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# Active Reflective Components for Adaptive Optical Zoom Systems

Matthew E. L. Jungwirth

Doctoral Defense

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Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

# Outline

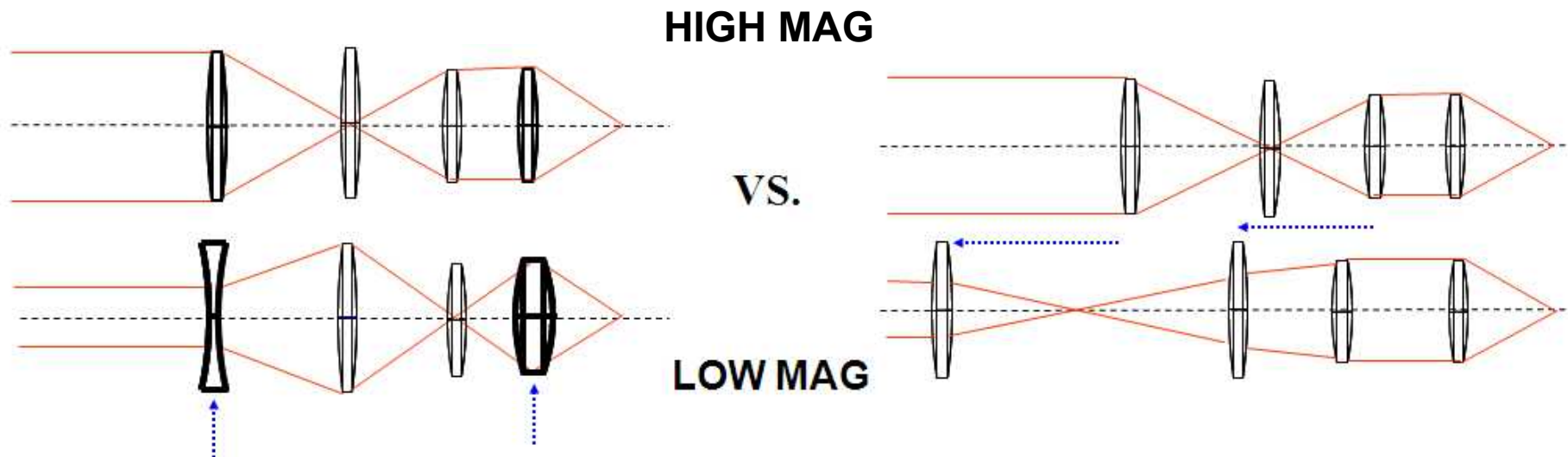
- Goal of research
- Overview of adaptive optical zoom
- Design theory of adaptive optical zoom
  - Derivation of theory
  - Tradespace analysis
  - Results in Zemax
- Active CFRP mirror
  - Design of active mirror system
  - Active mirror testbed to test mirror
  - Results
  - Improvements
- Summary

# Goal of Research

- Derive optical design theory for adaptive optical zoom systems
  - Two-element, Cassegrain objective
  - Tradespace analysis to analyze millions of designs
  - Design large-aperture, two-state system
- Design, construct, and test a large-aperture active mirror
  - Change radius of curvature
  - Clear aperture is 160mm
  - Mirror fabricated of carbon fiber reinforced polymer (CFRP)
- Adaptive optical zoom system
  - Design system with theory/tradespace analysis
  - Utilize developed mirror in actual system
  - Applications are defense/aerospace

# Adaptive optical zoom

- Traditionally move elements along optical axis for zoom
- Adaptive optical zoom (AOZ) uses variable focal length elements



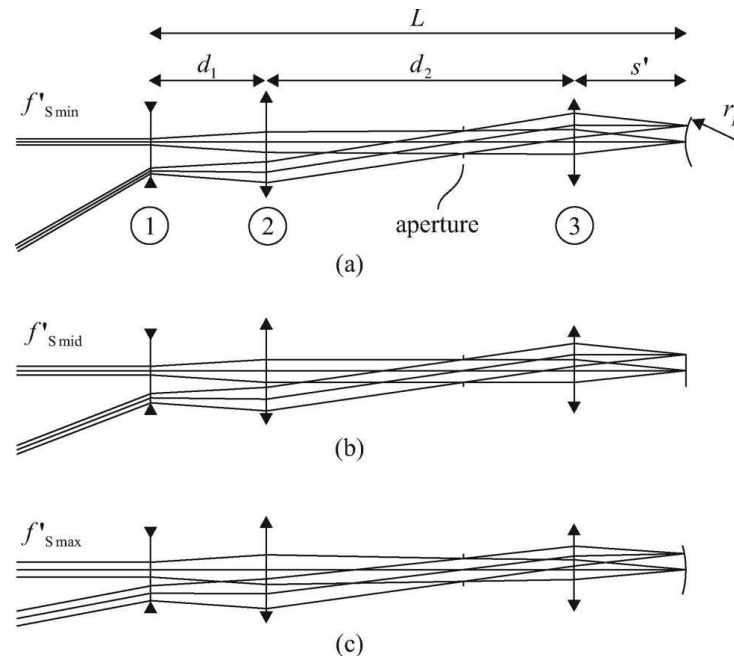
- Best option for zoom at large apertures

# Existing AOZ Theories

- Gaussian reduce two-element polymer lens system (Opt.Exp. **18** (7), 2010)
- Minimize Petzval sum in first-order design

$$\frac{1}{\hat{r}_p} = \sum_N \hat{\phi}_i = \sum_N \frac{1}{\hat{f}_i}$$

App. Opt. **48**(21),  
4097-4107 (2009).



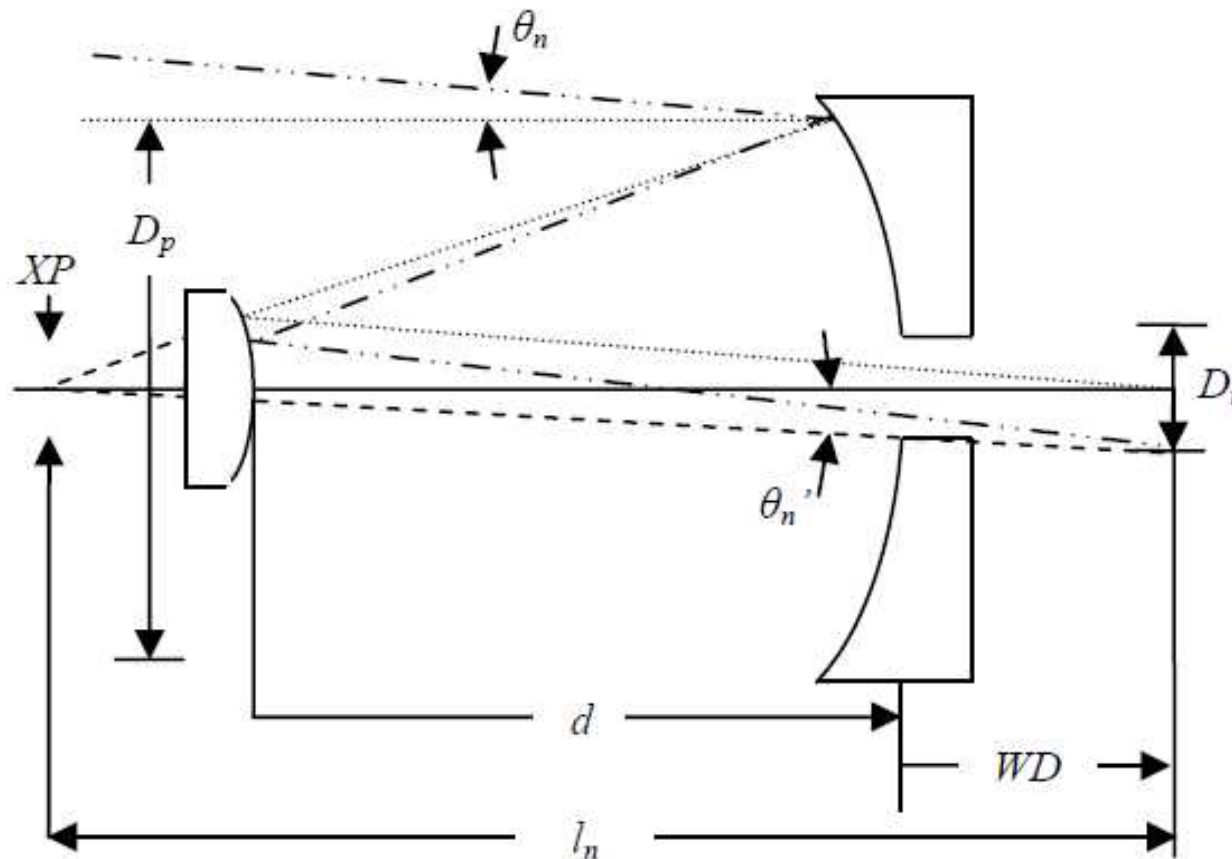
- Experimental system has 4 mirrors

# Brief of Theory

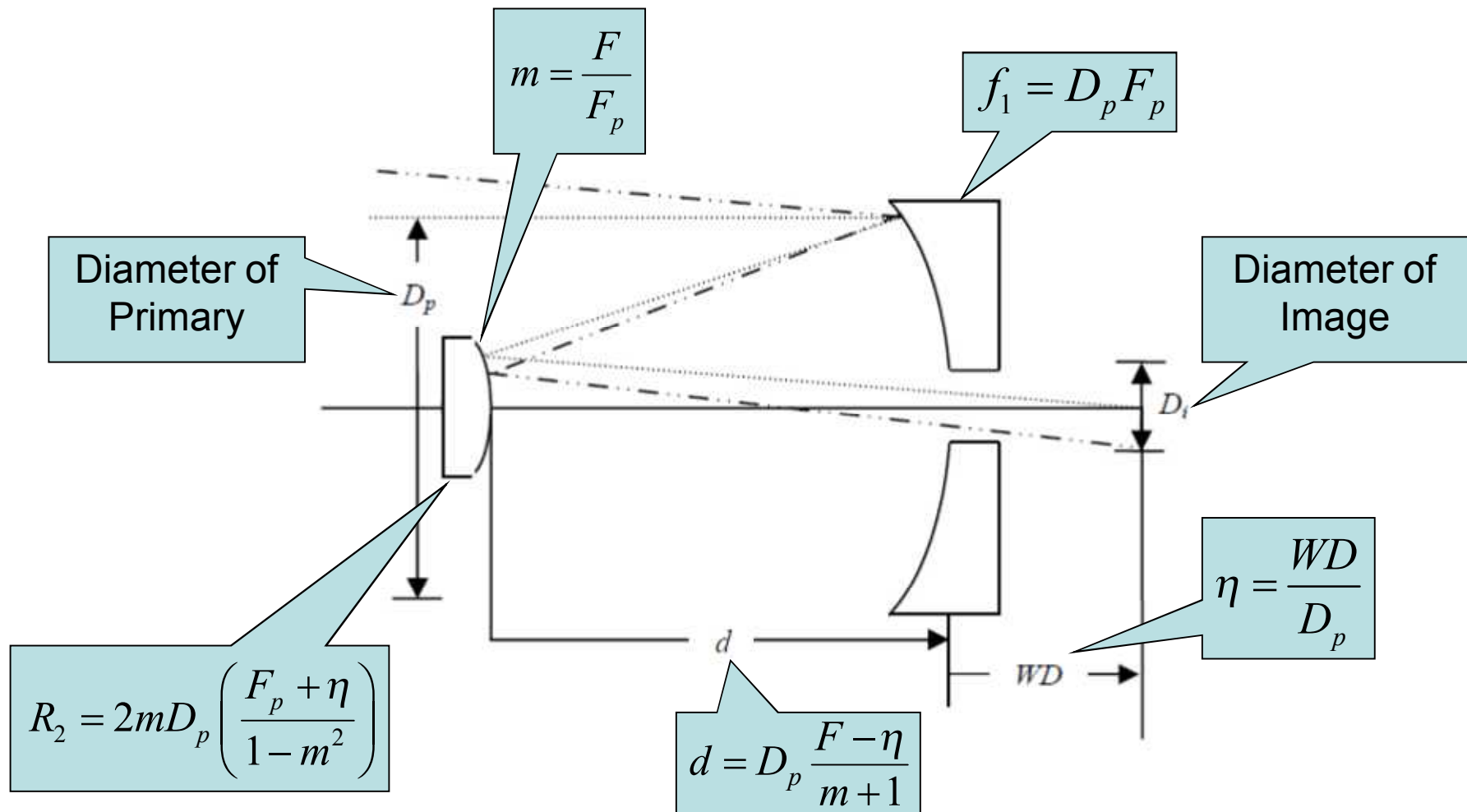
- Design an AOZ Cassegrain objective
  - Primary and secondary are active elements
  - Classical Cassegrain topology
  
- Combination of existing theories
  - 3<sup>rd</sup>-order objective design
  - 3<sup>rd</sup>-order aberration simulation
  
- Tradespace analysis
  - Simulate hundreds of millions of designs
  - Down-select based on given criteria

# Cassegrain Telescope Design

- Two active element Cassegrain objective



# Existing Design Equations



→ Distances are fixed, focal lengths vary



# Third-Order Design Theory

- Solving given equations for an adaptive system

$$R_{21} = \frac{2D_p f_{11} F_1 F_2 (f_{11} - f_{12})}{(f_{11} - D_p F_1)(f_{11} F_2 - f_{12} F_1)}$$

$$R_{22} = \frac{2D_p f_{12} F_1 F_2 (f_{12} - f_{11})}{(f_{12} - D_p F_2)(f_{12} F_1 - f_{11} F_2)}$$

$$d = \frac{f_{11} f_{12} (F_2 - F_1)}{f_{11} F_2 - f_{12} F_1}$$

$$WD = \frac{D_p f_{12} F_1 F_2 - f_{11} (f_{12} F_1 - f_{12} F_2 + D_p F_1 F_2)}{f_{12} F_1 - f_{11} F_2}$$

- Free parameters are  $F_{\#}$  and  $f_1$  (both states),  $D_p$  and  $D_l$
- Parameter sweep establishes values

