

# New Directions in Causality and Causal Modeling

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*PRESENTED BY*

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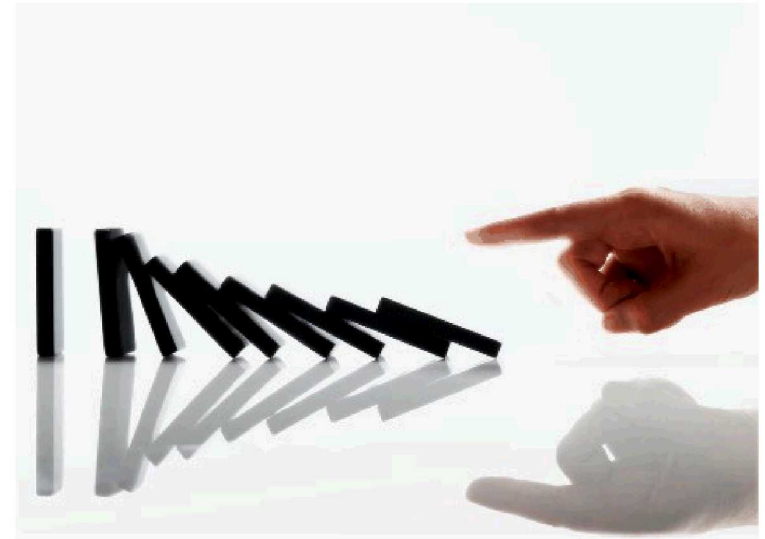


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The world is causal

Understanding causality can improve our ability to:

- Explain the world
- Predict
- Influence



Dangers of untested causal assumptions

- Superstition and the illusion of controllability

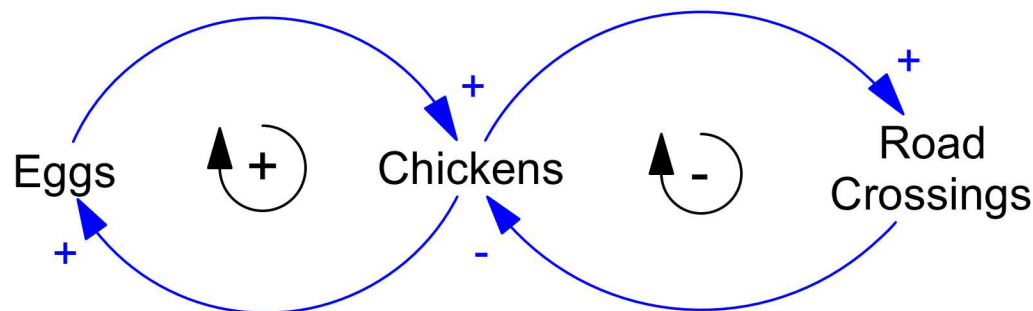


## Theory-based modeling already incorporates causality

- But are the assumptions correct?

## “Recent” academic interest in causality

- Symbolic and logical language to study causality
- Interest in incorporating into AI
  - Pearl: “strong AI” will necessitate causal understanding
  - Judea Pearl: One of the well-known causality researchers/writers, 2011 winner of ACM Turing award
  - “Strong AI”: Hypothesis that machines could act intelligently by actually thinking (as opposed to simulated thinking)
    - Artificial Intelligence, A Modern Approach. 2nd Edition. Russell & Norvig, 2003. page 947ff





What does causality mean for System Dynamics modelers?

- Assumptions, conceptual models
- Concepts of causality are different!

Why does it matter what else is going on in causality and causal modeling?

- Put system dynamics in context
- Improve/combine methods
- New opportunities

## A few intuitive definitions (from Wikipedia)

**Causality:** How one process or state (the *cause*) relates to another (the *effect*), where the first is partly responsible for the second, and the second is partly dependent on the first

- Examples:

- If it rains, then the ground gets wet.
- If you study, then you will get a better grade on the test



**Counterfactual:** A conditional containing an if-clause which is contrary to fact

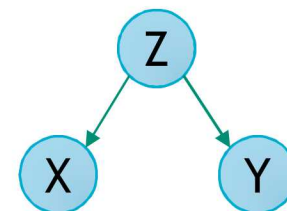
- Examples:

- If it had rained yesterday, then the party would have been cancelled.
- If you had not taken a wrong turn, then you would have gotten there on time.

