



*Energy and Transport Sciences Laboratory*



# Microstructural Variability in Graphite Electrodes

Chance Norris<sup>1</sup>, Aashutosh Mistry<sup>1</sup>, Scott Roberts<sup>2</sup> and Partha P. Mukherjee<sup>1</sup>

<sup>1</sup> School of Mechanical Engineering, Purdue University, West Lafayette, Indiana 47907, USA

<sup>2</sup> Engineering Sciences Center, Sandia National Laboratories, Albuquerque, New Mexico 87185, USA

# Motivation

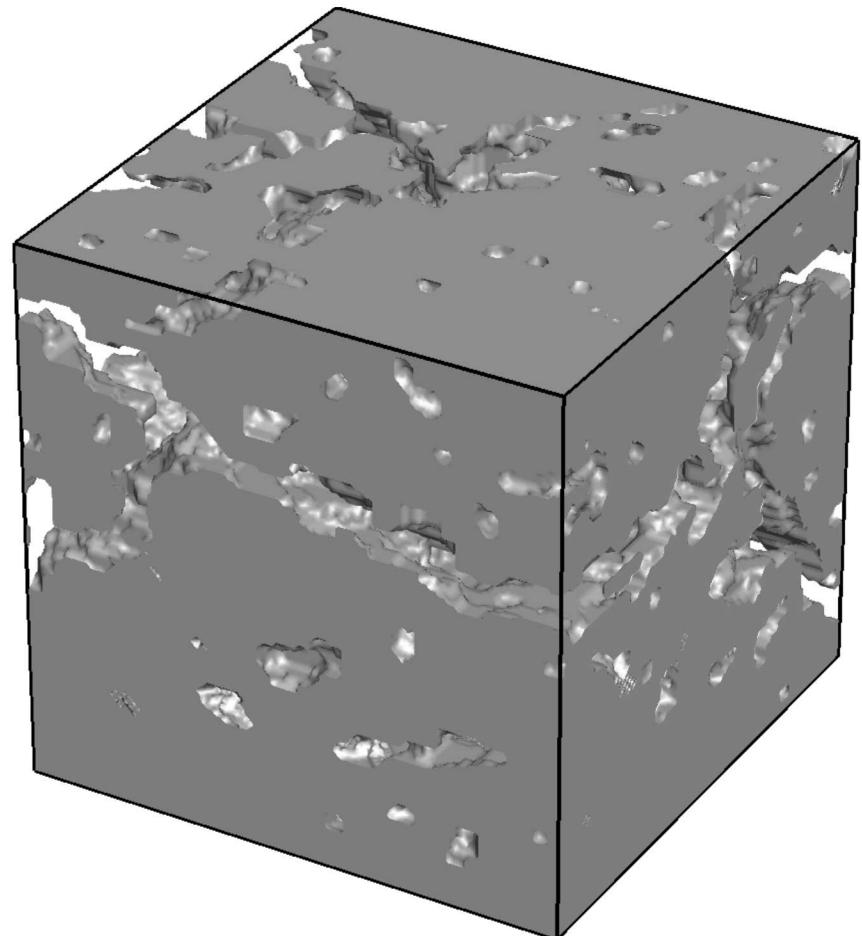
---

Q. Why are we interested in microstructural variations in graphite electrodes?

Fast charging or long-term cycling is negative electrode limited.

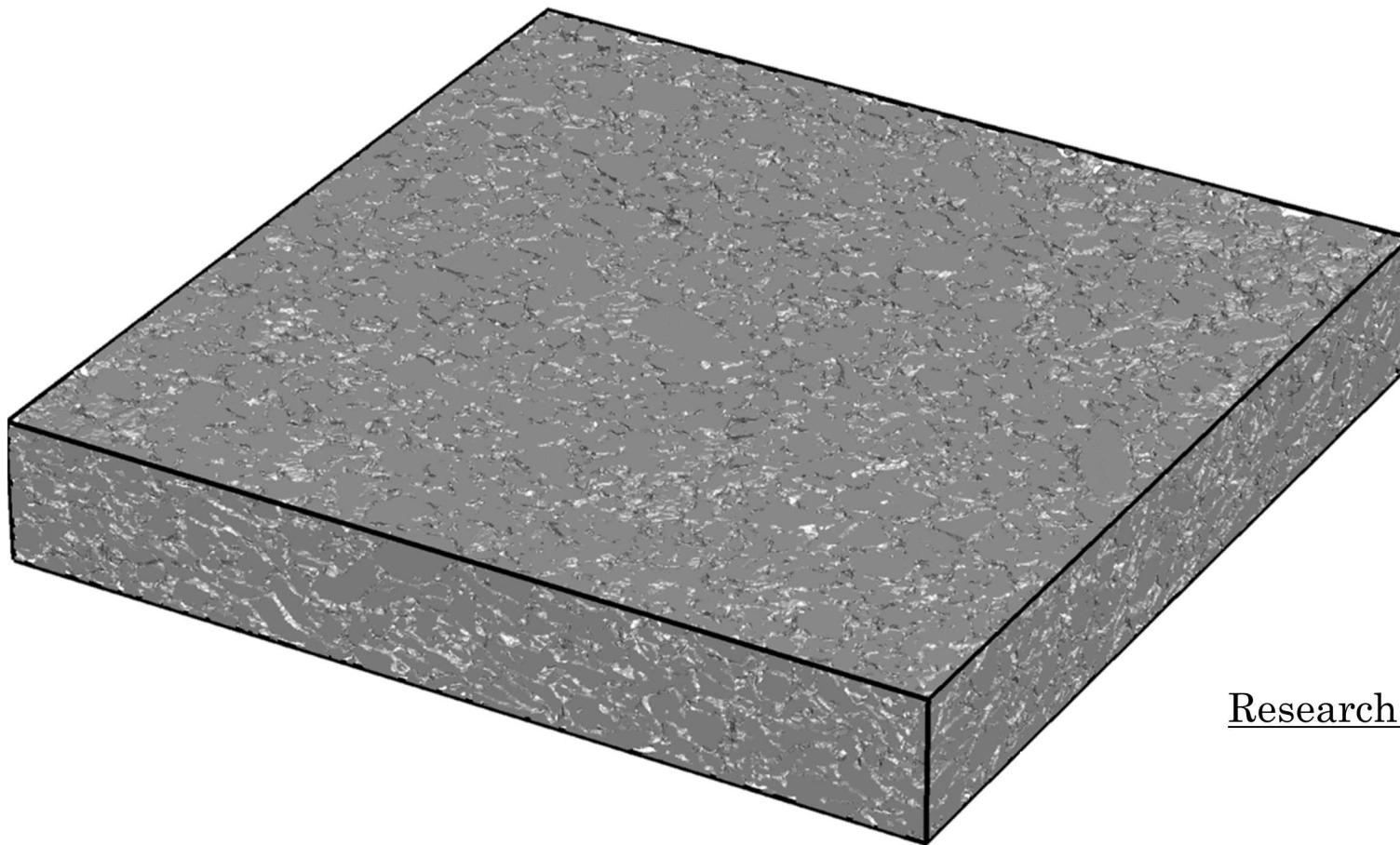
Graphite is one of the most used anodes in Li-ion batteries to date.

Many varying particle morphologies in graphite.



# Objective

---



Research Questions

# Graphite Anodes

---

## Numbered Electrodes

Ia	IIa	IIIa	IVa
Ib	IIb	IIIb	IVb
Ic	IIc	IIIc	IVc

Where a, b and c denotes three samples taken from one commercial sheet

## Named Electrodes

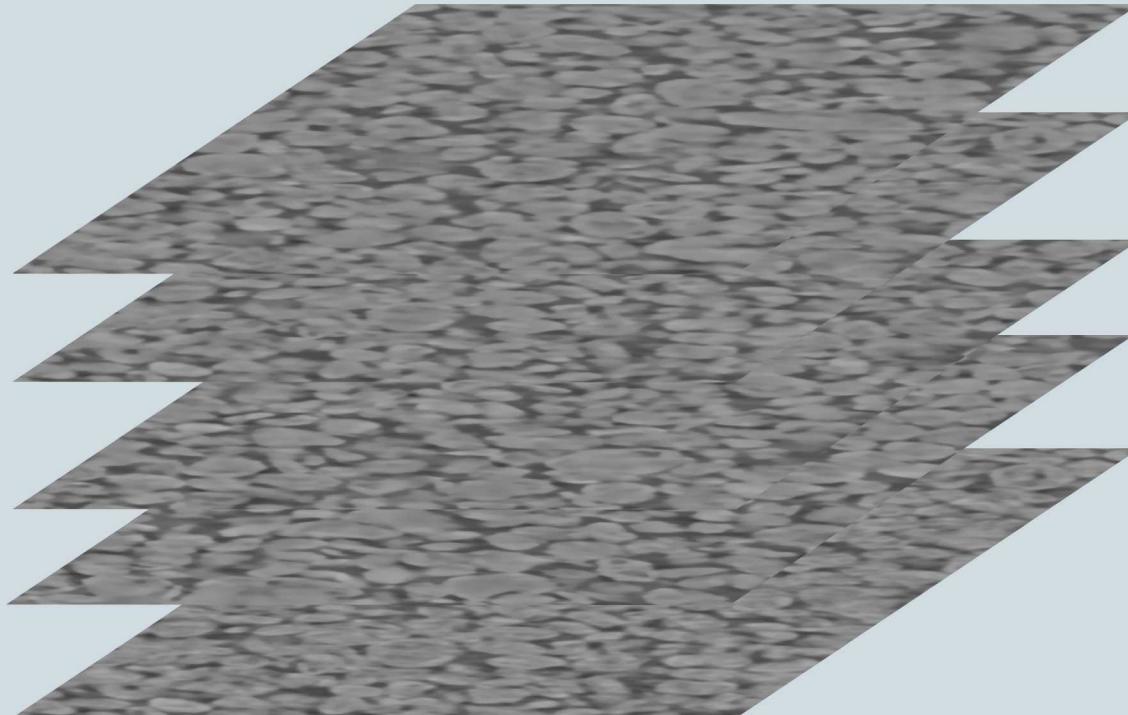
Litarin	Tesla	SamsungE35	Samsung 25R6	GCA400	GCA2000
---------	-------	------------	--------------	--------	---------

All electrode data is open source provided by Vanessa Woods group from  
ETH Zurich

