

# **Toward a game-theoretic metric for nuclear power plant security**

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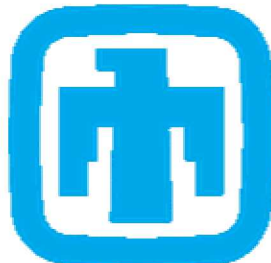
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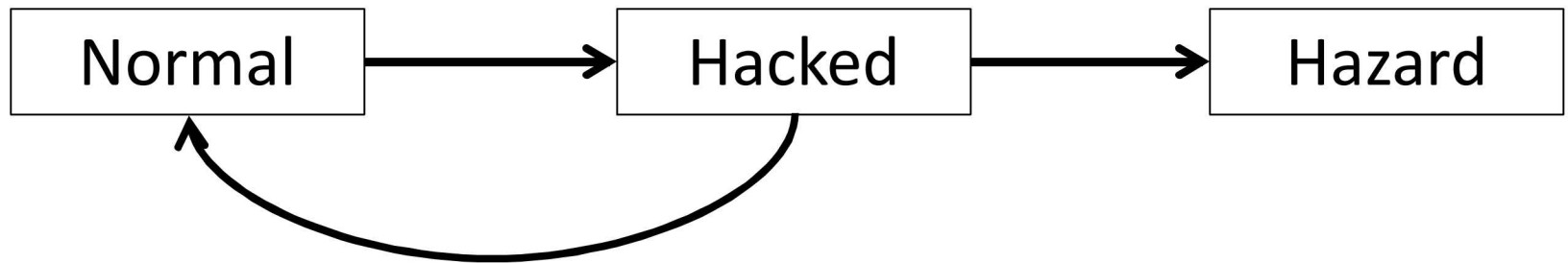
