

# Insights into spin-orbit coupling at the Si/SiO<sub>2</sub> interface using an inter-valley hot spot singlet/triplet qubit

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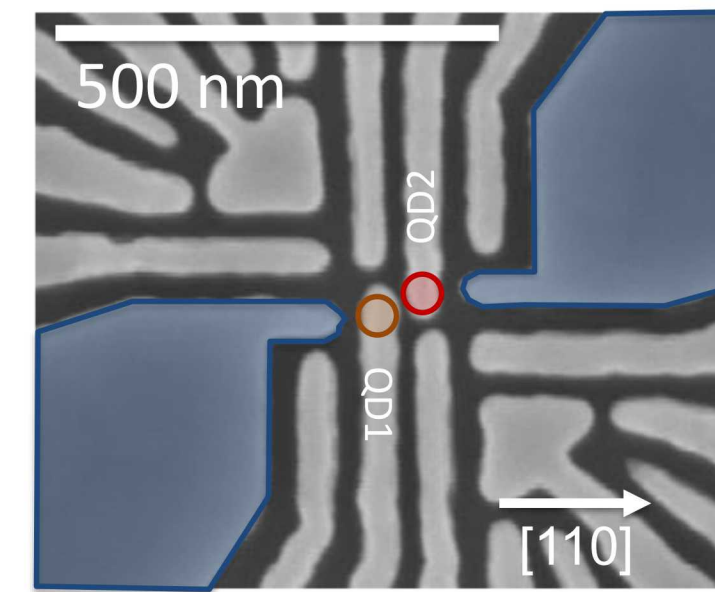
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## Introduction

- When valley splitting and Zeeman splitting are in resonance, the well-known spin-valley “hot spot” results in an enhanced spin relaxation rate [1-4] for electrons confined to silicon quantum dots (QDs). While this spin-valley mechanism drives decoherence, it can also drive qubit rotations [5-8].
- Here, we demonstrate a S/T<sub>0</sub> qubit driven by intra- and inter-valley SOC. We have measured the frequency dependence of S/T<sub>0</sub> rotations near the hot spot for a thorough range of B-field orientations.
- We have extended a comprehensive intra-/inter-valley theory that captures the observed B-field dependence, in good agreement with the experiment.
- This technique allows for very precise measurement of valley splitting in this system, and may provide further insights into the nature of SOC at the Si/SiO<sub>2</sub> interface.

