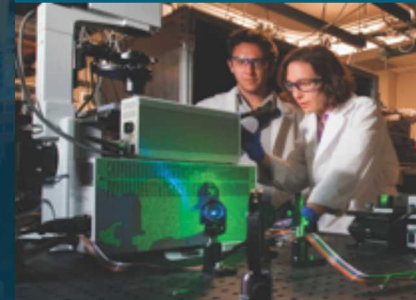


Multiscale modeling to determine the effect of porosity distribution on shocked hexanitrostilbene



Europyro/44th International Pyrotechnics
Society Seminar

Tours, France

June 3-7, 2019

PRESENTED BY

Judith Brown, David Kittell, Mitchell Wood,
Aidan Thompson, Dan Bolintineanu

June 5, 2019



❖ Introduction

❖ Synthetic Microstructure Generation

❖ Continuum Hydrocode Simulations (CTH)

- ❖ Temperature distribution statistics for many microstructures

❖ Molecular Dynamics Simulations (LAMMPS)

- ❖ High-fidelity study of particular microstructures

❖ Conclusions & Future Work

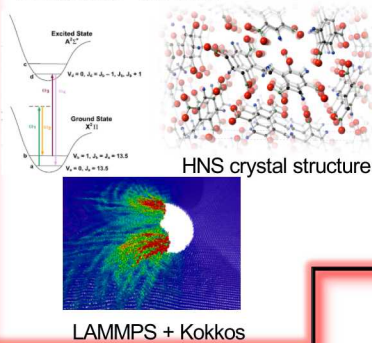
3 Shock Initiation of Explosives at Sandia



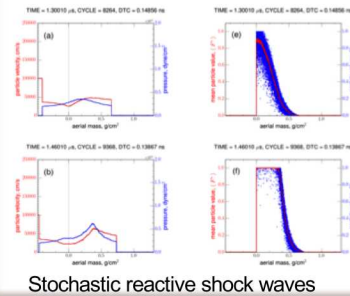
Generate a high fidelity baseline



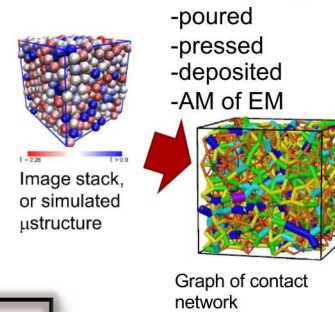
Quantum / MD Large Scalable Codes



New Continuum Codes



Formation Modeling

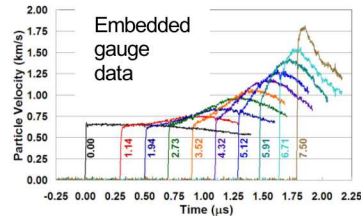


Images from SAND2018-4593PE
(J. Lechman and D. Bolintineanu)

Objective: Science-based engineering and design of new explosive components

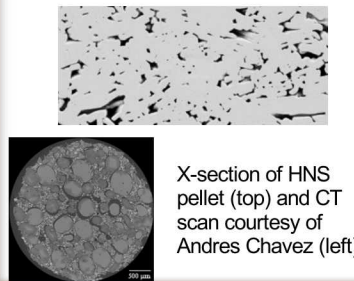
Tests and Experiments

- Performance
- Sensitivity
- Threshold and UQ

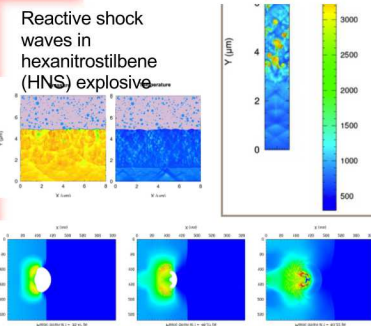


Burns *et al.* J. Appl. Phys. (2012)

