

InGaN LED efficiency droop without Auger

SAND2012-1224P

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Semiconductor lights, III-N material system

Efficiency challenge: intrinsic or extrinsic?

Thanks to:

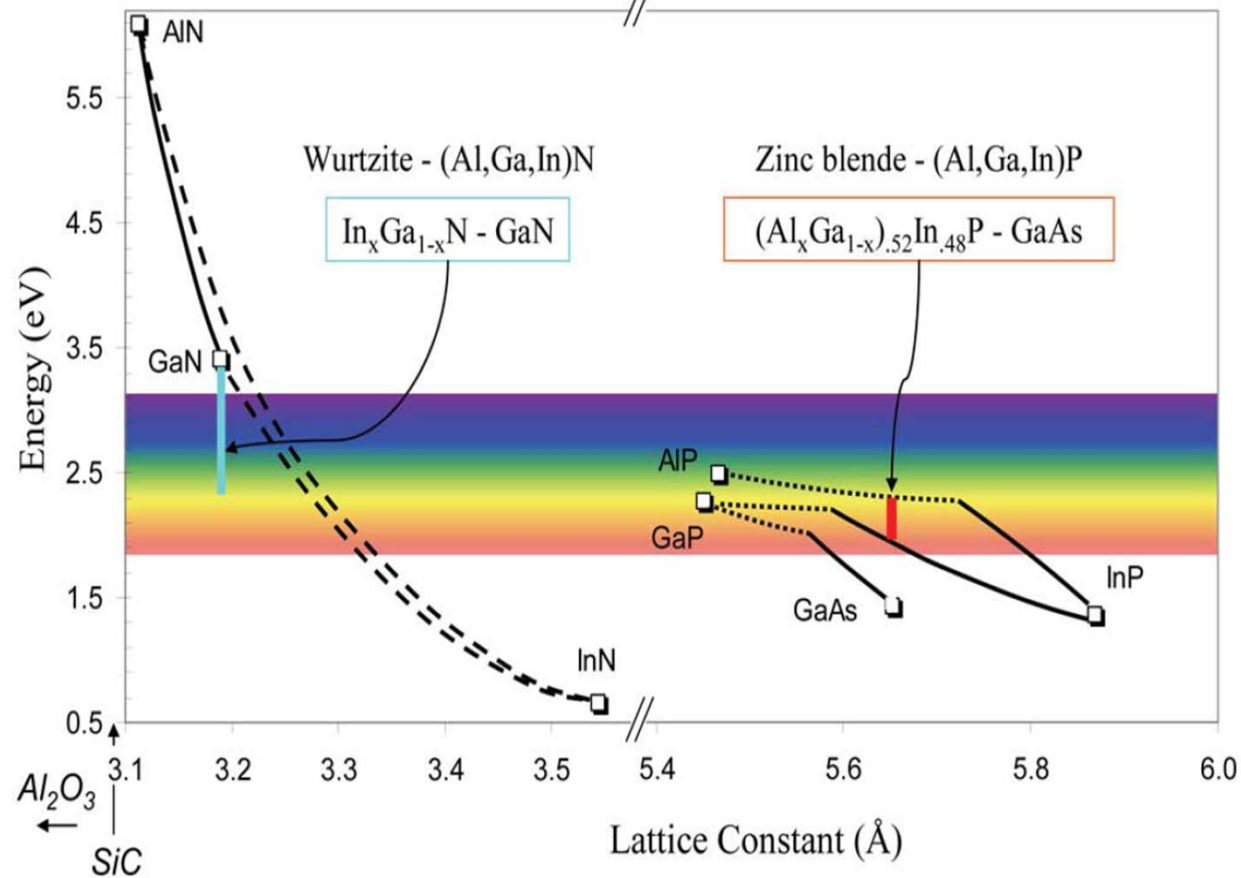
Sandia's Energy Frontier Research Center (EFRC)

DOE, Basic Energy Sciences

Sonderforschungsbereich (SFB) 787

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Wide bandgap Group-III Nitrides



Krames et al, J. Display Technology **3**, 1551 (2007)

Important applications: visible and ultraviolet lasers and LEDs

Interesting physics: Strong quantum-confined Stark effect
Strong many-body interaction

Significant excitation dependences in transition energies and matrix elements

Problem

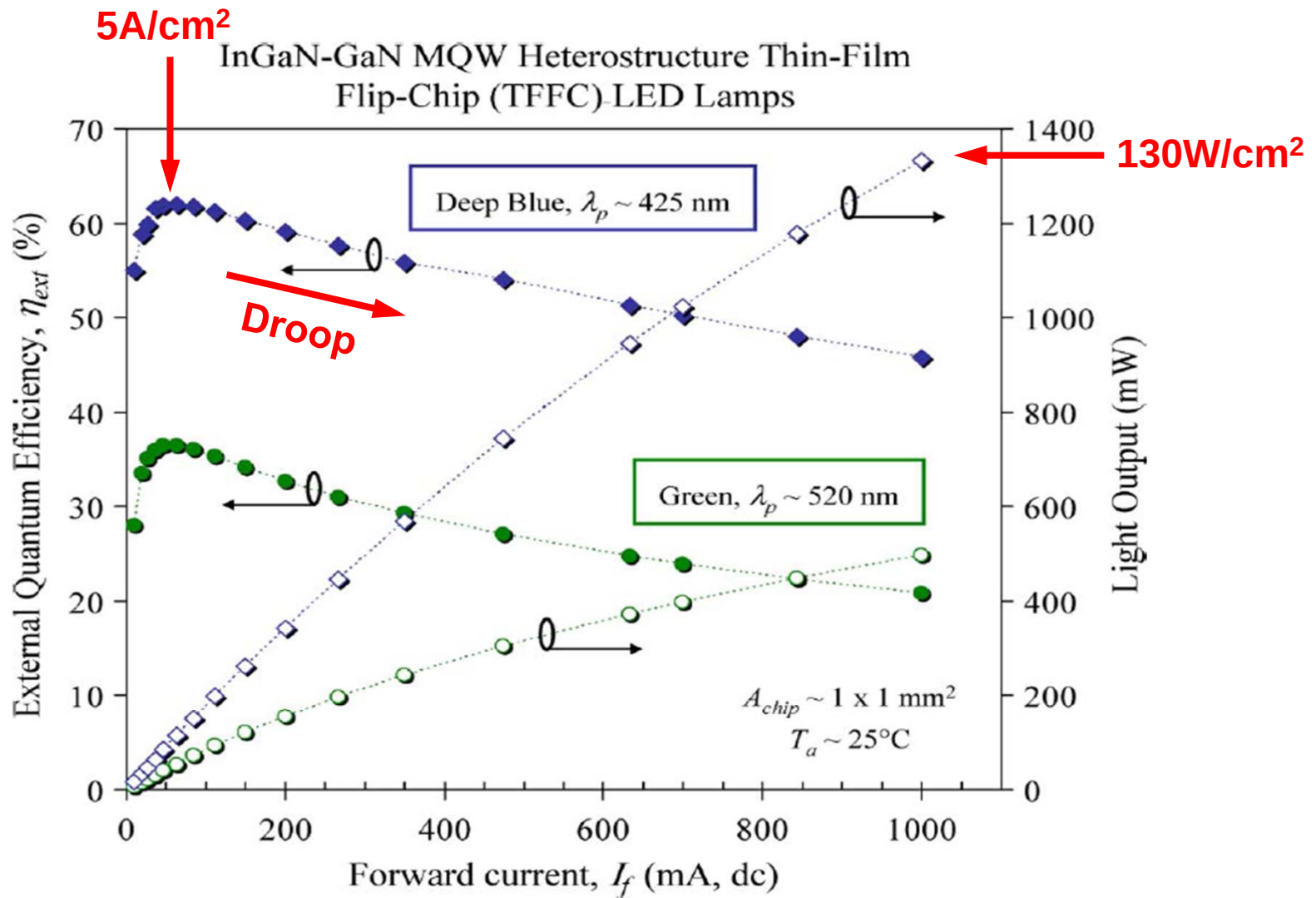


Fig. 8. External quantum efficiency and light output versus dc forward current for both blue and green InGaN-GaN QW-based TFFC LED lamps. Chip sizes are $1 \times 1 \text{ mm}^2$.

LED efficiency

Internal Quantum Efficiency

$$\frac{\text{\# photons created}}{\text{\# electrons injected}}$$

Wall plug efficiency

$$= \frac{\hbar\omega}{eV} \text{ IQE } \eta_{outcoupling}$$

External quantum efficiency (EQE)

Chemical potential separation $\frac{\mu_{eh}}{e} + IR$ **Series resistance**
(=0 for 'Manley-Rowe' limit)

ABC model for LED efficiency

Carrier density rate equation

Injection efficiency
(carrier overshoot and escape)

↓

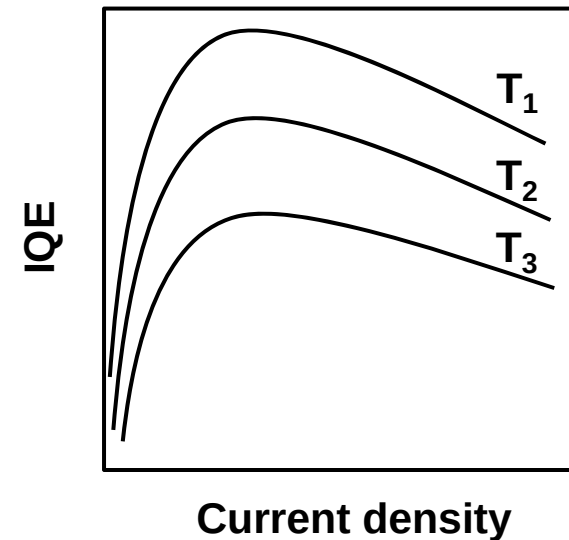
$$\frac{dN}{dt} = \frac{\eta_{inj} J}{ed} - AN - BN^2 - CN^3$$