# Zoom & Obscuration Ratios

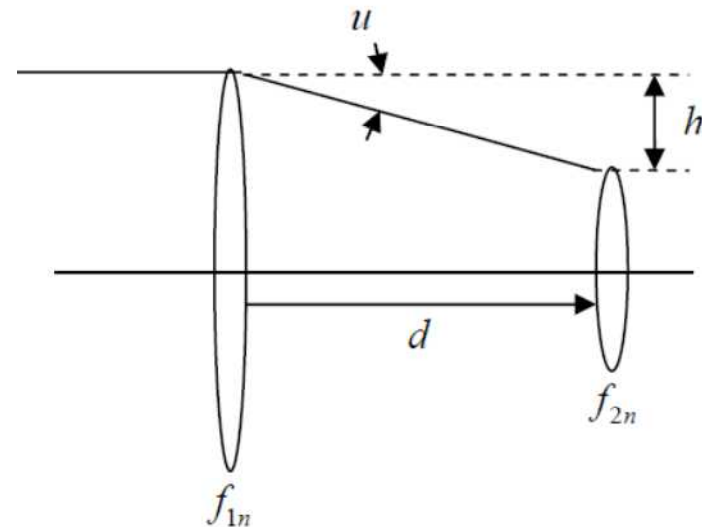
- Ratio of maximum to minimum system focal lengths

$$Z_R = \frac{f_{\max}}{f_{\min}}$$

- Ratio of secondary to primary diameters

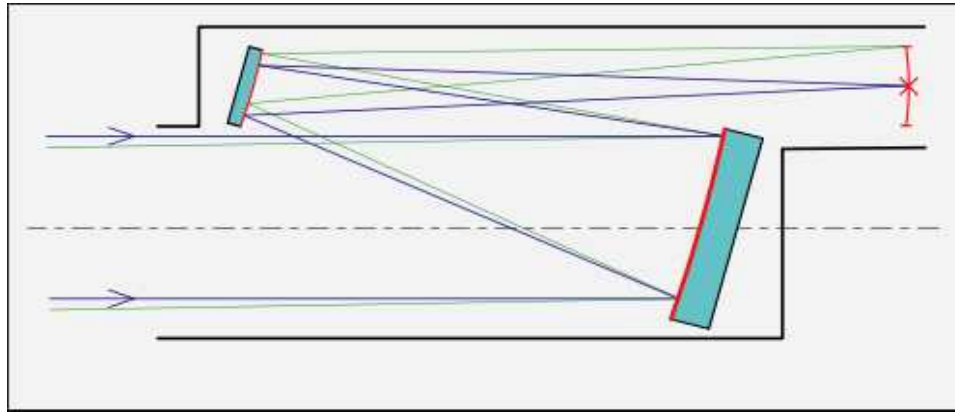
$$\varepsilon = \frac{D_s}{D_p}$$

$$\varepsilon = 1 + \frac{d}{f_{1n}}$$



# Bilateral System Theory

- Paraxial aberration theory for bilateral systems
  - One plane of symmetry



Courtesy: ArtMechanic

- Result is Seidel aberration coefficients

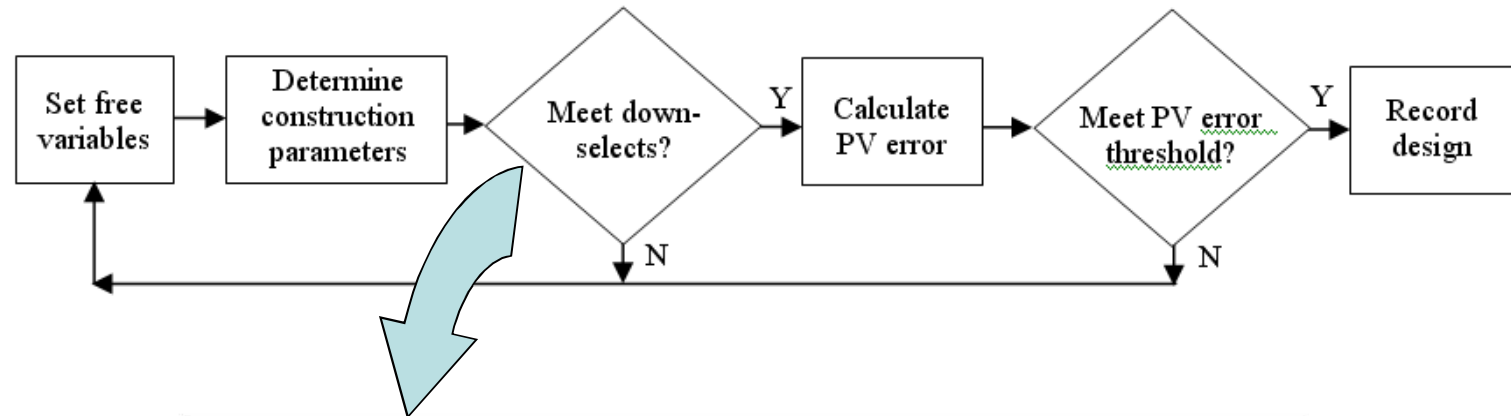
$$W(\vec{H}, \vec{\rho}) = \sum_{k,m,n}^{\infty} W_{2k+n, 2m+n, n} (\vec{H} \cdot \vec{H})^k (\vec{\rho} \cdot \vec{\rho})^m (\vec{H} \cdot \vec{\rho})^n$$

- Optimize further in Zemax/CodeV/etc

Opt. Eng. 33(6), 2045-2061 (1994).

# Parameter Sweep Logic

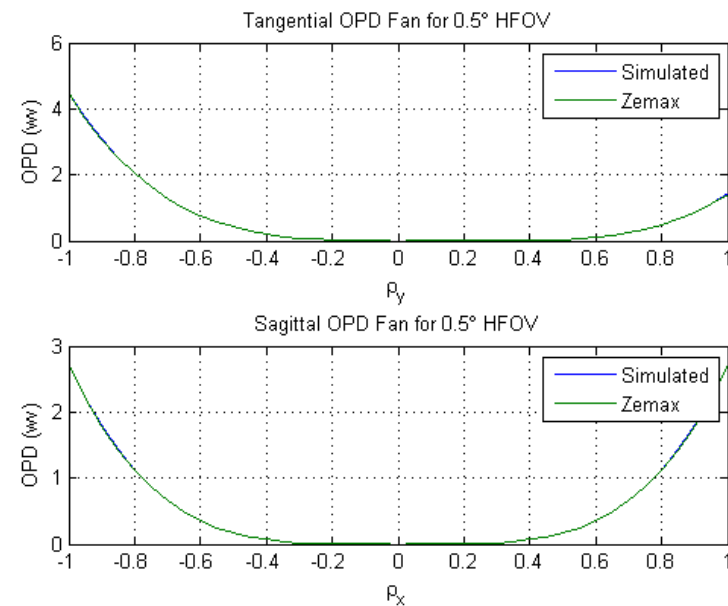
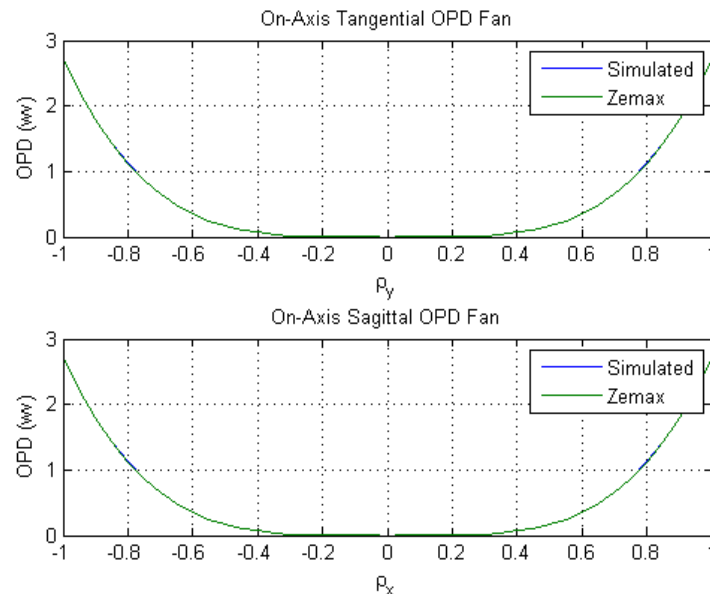
- Solve derived equations in Matlab code



| Criterion                     | Description   |
|-------------------------------|---|
| $d > 0$                       | The distance $d$ is defined to be positive.                   |
| $WD > 0$                      | The distance $WD$ is defined to be positive.                  |
| $R_{21} \neq R_{22}$          | The secondary ROC must change between states to achieve zoom. |
| $(d + WD) < T_L$              | The system length must be less than the threshold.            |
| $Z_R > T_{Z_R}$               | The zoom ratio must be greater than the threshold.            |
| $\varepsilon < T_\varepsilon$ | The obscuration ratio must be less than the threshold.        |

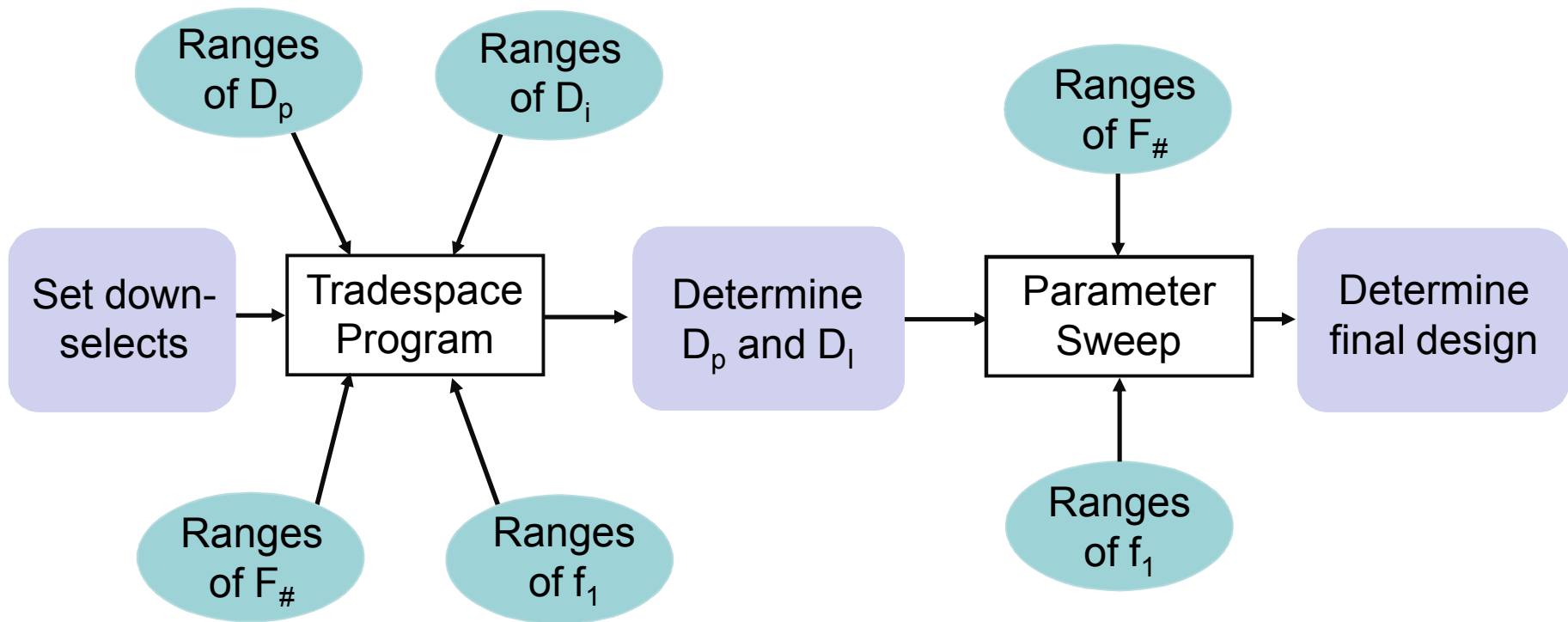
# Verification of Code

- Simulate non-zooming Cassegrain



- Residual focus due to poor original design
- Defocus cannot be modeled with bilateral theory

# Tradespace Analysis

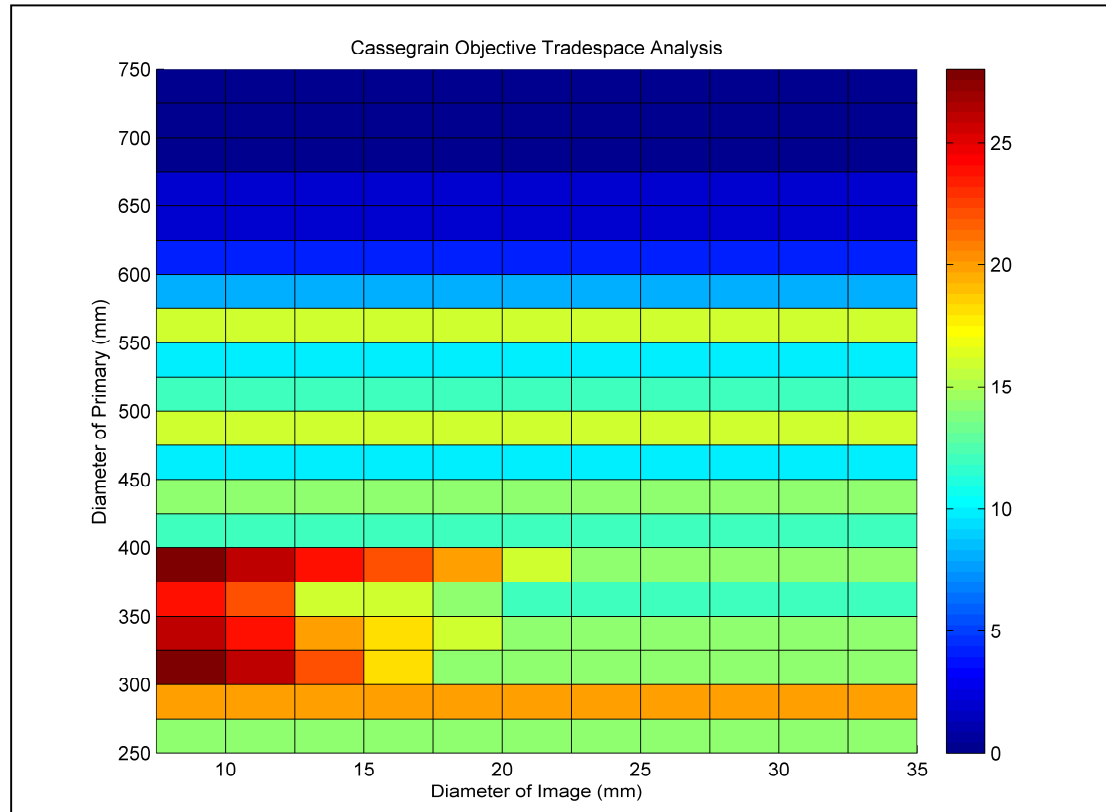


- Down-selects

- $Z_r > 3$ ,  $\varepsilon < 0.35$ ,  $PV < 150\text{wv}$ ,  $L < 3000\text{mm}$

# Set Primary & Image Diameters

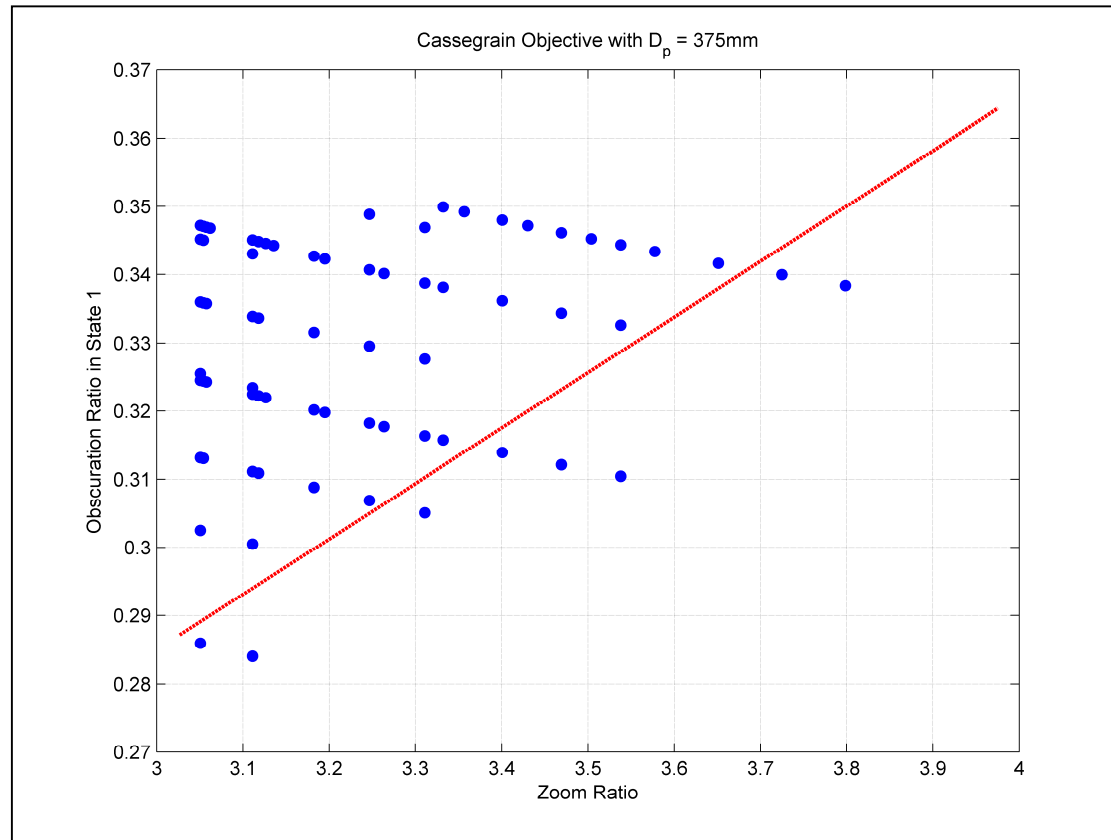
- Heat map of settings that resulted in many designs



