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SAND2019-8954C

# Enhanced Optical Nonlinearities in All-Dielectric Metasurfaces

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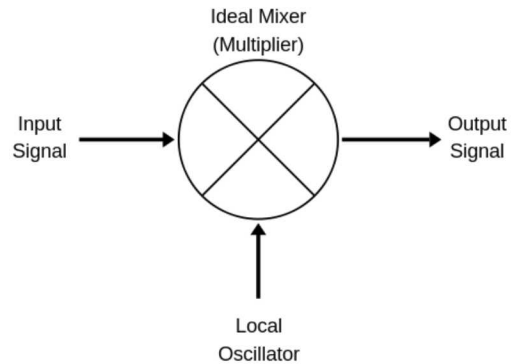
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SAND2019-5033 C

# Frequency mixing – from electronics to optics

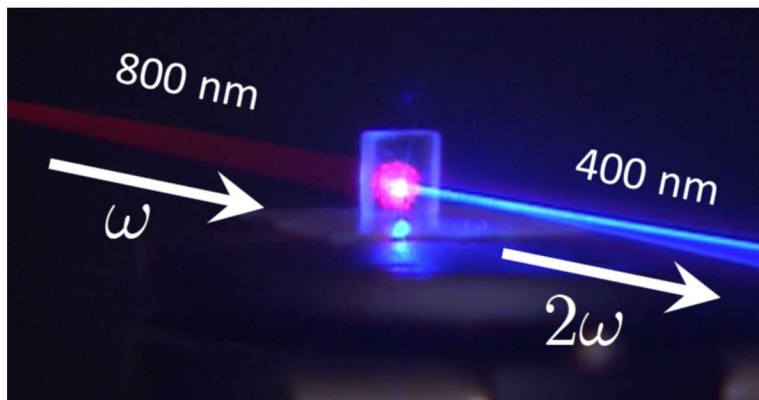


**Electronics** - signal processing: modulators, phase detectors, frequency synthesizers, heterodyne, etc.



▪ Electronics component dimensions  $\ll$  wavelengths

- **Nonlinear optics**



**Variety of frequency conversion effects:**

Second Harmonics Generation (SHG)

Third Harmonics Generation (THG)

Sum frequency Generation (SFG)

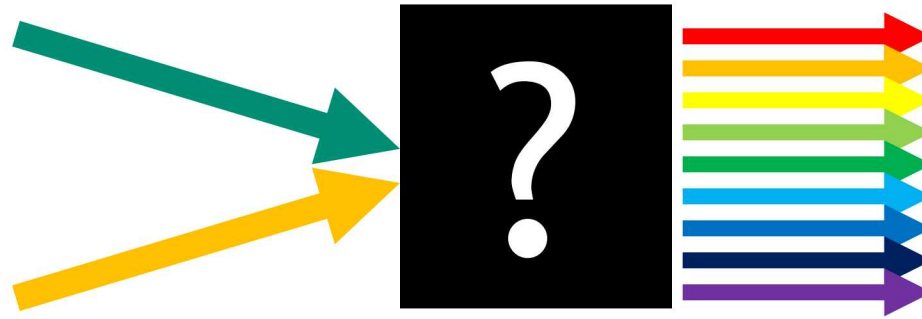
etc.

$$\mathbf{P}(t) = \varepsilon_0 (\chi^{(1)} \mathbf{E}(t) + \chi^{(2)} \mathbf{E}^2(t) + \chi^{(3)} \mathbf{E}^3(t) + \dots)$$

**Phase matching (dispersion) is critical**

Nonlinear crystal dimensions  $\gg$  wavelengths

# “Super” frequency mixing?

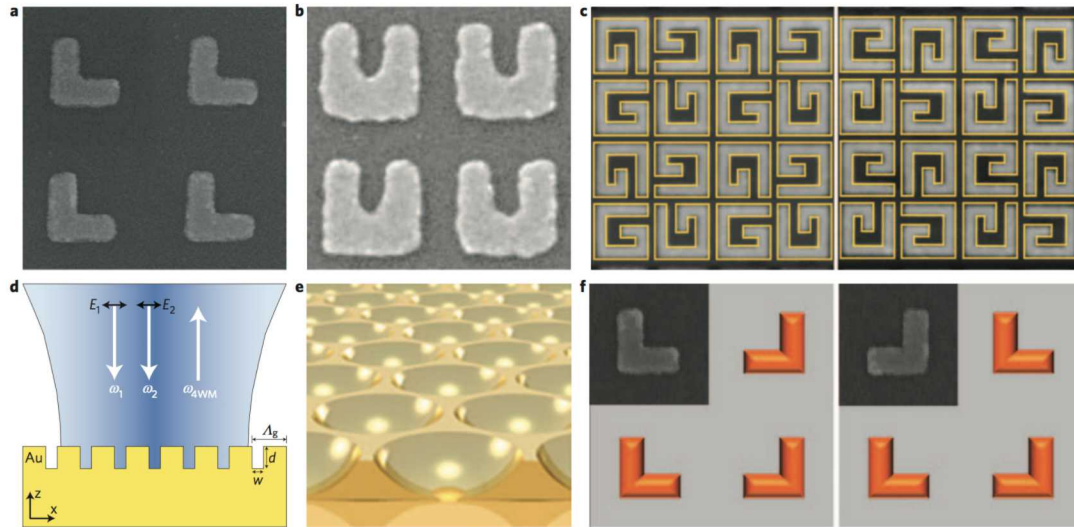


Can we see all of these mixings at the same time?

Require:

- Relaxed phase matching
- Strong nonlinear materials
- High field intensity

# Nonlinear Photonic Metasurfaces

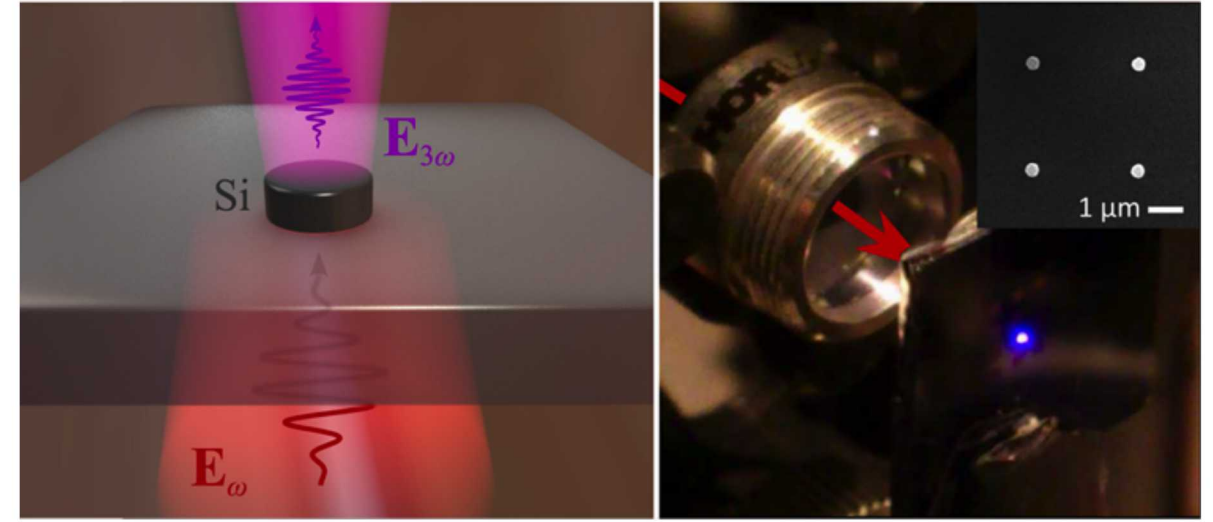


Kauranen, M., and Zayats, A. V. *Nature Photonics*, 6(11), 737, (2012)

- Surface/Local Plasmon resonances
- Mie resonances



**Resonant enhancement of EM field**



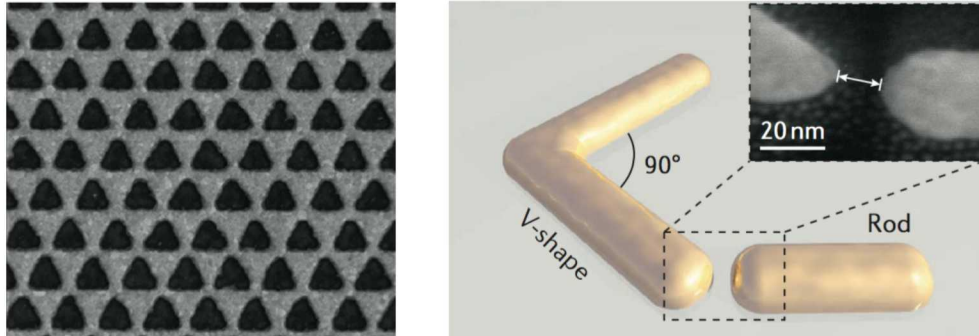
M .R. Shcherbakov, et. al. *Nano Letters* **14**, 11, 6488–6492, 2014

Dimensions < wavelength

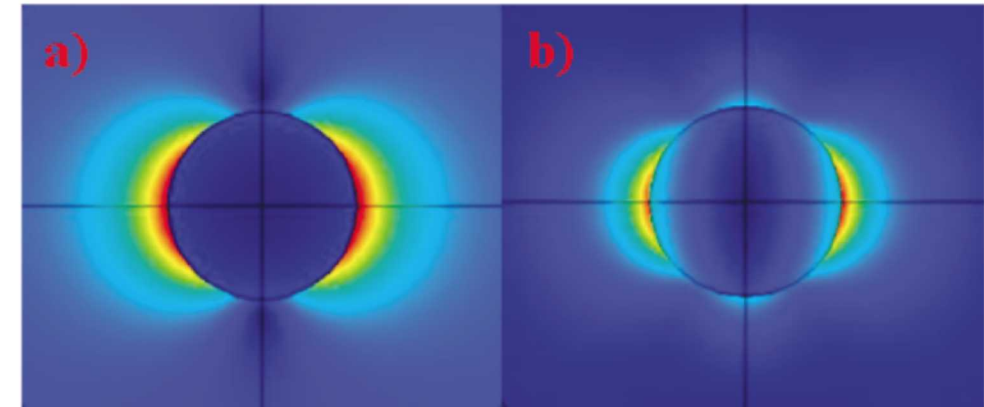


**Relaxed phase matching conditions**

## a Metasurfaces for SHG



Li, G., Zhang, S. and Zentgraf, T., "Nonlinear photonic metasurfaces" *Nature Reviews Materials*, (2017), 2(5), p.17010

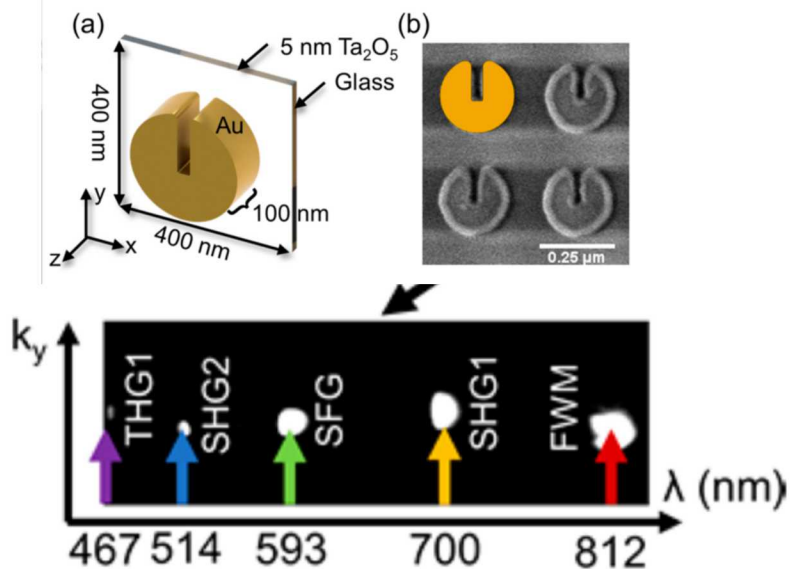


Butet, Jérémy, et al. *Nano letters* 10.5 (2010): 1717-1721.

## Plasmonic metasurfaces:

- Ohmic losses
- Plasmonic structure: small modal volume (surface nonlinearities)

**SHG efficiency  $\sim 5.1 \times 10^{-10} \text{ W/W}^2$**

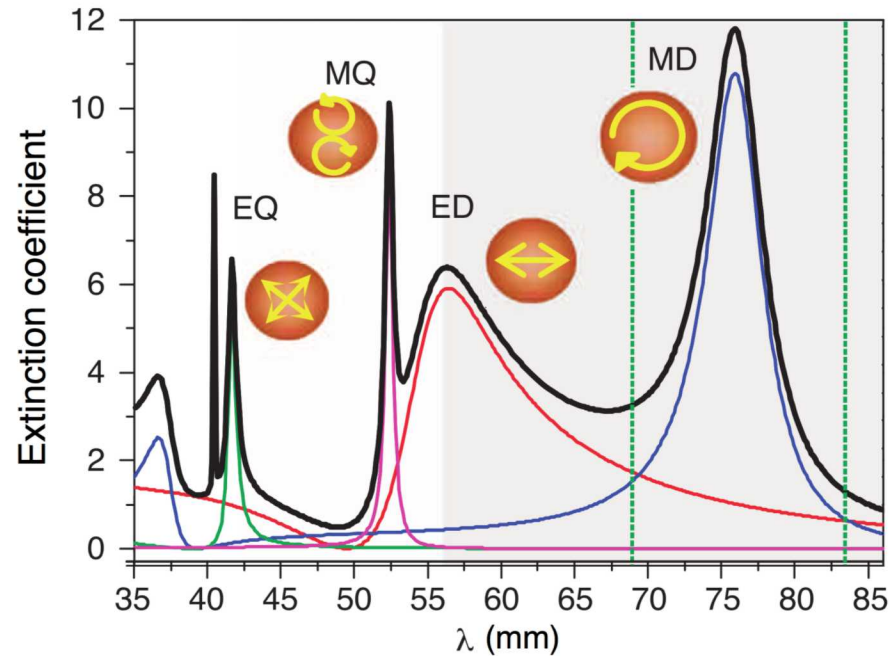


Sartorello, et al. *ACS Photonics* 3.8 (2016): 1517-1522.

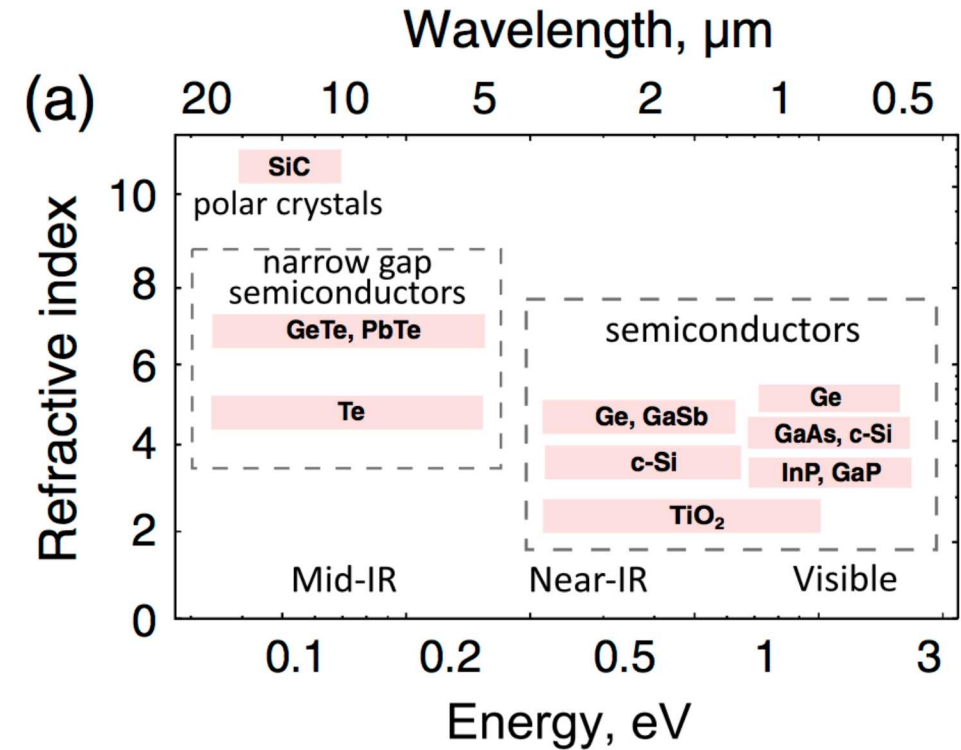
# Mie resonances in dielectric spheres



Mie resonances in Dielectric spheres



Geffrin, J.-M., et al. *Nat. Commun.* 3, 1171, **2012**



Baranov, D.G., et al. *Optica* 4.7, 814-825, **2017**

## Mie resonances

- Low losses
- Much larger mode volume
- High nonlinear coefficient materials (GaAs:  $\sim 200 \text{ pm/V}$ )

# Nonlinear dielectric metasurfaces

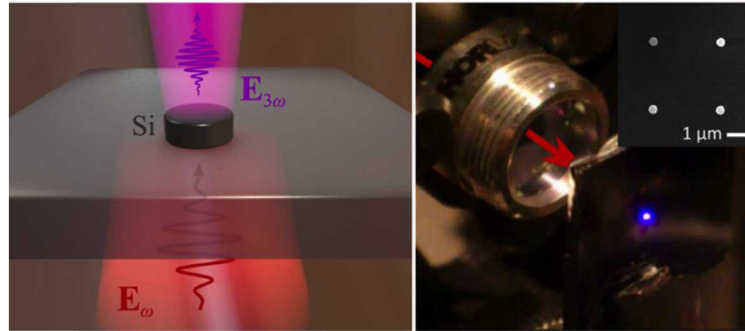
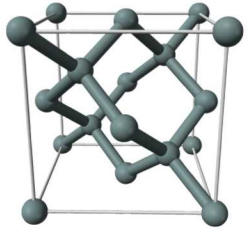
7



## Third Harmonic Generation

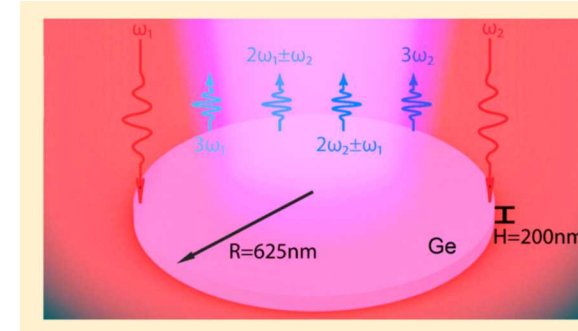
centrosymmetric

Si  
Ge



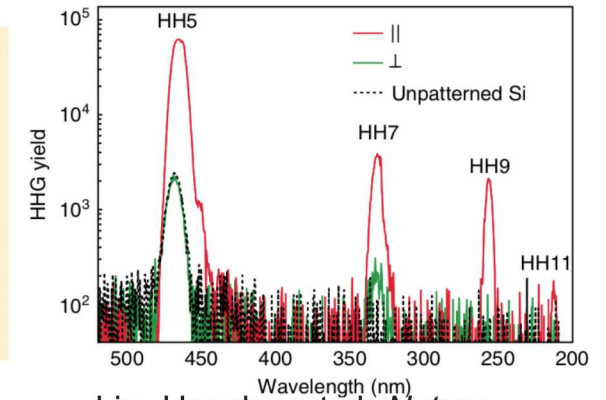
M .R. Shcherbakov, et. al. *Nano Letters* **14**, 11, 6488–6492, **2014**

## Four-Wave Mixing



Grinblat, G., et al, *ACS Photonics* **4**, 2144-2149, **2017**

## High-Harmonic Generation

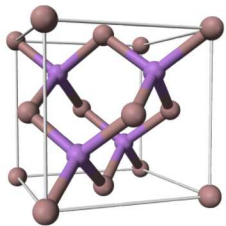


Liu, Hanzhe, et al. *Nature Physics* **14**, 10, 1006, **2018**

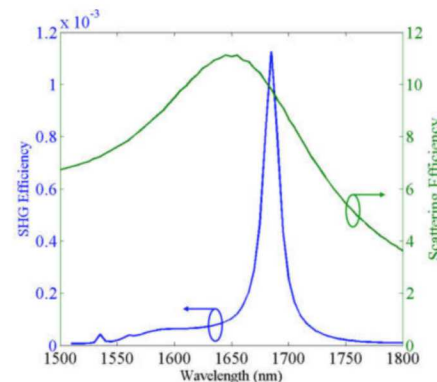
Non-centrosymmetric

## Second Harmonic Generation ( $10^{-8}$ W/W<sup>2</sup>)

GaAs  
AlGaAs



<https://www.wikipedia.org>



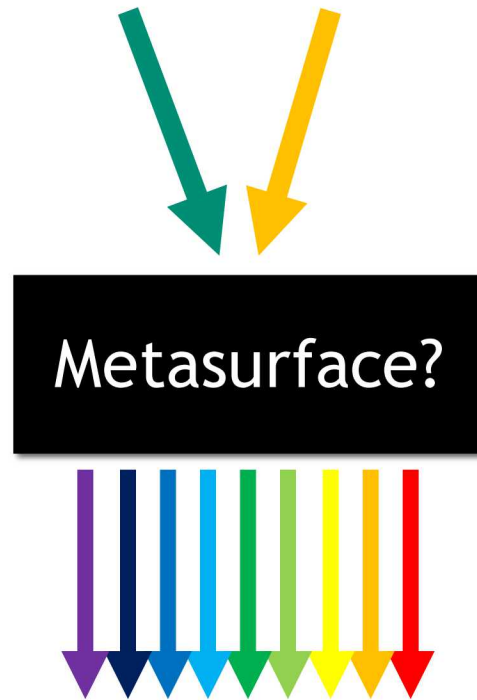
L. Carletti et al., *ACS Photonics*, **3**(8), 1500-1507, **2016**

