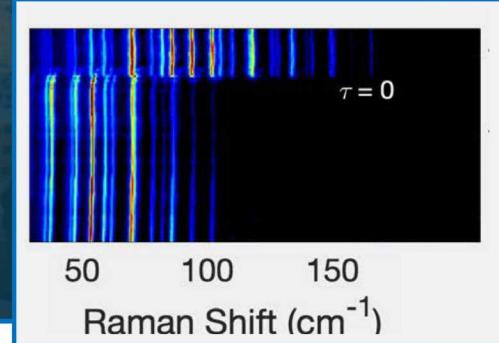
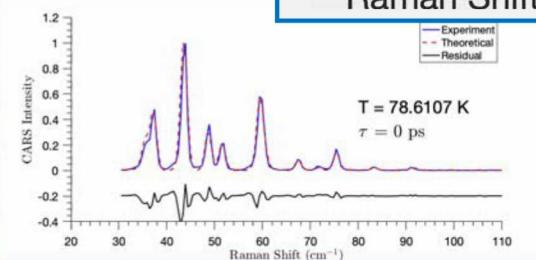
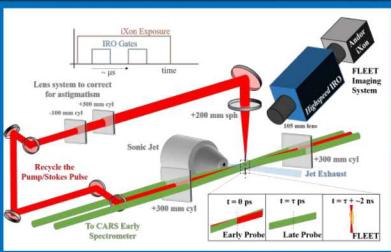
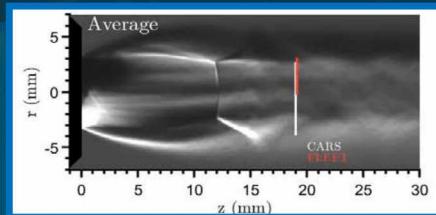


# Simultaneous Temperature/Pressure Monitoring in Compressible Flows using Hybrid fs/ps Pure-Rotational CARS

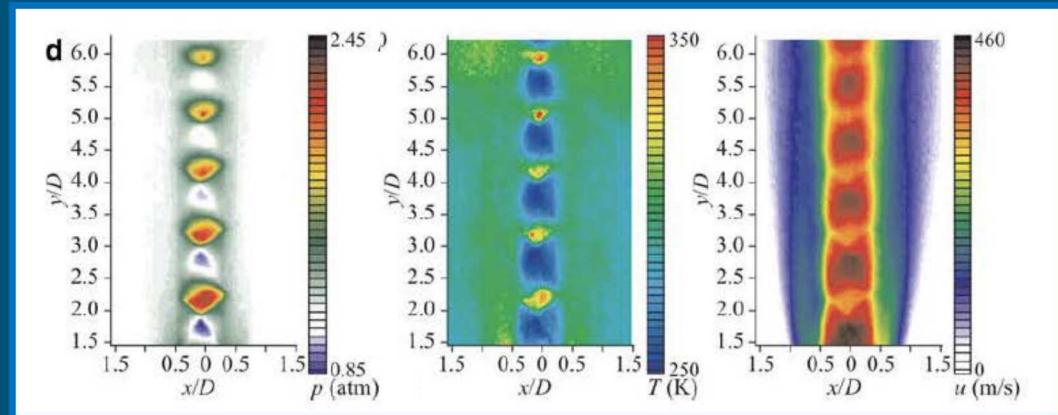


Sean P. Kearney, Daniel R. Richardson, Jonathan Retter  
Sandia National Laboratories, Albuquerque, NM

Chloe Dedic  
University of Virginia, Charlottesville, VA

Paul M. Danehy  
NASA Langley Research Center, Hampton, VA

- There is renewed interest in supersonic and hypersonic ground-test facilities
- Cold-flow facilities require measurement of temperature, pressure, velocity, even thermal distribution functions
- Noninvasive tools for temperature/pressure monitoring
  - Laser-induced fluorescence (LIF)
  - Filtered Rayleigh scattering
- Two-dimensional imaging
- kHz repetition rate
- May require seed/tracer molecule (LIF)
- Multi-camera, multi-angle detection scheme (Rayleigh)

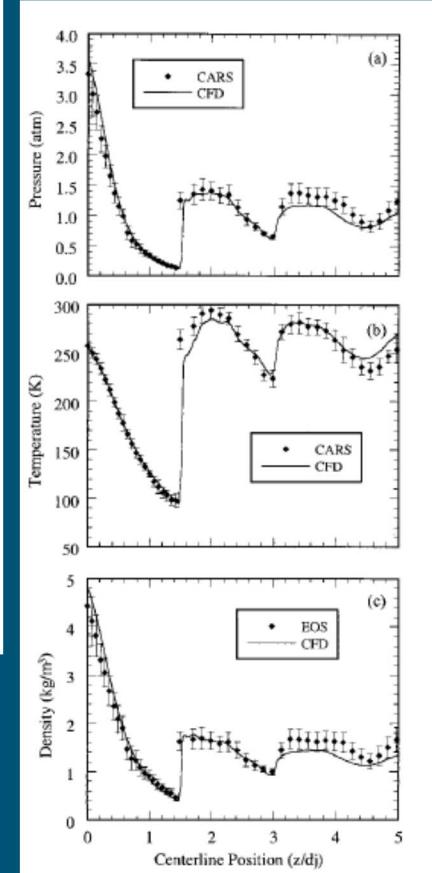
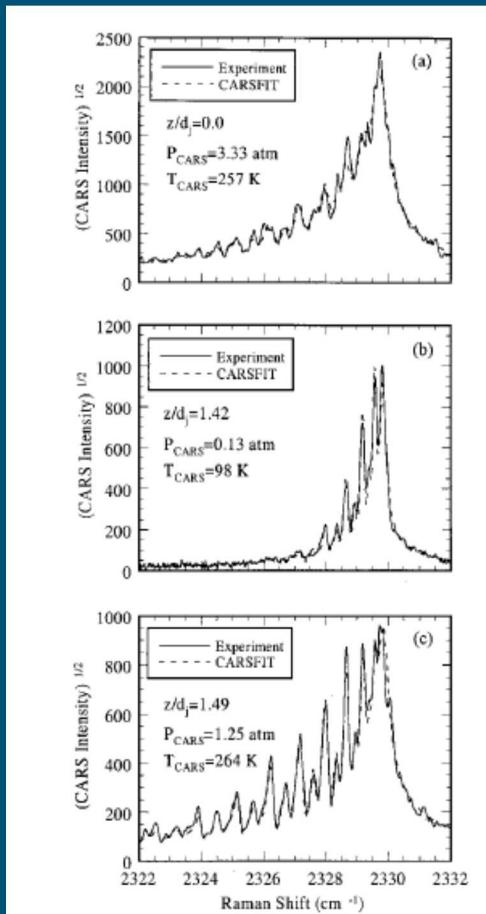


Time-scanned FRS detection of T,P,V  
Boguszko and Elliott, AIAA J. (2005)

## Coherent anti-Stokes Raman Scattering (nanosecond)



- CARS demonstrations for simultaneous T/P measurement
- Nanosecond-duration laser pulses
- High spectral resolution to deconvolve the effects of T and P
  - Temperature from line intensity distribution
  - Pressure from collision-broadened linewidths (Woodmansee et al., Farrow)
  - Density from calibrated signal amplitude (Grisch *et al.*)

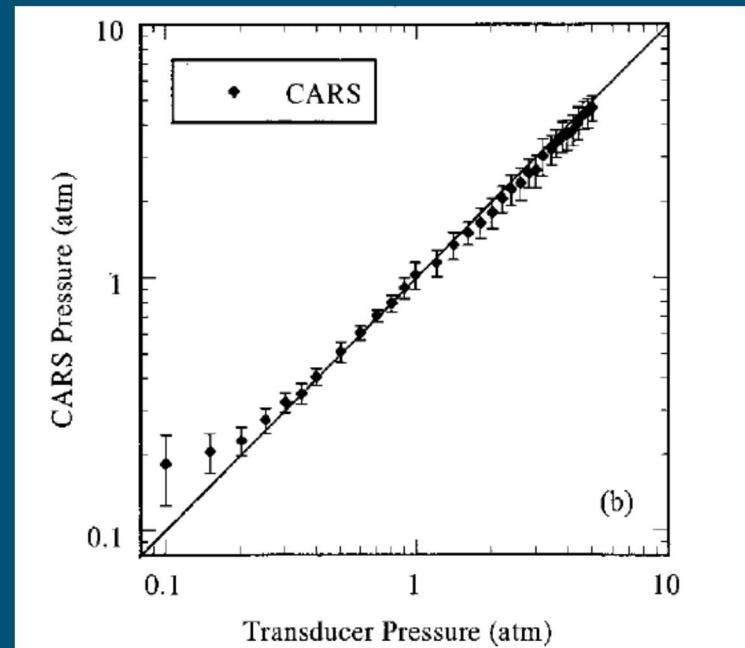


Woodmansee *et al.*,  
*Appl. Opt.* (2000).

## Coherent anti-Stokes Raman Scattering (nanosecond)

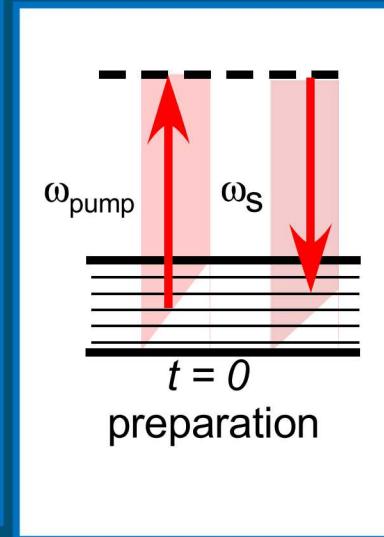
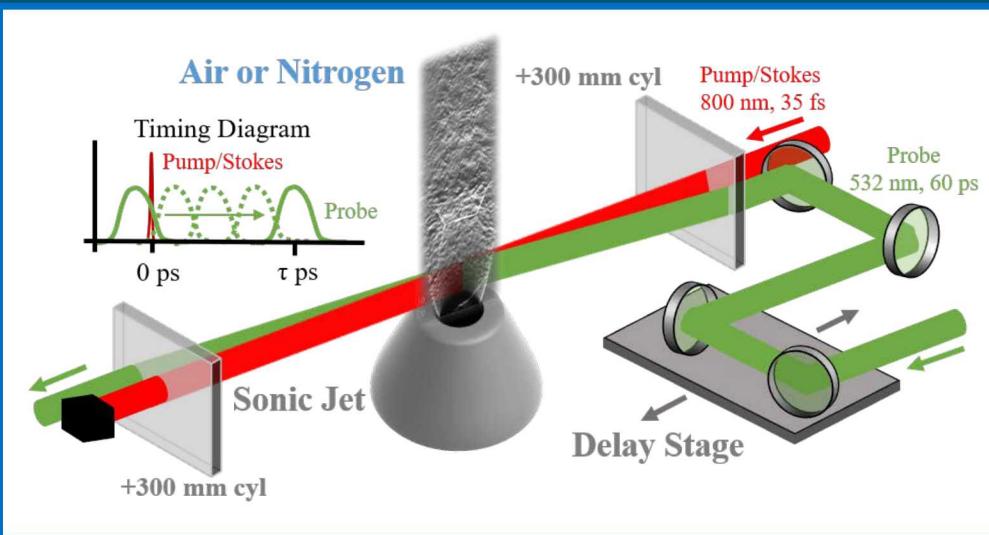


- CARS demonstrations for simultaneous T/P measurement
- Nanosecond-duration laser pulses
- High spectral resolution to deconvolve the effects of T and P
  - Temperature from line intensity distribution
  - Pressure from collision-broadened linewidths (Woodmansee et al., Farrow)
  - Density from calibrated signal amplitude (Grisch *et al.*)
- Spectroscopy of the  $N_2$  Q branch
  - Overlapping lines
  - Doppler contributions at  $P \sim 0.1$  atm and below
  - Limited low-pressure sensitivity in ground testing

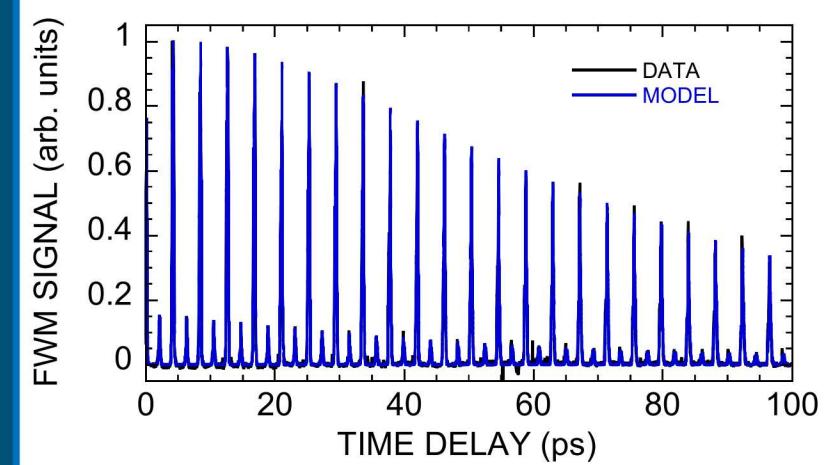
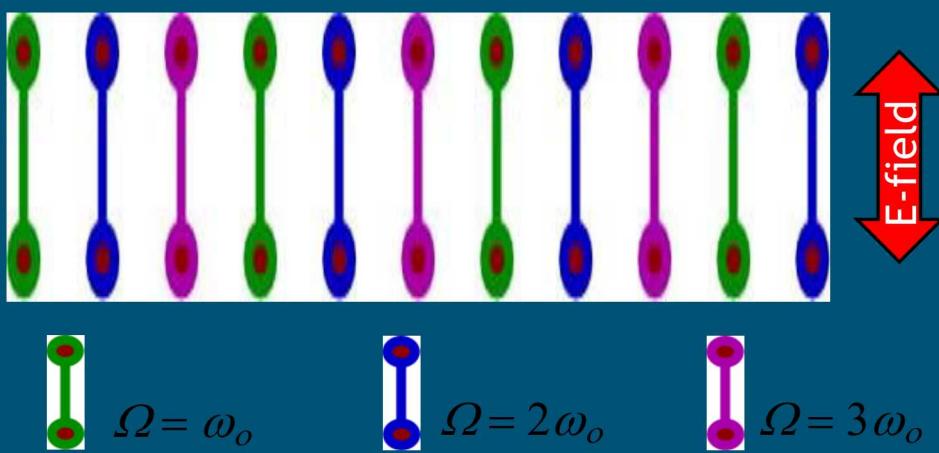


Woodmansee *et al.*, *Appl. Opt.* (2000).

