

# Role of Hydrodynamic Stability in Velocity-Coupled Combustion Instability

Jacqueline O'Connor

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IWFSCI-2012

Session III: Combustion instability – observations, mechanisms, & control

## Overview

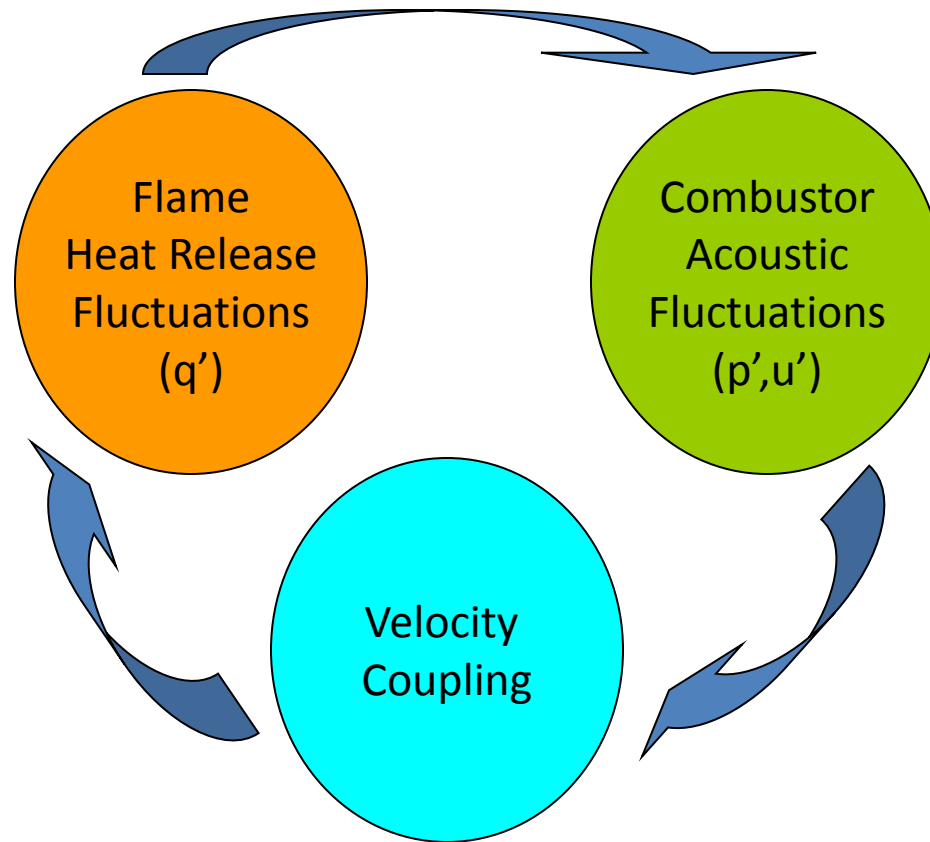
- Velocity coupled combustion dynamics
  - Mechanism
  - Examples
- Hydrodynamic instability of swirling flow
- Forced response characteristics of swirling flow
- Local and global flame response considerations
- Future research directions

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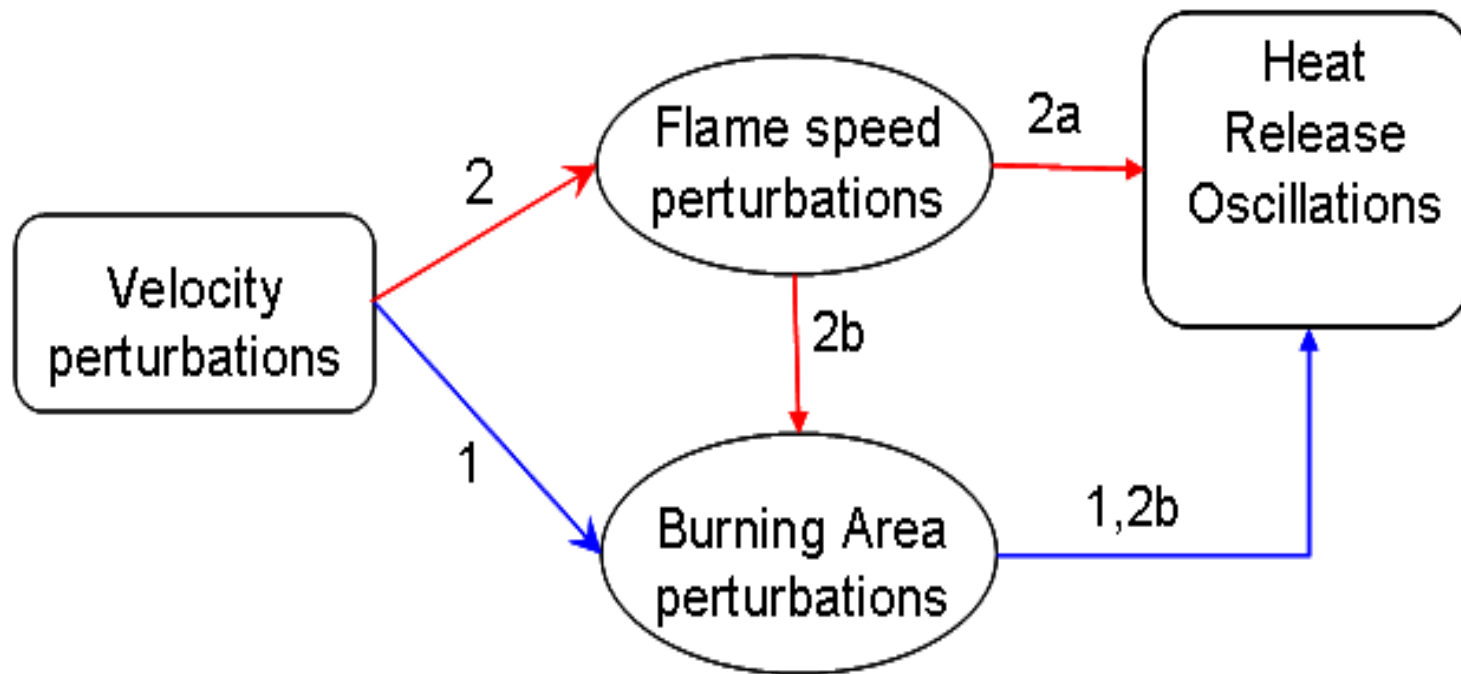
# Velocity-Coupled Combustion Instability – Mechanism

- Velocity fluctuations stem from both acoustic and vortical velocity fluctuation sources



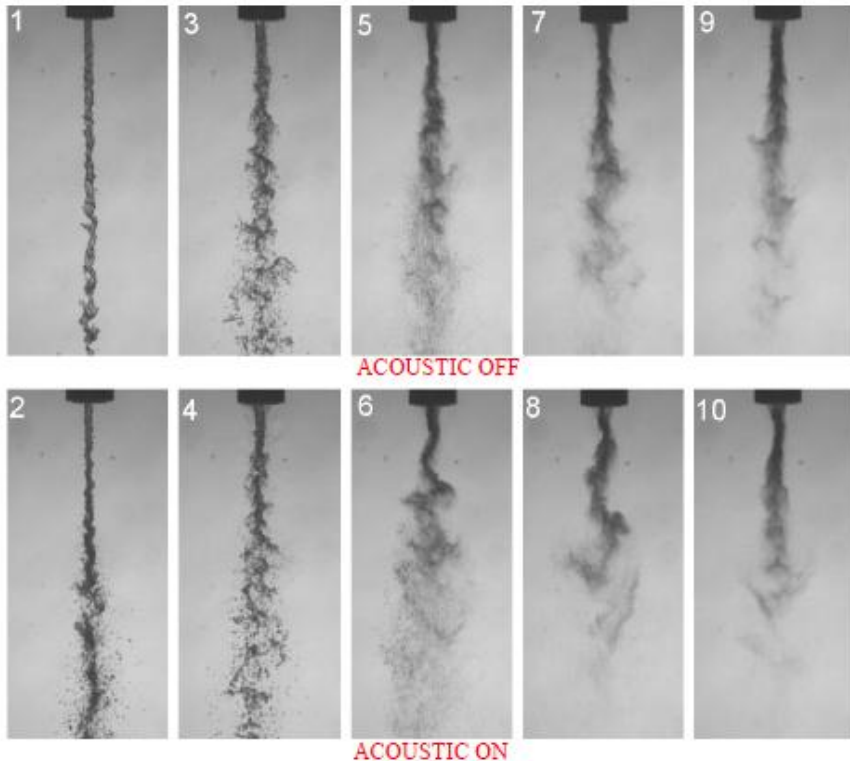
## Velocity-Coupled Combustion Instability – Mechanism

- Velocity fluctuations lead to global heat release fluctuations largely through a flame area fluctuation mechanism



# Velocity-Coupled Combustion Instability – Rockets

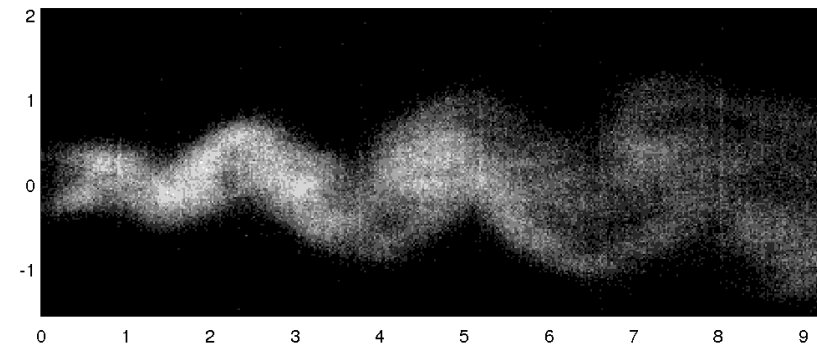
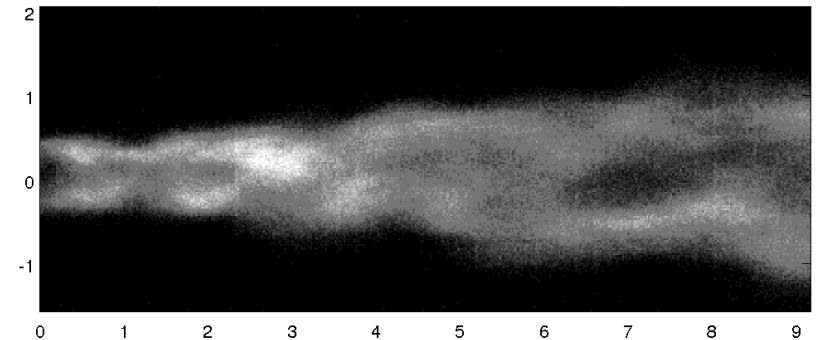
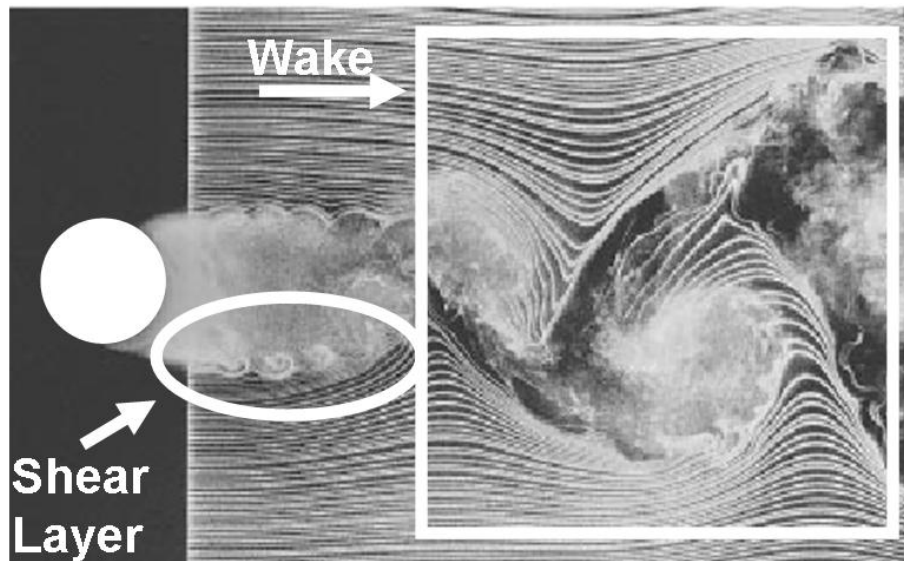
- Acoustic velocity fluctuations lead to variable jet breakup and high-amplitude heat release fluctuations



*Davis and Chehroudi, AIAA2004-1330*

# Velocity-Coupled Combustion Instability – Augmentors

- Flame fluctuations are due to both wake and shear layer instability



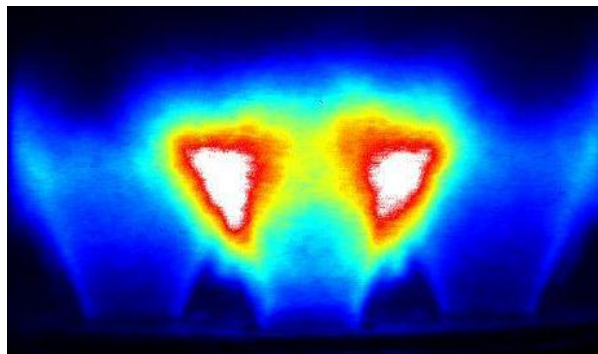
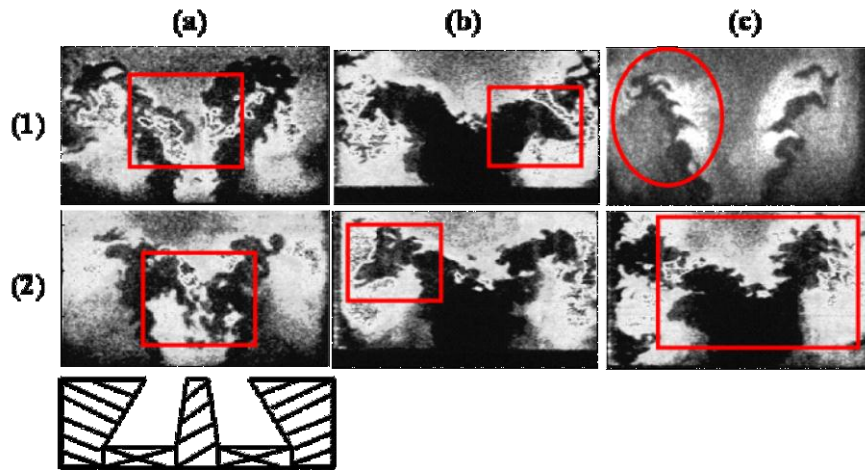
*Prasad and Williamson, JFM, 1997*

*Emerson et al., AIAA, 2011*



# Velocity-Coupled Combustion Instability – Gas Turbine Combustors

- Several instability modes in swirling flows disturb the flame

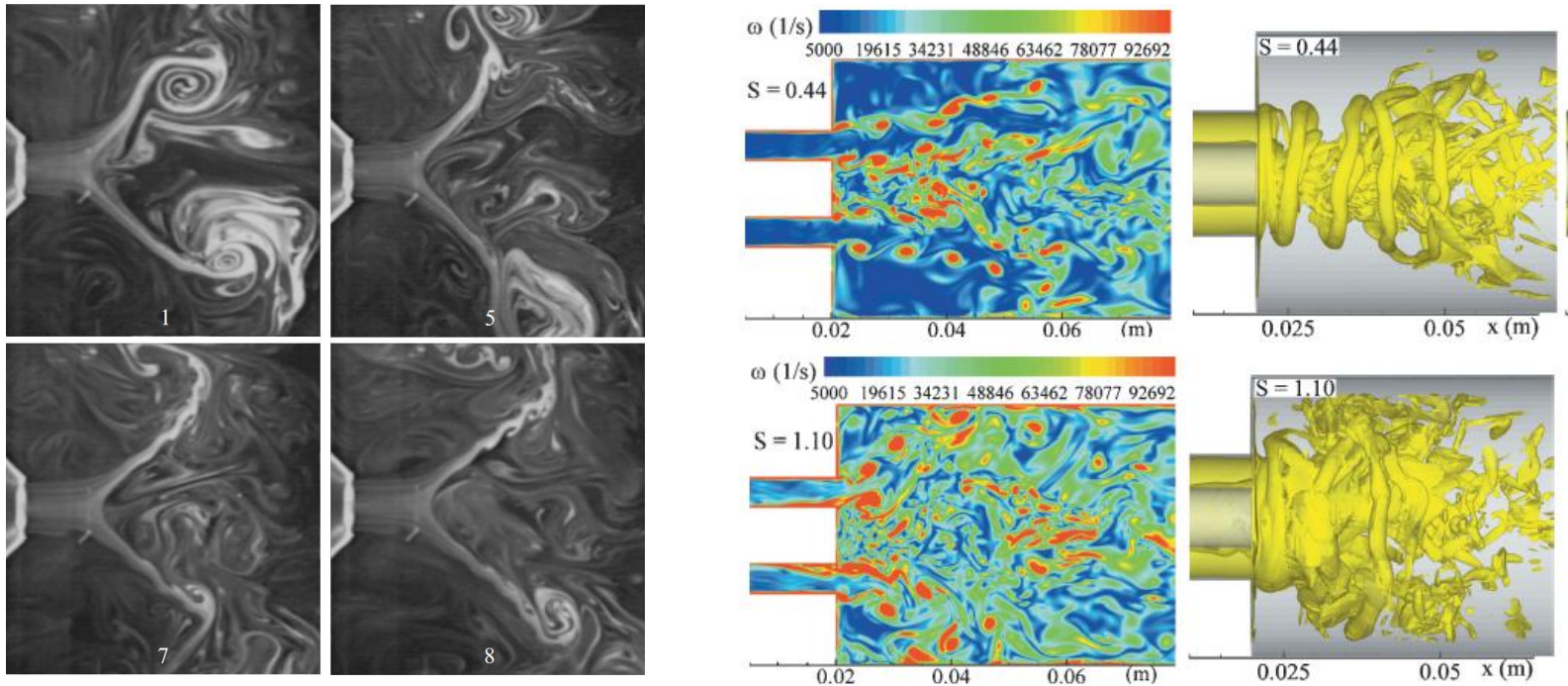


Lieuwen and Yang, AIAA, 2005  
Thumuluru and Lieuwen, Proc. Comb. Inst., 2009  
Szedlmayer et al., GT2011-46080



