



Energy and Transport Sciences Laboratory



Microstructural Variability in Graphite Electrodes

Chance Norris¹, Aashutosh Mistry¹, Scott Roberts² and Partha P. Mukherjee¹

¹ School of Mechanical Engineering, Purdue University, West Lafayette, Indiana 47907, USA

² Engineering Sciences Center, Sandia National Laboratories, Albuquerque, New Mexico 87185, USA

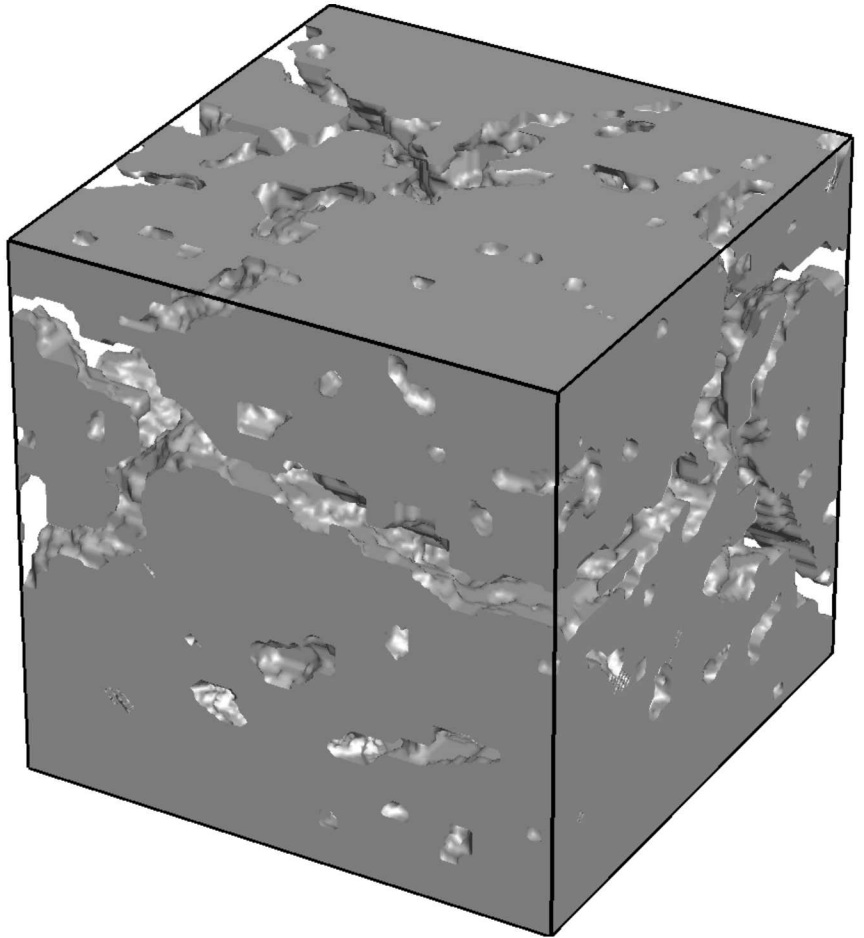
Motivation

Q. Why are we interested in microstructural variations in graphite electrodes?

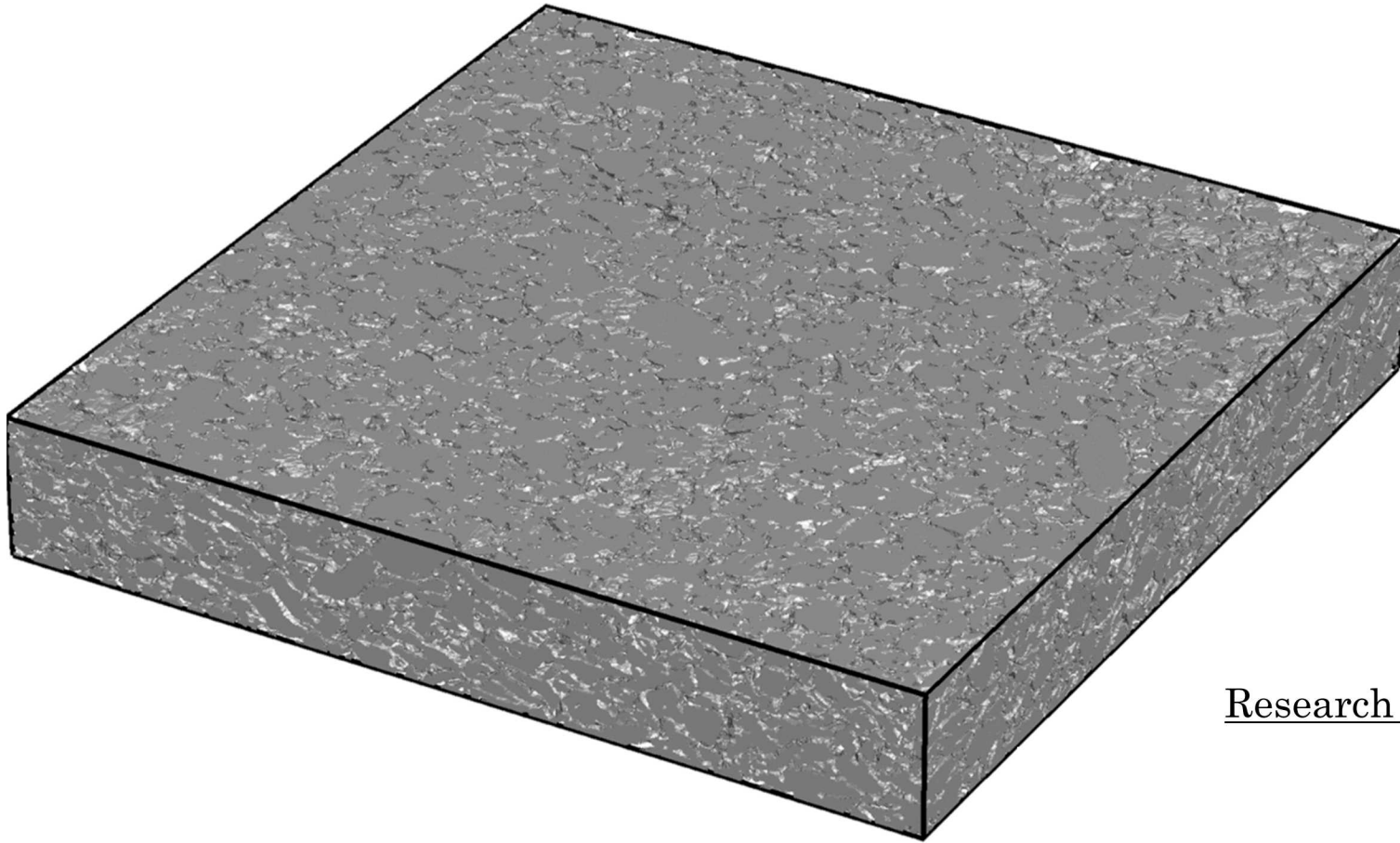
Fast charging or long-term cycling is negative electrode limited.

Graphite is one of the most used anodes in Li-ion batteries to date.

Many varying particle morphologies in graphite.



Objective



Research Questions

Graphite Anodes

Numbered Electrodes			
Ia	IIa	IIIa	IVa
Ib	IIb	IIIb	IVb
Ic	IIc	IIIc	IVc

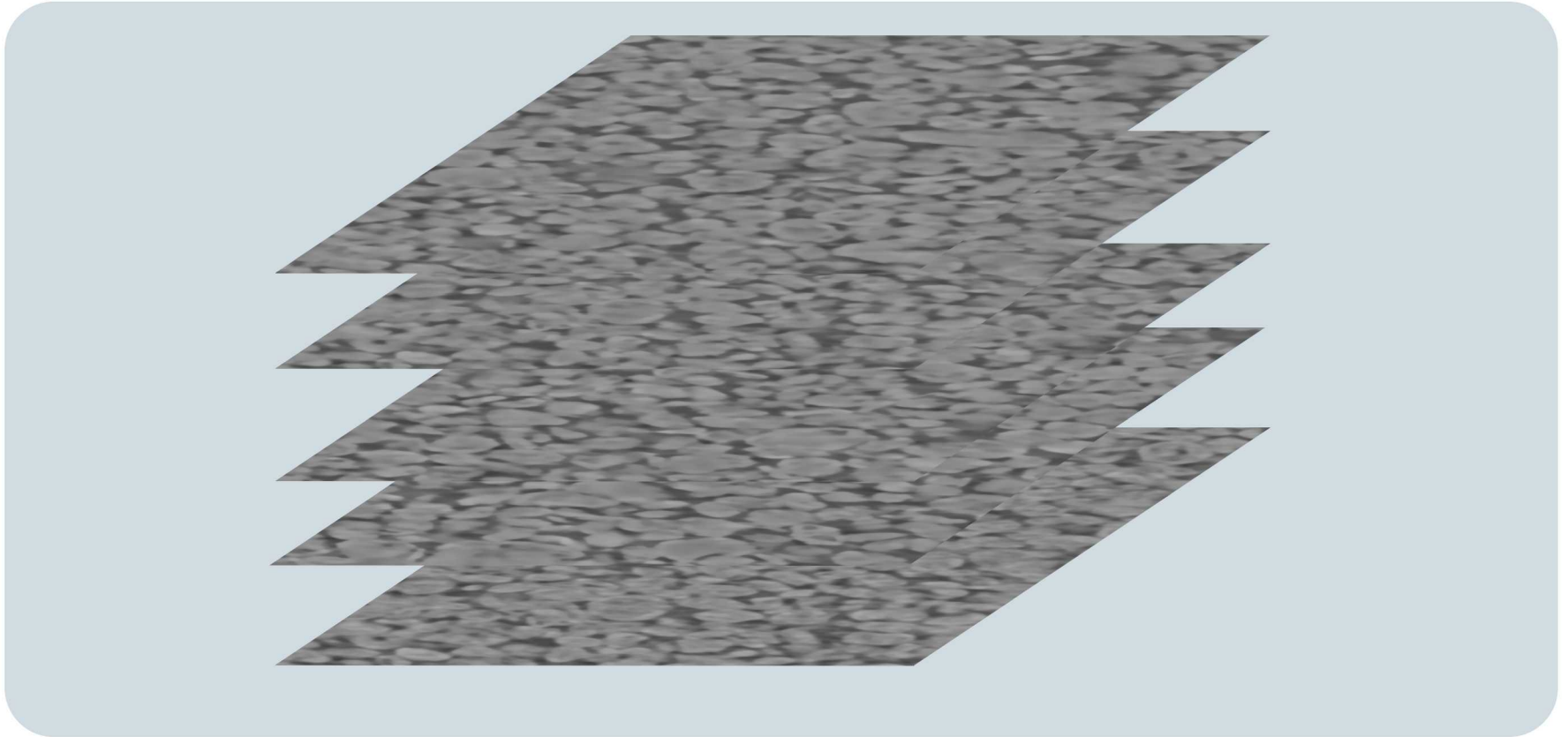
Where a, b and c denotes three samples taken from one commercial sheet

Named Electrodes					
Litarin	Tesla	SamsungE35	Samsung 25R6	GCA400	GCA2000

All electrode data is open source provided by Vanessa Woods group from
ETH Zurich