**AlGaAs** – Carletti, L., et al. *Optics express* **23**, 20, 26544-26550, **2015**

Camacho-Morales, R., et al. *Nano letters* **16**, 11, 7191-7197, **2016**

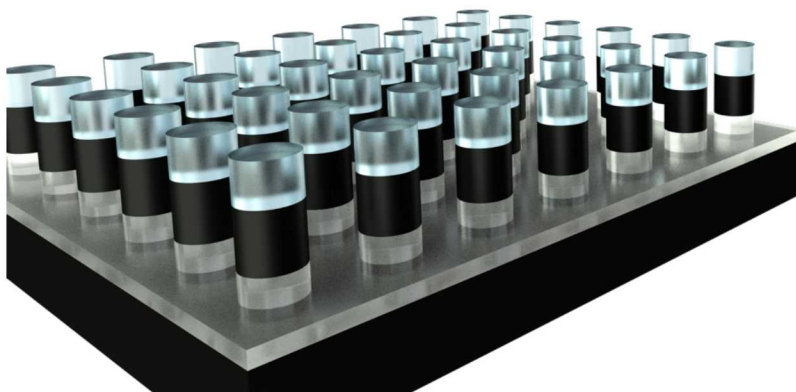
Kruk, S. et al. *Nano Lett.*, **17** (6), pp 3914–3918, **2017**

**GaAs** – Liu, S. et. al. *Nano letters* **16**, 9, 5426-5432, **2016**



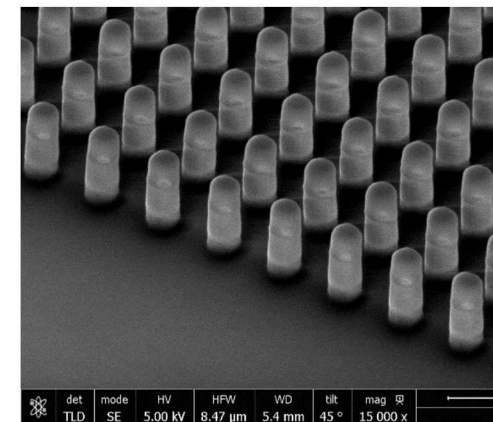
**Multiple frequency mixing in dielectric metasurfaces**

# GaAs based dielectric metasurface

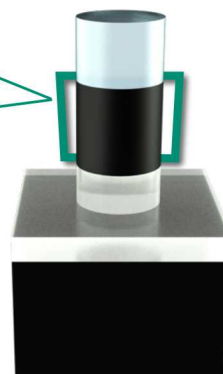
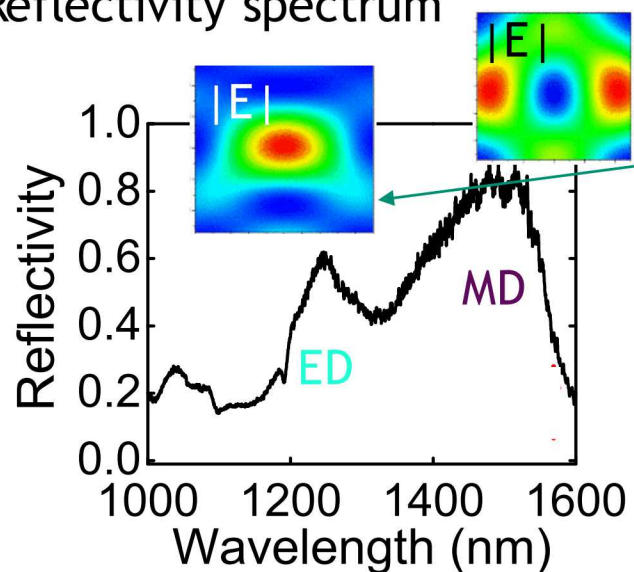


$\text{SiO}_x$  - 300 nm  
GaAs - 400 nm  
 $(\text{Al}_x\text{Ga}_{1-x})_2\text{O}_3$  - 450 nm  
Diameter 400 nm  
Period 840 nm

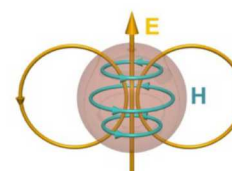
SEM image



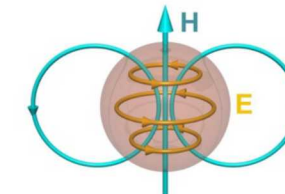
Reflectivity spectrum



**Electric  
Dipole**



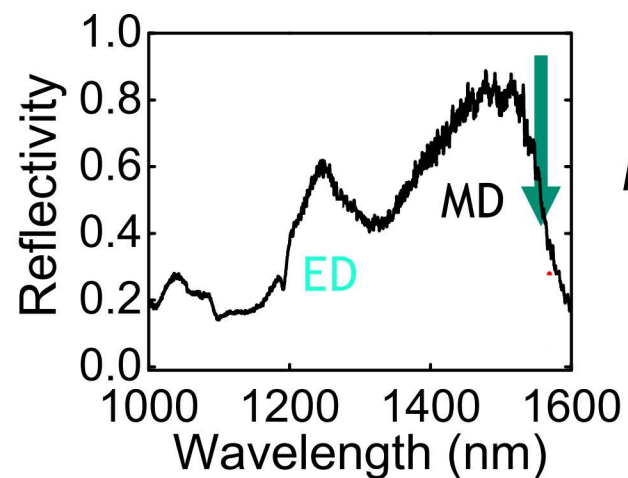
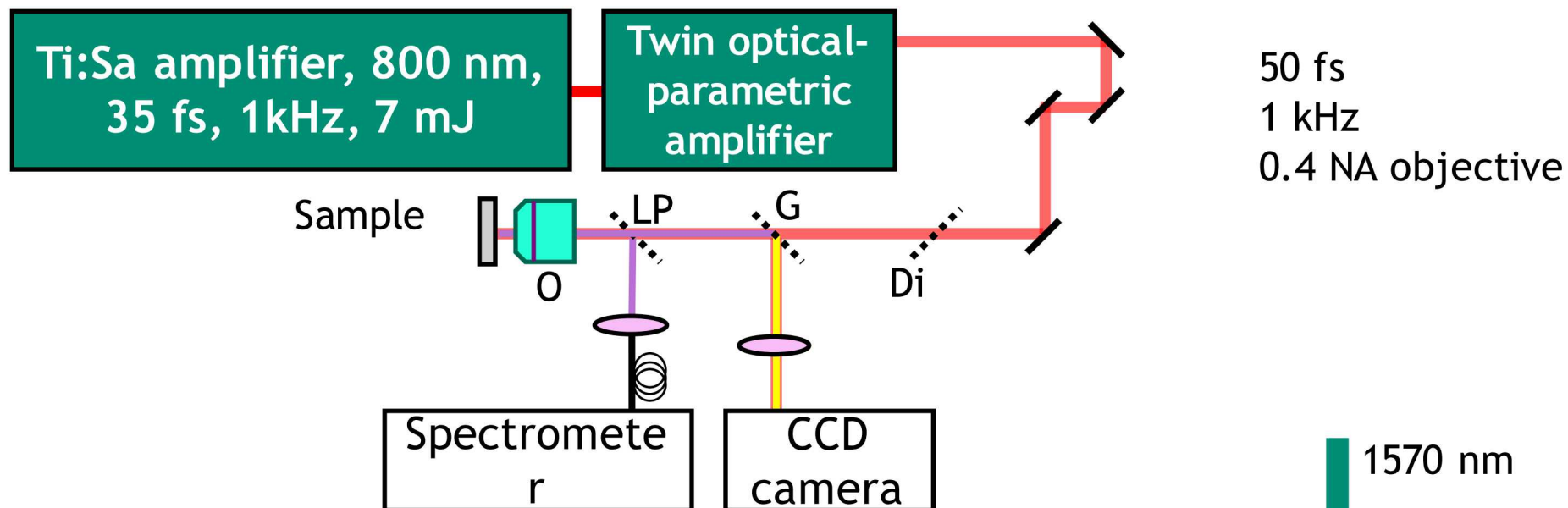
**Magnetic  
Dipole**



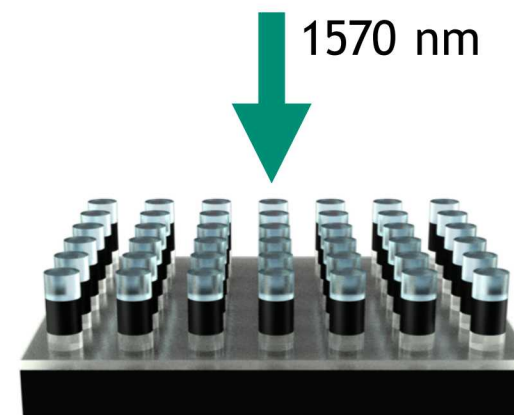
Images: A. Miroshnichenko

- High nonlinear coefficient material
- Resonance enhancement of EM field

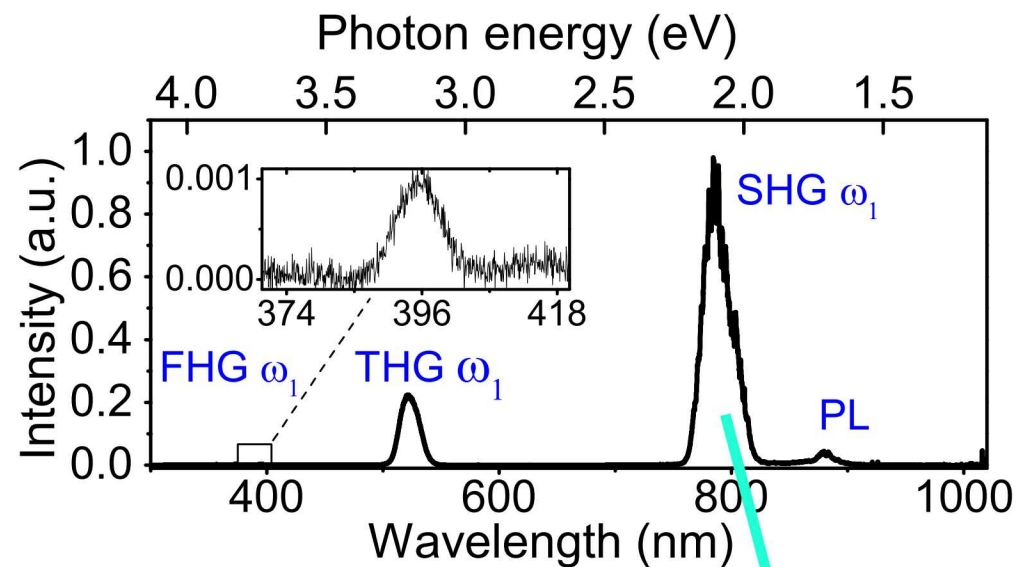
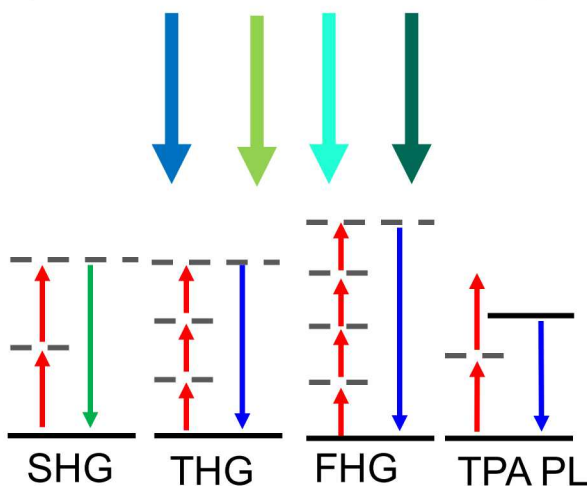
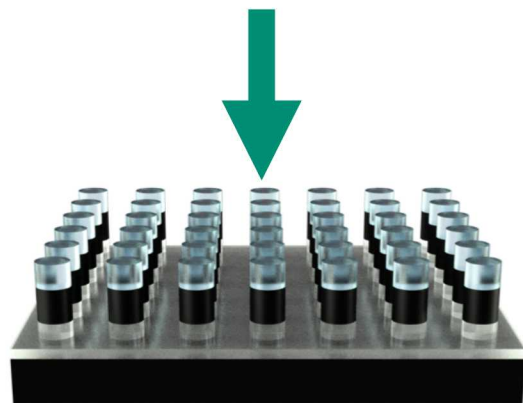
# Single beam experiment



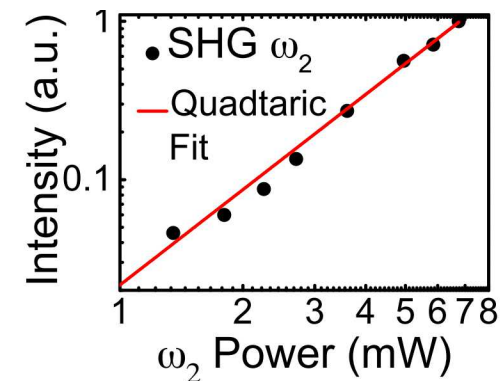
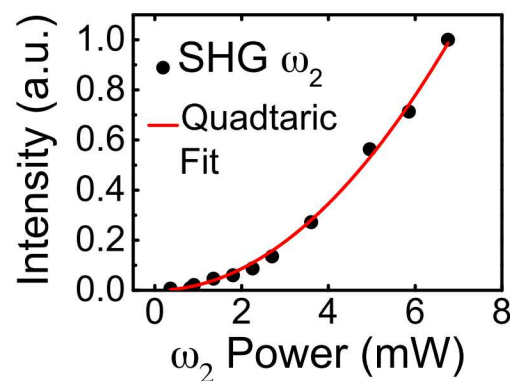
Magnetic dipole resonance



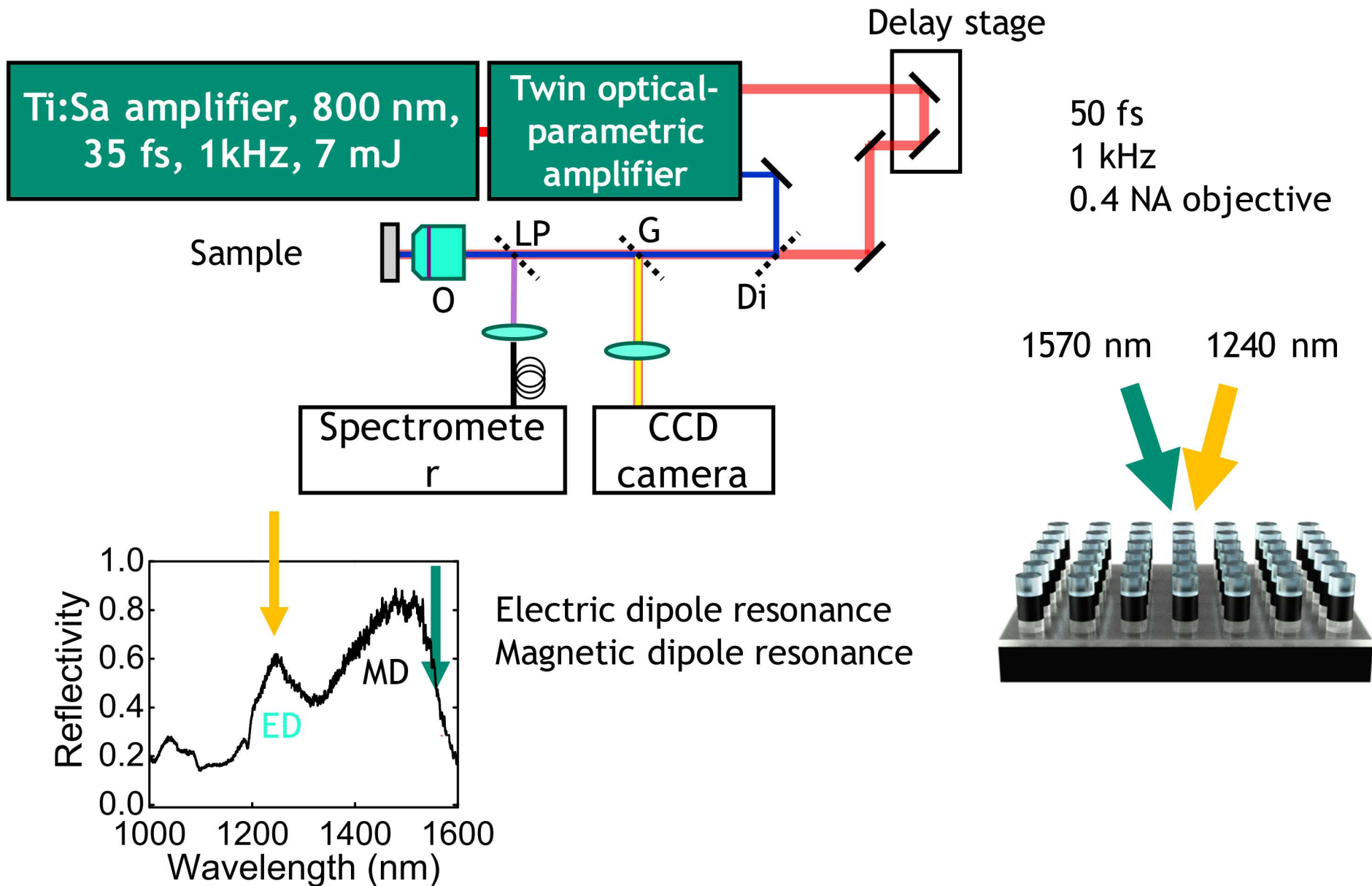
# 2<sup>nd</sup>, 3<sup>rd</sup>, 4<sup>th</sup> harmonic generation spectra



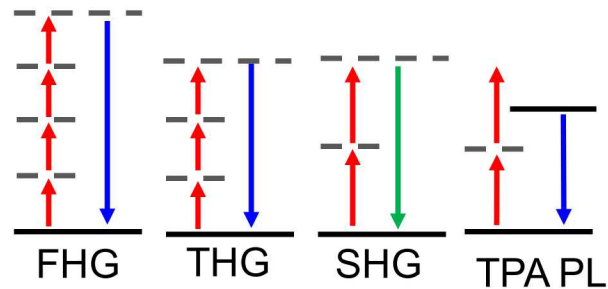
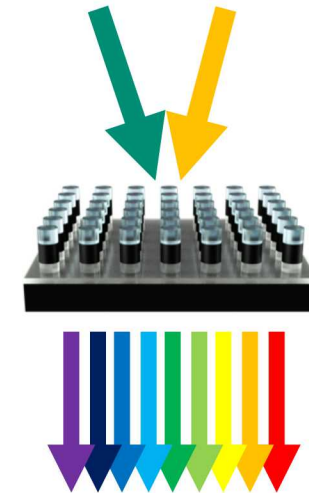
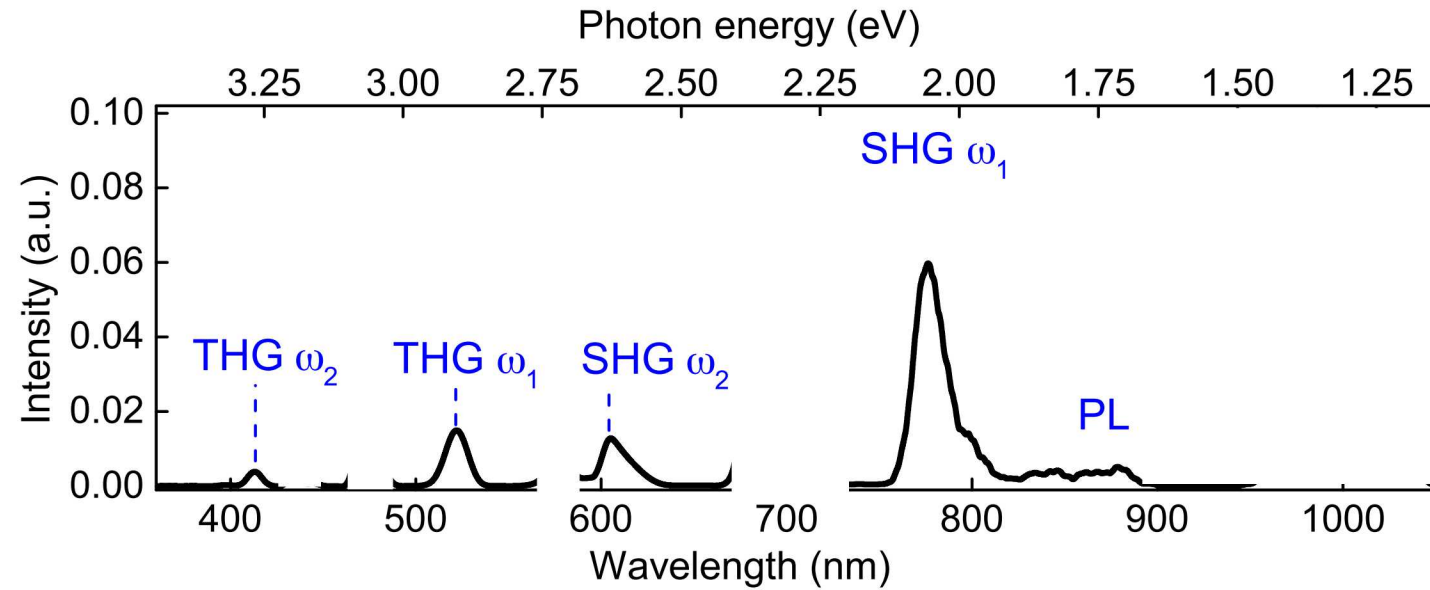
## SHG power dependence



