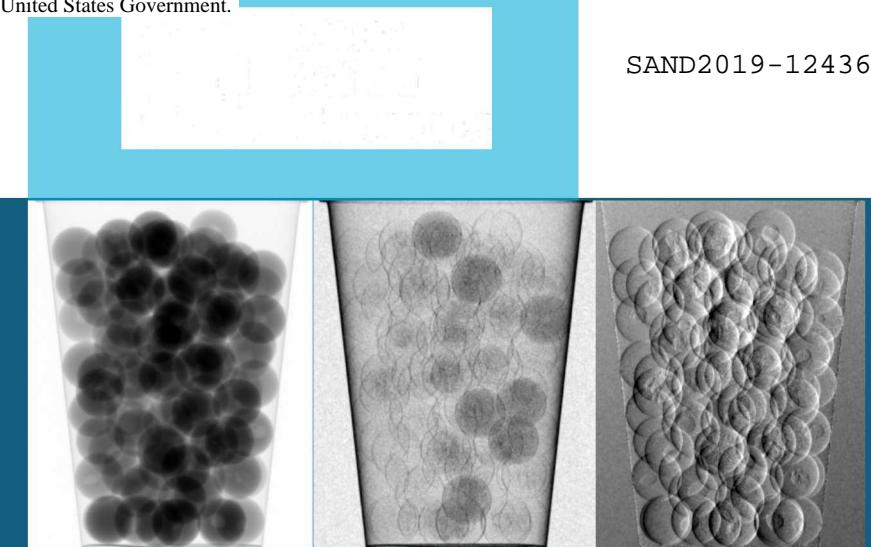
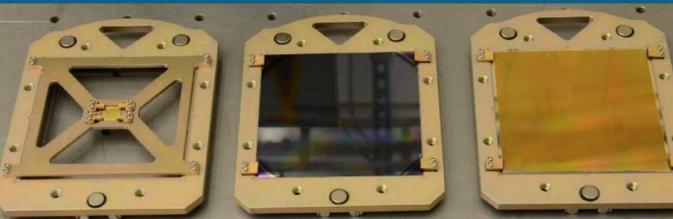


# The Effects of Thermal Expansion of Gratings in Talbot-Lau Lab-Based X-Ray Phase Contrast Imaging



## PRESENTED BY

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## Hypothesis

Grating-based XPCI systems can be tuned to, and operated at high-sensitivity to achieve high-contrast images. To do this requires quality system components and **control of the acquisition environment**.

# Outline

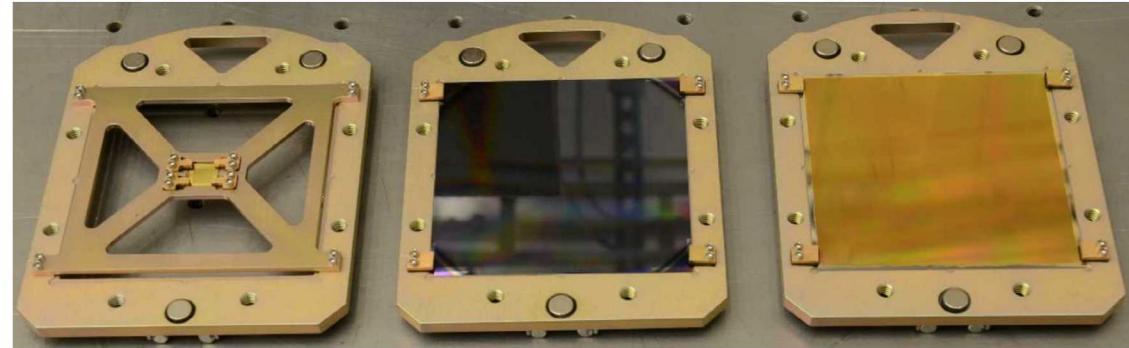
## 1. Overview of XPCI

- a. Talbot-Lau Cone-Beam XPCI System Design
- b. Operating XPCI System at *High Sensitivity*
- c. Signal Model

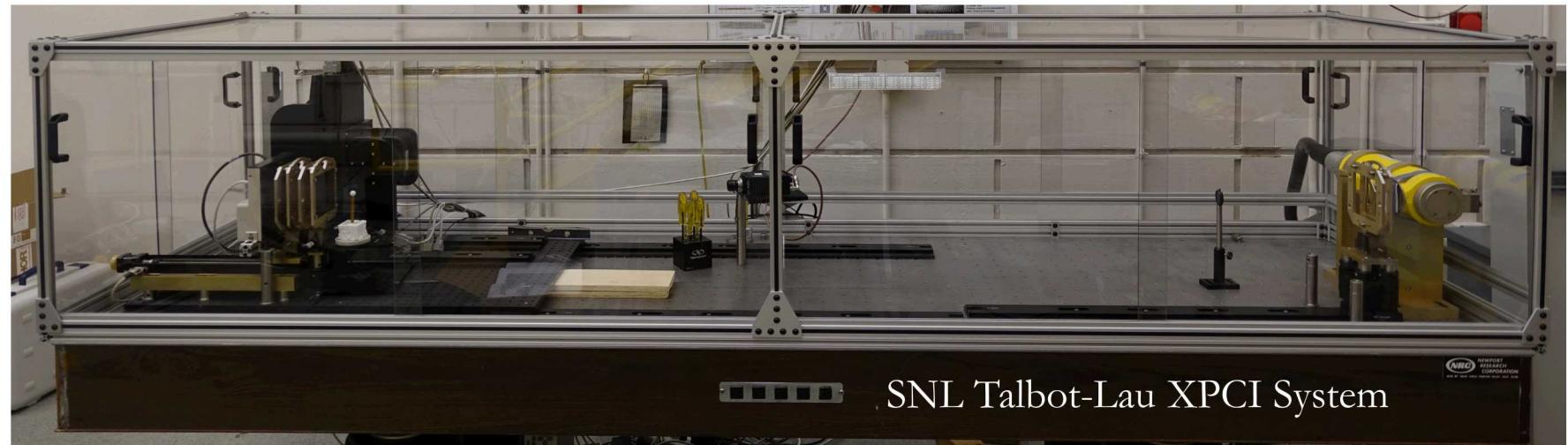
## 2. Thermal Expansion of Gratings

- a. Sources of Heat
- b. Effect of Thermal Expansion on Signal Parameters
- c. Mitigation of Thermal Expansion

## 3. Questions



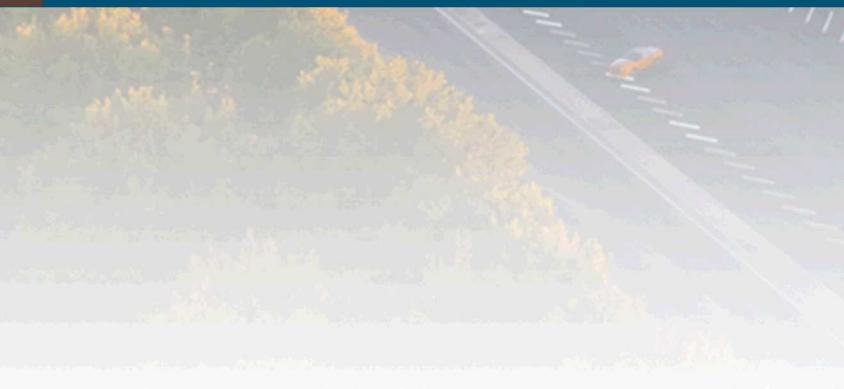
SNL large-area Talbot-Lau interferometer gratings