- Maximum at  $D_p = 375\text{mm}$ ,  $D_i = 7.5$

# Set Design Parameters

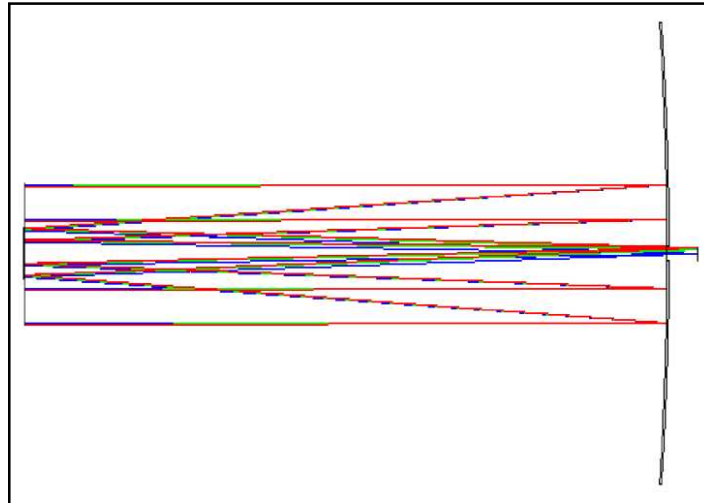
- Single parameter sweep



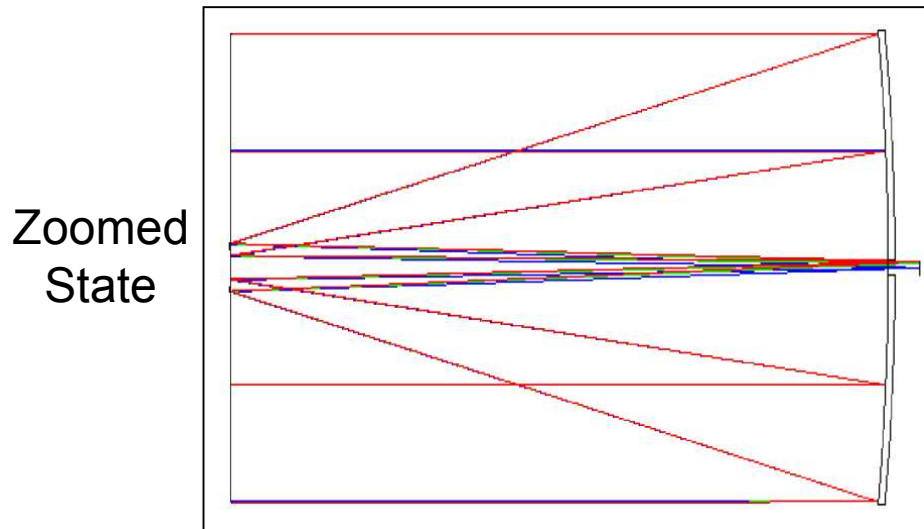
- Merit function is max.  $Z_R$  and min.  $\varepsilon$



# Design Results



Unzoomed  
State



Zoomed  
State

| Design Prescription |               |
|---------------------|---------------|
| Parameter           | Value         |
| $Z_R$               | 3.3           |
| $\varepsilon$       | 0.34          |
| $D_p$ (mm)          | 113.6, 375.0  |
| $F_n$               | 19.7, 19.7    |
| $f_{1n}$ (mm)       | 1088.9, 803.4 |
| $\kappa_{1n}$       | -1.0, -1.0    |
| $f_{2n}$ (mm)       | -714.8, -91.8 |
| $\kappa_{2n}$       | -8.37, -1.54  |
| $d$ (mm)            | 721.5         |
| $WD$ (mm)           | 3.4.4         |
| $HFOV$ (deg)        | 0.13, 0.04    |
| $PV$ (waves)        | 0.1, 0.07     |

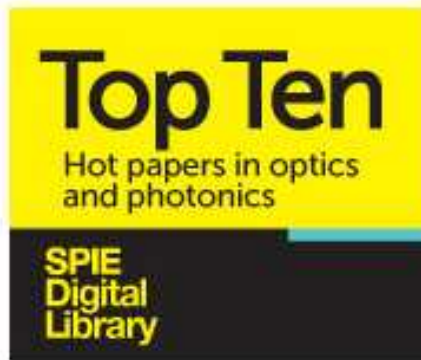
# Theory Fidelity

- Goal was to decrease gulf between theory and design
- Most parameters agree well
- Largest difference is focal ratio in unzoomed state
  - Need down-select on focal ratio

| Parameter     | Simulated Value        | Final Value             | Difference        |
|---------------|------------------------|-------------------------|-------------------|
| $Z_R$         | 3.8                    | 3.3                     | 15.1%             |
| $\varepsilon$ | 0.34                   | 0.34                    | 0.0%              |
| $F_n$         | 5.26,<br>20            | 19.7,<br>19.7           | -73.3%,<br>1.5%   |
| $f_{1n}$      | 991.8mm,<br>720.4mm    | 1088.9mm,<br>803.4mm    | -8.9%,<br>-10.3%  |
| $R_{2n}$      | -1348.6mm,<br>-141.9mm | -1429.6mm, -<br>183.7mm | -5.6%,<br>-22.7%  |
| $d$           | 656.2mm                | 721.5mm                 | -9.1%             |
| $WD$          | 11.86mm                | 34.4mm                  | -65.5%            |
| $HFOV$        | 0.10°,<br>0.02°        | 0.13°,<br>0.04°         | -23.1%,<br>-50.0% |

# Journal Article

- Worked published in *Opt. Eng.* **51**(8)
  - Invited paper at SPIE DSS 2012
- Currently most downloaded optics paper in SPIE's Digital Library



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## Optics

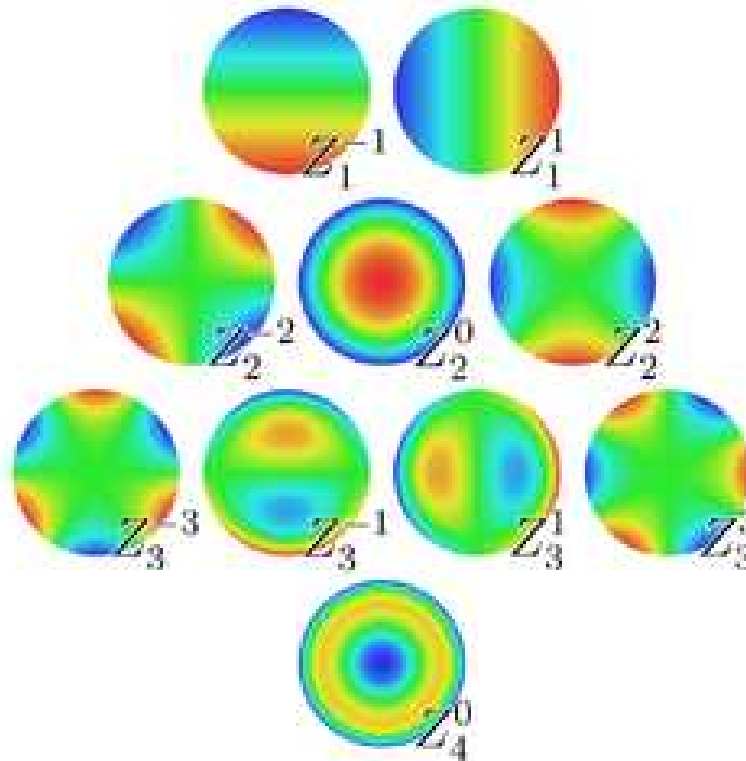
*Optical Engineering* | June 5, 2012

Theory and tradespace analysis of a reflective axial adaptive optical zoom system

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# Zernike Polynomials

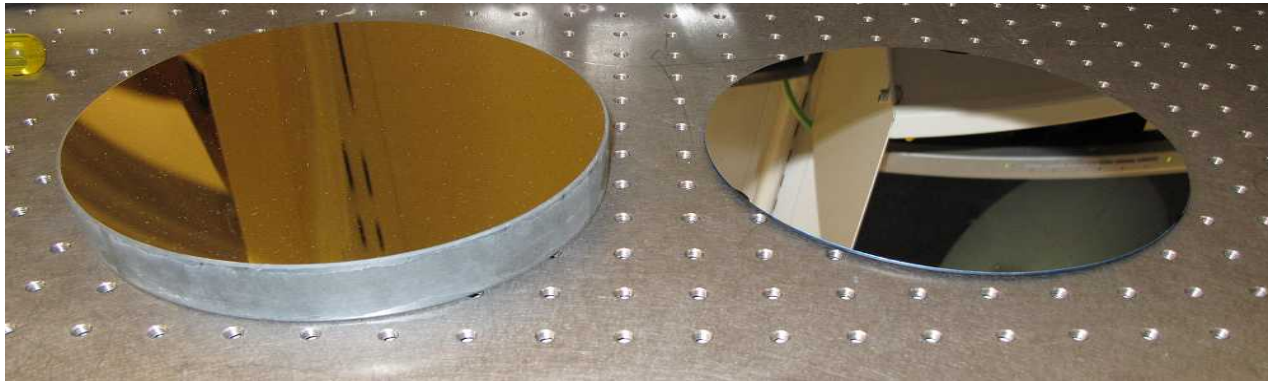
- Orthonormal basis set to describe aberrations



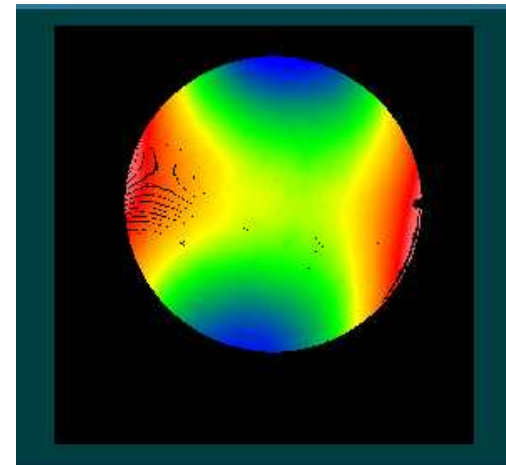
- Modal description of wavefront error (WFE)

# Carbon Fiber Reinforced Polymer

- Mirror is carbon fiber reinforced polymer (CFRP)



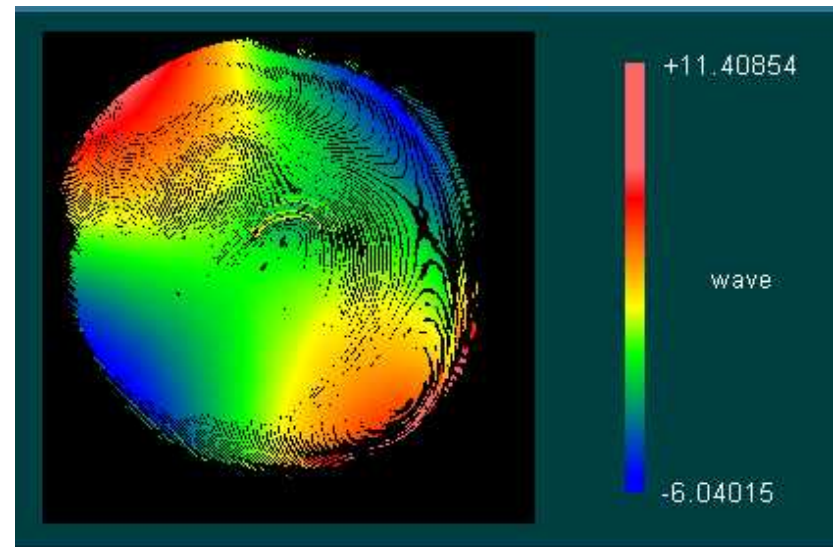
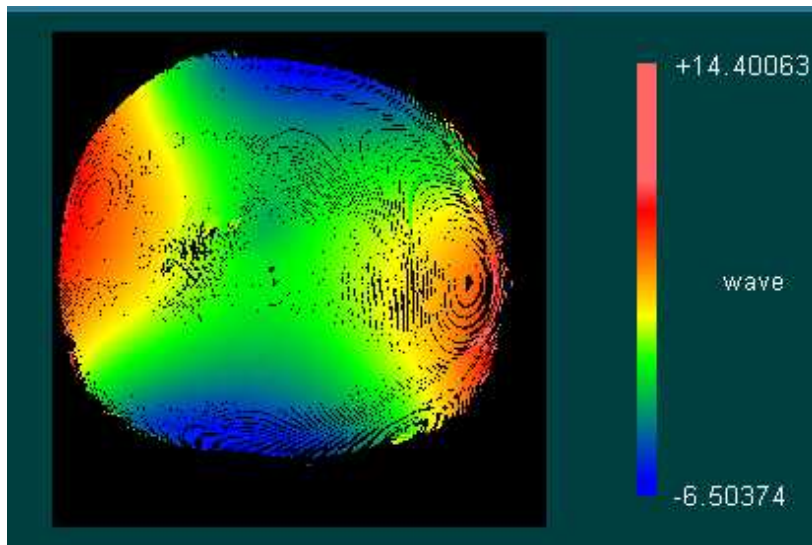
- Benefits
  - Very low CTE/hysteresis
  - Fabricated via replication
- Drawbacks
  - Not diffraction limited mirrors
  - Temporal degradation



13.9wv PV, 2.58wv RMS

# Cause of Astigmatism

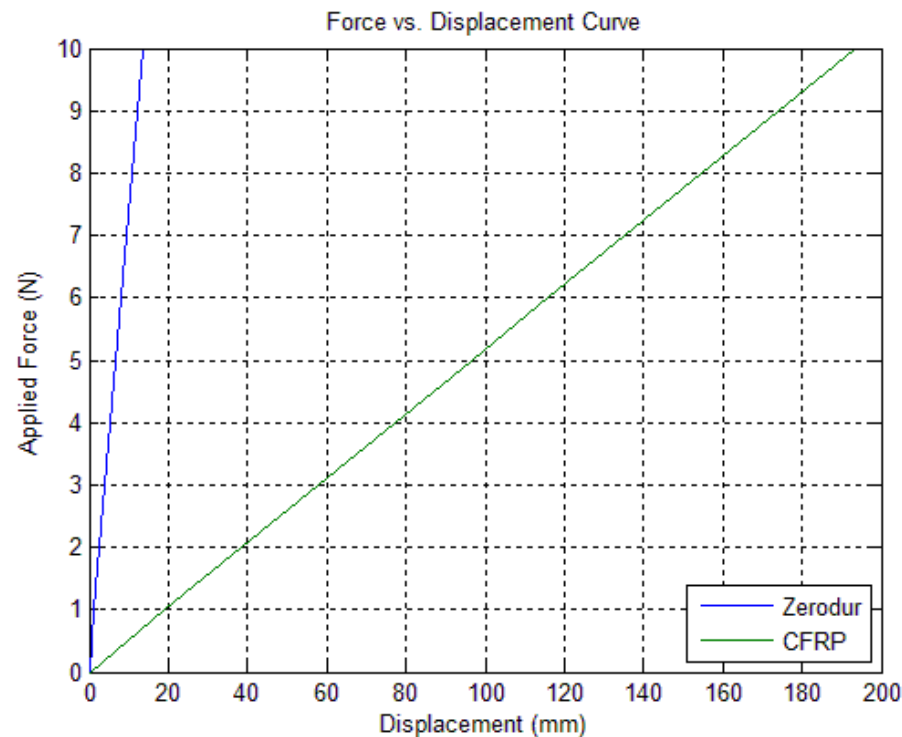
- Large astigmatism in CFRP mirror
- Literature suggests main cause is gravitational sag