Methodology

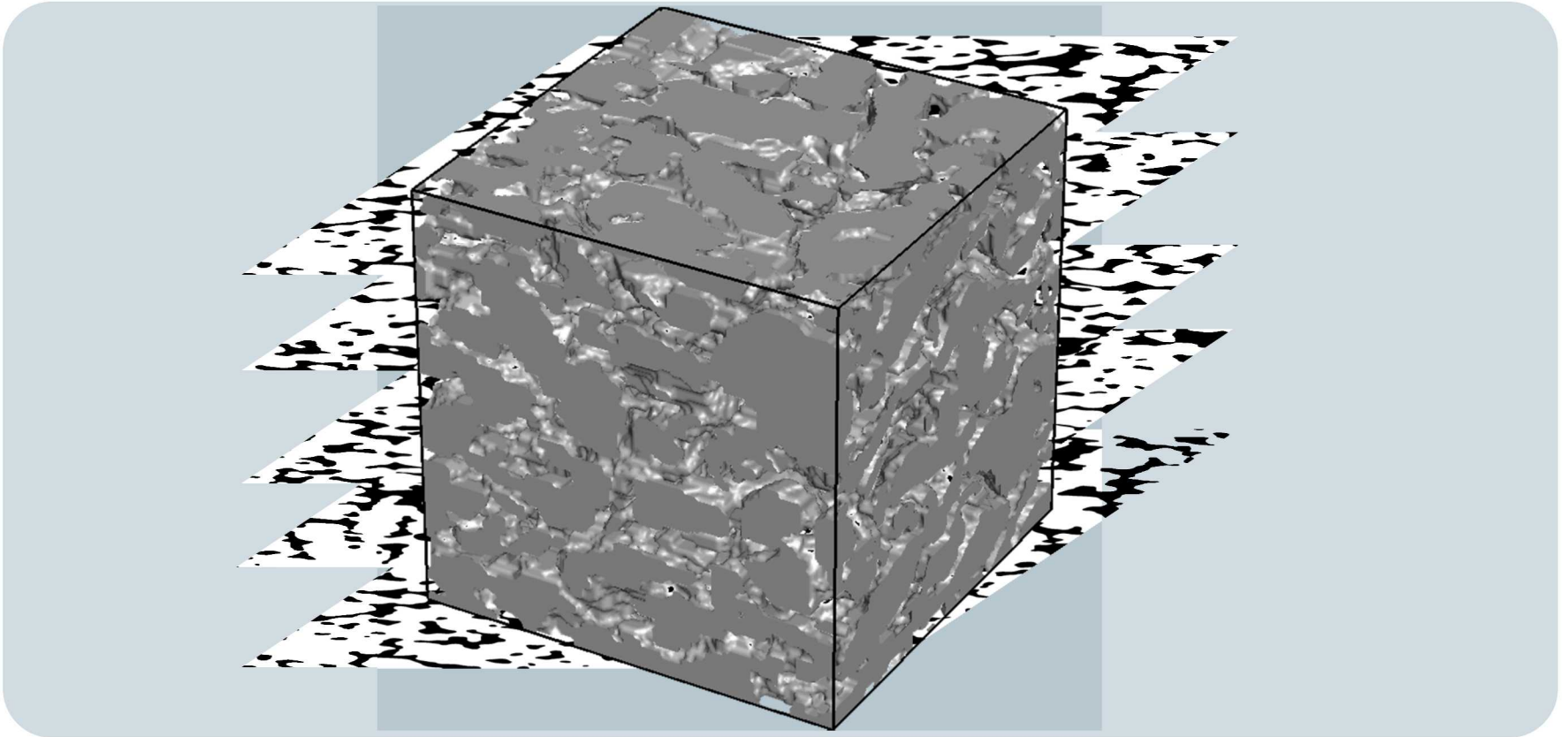
Q. How are structures acquired?



Stacks of images are acquired

Methodology

Q. How are structures acquired?



Stacks of images are acquired

Greyscale images are binarized to black and white

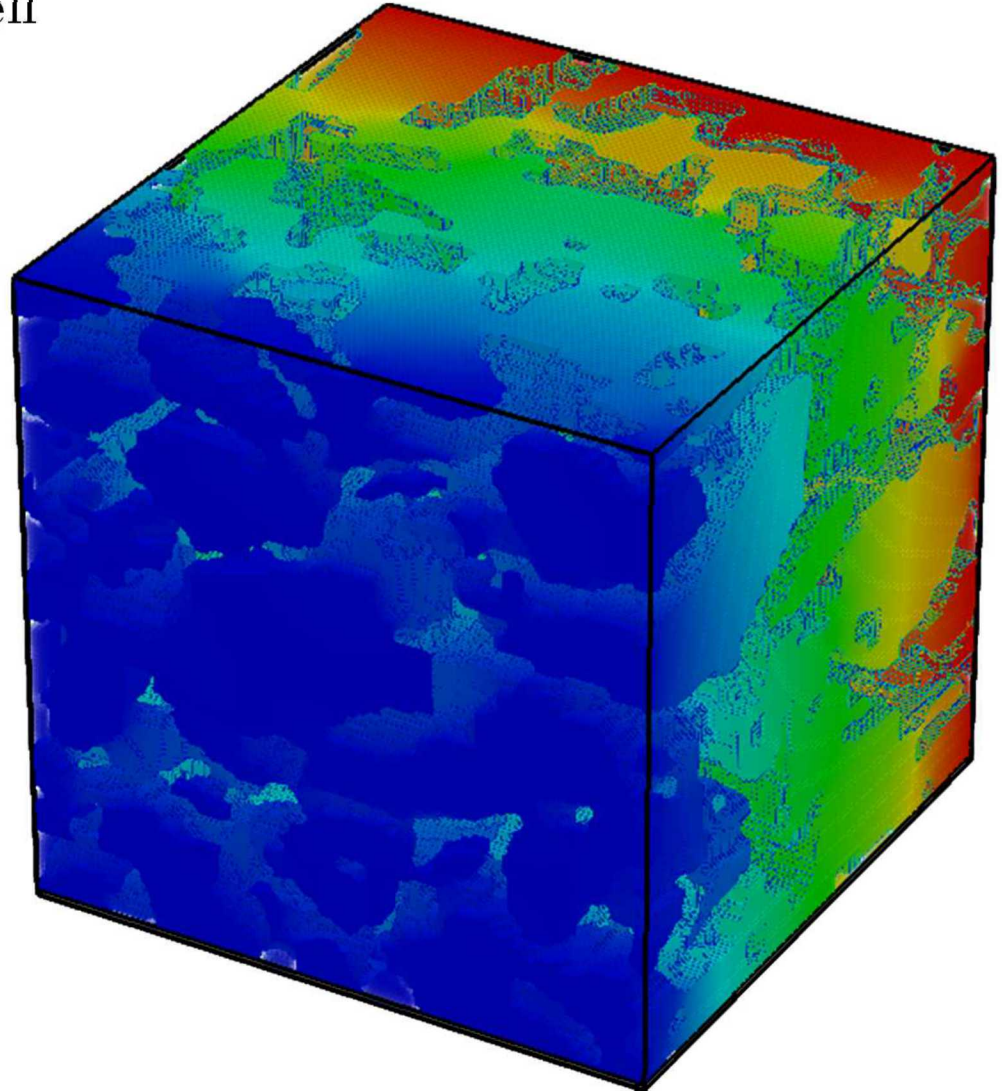
These can then be made into a two-phase 3D structure

Methodology

Q. What can these structures tell us?

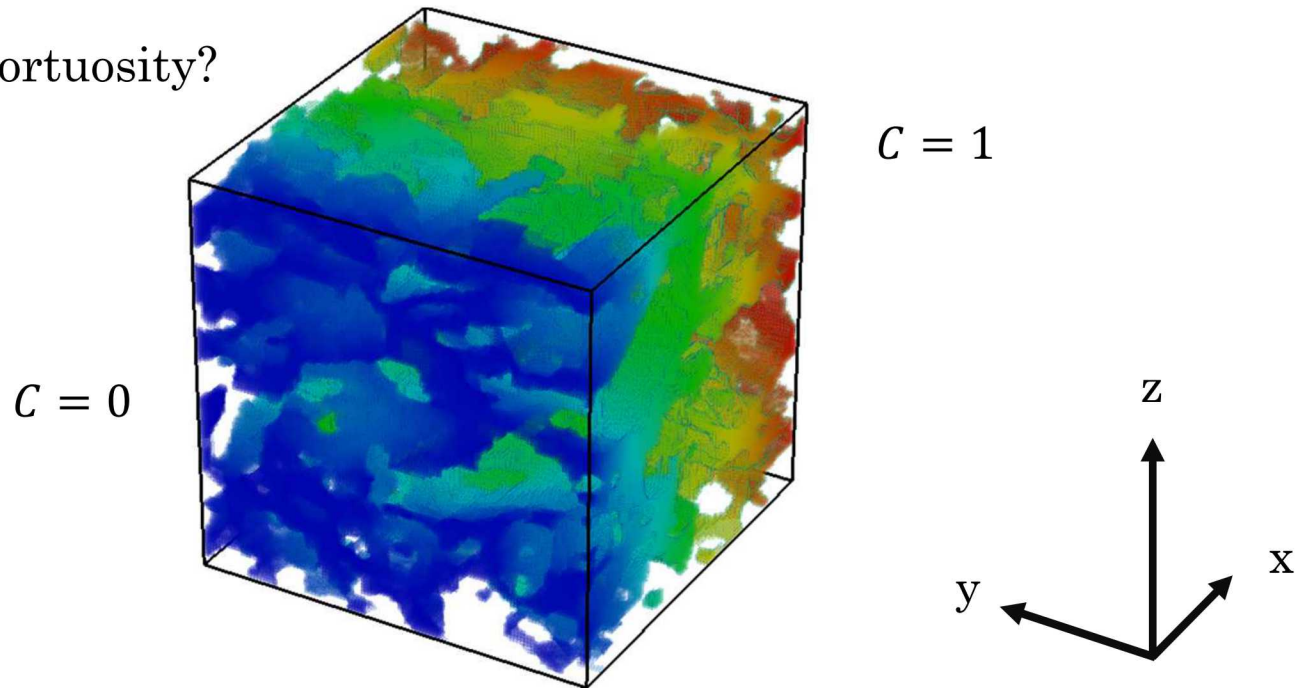
These structures can provide:

