

Assembly of Polymer-Grafted Nanoparticles

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Jason Koski



Rob Riggelman



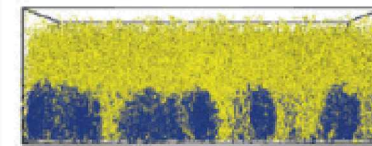
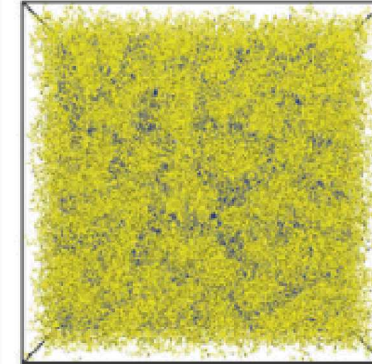
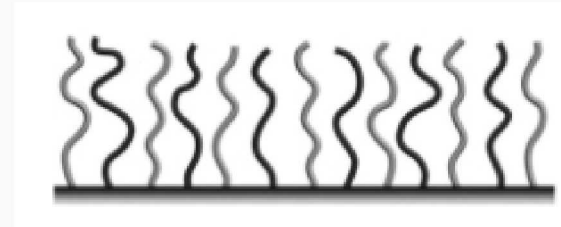
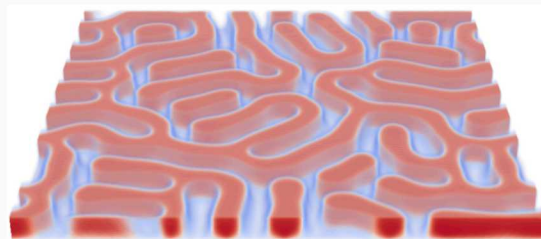
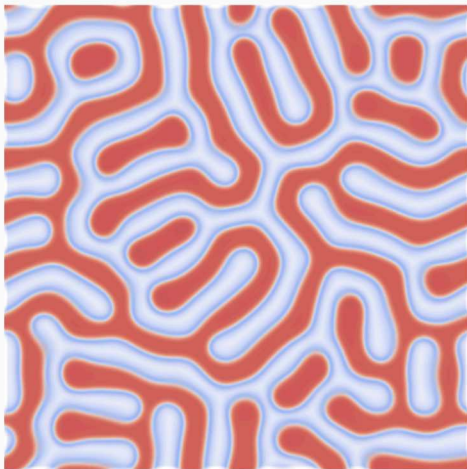
Russ Composto

U Penn

Mixed polymer brushes

- multiple polymer species grafted to surface
- microphase separation
 - lateral
 - vertical

lateral phase separation

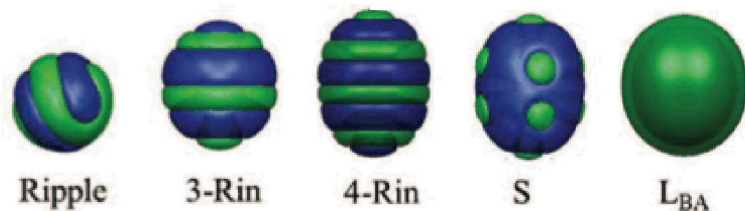


vertical
phase
separation

Wang, J. & Mueller, M. *J Phys Chem B* 113, 11384-11402 (2009).

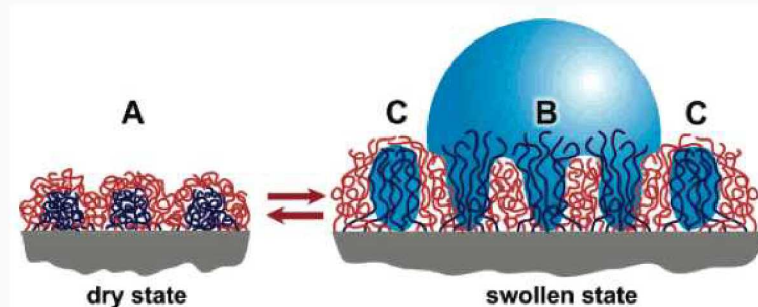
Mixed polymer brushes

patchy
nanoparticles



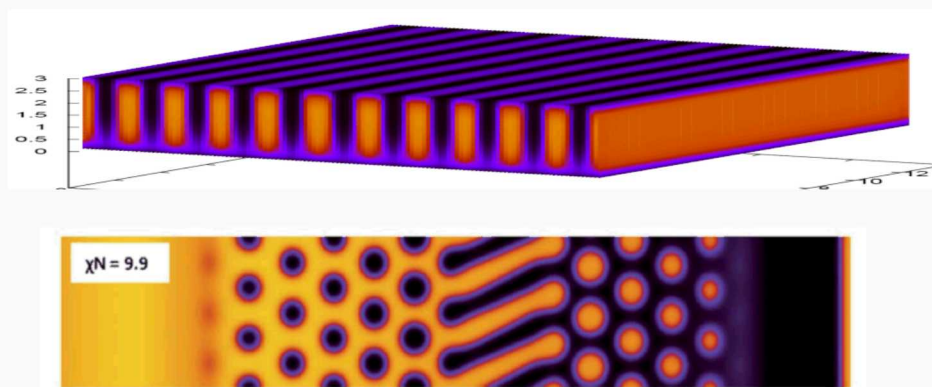
X. Ma, et al J Chem Phys **139**, 214902 (2013).

switchable surfaces



Motornov, M., Sheparovych, R., Tokarev, I.,
Roiter, Y. & Minko, S. *Langmuir* **23**, 13-19 (2007).

surface patterning

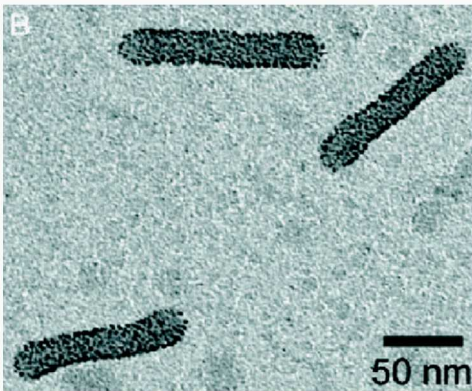
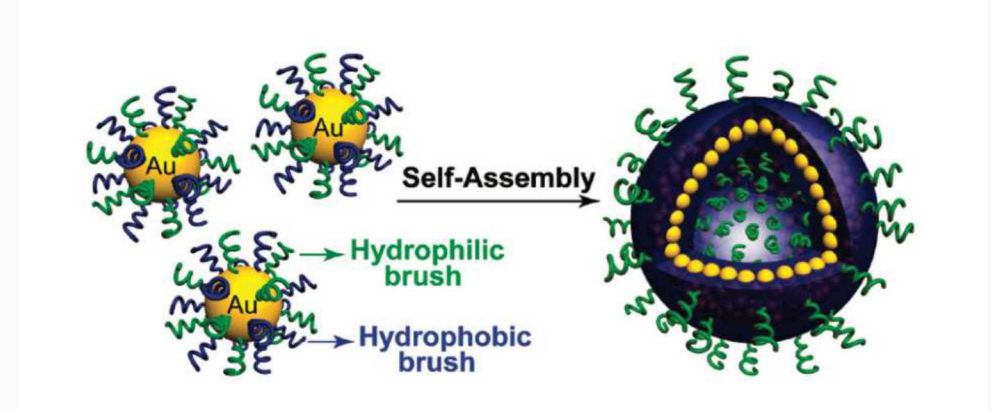


S-M. Hur, et al, *Soft Matter* **7**, 8776 (2011);
Soft Matter **9**, 5341 (2013).

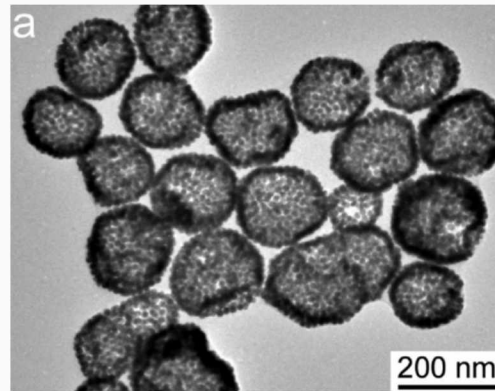
Assembly of mixed-brush nanoparticles in solution

Interest for

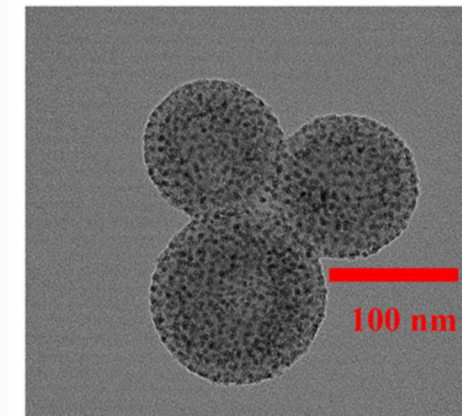
- solvent processing of nanocomposites
- optical applications (eg sensing, plasmonics)
- catalysis
- drug delivery



Zubarev *et al.*, JACS, 2006



Song *et al.*, JACS, 2012



Guzman-Juarez *et al.*, Macromolecules, 2018

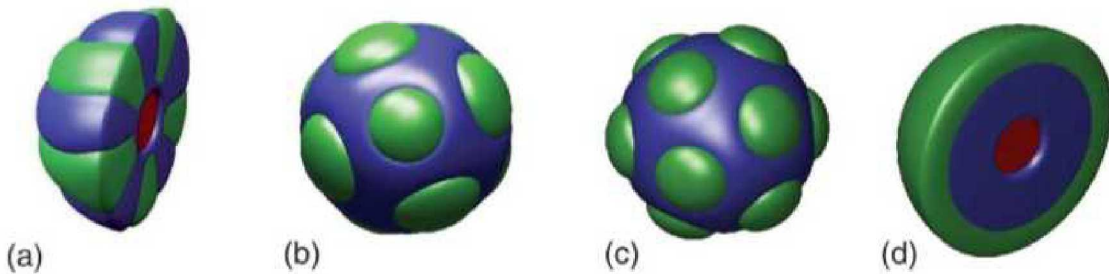
What is the structure of mixed-brush nanoparticles?

What governs the self-assembly of mixed-brush nanoparticles?

Previous modeling of mixed brush nanoparticles

polymer self-consistent field theory (SCFT)

non-selective good solvent
 $\chi_{AB}N = 40$



Wang et al., *J. Chem. Phys.*, 2011

neat particles
 $\chi_{AB}N = 20$

Morphology of single particle				
Hierarchical superstructure				

Chen et al., *ACS Macro Lett.*, 2016

How realistic are these structures? What about fluctuations?

Theoretically-Informed Langevin Dynamics (TILD)

discrete Gaussian chains + NPs

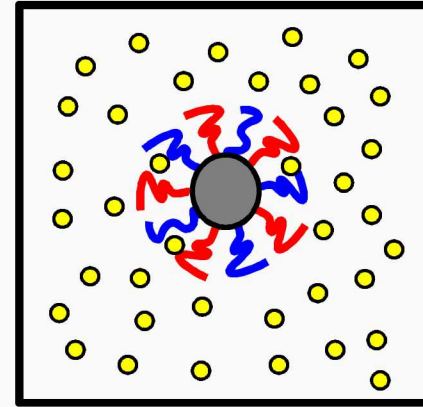
monomer shape function

$$h_m(\mathbf{r}) = (2\pi a^2)^{-3/2} e^{-|\mathbf{r}|^2/2a^2}$$

nanoparticle shape function

$$h_P(\mathbf{r}) = \frac{\rho_0}{2} \operatorname{erfc} \left(\frac{|\mathbf{r}| - R_P}{\zeta} \right)$$

bond length b , $a = \zeta = b/2$



Langevin eq for chains, particles:

$$m_i \frac{d^2 \mathbf{r}_i}{dt^2} = \mathbf{F}_i - D \frac{d\mathbf{r}_i}{dt} + \eta_i(t)$$

$$\mathbf{F}_i = \mathbf{F}_{\text{bond}} + \mathbf{F}_{\text{int}}$$

η_i = Gaussian white noise

monomer-monomer interactions: $u(\mathbf{r}) = \frac{\chi_{AB}}{\rho_0} (h_A * h_B)(\mathbf{r})$

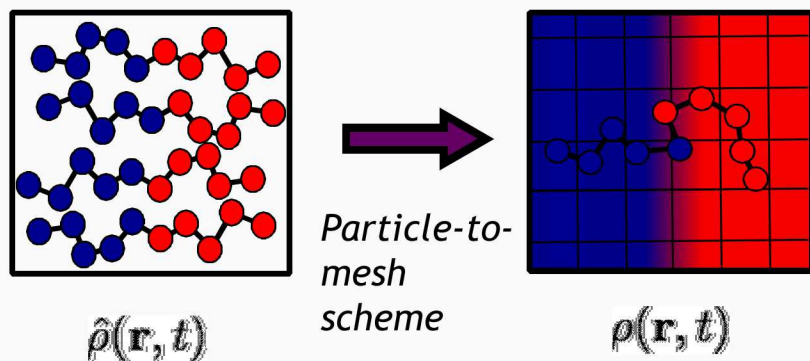
repulsive interactions:

$$u_c(\mathbf{r}) = \frac{\kappa}{2\rho_0} (h_i * h_j)(\mathbf{r})$$

bonding potential:

$$\beta u_{\text{bond}} = \frac{3}{2b^2} |\mathbf{r}_s - \mathbf{r}_{s+1}|^2$$

Theoretically-Informed Langevin Dynamics (TILD)



Similar to:

- Ganesan (SCBD: self-consistent Brownian dynamics)
- Müller (SCMF: single-chain-in-mean-field)
- de Pablo (TICG: theoretically-informed coarse-grained sims)

1. Evaluate bonded forces on all particles (beads in chains)
2. Interpolate particle positions to density on mesh
3. Calculate non-bond forces as fields on the mesh
4. Translate to forces on each particle; update particle positions

$\longrightarrow$ evaluate $F_{int}(\mathbf{r}, t) = - \int d\mathbf{r}' \nabla u(\mathbf{r} - \mathbf{r}') \rho(\mathbf{r}', t)$
 (in k-space with FFT)

Riggleman group implementation

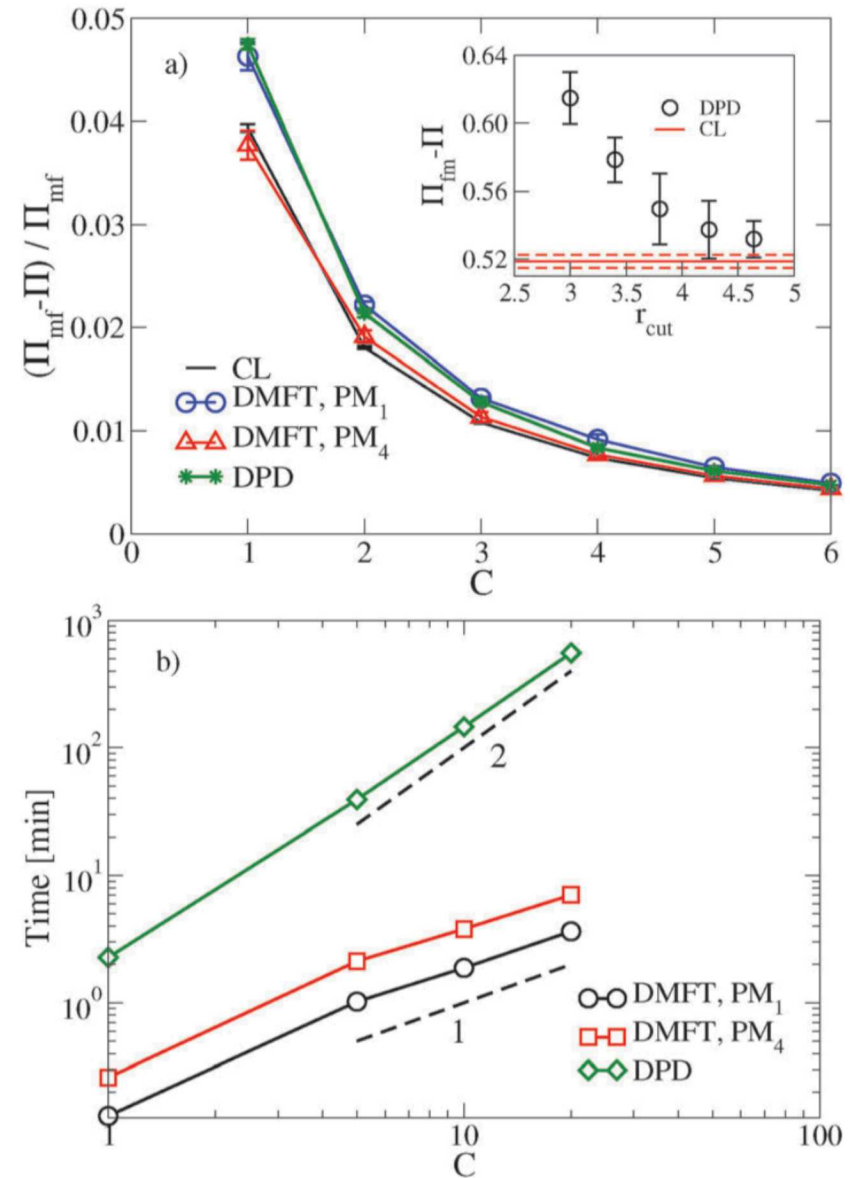
Include torques on grafted nanoparticles

