

# Multiple Instance Learning: Application to Seismic Event Detection and Open Problems

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***Unclassified***

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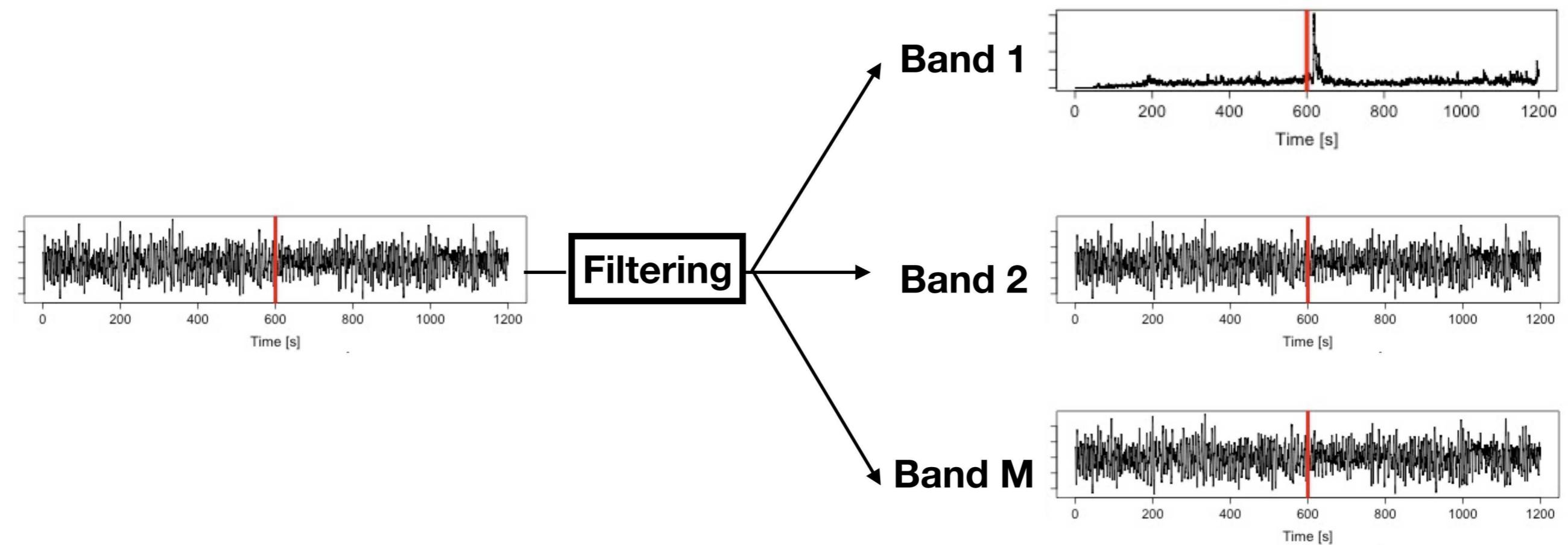
# Background

- There exists a network of 120-odd seismic stations to detect nuclear blasts.
- Called International Monitoring System
- Earthquakes, mine blasts, and nuclear blasts give rise to seismic waves
- These travel through the earth and are detected at the IMS stations.
- Most of the detections are earthquakes, followed by mining blasts. ~100 a day per station.
- Being able to detect these seismic wave arrivals quickly with minimum manual intervention is critical.
- Detecting weak seismic waves / faint arrivals is tough.