**Confounder:** A variable that influences both the dependent variable and independent variable causing a spurious association (correlation, not causation).

- Examples:

- Weather affects murder rates and ice cream sales
- Economic development affects piracy and climate change



### 1. Felix Wang:

- How can causality enable transportability and inference between application areas?

### 2. Lauren Hund:

- How can causal modeling make sense of imperfect data?

### 3. Ryan Dellana:

- How can machine learning best incorporate causality?

Help you understand what's going on in causality research to:

**Put system dynamics in context**

**Improve/combine methods**

**New opportunities**



# Inference Using Causal Models



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Felix Wang



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Causal models can be thought of as an “inference engine” taking inputs

- *Causal assumptions* and a structural model to encode these assumptions
- *Queries* about variables of interest and their relationships
- *Data* from observations (seeing) and interventions (doing)

... and producing outputs

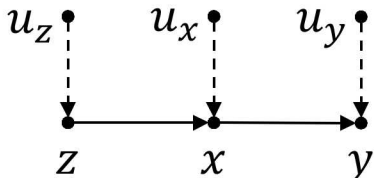
- *Logical implications* of our assumptions
- *Statistical implications* of our assumptions
- *Claims* about the answers to our queries

Some examples of causal queries

- Was it move/action X that led to winning/losing the game?
- Will a proposed policy on X have the intended results Y?
- How will the release of product X impact the sales of product Y?
- Does the evidence prove, beyond a shadow of a doubt, the crime Y was committed by X...  
Or was it an accident that would have happened anyway, because of Z?

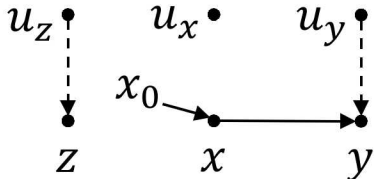
## Structural Equations Models (SEMs)

- Variables of interest and their background factors
- Probability distributions over the background factors
- Functions that map from variables (and background factors) to variables
- Visually represented as a Directed Acyclic Graph (DAG)

$$\begin{aligned}
 & z \leftarrow f_Z(u_Z) \\
 M: & \quad x \leftarrow f_X(z, u_X) \\
 & \quad y \leftarrow f_Y(x, u_Y)
 \end{aligned}$$


Changes to the model can be reflected as changes in the graph

- Operations (e.g. interventions  $do(x)$ ) add/remove edges

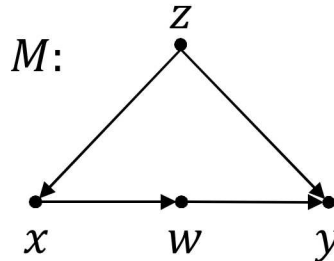
$$\begin{aligned}
 & z \leftarrow f_Z(u_Z) \\
 M_x: & \quad x \leftarrow x_0 \\
 & \quad y \leftarrow f_Y(x, u_Y)
 \end{aligned}$$


$$P_M(y|do(x)) = P_{M_x}(y)$$

Many tools available for working with causal models

- D-separation, belief propagation, adjustment criteria and formulae, etc.
- Graphical representation supplements the discovery of solutions

Variables:  $x$  = smoking,  
 $w$  = tar,  $y$  = cancer,  
 $z$  = genes (unobserved)

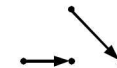


$$\begin{aligned}
 z &\leftarrow f_Z(u_Z) \\
 x &\leftarrow f_X(z, u_X) \\
 w &\leftarrow f_W(x, u_W) \\
 y &\leftarrow f_Y(w, z, u_Y)
 \end{aligned}$$

Query:  $P(y|do(x))$

$$\begin{aligned}
 &= \Sigma_w P(y|do(x), w) P(w|do(x)) \\
 &= \Sigma_w P(y|do(x), do(w)) P(w|do(x)) \\
 &= \Sigma_w P(y|do(x), do(w)) P(w|x) \\
 &= \Sigma_w P(y|do(w)) P(w|x) \\
 &= \Sigma_{x'} \Sigma_w P(y|do(w), x') P(x'|do(w)) P(w|x) \\
 &= \Sigma_{x'} \Sigma_w P(y|w, x') P(x'|do(w)) P(w|x) \\
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 \end{aligned}$$