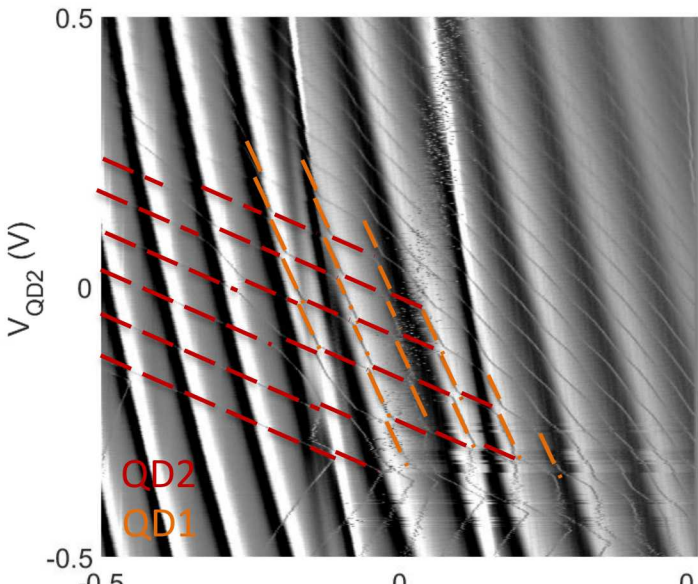
## MOS DQD SO Driven S-T Qubits

Device Layout

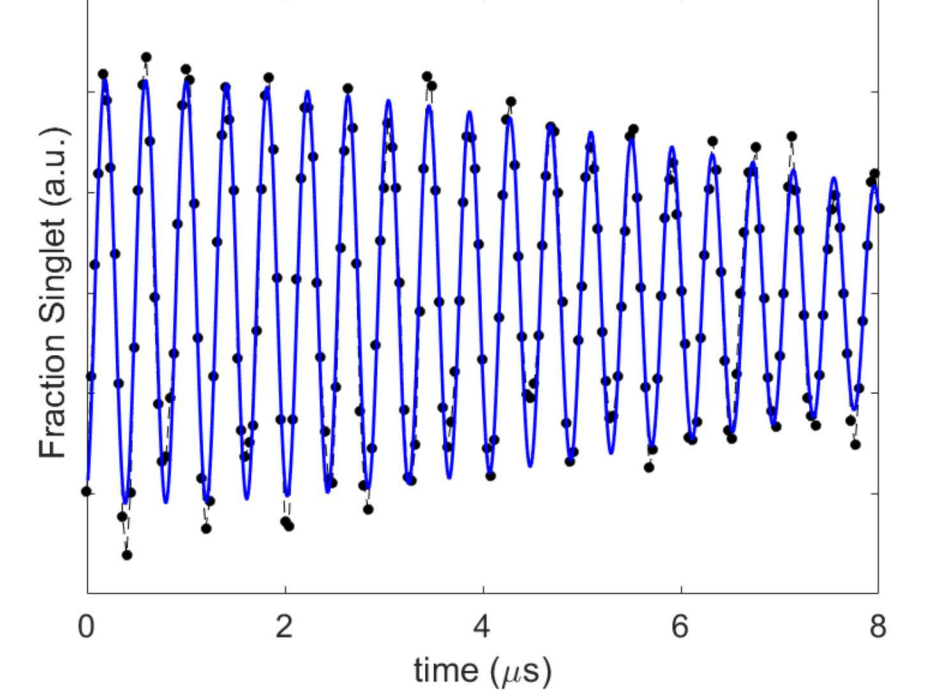