# Methodology

---

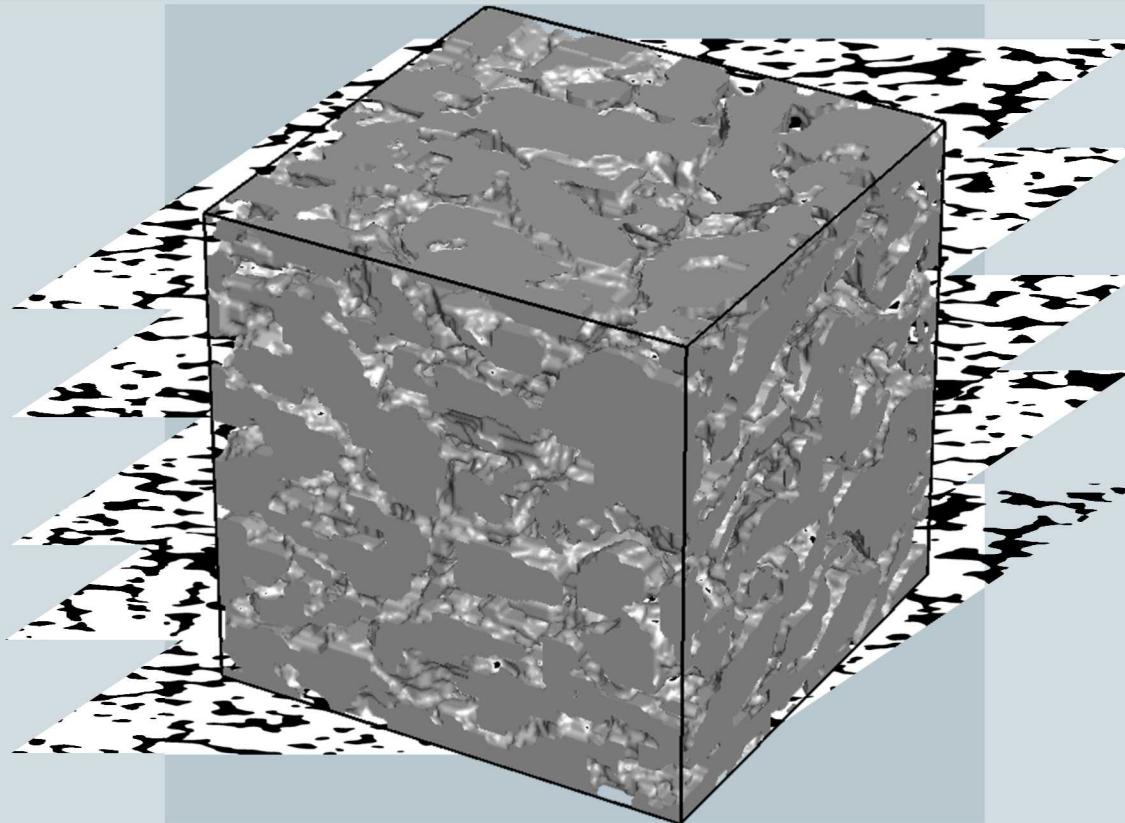
Q. How are structures acquired?



Stacks of images are acquired

# Methodology

Q. How are structures acquired?



Stacks of images are acquired

Greyscale images are binarized to black and white

These can then be made into a two-phase 3D structure

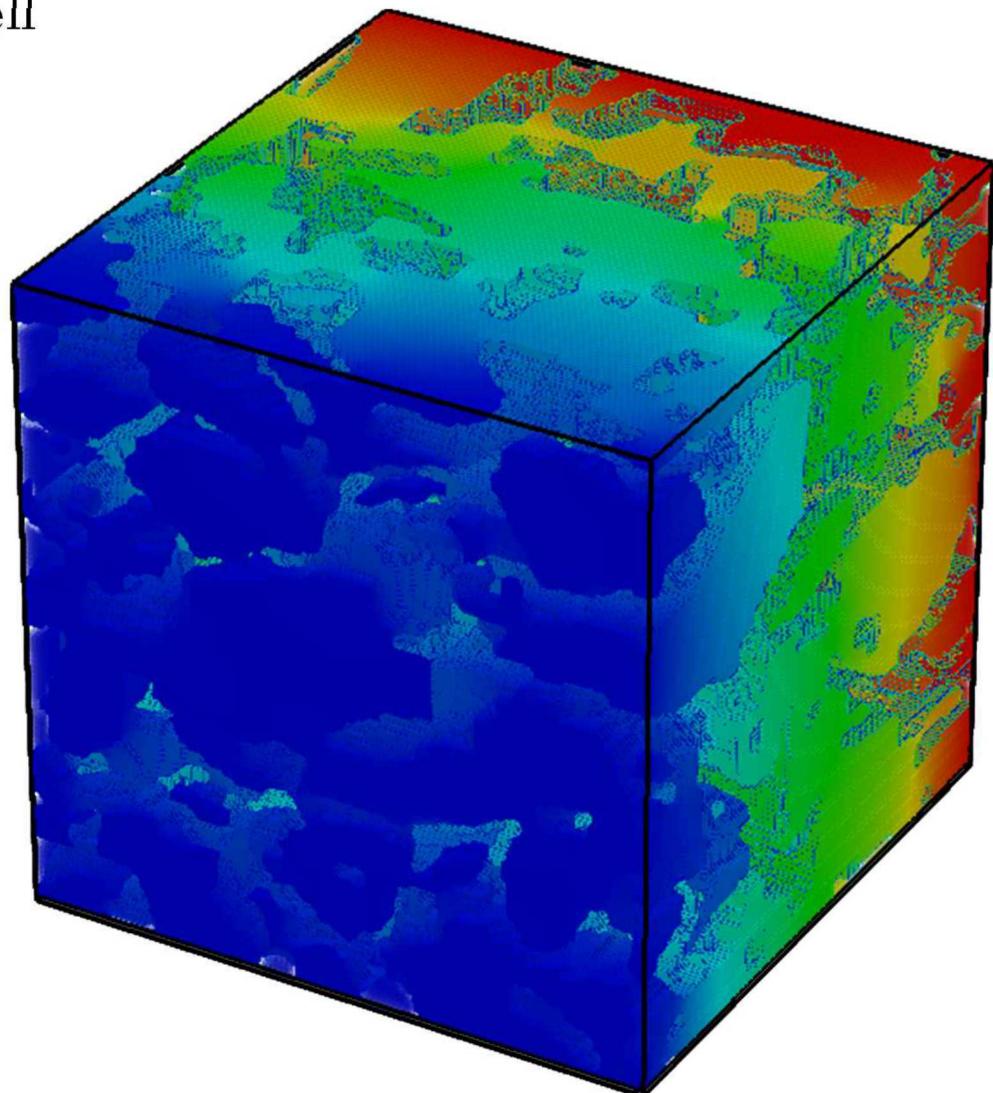
# Methodology

---

Q. What can these structures tell us?

These structures can provide:

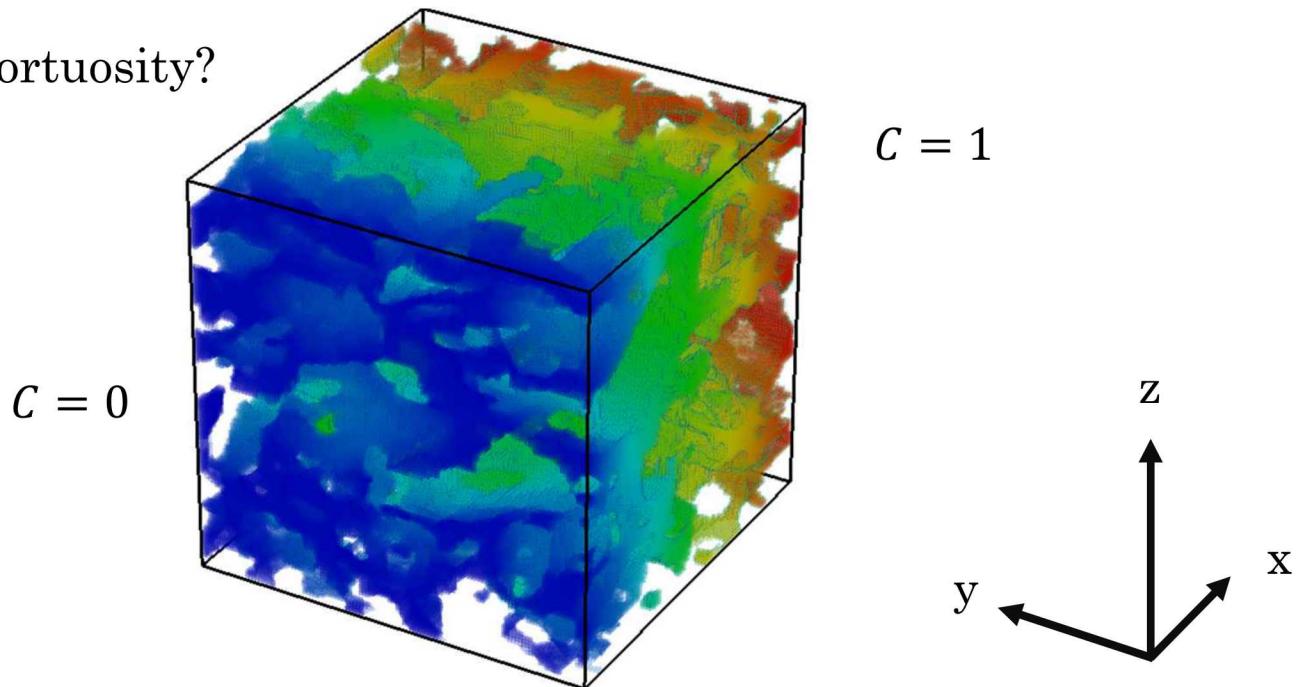
1. Porosity
2. Tortuosity
3. Conductivity
4. Surface Area



# Methodology

---

Q. How to find tortuosity?



**Tortuosity**

$$\nabla^2 C = 0$$

Boundary Conditions

$$C(x = 0) = 0$$

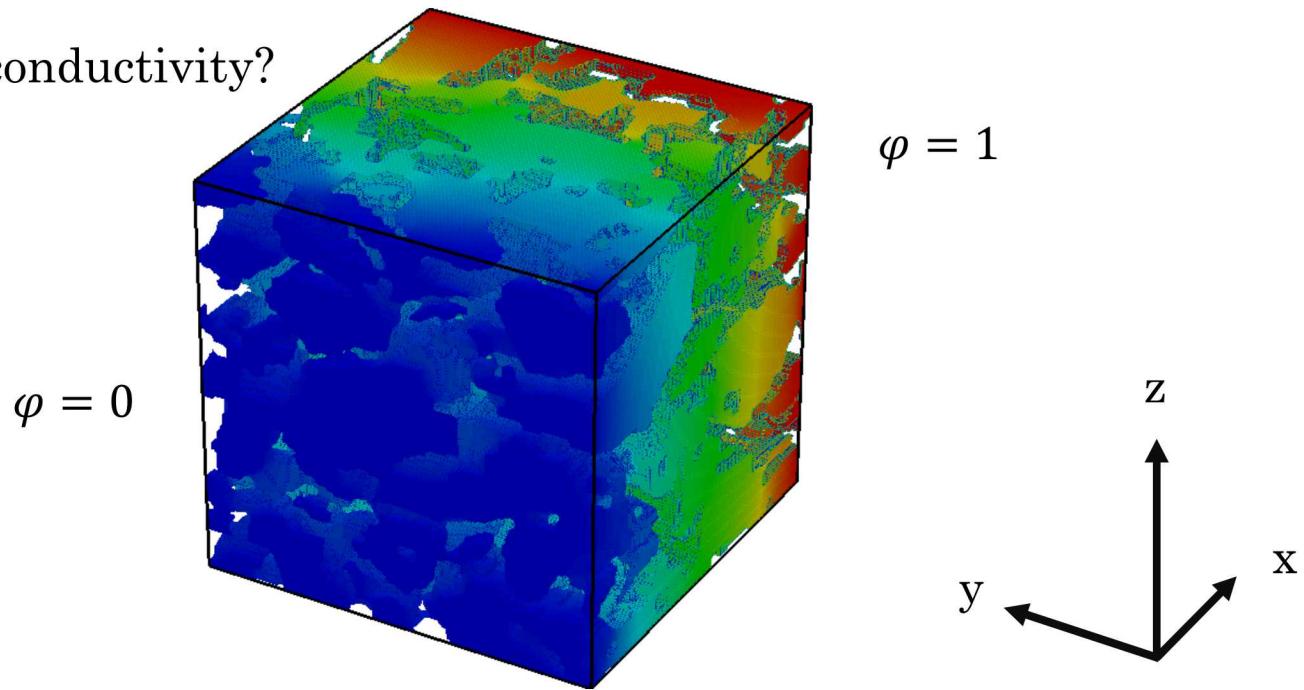
$$C(x = L_x) = 1$$

Four planes ( $y=0$ ,  $z=0$ ,  $y=L_y$ ,  $z=L_z$ )

