

Linewidth enhancement in quantum dot lasers

Weng Chow
Sandia National Laboratories

An illustration of device modeling:

What calculations are useful for device development

What are the requirements on the theory

International Symposium "Semiconductor Nanophotonics"
Collaborative Research Centre 787, Technische Universität Berlin, November 4th - 5th, 2019

Why quantum dots

- Quantum wells have replaced bulk active regions for virtually all commercial applications
- Quantum-well laser technology (> 20 years old) is reaching fundamental performance limits
- Search for improvement at underlying physics level
- Quantum-dot laser is a strong candidate

Some history

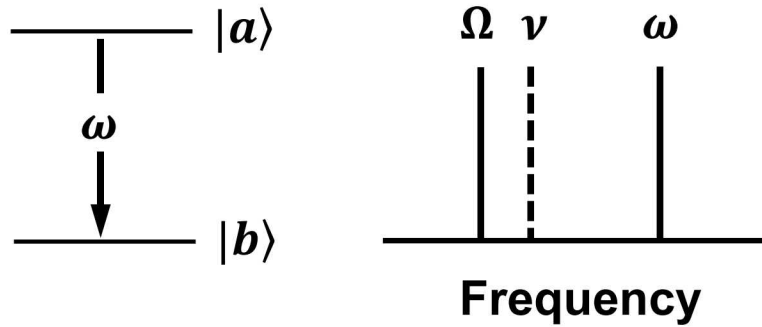
- Improvement via 1-d to 3-d quantum confinement (2-d to 0-d electron density of state) -- proposed 1982
- Demonstrated atomic-like laser emission – mid 1990
- Low threshold, high temperature, defect & optical-feedback tolerances, silicon integration – shown

Why linewidth enhancement factor

- Attention shifting to above-threshold properties
- Laser linewidth, chirp under high-speed modulation, optical feedback sensitivity
- Applications: datacom & telecom, chemical sensing, laser radar (LIDAR)

Laser theory

(e.g. Sargent, Scully and Lamb)



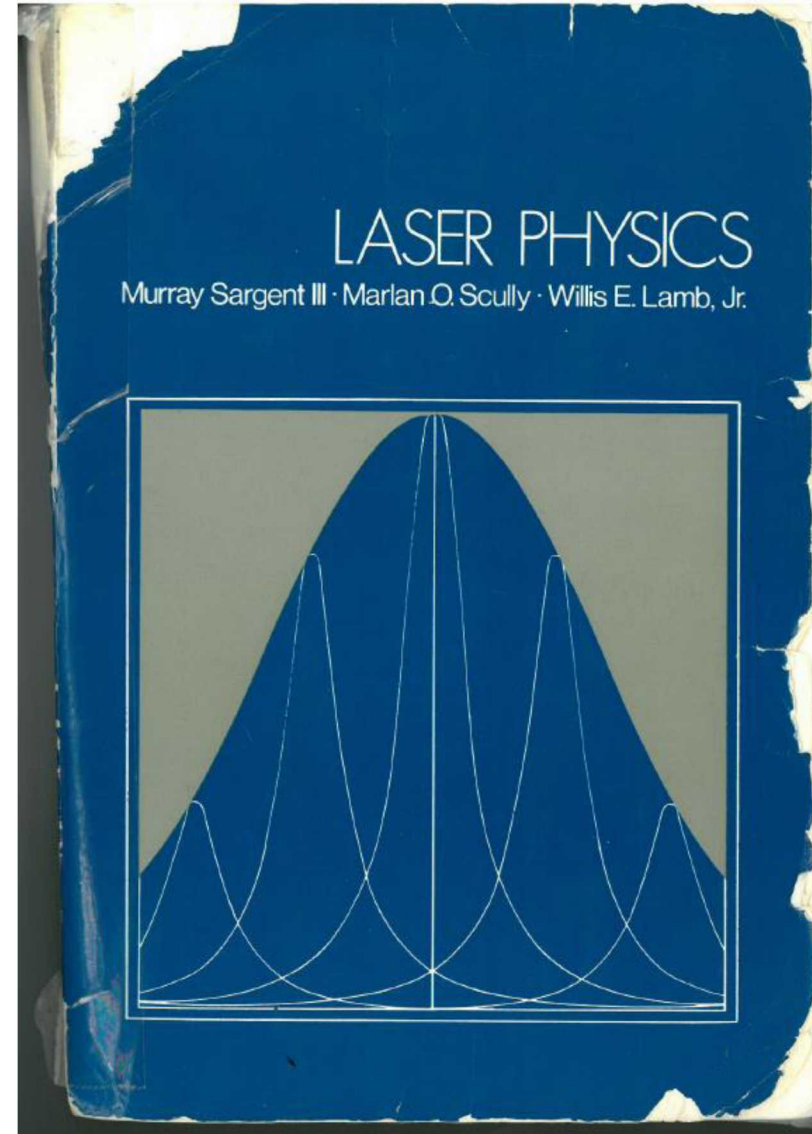
Lasing frequency

$$\nu = \Omega + \frac{(\omega - \Omega)}{\gamma^2 + (\omega - \Omega)^2} [n_a(\omega) - n_b(\omega)]$$

Cavity resonance **Atomic resonance**

Frequency pulling

The diagram shows the equation for the lasing frequency ν . An upward arrow points from the label "Lasing frequency" to ν . A downward arrow points from Ω to the label "Cavity resonance". A downward arrow points from $n_a(\omega) - n_b(\omega)$ to the label "Atomic resonance". A horizontal bracket above the fraction is labeled "Frequency pulling".



Laser theory

(e.g. Sargent, Scully and Lamb)

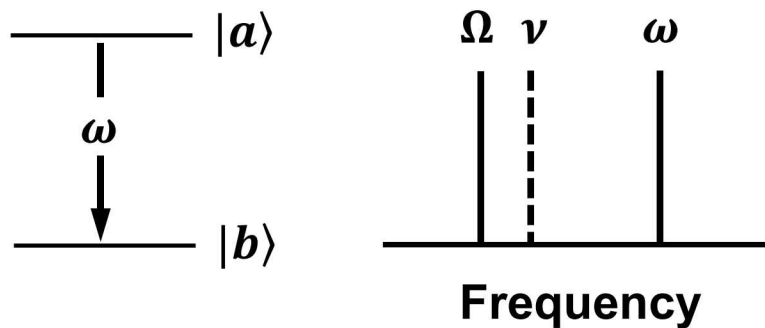


Diagram illustrating the relationship between the lasing frequency, cavity resonance, and atomic resonance, showing frequency pulling.

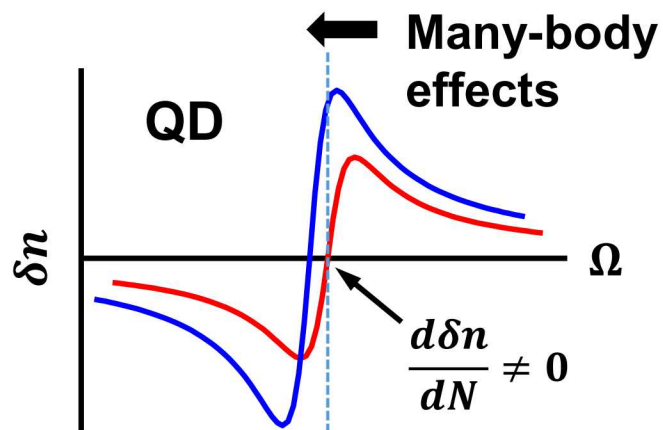
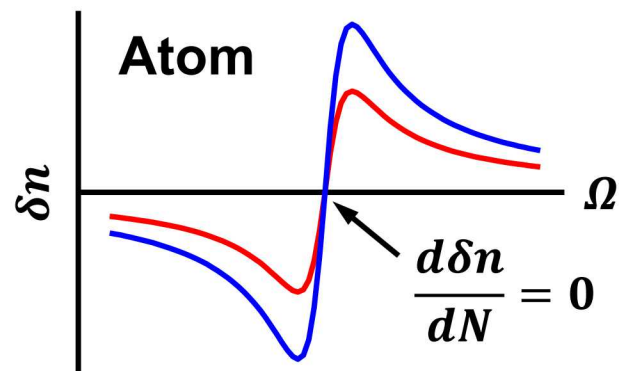
$$\nu = \Omega + \frac{(\omega - \Omega)}{\gamma^2 + (\omega - \Omega)^2} [n_a(\omega) - n_b(\omega)]$$

The equation shows the lasing frequency ν as a function of the cavity resonance Ω and the atomic resonance ω . The term $n_a(\omega) - n_b(\omega)$ represents the atomic polarization. The diagram indicates that the lasing frequency is pulled towards the atomic resonance frequency ω due to the frequency pulling effect.

