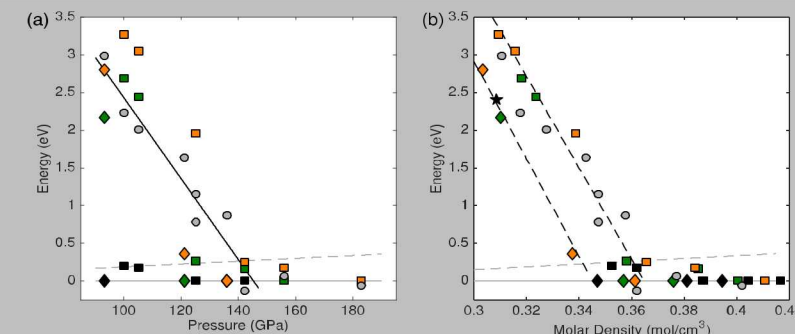
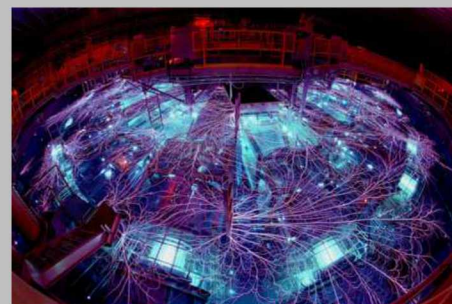
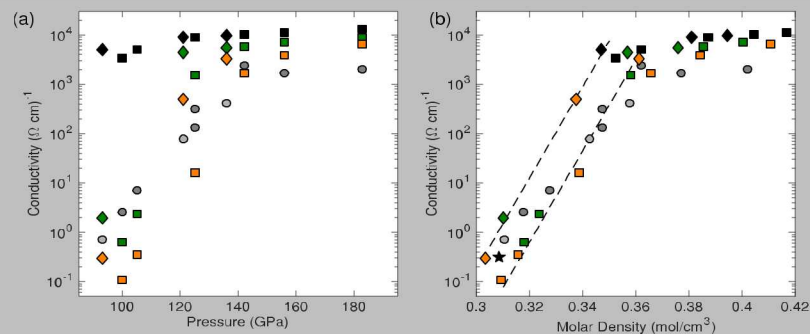




First-principles calculations of multiple-shock conductivity measurements in hydrogen and deuterium

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SAND2019 -

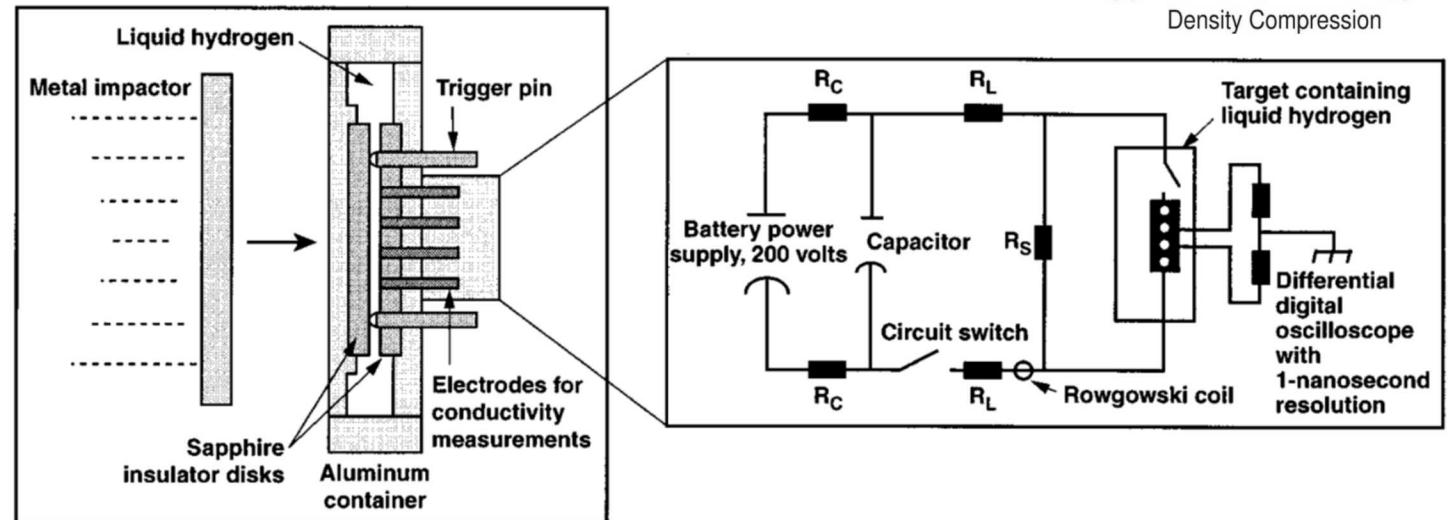
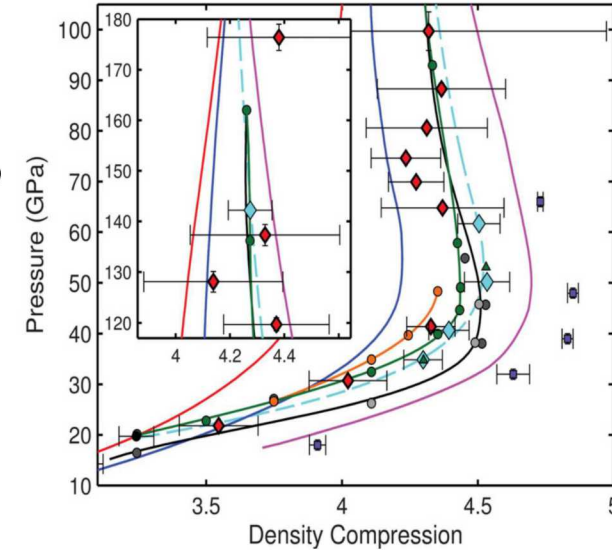
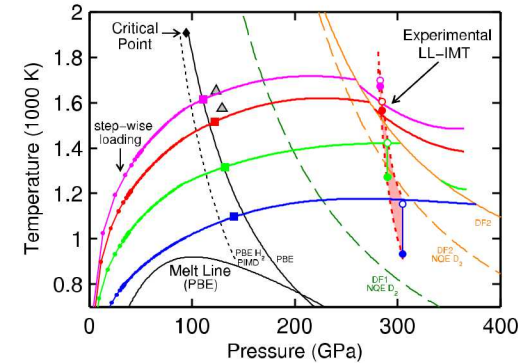
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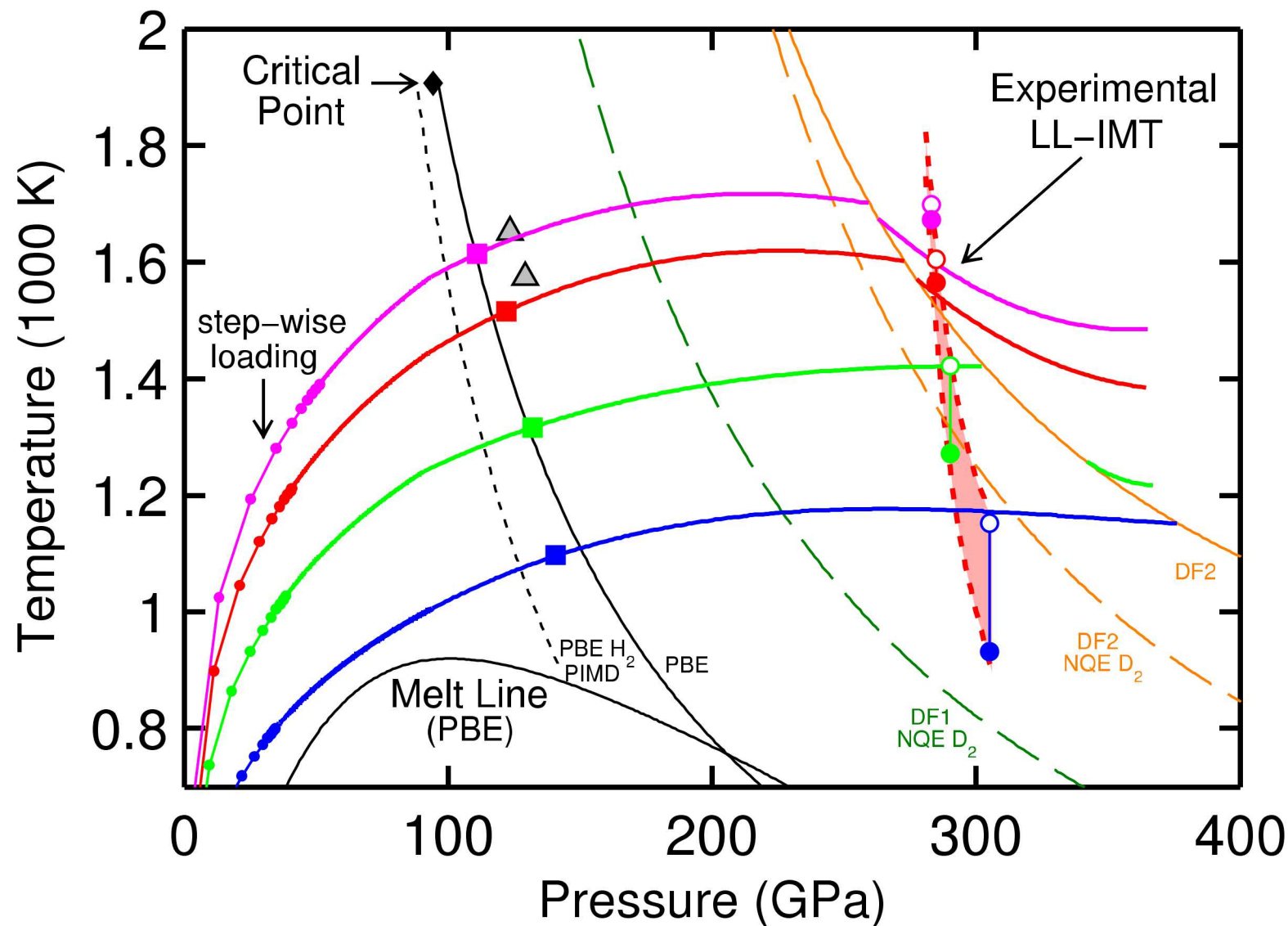
Outline