Microstructural Analysis



Mesoscale Simulations



Adapt/remove approximations to agree with MD

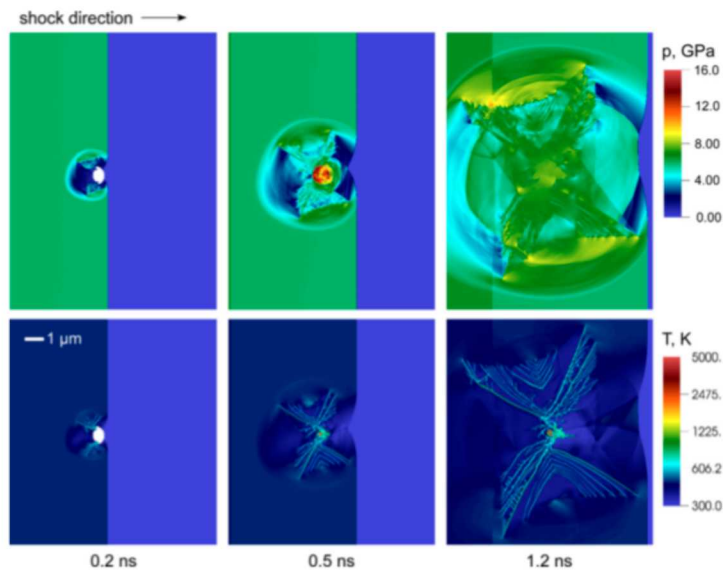


Role of Porosity in Shock Initiation

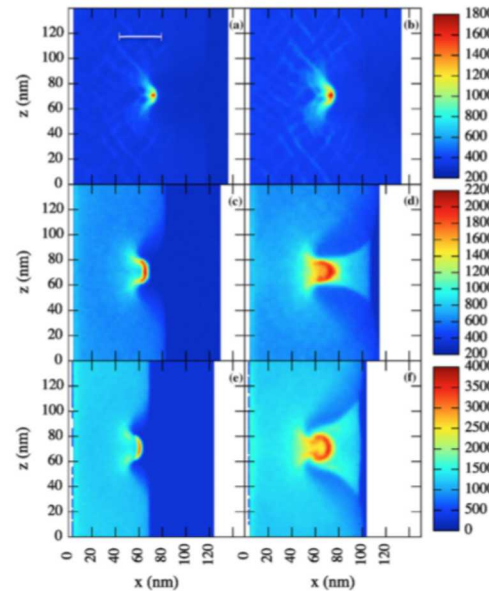


- ❖ Some degree of porosity present in almost all energetic materials
- ❖ Pore collapse can be key mechanism for hot spot formation

Many Single-Pore Collapse Studies



Austin et. al, J. App. Phys. 117 (2015), 185902



Eason and Sewell, J. Dynamic Behavior Mater. 1 (2015), 423-438

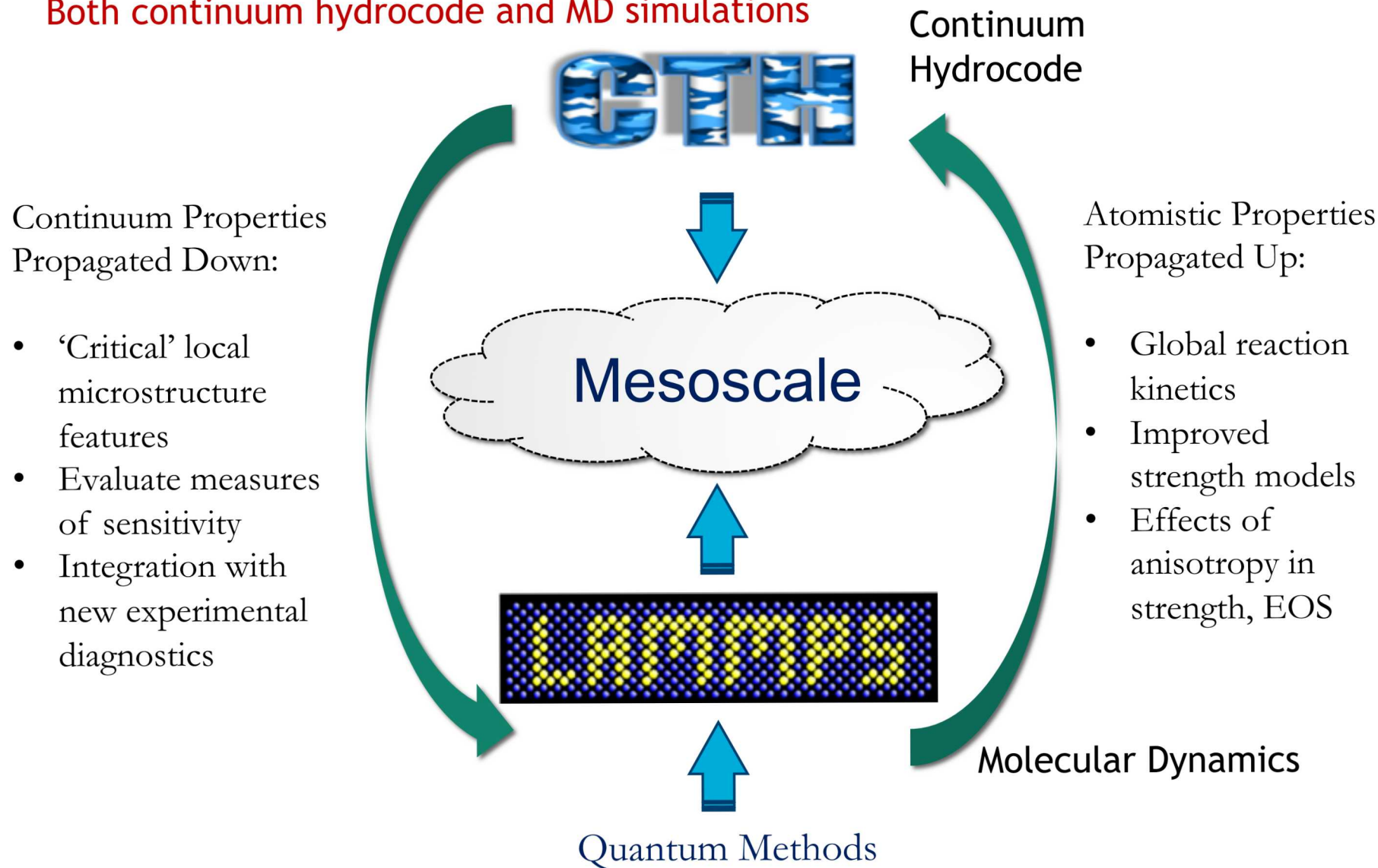
What about pore interactions?