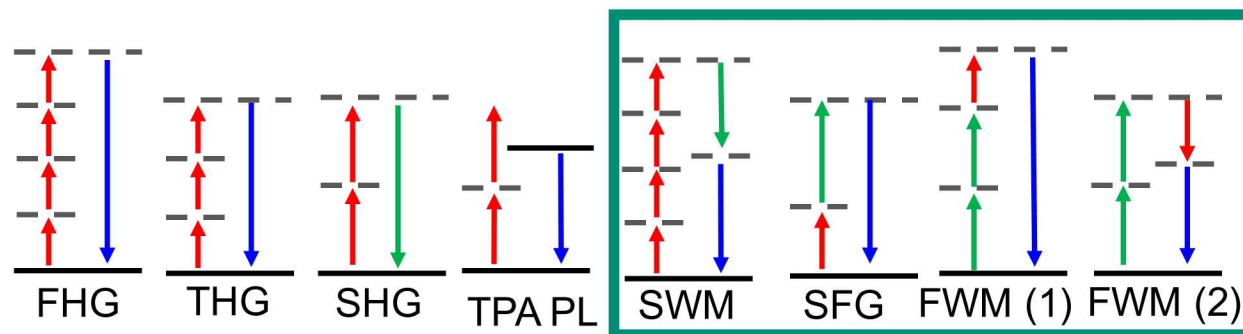
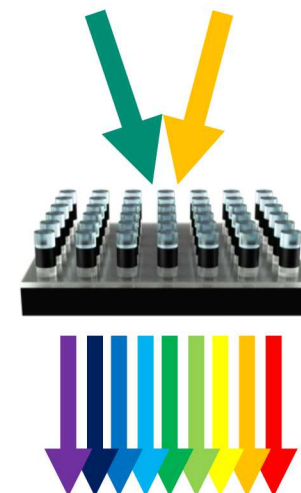
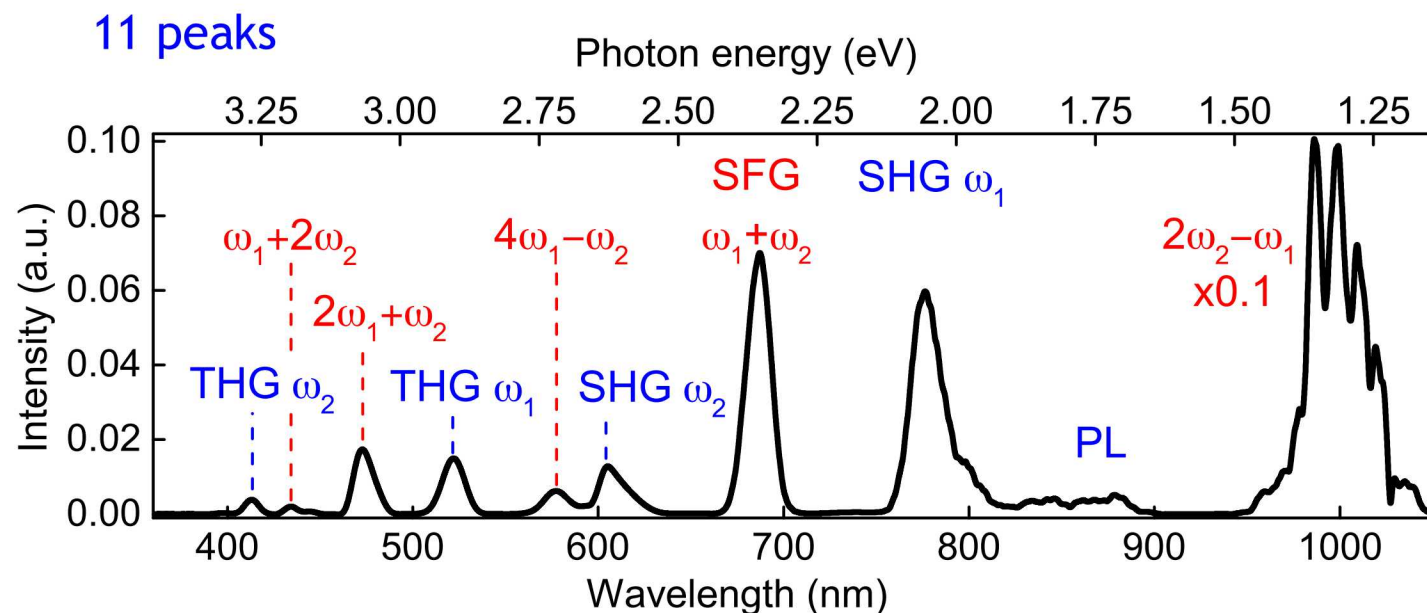
# Two-beam experiment



# Frequency mixing spectra



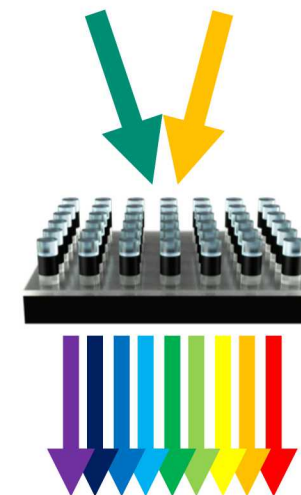
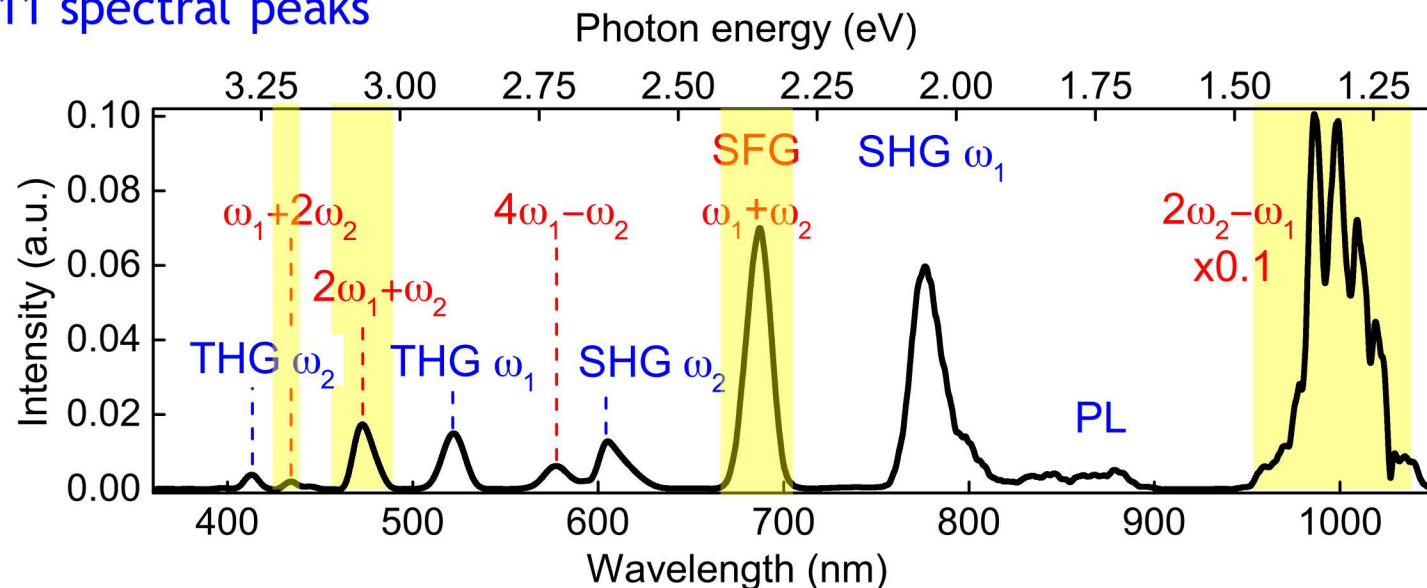
# Frequency mixing spectra



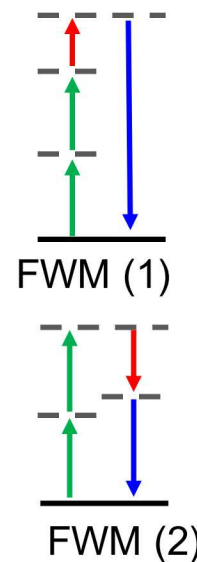
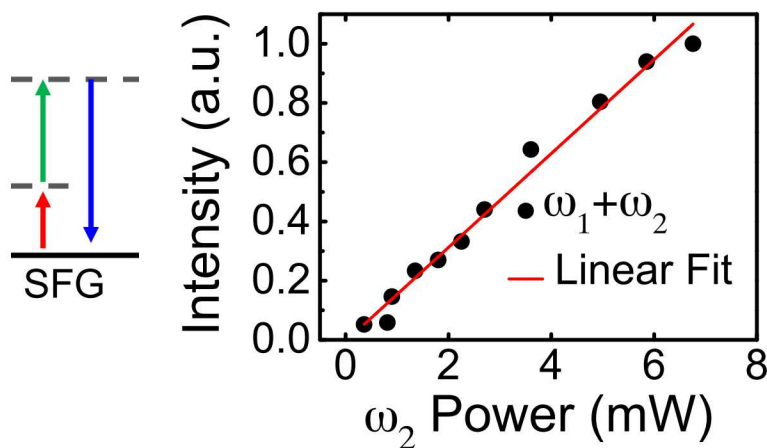
7 different nonlinear processes: 2<sup>nd</sup>, 3<sup>rd</sup>, 4<sup>th</sup> harmonics, sum frequency generation, 4 wave-mixing, six-wave mixing, PL induced by two-photon absorption

# Frequency mixing spectra

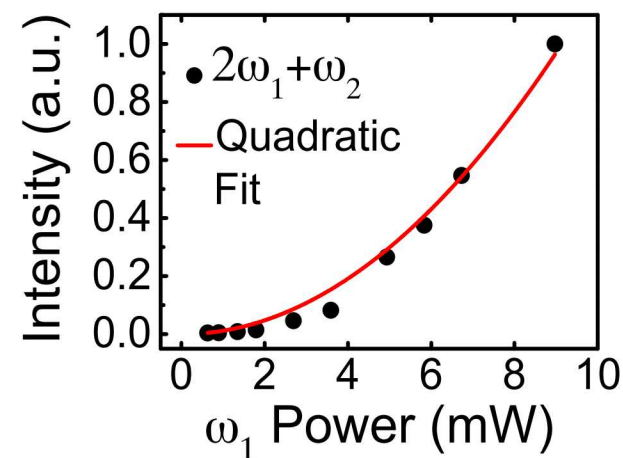
11 spectral peaks



SFG power dependence



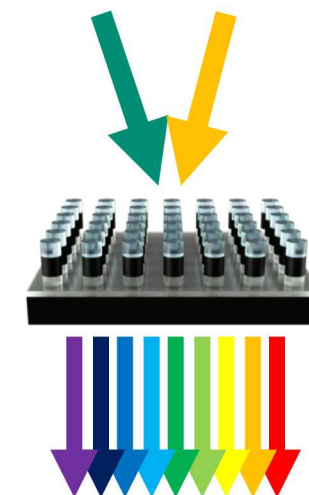
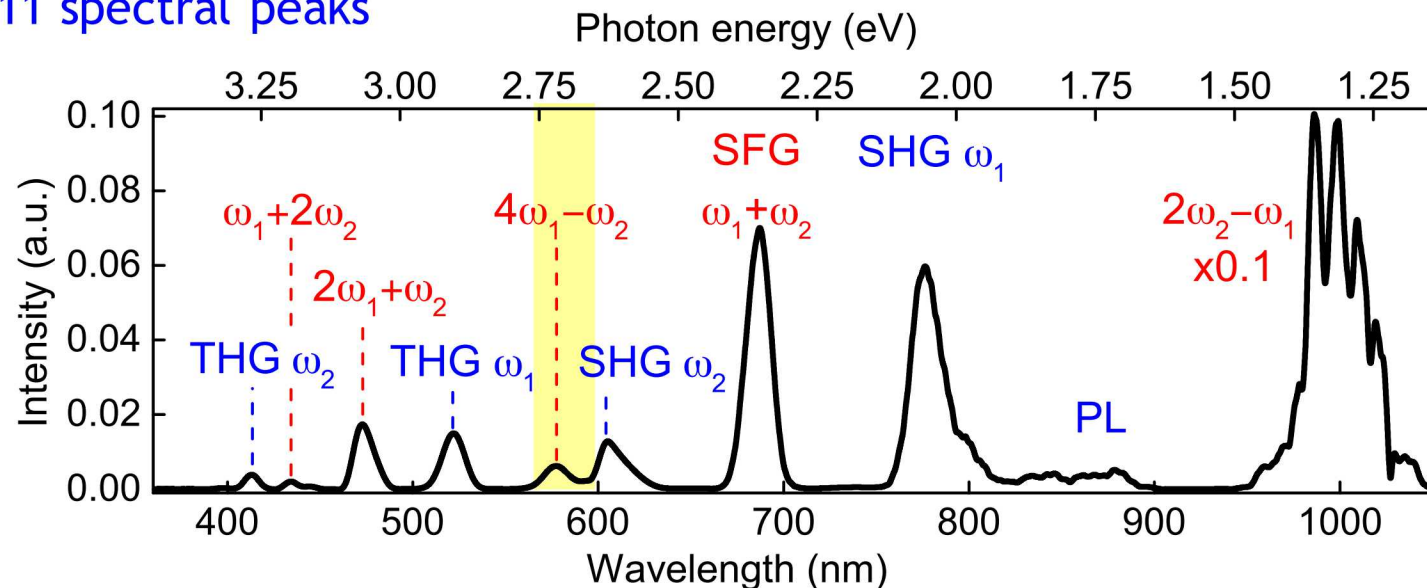
FWM power dependence



# Frequency mixing spectra: six wave mixing

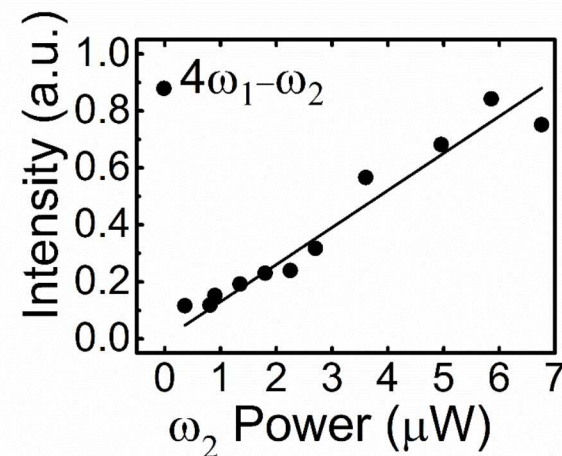
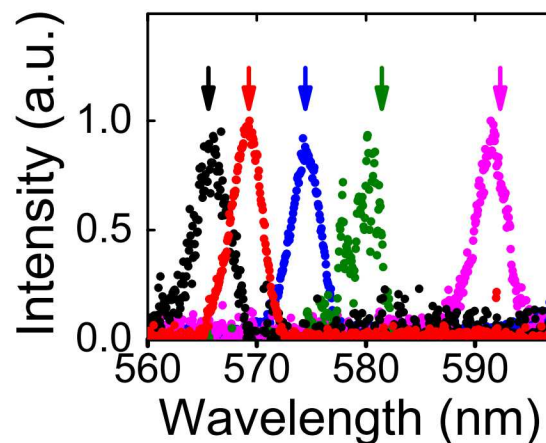
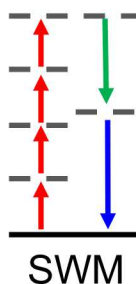


11 spectral peaks

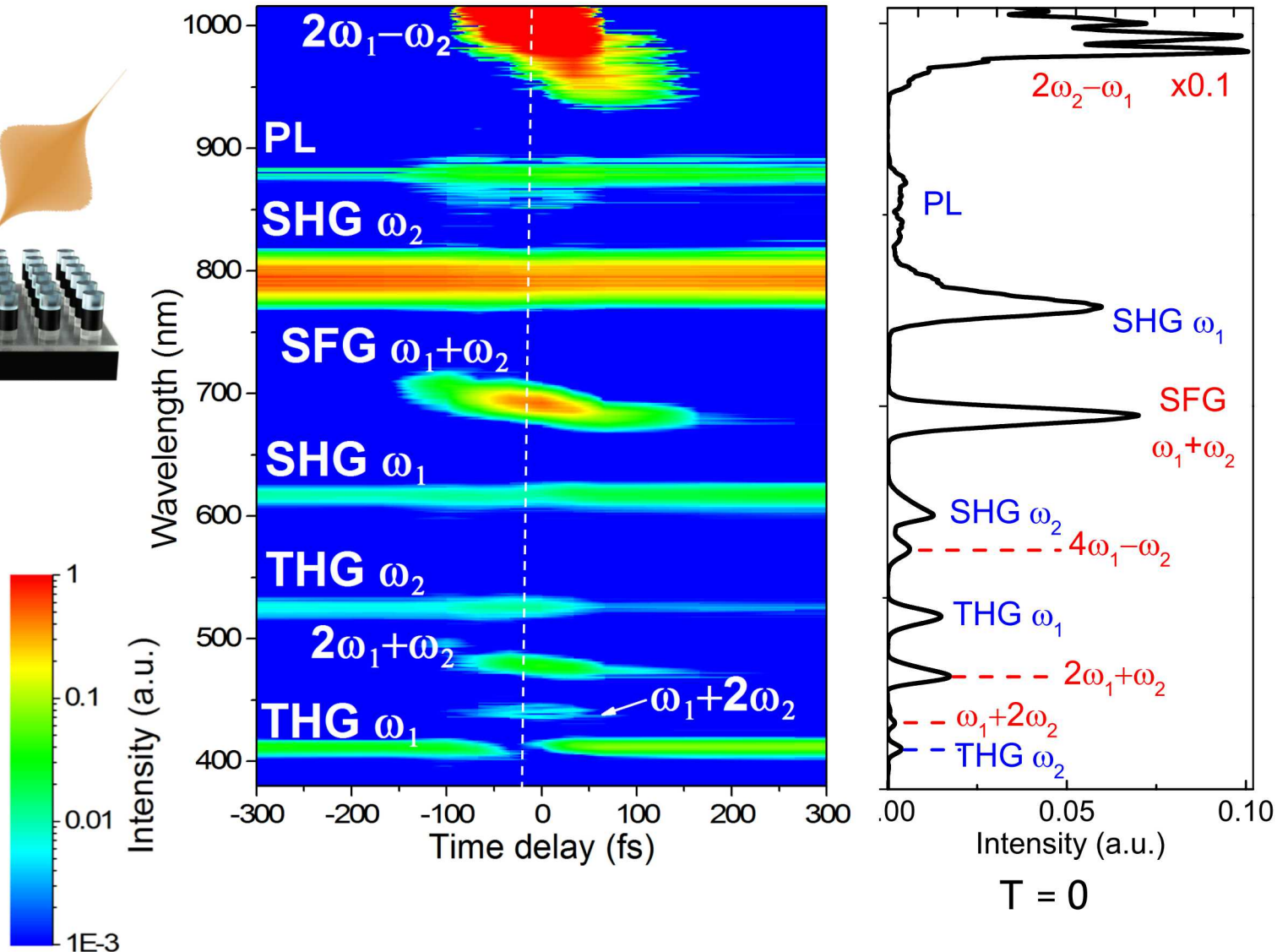
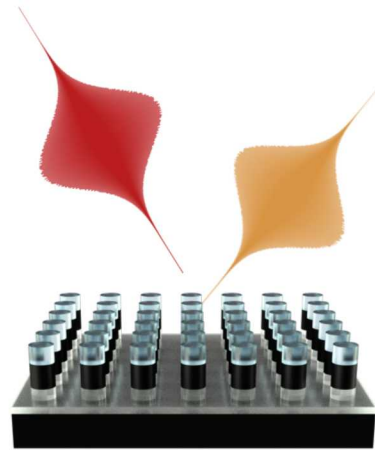


Wavelength shift

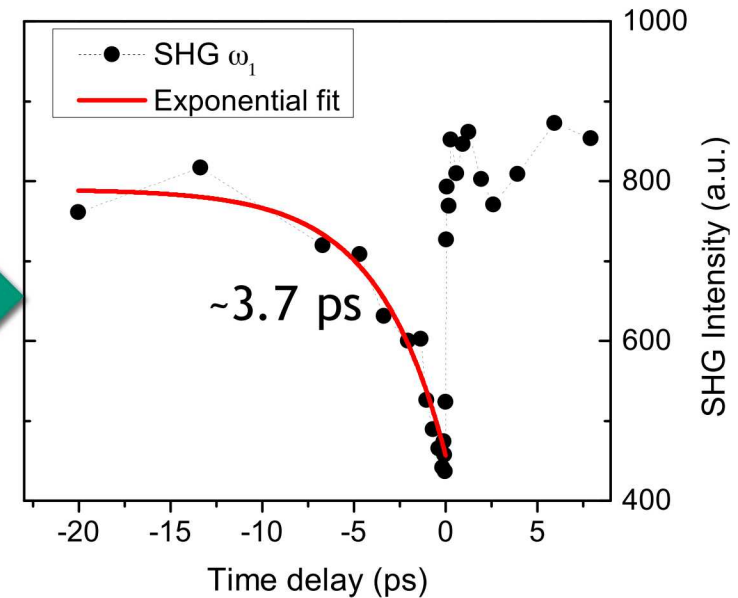
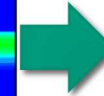
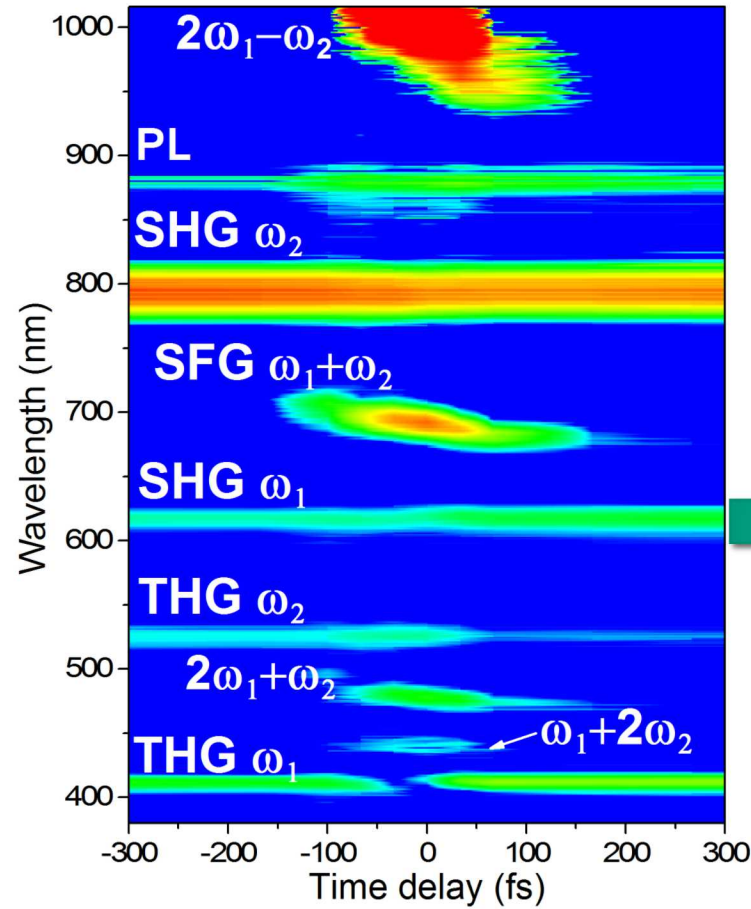
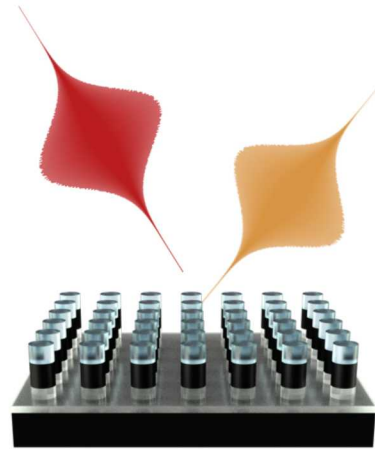
SWM power dependence



# Temporal dynamics of frequency mixing



# Temporal dynamics of frequency mixing



Shcherbakov, Maxim R., et al.  
*Nature communications* 8.1 (2017): 17

| Our work                                              | Other Dielectric metasurfaces | Plasmonic Nanstructures  |
|-------------------------------------------------------|-------------------------------|--------------------------|
| SHG<br>THG<br>FHG<br>SFG<br>FWM (1)<br>FWM (2)<br>SWM | SHG<br>THG<br>SFG<br>FWM      | SHG<br>THG<br>SFG<br>FWM |

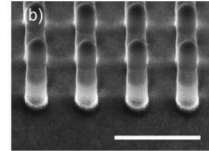
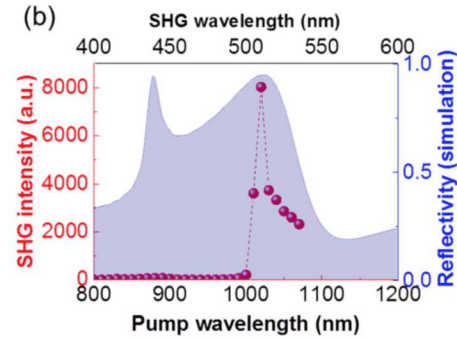
- The even and odd order nonlinearities of GaAs enable our observation of second-, third- and fourth-harmonic generation, sum-frequency generation, two-photon absorption induced photoluminescence, four-wave mixing, and six-wave mixing.