SNL Talbot-Lau XPCI System



# Overview of XPCI



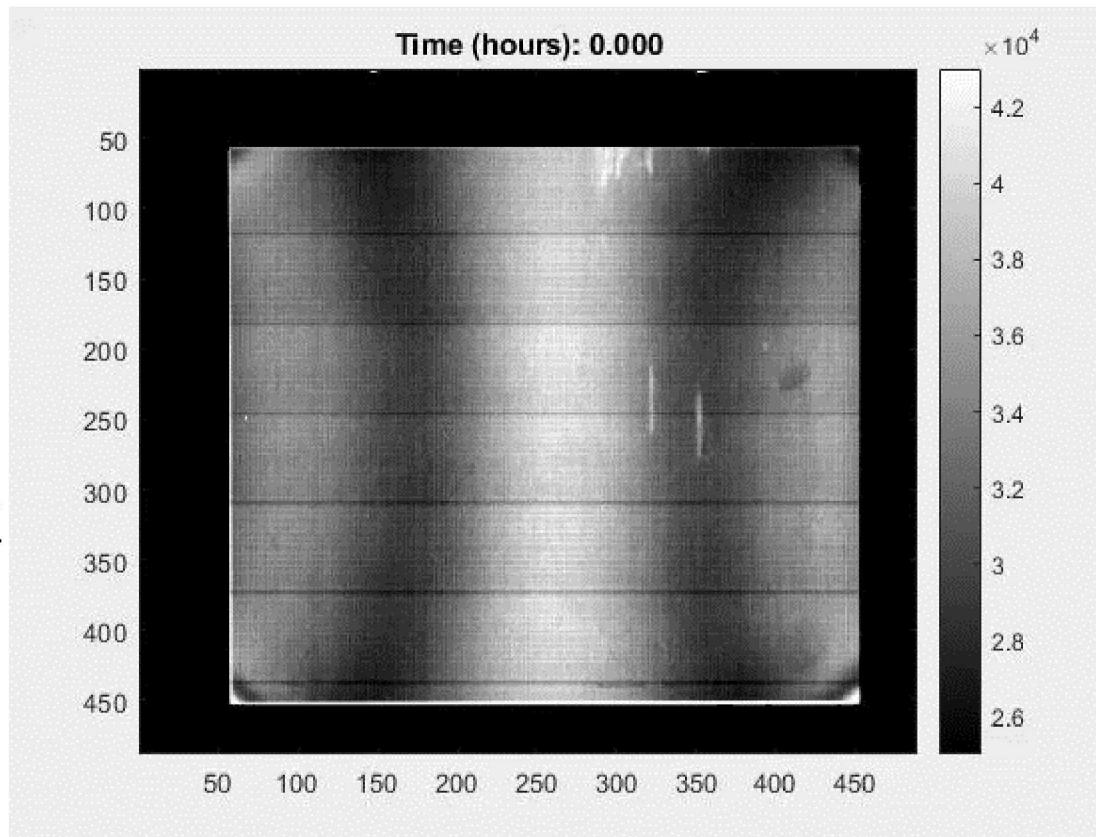
# Talbot-Lau Cone-Beam XPCI System Design



1. A Talbot-Lau XPCI system<sup>1,2</sup> has three gratings:  $G_0$ ,  $G_1$ , and  $G_2$  Video: Detector, no heat shield.
2. A ***High-sensitivity*** XPCI system has:
  - Matched set of gratings
  - Ideal  $L$  and  $d$  distances
  - Low fringe count
  - High Fringe Contrast/Visibility
3. Signal model for reference and sample data:<sup>3-5</sup>

$$f_M(x) = A_M \sin(\omega_M x(n) + \phi_M) + b_M, \text{ where } \omega = \frac{2\pi}{p_2}$$

Subscript  $M$  represents reference (R) and sample (S)



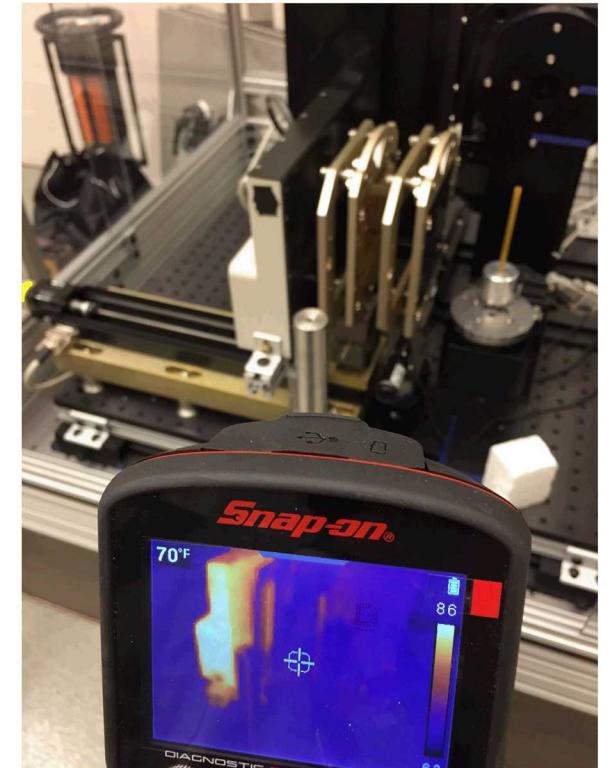


# Thermal Expansion of Gratings



# Temperature

1. Room temperature and heat from system electronics, such as the X-ray source and detector, can cause thermal expansion of the gratings
2. Thermal expansion changes the period and duty cycle of the gratings



## 8 Thermal Expansion of Gratings Effects the Moiré Frequency

1. The Moiré spatial frequency from a cone-beam XPCI system is related to the grating periods by,

$$f_{Moiré} = \frac{p_0 p_1 - 2p_0 p_2 + p_1 p_2}{p_1 p_2 (p_0 + p_2)}.$$

2. Derivatives with respect to the grating periods are,

$$\frac{\partial f_{Moiré}}{\partial p_0} = \frac{-2p_1 p_2^3}{(p_1 p_2 (p_0 + p_2))^2},$$

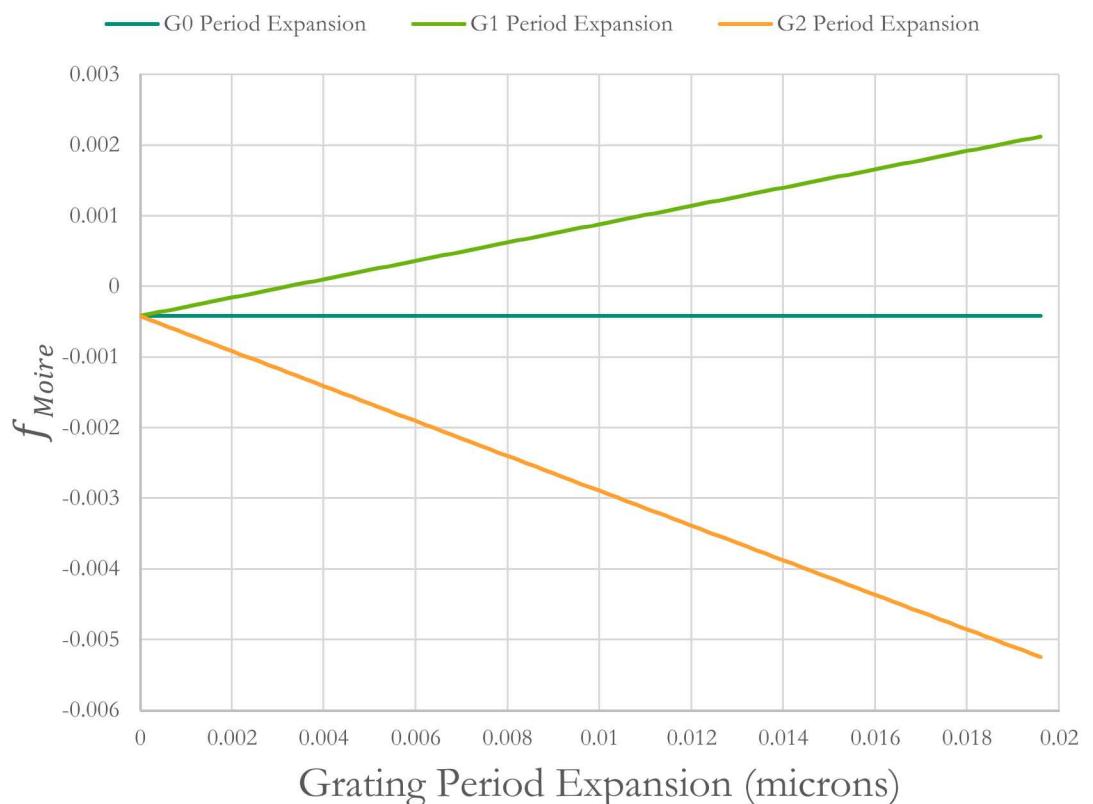
$$\frac{\partial f_{Moiré}}{\partial p_1} = \frac{2p_0 p_2^2 (p_0 + p_2)}{(p_1 p_2 (p_0 + p_2))^2},$$