1. Porosity
2. Tortuosity
3. Conductivity
4. Surface Area



Methodology

Q. How to find tortuosity?



Tortuosity

$$\nabla^2 C = 0$$

Boundary Conditions

$$C(x = 0) = 0$$

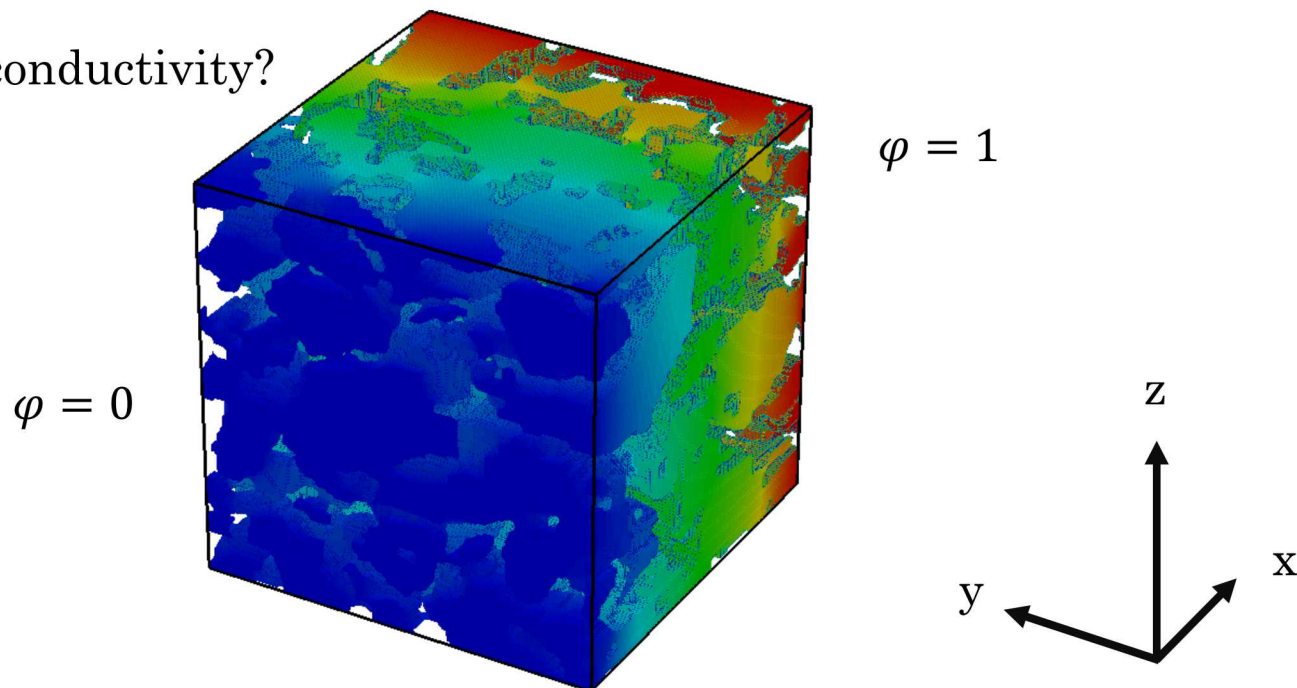
$$C(x = L_x) = 1$$

Four planes ($y=0$, $z=0$, $y=L_y$, $z=L_z$)

$$\frac{\partial C}{\partial n} = 0$$

Methodology

Q. How to find conductivity?



Conductivity

$$\nabla \cdot (\sigma \nabla \varphi) = 0$$

Boundary Conditions

$$\varphi(x = 0) = 0$$

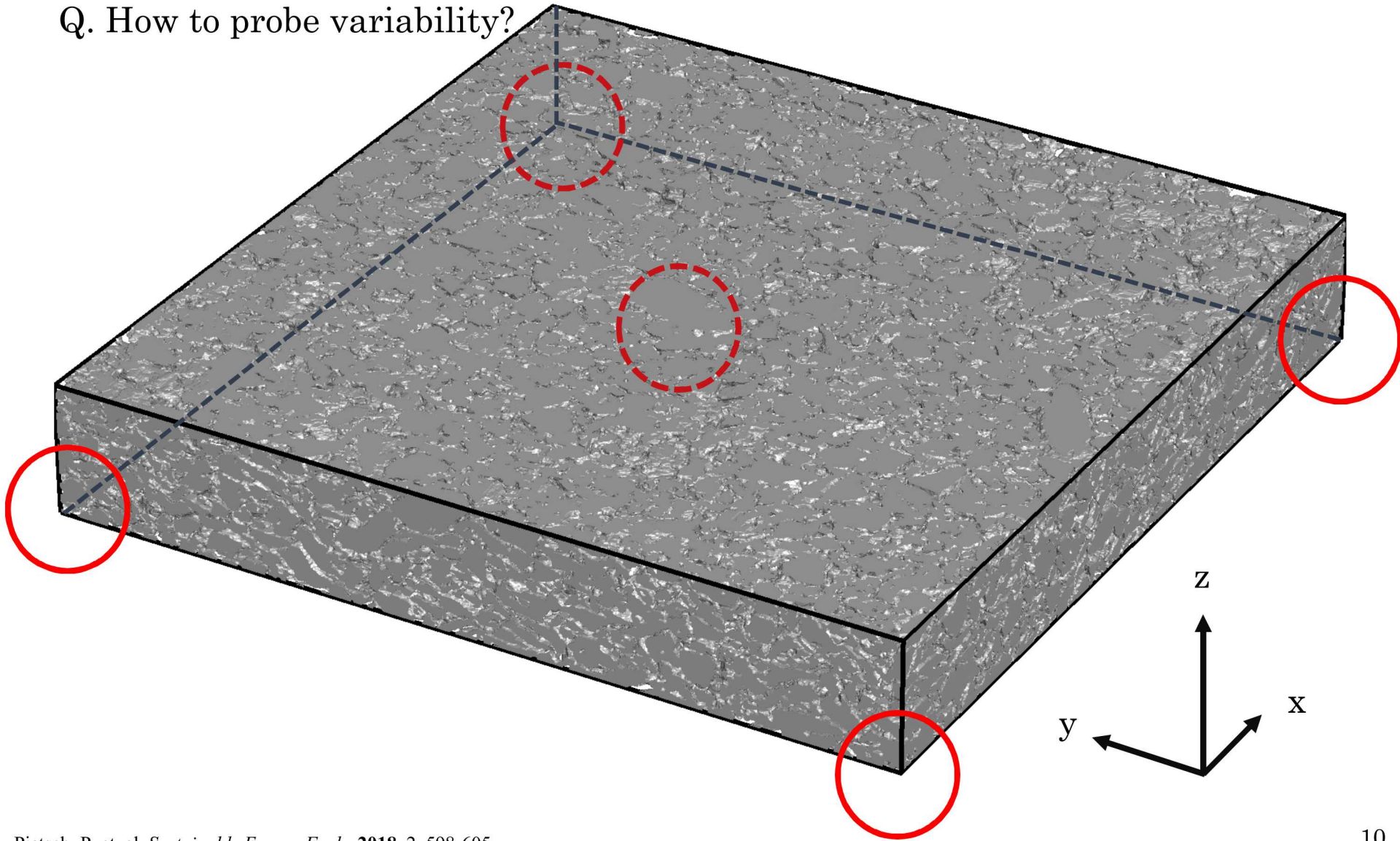
$$\varphi(x = L_x) = 1$$

Four planes ($y=0$, $z=0$, $y=L_y$, $z=L_z$)

