



# Simulation of Ionic Aggregation and Ion Dynamics in Ionomers

Amalie L. Frischknecht

January 24, 2013



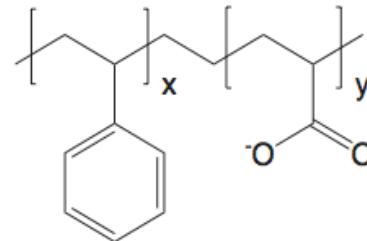
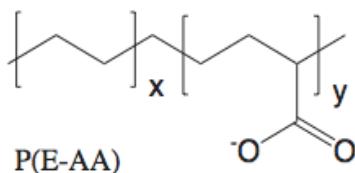
*Exceptional  
service  
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interest*



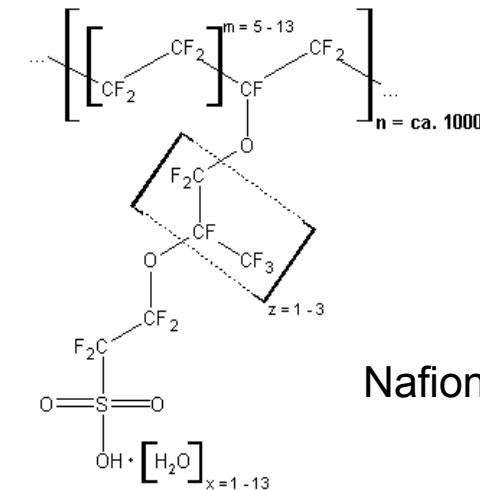
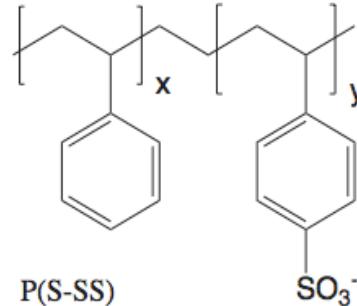
Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

# What is an ionomer?

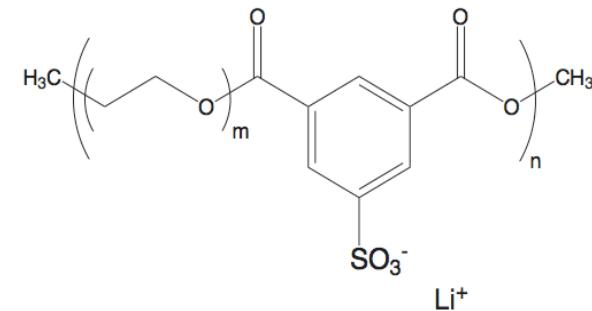
a copolymer  
with a small fraction  
of covalently-bonded ionic groups



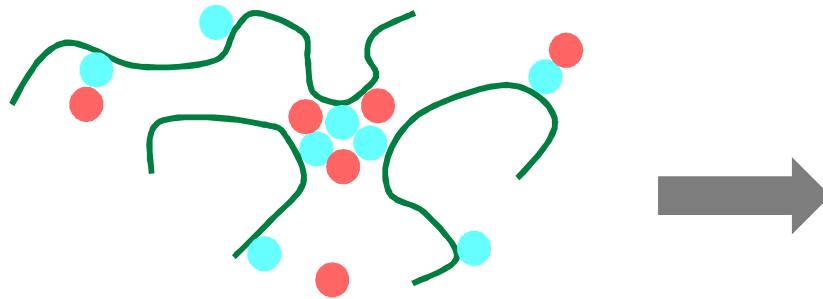
### P(S-MAA)



Nafion™

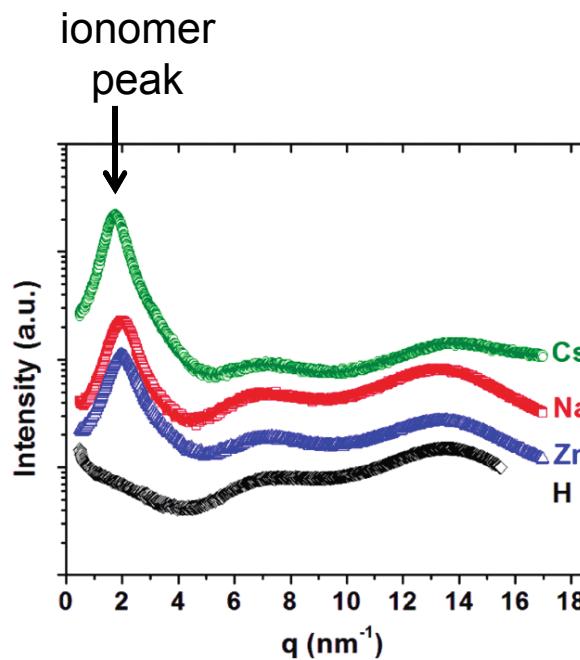
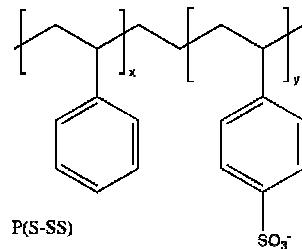


# Aggregates in Ionomer Melts



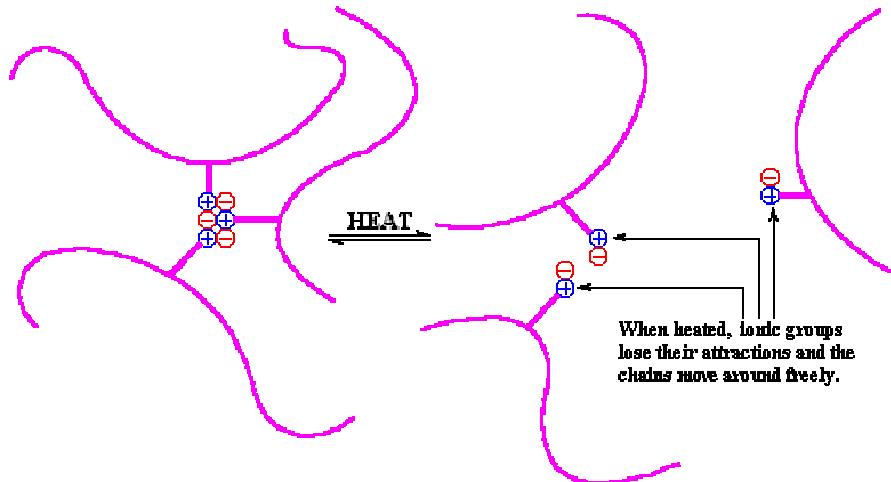
- “ionomer peak”
- ubiquitous
- low wavevector peak in scattering
- from inter-aggregate scattering

Coulombic forces favor aggregates  
strong pair energy,  $\approx 40 \text{ kT}$   
polymer entropy limits size



# Applications of Ionomers

## thermoplastic elastomers



- low T: ionic aggregates behave like crosslinks
  - material is elastic
  - high strength
- high T: ionic aggregates break up
  - material flows (is a liquid)

- golf balls: covers, mantles, intermediate layers, ...
- coatings
- packaging (e.g. foods, cosmetics, ...)
- clear plastic parts
- modifiers in other plastics

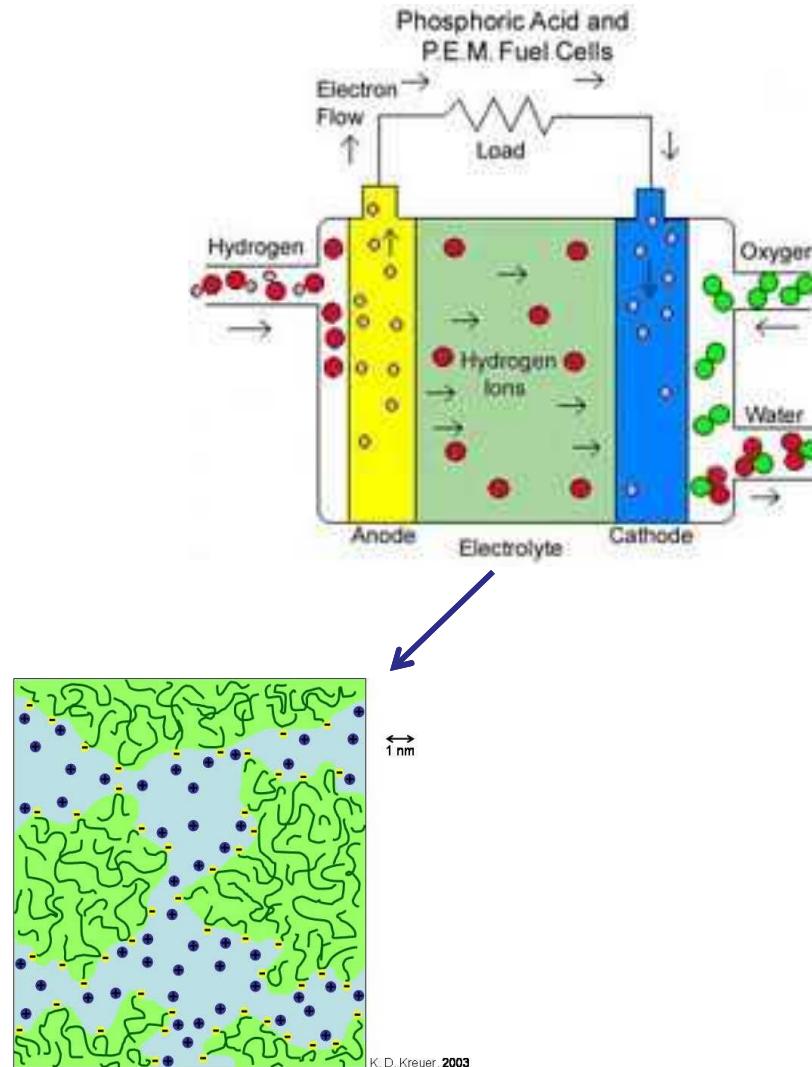
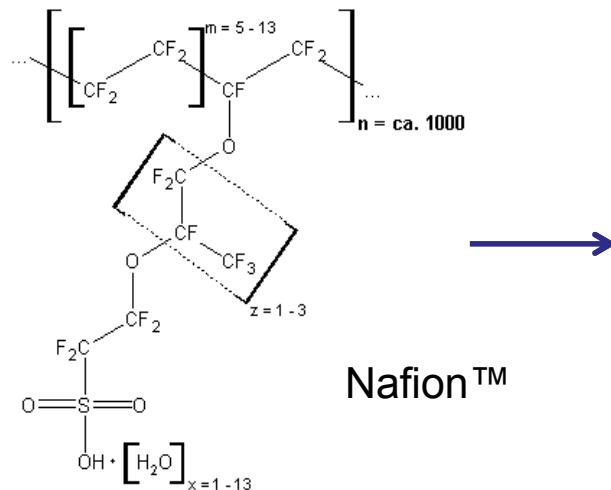


DuPont™ Surlyn®

# Membranes

ion-selective membranes  
typically in water

- water purification
- fuel cells



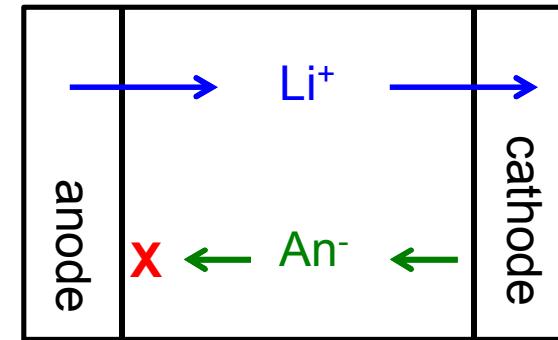
# Possible Application: Batteries

Issues with current electrolytes in Li-ion batteries:

- organic solvents
- PEO + lithium salts + solvent
  - need containment
  - flammable!



- solvent free PEO + salt
- conductivity dominated by anions
- salt concentration at electrodes
- extra heating



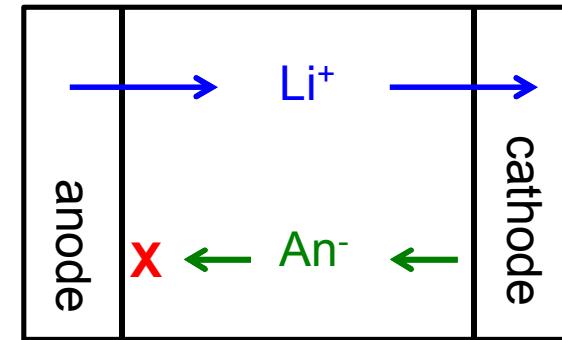
# Possible Application: Batteries

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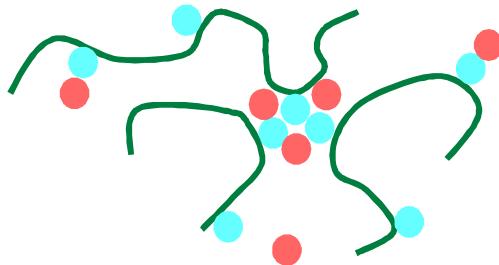
- solvent free PEO + salt
- conductivity dominated by anions
- salt concentration at electrodes
- extra heating



ionomers as next generation electrolytes?

- safer: no solvent
- serve as electrolyte & separator
- less packaging
- improved electrochemical stability
- higher efficiency: single ion conductors

# Ionomer Conductivities



- conductivity too low
  - needed for Li-ion batteries:  $\geq 10^{-3}$  S/cm
  - Li salt + solvent:  $\approx 10^{-2}$  S/cm
  - gel polyelectrolytes: 1-3  $10^{-3}$  S/cm
  - ionomers: generally  $< 10^{-5}$  S/cm
- why?
  - few mobile ions (ion pairs instead)
  - often get ionic aggregates

Need for electrochemical apps:

- relation between molecular architecture & morphology
- effects of morphology on ion transport
- understanding of ion transport mechanisms

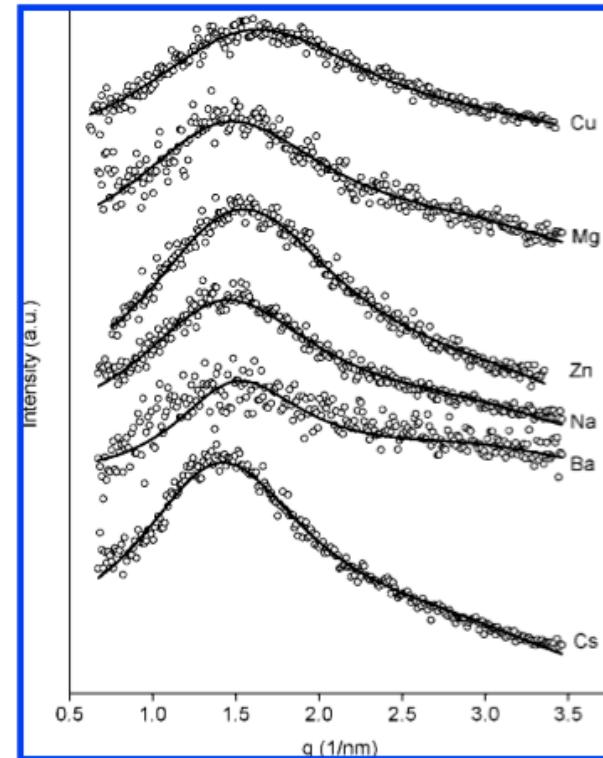
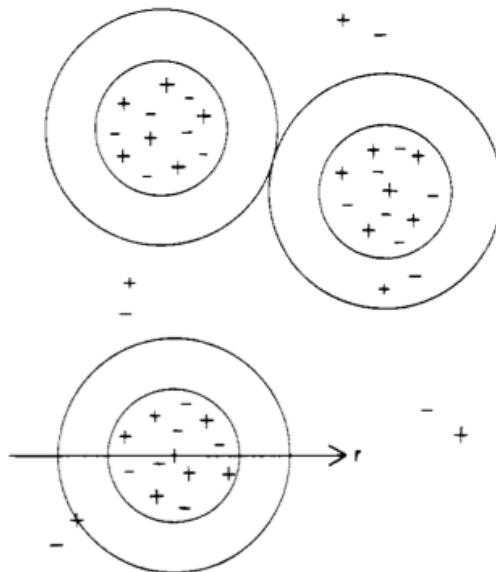
# Historical View of Ionomer Melts

- spherical ion-rich aggregates
- surrounded by ion-poor polymer
- arranged with liquid-like order



“ionomer peak”

- ubiquitous
- low wavevector peak in scattering
- from inter-aggregate scattering



Zhou et al. *Macromolecules* (2008) vol. 41 (16) pp. 6134-6140

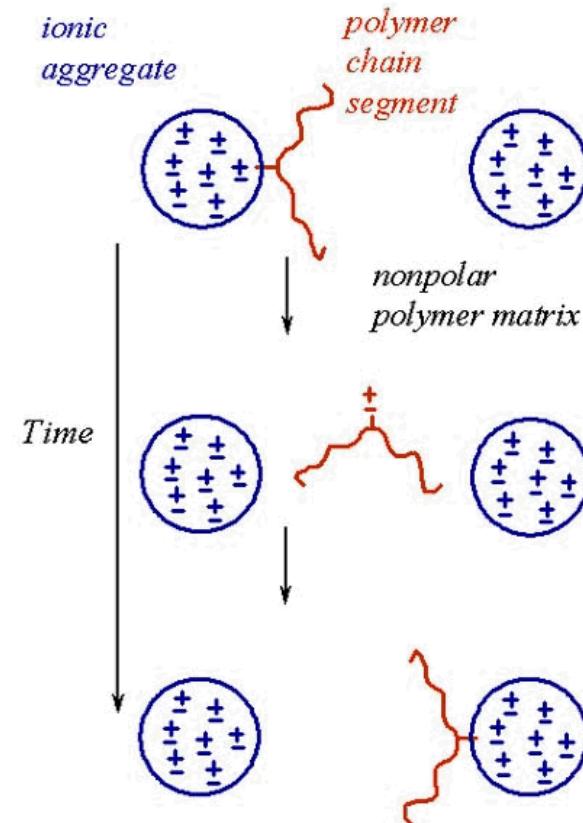
D. J. Yarusso; S. L. Cooper; *Polymer* 1985, 26, 371-378.