Charge Stability

Diagram



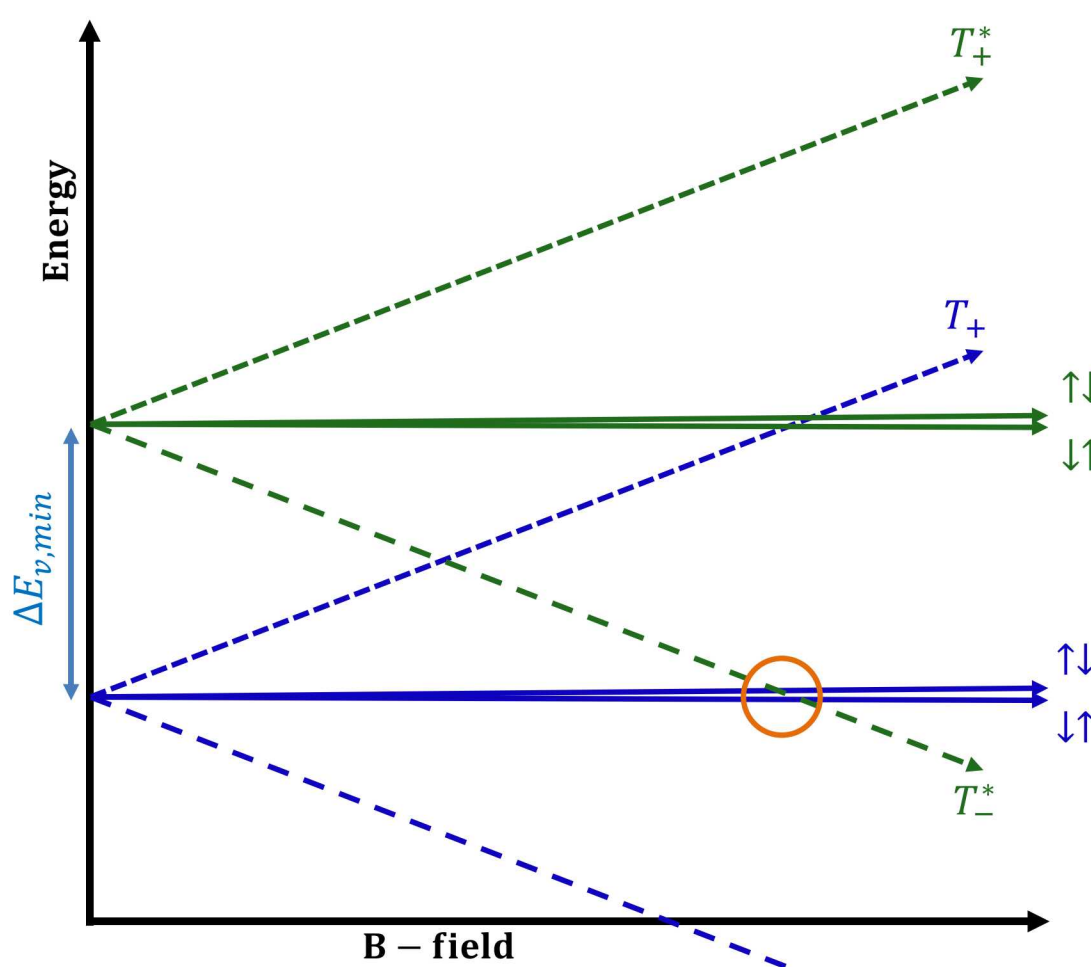
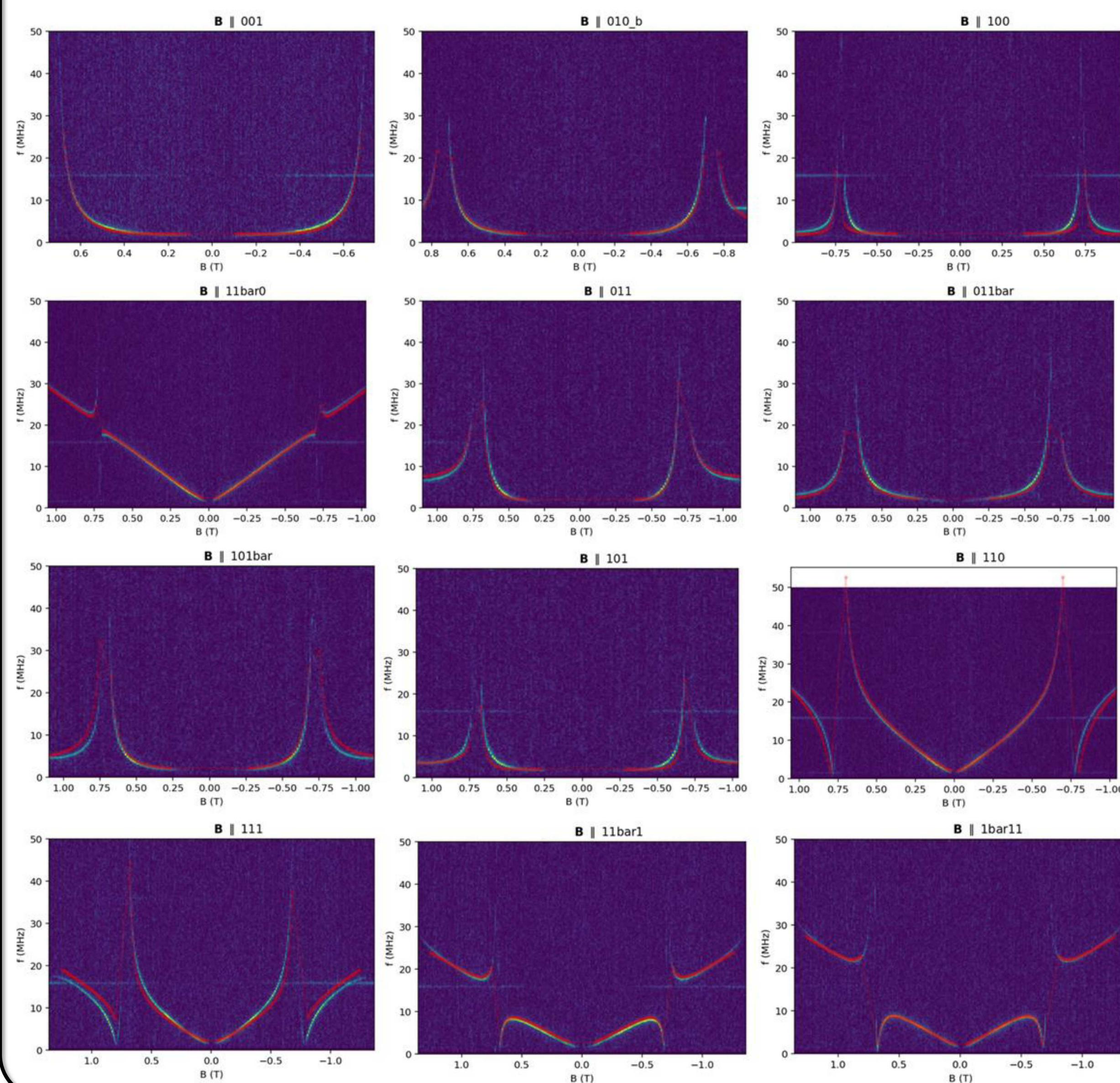
Singlet-Triplet FID



