

# 4D particle tracking using space-time interlaced tomography and apparent mass loss due to image blur



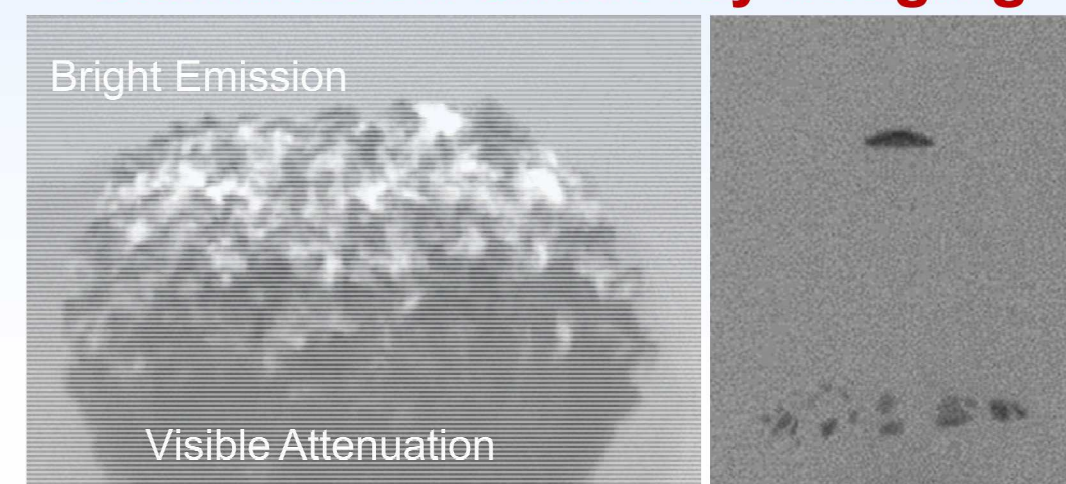
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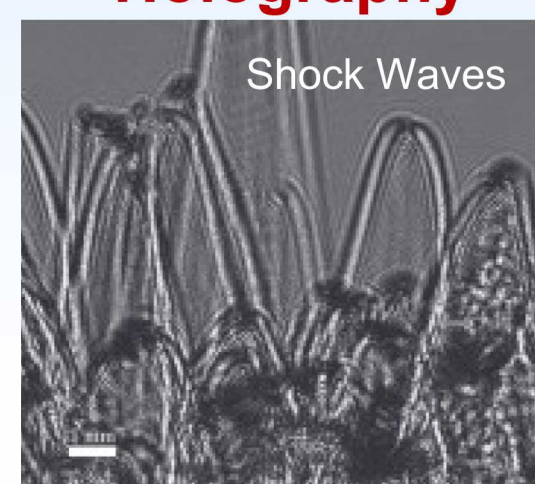
## High-Speed, Polychromatic, Multi-Dimensional X-ray Imaging

High-speed x-ray radiography and tomography were used to track particles and quantify their mass during impulsively driven events. Because attenuation is the dominant interaction between x-rays and matter, refraction and multiple photon scattering events can be neglected. The resulting images are a function of the material properties and the x-ray spectrum. The main sources of uncertainty are the instrument function, out-of-plane motion (for radiography), and image blur, image parallax and the number of sources.

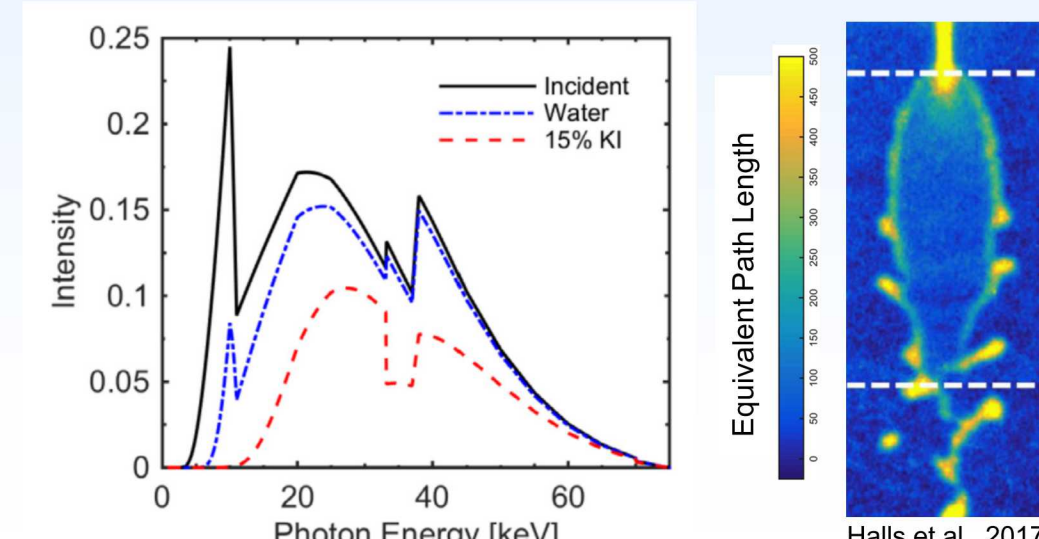
### Simultaneous Diffuse Back-Illumination and X-ray Imaging