- Motivation
 - Insulator-metal transition at high- ρ and low- T
 - Insulator-metal transition at low- ρ and high- T
- Reanalysis of multiple-shock conductivity (σ) measurements
 - Original study included inconsistencies in both the inferred T and fit to the semiconductor model used to interpret the measured σ
- Comparison of conductivity with various exchange-correlation (xc) functionals
 - PBE
 - vdW-DF1
 - vdW-DF2
- Conclusions



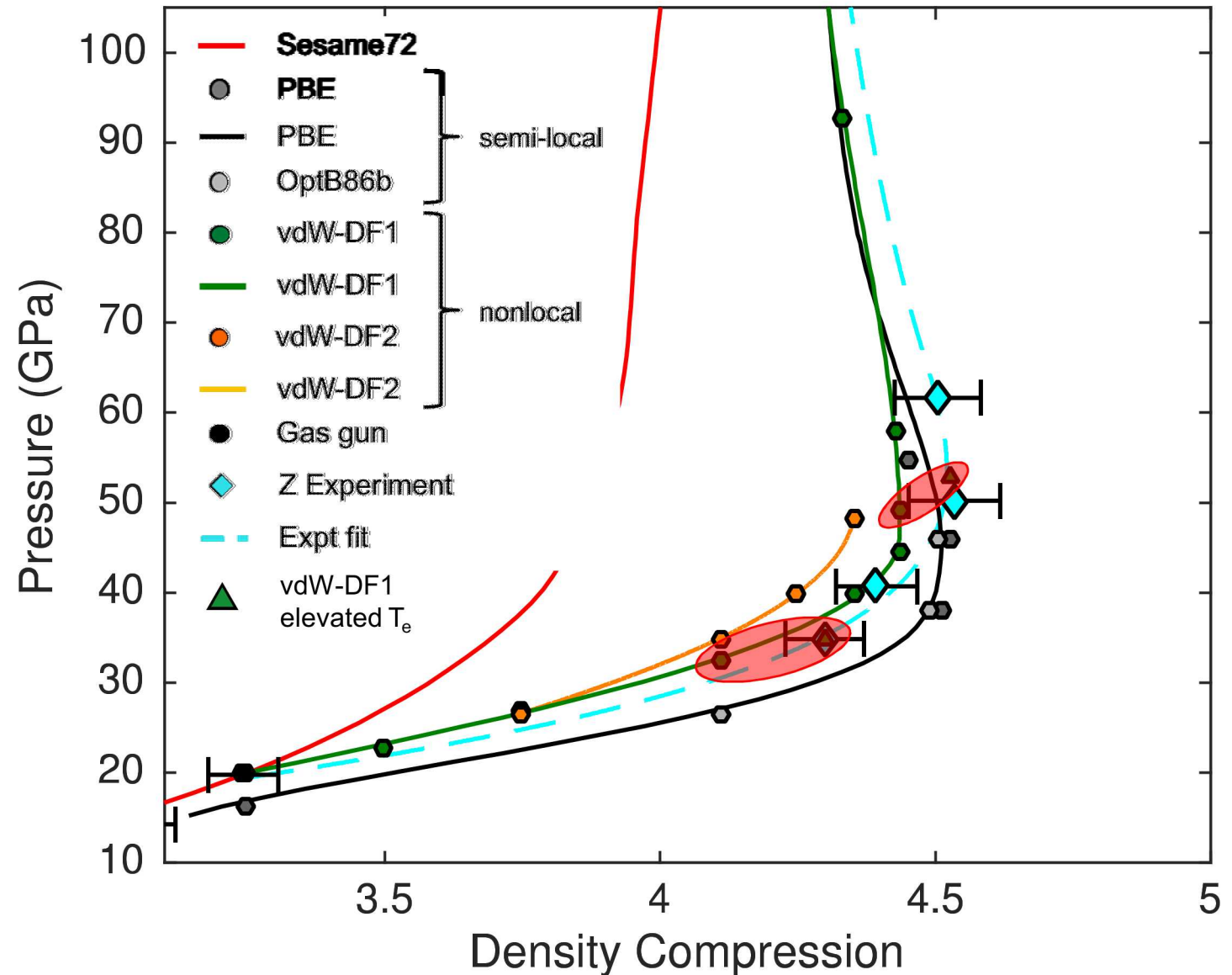
Insulator-metal transition at high- ρ and low- T