Liu, S.\*, Vabishchevich, P. P.\*, Vaskin, A., Reno, J. L., Keeler, G. A., Sinclair, M. B., ... & Brener, I. (2017). An optical metamixer. *arXiv preprint arXiv:1711.00090*.

# Enhancement of nonlinear processes in metasurfaces



## SHG efficiency



Efficiency: power of generated SHG/pump power

## Second Harmonic Generation ( $10^{-4}$ - $10^{-5}$ )

Carletti, L., et al. *Optics express* 23.20, 26544-26550, **2015**

Camacho-Morales, R., et al. *Nano letters* 16.11, 7191-7197, **2016**

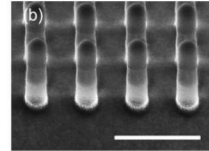
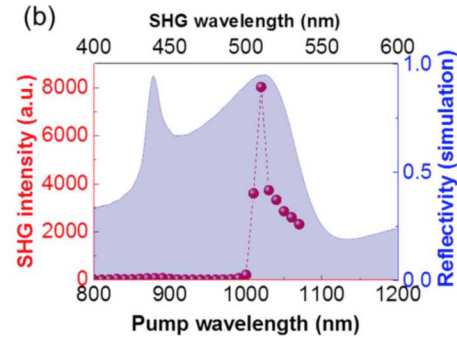
Kruk, S. et al. *Nano Lett.*, 17 (6), pp 3914–3918, **2017**

Liu, S. et. al. *Nano letters* 16.9, 5426-5432, **2016**

# Enhancement of nonlinear processes in metasurfaces



## SHG efficiency



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## Second Harmonic Generation ( $10^{-4}$ - $10^{-5}$ )

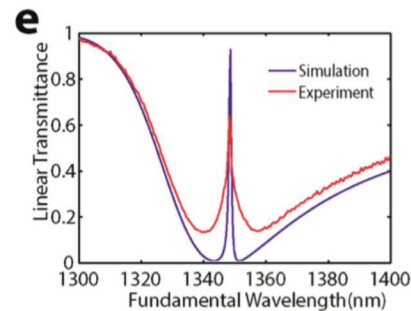
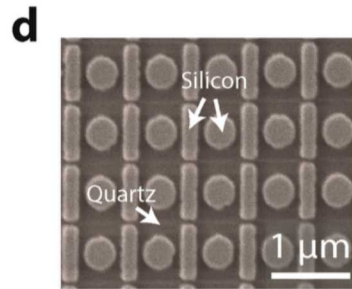
Carletti, L., et al. *Optics express* 23.20, 26544-26550, **2015**

Camacho-Morales, R., et al. *Nano letters* 16.11, 7191-7197, **2016**

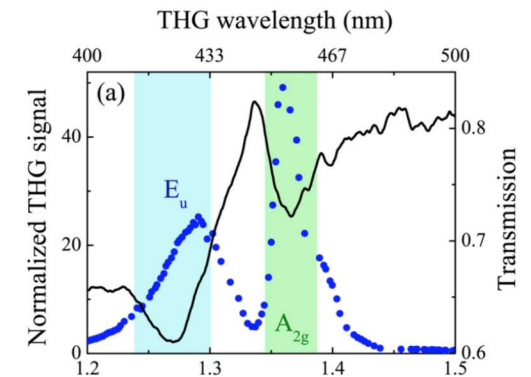
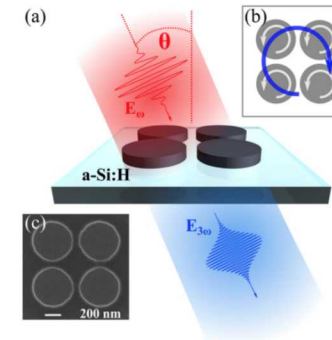
Kruk, S. et al. *Nano Lett.*, 17 (6), pp 3914–3918, **2017**

Liu, S. et. al. *Nano letters* 16.9, 5426-5432, **2016**

## Fano resonances and BIC modes: Slit and bar metasurface design



## Oligomer metasurfaces



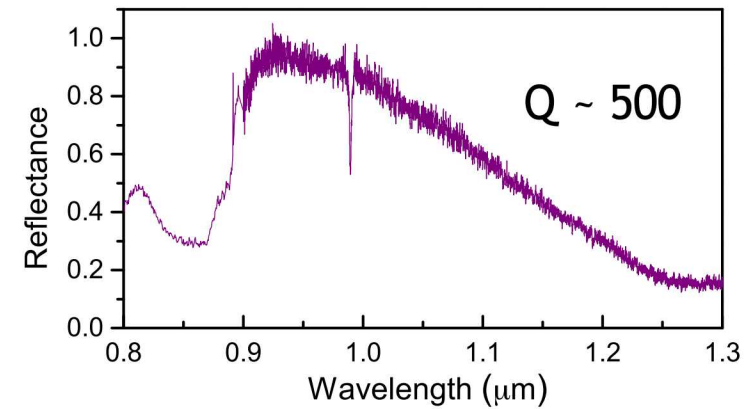
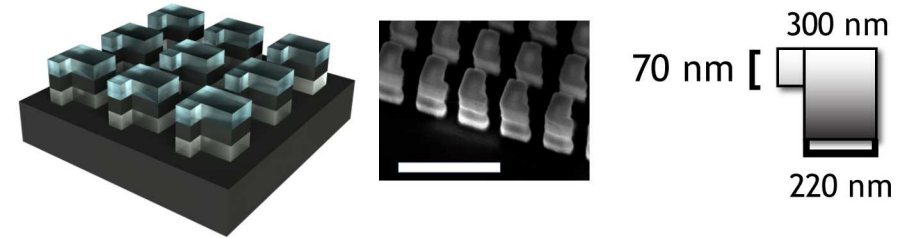
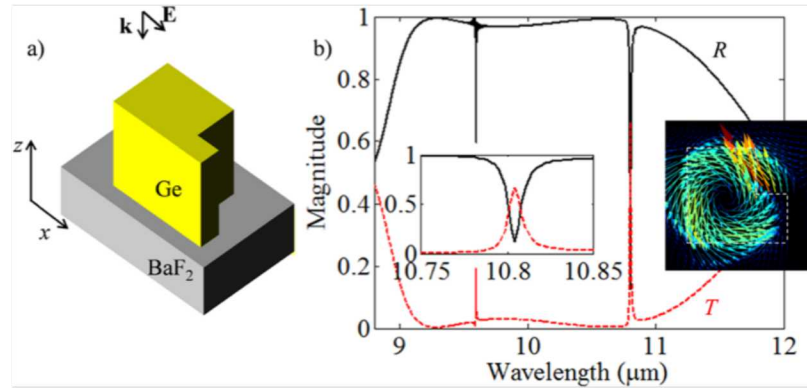
Yang, Y et. al *Nano Lett.* 2015, 15 (11), 7388–7393.

Shorokhov, A. S et. al *Nano Lett.* 2016, 16 (8), 4857–4861.

Carletti, Luca, et al. *Physical review letters* 121.3 (2018): 033903.

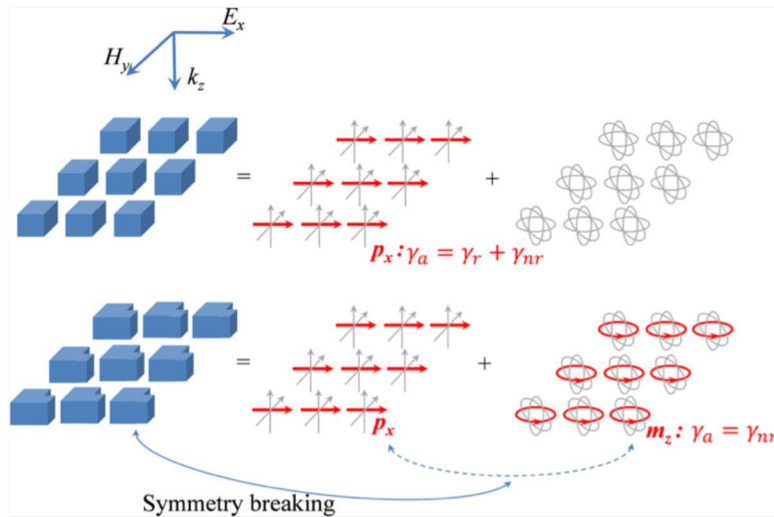
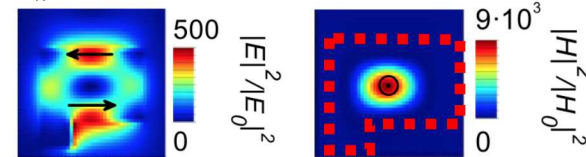
# Metasurface with broken symmetry design resonators: High-Q factor resonance

22



Fano resonance

$\lambda_R \sim 0.98 \text{ nm}$



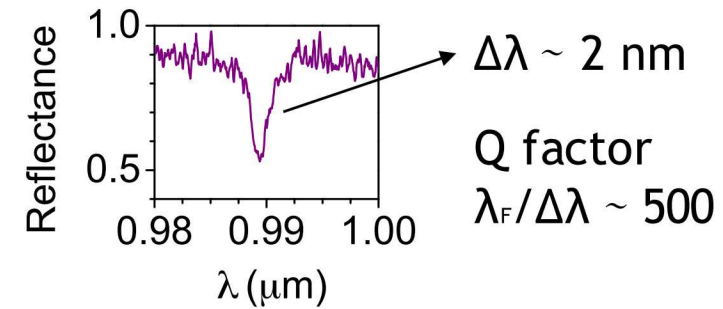
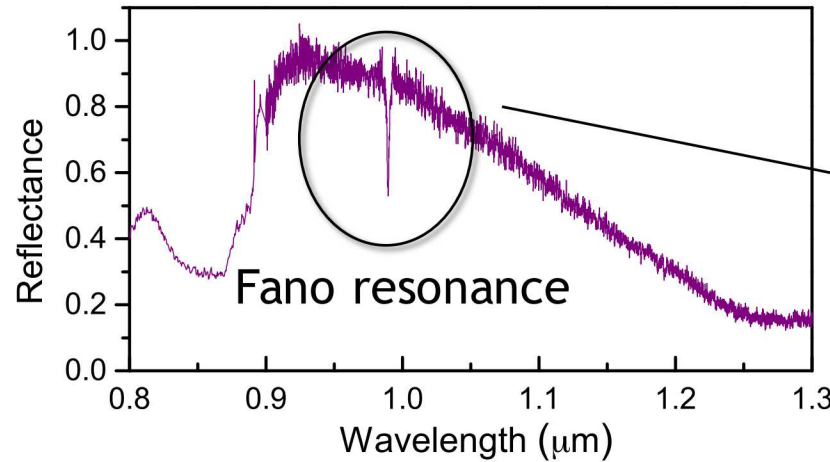
Campione, S. et al ACS Photonics 3 (12), 2362–2367, **2016**

Vabishchevich, P., et al. ACS Photonics, 5 (5), pp 1685-1690, **2018**

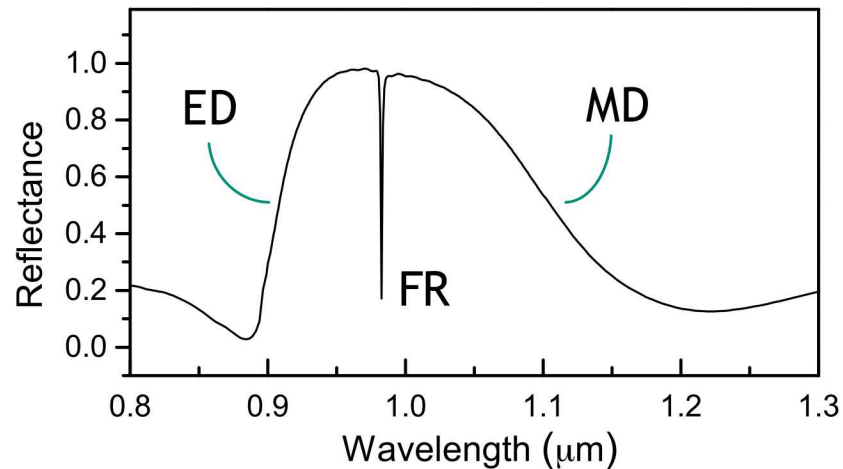
# Fano metasurface reflectance spectrum



## Experimental measurements

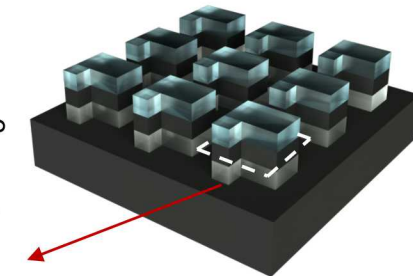
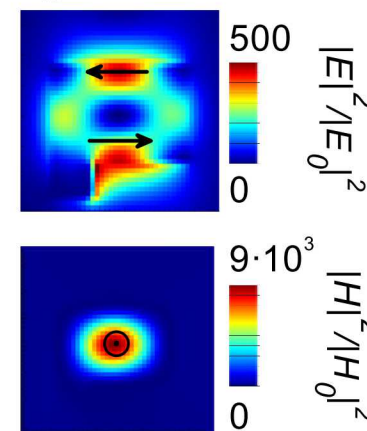