- Astigmatism tracks mirror rotation
- Thus, CFRP mirror itself is cause

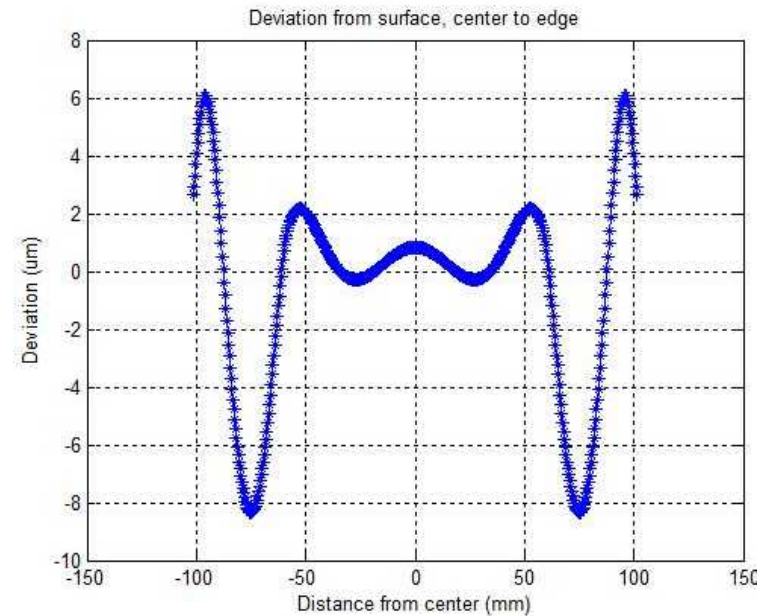
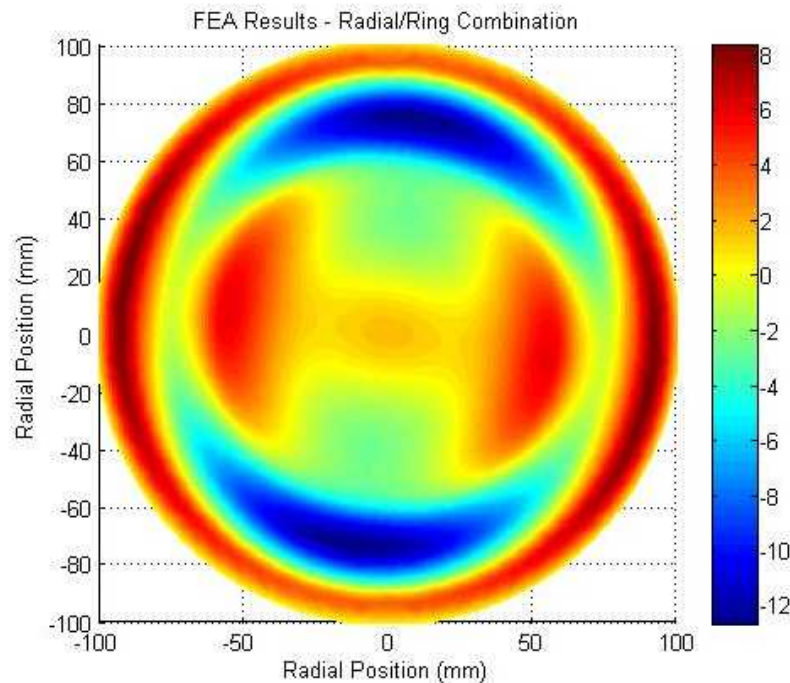
# CFRP vs. Zerodur

- CFRP much lower weight than Zerodur
- Robustness during actuation

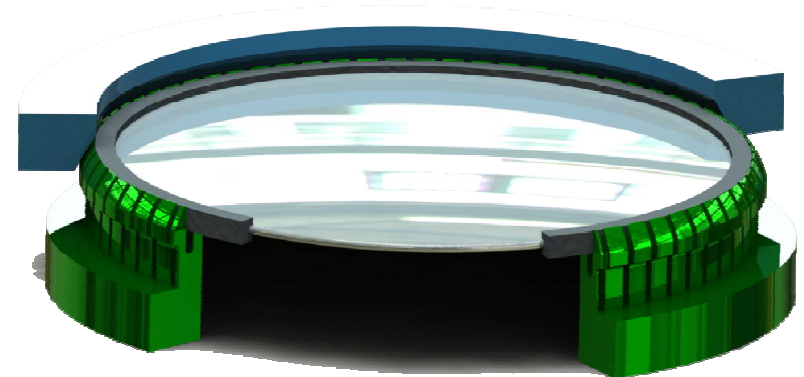


- Overall, great reduction in SWaP-C

# FEM of Actuation Modalities



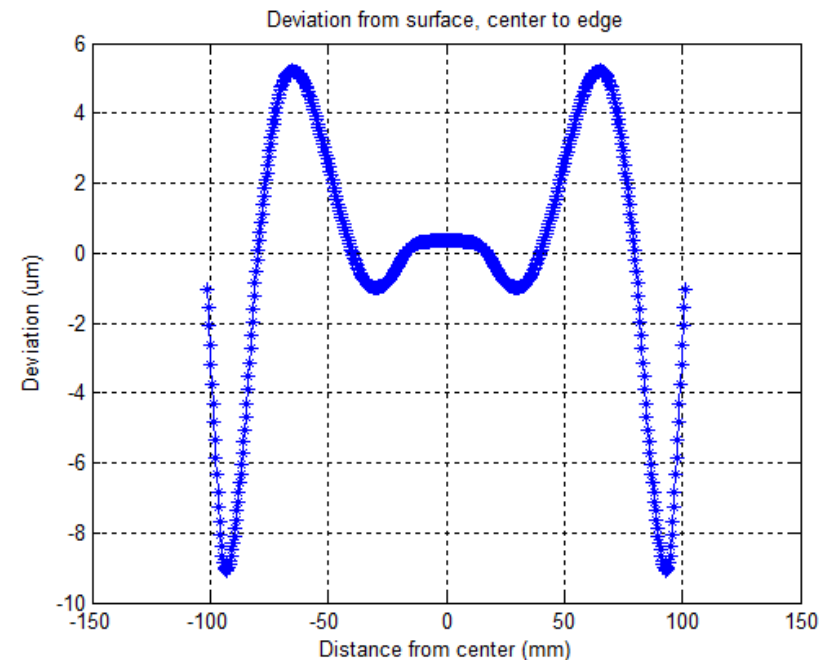
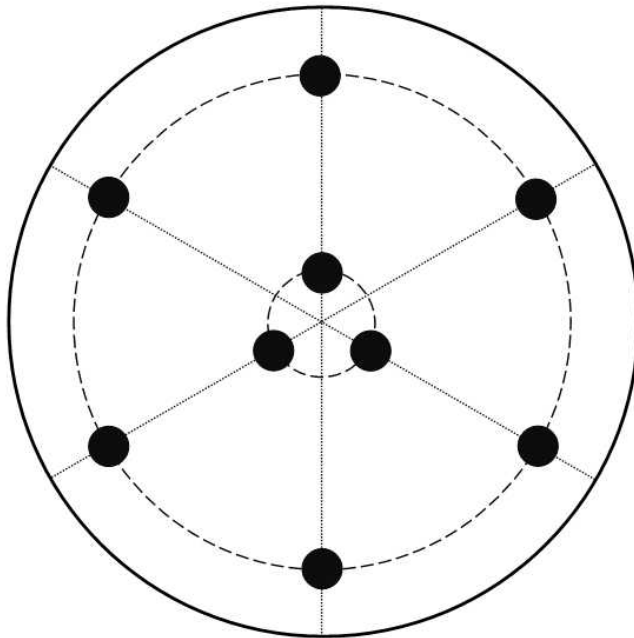
- Radial/Ring force
- ROC – 2m to 1.25m
- 24.6wv PV, 20kN total force





# Actuation Modality

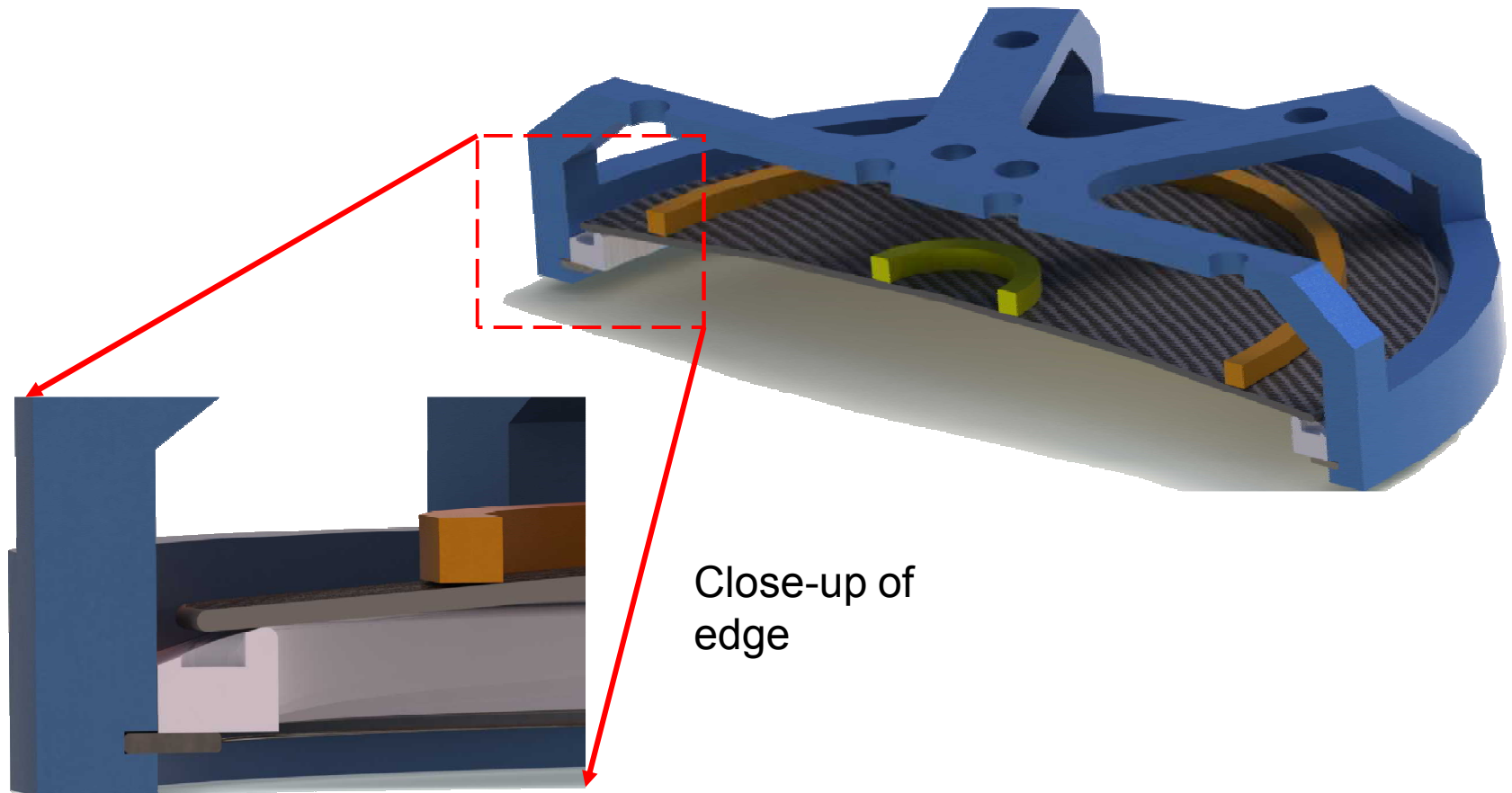
- Lower force, lower WFE
- Force perpendicular to stiffness gradient



- Nine actuators (black dots) on two annular rings

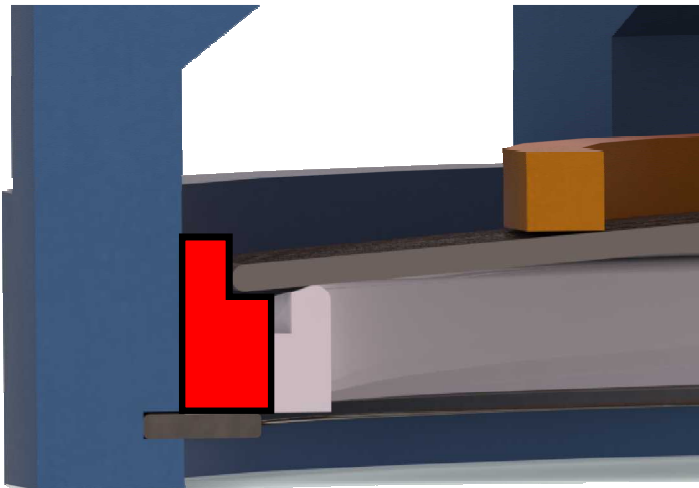
# Opto-Mechanical Apparatus

- CAD model of mount

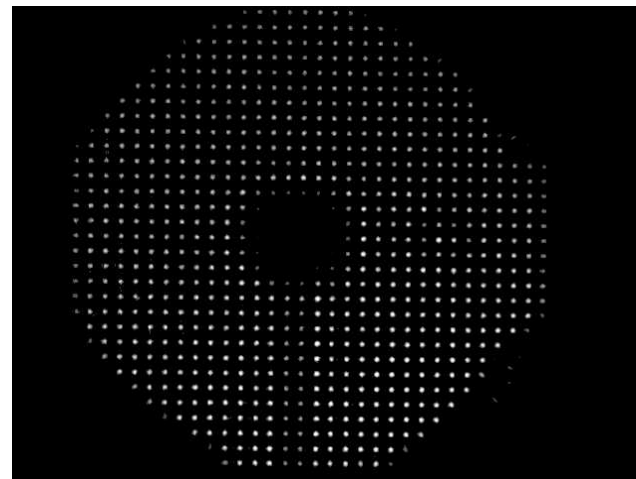
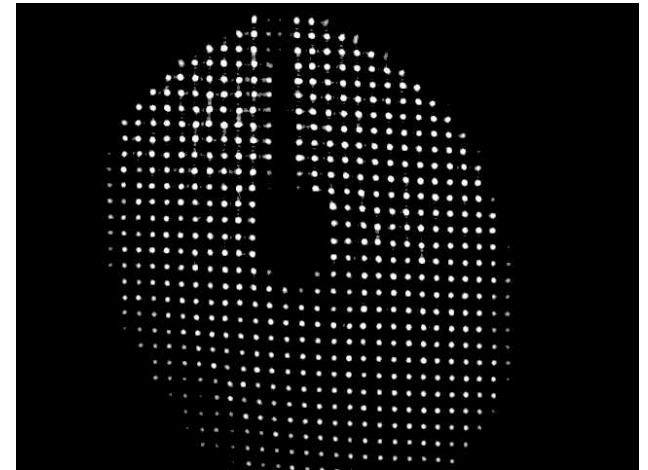


