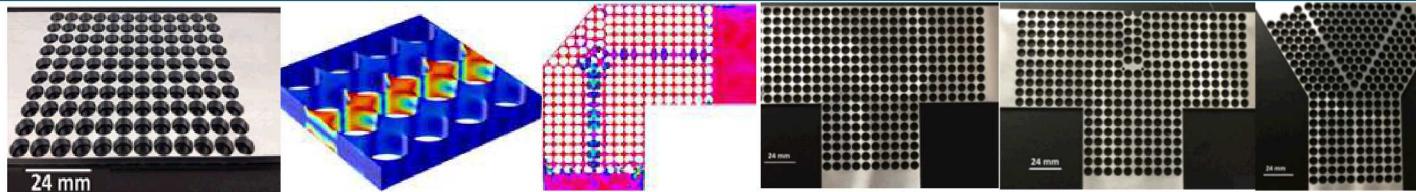


# Demonstration of Waveguiding, Bends, Splitters in Macro-Scale Phononic Crystal Devices



*PRESENTED BY*

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**Charles M. Reinke**, Ihab El-Kady, and Zayd C. Leseman



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# Phononic Crystals

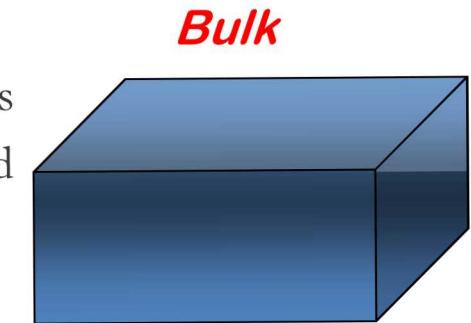


- What is a Phononic Crystal (PnC)?

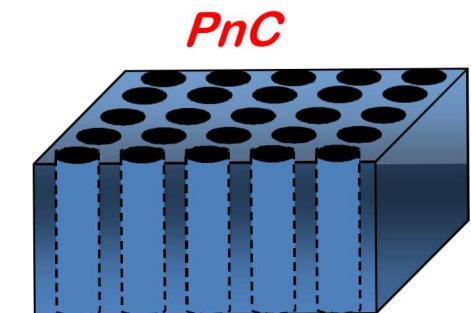
- A periodic arrangement of two or more materials which exhibits anomalous dispersion for phonons
- Can have bandgaps, i.e. frequency ranges in which phonon transmission in the material is prohibited

- How does a PnC Work?

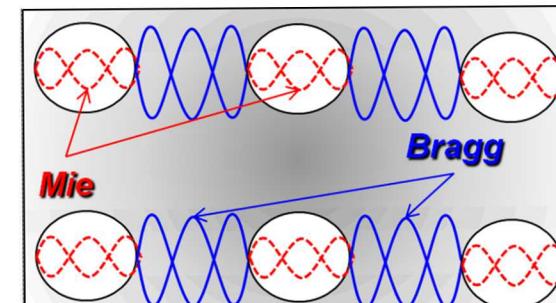
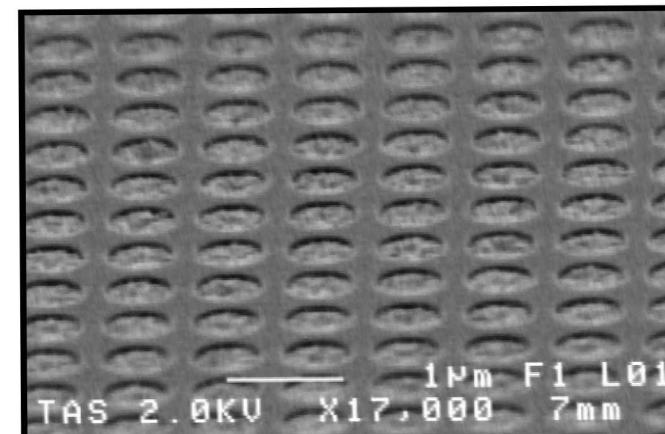
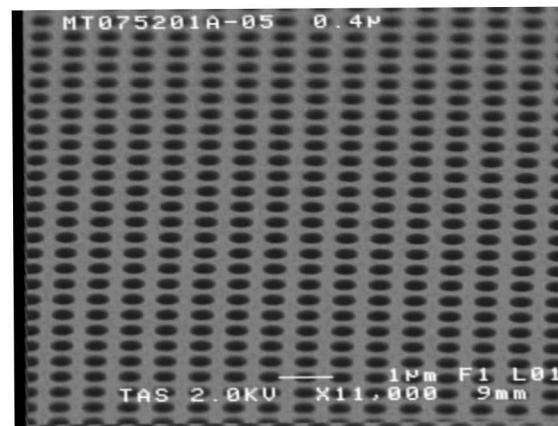
- Created by superposing Mie and Bragg resonant scattering by a periodic arrangement of scattering centers in a lattice
- Requires sufficient acoustic impedance mismatch
- Provides macro-to-micro scalable (N+1)D control (2D lattice → 3D control) of the phonon distribution



**Bulk**

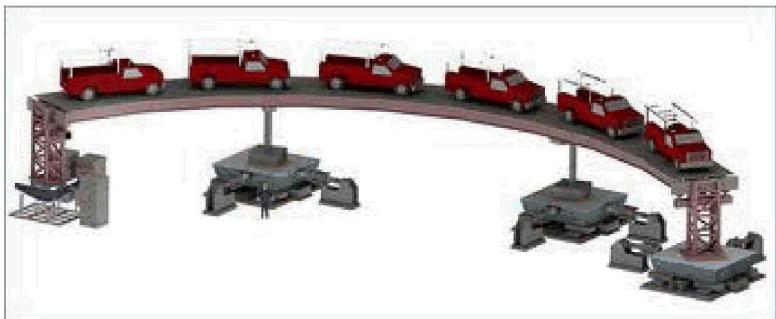


**PnC**



# Applications of Phononic Crystals

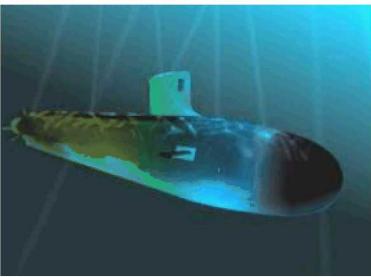
- RF signal processing (filters, delay lines)
- Acoustic and ultrasonic applications
- High Q-factor Cavities
- Phonon density of states (DoS) manipulation
- Thermal conductivity engineering
- Frequency-selective vibration dampening