## FDTD simulations

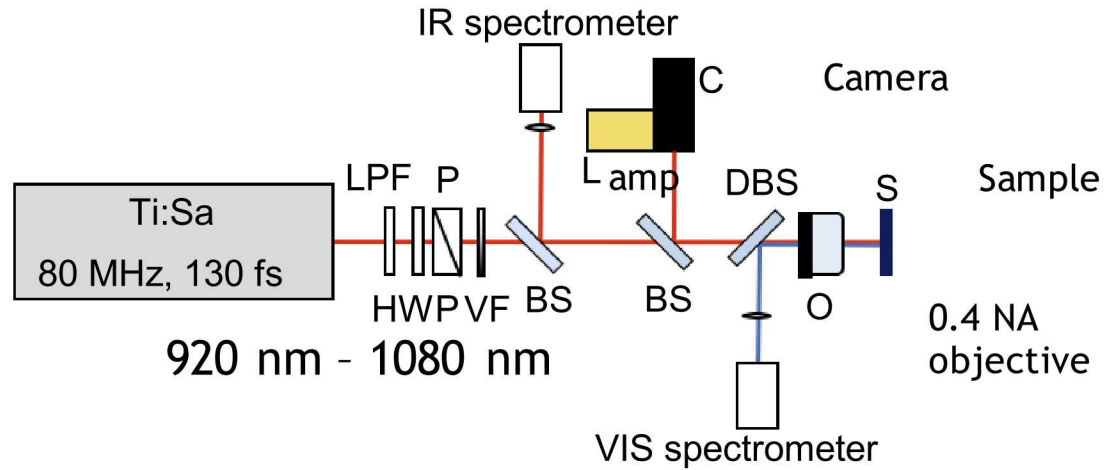


## Fano resonance

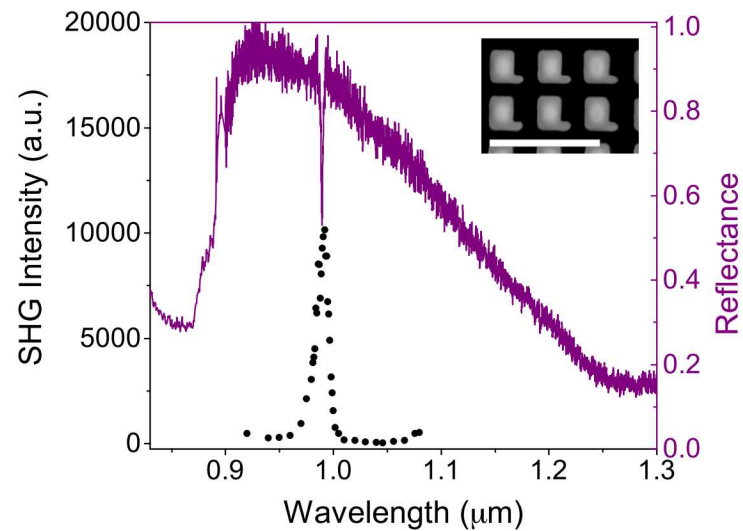
$\lambda_R \sim 0.98 \text{ nm}$



# SHG in Fano metasurface

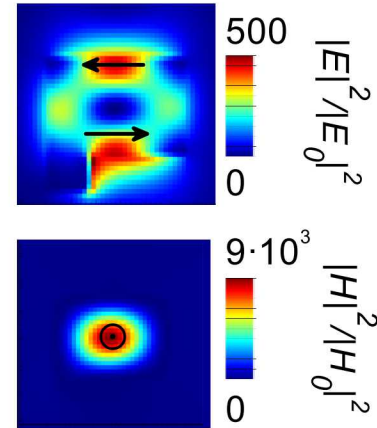


## SHG intensity enhancement in the vicinity of the Fano resonance x300



Fano resonance

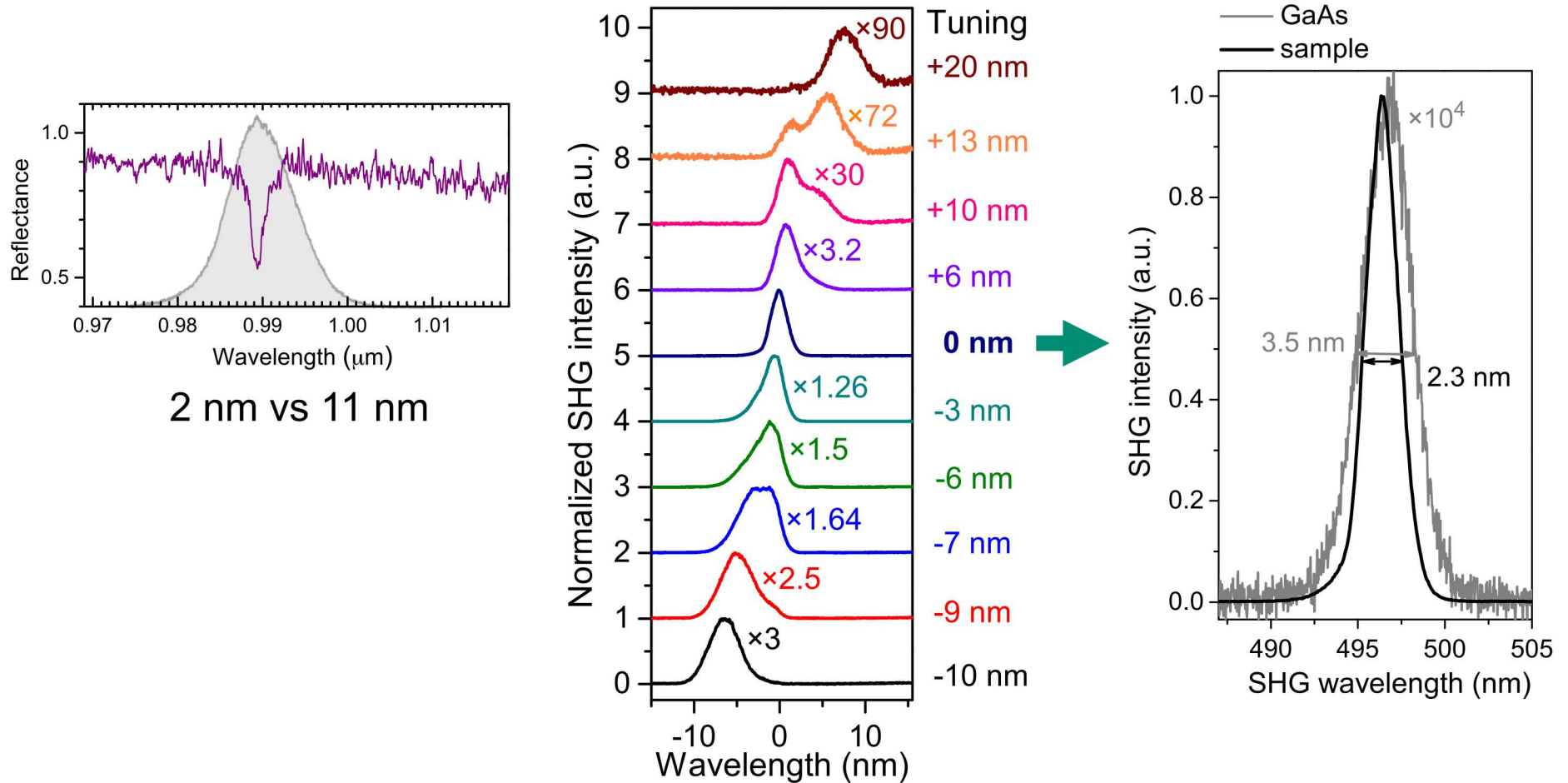
$\lambda_R \sim 0.98 \text{ nm}$



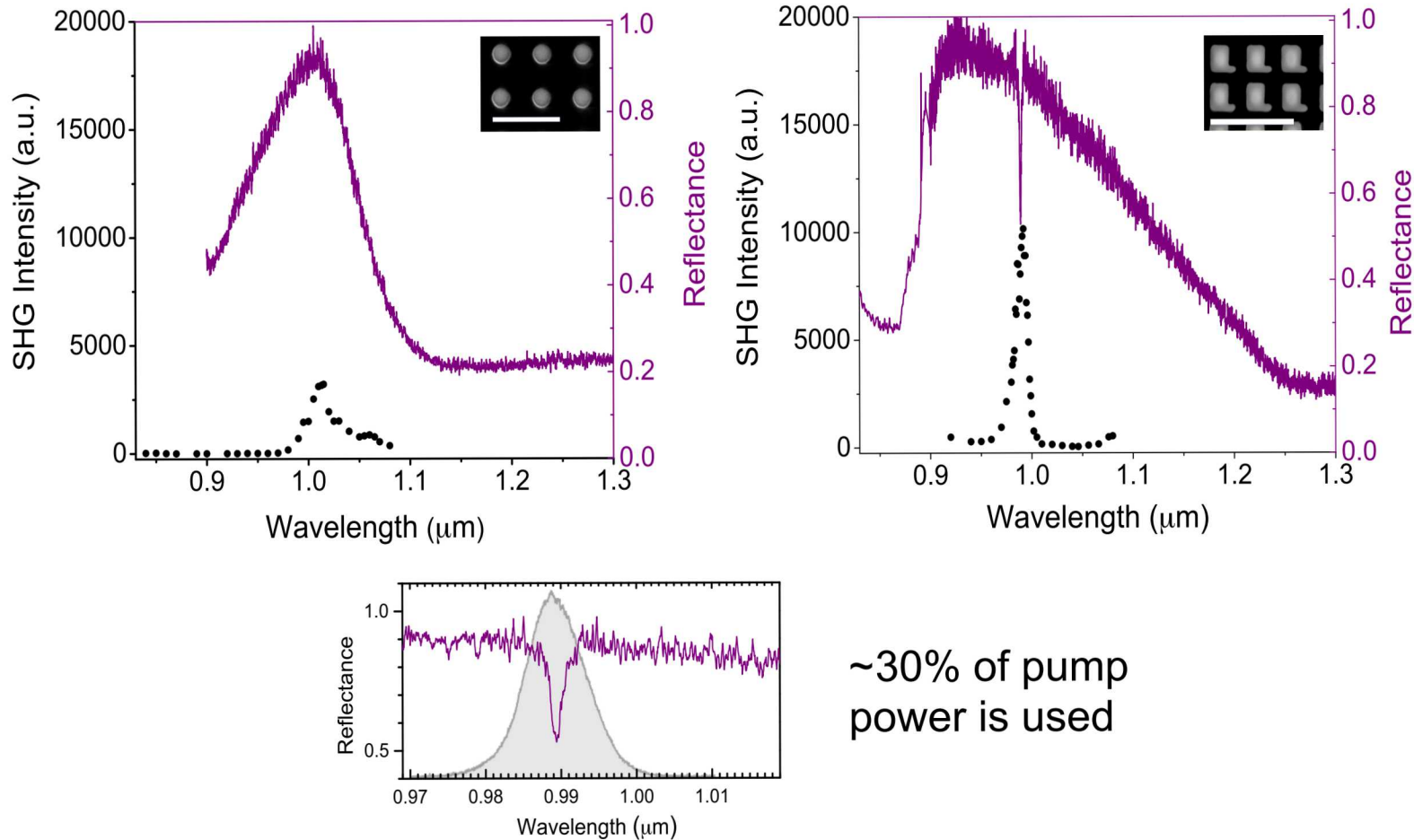
# SHG spectra modification



The modification of a SHG spectrum when the pump carrier wavelength is detuned from the Fano resonant wavelength

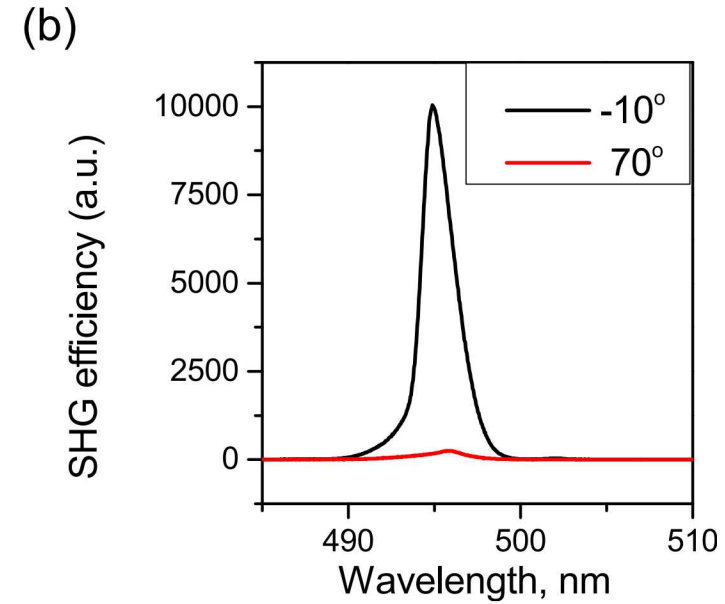
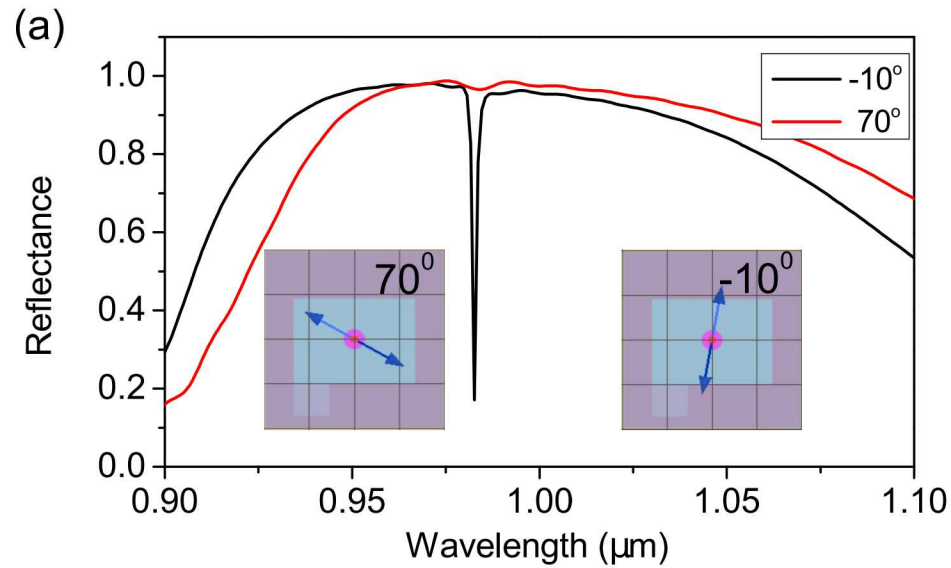


# Nanodisk metasurface vs Fano metasurface

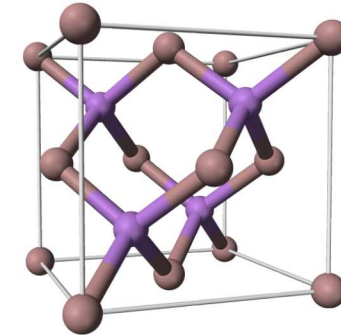


**13-fold enhancement of SHG in Fano metasurface in comparison with the nanodisk metasurface**

# Polarization dependence of SHG

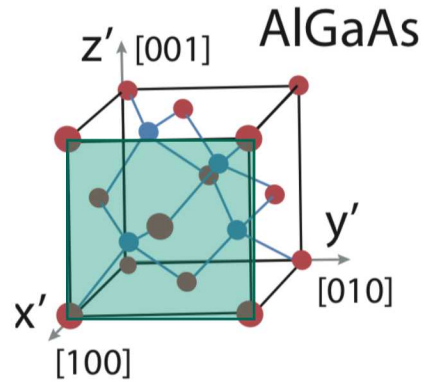


Match the asymmetric shape of the sample with the crystalline axis of GaAs



<https://www.wikipedia.org>

# GaAs (100) lattice plane

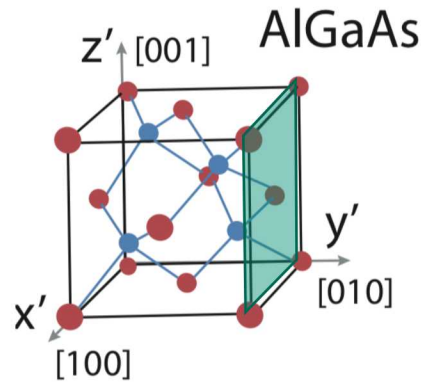


$$\begin{pmatrix} P_x(2\omega) \\ P_y(2\omega) \\ P_z(2\omega) \end{pmatrix} = 2\varepsilon_0 d_{eff} \begin{pmatrix} E_x(\omega)^2 \\ E_y(\omega)^2 \\ E_z(\omega)^2 \\ 2E_y(\omega) \cdot E_z(\omega) \\ 2E_x(\omega) \cdot E_z(\omega) \\ 2E_y(\omega) \cdot E_x(\omega) \end{pmatrix}$$

$$d_{eff} = \begin{pmatrix} 0 & 0 & 0 & d_{41} & 0 & 0 \\ 0 & 0 & 0 & 0 & d_{41} & 0 \\ 0 & 0 & 0 & 0 & 0 & d_{41} \end{pmatrix}$$

Absence of SHG in normal direction

# GaAs (100) single disk and metasurface emission patterns

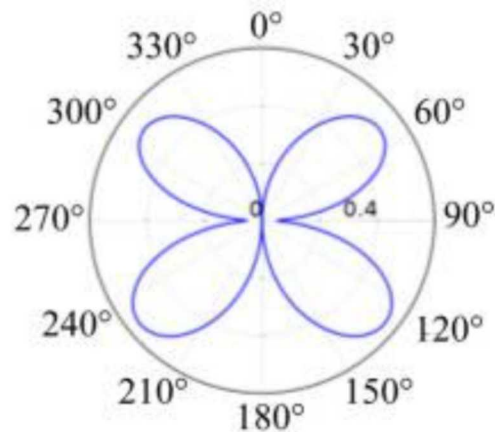
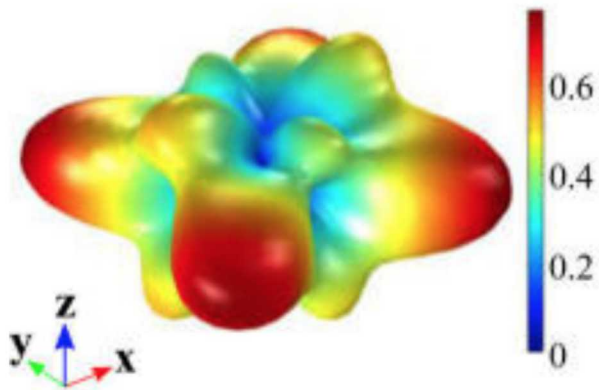


$$d_{eff} = \begin{pmatrix} 0 & 0 & 0 & d_{41} & 0 & 0 \\ 0 & 0 & 0 & 0 & d_{41} & 0 \\ 0 & 0 & 0 & 0 & 0 & d_{41} \end{pmatrix}$$



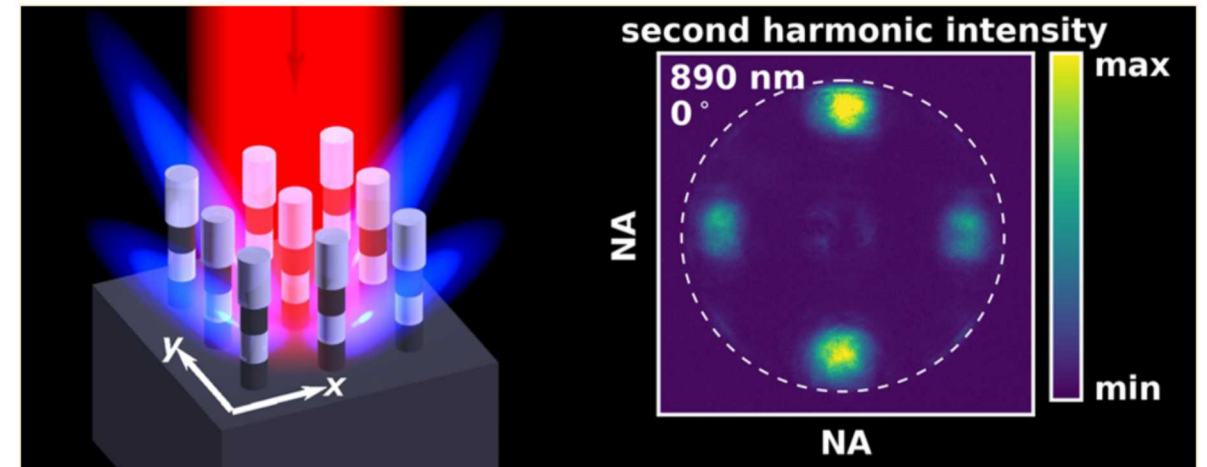
Absence of SHG in normal direction

**SHG radiation pattern in AlGaAs (100) nanodisks at MD resonance**



L. Carletti et al., *ACS Photonics*, 3(8), 1500-1507, 2016

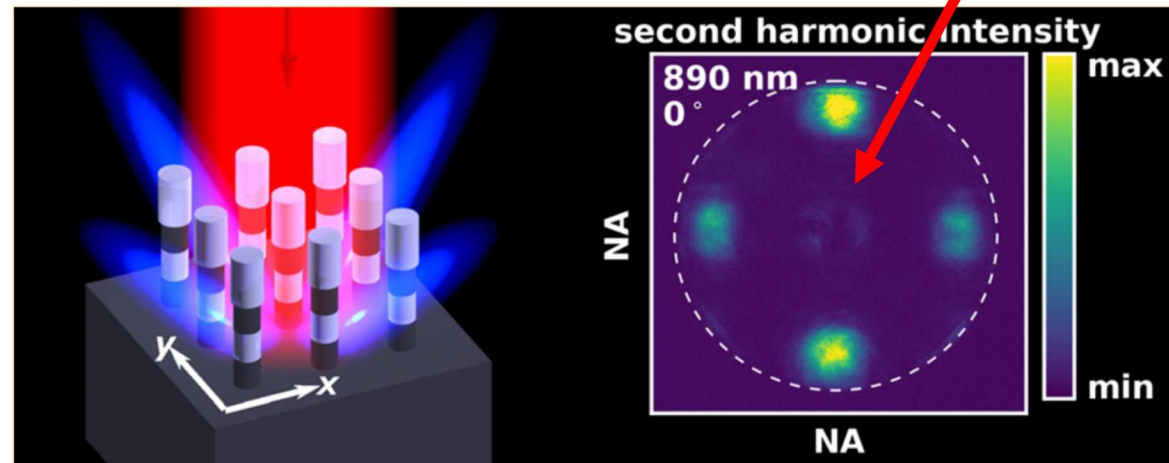
**SHG diffraction in the GaAs (100) metasurface**



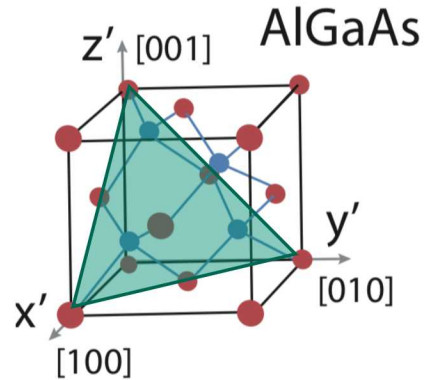
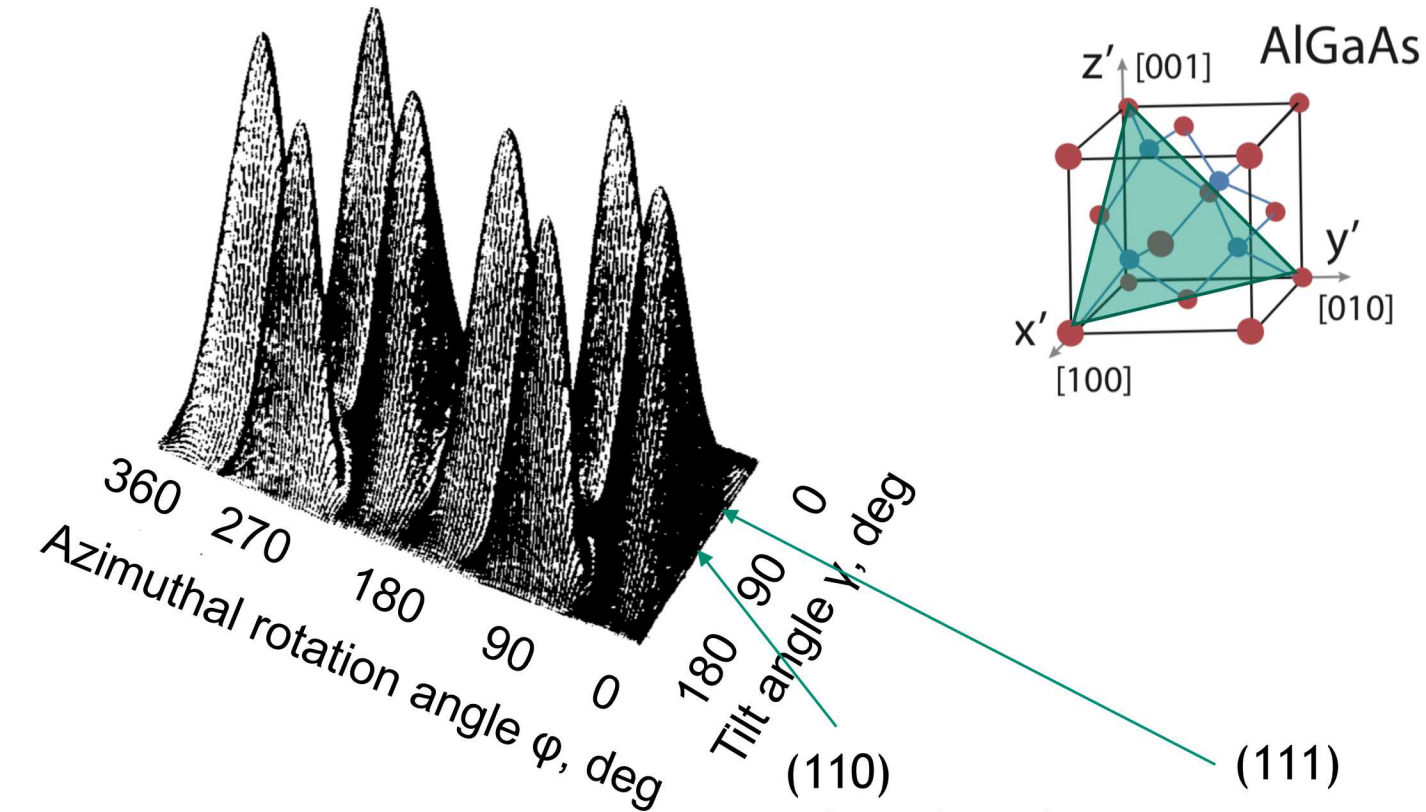
Löchner, F. J., *ACS Photonics*, 5(5), 1786-1793, 2018

**Absence of the zeroth-order**

Goal: Redirection of the SHG emission  
to zeroth diffraction order in GaAs  
metasurfaces



# SHG in GaAs for different orientations of the crystal, (111), (110)



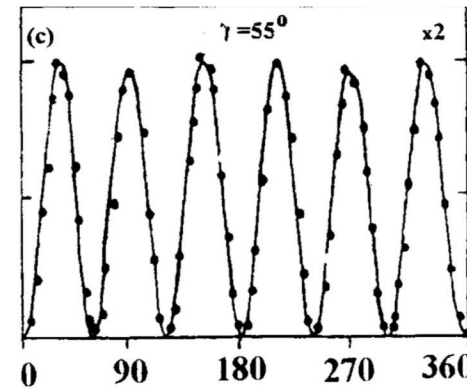
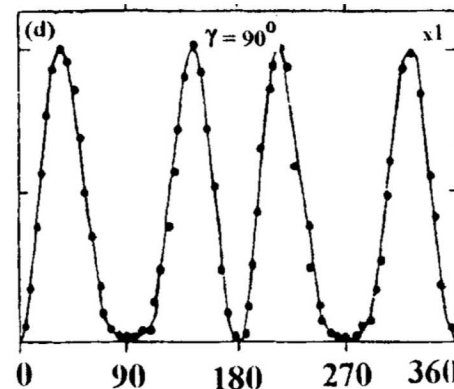
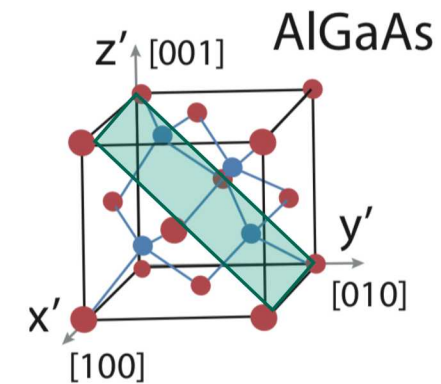
$$d_{eff} = \begin{pmatrix} -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{6}} & 0 & 0 & -\frac{1}{\sqrt{3}} & 0 \\ 0 & 0 & 0 & -\frac{1}{\sqrt{3}} & 0 & -\frac{1}{\sqrt{6}} \\ -\frac{1}{2\sqrt{3}} & -\frac{1}{2\sqrt{3}} & \frac{1}{\sqrt{3}} & 0 & 0 & 0 \end{pmatrix} \cdot d_{41}$$