$$\frac{\partial C}{\partial n} = 0$$

# Methodology

Q. How to find conductivity?



## ***Conductivity***

$$\nabla \cdot (\sigma \nabla \varphi) = 0$$

Boundary Conditions

$$\varphi(x = 0) = 0$$

$$\varphi(x = L_x) = 1$$

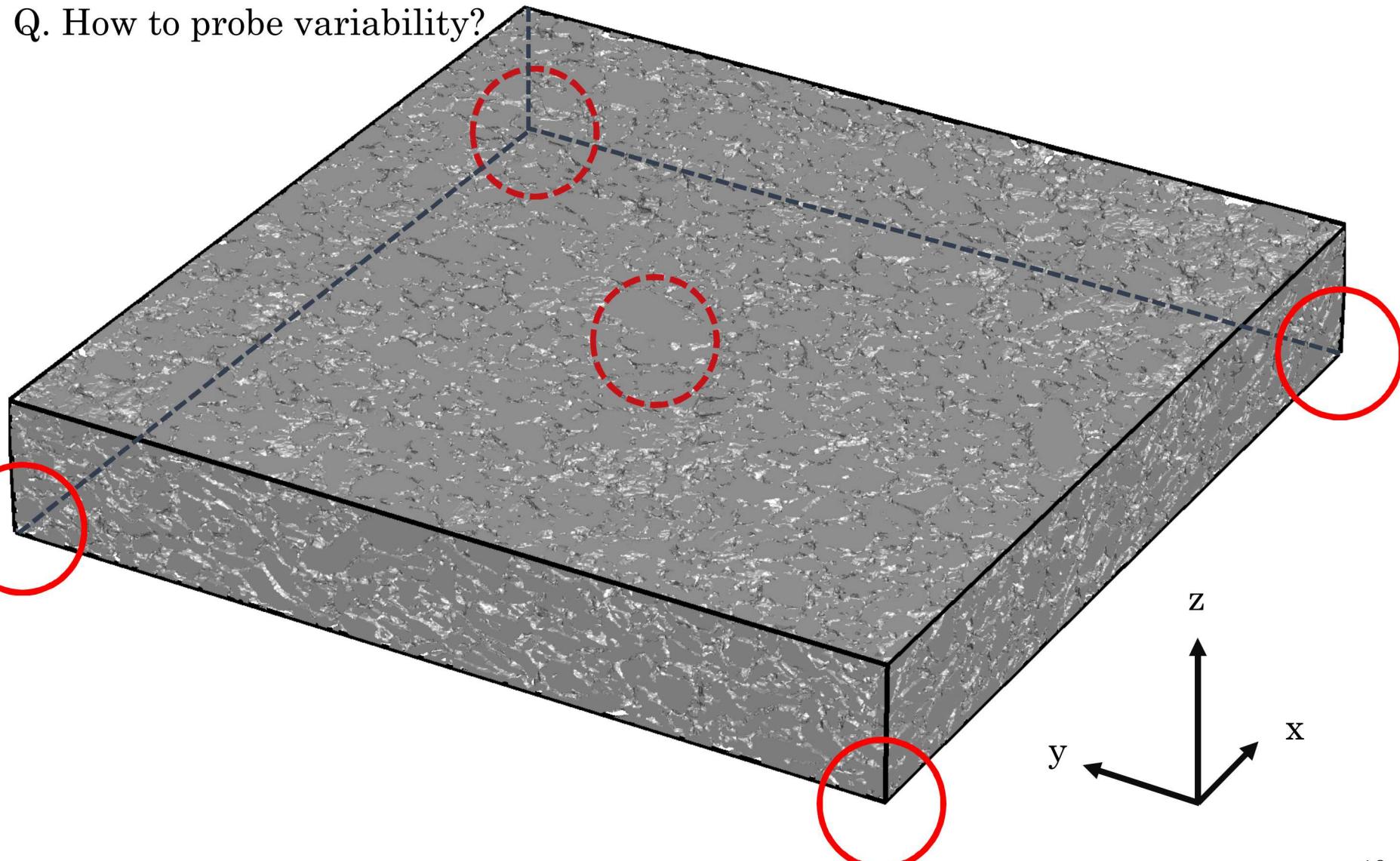
Four planes ( $y=0$ ,  $z=0$ ,  $y=L_y$ ,  $z=L_z$ )

$$\frac{\partial \varphi}{\partial n} = 0$$

# Methodology

---

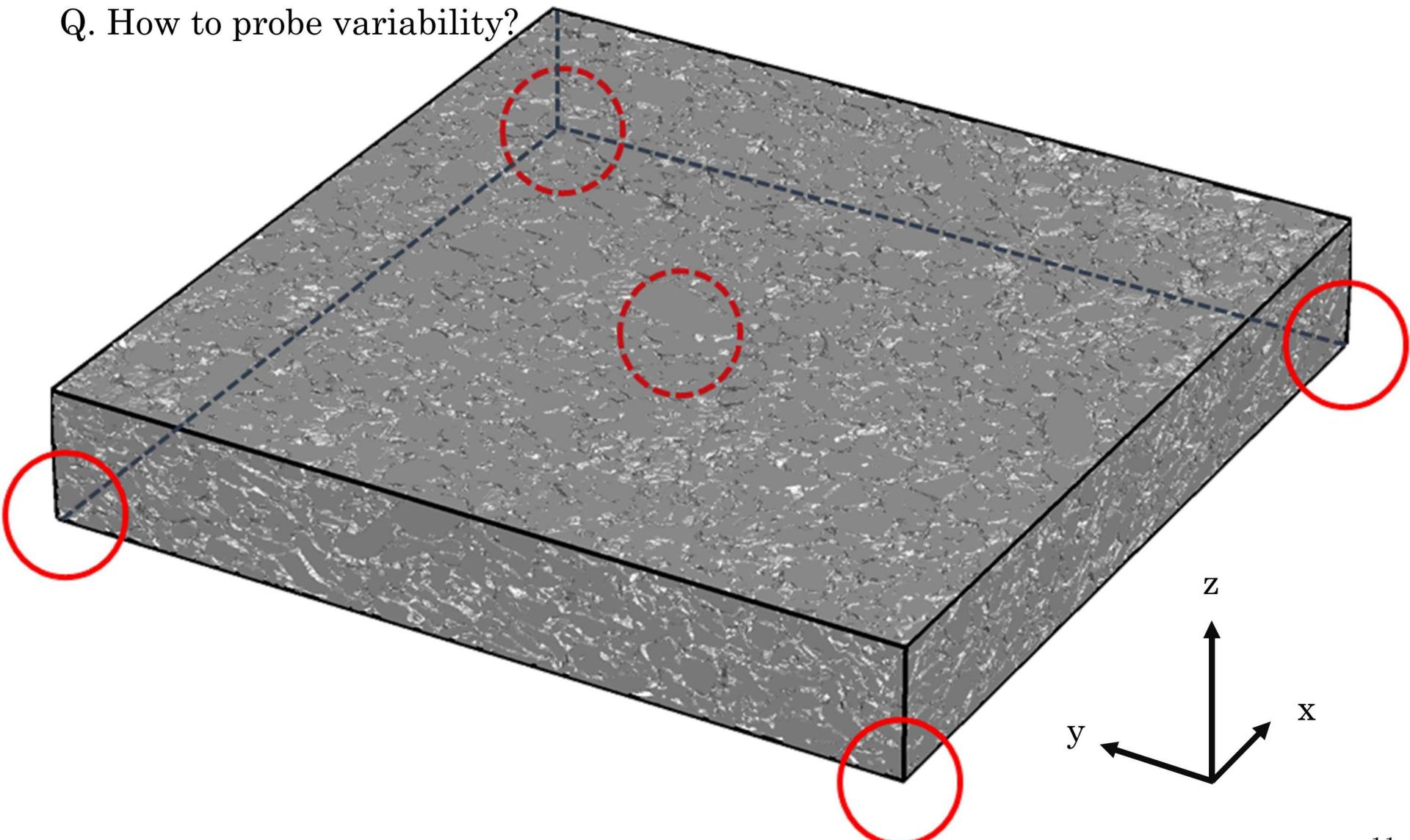
Q. How to probe variability?