PSS ionomers

# Historical View of Dynamics

- requires traversing low dielectric polymer matrix
- large activation energy barrier
- ion **pairs** “hop” between aggregates

this is SLOW

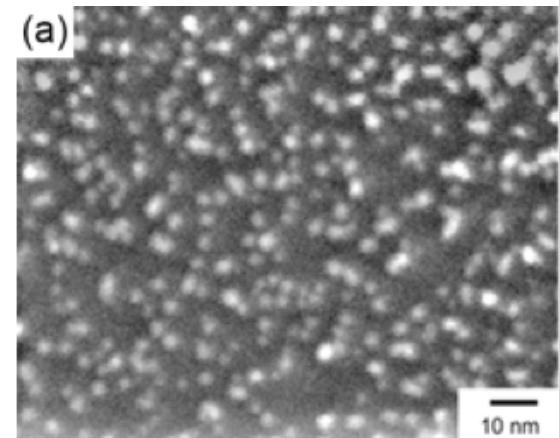


<http://www.princeton.edu/cbe/people/faculty/register/group/research/ionomers/ionomer-melt-rheology-and/>

# Outstanding Questions

- What do the aggregates look like, exactly?
  - composition
  - size
  - shape
- What's the dependence on polymer architecture?
  - spacing between charged groups
  - cations
  - anions
- How does ion association affect dynamics?

spherical aggregates



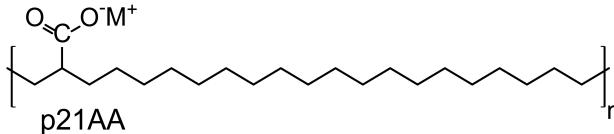
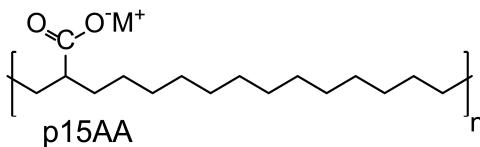
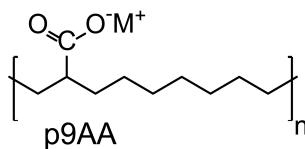
Karen Winey  
U Penn

Difficult to measure local  
structure experimentally.

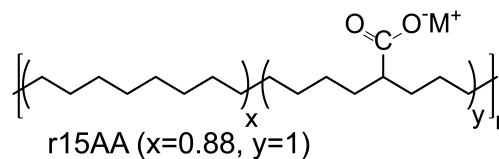
Can simulations resolve issue?

# New Materials

# Acyclic Diene Metathesis (ADMET) Precise Copolymer



# Ring-Opening Metathesis Polymerization (ROMP) Pseudo-Random Copolymer



## precise polymers:

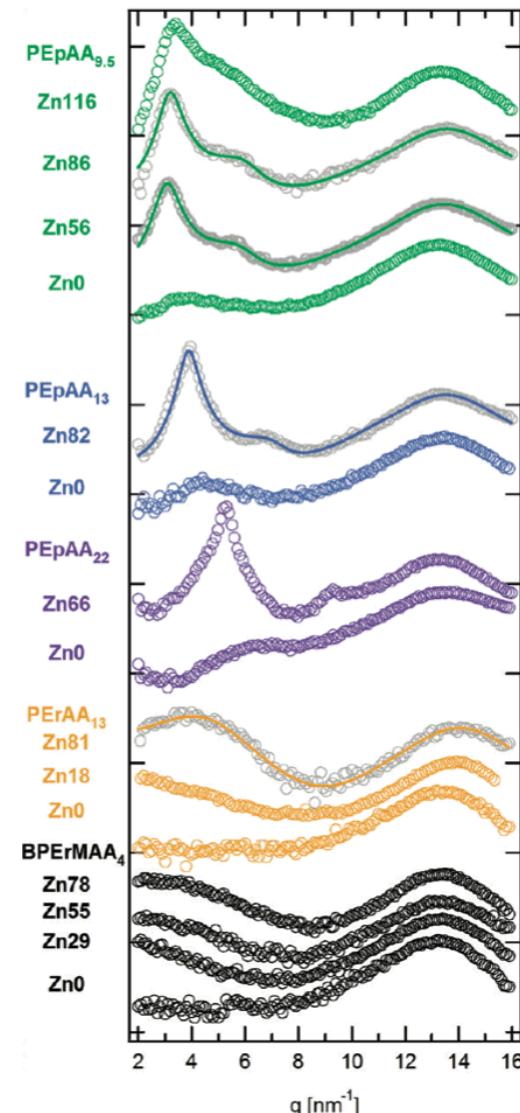
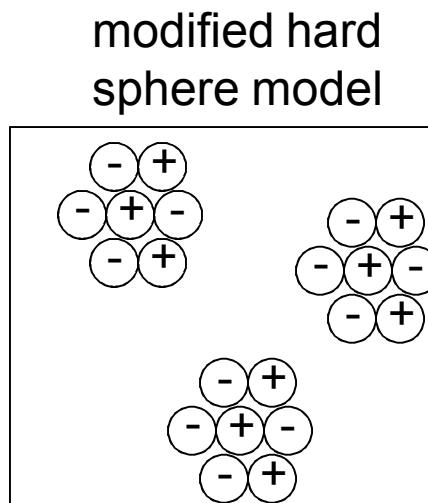
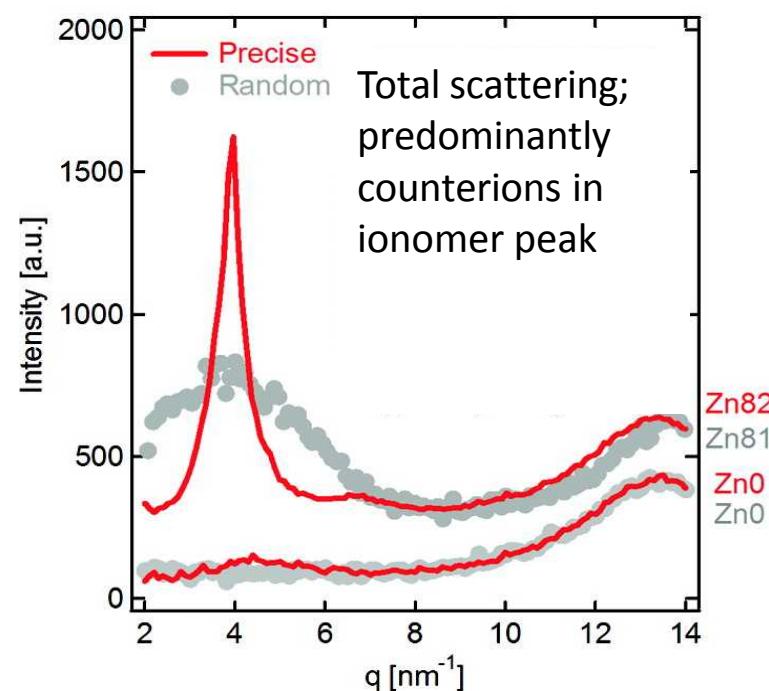
- acid group every 9, 15, 21 carbons
- swap H for  $Zn^{2+}$ ,  $Li^+$ ,  $Na^+$ ,  $Cs^+$
- nomenclature: pxAA-y%M



Ken Wagener,  
University of Florida

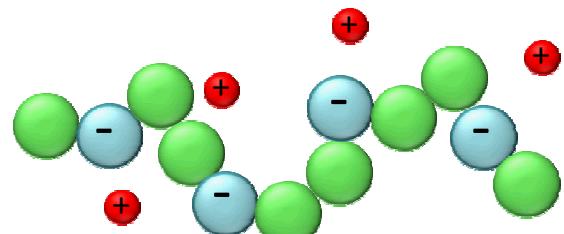
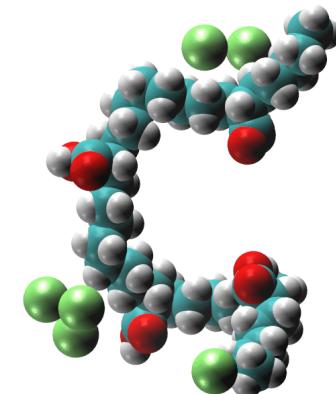
# Zn-neutralized Precise Ionomers

much more defined peak from precise ionomers  
ideal for comparison to simulation



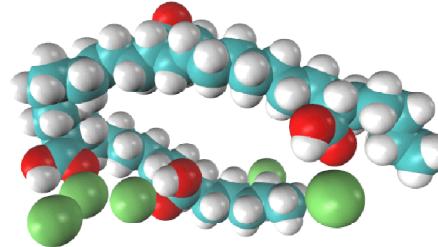
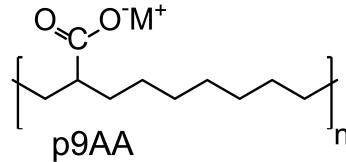
# Outline

- atomistic simulations
  - varying cations:  $\text{Li}^+$ ,  $\text{Na}^+$ ,  $\text{Cs}^+$ ,  $\text{Zn}^{2+}$
  - varying neutralization
  - compare directly to experiment
  - limited dynamics
- coarse-grained simulations
  - morphology
  - dynamics



# Atomistic Ionomer Simulations

- pAA materials:



- Variations in:
  - cation type:  $\text{M}^+ = \text{Li}^+, \text{Na}^+, \text{Cs}^+, \text{Zn}^{2+}$
  - neutralization level = %  $\text{COO}^-\text{M}^+$  vs  $\text{COOH}$
  - spacing between acid groups
- All atom OPLS force-field
- $n = 4$  repeat units (4 acid groups)
- $\sim 64 \text{ \AA}$  box, total of  $\sim 25,000$  atoms
- $T = 150 \text{ C}$

# Correlation Functions

O-ion - +

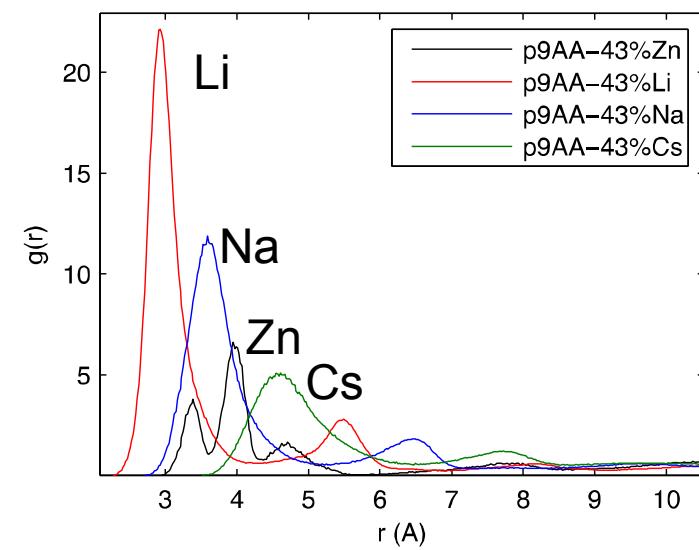
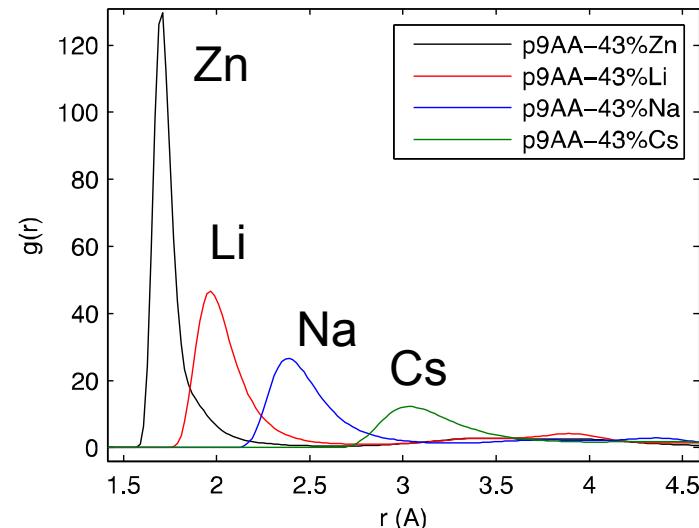
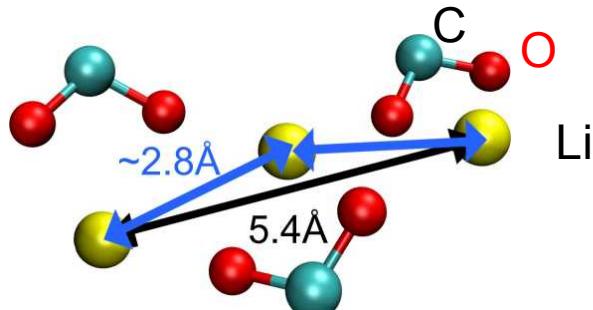
- very large peaks
- peak ~ ion size
- height decreases for larger ions

cluster analysis:

O-ion in same cluster if separation within 1<sup>st</sup> peak  
carbonyl O (OH) in same cluster

ion-ion ++ --

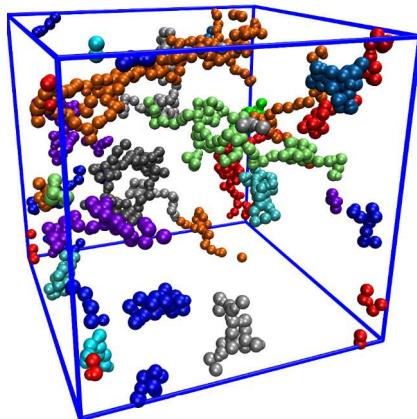
- 1<sup>st</sup> peak at next-nearest neighbor distance
- secondary peaks visible