**Earthquake Mitigation**



**Quieter tires**



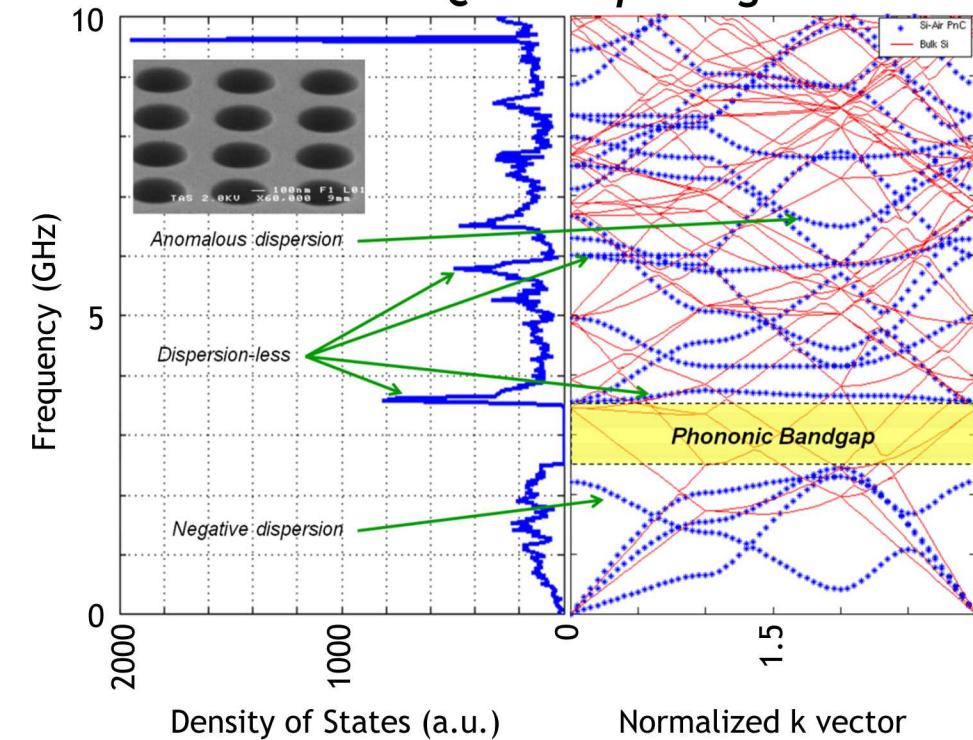
**Underwater stealth**



**Quiet engines**



**Quiet ship design**



**Phonon DoS engineering**

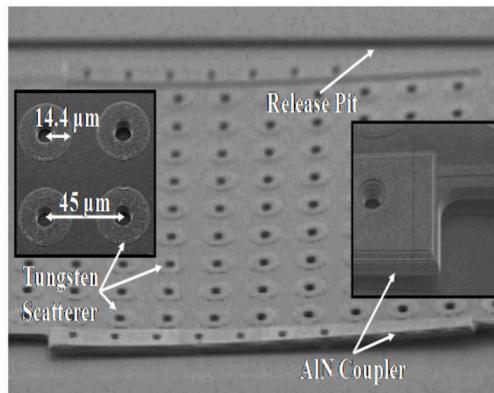
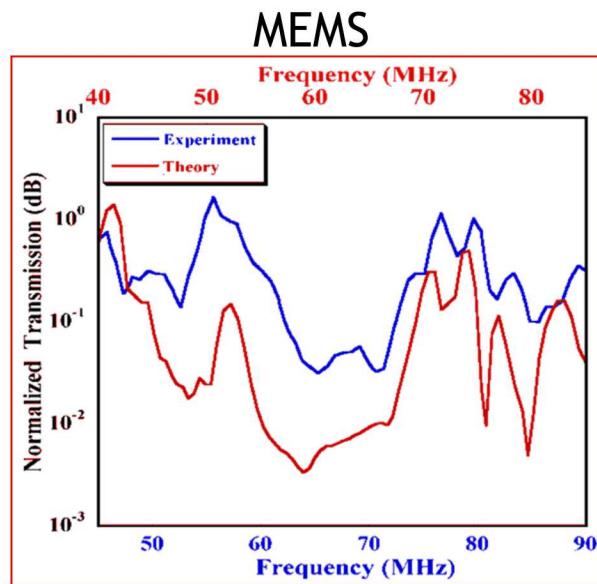


**Vibration isolation**



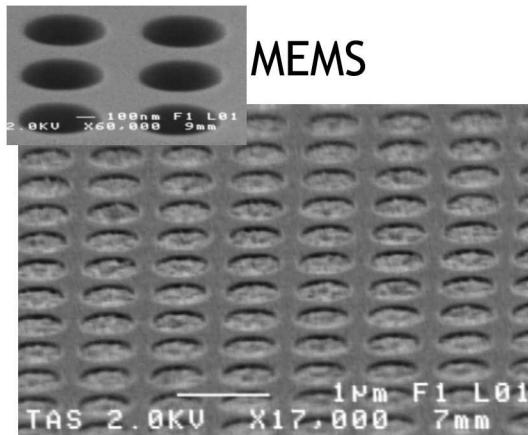
# Signal Processing with Phononic Crystals

## 1<sup>st</sup> MHz MEMS PnC (VHF) 2008

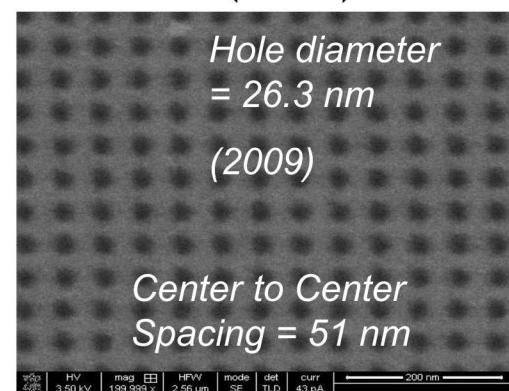


I. El-Kady, et.al., APL, 2008

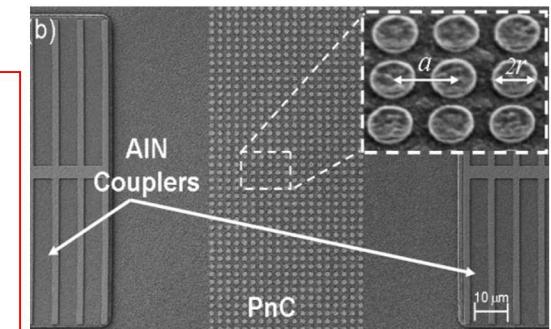
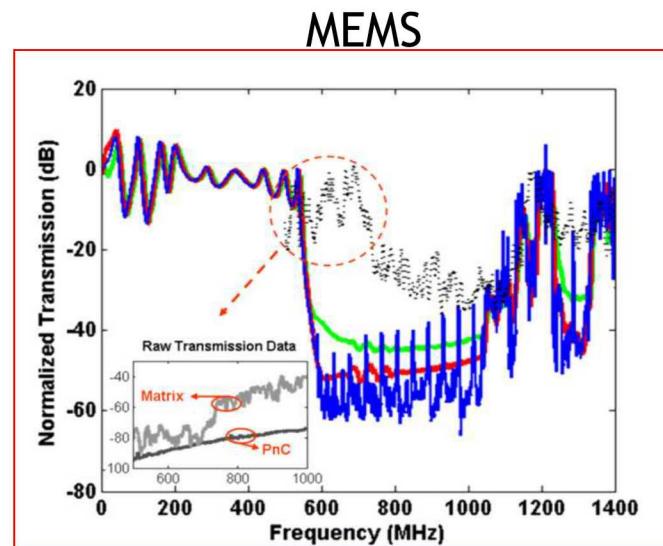
## 10 GHz PnCs (UHF) 2009



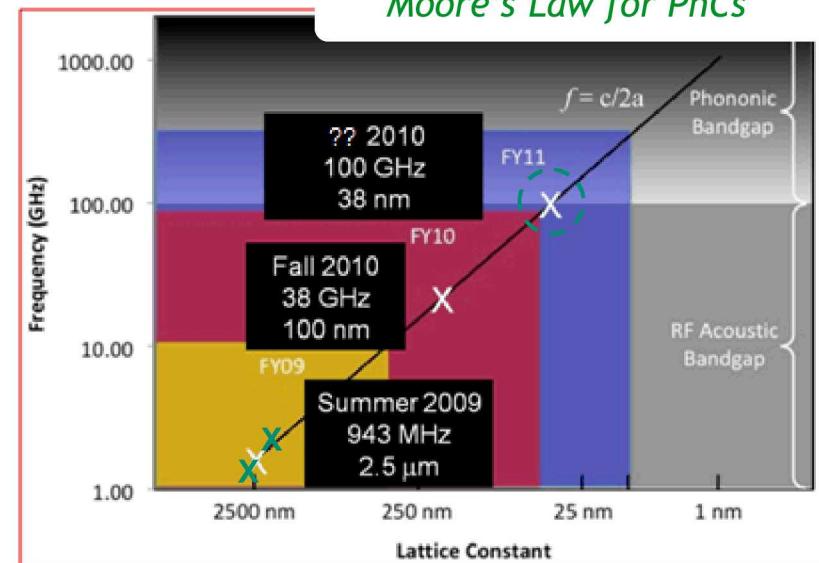
## 38 GHz PnCs (UHF) 2010



## 1<sup>st</sup> GHz MEMS PnCs (UHF) 2009



Moore's Law for PnCs

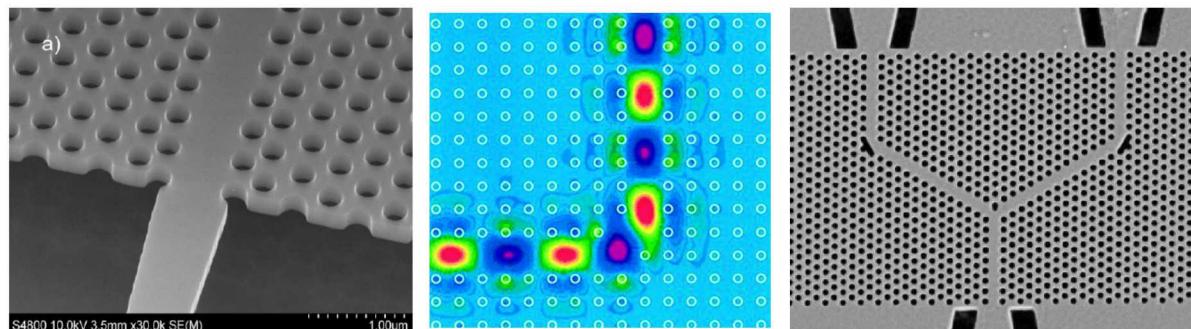
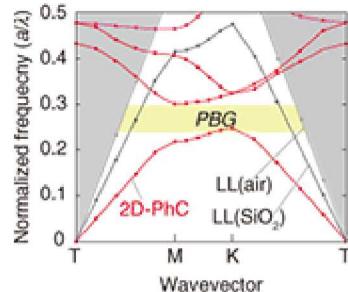
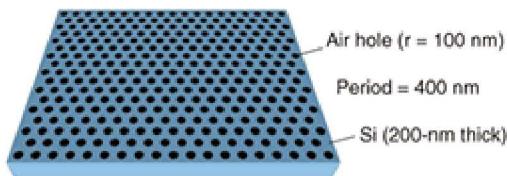