# Methodology

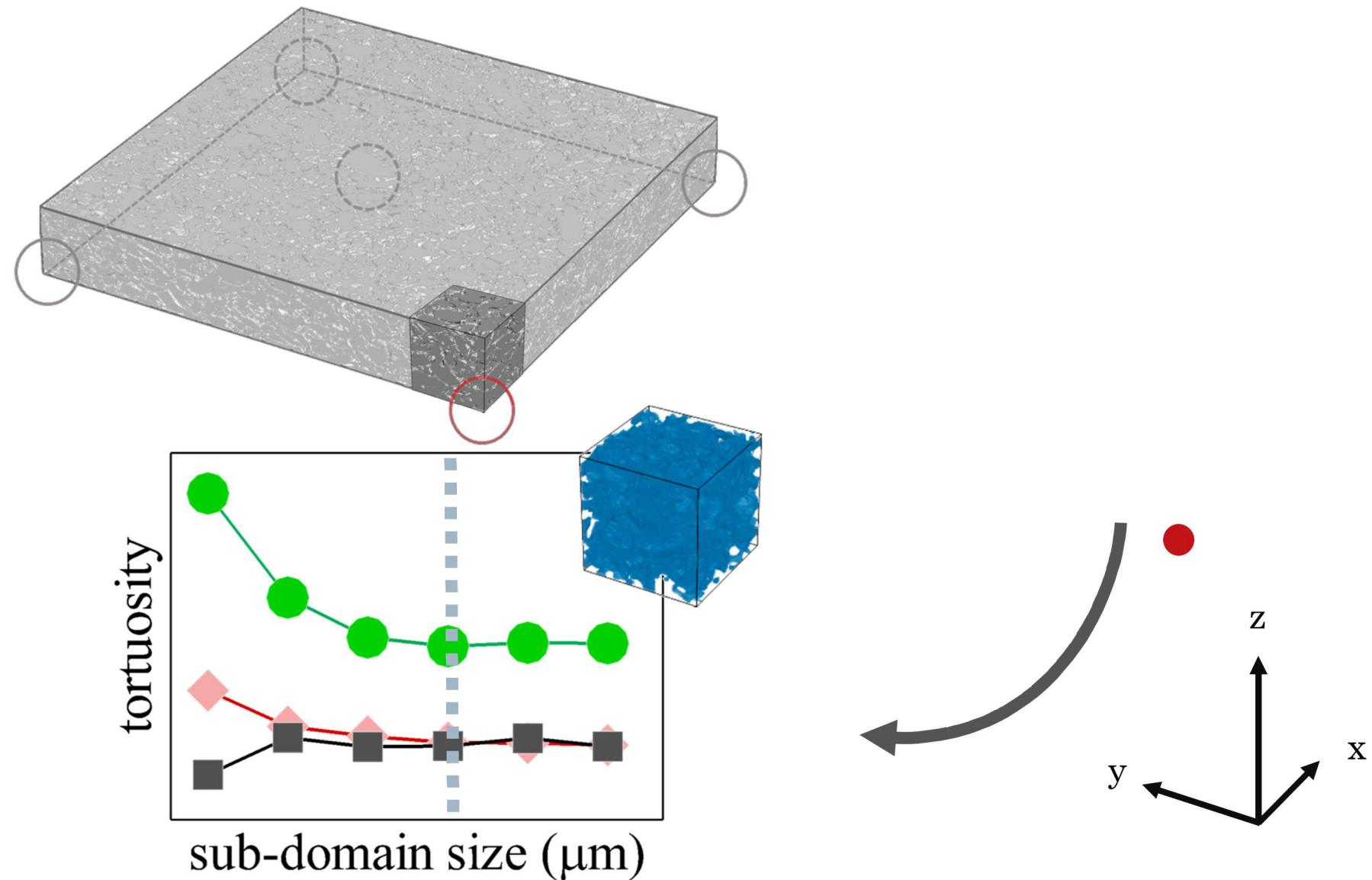
---

Q. How to probe variability?



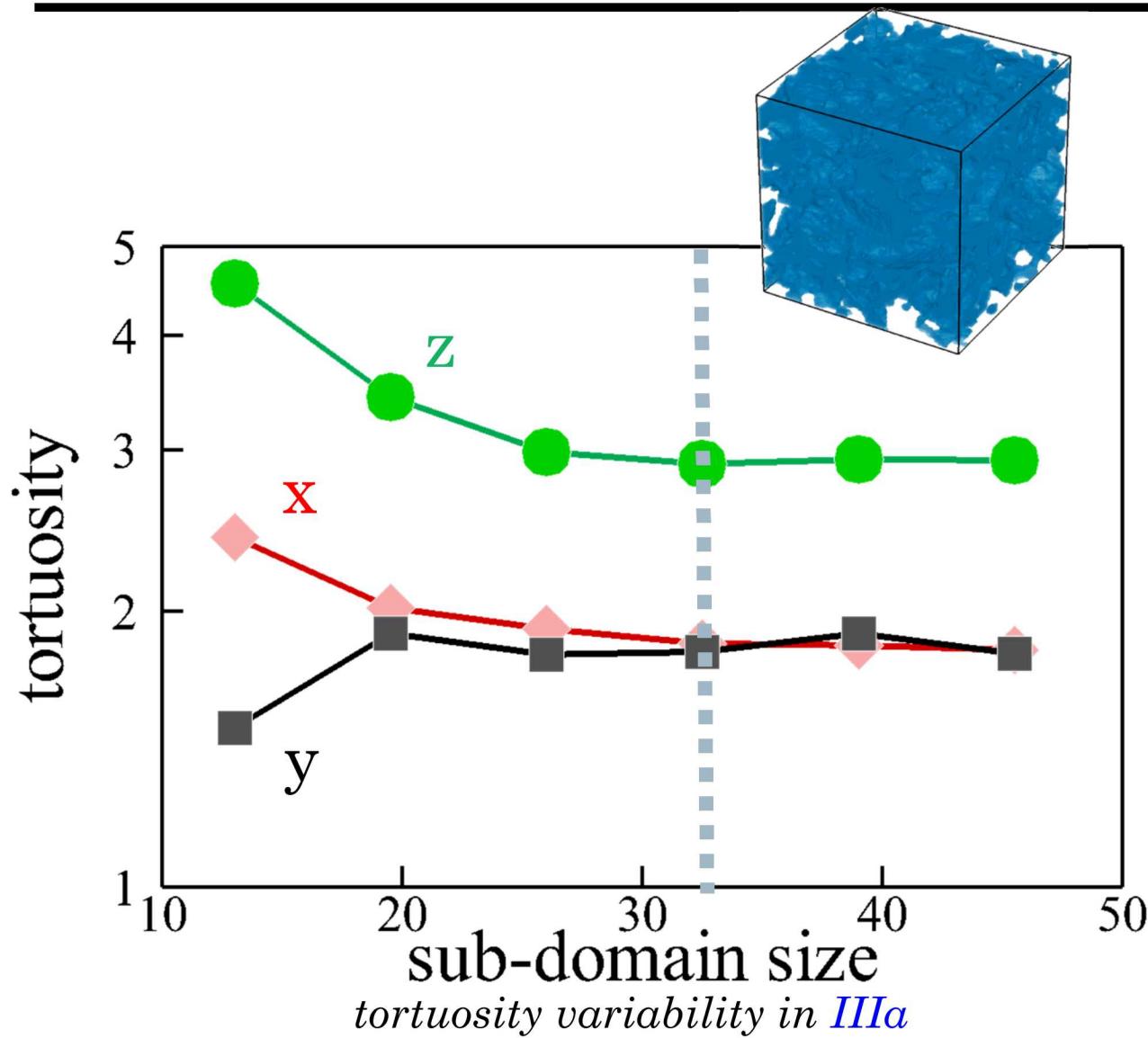
# Methodology

---



# Methodology

---



Visual convergence of values as sub-domain size increases.

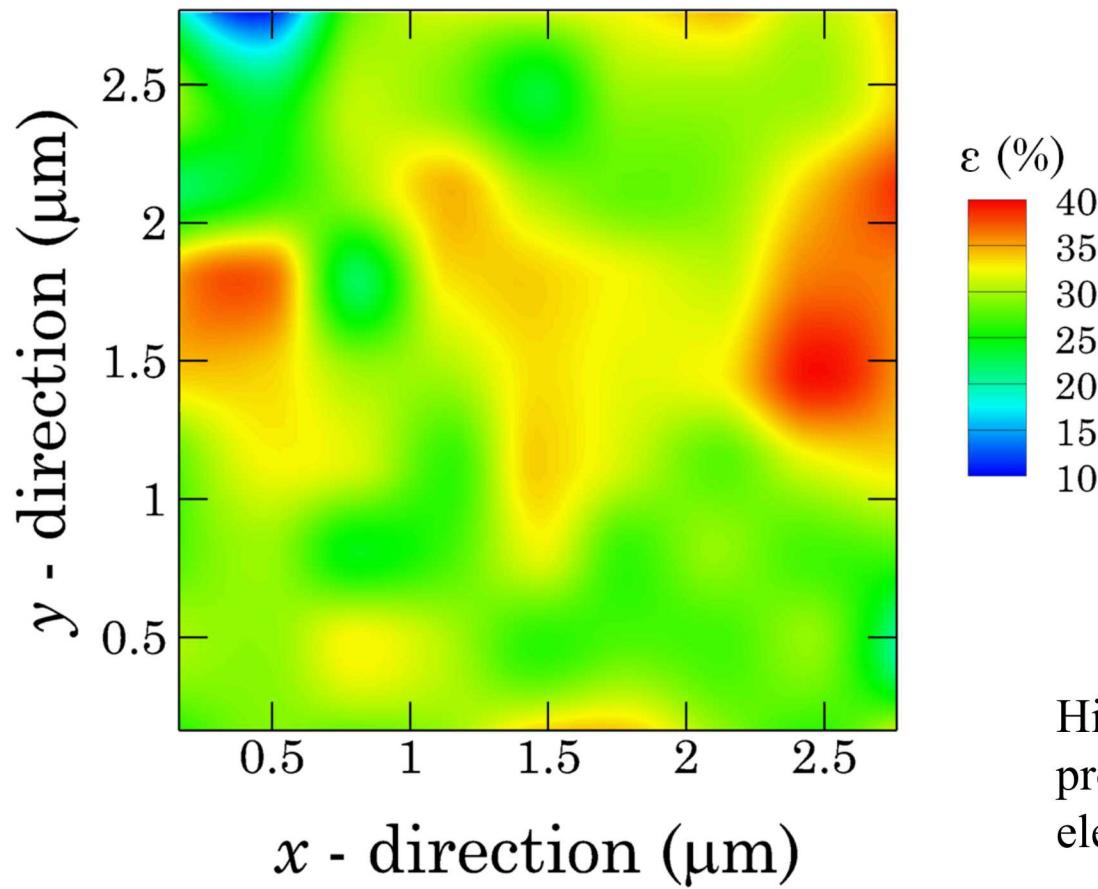
Choosing the smallest value where visual convergence occurs among all nodes.

This value can then be used to probe spatial variability.

# Variability Within an Electrode

---

Q. How can variability be quantified?

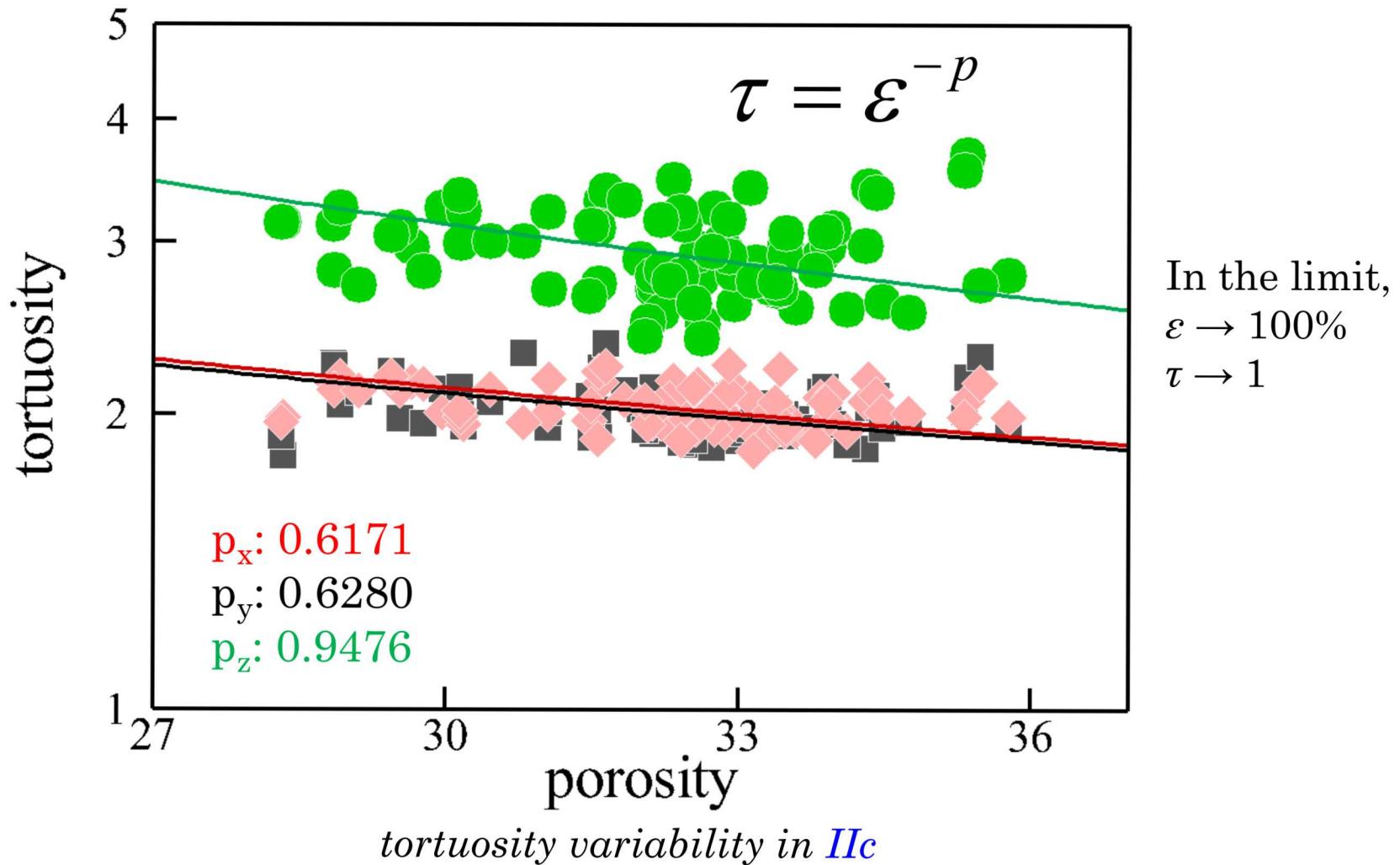


*Porosity (%) variation in electrode Ib*

Higher local regions of effective properties can be seen in every electrode.