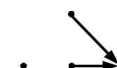
Probability Axioms



Observation to Intervention



Intervention to Observation



Delete Intervention

Probability Axioms



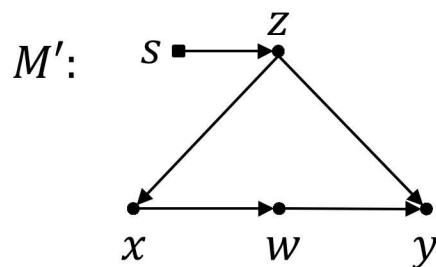
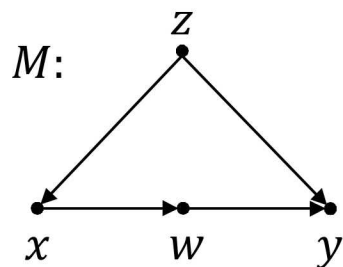
Intervention to Observation



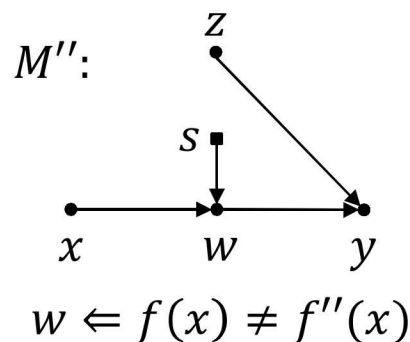
Delete Intervention

Selection diagrams identify where two domains of interest may differ

- E.g.: distribution of background factors, mapping functions, causal structure
- Represented graphically through selection variables (adding an edge  $s_i \rightarrow v_i$ )



$$P(z) \neq P'(z)$$



$$w \Leftarrow f(x) \neq f''(x)$$

Example: Given studies in  $M', M''$  how effective will marketing be in population  $M$ ?

- Variables:  $x$  = advertisements,  $y$  = purchase,  $z$  = age,  $w$  = click-through rate
- Study in  $M'$  differs from target population in age
- Study in  $M''$  was done as a randomized trial, and on a platform with high click-through rates

## Transportability of Causal Models

Transportability allows us to make inferences between domains of interest

- Determine if generalizations are valid or invalid
- “License assumptions” about the transfer of causal relationships
- Different assumptions will yield different routes for transporting information
- Synthesize observational and interventional information from multiple domains

Some more examples highlighting transportability

- How do I navigate/find where I need to go when traveling in a new city?
- Why don't my physics simulations  $N$  match the new experimental measurements  $M$ ?
- Should I have expected them to match in the first place?
- It's difficult to measure  $Y$  because of cost, what can I use as a proxy?
- Will a government program  $X$  in country  $N$  be effective if applied to country  $M$ ?
- What experiments should be conducted to fill in the gaps of understanding?

## Dealing with data in a smarter way for machine learning

- How the data gets generated is important
- Model-based ML produces specific solutions to specific problems
- Combining human expertise in generating assumptions with ML methods for data analysis

## Leveraging causal structure in AI agents

- Transfer learning during domain shift
- Sample efficiency and learning from counterfactuals
- Giving AI “free will”

- Pearl, Judea and Bareinboim, Elias. “External Validity: From Do-Calculus to Transportability Across Populations” *Statistical Science*, 2014, Vol. 20. No. 4, 579-595
- Pearl, Judea. *Causality: Models, Reasoning, and Inference*, 2nd ed. Cambridge Univ. Press, 2009
- Pearl, Judea and Mackenzie, Dana. *The Book of Why: The New Science of Cause and Effect*, Basic Books, New York, 2018