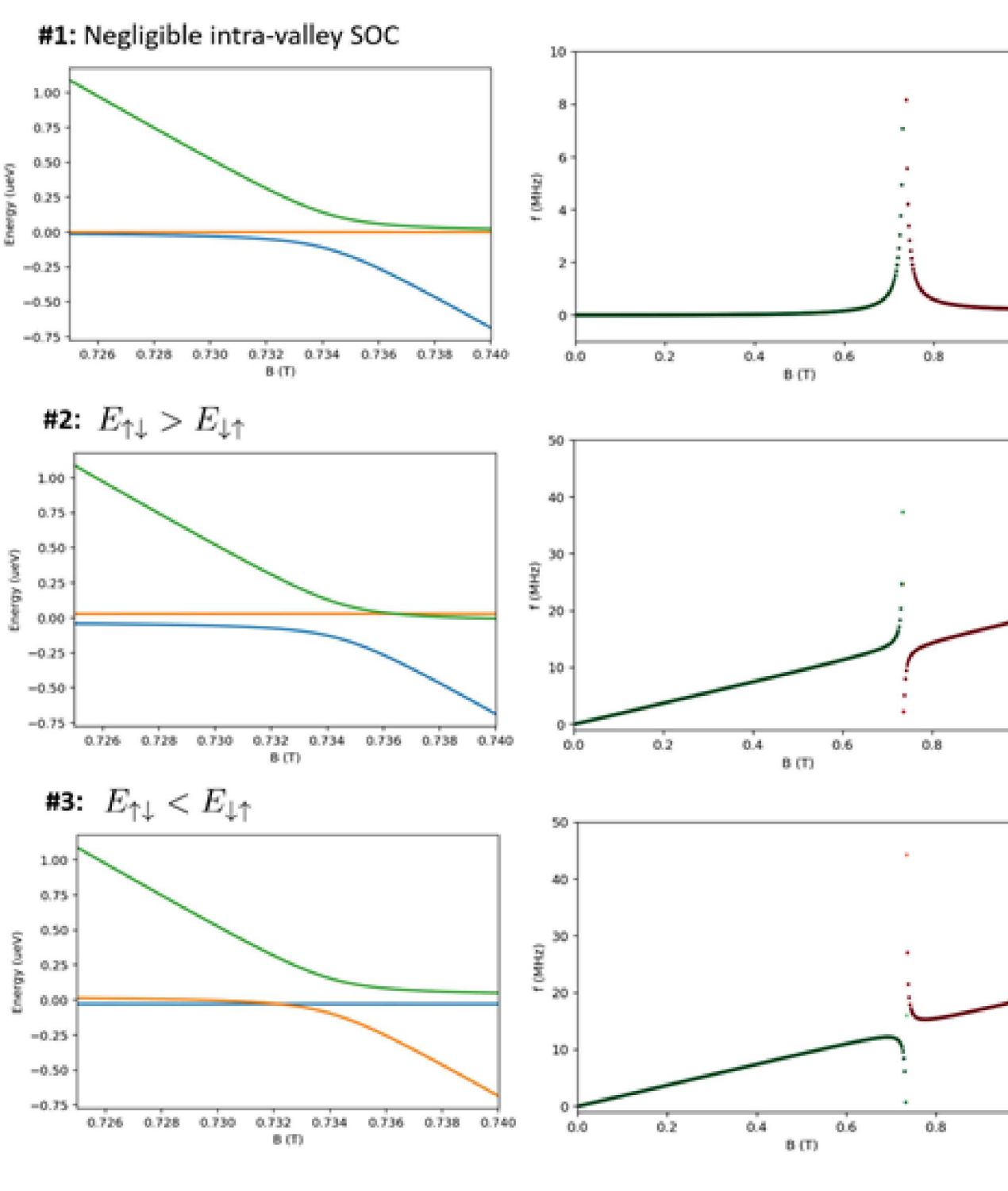
- Single poly-silicon gate layout
- 50nm gate oxide
- Isotopically enriched epi-layer with 500ppm residual <sup>29</sup>Si.
- Qubit Pair: (0,4) — (1,3) charge occupations on QD1 and QD2