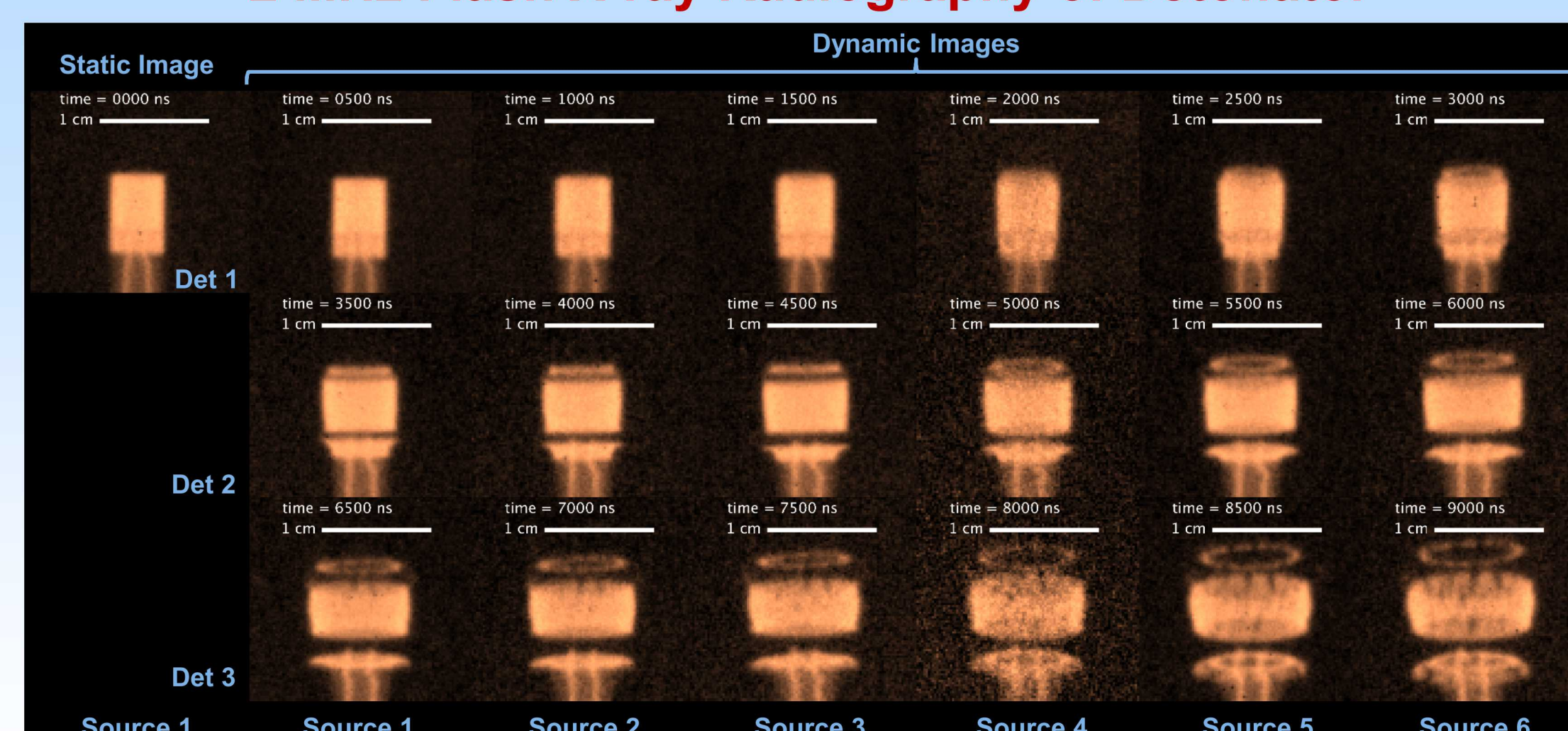
### Digital Inline Holography



### Quantitative Mass Distribution

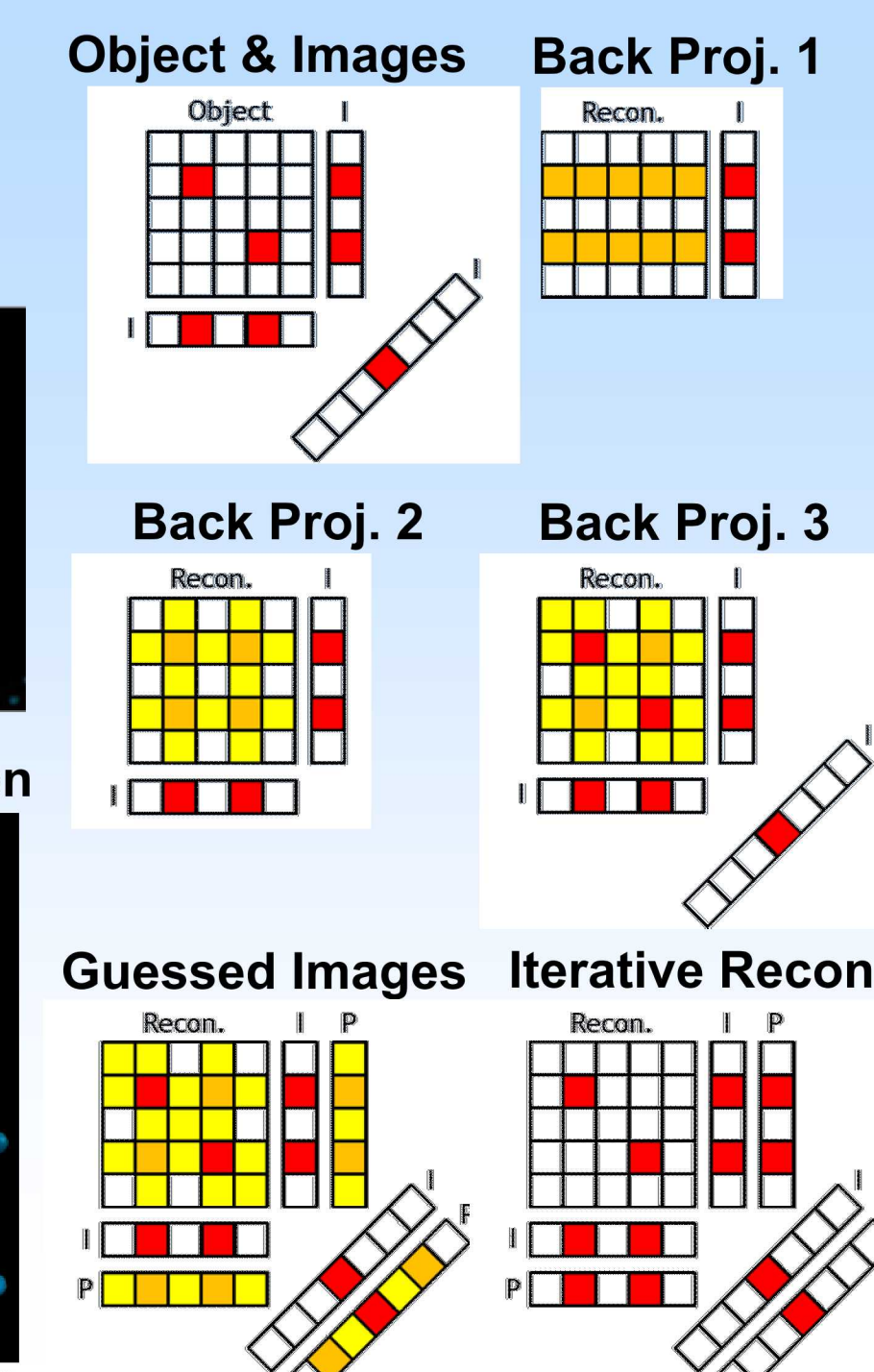
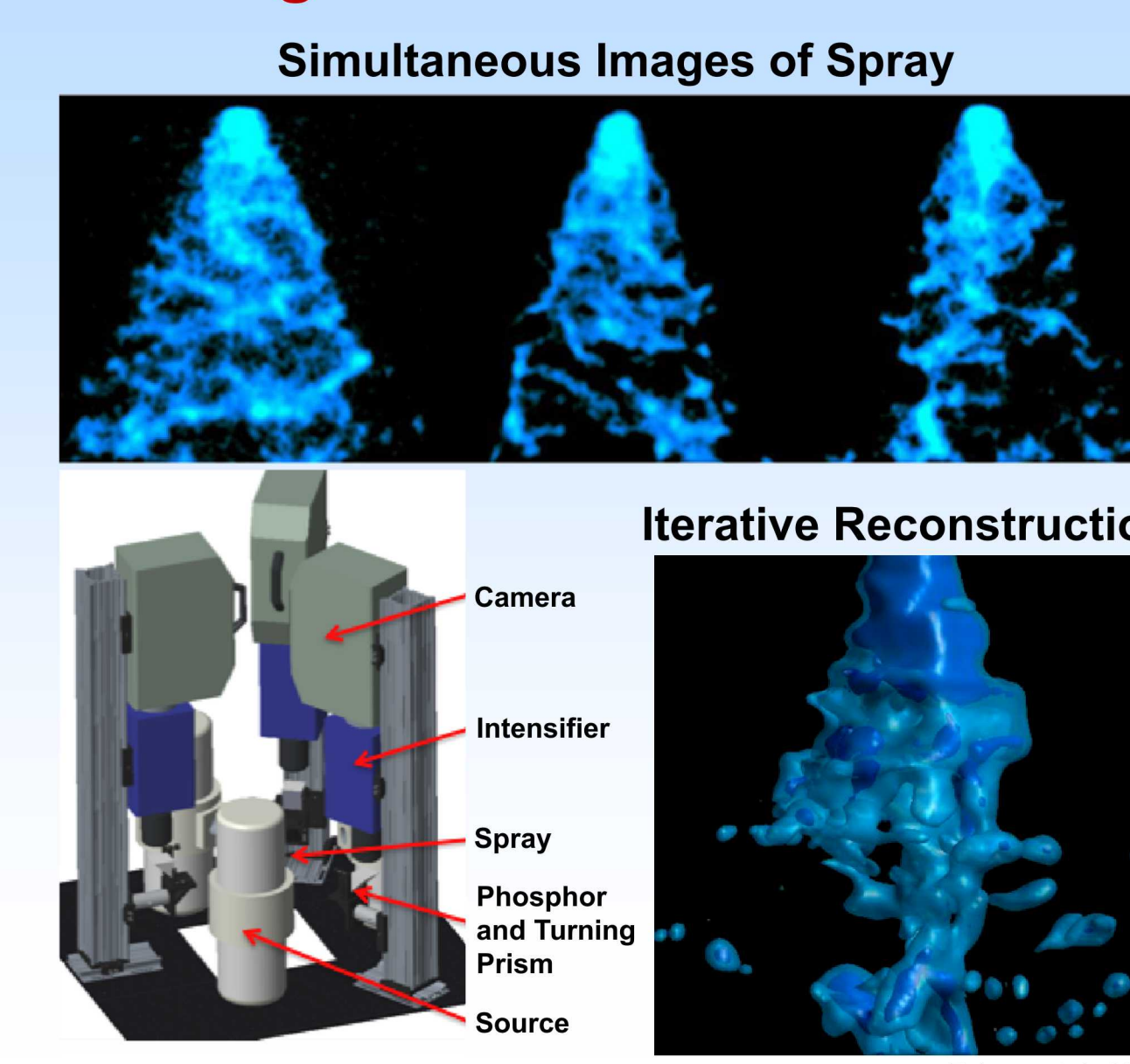