# Combustion Instabilities in Gas Turbines

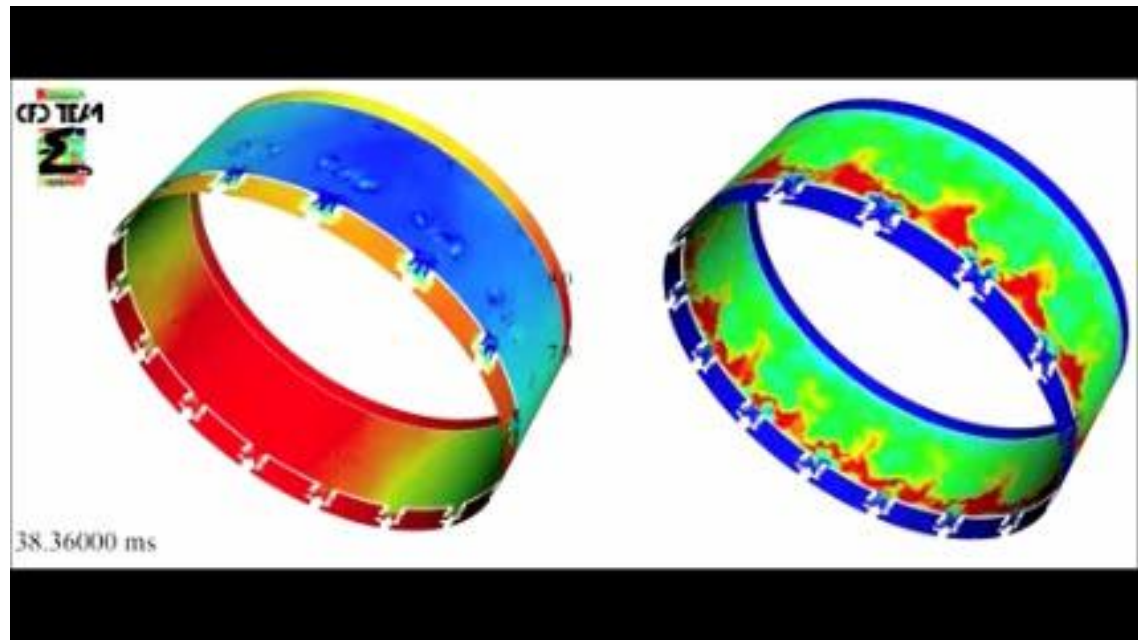
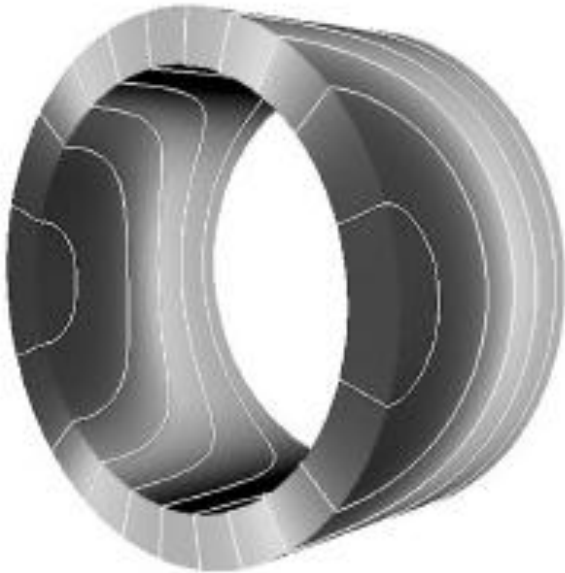
- What are some of the specific issues in gas turbine combustor instabilities?
  - Complicated flow fields – swirling flows are hydrodynamically unstable and susceptible to acoustic forcing



*Billant et al., JFM, 1998, Huang et al., AIAA J., 2006*

# Combustion Instabilities in Gas Turbines

- What are some of the specific issues in gas turbine combustor instabilities?
  - Mixed acoustic mode shapes



*C. Sensiau et al., Int. J. of Aeroacoustics, 2009*

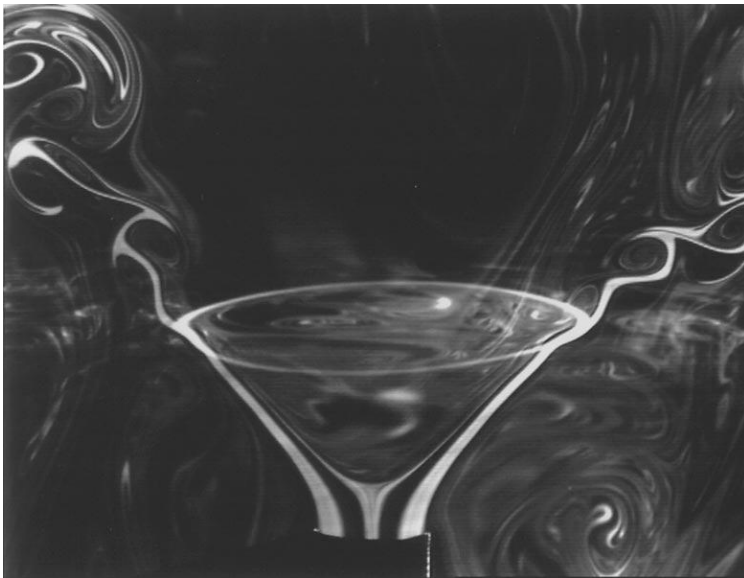
*P. Wolf, G. Staffelbach, L. Gicquel and T. Poinsot, CERFACS, 2010*

## Overview

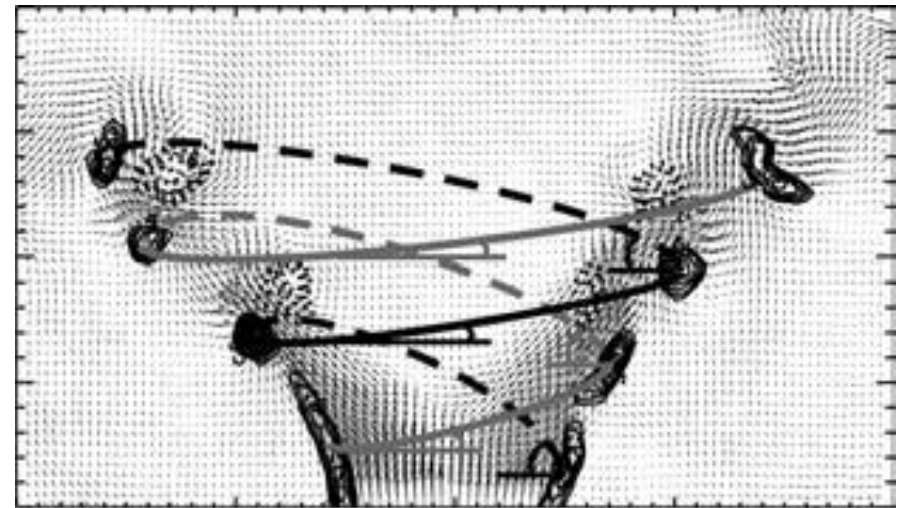
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# Velocity Fluctuations from Hydrodynamic Instability

- Unsteady motions in swirling flows due to at least two hydrodynamic instability mechanisms
  - Swirling jet instability – vortex breakdown (AI)
  - Shear layer instability – Kelvin-Helmholtz (CI)



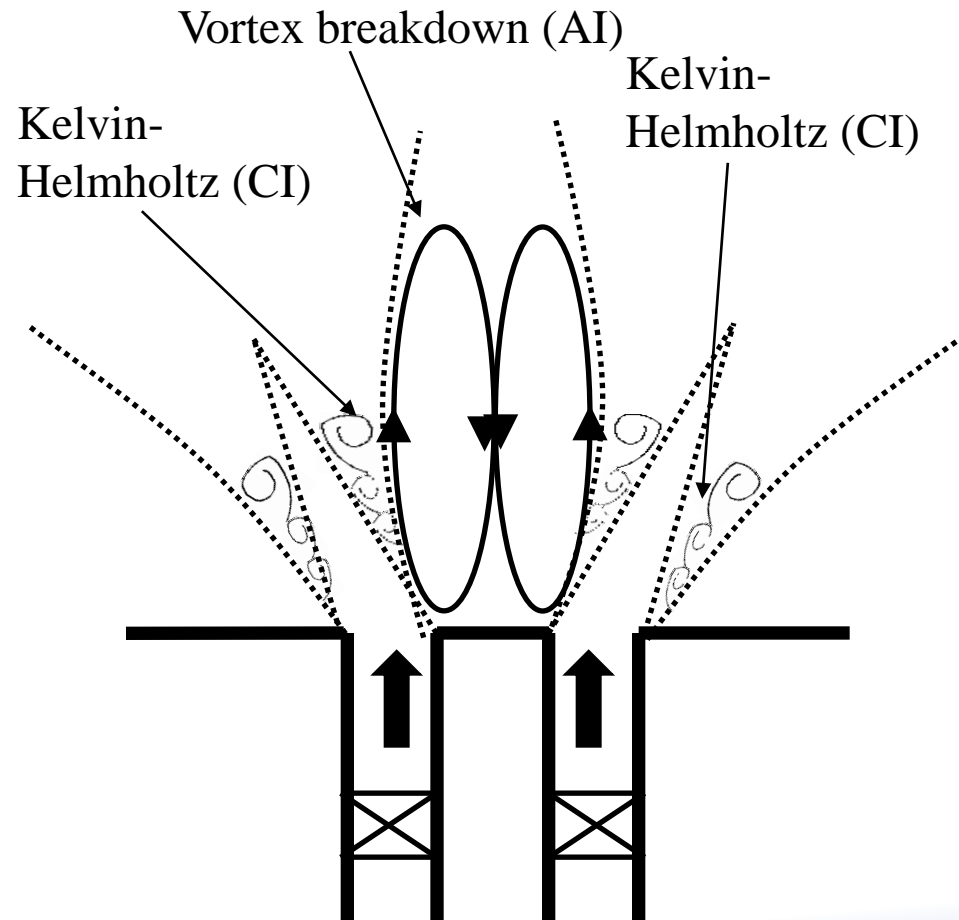
*Billant et al., JFM, 1998*



*Liang and Maxworthy, JFM, 2006*

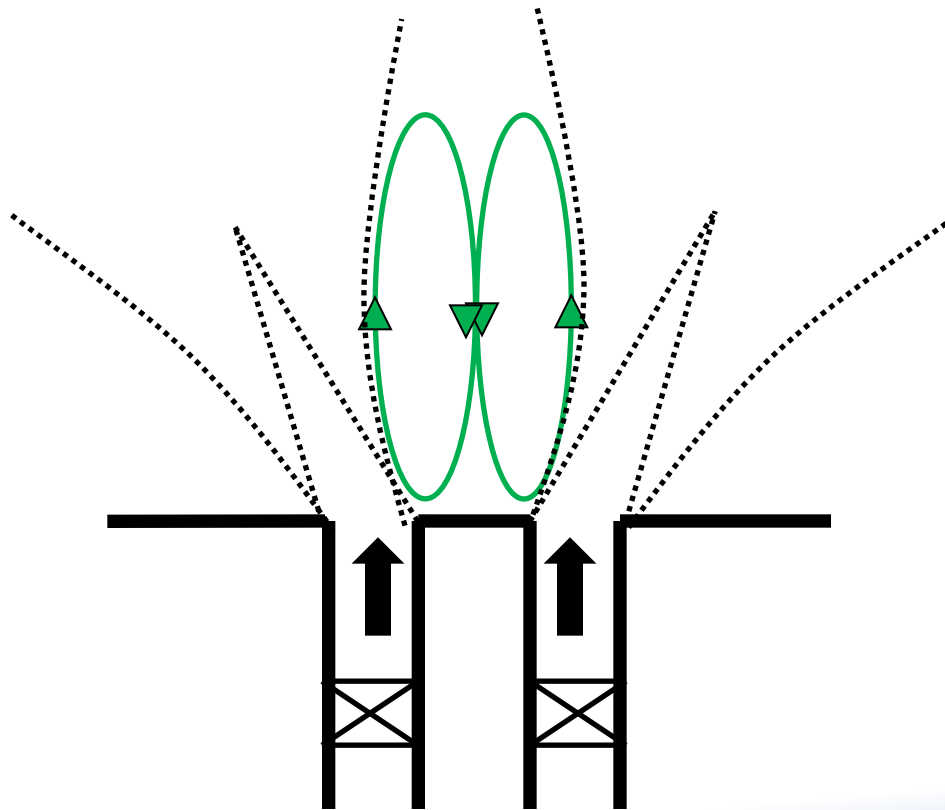
# Velocity Fluctuations from Hydrodynamic Instability

- Unsteady motions in swirling flows due to at least two hydrodynamic instability mechanisms



# Swirling Flow Instability

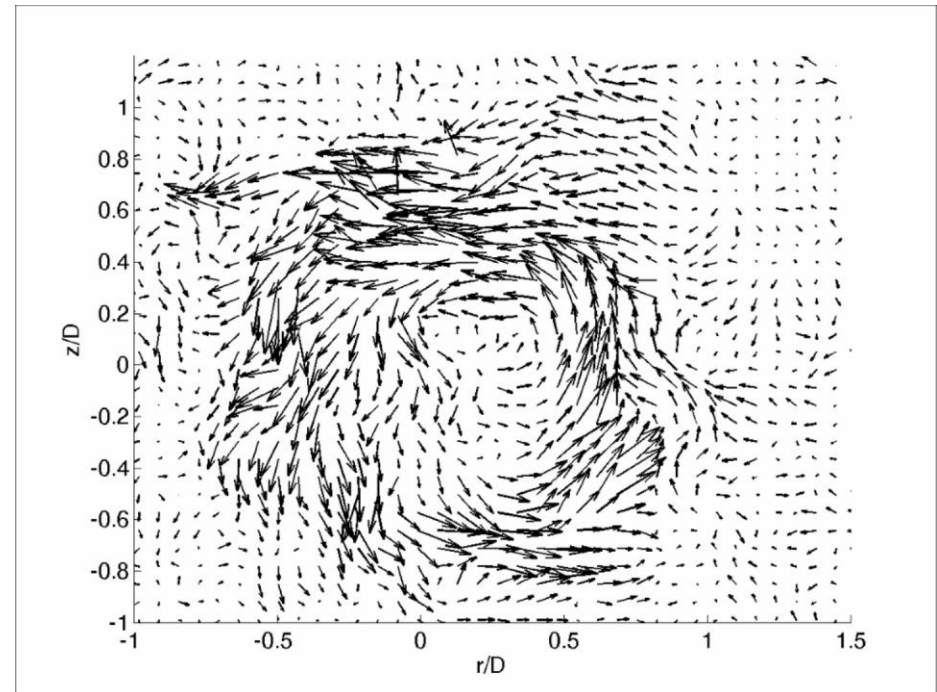
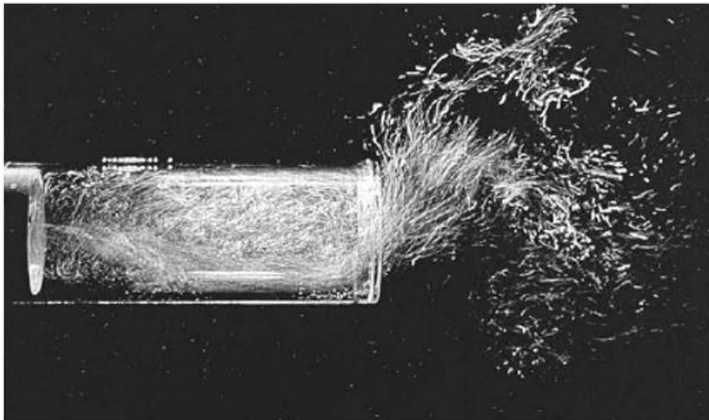
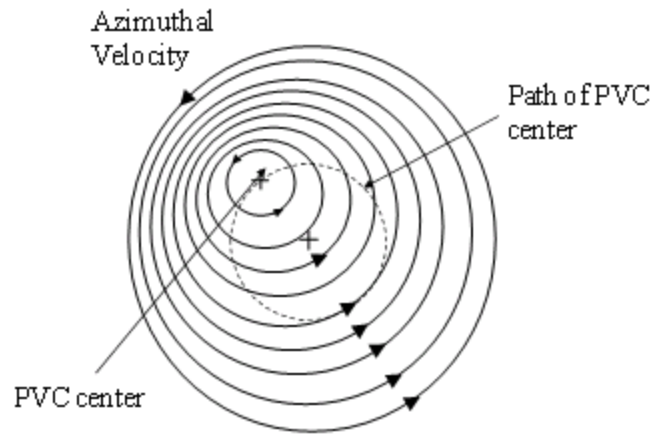
- Swirling jet instability – vortex breakdown (AI)
  - Absolute instability – self-excited oscillator
    - Displays intrinsic dynamics except at high-amplitude forcing
  - Function of Reynolds number, swirl number, geometry