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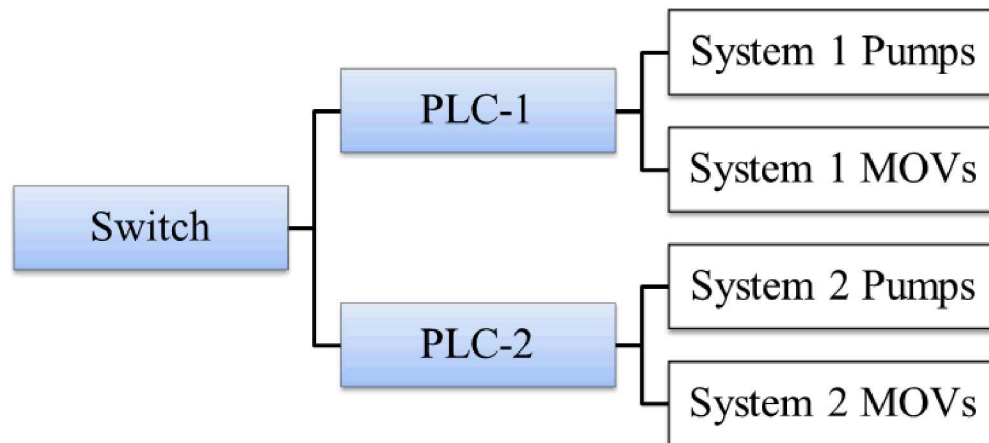
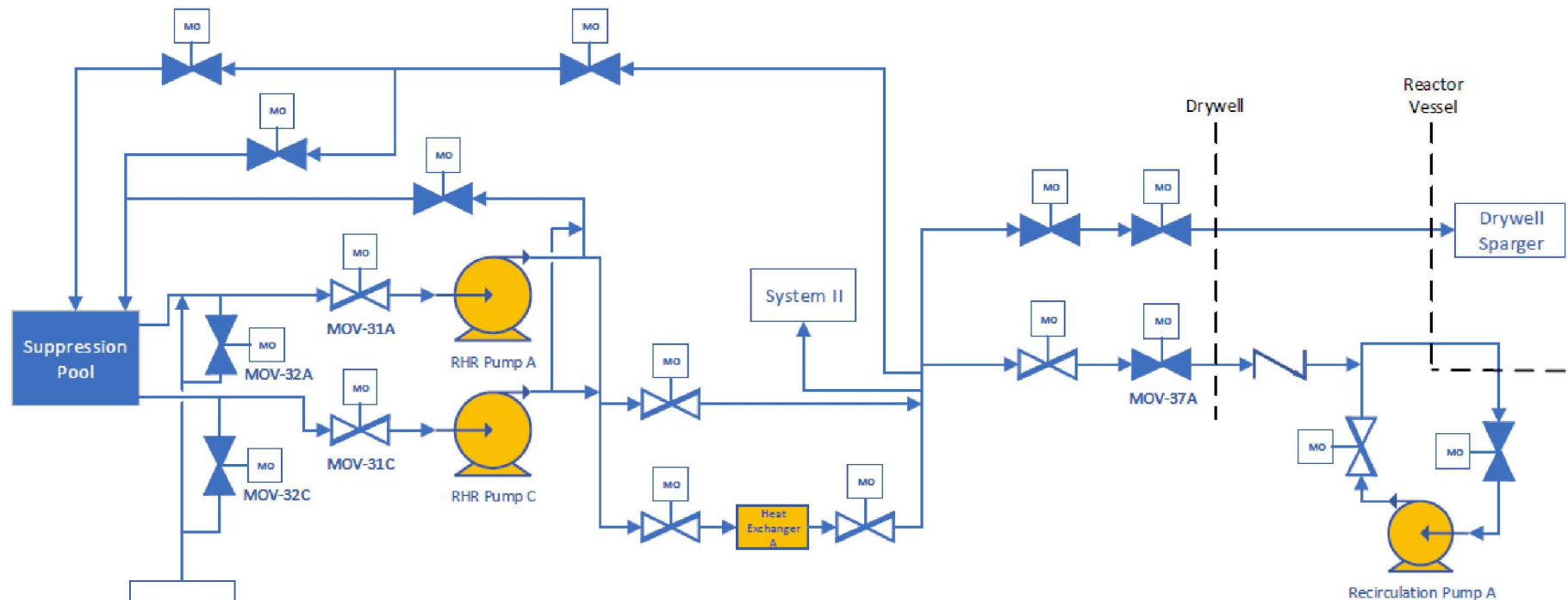
**Stochastic game theory is used to analyze interactions where the outcome is uncertain**