- Shock-ramp technique enabled experimental access to liquid-liquid, insulator-metal transition (LL-IMT)
- Experiments above ~ 250 GPa show clear evidence of metallization of deuterium
- Best agreement with nonlocal xc functionals
 - More complex T -dependence
- Not consistent with semi-local xc functional PBE
 - Dissociation occurs at much too low P



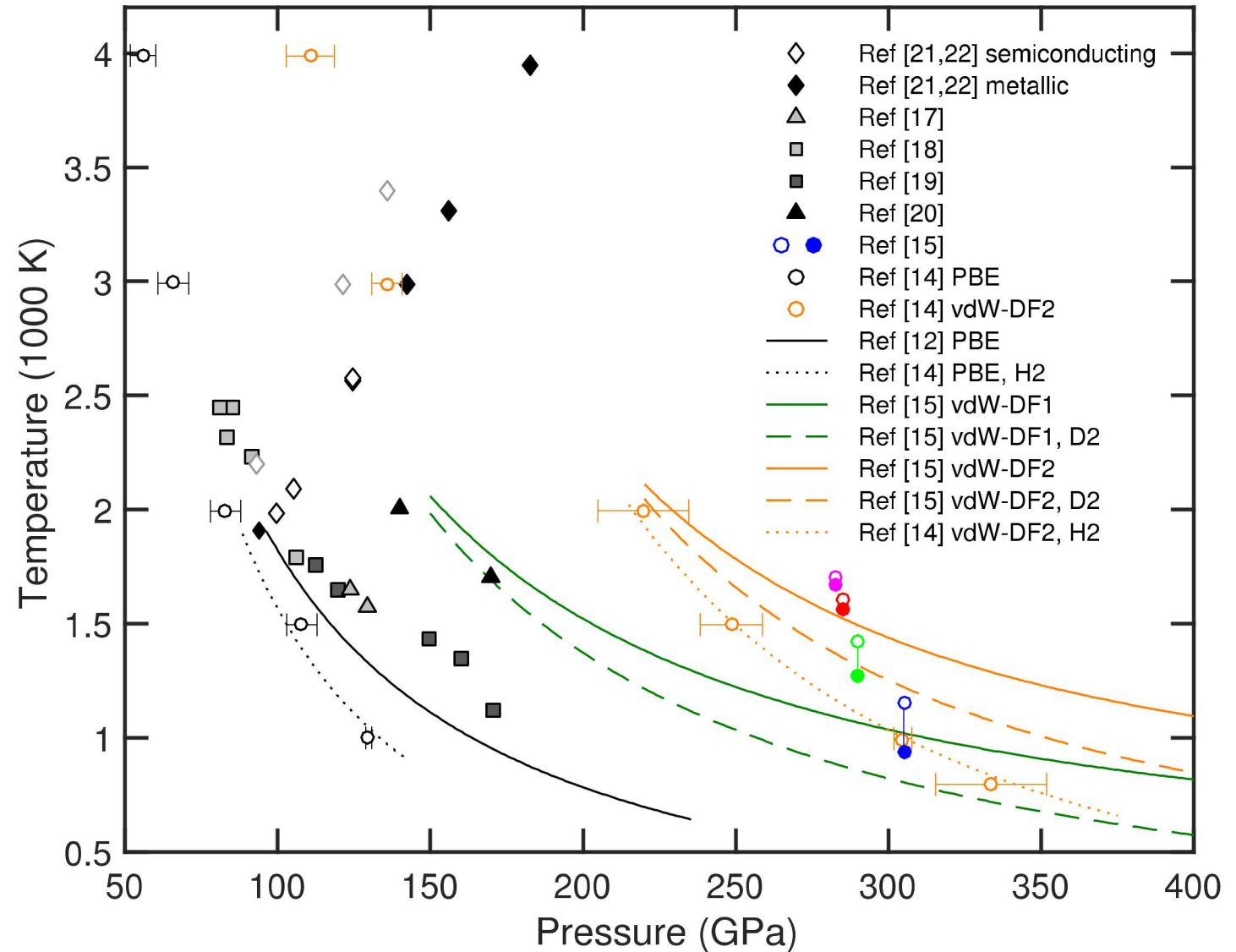
Insulator-metal transition at low- ρ and high- T

- Recent precision measurements of the deuterium Hugoniot near the IMT
 - Provides unique insight into the dissociation process
- Results compared with various xc functionals
 - Nonlocal functionals better describe the onset of dissociation
 - These same functionals exhibit a significantly wider P range for dissociation to complete
- Provide means for evaluation of future theoretical developments and new xc functionals