# Goal of this work

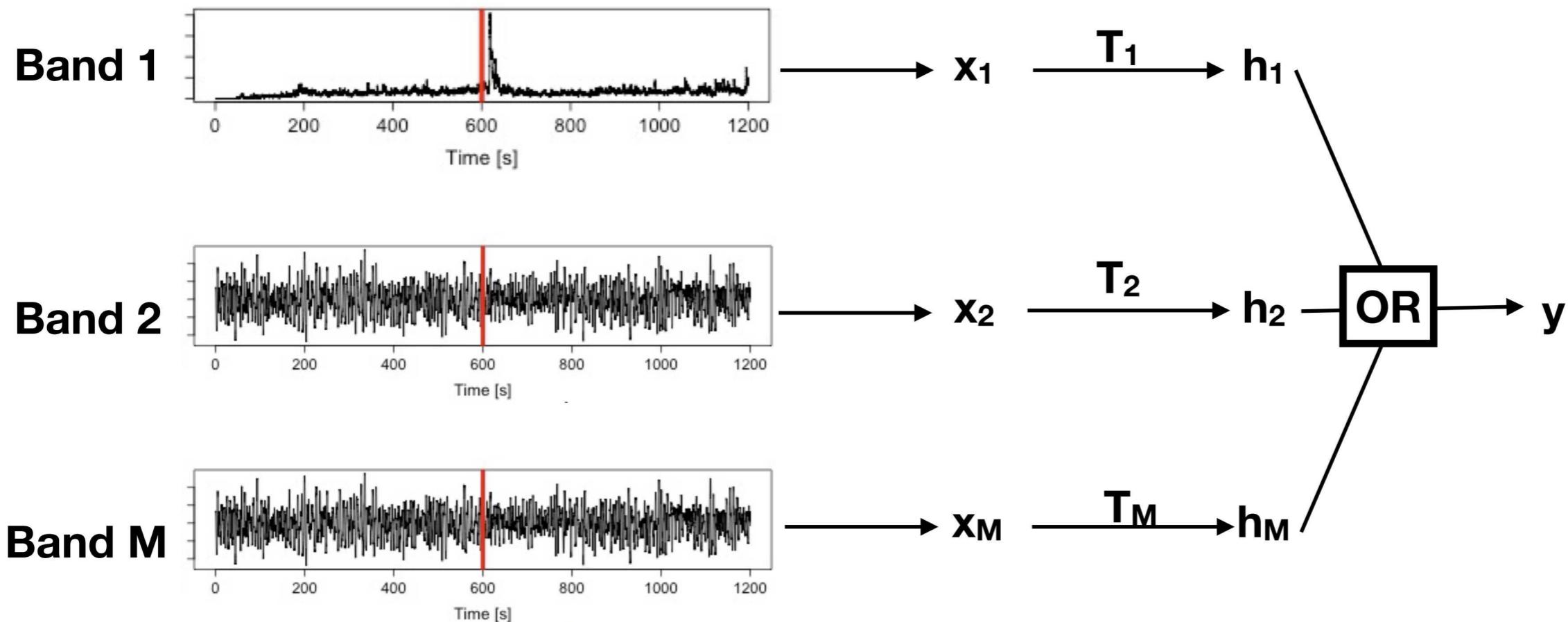
- Seismic waves currently detected using manually chosen rules of thumb.
- Want to replace rules of thumb with classifier learned from data.
- Data has shortcomings that require use of ML method called multiple instance learning.

# This is a time series classification problem



- Need to filter raw signal to the frequency band in which event occurs in order to detect it.

# Detection is currently done without ML using rules of thumb

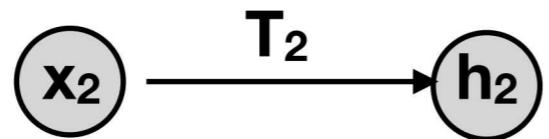
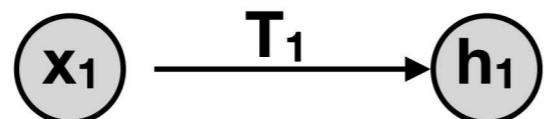


- Rule of thumbs  $T_1 \dots T_M$  currently chosen manually!
- $x_i = (x_{i1}, x_{i2}, \dots, x_{iD})$
- $T_i(x_i) = 1$  if  $x_{i1} > \theta_{i1}$  or  $x_{i2} > \theta_{i2} \dots$  or  $x_{iD} > \theta_{iD}$ .  $M \times D$  thresholds

# There are a lot of features

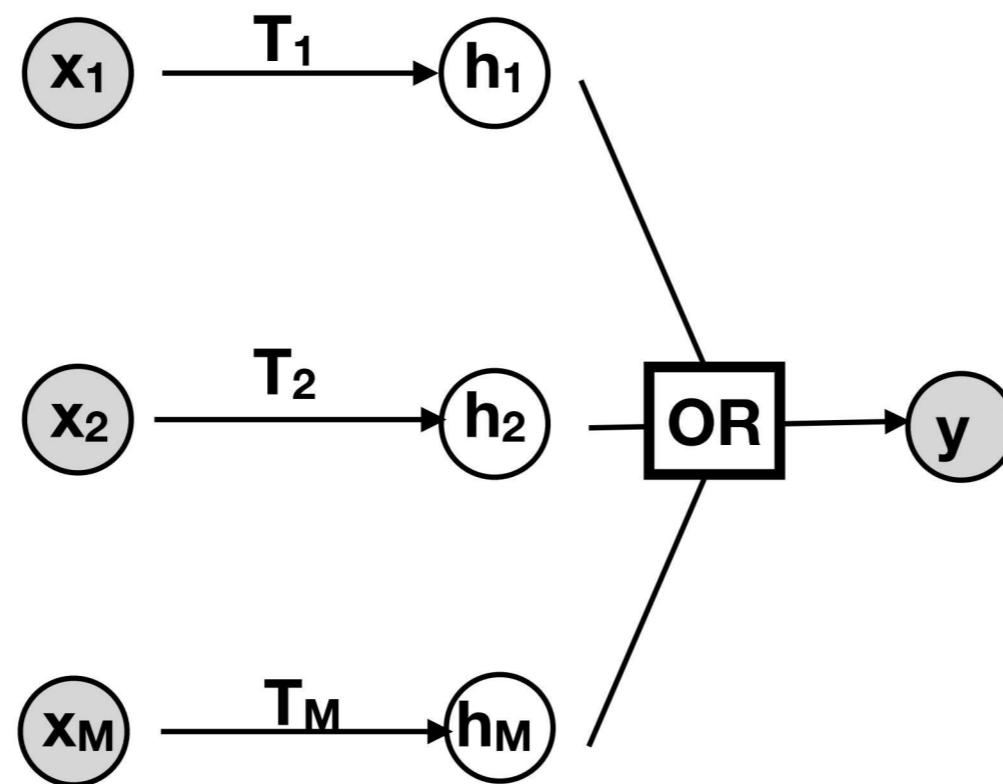
- The filtered signal has 3 channels
- For each channel, apply different transforms (LTA/STA, recursive LTA\_STA), and features are the maximum value of those features in the time series.
- > 6 features
- More if we consider the 95-th percentile of a transform, 50th percentile, etc.
- This leads to a high false positive rate.