### 2 MHz Flash X-ray Radiography of Detonator



Images were phase matched over 3 detonators using six sources in each shot. Images from 7500 ns to 9000 ns display effect of image parallax, the detonator appears to rotate.

### 10 kHz X-ray Tomography using Iterative Reconstruction



## Space-Time Interlaced Tomography

Particles were tracked in three dimensions using space-time interlaced tomography. When a limited number of frames are available and linear trajectories are assumed, the three-dimensional particle locations can be determined by fitting a unique line to the possible particle locations. These particle locations are determined by interlacing the temporal and angular information of the scene.

### Image parallax becomes a benefit

#### Flexible imaging systems

#### 150 kVp x-ray sources

#### Spatial resolution of volume

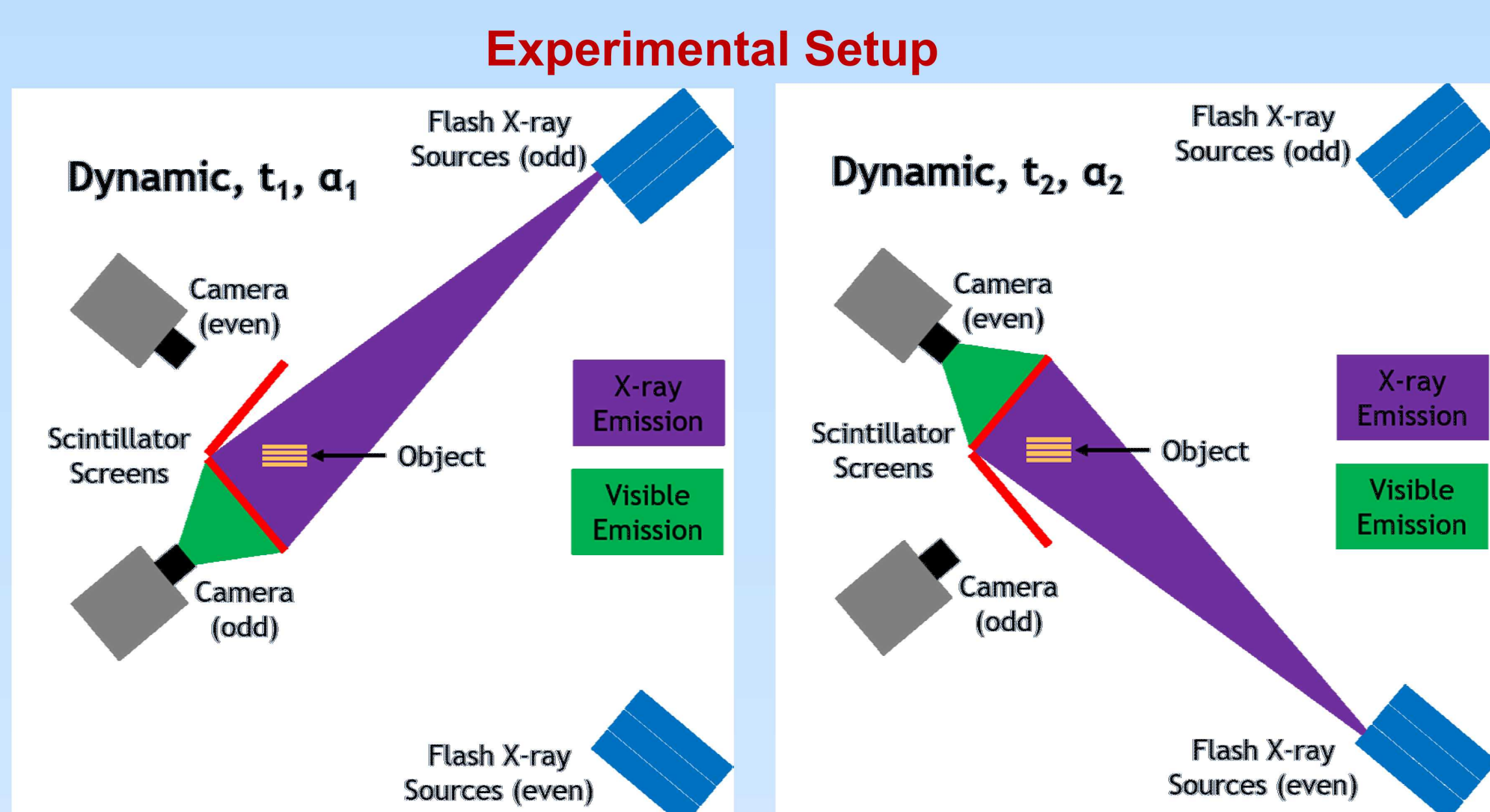
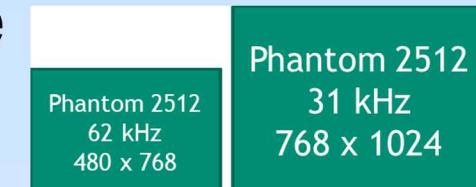
• 10–90% Rise dist. = 1.6 mm