Steady-state

$$\frac{dN}{dt} = 0 \rightarrow \frac{\eta_{inj} J}{ed} = AN + BN^2 + CN^3$$

Internal quantum efficiency

$$IQE = \frac{BN^2}{\frac{J}{ed}} = \frac{\eta_{inj} BN^2}{AN + BN^2 + CN^3}$$



ABC model for LED efficiency

Carrier density rate equation

Injection efficiency
(carrier overshoot and escape)

$$\frac{dN}{dt} = \frac{\eta_{inj} J}{ed} - \underset{\substack{\uparrow \\ \text{Defects}}}{AN} - \underset{\substack{\uparrow \\ \text{Spontaneous} \\ \text{emission}}}{BN^2} - \underset{\substack{\uparrow \\ \text{Auger}}}{CN^3}$$

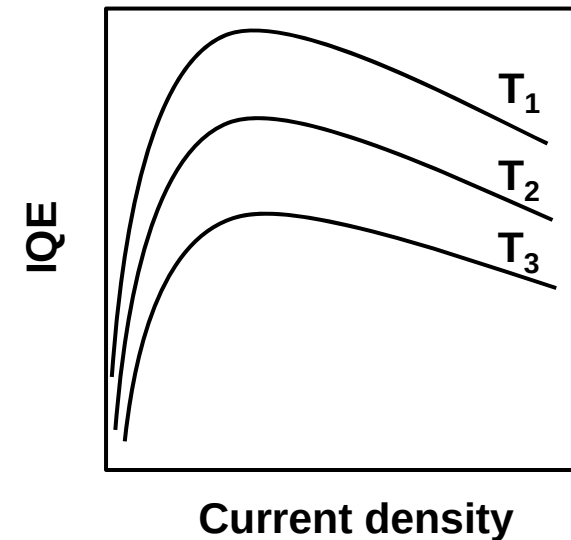
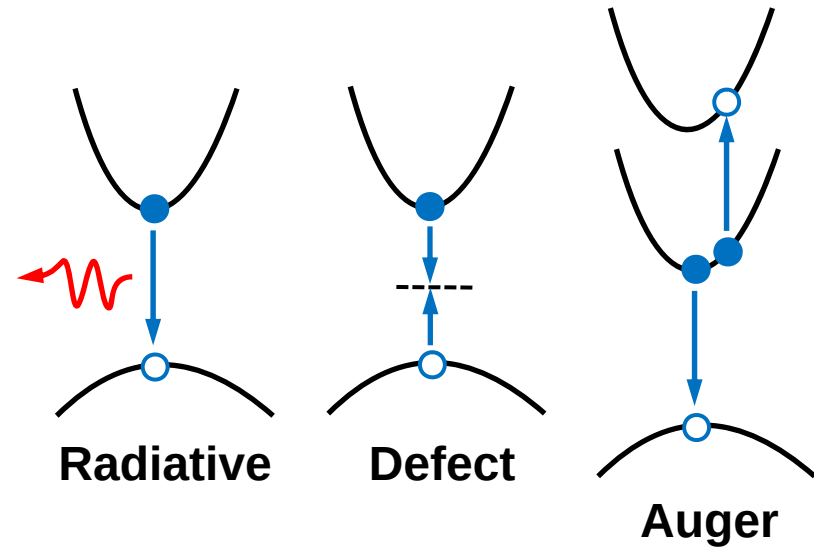
Steady-state

$$\frac{dN}{dt} = 0 \Rightarrow \frac{\eta_{inj} J}{ed} = AN + BN^2 + CN^3$$

Internal quantum efficiency

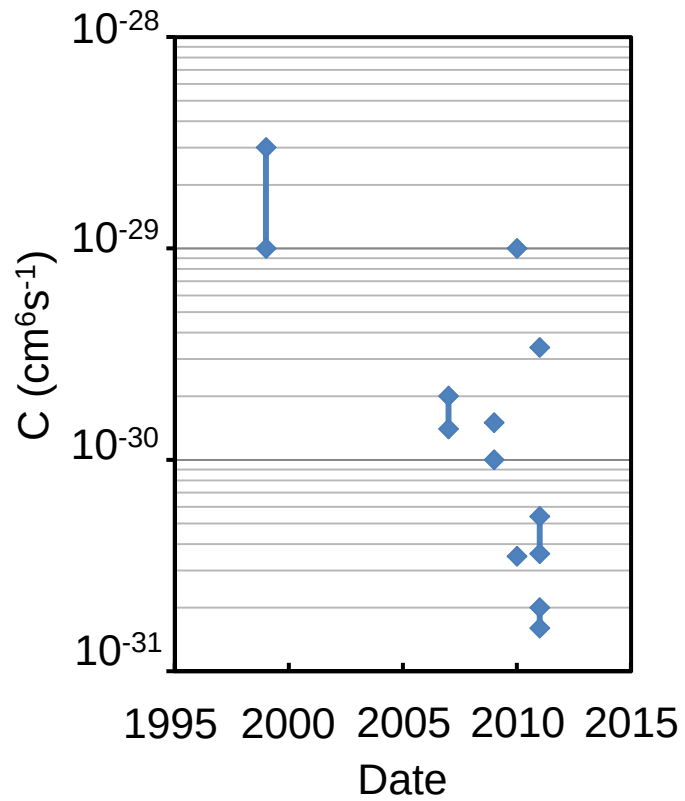
$$IQE = \frac{BN^2}{J} = \frac{\eta_{inj} BN^2}{AN + BN^2 + CN^3}$$

Carrier losses



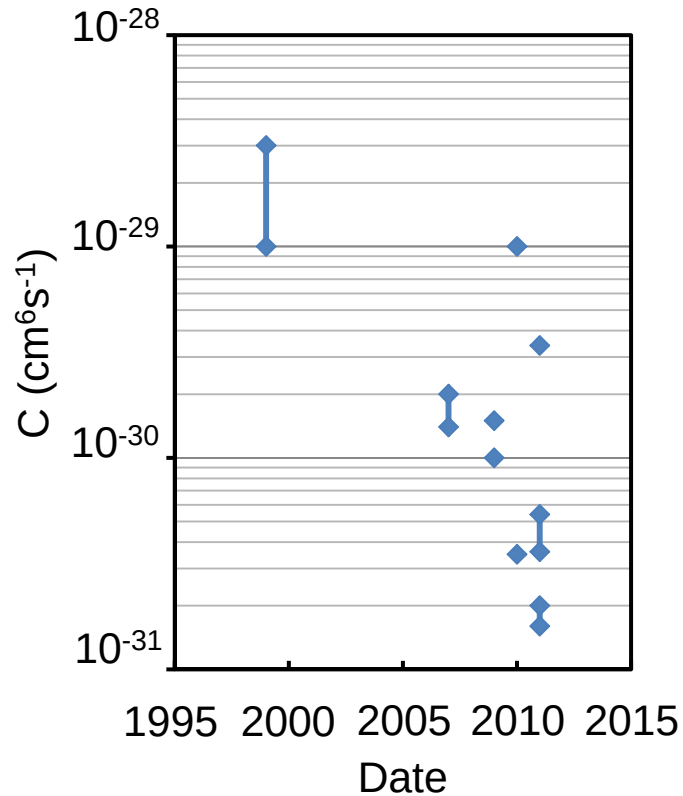
Motivations for a more detailed model

Variation in Auger coefficient from
IQE curve fitting with ABC model

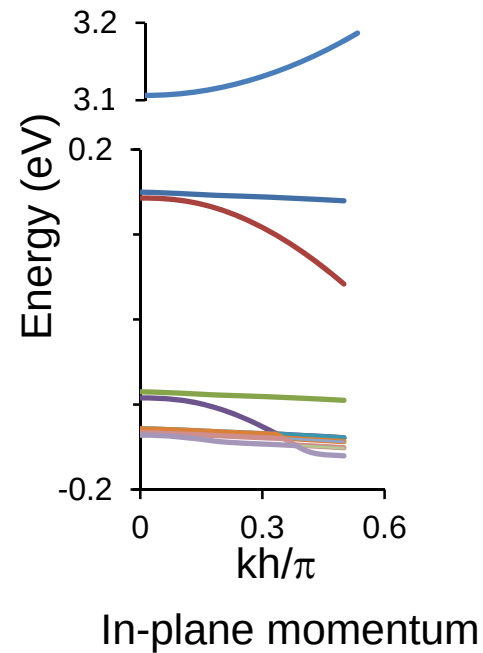


Motivations for a more detailed model

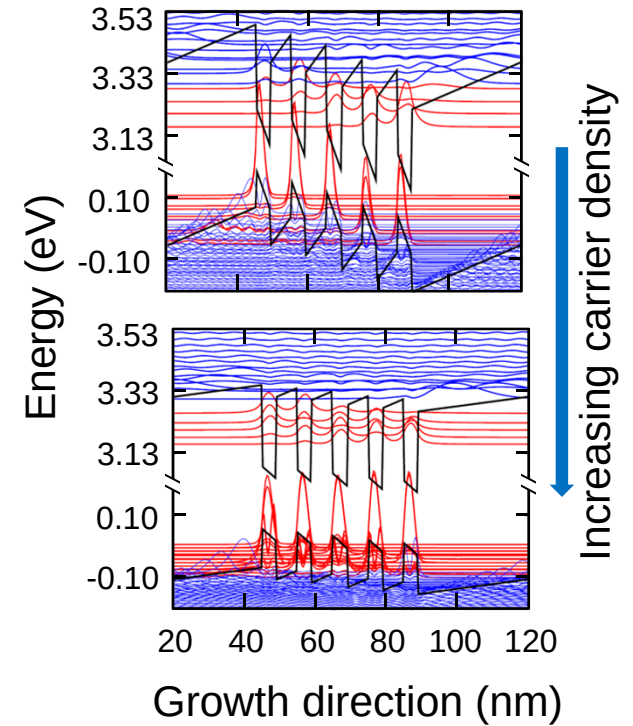
Variation in Auger coefficient from IQE curve fitting with ABC model