Refractive index

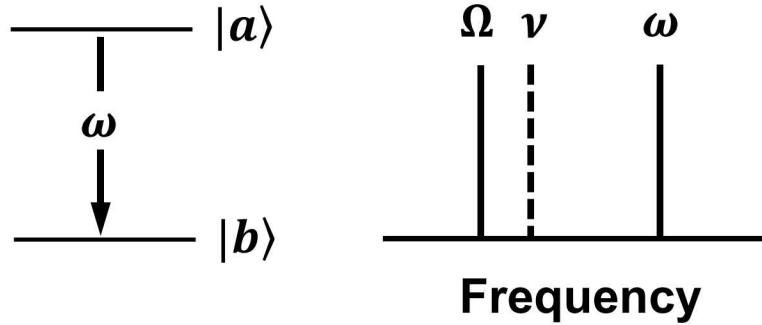
$$\nu = \frac{c}{2L(n + \delta n)} = \Omega \left(1 - \frac{\delta n}{n} \right)$$

Carrier-induced refractive index change



Laser theory

(e.g. Sargent, Scully and Lamb)



Lasing frequency $\uparrow$

$$\nu = \Omega + \frac{(\omega - \Omega)}{\gamma^2 + (\omega - \Omega)^2} [n_a(\omega) - n_b(\omega)]$$

$\downarrow$ **Cavity resonance**

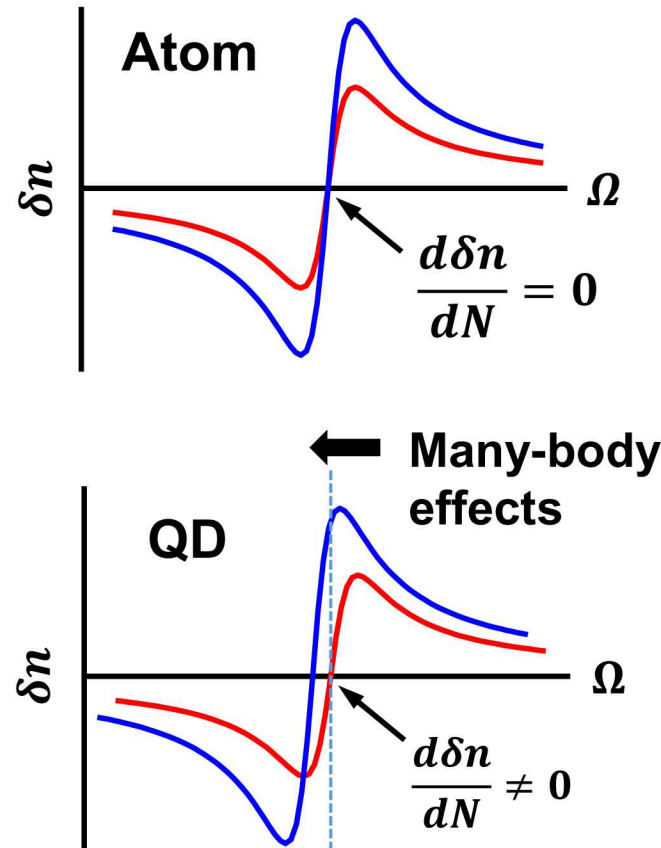
Frequency pulling $\longleftarrow$

$\downarrow$ **Atomic resonance**

Refractive index

$$\nu = \frac{c}{2L(n + \delta n)} = \Omega \left(1 - \frac{\delta n}{n} \right)$$

$\downarrow$
Carrier-induced refractive index change



Linewidth enhancement factor

$$\alpha_H = -K \frac{d(\delta n)}{dN_e} \left(\frac{dg}{dN_e} \right)^{-1}$$

Laser linewidth

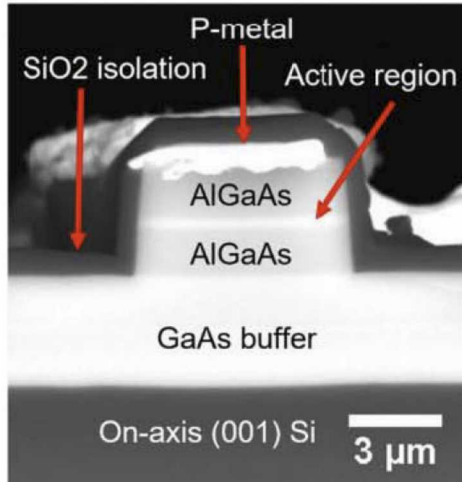
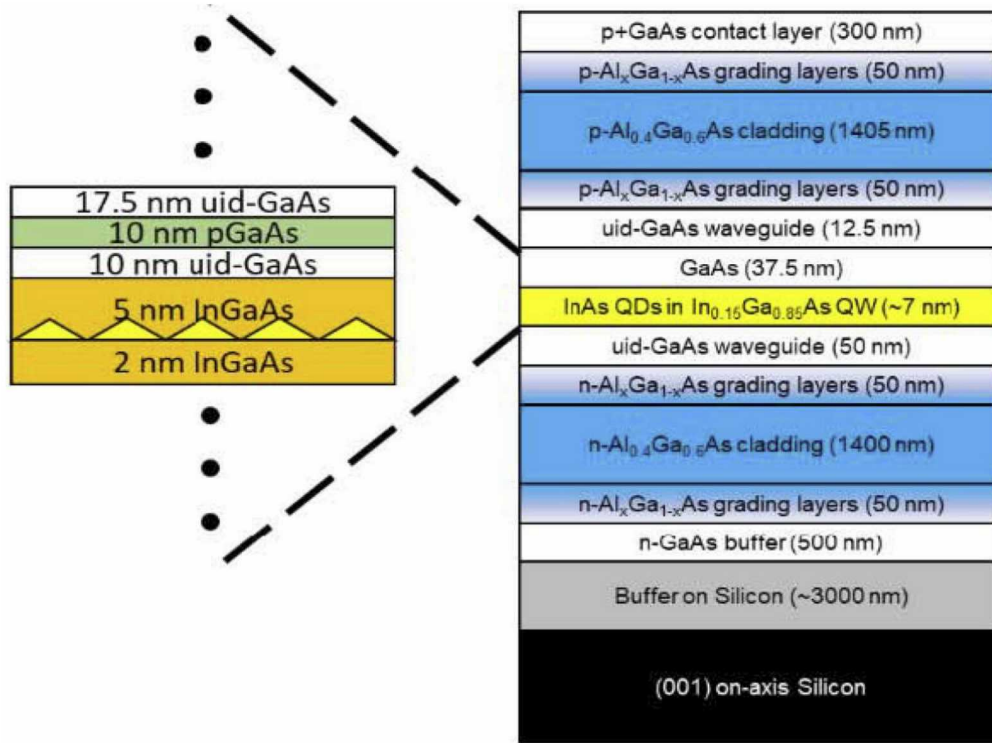
$$\Delta\nu = \Delta\nu'_{ST} (1 + \alpha_H^2)$$

Feedback instability

$$f_{crit} = \xi \frac{1 + \alpha_H^2}{\alpha_H^4}$$

Chirp during high-speed operation

Typical gain and α_H for quantum dot laser



8nm $\text{In}_{0.15}\text{Ga}_{0.85}\text{As}$ QW

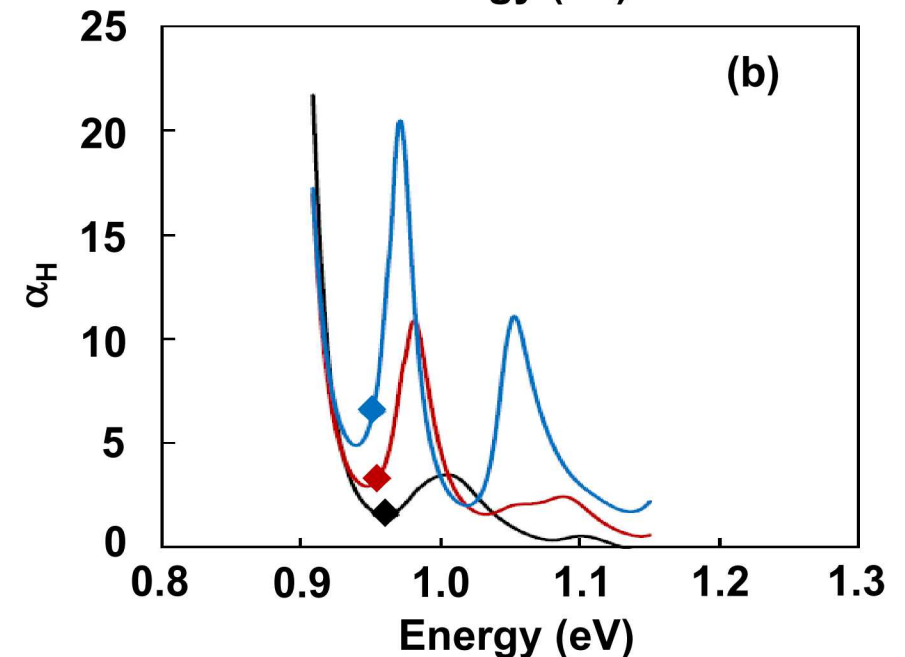
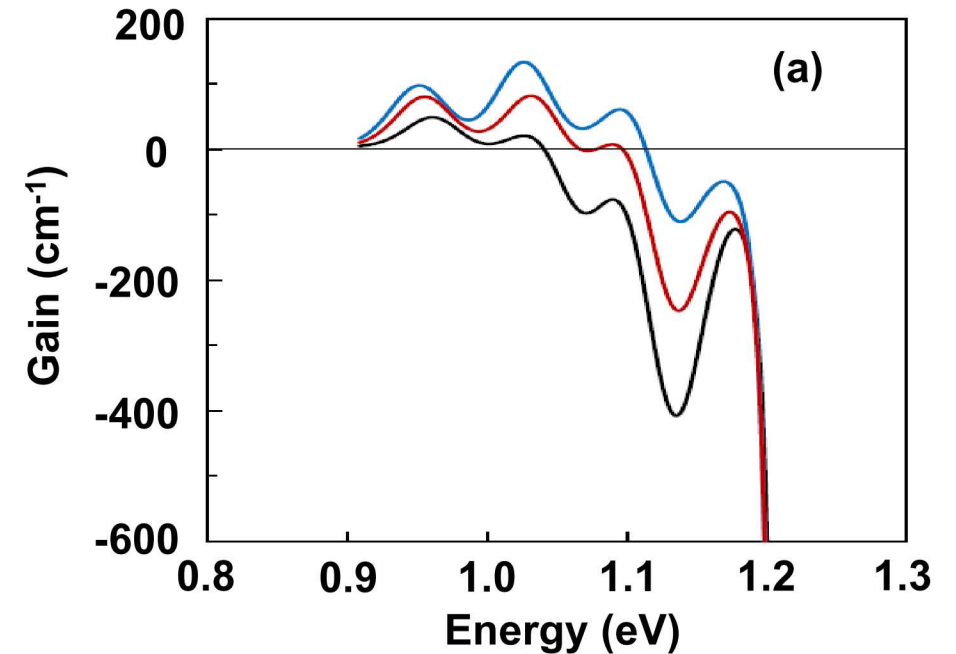
$5 \times 10^{10} \text{cm}^{-2}$ InAs QDs