$$\frac{\partial f_{Moiré}}{\partial p_2} = \frac{-p_1^2 (p_0 + p_2)^2 + 2p_0 p_1 p_2^2}{(p_1 p_2 (p_0 + p_2))^2},$$

3. Thus, expansion of  $p_0$  decreases the Moiré frequency while expansion of  $p_1$  increases it.
4. Expansion of  $p_2$  is more complicated:

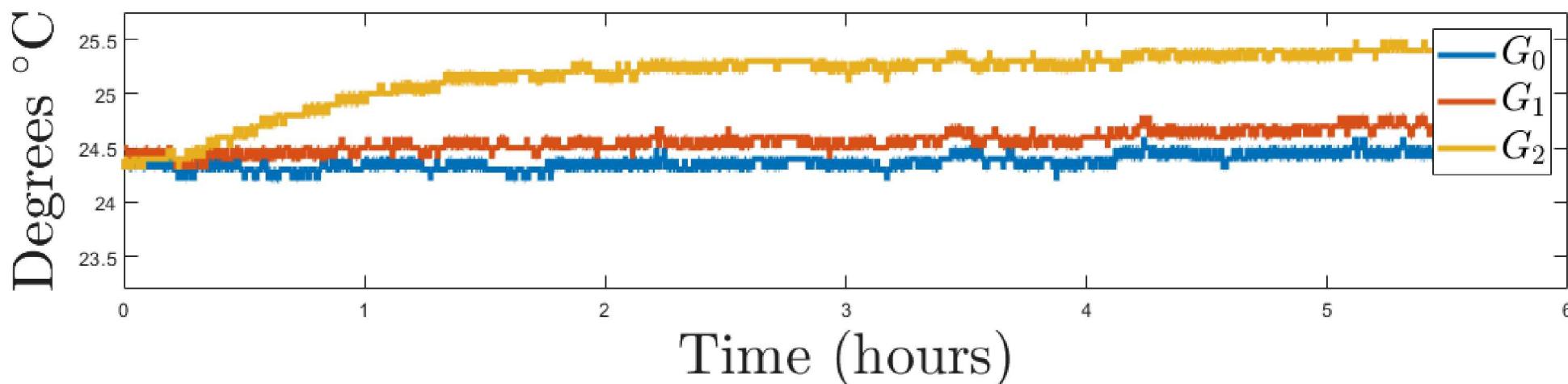
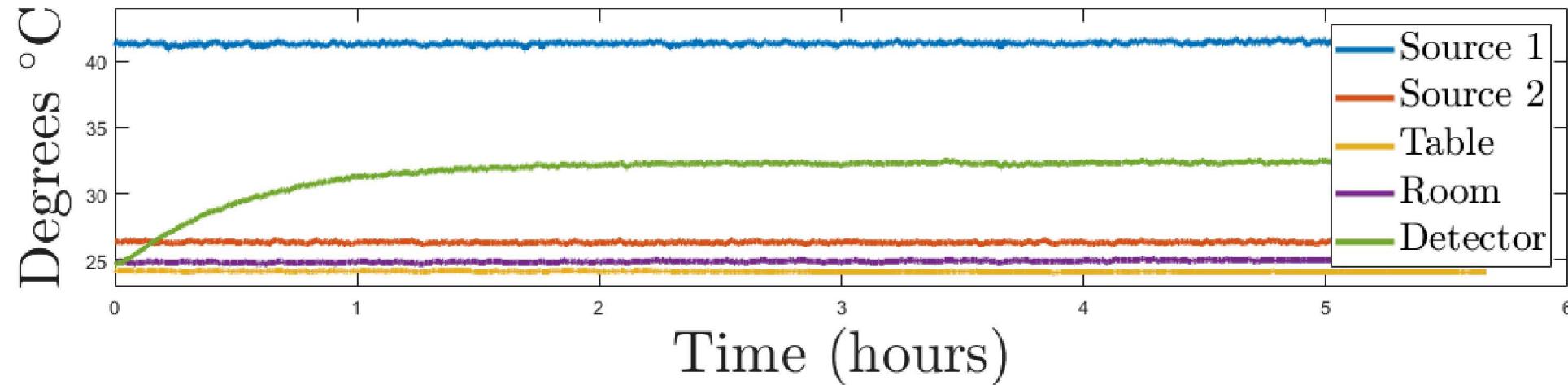
$$\frac{\partial f_{Moiré}}{\partial p_2} < 0 \text{ if } p_1(p_0 + p_2)^2 > 2p_0 p_2^2$$