# “Hybrid” time- and frequency domain CARS detection

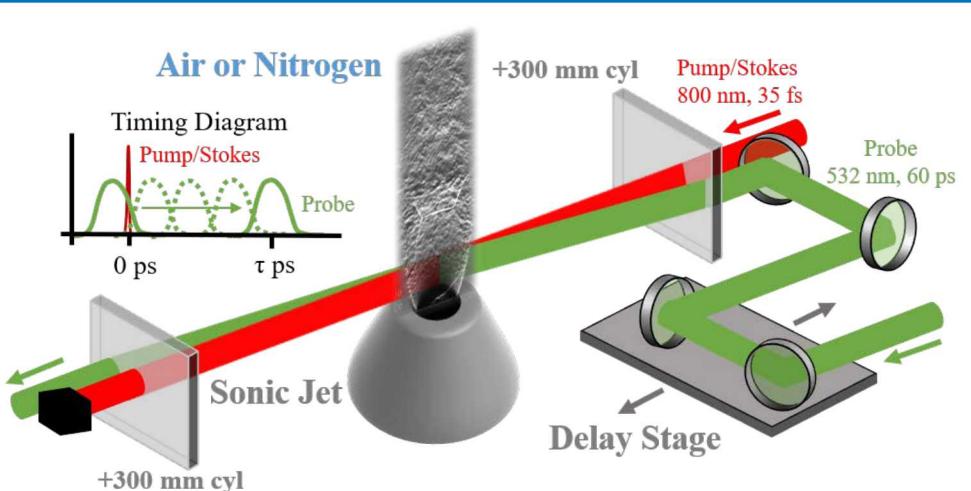


## Impulsive pump/Stokes Raman preparation



## Time Evolution of Raman Coherence

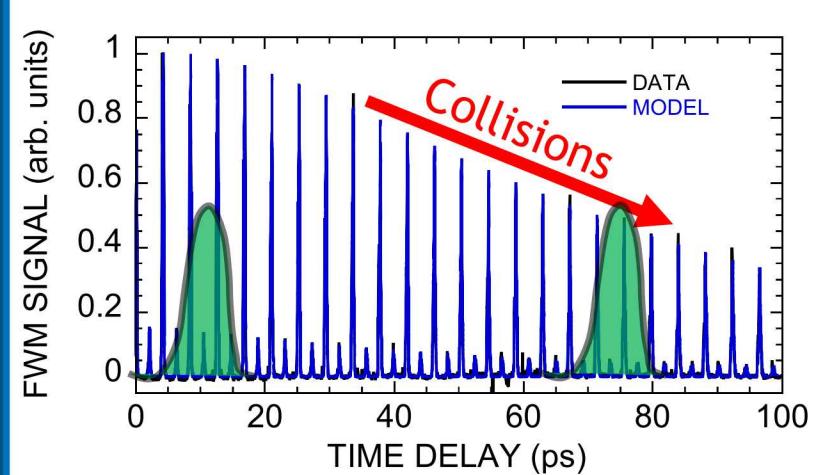
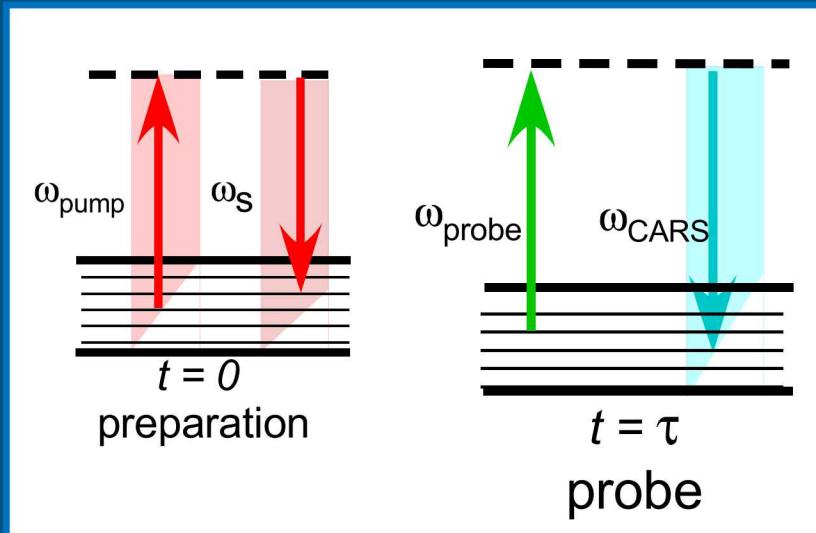
# “Hybrid” time- and frequency domain CARS detection



$$\chi = \sum_J W_J \exp(i \omega_J t) \exp(-\Gamma_J t)$$

- Hybrid time/frequency detection decouples effects of T and P
- Pure-Rotational spectroscopy delays onset of Doppler effects to much lower pressure

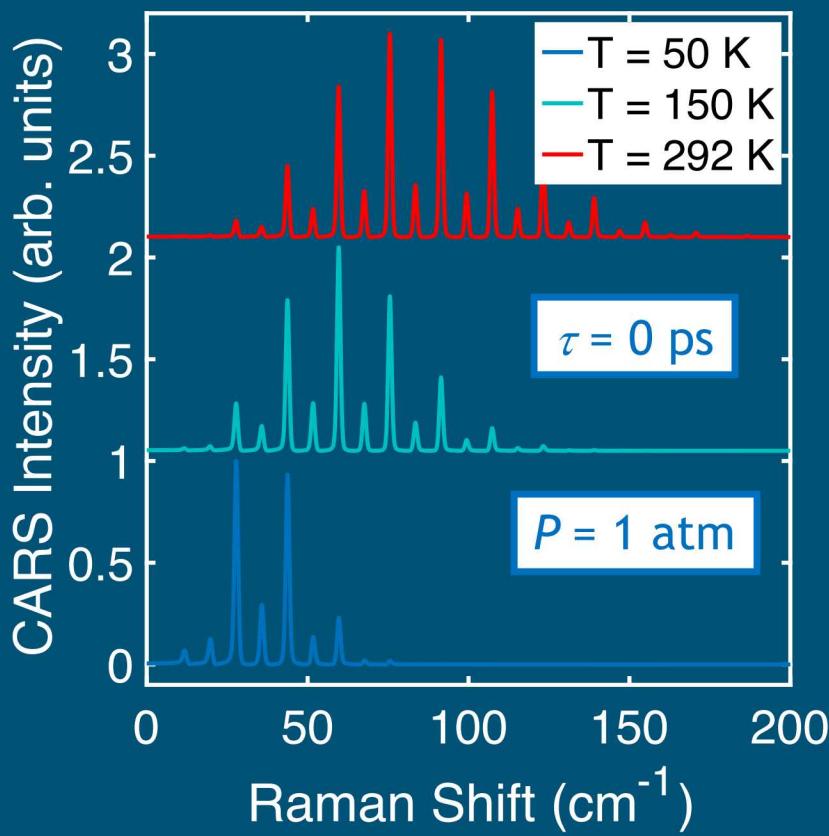
$$\Delta\omega_D = 2\omega_R \sqrt{\frac{2\log(2)kT}{m}}$$





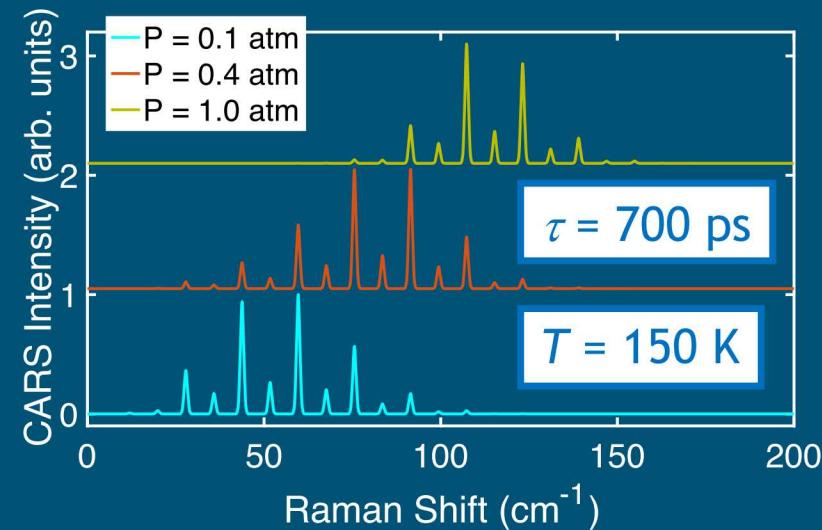
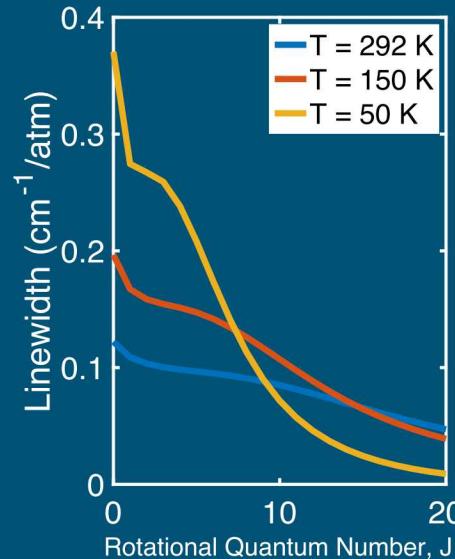
### Step 1: Thermometry at Early Time

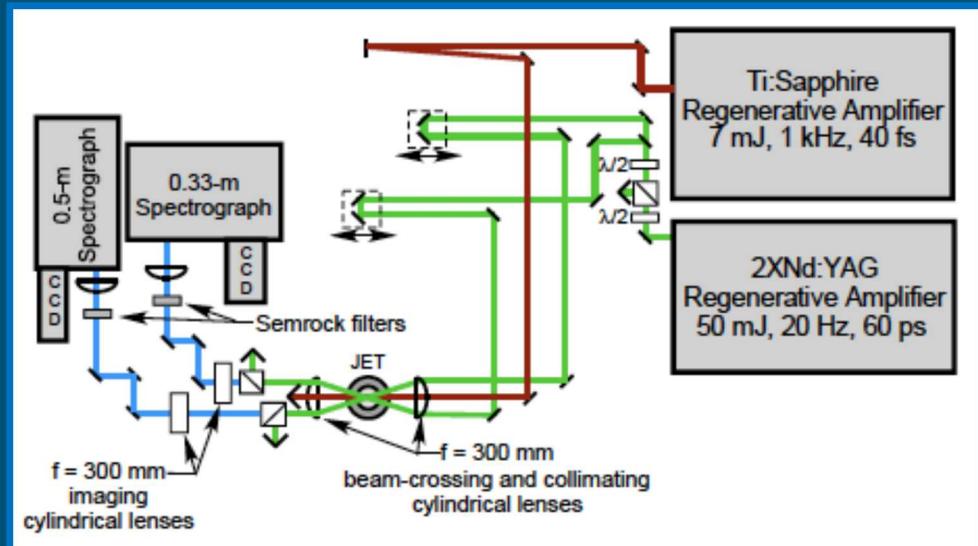
- “Collision-Free” spectra temperature sensitive independent of pressure
- Spectra largely reflect rotational Boltzmann populations



### Step 2: Sample late-time collisions for pressure

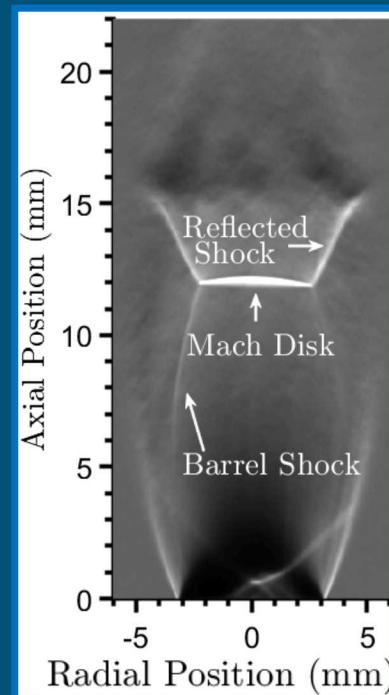
- Monotonic decrease in  $\Gamma$  with  $J$
- High energy transitions have longer lifetimes
- Spectra look “hotter” with increasing  $P$  or delay