# How to learn rule of thumbs in ideal scenario?



- Fit  $T_i()$  using many samples of  $(x_i, h_i)$ . Easy.

# But we have a data problem



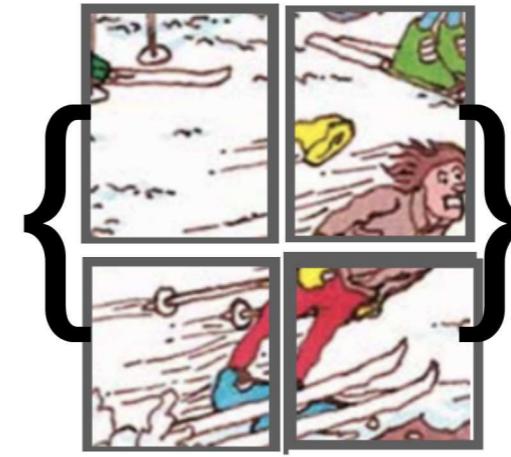
- No one bothered recording the frequency band in which past events occurred.
- Can't impute  $h_i$ . Events occur in different frequency bands.
- Need Multiple Instance Learning

# What is the Multiple Instance Learning Scenario?

- Training Data is Weakly Labelled
- Consists of bags of instances
- Unobserved: instance labels
- Observed: whether each bag has some positive instance



Contains a Waldo instance



Has no Waldo instance

# What are the goals in MIL?

- Learn instance classifier

Is  a Waldo instance?

- Learn bag classifier

Does  have a Waldo instance?

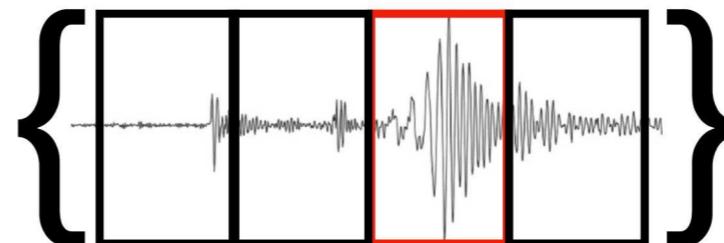
- Do both: **interpretability**

Does  have a Waldo instance?

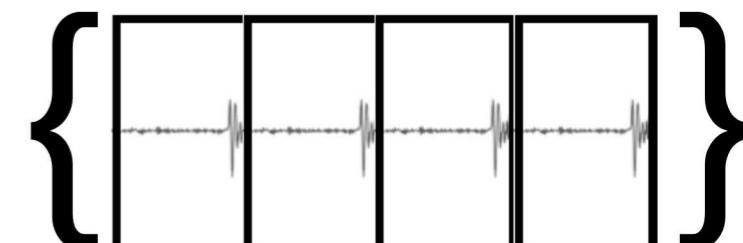
If yes, where is Waldo?

# SPAN Application: Seismic Event Detection

- Training data:

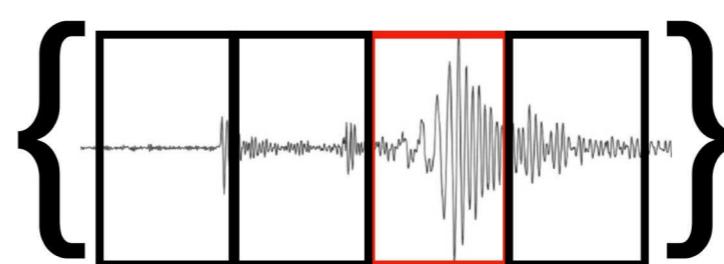


Contains frequency  
with event



Contains no frequency  
with event

- Goal:

Does   
contain frequency w/ event?

If yes, which frequency is the event?