Insulator-metal transition at intermediate ρ and T

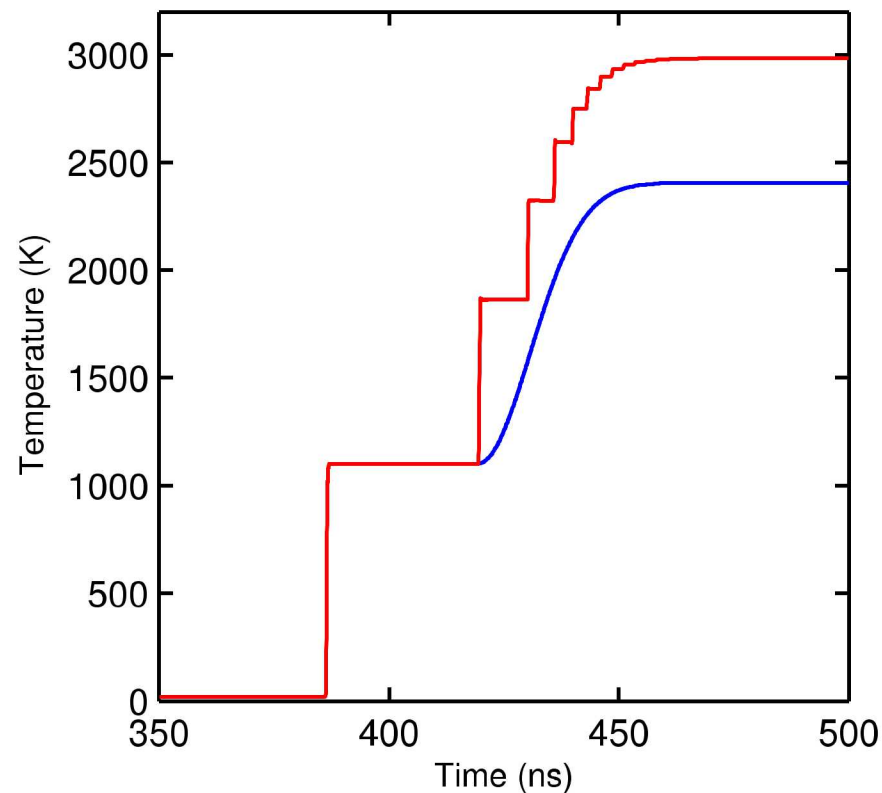
- The first experiments to address the IMT in liquid hydrogen and deuterium were performed by Nellis, Weir, and Mitchell in the 1990's
- Gas-gun technique
 - Multiple-shock compression at successively higher P and T states
 - Measured electrical conductivity
- Set of experiments provides a very good test of first-principles methods
 - Probes a regime in which both T and ρ (or P) play an important role



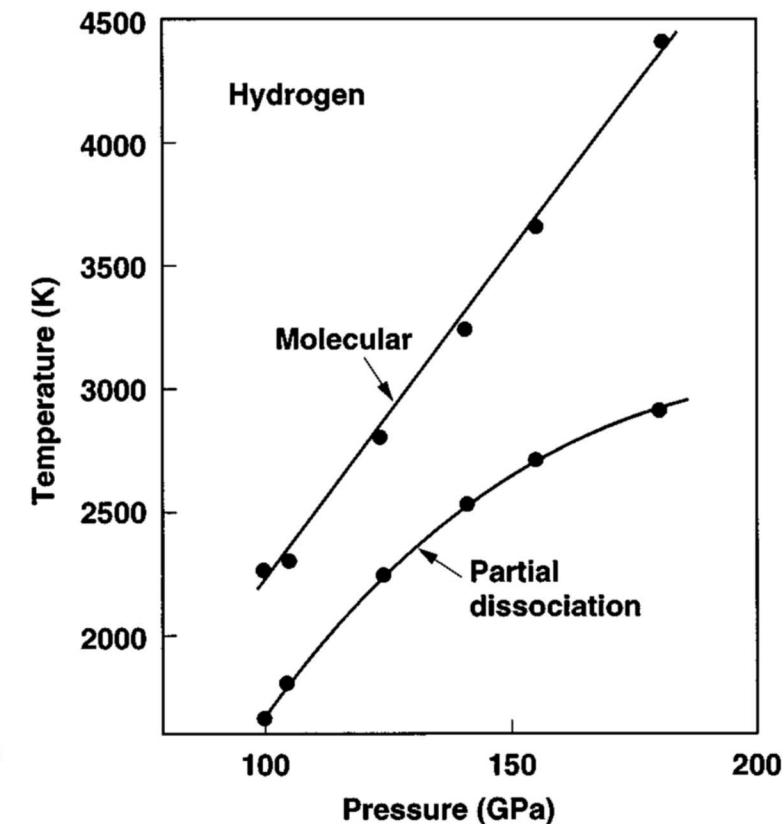
Reanalysis of inferred temperature states

- Nellis et al used two different methods to infer T and ρ
 - Method 1: Hydrocode simulation using Kerley EOS
 - Method 2: Isentrope calculation from first shock state for Ross EOS
- These methods described as being different but equivalent
 - This is incorrect
 - Method 2 fails to account for non-negligible increase in entropy from subsequent shocks during ring-up
- Reported T is too low and reported ρ is too high

T profiles using the two methods from Nellis et al



Comparison of inferred T from the two different methods



Determination of the peak state of the system

- P is experimentally constrained and does not depend upon the hydrogen/deuterium EOS
- In this regime P depends much more strongly on ρ than T
- Chose to fix T, then varied ρ to match experimentally measured P