#### Scintillator screens

• GOS:Pr, ~4  $\mu$ s decay time

#### High-speed cameras

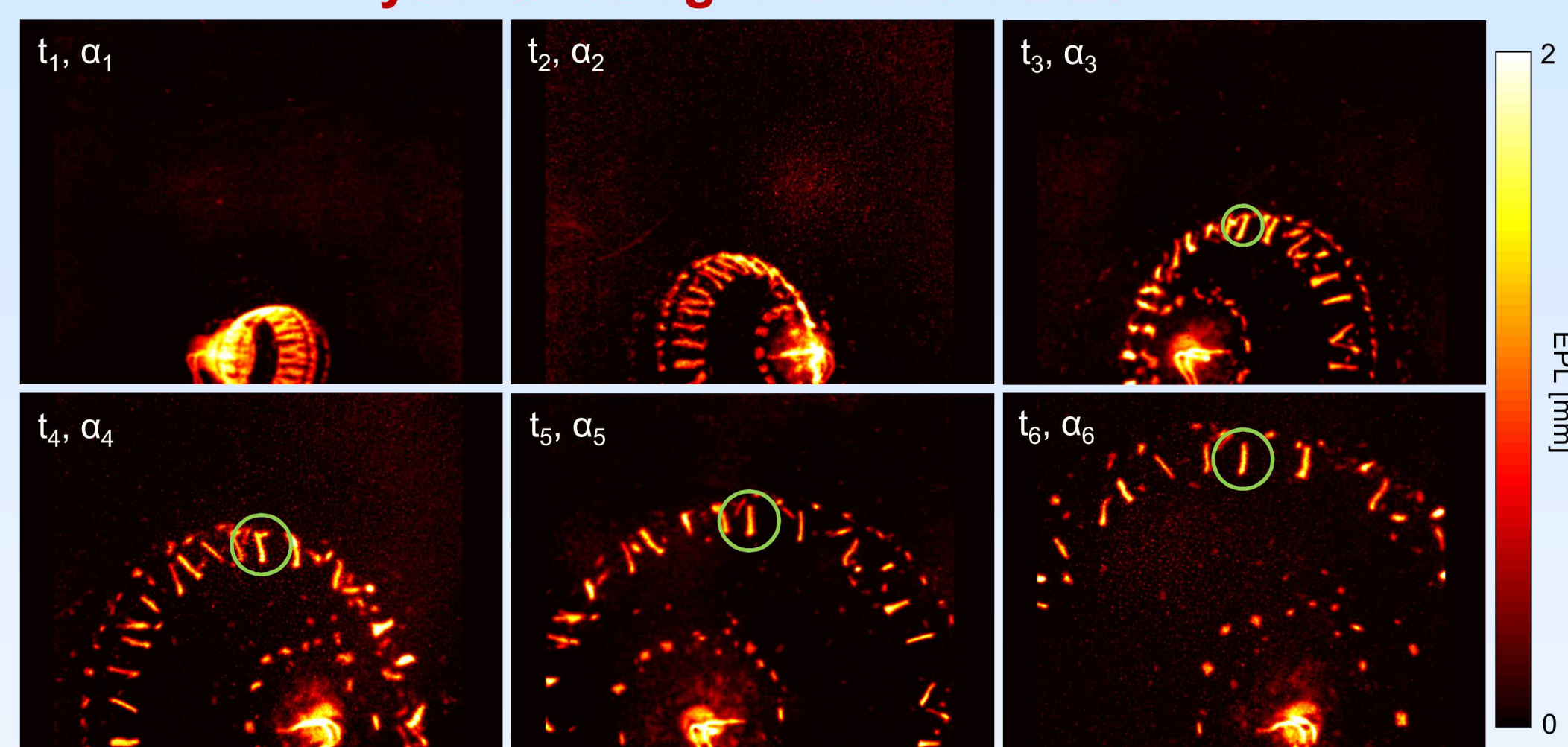
• Phantom 2512, 50 mm f/1.4 Nikon  
 • 62 kHz x-ray imaging, 31 kHz camera frame rate



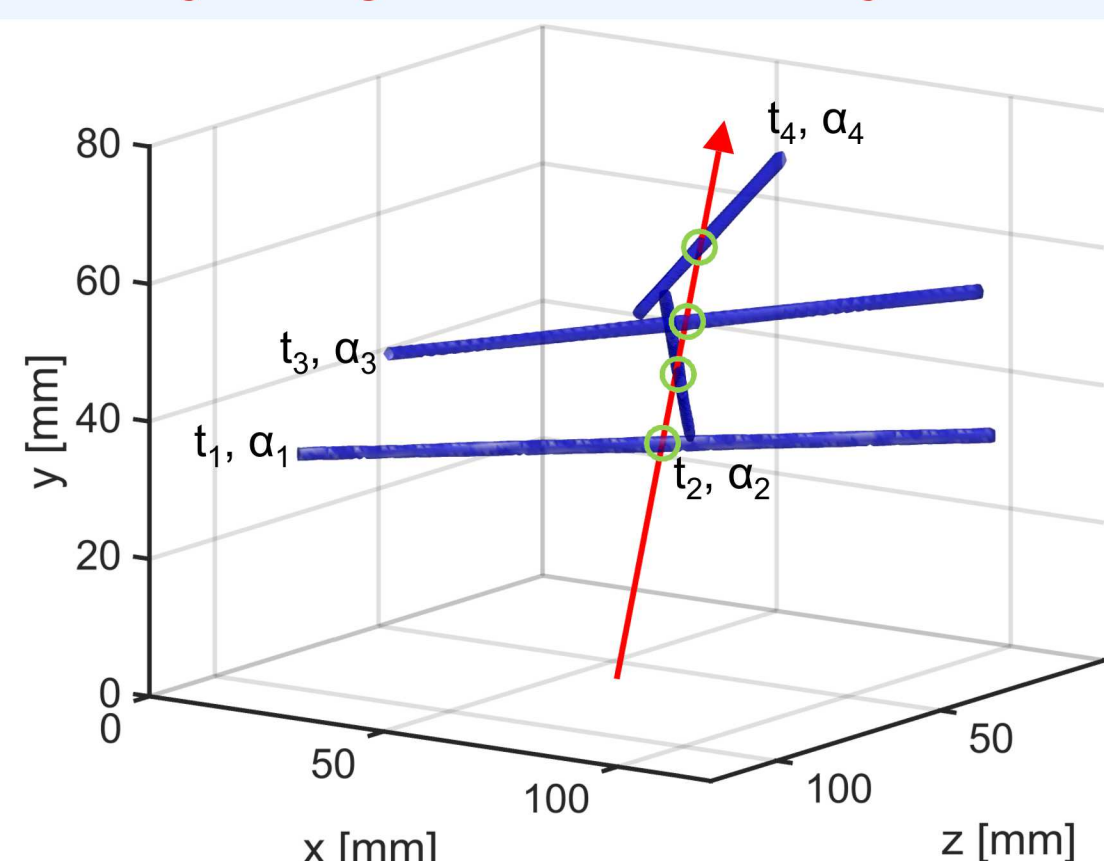
### Data processing

- Dot target calibration
- Remove salt noise from images
- Normalize and convert images to Equivalent Path Length (EPL)
- Segment particles, images were binarized to isolate particles, particle location was determined by center of mass
- Possible particle locations were back projected through volume, no lines intersected because the particle has moved in time
- Unique linear trajectories were fit to the possible particle locations