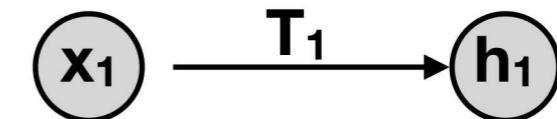
- Knowing frequency band would inform the event type

# How to model the ideal scenario?

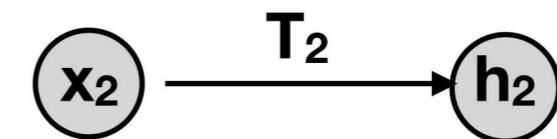
- Use probabilistic

model

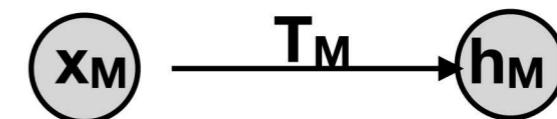
- Variables for each bag:



- Instance feature vectors  $x_1..x_M$



- instance labels  $h_1..h_M$  (0/1)



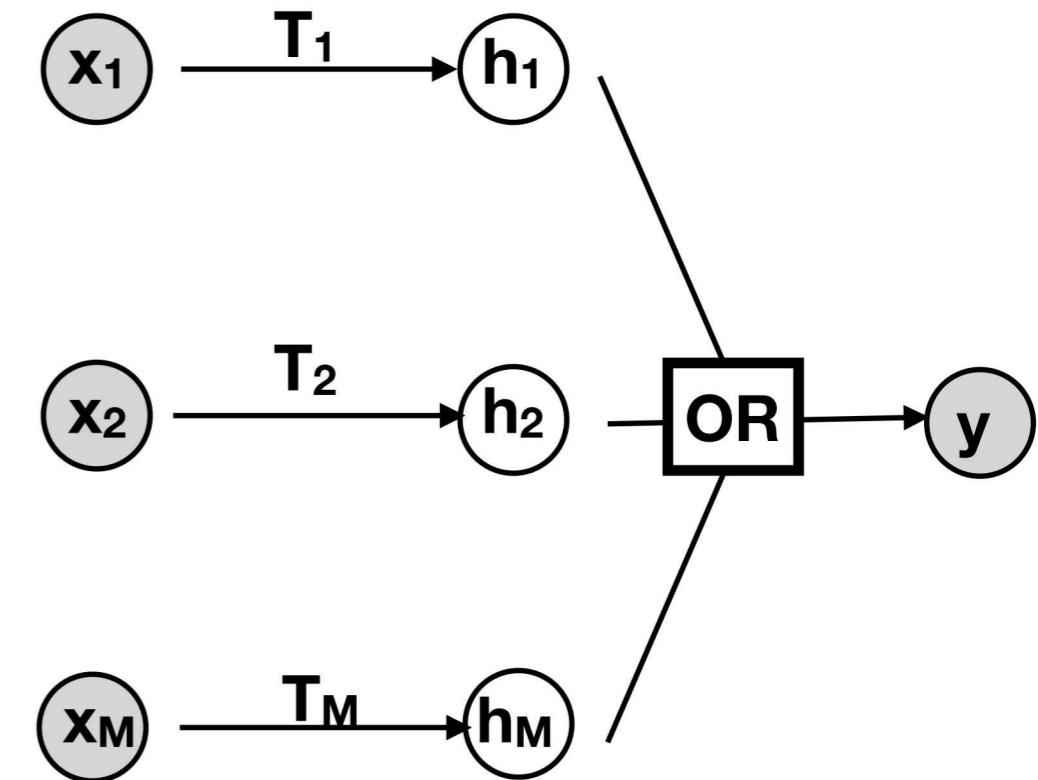
- Learn probabilistic rule of thumb:  $T_i(x_i) = P(h_i=1|x_i)$

# How to do multiple instance learning?

- Use probabilistic **latent** variable model

- Variables for each bag:

- Bag label  $y$  (0/1)
- Instance feature vectors  $x_1..x_M$
- **Latent** instance labels  $h_1..h_M$  (0/1)



- Multiple instance assumption:  $y = 1$  if some  $h_i = 1$
- Learn probabilistic rule of thumb:  $T_i(x_i) = P(h_i=1|x_i)$

# Options for rules of thumb

- Logistic regression “MI-Logreg”
  - $P(h_i=1|x_i; B_i) = \text{sigmoid}(B_i^T x_i)$
- Threshold function (similar to heuristic) “MI-Thresh”
  - $P(h_i=1|x_i; \theta_i) = 1 \text{ if } x_{i1} > \theta_{i1} \text{ or } x_{i2} > \theta_{i2} \dots \text{ or } x_{iD} > \theta_{iD}.$

# Data Preparation

- Available data: raw signal from seismometers and timestamps of known seismic events
- To generate bags: ~ raw signal divided into 20 minute windows. Windows that contain a known seismic event are positive bags.
- To generate instances: each 20 minute raw signal (bag) decomposed into contributions from  $M$  non-overlapping frequency bands to obtain  $M$  instances per bag.