# Using causal models to analyze imperfect data



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Lauren Hund



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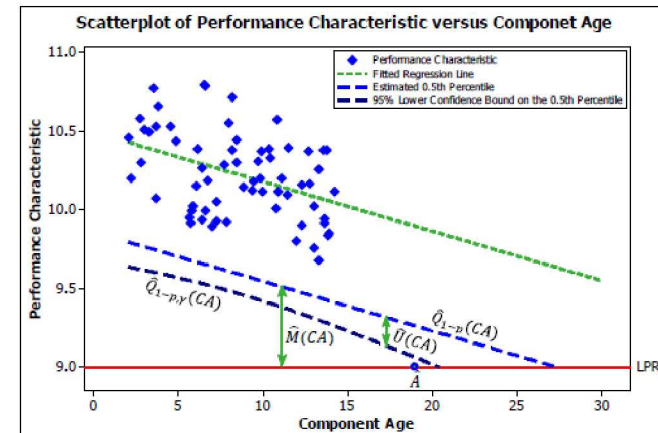
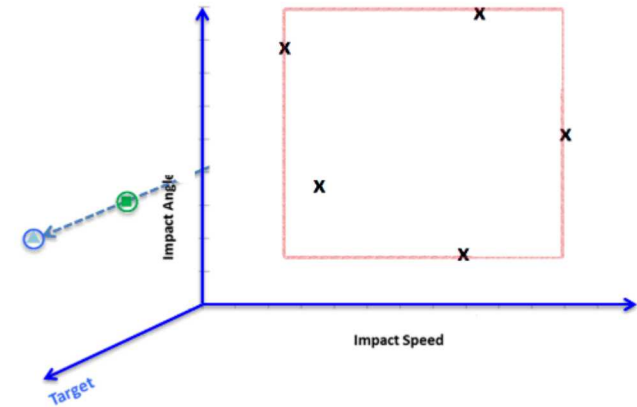


## Sandia problems commonly concern “extrapolative prediction.”

- Generating a predictive distribution for an unobserved outcome – prediction of a counterfactual.

### Some examples:

- Nuclear weapons are the ultimate counterfactual predictions - without full-system tests, we certify weapons.
- Weapon components: How will a component perform across a variety of conditions (temperature, environments, age?)
- Computer models: Run model and predict to setting without data (counterfactual).





**Causality gives a language to talk about credibility of a prediction given less-than-ideal data.**

- Much of causal inference is simply ensuring that your data analysis methods accurately reflect the “**data generating mechanism**,” i.e. how your data were generated.
- Under what set of assumptions is my counterfactual prediction valid?

**Structural causal modeling is one language of causality.**

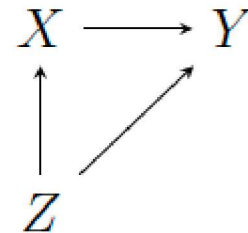
## Steps for causal analysis:

1. Define a causal query.
  - Often a function of a counterfactual.
2. Determine how the collected data relates to the true underlying structural causal model.
  - Make a DAG!
3. Check if sufficient data to estimate query.
4. Estimate the query from the data.

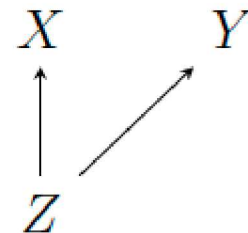
Step 1: Causal query

$$P(Y = do(X = x))$$

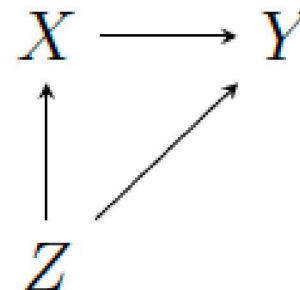
Step2: DAG



Step 3: Check criteria



In practice, we want to move from *qualitative* DAG model to *quantitative* statistical model in order to estimate a causal query.



**Adjustment formula:**

$$P(Y = do(X = x)) = \sum_z P(Y|X = x, Z = z)P(Z = z)$$

Unobserved counterfactual

Observed in data

Stratifying on  $Z$ , we can estimate the counterfactual of interest from the data.

- Other formulations of the adjustment formula exist, e.g. for selection variables and for the front-door criterion.



**Causal inference is all about models and assumptions.**

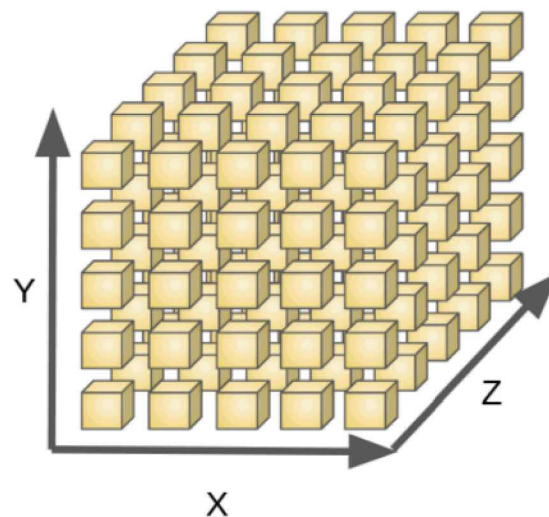
- What assumptions are you willing to make?
- Do you have enough data to fit a “good” statistical model under those assumptions?