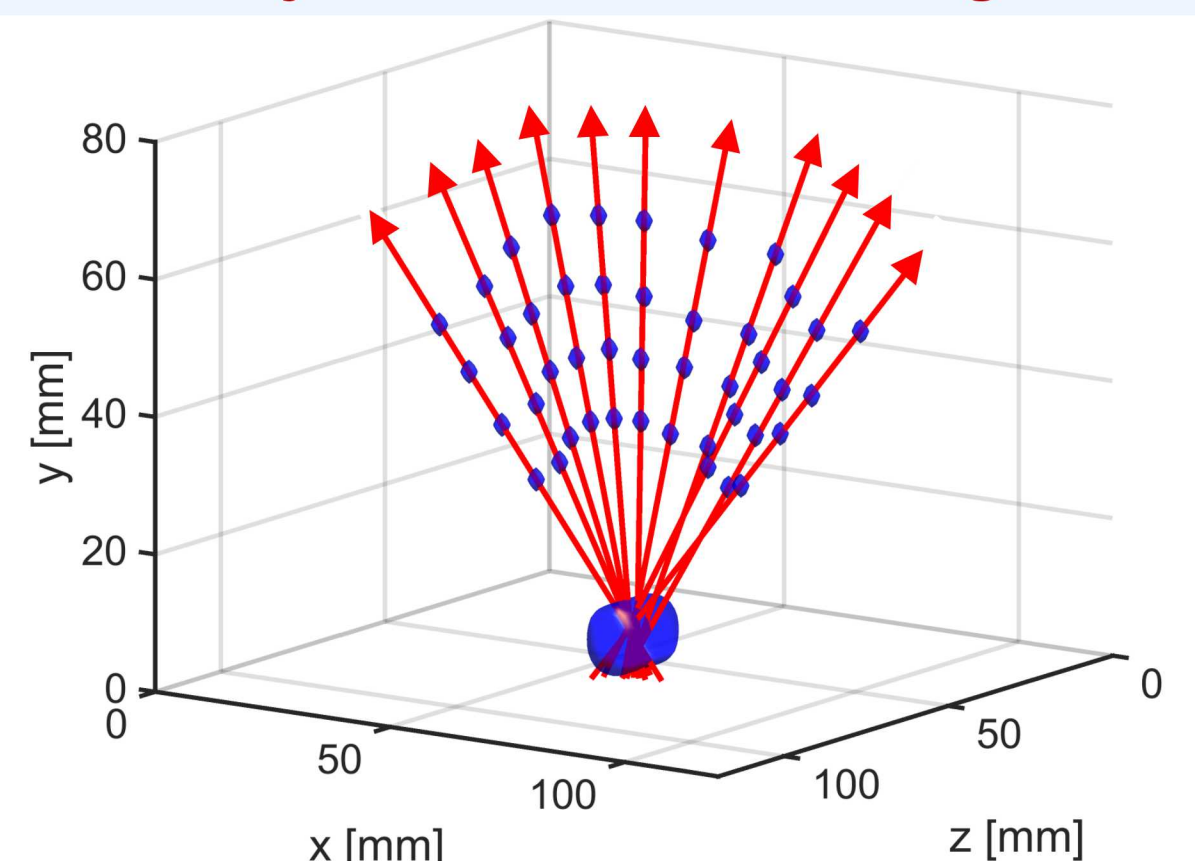
### Dynamic Images of Detonator



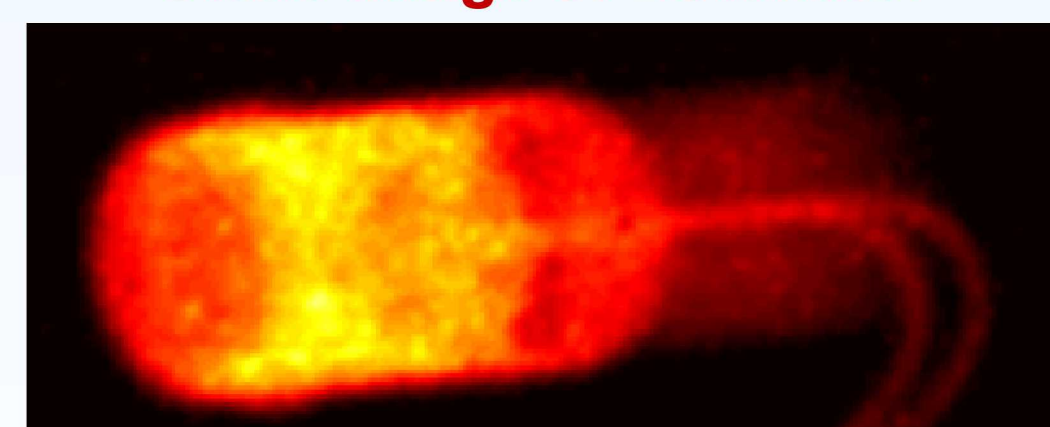
### Trajectory Fit to Back Projections



### Trajectories Traced to Origin



### Static Image of Detonator