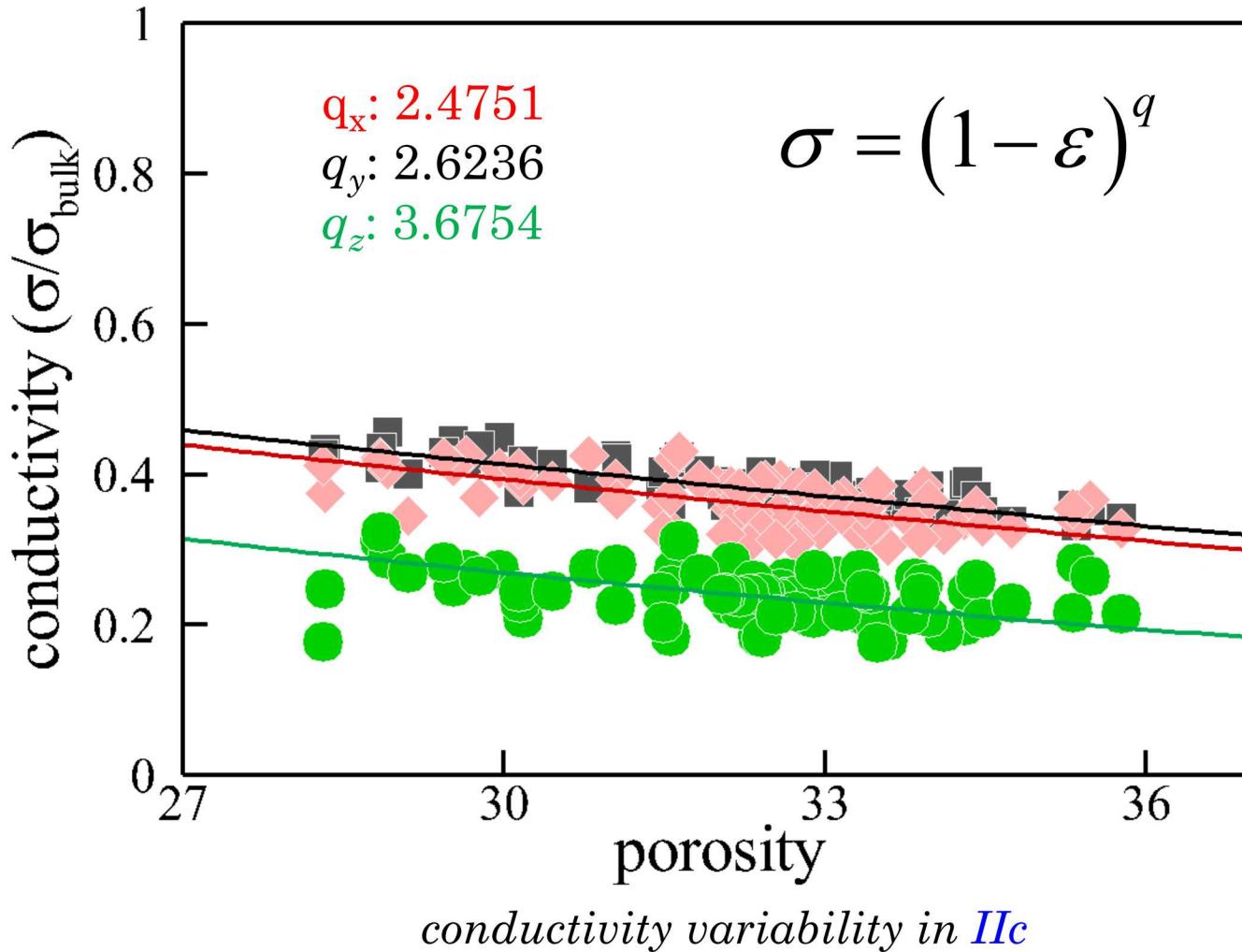
# Variability Within an Electrode

Q. How can variability be quantified?

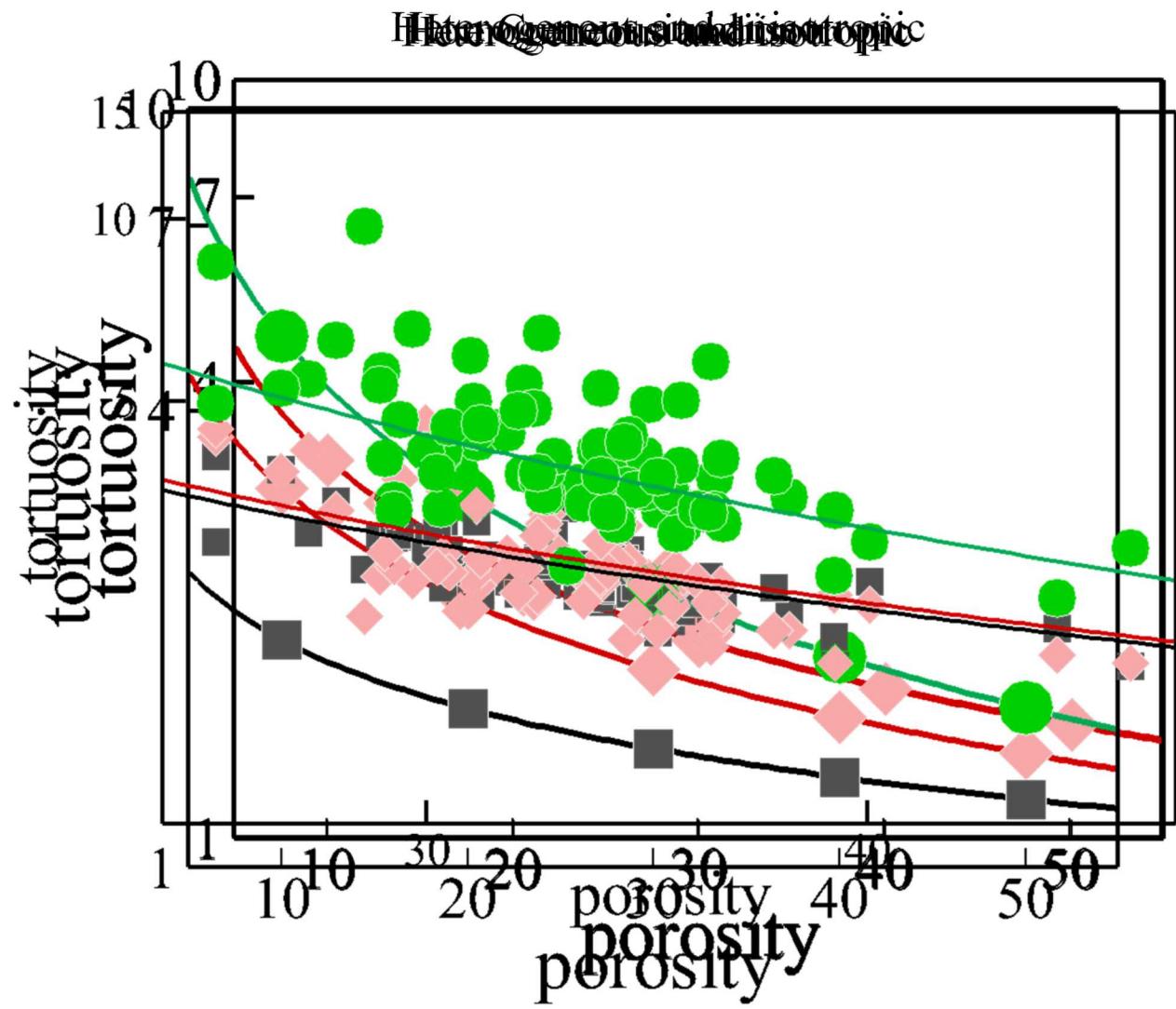
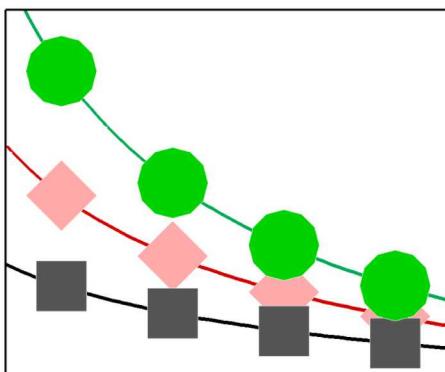
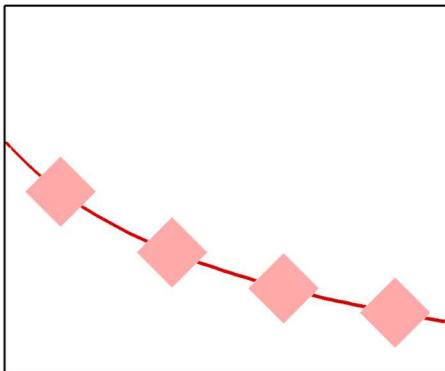
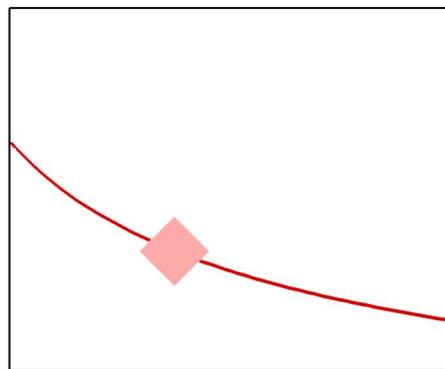