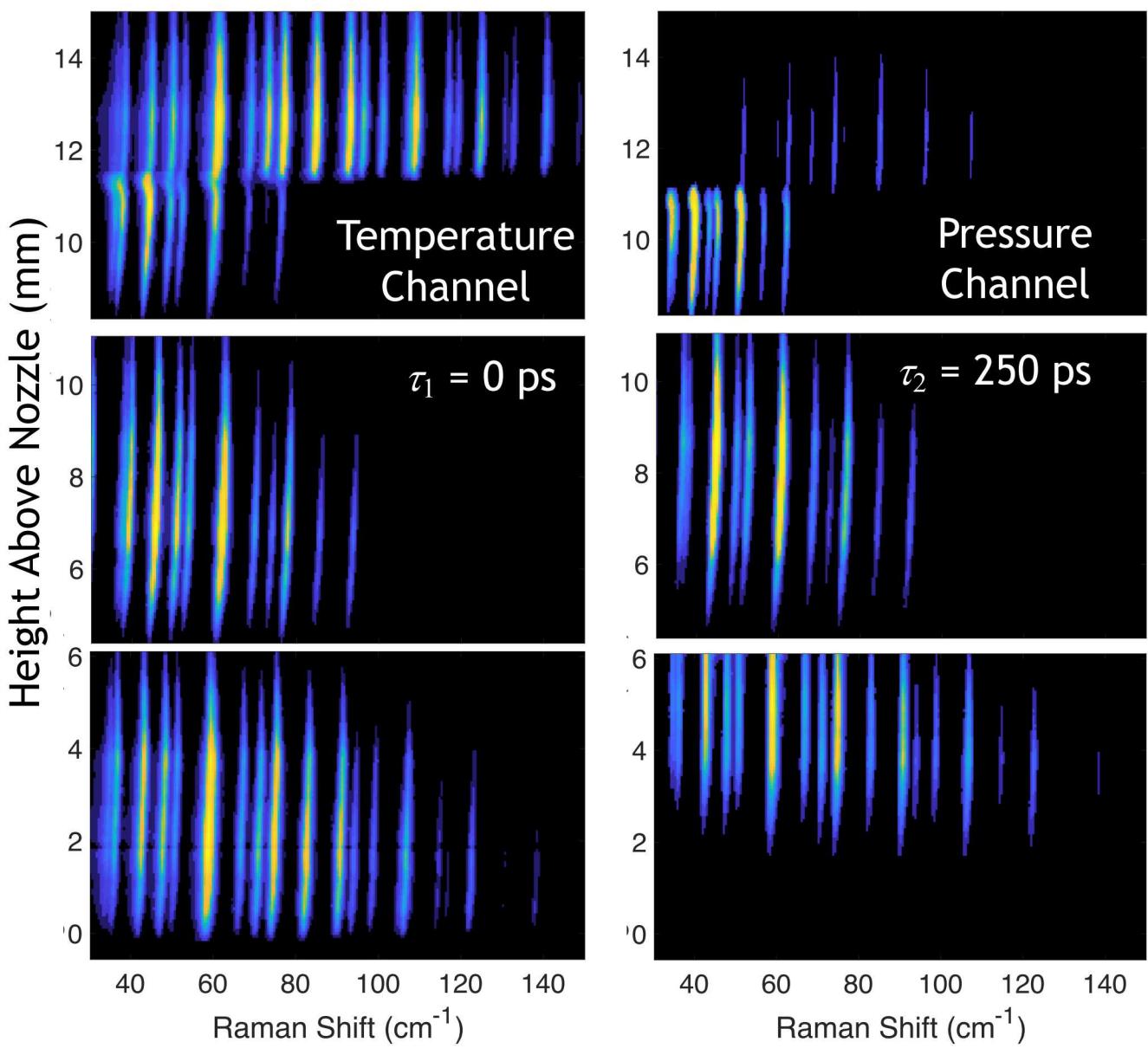


- 1D imaging scheme developed by Bohlin and Kliewer
- Two independent detection channels for early (T) and late (P) measurements
- 50-fs pump,  $\sim 250 \text{ cm}^{-1}$  bandwidth, 4 mJ
- 60-ps probe near transform limit, 50 mJ
- 6-mm long measurement line
- $1000 \mu\text{m} \times 67 \mu\text{m} \times 30 \mu\text{m}$  resolution

- 6.35 mm underexpanded sonic jet
- $P_0 = 7.62 \text{ atm}$ ,  $T_0 = 292 \text{ K}$
- Working fluid = air
- 3 independent ROIs required to span jet exit past Mach disk
- 50-laser-shot ensembles at  $\tau_2$  probe delay

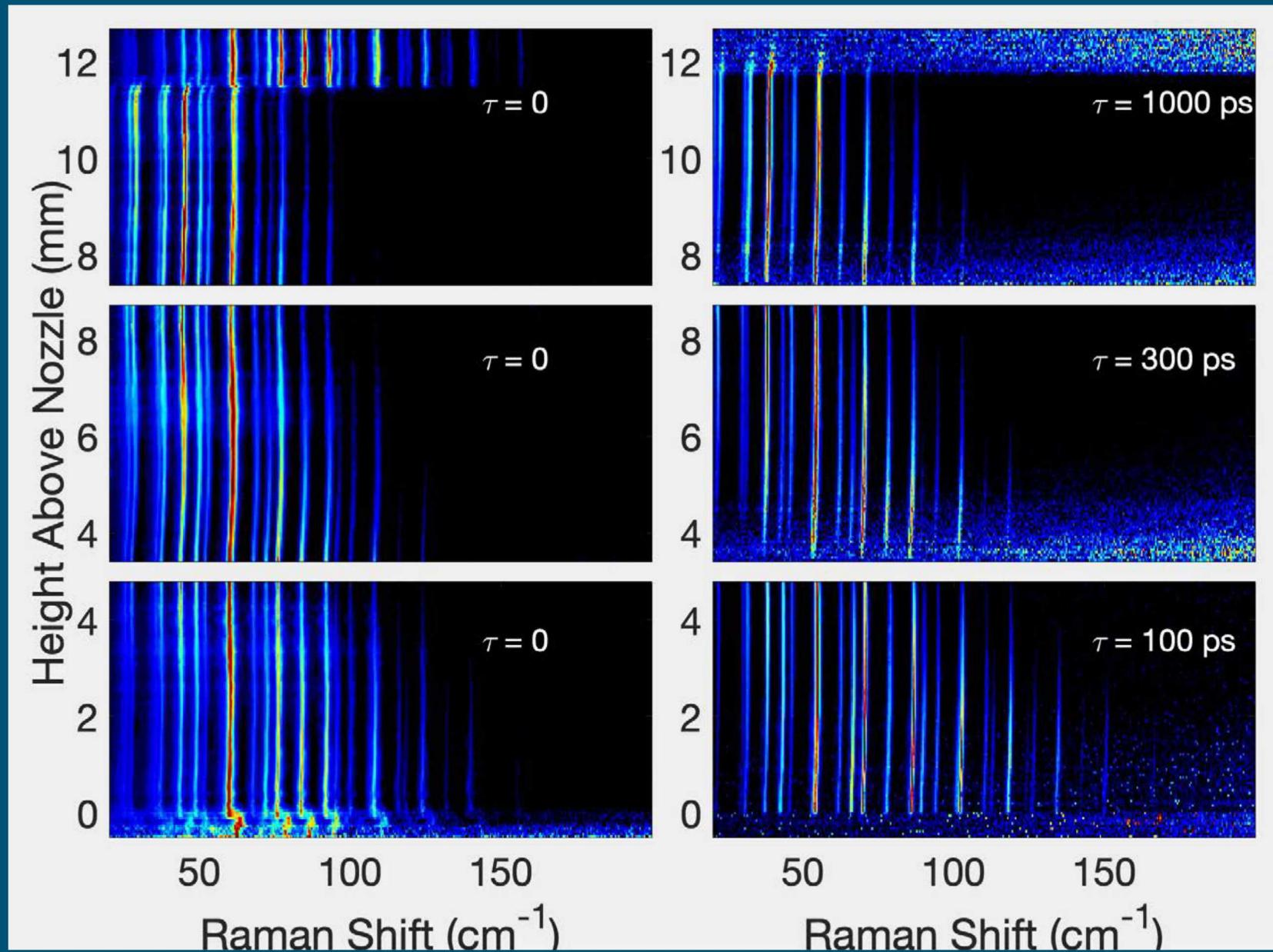


## One-dimensional R-CARS Imaging: 50-shot averages



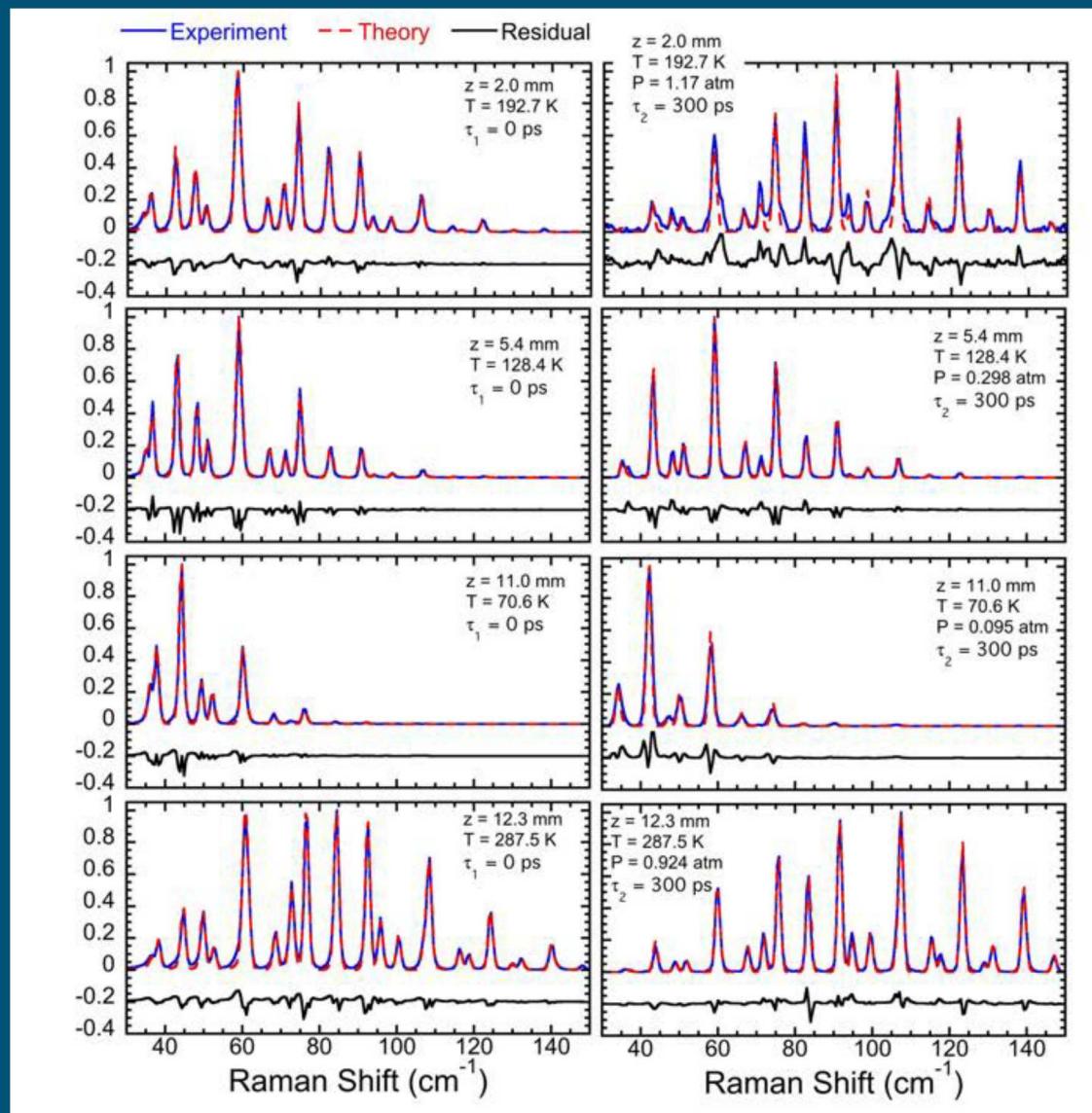
- Pressure challenges dynamic range
- High-pressure regions require low  $\tau$
- Low-pressure regions require very long  $\tau$  (ns!)
- Pressure sensitivity maximized in near-jet and post-shock regions at  $\tau = 250$  ps