$$\frac{\partial \varphi}{\partial n} = 0$$

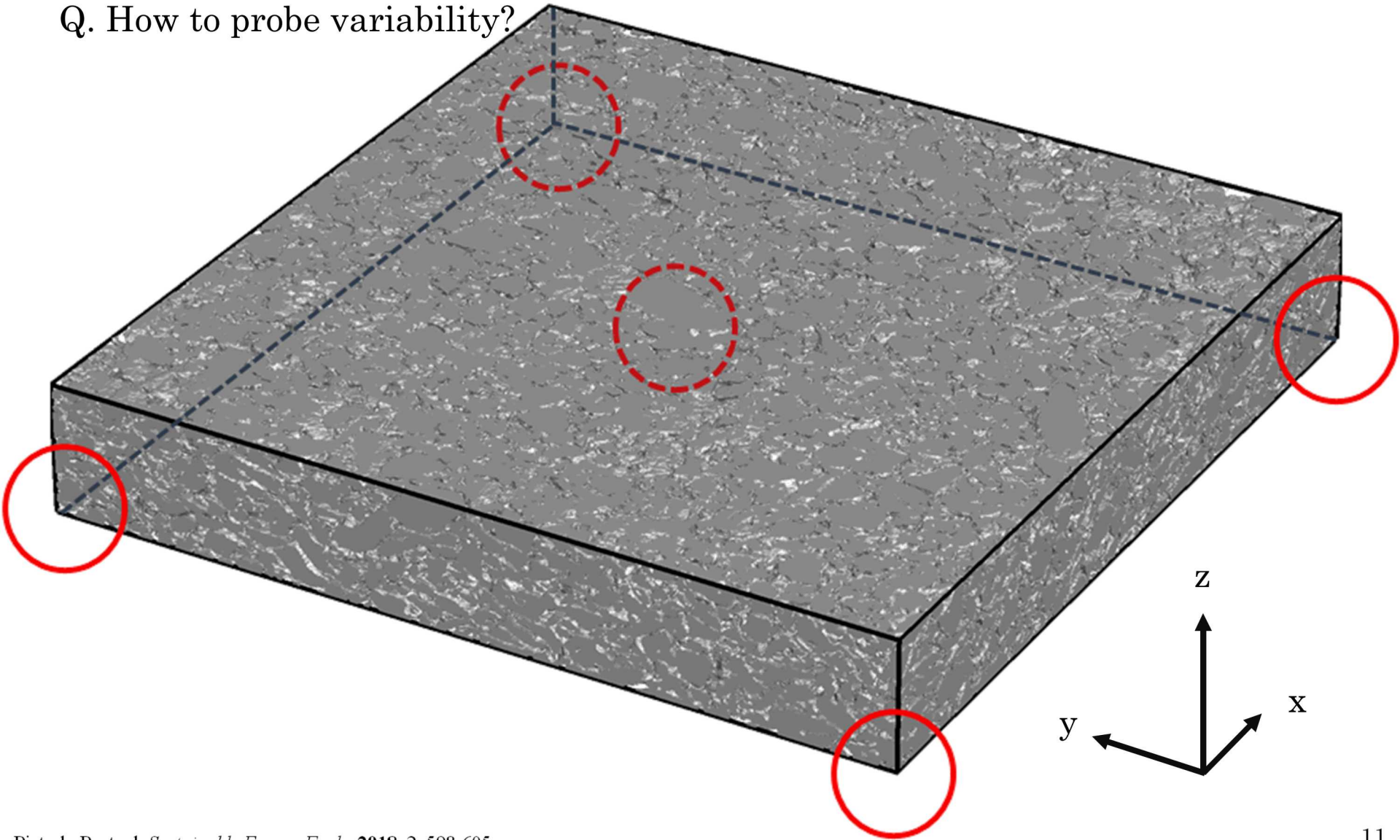
Methodology

Q. How to probe variability?

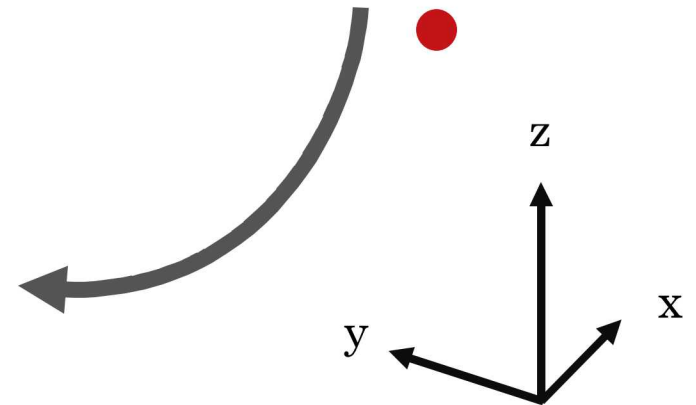
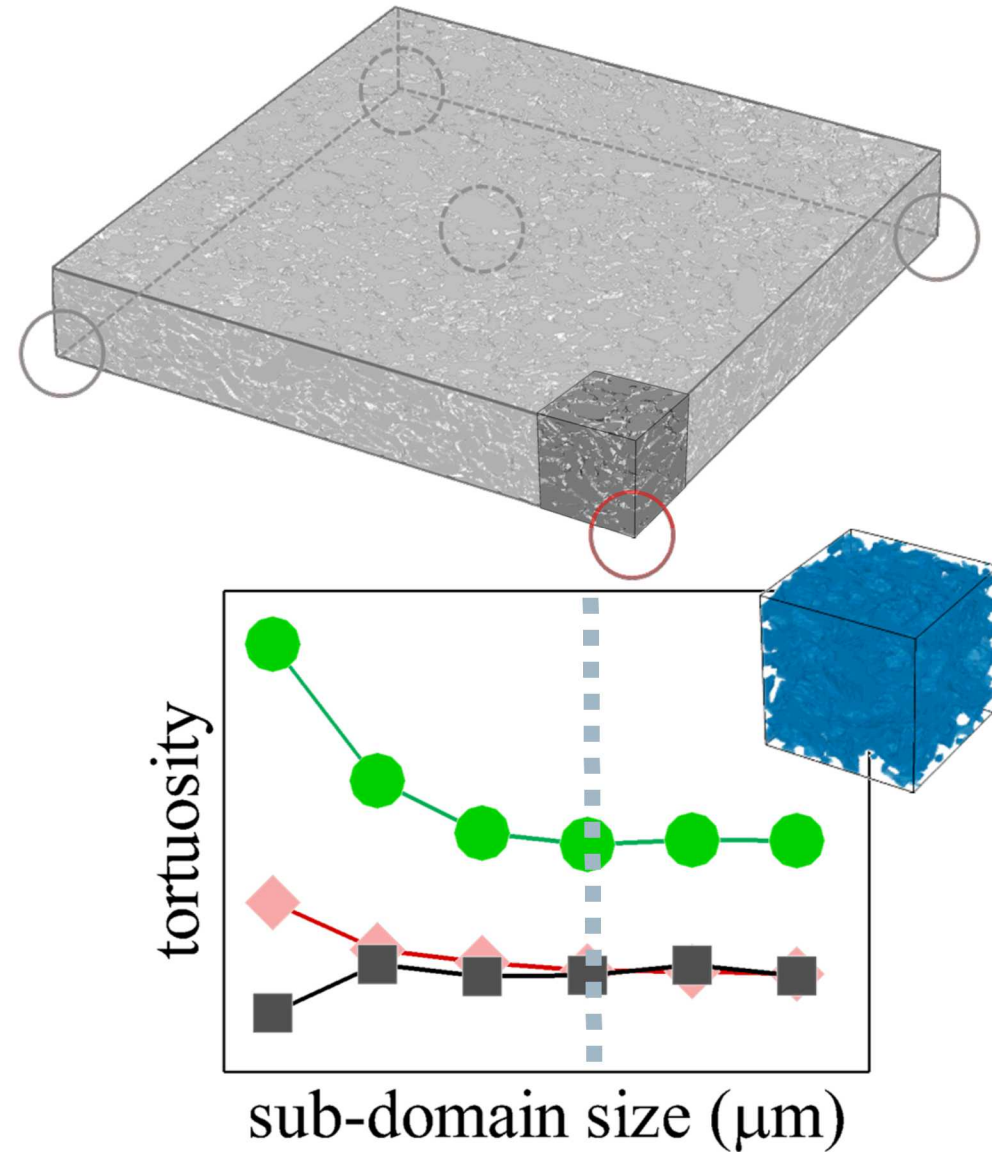


Methodology

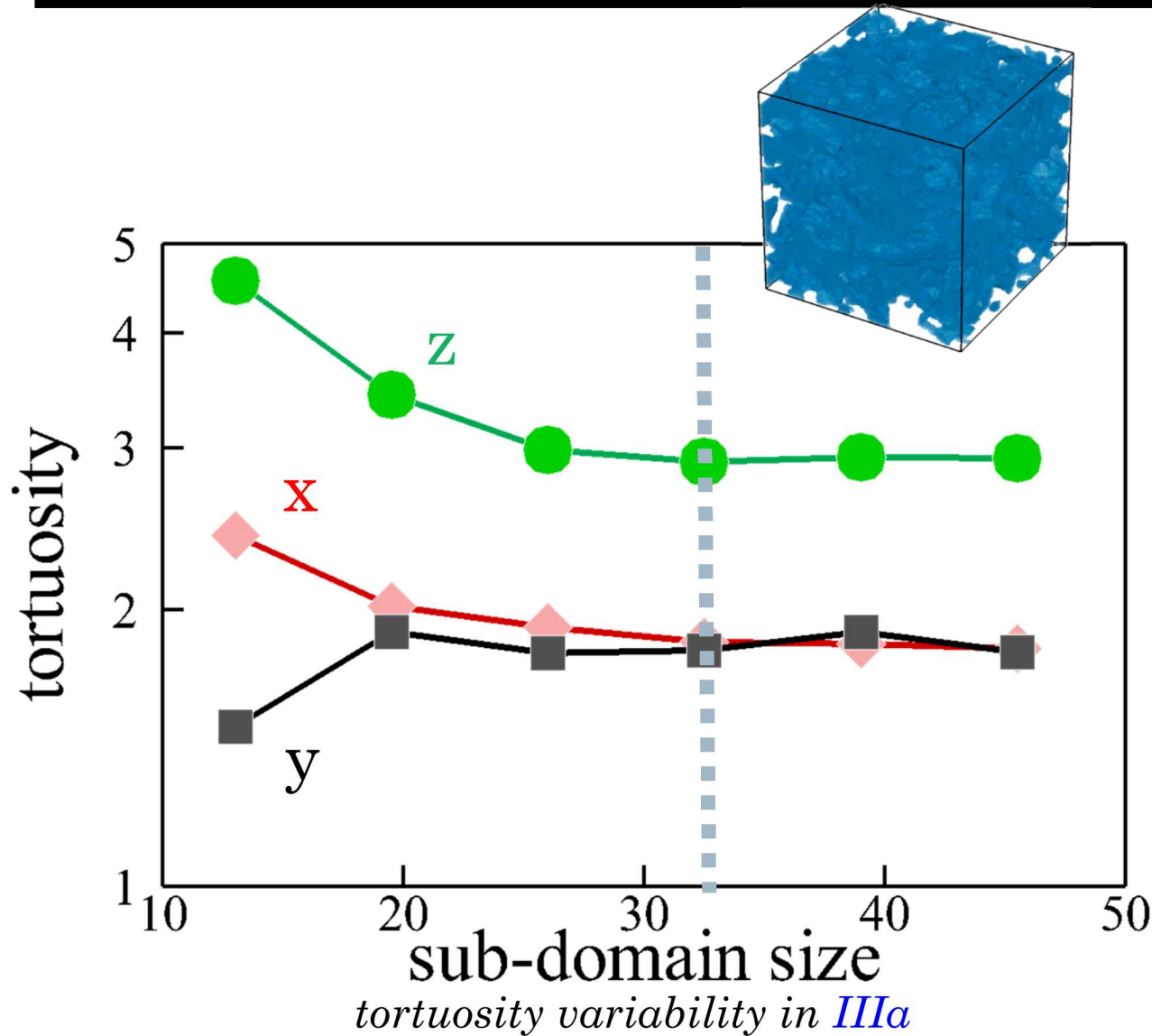
Q. How to probe variability?



Methodology



Methodology



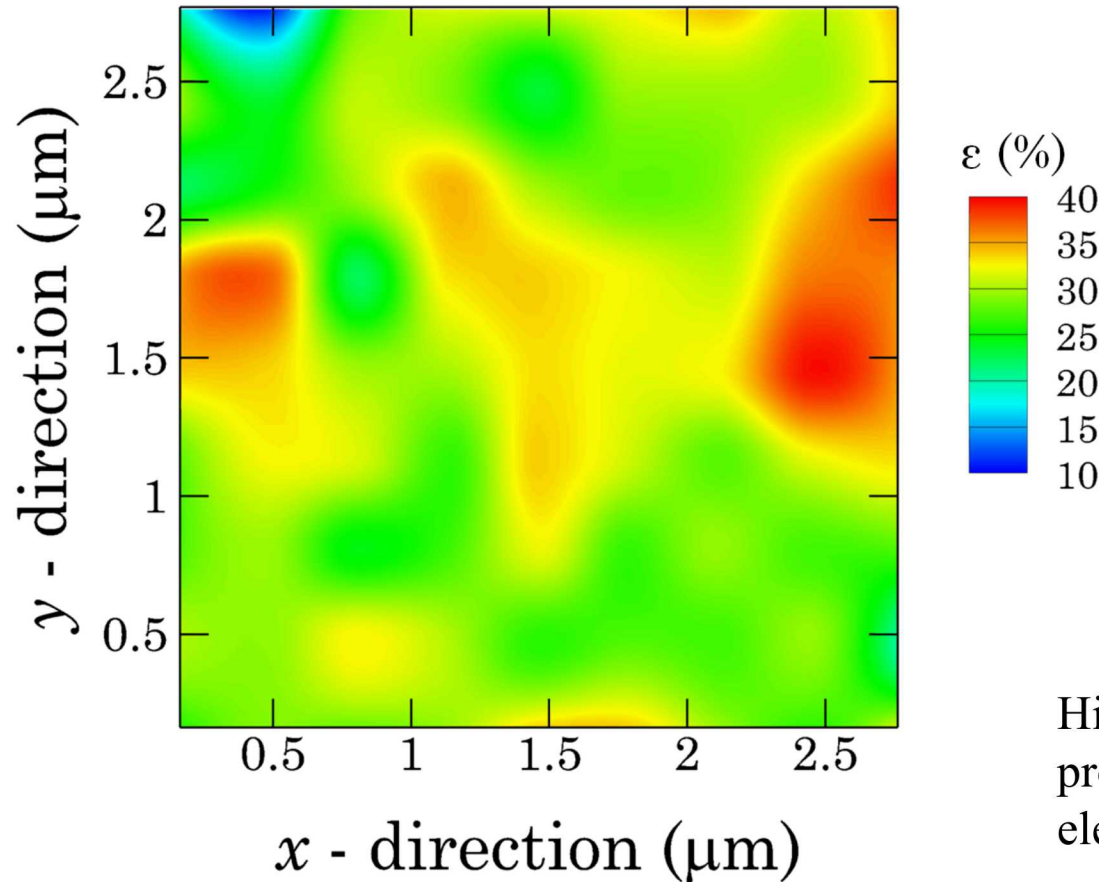
Visual convergence of values as sub-domain size increases.

Choosing the smallest value where visual convergence occurs among all nodes.

This value can then be used to probe spatial variability.