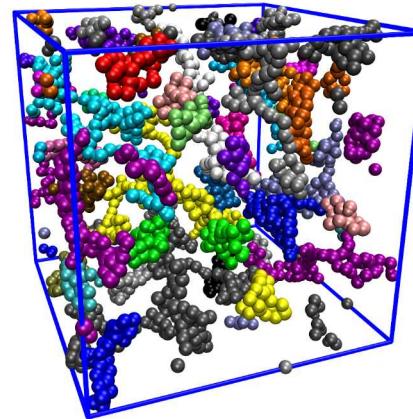
# Morphology: Li-neutralized pAA

coloring by cluster

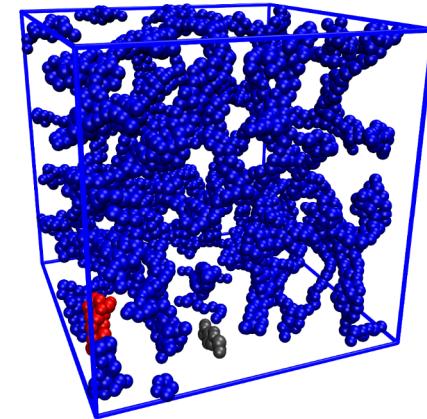
p9AA-10%Li



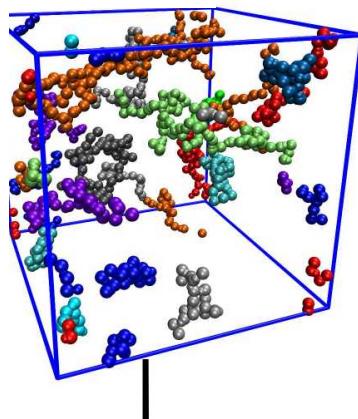
p9AA-43%Li



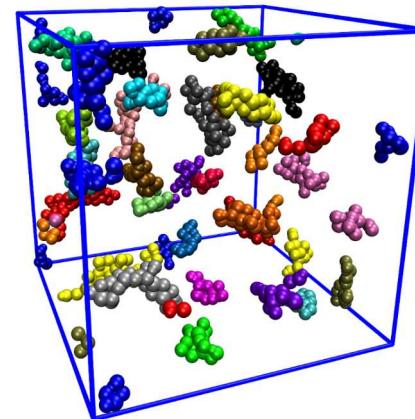
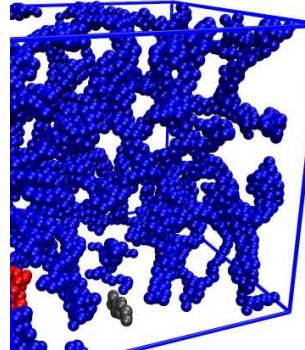
p9AA-100%Li



p21AA-43%Li



c. p9AA-100%Li  
FP

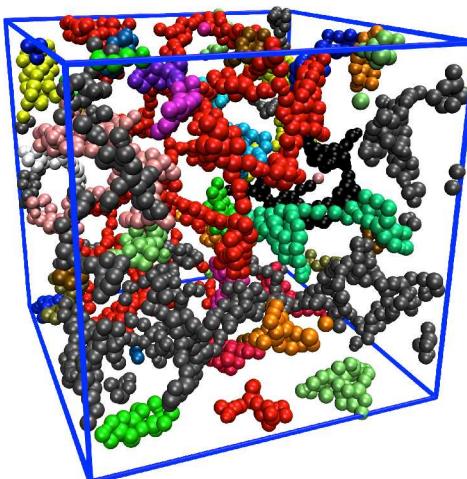
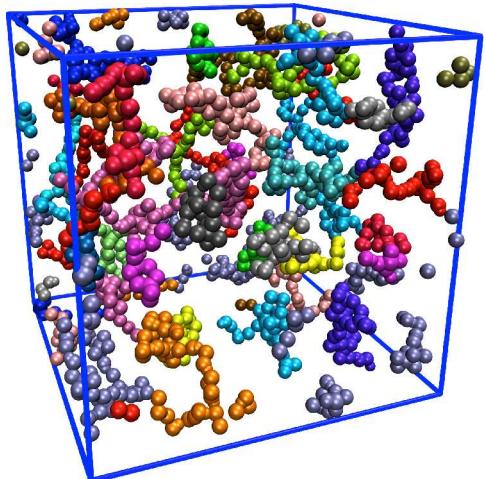


# Morphology for Different Cations

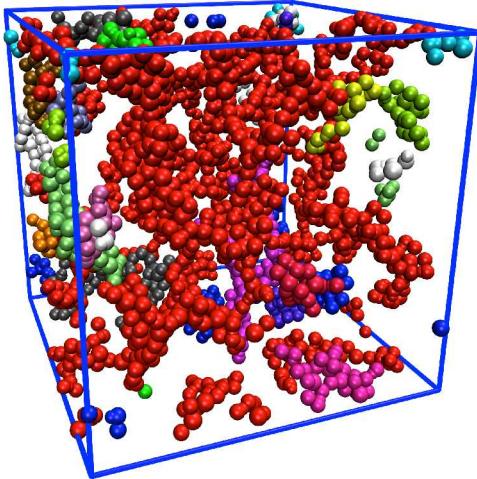
$Zn^{2+}$

p9AA-43%M

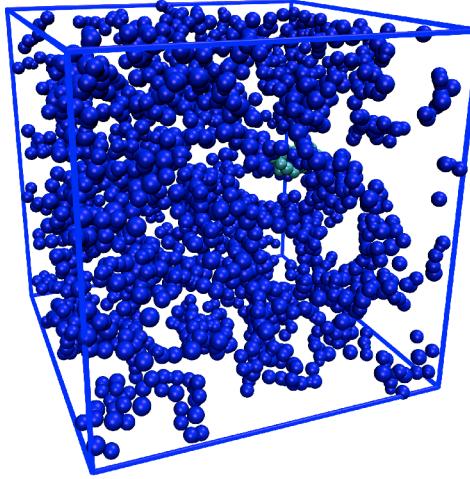
$Li^+$



$Na^+$



$Cs^+$



p9AA- $y\%$ M

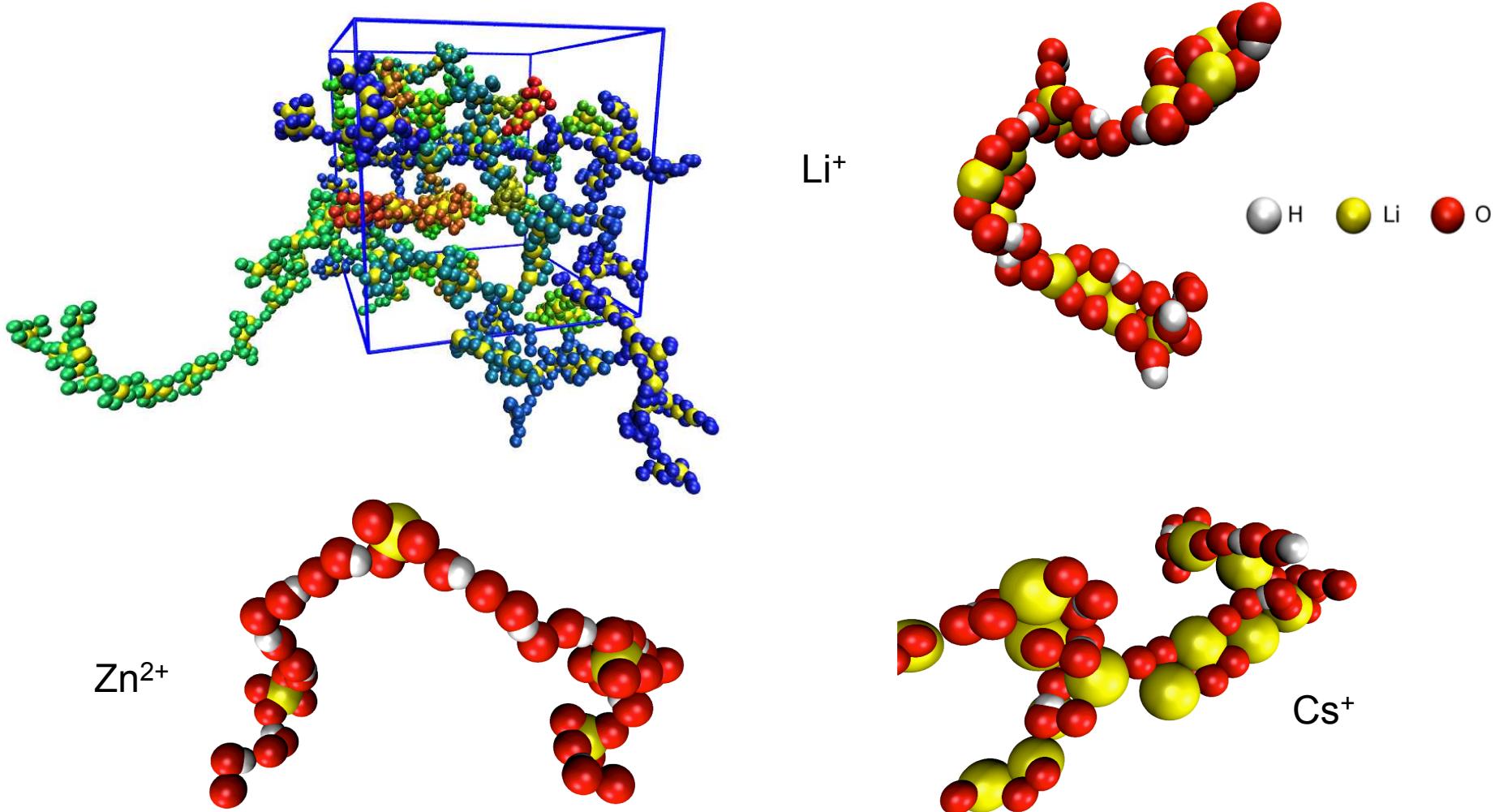
	10%	25%	43%	75%	100%
<b>Zn</b>	LS	LS	SS	SS	SS/CS
<b>Li</b>	SS/LS	LS	LS	LS/PP	PP/FP
<b>Na</b>	SS	SS/LS	PP	FP	FP
<b>Cs</b>	LS	PP	FP	FP	FP

pxAA-43%M

	p9	p15	p21
<b>Zn</b>	SS	SS/CS	CS
<b>Li</b>	LS	SS	SS/CS
<b>Na</b>	PP	SS	SS/CS
<b>Cs</b>	FP	LS/PP	LS/SS

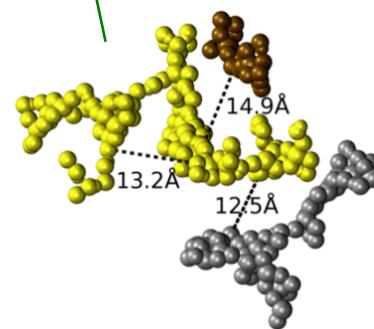
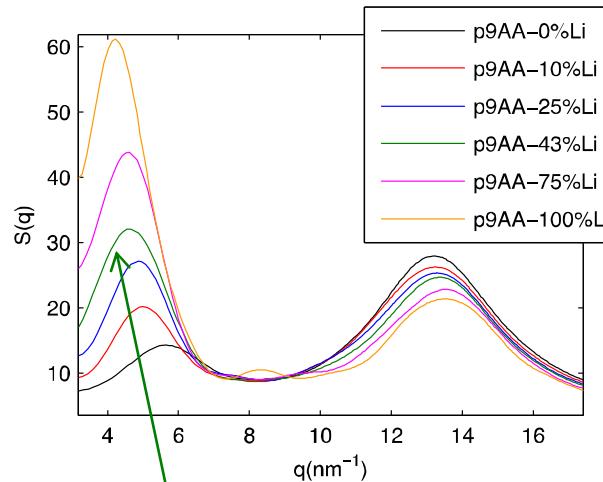
# Stringy Aggregates

hydrogen bonding contributes to clusters

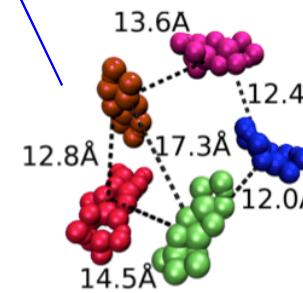
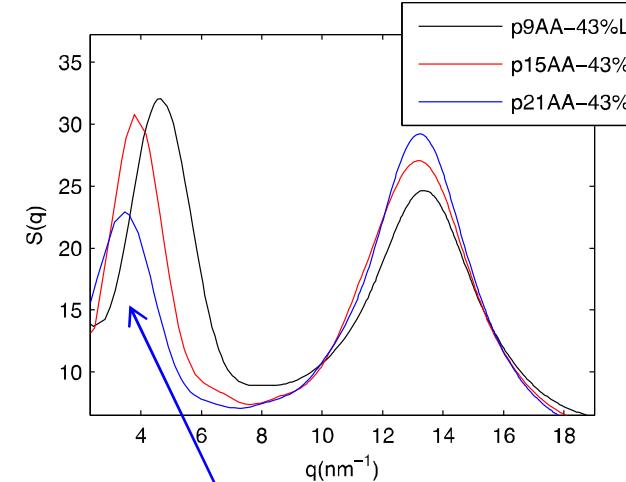


# Total Structure Factors for Li-neutralized pAA

$$S(q) = \sum_i c_i f_i^2 + 4\pi\rho \int_0^\infty \frac{\sin(qr)}{qr} r^2 \sum_{i,j} c_i c_j f_i f_j (g_{ij}(r) - 1) dr$$



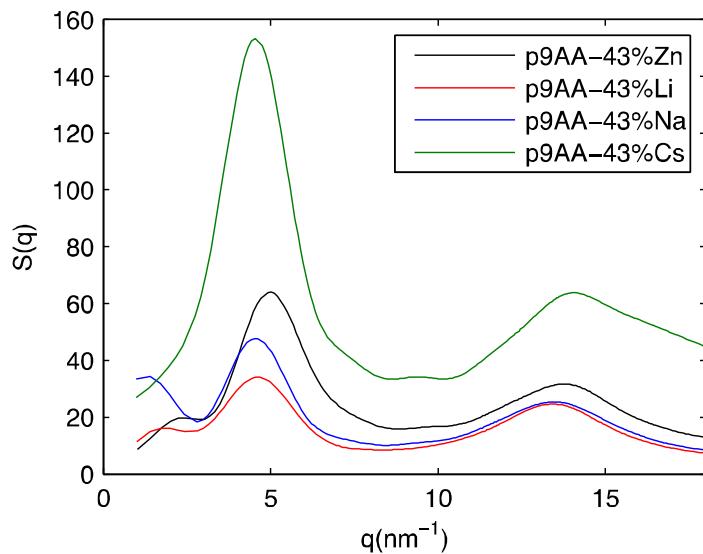
12-17 Å  
 $q \approx 3.6-5.2/\text{nm}$



ionomer peak from inter-aggregate scattering

# Structure Factors vs Cation

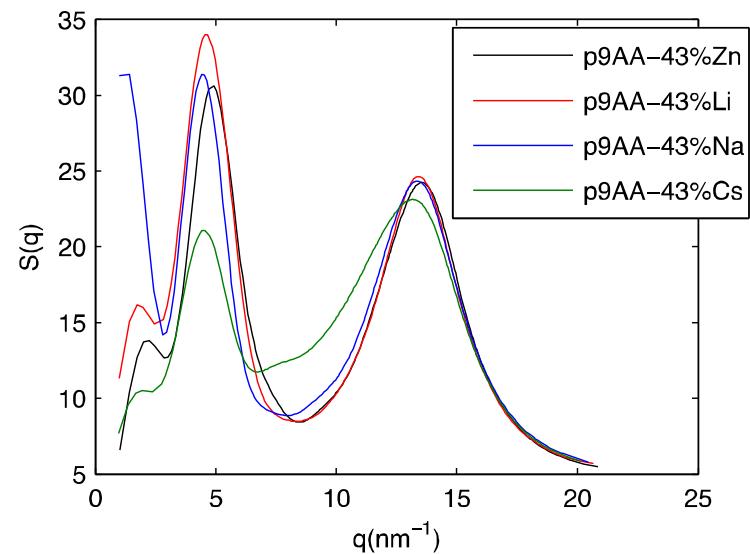
## Alchemy



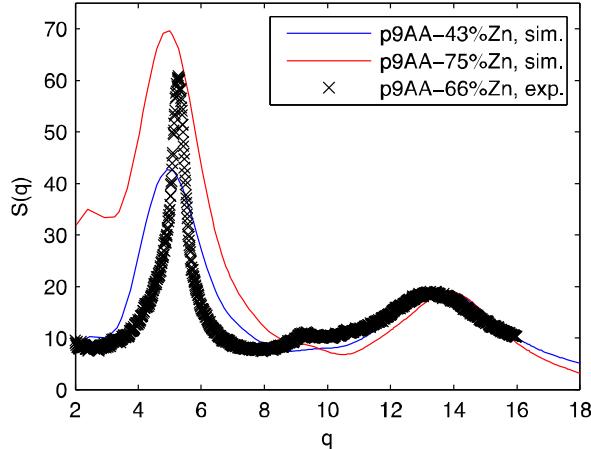
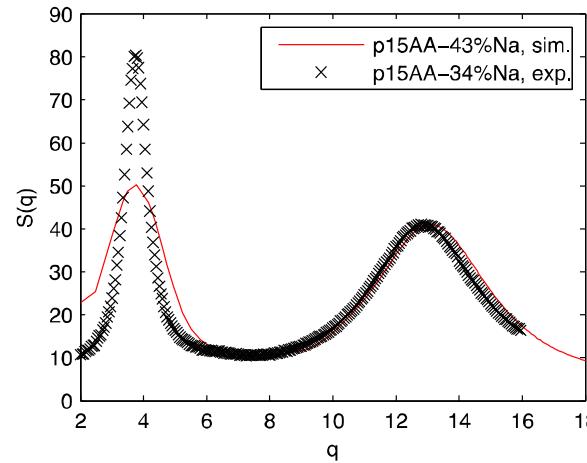
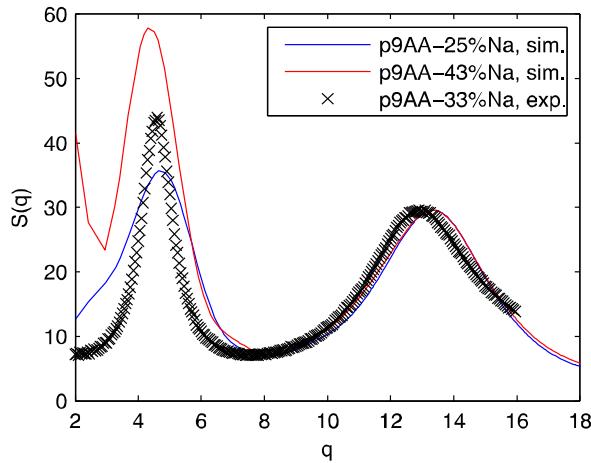
$\text{Li}^+$  form factor  
for all ions