Non-zero SHG signal for  
under normal incidence

$$P_x(2w) = 2\varepsilon_0 d_{eff} \left(-\frac{1}{\sqrt{6}}\right) E_x(w)^2 + \frac{1}{\sqrt{6}} E_y(w)^2 - \frac{1}{\sqrt{3}} E_x(w) E_z(w)$$

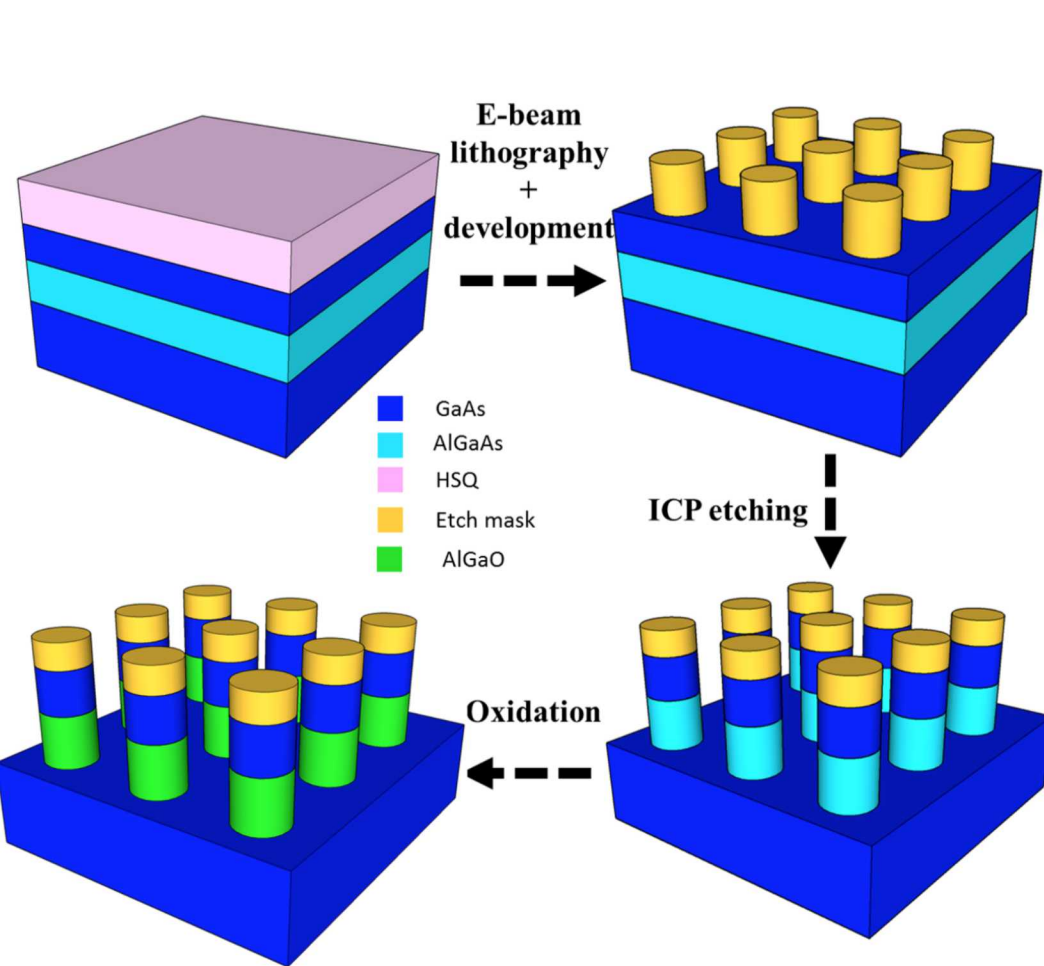
$$P_y(2w) = 2\varepsilon_0 d_{eff} \left(-\frac{2}{\sqrt{3}}\right) E_y(w) E_z(w) - \frac{1}{\sqrt{6}} E_x(w) E_z(w)$$

$$P_z(2w) = 2\varepsilon_0 d_{eff} \left(-\frac{1}{2\sqrt{3}}\right) E_x(w)^2 - \frac{1}{2\sqrt{3}} E_y(w)^2 - \frac{1}{1\sqrt{3}} E_z^2$$

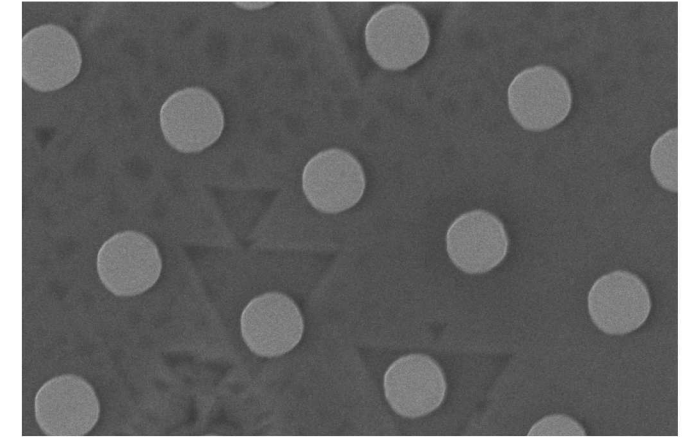


ROTATION ANGLE  $\varphi$  (degree)

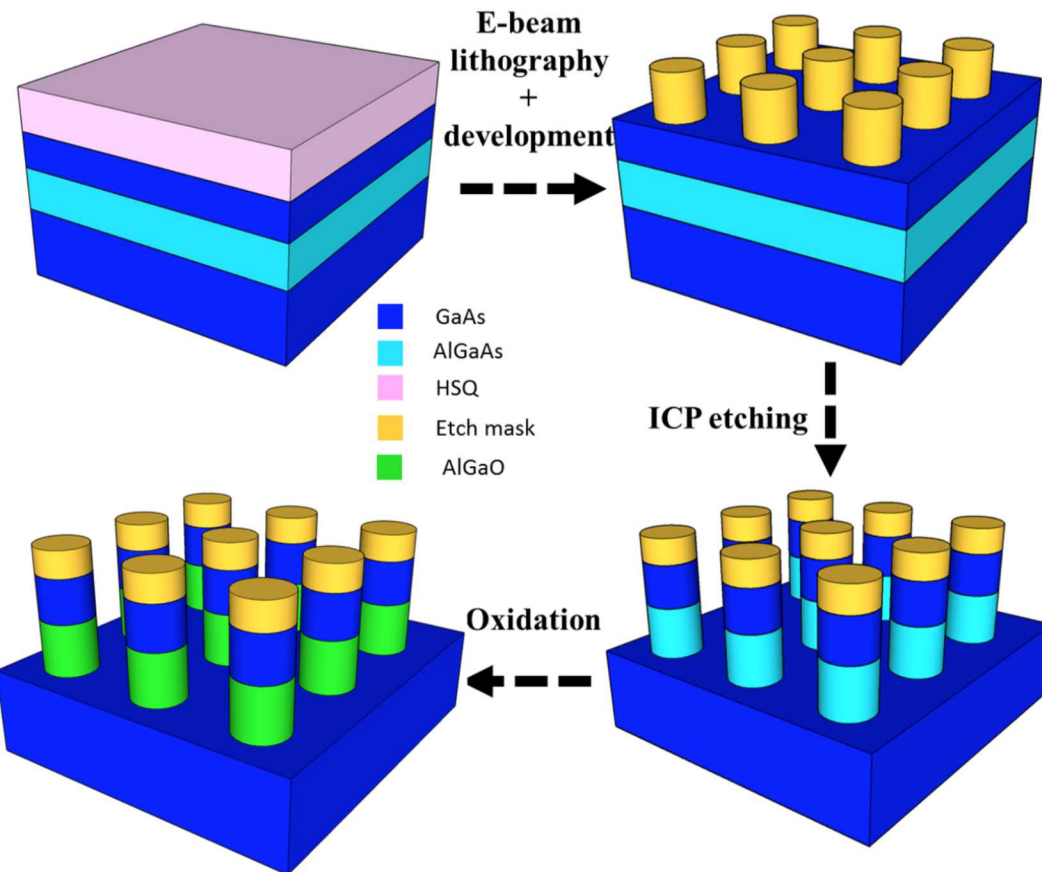
# Fabrication of GaAs metasurface



$\text{SiO}_x$  – 400 nm  
 **$\text{Al}_{0.1}\text{Ga}_{0.9}\text{As}$  – 400 nm**  
 $(\text{Al}_x\text{Ga}_{1-x})_2\text{O}_3$  – 500 nm  
Diameter – 340 nm  
Period – 1200 nm

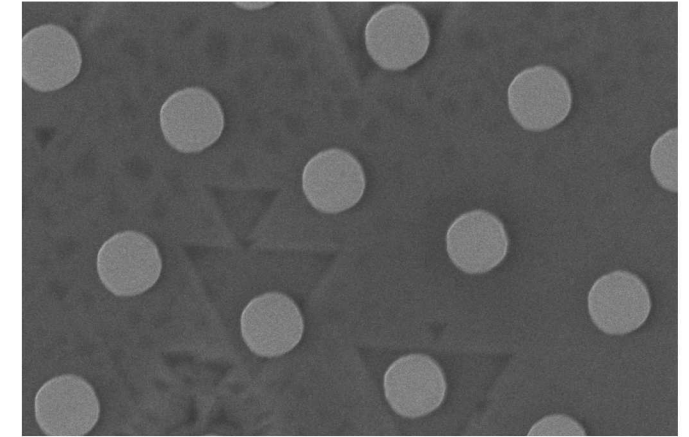


# Fabrication of GaAs metasurface

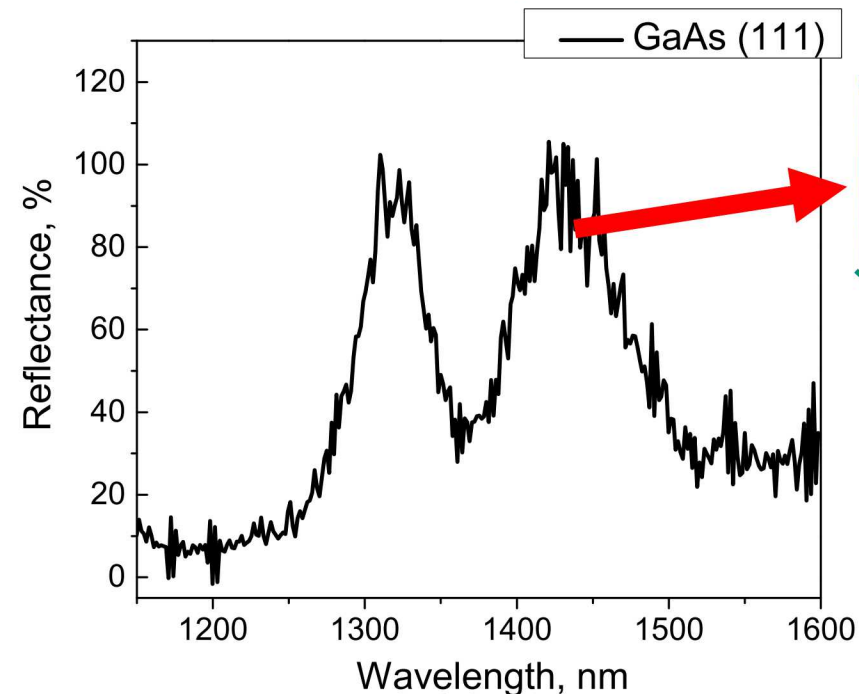


Liu, S. et. al. *Nano letters* 16.9: 5426-5432, 2016

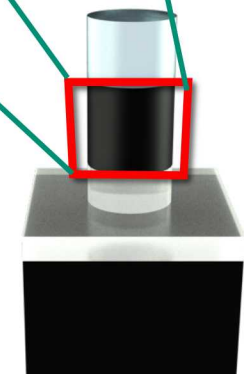
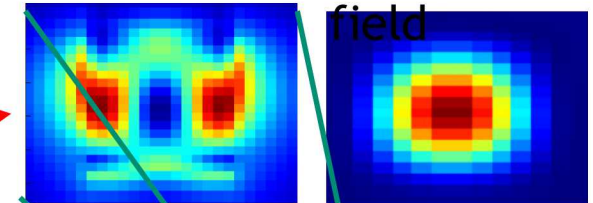
$\text{SiO}_x$  – 400 nm  
 $\text{Al}_{0.1}\text{Ga}_{0.9}\text{As}$  – 400 nm  
 $(\text{Al}_x\text{Ga}_{1-x})_2\text{O}_3$  – 500 nm  
 Diameter – 340 nm  
 Period – 1200 nm