# Dynamical Role of Vortex Breakdown

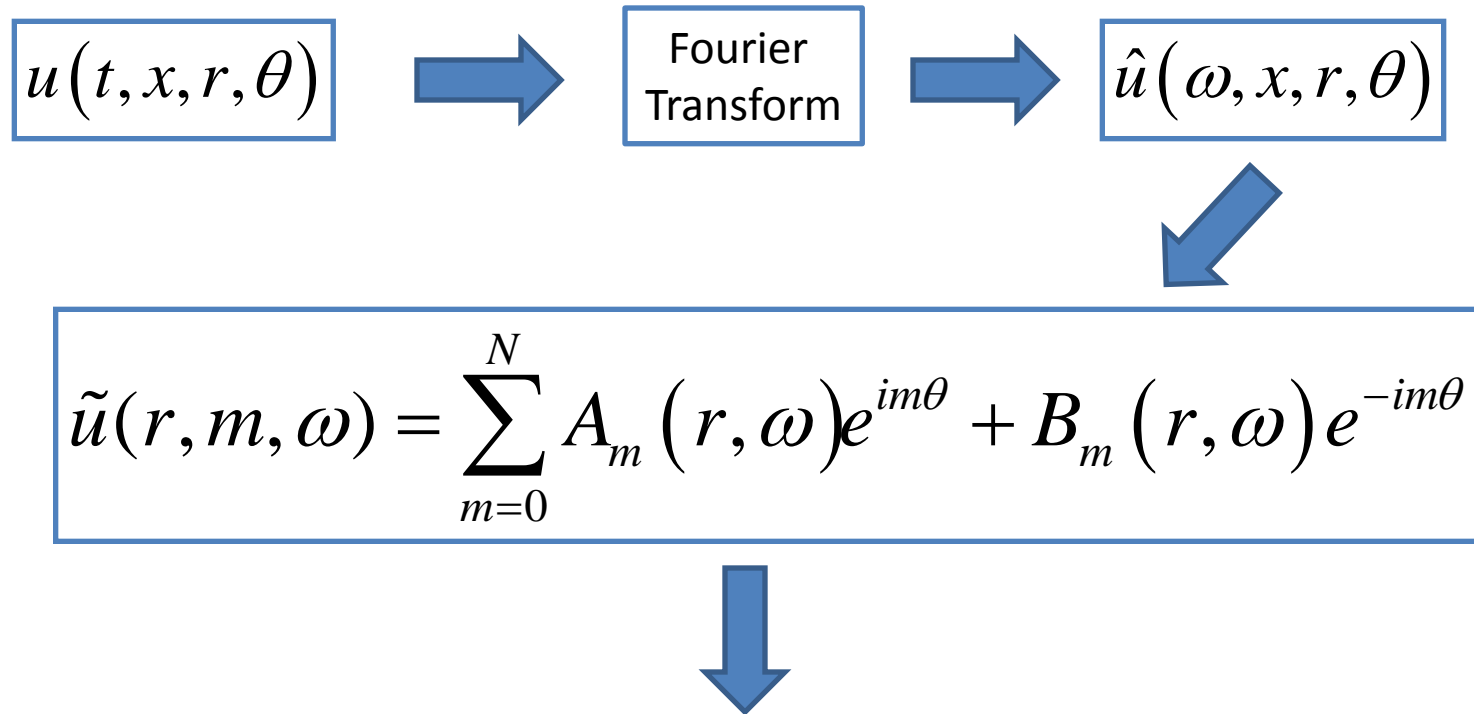
- The vortex breakdown region does have a dynamical role in the flow field, particularly in the form of a precessing vortex core





## Spatial Modal Decomposition

- Spatial mode decomposition in the  $r$ - $\vartheta$  plane

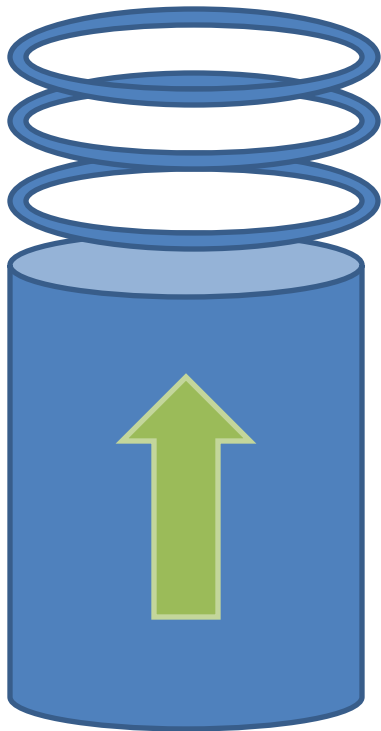


$A_m, m < 0$  – co-swirling (counter-clockwise)

$B_m, m > 0$  – counter-swirling (clockwise)

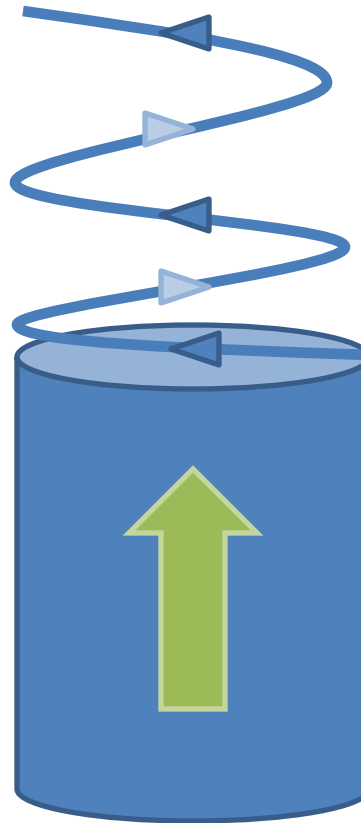
# Spatial Modal Decomposition

$m=0$



Symmetric

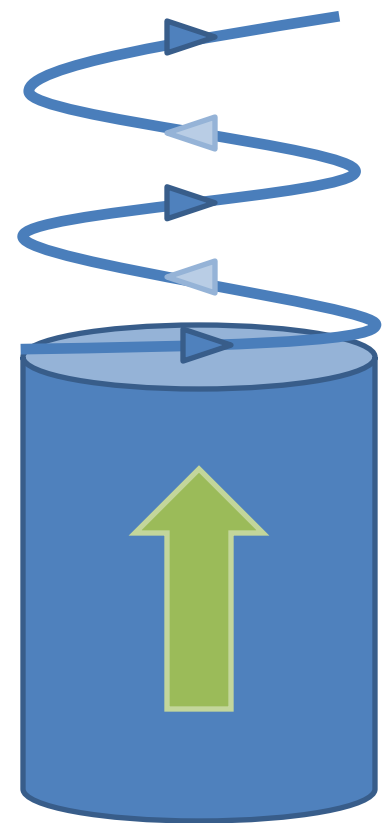
$m=1$   
Clockwise



Asymmetric

$m=-1$

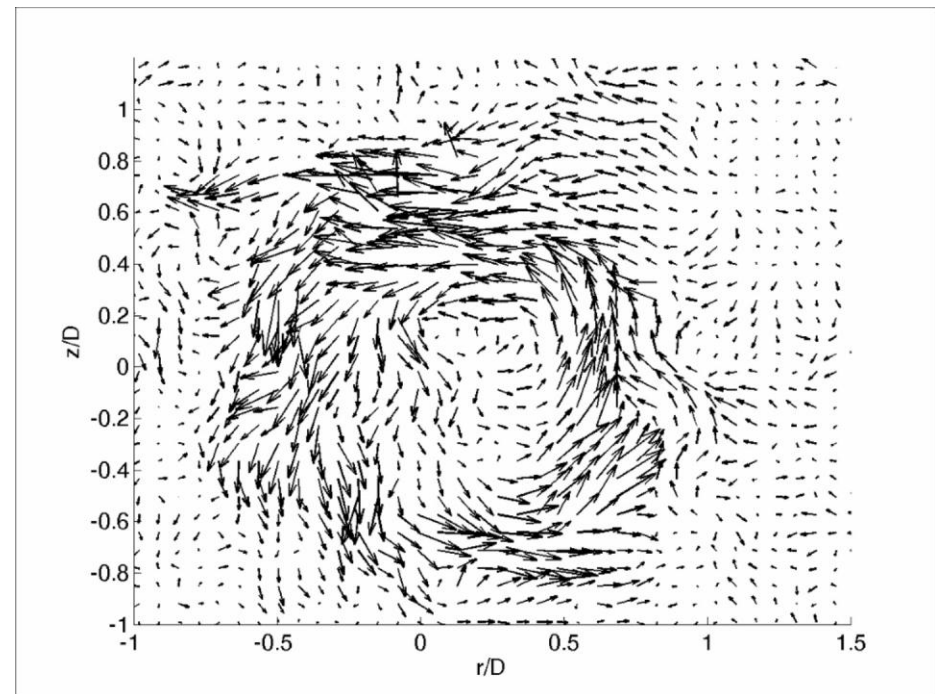
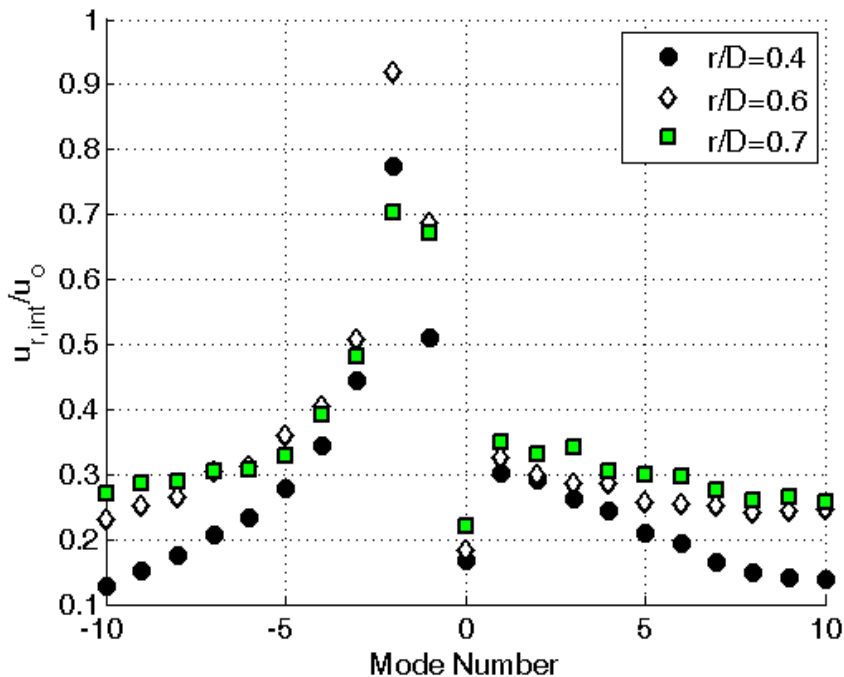
Counter-clockwise



Asymmetric

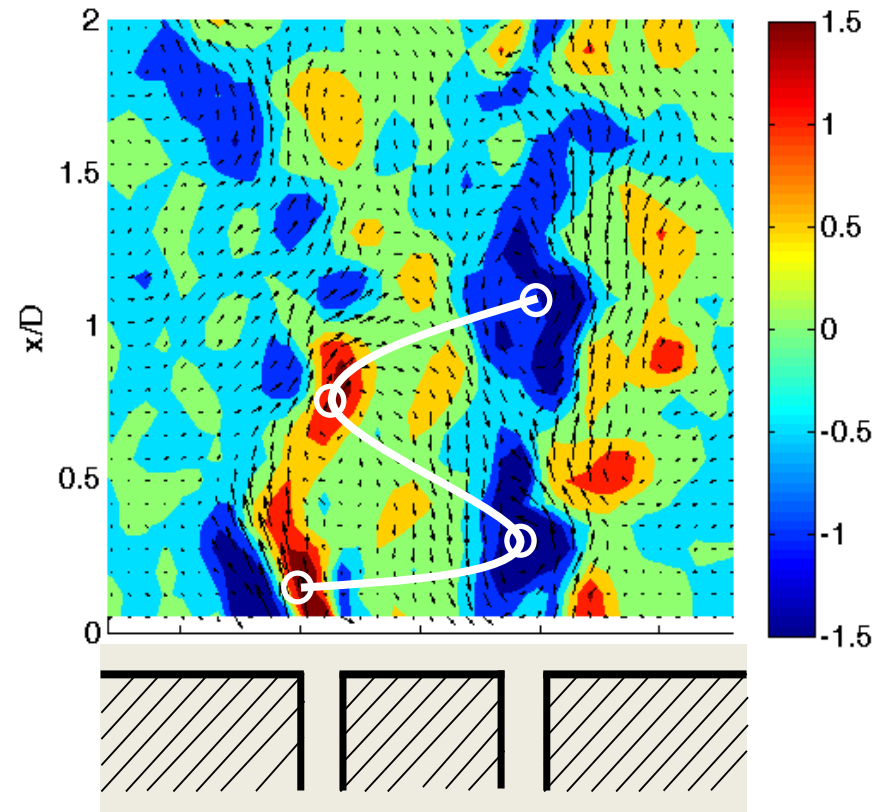
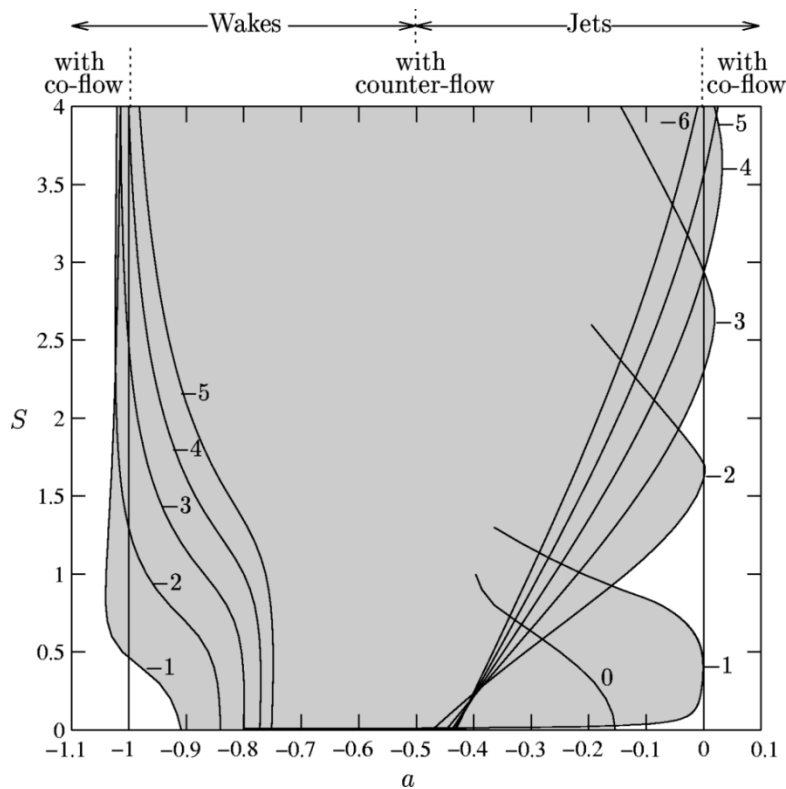
## Role of Vortex Breakdown in Disturbance Field

- Several spatial modes of instability are present, but in particular,  $m=-1$  and  $m=-2$



# Swirling Flow Instability

- Shear layer instability – Kelvin-Helmholtz
  - Most amplified shear layer mode is helical
  - Bias due to the action of swirl

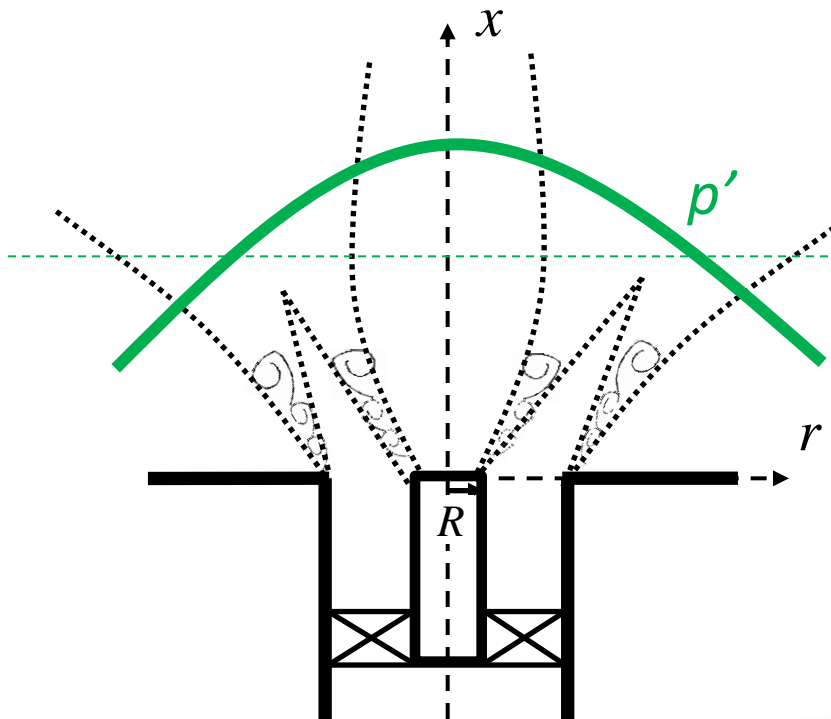


Loiseleux et al., *Phys. of Fluids*, 1998

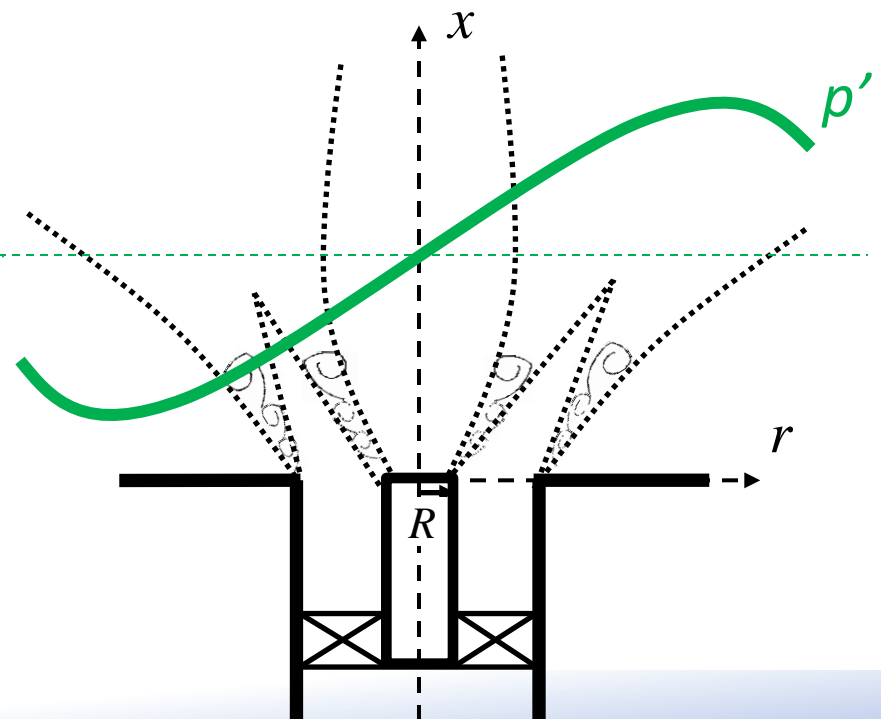
# Swirling Flow Instability

- Shear layer instability – Kelvin-Helmholtz
  - Convectively unstable – disturbance amplifier
  - Strong response to external excitation (acoustic forcing)
  - Response is a function of frequency, amplitude, **symmetry**