# Mechanical Analogue to Photonic Crystals



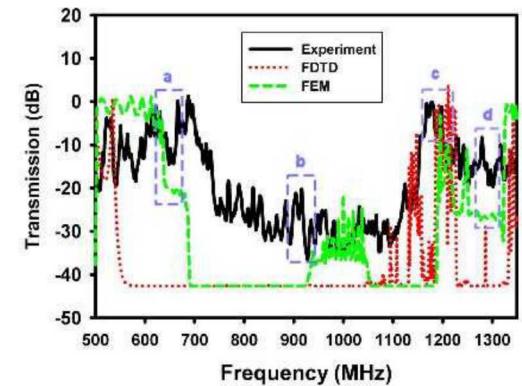
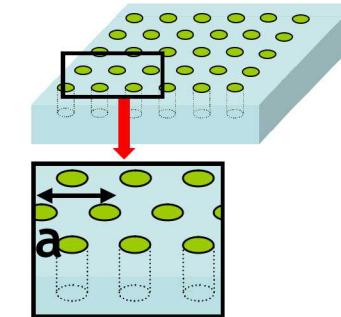
- Photonic crystals

- Periodic refractive index mismatch
- Manipulate photon propagation with periodicity of photon wavelength



- Phononic crystals

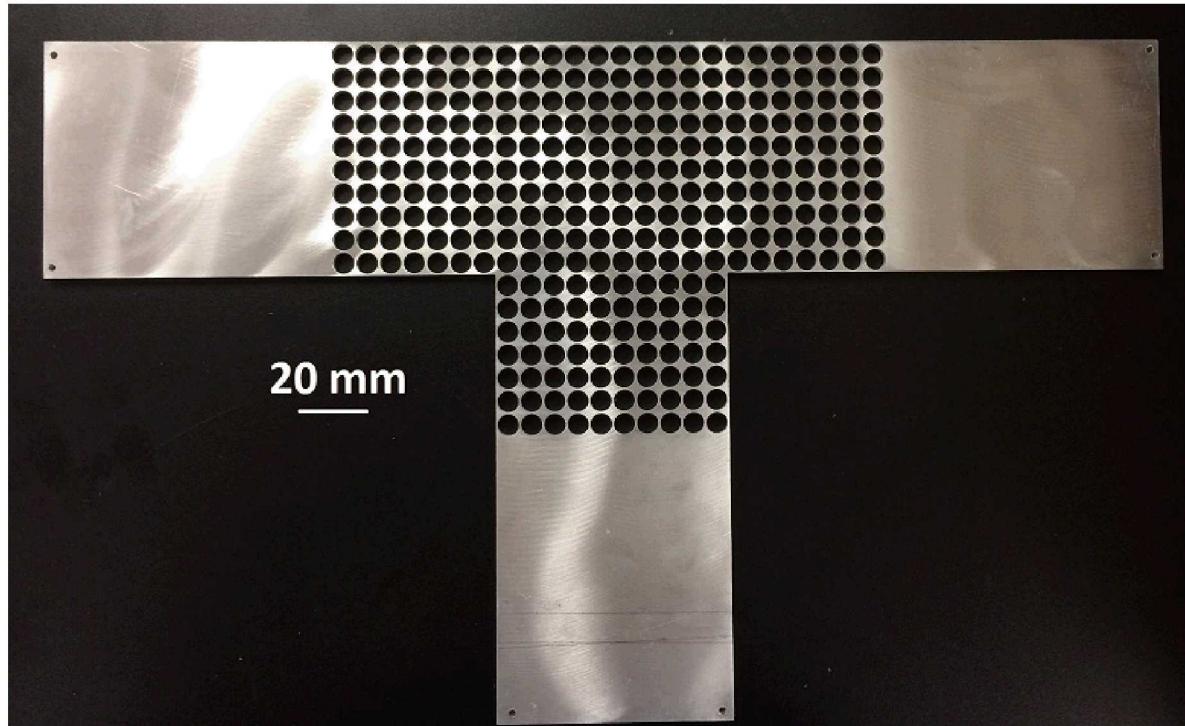
- Periodic mechanical impedance mismatch
- Manipulate the propagation of elastic/acoustic waves with periodicity of the acoustic wavelength



## 6 Macro-Scale Phononic Crystals



- Aluminum-air macro-scale PnC
  - Excellent machinability
  - Relaxed fabrication constraints
  - Rapid fabrication turn around
- Simple cubic lattice geometry
  - Able to achieve large bandgaps
- Simulations and measured results are scaled to the reduced frequency  $\Omega = \omega a / 2\pi C_t$ 
  - $\omega$  is the angular frequency,  $C_t$  is the transverse sound velocity, and  $a$  is the lattice constant
  - Behavior scales directly to the micro-/nano-scale