$$f_M \rightarrow f_{\text{Li}}$$

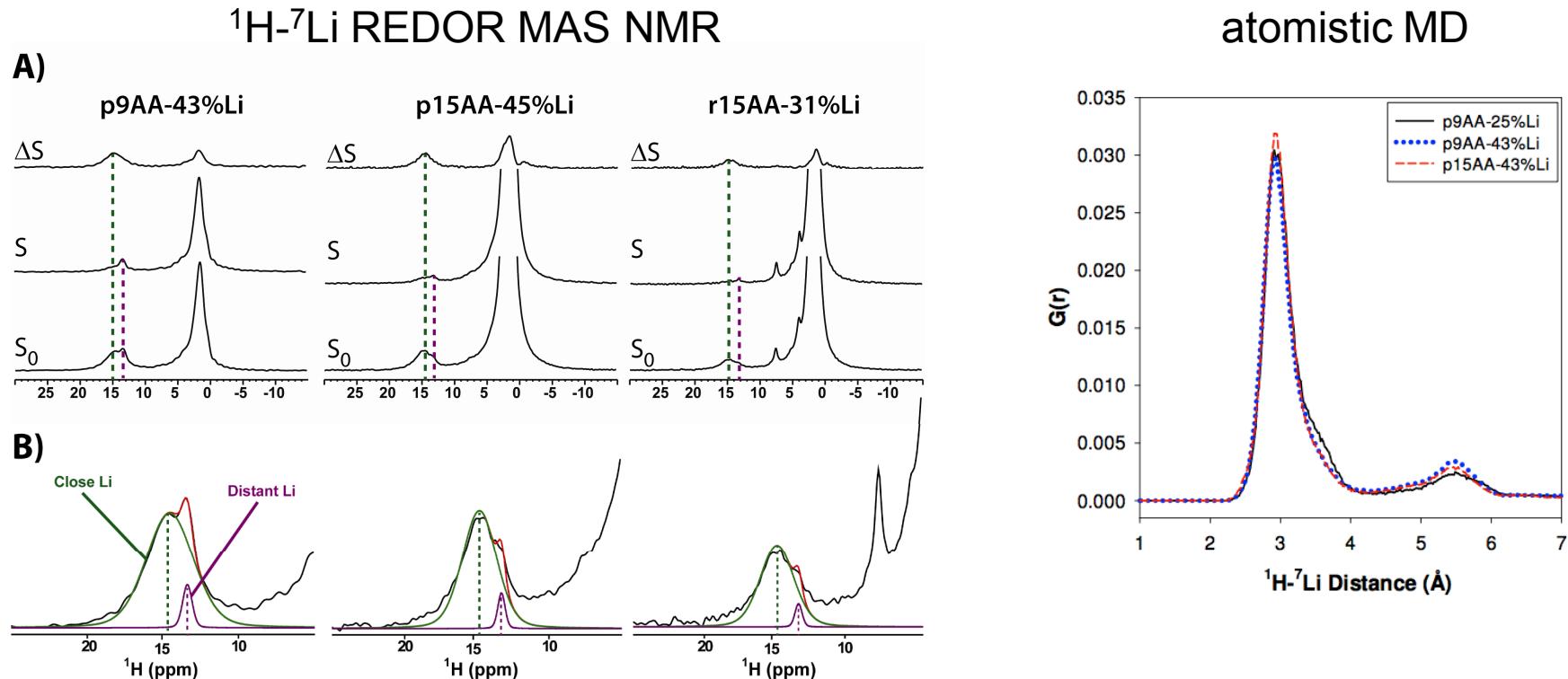


# Comparison to X-ray Scattering

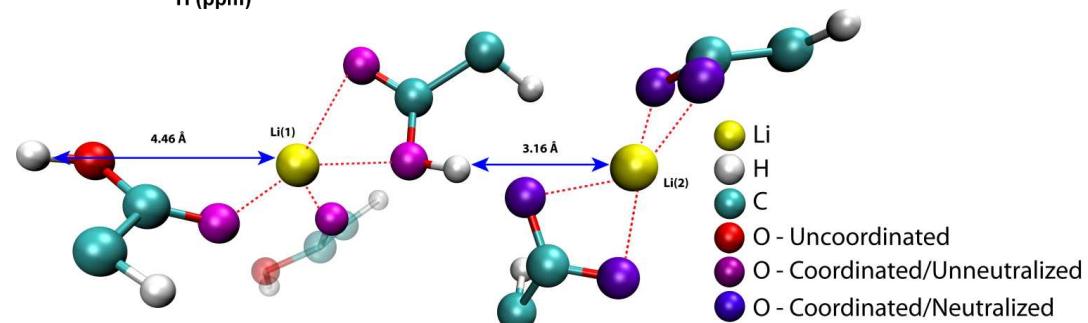


- peaks in correct locations
  - also true for Li, Cs
- x-ray intensity in arbitrary units
  - fit to height of amorphous halo

# Local Li<sup>+</sup> Environment



- 2 H-Li distances
- reflects variety of coordination in aggregates

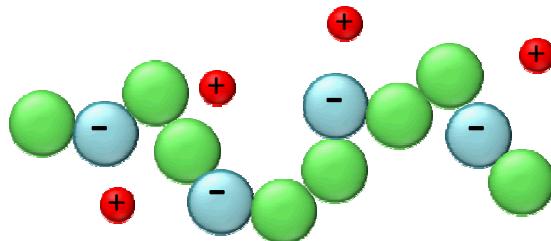


# Summary of Atomistic Simulations

- range of morphologies
  - stringy
  - can be percolated
  - not all spherical as previously assumed (except maybe Zn)
  - not well resolved in scattering
  - ionomer peak due to interaggregate scattering
- trends
  - longer aggregates as neutralization increases
  - shorter aggregates as spacer length increases
- hydrogen bonding important in partially neutralized systems
- simulations match experimental  $S(q)$  well

# Coarse-grained Simulations

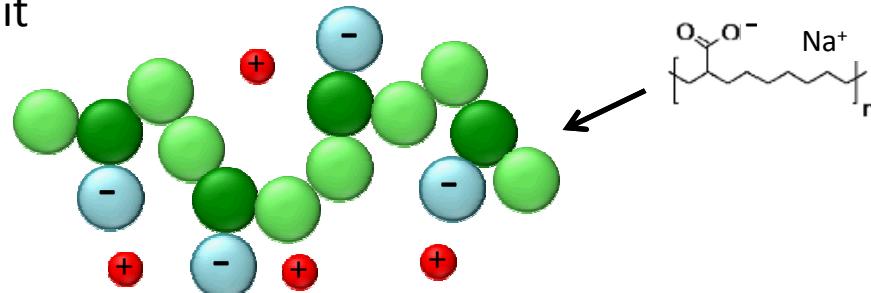
Ions in the polymer backbone:  
“ionenes”



Ions pendant to the backbone:  
“pendants”

backbone beads  
per repeat unit

$$N_{bb} = 3$$

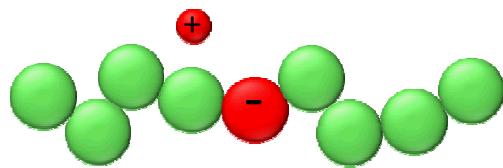


$N_{bb} = 3, 5, 7, 9 (11)$   
 800 polymers  
 100% neutralization  
 bulk dielectric constant = 4  
 counterion size =  $\frac{1}{2}\sigma$   
 Bjerrum length =  $35.7\sigma$   
 $10^8$  time steps

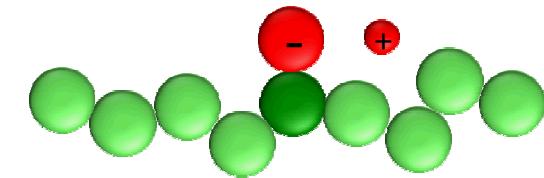
$$\ell_B = \frac{e^2}{4\pi\epsilon_0\epsilon_r kT} = 35.7\sigma$$

$$R_g \approx 3.1 - 3.3\sigma$$

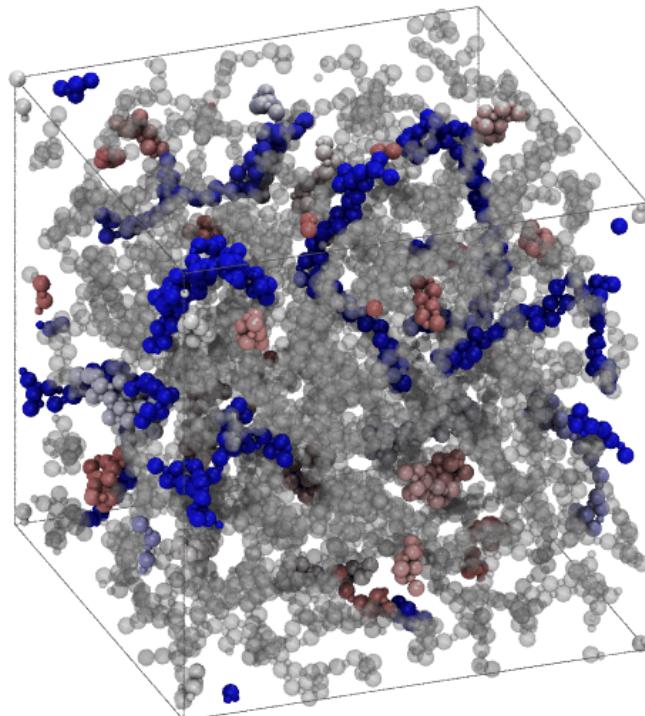
# Aggregate Morphology: Architecture Matters