Energy dispersions



Carrier density dependent band structure changes



Approach

Hamiltonian

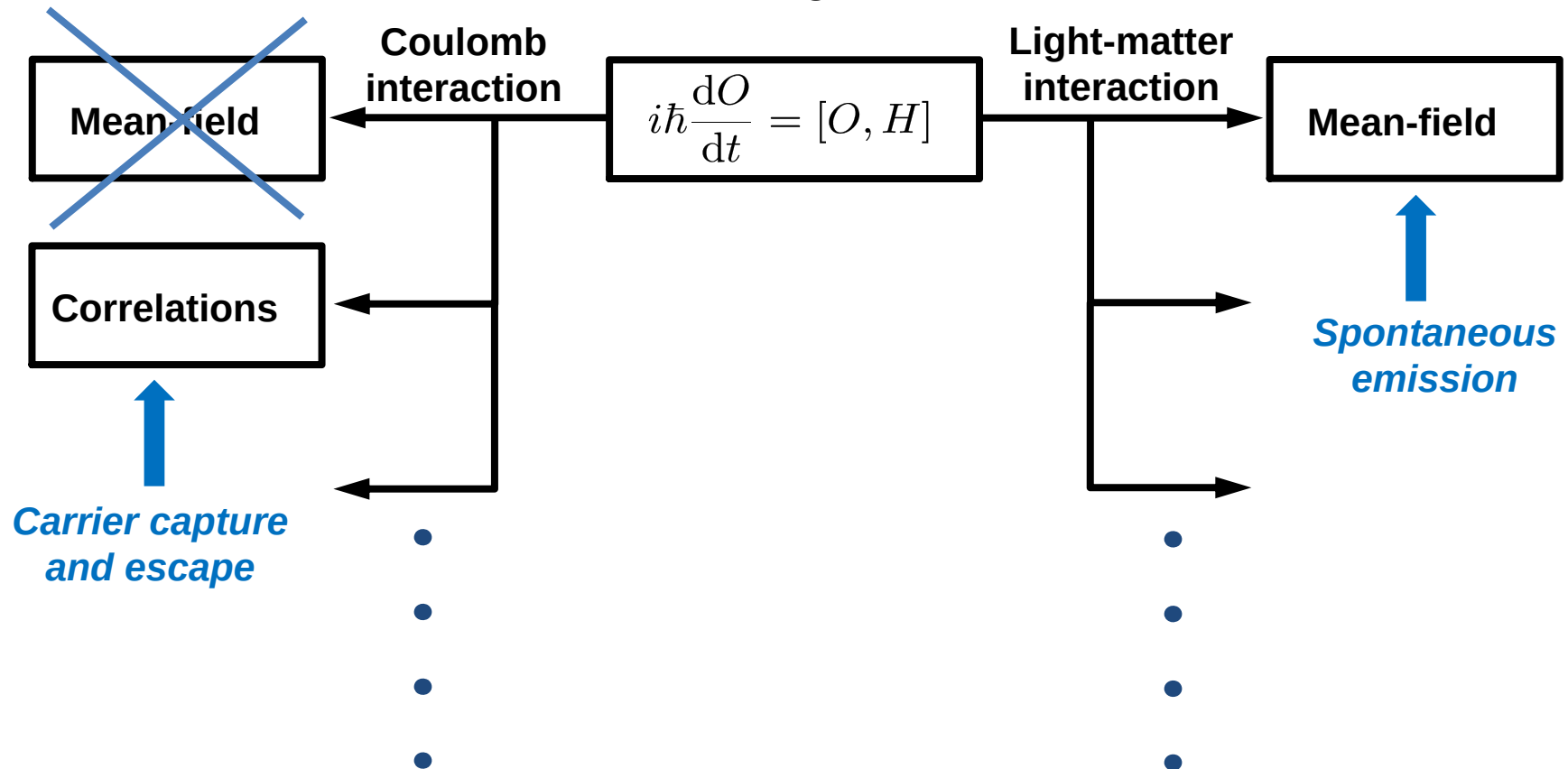
Single-particle energies

Light-matter interaction

$$H = \sum_i \varepsilon_i^e a_i^\dagger a_i + \sum_j \varepsilon_j^h b_j^\dagger b_j + \sum_q \hbar \Omega_q c_q^\dagger c_q - \sum_{i,j,q} \wp_{ij} \sqrt{\frac{\hbar \Omega_q}{V \epsilon_b}} (a_i b_j c_q^\dagger + c_q b_j^\dagger a_i^\dagger)$$

+ Coulomb interaction

Hiesenberg Picture



Model

$$\begin{aligned}
 \frac{dn_{\sigma, \alpha_{\sigma}, k_{\perp}}}{dt} &= -n_{\sigma, n_{\sigma}, k_{\perp}} \sum_{\alpha_{\sigma'}} b_{\alpha_{\sigma}, \alpha_{\sigma'}, k_{\perp}} n_{\sigma', \alpha_{\sigma'}, k_{\perp}} - A n_{\sigma, n_{\sigma}, k_{\perp}} \\
 &\quad - \gamma_{c-c} [n_{\sigma, n_{\sigma}, k_{\perp}} - f(\varepsilon_{\sigma, k_{\perp}}, \mu_{\sigma}, T)] \\
 &\quad - \gamma_{c-p} [n_{\sigma, n_{\sigma}, k_{\perp}} - f(\varepsilon_{\sigma, k_{\perp}}, \mu_{\sigma}^L, T_L)]
 \end{aligned}$$

e or h

$$\begin{aligned}
 \frac{dn_{\sigma, k}^b}{dt} &= -b_k n_{e, k}^b n_{h, k}^b + \frac{J}{e N_{\sigma}^p} f(\varepsilon_{\sigma, k}^b, \mu_{\sigma}^p, T_p) (1 - n_{\sigma, k}^b) + A_b n_{\sigma, k} \\
 &\quad - \gamma_{c-c} [n_{\sigma, k}^b - f(\varepsilon_{\sigma, k}^b, \mu_{\sigma}, T)] \\
 &\quad - \gamma_{c-p} [n_{\sigma, k}^b - f(\varepsilon_{\sigma, k}^b, \mu_{\sigma}^L, T_L)]
 \end{aligned}$$

Similar for holes

Model

$\frac{dn_{\sigma, \alpha_{\sigma}, k_{\perp}}}{dt} = \underbrace{-n_{\sigma, n_{\sigma}, k_{\perp}} \sum_{\alpha_{\sigma'}} b_{\alpha_{\sigma}, \alpha_{\sigma'}, k_{\perp}} n_{\sigma', \alpha_{\sigma'}, k_{\perp}} - A n_{\sigma, n_{\sigma}, k_{\perp}}}_{\text{Spontaneous emission } (> \text{ns})}$

$\underbrace{-\gamma_{c-c} [n_{\sigma, n_{\sigma}, k_{\perp}} - f(\varepsilon_{\sigma, k_{\perp}}, \mu_{\sigma}, T)] - \gamma_{c-p} [n_{\sigma, n_{\sigma}, k_{\perp}} - f(\varepsilon_{\sigma, k_{\perp}}, \mu_{\sigma}^L, T_L)]}_{\text{Carrier injection}}$

$\frac{dn_{\sigma, k}^b}{dt} = \underbrace{-b_k n_{e, k}^b n_{h, k}^b}_{\text{Spontaneous emission } (> \text{ns})} + \underbrace{\frac{J}{e N_{\sigma}^p} f(\varepsilon_{\sigma, k}^b, \mu_{\sigma}^p, T_p) (1 - n_{\sigma, k}^b) + A_b n_{\sigma, k}}_{\text{Carrier injection}}$

$\underbrace{-\gamma_{c-c} [n_{\sigma, k}^b - f(\varepsilon_{\sigma, k}^b, \mu_{\sigma}, T)] - \gamma_{c-p} [n_{\sigma, k}^b - f(\varepsilon_{\sigma, k}^b, \mu_{\sigma}^L, T_L)]}_{\text{Carrier injection}}$

Similar for holes

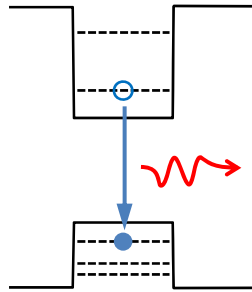
Model

$$\frac{dn_{\sigma,\alpha_{\sigma},k_{\perp}}}{dt} = \underbrace{-n_{\sigma,n_{\sigma},k_{\perp}} \sum_{\alpha_{\sigma'}} b_{\alpha_{\sigma},\alpha_{\sigma'},k_{\perp}} n_{\sigma',\alpha_{\sigma'},k_{\perp}} - A n_{\sigma,n_{\sigma},k_{\perp}}}_{\text{Spontaneous emission } (>\text{ns})}$$

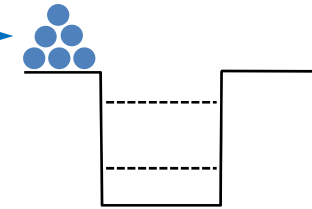
$$- \gamma_{c-c} [n_{\sigma,n_{\sigma},k_{\perp}} - f(\varepsilon_{\sigma,k_{\perp}}, \mu_{\sigma}, T)]$$

$$- \gamma_{c-p} [n_{\sigma,n_{\sigma},k_{\perp}} - f(\varepsilon_{\sigma,k_{\perp}}, \mu_{\sigma}^L, T_L)]$$

Spontaneous emission (>ns)