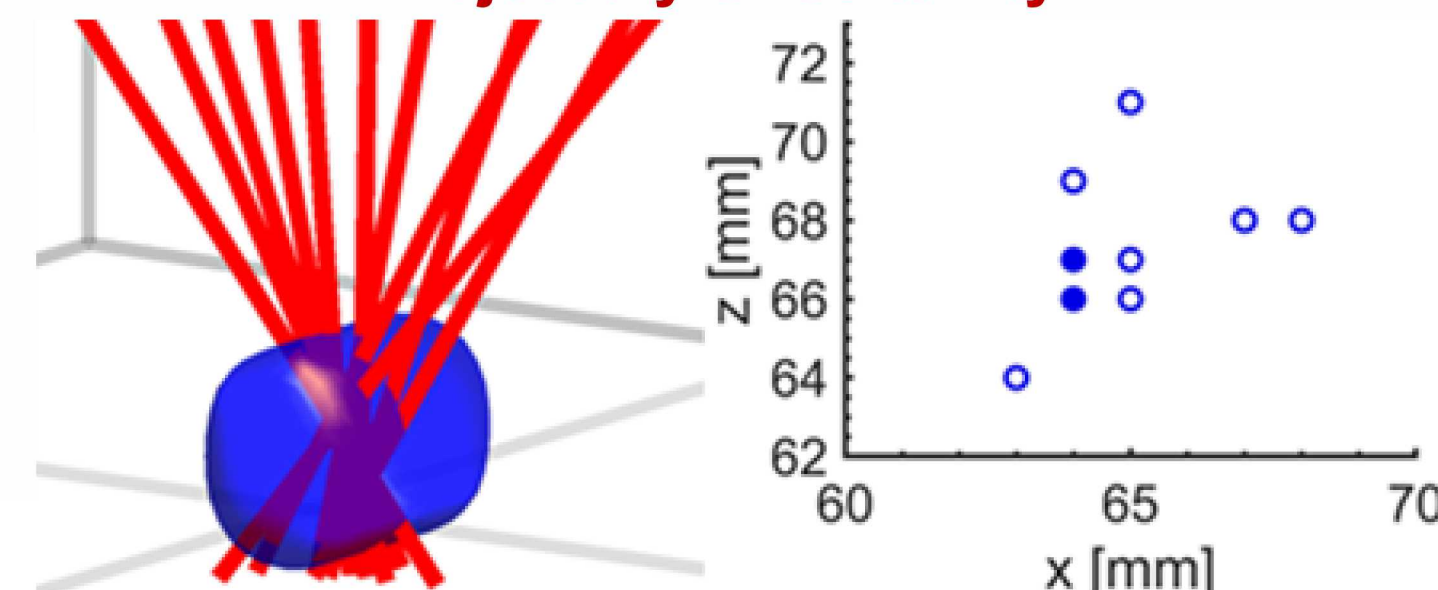
### Uncertainty

• Volume resolution ~1.6 mm, spread of trajectories ~5 mm

### Causes of uncertainty:

- Velocity / Direction: calibration, particle segmentation, center of mass determination, spatial resolution