## Single-laser-shot imaging (20 Hz)



# Temperature and pressure dependence of CARS spectra

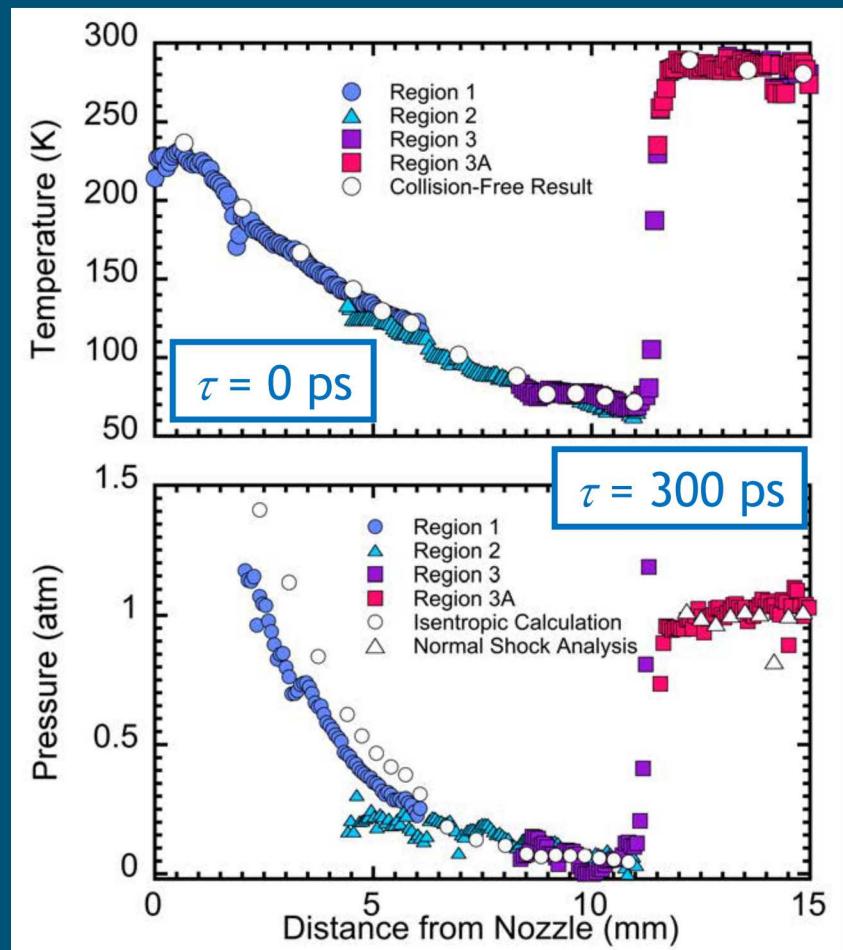
- 50 laser-shot average spectra
- $\tau_1$  channel (left) indicates temperature nearly independent of pressure
- $\tau_2 = 300$  ps delay on pressure channel
- $\tau_2$  delay results in pressure sensitive intensity to higher  $\text{cm}^{-1}$  (shown at right)
- Pressure sensitivity optimized near  $P = 1\text{ atm}$  for  $\tau_2 = 300$  ps
- Improved P sensitivity at low P for longer  $\tau_2$



## Time-mean temperature/pressure results (MEG)



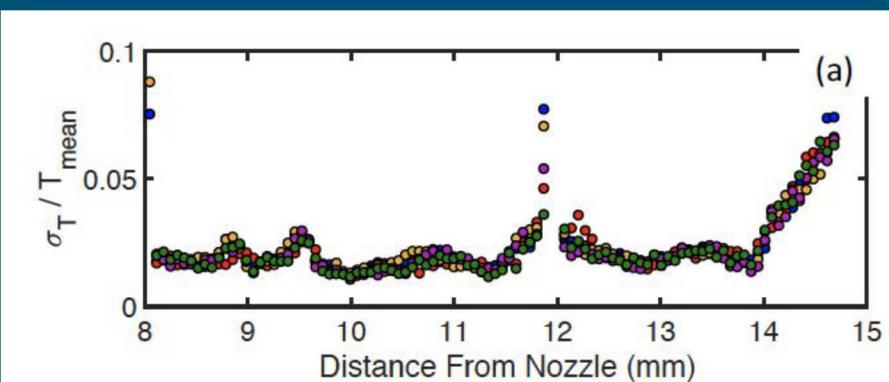
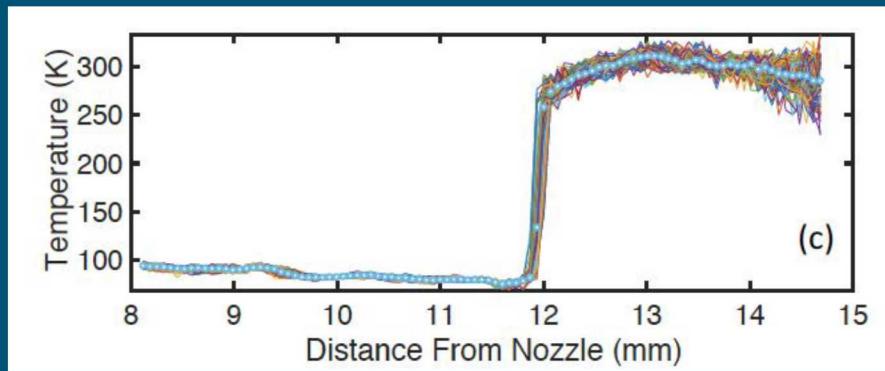
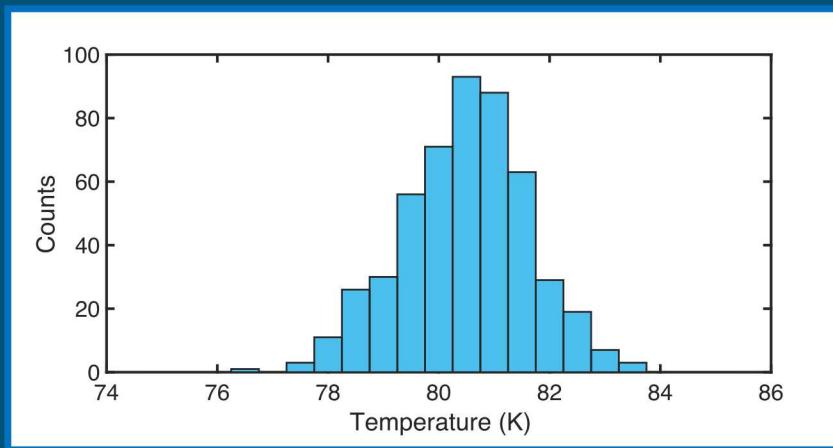
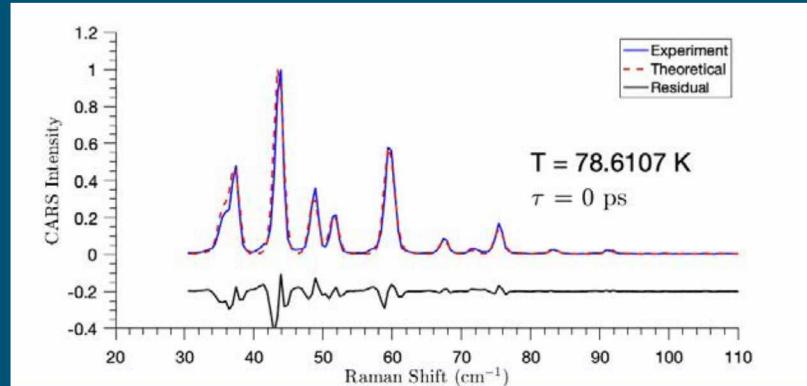
- Profiles spliced together from 4 different 6.7-mm line images
- Each image averaged for 50 laser shots
- Pressure data reported for  $\tau = 300$  ps probe delay
- Dynamic range across the shock captured using two images with different filter settings
- Reduced sensitivity at lower pressures  $\rightarrow$  need delays in excess of 1 ns.
- Poor signal at  $P > 1.2$  atm  $\rightarrow$  need delays of 100 ps or less
- Near-jet temperature consistent with sonic nozzle exit
- T/P across shock consistent with  $M = 3.8$



Pressures consistently lower than isentropic predictions!

## Single-laser-shot precision: Temperature

- Signal-to-noise and measurement precision are very good for thermometry at  $\tau = 0$
- $\sigma_T/T$  evaluated within steady barrel-shock region upstream of Mach disk along jet centerline
- $\sigma_T/T$  is 1–2% upstream of Mach disk
- This high precision persists downstream of Mach disk
- Shock front appears to be resolved within 130–200  $\mu\text{m}$  (1–3 data pts)

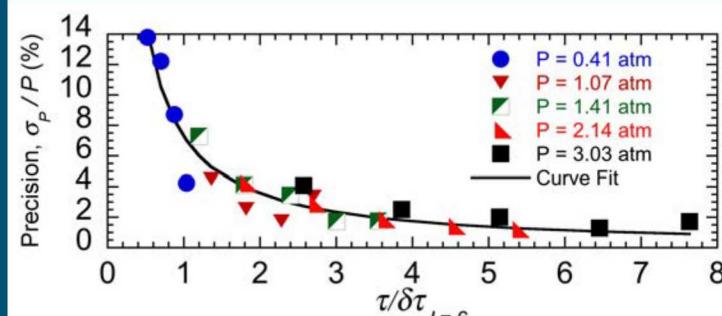


## Single-laser-shot precision: Pressure

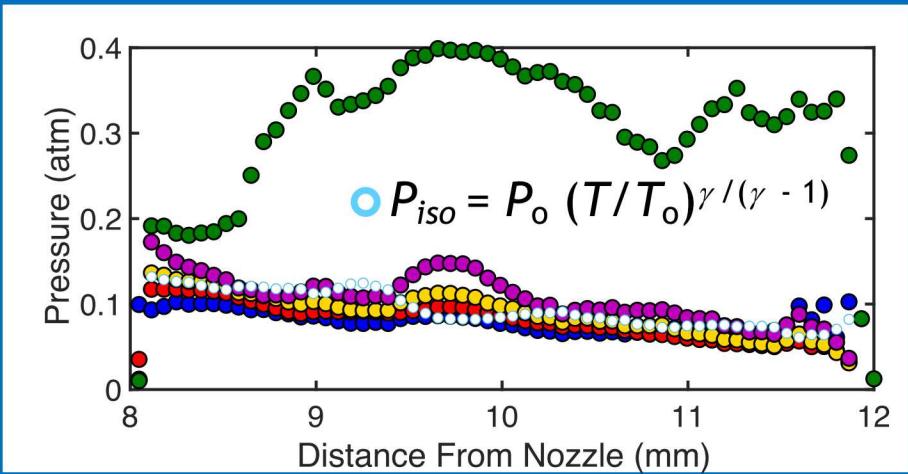
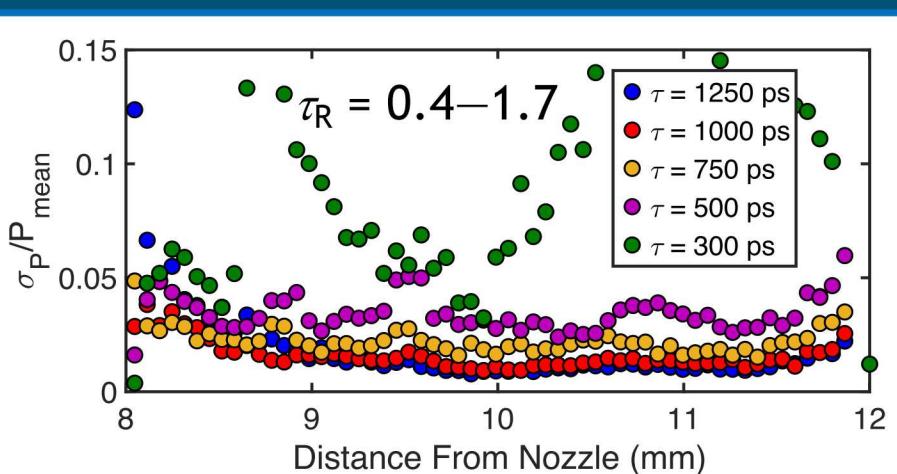
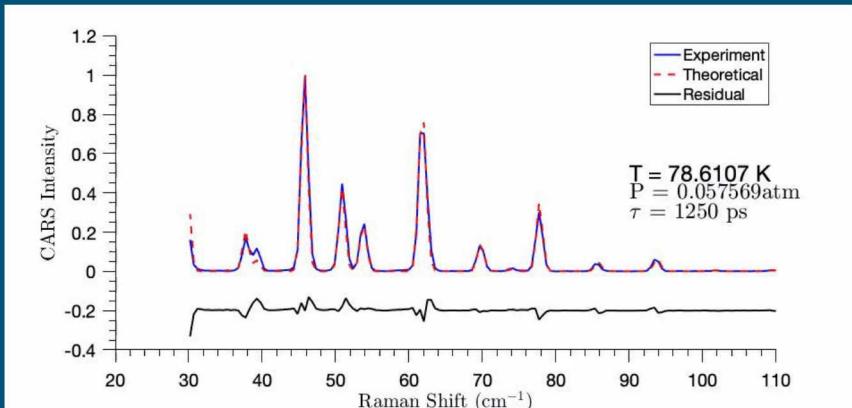
- Tradeoff between SNR and sensitivity with increasing probe delay
- “Raman lifetime”

$$\tau_R = (P \pi C \Gamma)^{-1}$$

- Room-temperature data suggest  $\tau \sim 2.5\text{--}3 \tau_R$  for optimal precision
- sP/P optimized at 1-3% at  $\tau \sim 1\text{--}1.7 \tau_R$  in low (T,P) region of jet
  - $T = 75\text{--}100 \text{ K}$ ,  $P = 50\text{--}75 \text{ Torr}$



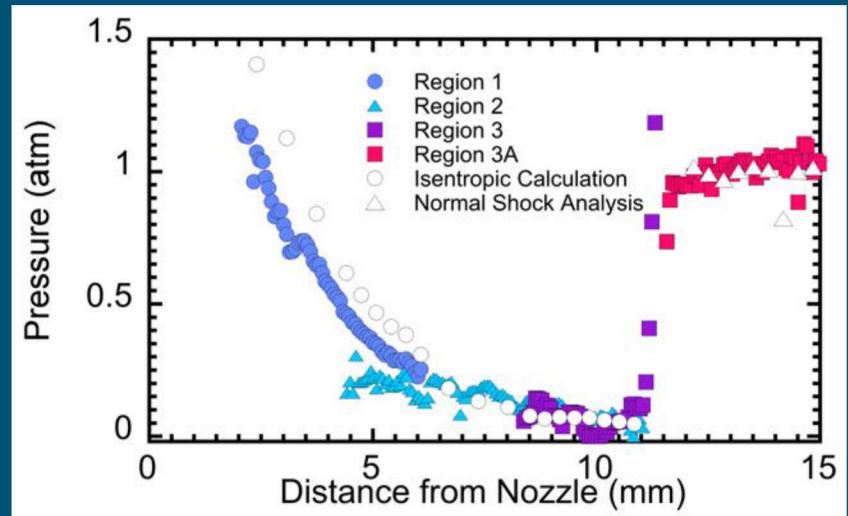
Kearney and Danehy, *Opt. Lett.* (2015)