Solve Langevin equation with Gronbech-Jensen and Farago (GJF) scheme

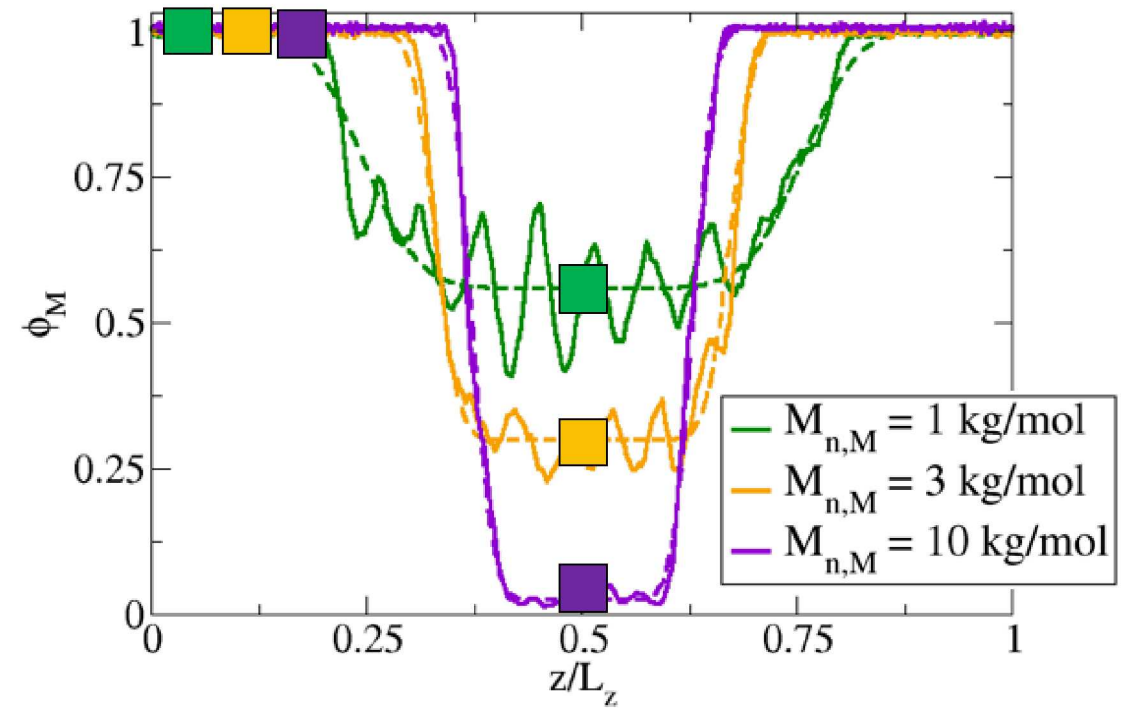
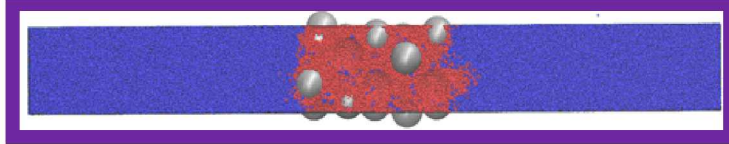
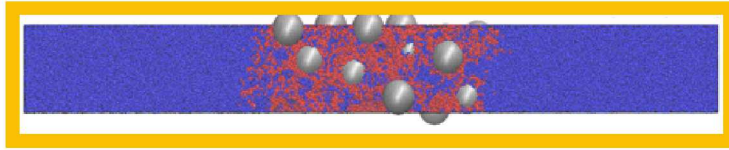
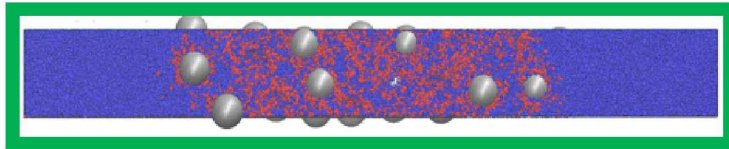
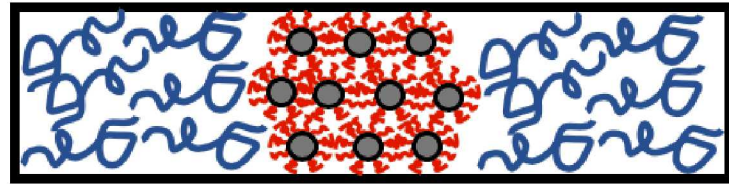
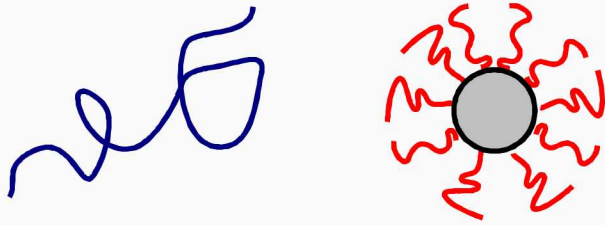
allows large timesteps
good performance compared to DPD simulation

N. Gronbech-Jensen and O. Farago, *Molecular Physics* (2013)

Chao, H., Koski, J. & Riggleman, R. A. *Soft Matter* **13**, 239-249 (2017).



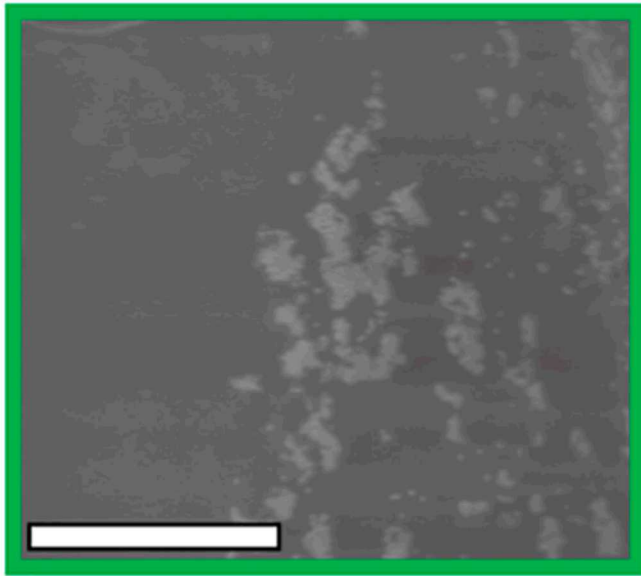
9 Digression: grafted NPs in homopolymer matrix



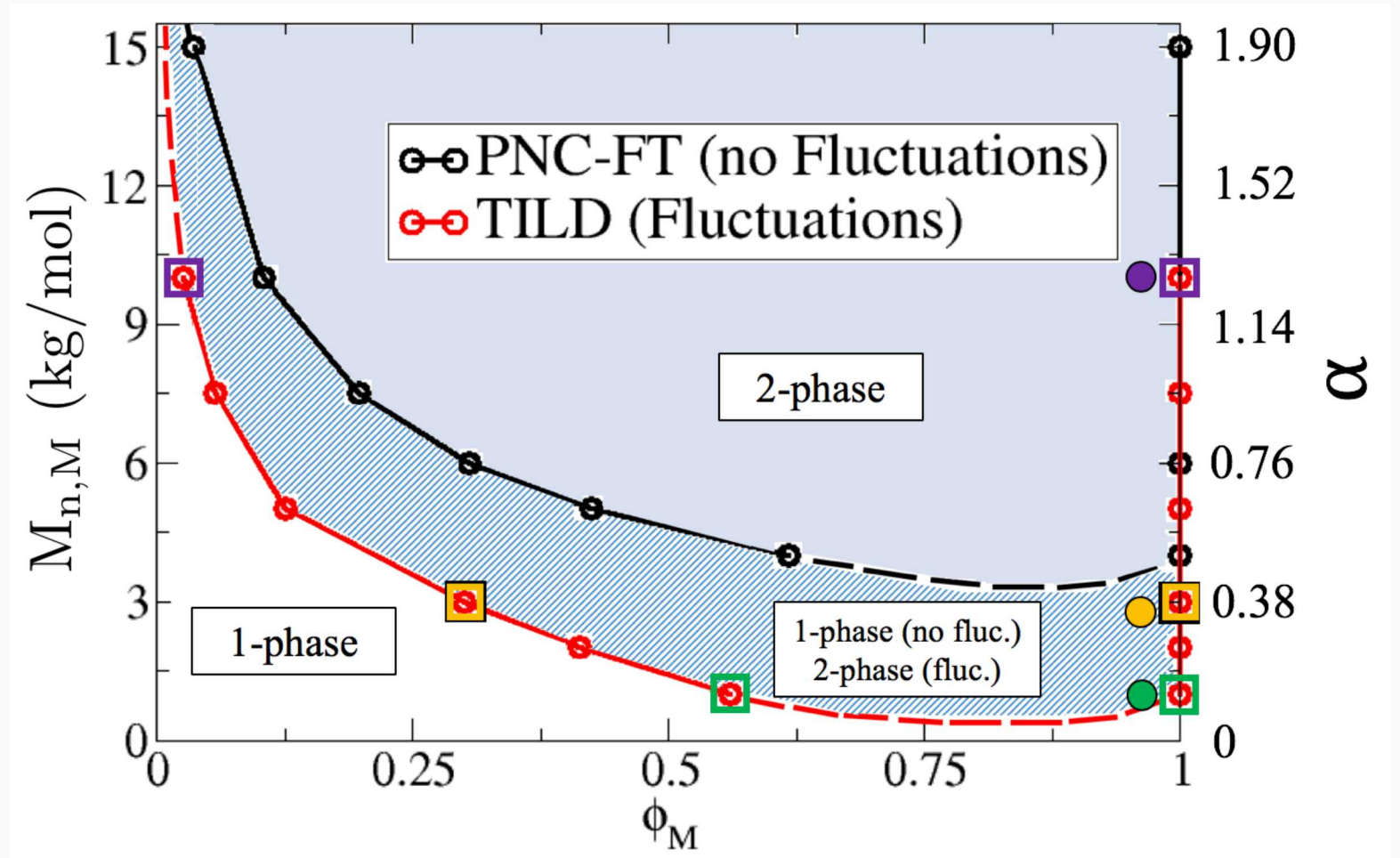
Digression: grafted NPs in homopolymer matrix

PMMA-g-SiO₂ in PS

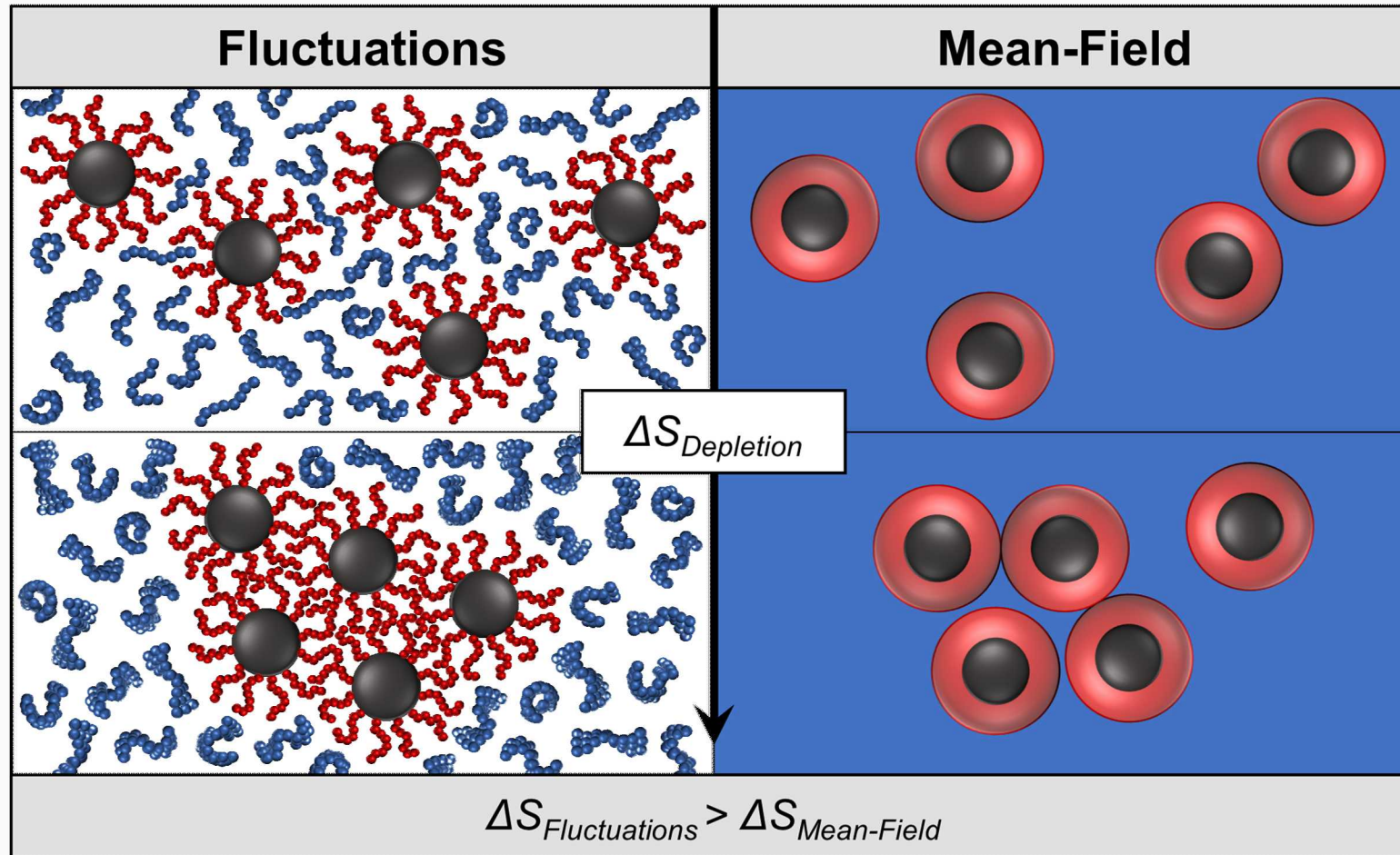
$M_{n,M} = 0.95$ kg/mol (PS)
 $M_{n,G} = 7.9$ kg/mol (PMMA)
 $\sigma = 0.26$ chains/nm²



scale = 1 μ m



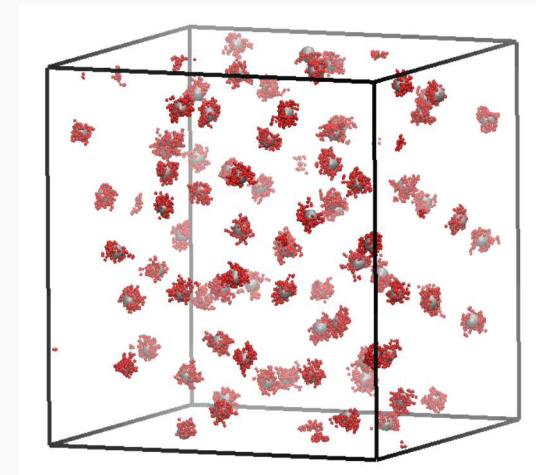
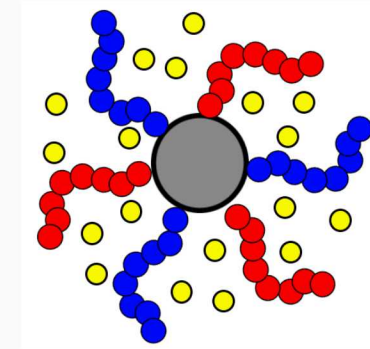
Digression: grafted NPs in homopolymer matrix



extra entropy leads to extra depletion interactions

Rest of the talk

- mixed brushes on single particles
 - SCFT structure
 - TILD structures
- assembly of mixed brush NPs
 - TILD only



Single mixed brush NPs: nonselective solvent

equal chain lengths, $N_A = N_B = 60$

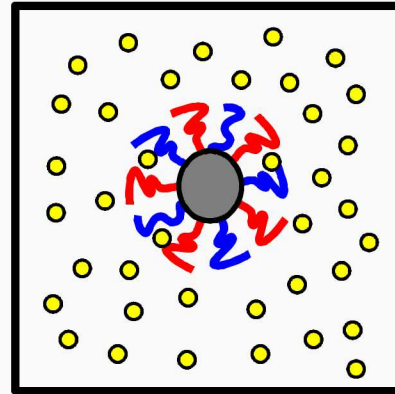
equal fractions, $f_A = f_B = 0.5$

monomer size $d = 0.73b$

$\chi_{AB}N = 28.3$

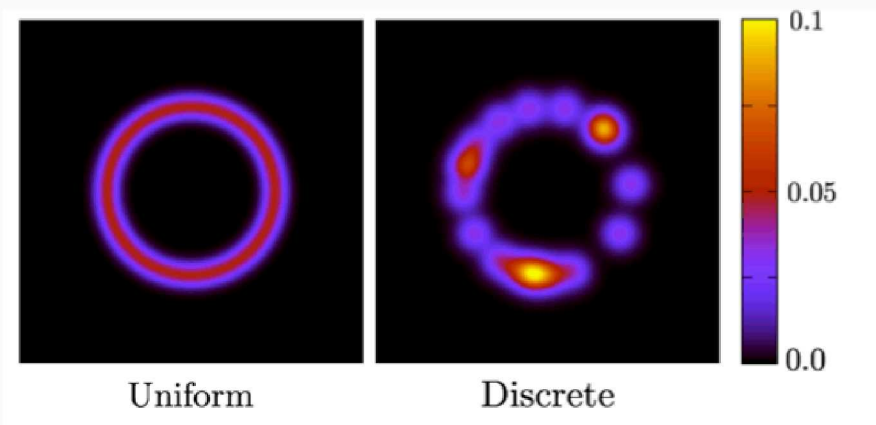
$\chi_{AS} = \chi_{BS} = \chi_S$

vary: R_p/R_g , σ , χ_S



Three calculations:

1. SCFT with uniform grafting density
2. SCFT with random grafting density
3. TILD with random grafting density



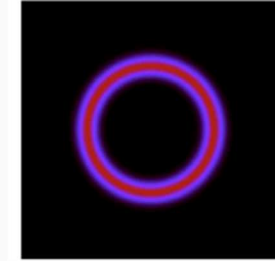
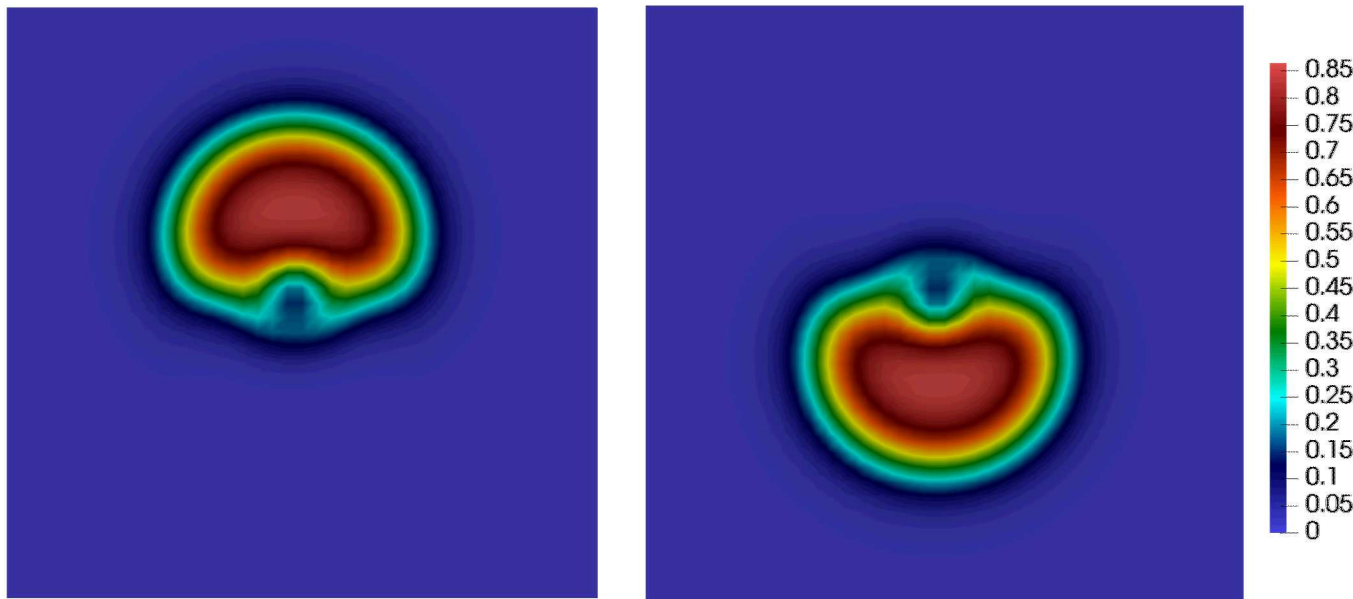
SCFT for single particles