# Variability Within an Electrode

Q. How can variability be quantified?

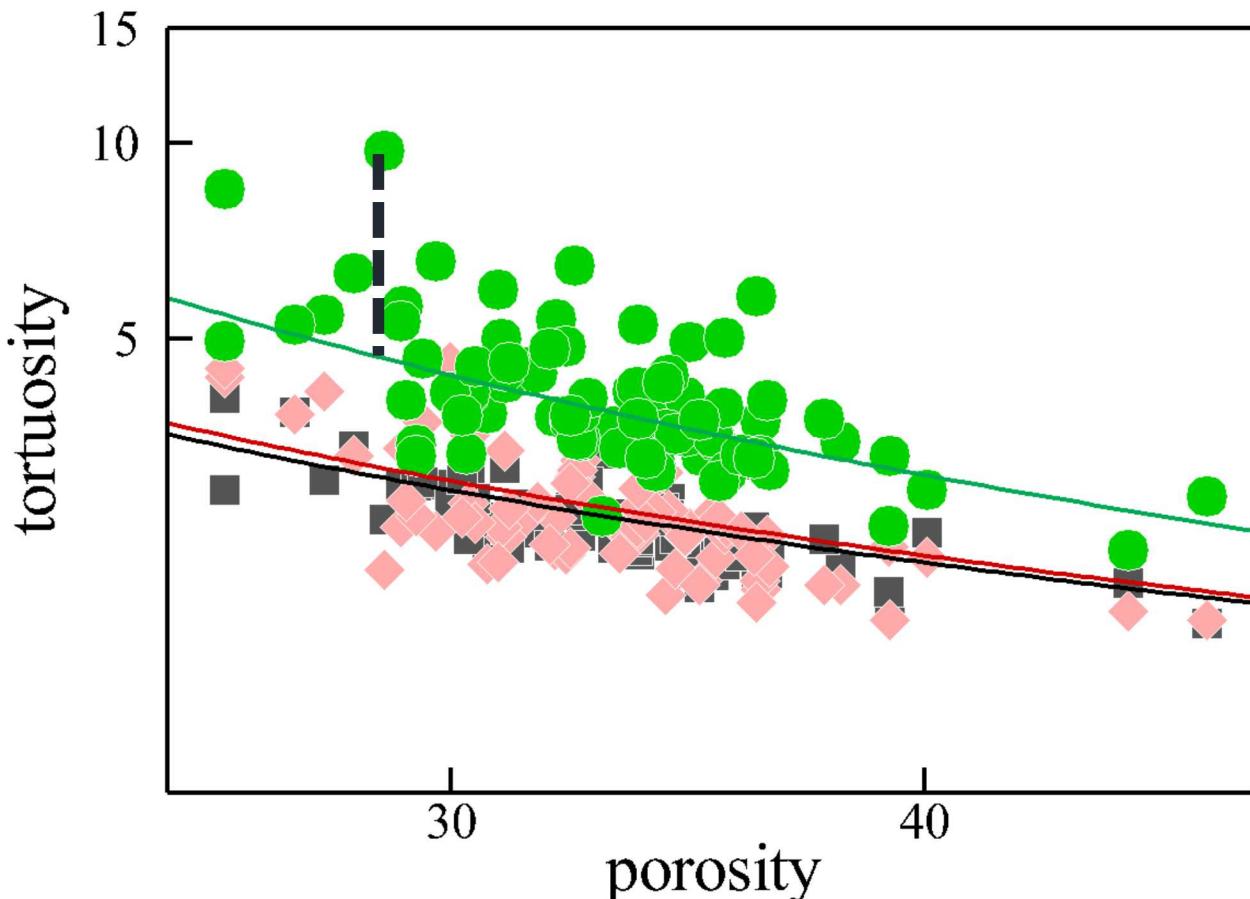


# Variability Within an Electrode



# Variability Within an Electrode

Deviation,  $\delta$



*tortuosity variability in  $I_c$*

Individual  $\delta$  values for each point

$$\delta_\tau = \frac{\tau_{measured} - \tau_{fitted}}{\tau_{fitted}}$$

These normalized points now act as another data point

This can be seen as the internal RVE variability.

# Particle Characterization

---

By implementing a 3D Sobel operator we can apply this to three dimensions for our particles.

1	2	1
2	4	2
1	2	1

$$h_z(:,:, -1)$$

0	0	0
0	0	0
0	0	0

$$h_z(:,:, 0)$$

-1	-2	-1
-2	-4	-2
-1	-2	-1

$$h_z(:,:, 1)$$

$$G_z = h_z * I$$

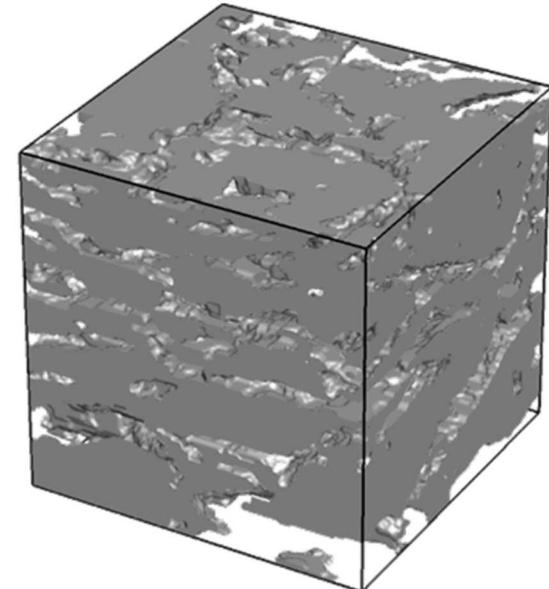
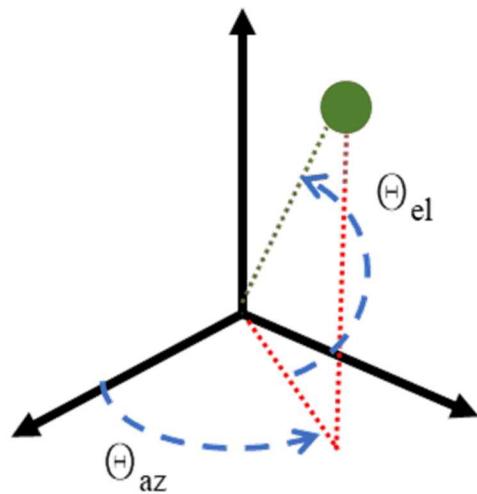
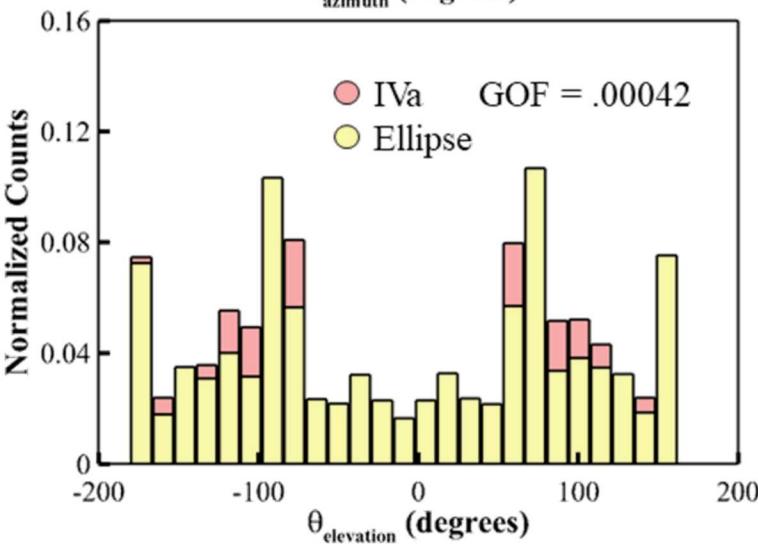
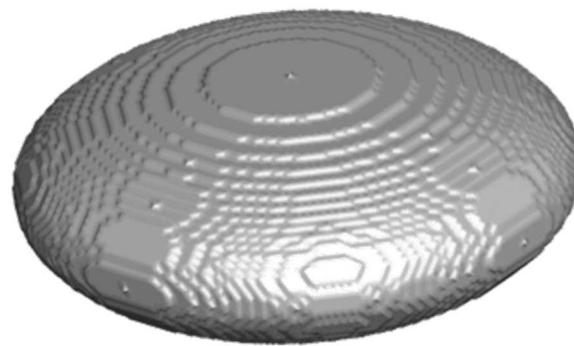
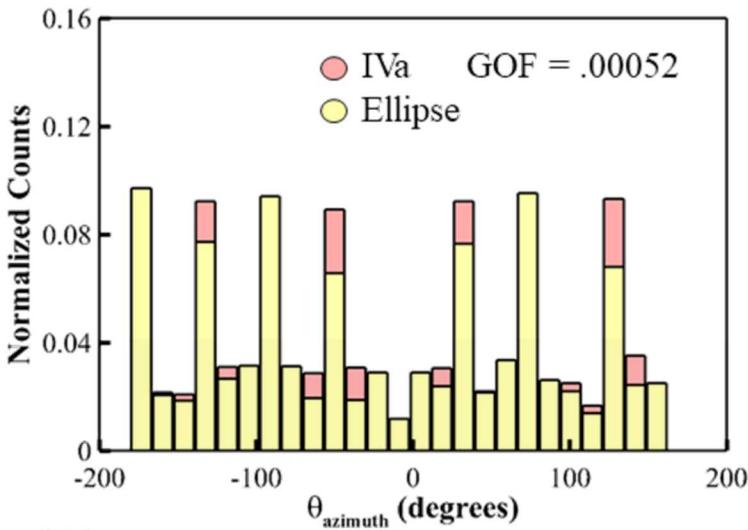
$$G_{mag} = \sqrt{G_y^2 + G_x^2 + G_z^2}$$

$$\phi = \arctan\left(\frac{G_z}{\sqrt{G_x^2 + G_y^2}}\right)$$

$$\theta = \arctan\left(\frac{G_y}{G_x}\right)$$

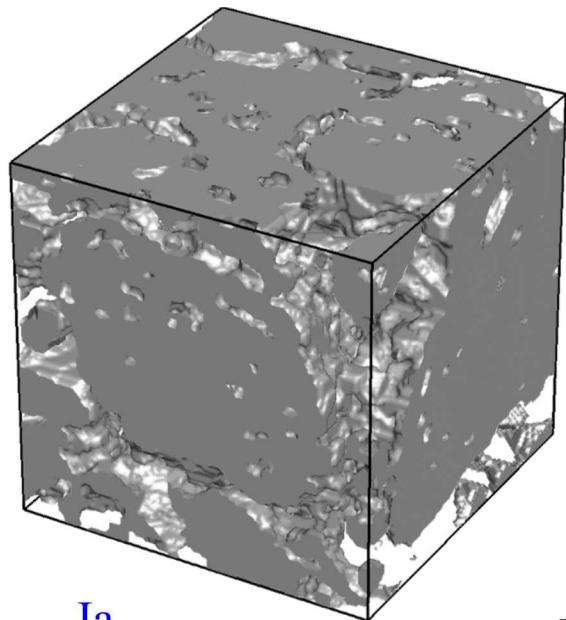
# Particle Characterization

By varying ellipsoid parameters we can find reference particles to help describe the electrode.