## Low-temperature Raman Linewidths (motivation)



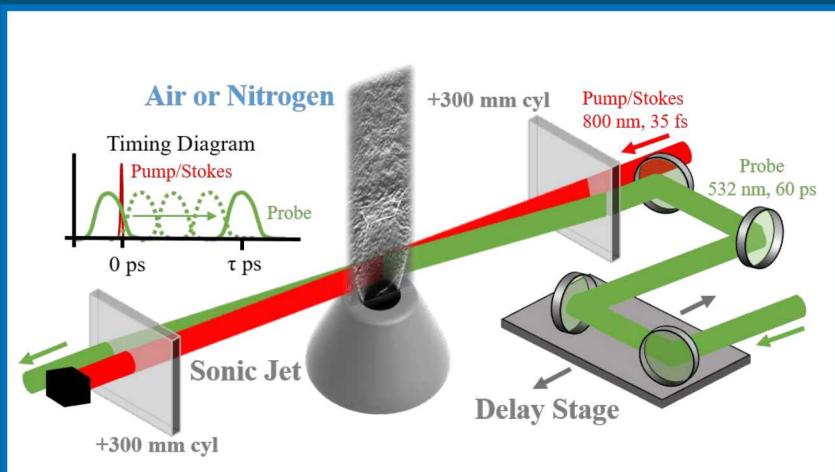
- The Modified Exponential Gap (MEG) model has been used to compute Raman linewidths
- Developed using *Q*-branch linewidth measurements for  $T = 292\text{--}2200\text{ K}$
- Extrapolation to low-temperatures is precarious
- Different line-broadening mechanisms
  - Isotropic *Q* branch
  - Anisotropic rotational transitions
- CARS pressure measurements fall below isentropic predictions based on measured  $T$  in the near field



### Solution

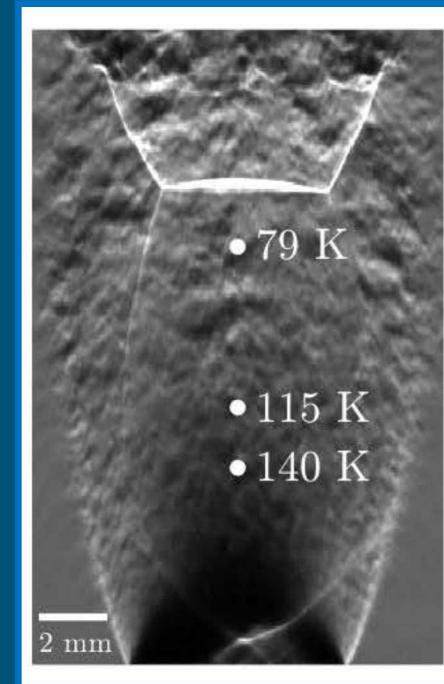
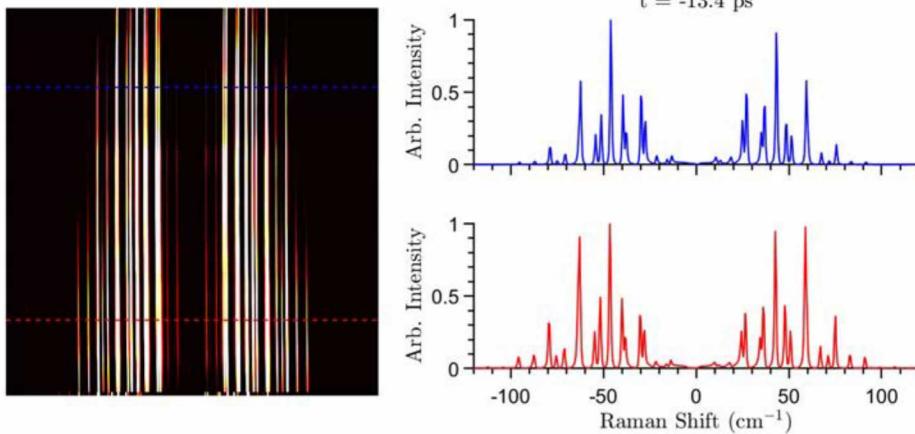
- Use (collision-free) CARS- measured temperatures on jet centerline
- Compute  $P_{iso} = P_0 (T/T_0)^{\gamma/(\gamma - 1)}$
- Measure the lifetime,  $\tau_{CARS,J} = \tau_R/2$ , via probe delay scans
- Compute  $T$ - and  $J$ -dependent linewidths,  $\Gamma_J = (2\pi c \tau_{CARS,J})^{-1}$

# Low-temperature Raman Linewidths (apparatus and methods)

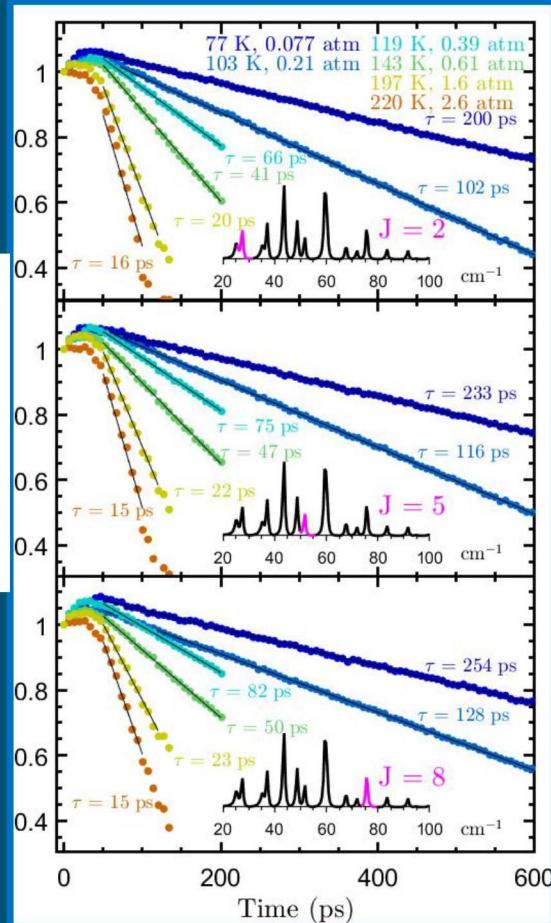


- Probe time-delay mechanically scanned
- Jet centerline measurements within barrel shock region
- Decay of  $\text{N}_2$  examined in both air and pure  $\text{N}_2$

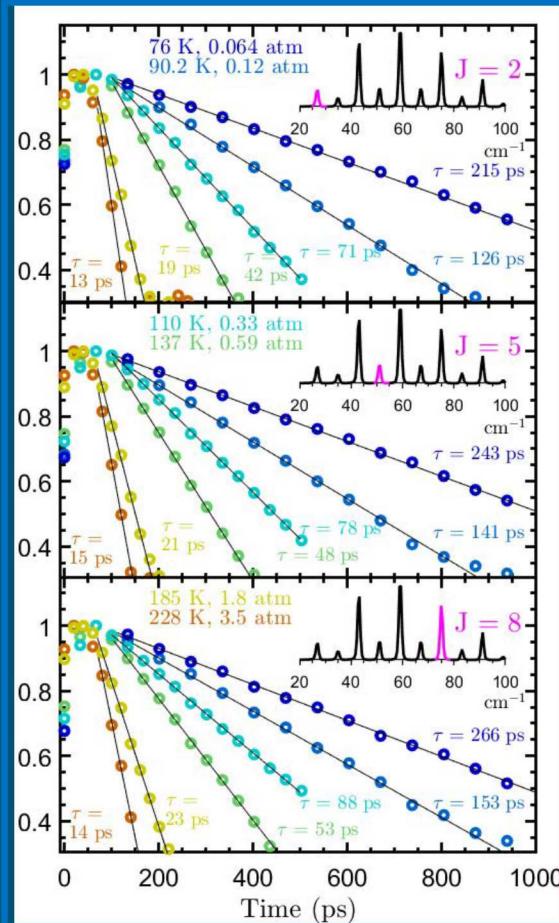
## Probe Time Delay Scan in Air Jet



## N<sub>2</sub> self-broadening



## N<sub>2</sub> broadened in air

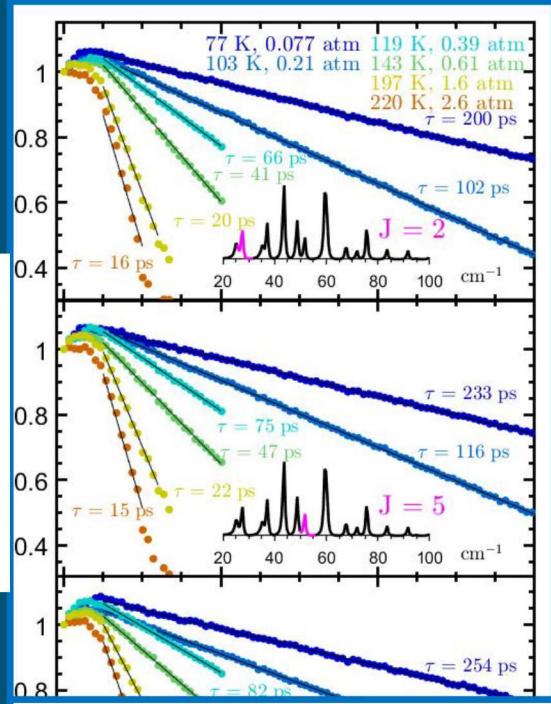


- N<sub>2</sub> Coherence decay shown for T = 77–220 K, P = 0.08–2.6 atm
- Rotational levels up to J = 10 measured at low-T
- Results for O<sub>2</sub> complicated by <sup>3</sup>Σ ground state (not shown here)
- Slower decay times with increasing J

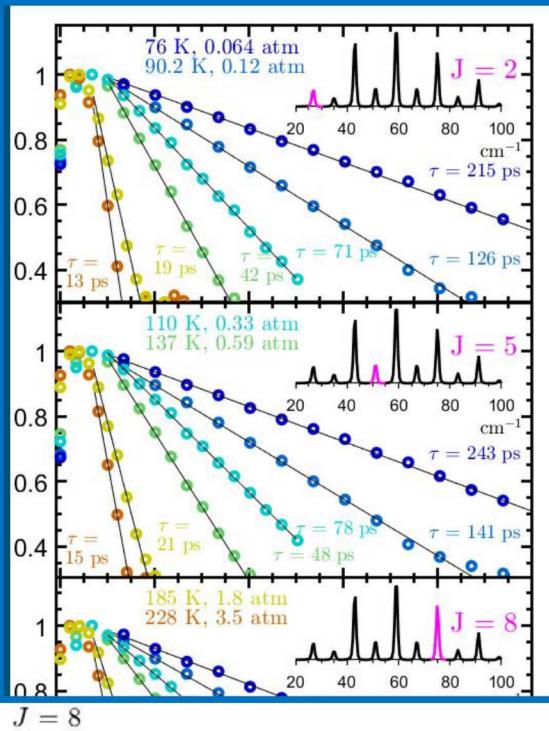
# Low temperature Raman Linewidths (time-domain fits)