GaAs barriers

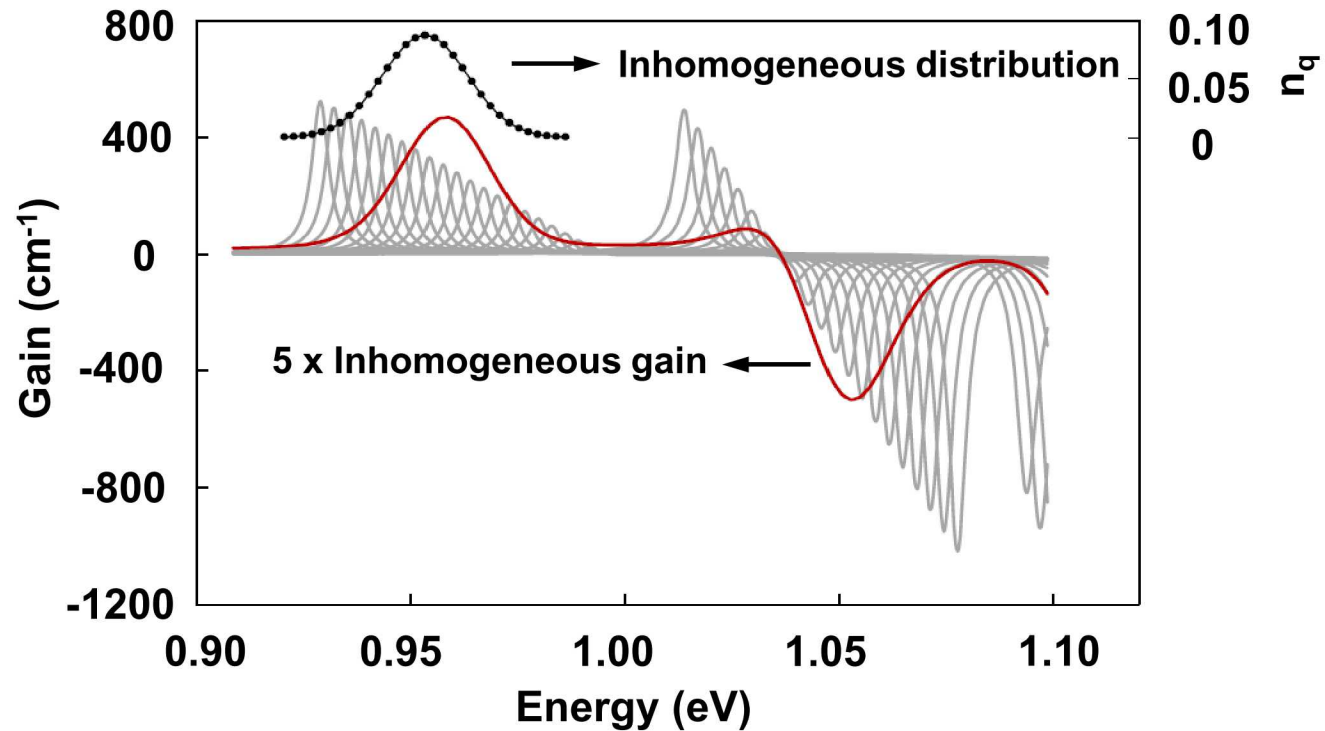
$\Delta_{\text{inh}} = 20 \text{ meV} \rightarrow \Delta_{\text{sp}} = 48 \text{ meV}$

Undoped, $N_e = 3 \times, 5 \times, 7 \times 10^{11} \text{cm}^{-2}$

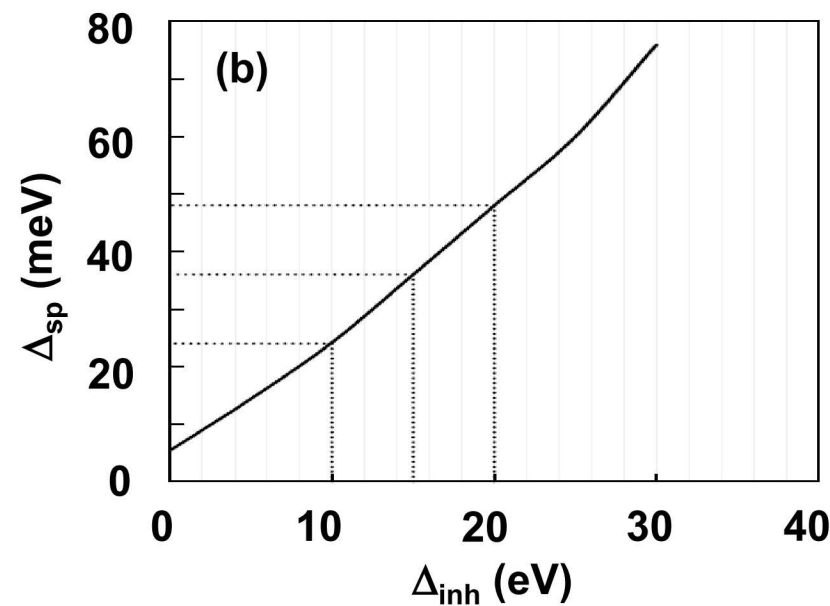
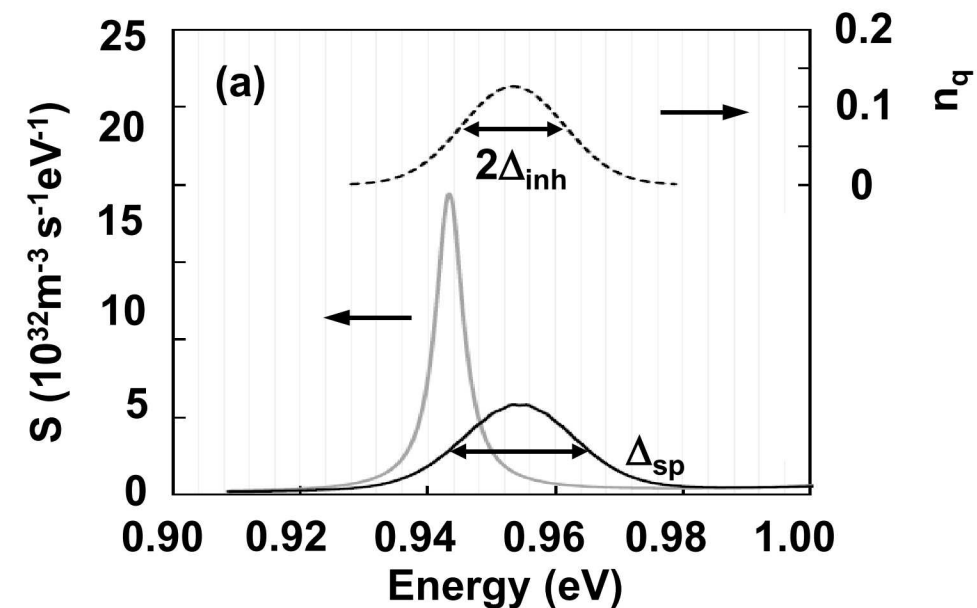
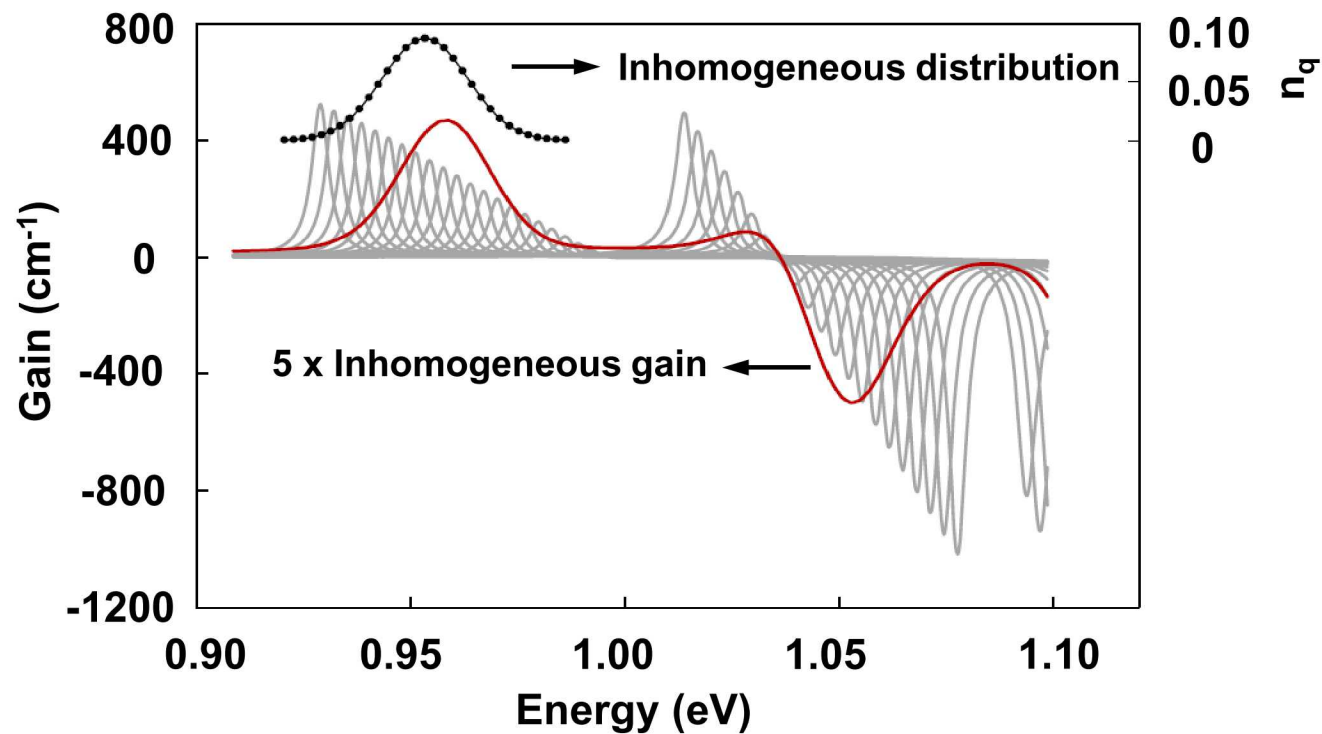
APL 107, 1171106 (2015)