Moiré Frequency Shift vs. Grating Period Expansion



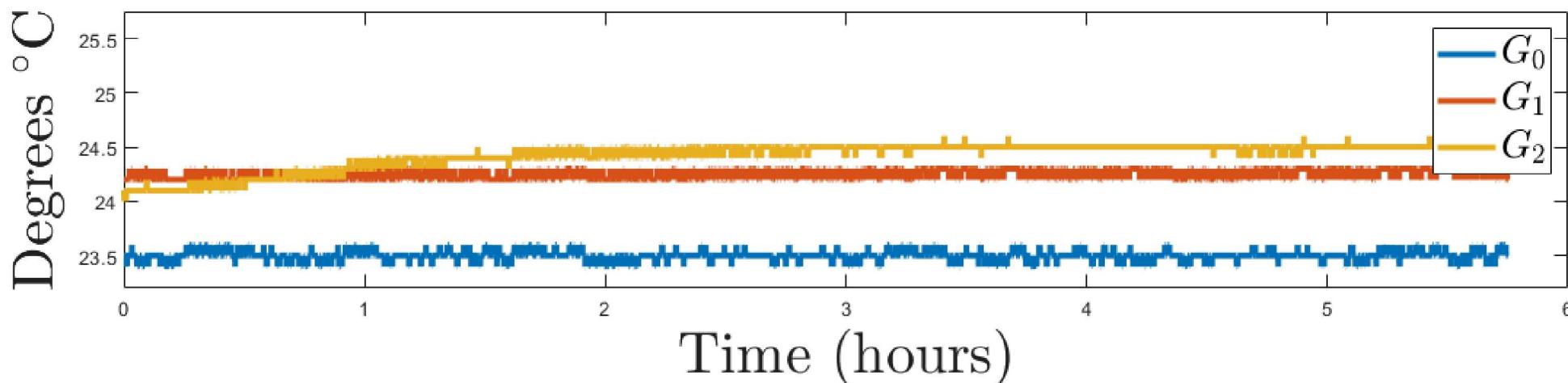
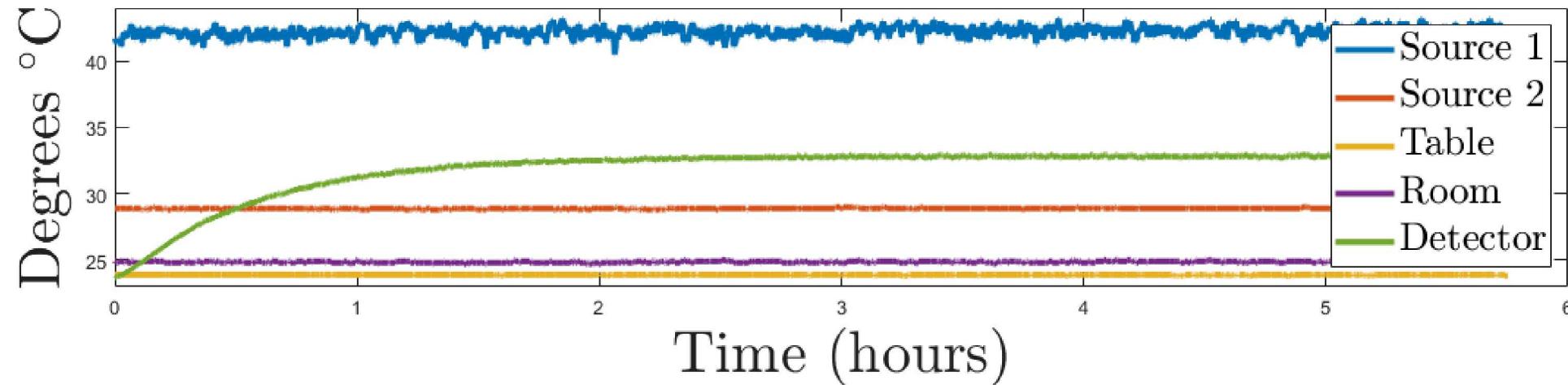
## 9 | Thermal Measurements Without Heat Shield

The source,  $G_0$ , room, and table are at thermal equilibrium before the detector is powered on. Powering the detector causes  $G_1$  and  $G_2$  to increase in temperature and also causes a slight temperature increase of  $G_0$ .



# Thermal Measurements With Heat Shield

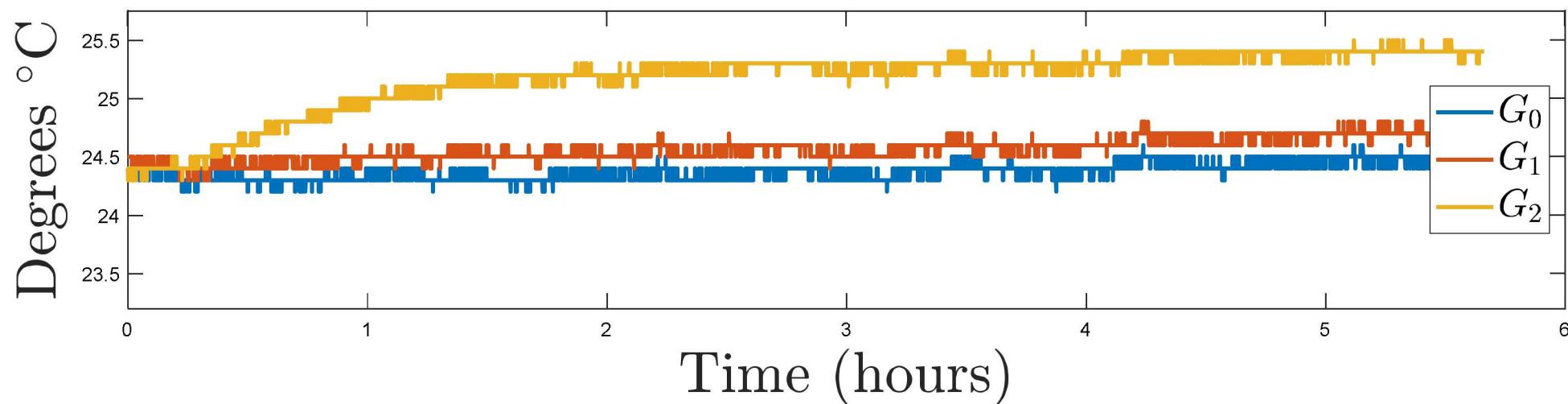
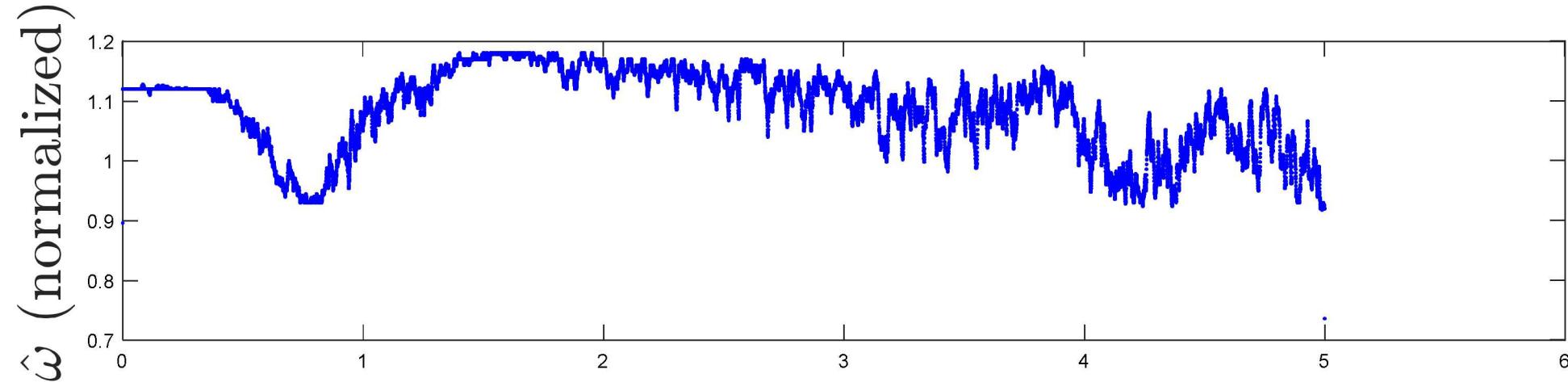
The source,  $G_0$ , room, and table are at thermal equilibrium before the detector is powered on. Powering the detector with the heat shield in place only causes a slight increase in the temperature of  $G_1$  and  $G_2$ .