## Symmetric Forcing



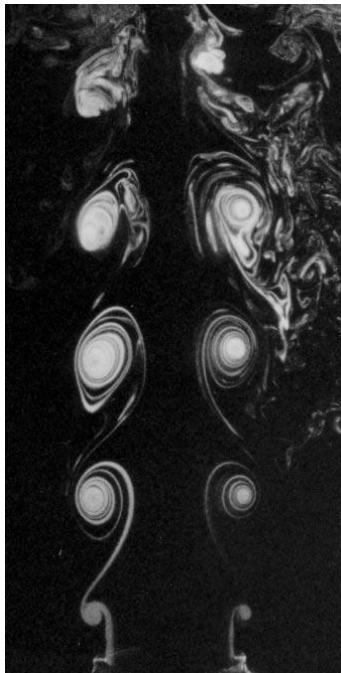
## Asymmetric Forcing



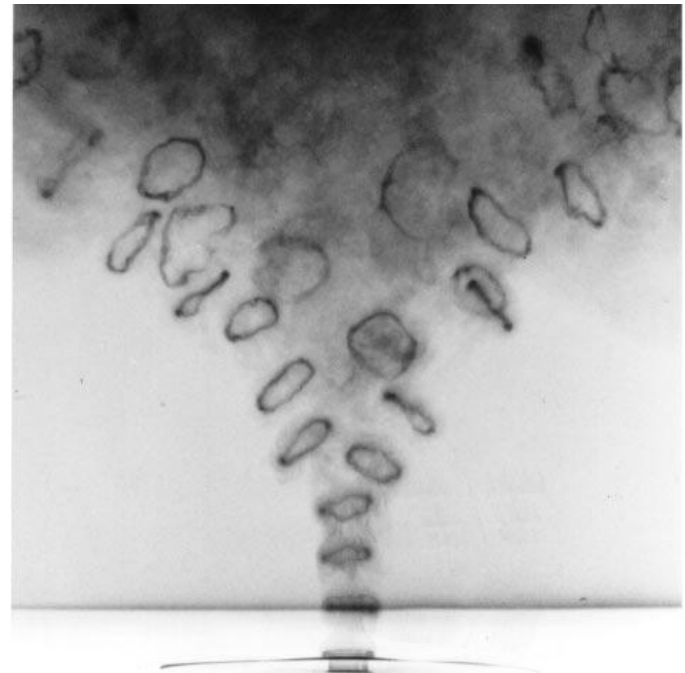
# Swirling Flow Instability

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## Symmetric Forcing



## Asymmetric Forcing



*Reynolds et al., ARFM, 2003*

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## Overview

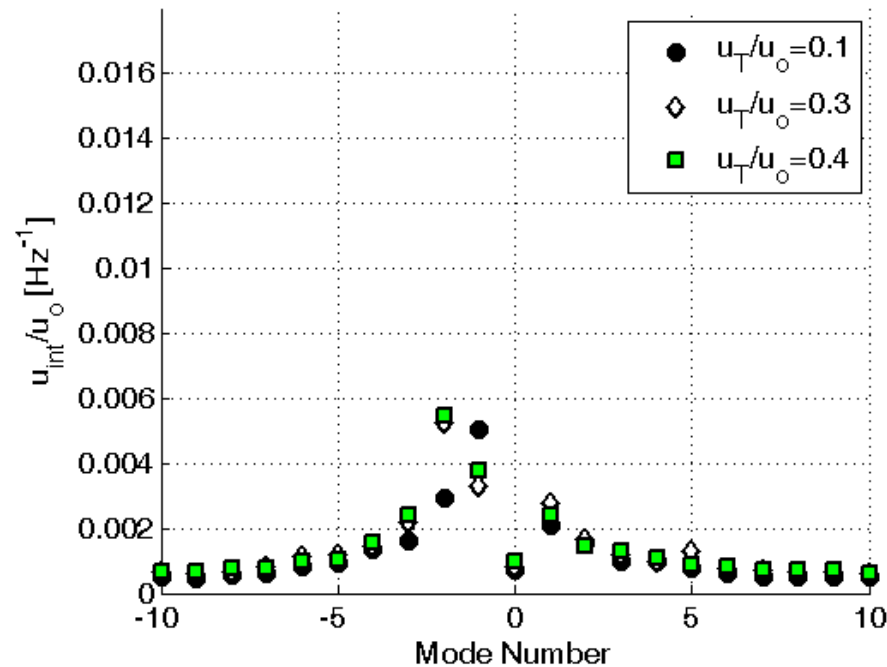
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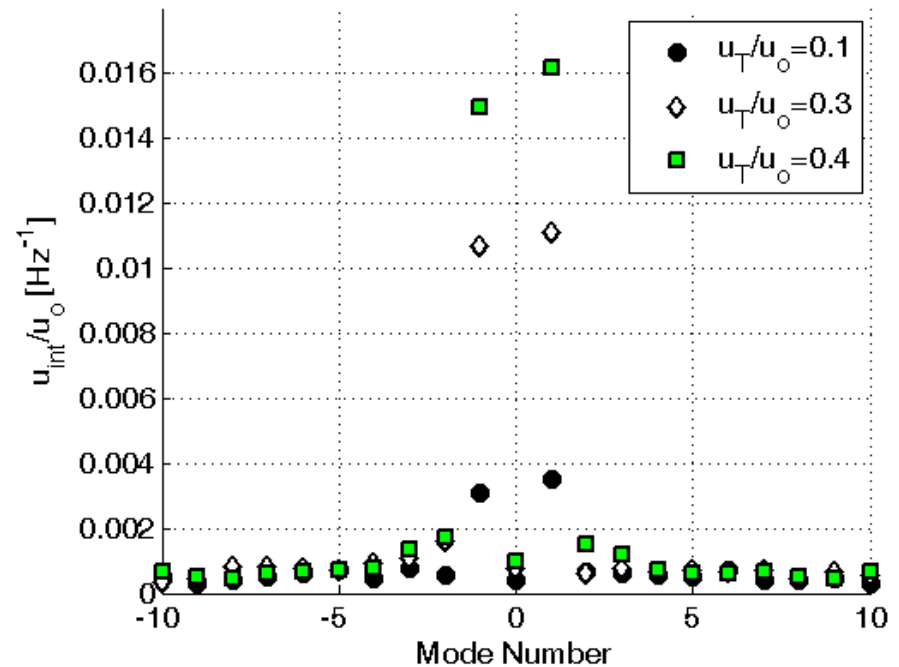
## Role of Vortex Breakdown in Disturbance Field

- Compared to the response of the shear layers, the contribution of the precessing vortex core to the overall velocity disturbance field is small

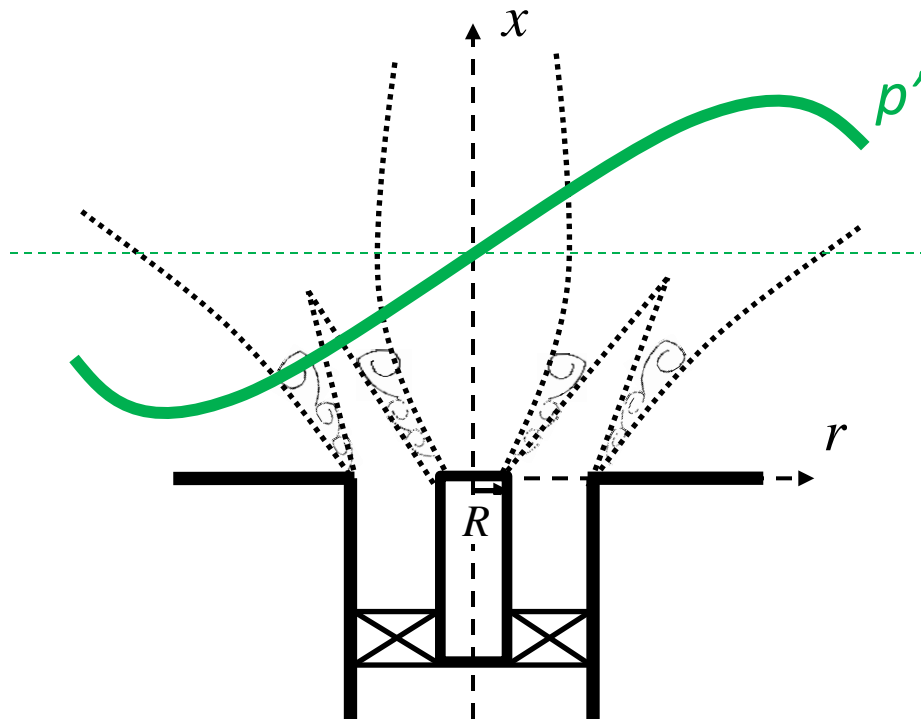
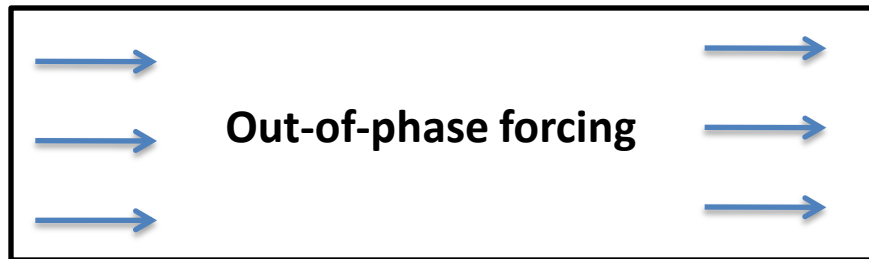
Response at Low Frequency (0-200Hz)



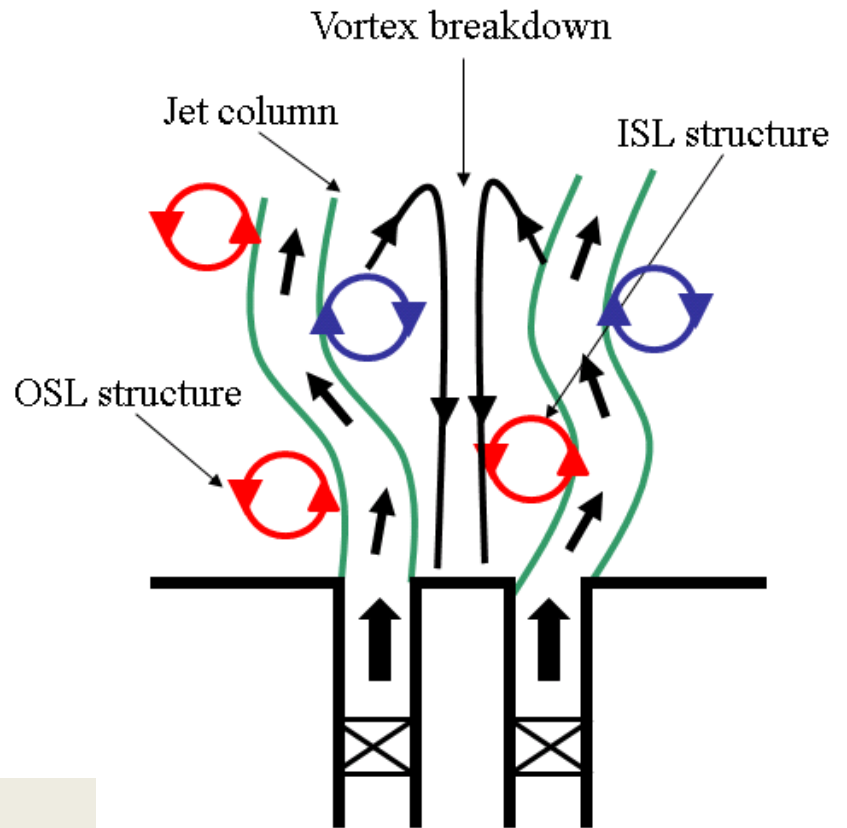
Response at Forcing Frequency (800HzOP)



# Flow Field Topology



## Out-of-phase Forcing

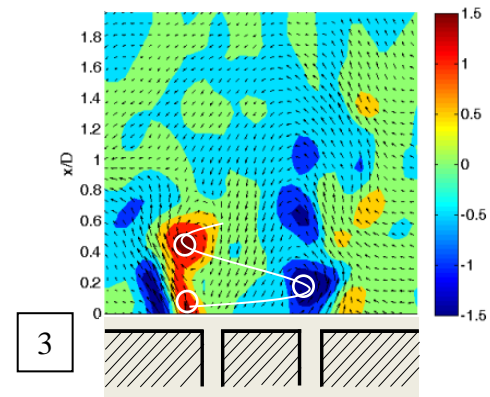
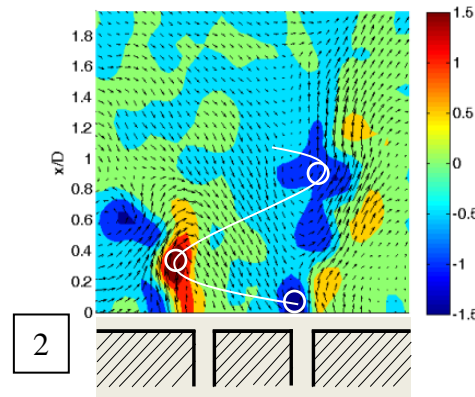
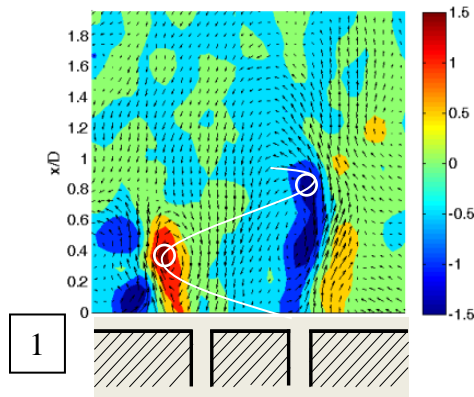


Asymmetric acoustic velocity  
Helical shear layer response

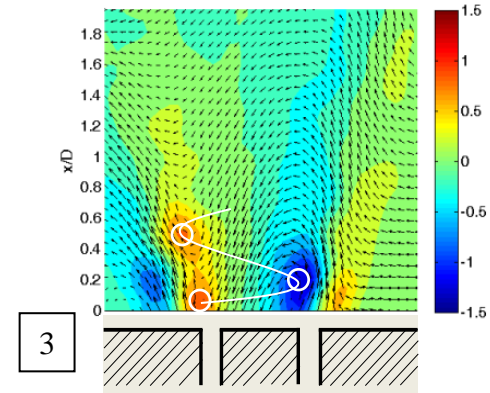
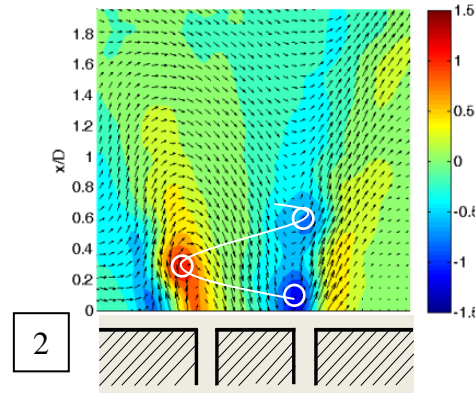
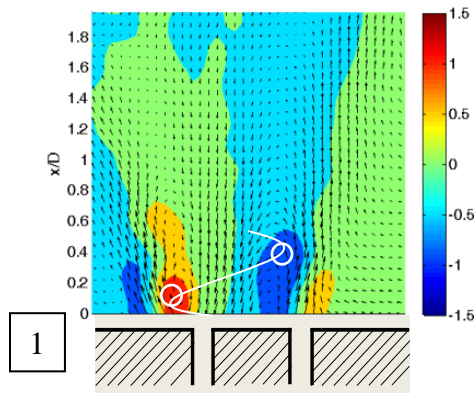
# Flow Field Topology – Phase-Averaged Velocity

## Out-of-phase Forcing

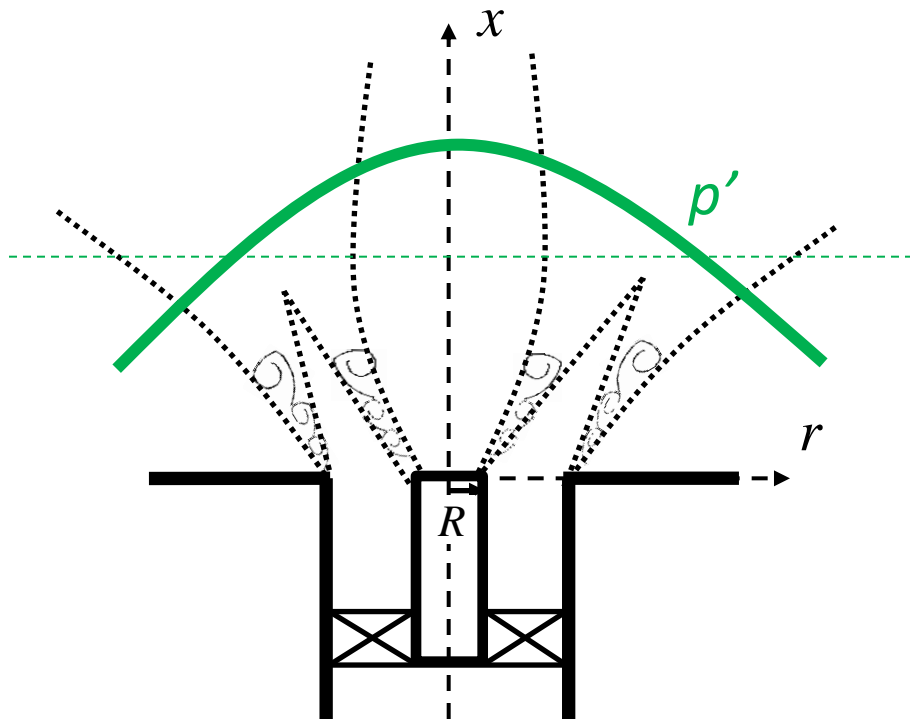
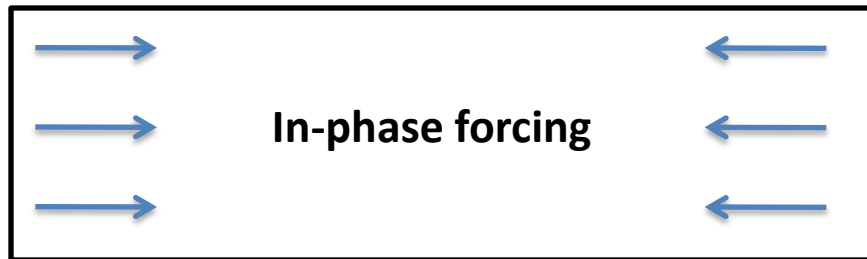
Instantaneous