Ionenes: percolated



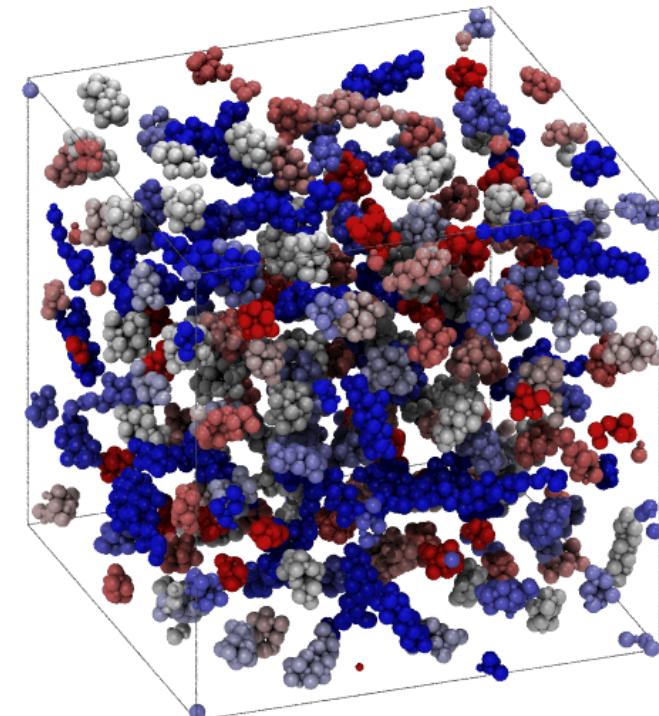
Pendants: not percolated



$$N_{bb} = 9$$

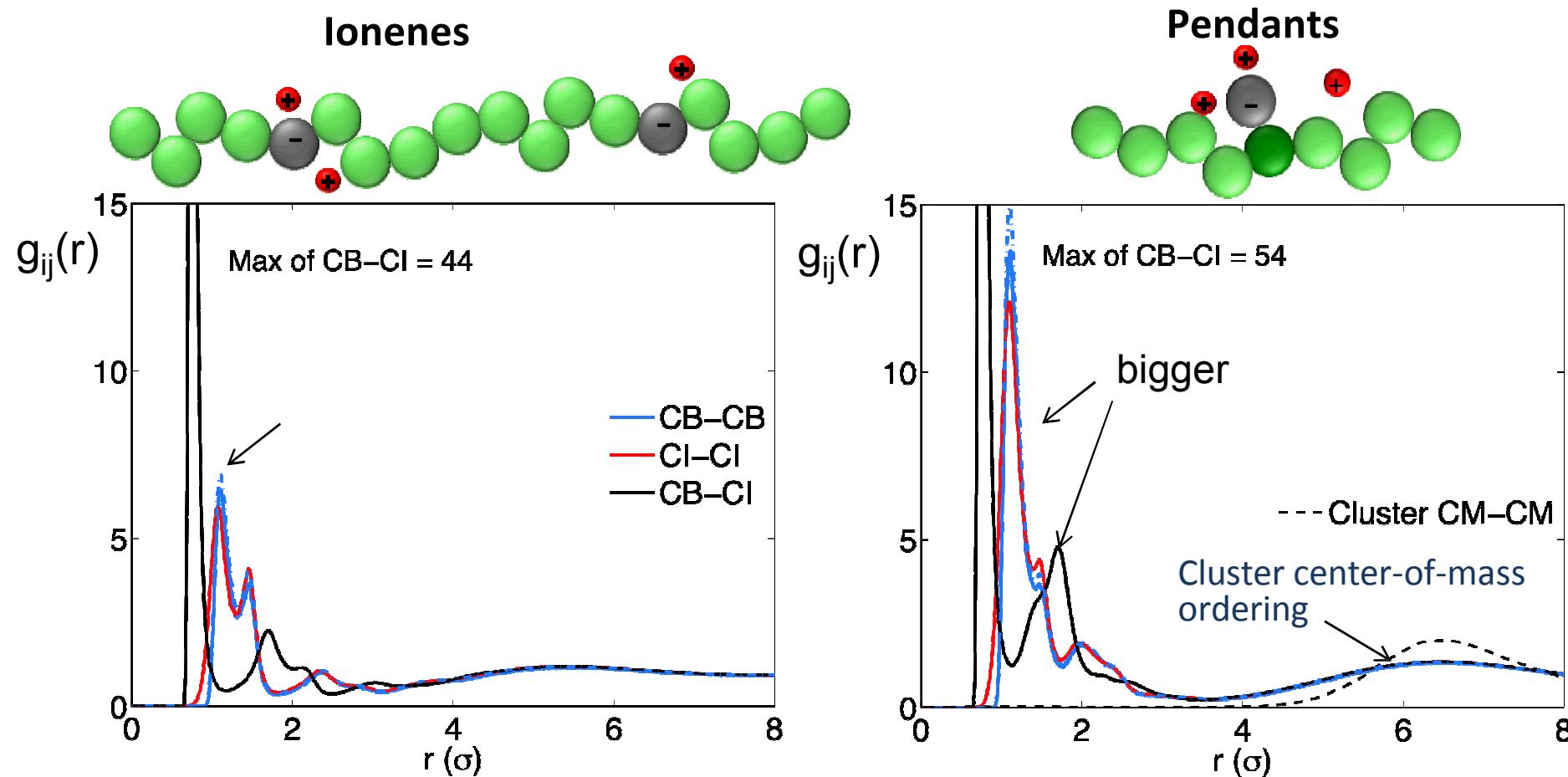
$$\epsilon_r = 4$$

Small clusters  Large clusters  
Only charged beads shown



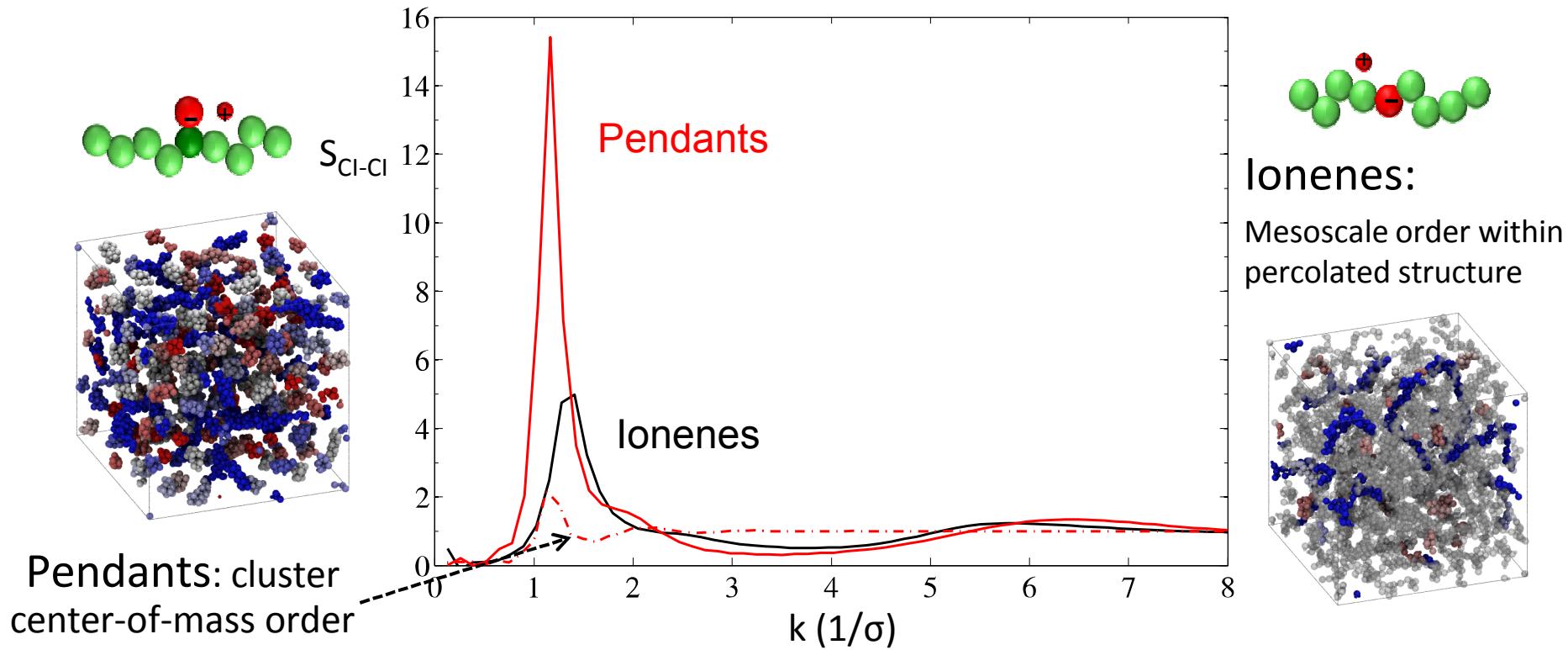
# Ion-Ion Pair Correlation Functions

- A clue to difference between ionenes and pendants
- Pendants have larger peaks
- More counterions about pendant charge in polymer



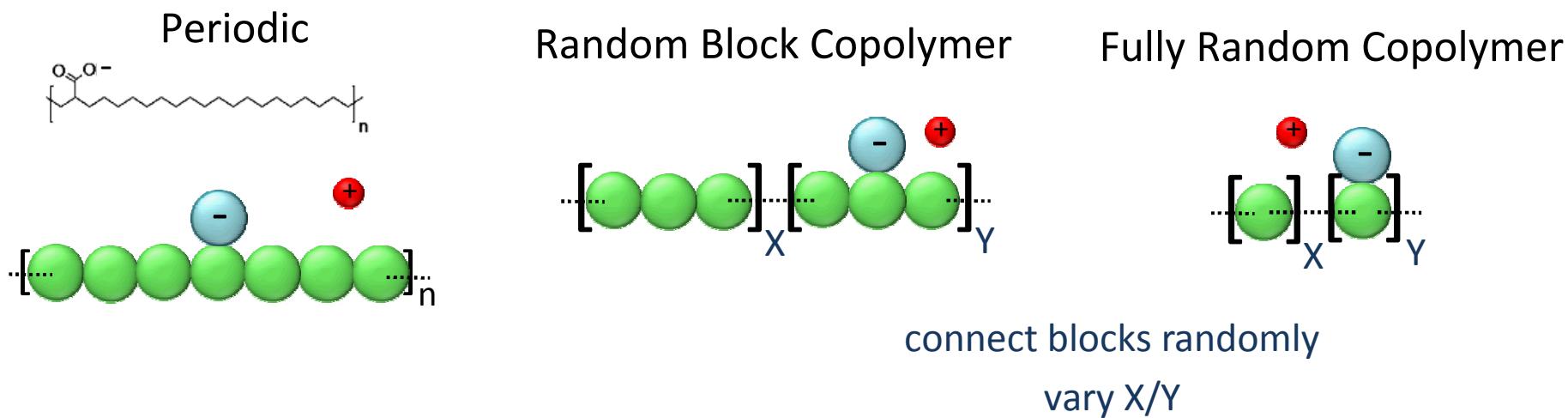
# Structure Factor (Scattering)

- Ionomer peak for *both* ionenes, pendants
  - Ionene peak: mesoscale order within percolated aggregate
  - Pendant peak: cluster center-of-mass to center-of-mass order
- Experimental peak  $\sim 4 \text{ nm}^{-1}$ , MD peak  $1.2\text{-}1.8 \sigma^{-1} \rightarrow \sim 3\text{-}4 \text{ nm}^{-1}$



# Randomly Spaced Ionomer Model

- random block
  - mimic ROMP
- fully random
  - mimics typical random polymerization

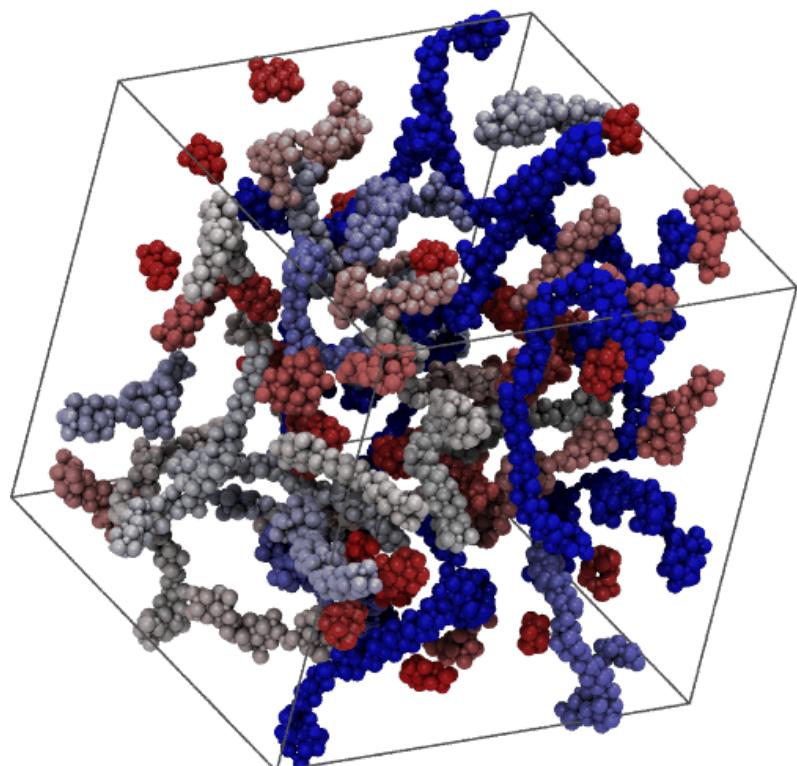


$N_{bb}$  = Number of **backbone beads** per charged bead

# Aggregate Morphology: Random vs. Periodic

**Random Block Copolymer  
Pendants:** stringy, large clusters

Mean cluster size 87

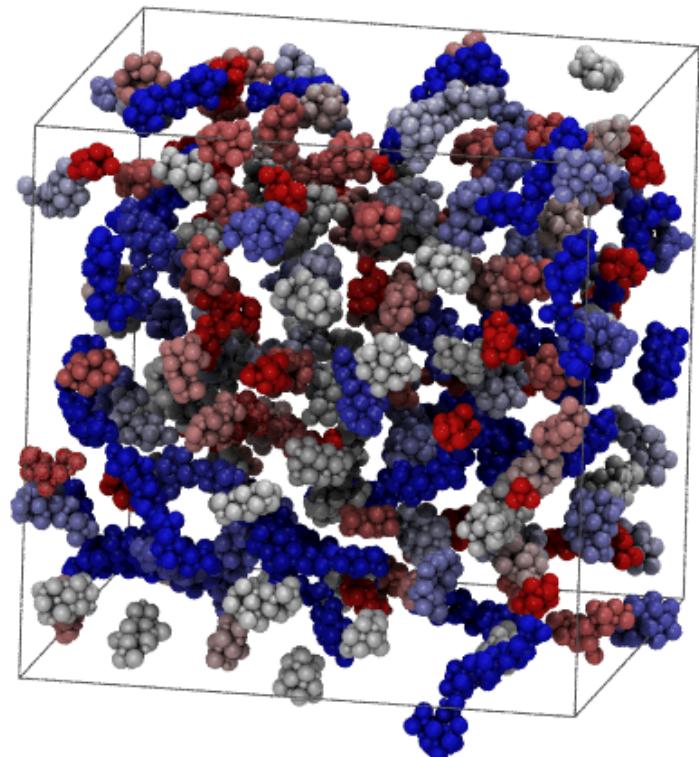


$$\begin{aligned}\varepsilon_r &= 4 \\ N_{bb} &= 9\end{aligned}$$

Small clusters

**Periodic Pendants:**  
narrow cluster size distribution

Mean cluster size 31

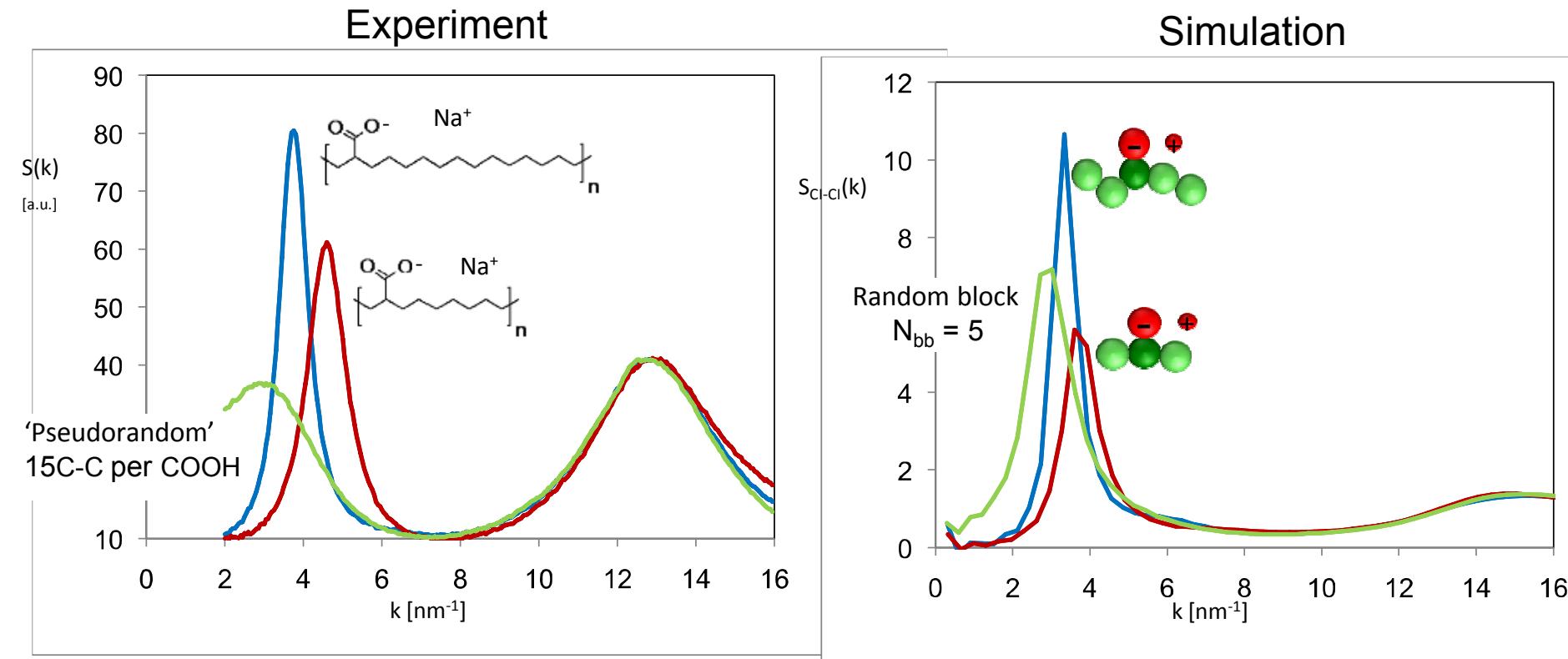


Large clusters

# CG MD: Comparison to X-ray Scattering Sandia National Laboratories



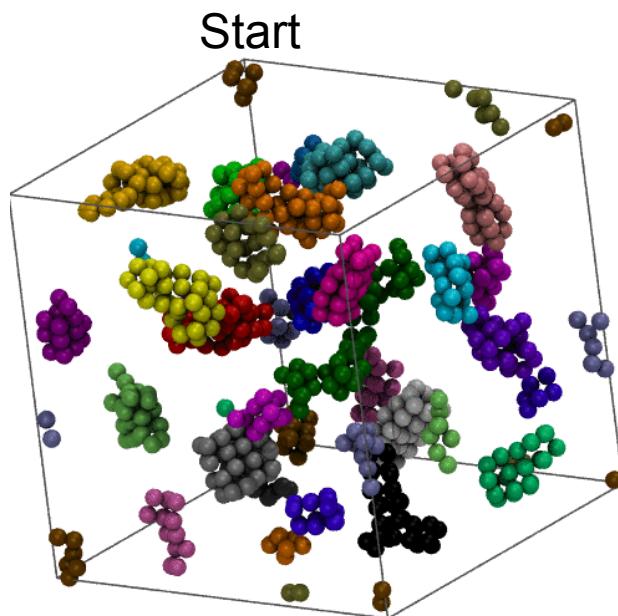
- Experimental/Simulation Agreement
  - Peak location similar
  - Increasing spacing moves peak to left
  - Random spacing moves and broadens peak



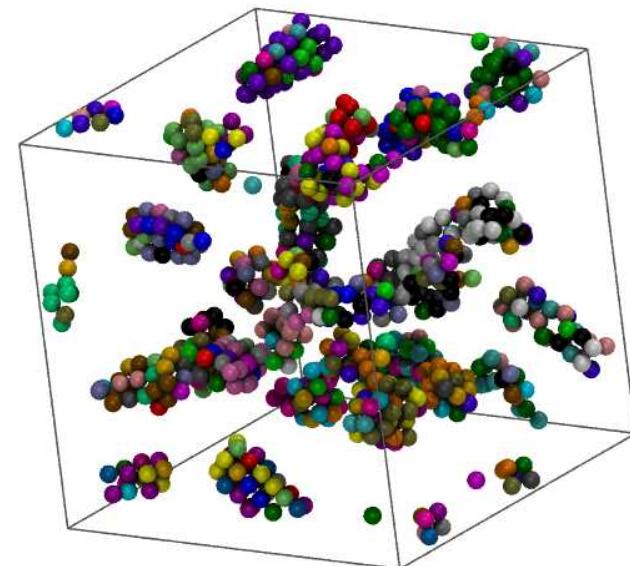
# Cluster Dynamics

Is there any?

Color distinct clusters by  
different color



Finish ( $10^7$  steps later)

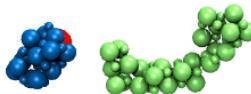


*Ions move.*

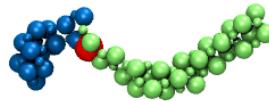
# Ion Trajectories

periodic pendants  $N_{bb}=9$

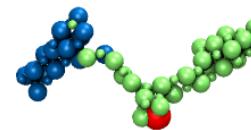
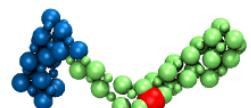
2 separate clusters  
Follow one **counterion**



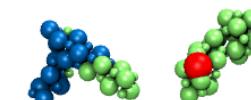
Clusters have collided



Ion has moved to other cluster.  
**NEVER** separated from a cluster.