## Valley Hot-Spot Interaction

Model fits (red) superimposed on FFT of measured qubit rotation frequency as a function of B-field magnitude for 12 distinct B-field orientations. The full angular dependence is captured by the model



### Hot spot Taxonomy



Effective Hamiltonian near the hot spot (for fixed B-field orientation)

$$H_{3 \times 3} = \begin{pmatrix} |S\rangle & |T_0\rangle & |T_-^*\rangle \\ 0 & B\delta & B\gamma e^{i\phi} \\ B\delta & 0 & -B\gamma e^{i\phi} \\ \gamma B e^{-i\phi} & -B\gamma e^{-i\phi} & \Delta_{vs} - g\mu_B B \end{pmatrix}$$

Depend strongly on orientation of **B**  $\begin{cases} \delta = \text{intra-valley SOC strength} \\ \gamma = \text{inter-valley SOC strength} \\ \Delta_{vs} = \text{valley splitting} \end{cases}$

Eigenenergy	Eigenstate
$\delta B$	$\frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}$
$\frac{1}{2}(\Delta_{vs} - (\delta + g\mu_B B) + \frac{1}{2}\sqrt{(\Delta_{vs} + (\delta - g\mu_B B))^2 + 8\gamma^2 B^2})$	$\frac{1}{\sqrt{2}} \begin{pmatrix} \frac{1}{2}e^{i\phi/2}w_- \\ -\frac{1}{2}e^{i\phi/2}w_- \\ -\frac{1}{2}e^{-i\phi/2}w_+ \end{pmatrix}$
$\frac{1}{2}(\Delta_{vs} - (\delta + g\mu_B B) - \frac{1}{2}\sqrt{(\Delta_{vs} + (\delta - g\mu_B B))^2 + 8\gamma^2 B^2})$	$\frac{1}{\sqrt{2}} \begin{pmatrix} -\frac{1}{2}e^{i\phi/2}w_+ \\ \frac{1}{2}e^{i\phi/2}w_+ \\ -\frac{1}{2}e^{-i\phi/2}w_- \end{pmatrix}$