# Edge Constrain

- Edge of mirror must be completely unconstrained
- Notice difference in Hartmannograms



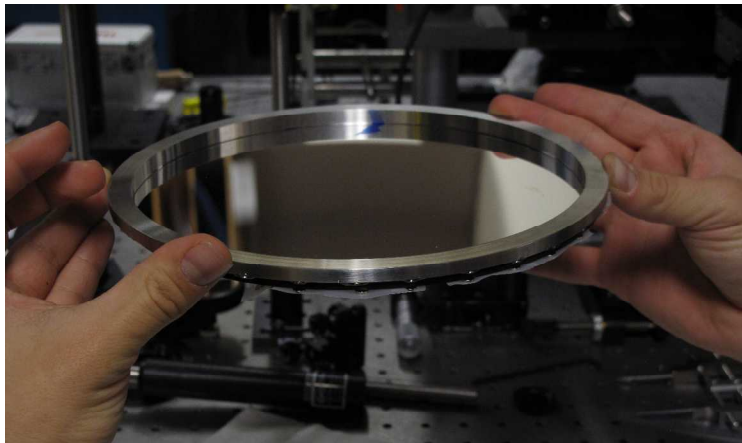
Rubber  
Gasket



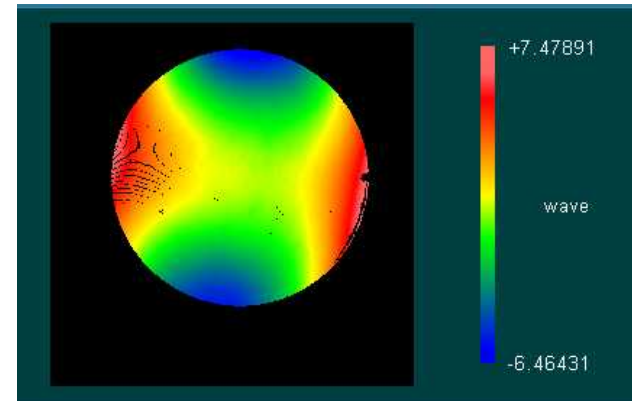
'Plunger'

# 'Plunger' Mirror Mount

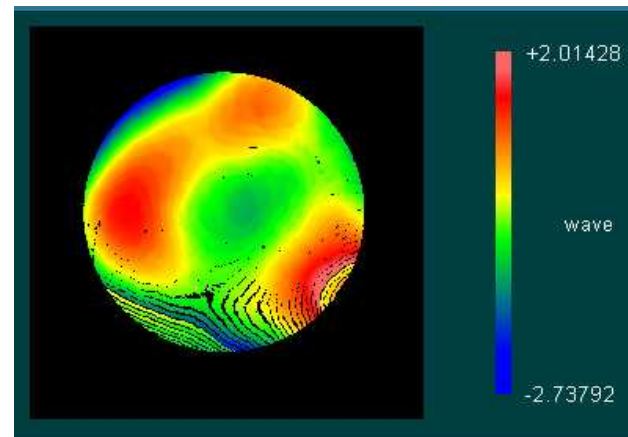
- Plunger provides clean boundary condition
- Magnets hold mirror in place
- Reduces WFE PV by 66%



Mirror held by  
magnets



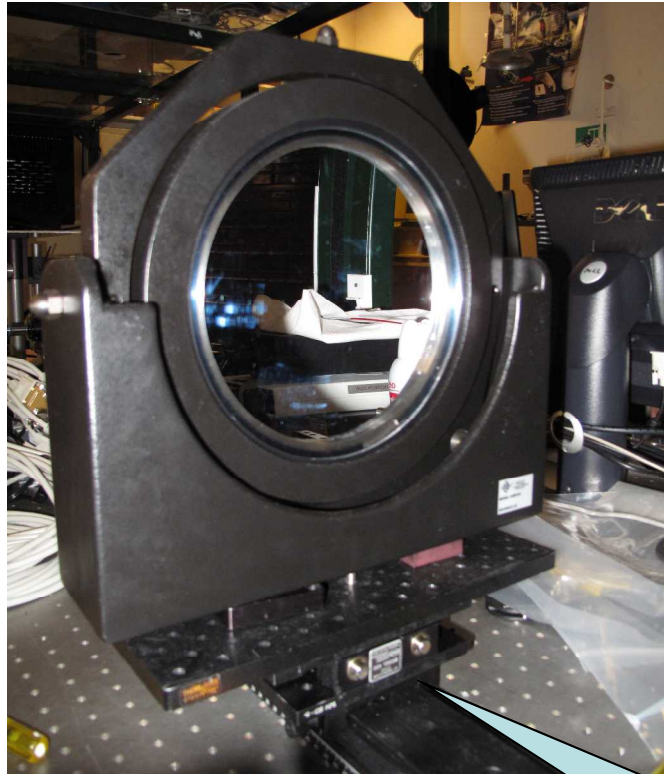
13.9wv PV, 2.58wv RMS



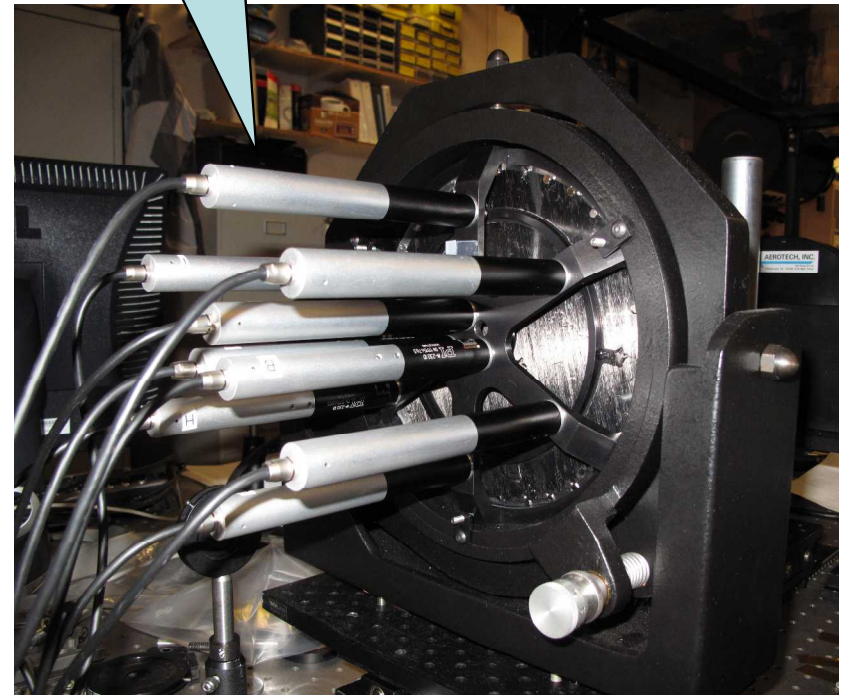
4.87wv PV, 0.79wv RMS

# Final Apparatus

Physik  
Instrumente  
M230.10



Front

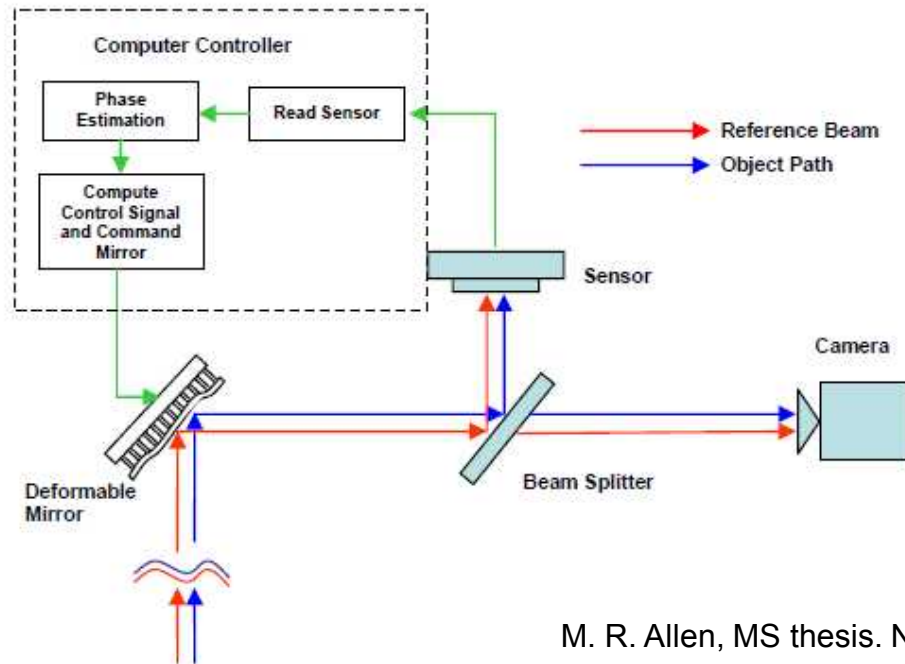


Back

Apparatus on rail

# Adaptive Optics

- Active mirror tested with AO testbed
- Basic AO layout below

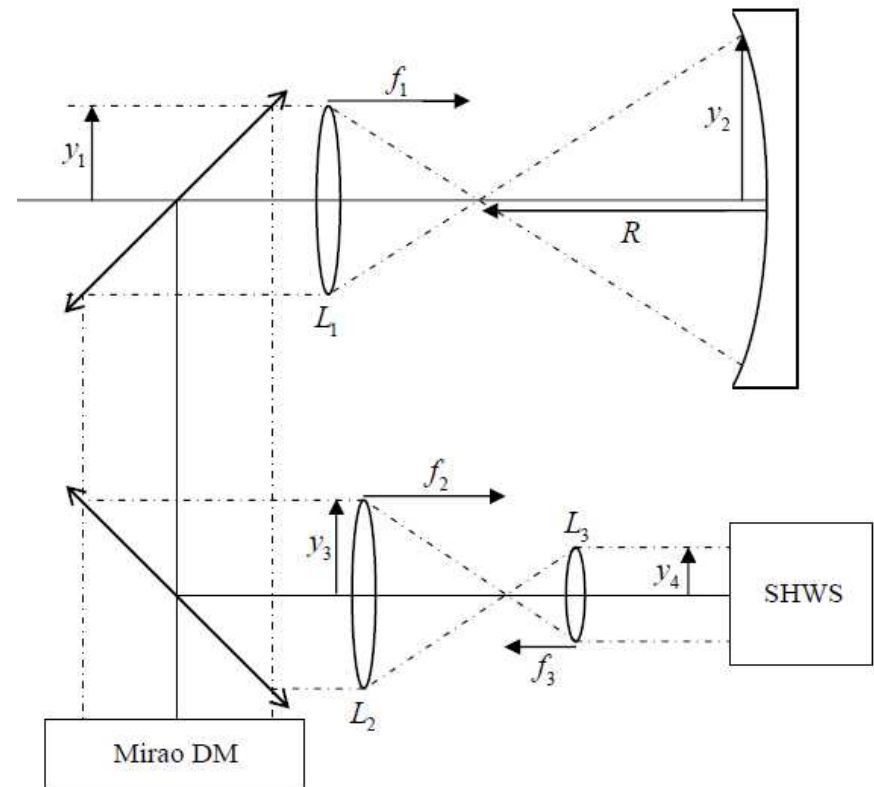


M. R. Allen, MS thesis. Naval Postgraduate School, 2007.

- Modal reconstruction of wavefront with Zernike coefficients

# Active Mirror Testbed

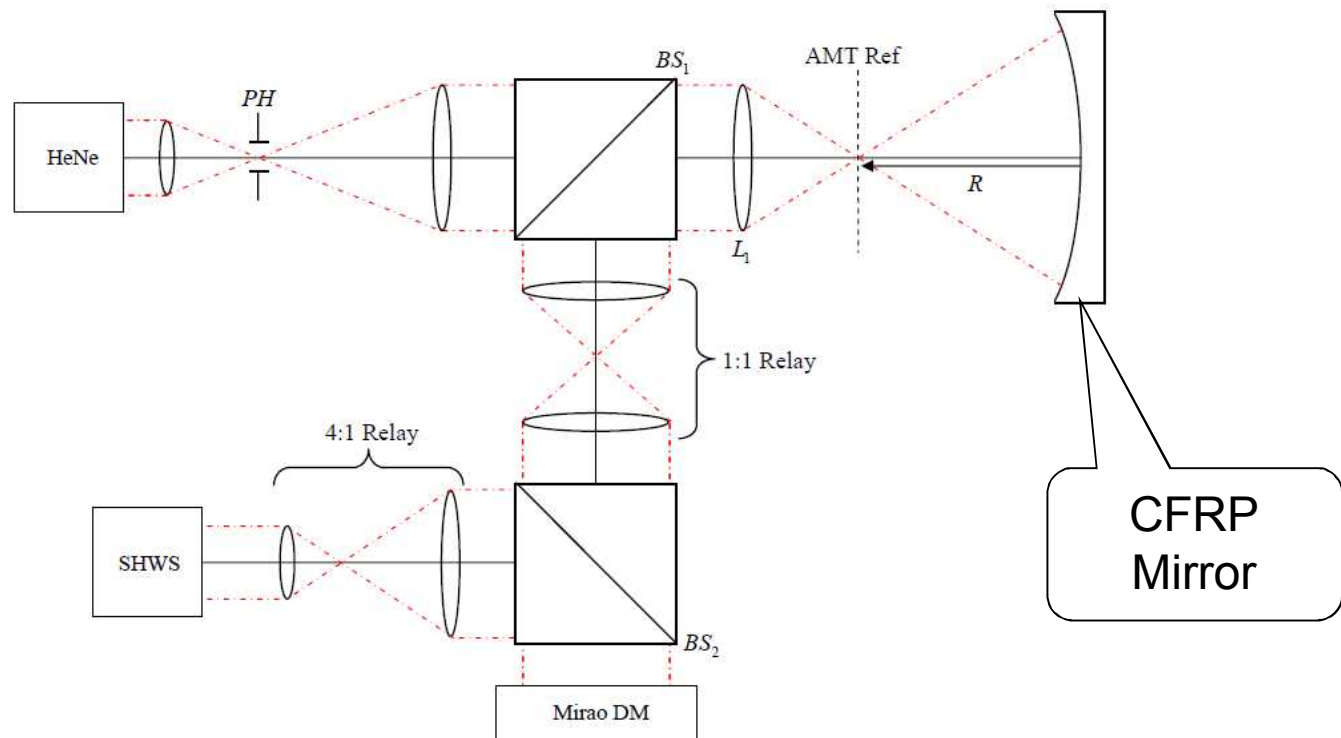
- Design criteria:
  - Minimize # optics
  - Test with spherical beam
  - Use COTS components
  - Correct beam diameters
  - Correct conjugation
- Extra optics eliminated with beam sizing





# Active Mirror Testbed

- Two deformable mirrors – CFRP mirror and COTS mirror
- Shack-Hartmann wavefront sensor measures beam