## $N_2$ self-broadening



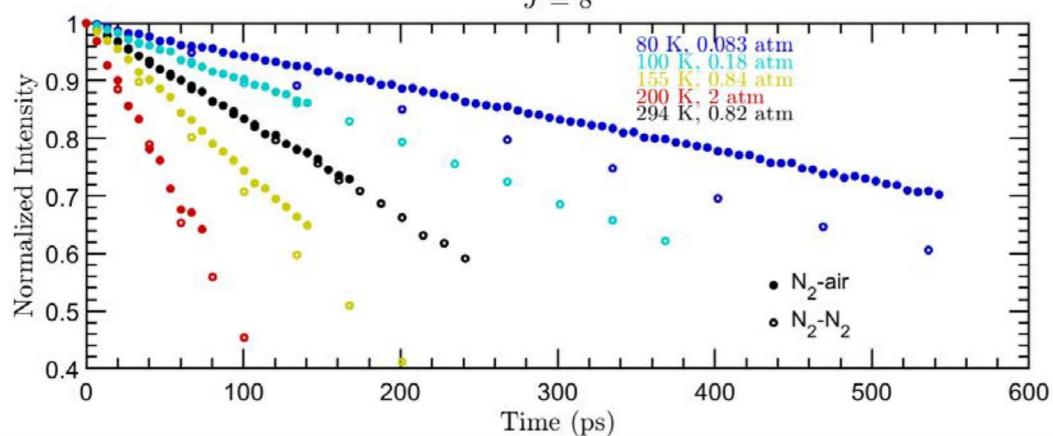
## $N_2$ broadened in air



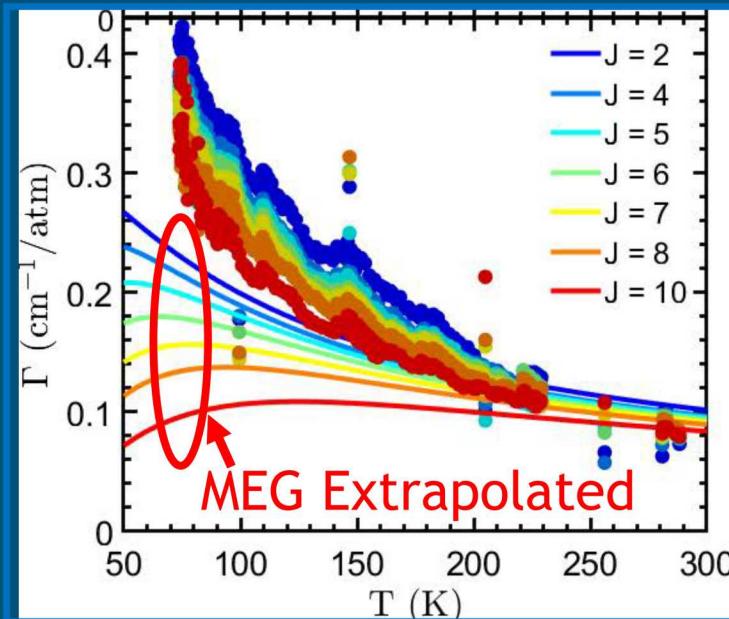
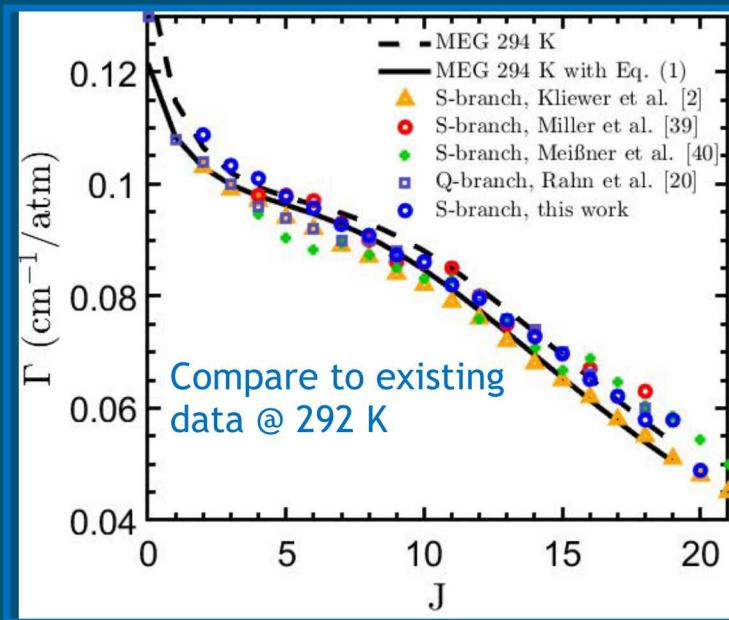
- $N_2$  Coherence decay shown for  $T = 77\text{--}220\text{ K}$ ,  $P = 0.08\text{--}2.6\text{ atm}$
- Rotational levels up to  $J = 10$  measured at low-T
- Results for  $O_2$  complicated by  $^3\Sigma$  ground state (not shown here)

Slower decay times with increasing  $J$

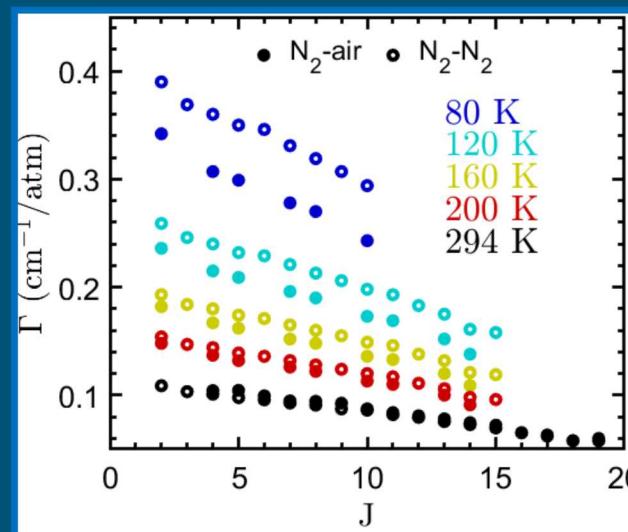
$N_2$  dephases more rapidly in air below  $T = 292\text{ K}$



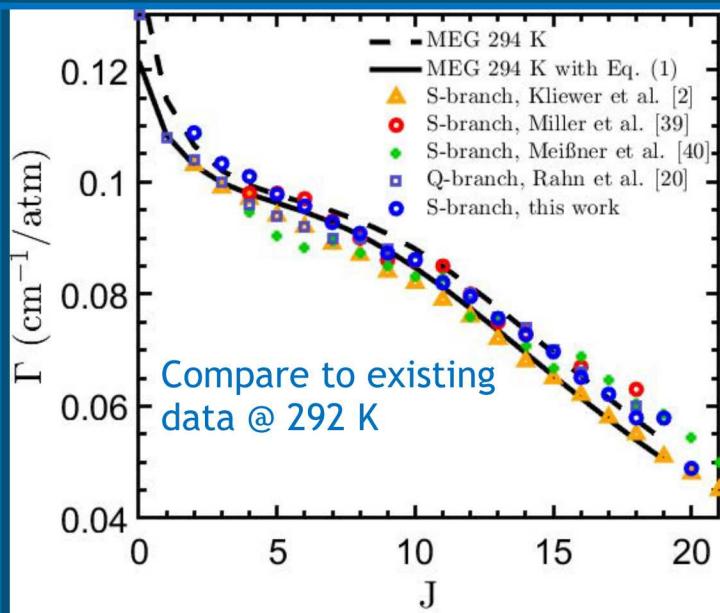
# Low-temperature Raman linewidths: Results I



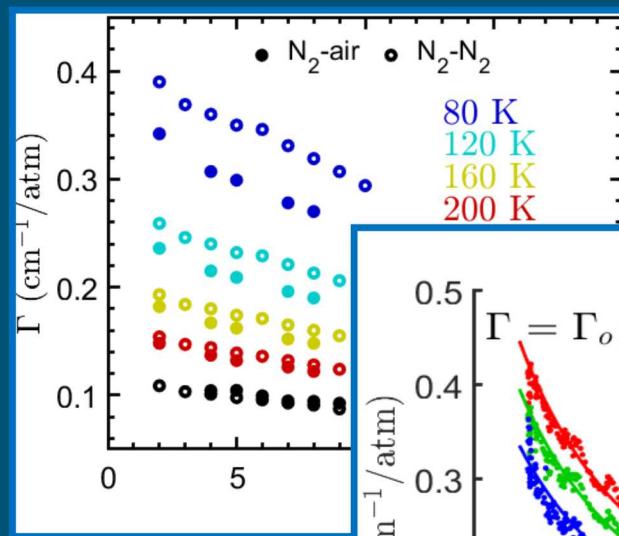
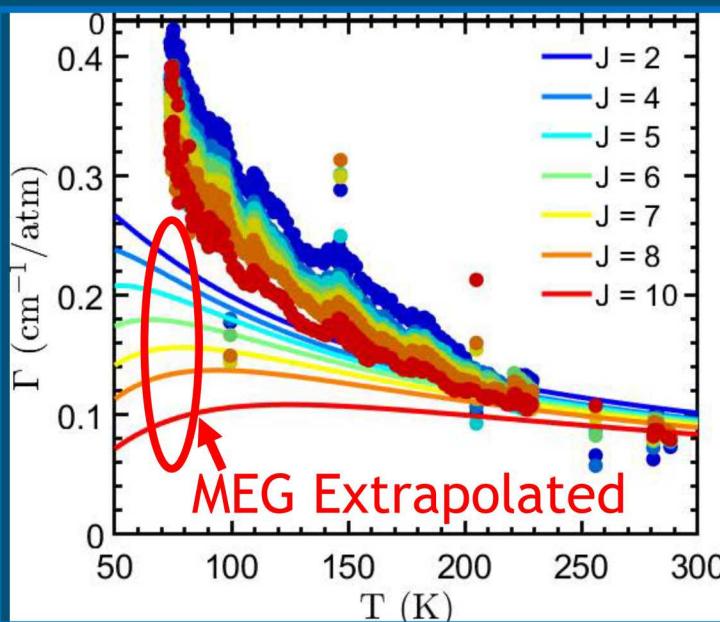
- Current facility provides data consistent with previous measurements at  $T = 292$  K
- Measured linewidths depart significantly from MEG at low  $T$
- Pressure measurements are sensitive to the  $J$  dependence of  $\Gamma$ —not the magnitude



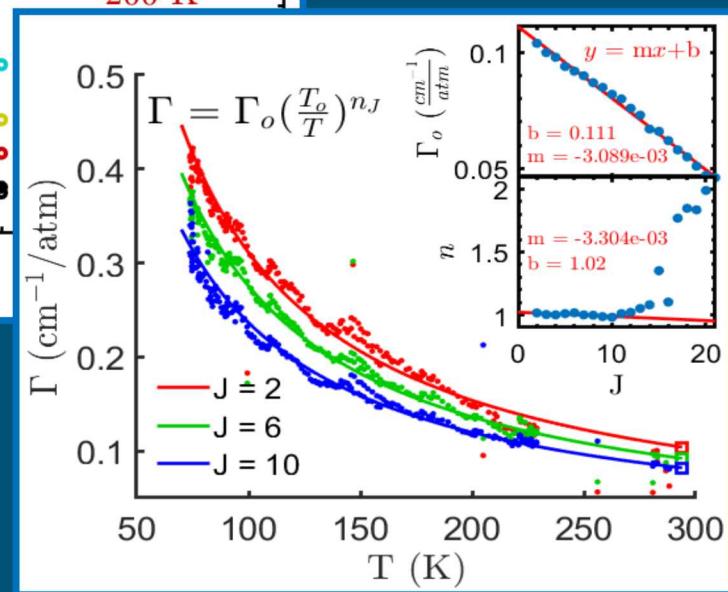
# Low-temperature Raman linewidths: Results I



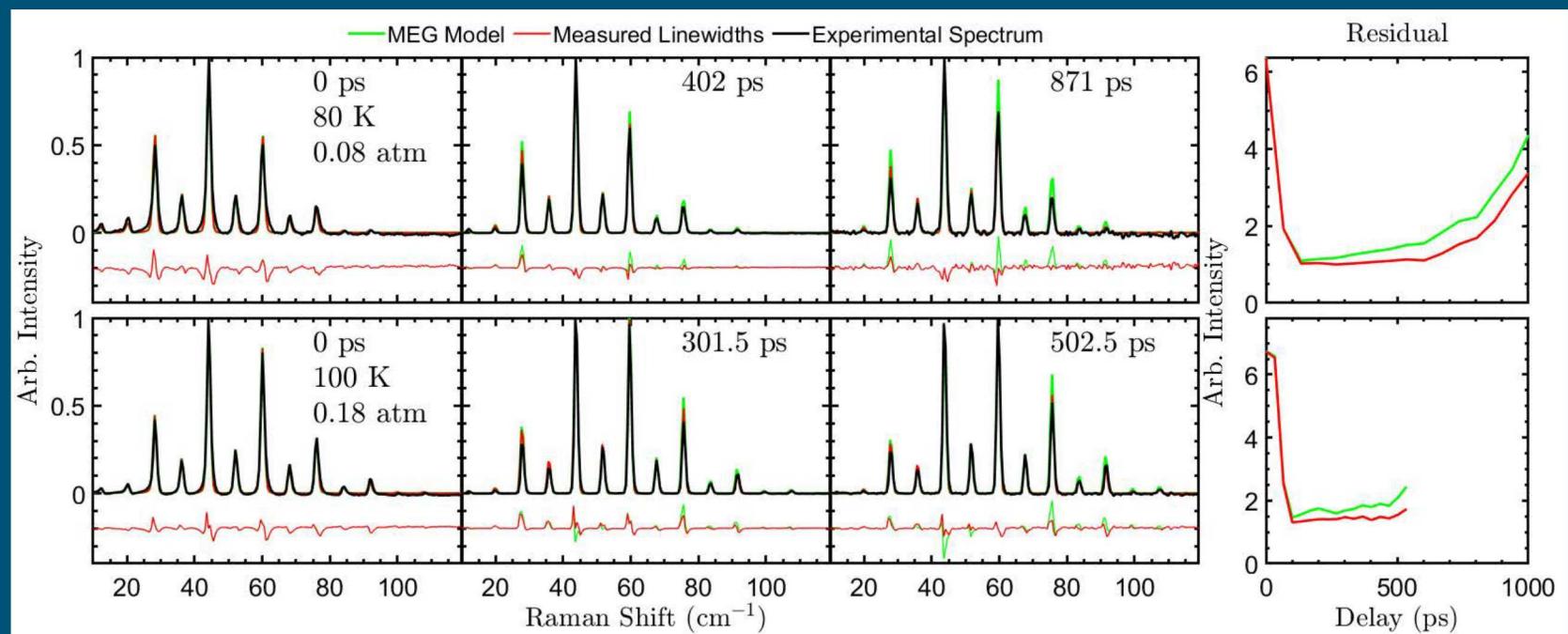
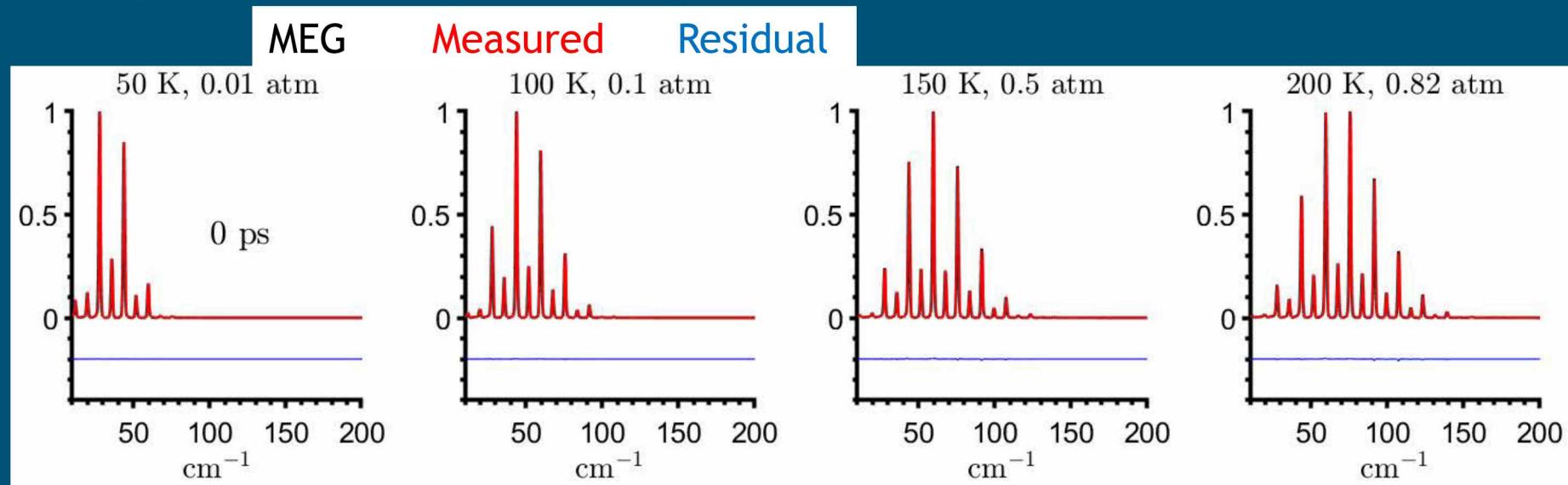
- Current facility provides data consistent with previous measurements at  $T = 292$  K
- Measured linewidths depart significantly from MEG at low T
- Pressure measurements are sensitive to the  $J$  dependence of  $\Gamma$ —not the magnitude