Variability Within an Electrode

Q. How can variability be quantified?

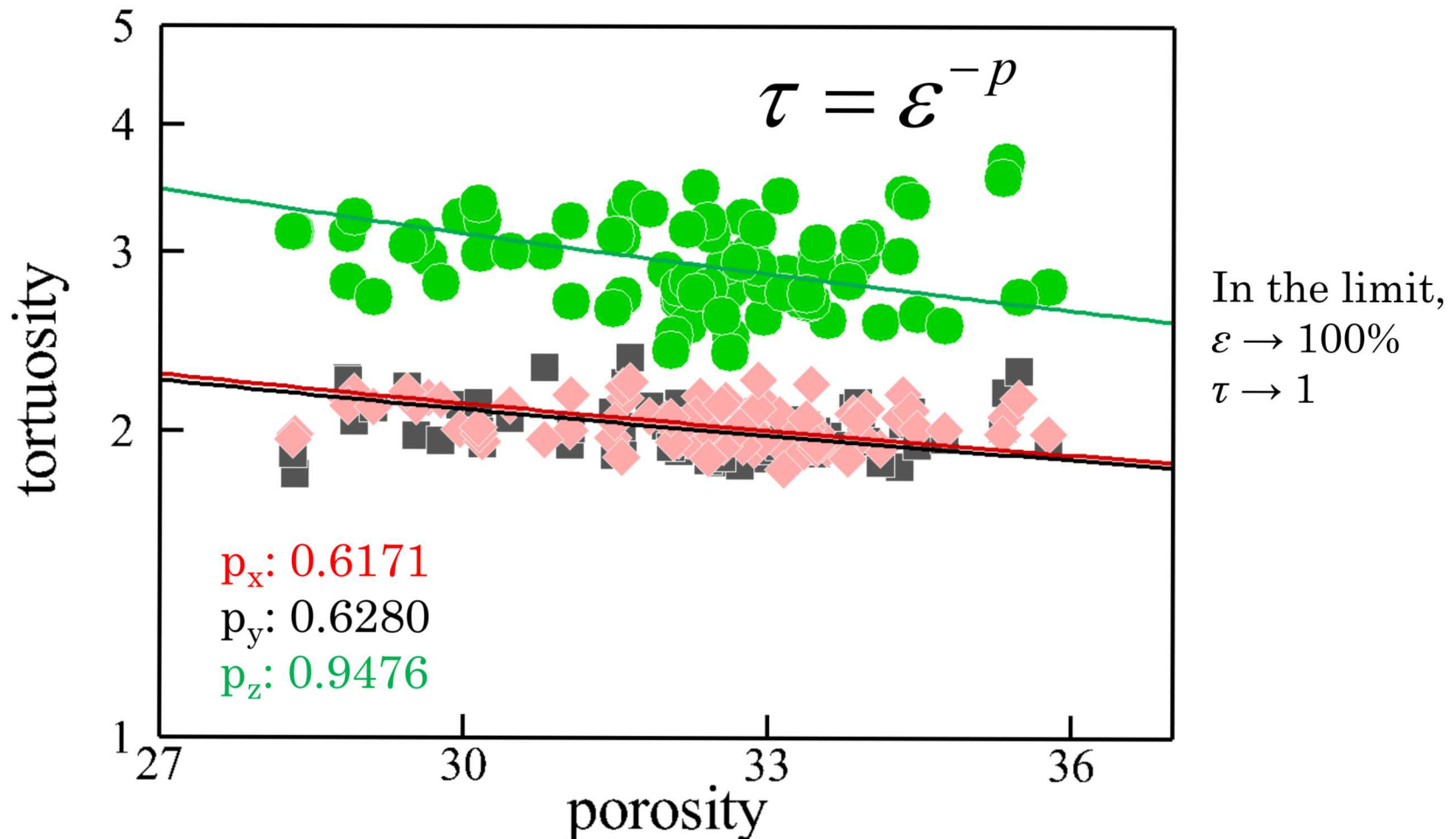


Higher local regions of effective properties can be seen in every electrode.

Porosity (%) variation in electrode Ib

Variability Within an Electrode

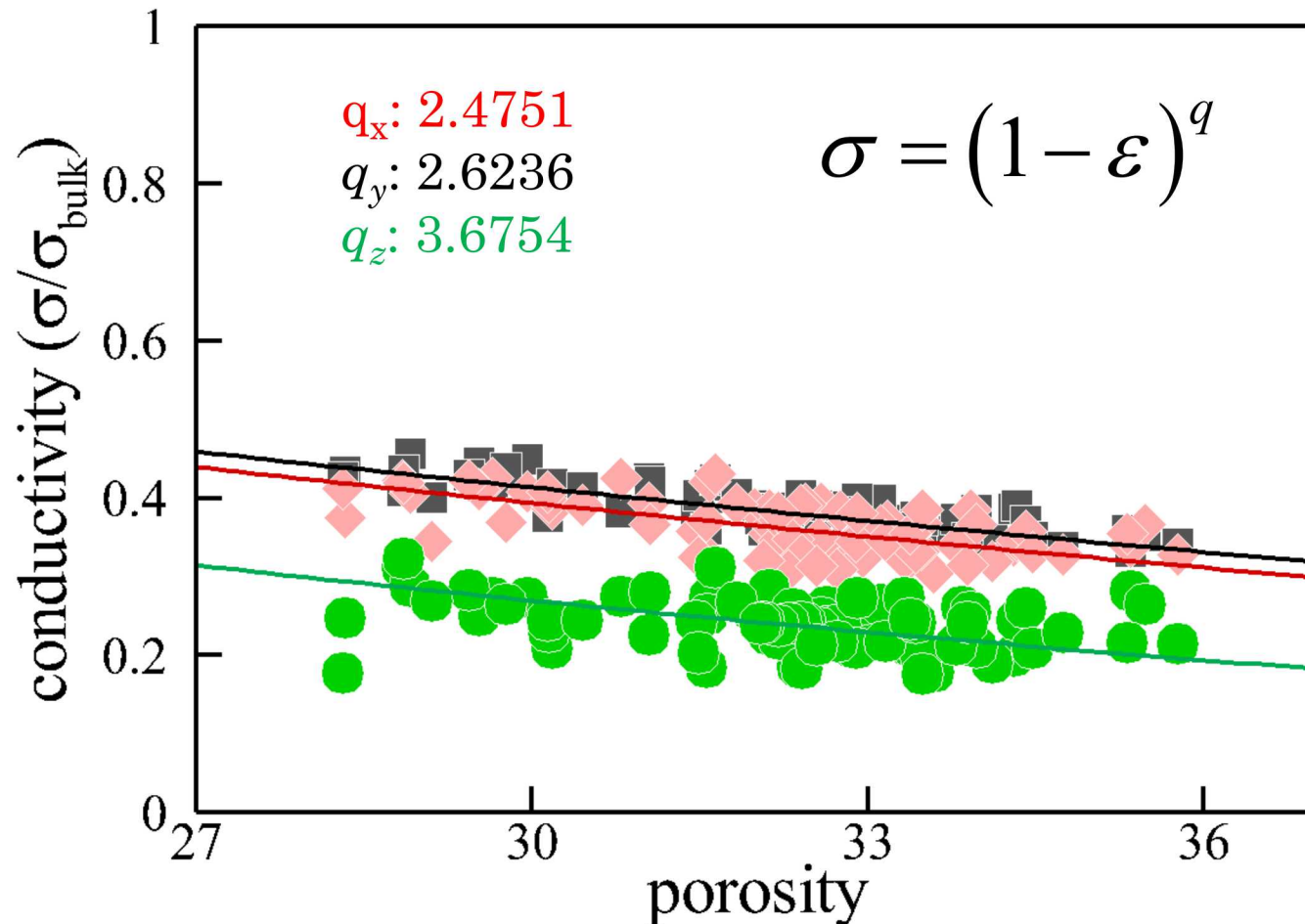
Q. How can variability be quantified?



*tortuosity variability in *IIc**

Variability Within an Electrode

Q. How can variability be quantified?



In the limit,

$\varepsilon \rightarrow 0\%$

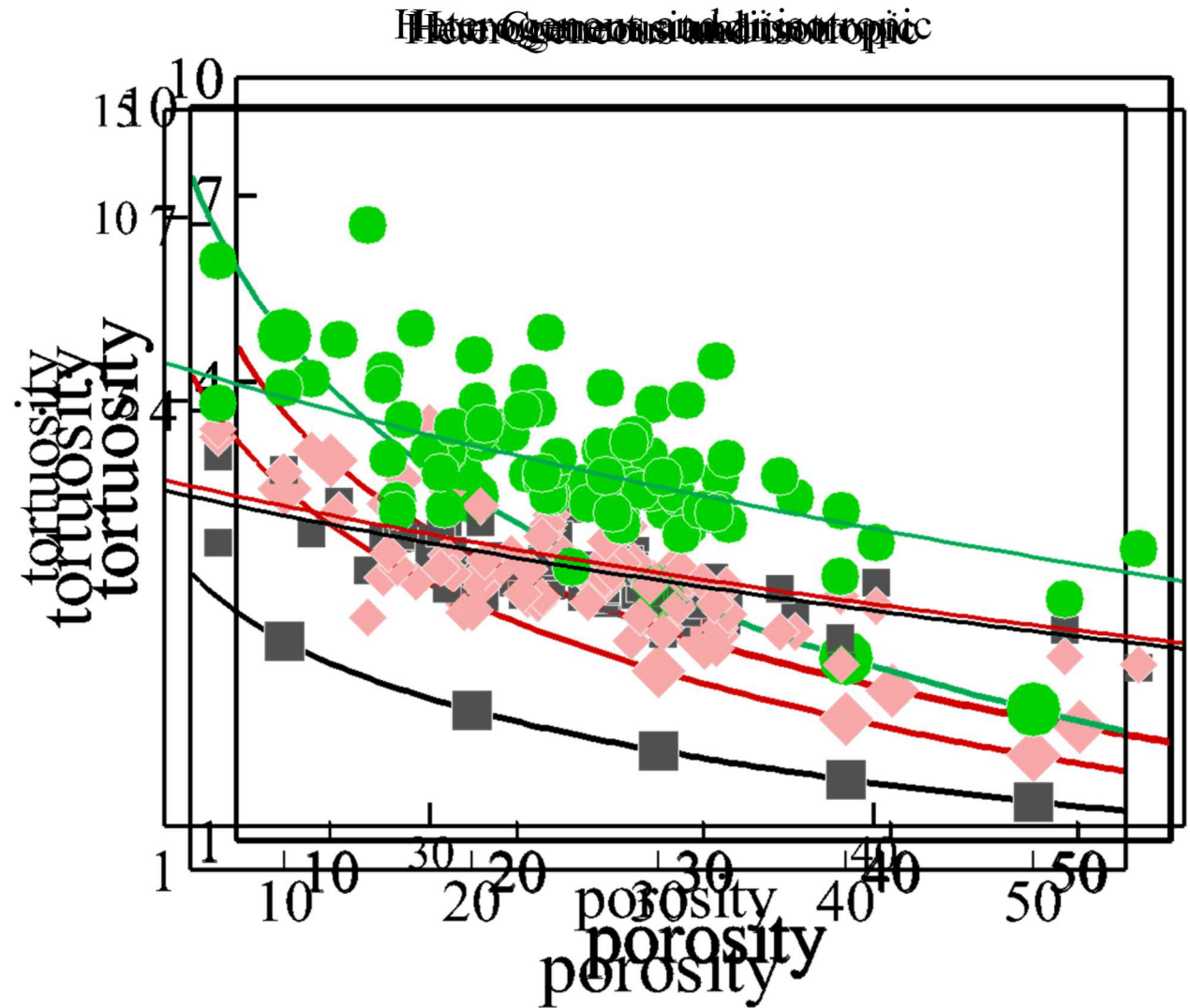
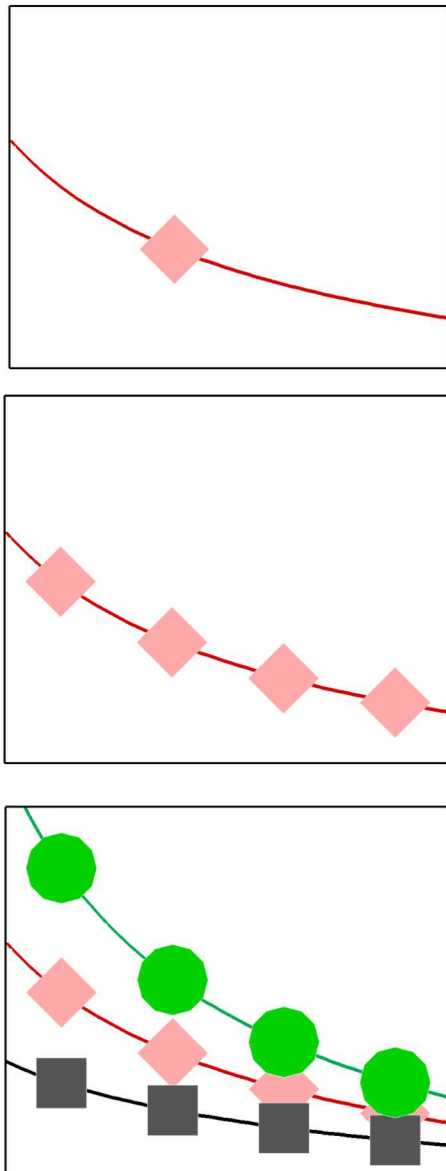
$\sigma/\sigma_{\text{bulk}} \rightarrow 1$