$$\chi_{AB}N = 28.3$$

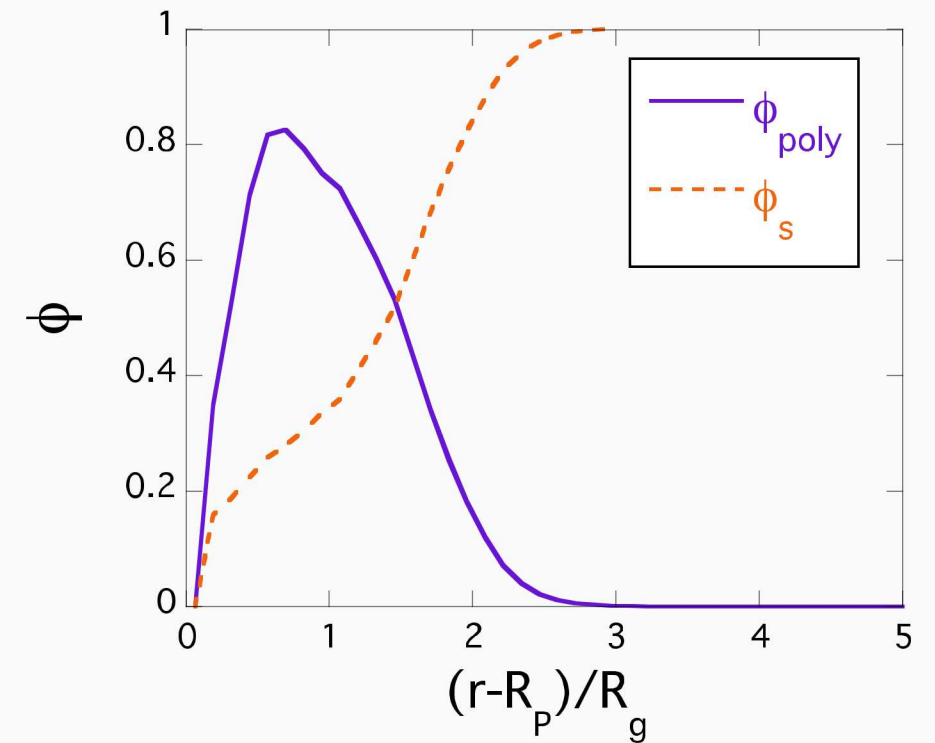
$$\chi_S = 1$$

$$R_p/R_g = 1/3$$

$$\sigma = 1.7/d^2$$


 ϕ_A
 ϕ_B


radial brush/solvent profiles



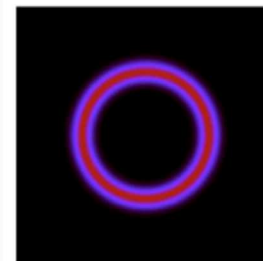
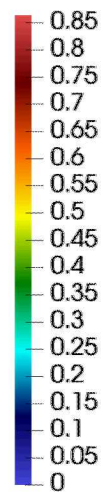
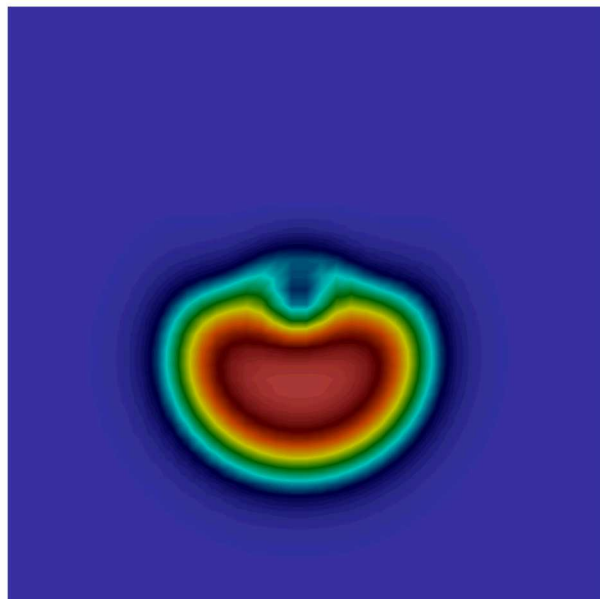
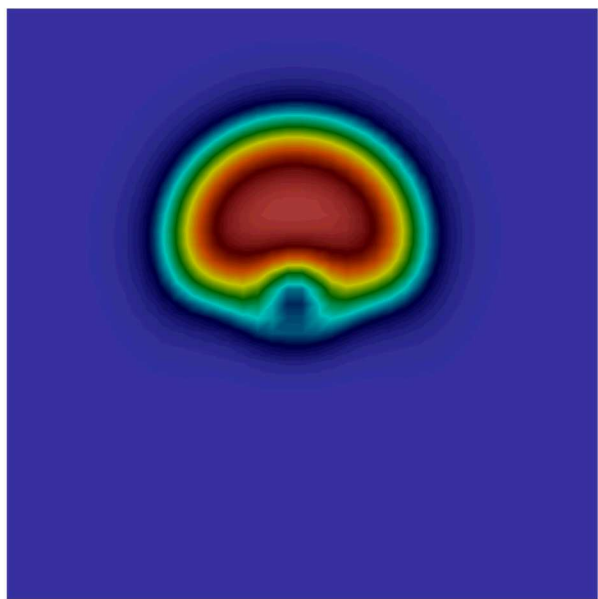
SCFT for single particles

$$\chi_{AB}N = 28.3$$

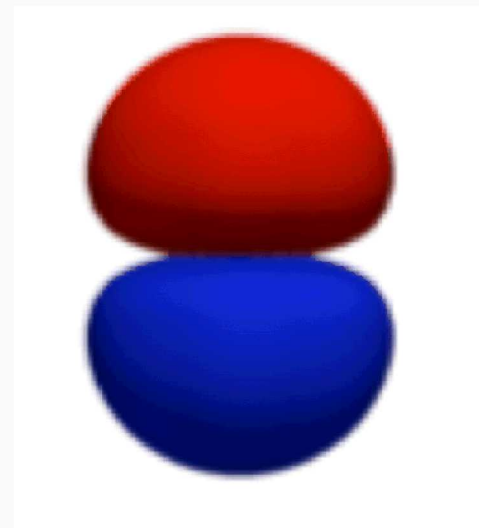
$$\chi_S = 1$$

$$R_p/R_g = 1/3$$

$$\sigma = 1.7/d^2$$

 ϕ_A ϕ_B 

density isosurfaces at $\phi = 0.5$

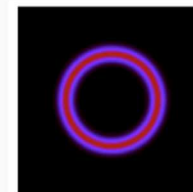


SCFT for single particles

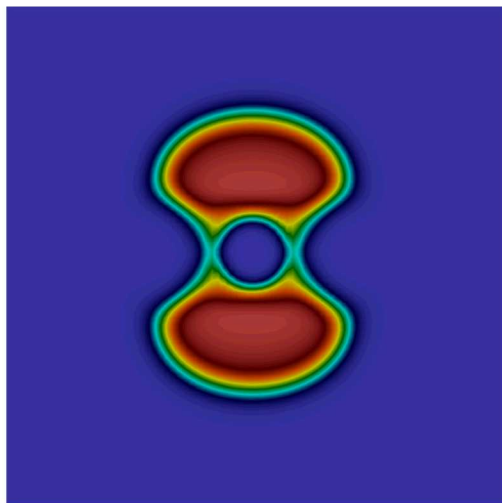
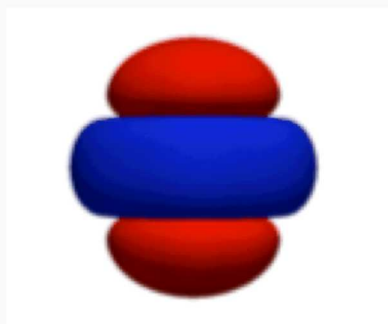
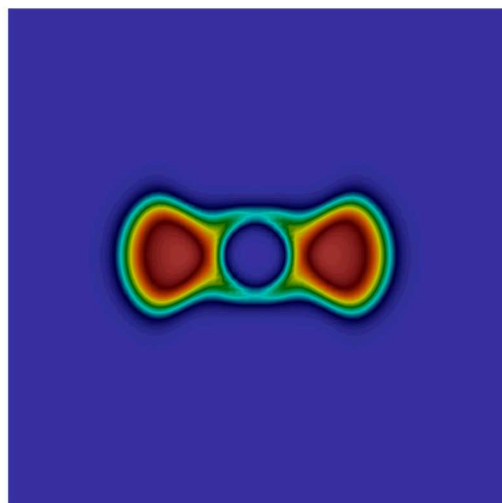
$$\chi_{AB}N = 28.3$$

$$\chi_S = 1$$

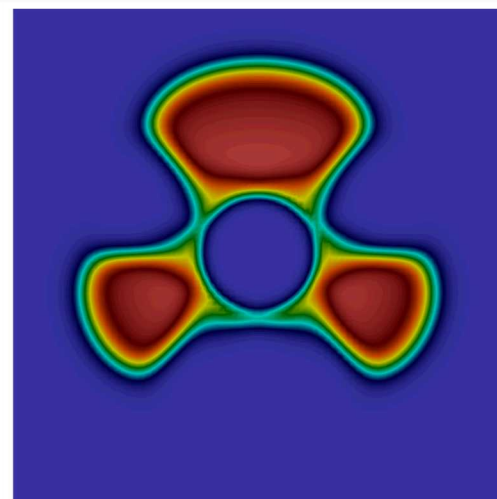
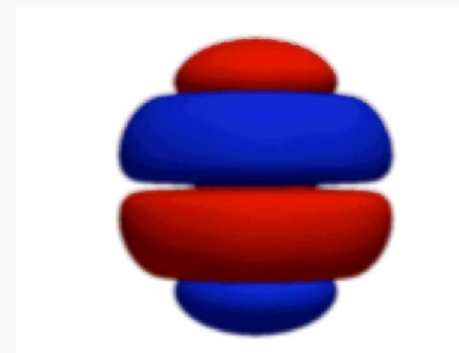
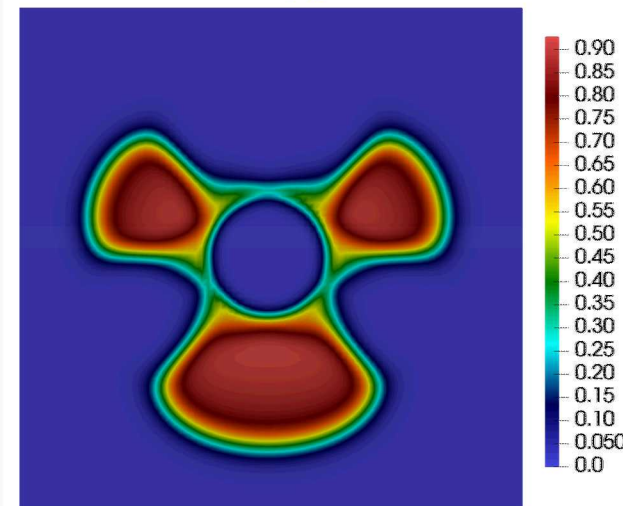
$$\sigma = 1.7/d^2$$



$$R_p/R_g = 1$$

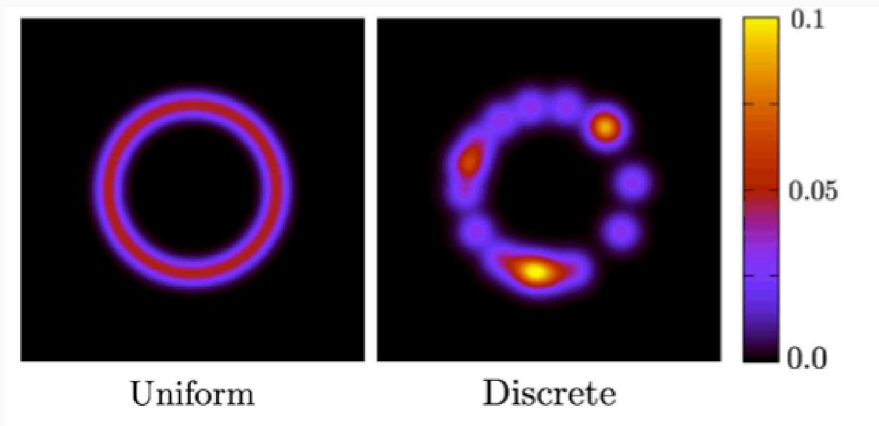
 ϕ_A

 ϕ_B


$$R_p/R_g = 5/3$$

 ϕ_A

 ϕ_B


Random discrete grafting sites, SCFT

uniform grafting is unlikely
allow random discrete grafting



$$\chi_{AB}N = 28.3$$

$$\chi_S = 1.0$$

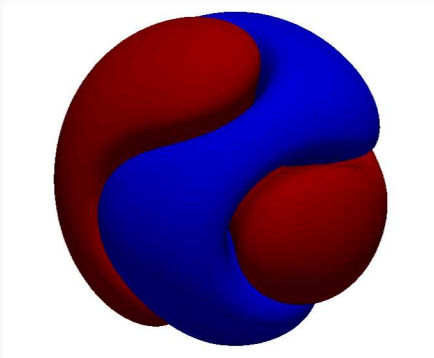
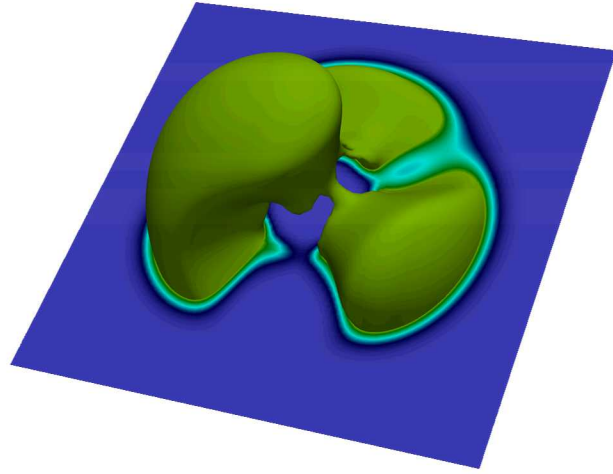
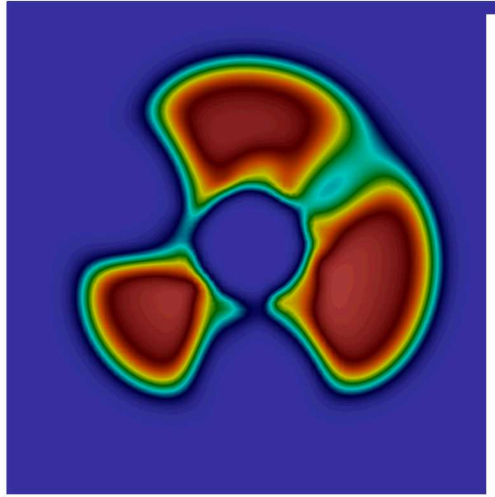
$\sigma = 1.7/d^2$	$R_p/R_g = 1/3$	$R_p/R_g = 1$	$R_p/R_g = 5/3$
Uniform Grafting Mean-Field			
Discrete Grafting Mean-Field			

random grafting structures are less ordered

Disordered brush structures, $R_p/R_g = 5/3$

SCFT, random grafting

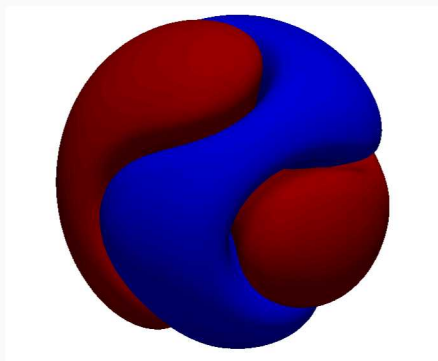
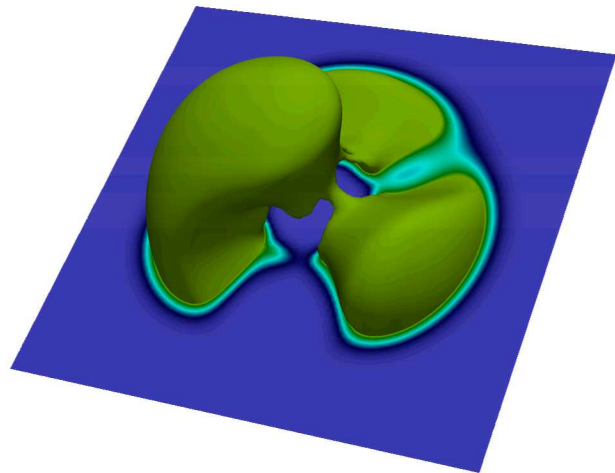
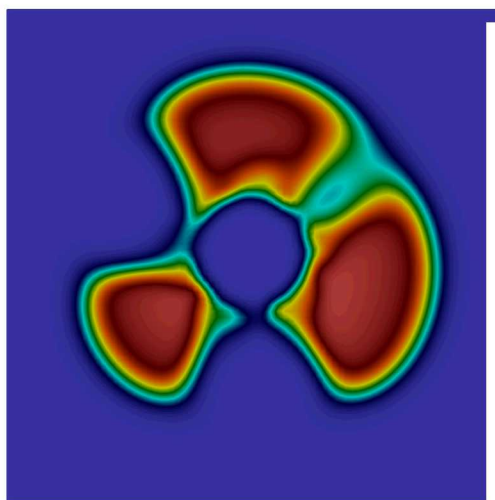
ϕ_A



Disordered brush structures, $R_p/R_g = 5/3$

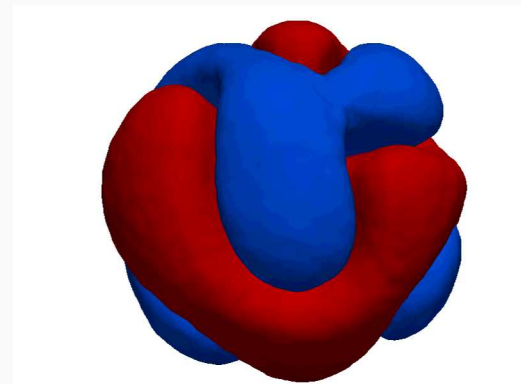
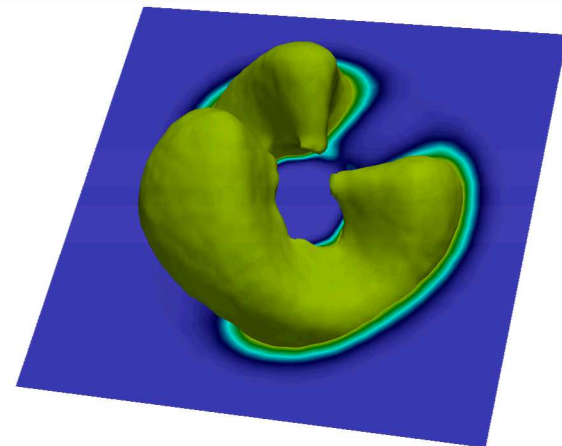
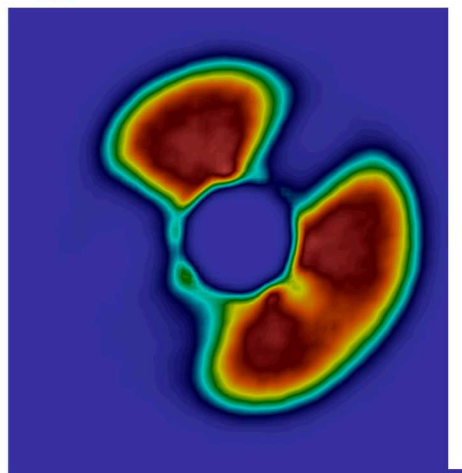
SCFT, random grafting