**Fundamental assumptions of causality:** Given a random sample from a population:

- ***Exchangeability***: no unmeasured confounding
  - Measure enough variables?
- ***Positivity***: enough data to estimate  $P(Y|X = x, Z = z)$ .
  - Have enough data?
- ***Consistency***: no multiple versions of treatment
  - Treatment can be hypothetically manipulated in a consistent manner
  - Example: drug; counterexample: BMI.



**Curse of dimensionality** – use statistical models to approximate distribution of  $Y|X,Z$ .  
“Art” of statistical modeling.



Picture taken from: <https://medium.freecodecamp.org/the-curse-of-dimensionality-how-we-can-save-big-data-from-itself-d9fa0f872335>

**There is an implicit fourth assumption needed for causal estimation: correct model specification.**

- Causal methods are often ‘model-agnostic’: how you model is separate from how you calculate causal estimands given the model.
- The ‘modeling’ stage is where good statistical and ML models come into play.

“Use of technical causal language, a good use, in our estimation, must be recognized as simply a shorthand for better versus worse analyses, as judged by the author, and not a metaphysical statement about causation per se...”

Lipton and Odegaard (2005)

# Generative Models in Machine Learning



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## Definition of “Generative Model”

As a probabilistic expression

$X$  = State variable

$Y$  = Observable variable

Discriminative model:

$$P(X | Y)$$

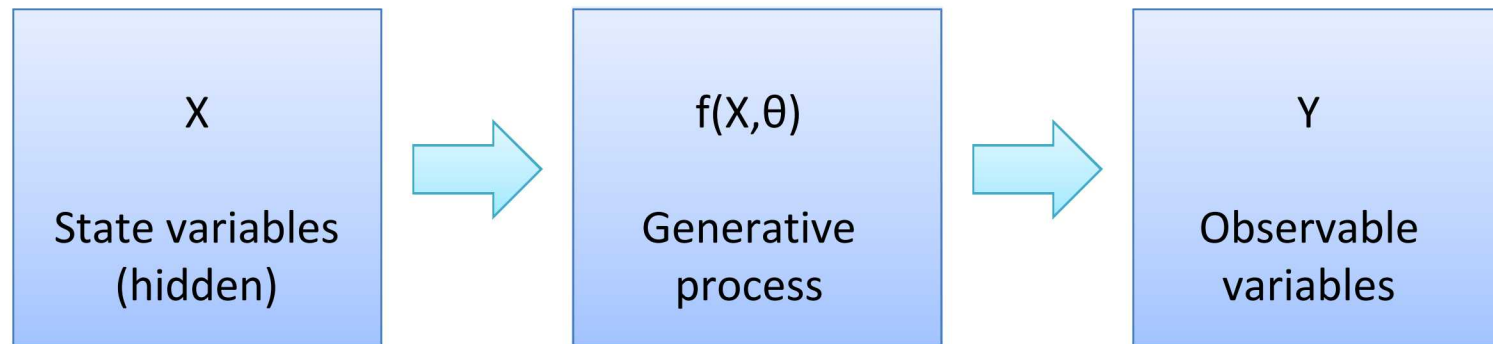
Generative model:

$$P(X, Y)$$

or  $P(Y | X)$ , where  $P(X)$  is known or estimated

## Definition of “Generative Model”

As a procedure

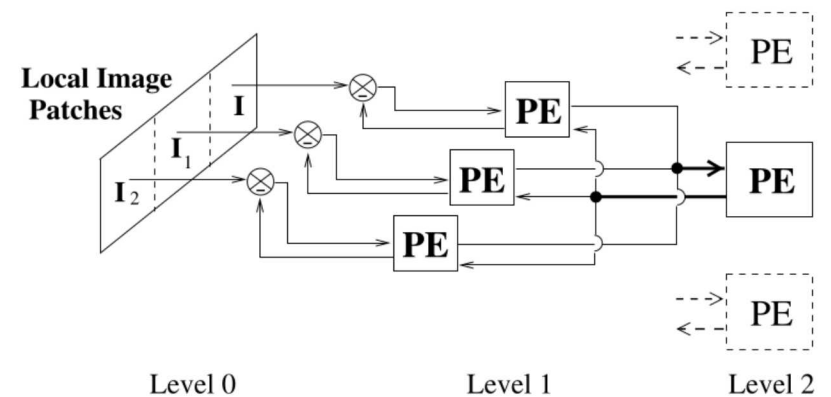
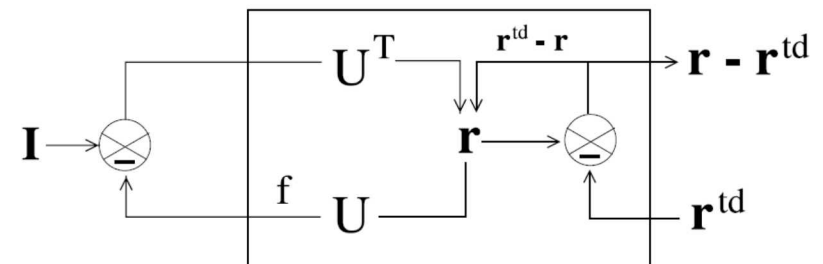
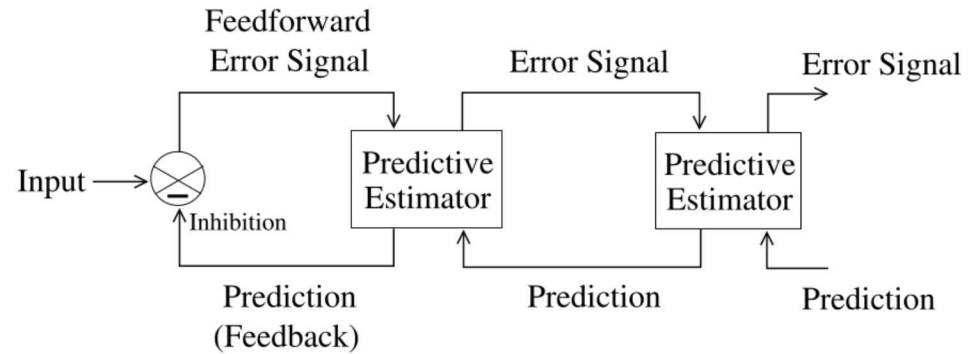
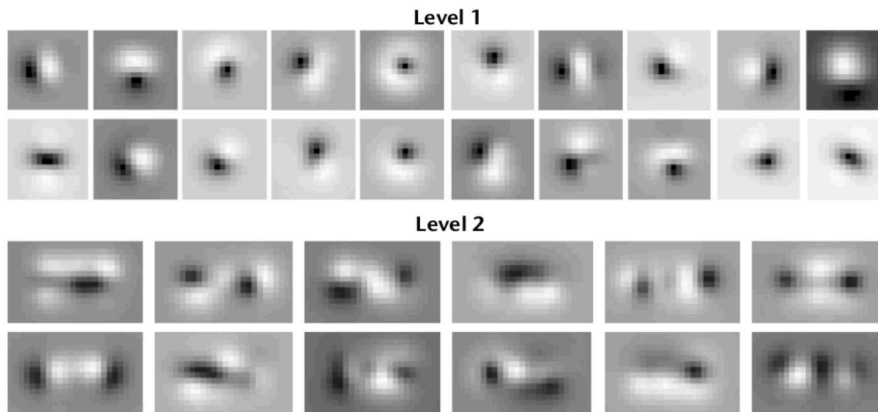


Assumes a chain of causality from X, through mechanisms  $f(\theta)$ , to Y.