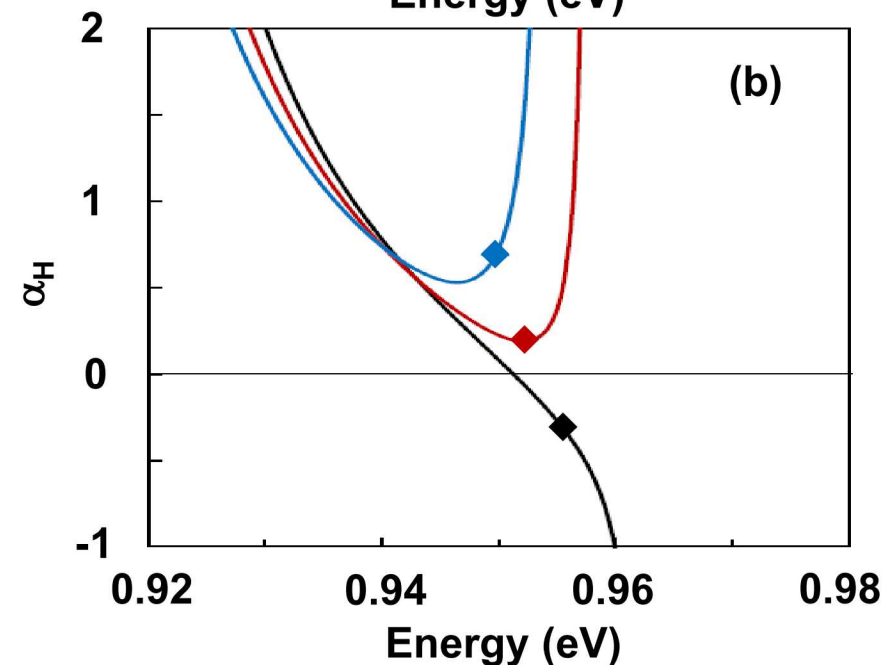
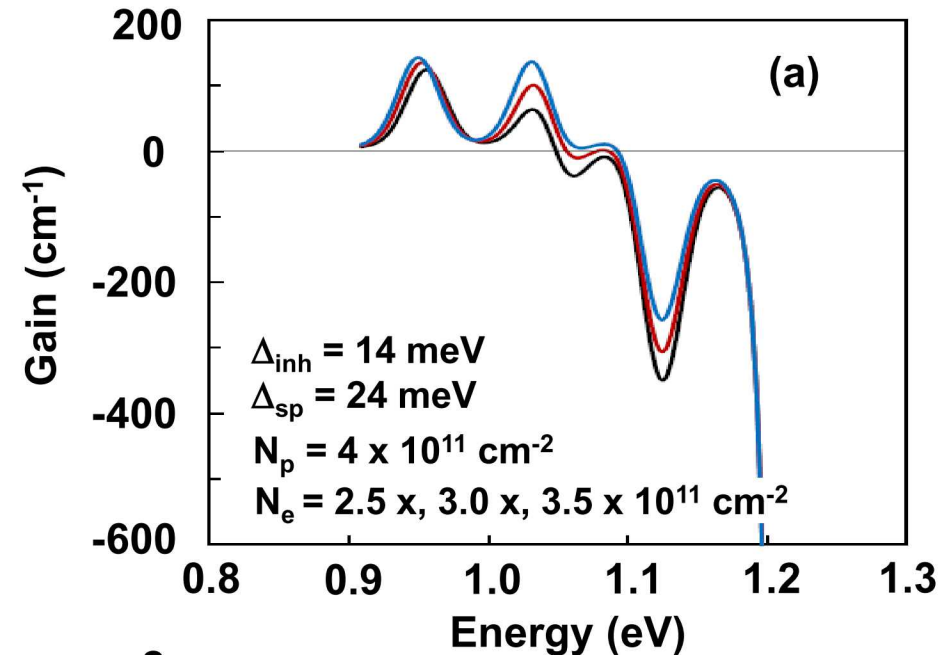
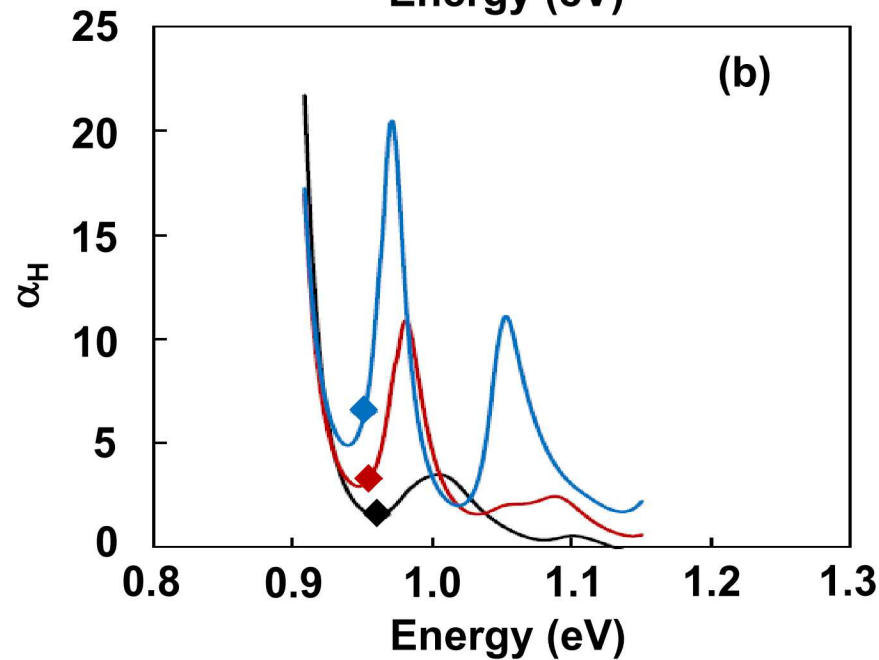
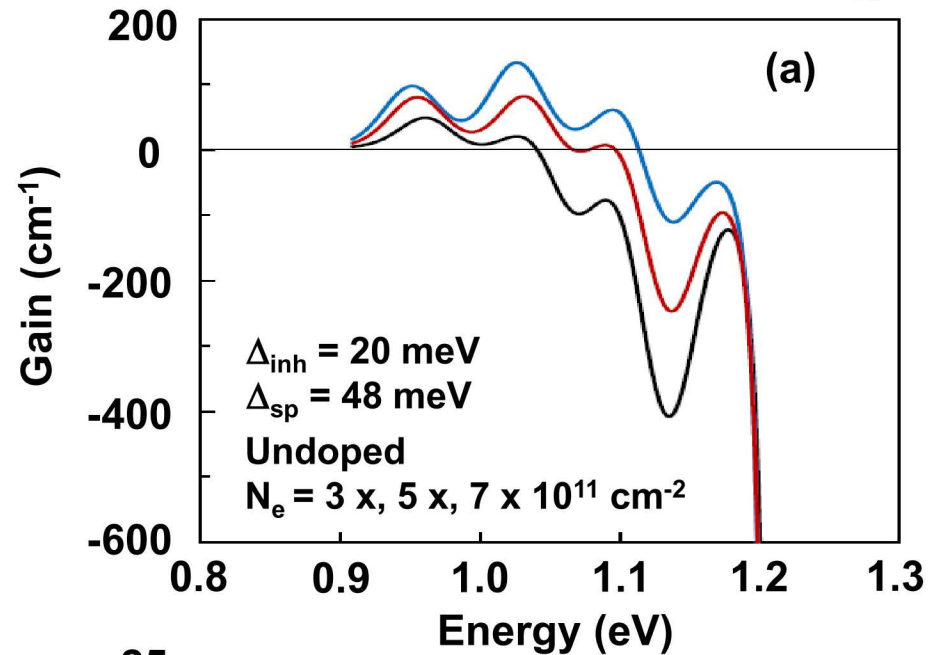
Inhomogeneously broadened $\uparrow$
 $P_{inh}(\nu) = \sum_q n_q p(\nu, \omega_q)$
 Homogeneously broadened $\uparrow$
 $\downarrow$ Electronic structure
 Inhomogeneous distribution $\frac{1}{\sqrt{2\pi}\Delta_{inh}} \exp\left[-\left(\frac{\omega_q - \omega_0}{\sqrt{2}\Delta_{inh}}\right)^2\right]$
 $\downarrow$ Inhomogeneous width