# Moiré Frequency: Without Heat Shield

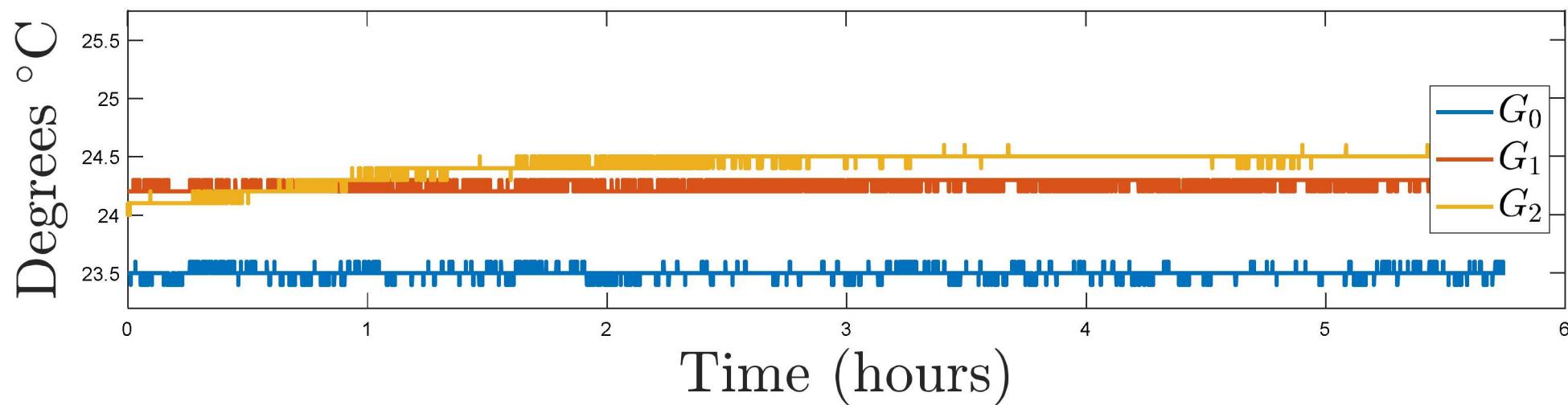
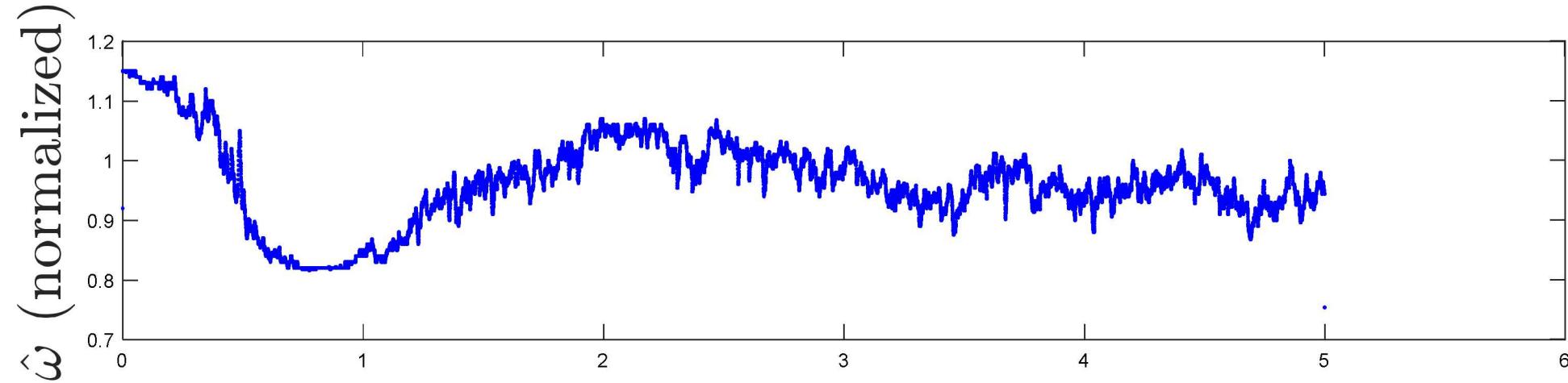


The interplay between grating expansions is complicated, but does affect the Moiré spatial frequency.



# Moiré Frequency: With Heat Shield

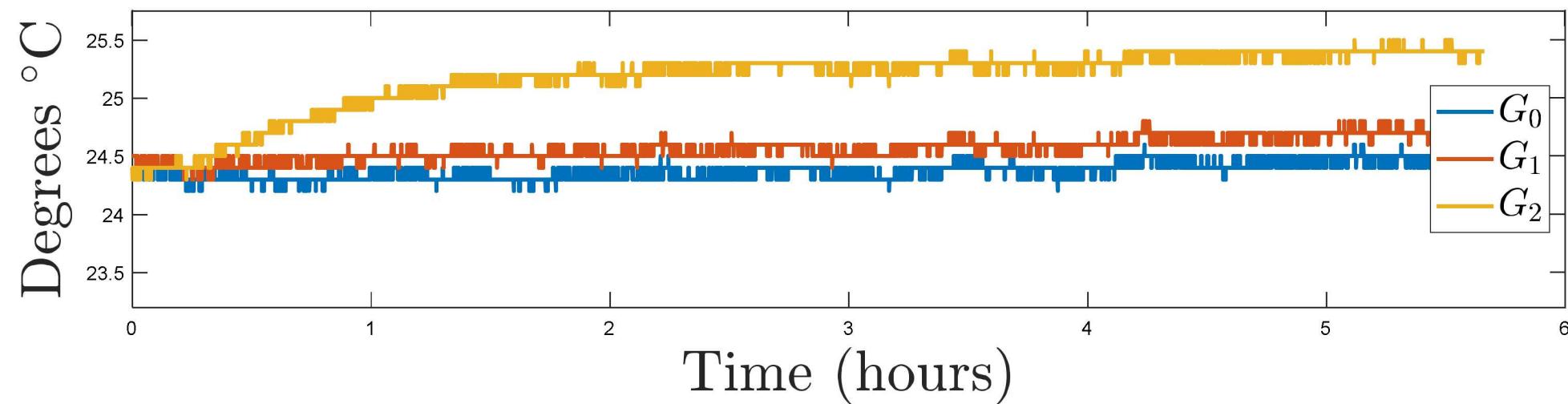
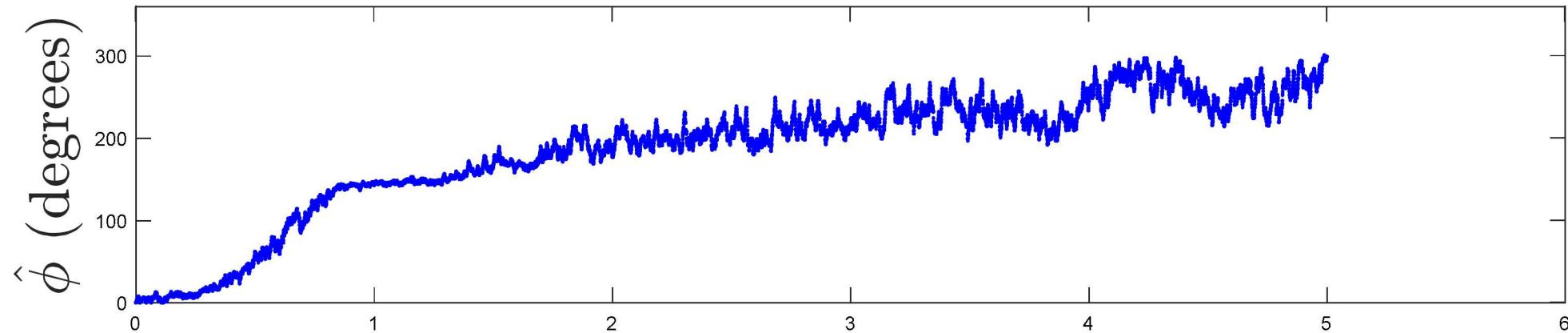
With the heat shields, the Moiré frequency settles close to one, which is where it should be.