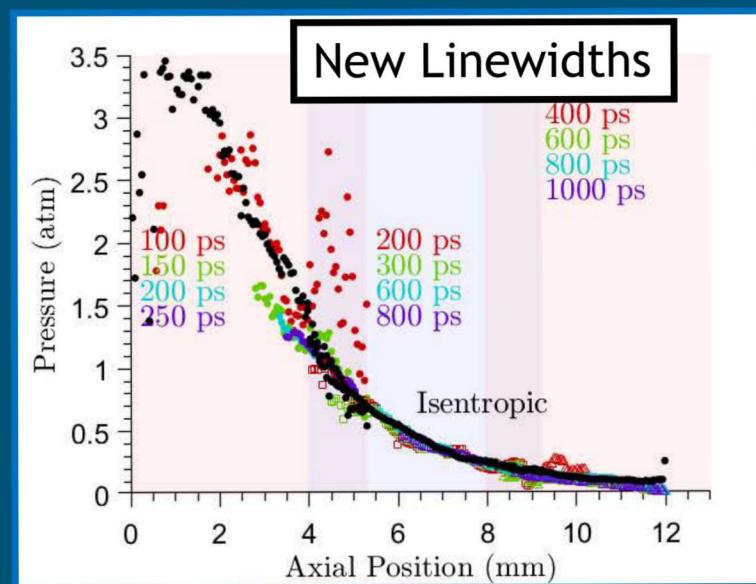
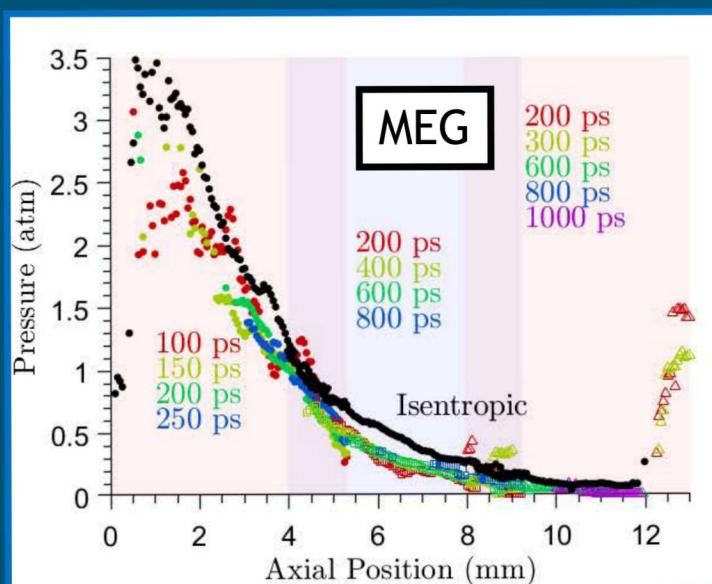
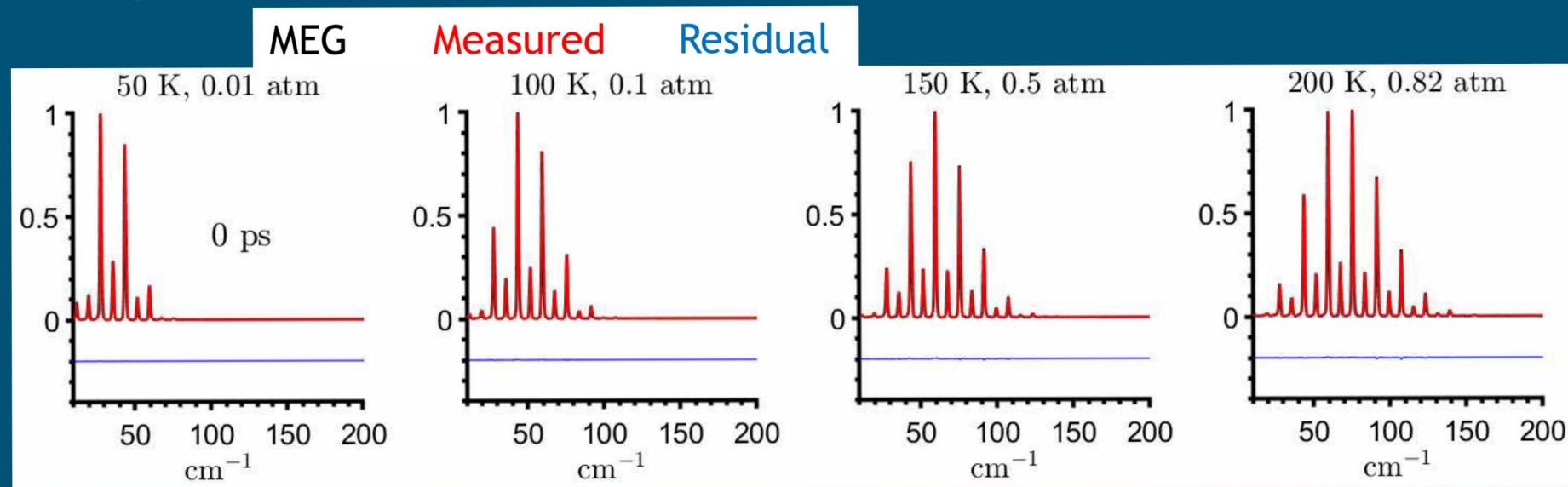
T dependence of  $\Gamma$  correlated by power-law expression



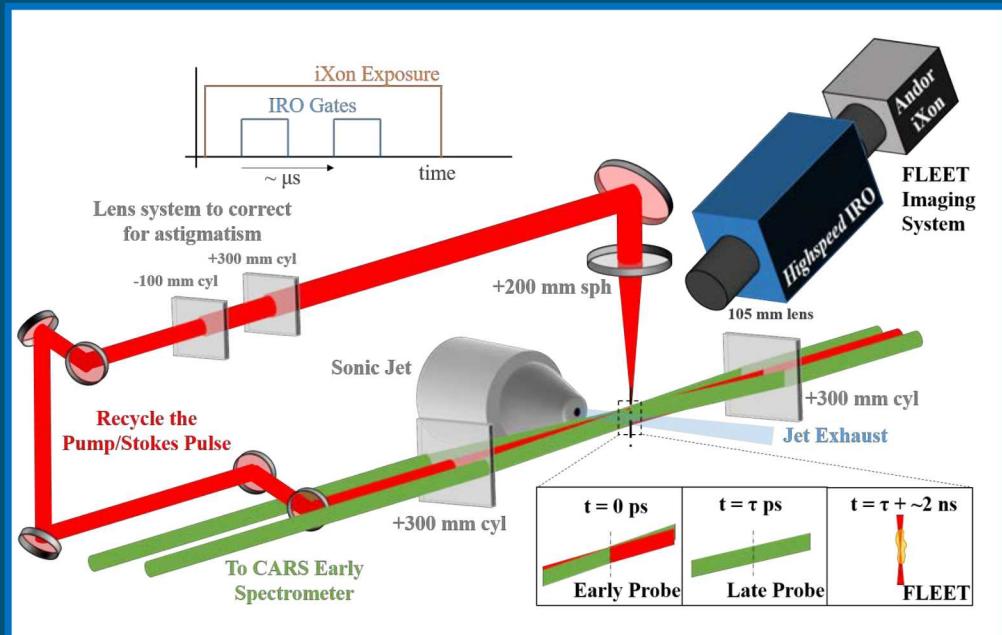
# Impact on CARS spectra and pressure measurements



# Impact on CARS spectra and pressure measurements

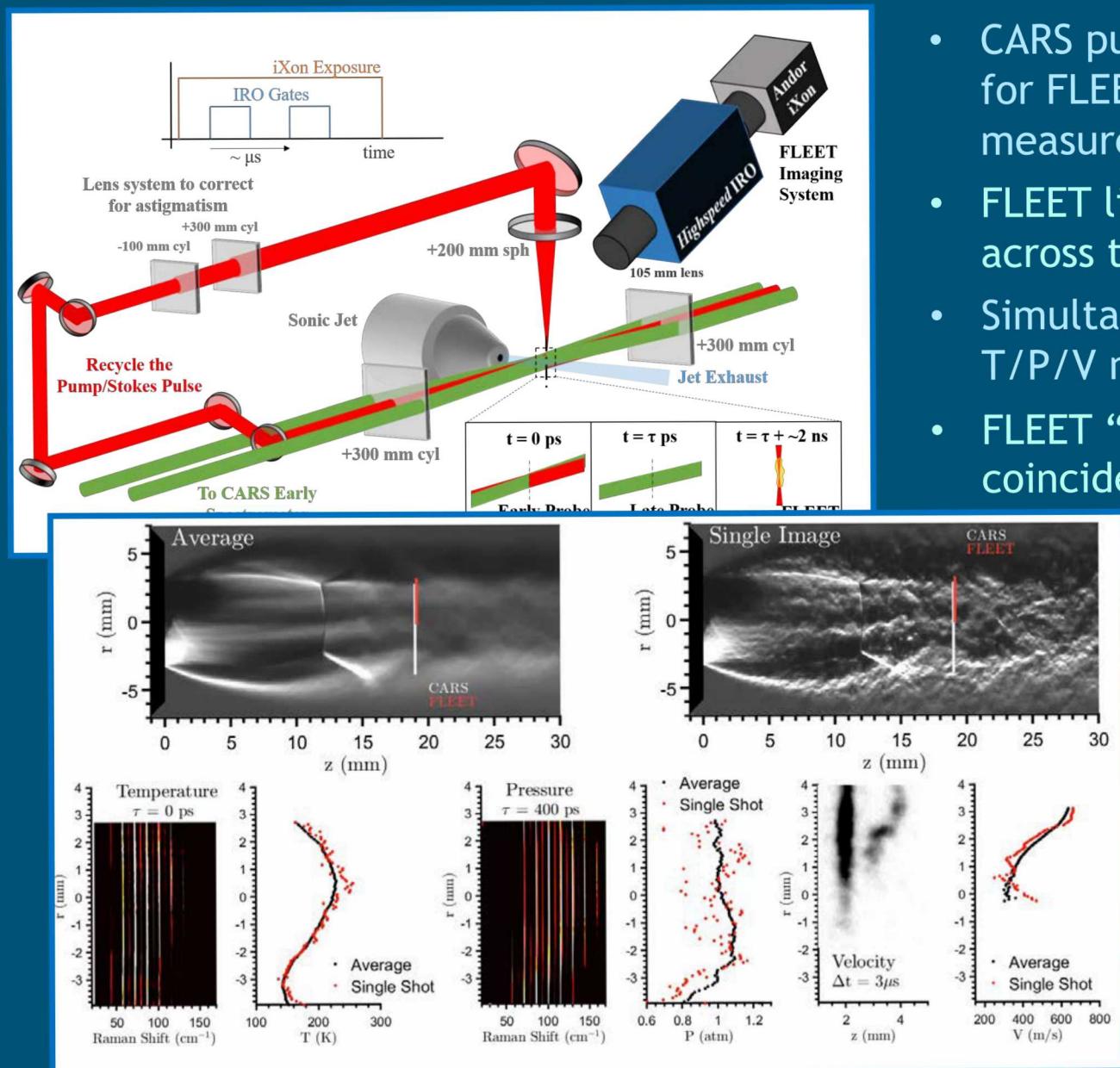


# Addition of FLEET Velocimetry



- CARS pump beam “recycled” for FLEET molecular-tagging measurement
- FLEET line oriented radially across the jet
- Simultaneous CARS/FLEET for T/P/V measurement
- FLEET “ $t = 0$ ” line written coincident with CARS beam crossing