$\varepsilon \rightarrow 100\%$

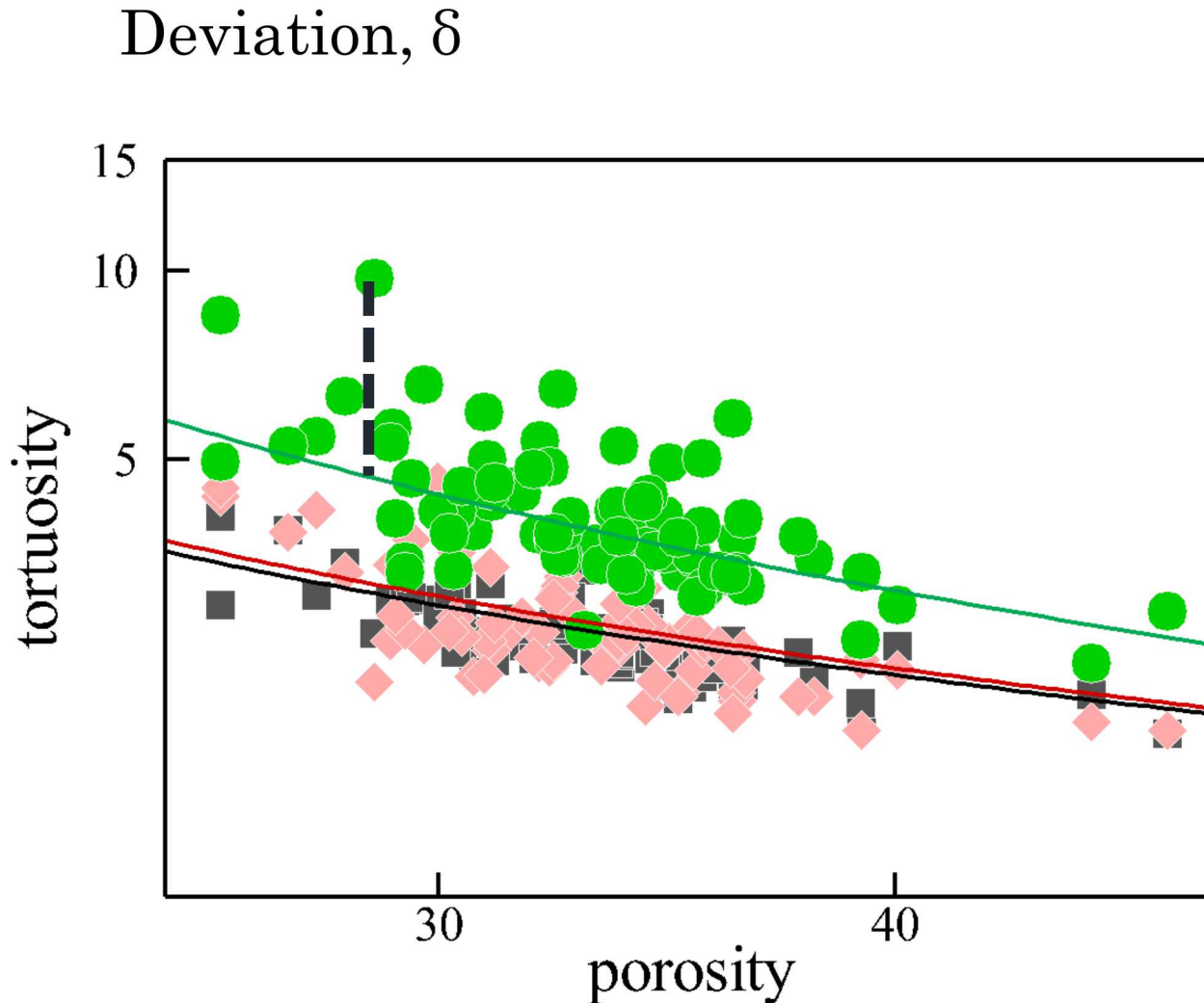
$\sigma/\sigma_{\text{bulk}} \rightarrow 0$

conductivity variability in Ilc

Variability Within an Electrode



Variability Within an Electrode



Individual δ values for each point

$$\delta_{\tau} = \frac{\tau_{measured} - \tau_{fitted}}{\tau_{fitted}}$$

These normalized points now act as another data point

This can be seen as the internal RVE variability.

tortuosity variability in I_c

Particle Characterization

By implementing a 3D Sobel operator we can apply this to three dimensions for our particles.

1	2	1
2	4	2
1	2	1

$$h_z(:, :, -1)$$

0	0	0
0	0	0
0	0	0

$$h_z(:, :, 0)$$

-1	-2	-1
-2	-4	-2
-1	-2	-1

$$h_z(:, :, 1)$$

$$G_z = h_z * I$$

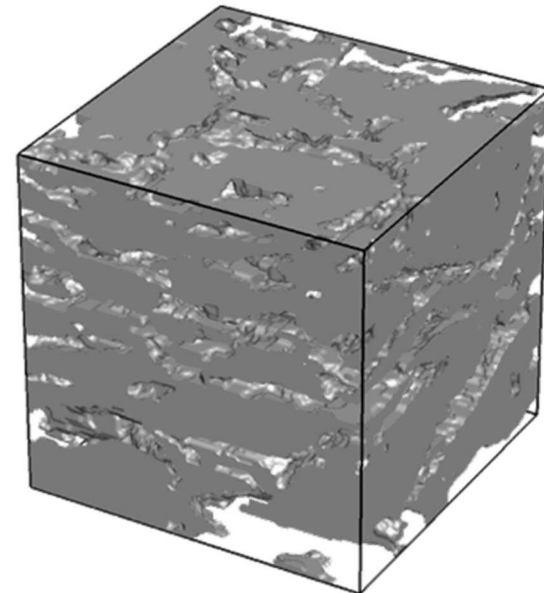
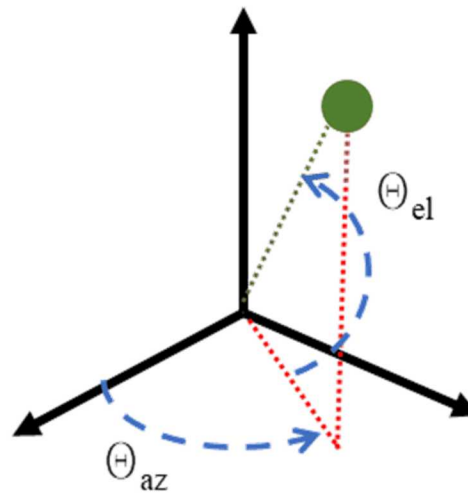
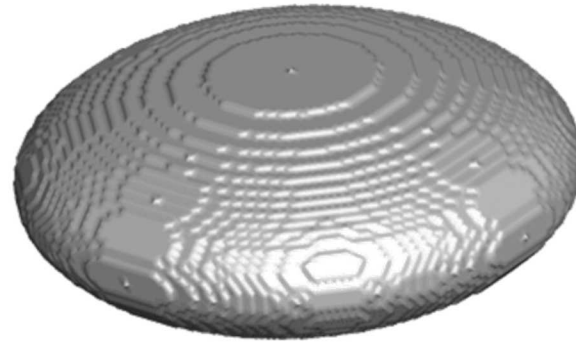
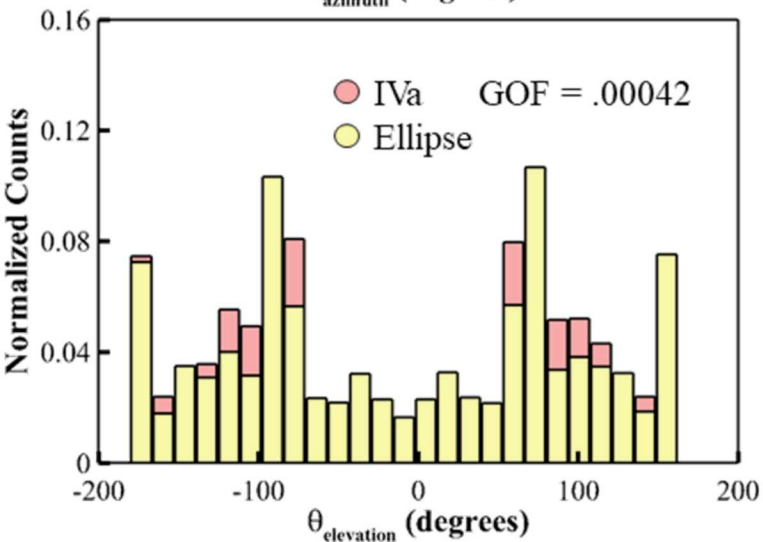
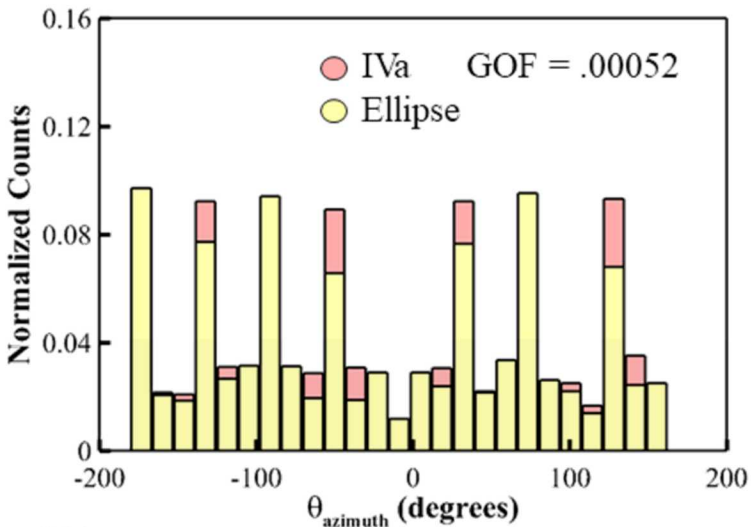
$$G_{mag} = \sqrt{G_y^2 + G_x^2 + G_z^2}$$

$$\phi = \arctan\left(\frac{G_z}{\sqrt{G_x^2 + G_y^2}}\right)$$

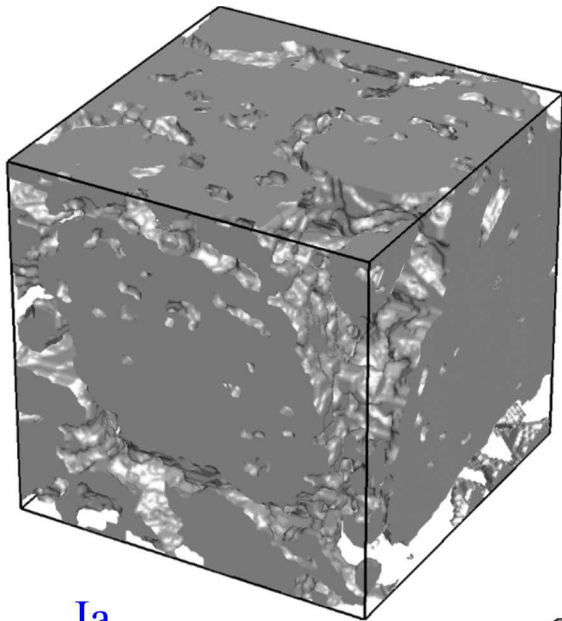
$$\theta = \arctan\left(\frac{G_y}{G_x}\right)$$

Particle Characterization

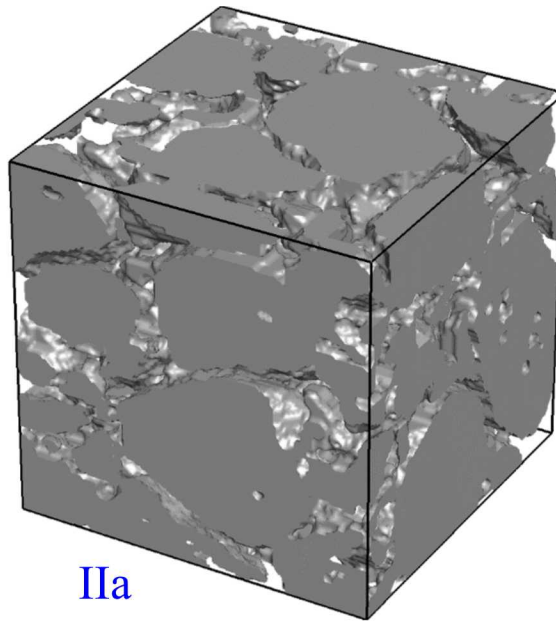
By varying ellipsoid parameters we can find reference particles to help describe the electrode.