# Phononic Crystal Design

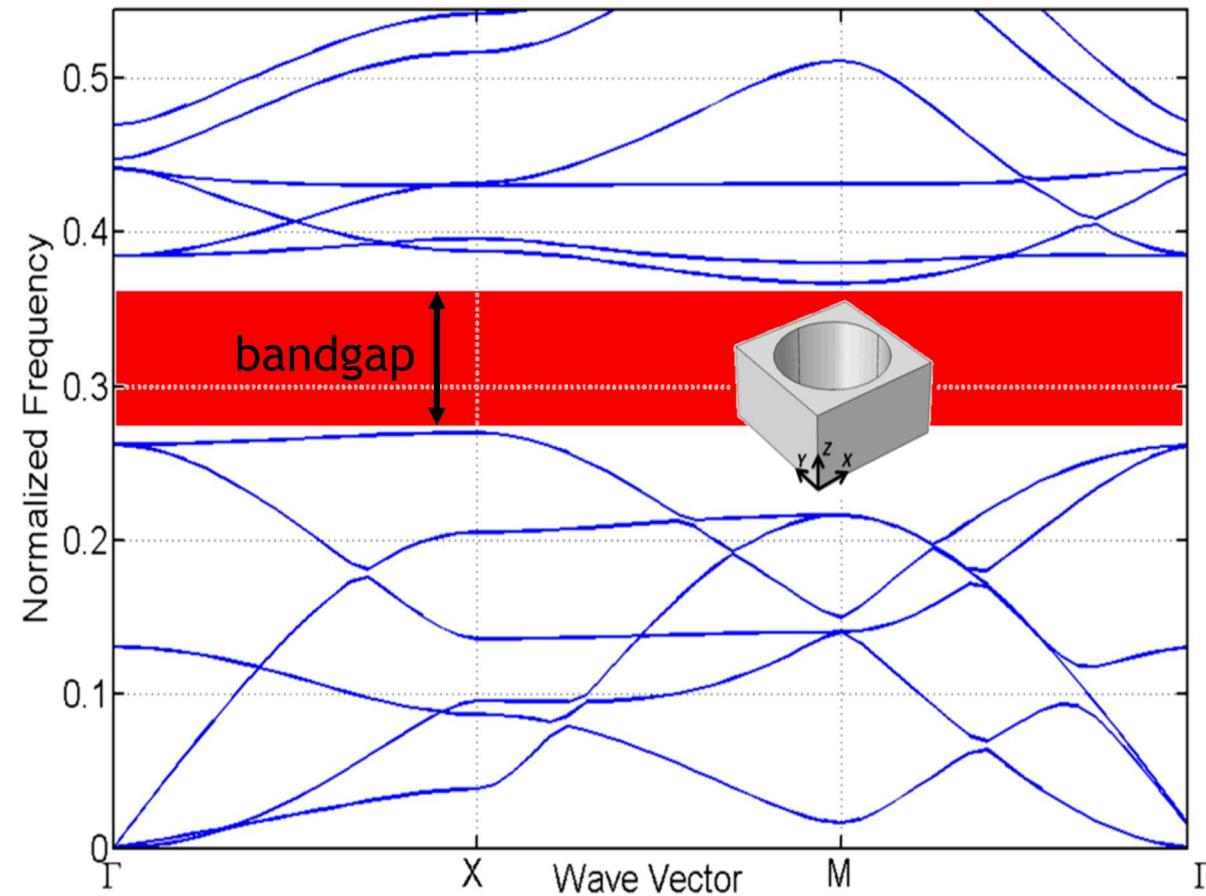


- Material: Al

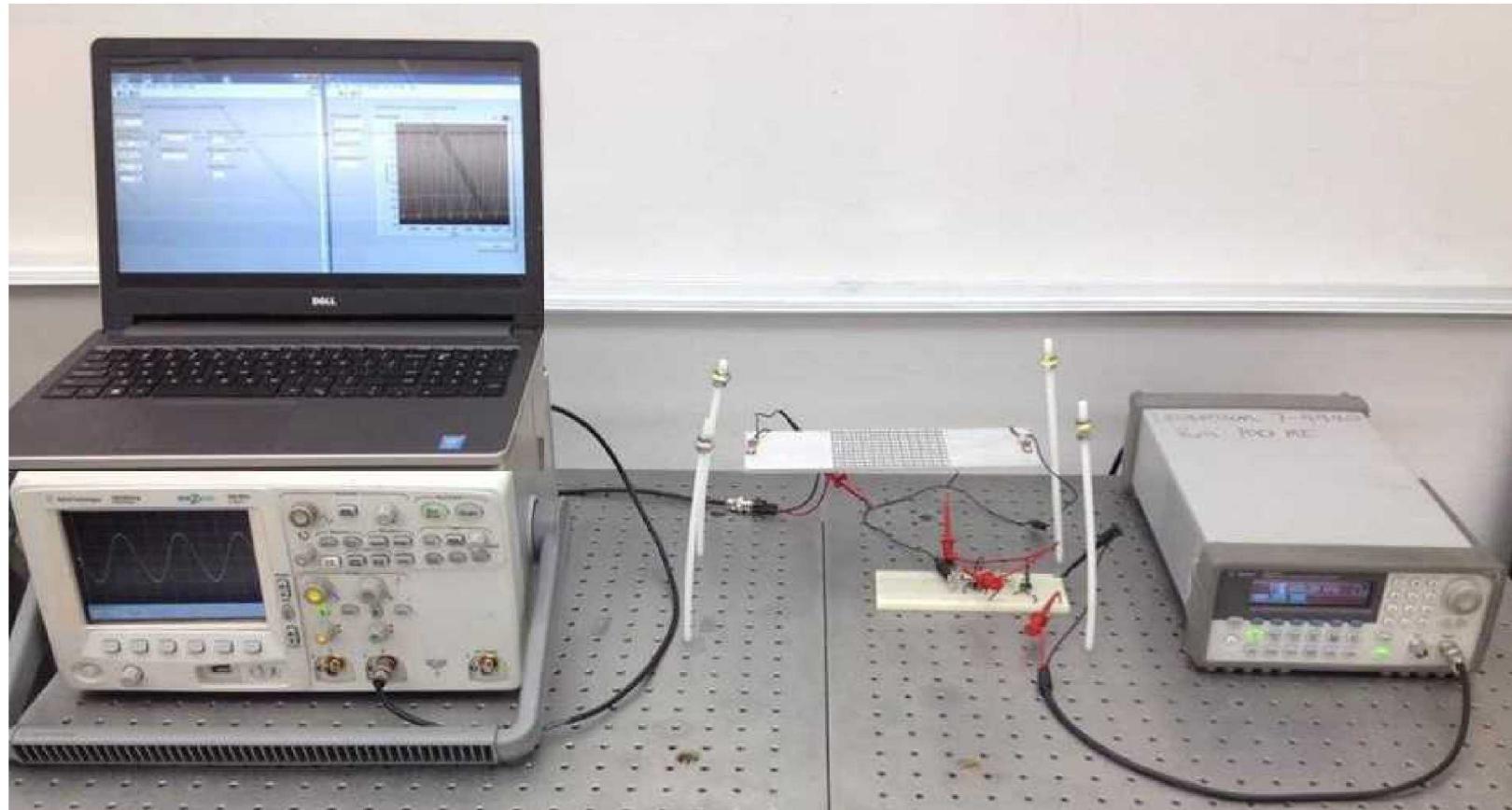
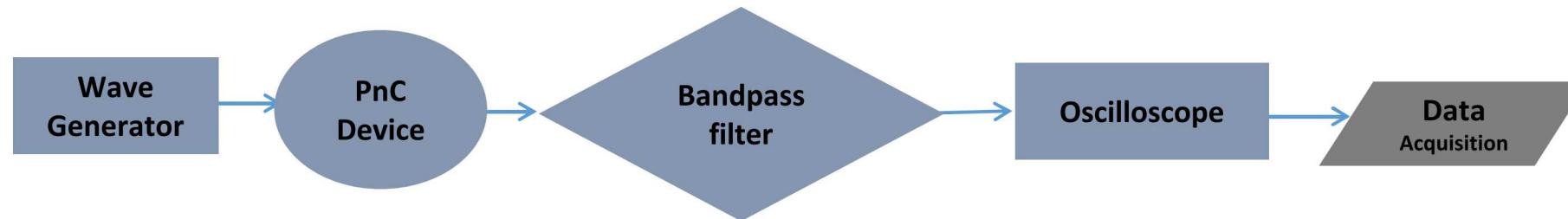
- Lattice constant  $a = 8\text{mm}$
- Slab thickness  $t = 4\text{mm}$  ( $t/a = 0.5$ )
- Hole radius  $r = 3.84\text{mm}$  ( $r/a = 0.48$ )

- Bandgap range :

- Calculated bandgap for the full irreducible Brillouin zone from 149 – 202kHz, corresponding to 0.27 to 0.366 in normalized frequency
- Gap-to-midgap ratio = 30%



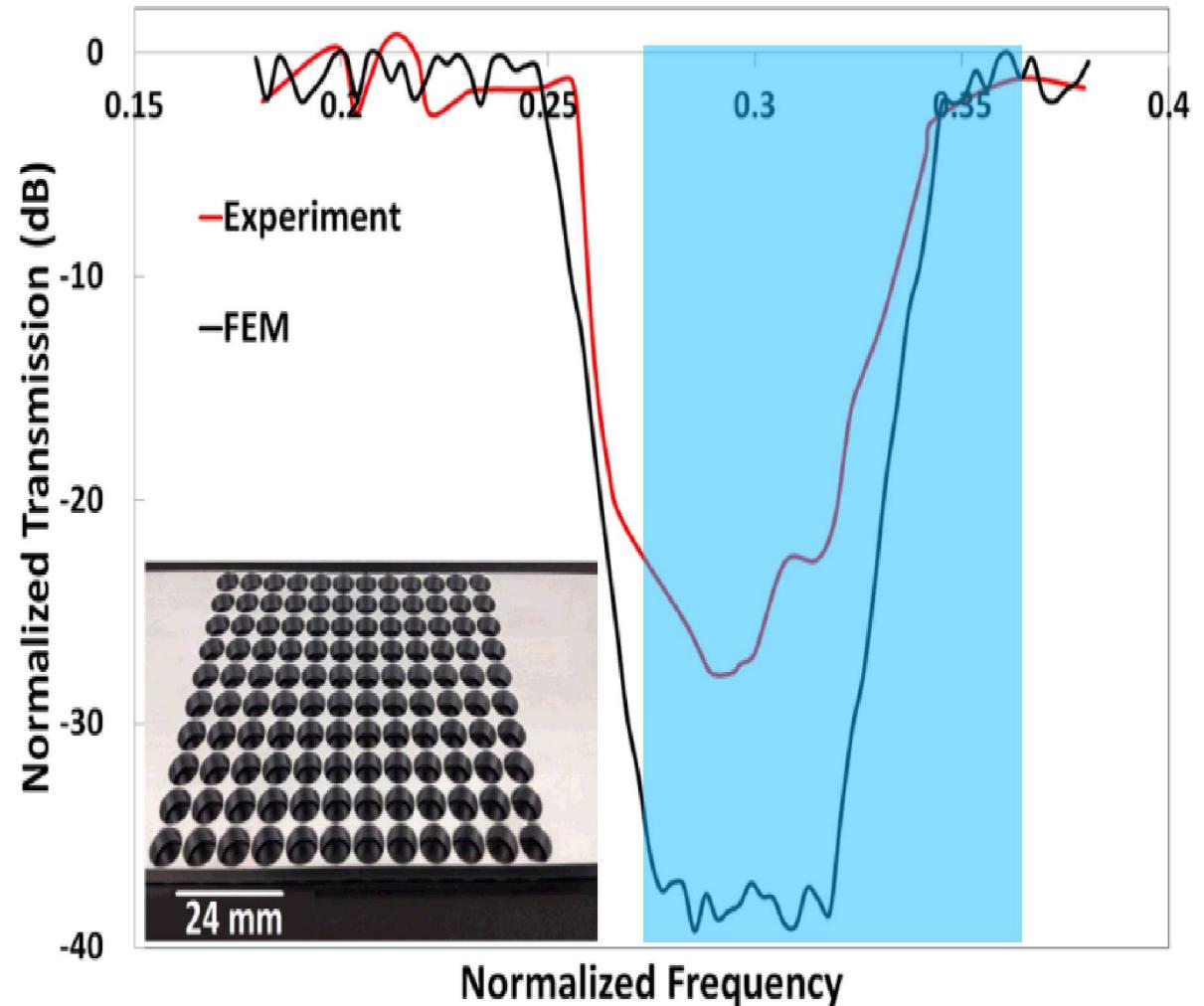
# 8 Experimental Setup



## 9 PnC Bandgap Characterization



- Measured transmission was normalized with slab (bulk Al with no holes)
  - Transmission is attenuated by >20dB in the frequency range  $0.26 < \Omega < 0.34$
  - Agrees well with the [theoretically predicted  \$0.27 < \Omega < 0.366\$](#)
- Finite-element method simulation used to verify the results
  - Difference due to fabrication imperfection and finite size of the fabricated sample



# 10 PnC Waveguide Design

- Waveguide created by introducing a line defect in the PnC along the propagation direction.