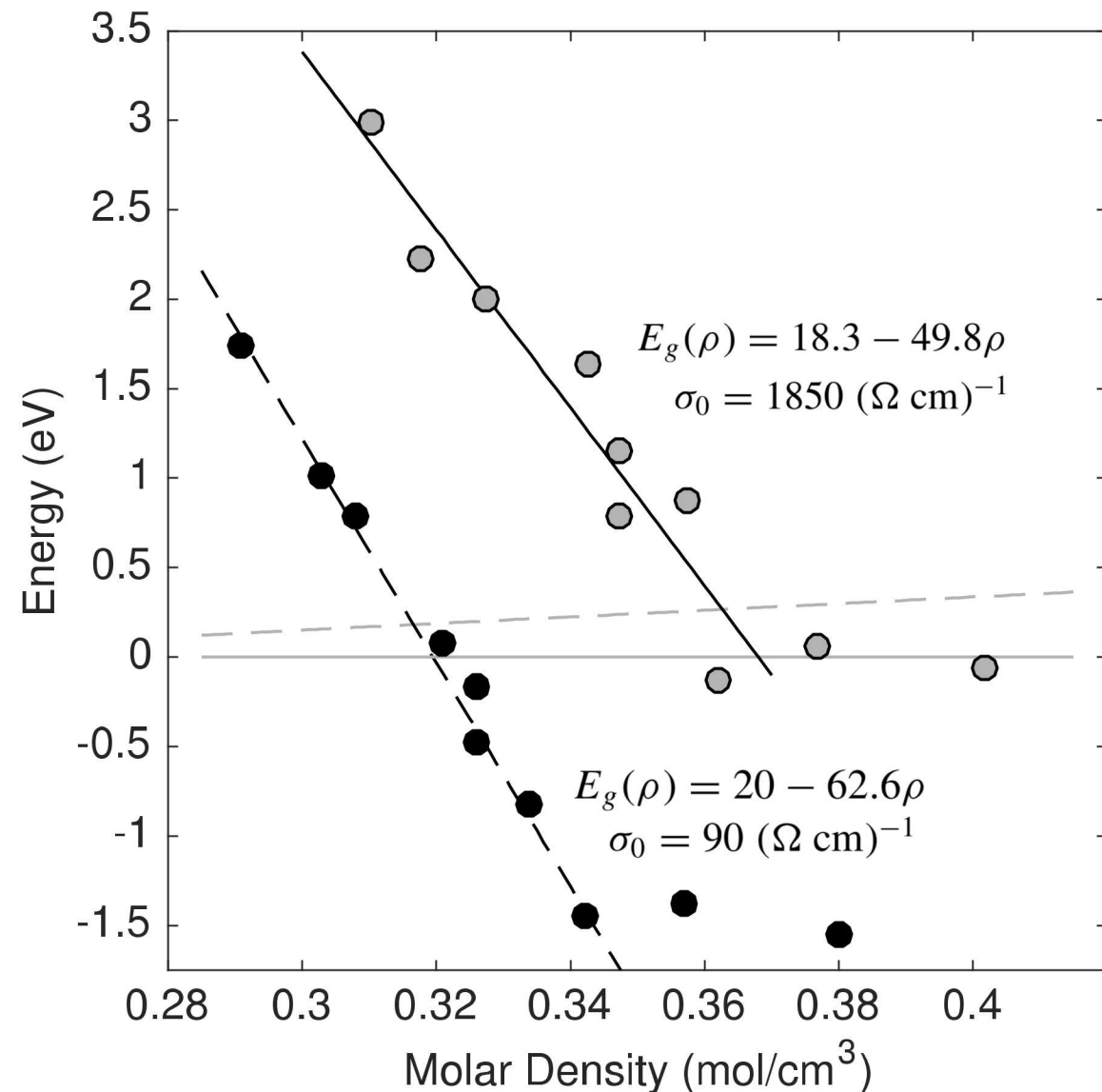
Experiment	σ ($\Omega \text{ cm}$) ⁻¹	Kerley03			PBE		DF1		DF2	
		P (GPa)	T (K)	ρ (g/cm ³)	σ ($\Omega \text{ cm}$) ⁻¹	ρ (g/cm ³)	σ ($\Omega \text{ cm}$) ⁻¹	ρ (g/cm ³)	σ ($\Omega \text{ cm}$) ⁻¹	ρ (g/cm ³)
SLDMS4-D ₂	0.71	93	2204	1.25	4989	1.397	1.99	1.249	0.30	1.222
SLDMS5-D ₂	77	121	2987	1.38	8919	1.534	4518	1.437	493	1.359
SLDMS8-D ₂	417	136	3397	1.44	9970	1.589	5461	1.514	3234	1.455
SLDMS6-H ₂	2.6	100	1978	0.64	3456	0.710	0.62	0.641	0.11	0.624
SLDMS13-H ₂	7.1	105	2093	0.66	4990	0.729	2.32	0.652	0.35	0.636