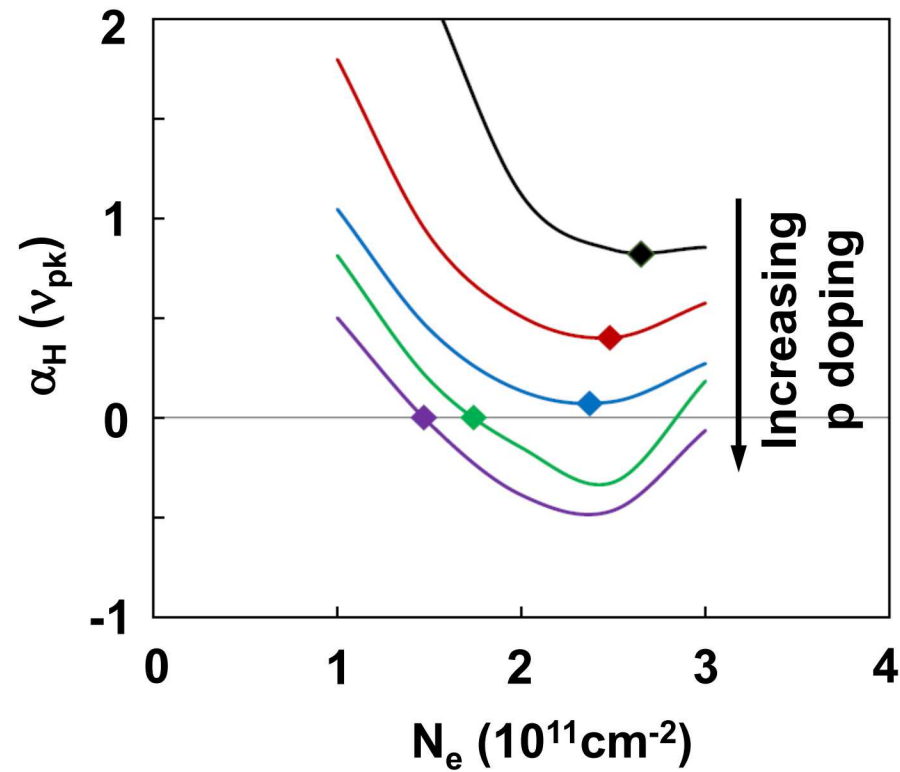
Inhomogeneously broadened $\uparrow$
 $P_{inh}(\nu) = \sum_q n_q p(\nu, \omega_q)$
 Homogeneously broadened $\uparrow$
 $\downarrow$ Electronic structure
 Inhomogeneous distribution $\frac{1}{\sqrt{2\pi}\Delta_{inh}} \exp\left[-\left(\frac{\omega_q - \omega_0}{\sqrt{2}\Delta_{inh}}\right)^2\right]$
 $\downarrow$ Inhomogeneous width



Gain and α_H spectra of quantum dot laser



Linewidth enhancement factor at gain peak for ground-state lasing



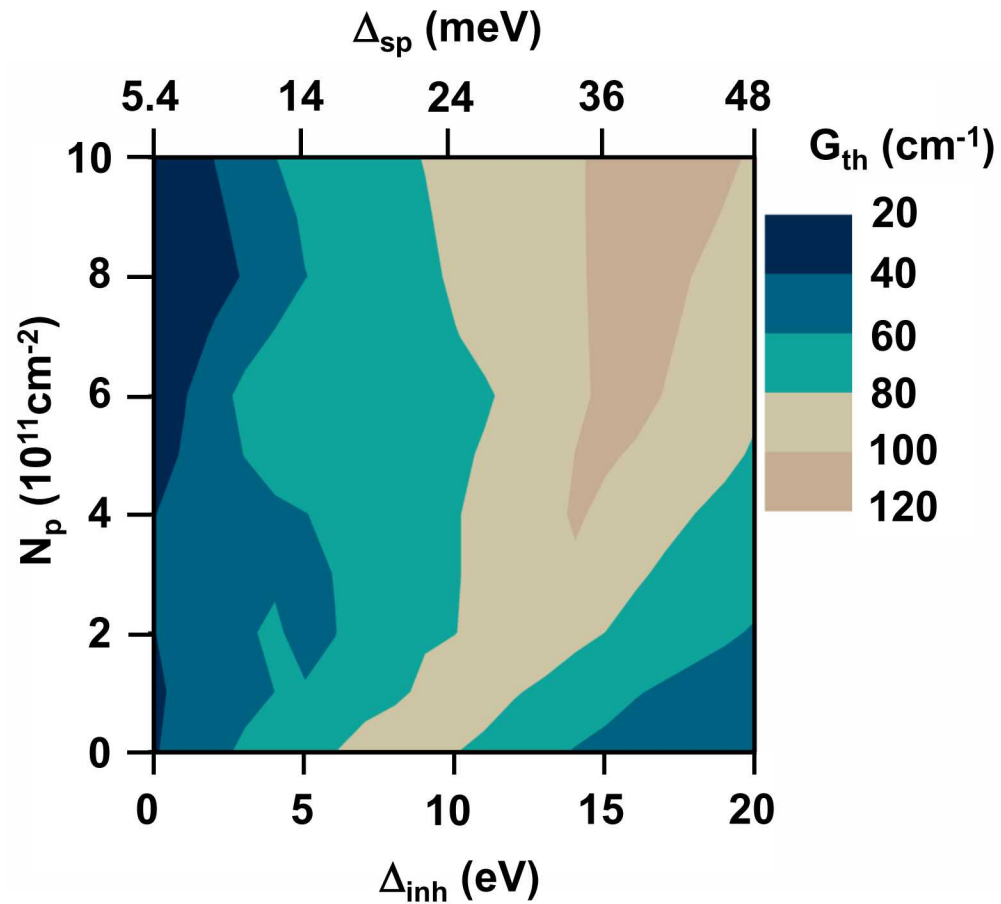
$$\Delta_{inh} = 14 \text{ meV} \rightarrow \Delta_{sp} = 24 \text{ meV}$$

$$N_p = 0 \text{ x, } 2 \text{ x, } 4 \text{ x, } 6 \text{ x, } 8 \text{ x } 10^{11} \text{ cm}^{-2}$$