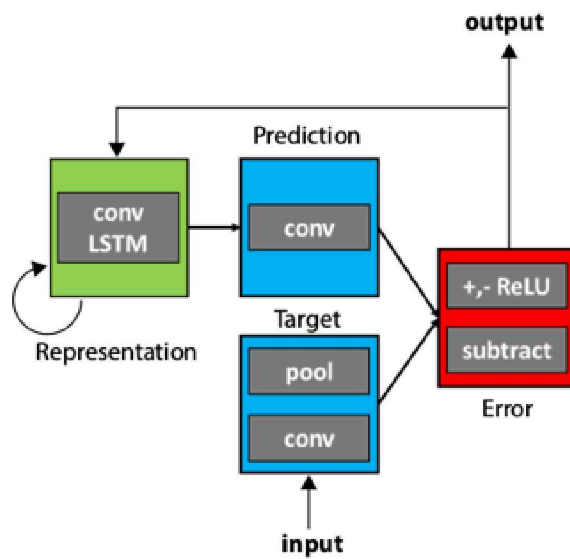
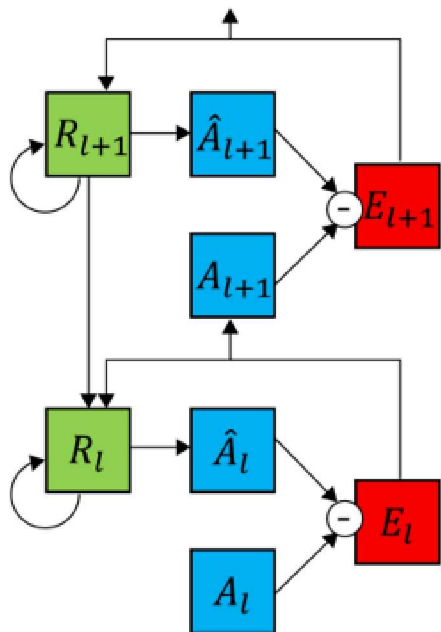
Example: 3D graphics (such as video games or special effects in movies)

- X = Position/orientation of various objects in scene
- $\theta$  = Shape/surface material of objects
- f = Projection process. In the real world, it is reflected light reaching your eye.
- Ray-tracing and other 3D rendering methods simulate this.
- Y = Resulting pixels on the movie screen.

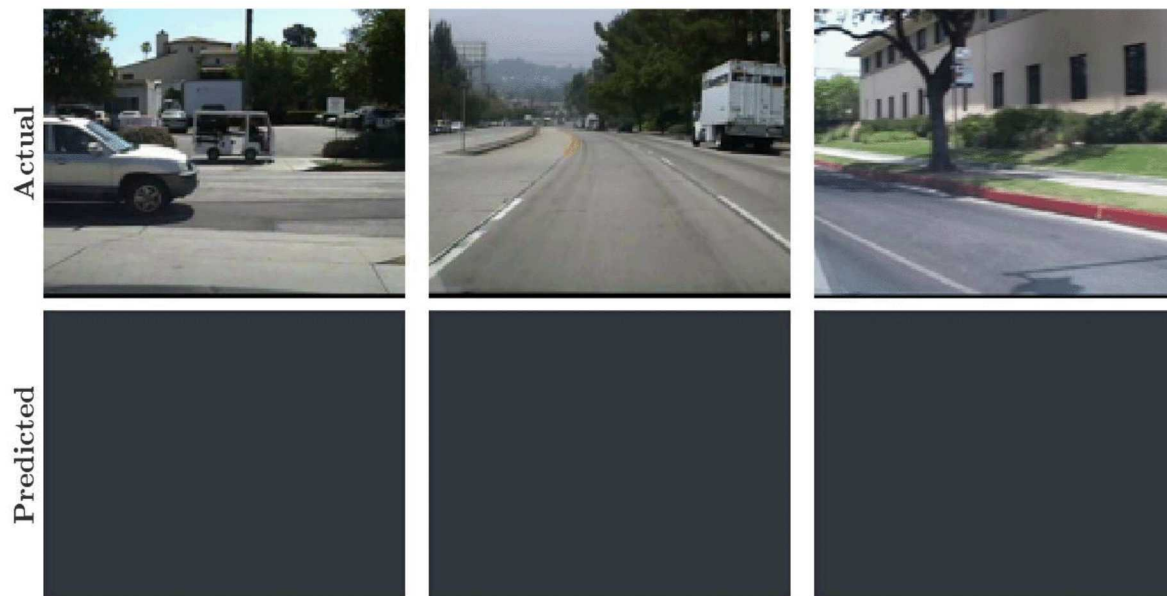
# Example: Rao & Ballard



## Example: PredNet



[<https://coxlabs.github.io/prednet>]