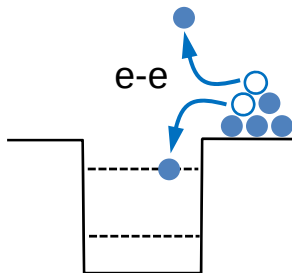


Carrier injection

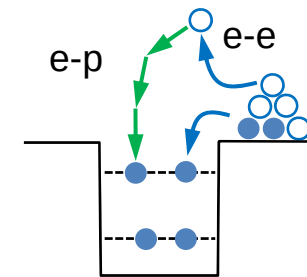


$$\frac{dn_{\sigma,k}^b}{dt} = \underbrace{-b_k n_{e,k}^b n_{h,k}^b}_{\text{Carrier-carrier (100fs)}} + \underbrace{\frac{J}{e N_{\sigma}^p} f(\varepsilon_{\sigma,k}^b, \mu_{\sigma}^p, T_p) (1 - n_{\sigma,k}^b) + A_b n_{\sigma,k}}_{\text{Carrier-phonon } (<1\text{ps})}$$

Carrier-carrier (100fs)

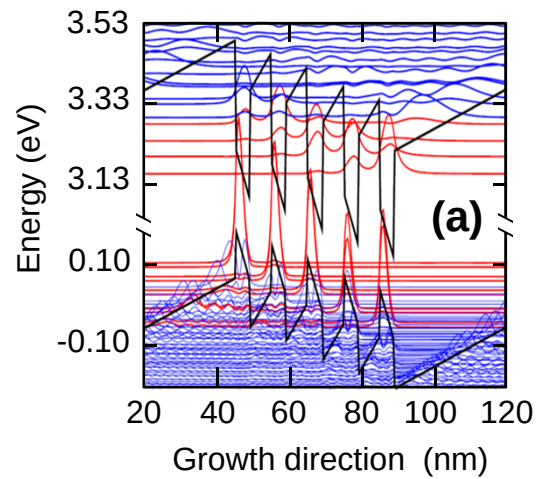
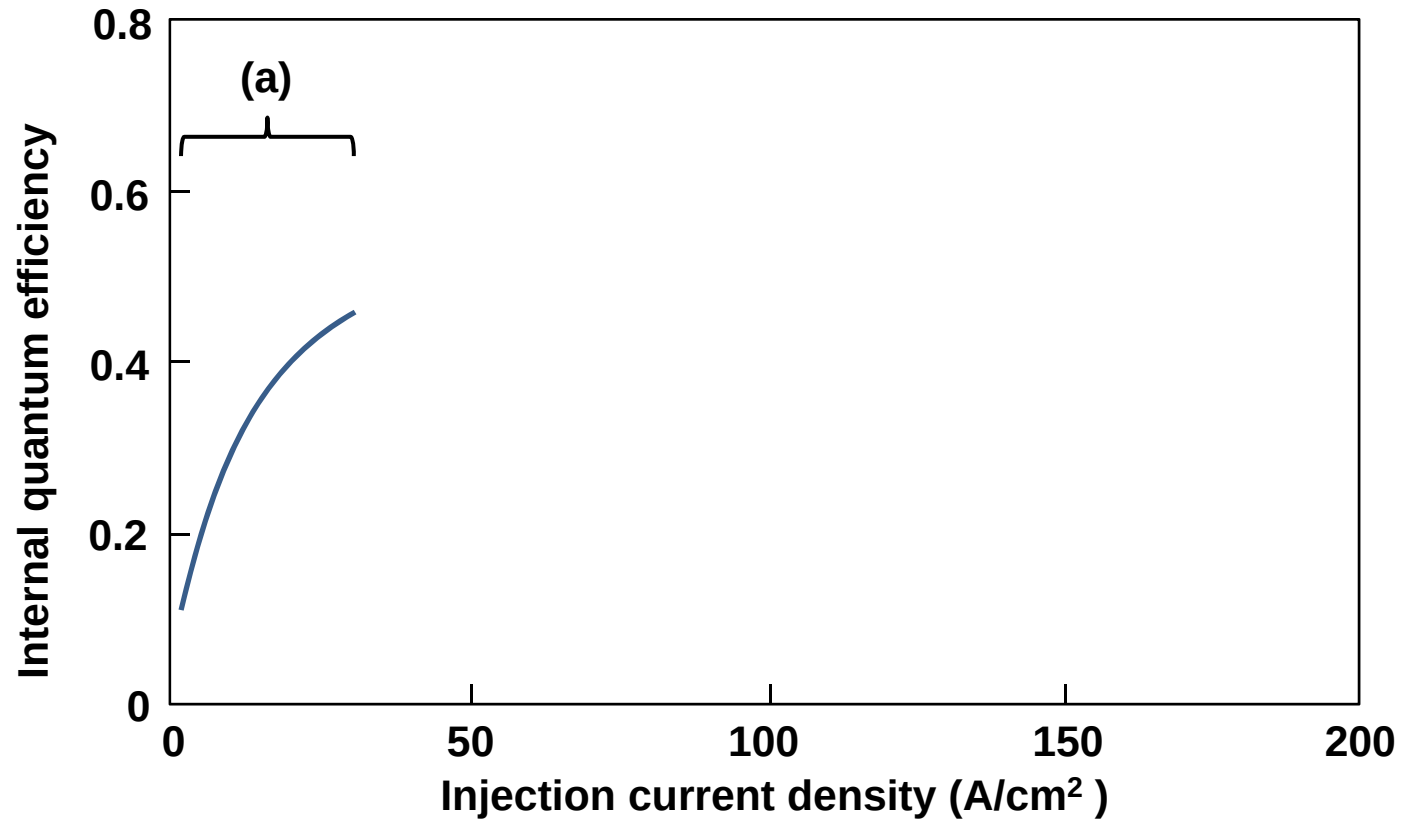


Carrier-phonon (<1ps)

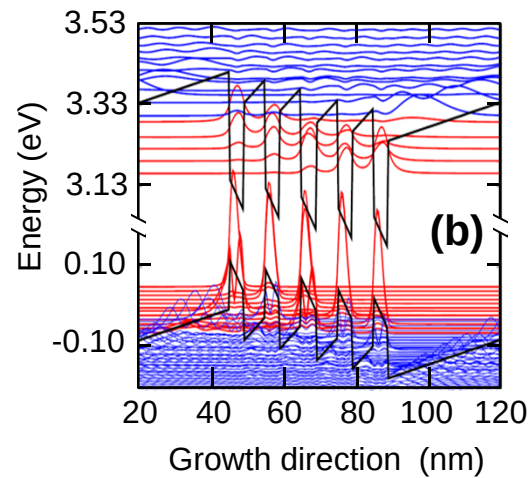
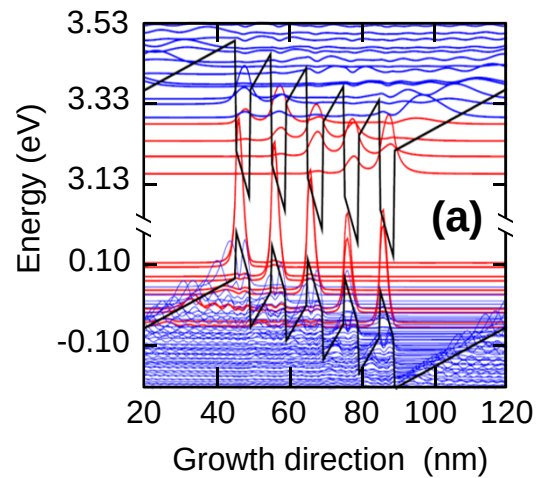
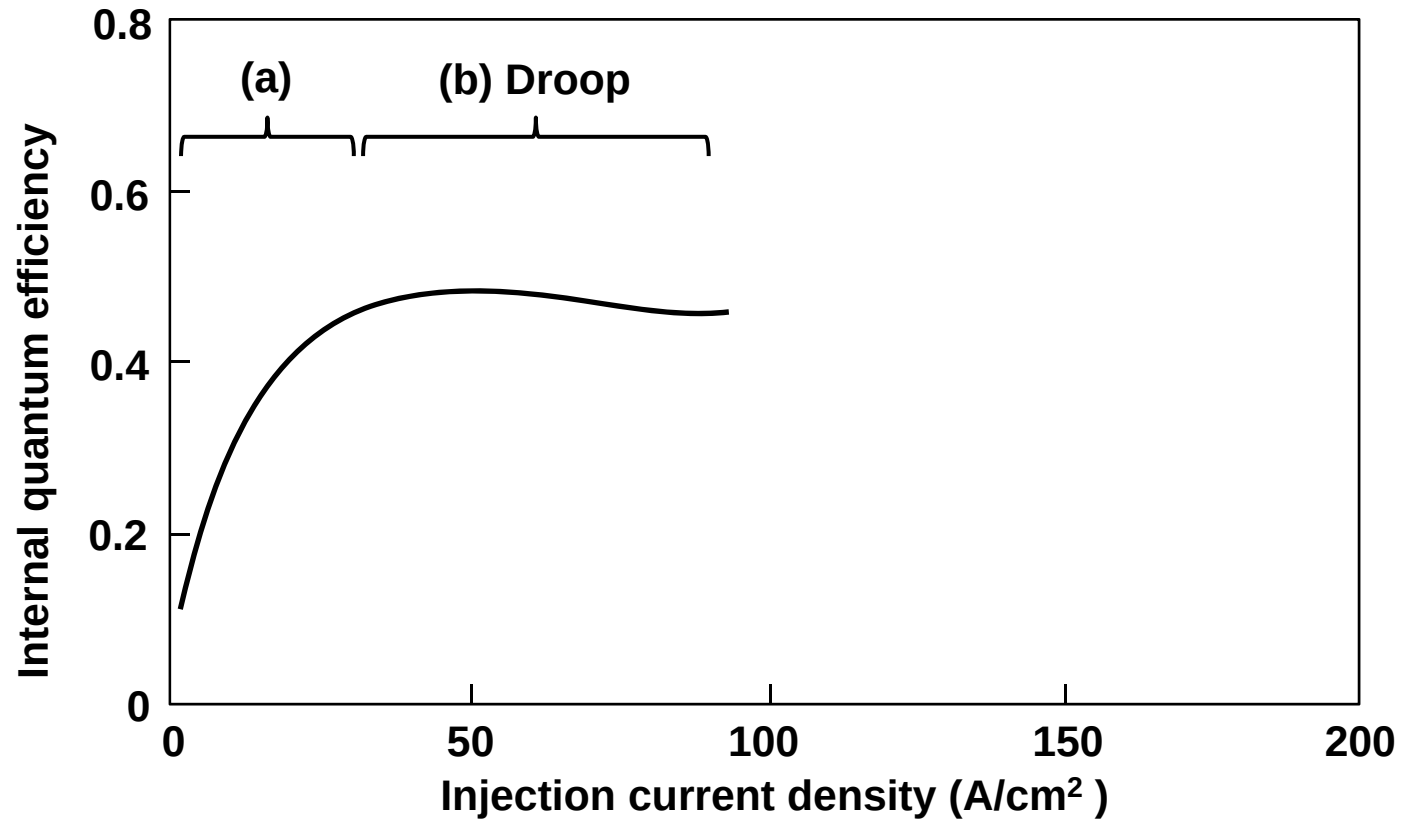