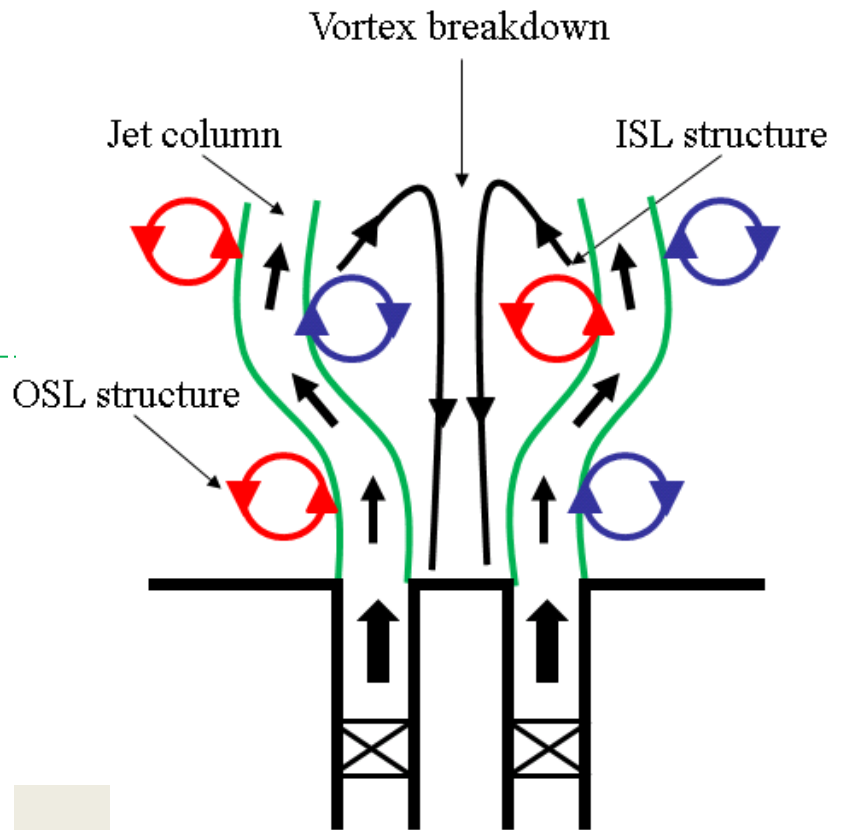
Phase-average



# Flow Field Topology



## In-phase Forcing

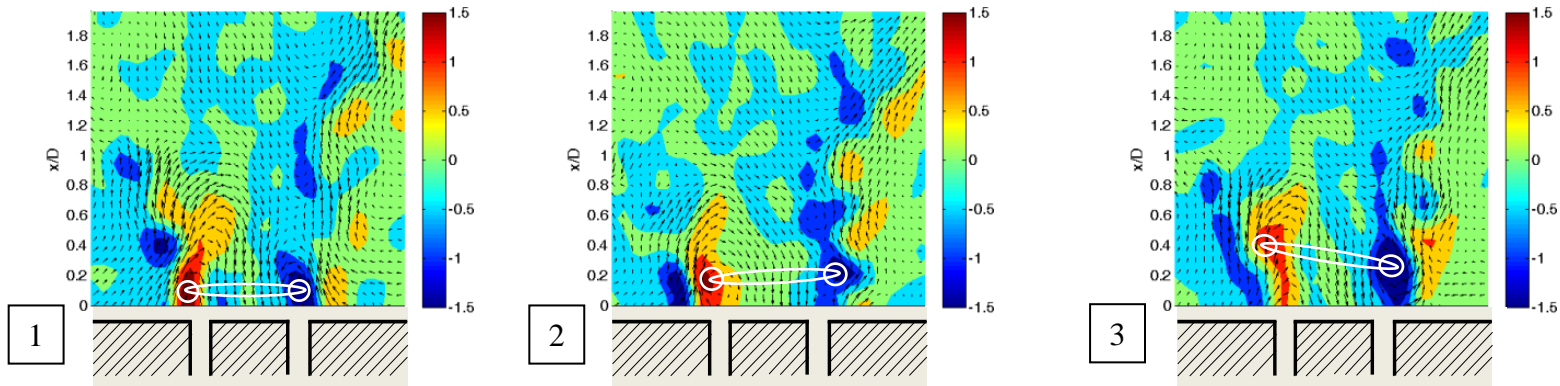


Symmetric acoustic velocity  
Ring vortex shedding

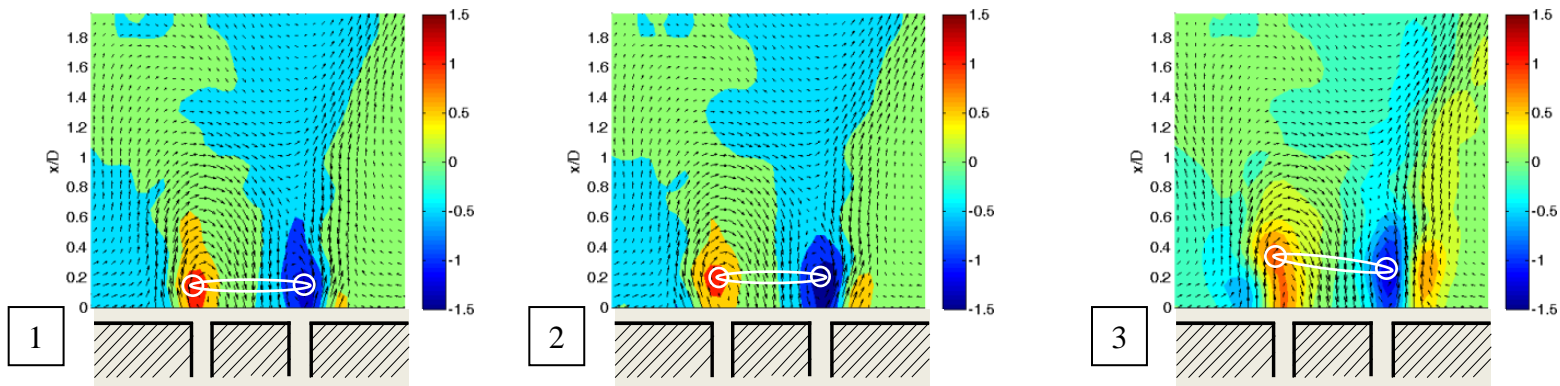
# Flow Field Topology – Phase-Averaged Velocity

## In-phase Forcing

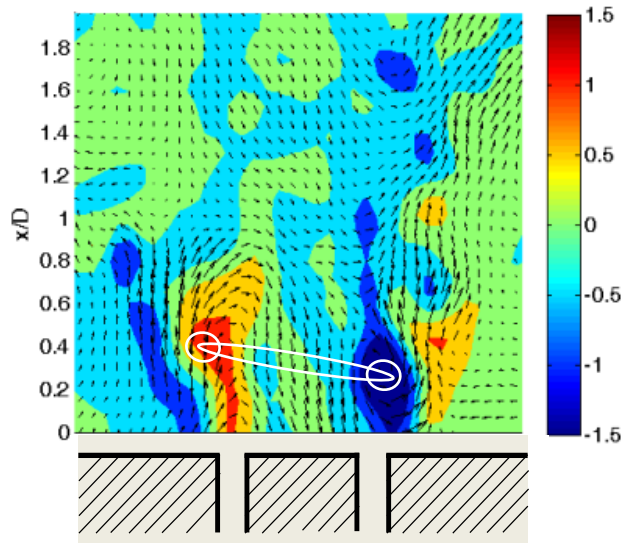
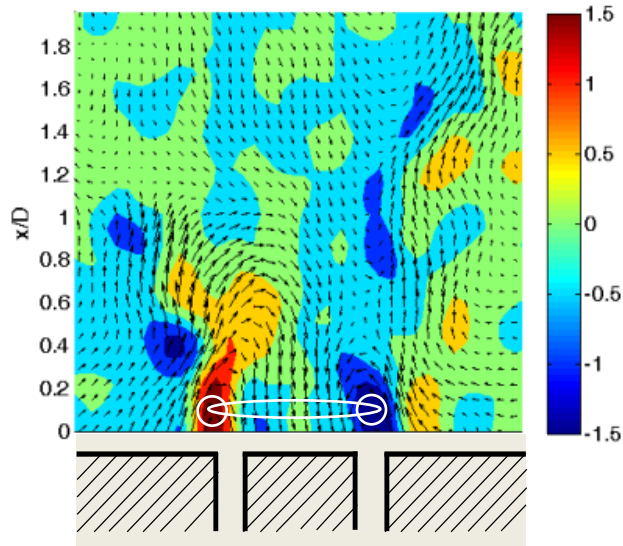
Instantaneous



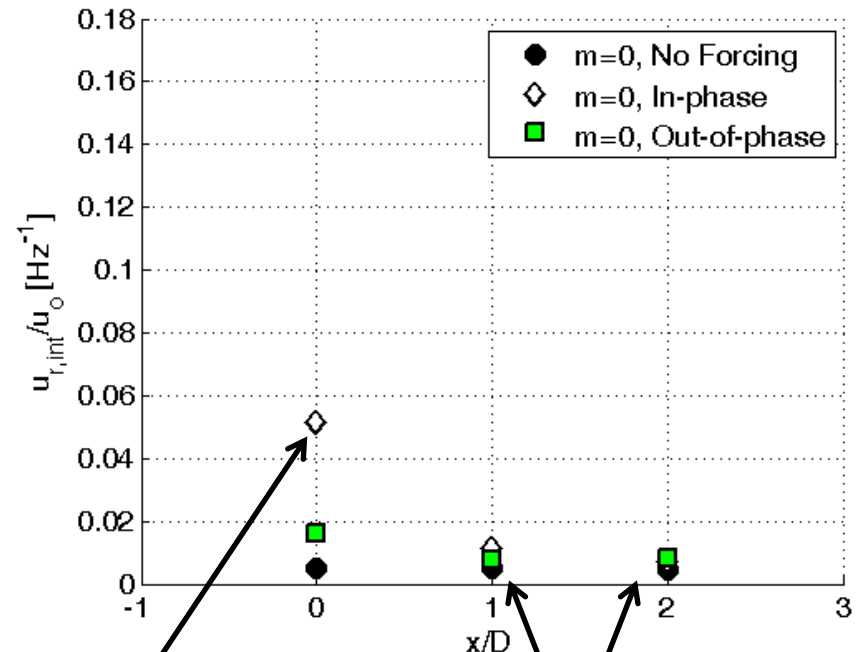
Phase-average



# Flow Field Topology – Downstream Development



## Mode $m=0$



Ring vortex,  
symmetric

Tilted ring-vortex,  
asymmetric

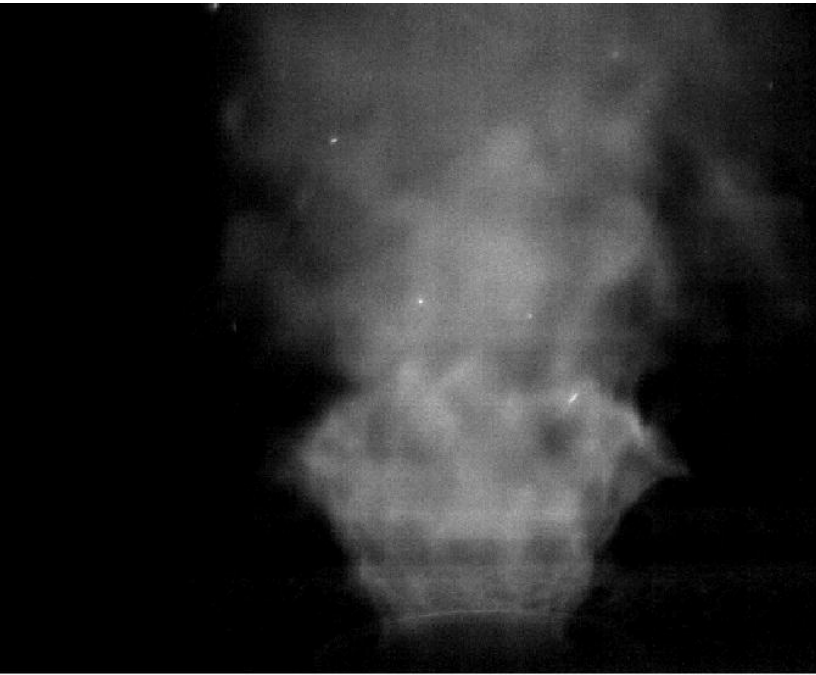
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# Role of Acoustic Field Symmetry in Flame Response

## Symmetric Forcing



400 Hz in-phase,  
 $U_o=10$  m/s,  $\phi=0.9$

Symmetric acoustic velocity  
Ring vortex shedding

## Asymmetric Forcing

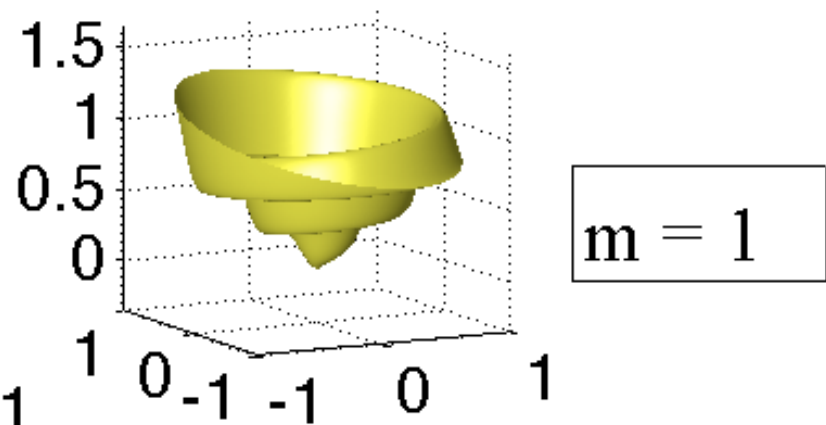
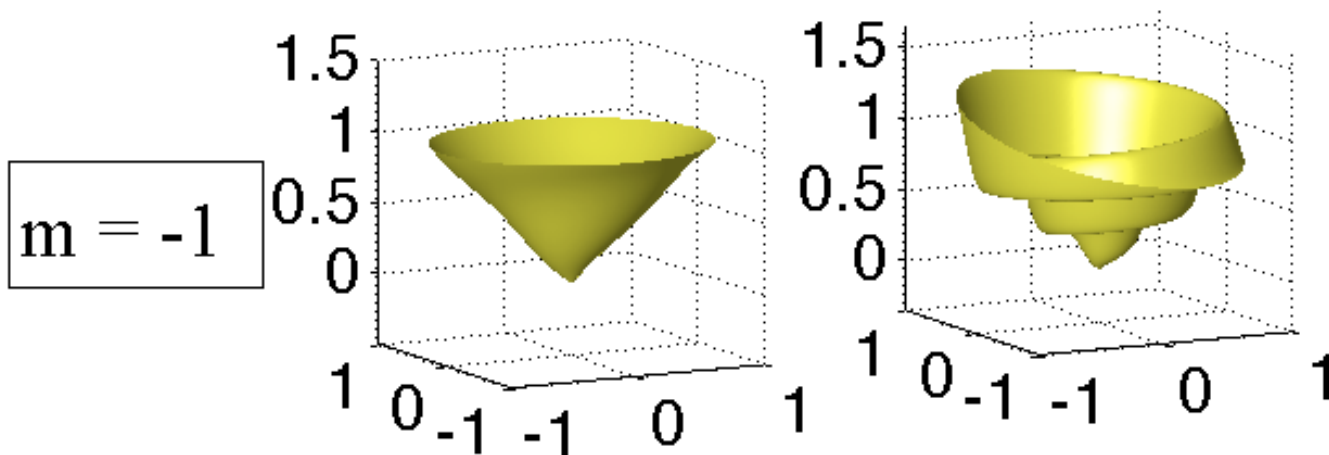
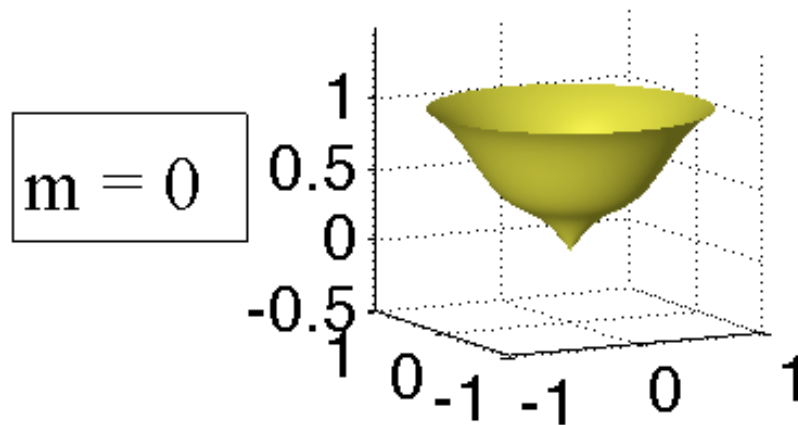