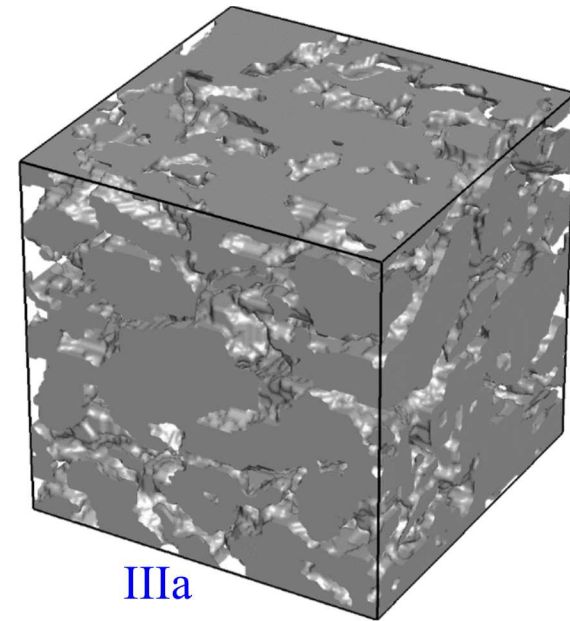
Particle Morphology Effects



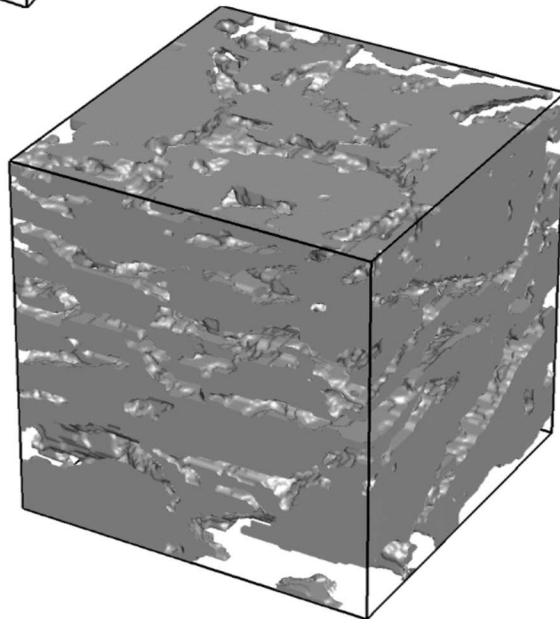
Ia



IIa



IIIa

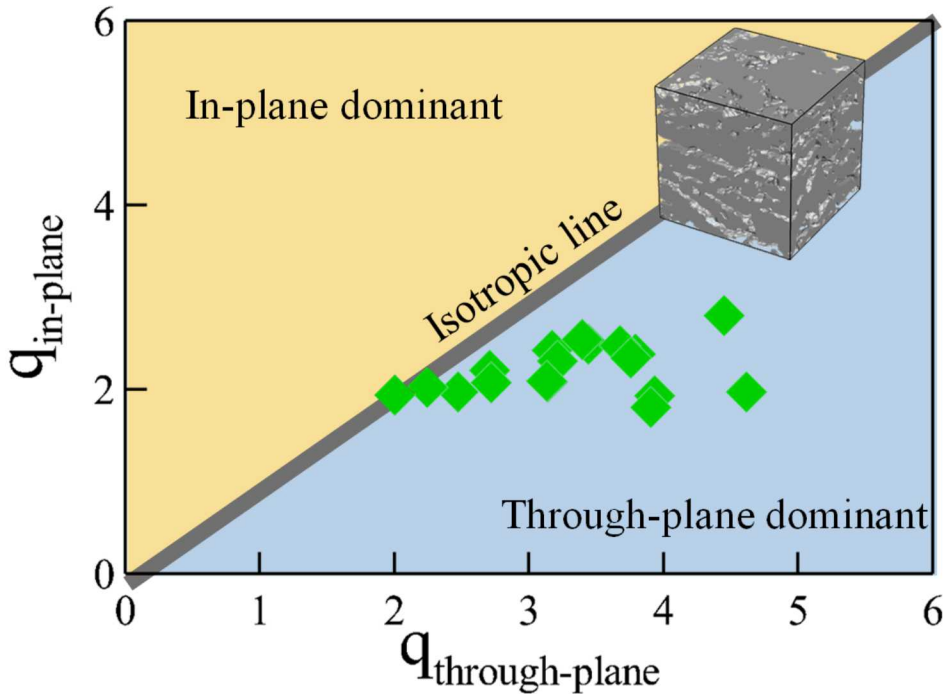


IVa

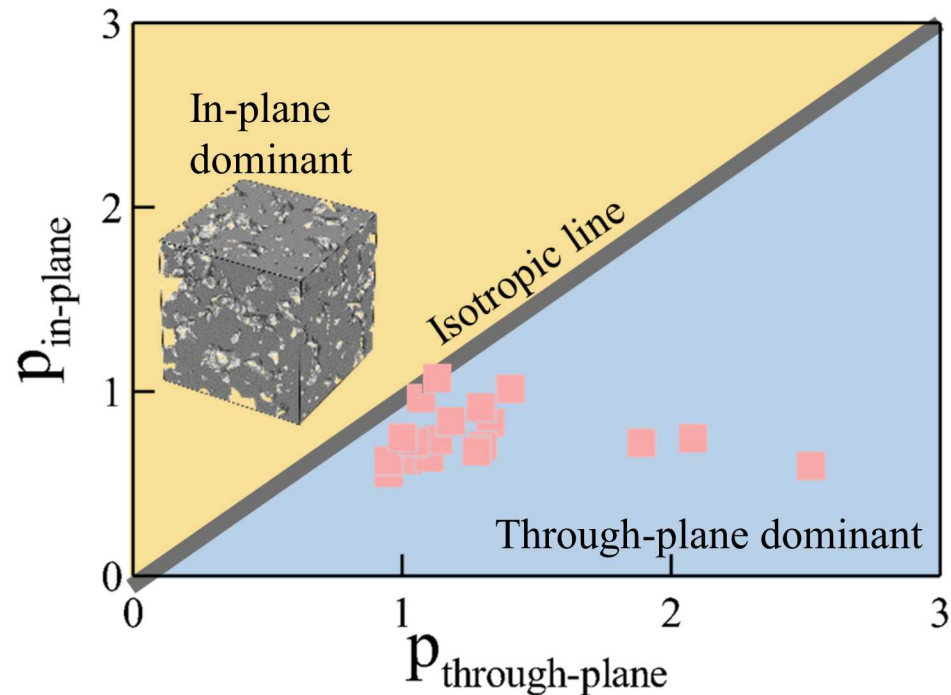
Q. How does differing morphologies influence effective properties?

Particle Morphology Effects

$$\sigma = (1 - \epsilon)^q$$



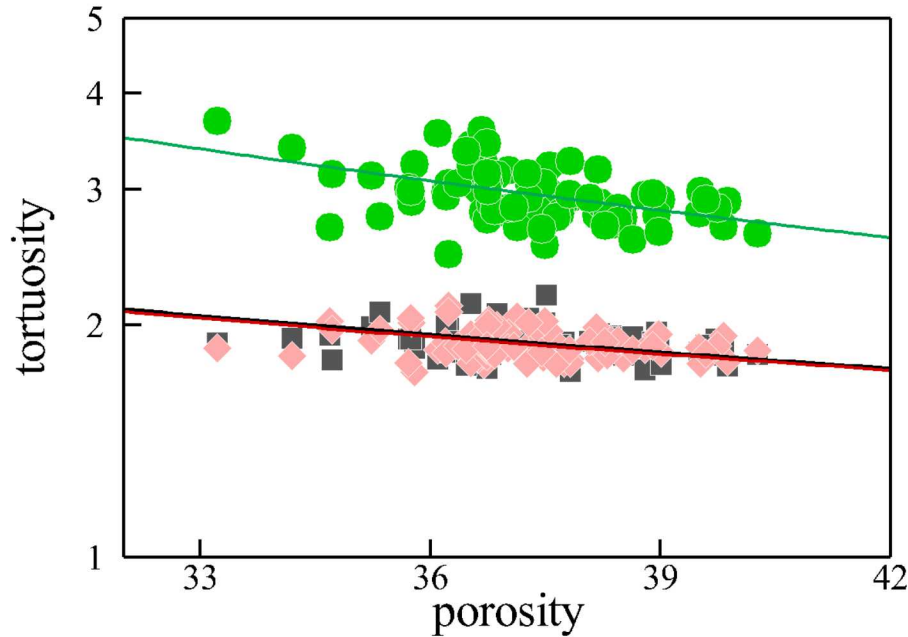
$$\tau = \epsilon^{-p}$$



Many electrodes show varying degrees of anisotropies

Particle Morphology Effects

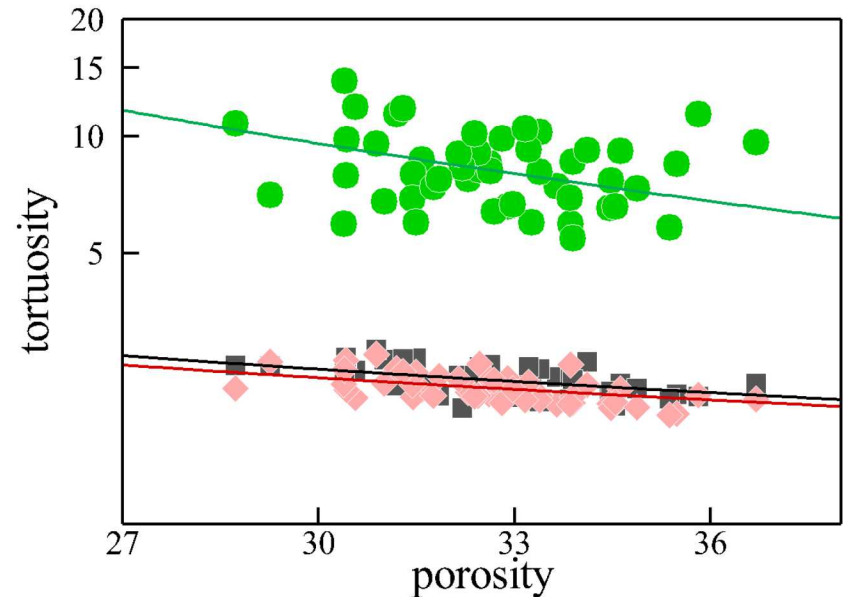
Q. What causes these variations in delta?