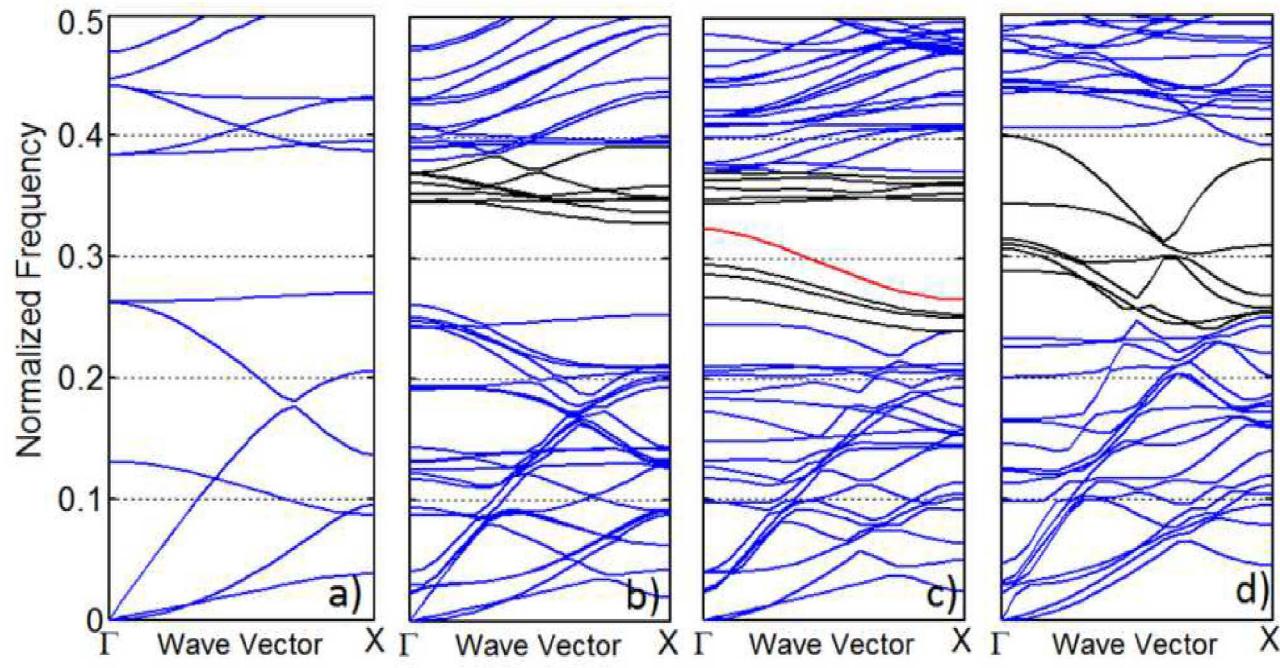
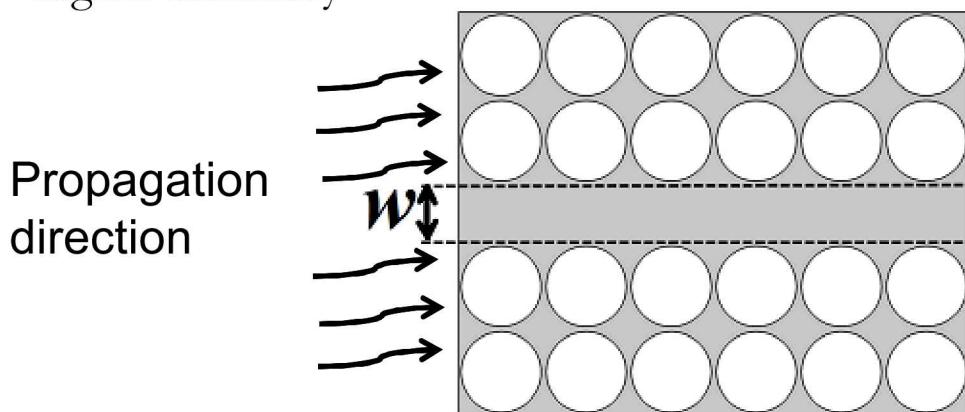
- The defect width is defined as:

$$w = (1+\alpha) a - 2r$$

- $\alpha = 0$  corresponds to the perfect PnC (no defect)
- $\alpha = 1$  corresponds to the so-called W1 waveguide

- The band structure was studied versus defect width

- An isolated, **single-mode** waveguide was found for  $\alpha = 0.1$
- Stronger confinement of the propagating energy → higher efficiency



a)  $\alpha = 0$   
(Perfect PnC)