Clusters reform with ion moved



ions move by cluster  
rearrangement/collision

# Energies and Cluster Dynamics

$+$  – pair energy (contact) is  $48 \text{ kT}$ .

pairs are not likely to separate.

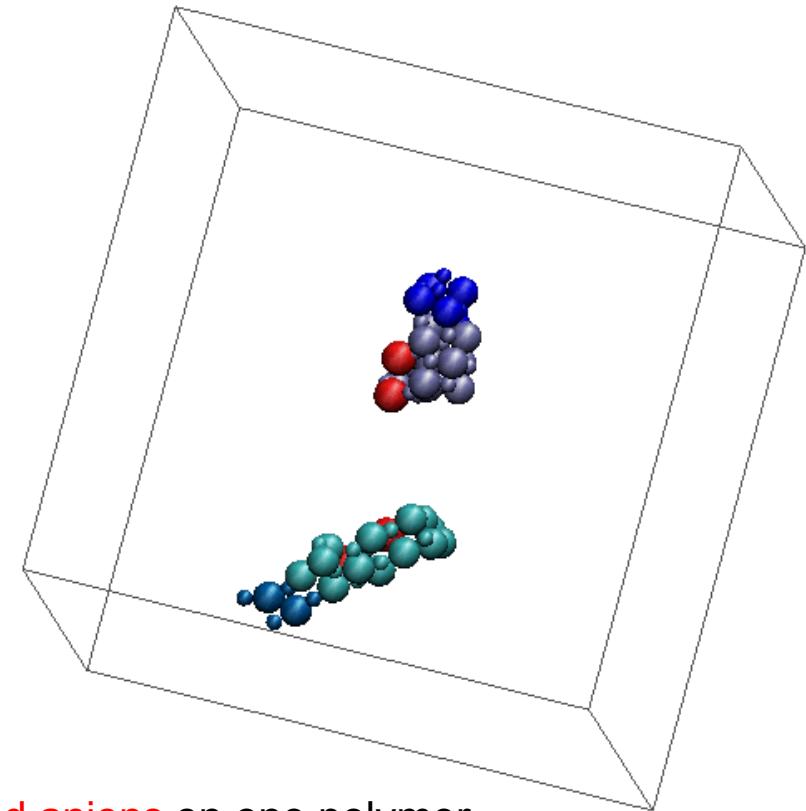
energy to split a cluster is much less  
ideal, 2D crystallite has a separation energy of  
only  $20 \text{ kT}$ :



simulations show clusters are flexible (they're liquids after all) and the energies will be less than these crystallite calculations.

ions move a lot within a cluster

Pendant (discrete clusters)



Red anions on one polymer.

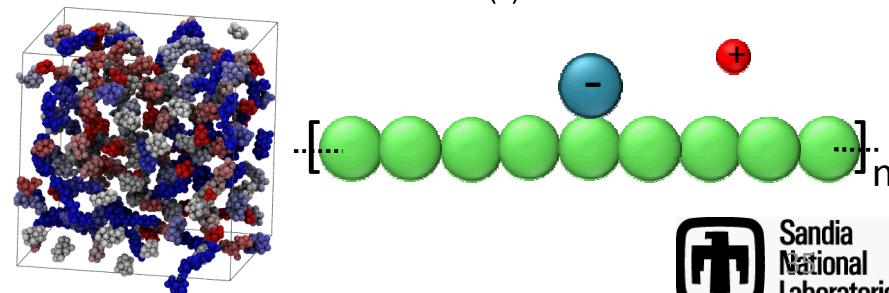
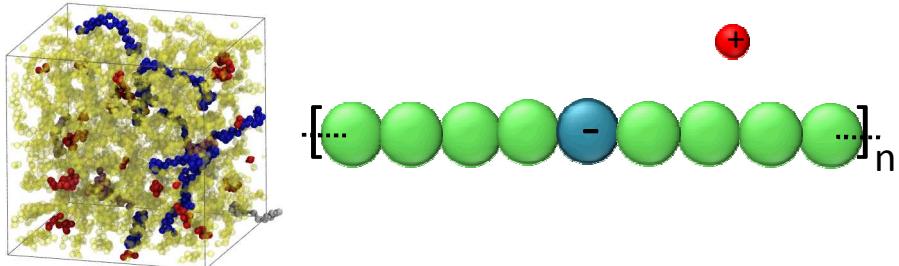
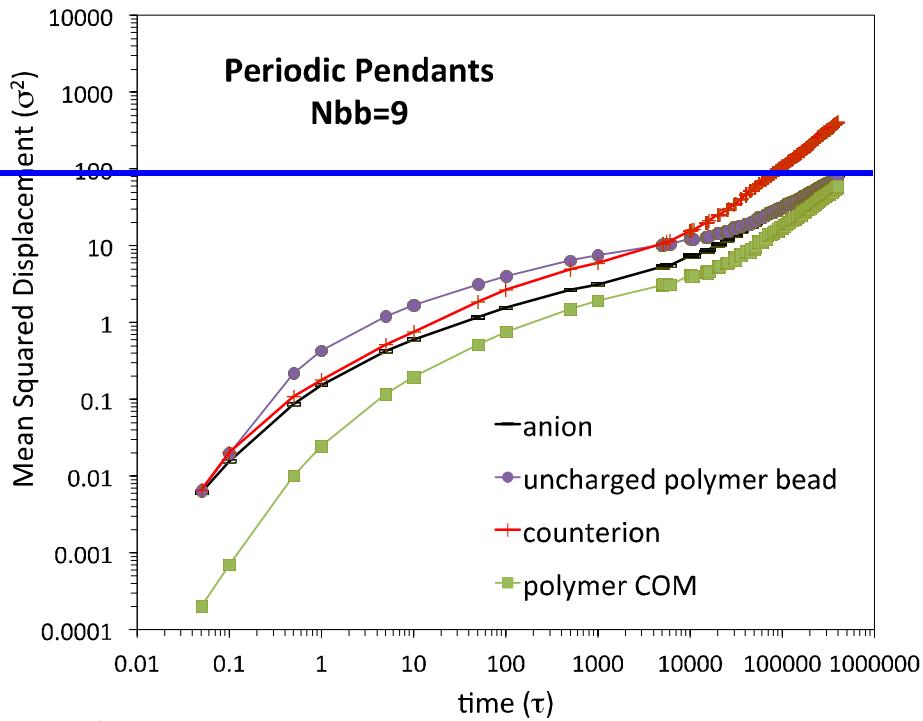
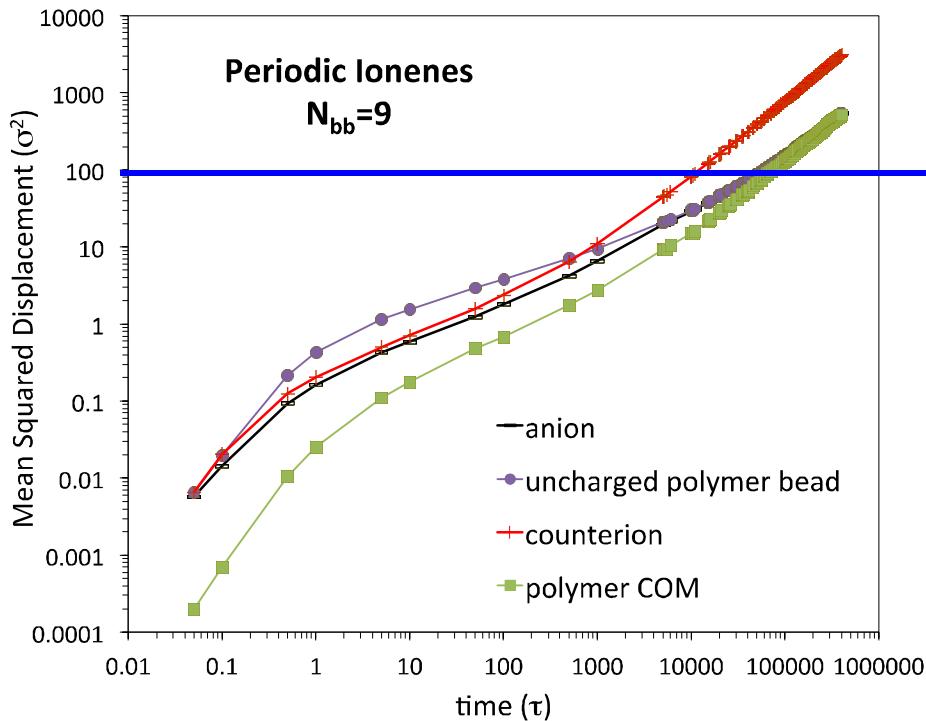
Blue ions initially within  $3\sigma$  of red anions.

Other ions which temporarily come within  $3\sigma$  are transparent.

5000  $\tau$  X million time steps

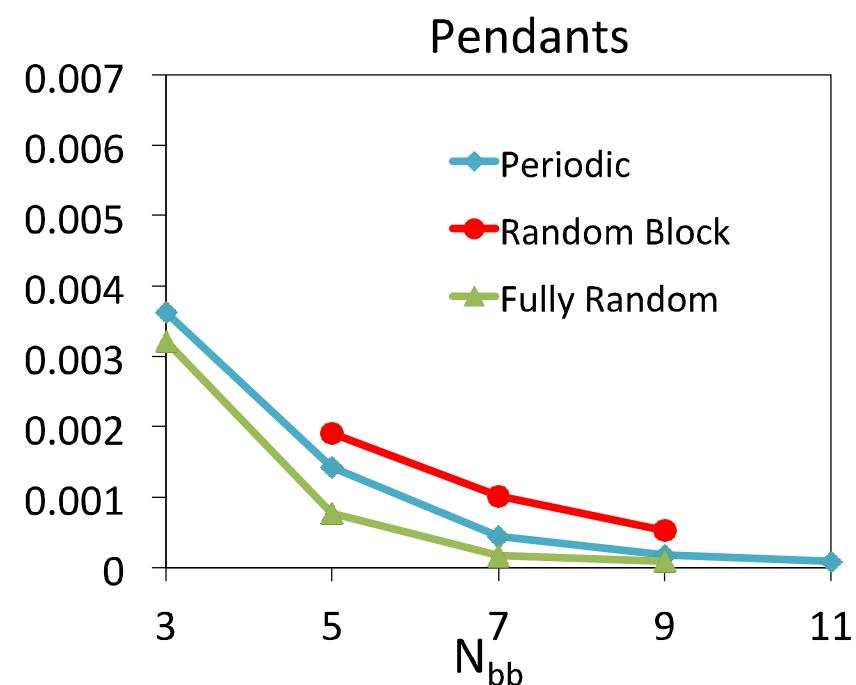
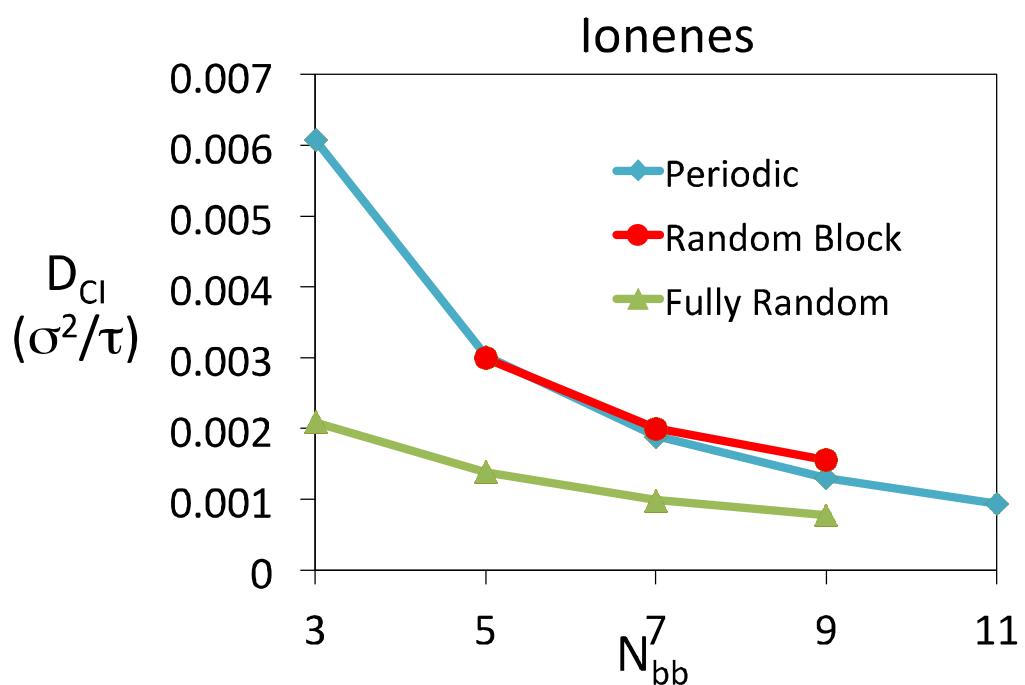
# Mean Squared Displacements

- Ionenes, pendants similar at short times
- Pendants slower but qualitatively similar at long times



# Counterion Diffusion Constants

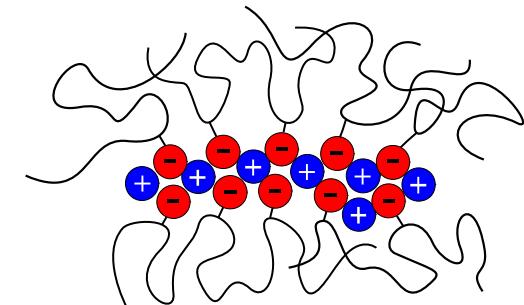
- Ionenes conduct better than pendants
- Greater concentration of ions increases diffusion
- Blocky random copolymerization increases diffusion



$$\varepsilon_r = 4$$

# The New Picture

- Aggregates are stringy
  - + – + – ordering
  - polymer backbone constraints
- Counterion influences structure (partial neutralization)
  - $\text{Na}^+$ ,  $\text{Li}^+$ : medium-sized, stringy aggregates
  - $\text{Cs}^+$ : Percolated network
  - $\text{Zn}^{2+}$ : small, isolated clusters
  - Small ion- $\text{O}^-$  clusters are bridged by  $-\text{OH}$  and  $=\text{O}$  groups
- molecular architecture important
  - pendant vs ionene
  - isolated aggregates for pendants or large spacing
  - percolation for ionenes or short spacing
- ion motion by cluster rearrangement
- ions diffuse faster in percolated morphologies



# Acknowledgments



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(now at OSU)



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Todd Alam



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Michelle Seitz (now at DSM)  
Francisco Buitrago  
University of Pennsylvania



Janelle Jenkins



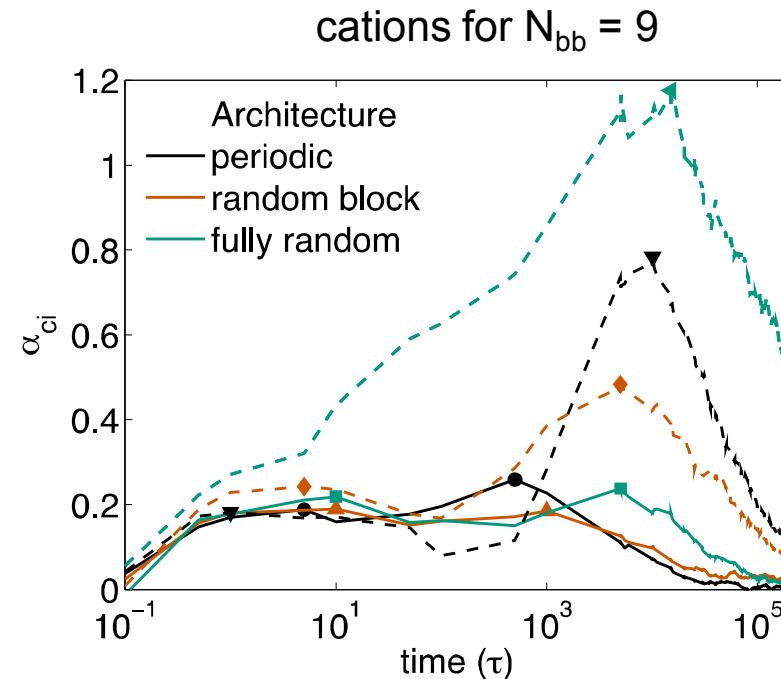
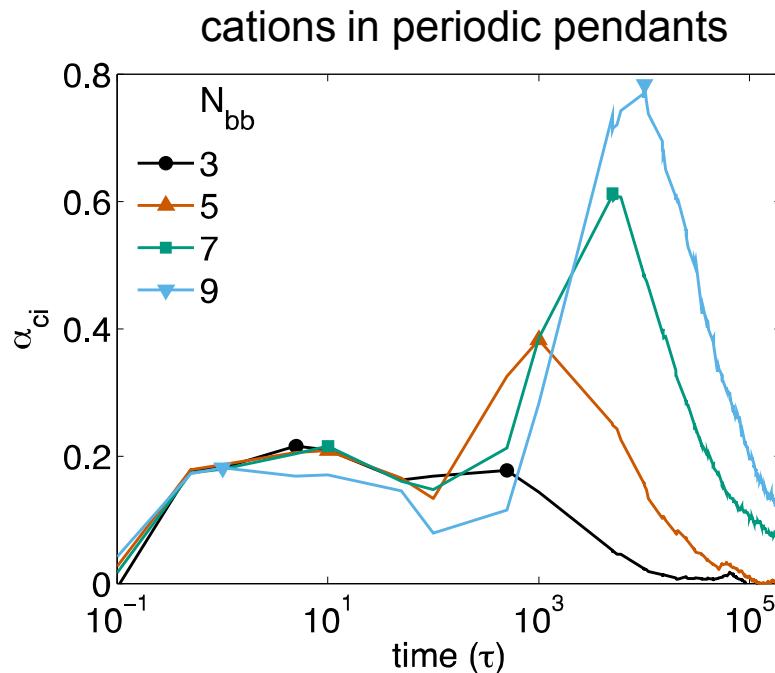
The “Ionomers” LDRD team  
Funding: Sandia LDRD Program  
CINT  
NERSC