- Mass: atten. coeff., image blur, image characteristics, noise

### Trajectory Uncertainty

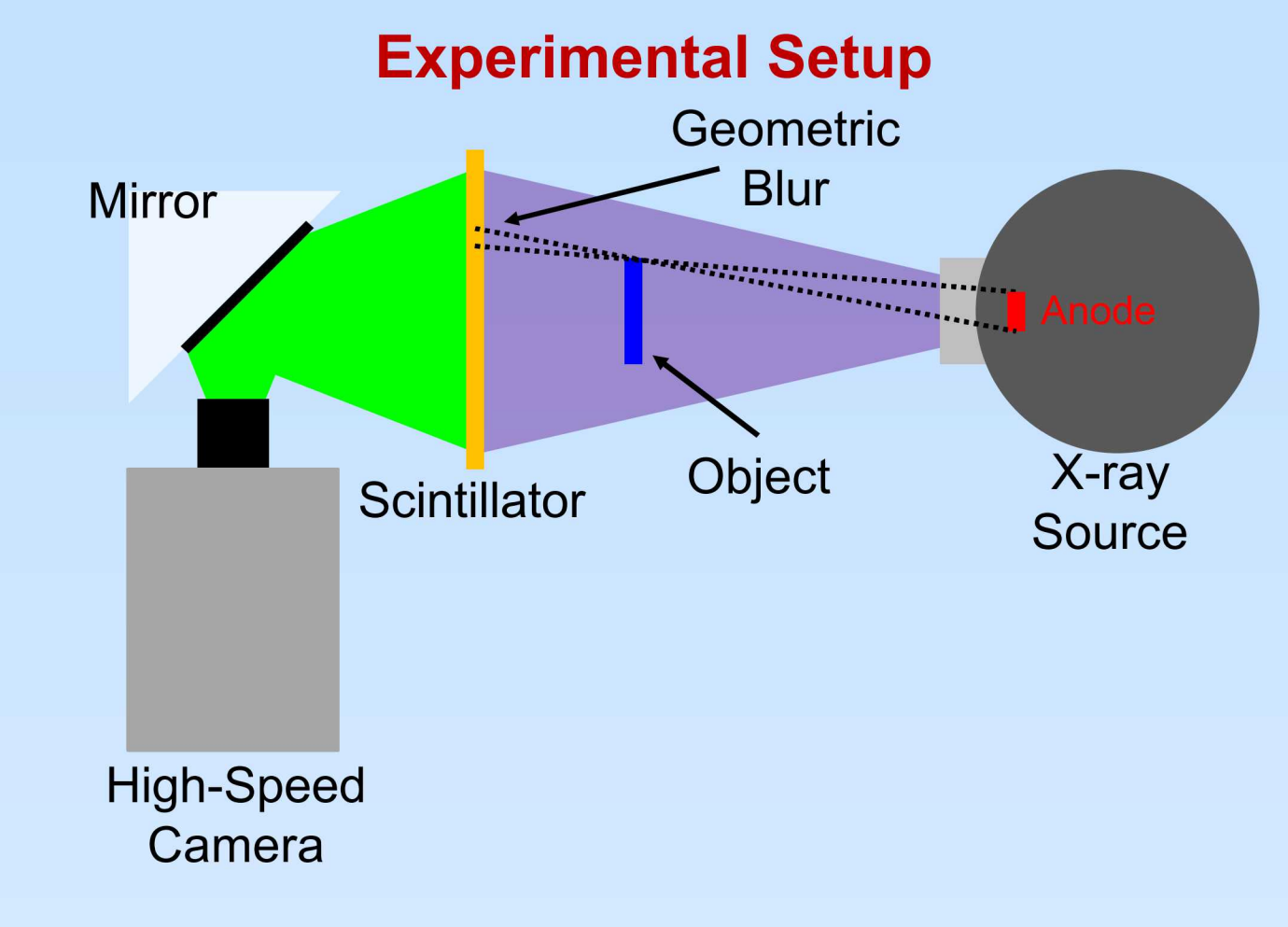
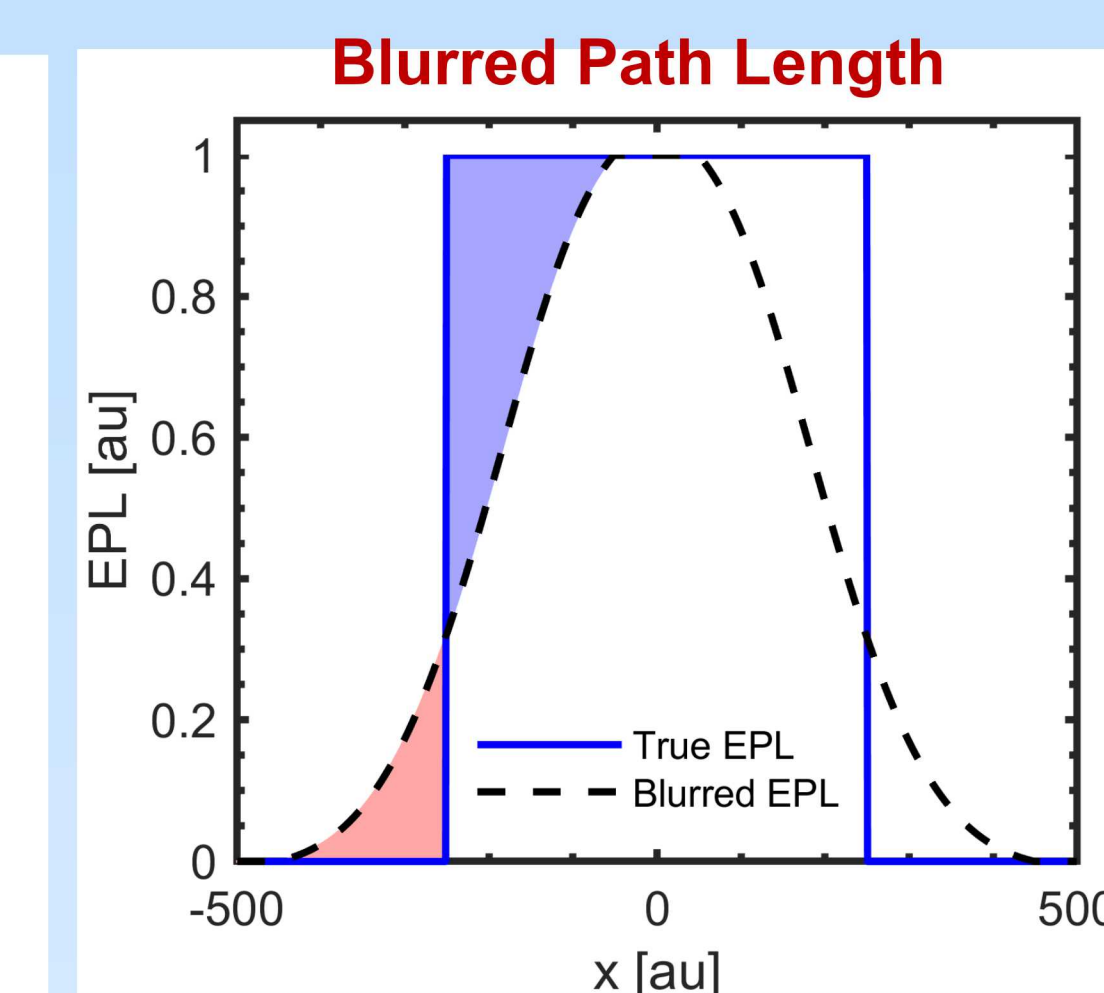
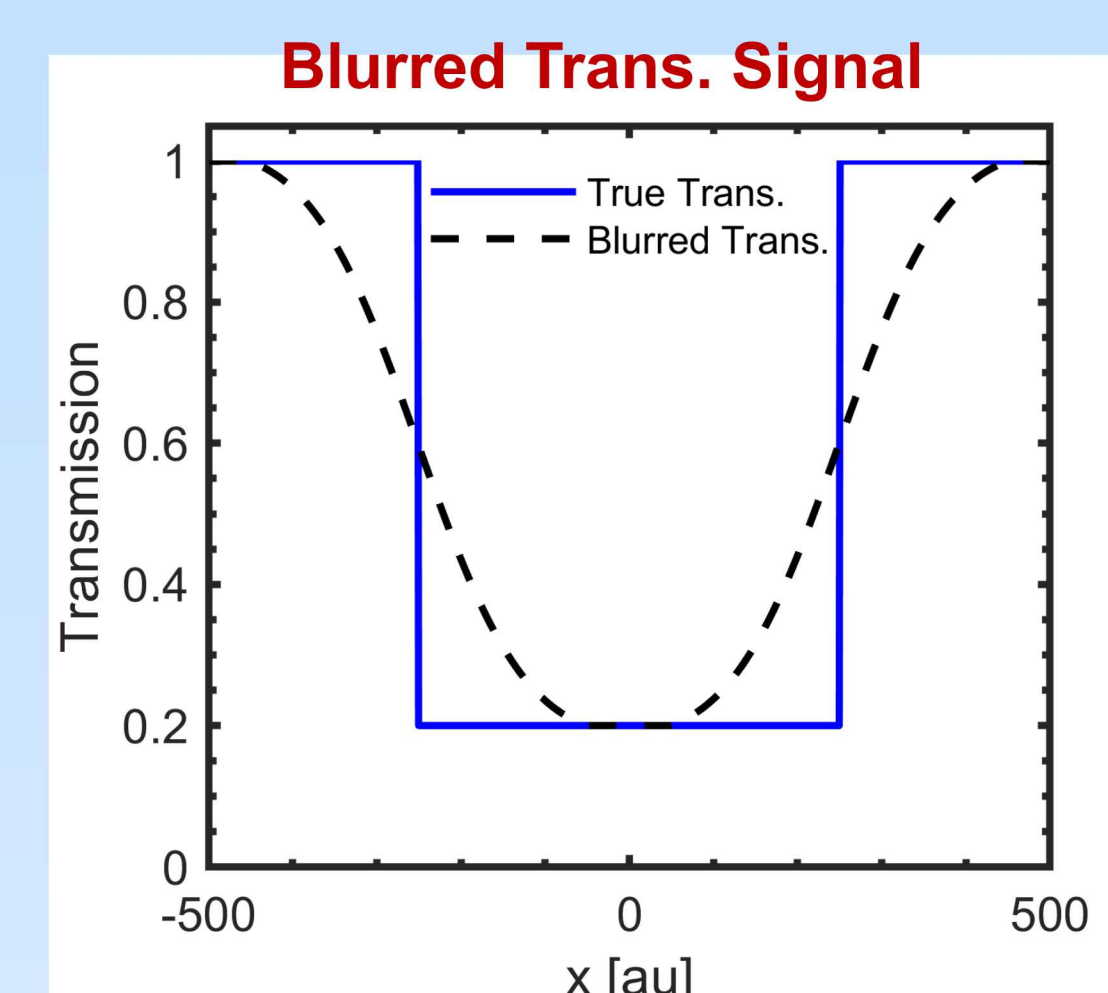