b)  $\alpha = 0.01$

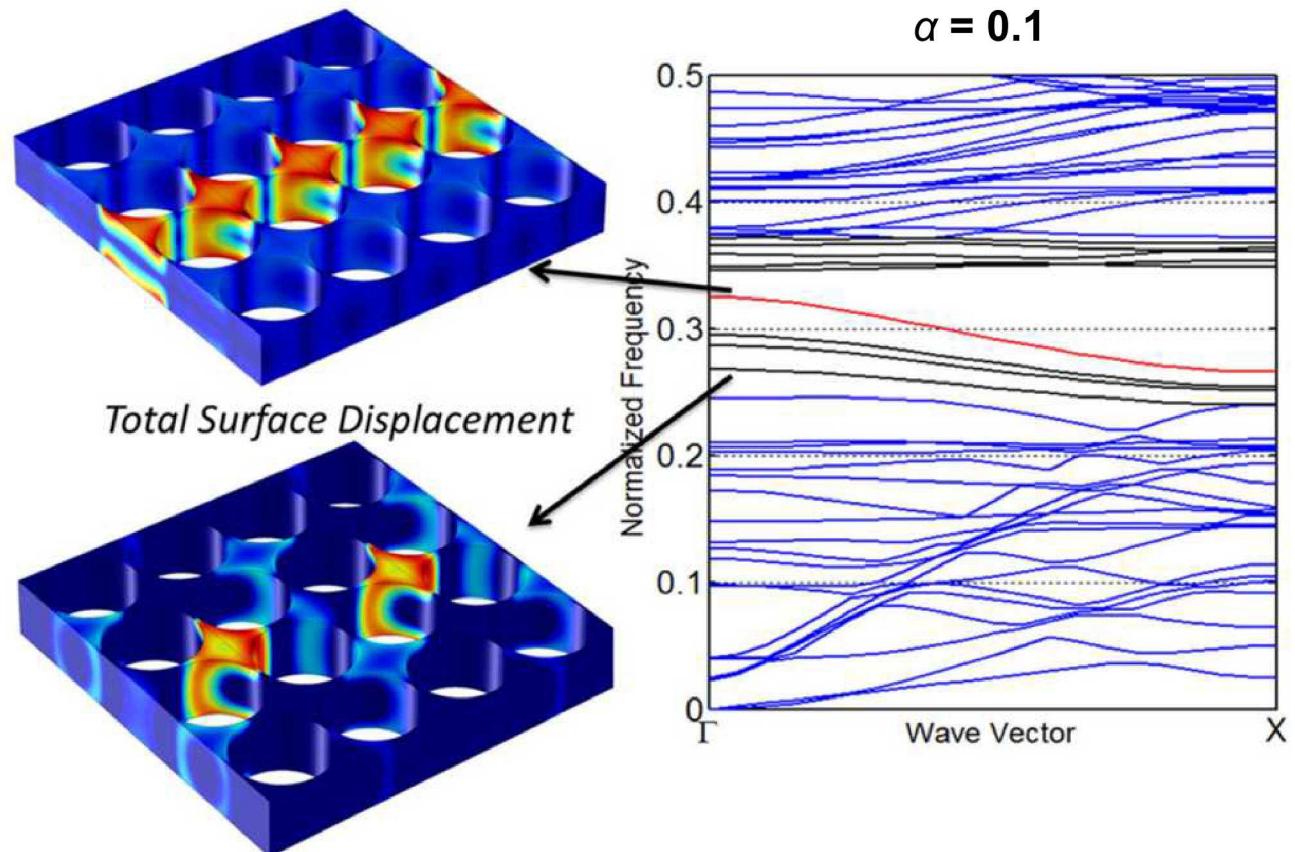
c)  $\alpha = 0.1$

d)  $\alpha = 0.5$

# PnC Waveguide Design



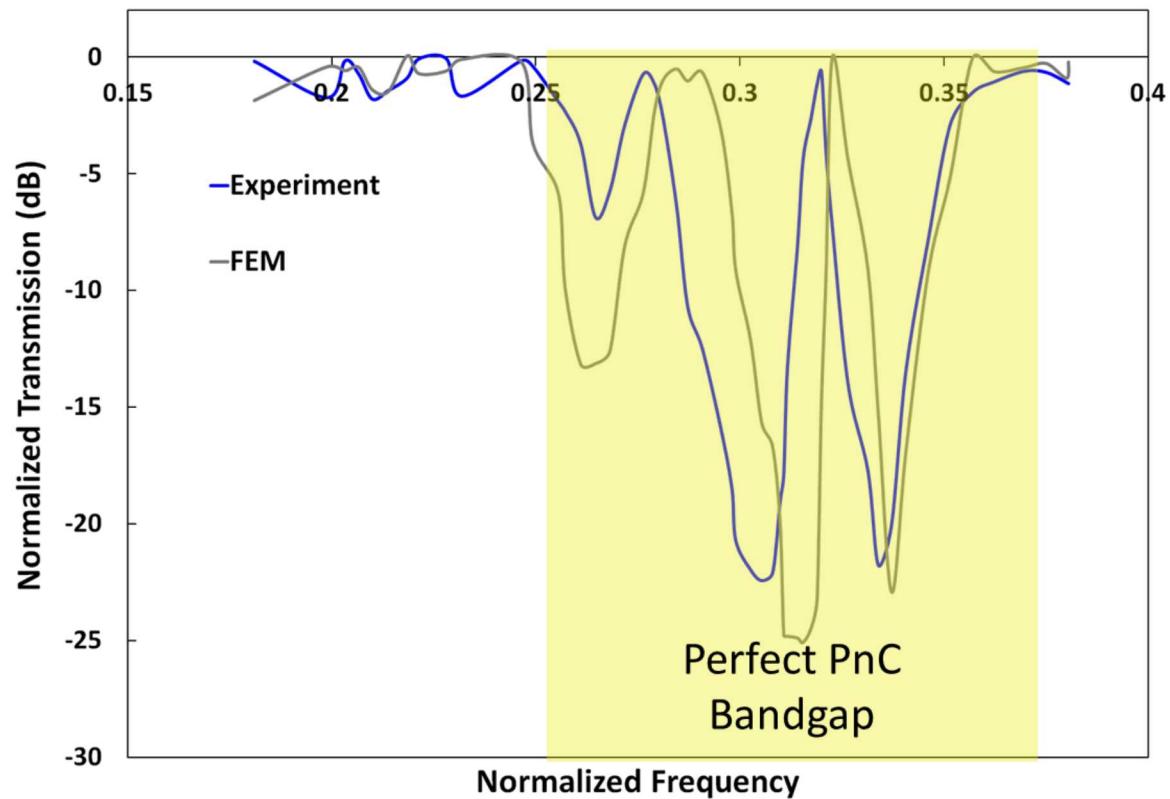
- The modes indicated in black and red result from the introduction of the line defect
- The lower-frequency mode is leaky
  - Energy propagates throughout the crystal and is not strongly guided
- The **higher-frequency mode** is a guided mode
  - Energy is well-confined
  - Waveguide is single-mode from about  $0.3 < \Omega < 0.32$



# PnC Waveguide Characterization



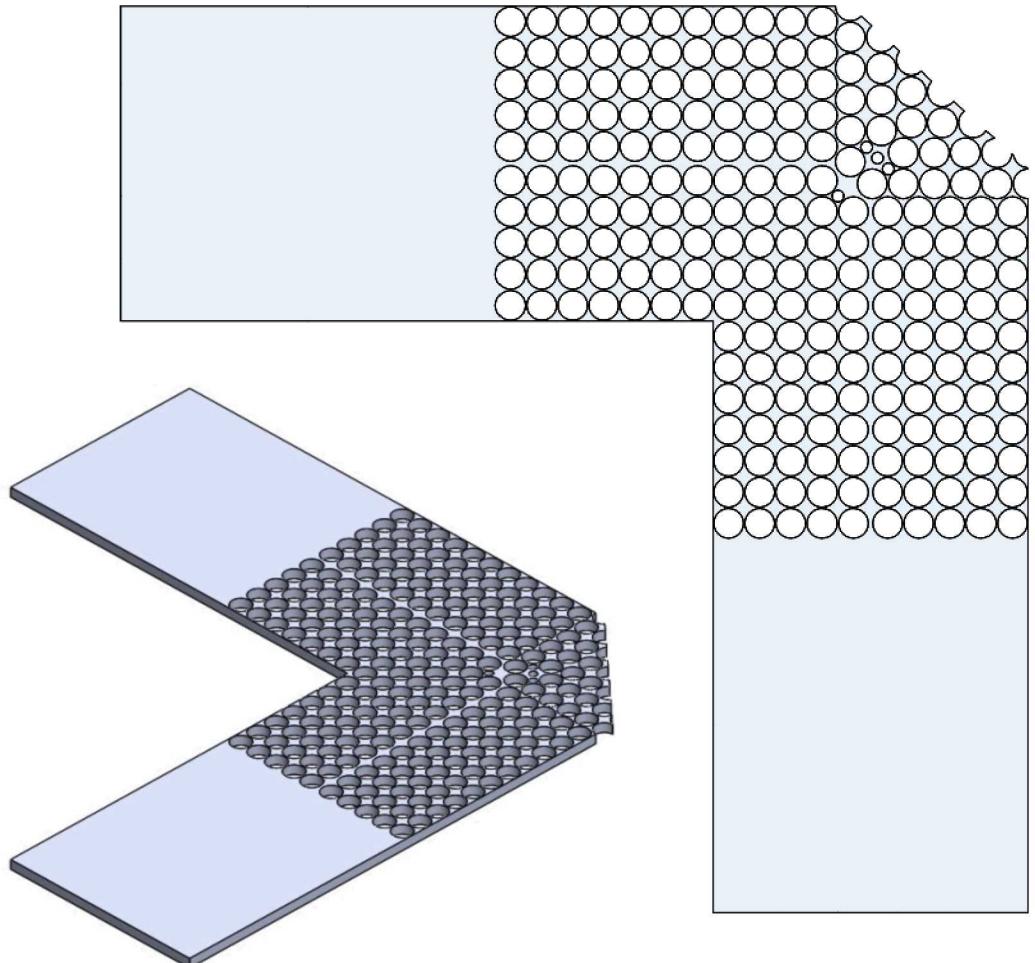
- Passband measured within the bandgap from  $0.25 < \Omega < 0.287$
- Transmission peak is centered at 0.32 in normalized frequency (177kHz) with only 1dB loss
- Disagreement in peak frequency between measurement and simulation is less than 2%
  - Discrepancy attributed to the difference between theoretical and actual material properties



# PnC Bent Waveguide Design

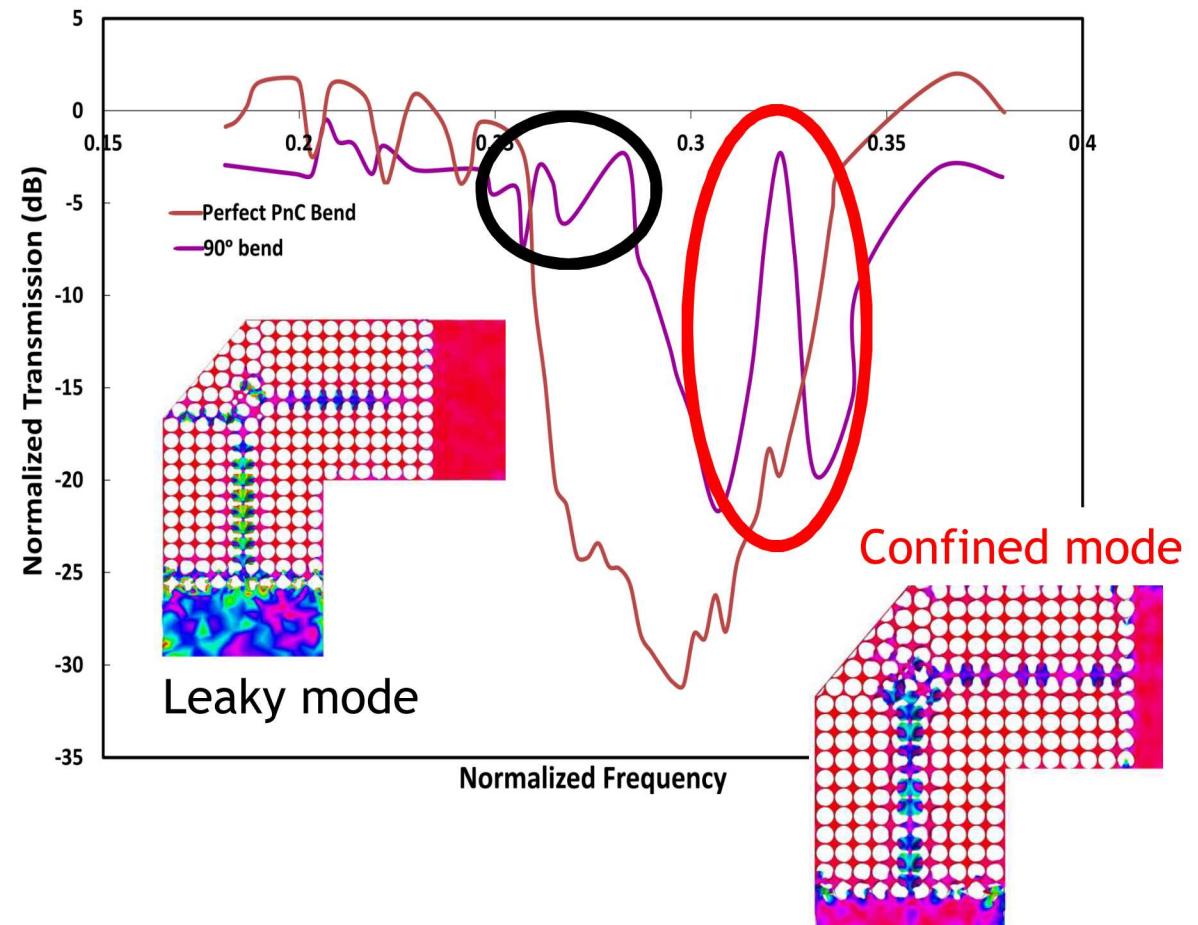


- A 90° bent waveguide was designed and fabricated with  $\alpha = 0.1$ 
  - Lattice was slightly perturbed in the bend region by the introduction of reduced-size holes
  - The size of the small holes were chosen to maintain the critical dimension (minimum hole separation distance)
  - A 45° chamfer angle was introduced at the outer edge of the bend