# Addition of FLEET Velocimetry



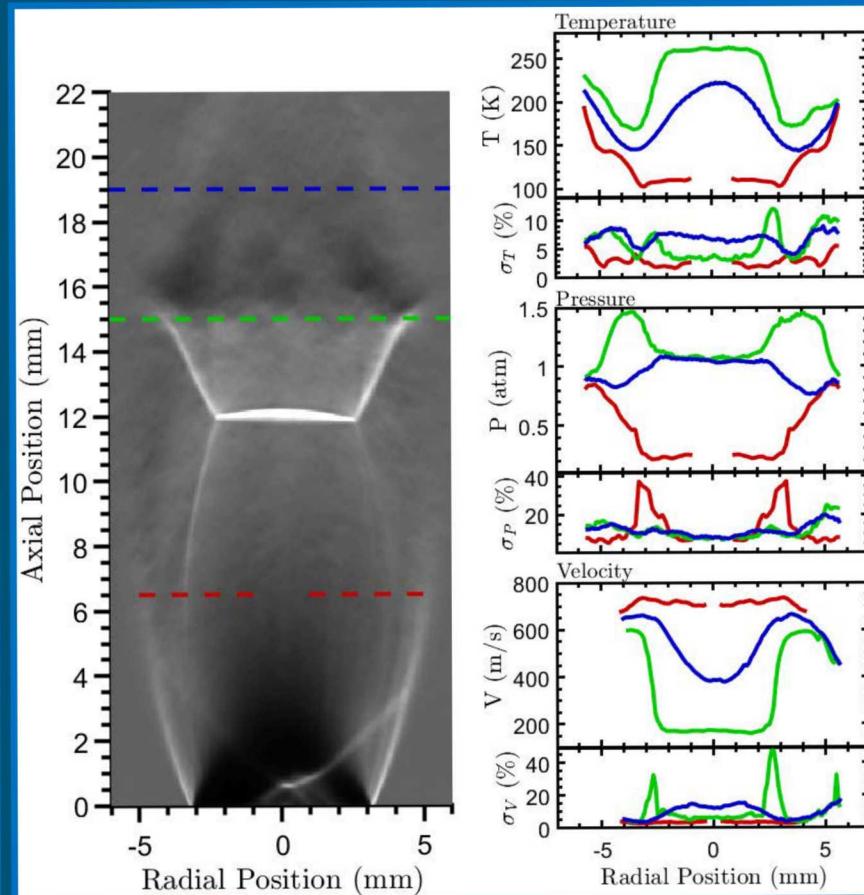
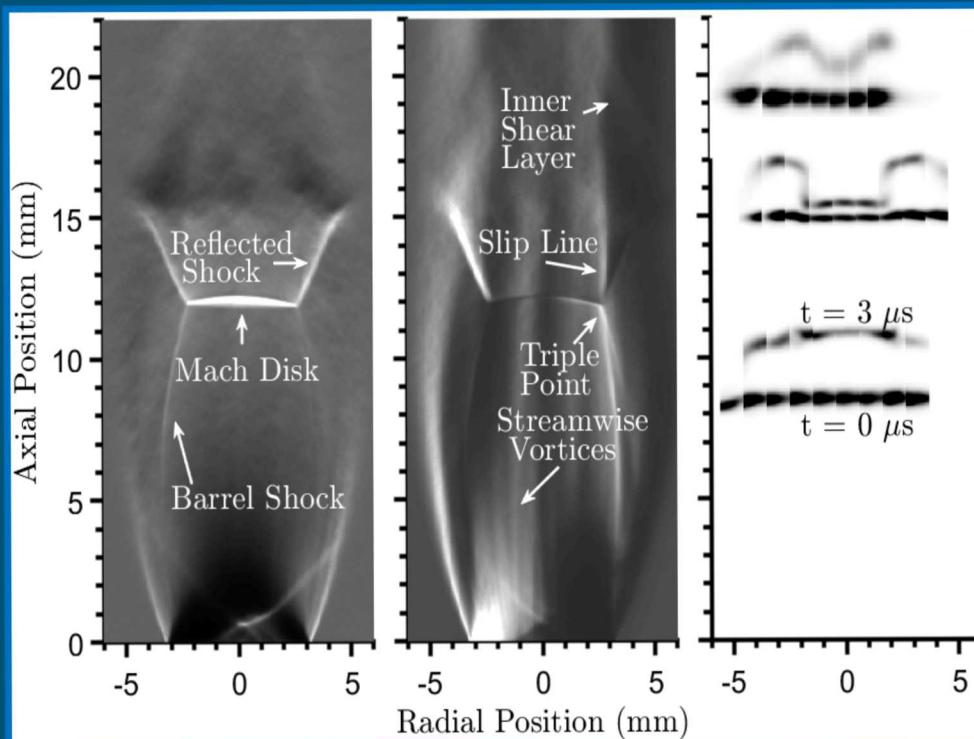
- CARS pump beam “recycled” for FLEET molecular-tagging measurement
- FLEET line oriented radially across the jet
- Simultaneous CARS/FLEET for T/P/V measurement
- FLEET “ $t = 0$ ” line written coincident with CARS beam

Sample instantaneous CARS/FLEET acquisition and processed T/P/V0 results

# Average T/P/V Radial Profiles



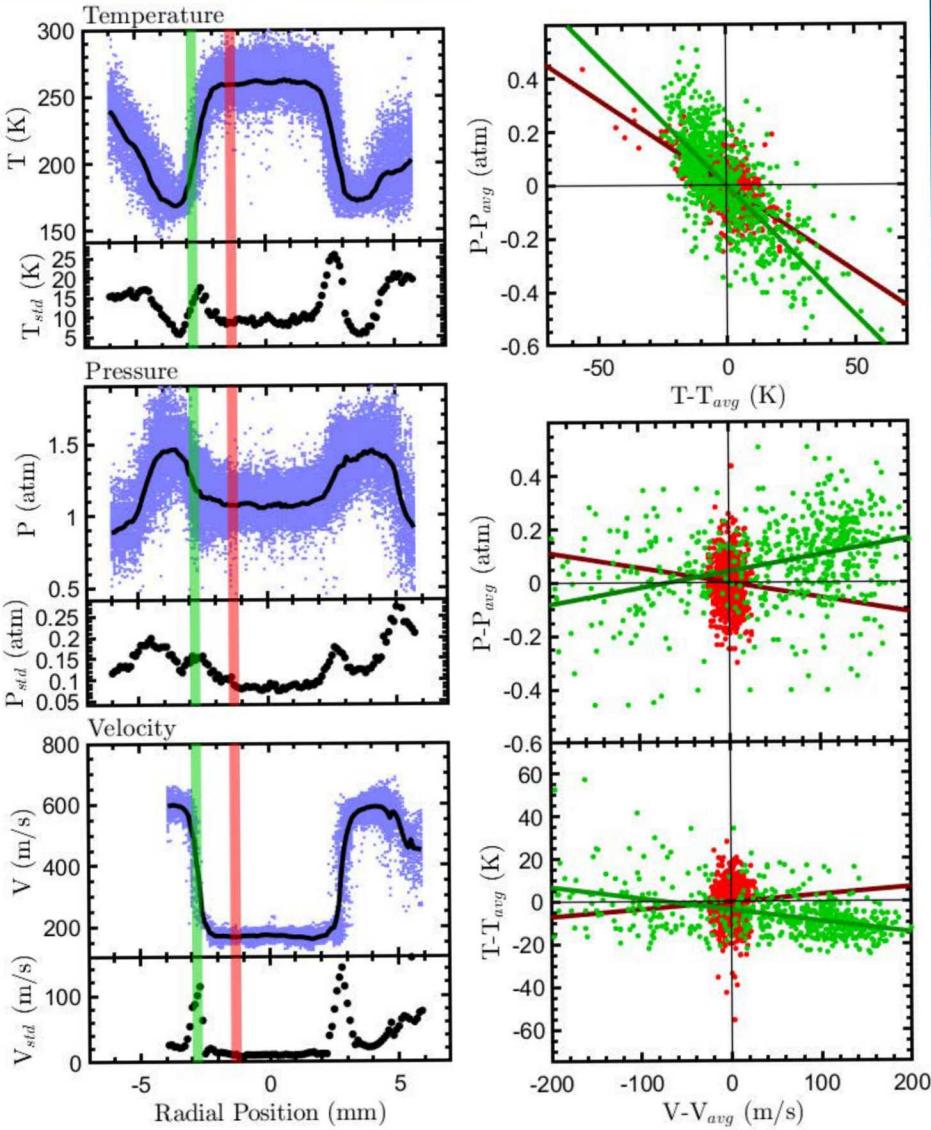
- FLEET velocimetry acquired in multiple segments
- Three axial locations
  - $z = 6.5 \text{ mm}$  (across barrel shock)
  - $z = 15 \text{ mm}$  (across slip line)
  - $z = 19 \text{ mm}$  (turbulent?)



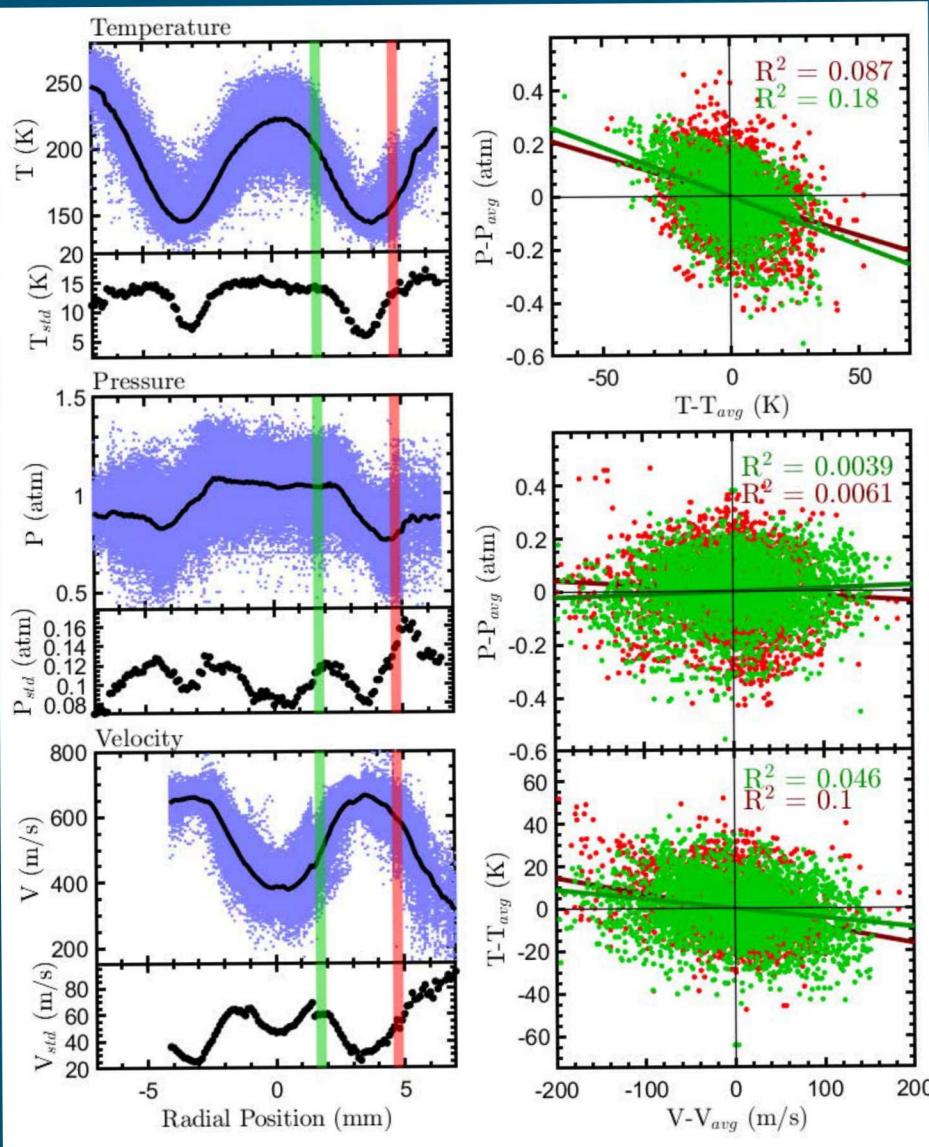
# P,T,V Correlations (400 $\mu\text{m}$ radial domain)



15 mm



19 mm



## Summary and Conclusion

- Hybrid fs/ps rotational CARS can be deployed in compressible flows for simultaneous temperature/pressure measurement
- Signal strengths in a sonic jet are sufficient for 1D line imaging on single laser shot
  - $T = 75\text{--}300 \text{ K}$
  - $P = 50\text{--}800 \text{ Torr}$
- Good dynamic range for thermometry
- Pressure measurements exhibit reduced dynamic range
- Jet measurements exhibit high single-shot precision of 1–3% in both T and P
- Extrapolation of high-temperature MEG linewidths results in underestimated pressure at low T
- New low-temperature S-branch linewidths provided based on isentropic jet assumption
- Combination with FLEET velocimetry demonstrated