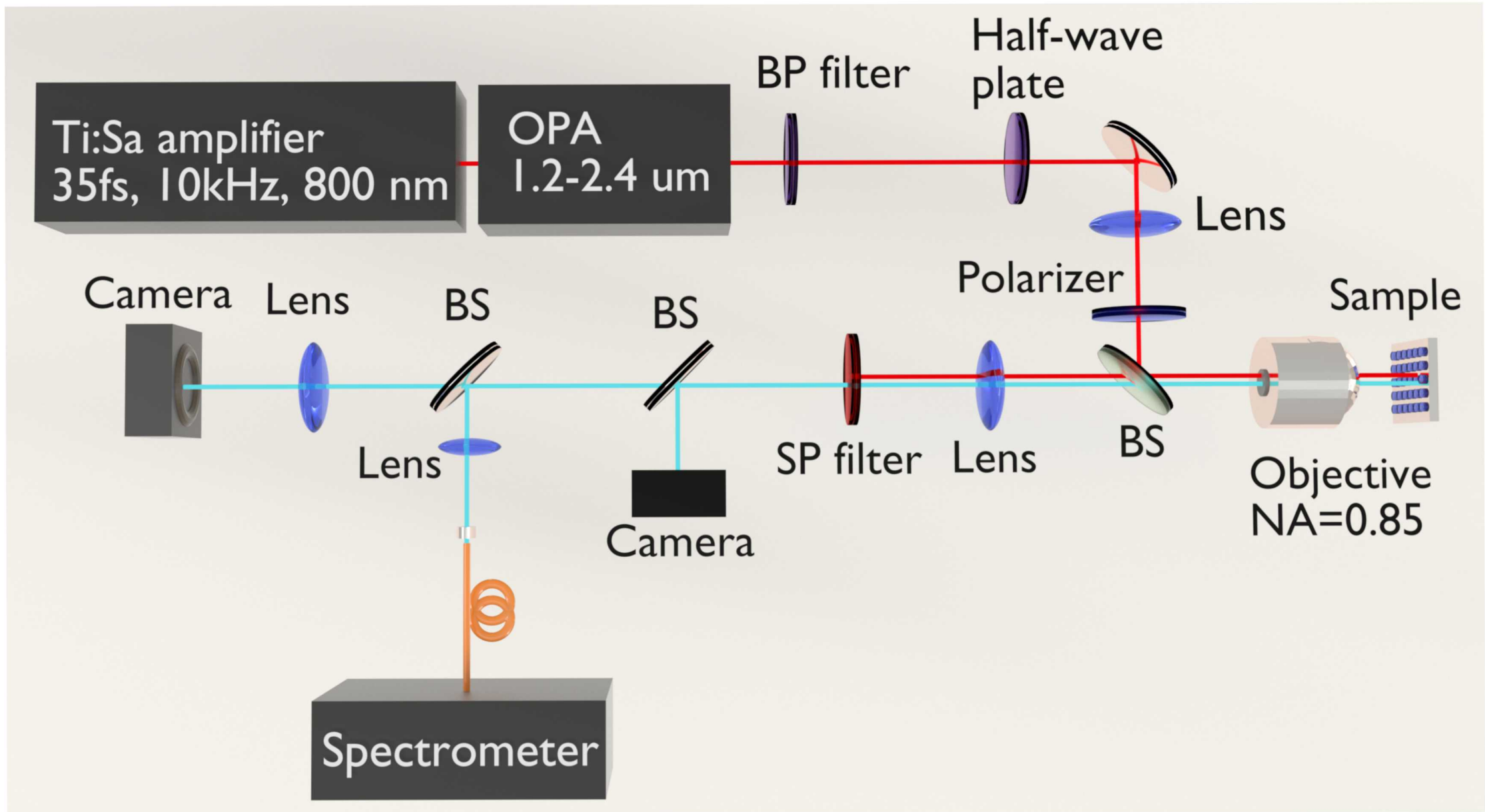
## Reflectance spectrum



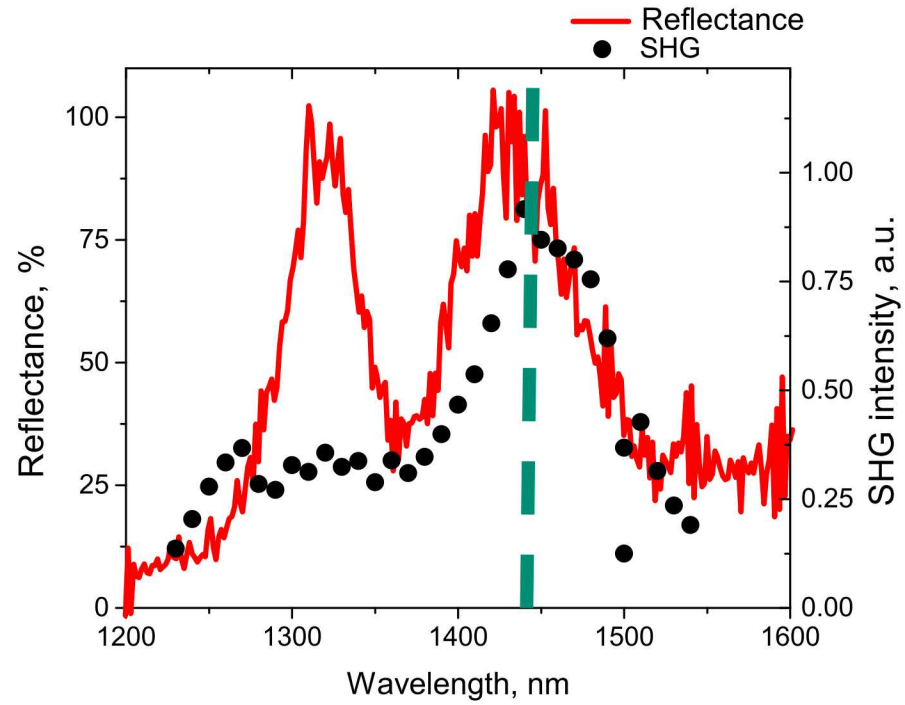
Electric field Magnetic field



# Experimental setup: Fourier-space imaging

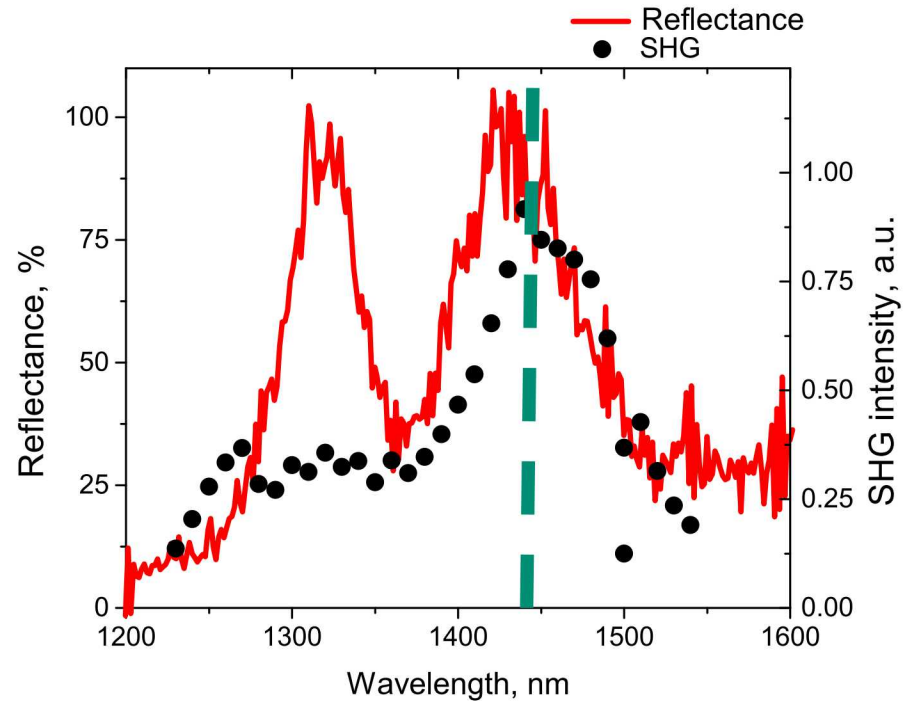


# SHG in GaAs (111) metasurface

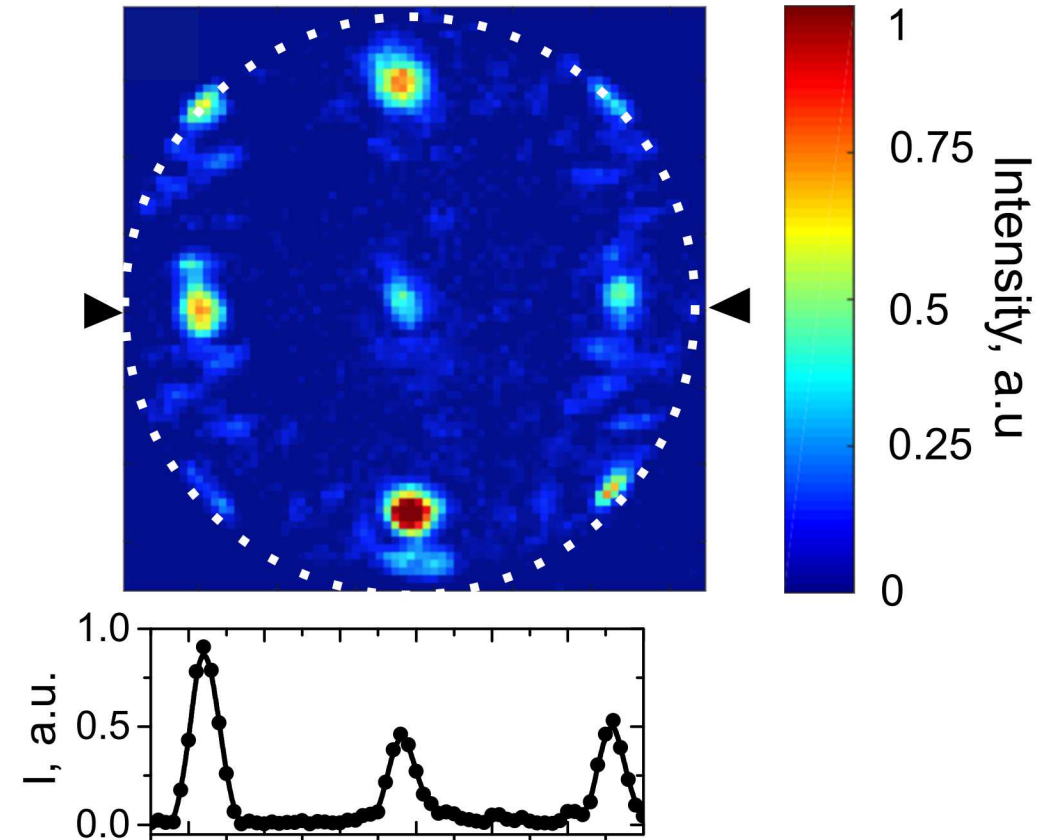


**SHG enhancement at the wavelength  
of MD resonance**

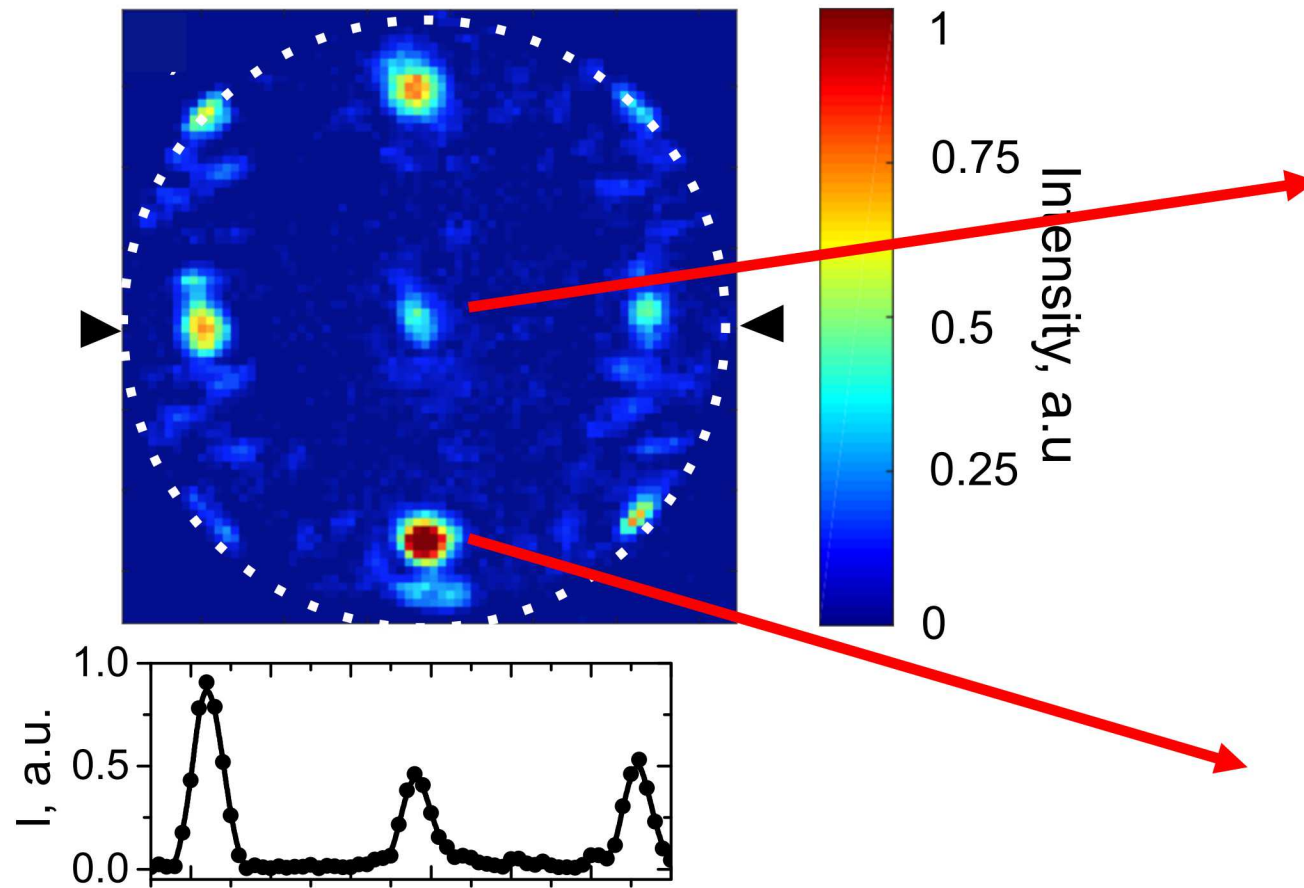
# SHG in GaAs (111) metasurface: Fourier-space image



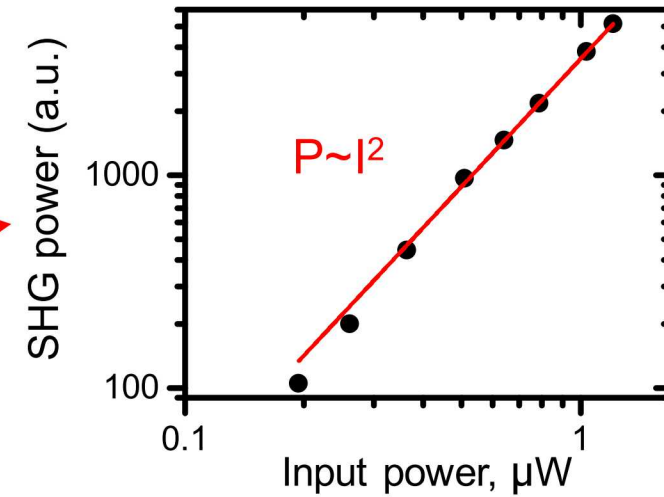
**SHG enhancement at the wavelength of MD resonance**



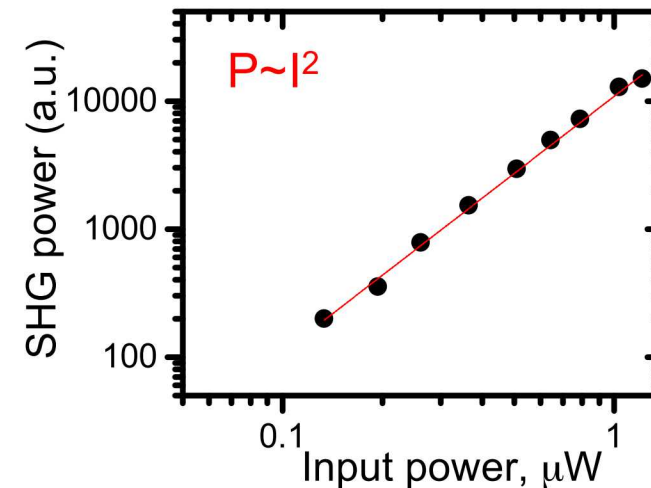
# SHG in GaAs (111) metasurface: Fourier-space image



Power dependence for the zeroth-order diffraction



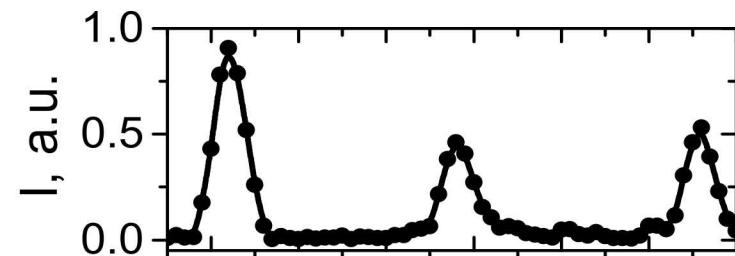
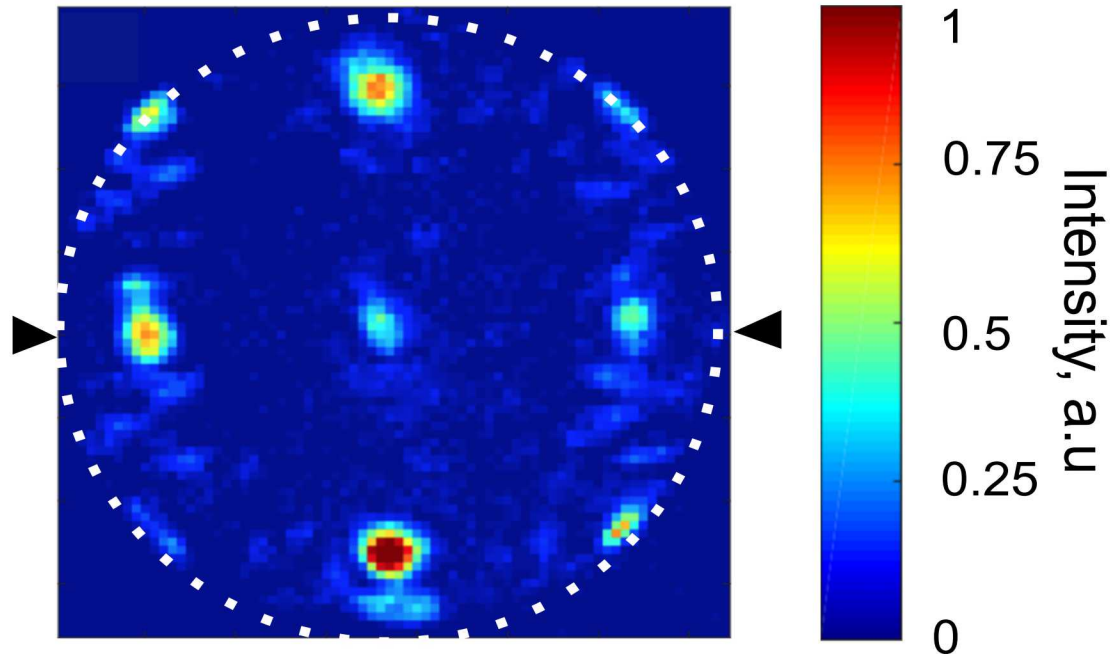
Power dependence for the bottom diffraction peak



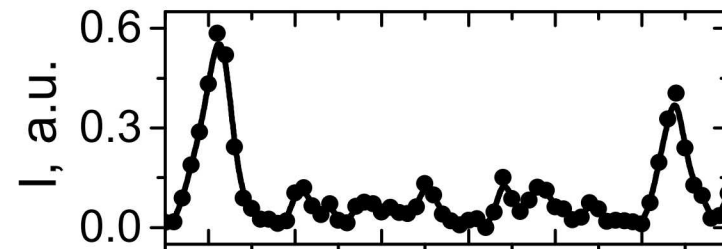
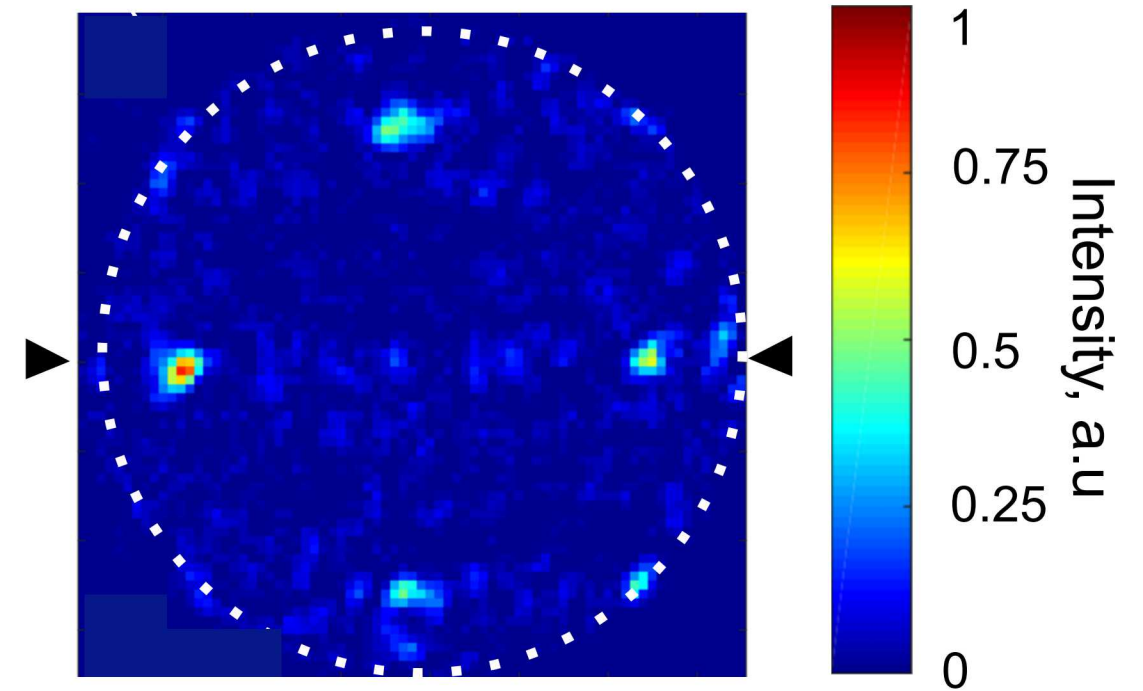
# Comparison: Fourier-space images for metasurfaces with different crystallographic planes



**(111)**



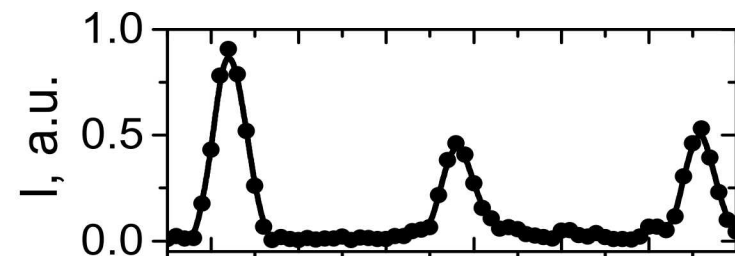
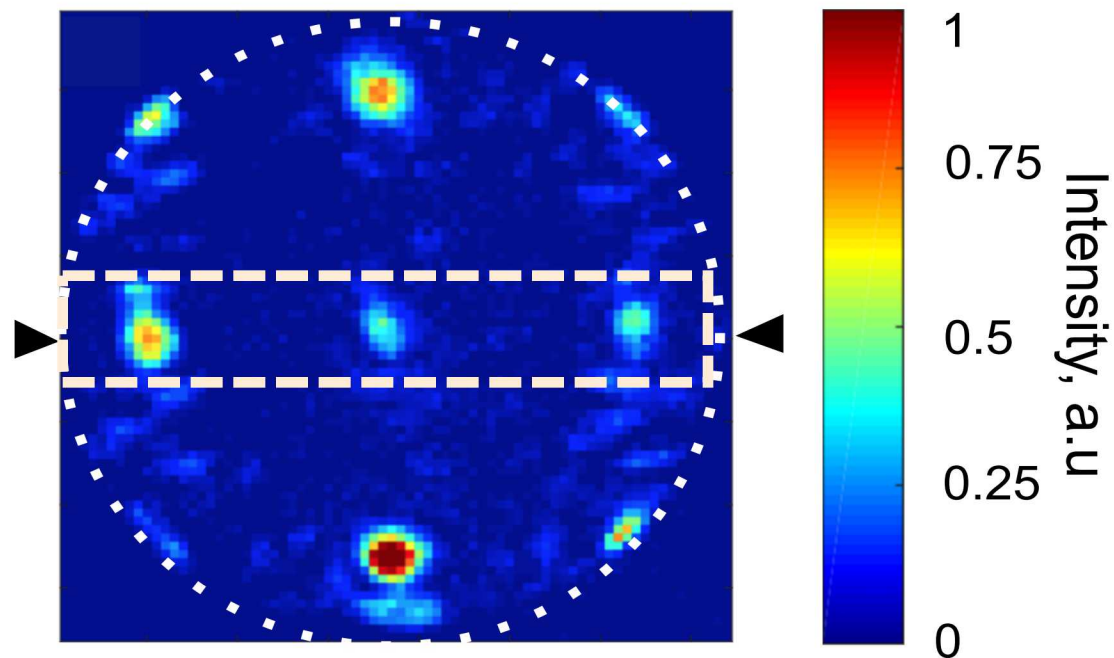
**(100)**



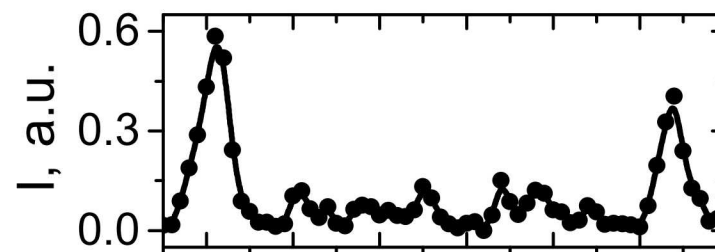
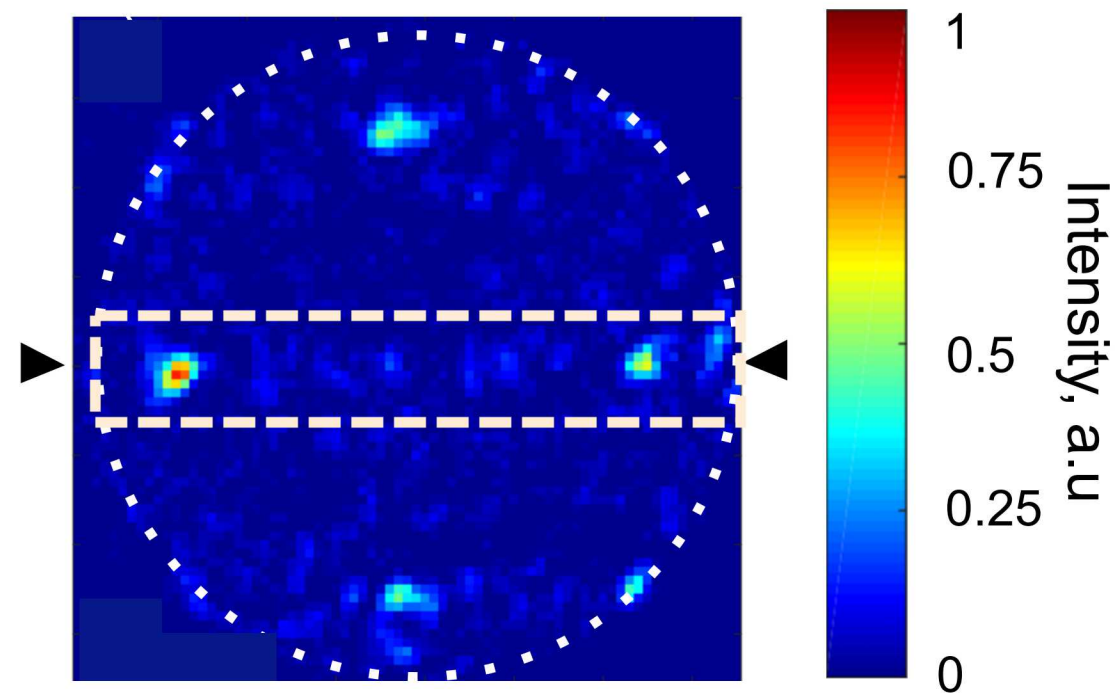
# Comparison: Fourier-space images for metasurfaces with different crystallographic planes