- ❖ Can we link particular porosity configurations/geometries with some metric of likelihood for hot spot formation??
- ❖ Use Multiscale approach with both continuum hydrocode and MD simulations to explore this

5 Multiscale Approach



Both continuum hydrocode and MD simulations



6 Microstructure of Pressed Hexanitrostilbene

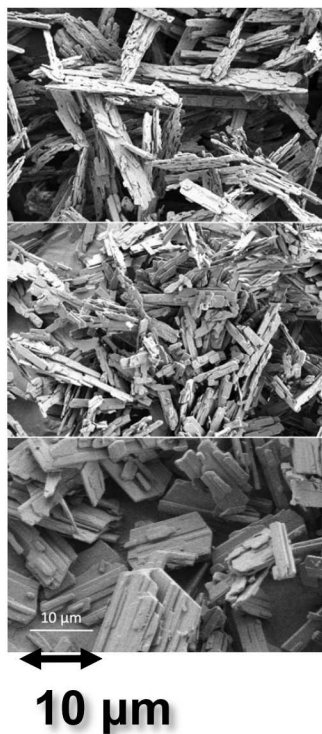


❖ HNS-IV powder pressed to 72 – 92% TMD

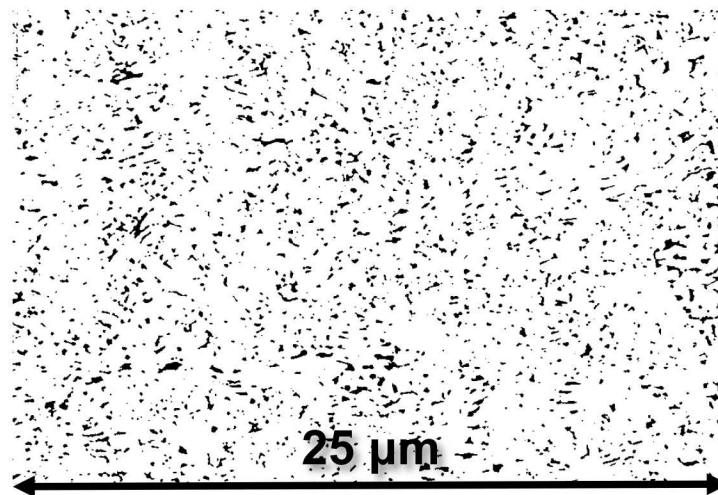
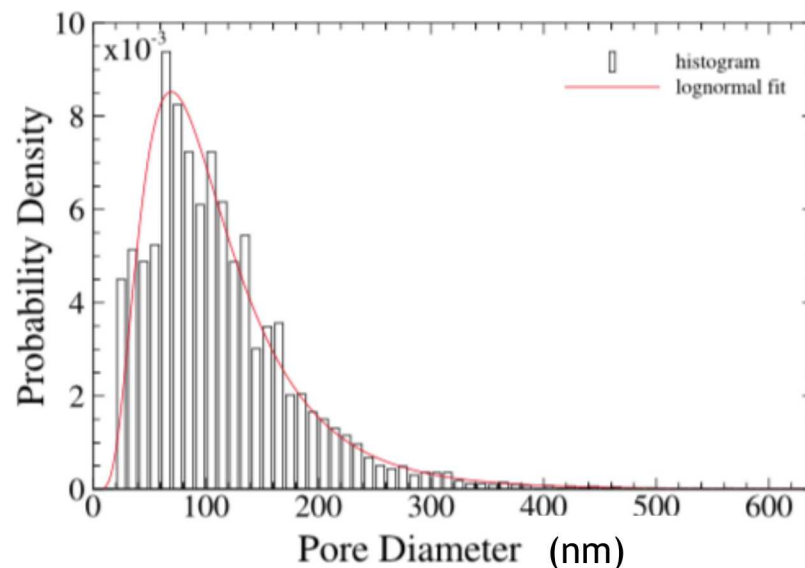
HNS-IV
Lot 1