# Experiment #1: Overview

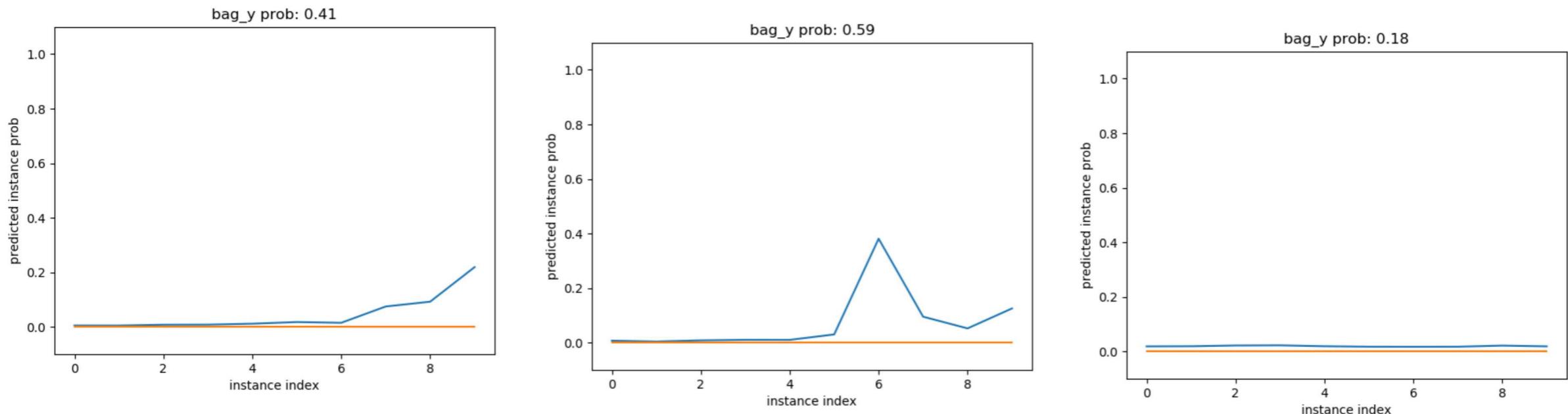
- Goal: Compare AUC's of MI-Logreg and vanilla classifiers
- Vanilla classifiers directly classify a bag by representing it as the concatenation of the feature vectors of the instances the bag contains
- Features: for each channel, (100, 95)-th percentiles of Ita/sta, 100-th percentile of sta
- Frequency bands: 10 bands spanning 0-5 hz.

# Experiment #1: Results

	AUC
MI-Logreg	.77(.01)
Logreg	.71(.01)
RF	.77(.01)

- Logreg and RF (random forest) are vanilla bag classifiers
- No instance labels, so all metrics are bag-level.
- MI-Logreg higher AUC than Logreg (better model, less parameters)
- RF higher AUC than Logreg.

# Experiment #1: Multi-instance learning is interpretable by design



Instances ordered by frequency on x-axis.

Blue line indicates probability a frequency contains event  $P(h_i=1|x_i)$

Orange line is 0/1 prediction of  $h_i$

# Experiment #2: Overview

- Goal: How does learning thresholds in threshold instance classifier improve performance compared to not learning them?
- Features: for “merged” channel, 100-th percentile of Ita/sta, 100-th percentile of recursive Ita/sta
- Frequency bands: 2 bands spanning 0-4 hz.
- Custom loss to minimize:  $FNR^2 + FPR^2 + (FNR - FPR)^2$ 
  - Want roughly equal FPR and FNR

# Experiment #2: Results

	FNR	FPR
MI-thresh	27.5%	20%
Naive	43%	4%

- “Naive” method: set  $\theta_{ij}$  equal to the 95-th percentile of  $x_{ij}$  in negative bags (raw time series without event).
- “Naive” method does not balance FPR and FNR.

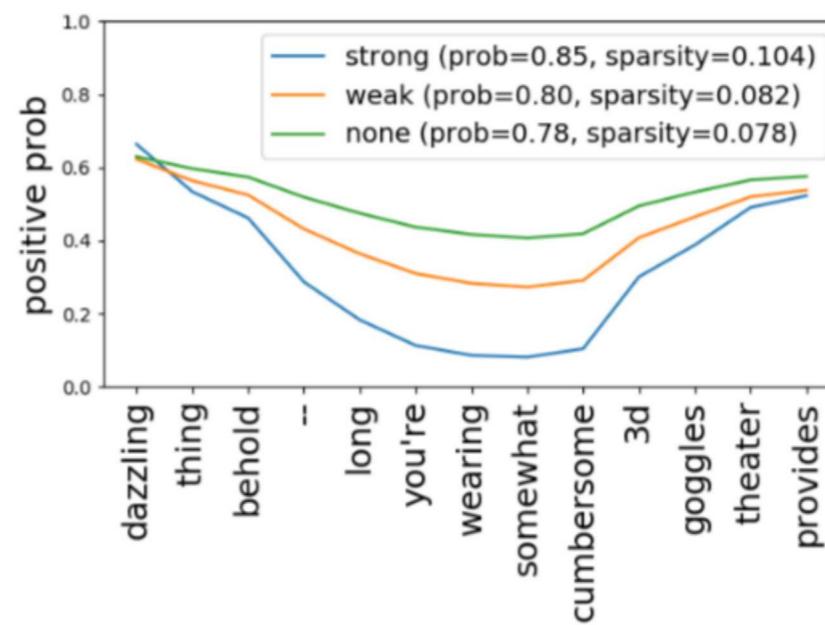
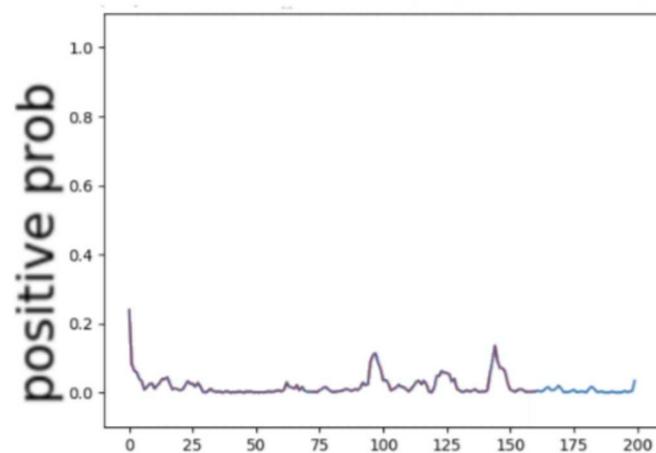
# Experiment #2: Results