tortuosity variability in IIIa

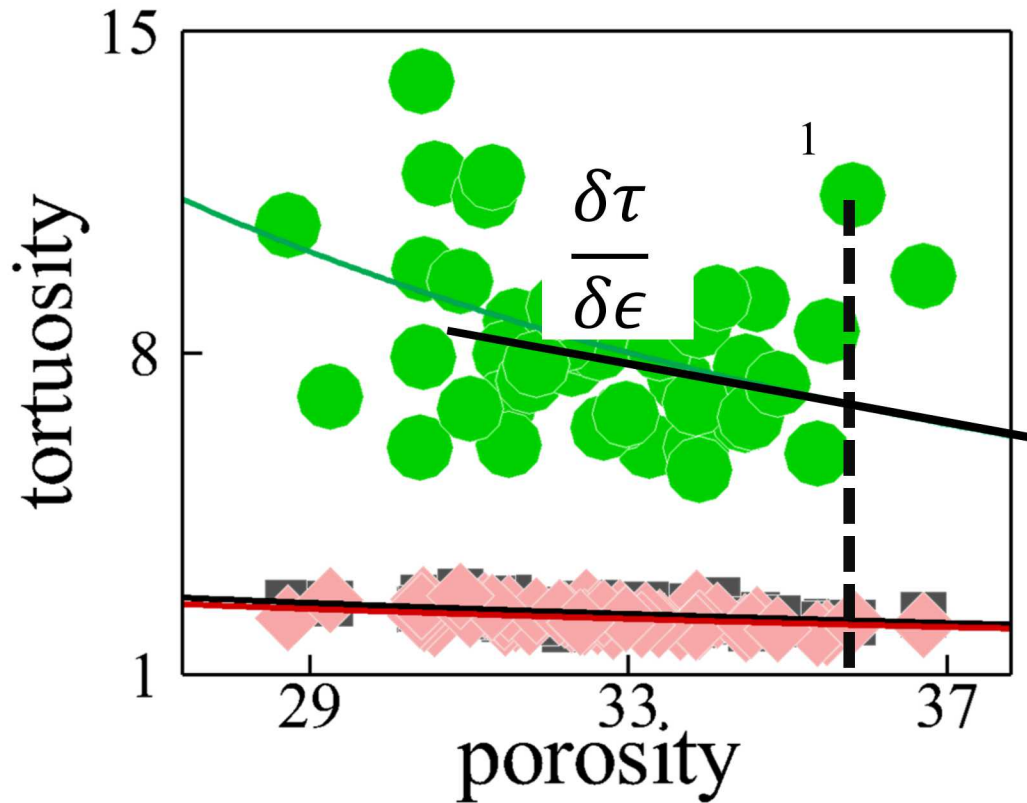
A directional correlation and proportionality to $\frac{dZ}{d\epsilon}$ is observed.

Electrode	$\overline{\delta_{\tau x}}$	$\overline{\delta_{\tau y}}$	$\overline{\delta_{\tau z}}$
IIIc	0.0331	0.0331	0.0543
IVb	0.0586	0.0602	0.1812



tortuosity variability in IVb

Particle Morphology Effects



$\frac{\delta\tau}{\delta\epsilon}$ represents the slope of the tortuosity at a given porosity value of the designated curve.

$$\tau = \epsilon^{-p}$$

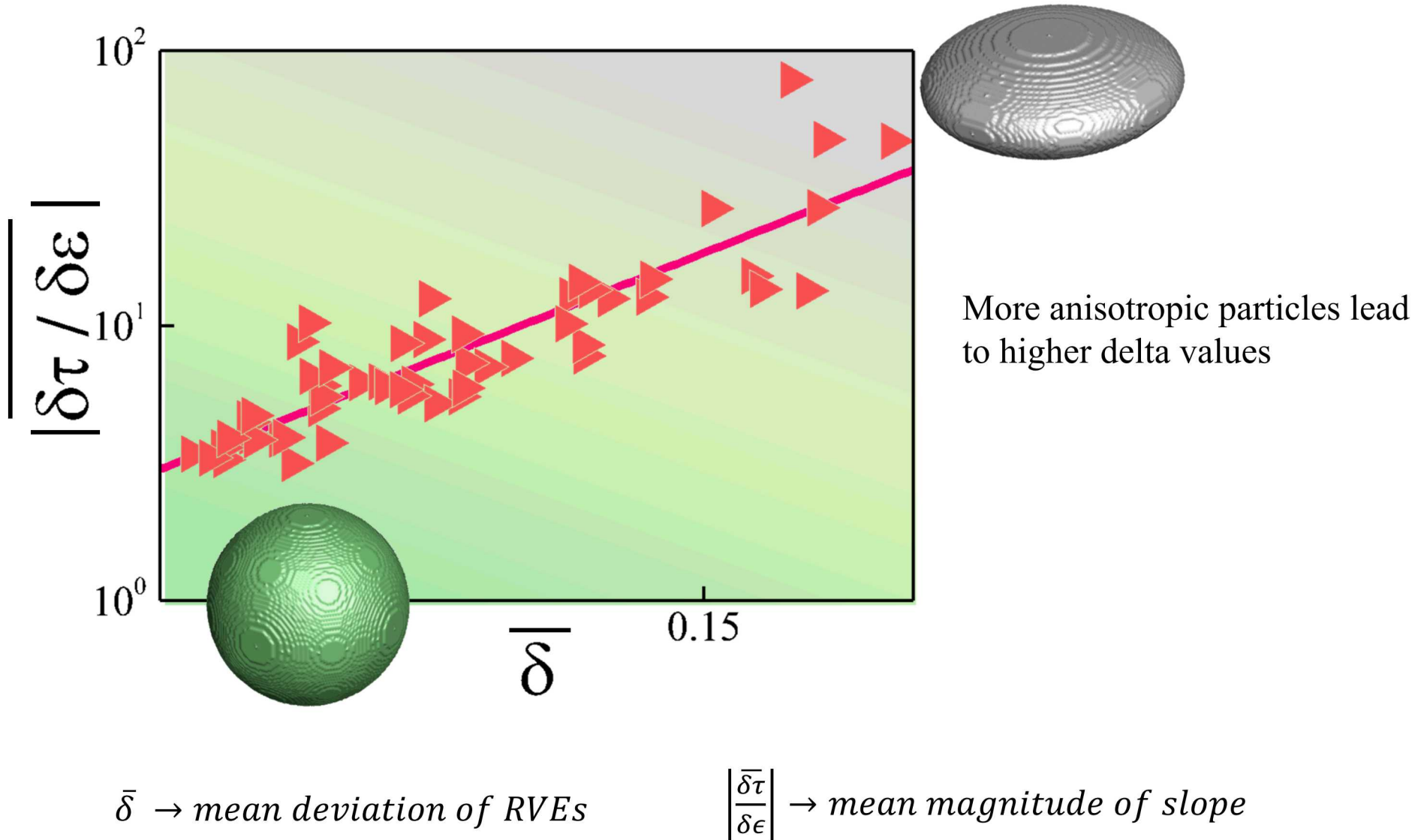
$\tau \rightarrow$ tortuosity

$\epsilon \rightarrow$ porosity

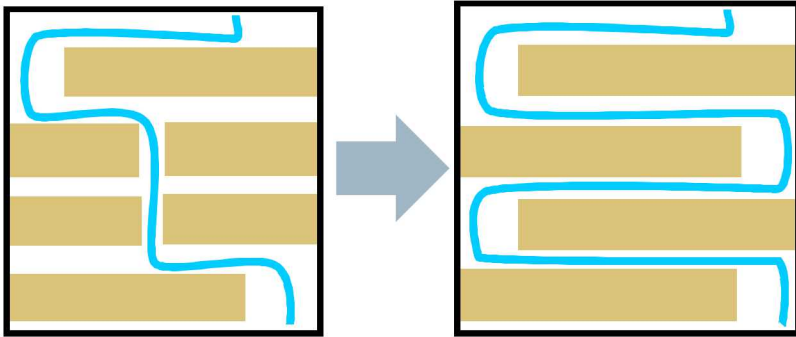
$$\frac{\delta\tau}{\delta\epsilon} = -p\epsilon^{-p-1}$$

$p \rightarrow$ exponential to curve fit

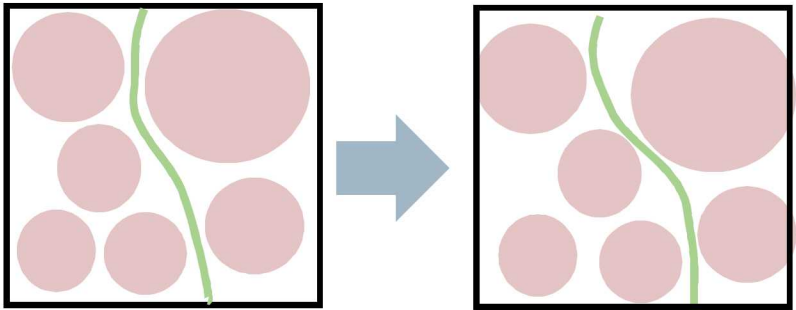
Particle Morphology Effects



Particle Morphology Effects

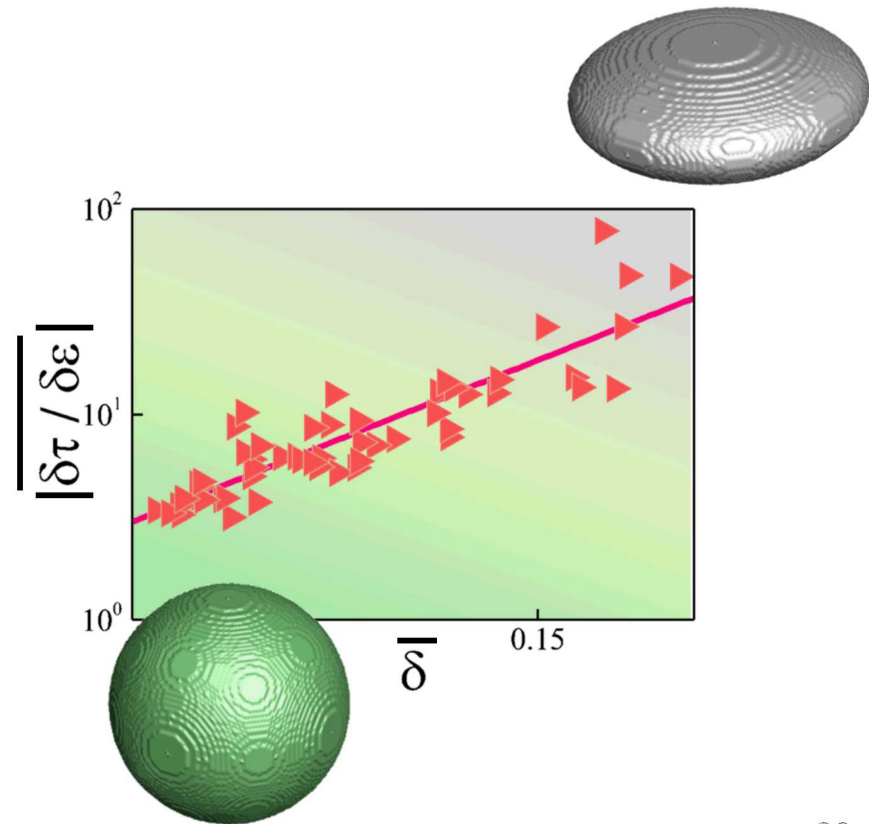


The sensitive nature of the platelet like particles is mirrored in the delta reliance plot (below).



Porosity is held constant in every case.

- With small changes in particle locations large tortuosity changes are seen.



Conclusion

- Successful screening method that can compare a multitude of morphologies without segmenting particles.
- Many morphologies exhibit anisotropy given varying morphologies.
- Internal RVE tortuous dispersion can arise from particle morphology where as conductivity does not show the same.

Acknowledgements

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Scott Roberts and team



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Thank You!