# Moiré Phase: Without Heat Shield



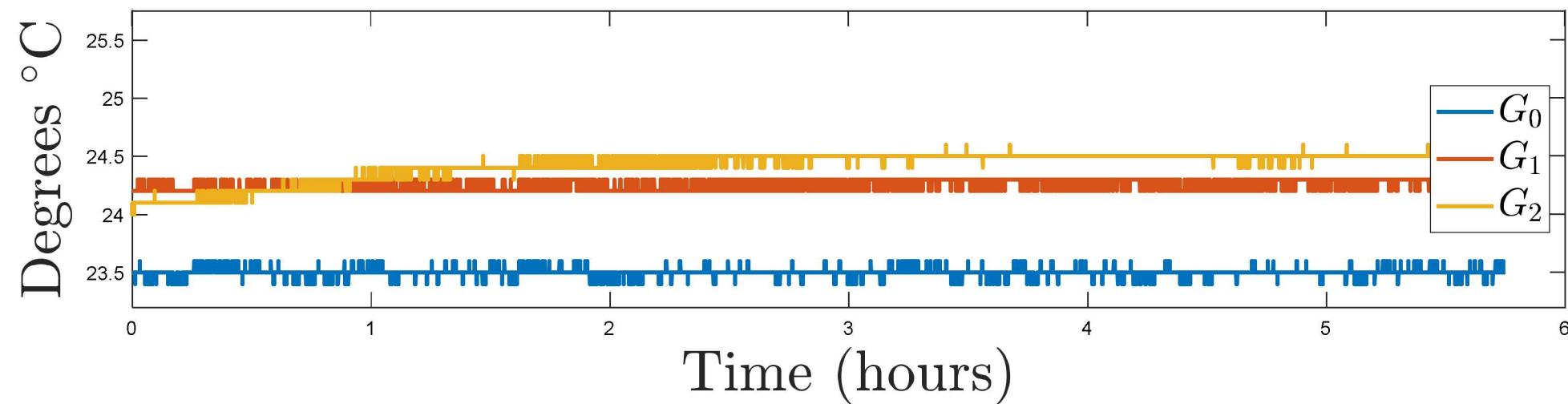
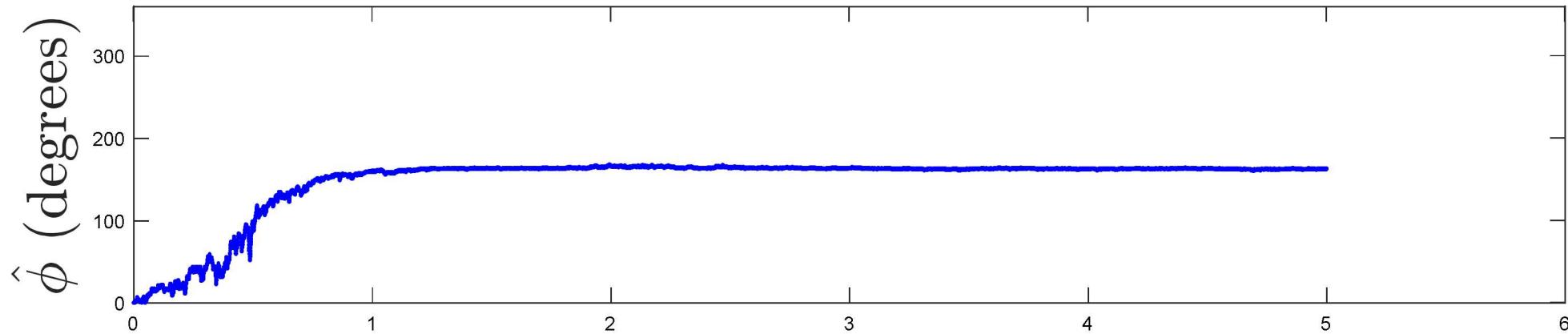
The phase (normalized to start at zero) of the Moiré pattern shifts with the thermal expansion of the gratings.



# Moiré Phase: With Heat Shield



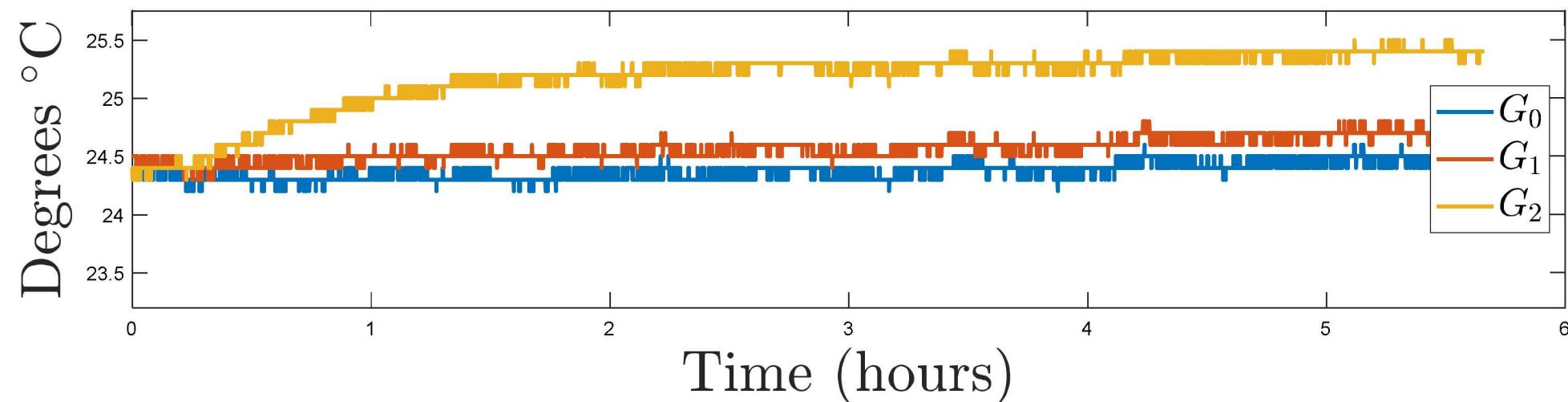
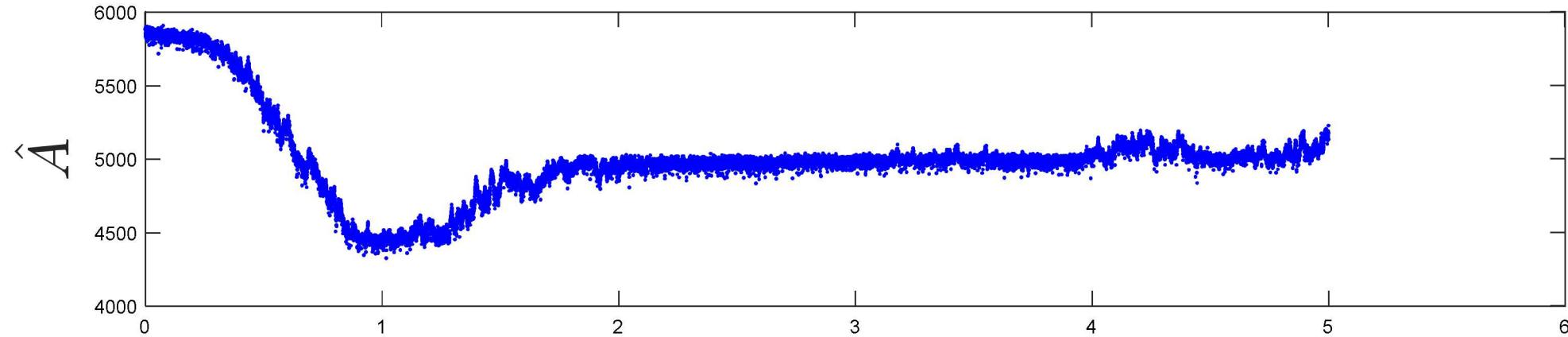
The phase stabilizes with the heat shield in place.