	FNR	FPR
LTA/STA, 0-2 hz	35%	9%
LTA/STA, 2-4 hz	53%	7%
Recursive LTA/STA, 0-2 hz	33.5%	13%
Recursive LTA/STA, 2-4 hz	53%	8%
MI-Thresh	27%	20%

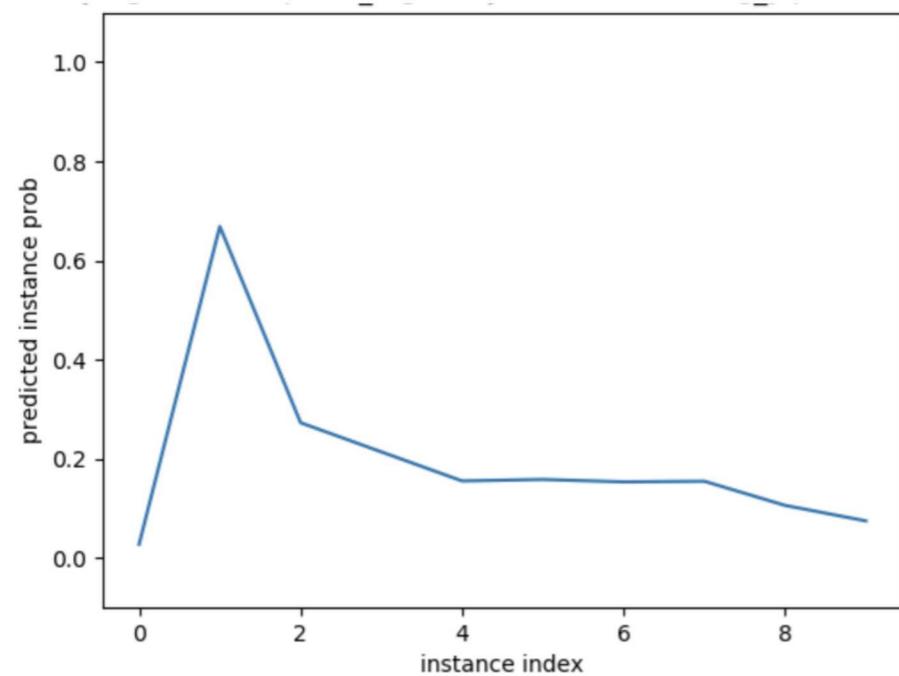
- Trained “MI-Thresh” classifier can be interpreted as “fusing”  $M \times D$  separate single-feature classifiers.
- How would those  $M \times D$  single-feature classifiers perform?

# Challenge: Handling other kinds of data types

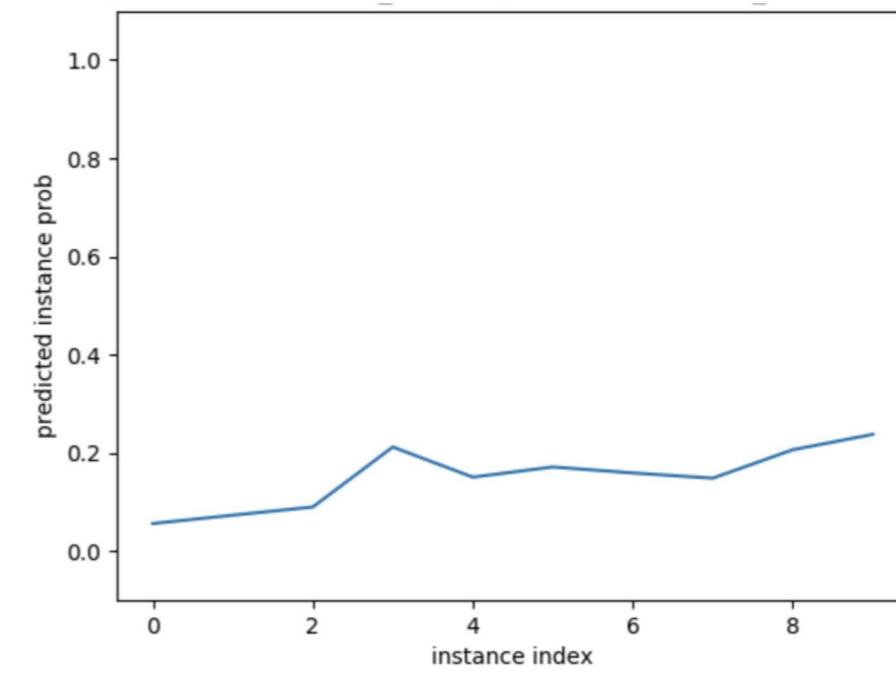
- Nonproliferation data includes structured data.
- Solution: model  $P(h_1..h_M | x_1..x_M)$  jointly with a conditional random field instead of  $P(h_i=1|x_i)$  independently using logistic regression