Similar for holes

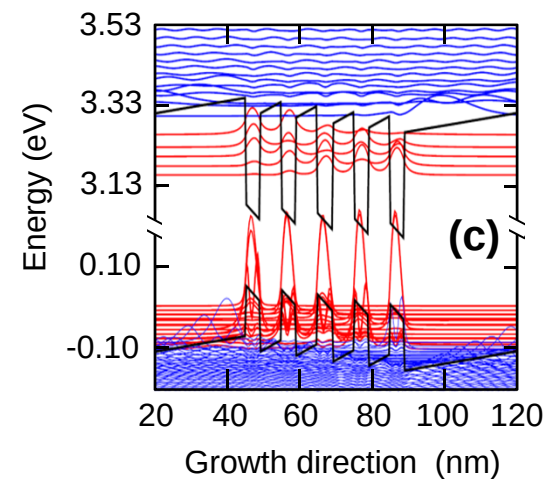
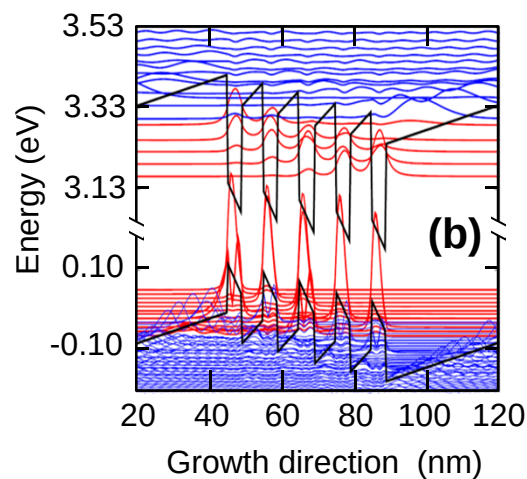
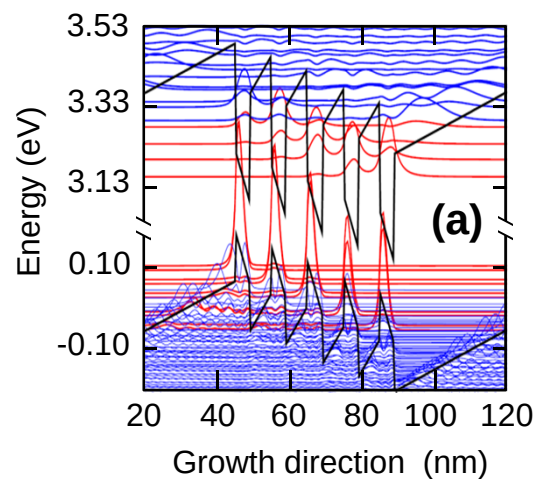
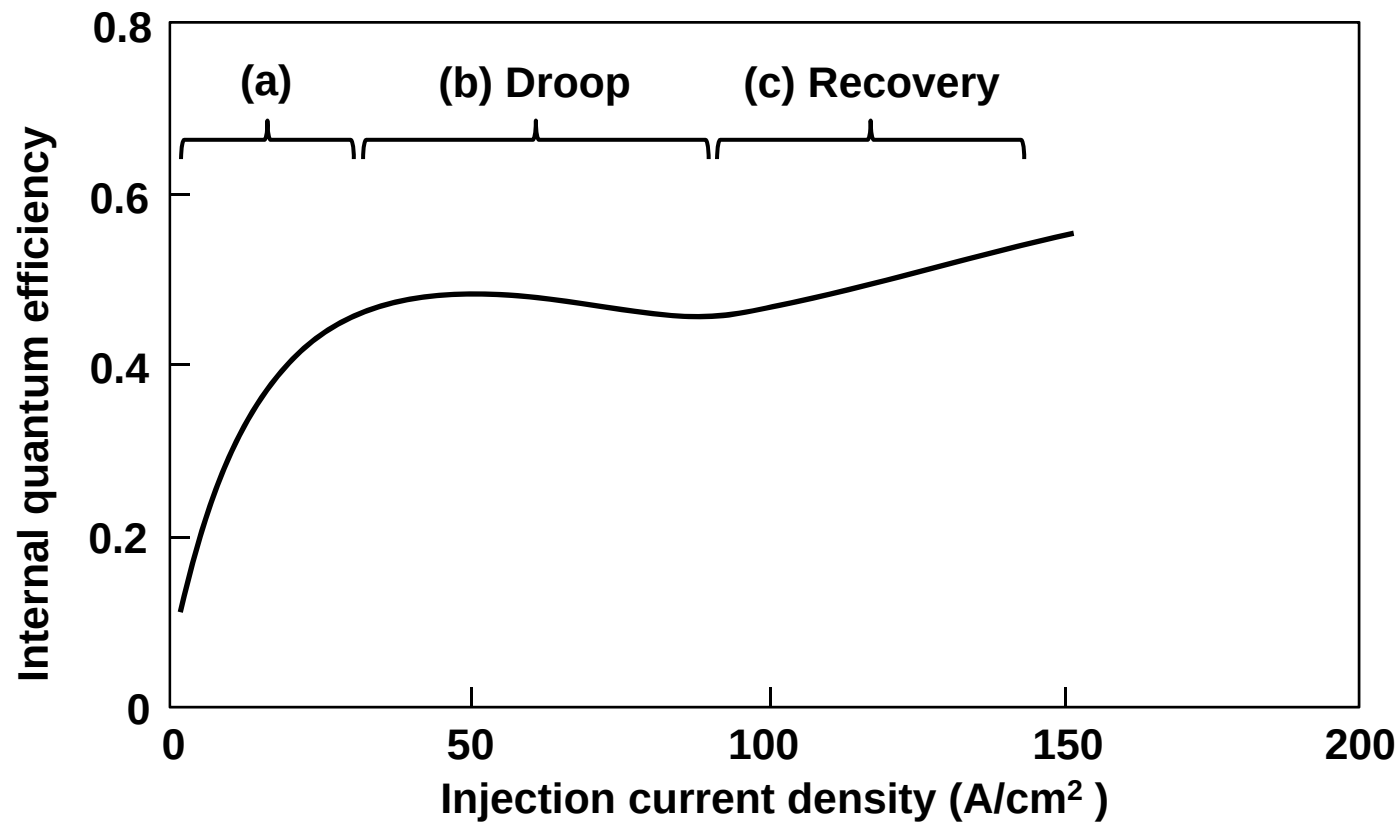
4nm In_{0.2}Ga_{0.8}N/6nmGaN, $T_L = 300\text{K}$, $\gamma_{c-c} = 5 \times 10^{13}\text{s}^{-1}$, $\gamma_{c-c} = 10^{13}\text{s}^{-1}$, $A = 10^{-7}\text{s}^{-1}$, $C = 0$