# Moiré Amplitude: Without Heat Shield



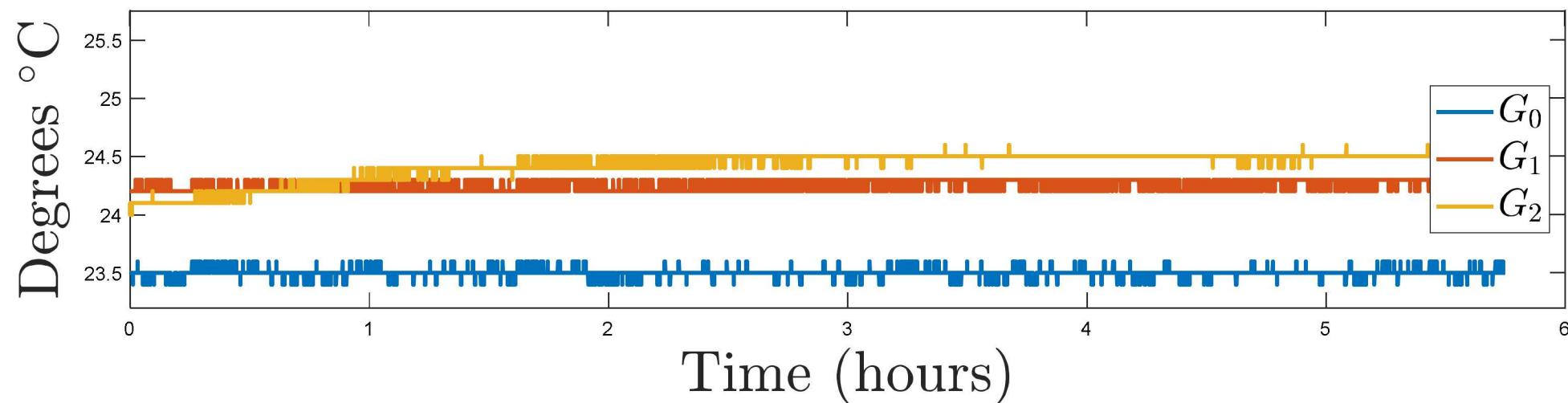
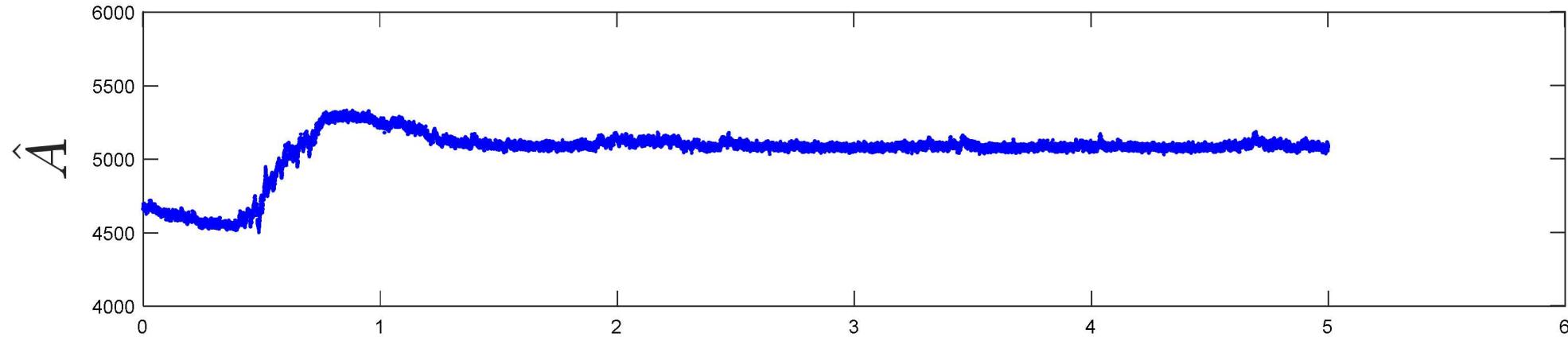
The amplitude of the Moiré pattern stabilizes, but has variability about the operating point.



# Moiré Amplitude: With Heat Shield

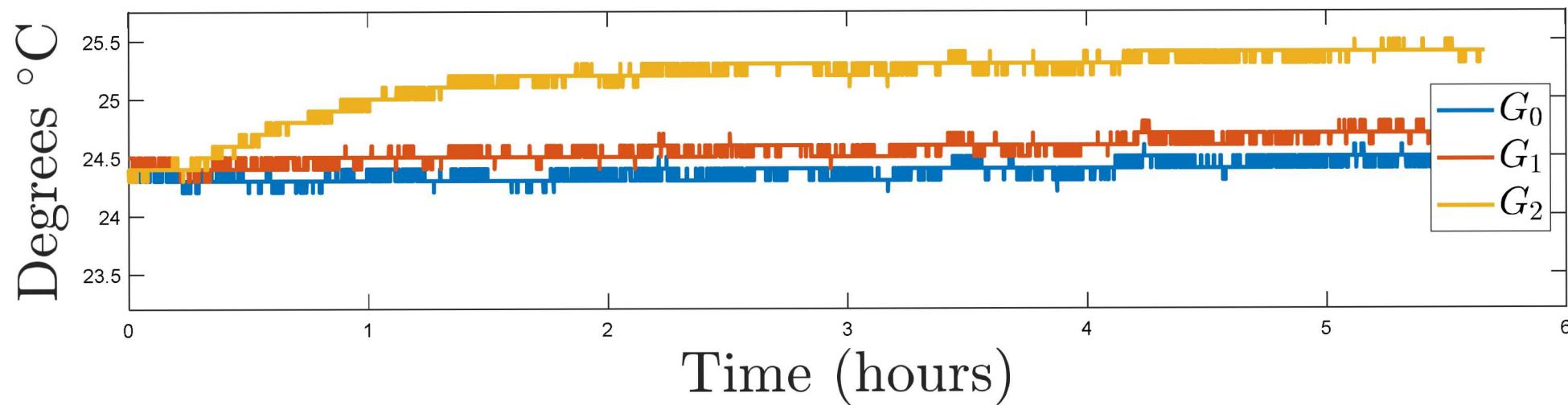
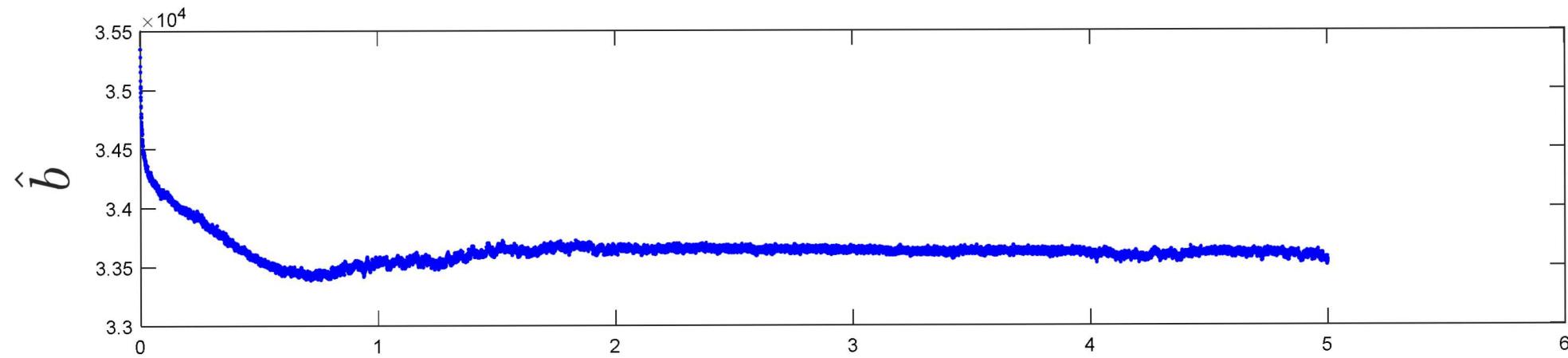


With the heat shield, the amplitude stabilizes and has less variability about the operating point.