$$\langle \tilde{S} | H | \tilde{T}_0 \rangle = \frac{1}{\sqrt{2}} \sin(\theta) (e^{i\phi} \langle S | H | T_- \rangle - e^{-i\phi} \langle S | H | T_+ \rangle)$$

$$\text{Intra-valley} = \frac{1}{2} \sin(\theta) [e^{i\phi} (h_{\uparrow\downarrow}^{LL} - h_{\uparrow\downarrow}^{RR}) + e^{-i\phi} (h_{\uparrow\downarrow}^{LL} - h_{\uparrow\downarrow}^{RR})]$$

$$\langle \tilde{S} | H | \tilde{T}_+^* \rangle = e^{-i\phi} \sin^2\left(\frac{\theta}{2}\right) \langle S | H | T_+^* \rangle + e^{i\phi} \cos^2\left(\frac{\theta}{2}\right) \langle S | H | T_-^* \rangle$$

$$\text{Inter-valley} = \frac{1}{\sqrt{2}} \left( \sin^2\left(\frac{\theta}{2}\right) e^{-i\phi} h_{\uparrow\downarrow}^{LR*} - \cos^2\left(\frac{\theta}{2}\right) e^{i\phi} h_{\uparrow\downarrow}^{RL*} \right)$$

$$\langle \tilde{T}_0 | H | \tilde{T}_+^* \rangle = -\langle \tilde{S} | H | \tilde{T}_+^* \rangle \quad (\text{reason for special structure of } 3 \times 3 \text{ Hamiltonian})$$

where  $h_{s_1 s_2}^{MN} \equiv \langle \phi_M s_1 | H_{SO} | \phi_N s_2 \rangle$

Interfacial SOC Hamiltonian:

$$H_{SO} = \delta(z) [f^R(x, y) (P_y \sigma_x - P_x \sigma_y) + f^D(x, y) (P_x \sigma_x - P_y \sigma_y)]$$