**(111)**

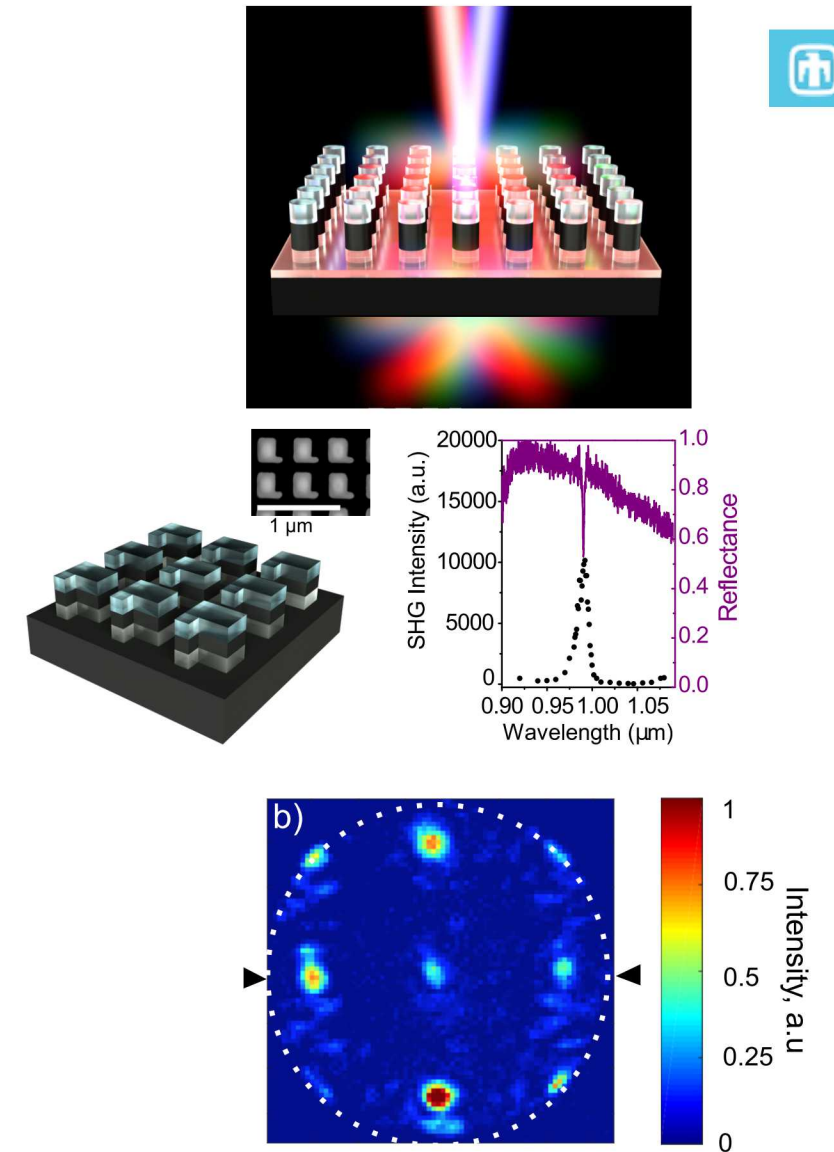


**(100)**

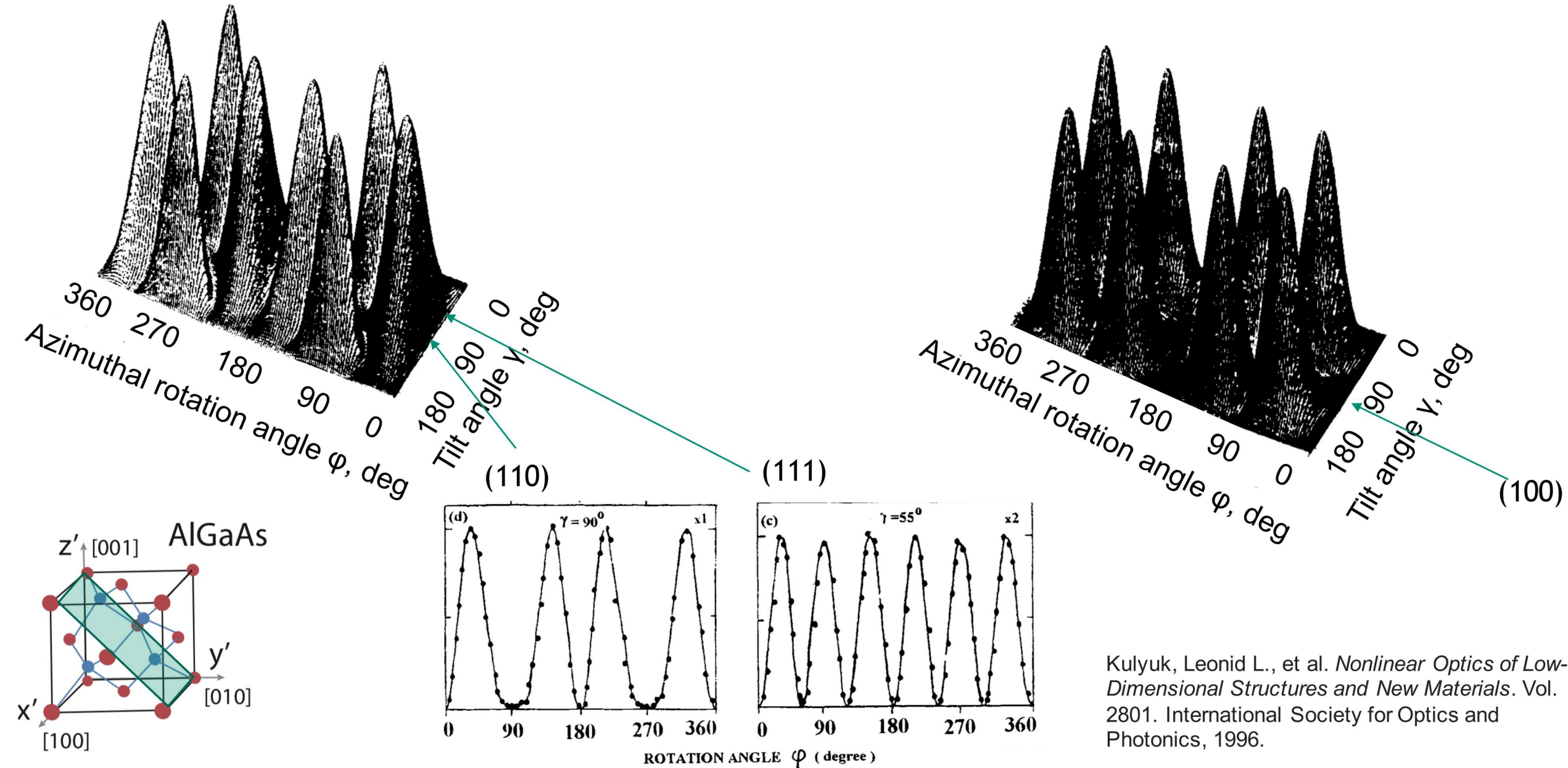


# Conclusions

- The even and odd order nonlinearities of GaAs enable our observation of second-, third- and fourth-harmonic generation, sum-frequency generation, two-photon absorption induced photoluminescence, four-wave mixing, and six-wave mixing.
- Nontrivial spectral shaping of second-harmonic spectra in symmetry broken III-V semiconductor metasurface.
- We utilize III-V semiconductor metasurface fabricated from GaAs grown on (111) lattice plane to control the spatial distribution of the SHG intensity. By changing the orientation of the GaAs crystal from (100) to (111) plane we were able to redistribute the SHG generation to the zeroth diffraction order.

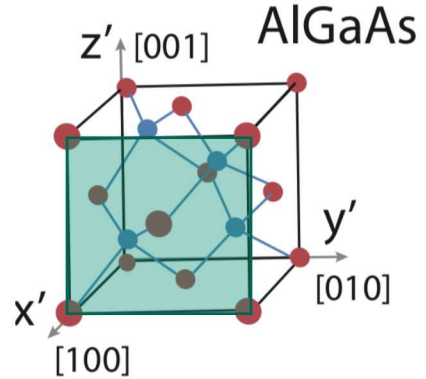


# SHG in GaAs for different orientations of the crystal, (111), (110), (100)



Kulyuk, Leonid L., et al. *Nonlinear Optics of Low-Dimensional Structures and New Materials*. Vol. 2801. International Society for Optics and Photonics, 1996.

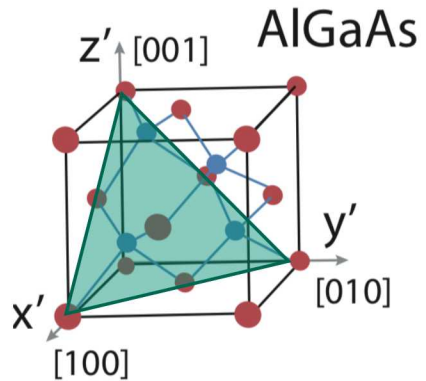
# Use of (111) GaAs/AlGaAs



$$d_{eff} = \begin{pmatrix} 0 & 0 & 0 & d_{41} & 0 & 0 \\ 0 & 0 & 0 & 0 & d_{41} & 0 \\ 0 & 0 & 0 & 0 & 0 & d_{41} \end{pmatrix}$$



Absence of SHG under normal incidence



$$d_{eff} = \begin{pmatrix} -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{6}} & 0 & 0 & -\frac{1}{\sqrt{3}} & 0 \\ 0 & 0 & 0 & -\frac{1}{\sqrt{3}} & 0 & -\frac{1}{\sqrt{6}} \\ -\frac{1}{2\sqrt{3}} & -\frac{1}{2\sqrt{3}} & \frac{1}{\sqrt{3}} & 0 & 0 & 0 \end{pmatrix} \cdot d_{41}$$



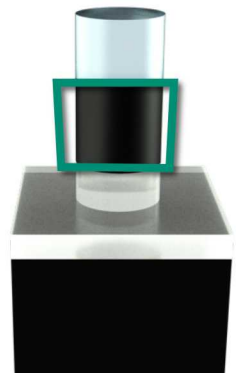
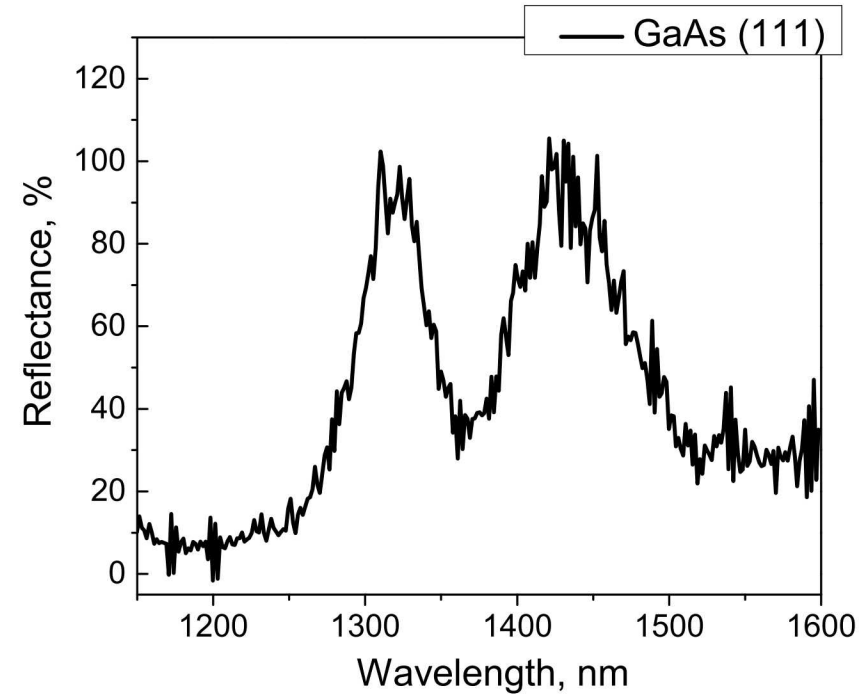
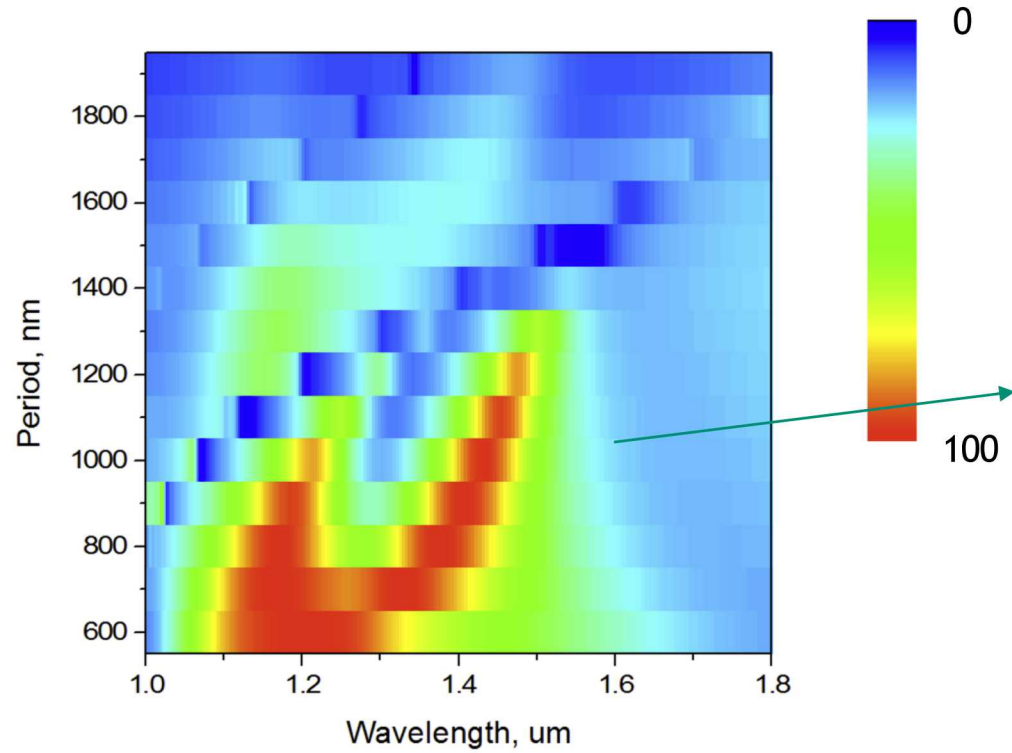
Non-zero SHG signal for  
(111) Lattice plane under normal  
incidence

$$P_x(2w) = 2\varepsilon_0 d_{eff} \left(-\frac{1}{\sqrt{6}}\right) E_x(w)^2 + \frac{1}{\sqrt{6}} E_y(w)^2 - \frac{1}{\sqrt{3}} E_x(w) E_z(w)$$

$$P_y(2w) = 2\varepsilon_0 d_{eff} \left(-\frac{2}{\sqrt{3}}\right) E_y(w) E_z(w) - \frac{1}{\sqrt{6}} E_x(w) E_z(w)$$

$$P_z(2w) = 2\varepsilon_0 d_{eff} \left(-\frac{1}{2\sqrt{3}}\right) E_x(w)^2 - \frac{1}{2\sqrt{3}} E_y(w)^2 - \frac{1}{1\sqrt{3}} E_z^2$$

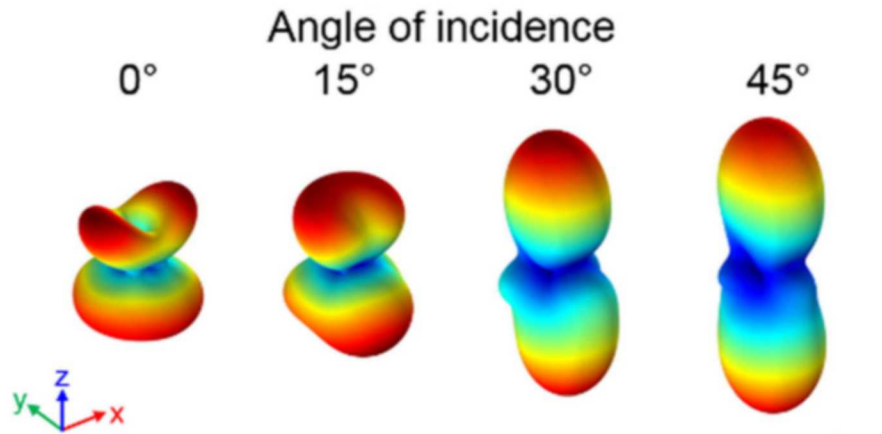
# Reflectance spectrum



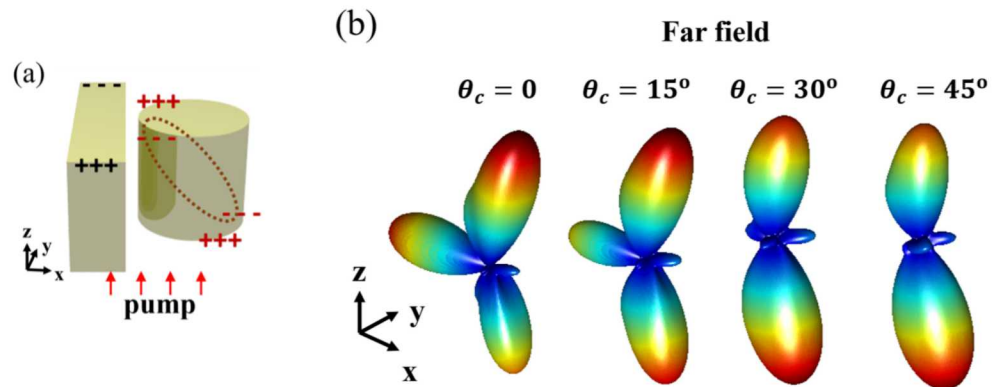
# Tailoring of SHG in normal direction



## Use of non-normal incidence

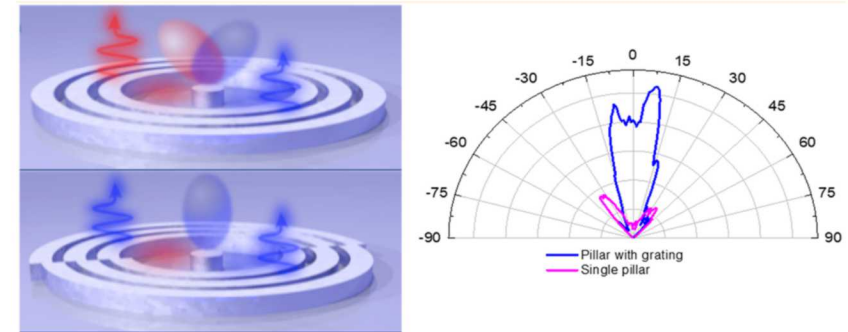


Carletti, L., *Nanotechnology*, 28(11), 114005, **2017**

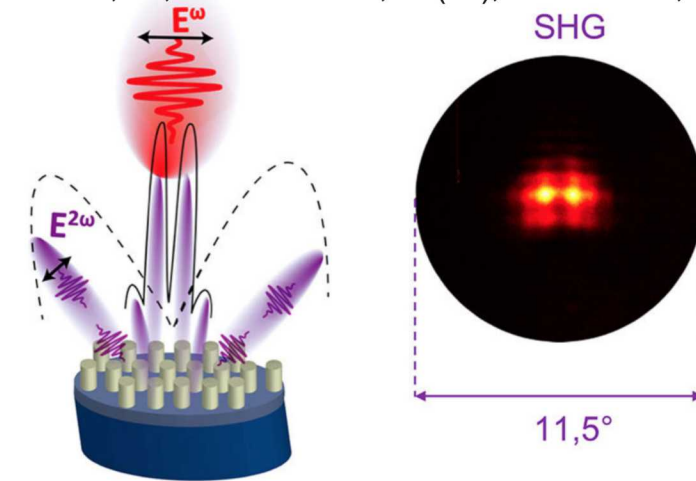


Xu, L., Rahmani, In *Photonics* (Vol. 5, No. 3, p. 29). Multidisciplinary Digital Publishing Institute, **2018**

## Use of additional gratings



Ghirardini, L., *Nano letters*, 18(11), 6750-6755, **2018**

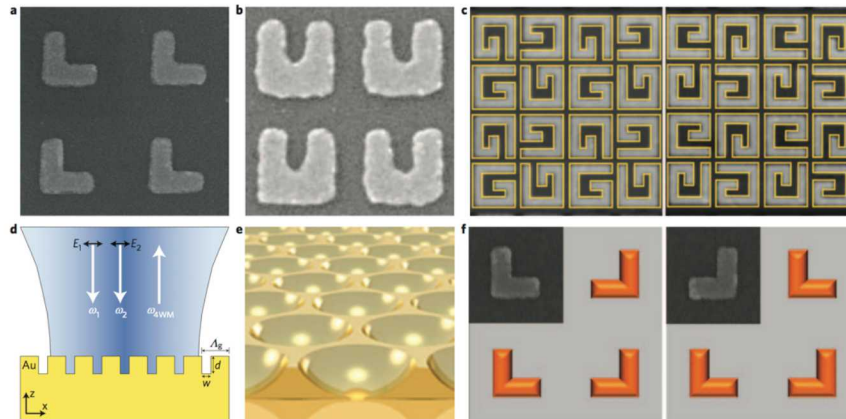


Marino, G., *ACS Photonics*, Articles ASAP **2019**

# Nonlinear optical frequency mixing in nanostructures

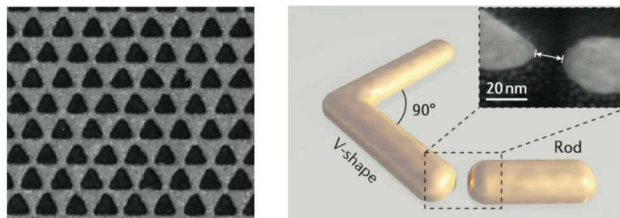
Engineered structures that have specific optical properties on demand by choosing materials, shapes and dimensions of the meta-atoms

- **Resonant enhancement of EM field**
- **Relaxed phase matching conditions**

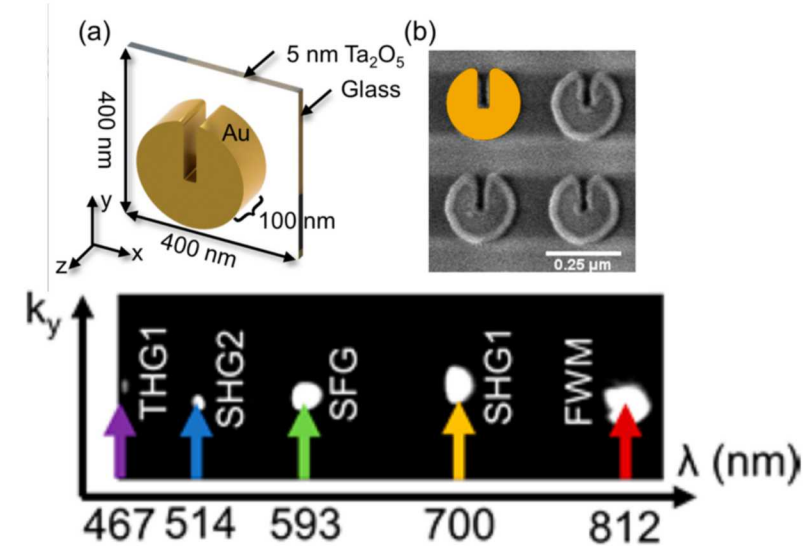


Kauranen, M., and Zayats, A. V. (2012) "Nonlinear plasmonics" *Nature Photonics*, 6(11), 737.

a Metasurfaces for SHG



Li, G., Zhang, S. and Zentgraf, T., "Nonlinear photonic metasurfaces" *Nature Reviews Materials*, (2017), 2(5), p.17010



Sartorello, et al. *ACS Photonics* 3.8 (2016): 1517-1522.

- Ohmic losses
- Plasmonic structure: small modal volume (surface nonlinearities)

**SHG efficiency  $\sim 5 \times 10^{-10} \text{ W/W}^2$**