ϕ_A



TILD, random grafting

ϕ_A



TILD vs SCFT

random grafting + thermal fluctuations

$$\chi_{AB}N = 28.3$$

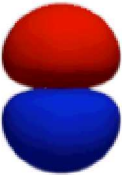
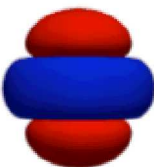
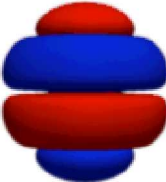
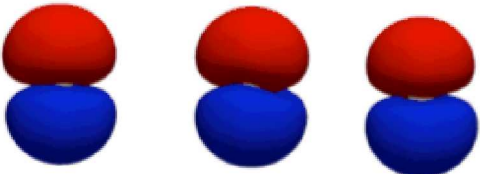
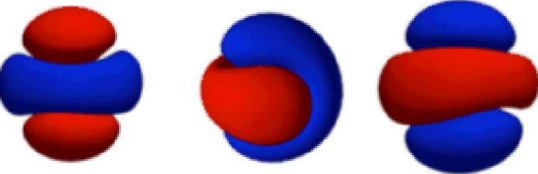
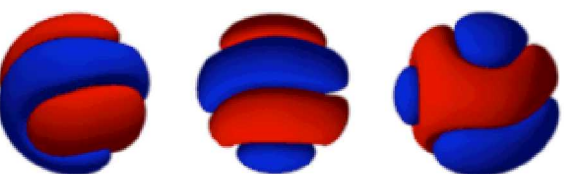
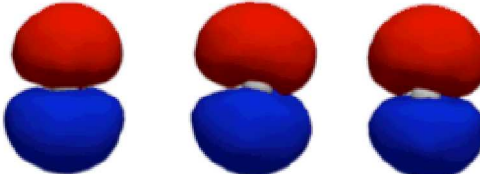
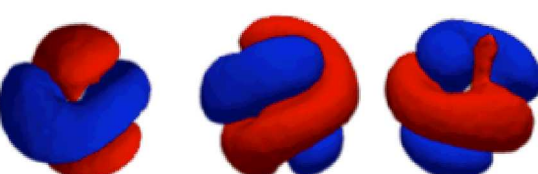
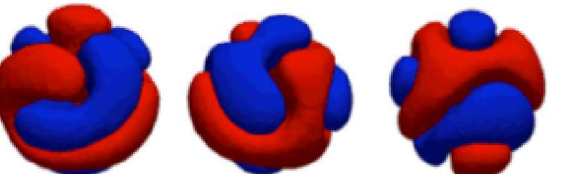
$$\chi_S = 1.0$$

$$\sigma = 1.7/d^2$$

$$R_p/R_g = 1/3$$

$$R_p/R_g = 1$$

$$R_p/R_g = 5/3$$

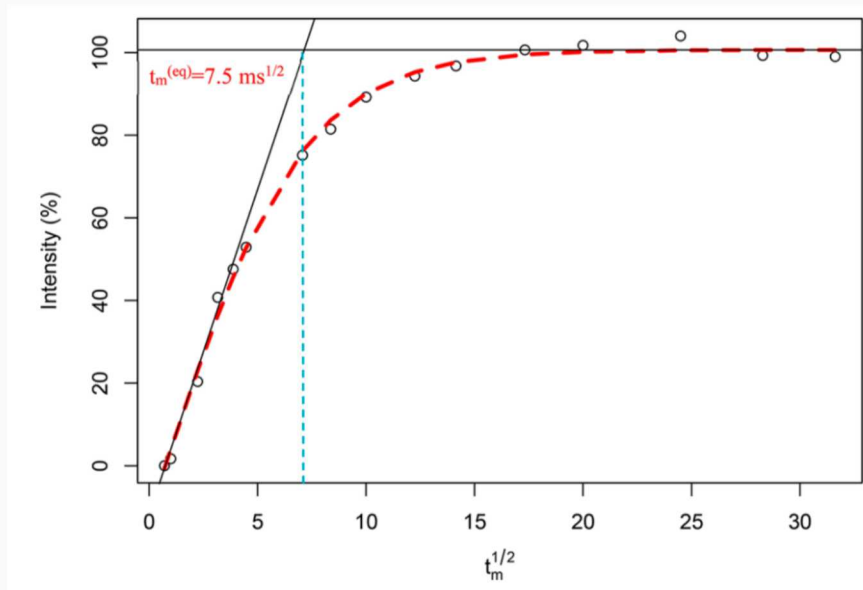
	$R_p/R_g = 1/3$	$R_p/R_g = 1$	$R_p/R_g = 5/3$
Uniform Grafting Mean-Field			
Discrete Grafting Mean-Field			
Discrete Grafting Fluctuations			

prediction: Janus phase robust to fluctuations!

Experimental evidence of grafted Janus NPs?

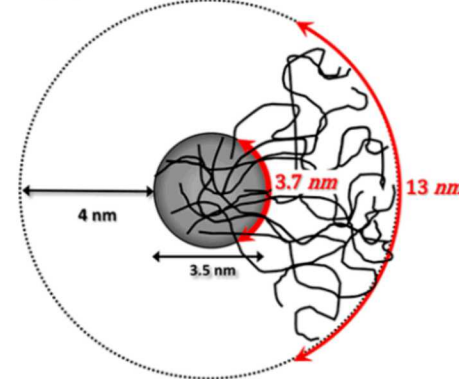
PS-PEO on ZrO_2 NPs

^1H NMR spin diffusion

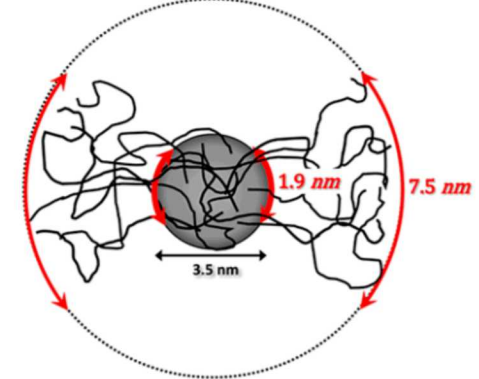


consistent with

(a) Single patch



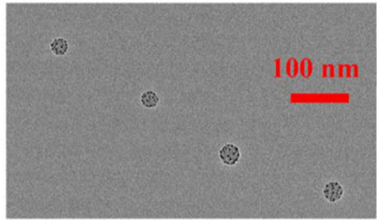
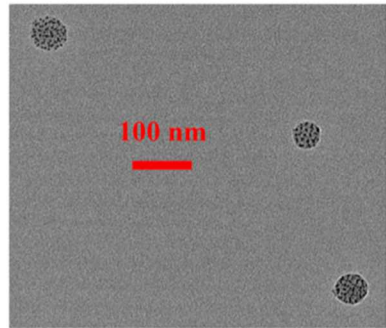
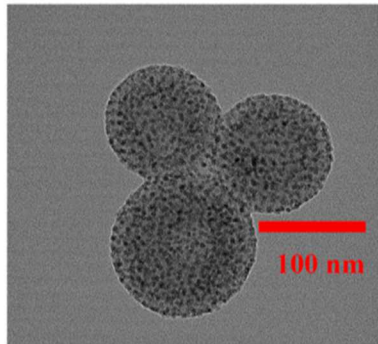
Two patches



Mixed brush NP assembly in selective solvent

example: PEO-PS on ZrO_2 in THF/water

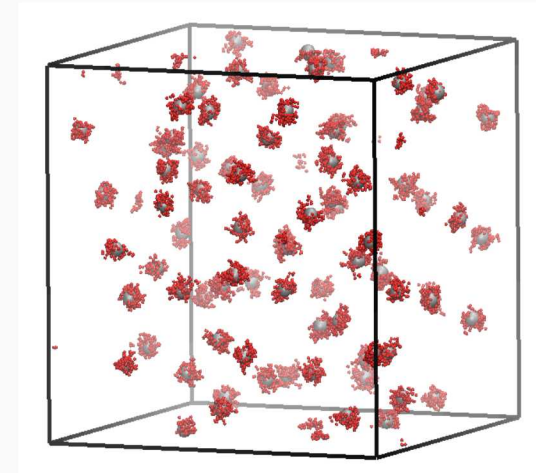
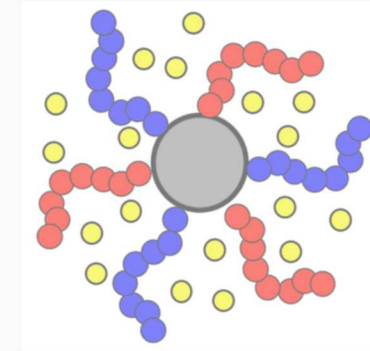
PS fraction

0.19	Densely packed spheres (dia. 30-36 nm)	
0.40	Densely packed spheres (dia. 45-60 nm)	
0.93	Vesicles, (dia. 75-115 nm)	

Guzman-Juarez, et al,
Macromolecules **51**, 9951–9960
(2018).

Rest of the talk

- mixed brushes on single particles
 - SCFT structure
 - TILD structures
- assembly of mixed brush NPs
 - TILD only



Mixed brush NPs in selective solvent

A chains in bad solvent: $\chi_{AS} = \chi_S$

Rest of talk: **B chains** in good solvent: $\chi_{BS} = 0$

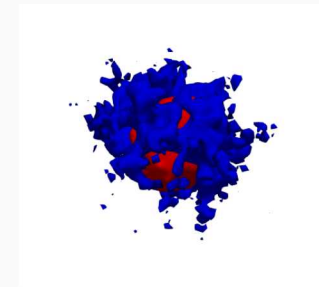
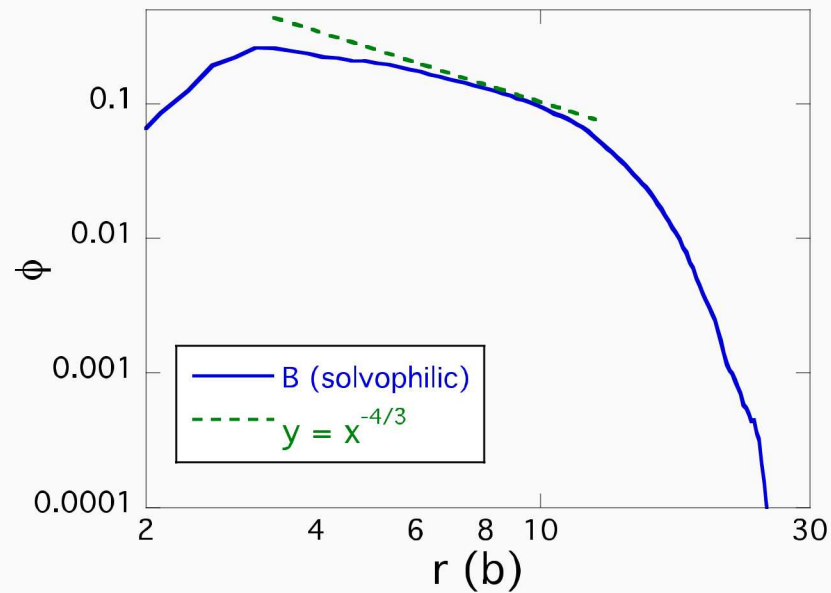
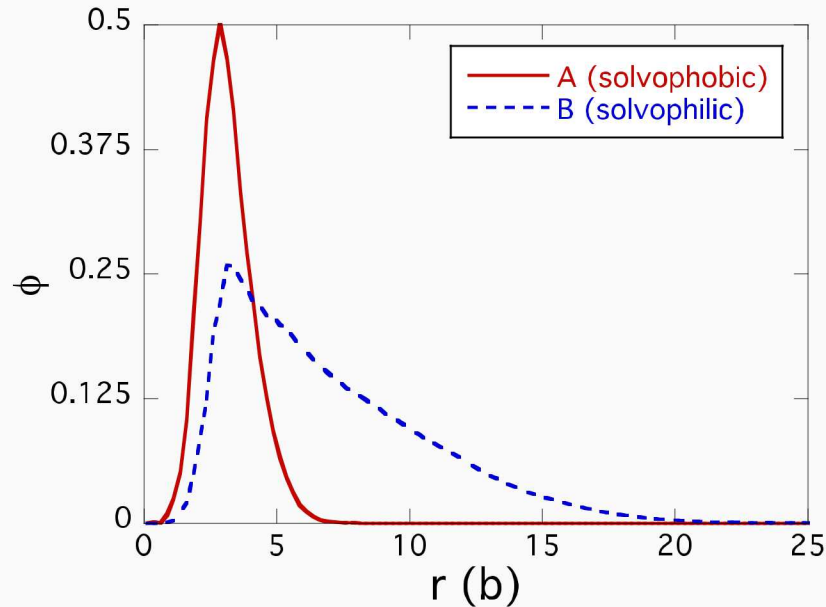
immiscible chains: $\chi_{AB} = 1$

$R_p = 2b$, $\sigma = 1/b^2$ (50 grafted chains per particle)

For asymmetric chain lengths,
get vertical phase separation

$$\chi_S = 1.25, N_A = 6, N_B = 54$$

$$f_A = 0.5$$



Daoud-Cotton for stars

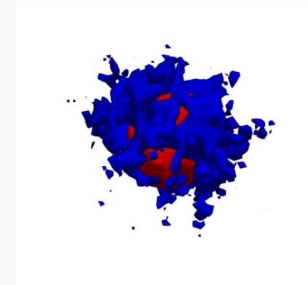
$$\phi(r) \sim r^{-4/3}$$

Dispersed phase

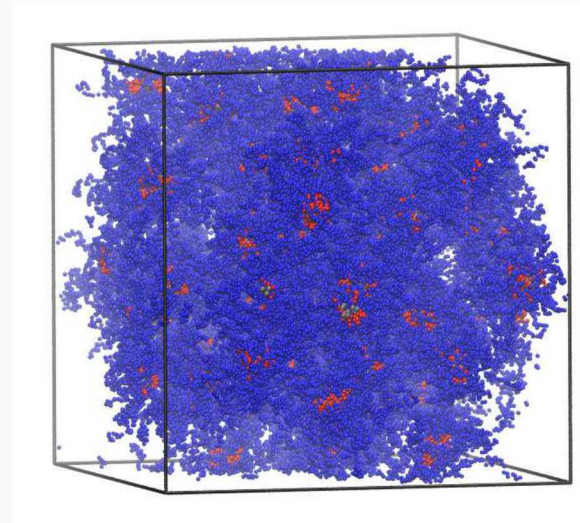
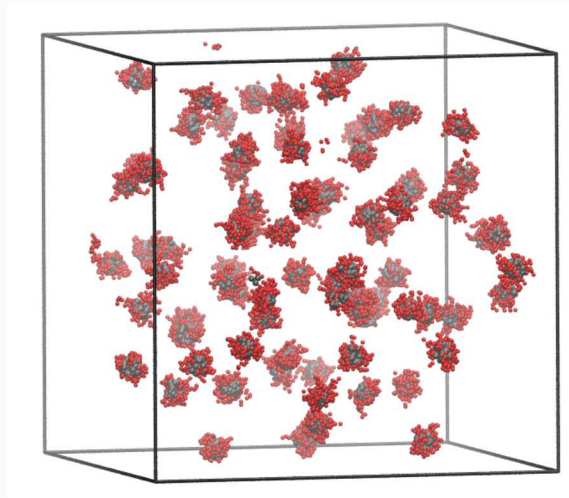
$$\chi_S = 1.25, N_A = 6, N_B = 54$$

$$f_A = 0.5$$

long solvophilic chains
short solvophobic chains



80 particles initially in center of box

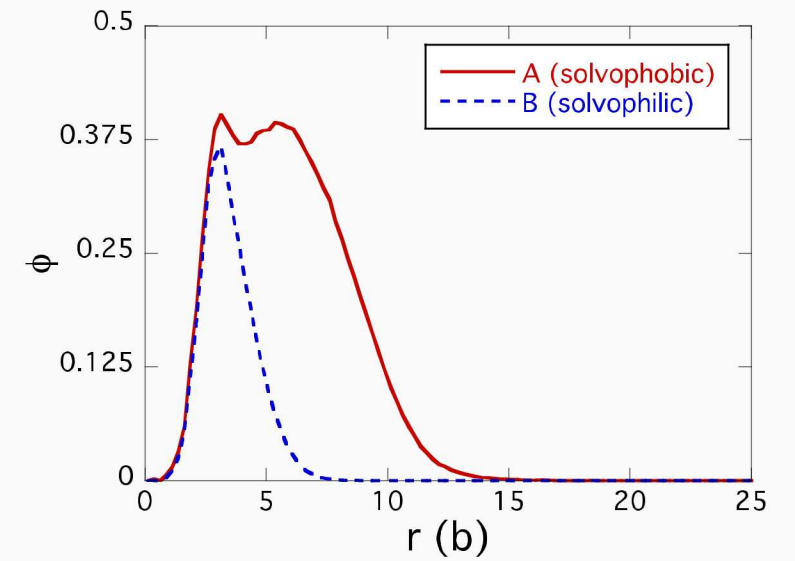
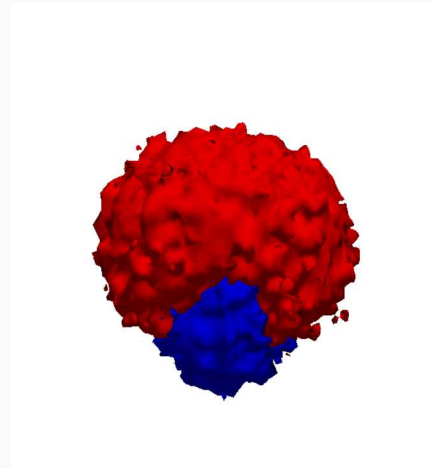
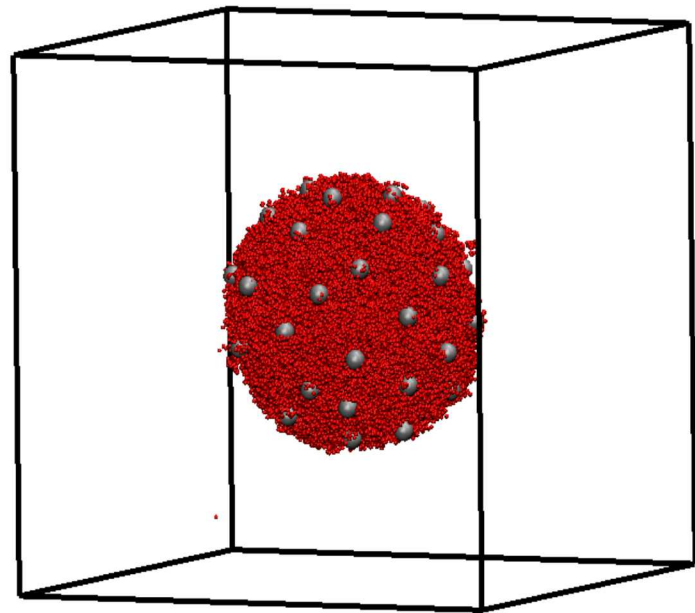