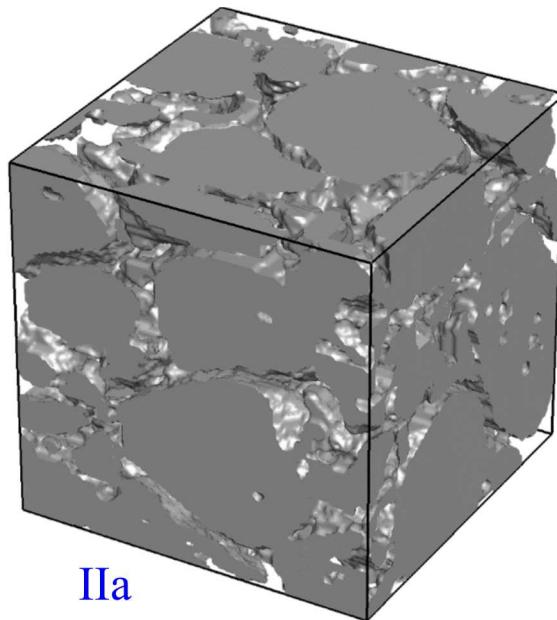


# Particle Morphology Effects

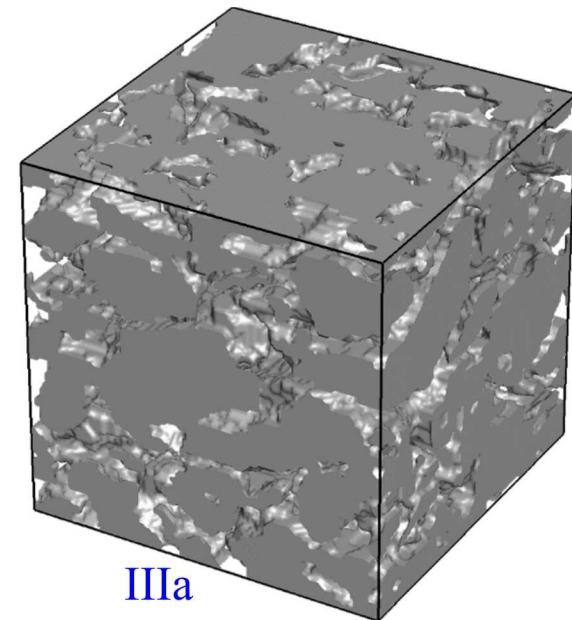
---



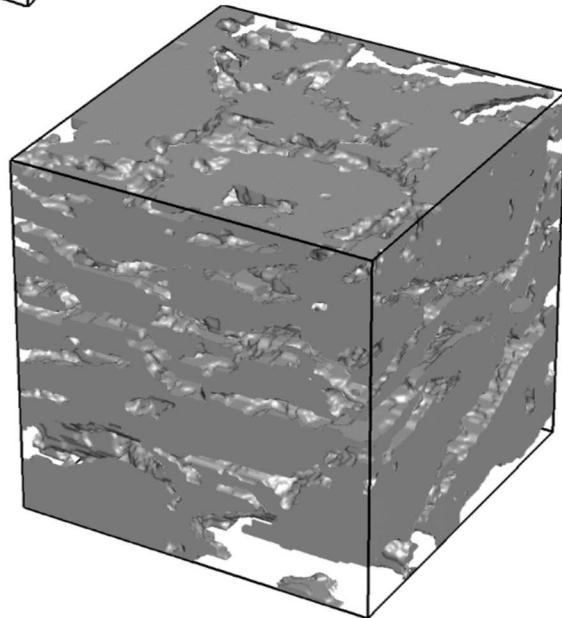
Ia



IIa



IIIa

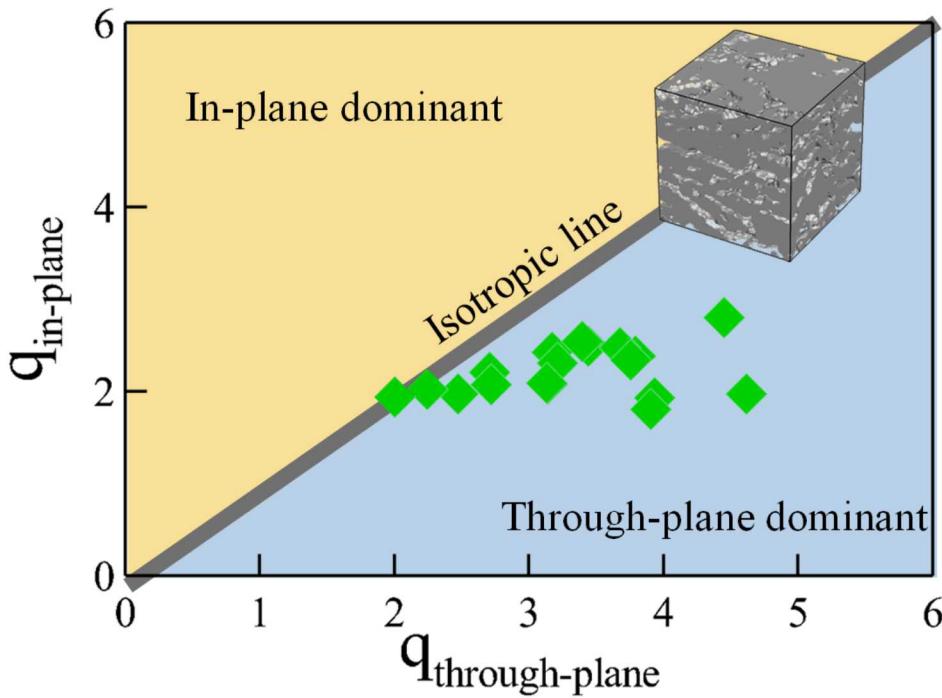


IVa

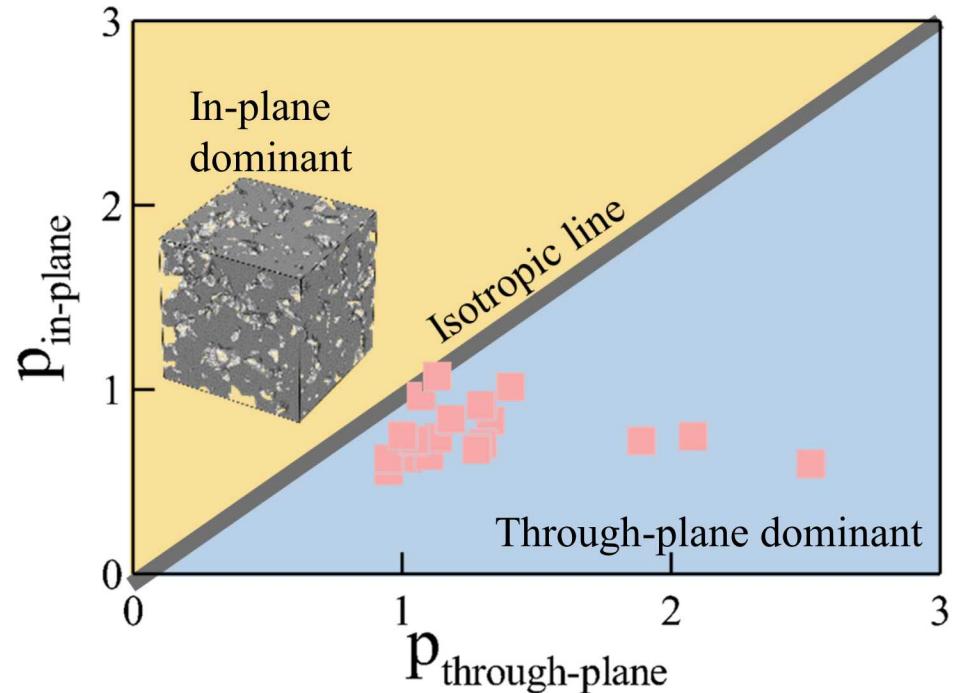
Q. How does differing morphologies influence effective properties?

# Particle Morphology Effects

$$\sigma = (1 - \epsilon)^q$$



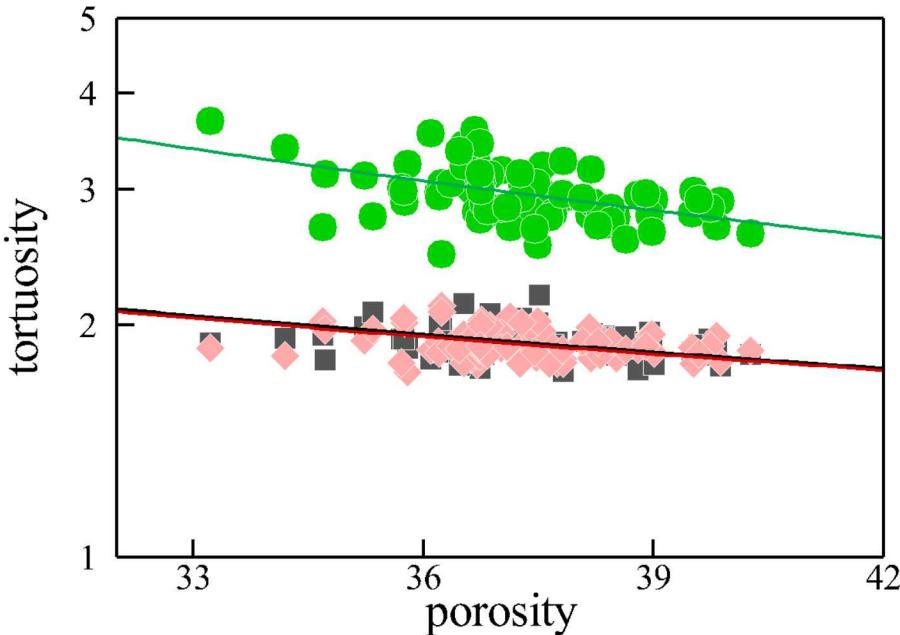
$$\tau = \epsilon^{-p}$$



Many electrodes show varying degrees of anisotropies

# Particle Morphology Effects

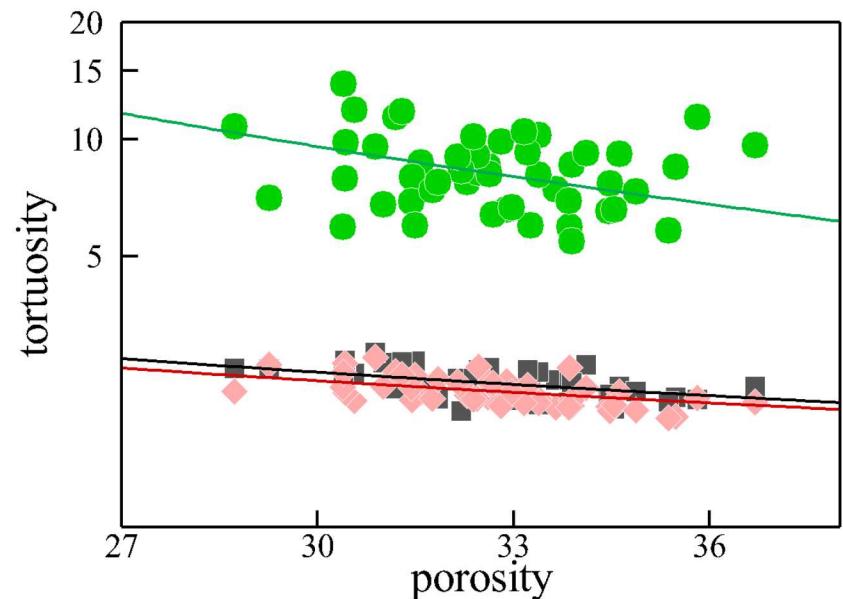
Q. What causes these variations in delta?