# Ion Dynamics

non-Gaussian parameter

$$\alpha(t) = \frac{3 \langle (r(t))^4 \rangle}{5 \langle (r(t))^2 \rangle^2} - 1$$



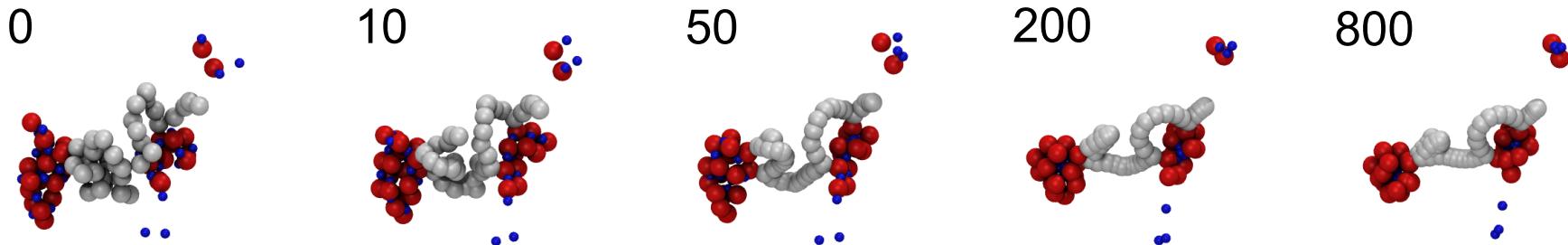
indicative of 2 time scales:

- local motion in clusters
- slower rearrangement between clusters

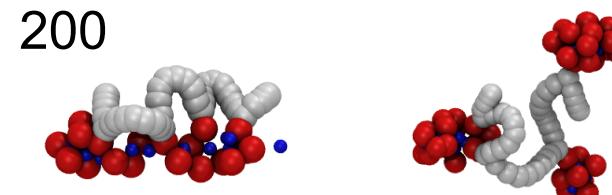
# Average Local Structure

one polymer (white, red anions) and nearby ions (red anions, blue counterions)  
 $N_{bb}=9$ , frames are 1000 steps apart

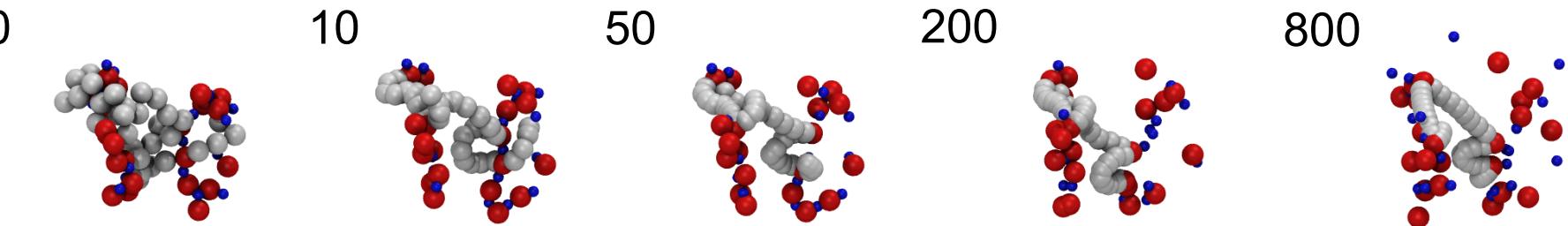
periodic pendant, frames averaged:



other periodic pendant  
examples

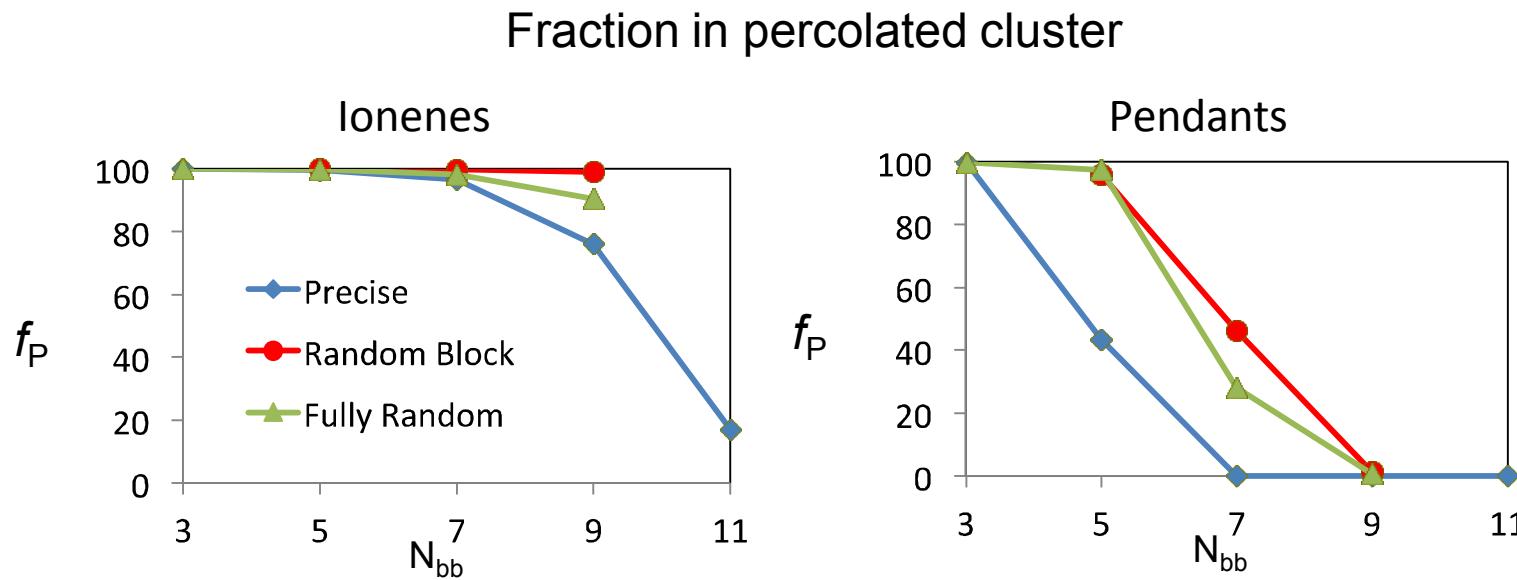


periodic ionene, frames averaged:



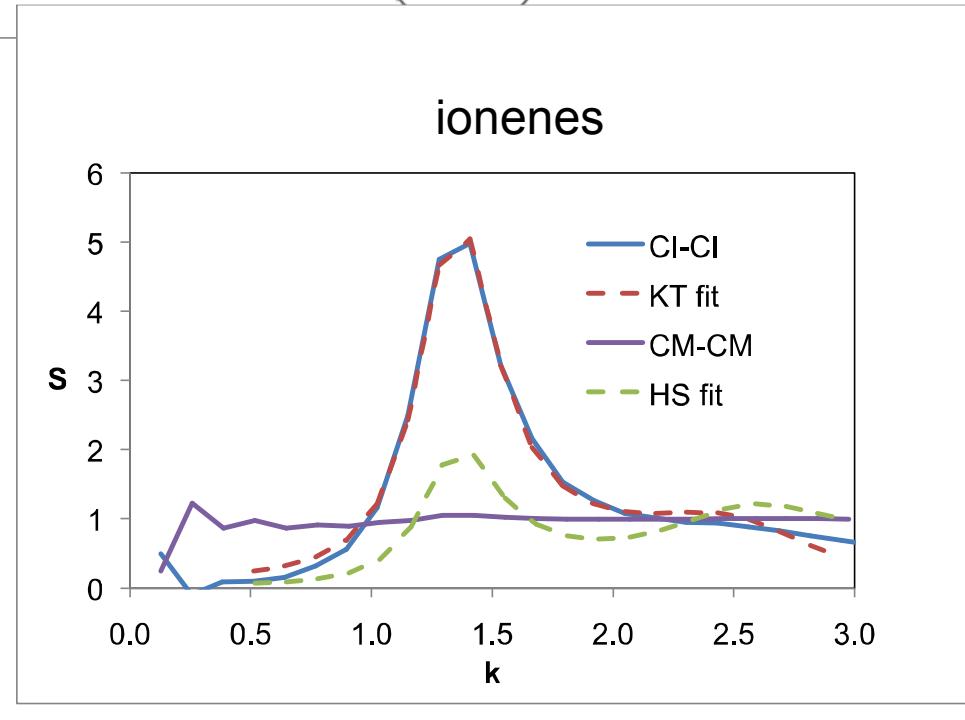
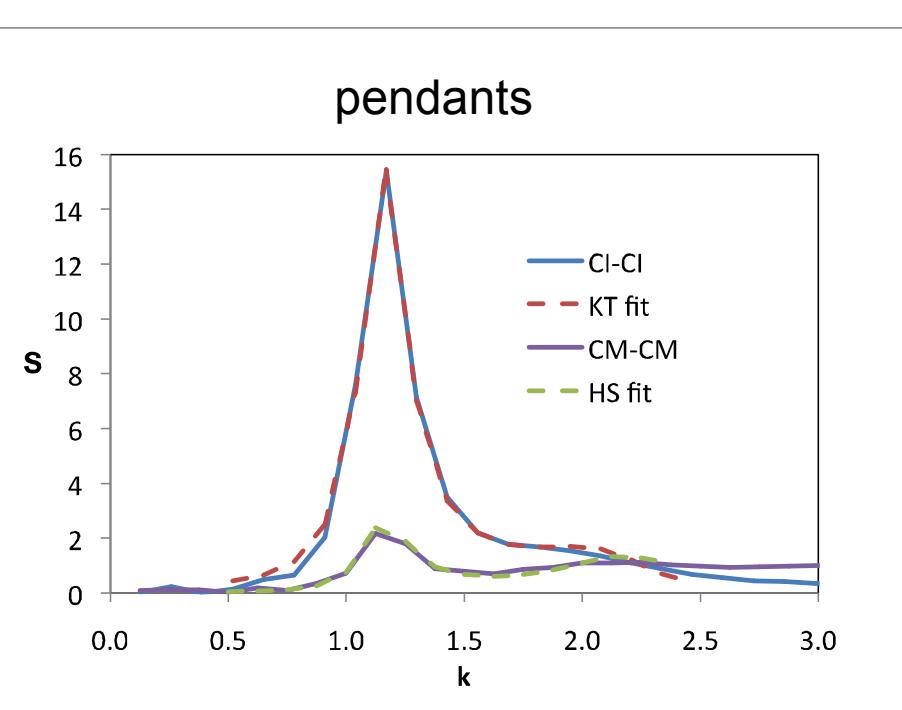
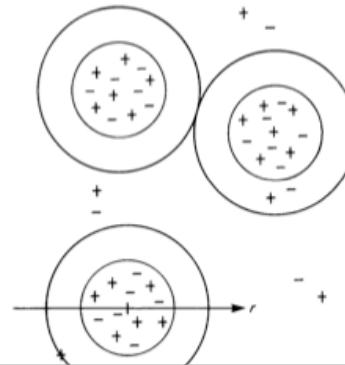
# Effect of Architecture on Clustering

- Ionene architecture, randomness increases percolation
- Randomness usually increases non-percolated cluster size



# Fit to Scattering

- modified hard sphere model
  - fits pendants well
    - fit parameters match physical meaning
  - fits ionenes well
    - fit parameters don't match



# Equilibration of Simulations

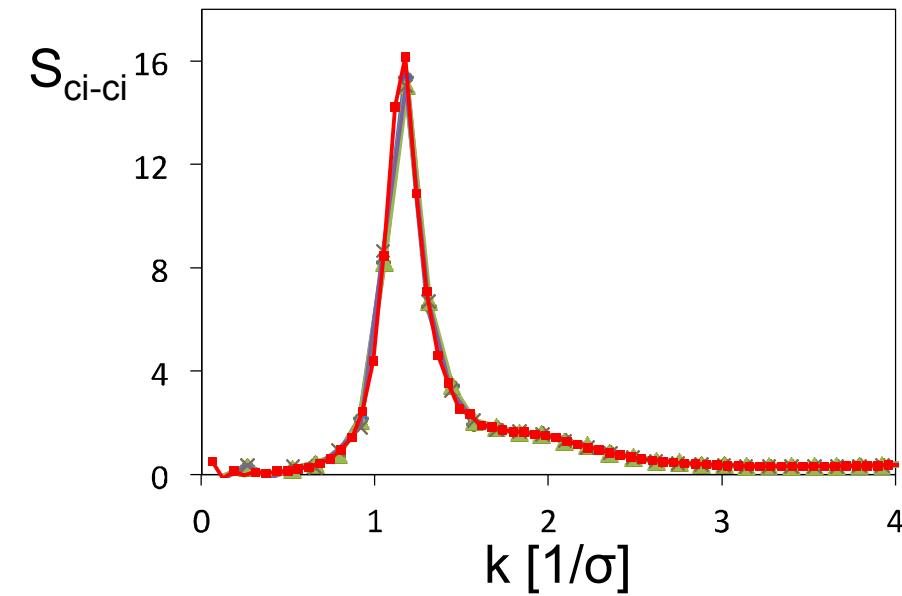
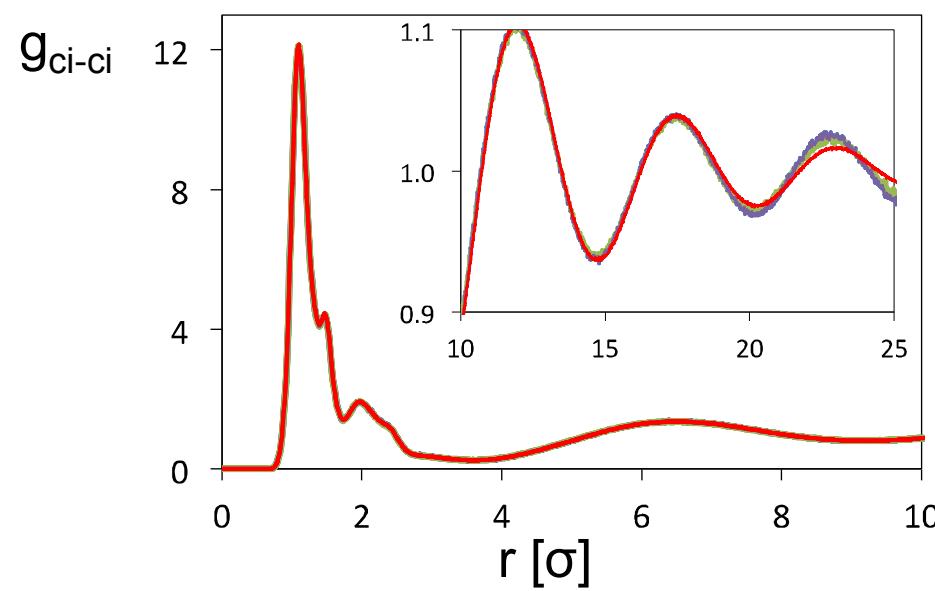
- From random initial configuration, equilibrate for  $10^7$  steps
- MSD of polymer centers of mass during equilibration  $> R_g^2$
- Dynamics data collection start at  $3 \times 10^7$  steps