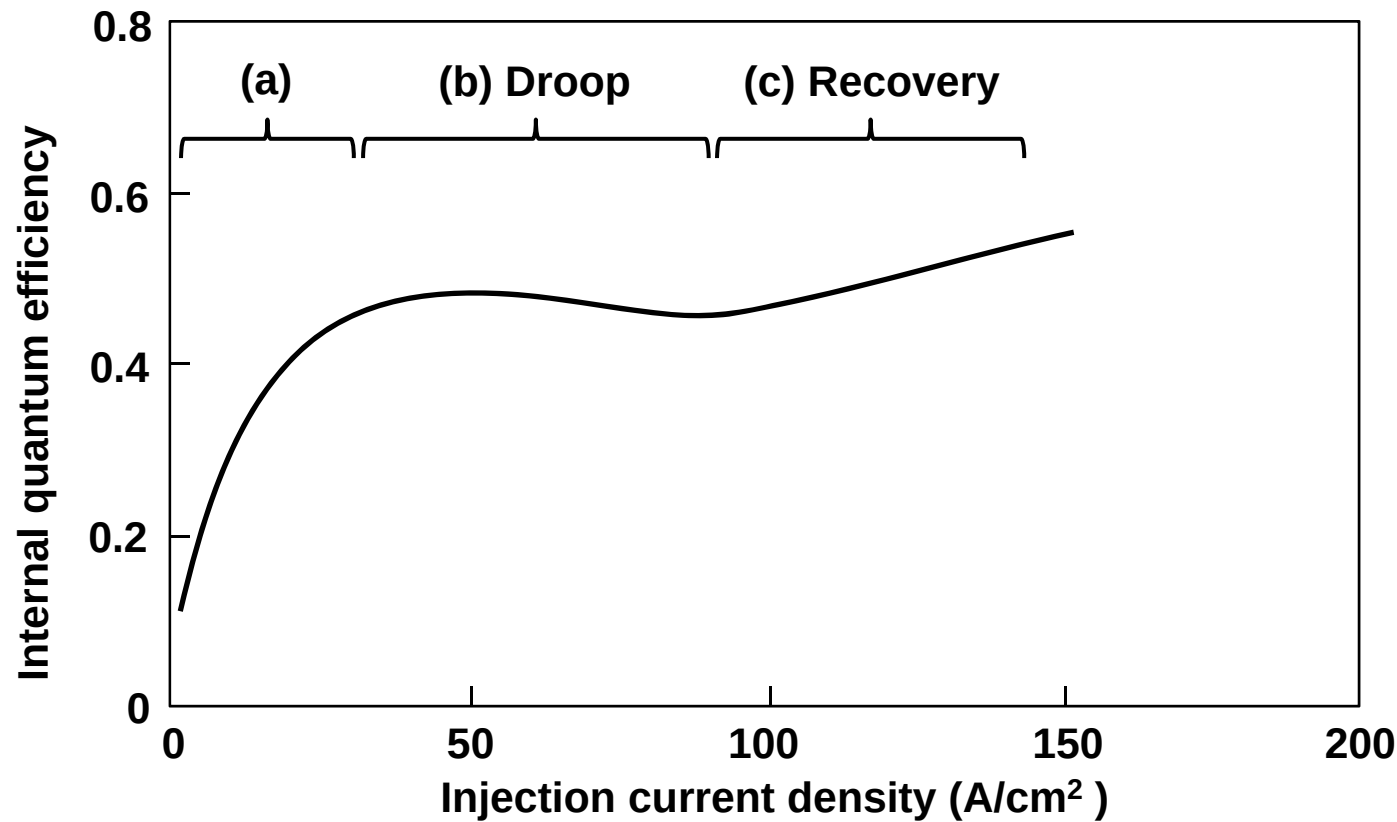
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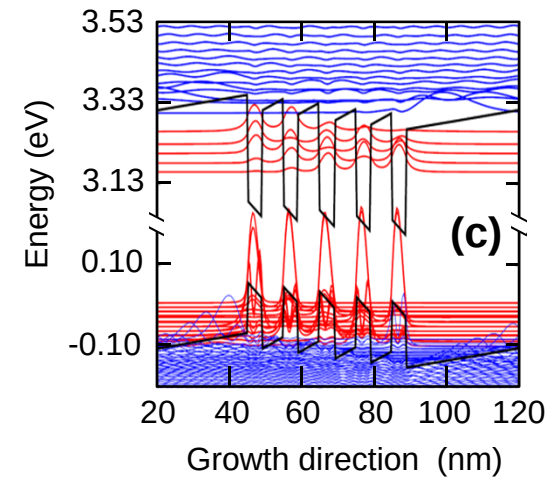
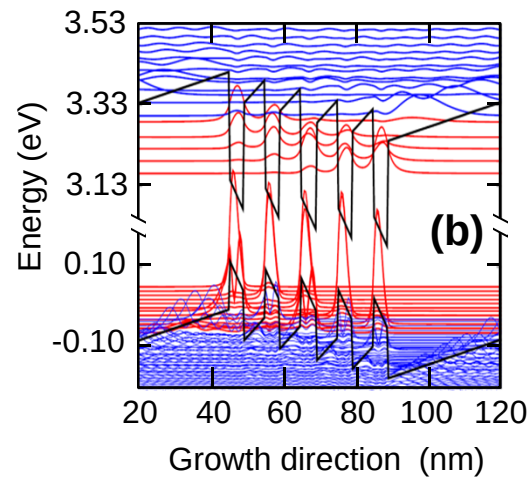
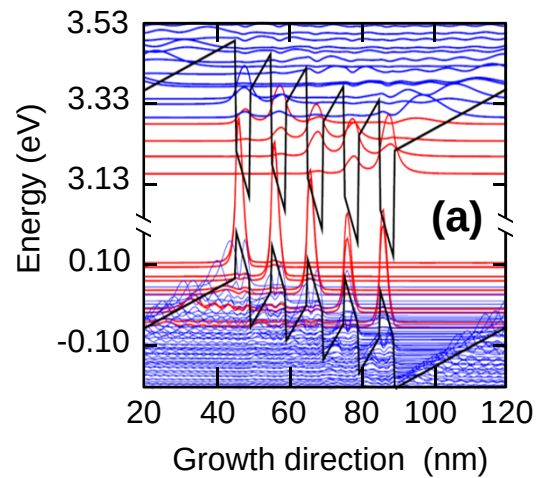
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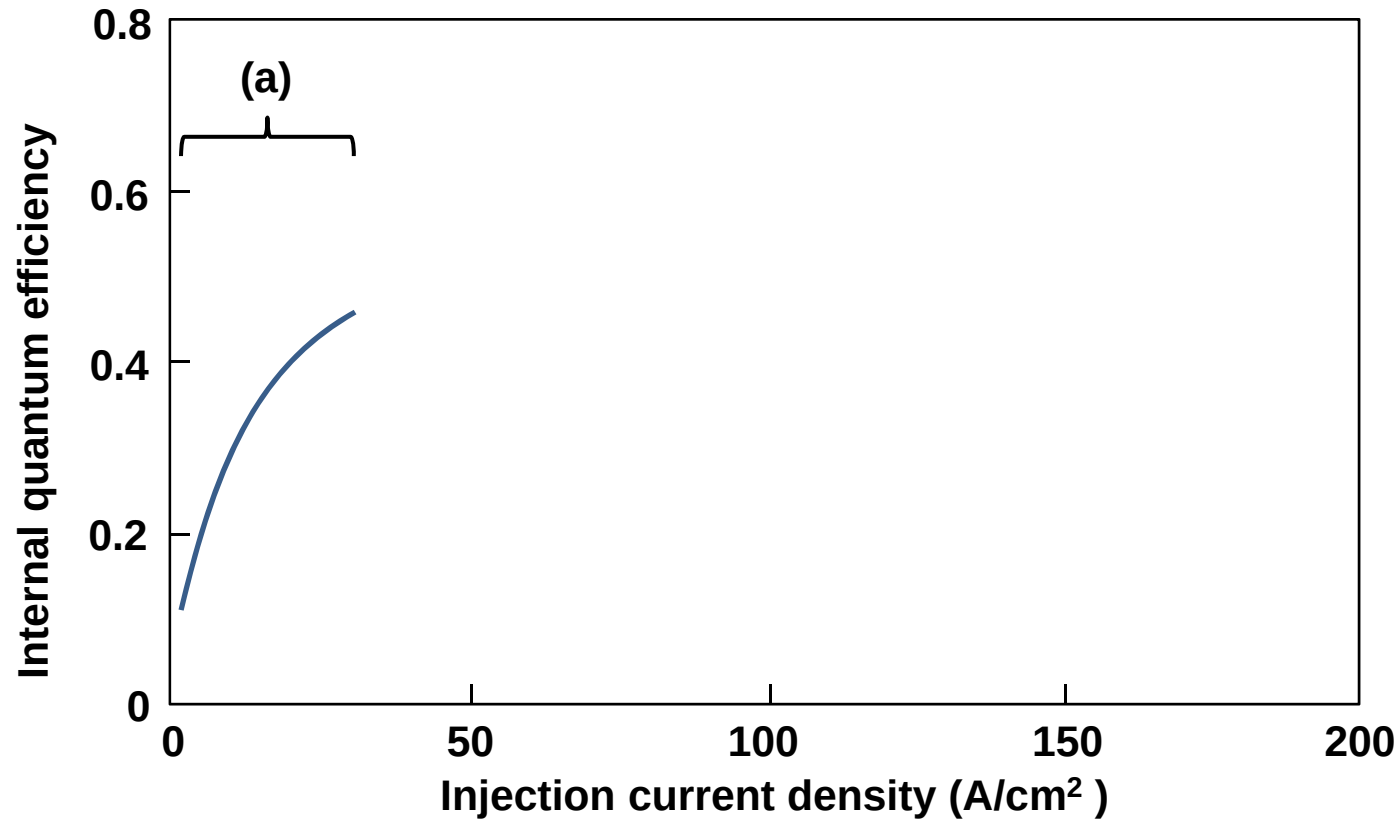
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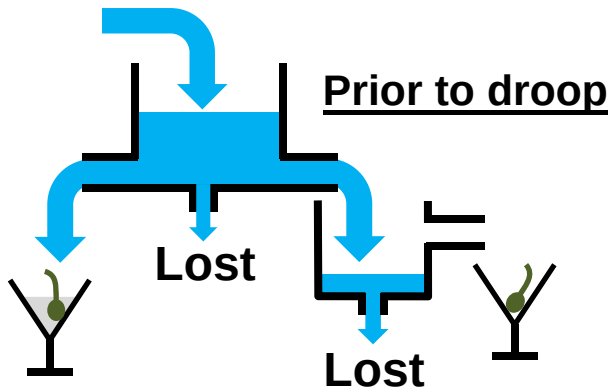
No Auger!