Macrophase separation

$$\chi_S = 2, N_A = 54, N_B = 6$$

$$f_A = 0.5$$

short solvophilic chains
long solvophobic chains



“Ordered” NP assemblies: similar chain lengths

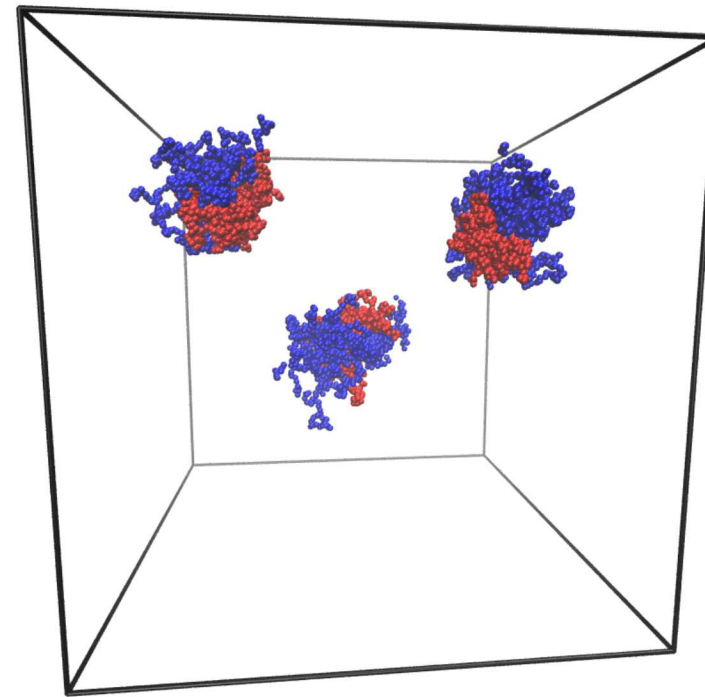
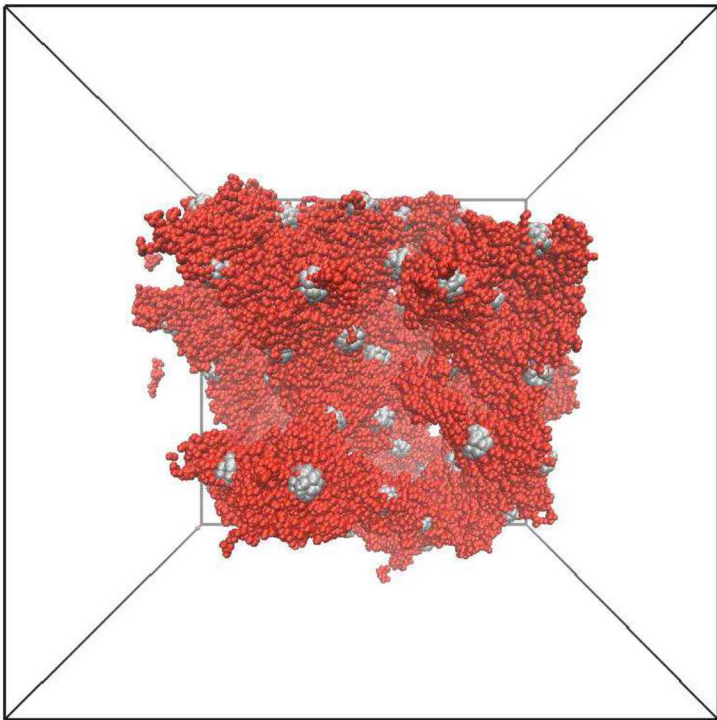
A chains in bad solvent: $\chi_{AS} = 1.25$

B chains in good solvent: $\chi_{BS} = 0$

immiscible chains: $\chi_{AB} = 1$

80 particles initially in center of box

$$N_A = N_B = 54, f_A = 0.5, \sigma = 1/b^2$$



“Ordered” NP assemblies

A chains in bad solvent: $\chi_{AS} = 1.25$

B chains in good solvent: $\chi_{BS} = 0$

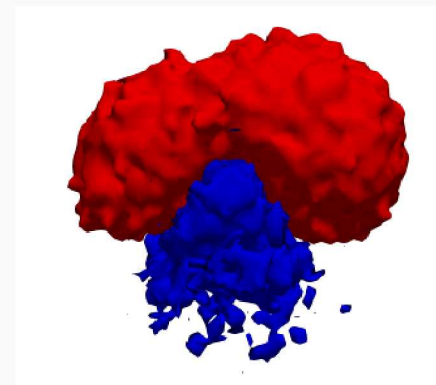
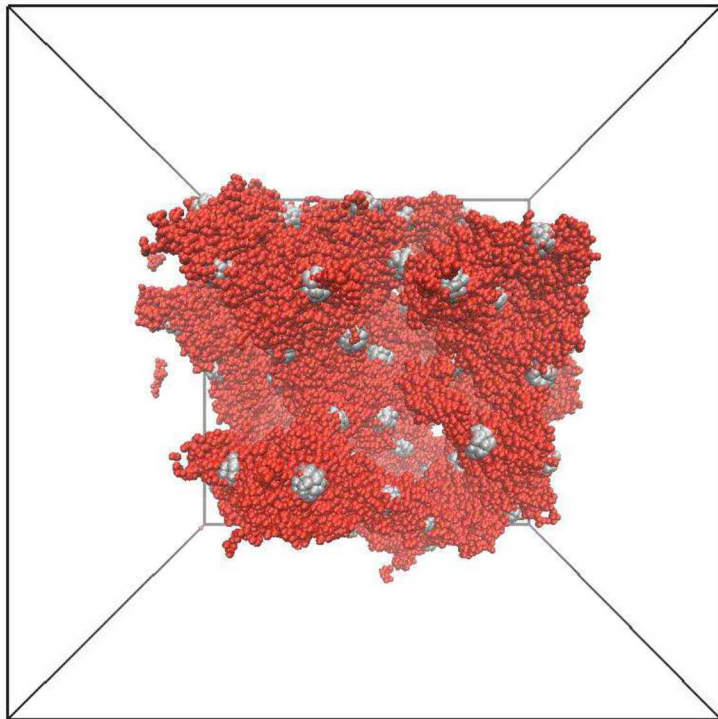
immiscible chains: $\chi_{AB} = 1$

80 particles initially in center of box

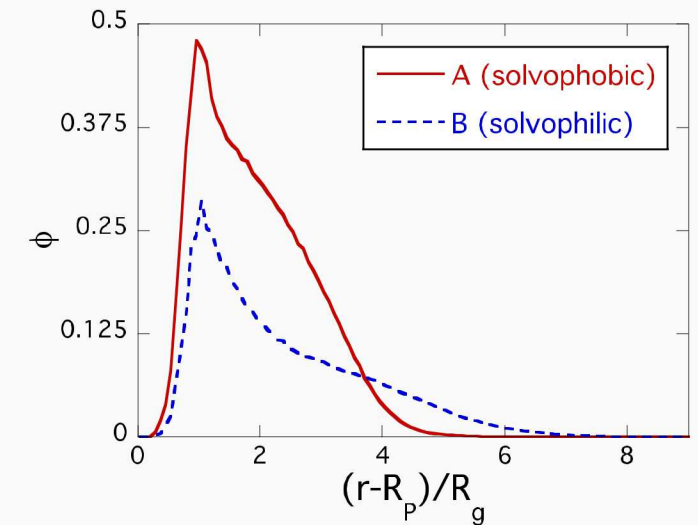
$$N_A = N_B = 54, f_A = 0.5, \sigma = 1/b^2$$

$$R_p = 0.7R_g$$

equivalent single NP



average configuration

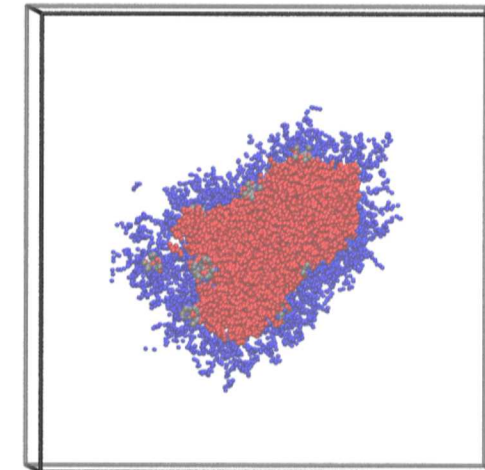
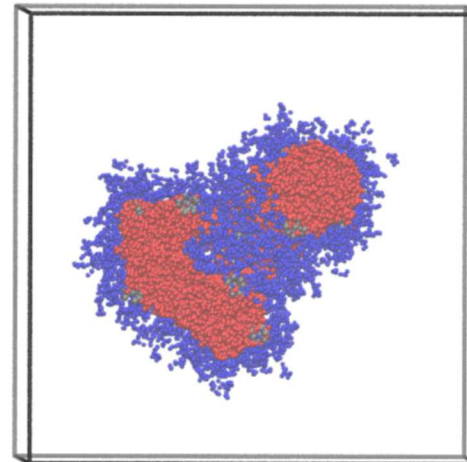
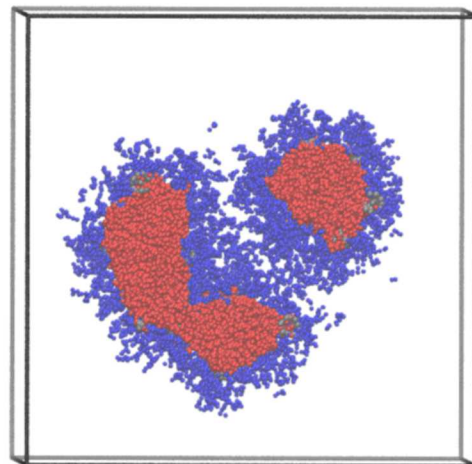
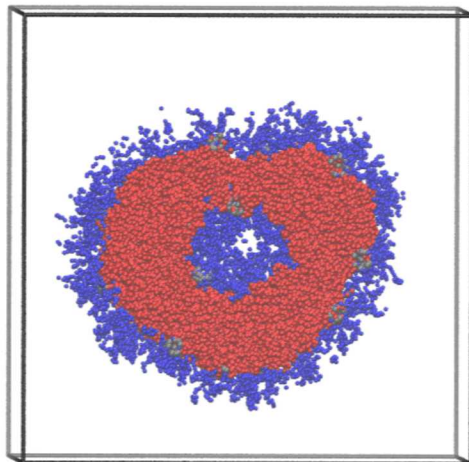
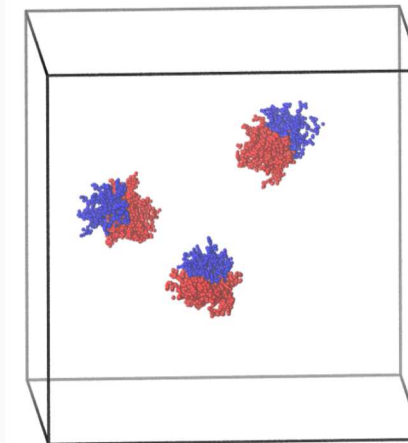
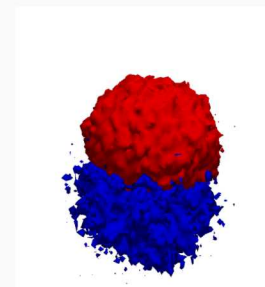
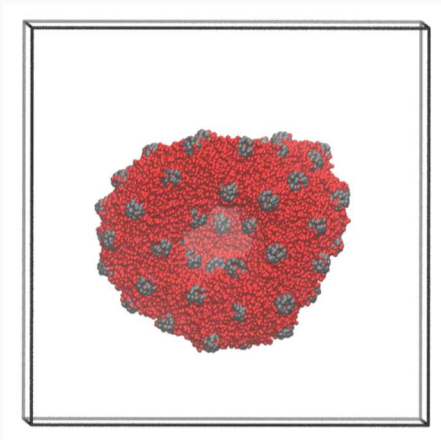


“Nearly Vesicle”

$$\chi_S = 2, N_A = 54, N_B = 24$$

$$f_A = 0.5$$

10b thick slices:

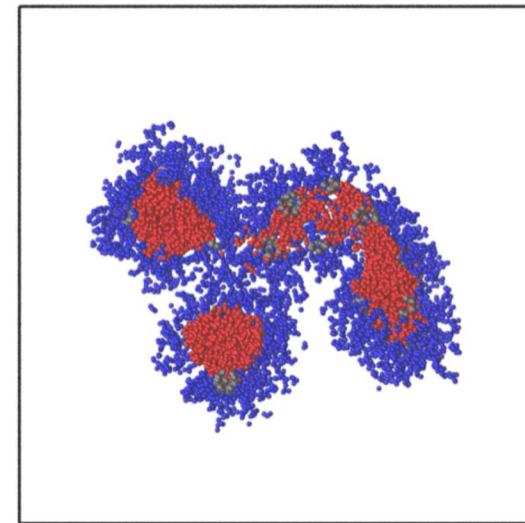
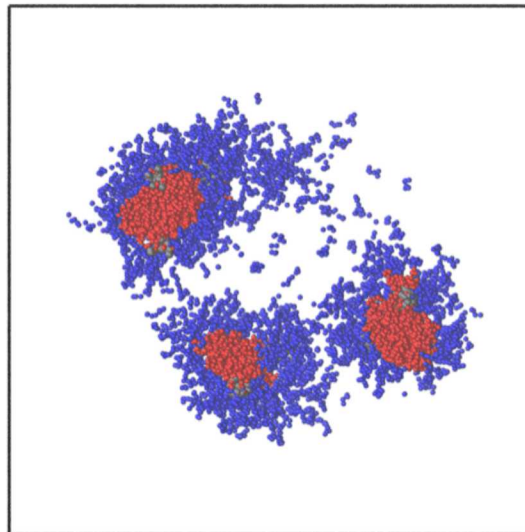
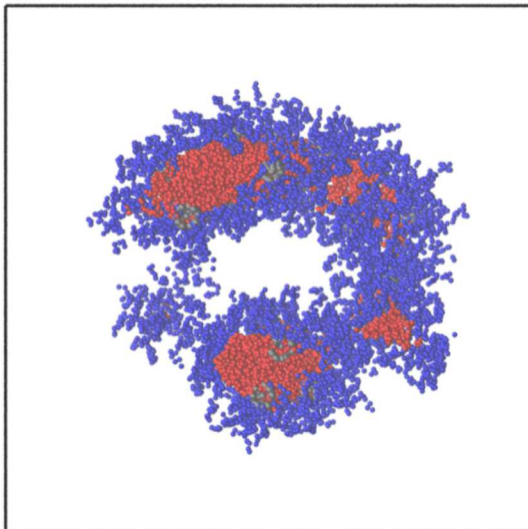
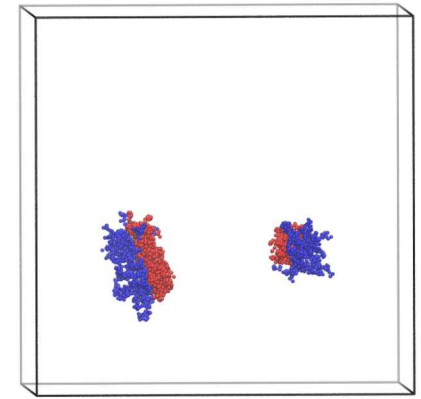
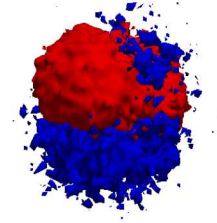
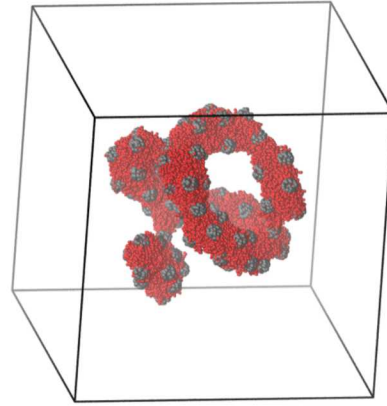


“Connected strings”

$$\chi_S = 2, N_A = 24, N_B = 24$$

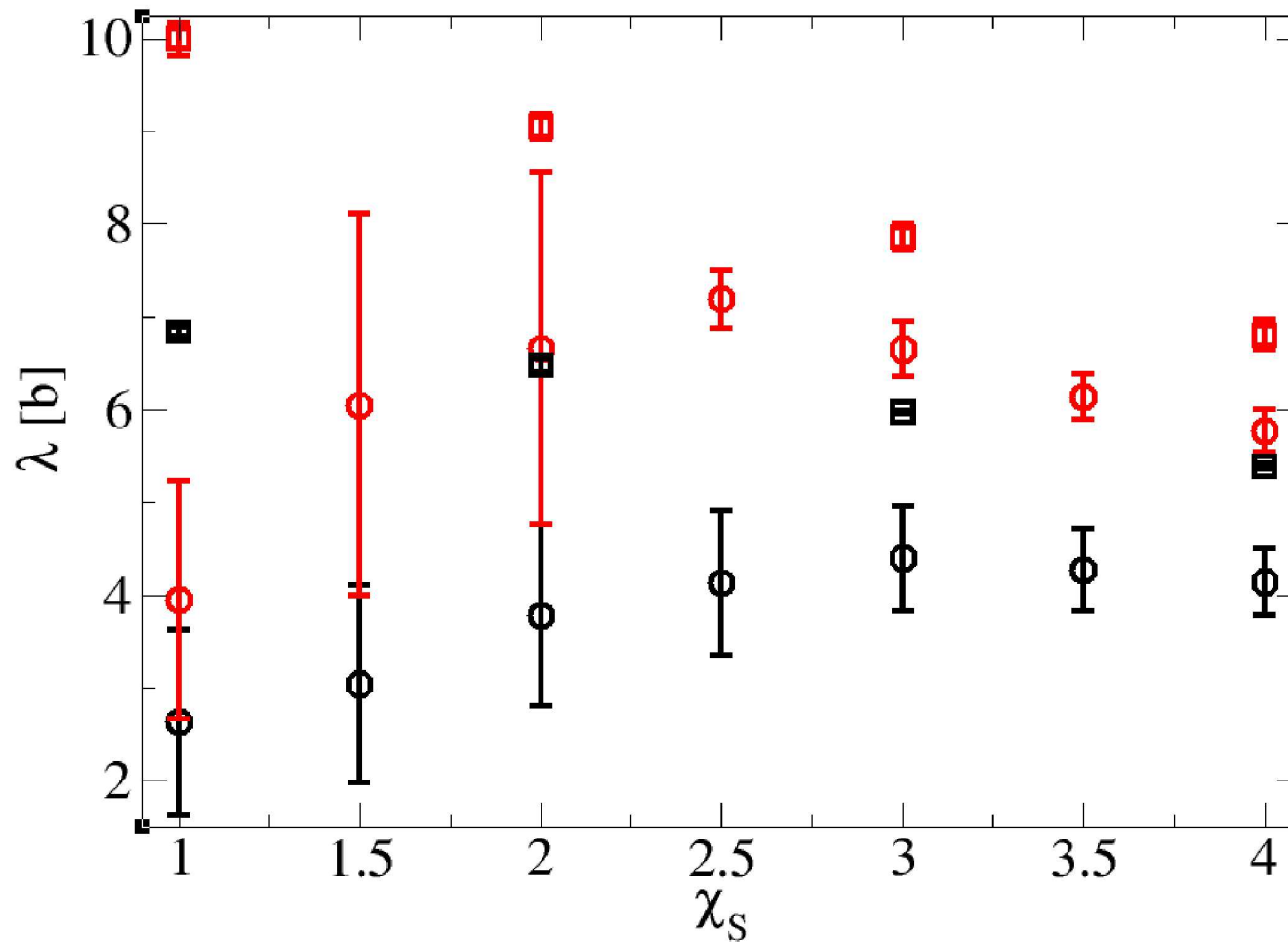
$$f_A = 0.5$$

10b thick slices:



“Janus” nature of mixed brush NPs

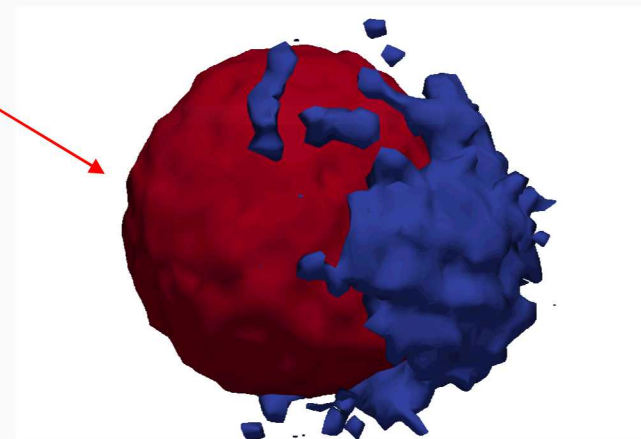
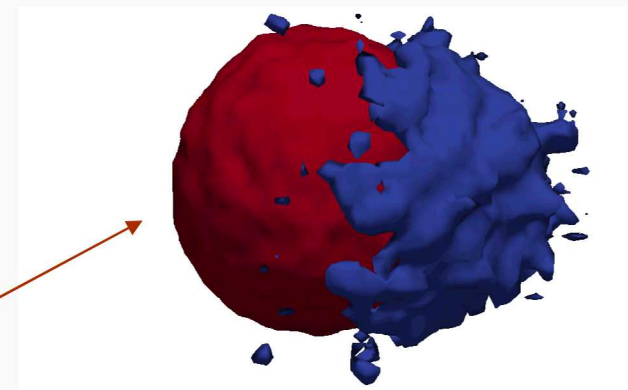
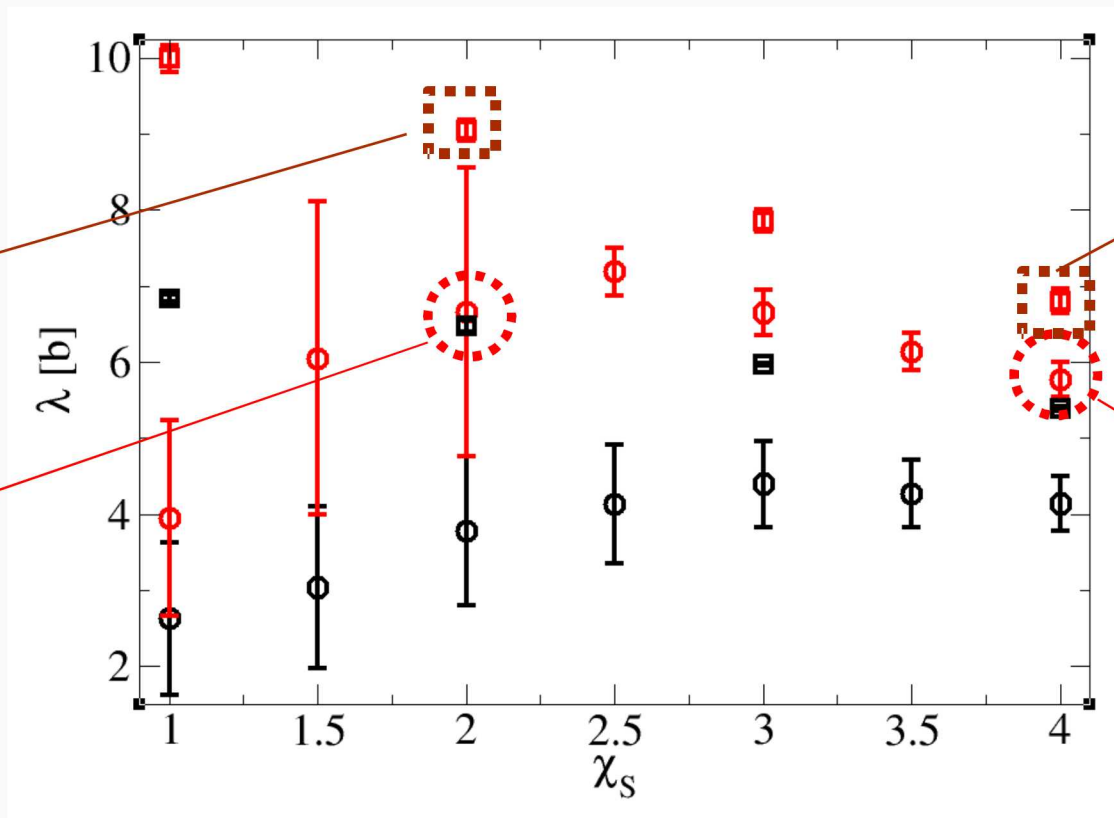
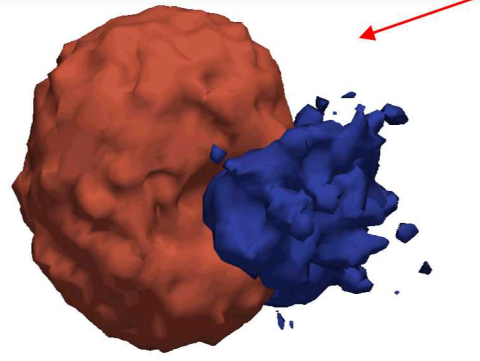
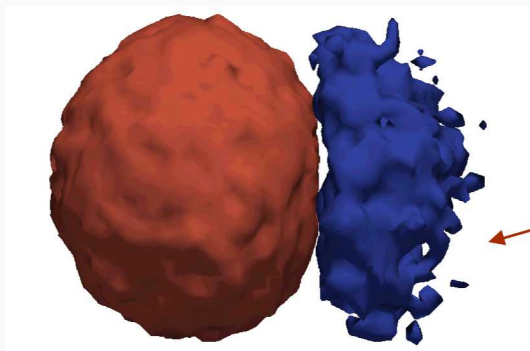
$$\lambda = ||(\text{com}_A) - (\text{com}_B)||$$



- mixed, $N_A = N_B = 24$
- mixed, $N_A = N_B = 54$
- Janus, $N_A = N_B = 24$
- Janus, $N_A = N_B = 54$

“Janus” nature of mixed brush NPs

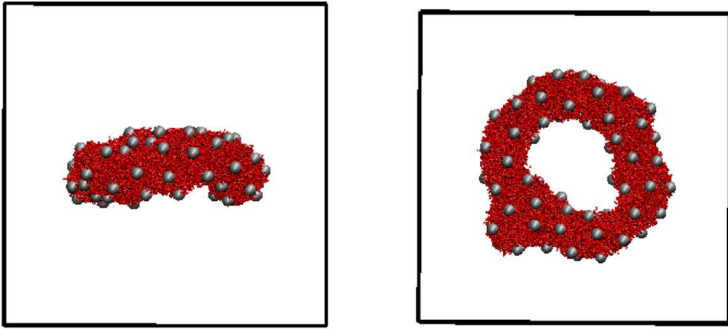
$$\lambda = ||(\text{com}_A) - (\text{com}_B)||$$



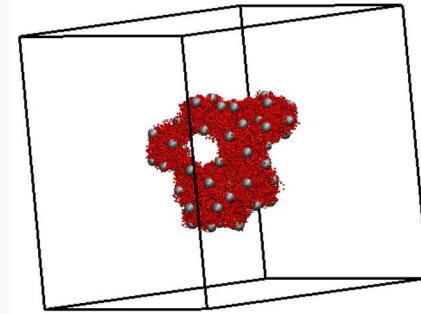
Janus-grafted vs random-grafted NPs

$$\chi_S = 3, N_a = 24, N_b = 24$$

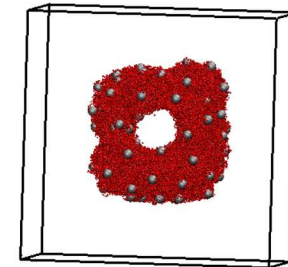
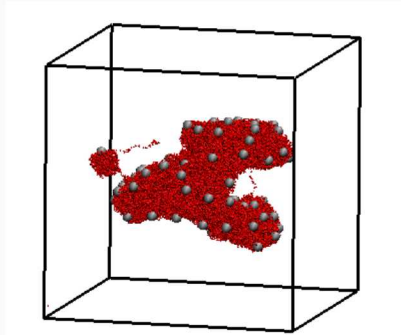
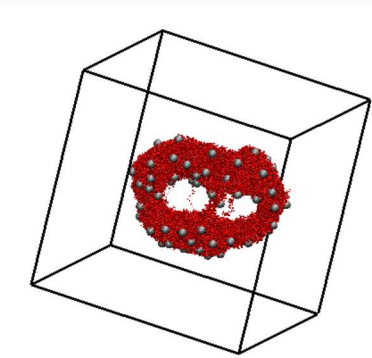
Janus



random



$$\chi_S = 3, N_a = 54, N_b = 54$$

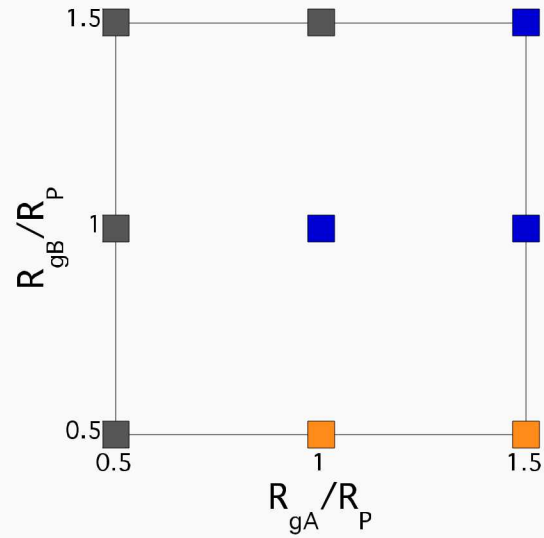


Phase maps for random-grafted

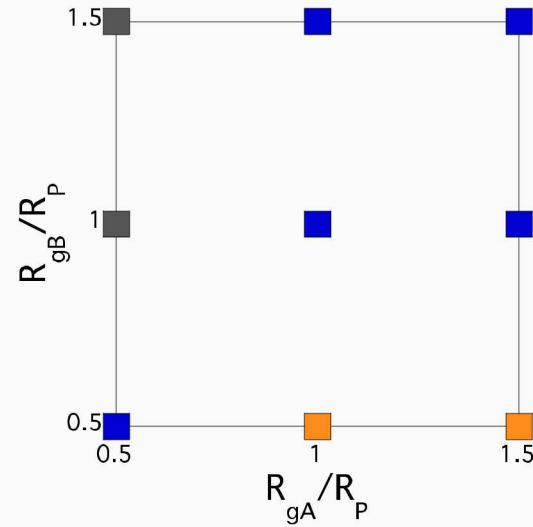


$$\chi_s = 2$$

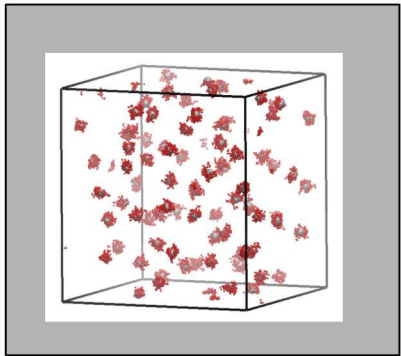
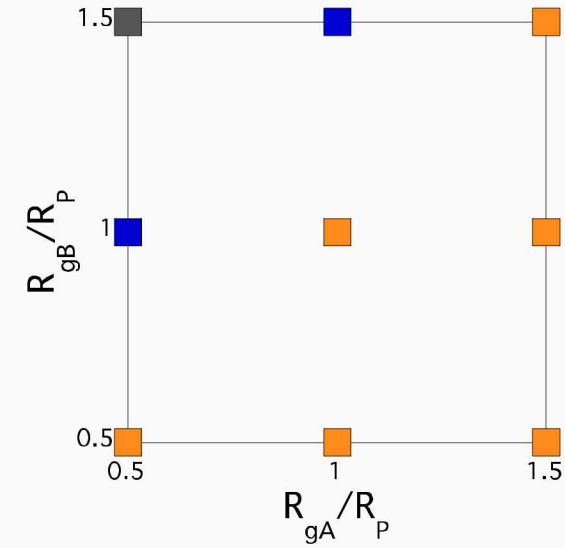
$$f_A = 0.25$$



$$f_A = 0.5$$

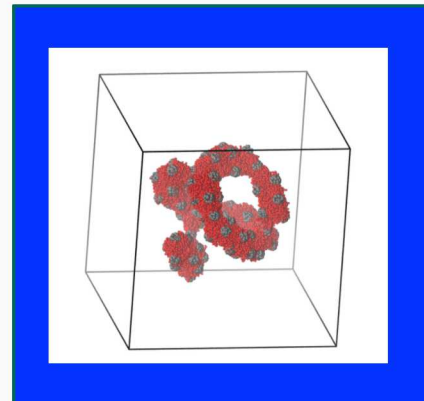


$$f_A = 0.75$$



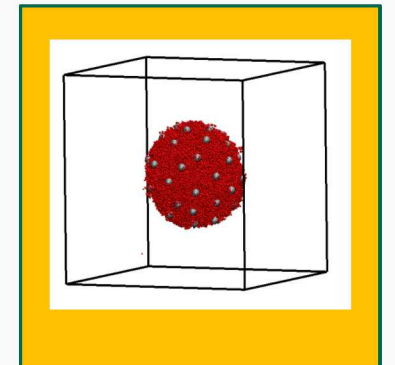
long solvophilic
short solvophobic

Dispersed



“Janus”: Ordered

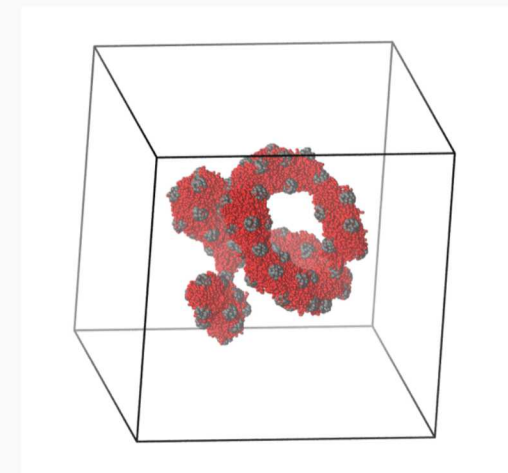
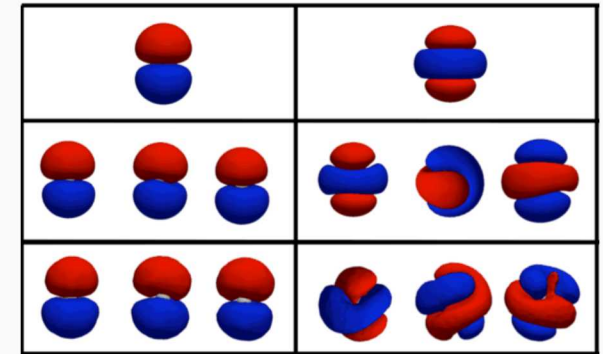
short solvophilic
long solvophobic



Phase Separated

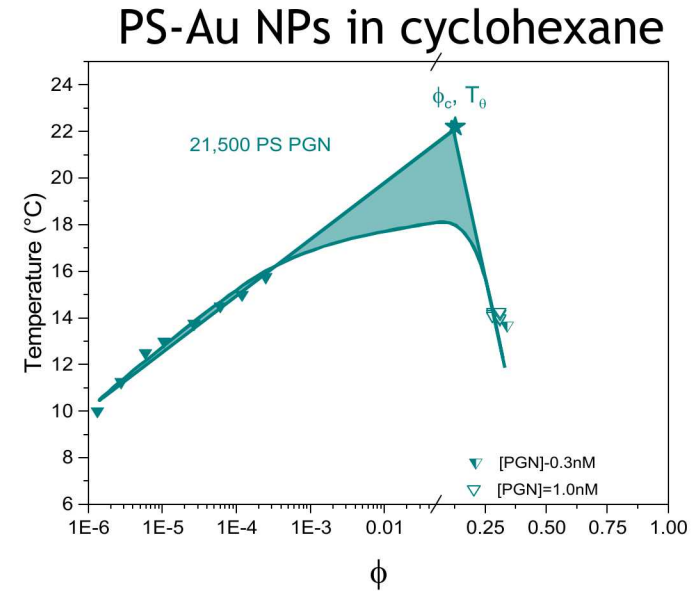
Conclusions

- single mixed brush NPs
 - TILD predicts more defective NPs than SCFT
 - Janus phase robust to fluctuations
- mixed brush NP assembly
 - very asymmetric systems: dispersed or phase separated
 - similar chain lengths, volume fractions
 - Janus-like single particles
 - stringy or vesicle-like aggregates
 - more clear structure for higher χ_s



Future Directions

- further quantify assembly
- phase behavior of homopolymer-grafted NPs in solvent
- dynamics?



courtesy Rich Vaia

Structure of polymer brushes

free polymers are random walks

$$R_e \sim N^{1/2}$$

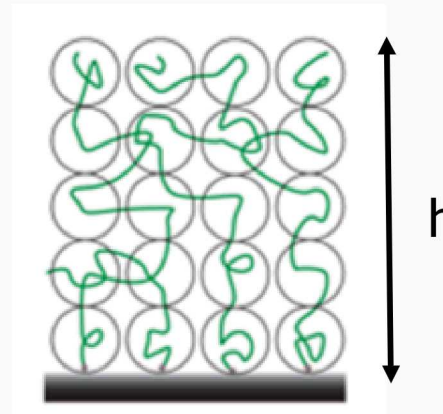
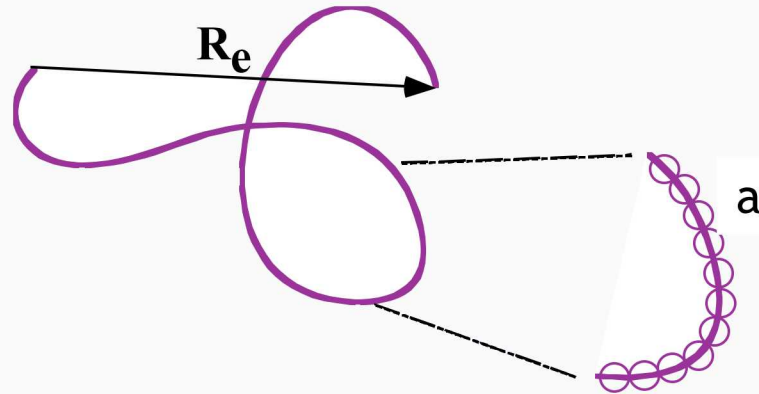
brush: put σ chains/unit area

if close enough in a brush,
polymers must stretch:

$$F = k_B T \left[\underbrace{\frac{3h^2}{2Na^2}}_{\text{stretching entropy}} + \underbrace{\frac{wN^2\sigma}{h}}_{\text{interactions}} \right]$$

minimize free energy:

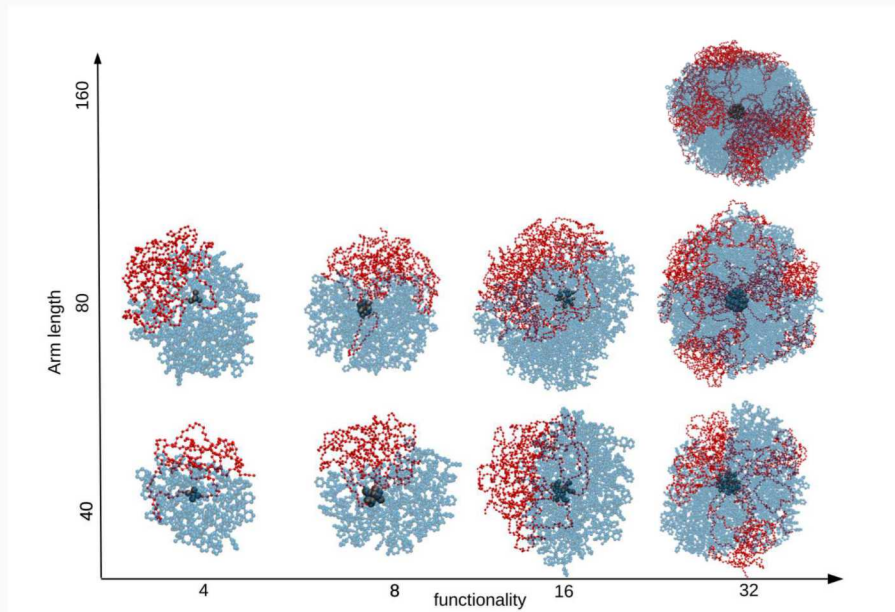
$$h \sim N(\sigma w)^{1/3}$$



Challenges in modeling mixed brush nanoparticles

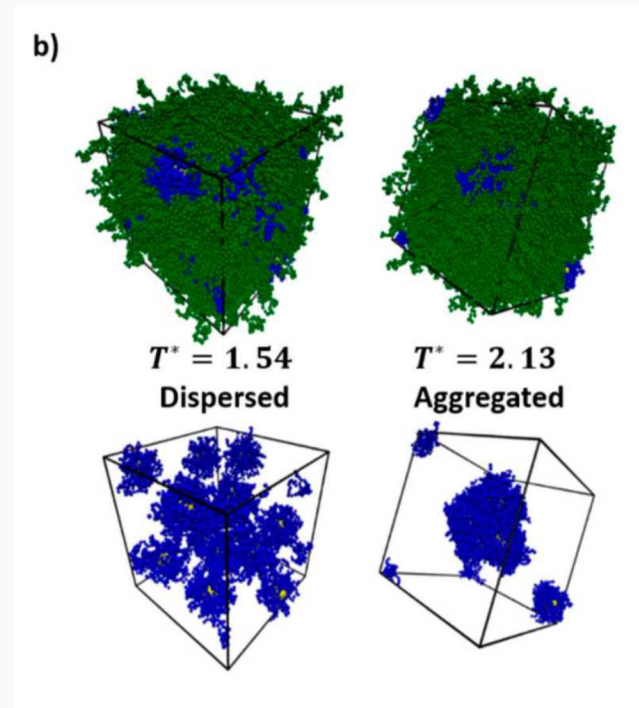
challenge 1: size scales make direct particle simulations difficult

atomistic: miktoarm stars



Bačová, P., Glynos, E., Anastasiadis, S. H. and Harmandaris, V. *ACS Nano* **13**, 2439-2449 (2019).

Brownian dynamics



$N = 10$
 $P = 50$

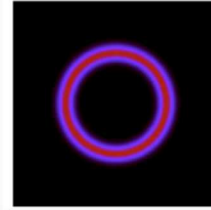
Martin, T. B. *et al. J Am Chem Soc* **137**, 10624–10631 (2015).

SCFT for single particles

$$\chi_{AB}N = 18.9$$

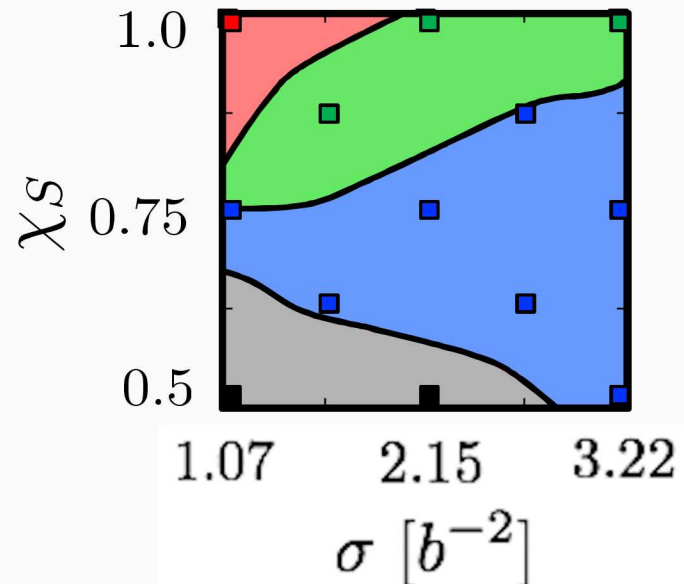
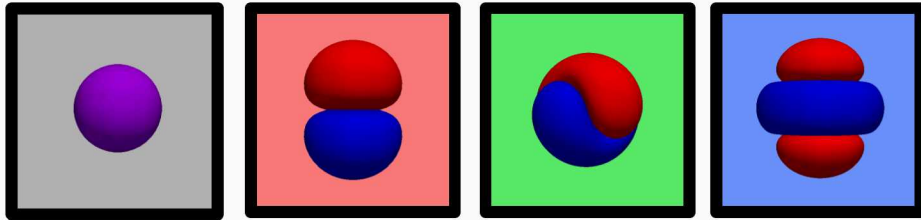
$$R_P = (2/3)R_g$$

uniform grafting density



$$\chi_{AB}N = 28.3$$

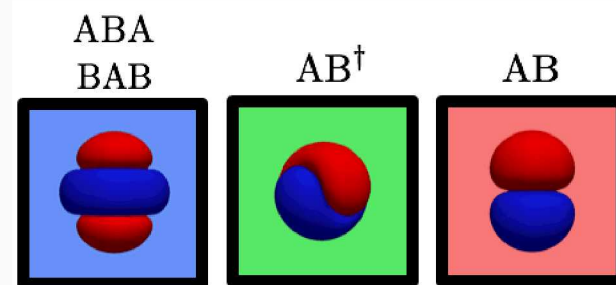
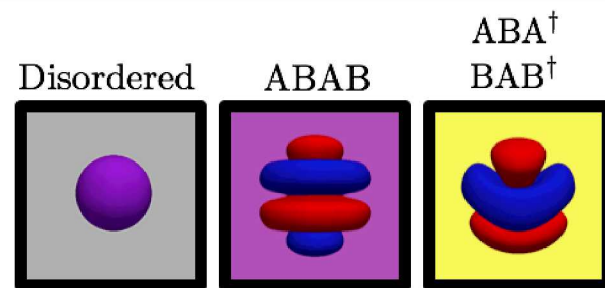
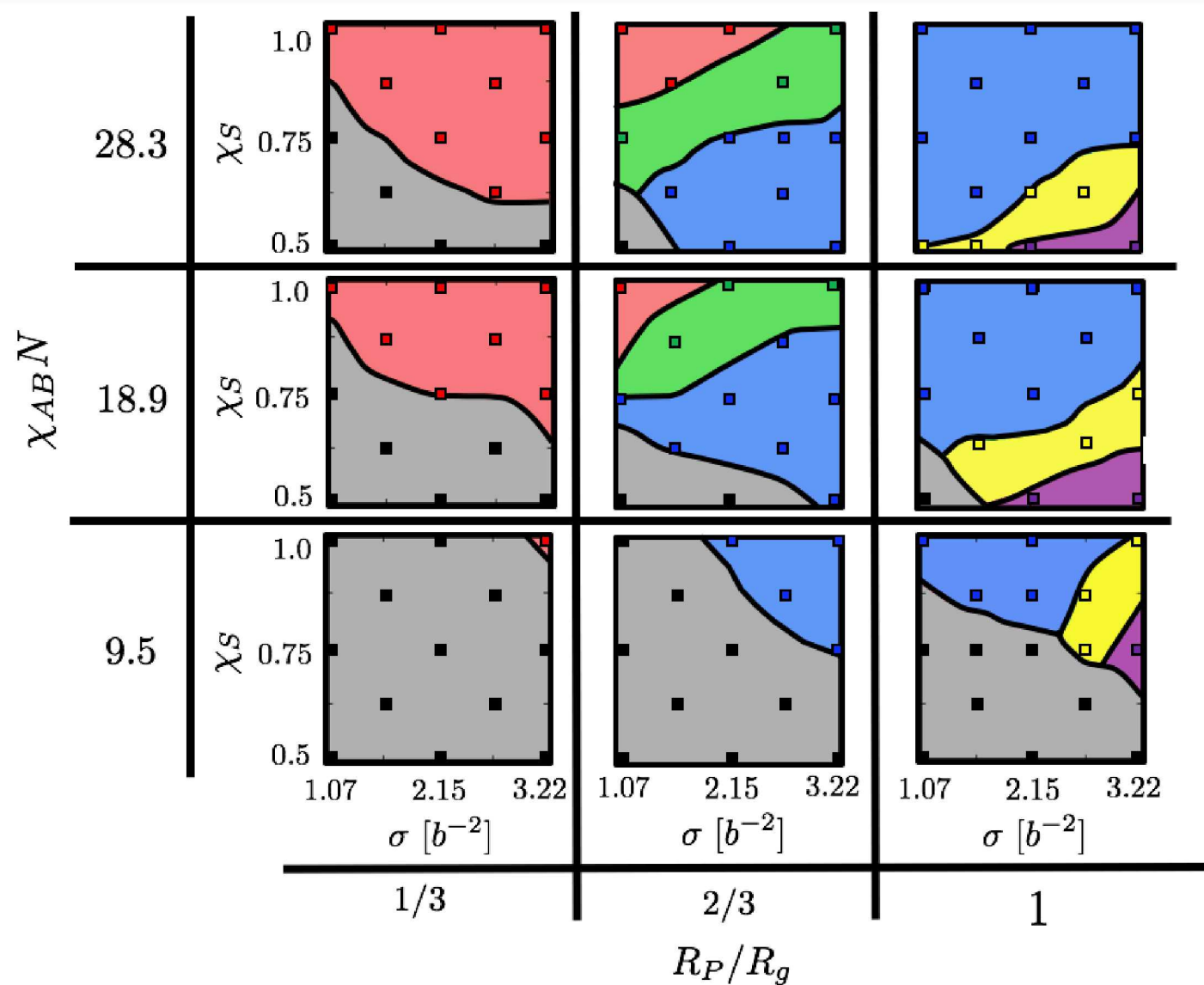
$$\chi_S = 1.0$$



use Boltzmann weight to interpolate phase boundaries

$$P_i = \frac{\exp(-\beta F_i)}{\sum_j \exp(-\beta F_j)}$$

Full SCFT phase diagram



Riggleman group implementation

Include torques on grafted nanoparticles

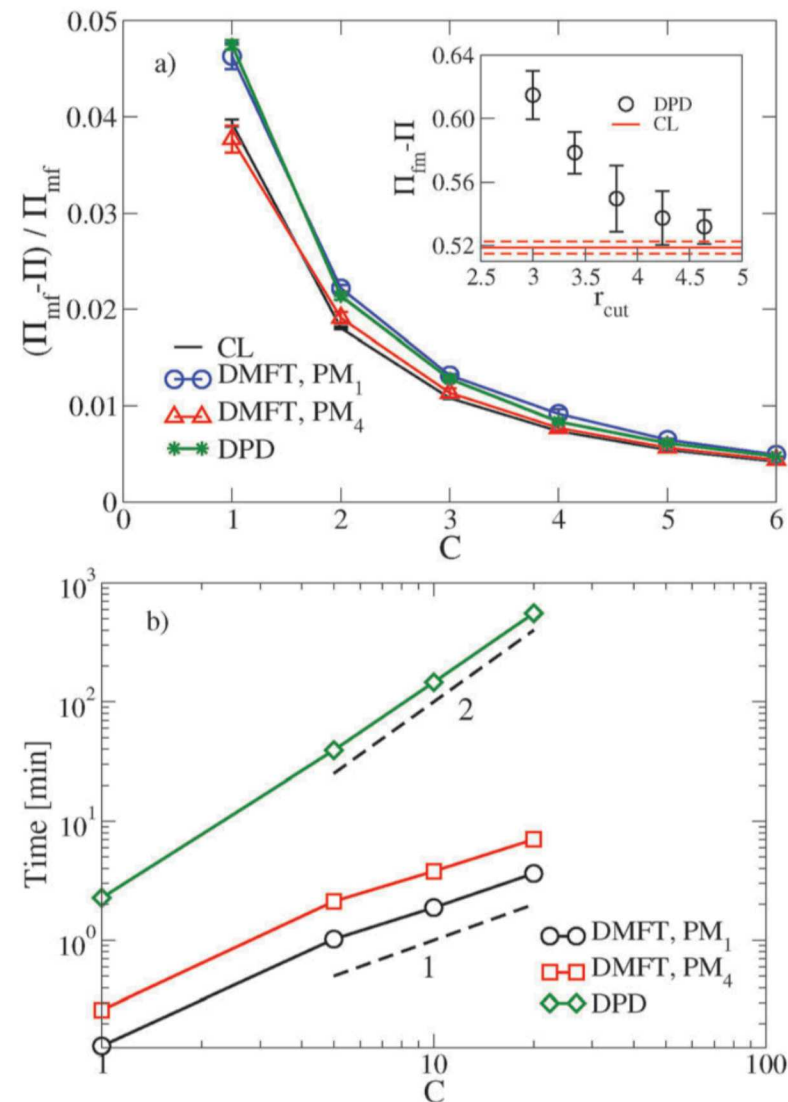
Solve Langevin equation with Gronbech-Jensen and Farago (GJF) scheme

$$\mathbf{r}_{k,s}(t_n) = 2b\mathbf{r}_{k,s}(t_{n-1}) - a\mathbf{r}_{k,s}(t_{n-2}) + b\delta t^2[\mathbf{f}_{k,s}^{(b)}(t_{n-1}) + \mathbf{f}_{k,s}^{(nb)}(t_{n-1})] + \frac{b\delta t}{2}[\theta_{k,s}(t_n) + \theta_{k,s}(t_{n-1})],$$

allows large timesteps
good performance compared to DPD simulation

N. Gronbech-Jensen and O. Farago, *Molecular Physics* (2013)

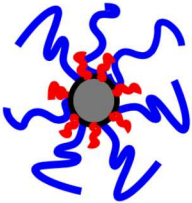
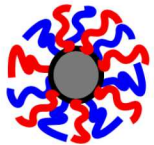
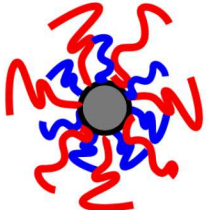
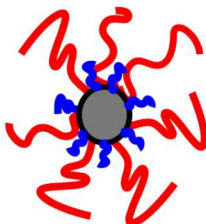
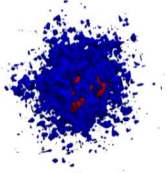
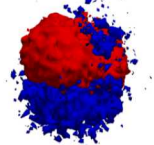
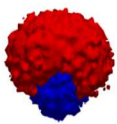
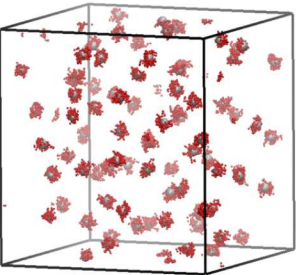
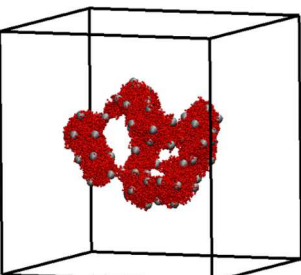
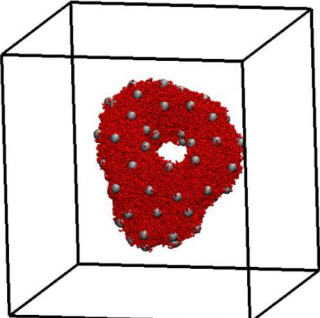
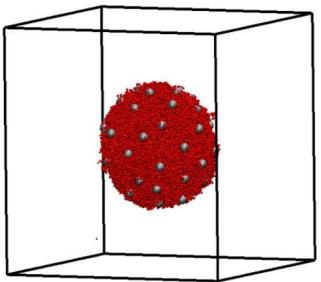
Chao, H., Koski, J. & Riggleman, R. A. *Soft Matter* **13**, 239-249 (2017).