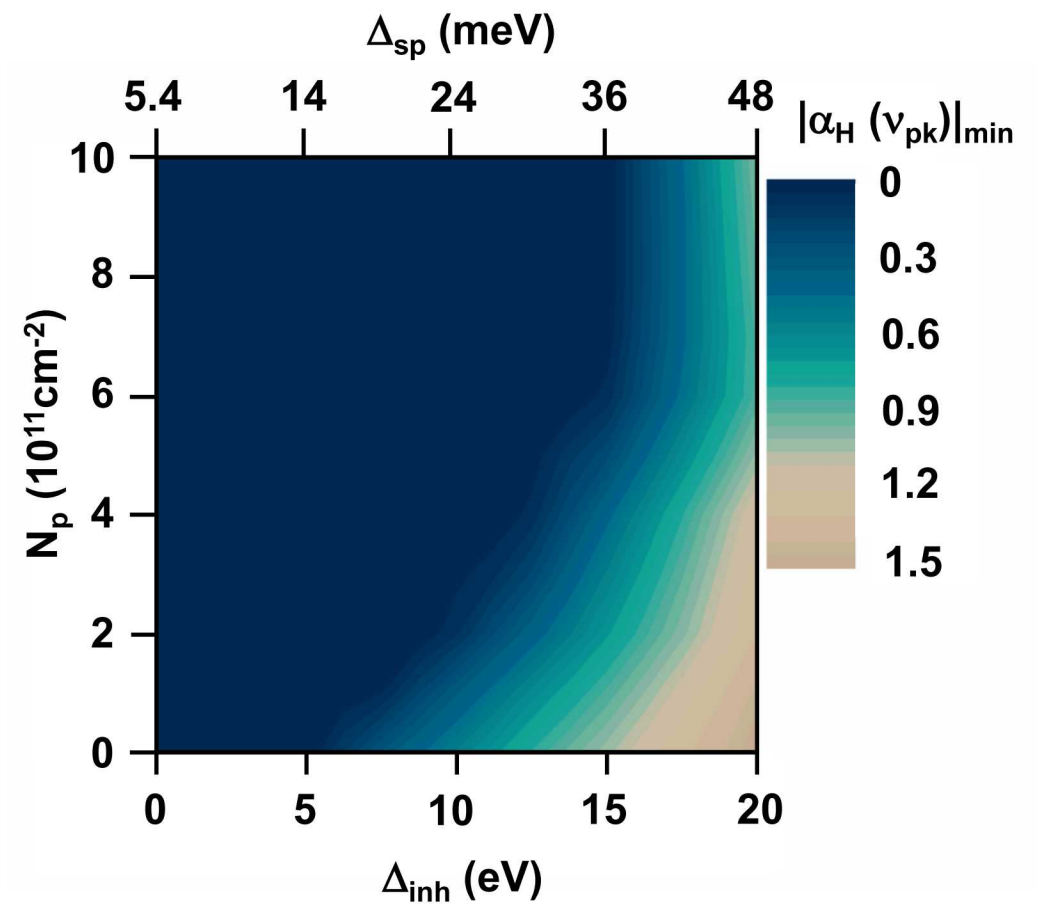
Designing QD lasers with minimum $\alpha_H(v_{pk})$

Combinations of $(\Delta_{inh}, N_p, G_{th})$

giving $|\alpha_H(v_{pk})|_{min}$

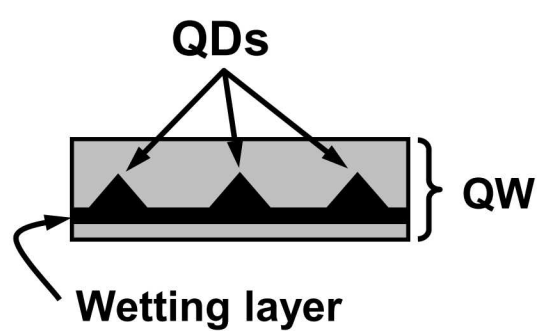


$|\alpha_H(v_{pk})|_{min}$ resulting from
 $(\Delta_{inh}, N_p, G_{th})$ combinations



QD laser theory

Semiclassical laser theory



Carrier-induced
refractive index

$$[2K\delta n(\nu) + \underset{\substack{\uparrow \\ \text{Intensity gain}}}{iG(\nu)}]E = \frac{2\nu}{\epsilon_0 n_B c \hbar} \left[N_{QD}^{2d} \sum_n \wp_n \sum_q \underset{\substack{\downarrow \\ \text{QD polarization}}}{n_{n,q}^{inh} p_{n,q}(\nu)} + \frac{1}{A} \sum_k \wp_k \underset{\substack{\downarrow \\ \text{QW polarization}}}{p_k(\nu)} \right]$$

e-h polarization

Absorption and
stimulated emission

$$\frac{dp_{n,q}}{dt} = i(\nu - \omega_{n,q}^{(0)})p_{n,q} - i \frac{2\wp_n \mathcal{E}}{\hbar} (f_{n,q}^e + f_{n,q}^h - 1) \quad \text{Single-particle contributions}$$

$$+ \frac{i}{\hbar} \sum_k V_{n,k} (f_k^e + f_k^h) p_{n,q} + \frac{i}{\hbar} \sum_k V_{n,k} p_k \quad \text{Exchange and excitonic effects}$$

$$+ S_n^{c-p} + S_n^{c-c}$$

$\downarrow$ Carrier-phonon scattering $\downarrow$ Carrier-carrier scattering

Dephasing and screening

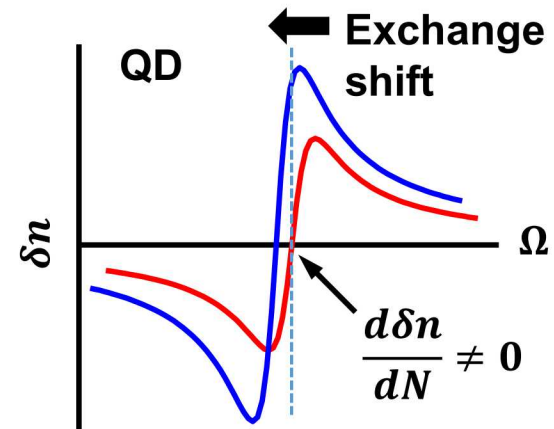
Many-body effects

Features of QD laser theory

1 QD/QW combination

Renorminizations:

H.C. Schneider, et al.
PRB 64, 115315 (2001)
PRB 66, 41310(R) (2002)

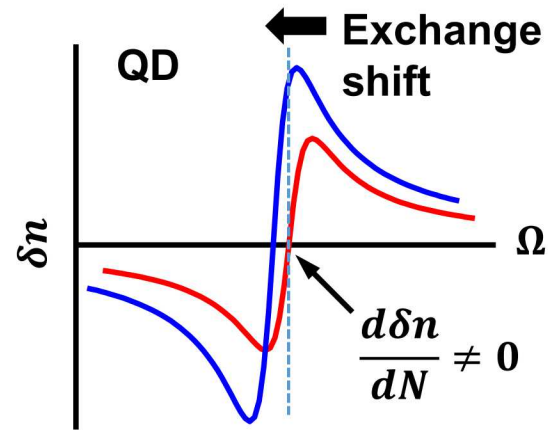


Features of QD laser theory

1 QD/QW combination

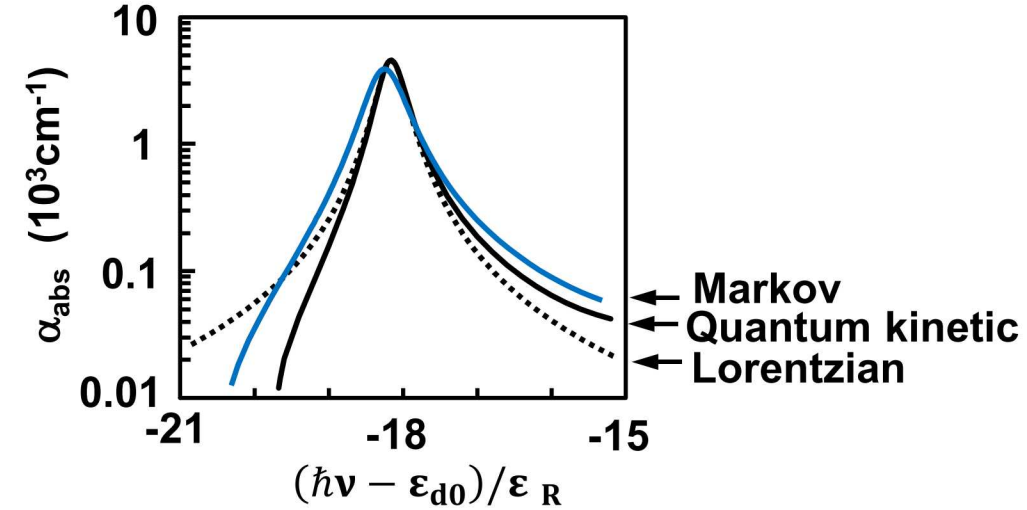
Renorminizations:

H.C. Schneider, et al.
PRB 64, 115315 (2001)
PRB 66, 41310(R) (2002)



2 Memory

H.C. Schneider, et al. PRB 70, 235308 (2004)