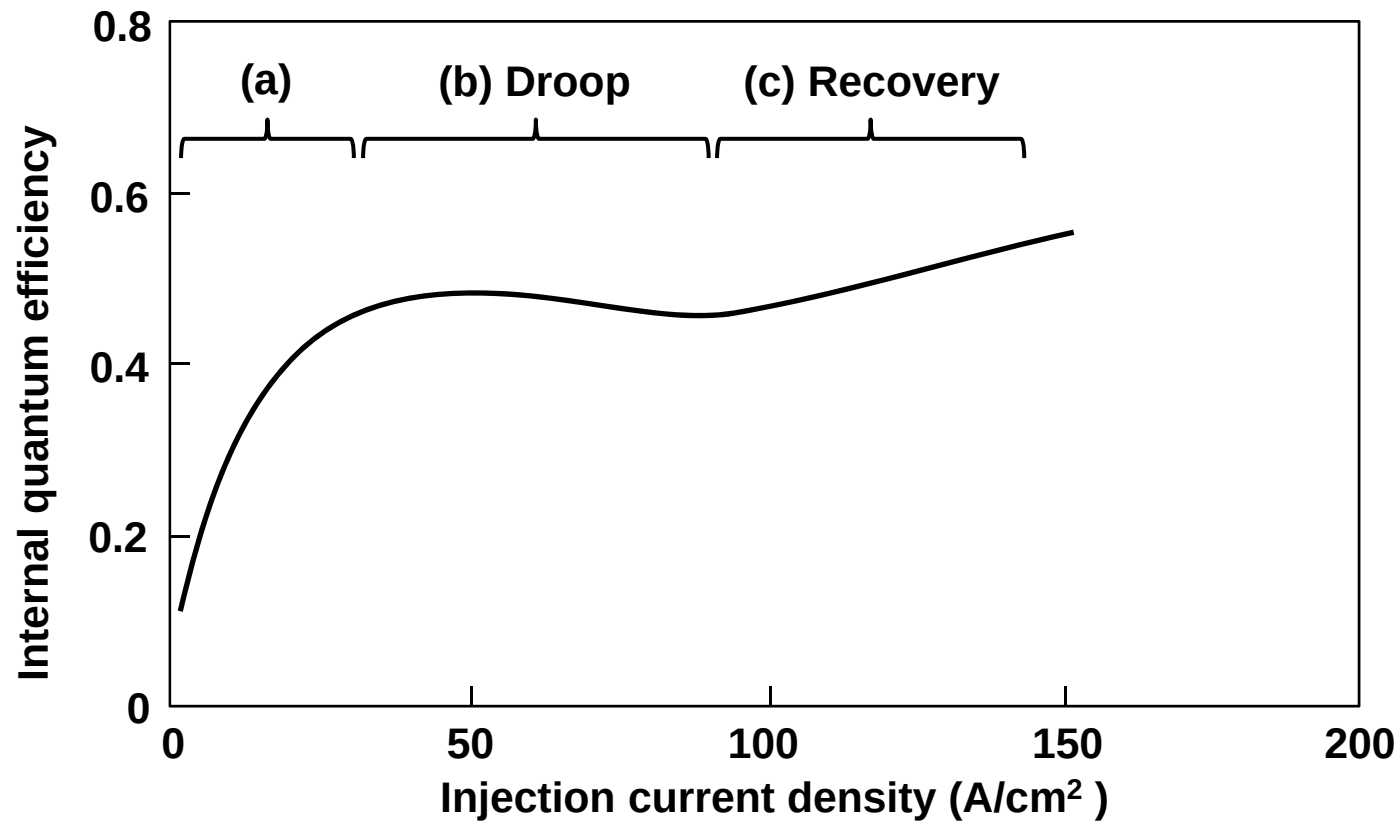
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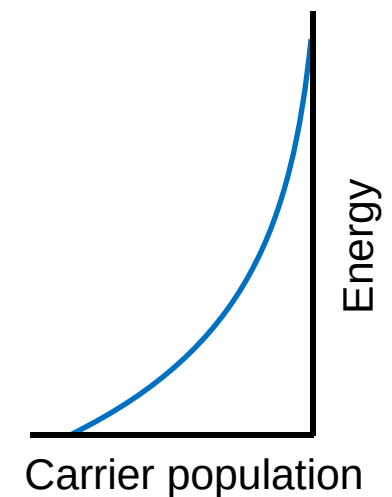
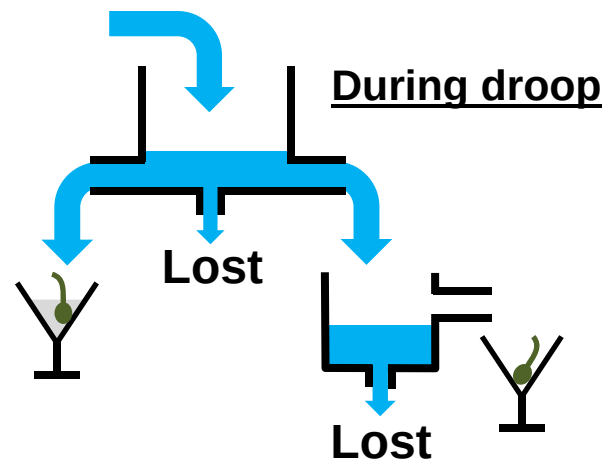
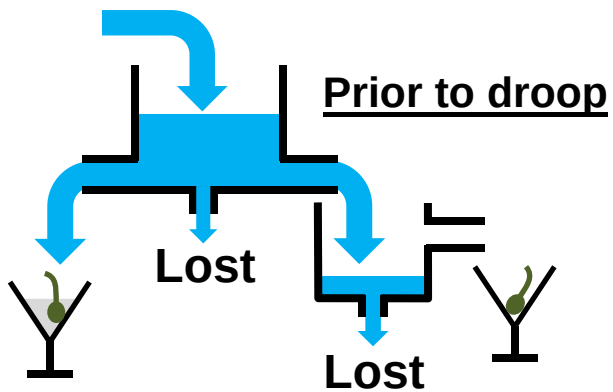
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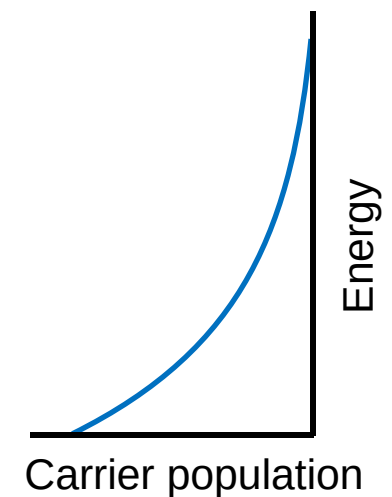
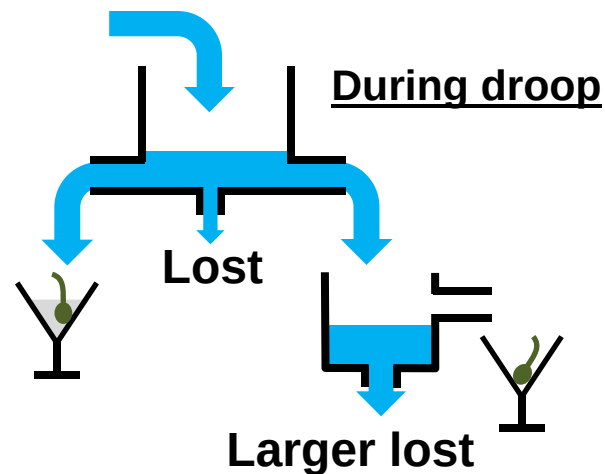
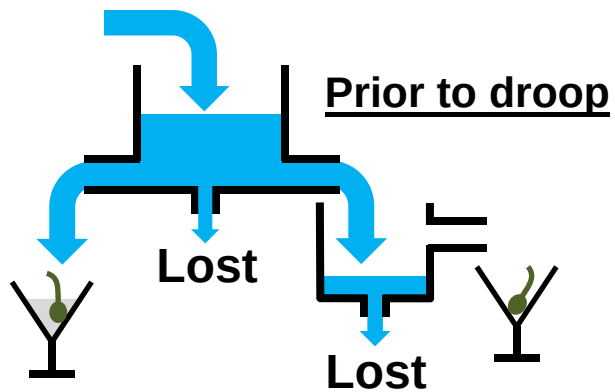
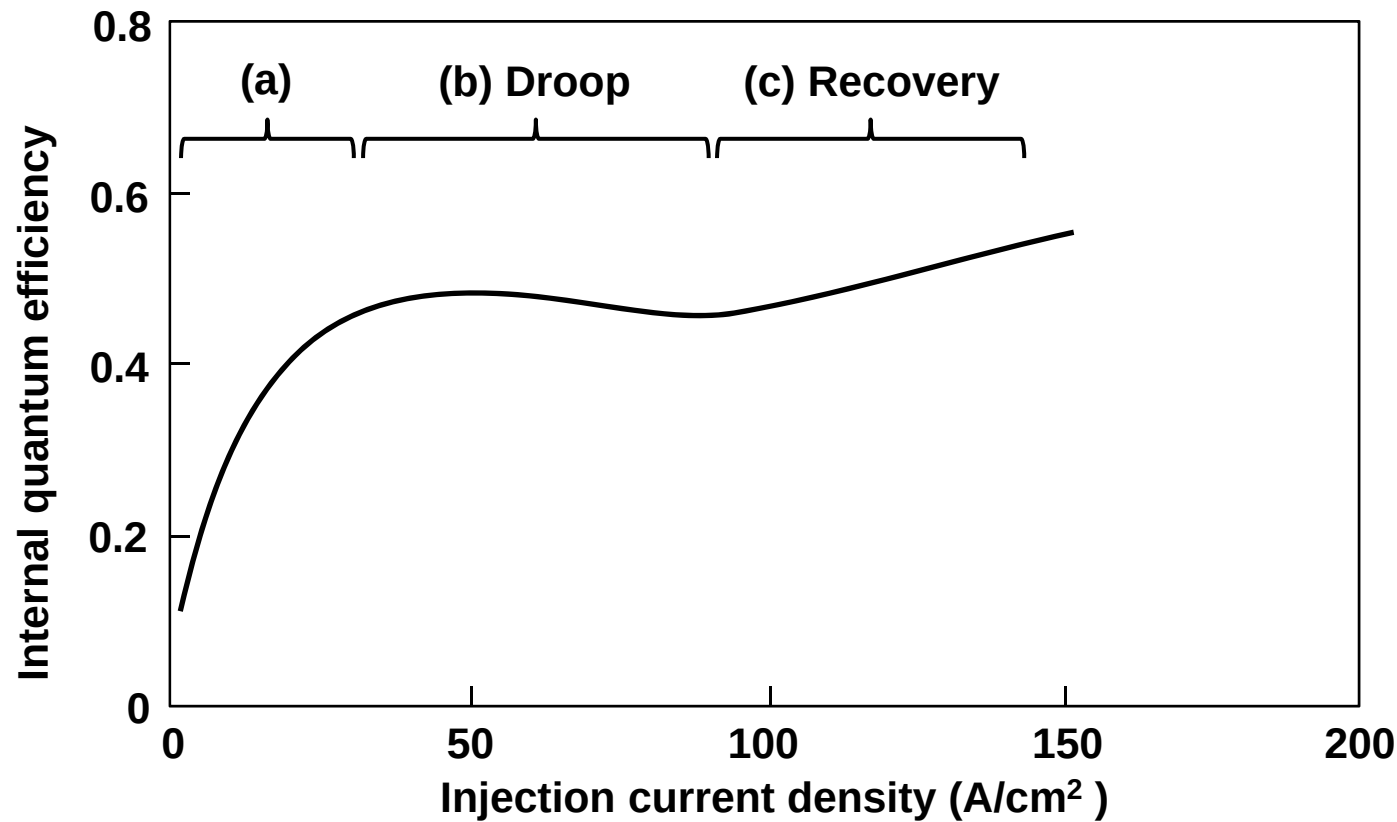
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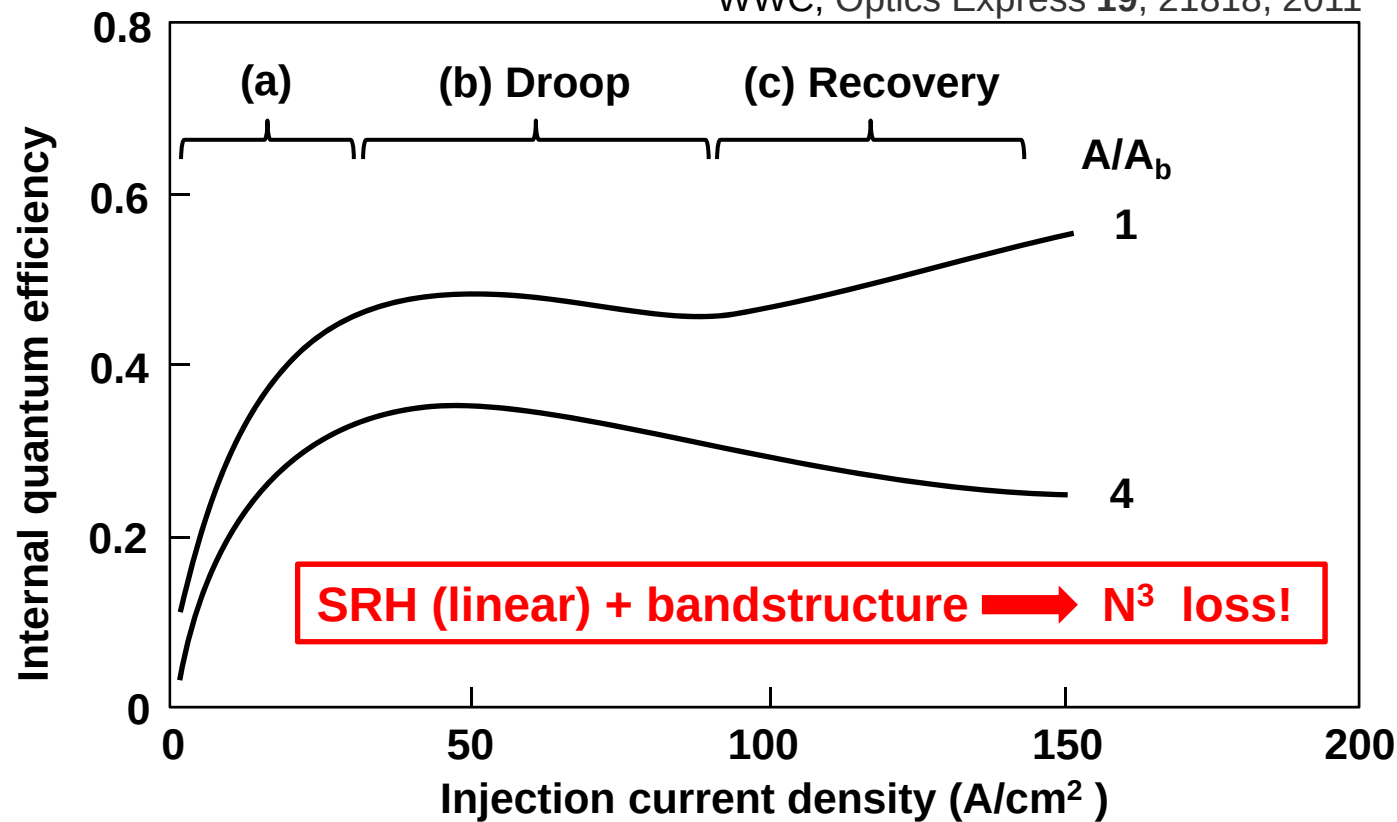