*tortuosity variability in IIIa*

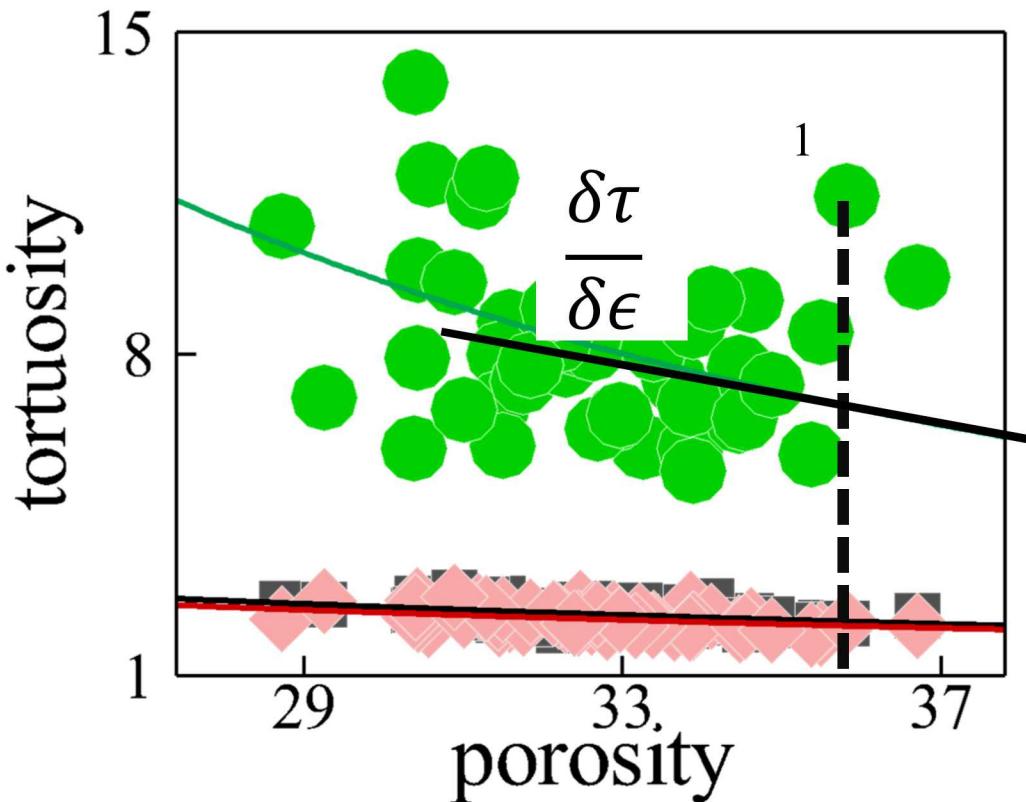
A directional correlation and proportionality to  $\frac{dZ}{d\epsilon}$  is observed.

Electrode	$\overline{\delta_{\tau x}}$	$\overline{\delta_{\tau y}}$	$\overline{\delta_{\tau z}}$
IIIc	0.0331	0.0331	0.0543
IVb	0.0586	0.0602	0.1812



*tortuosity variability in IVb*

# Particle Morphology Effects



$\frac{\delta\tau}{\delta\epsilon}$  represents the slope of the tortuosity at a given porosity value of the designated curve.

$$\tau = \epsilon^{-p}$$

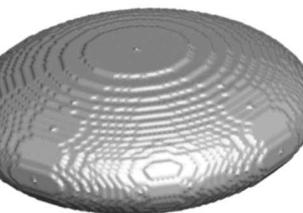
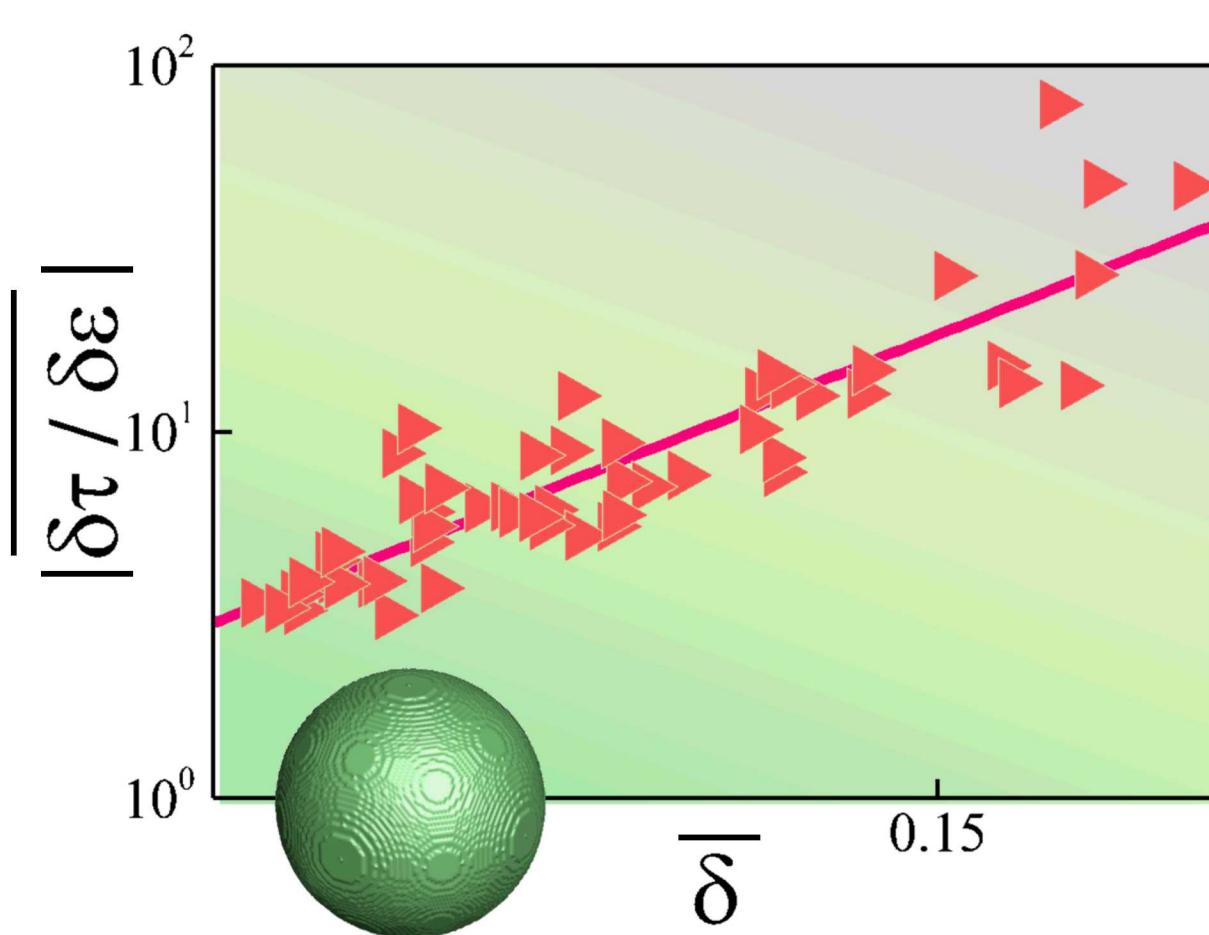
$\tau \rightarrow \text{tortuosity}$

$\epsilon \rightarrow \text{porosity}$

$$\frac{\delta\tau}{\delta\epsilon} = -p\epsilon^{-p-1}$$

$p \rightarrow \text{exponential to curve fit}$

# Particle Morphology Effects

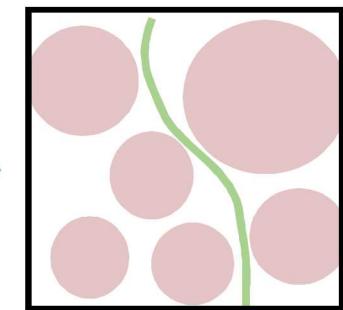
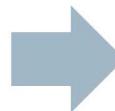
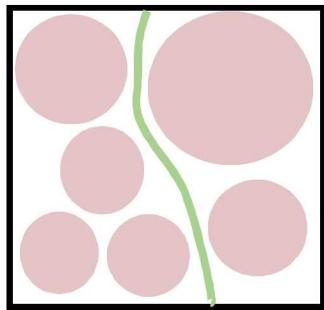
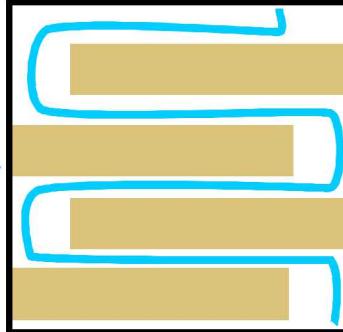
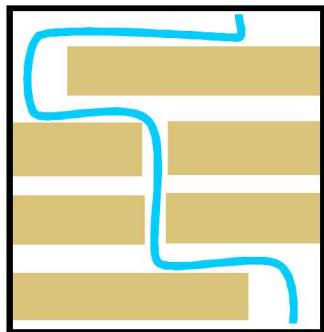


More anisotropic particles lead to higher delta values

$\bar{\delta} \rightarrow$  mean deviation of RVEs

$\left| \frac{\bar{\delta}\tau}{\delta\epsilon} \right| \rightarrow$  mean magnitude of slope

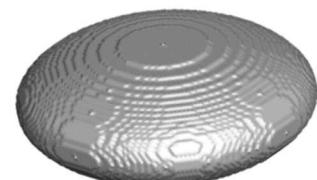
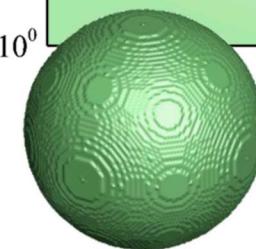
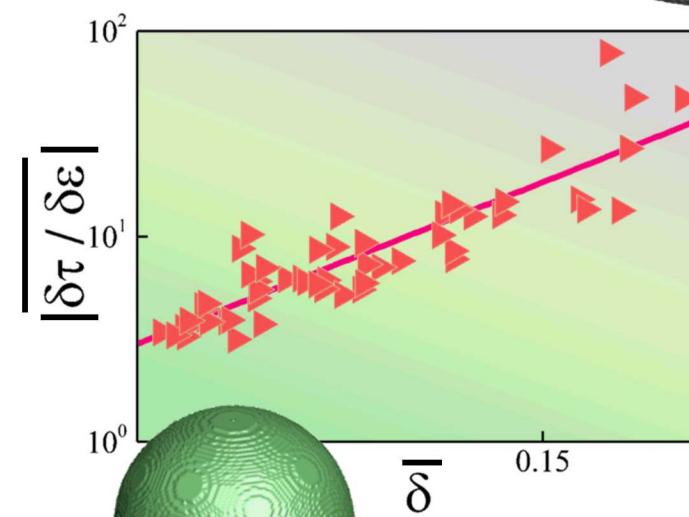
# Particle Morphology Effects



Porosity is held constant in every case.

- With small changes in particle locations large tortuosity changes are seen.

The sensitive nature of the platelet like particles is mirrored in the delta reliance plot (below).



# Conclusion

---

- Successful screening method that can compare a multitude of morphologies without segmenting particles.
- Many morphologies exhibit anisotropy given varying morphologies.
- Internal RVE tortuous dispersion can arise from particle morphology whereas conductivity does not show the same.

# Acknowledgements

---

Funding from Sandia National Lab

Scott Roberts and team



Sandia National Laboratories is a multimission laboratory managed and operated by National Technology and Engineering Solutions of Sandia LLC, a wholly owned subsidiary of Honeywell International Inc. for the U.S. Security Administration under contract DE-NA0003535



**Thank You!**