# Moiré Bias: Without Heat Shield

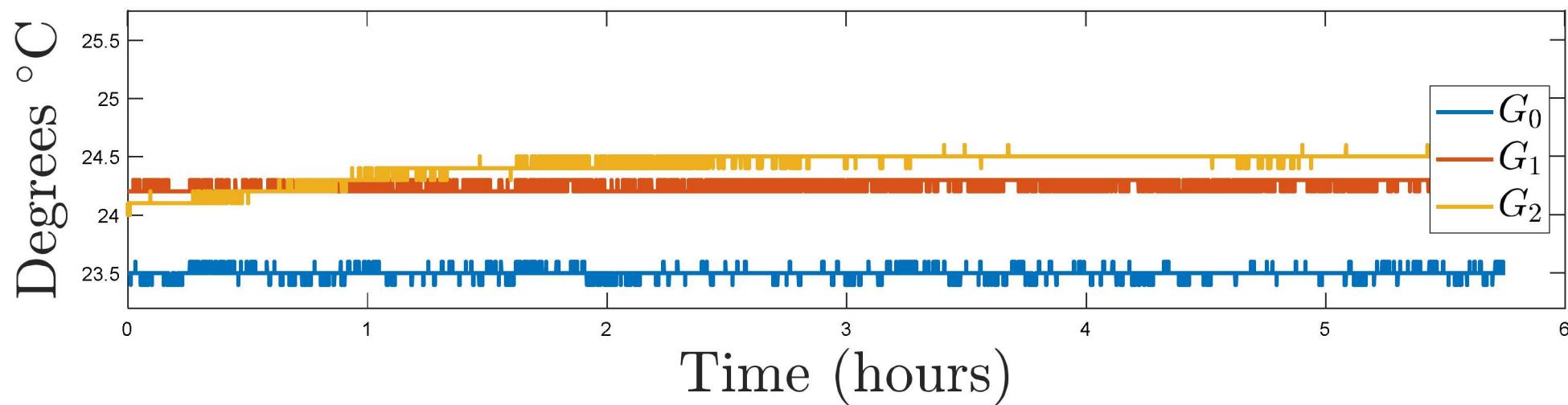
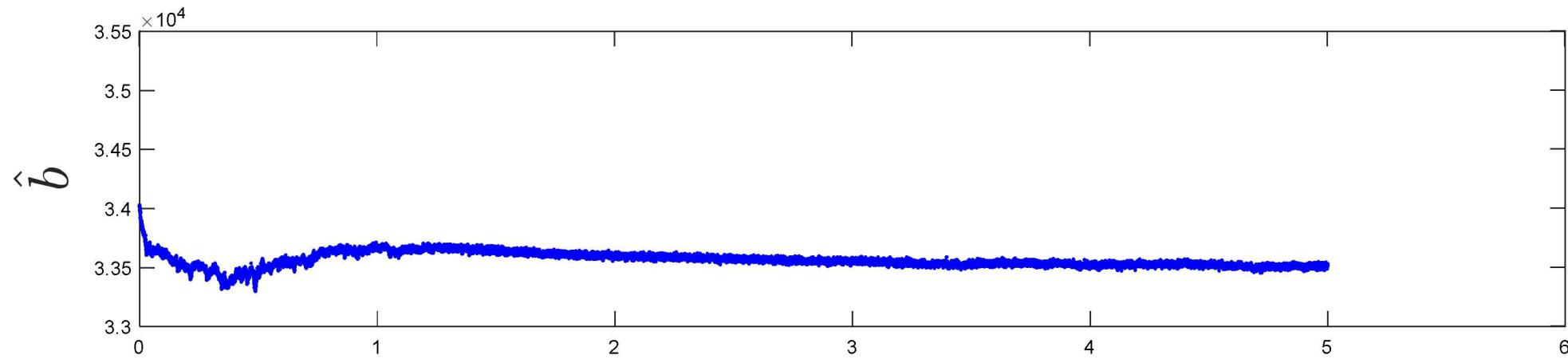
The bias without the heat shields...



# Moiré Bias: With Heat Shield



The bias is relatively unaffected by thermal expansion of the gratings.

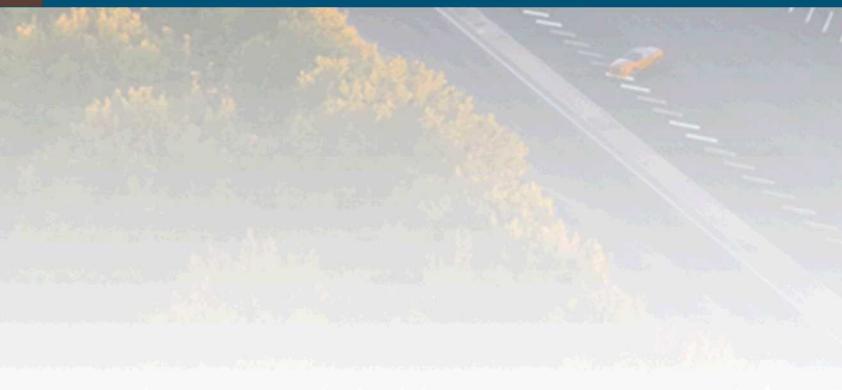


# Summary

- The signal model parameters most effected by thermal expansion of the gratings are the frequency and phase.
- The bias signal model parameter, which does not directly depend on the gratings, is the effected the least by thermal expansion
- Ideally the system should be thermally stable.
- Thermal changes will introduce changes in the system performance (i.e. change the fringe patterns).
- The XPCI system should be designed to minimize the influence of thermal sources.
- Component temperature monitoring may facilitate software corrections.
- Future work will explore the effect of variations in the x-ray source.



Questions?



# References

<sup>1</sup>Pfeiffer, F., Weitkamp, T., Bunk, O., and David, C., “Phase retrieval and differential phase-contrast imaging with low-brilliance x-ray sources,” *Nature Physics* 2 (Mar 2006).

<sup>2</sup>Kottler, C., Pfeiffer, F., Bunk, O., Grünzweig, C., Bruder, J., Kaufmann, R., Tlustos, L., Walt, H., Briad, I., Weitkamp, T., and David, C., “Phase contrast x-ray imaging of large samples using an incoherent laboratory source,” *physica status solidi (a)* 204(8), 2728-2733 (2007).

<sup>3</sup>Pfeiffer, F., Bech, M., Bunk, O., Kraft, P., Eikenberry, E. F., Brönnimann, C., Grünzweig, C., and David, C., “Hard-x-ray dark-field imaging using a grating interferometer,” *Nature Materials* 7 (Jan 2008).

<sup>4</sup>Pfeiffer, F., Bech, M., Bunk, O., Donath, T., Henrich, B., Kraft, P., and David, C., “X-ray dark-field and phase-contrast imaging using a grating interferometer,” *Journal of Applied Physics* 105(10), 102006 (2009).

<sup>5</sup>Wang, Z., Huang, Z., Chen, Z., Zhang, L., Jiang, X., Kang, K., Yin, H., Wang, Z., and Stampaoni, M., “Low-dose multiple-information retrieval algorithm for x-ray grating-based imaging,” *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment* 635(1), 103 - 107 (2011).