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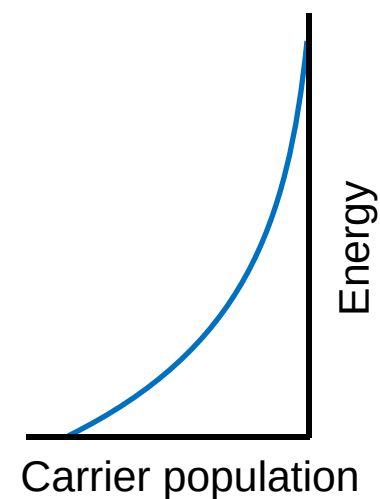
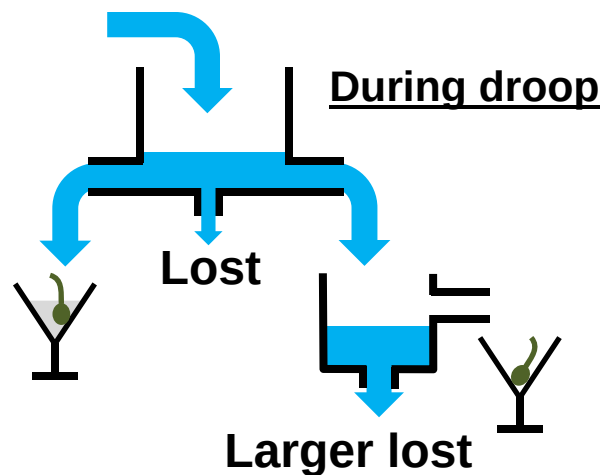
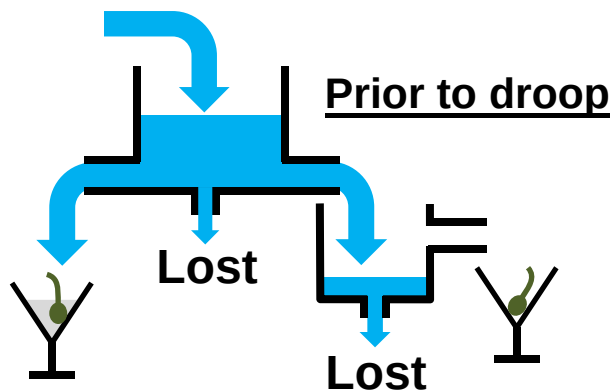


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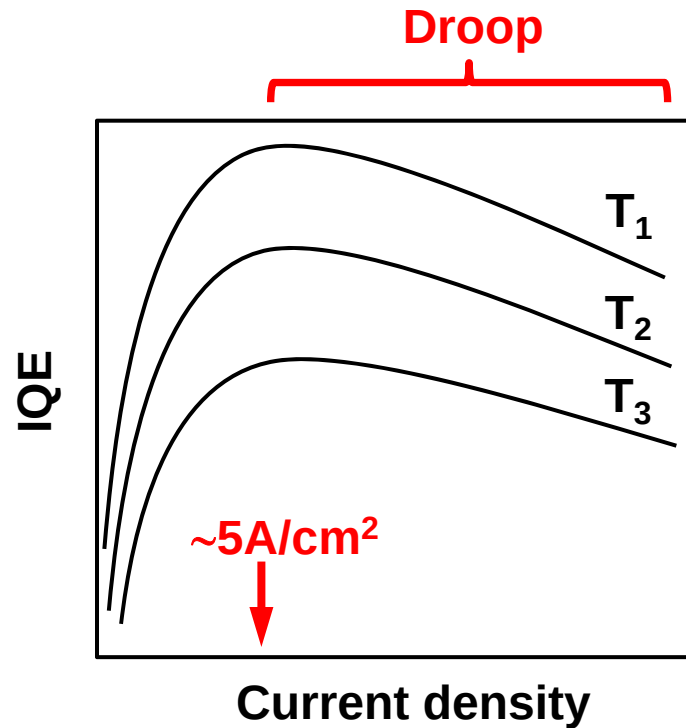
WWC, Optics Express **19**, 21818, 2011



No Auger!



Summary



Can fit experiment with :
$$\text{IQE} = \frac{BN^2}{AN + BN^2 + CN^3}$$

?

Extrinsic

Localization

Current leakage

Defect loss

?

Intrinsic

Auger

Screening of
piezoelectric field