Vary chain lengths

$$\chi_S = 2$$

$$f_A = 0.5$$

	Long 'Solvophilic' Short 'Solvophobic'	Medium 'Solvophilic' Medium 'Solvophobic'	Medium 'Solvophilic' Long 'Solvophobic'	Short 'Solvophilic' Long 'Solvophobic'
Schematic				
Single Particle				
Many Particle				
	Dispersed	"Connected Strings"	"Nearly Vesicle"	Phase Separated

Classify observed assemblies

define cluster: all particles with at least 1 A monomer located within $2b$ of another A monomer on a different particle

n_c = number of clusters

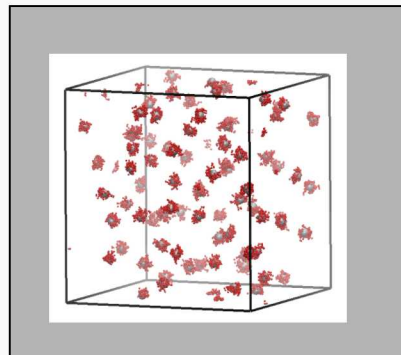
n_A = avg # of particles per cluster

κ^2 = relative shape anisotropy of clusters

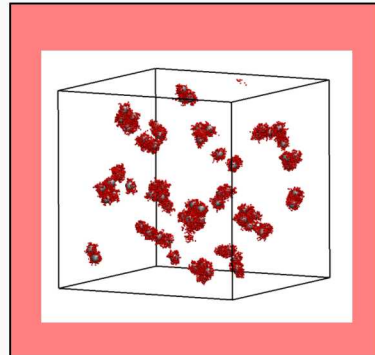
$\kappa^2 = 0$: sphere

$\kappa^2 = 1$: rod

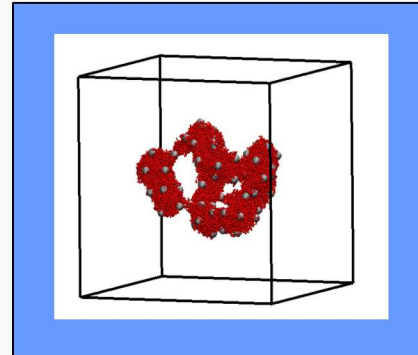
$n_A < 1.5$		dispersed
$1.5 < n_A < 3$		small clusters
$3 < n_A < n_{\max}$	$\kappa^2 > 0.22$	stringy aggregates
	$0.13 < \kappa^2 < 0.22$	loops/vesicles/?
	$\kappa^2 < 0.13$	macrophase separated
$n_A = n_{\max}$		macrophase separated



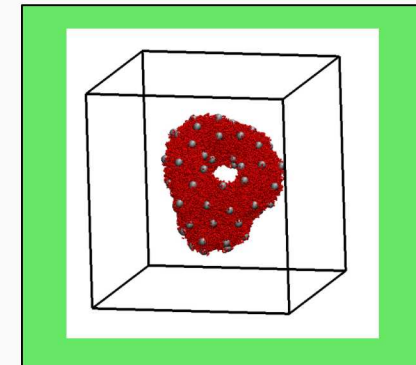
Dispersed



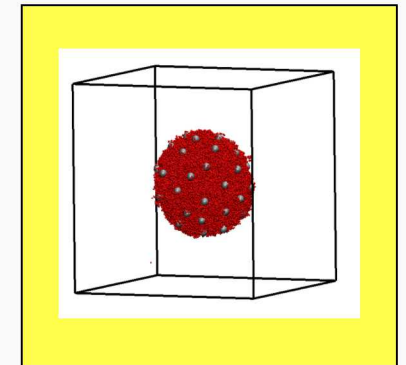
Small Clusters



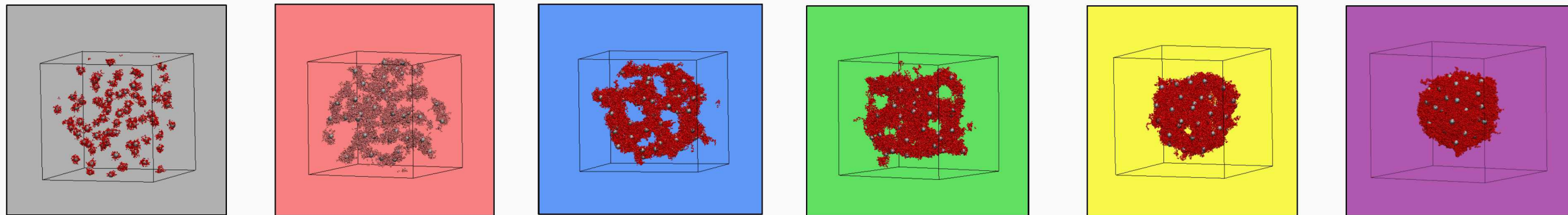
Connected Strings



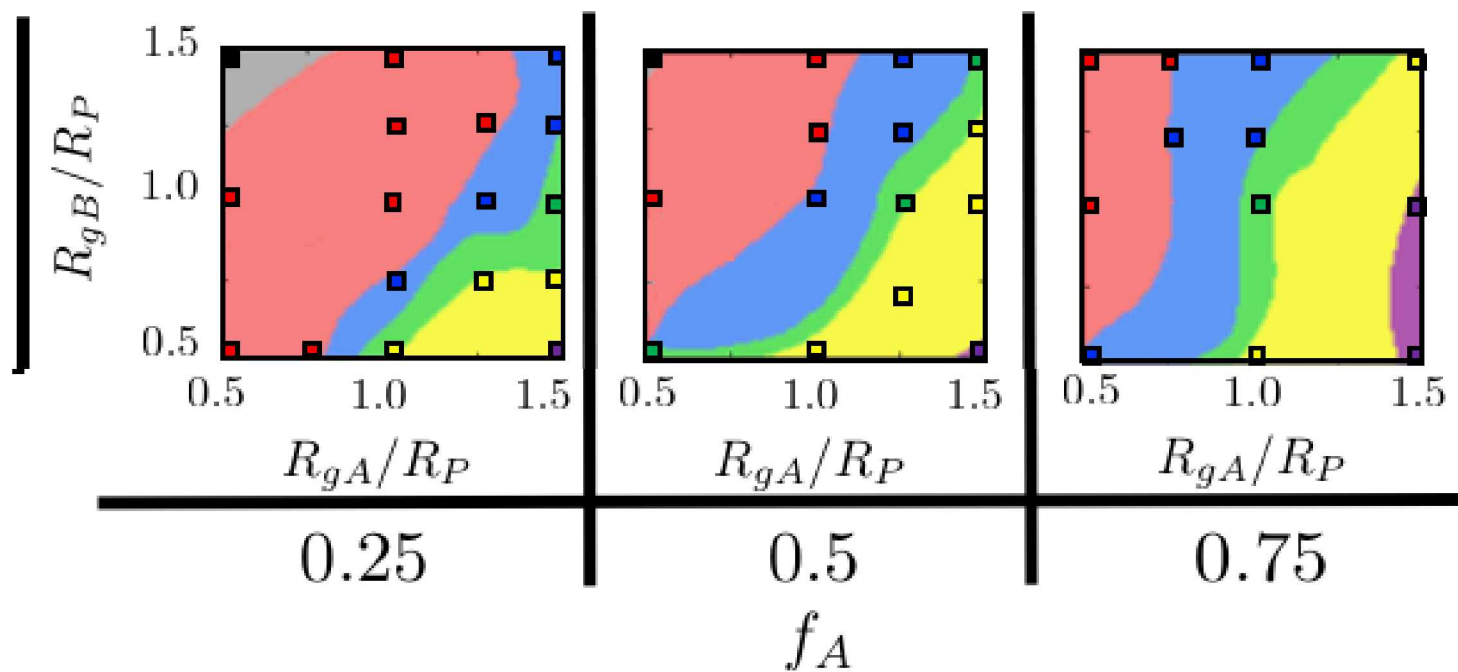
Nearly Vesicle



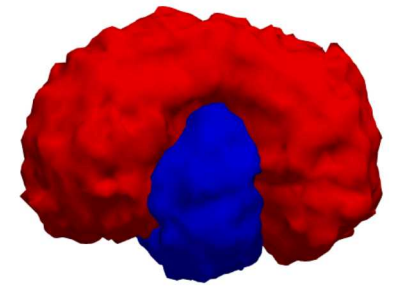
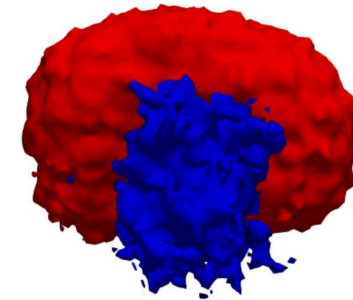
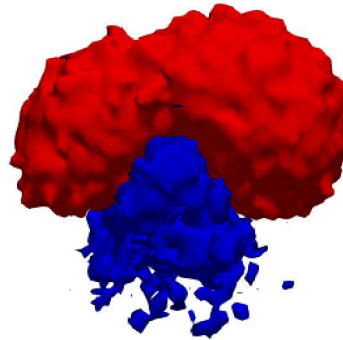
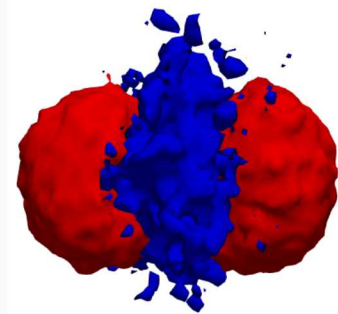
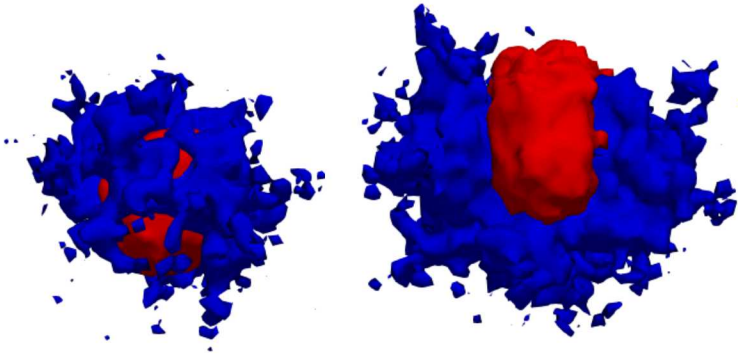
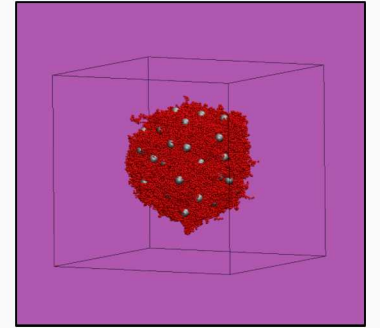
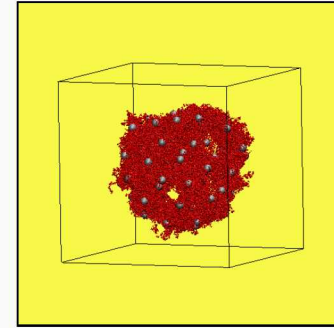
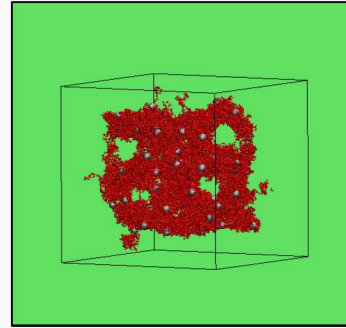
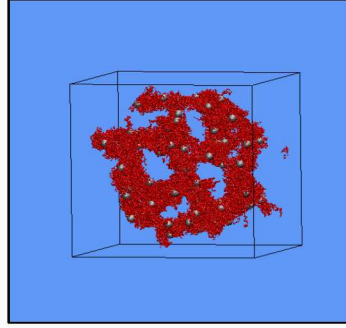
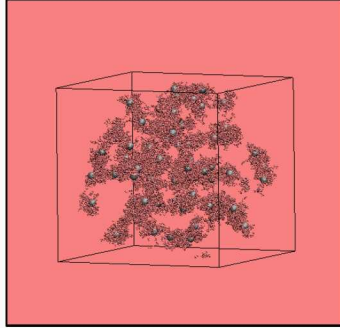
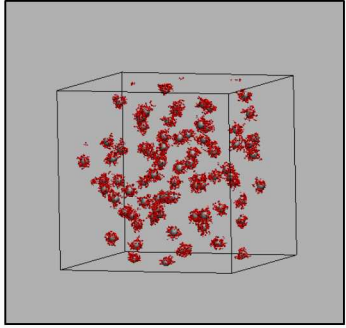
Phase Separated

Lower χ_s 

$$\chi_s = 1.25$$



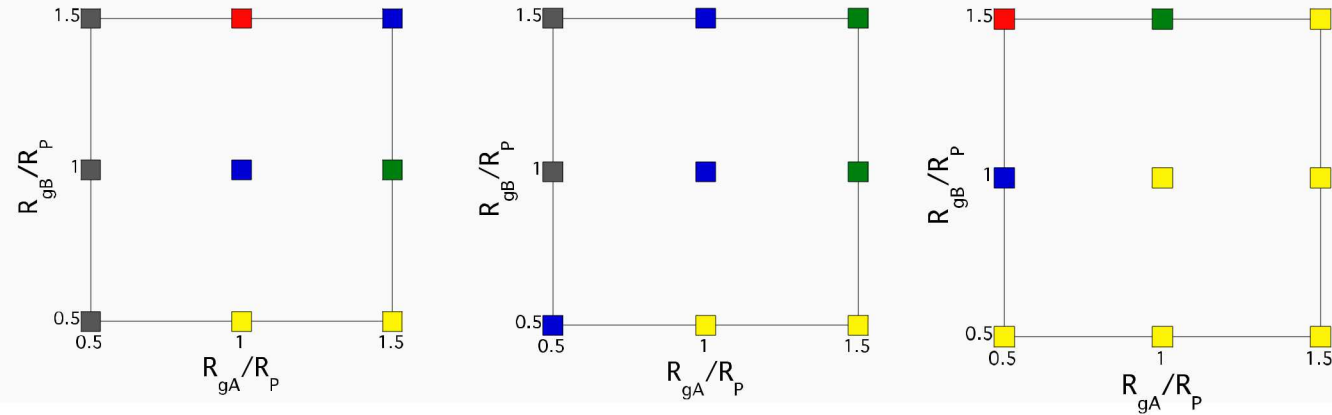
Lower χ_s



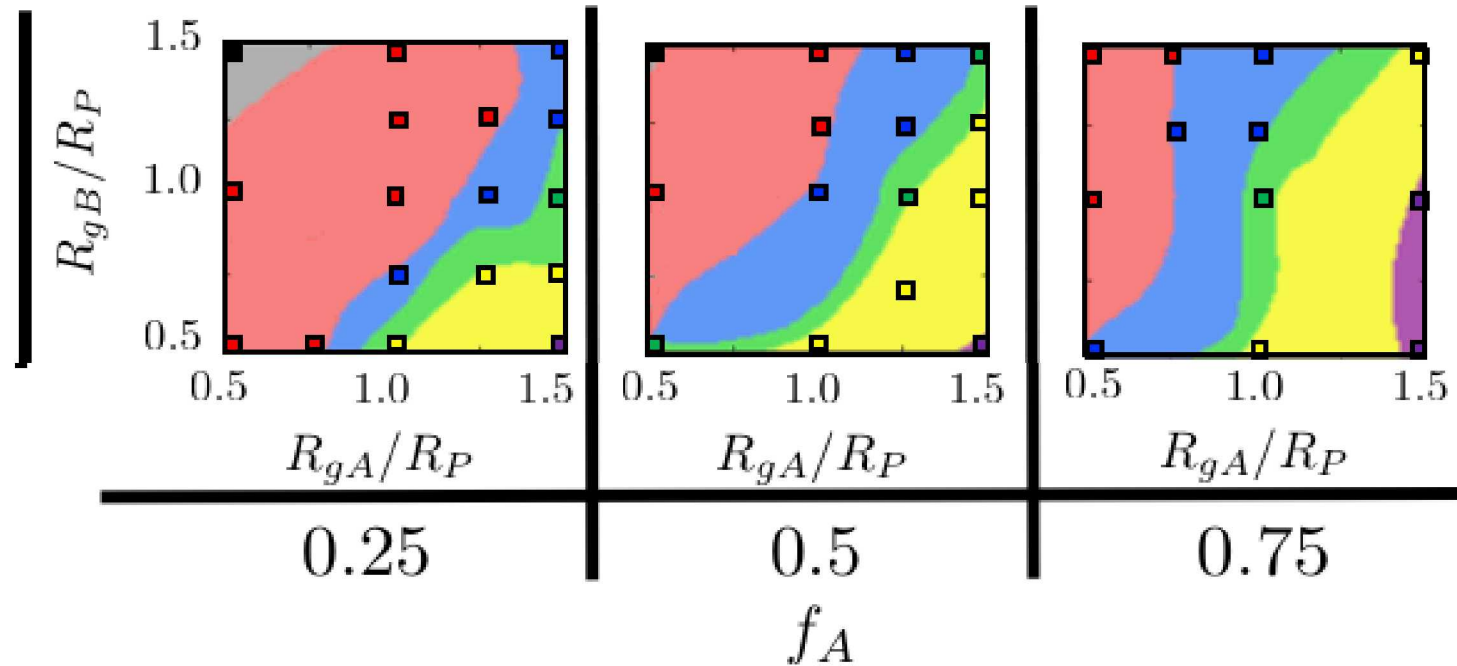
- less distinct brush structures
- more “messy” assemblies

Comparison of solvent qualities

$$\chi_s = 2$$



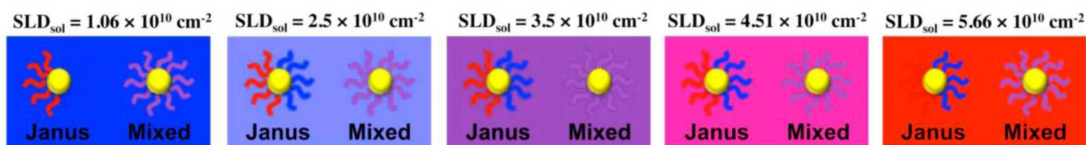
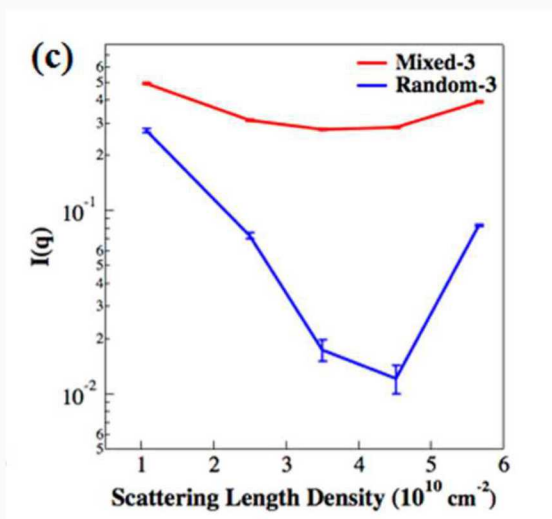
$$\chi_s = 1.25$$



Experimental evidence of grafted Janus NPs?

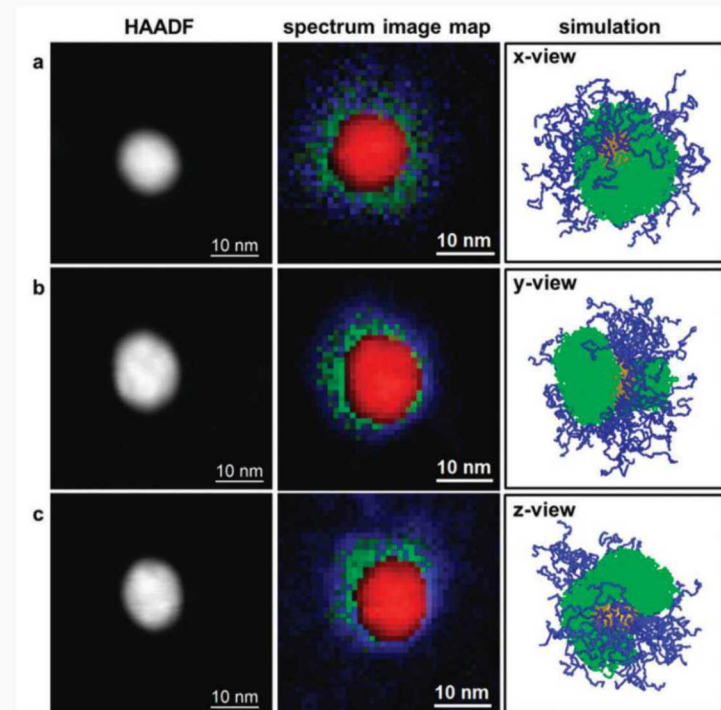
SANS

dPS-PMMA on Au NPs



Kim, S., Kim, T.-H., Huh, J., Bang, J. & Choi, S.-H. *ACS Macro Lett.* **4**, 417–421 (2015).

PS-PMMA on Au NPs



EELS for
polymers

Rossner, C., Tang, Q., Müller, M. & Kothleitner, G. *Soft Matter* **14**, 4551–4557 (2018).