# PnC Bent Waveguide Design

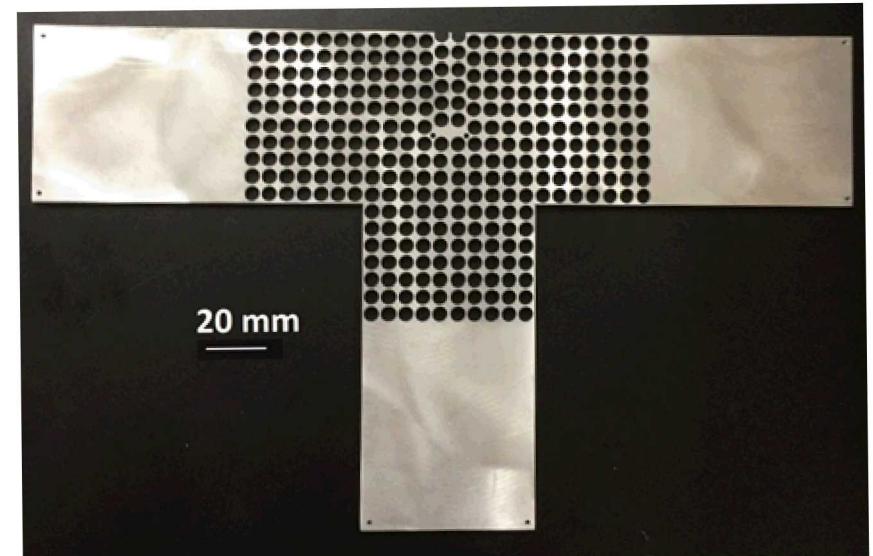
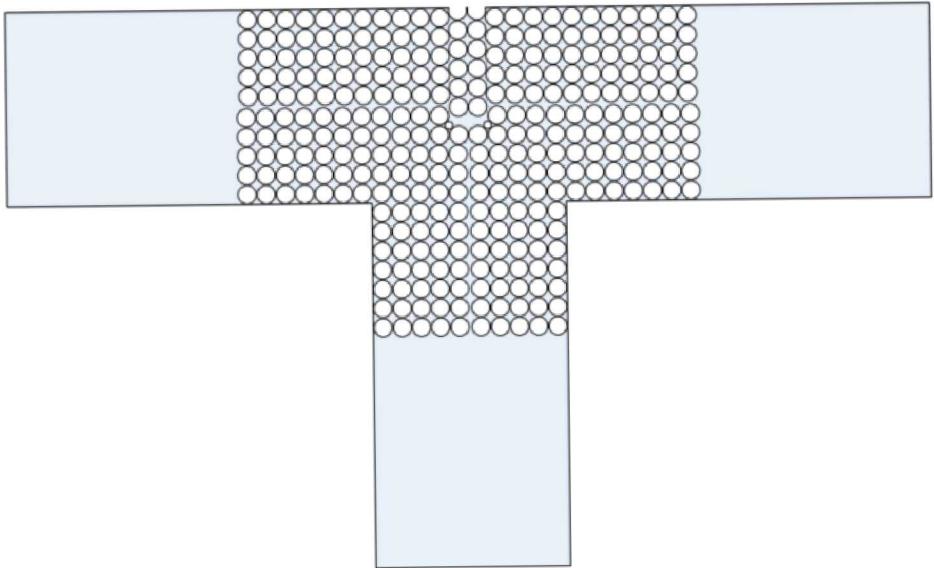
- Similar to the straight waveguide, the lower-frequency mode is not well-localized and mostly reflects back into the input
- The **higher-frequency mode** at  $\Omega=0.32$  is well-localized
  - The incident wave propagates couples efficiently in the perpendicular direction.
- Measured transmission coefficient of the bent waveguide = -2.3dB
  - Corresponds to 76% energy transmission efficiency



# PnC T-Splitter Design



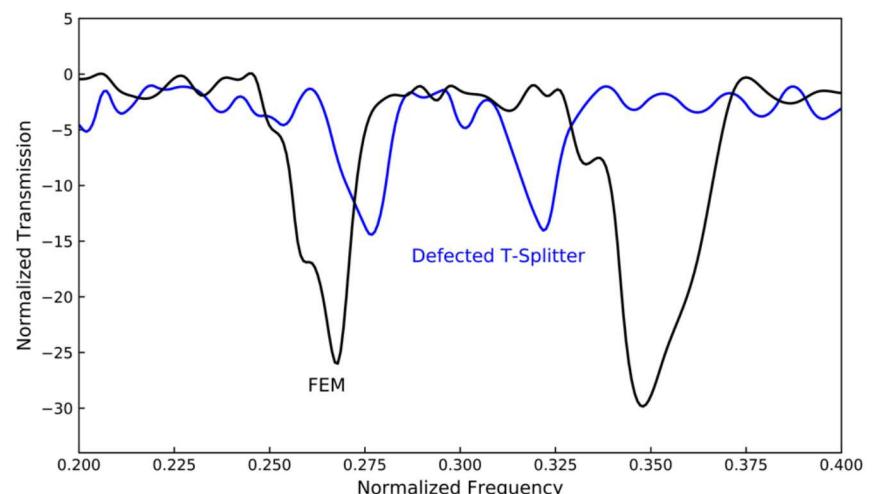
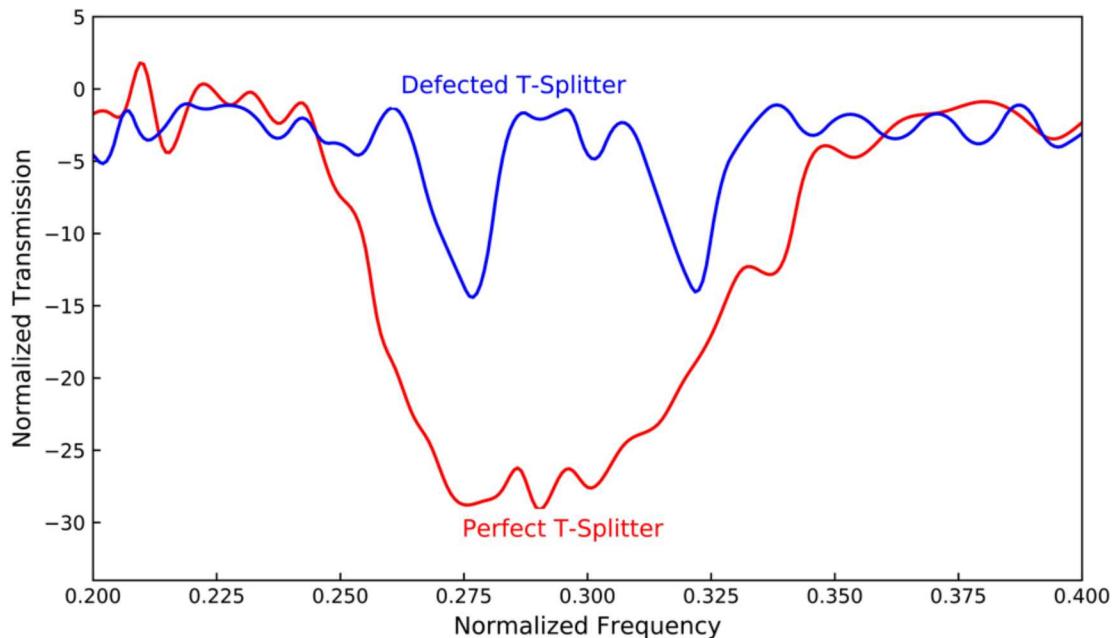
- A “T” splitter waveguide was designed and fabricated with  $\alpha = 0.1$ 
  - Splitting angle is  $180^\circ$
- As with the bent waveguide, the lattice was slightly perturbed in the bend region by the introduction of reduced-size holes
- Waves are excited at the bottom of the device and measured at either of the two output arms