400 Hz out-of-phase,  
 $U_o=10$  m/s,  $\phi=0.9$

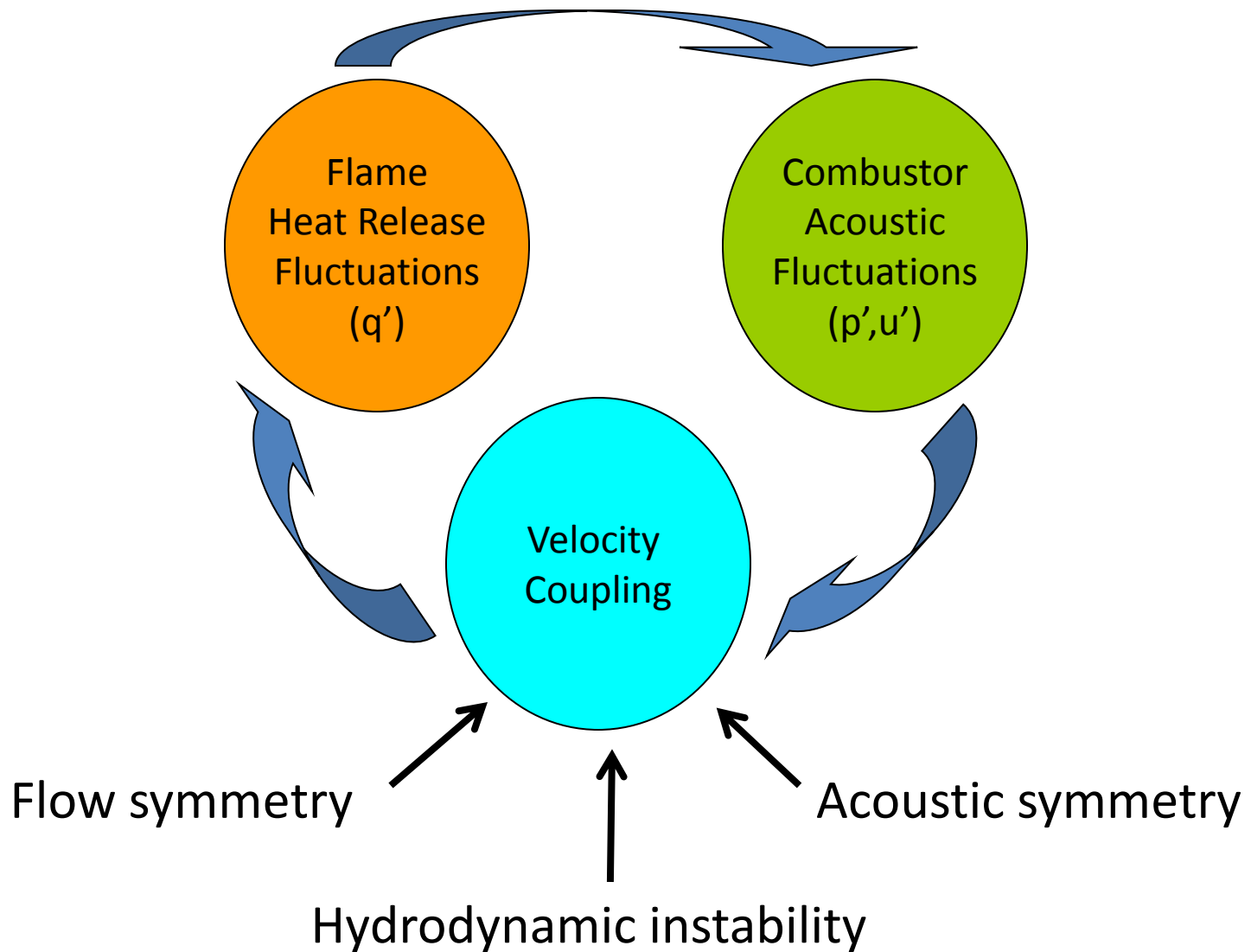
Asymmetric acoustic velocity  
Helical shear layer response

## Role of Acoustic Field Symmetry in Flame Response

- Analytical results show significant difference in **global** flame response characteristics between symmetric and asymmetric vortical velocity disturbance fields



# Velocity-Coupled Combustion Instability



## Key Points

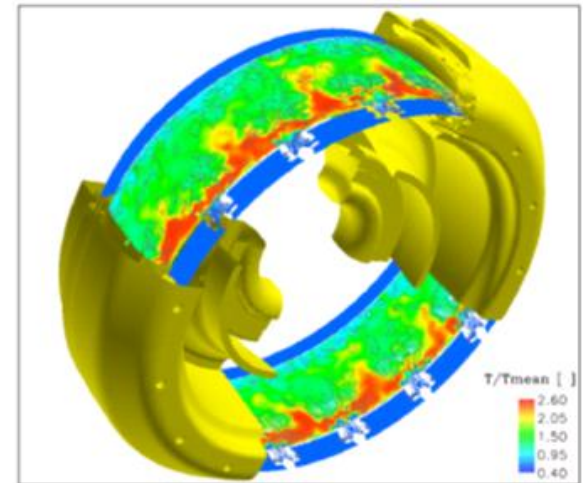
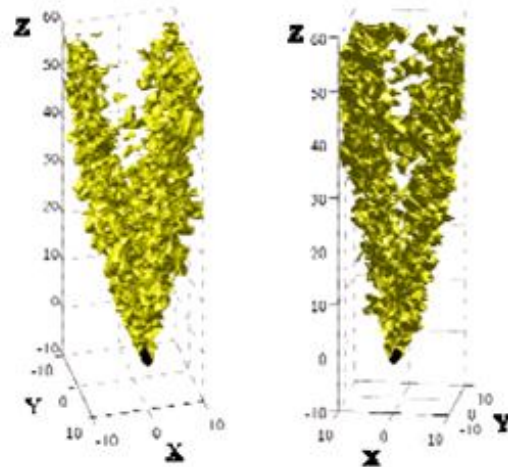
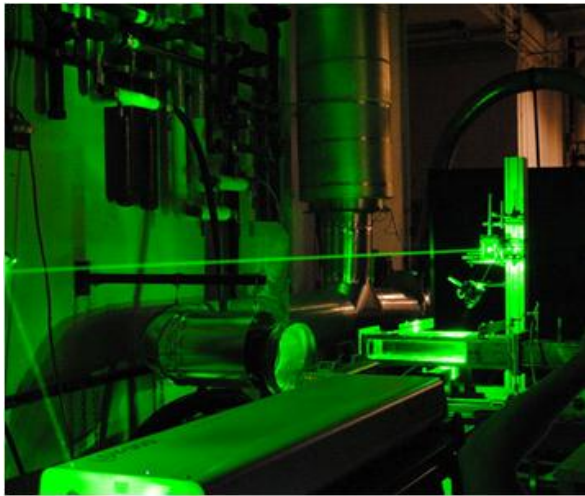
- Combustor flows are often hydrodynamically unstable
  - Rockets – jet instability, jet breakup
  - Augmentors – shear layer instability, wake instability
  - Gas turbines – shear layer instability, vortex breakdown
- Characteristics of these instabilities dictates how these flows will respond to combustor acoustic fields
  - Convectively unstable – disturbance amplifiers
  - Absolutely unstable – self-excited disturbances
  - Acoustic/flow instability symmetries
- Flow response determines local flame disturbances; varying response symmetries can produce vastly different global flame heat release fluctuations

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## Future Research Directions

- Several research needs address not only the subjects under investigation, but also the methodology:
  - Multi-physics understanding
  - High-fidelity diagnostics
  - Comparison between experiment and model
  - Transition of fundamental research to applications



Sources: D. Noble; Hemchandra and Lieuwen, *Comb. And Flame*, 157, 2010 ; Staffellbach et al., *Proc. Comb. Inst.*, 2008

## Acknowledgements

- Georgia Tech, Ben T. Zinn Combustion Laboratory
  - Tim Lieuwen, Professor
  - Michael Malanoski, Michael Aguilar, Vishal Acharya, Ben Emerson
- US Department of Energy under contract DEFG26-07NT43069 and contract monitor Mark Freeman



# Questions?

# Backup Slides

# Experimental Facility

Optical quartz  
window for  
laser access

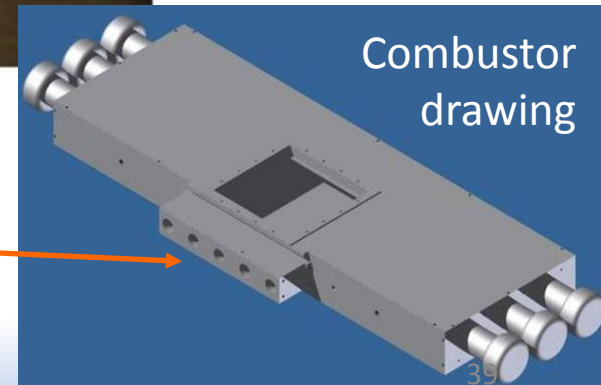


Acoustic drivers

Fuel/air  
premixing  
section

Optical quartz  
window

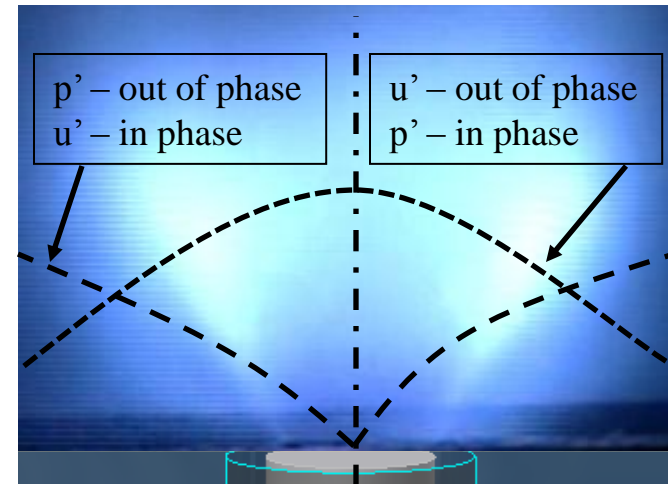
Swirler housing (1-5 swirlers)



Combustor  
drawing

# Transverse Motion in the Combustor

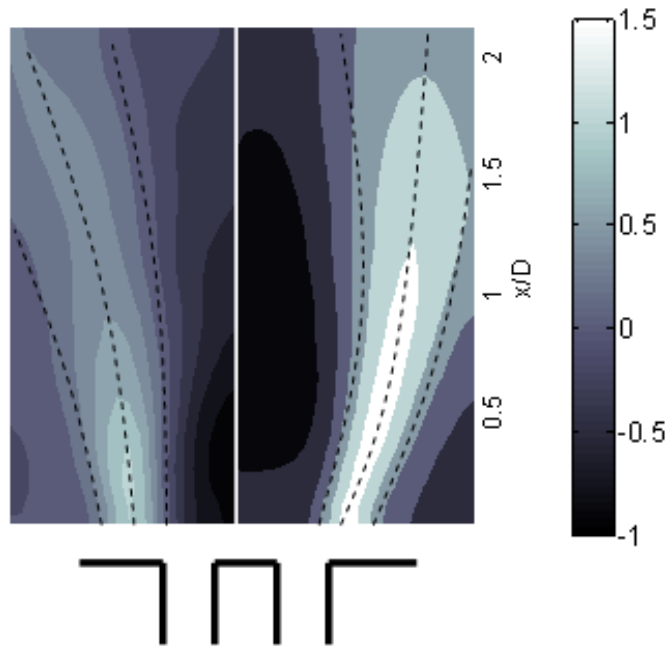
- Phase control
  - $\Phi = 0^\circ$ , approximate pressure maximum, velocity node, at center flame
  - $\Phi = 180^\circ$ , approximate velocity maximum, pressure node, at center flame



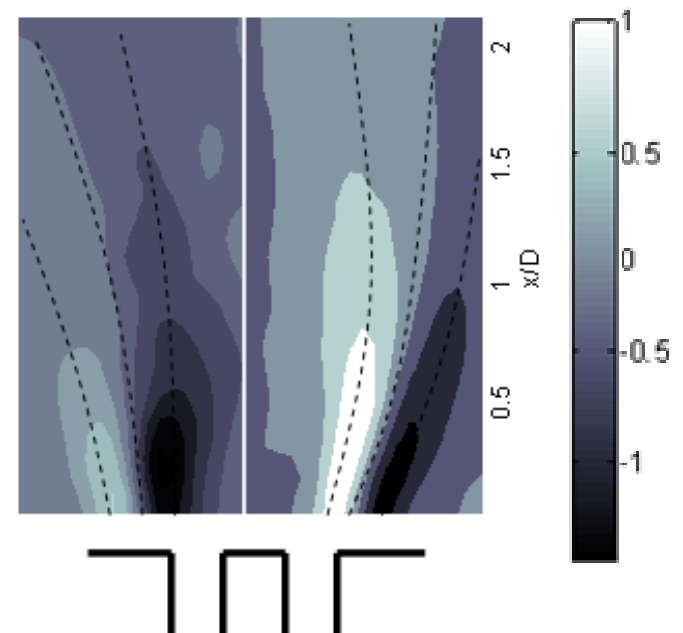
# Time-Average Flow Field

- Experimental conditions:
  - $U_o = 10$  m/s,  $S = 0.85$
  - $\varphi = 0.95$
  - $f_o = 400$  Hz – 1800 Hz

Time-average axial velocity

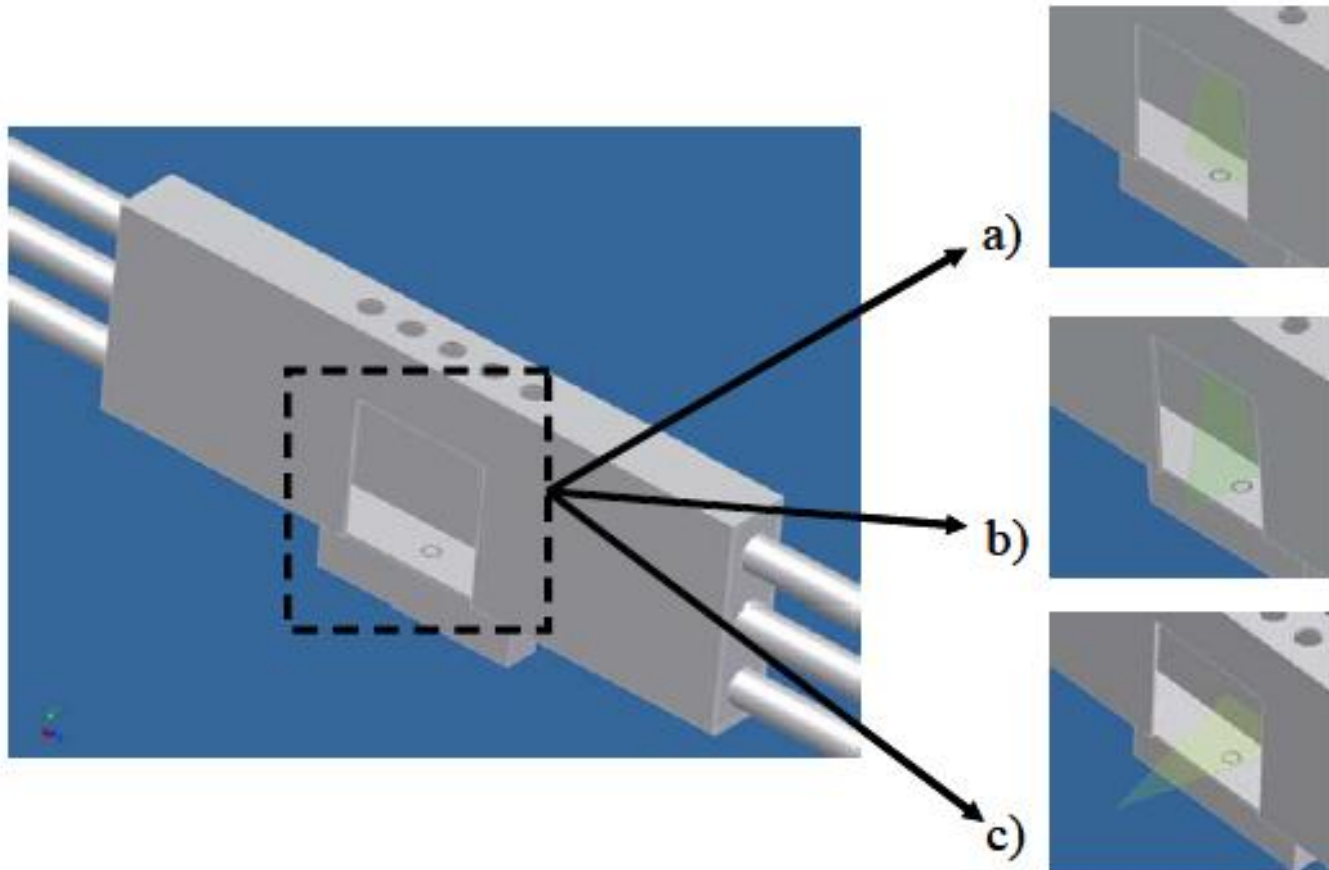


Time-average vorticity



## Swirling Flow Instability

- We can more closely examine the symmetry of the disturbances by looking in the  $r$ - $\vartheta$  plane