HNS-IV
Lot 2

HNS-I



Thresholded SEM
image of pressed
microstructure



7 Synthetic Microstructure Generation

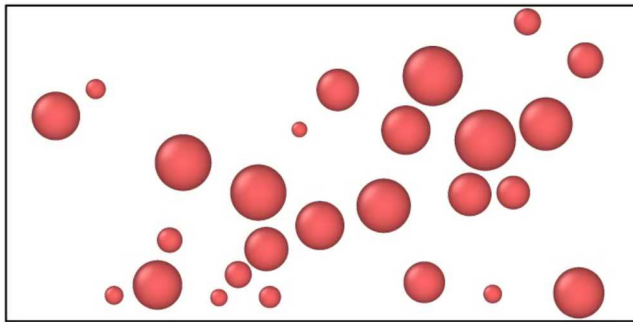


❖ 2D Discrete Element Method (DEM) simulations used to generate many microstructures with different porosity configurations

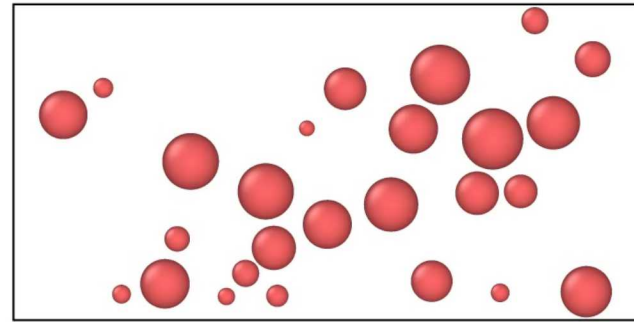
Initial state: spheres placed at random in 250 X 500 nm domain, no overlaps

Langevin dynamics with range of contact cohesion values:

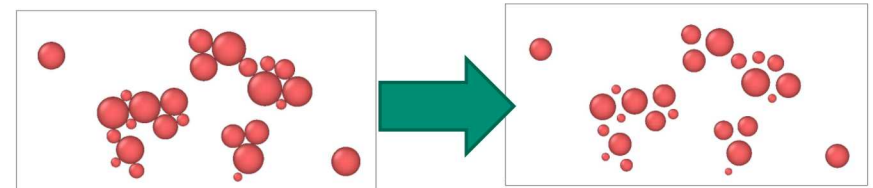
Low cohesion



High cohesion

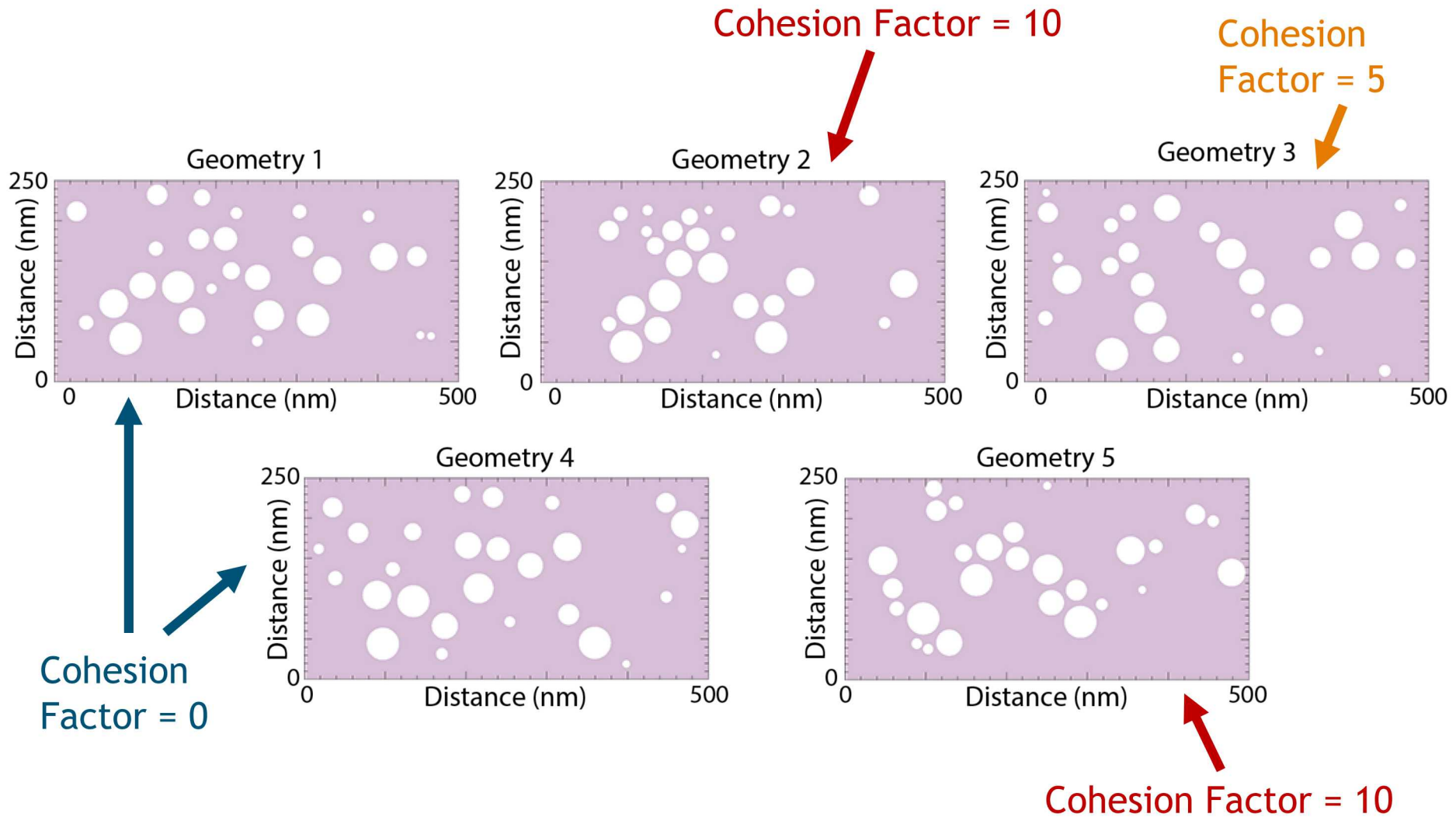


Final step: shrink particles uniformly to generate final configuration



Variations: Particle size distribution, TMD, cohesion, friction, random seed

Example Synthetic Microstructures



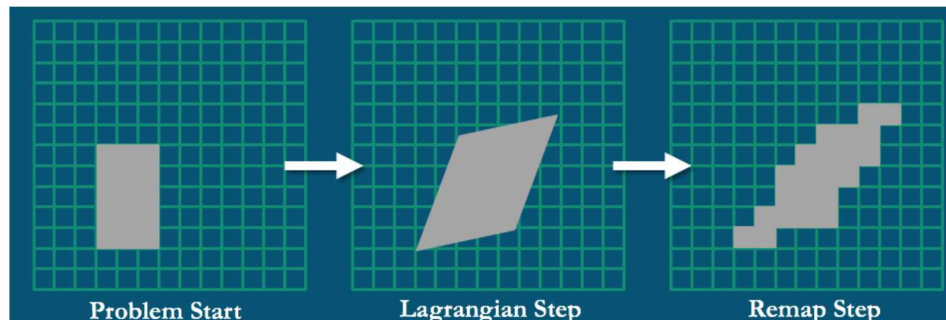
9 Continuum Hydrocode Simulations—CTH



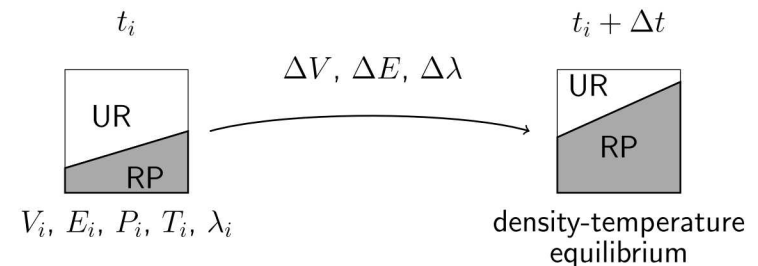
❖ CTH—3D, large deformation, multi-material shock physics hydrocode developed at Sandia National Laboratories

Mass	$\frac{d\rho}{dt} = -\rho \nabla \cdot \vec{V}$
Momentum	$\rho \frac{d\vec{V}}{dt} = -\nabla P - \nabla \cdot [\boldsymbol{\sigma} + \mathbf{Q}(\vec{V}, c_s)]$
Energy	$\rho \frac{dE}{dt} = -P \nabla \cdot \vec{V} - [\boldsymbol{\sigma} + \mathbf{Q}(\vec{V}, c_s)] \cdot \nabla \vec{V}$