$\varepsilon_r = 4$ ,  $N_{bb} = 9$  pendants: one of the slowest

no change in structure with:

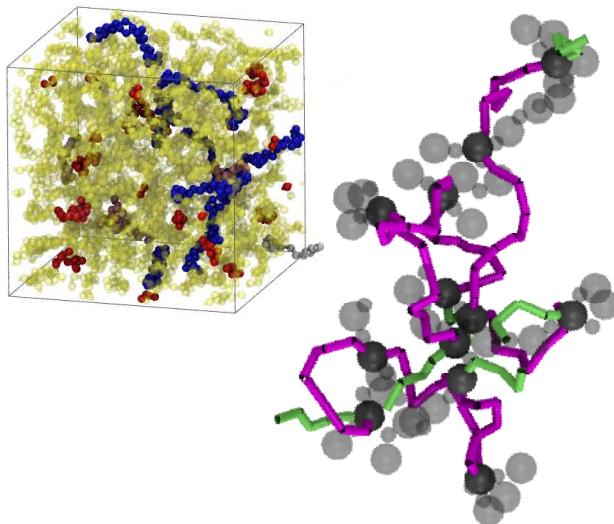
- equilibrating 4 times longer
- using twice the box length
- starting from a different random initial configuration

Longer equilibration  
Configuration A  
Configuration B  
Larger box



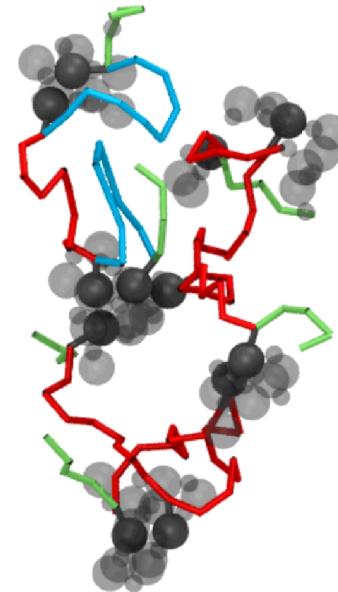
# Polymer Morphology

## Ionenes

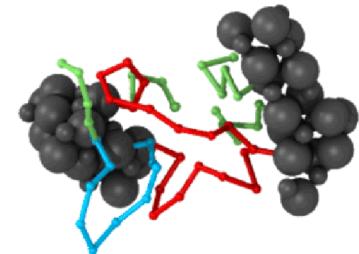


3 nearby polymers  
Charged beads  
End segments  
'Loops'  
Close loops  
Bridges

## Pendants



Polymer segments  
between 2 clusters

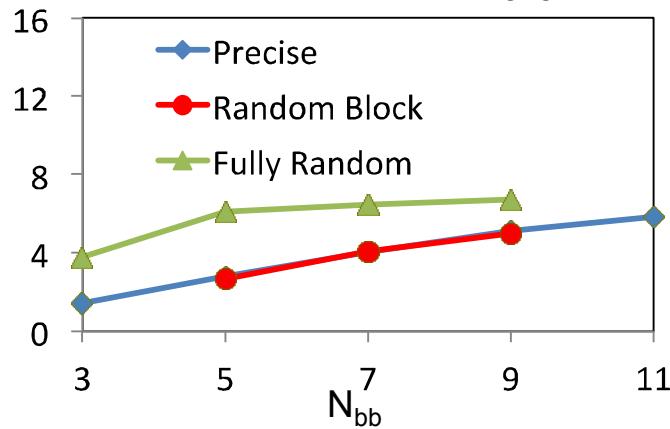


- Architecture determines aggregate morphology
  - Ionenes cannot easily form a compact cluster
  - Pendant backbone more separated from clusters
- Cluster-cluster length scale set by bridges?
  - Pairs of close loops or tails can set similar length scale
  - Decreasing backbone spacing leads to closer aggregates

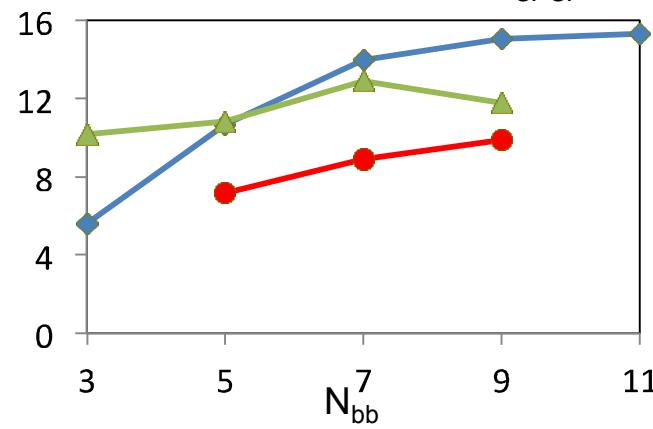
# Effect of Architecture on Ionomer Peak

- Pendants have larger peak than ionenes
- Randomness moves peak to lower wavevector

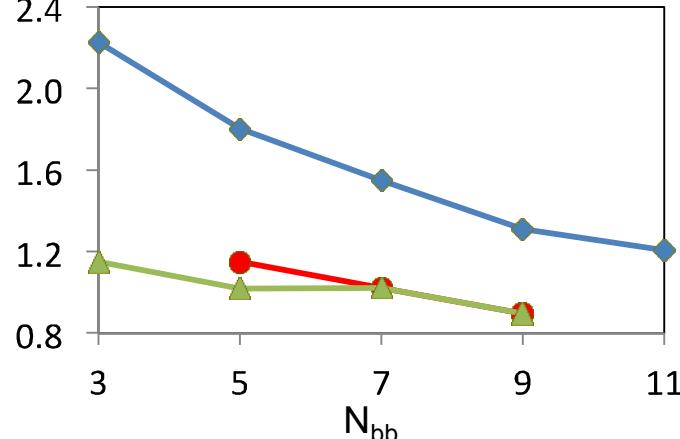
Ionene Peak Height  $S_{\text{Cl-Cl}}(k^*)$



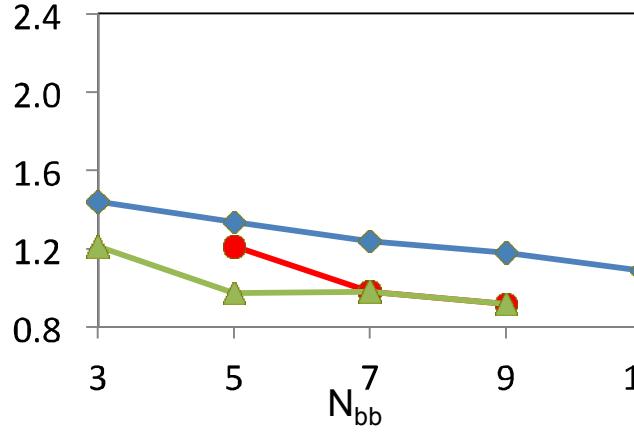
Pendant Peak Height  $S_{\text{Cl-Cl}}(k^*)$



Ionene Peak Location  $k^* [\sigma]$



Pendant Peak Location  $k^* [\sigma]$

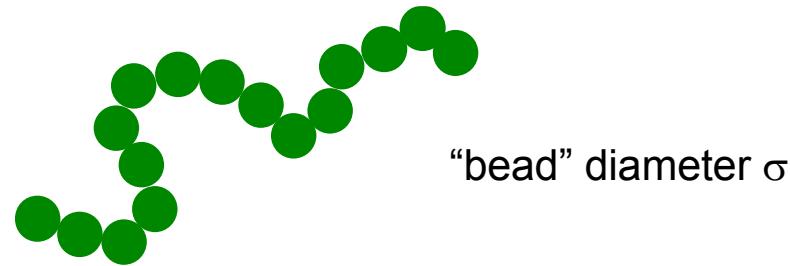


$\epsilon_r = 4$

# Molecular Dynamics Simulations

- put atoms in a box
- solve  $F = ma$  for each atom
- calculate statistical properties (averages) over trajectories

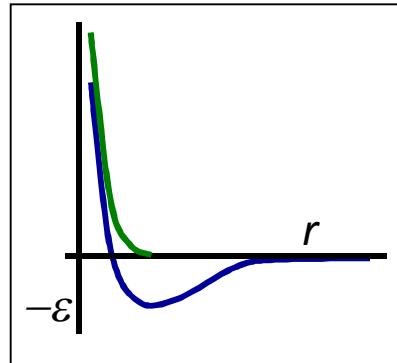
bead-spring polymer model  
(Kremer & Grest, 1990)



interactions between all “beads”

Lennard-Jones potential:

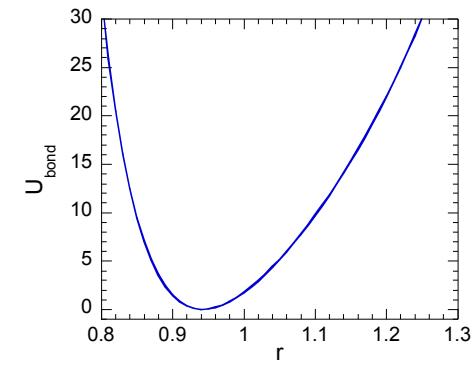
$$u_{LJ} = 4\epsilon \left[ \left( \frac{\sigma}{r} \right)^{12} - \left( \frac{\sigma}{r} \right)^6 \right]$$



interactions between bonded beads

FENE springs  $u(r) = -kR_0^2 \ln \left( 1 - \left( r / R_0 \right)^2 \right)$

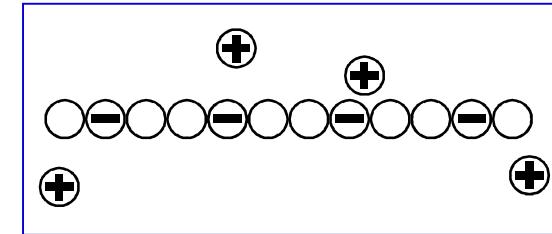
$$U_{\text{bond}} = u_{LJ} + u$$



# Ionomer MD Simulations

Coulomb interactions    
$$U(r) = \frac{q_1 q_2}{4\pi\epsilon_0\epsilon r}$$

counterions: single beads, size  $0.5\sigma$



NVT ensemble: Langevin thermostat

$$f_i = -m_i \Gamma \nu_i + W_i(t) \quad \text{noise } W \text{ sets temperature}$$

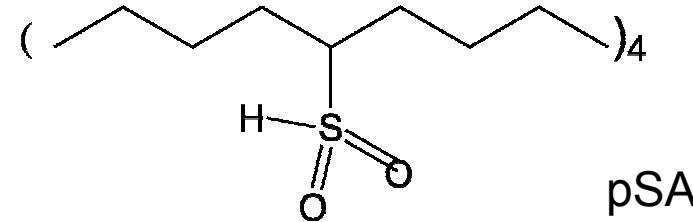
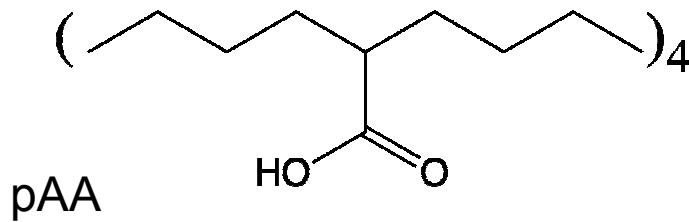
## System

- 800 chains of 35-36 beads; 4-12 charges per chain
- 1 counterion per charged bead;
- density  $\rho\sigma^3 = 0.7$  (polymer melt)

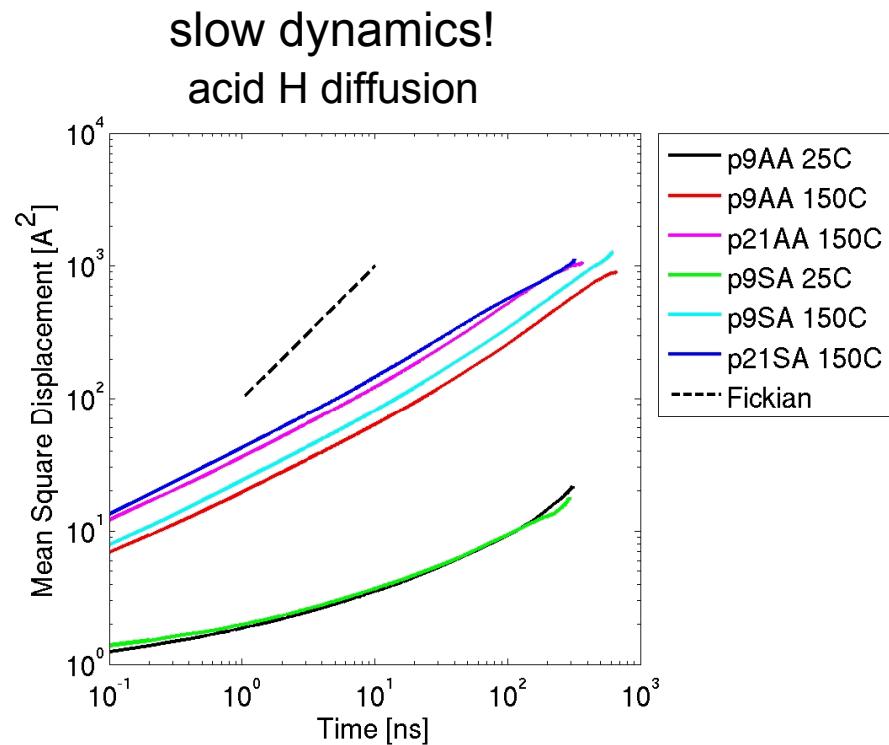
LAMMPS: open source MD code from Sandia

<http://lammps.sandia.gov/>

# Acid Copolymer Simulations

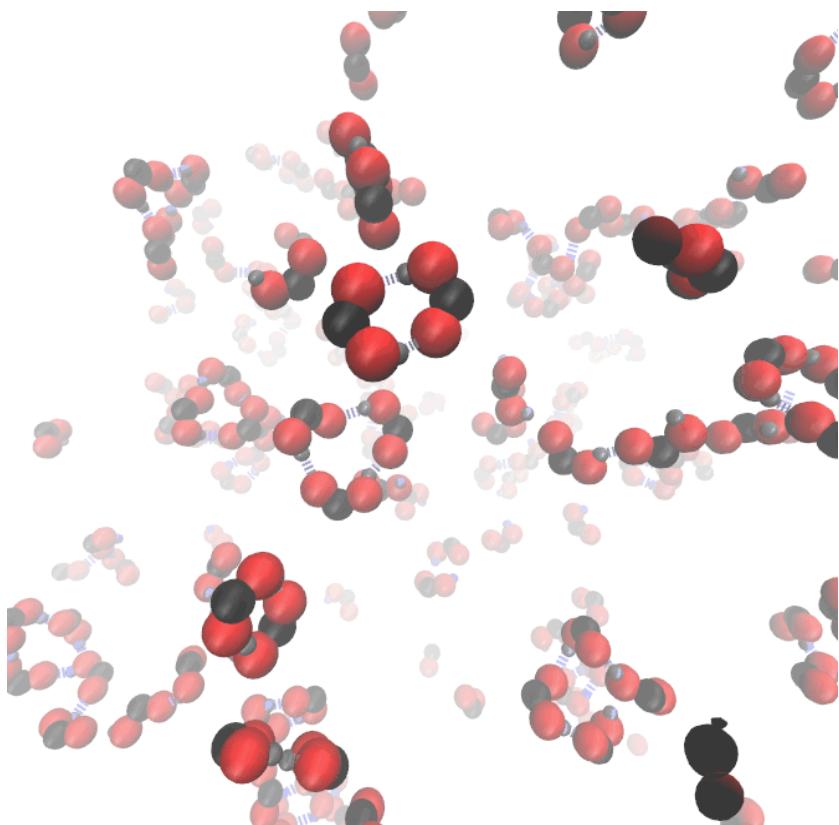


- all-atom OPLS force field
- p9AA, p9SA
  - 128 polymers
- p21AA, p21SA
  - 64 polymers
- box size  $55 \text{ \AA}^3$
- $150 \text{ }^\circ\text{C}$



# H-bonded Aggregates

p21AA



p21SA