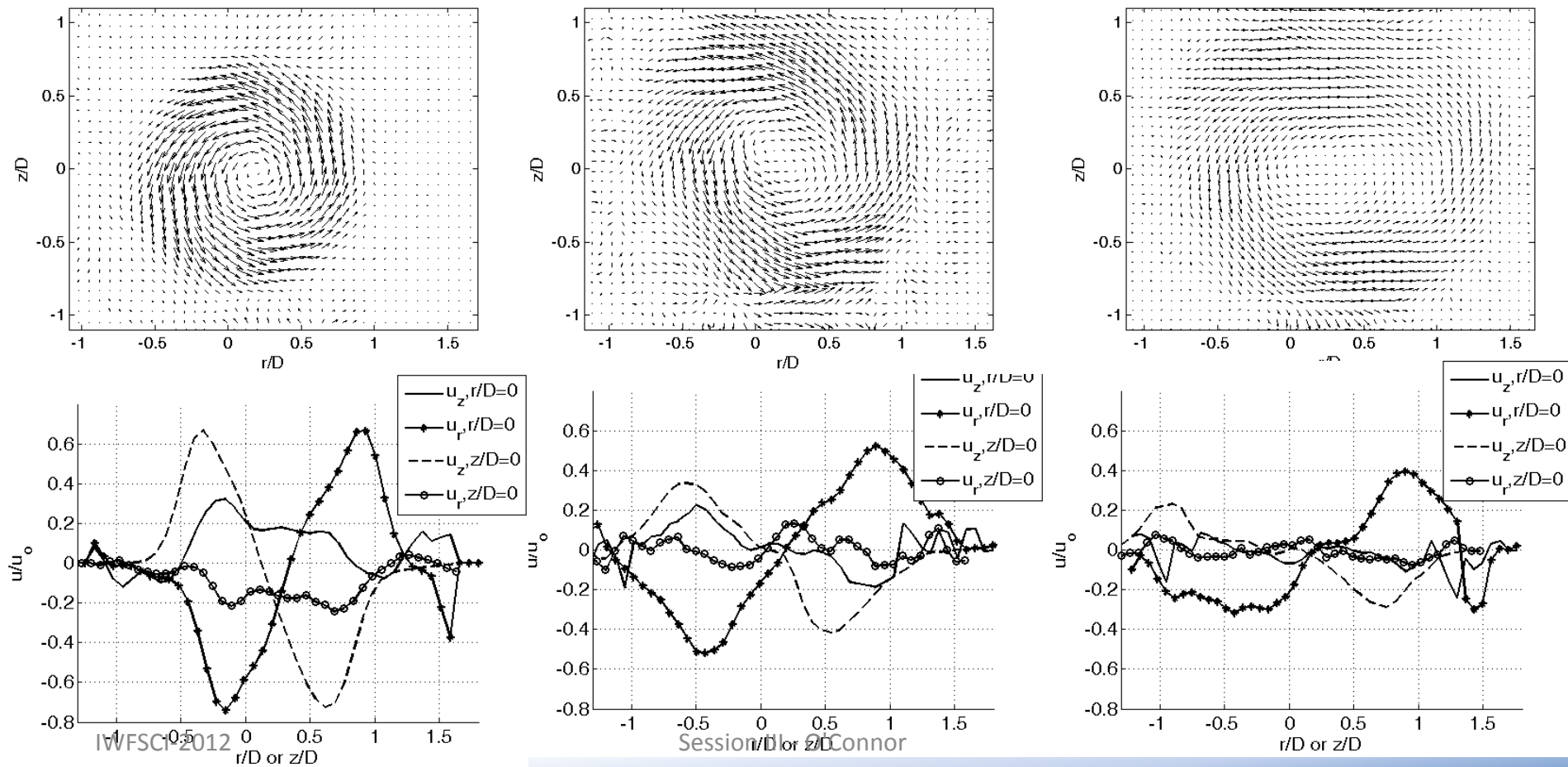
# Swirling Flow Instability

- We can more closely examine the symmetry of the disturbances by looking in the  $r$ - $\vartheta$  plane

$x/D = 0$

$x/D = 1$

$x/D = 2$



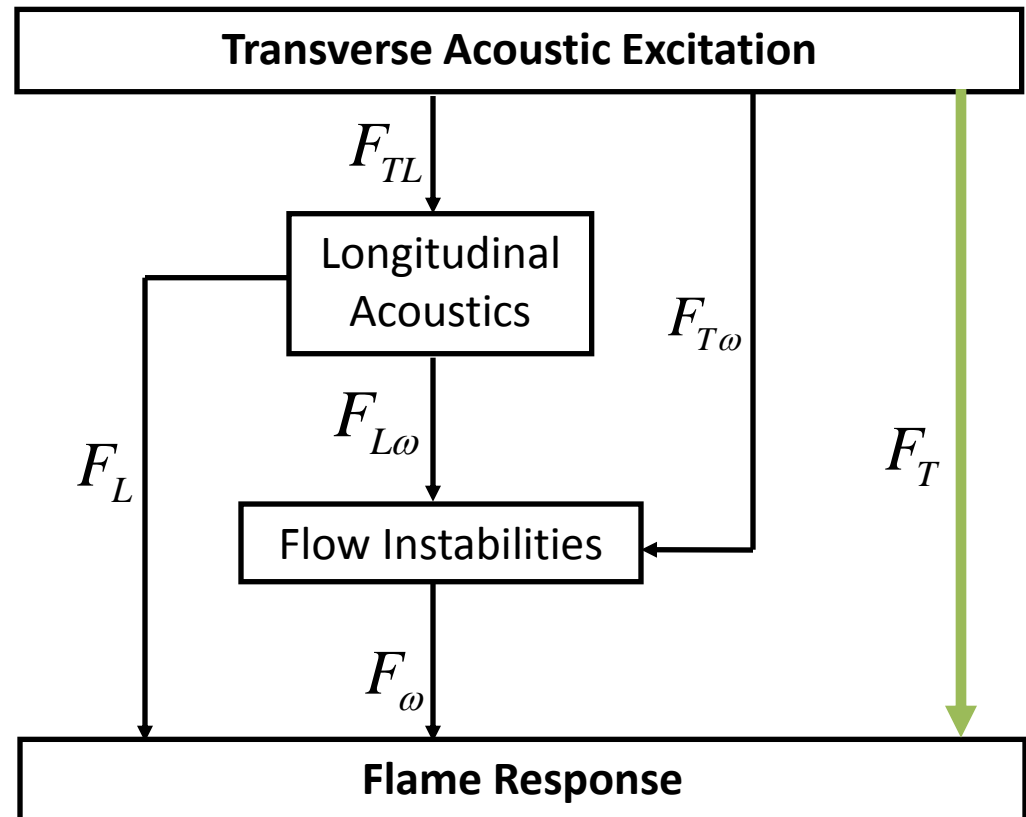


## Velocity-Coupled Transverse Instabilities

QUESTION: What are key physical processes controlling flame response during transverse instabilities?

$$F_T(f) = \frac{q'(f) / \bar{q}}{u'_{T,a}(f) / \bar{u}}$$

- **Minimal effect on flame response at most frequencies of interest**
  - No net mass flow through flame over acoustic cycle

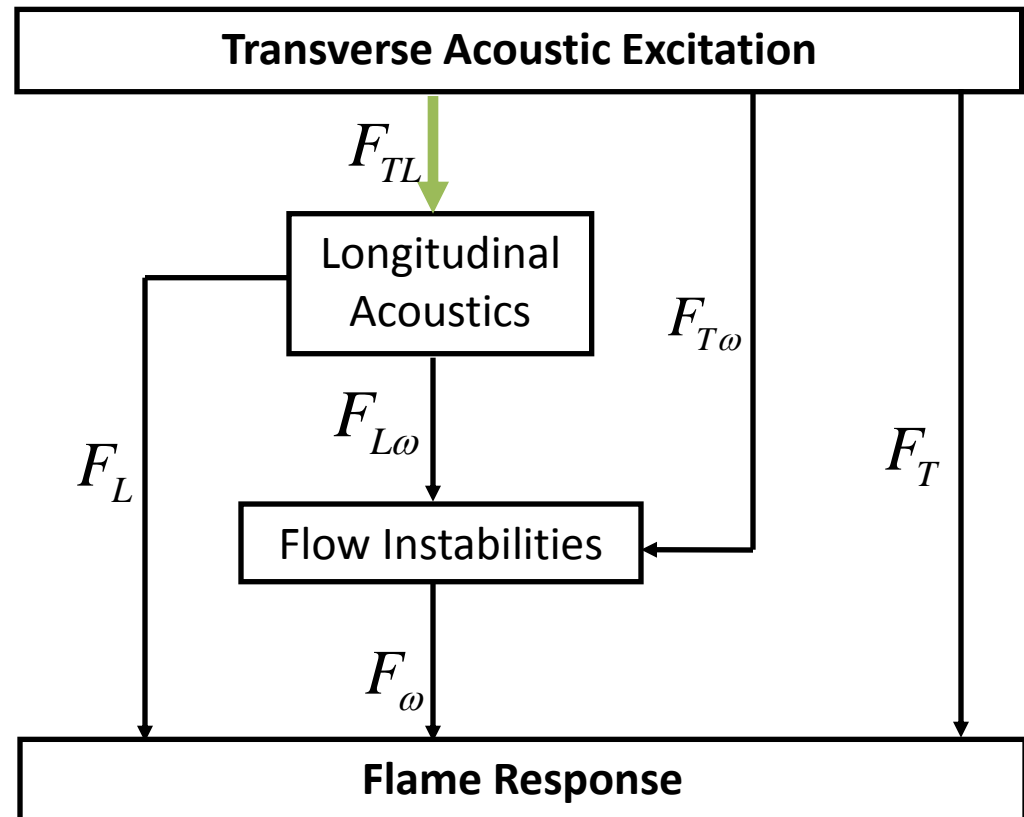


# Velocity-Coupled Transverse Instabilities

QUESTION: What are key physical processes controlling flame response during transverse instabilities?

$$F_{TL}(f) = \frac{u'_{L,a}(f)}{u'_{T,a}(f)}$$

- Describes acoustic coupling between combustor and swirler nozzle cavity
- Key coupling mechanism that determines the relative role of transverse vs. longitudinal motion
  - Suggests proper reference velocity for flame transfer functions

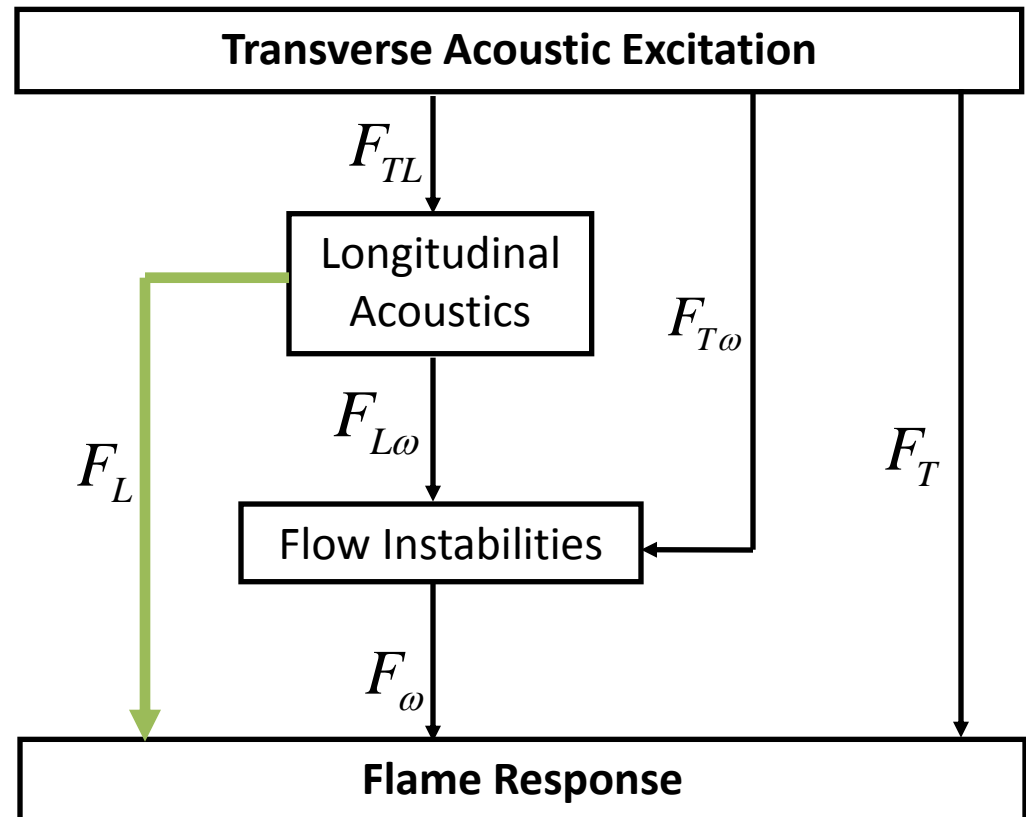


## Velocity-Coupled Transverse Instabilities

QUESTION: What are key physical processes controlling flame response during transverse instabilities?

$$F_L(f) = \frac{q'(f) / \bar{q}}{u'_{L,a}(f) / \bar{u}}$$

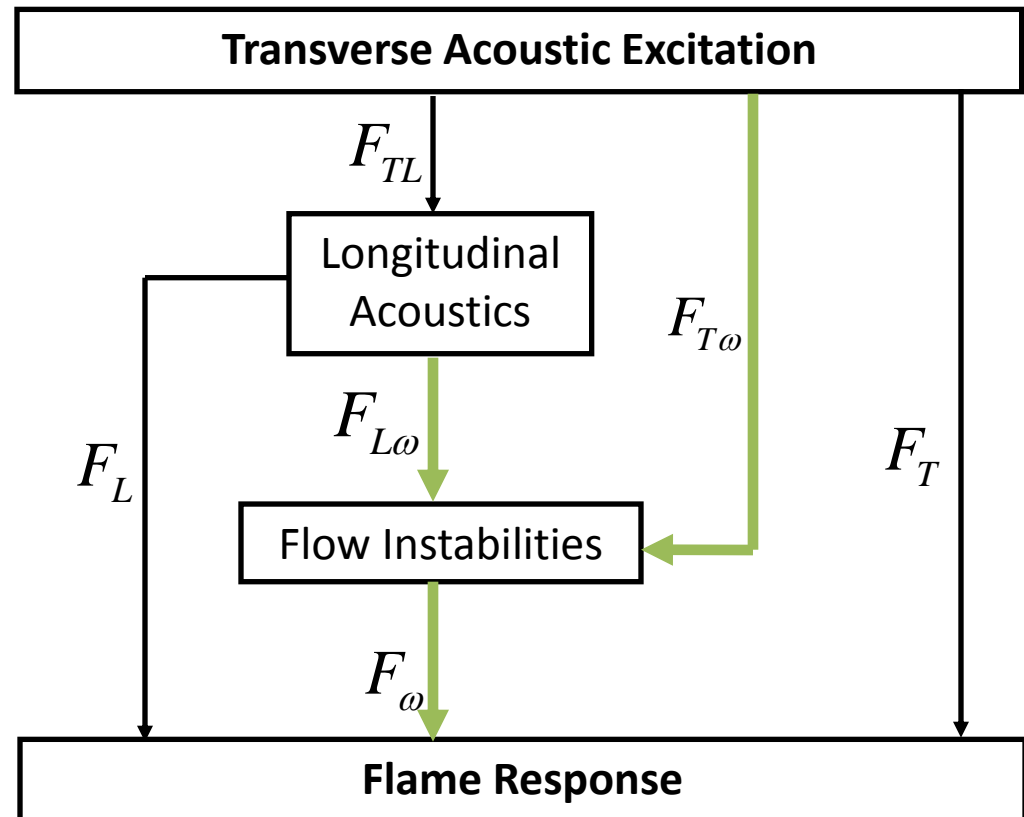
- **Definition of the flame transfer function of a longitudinally forced flame**
- **Important mechanism in  $F_{TL} > 1$  situations**
  - Often greater in magnitude than  $F_T$



## Velocity-Coupled Transverse Instabilities

QUESTION: What are key physical processes controlling flame response during transverse instabilities?

