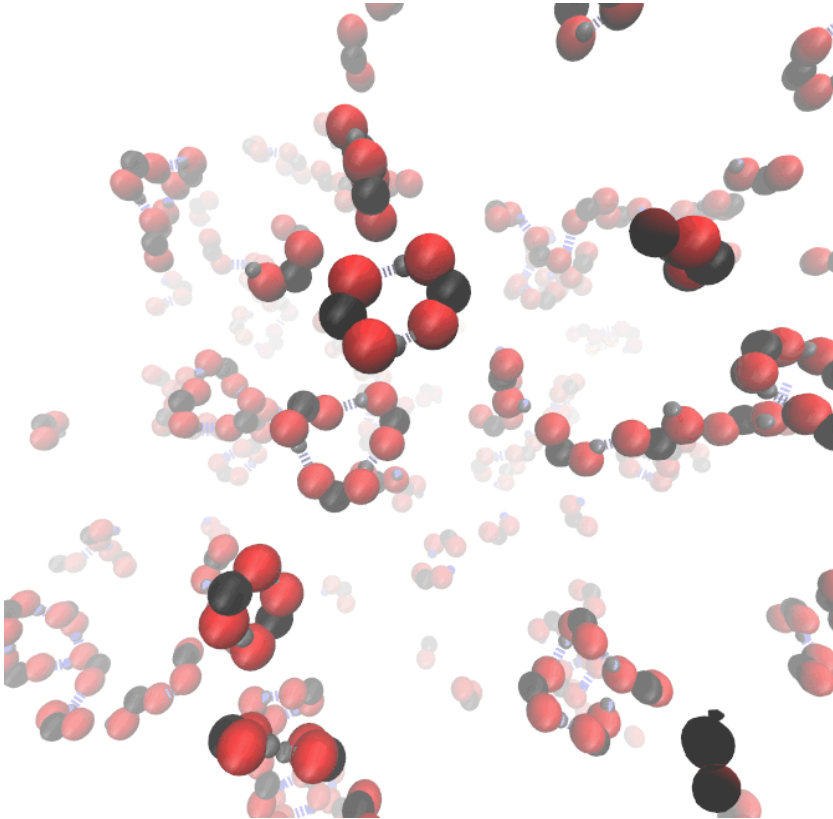
- all-atom OPLS force field
- p9AA, p9SA
 - 128 polymers
- p21AA, p21SA
 - 64 polymers
- box size 55 Å³
- 150 °C

slow dynamics!
acid H diffusion



H-bonded Aggregates

p21AA



p21SA