# Challenge: instance predictions not always interpretable



Interpretable



Not Interpretable

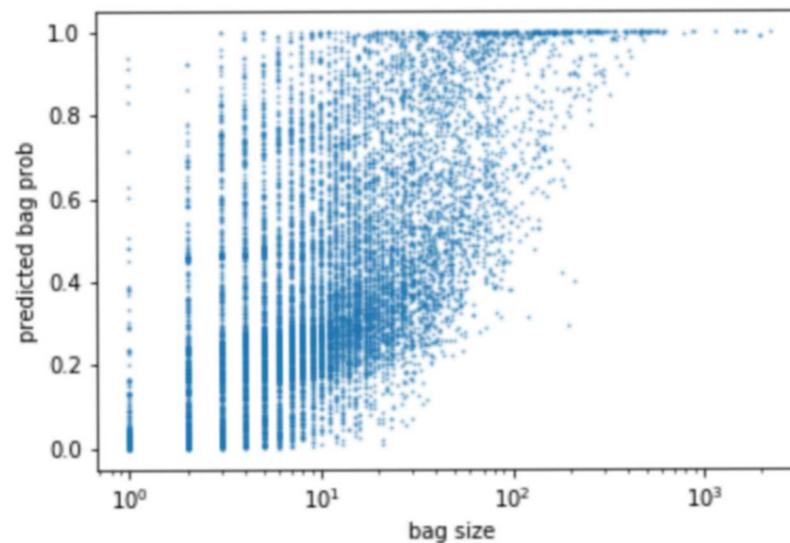
- Solution: encourage instance prediction to be high for a small number of instances via a regularizer

# Challenge: accounting for uncertainty

- Weak labels leave room for ambiguity, so that many models (and instance predictions) are plausible.
- Solution: need Bayesian multiple instance models. Currently developing Gaussian Process model which in addition to providing uncertainty estimates, models dependencies between instance labels.

# Challenge: bag size variability

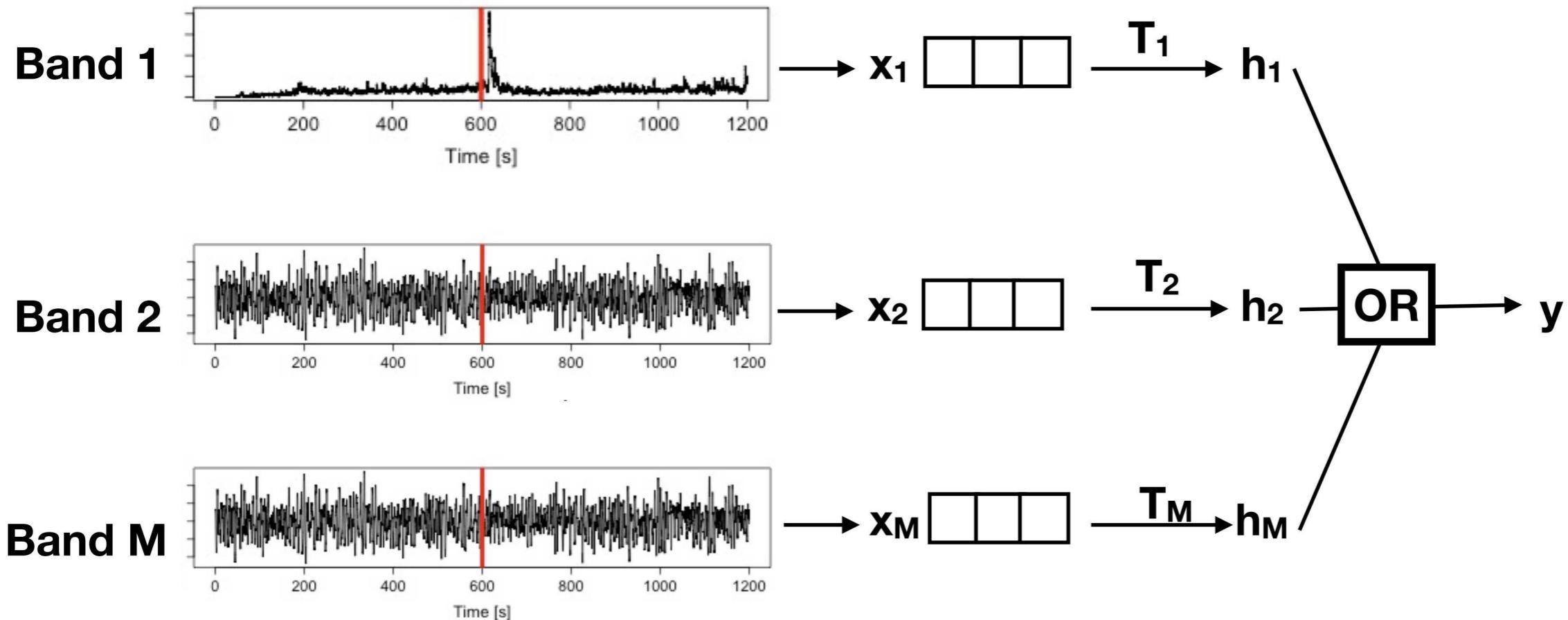
- You do not get to control the size of bags. There is variability in sentence length, width of time windows in which you know an event occurred.