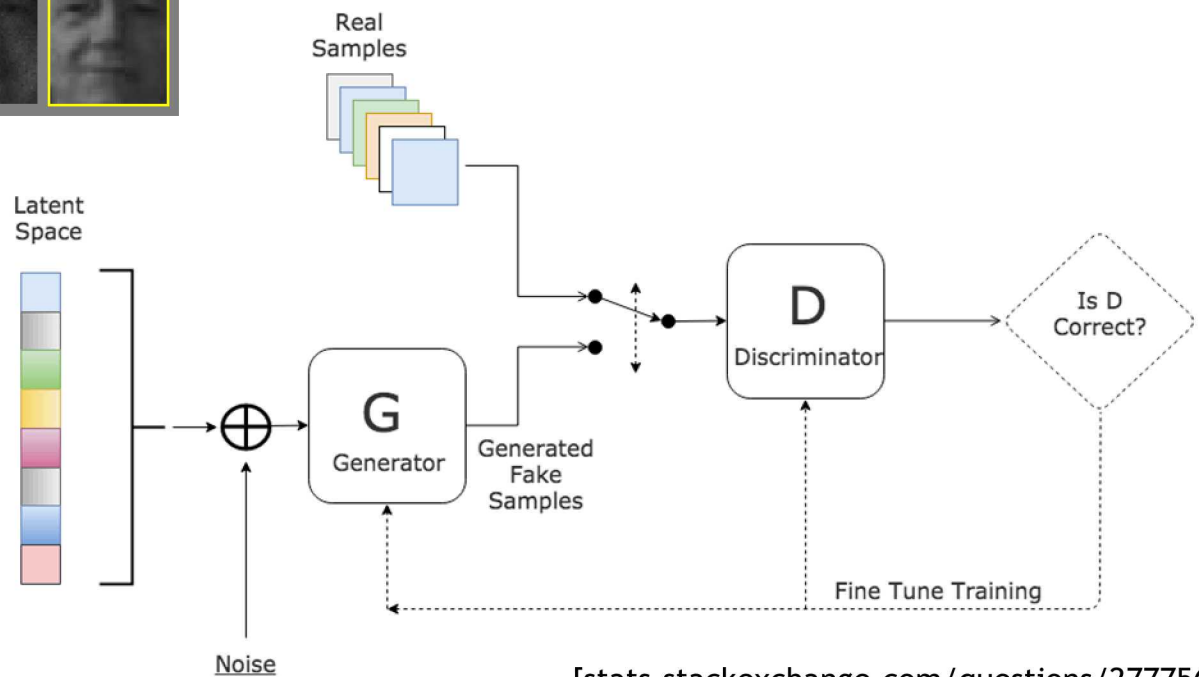




# Example: Generative Adversarial Network (GAN)



[Goodfellow 2014]



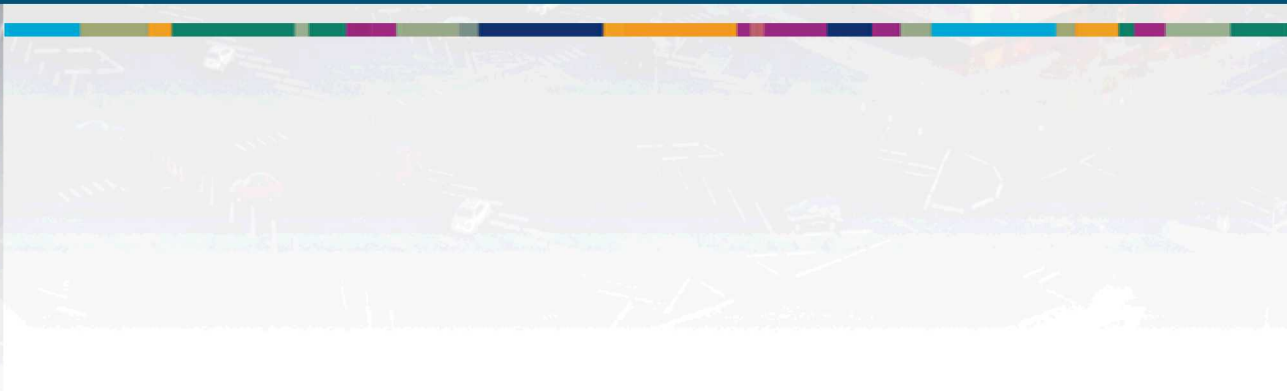
[stats.stackexchange.com/questions/277756]

## How to learn model structure

- The previous examples use neural networks and associated learning methods. Despite the generality, these have an implicit, hand-crafted structure.
- An alternative is to represent the generative process in a language suitable for genetic algorithm (GA) style random search.



Thank You!



Help you understand what's going on in causality research to:

**Put system dynamics in context**

**Improve/combine methods**

**New opportunities**