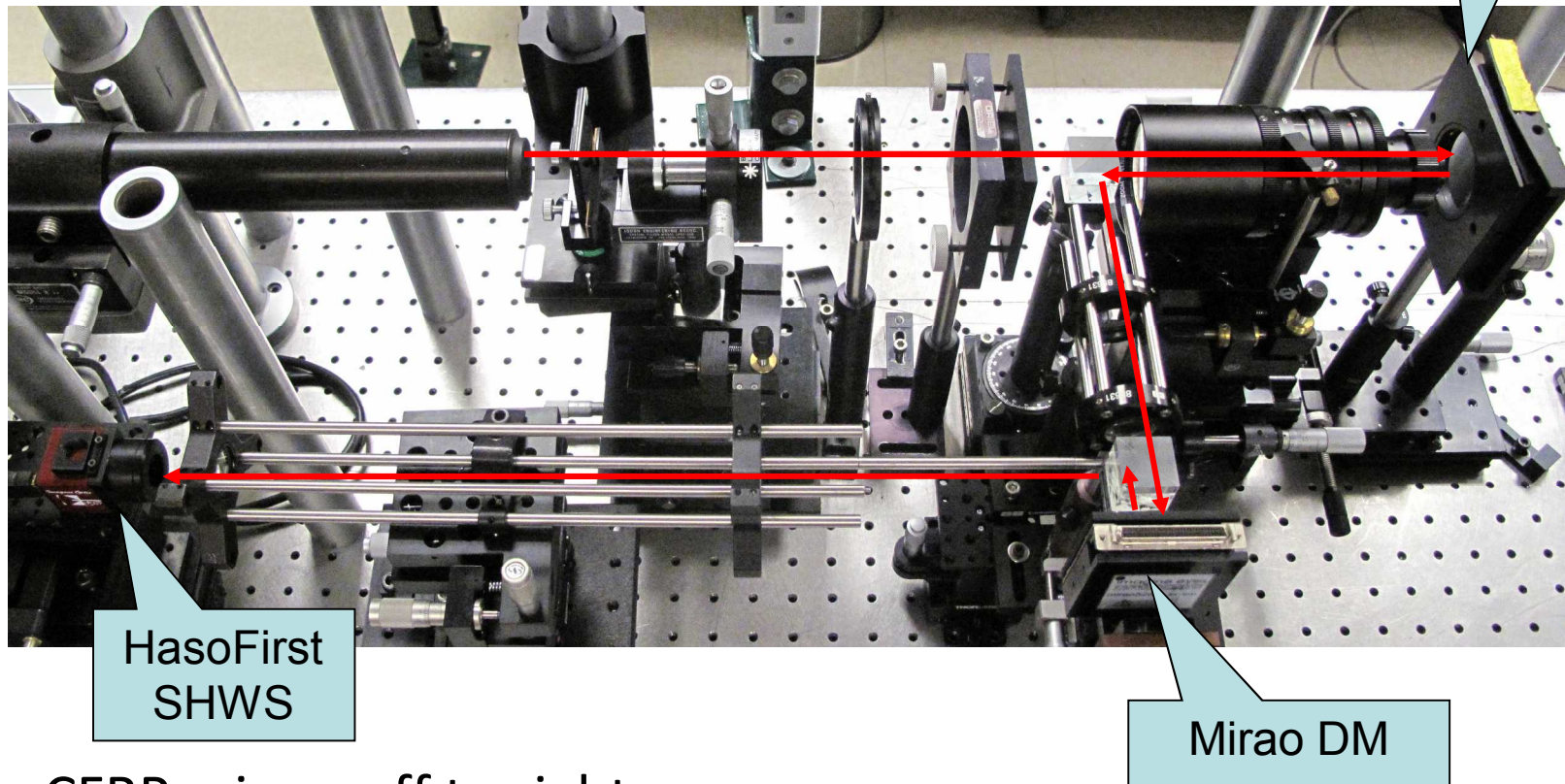


- Error of system is  $0.53\lambda$  PV



# AMT Picture

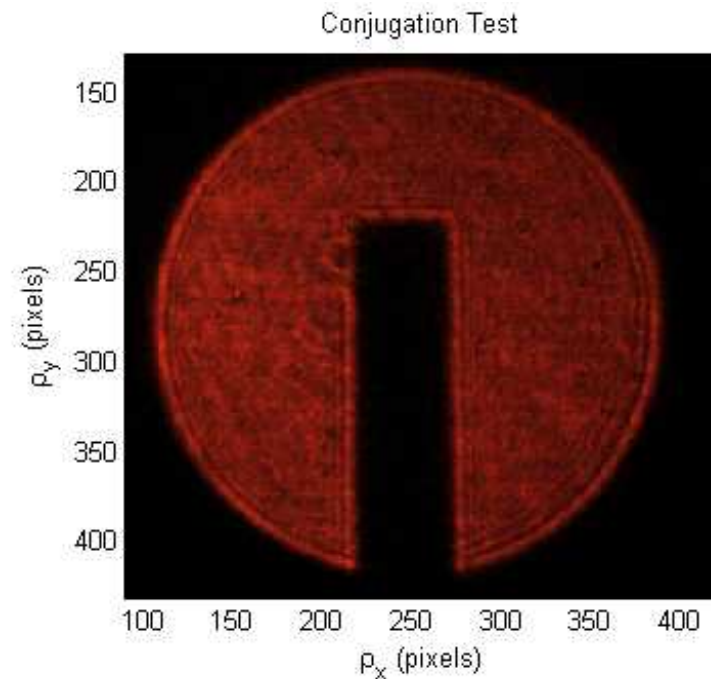
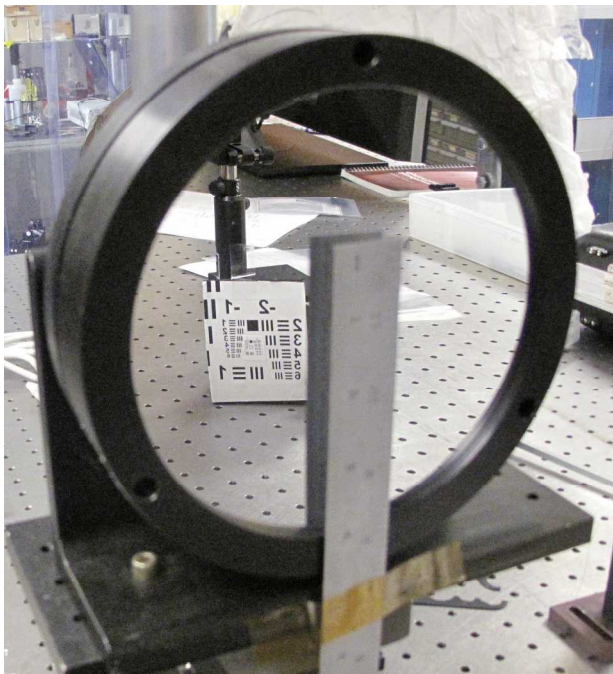
- Red line shows beam path



- CFRP mirror off to right

# Verification of Conjugation

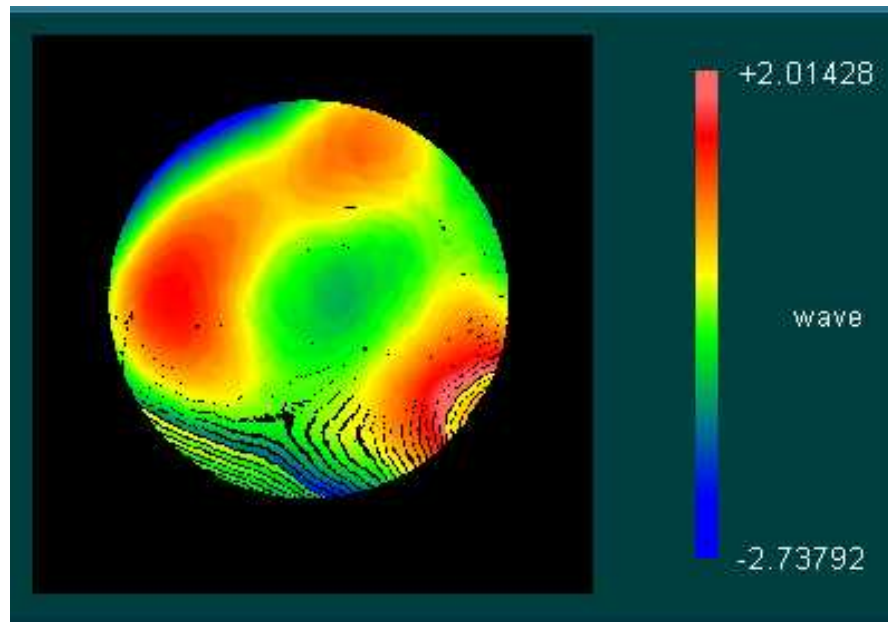
- CFRP/mirao/SHWS must be conjugated for proper wavefront sensing/correction



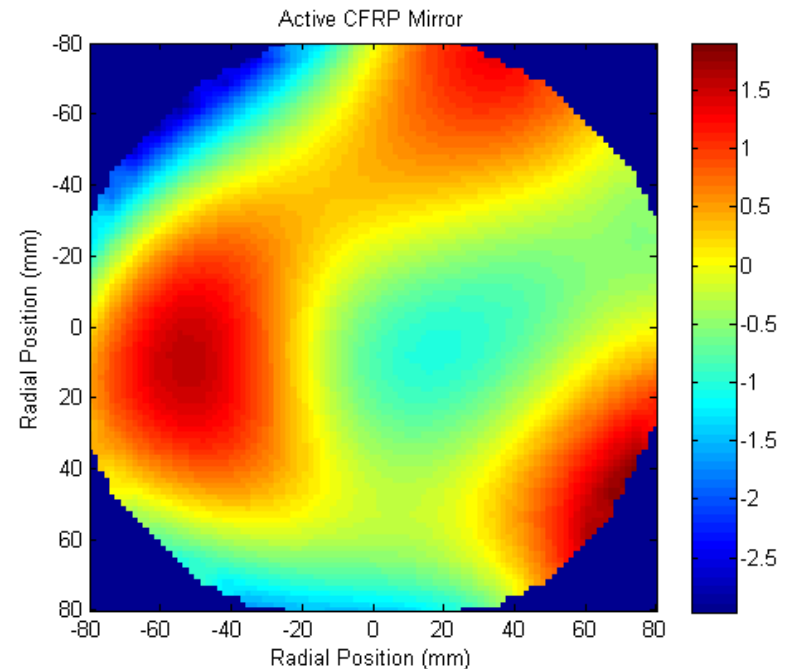
- Ruler in front of mirror demonstrates conjugation

# Verification with Zygo

- Wavefront error (WFE) of CFRP mirror below
- WFE agreement with Zygo Verifire is +2.5%
  - High functional form correlation



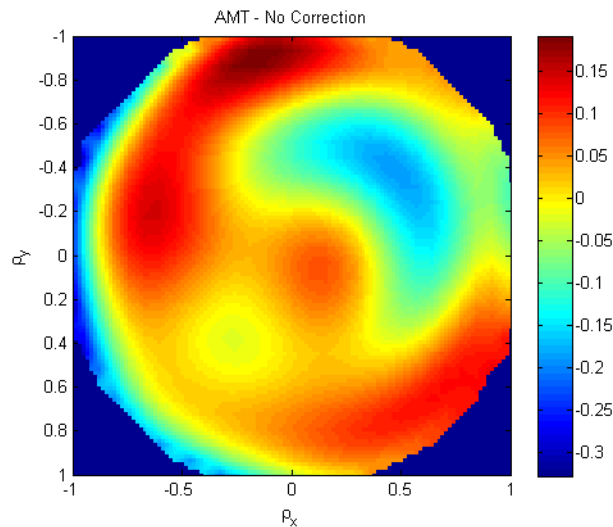
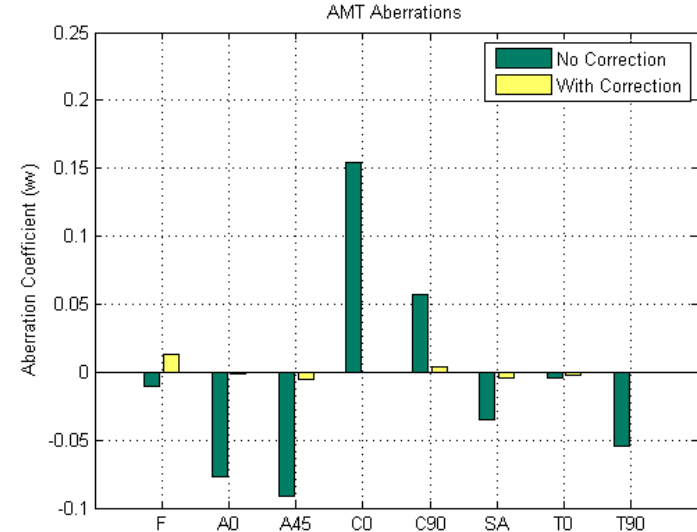
4.75wv PV, 0.73wv RMS



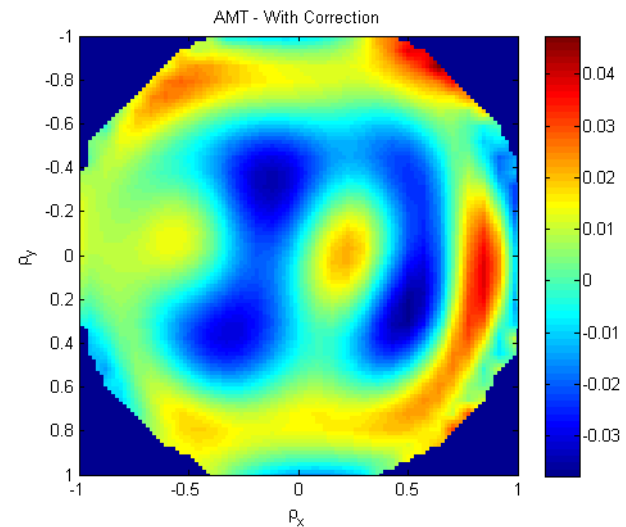
4.87wv PV, 0.79wv RMS

# System Reference

- Internal reference is plane wave
- Created system reference to remove AMT errors