# Conclusion

- Multiple instance learning can be used to predict the frequency in which seismic events occur despite the training data not containing such information.
- Event detection performance on par with less interpretable random forest
- Multiple instance learning can be useful in many other SPAN applications, with many open challenges.

# Detection is currently done without ML using rules of thumb



- Rule of thumbs  $T_1 \dots T_M$  currently chosen manually!
- $T_i(\boxed{x_{i1} \mid x_{i2} \mid x_{iD}}) = 1$  if  $x_{i1} > \theta_{i1}$  or  $x_{i2} > \theta_{i2} \dots$  or  $x_{iD} > \theta_{iD}$
- $M \times D$  different thresholds to choose manually.

# Ideal SPAN Scenario is not possible

- Observed: instance labels



- Not possible - only observe event timestamps. Need multiple instance learning.

# How to do model the ideal scenario?

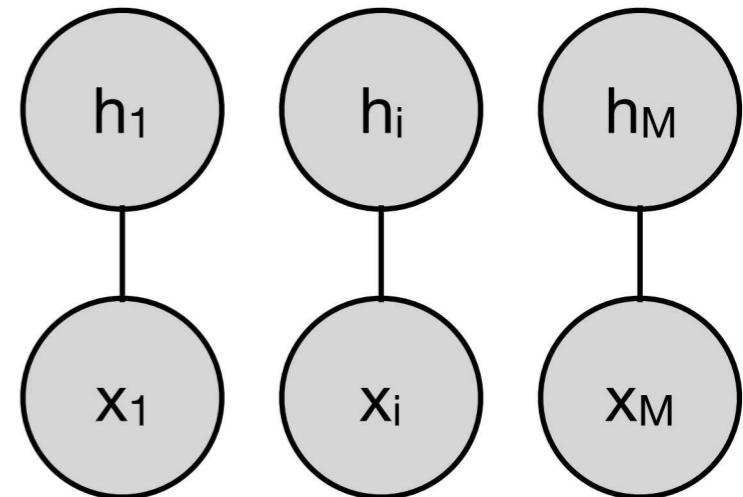
- Use probabilistic model

- Variables for each bag:

- Instance feature vectors  $x_1..x_M$
- instance labels  $h_1..h_M$  (0/1)

- Have probabilistic rule of thumb:

- $T_i(x_i) = P(h_i=1|x_i)$

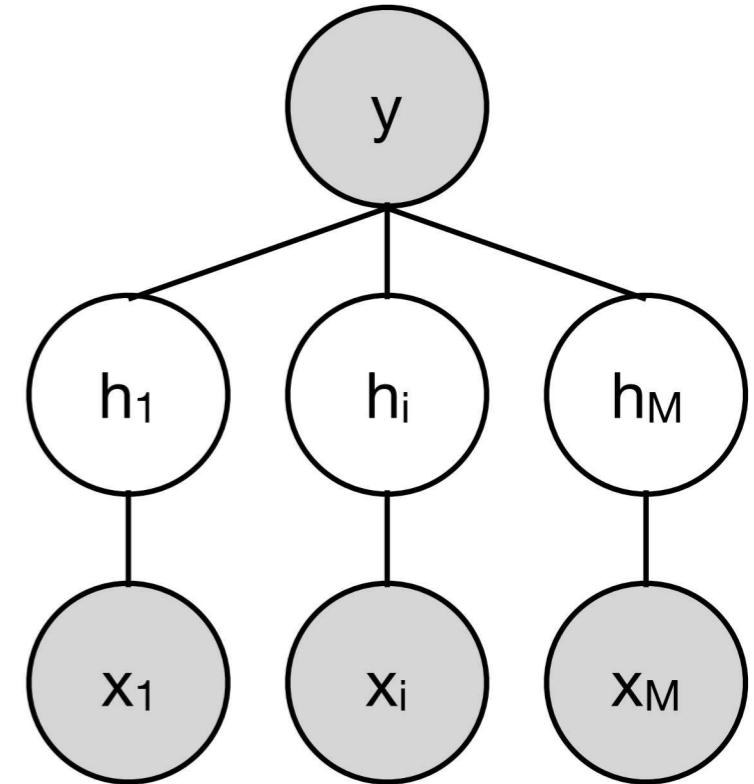


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- Have probabilistic rule of thumb:

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