Challenges:

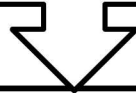
- Managing the size of the state space
- Defining transition probabilities
- Optimizing the solution

# The residual heat removal system maintains reactor water level during a loss of coolant accident

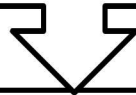


# System-theoretic process analysis was used to identify scenarios of interest

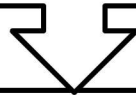
1. Identify losses, hazards, and constraints



2. Model the control structure

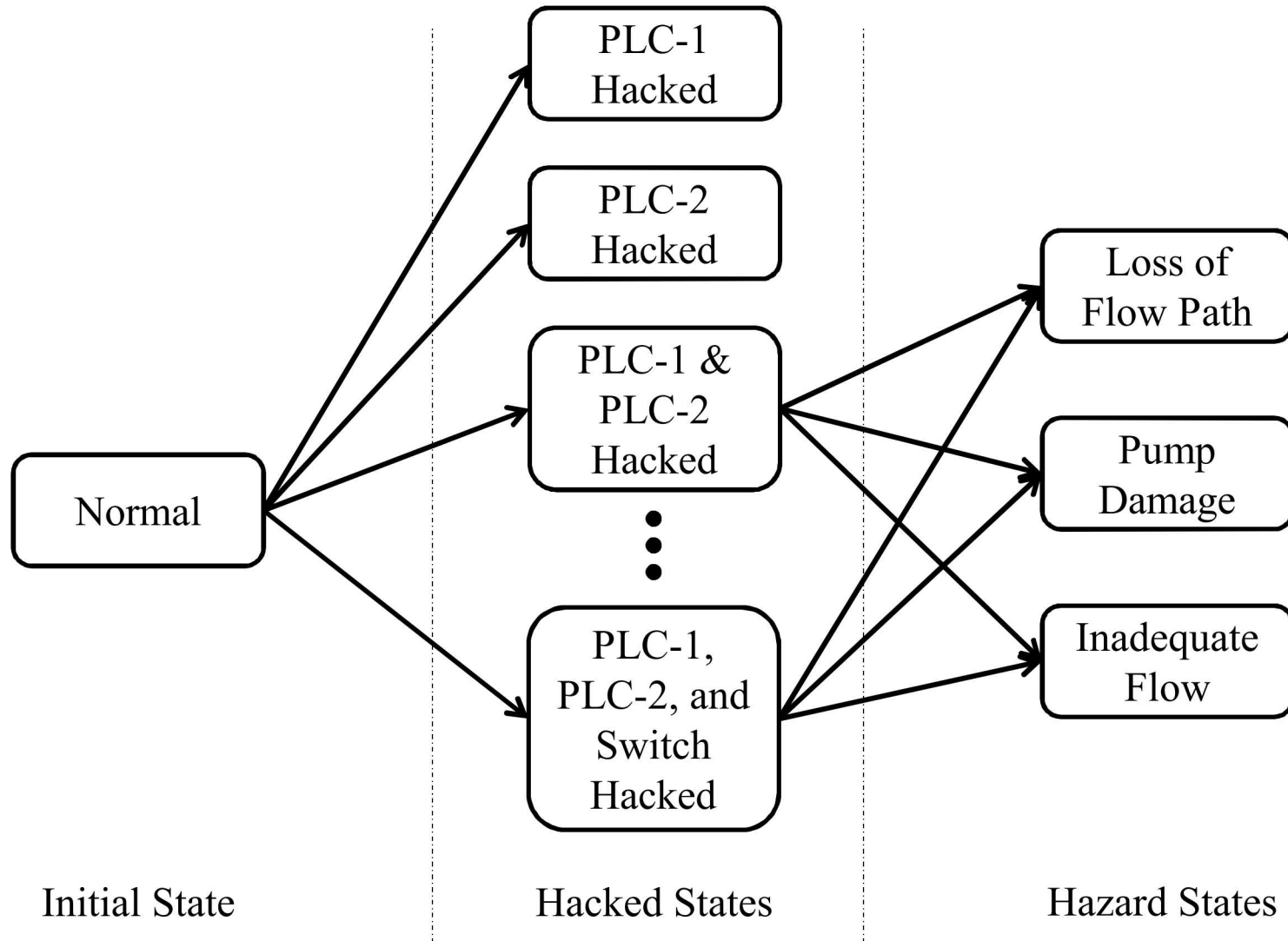


3. Identify the unsafe control actions

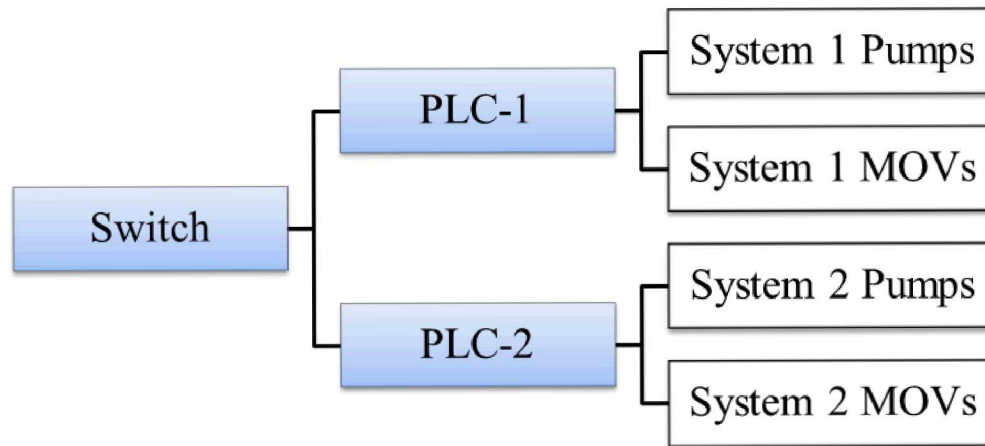


4. Identify loss scenarios

# The stochastic states define the environment of the players' interactions



# Actions were defined for both players at each state



	PLC-1 & PLC-2	Switch	Communication Network
<b>Defender's Choices</b>	Authentication: on/off Wireless: on/off	Authentication: on/off Firewall: on/off	Encryption: on/off
<b>Attacker's Choices</b>	Join: yes/no Wireless Exploit: yes/no	Join: yes/no Attack: yes/no	Decryption: yes/no