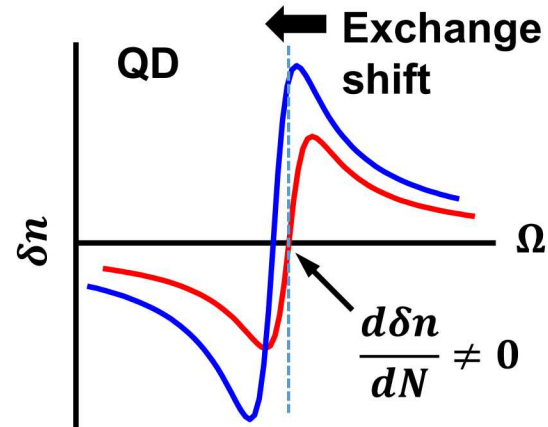


Features of QD laser theory

1 QD/QW combination

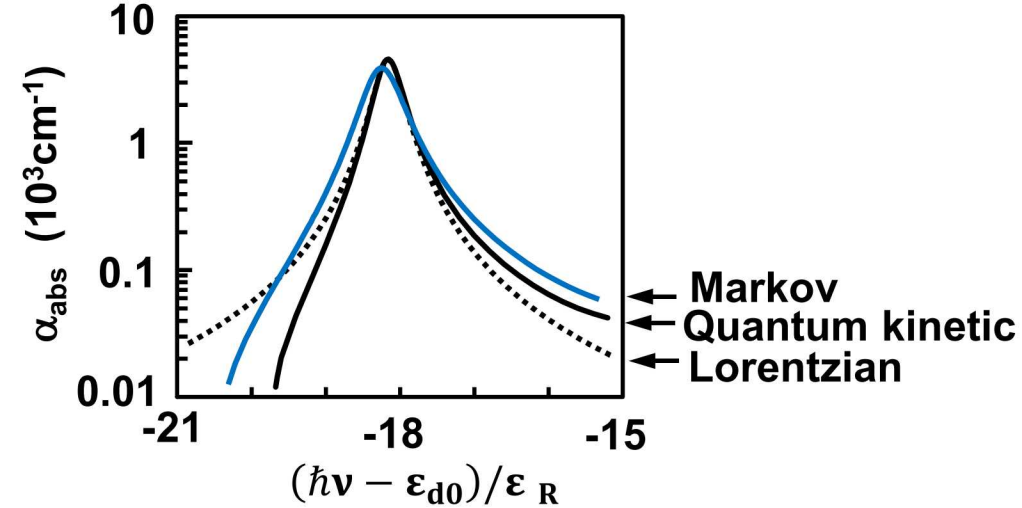
Renorminizations:

H.C. Schneider, et al.
PRB 64, 115315 (2001)
PRB 66, 41310(R) (2002)



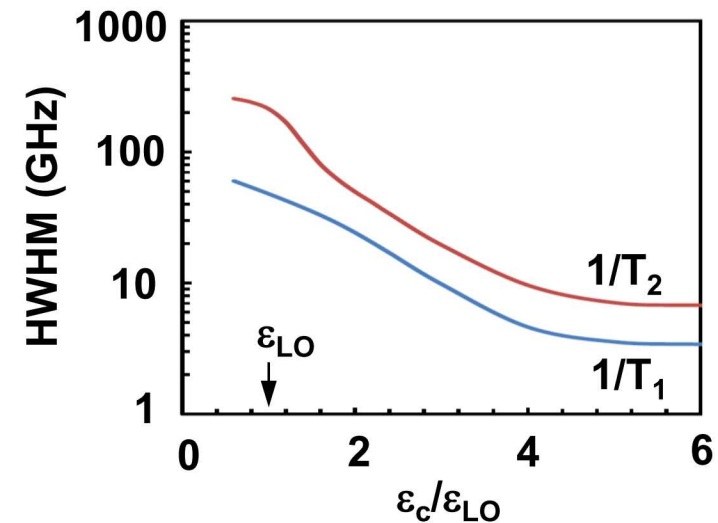
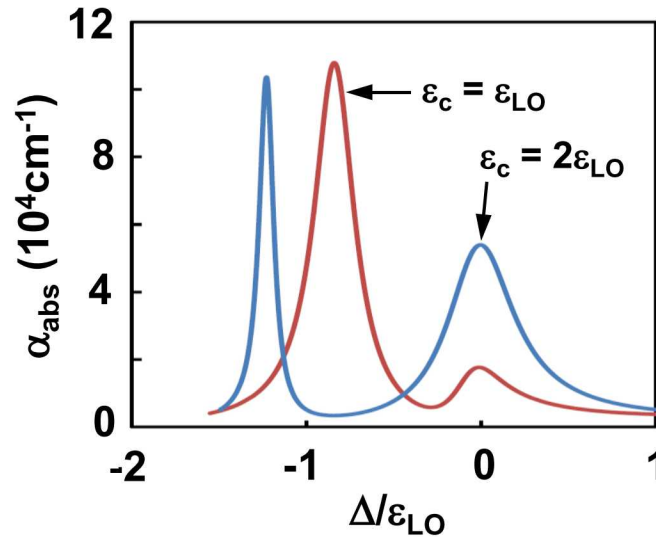
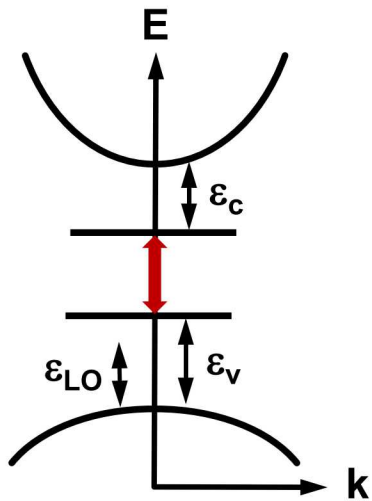
2 Memory

H.C. Schneider, et al. PRB 70, 235308 (2004)



3 Scattering (beyond 2nd Born approx.)

J. Seebeck, et al. PRB 71, 125327 (2005)



No phonon bottleneck as predicted by H. Benisty, et al. PRB 44, 10945 (1991)

Summary

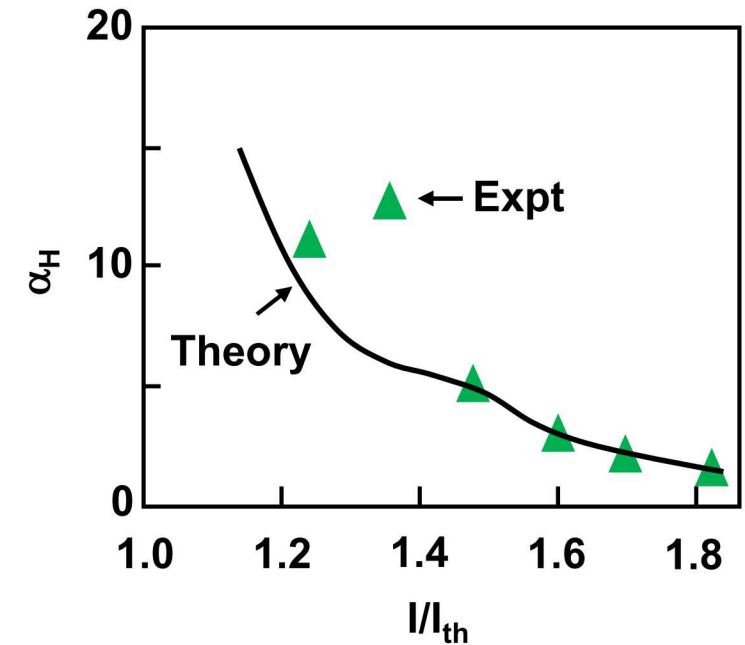
Calculations on devices a step from being ready for use in optoelectronics

Modeling devices versus modeling experimental results

Summary

Calculations on devices a step from being ready for use in optoelectronics

Modeling devices versus modeling experimental results



$\text{In}_{0.3}\text{Ga}_{0.7}\text{As}$ QD in GaAs QW

$N_{\text{QD}} = 5 \times 10^9 \text{cm}^{-2}$

$\Delta_{\text{inh}} = 30 \text{ meV}$

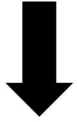
S. Holzinger, et al. Opt. Exp. 26,
31363 (2018)

Summary

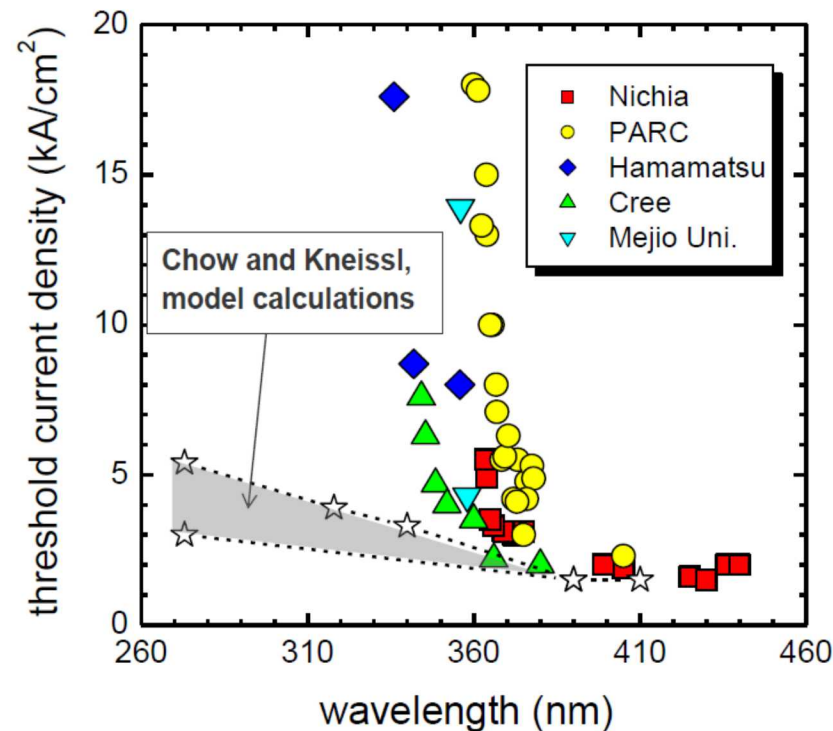
Calculations on devices a step from being ready for use in optoelectronics