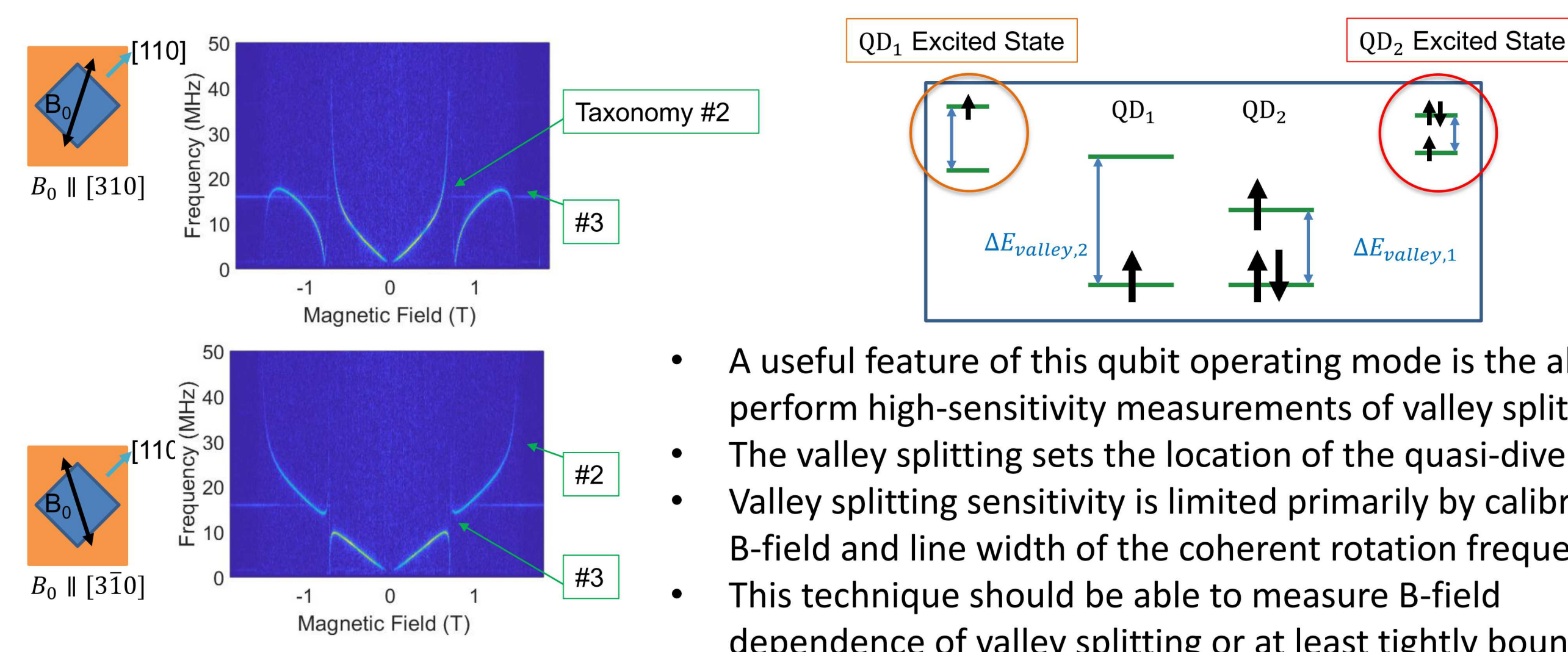
Momentum matrix elements

$$\begin{aligned} \langle L | \delta(z) f(x, y) P_x | L \rangle &= (1 - 0.24 \cos(\varphi_{v,L})) [\lambda_x^L B_x + \mu_x^L B_z] \\ \langle L | \delta(z) f(x, y) P_y | L \rangle &= -(1 - 0.24 \cos(\varphi_{v,L})) [\lambda_y^L B_x + \mu_y^L B_z] \\ \langle R | \delta(z) f(x, y) P_x | R \rangle &= (1 - 0.24 \cos(\varphi_{v,R})) [\lambda_x^R B_x + \mu_x^R B_z] \\ \langle R | \delta(z) f(x, y) P_y | R \rangle &= -(1 - 0.24 \cos(\varphi_{v,R})) [\lambda_y^R B_x + \mu_y^R B_z] \\ \langle R | \delta(z) f(x, y) P_x | R^* \rangle &= 0.24 * i \sin(\varphi_{v,R}) [\lambda_x^R B_x + \mu_x^R B_z] \\ \langle R | \delta(z) f(x, y) P_y | R^* \rangle &= -0.24 * i \sin(\varphi_{v,R}) [\lambda_y^R B_x + \mu_y^R B_z] \\ \langle R^* | \delta(z) f(x, y) P_x | R^* \rangle &= (1 + 0.24 \cos(\varphi_{v,R})) [\lambda_x^R B_x + \mu_x^R B_z] \\ \langle R^* | \delta(z) f(x, y) P_y | R^* \rangle &= -(1 + 0.24 \cos(\varphi_{v,R})) [\lambda_y^R B_x + \mu_y^R B_z] \end{aligned}$$

$\varphi_{v,L}$  = valley phase of left dot  
 $\varphi_{v,R}$  = valley phase of right dot

Factor of 0.24 comes from form factor approximation for Bloch functions

## Measurement of Valley Splitting



- A useful feature of this qubit operating mode is the ability to perform high-sensitivity measurements of valley splitting.
- The valley splitting sets the location of the quasi-divergence
- Valley splitting sensitivity is limited primarily by calibration of B-field and line width of the coherent rotation frequency
- This technique should be able to measure B-field dependence of valley splitting or at least tightly bound it

## Summary

- Our MOS DQD singlet-triplet qubit exhibits a complex angular dependence as a function of B-field orientation
- Our model for intra- and inter-valley SOC captures all features of a complete angular dependence and points towards further insights into the nature of SOC at the Si/SiO<sub>2</sub> interface
- This approach also provides a means of measuring valley splitting with high precision

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