# The Common Vulnerability Scoring System was used to estimate state transition probabilities

## CVSS Exploitability Metrics

1. Attack vector
2. Attack complexity
3. Privileges required
4. User interaction


$$p(s_j | s_i, a_D, a_A)$$

Probabilities may be validated with capture the flag games

**Reward functions were defined to quantify the costs and benefits for both players**

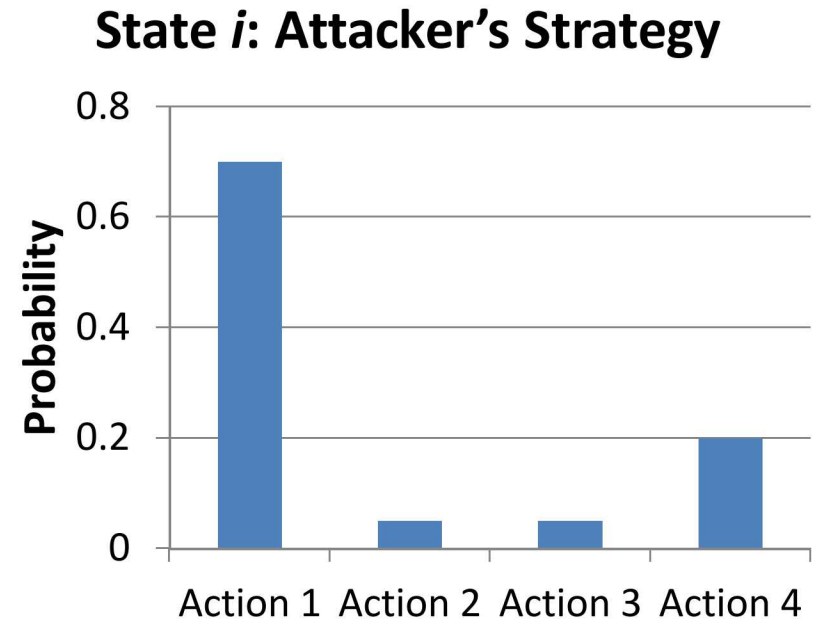
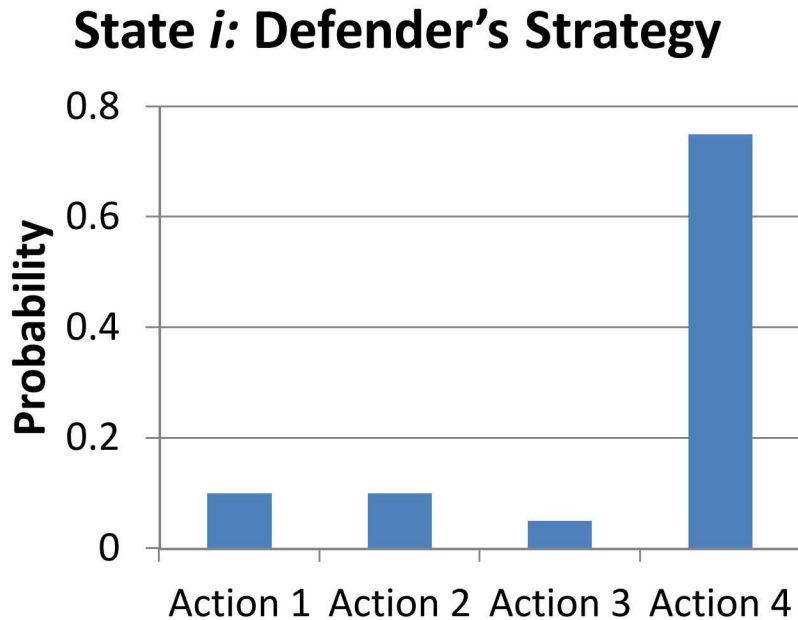
**Immediate reward function for player A/D:**

$$r_{A/D}(s_i, a_D, a_A, s_j) = \phi_{A/D}(s_j) - E_{A/D}(a_{A/D})$$

**Cumulative utility function for player A/D:**

$$u_{A/D}(s_N, \pi_A, \pi_D) = \sum_{t=0}^{\infty} \beta^t \mathbb{E}[r_{A/D}(s^t, a_D^t, a_A^t, s^{t+1})], \quad s^0 = s_N$$

# The Nash equilibrium provides the optimal action for each player at each state



**There are several challenges to finding the solution.**

- 1. Large parameter space: 576 probabilities**
- 2. Parameter constraints: probability laws**
- 3. Solution uniqueness**

# **Stochastic game theory is a promising method for selecting cybersecurity control actions for nuclear power plants.**

- Threat actor was defined using threat agent libraries
- System-Theoretic Process Analysis was used to manage the stochastic state space
- The Common Vulnerability Scoring System was used to estimate transition probabilities
- Solving the game presents additional optimization challenges

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