Modeling devices versus modeling experimental results

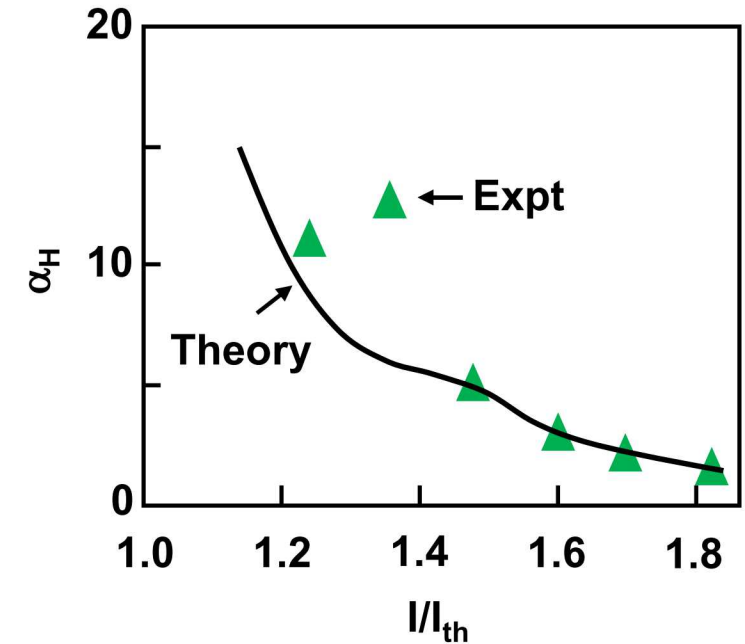
Zeeman laser
Multioscillator ring
laser gyro



Murray Sargent III (μ soft):
“Numerical experiments”



Chow and Kneissl, JAP 98, 114502 (2005)
Slide courtesy of Noble Johnson (PARC)
Funding: SFB 787



$\text{In}_{0.3}\text{Ga}_{0.7}\text{As}$ QD in GaAs QW

$N_{\text{QD}} = 5 \times 10^9 \text{cm}^{-2}$

$\Delta_{\text{inh}} = 30 \text{ meV}$

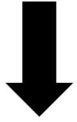
S. Holzinger, et al. Opt. Exp. 26, 31363 (2018)

Summary

Calculations on devices a step from being ready for use in optoelectronics

Modeling devices versus modeling experimental results

Zeeman laser
Multioscillator ring
laser gyro



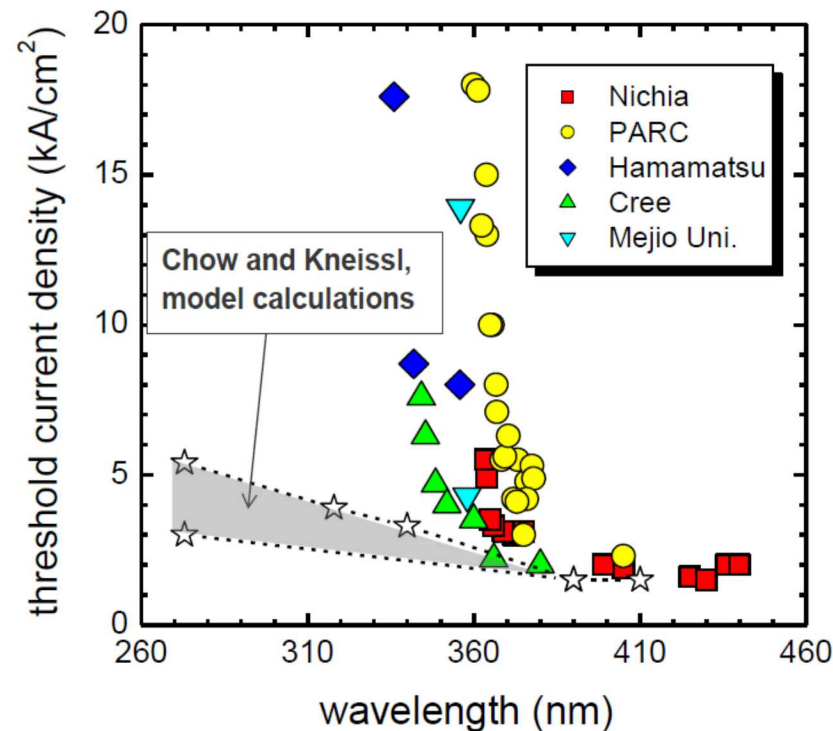
Murray Sargent III (μ soft):
“Numerical experiments”



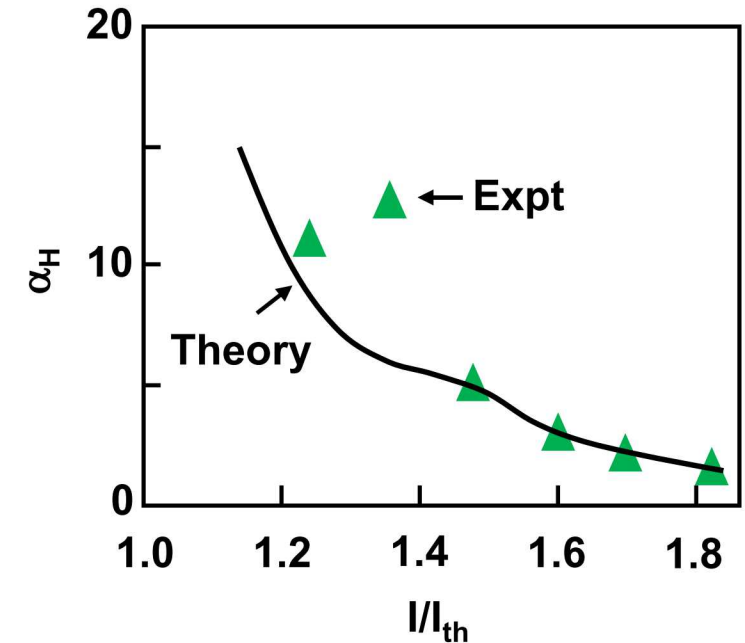
W. Chow, et al. ‘Extraction of inhomogeneous broadening and nonradiative losses in InAs quantum-dot laser’ APL 107, 1171106 (2015)

Z. Zhang, et al. ‘Effects of modulation p-doping in InAs quantum dot lasers on silicon’ APL 113, 061105 (2018)

Z. Zhang, et al. ‘Linewidth enhancement factor in InAs/GaAs quantum dot lasers and its implication in isolator-free and narrow linewidth applications’ IEEE J. Selected Topics in Quantum Electron. 25, 1900509 (2019)



Chow and Kneissl, JAP 98, 114502 (2005)
Slide courtesy of Noble Johnson (PARC)
Funding: SFB 787



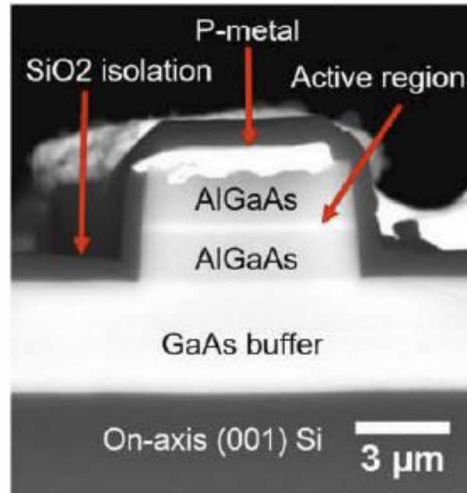
In_{0.3}Ga_{0.7}As QD in GaAs QW

$N_{QD} = 5 \times 10^9 \text{ cm}^{-2}$

$\Delta_{inh} = 30 \text{ meV}$

S. Holzinger, et al. Opt. Exp. 26, 31363 (2018)

The real laser



Quantum-dot gain



Justin Norman



Daehwan Jung



Robert Zhang

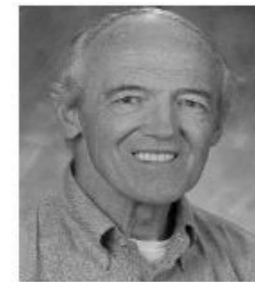


Shen Shang

Mode locking



Songtao Liu



Art Gossard

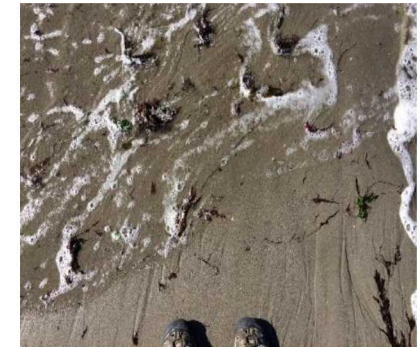


John Bowers

Nanolasers



Yating Wan



A review of high-performance quantum dot lasers on Silicon (IEEE JQE 55, 200511, 2019)

On the physics of semiconductor quantum dots for applications in lasers and quantum optics

Chow and Jahnke, Prog Quantum Electron 37, 109–184 (2013)

Quantum-optical influences in optoelectronics—An introduction

Chow and Reitzenstein, Applied Physics Reviews 5, 041302 (2018)