SLDMS7-H ₂	135	125	2567	0.70	9034	0.780	1546	0.722	16.2	0.683
SLDMS9-H ₂	313	125	2573	0.70	9034	0.781	1546	0.722	16.2	0.683
SLDMS12-H ₂	2380	142	2984	0.73	10410	0.816	5671	0.777	1693	0.737
SLDMS10-H ₂	1670	156	3310	0.76	11290	0.840	7061	0.807	3880	0.774
SLDMS11-H ₂	2000	183	3951	0.81	13180	0.881	8907	0.854	6551	0.827

Reanalysis of semiconducting model

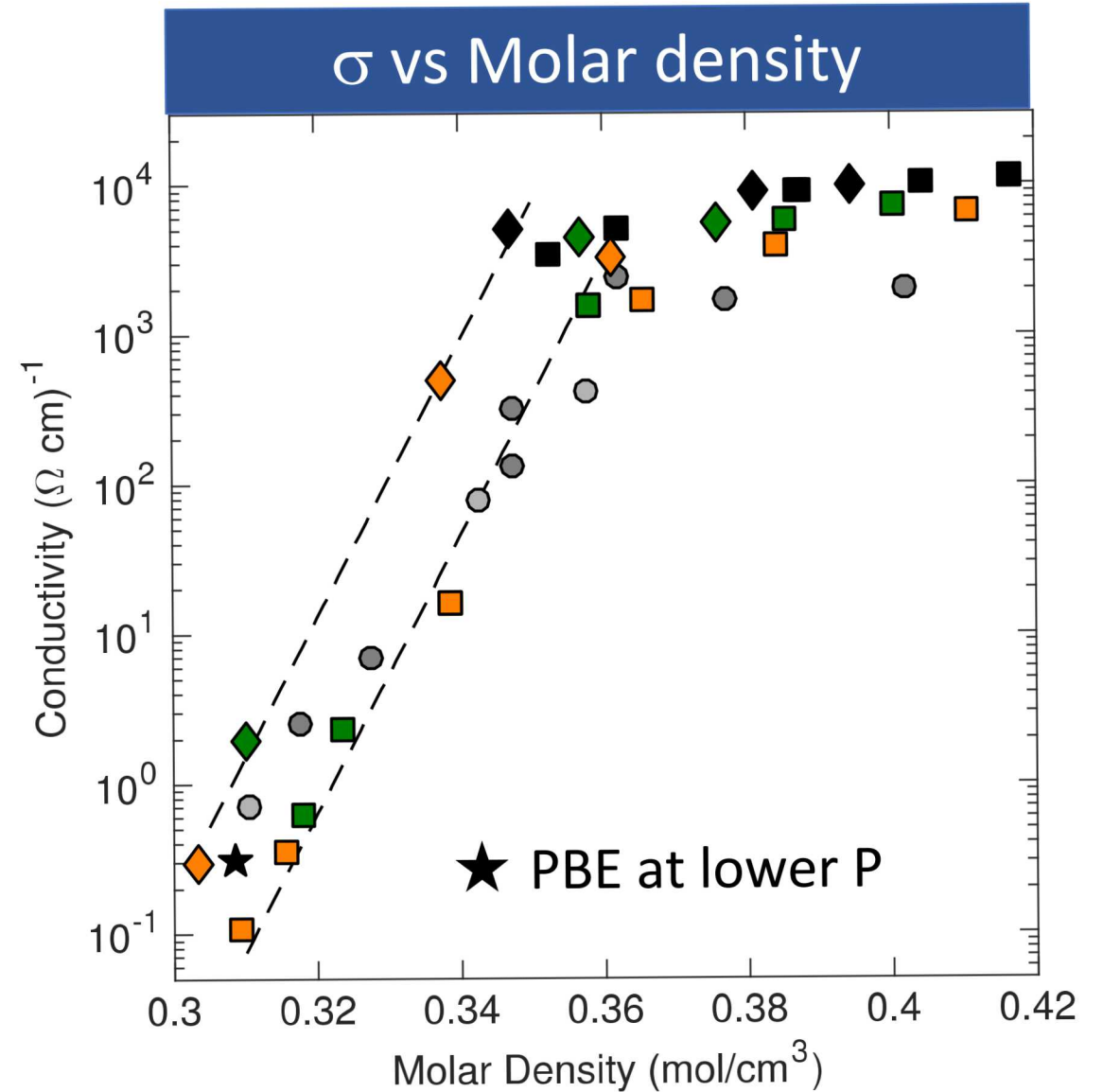
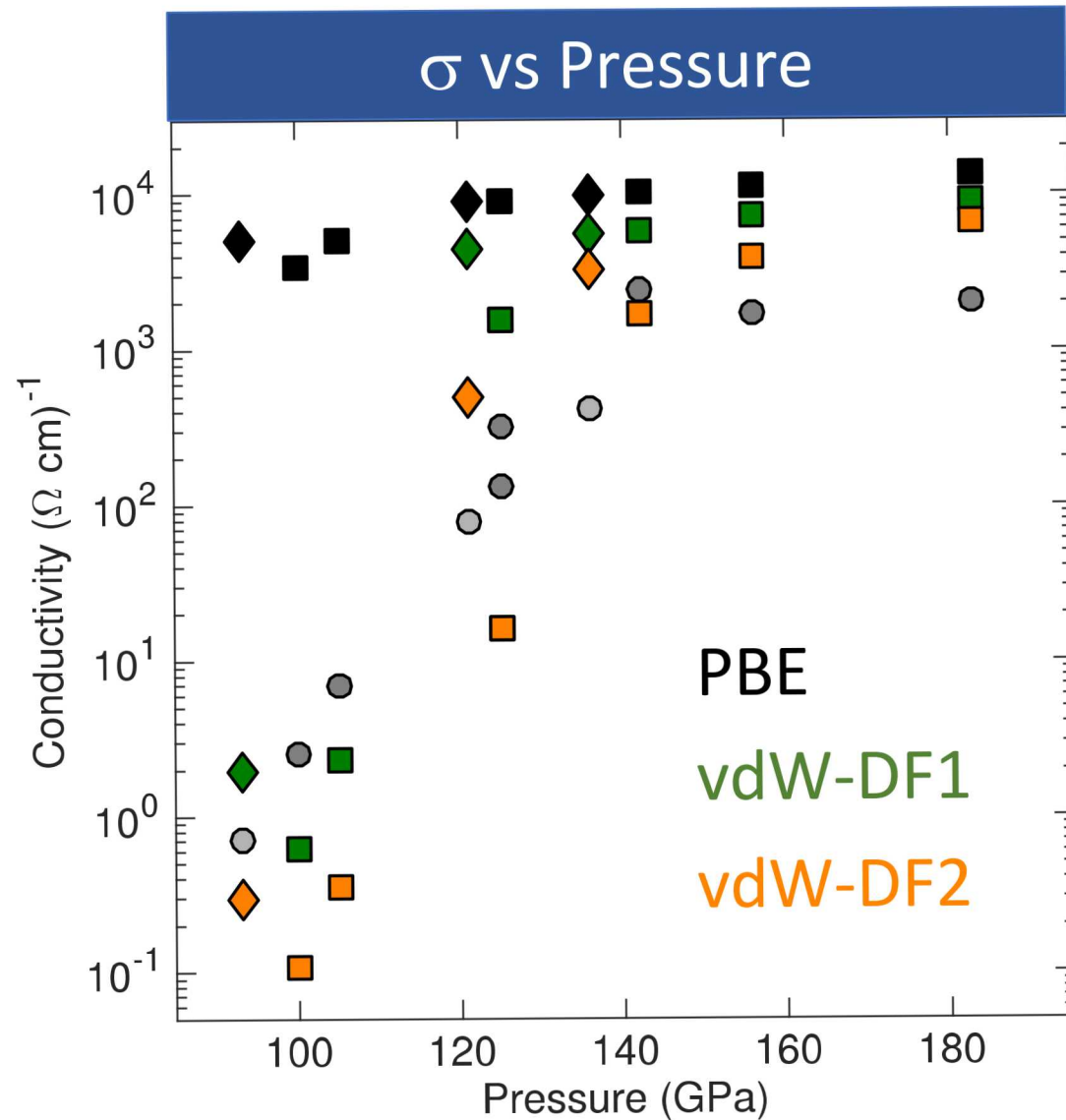
- Nellis et al appealed to a simplified semi-conducting model to infer an energy gap as a function of ρ