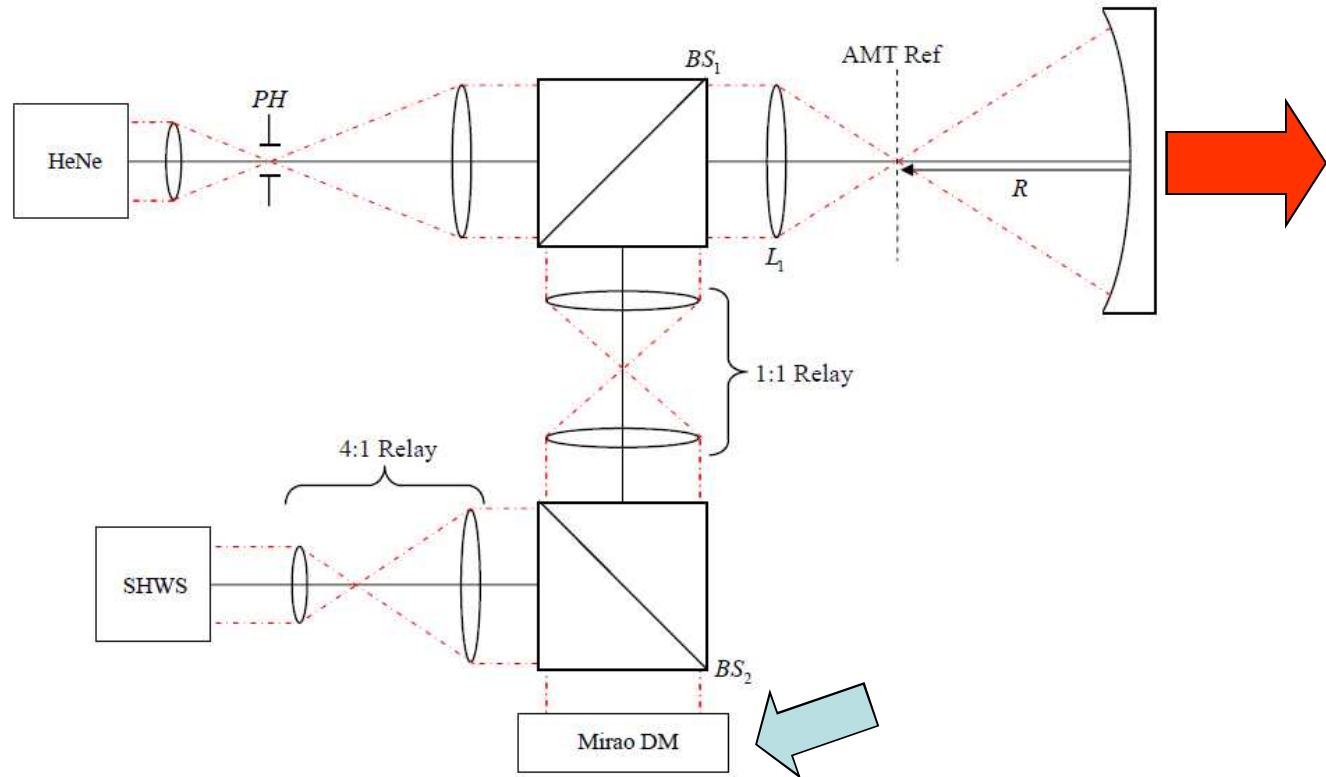
0.55wv PV, 0.09wv RMS



0.08wv PV, 0.01wv RMS

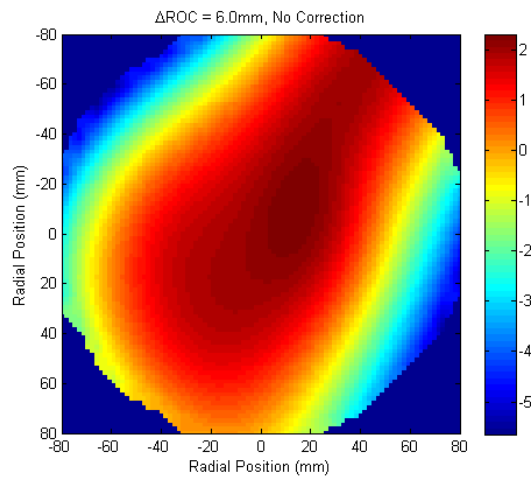
# Increasing ROC

- CFRP mirror physically moved

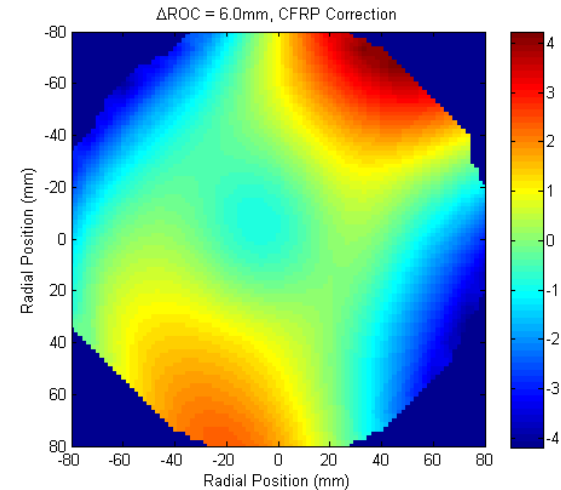


- Correct focus with CFRP mirror, mirao others

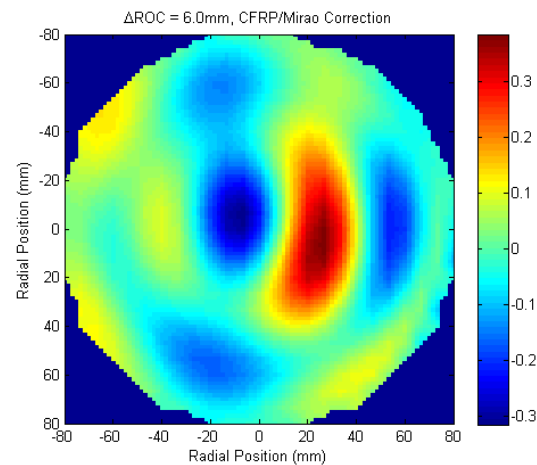
# Results for $\Delta\text{ROC} = 6\text{mm}$ (0.3%)



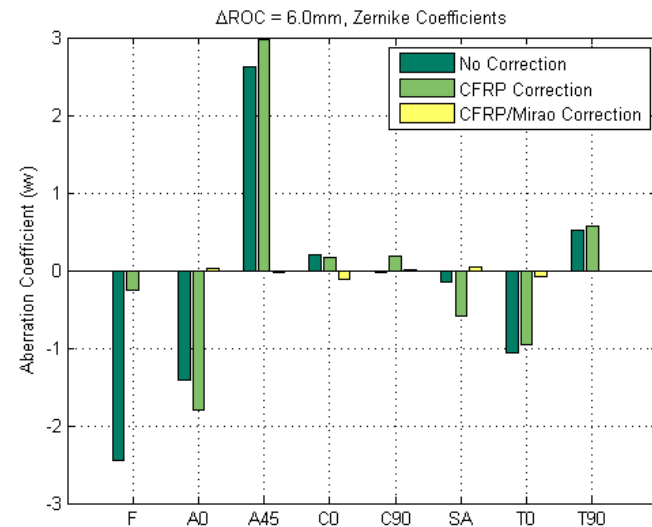
7.95wv PV, 1.875wv RMS



8.41wv PV, 1.501wv RMS

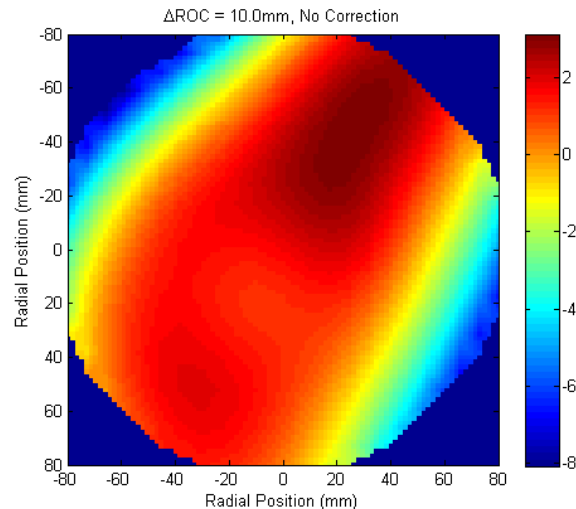


0.70wv PV, 0.111wv RMS

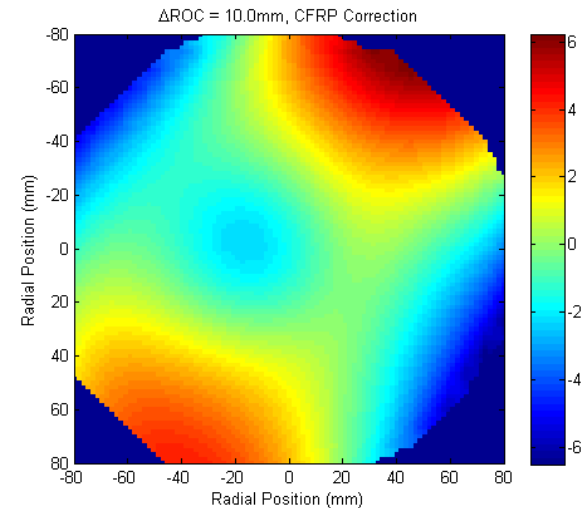




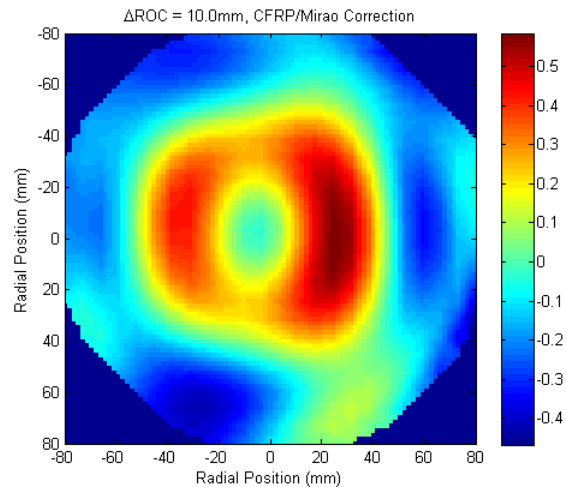
# Results for $\Delta\text{ROC} = 10\text{mm}$ (0.5%)



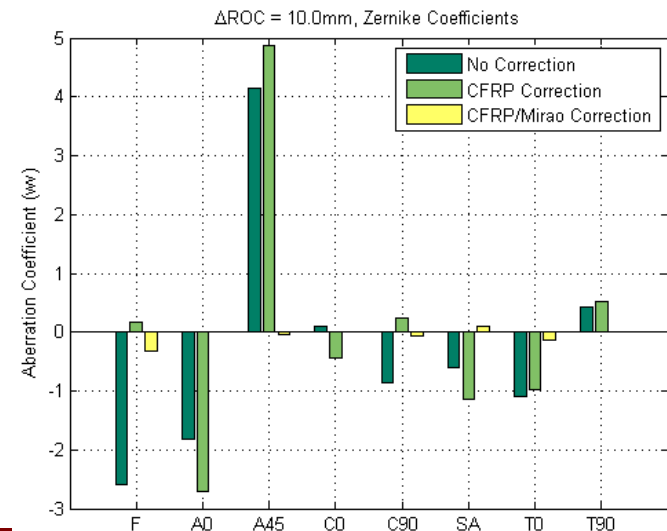
11.19wv PV, 2.38wv RMS



12.71wv PV, 2.32wv RMS

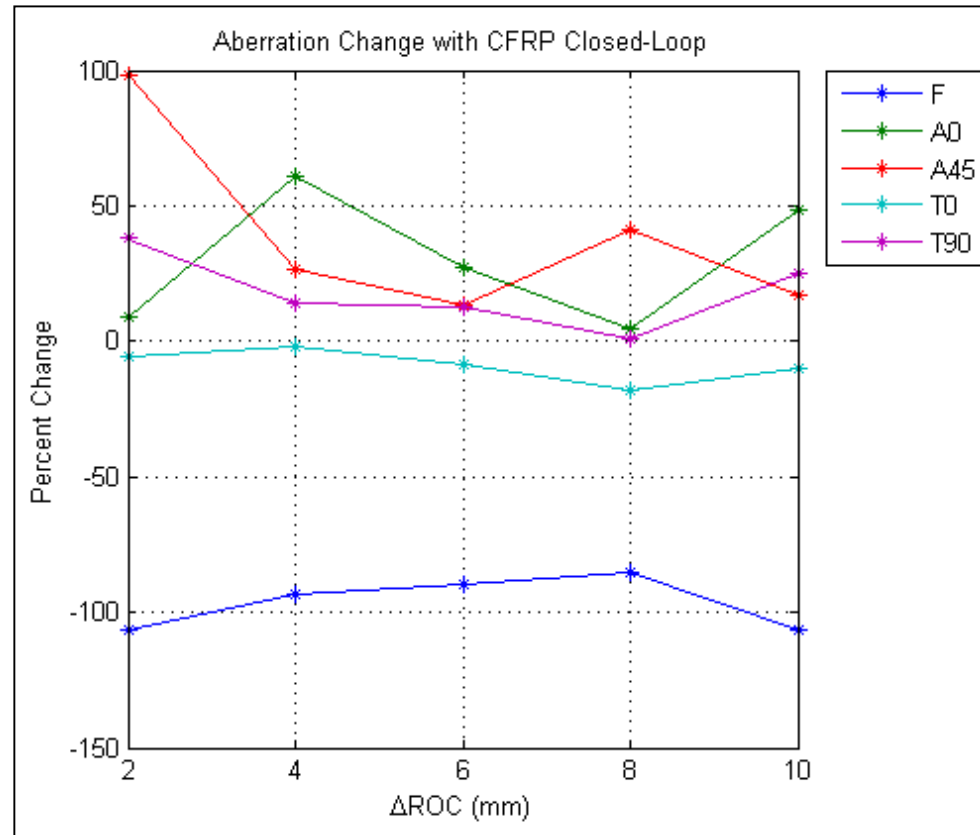


1.05wv PV, 0.23wv RMS



# Error Correction

- CFRP mirror decreases focus, increases astigmatism

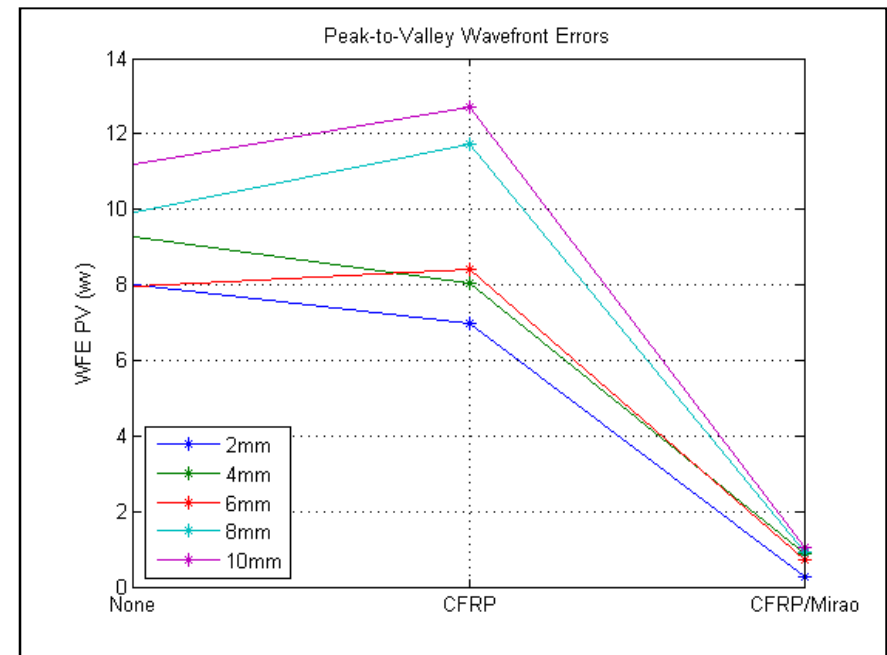
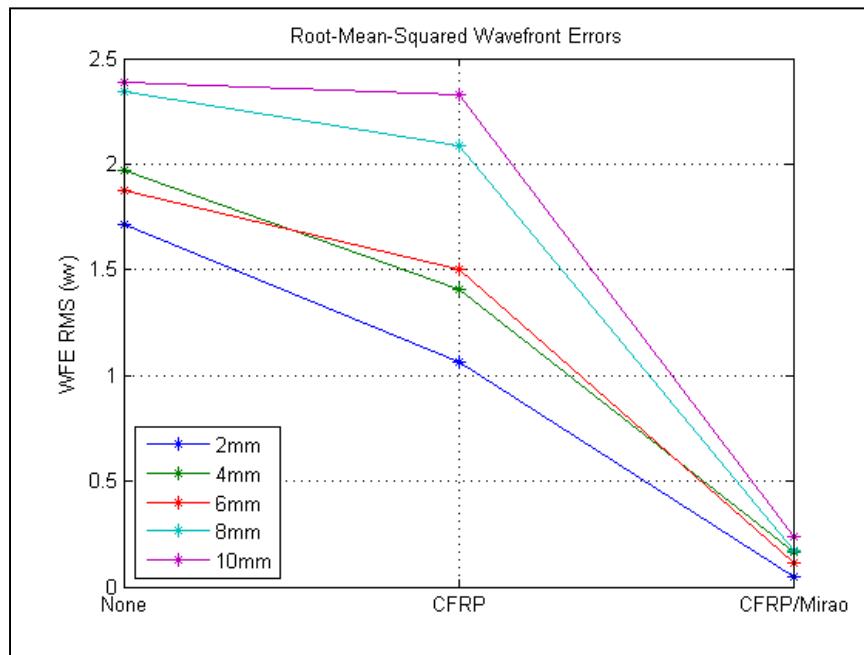