Lagrangian and remap solution steps as they appear in CTH



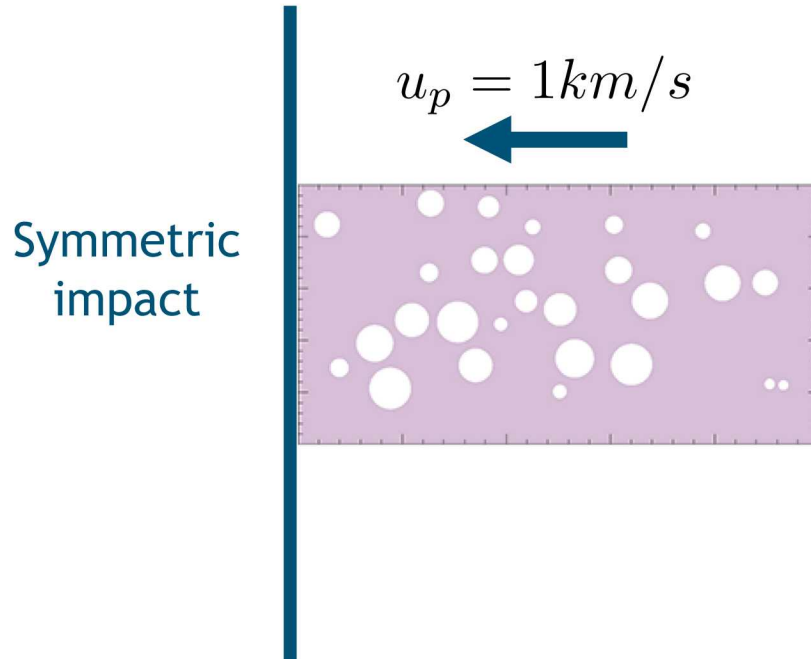
Density-temperature equilibrium for reactive burn models



Continuum Hydrocode Simulations—CTH



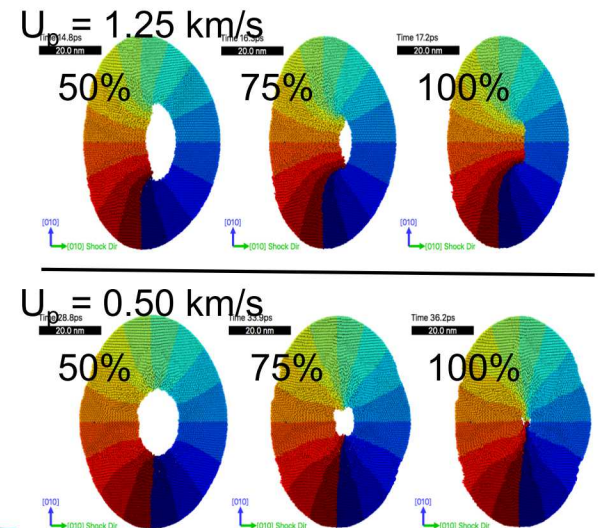
- ❖ Reverse ballistic impact calculation
- ❖ Evaluate large number of microstructures to elucidate geometries that show higher propensity for hot spot formation



Material Models

- ❖ Pores treated as void
- ❖ HNS matrix:
 - ❖ Mie-Grüneisen equation of state
 - ❖ Stienberg-Guinan-Lund viscoplastic strength model