## Apparent Mass Loss due to Image Blur

Image blur induces a bias error during the nonlinear conversion from transmission signal to path length when using a spectrally resolved version of Beer's Law. This bias error manifests as a measured mass less than the true mass. X-ray images were collected of objects of various sizes, shapes, and levels of spatial blur to investigate the uncertainty of measured mass. A numerical model of the imaging system investigated trends over a wide range of object shapes and sizes.

**Effects to consider:** Object size, Image blur, Level of transmission (degree of nonlinearity), Variance of trans., Pixel size, Noise (contrast-to-noise ratio of 5 results in mass gain of ~1%)

**Sources of blur:** penumbra (geometric blur), scintillator, intensifier, camera, lens

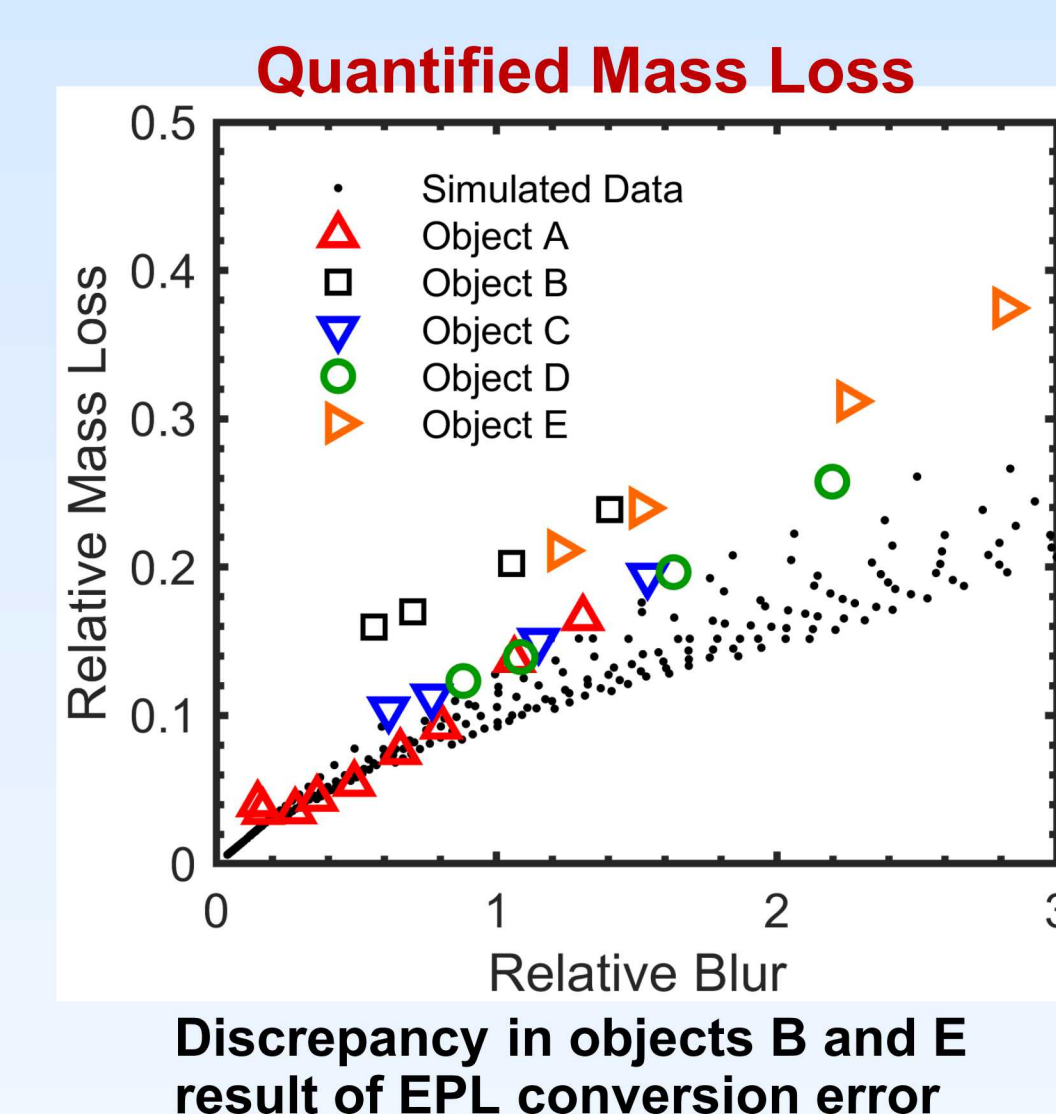
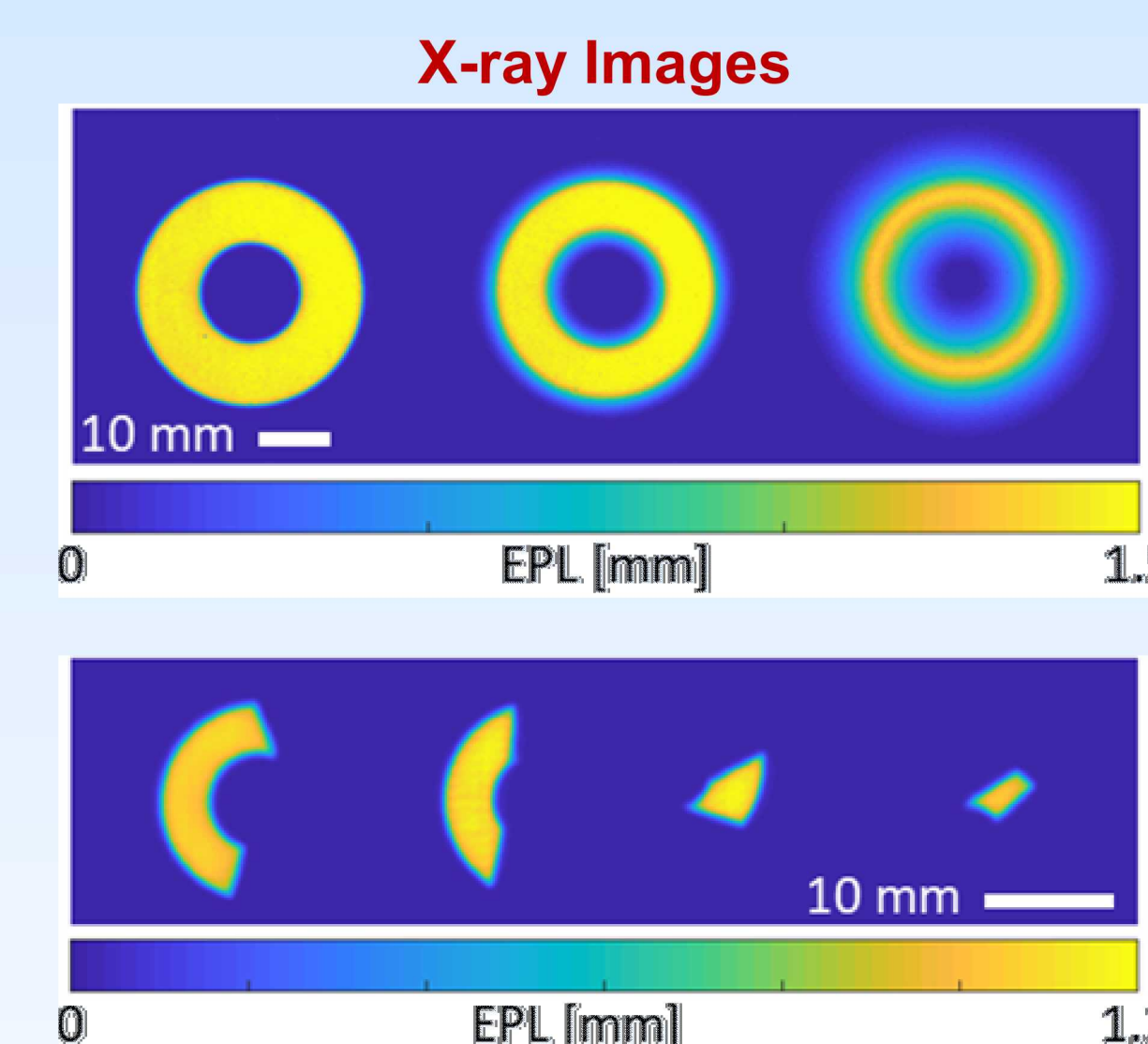


### Experimental Results

- Objects of various shapes and area-to-perimeter ratios were imaged and their masses compared to that measured on a scale

$$\text{Rel. Mass Loss} = \frac{(\text{true} - \text{measured})}{\text{true}}$$

$$\text{Rel. Blur} = \frac{\text{rise distance}}{(\text{area/perimeter})}$$



### Numerical Imaging Results

- Variables: diameter, thickness (transmission), degree of spatial blur, and pixilation (secondary)
- Increased transmission leads to increased mass loss
- Spread in data attributed to degree of object pixilation
- Mass loss tracks well with average attenuation