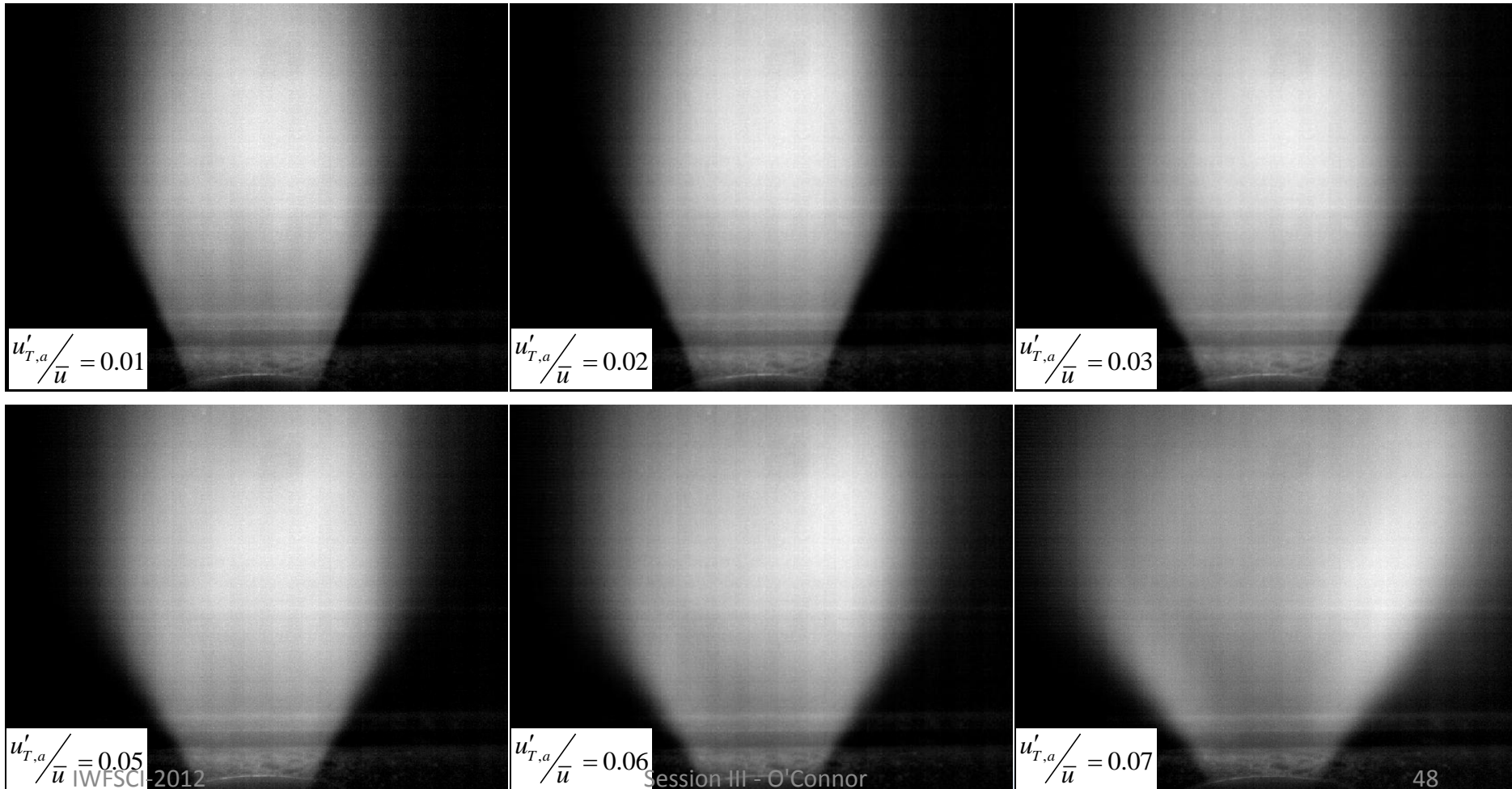
$$F_{L\omega}(f) = \frac{u'_{L,\omega}(f)}{u'_{L,a}(f)}$$
$$F_{T\omega}(f) = \frac{u'_{T,\omega}(f)}{u'_{T,a}(f)}$$
$$F_{\omega}(f) = \frac{q'(f)/\bar{q}}{u'_{\omega}(f)/\bar{u}}$$



## Effect of Forcing on Time-Average Flow

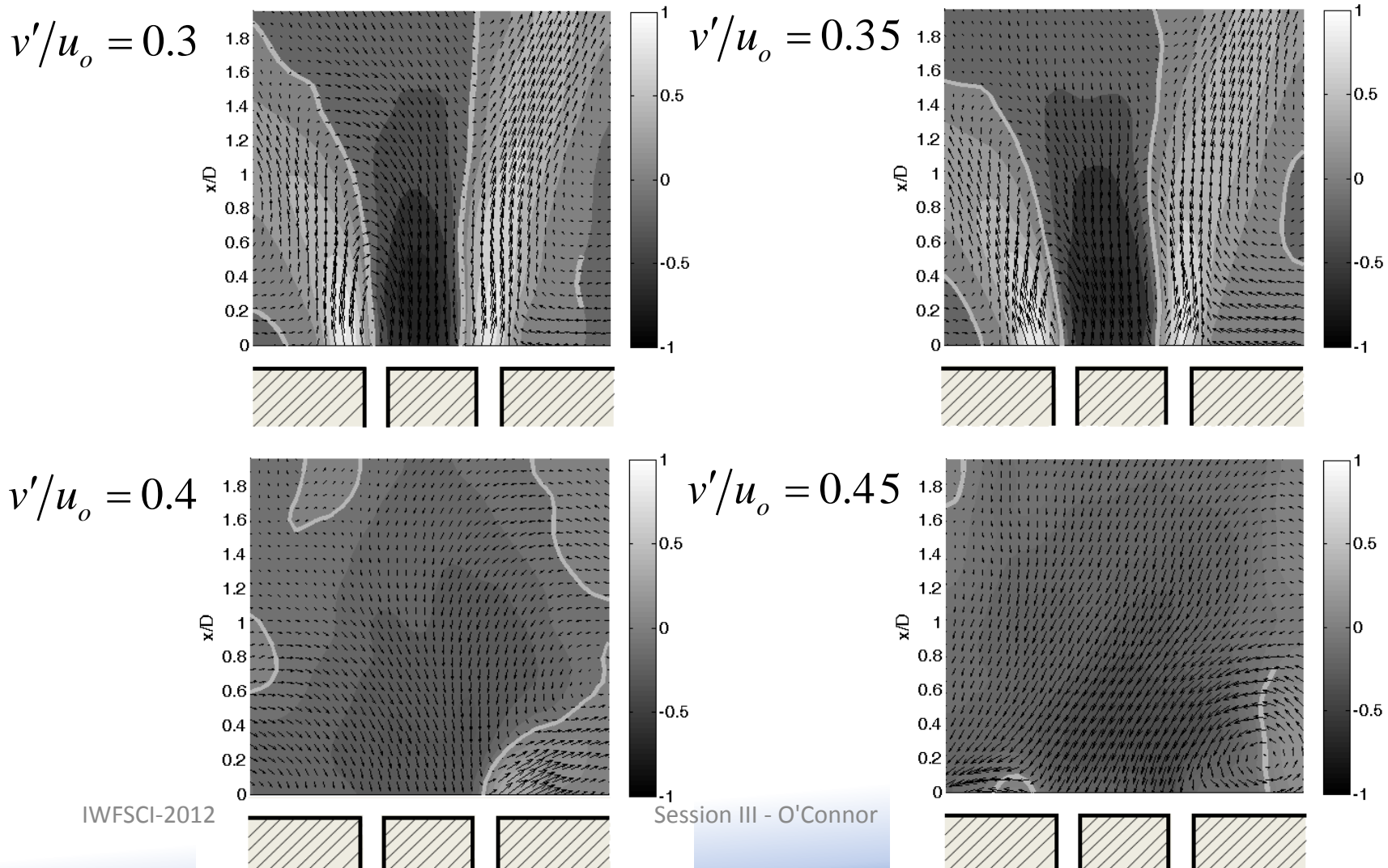
- The progression of the flow field shape as the amplitude of forcing increases is due to changes in the vortex breakdown bubble

1800 Hz in-phase



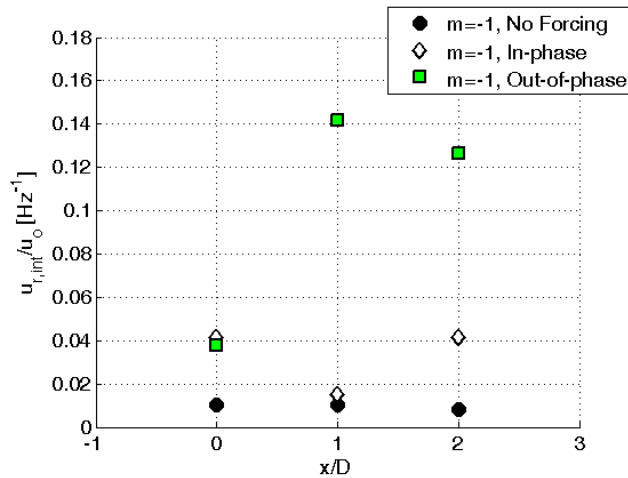
## Effect of Forcing on Time-Average Flow

- This behavior is reflected in changes in the structure of the vortex breakdown bubble at high amplitudes

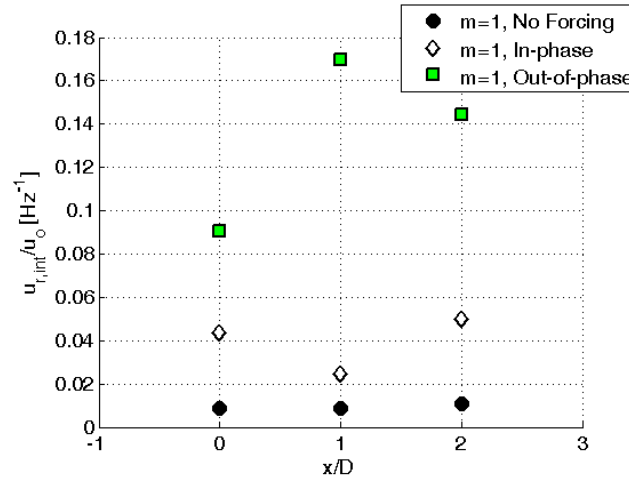


# Flow Field Topology – Downstream Development

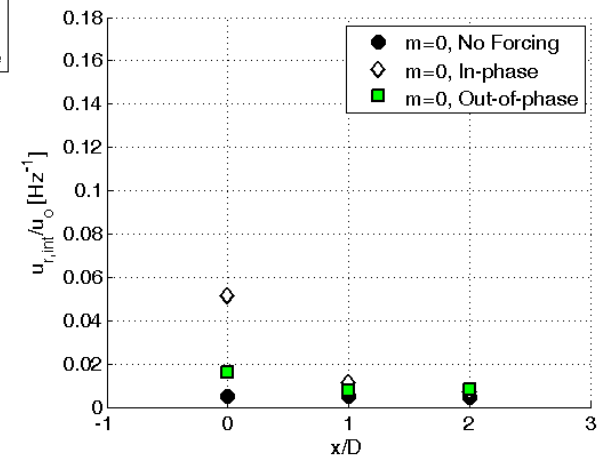
## Mode $m=-1$



## Mode $m=1$



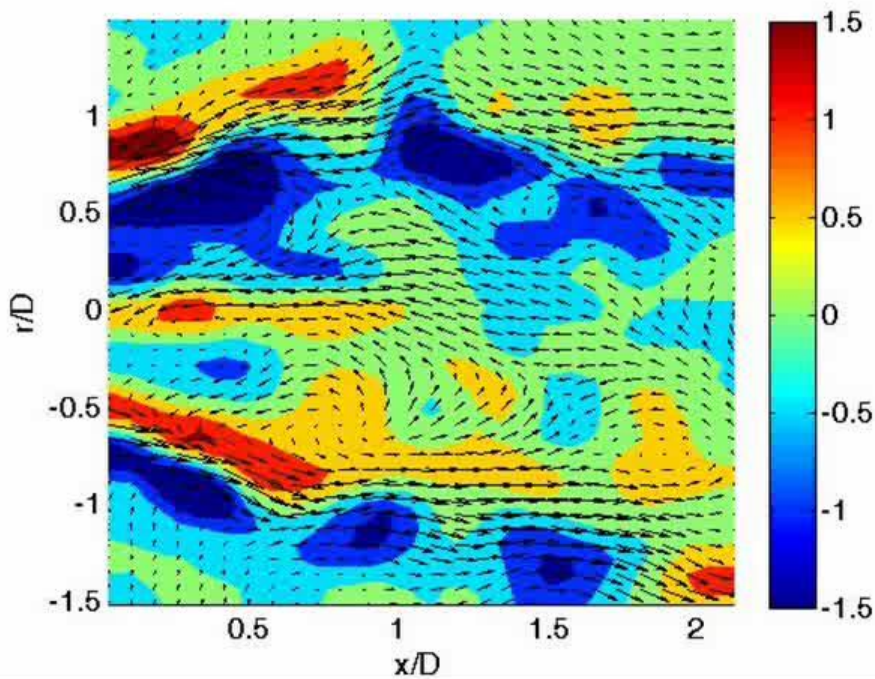
## Mode $m=0$





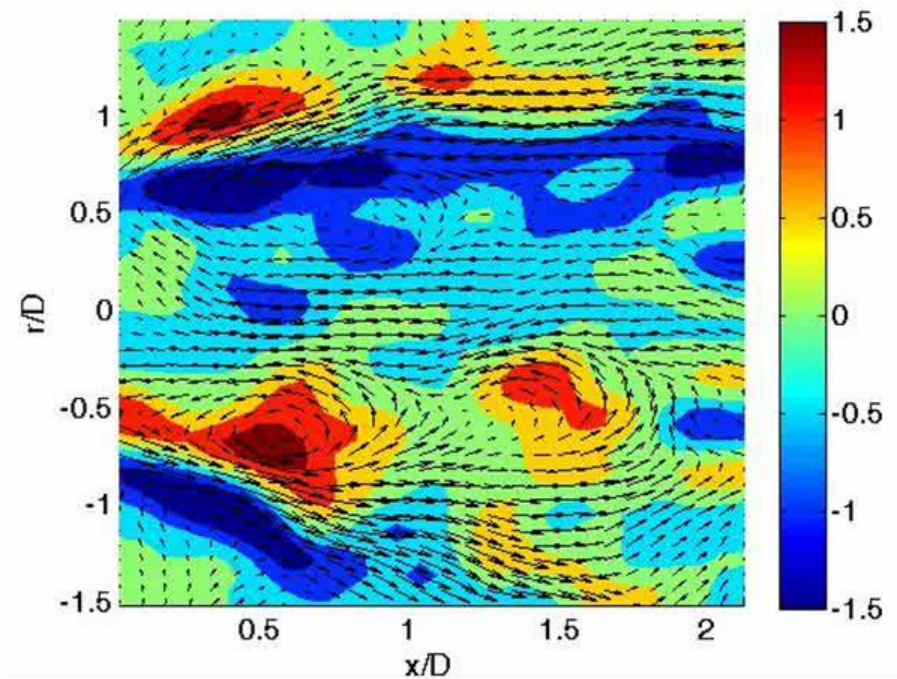
# Flow Field Topology – Instantaneous Velocity

## In-phase Forcing



400 Hz in-phase,  
 $U_o=10$  m/s

## Out-of-phase Forcing



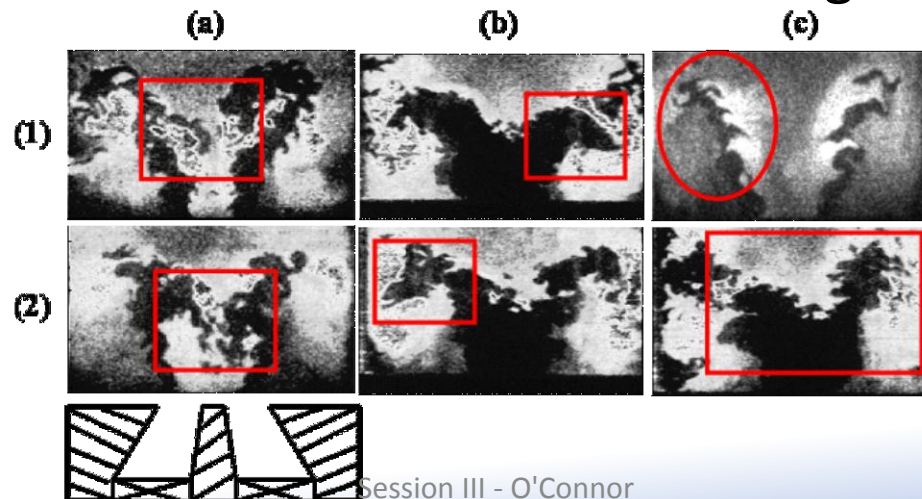
400 Hz out-of-phase,  
 $U_o=10$  m/s

# Swirling Flow Instability and Flame Response

- Flame response in velocity-coupled combustion instabilities is dictated by these two levels of instability
- The “base state” governs the flame shape and, in part, the magnitude of the flame response

$$\frac{\partial G}{\partial t} + (\vec{u} \cdot \vec{n} - S_L) |\nabla G| = 0$$

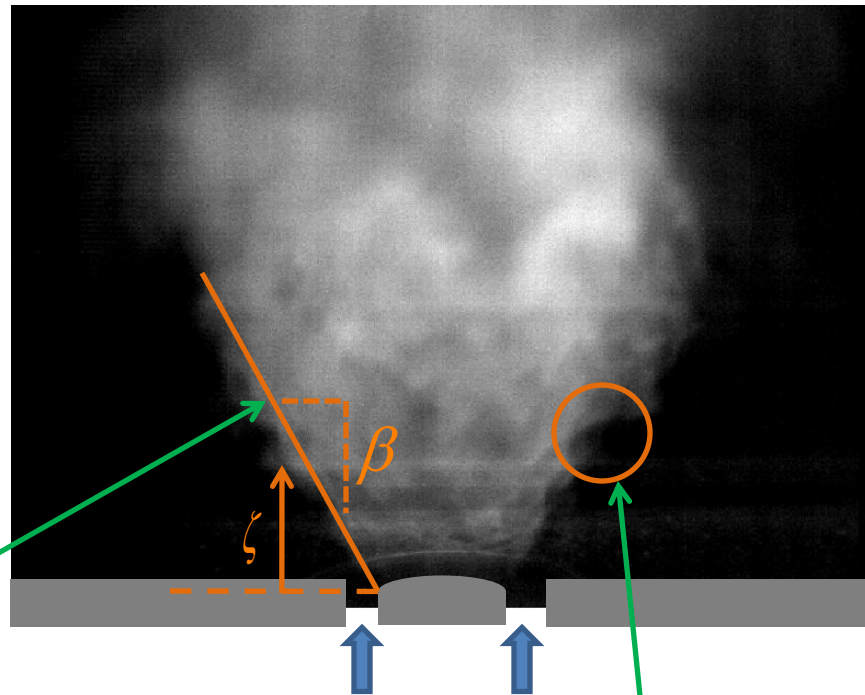
- The shear layer instabilities drive the oscillating heat release



# Swirling Flow Instability and Flame Response

Time-average behavior (base state)

Fluctuating behavior (flame wrinkling)



Swirling air + fuel

$$\bar{u} - \beta \bar{v} \bar{\zeta}_r - S_L(r) \sqrt{1 + \beta \bar{\zeta}_r^2}$$

$$\frac{\partial \zeta'}{\partial t} = u' - \beta \bar{v} \zeta_r' - \beta v' \bar{\zeta}_r - \frac{\beta^2 S_L \bar{\zeta}_r \zeta_r'}{\sqrt{1 + \beta^2 \bar{\zeta}_r^2}}$$

## High-Speed Data Database

- **Velocity data: 462 cases**
  - Non-reacting and reacting
  - $S=0.85$ ,  $S=0.5$
  - $R$ - $x$  and  $R$ - $\vartheta$  views
  - $u_o=10, 15, 20, 40$  m/s
  - $f_f = 400$ - $1800$  Hz, variety of amplitudes, symmetries
- **PLIF data: 38 cases**
  - $S=0.5$ ,  $u_o = 10$  m/s
  - $f_f = 400$ - $1800$  Hz, variety of amplitudes, symmetries
- **Flame luminescence data: 64 cases**
- **Smoke visualization data: 276 cases**
- **Flame transfer function data: 224 cases**