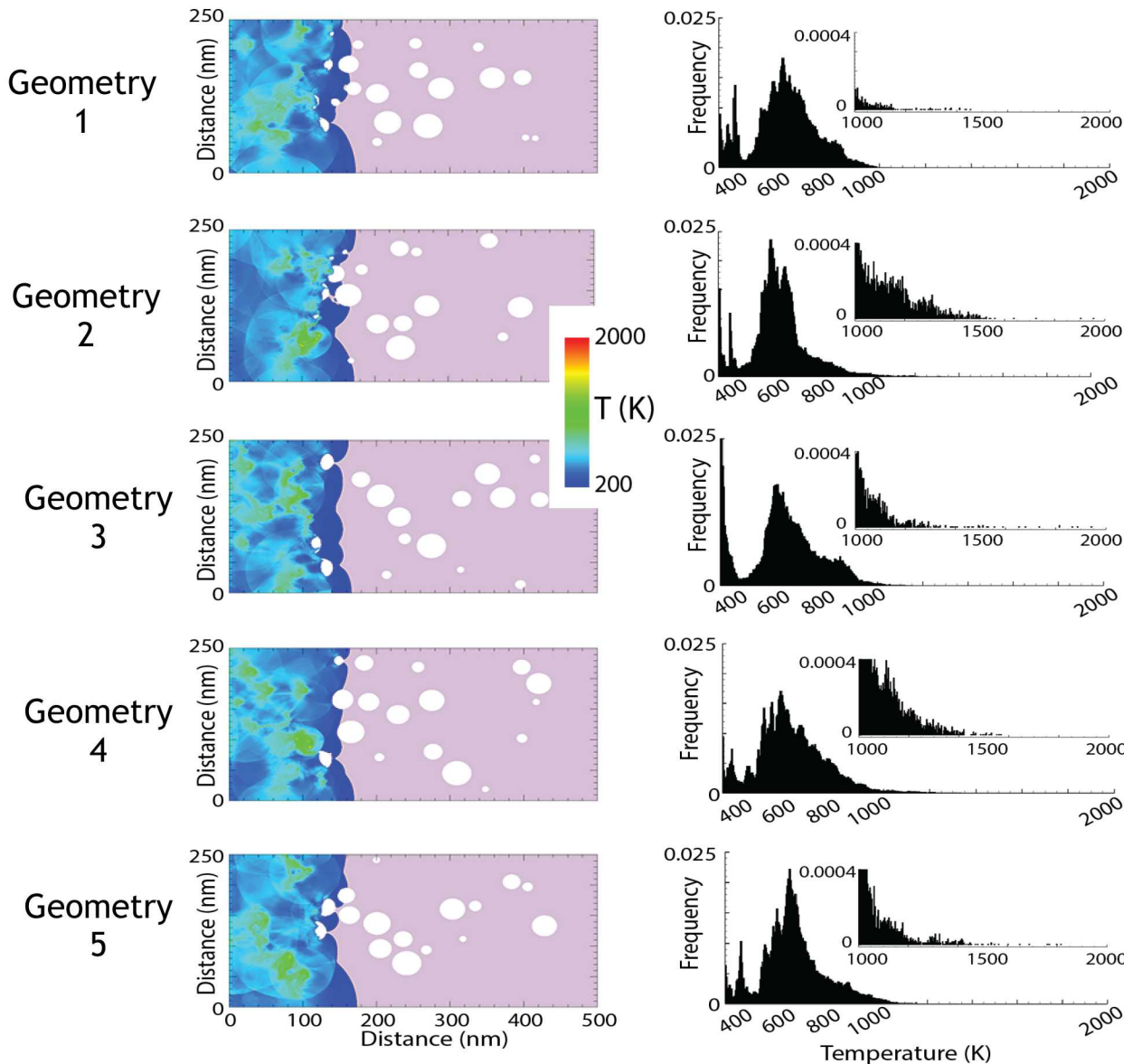
Single-pore collapse rate was used to calibrate SGL model from MD simulations



11

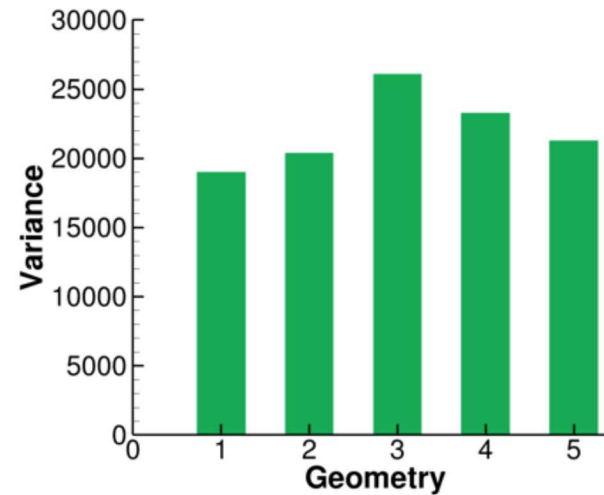
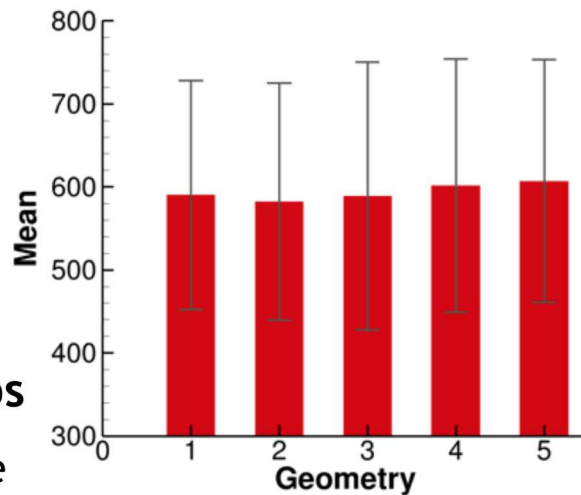