$$\sigma = \sigma_0 \exp[-E_g(\rho)/2k_B T]$$

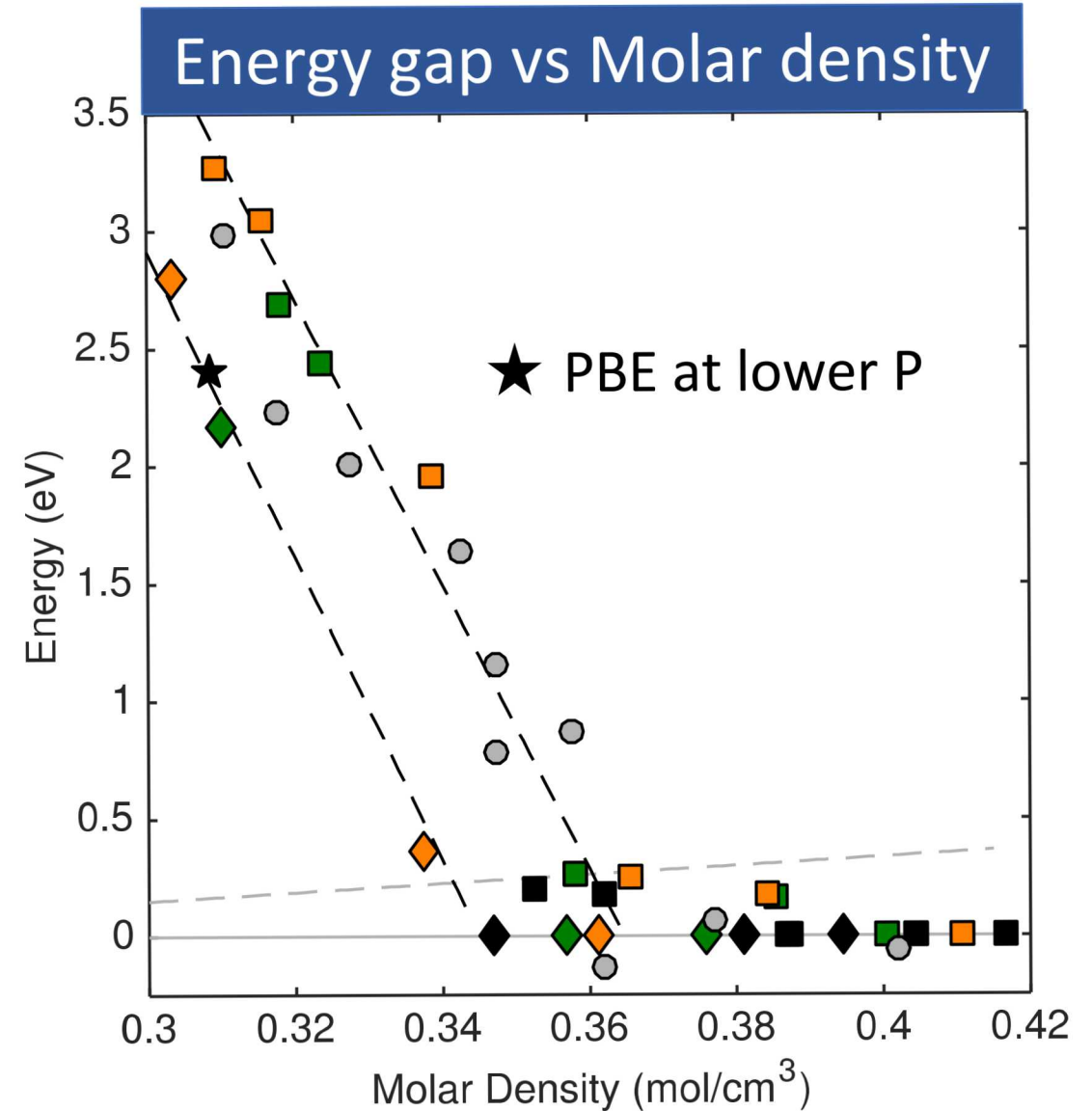
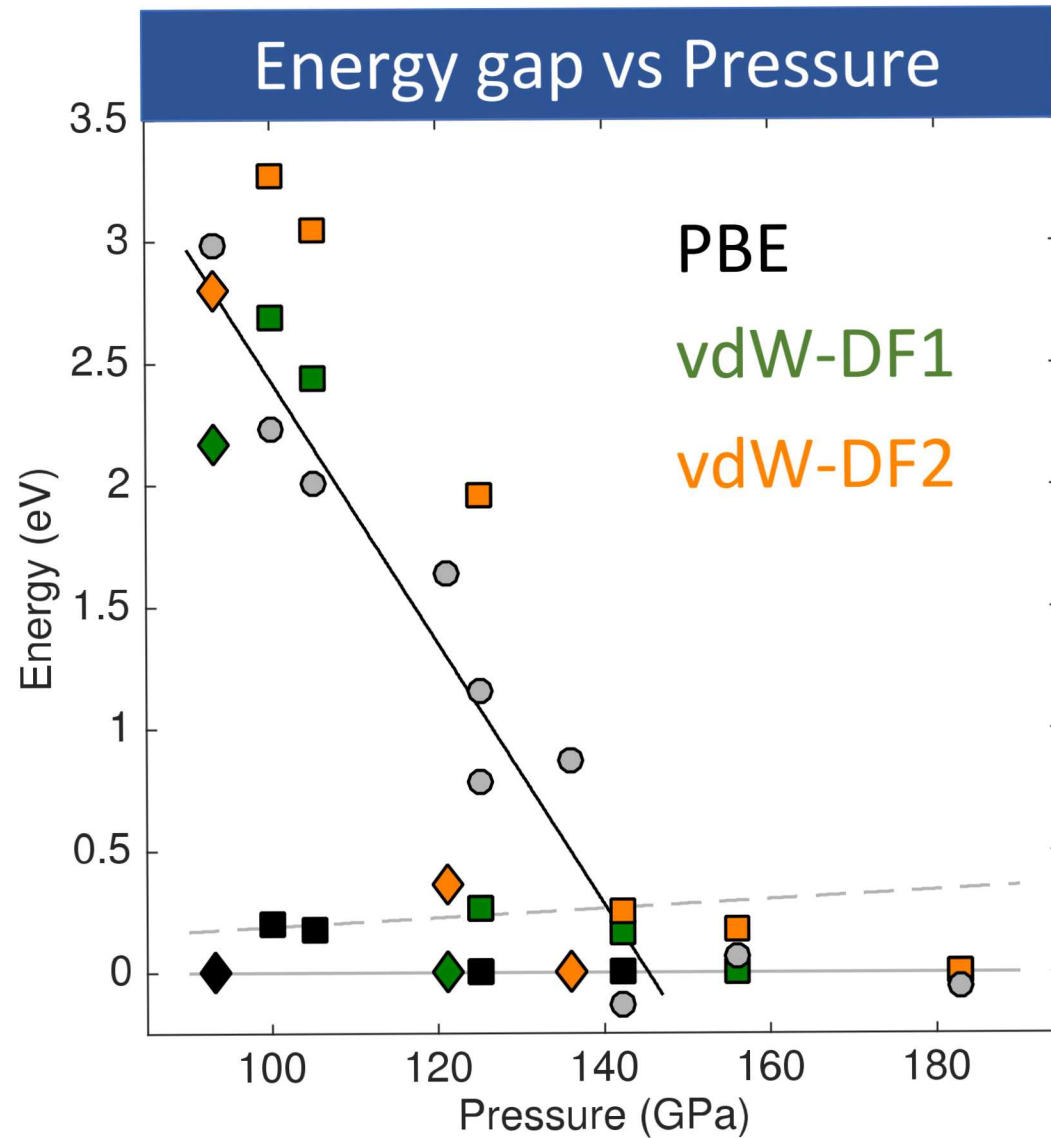
- The limiting conductivity was taken to be a free parameter
 - This results in a negative energy gap for $\rho > 0.34 \text{ mol/cm}^3$
- With the limiting conductivity taken from experiment the result is more physical
 - The gap closes at $\rho \sim 0.37 \text{ mol/cm}^3$