- CFRP mirror is good low, low-order corrector



# Error Correction

- RMS decreases at each corrective step

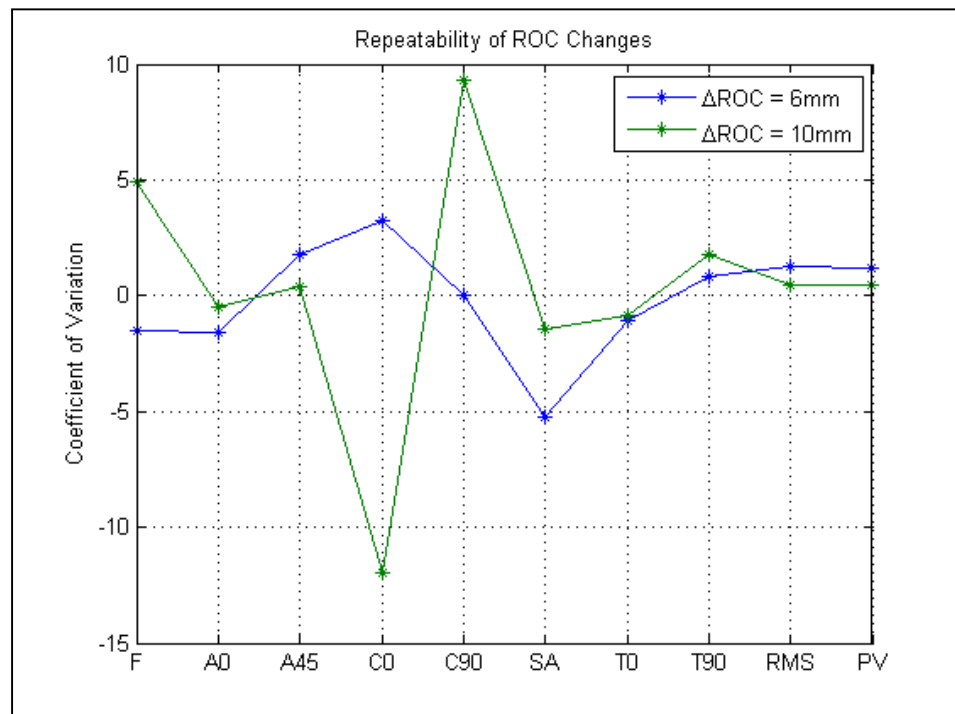


- PV increase due to astigmatism increase

# $\Delta$ ROC Repeatability

- Jump between states of  $\Delta$ ROC = 6mm and 10mm
- Track repeatability of low-order aberrations

$$CV = \frac{\mu}{\sigma}$$

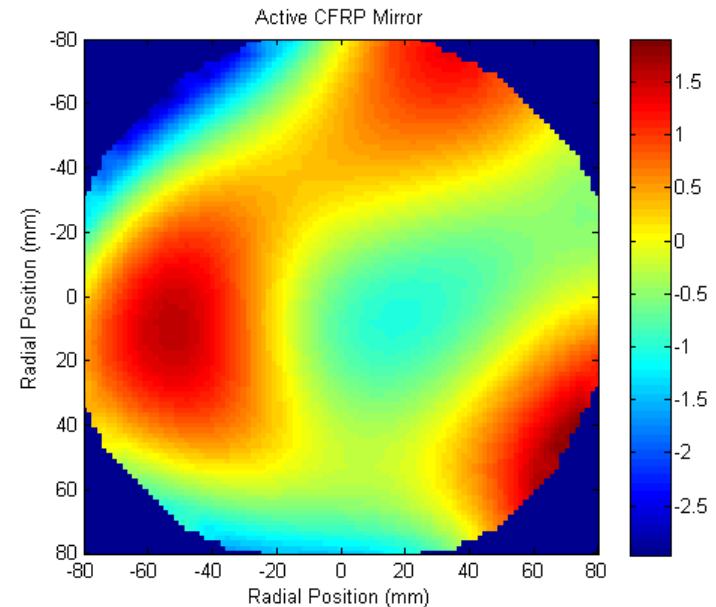


- Repeatability of ROC changes is quite high

# System Improvements

- Apparatus improvements
  - Diamond turn plunger to further clean-up boundary condition
  - Increase outer actuators to 8 for astigmatism control
  - Push correction with CFRP mirror to other low-order aberrations

- CFRP mirror itself
  - WFE is far too high
  - Improved fabrication techniques
  - Tailor properties



4.87wv PV, 0.79wv RMS

# Summary

- Novel AOZ optical design theory
  - Two-element Cassegrain objective
  - Tradespace analysis tested 260million designs
  - 3.3X, 375mm system
- Principle of active CFRP mirror demonstrated
  - ROC increased by 10mm (0.5%)
  - Focus controlled by mirror in closed-loop
  - Other low-order aberrations controlled by COTS DM
  - Aberrations measured by custom testbed
- AOZ system
  - ROC increase needs to be much larger
  - 5% very doable

# Questions?



- <http://spinsucks.com/social-media/social-media-questions/>

# HFOV Derivation

- Given equations from Wetherell & Rimmer

$$l_n = -\frac{m_n F_n (f_{1n} + D_p \eta)}{m_n F_n + \eta}$$

$$\theta'_n = \theta_n \frac{m_n F_n + \eta}{m_n (f_{1n} / D_p + \eta)}$$

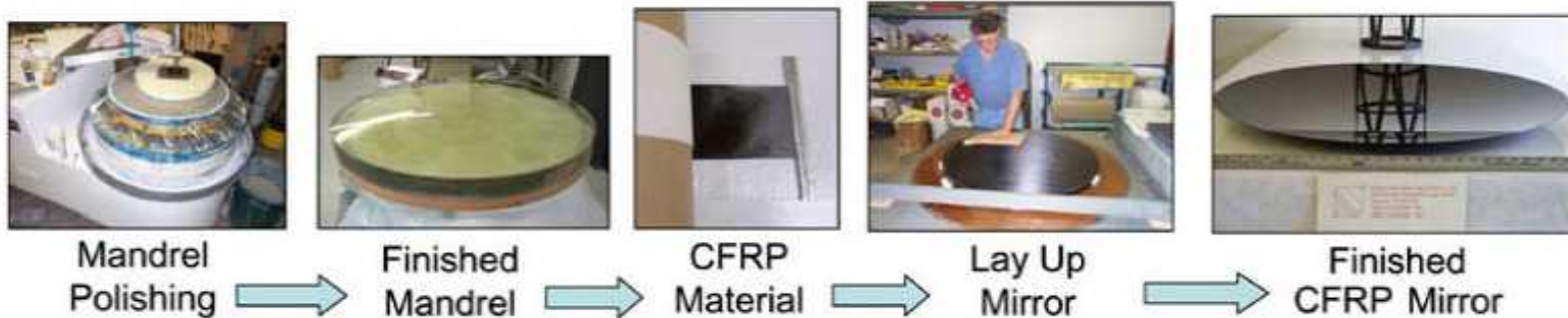
- Trigonometry gives HFOV

$$\tan \theta'_n = \frac{D_i / 2}{l_n}$$

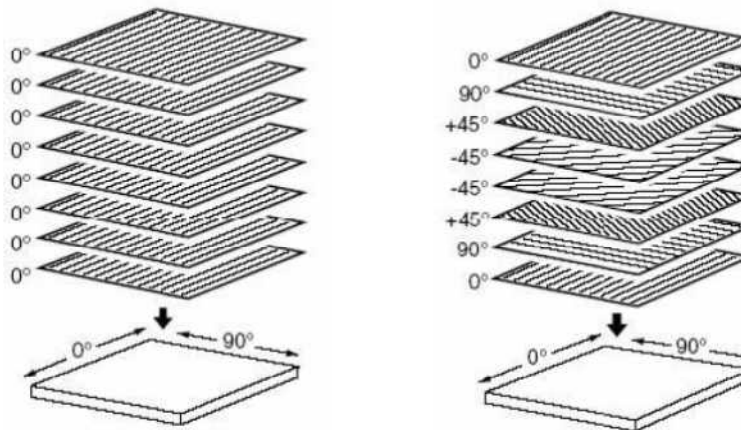
$$\theta_n = \frac{m_n (f_{1n} / D_p + \eta)}{m_n F_n + \eta} \tan^{-1} \left( \frac{D_i}{2l_n} \right)$$

# CFRP Mirror Fabrication

- Mirror fabricated via replication



- Varying fiber angles affects material properties



# Modality Choice

- Comparison of 5 different modalities

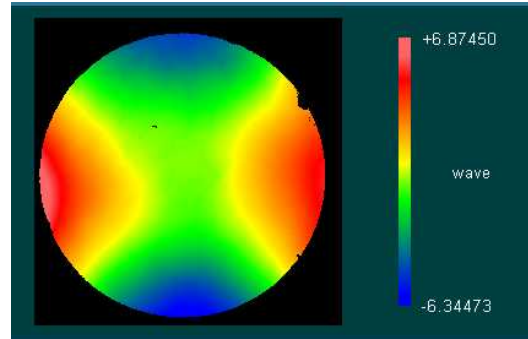
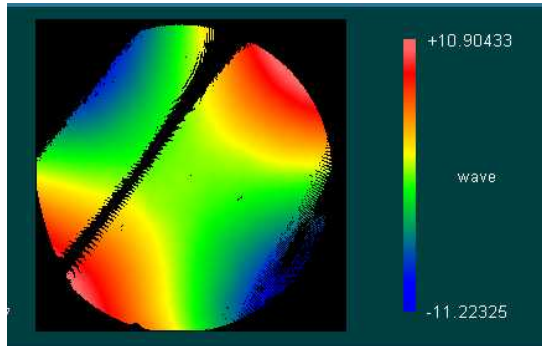
| Modality          | WFE (wv) | Total Force (N) | Ease of Control | Fine Control |
|-------------------|----------|-----------------|-----------------|--------------|
| Point-Load        | 493.2    | 462             | High            | Low          |
| Radial Force      | 116.6    | 12891           | High            | Low          |
| Radial/Ring       | 24.6     | 20577           | Medium          | Medium       |
| Constant Pressure | 166.1    | 1011            | High            | Medium       |
| Annular Ring      | 22.0     | 358             | Medium          | High         |

- WFE is most important
- Total required force is second to reduce SWaP

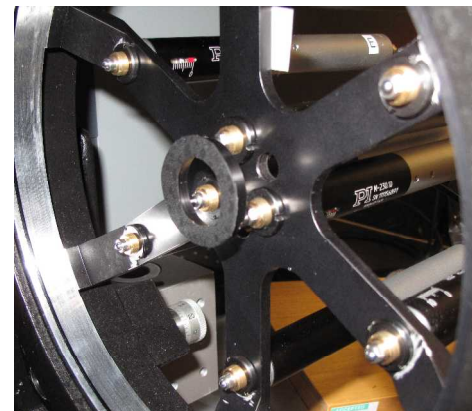
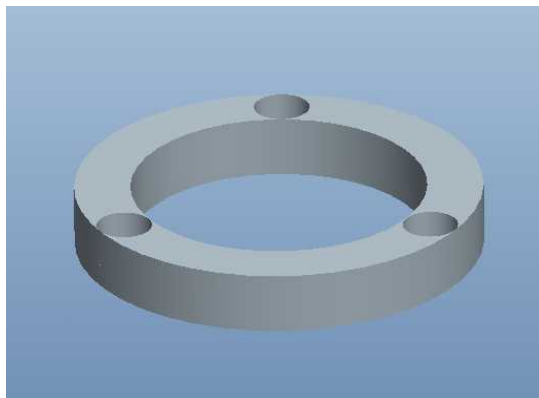


# Inner Ring

- Weight of rings increases astigmatism

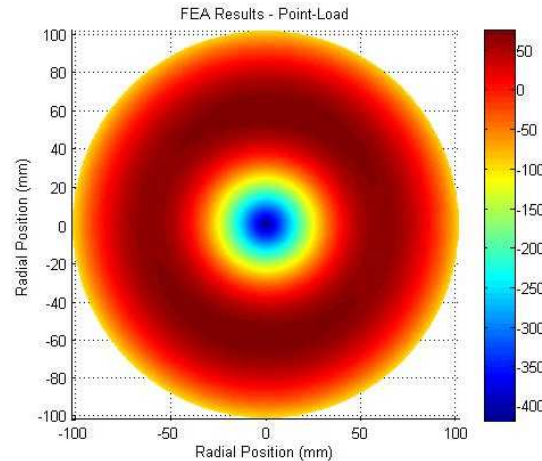


- Inner ring attached to actuators via magnets



# Actuator Influence

- FEM predicts large actuator influence function

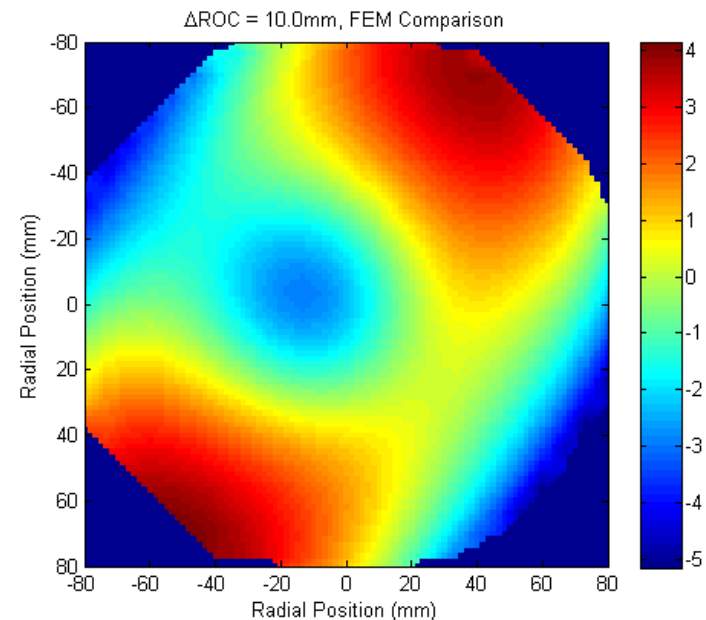
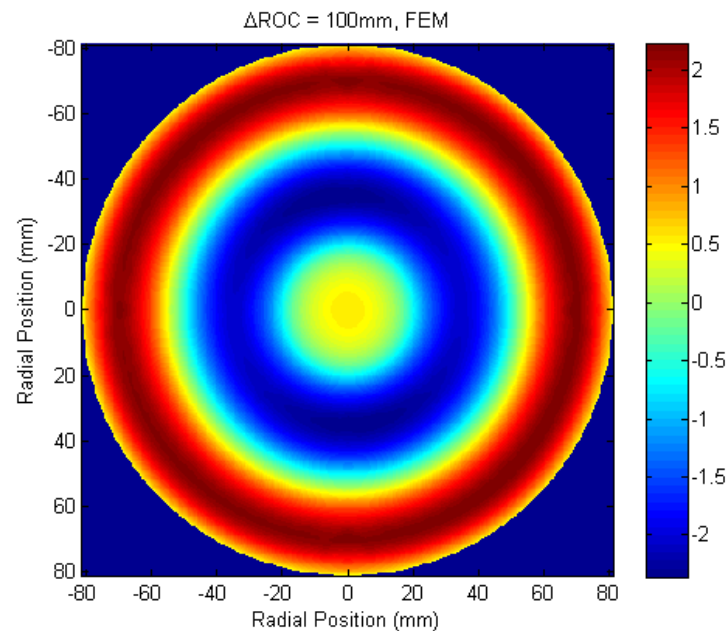


- Placed neoprene layer between ring/mirror



# Comparison to FEM

- FEM assumes perfect spherical surface initially
- Initial WFE subtracted from final



- Low correlation between theory and experiment