# PnC T-Splitter Design



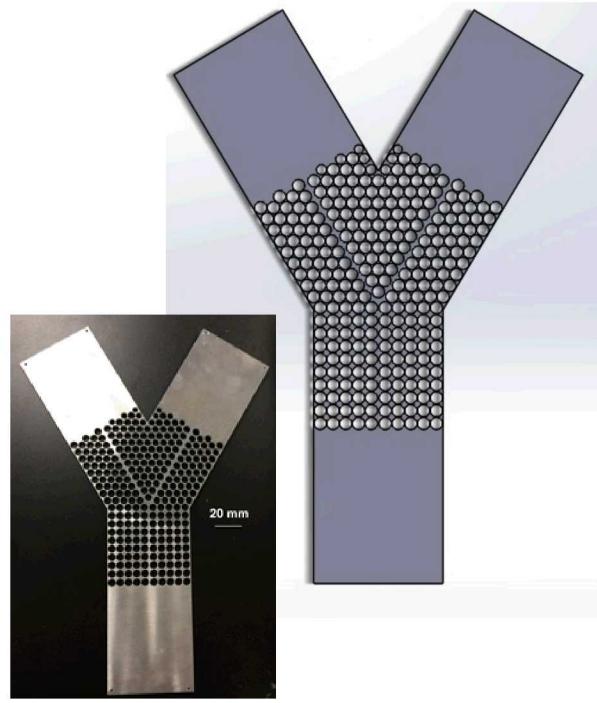
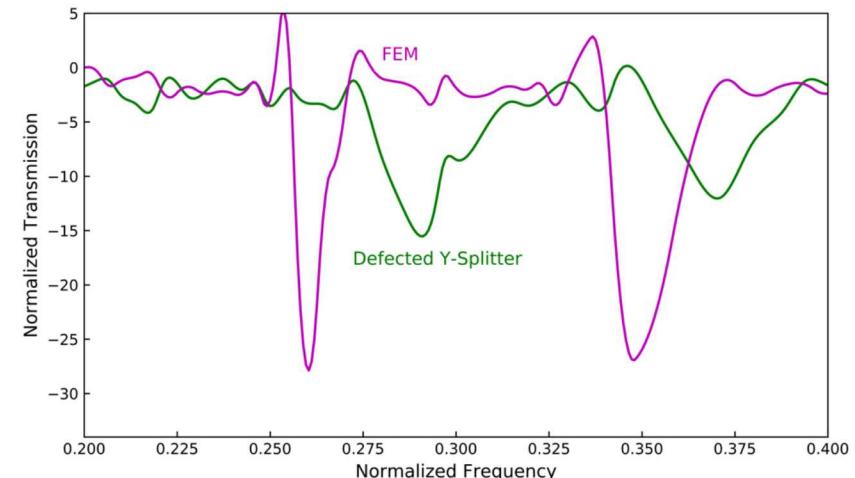
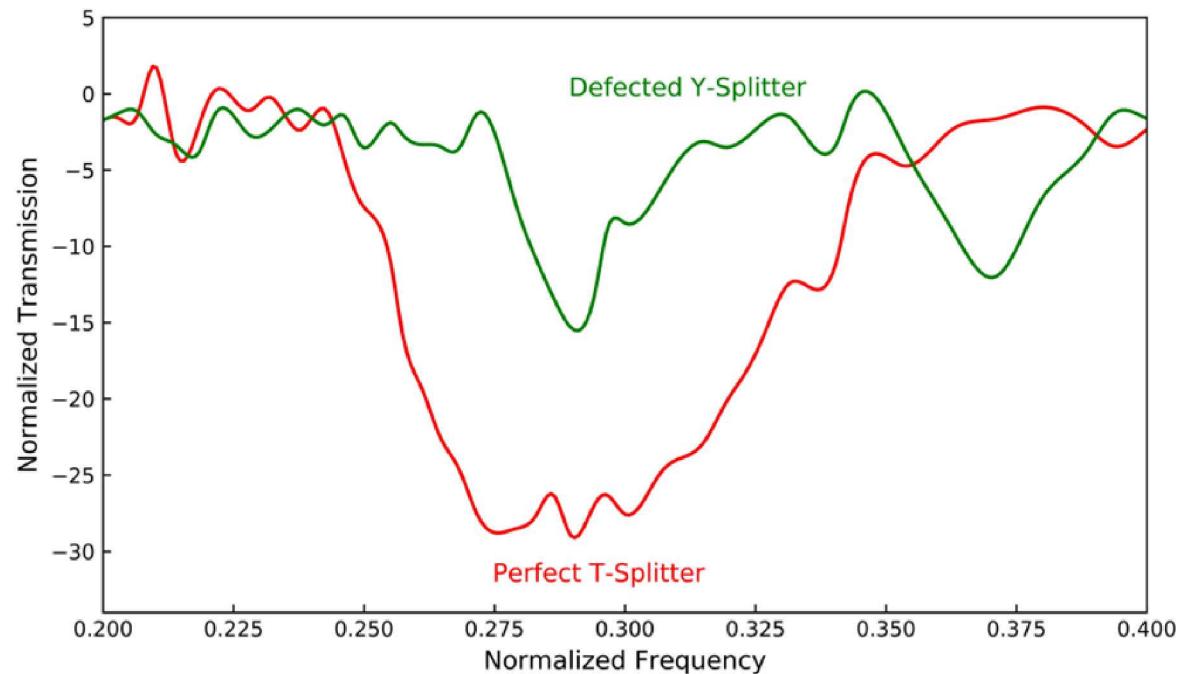
- The splitter shows a passband from 0.28-0.3 in normalized frequency
  - The average transmission is about -3.4dB, which corresponds to 80% energy transmission
- FEM results are in a good agreement with experimental measurement
  - FEM results shows a deeper and wider bandgap, similar to the perfect PnC
  - The bandgap moved slightly due to the change in the PnC lattice



# PnC Y-Splitter Design

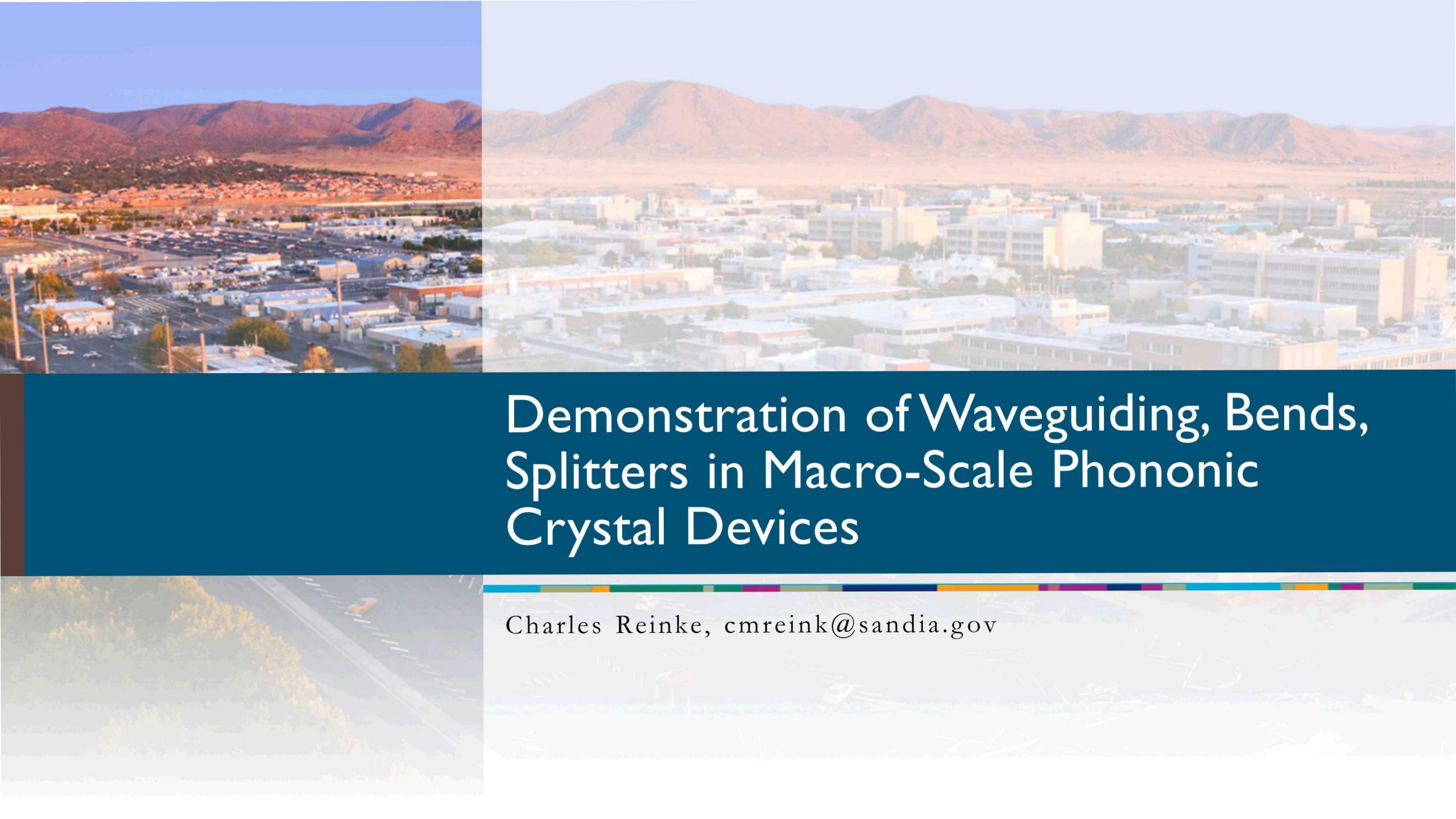


- A “Y” splitter waveguide was also designed and fabricated with  $\alpha = 0.1$
- Lattice is changed from cubic to hexagonal in the splitting region
  - Splitting angle is  $30^\circ$
- Measured average transmission is about  $-2.86\text{dB}$ , which corresponds to 72% energy transmission



## Conclusions

- Well-confined waveguiding can be realized by mode engineering in PnCs
- Transmission as high as 90% in the bent waveguide was demonstrated
- Efficient power splitting was demonstrated in both “T” (180°) and “Y” (30°) splitters
- These designs offers a paradigm based on bulk acoustic waves (BAW) for the design of next generation RF signal processing devices filters



# Demonstration of Waveguiding, Bends, Splitters in Macro-Scale Phononic Crystal Devices

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