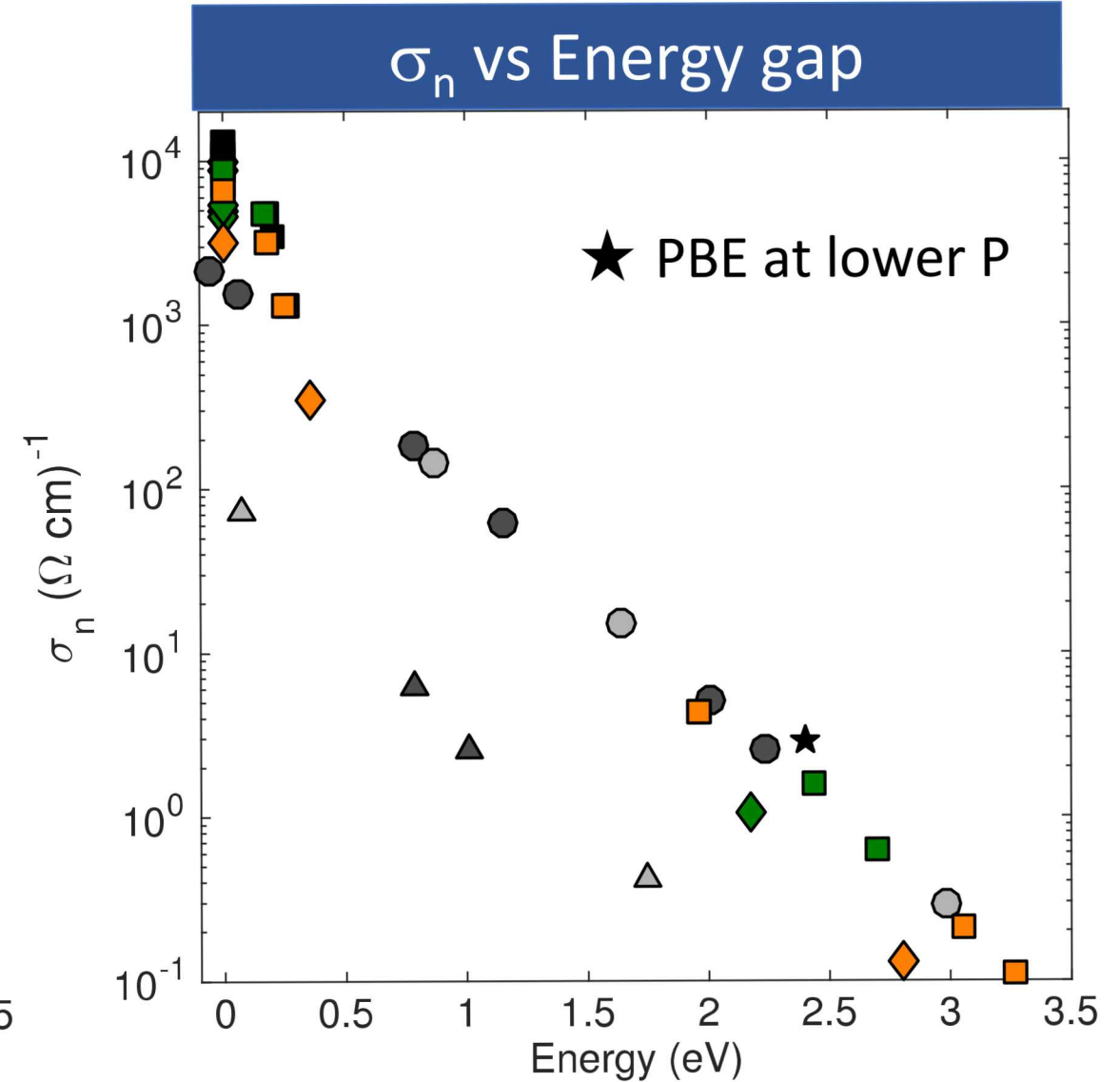
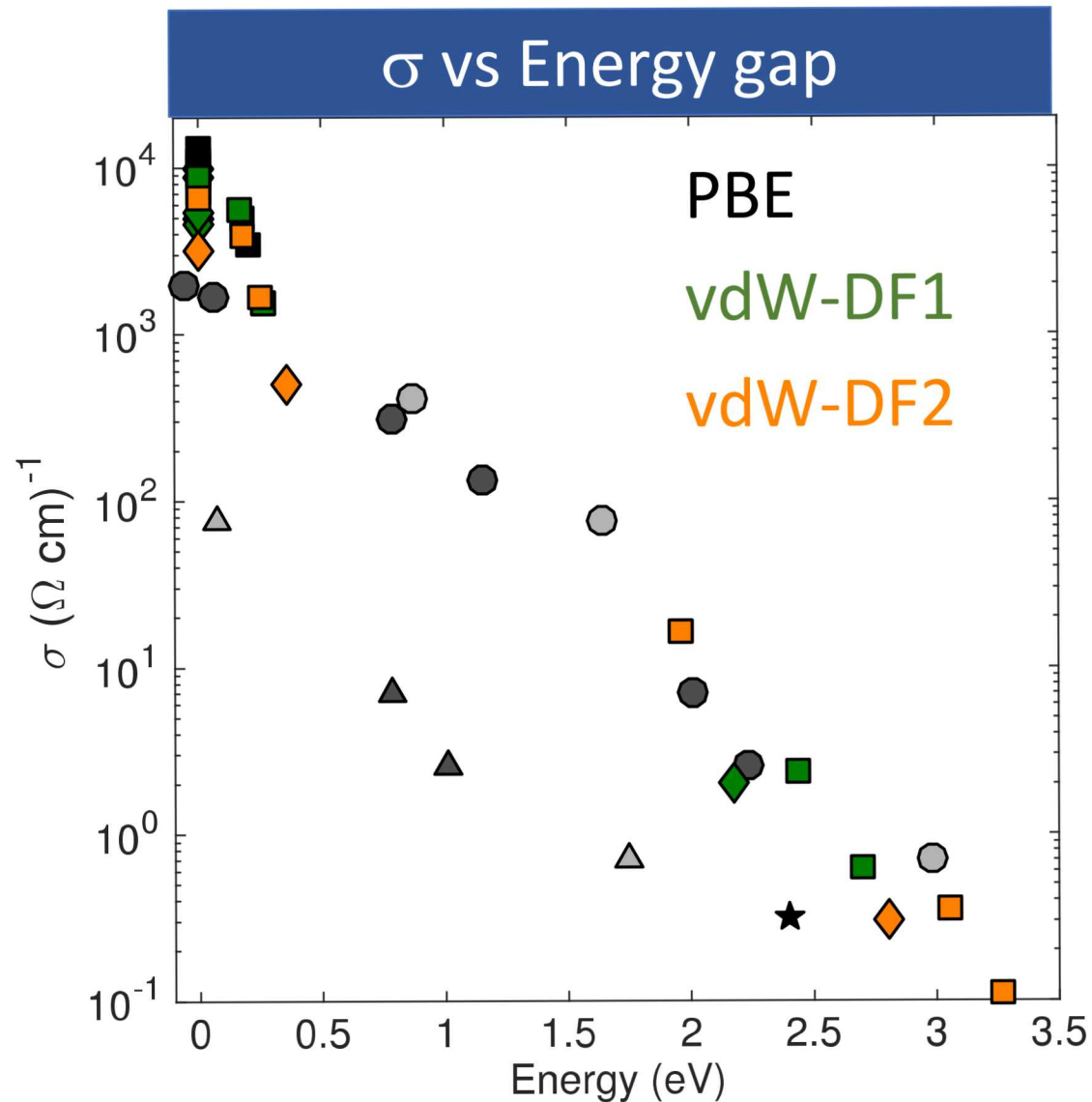
Predicted conductivity at the peak states



Predicted energy gap at the peak states



Conductivity and normalized conductivity vs energy gap



Conclusions



- Performed a reanalysis of the Nellis, Weir, and Mitchell experiments
 - Corrected an inconsistency in the inferred T and ρ states
- Performed a detailed comparison of the measured σ with first-principles density functional theory using various xc functionals
- Results found to be inconsistent with the semi-local xc functional PBE
 - Inconsistency likely stems from P errors associated with the PBE xc functional that result from premature dissociation
 - Calculated P are too low at these T and ρ conditions
- Results found to be in better agreement with non-local vdW functionals
- Together with previous comparisons at high- T , low- ρ and low- T , high- ρ , these results provide a consistent picture for the IMT over a wide T and ρ range