Time = 50 ps



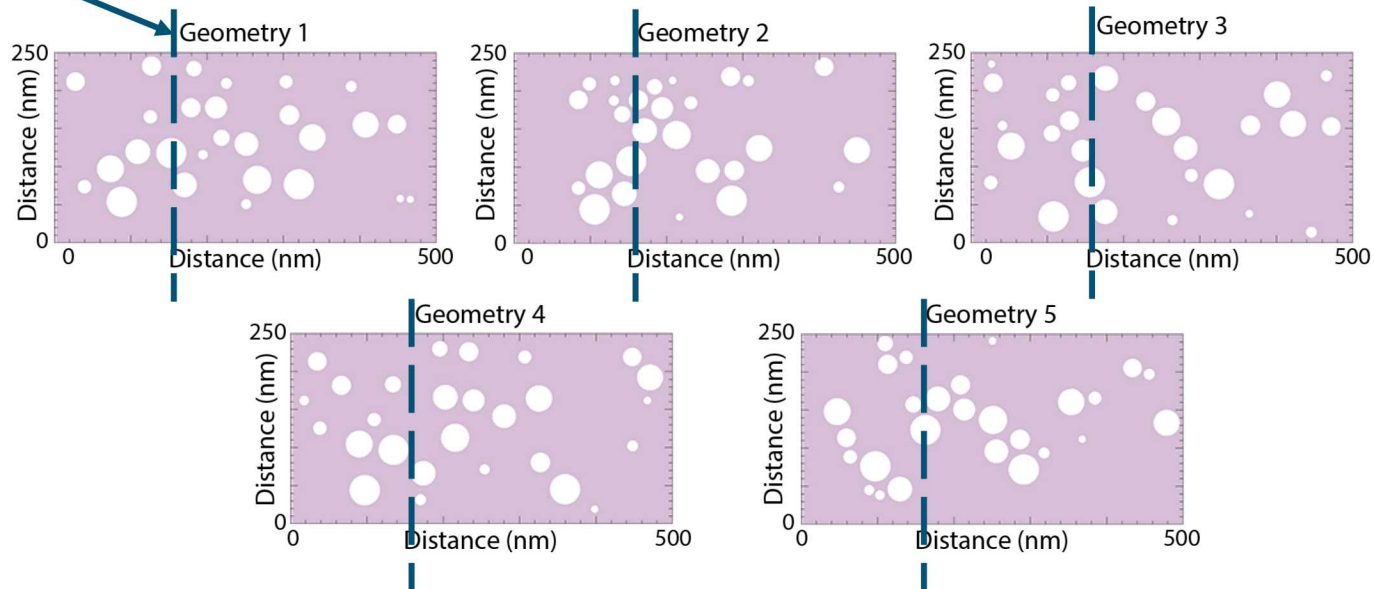
- ❖ Non-planar shock front due to multiple pore interactions
- ❖ Temperature histogram for each microstructure provides unique “fingerprint” at a given instant in time
- ❖ Most common temperature close to $T_H = 581 \text{ K}$
- ❖ Outlier temperatures $> 1000 \text{ K}$

Mean Temperatures Independent of Geometry

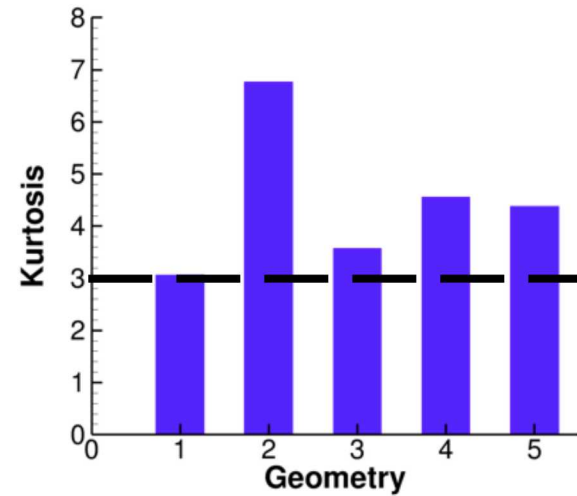
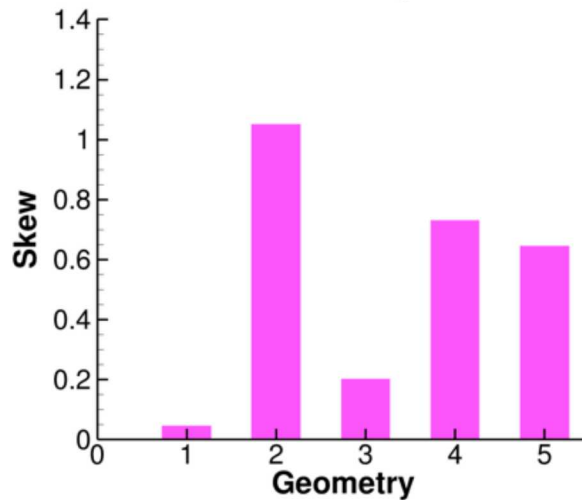


Time = 50 ps

Approximate
shock wave
position



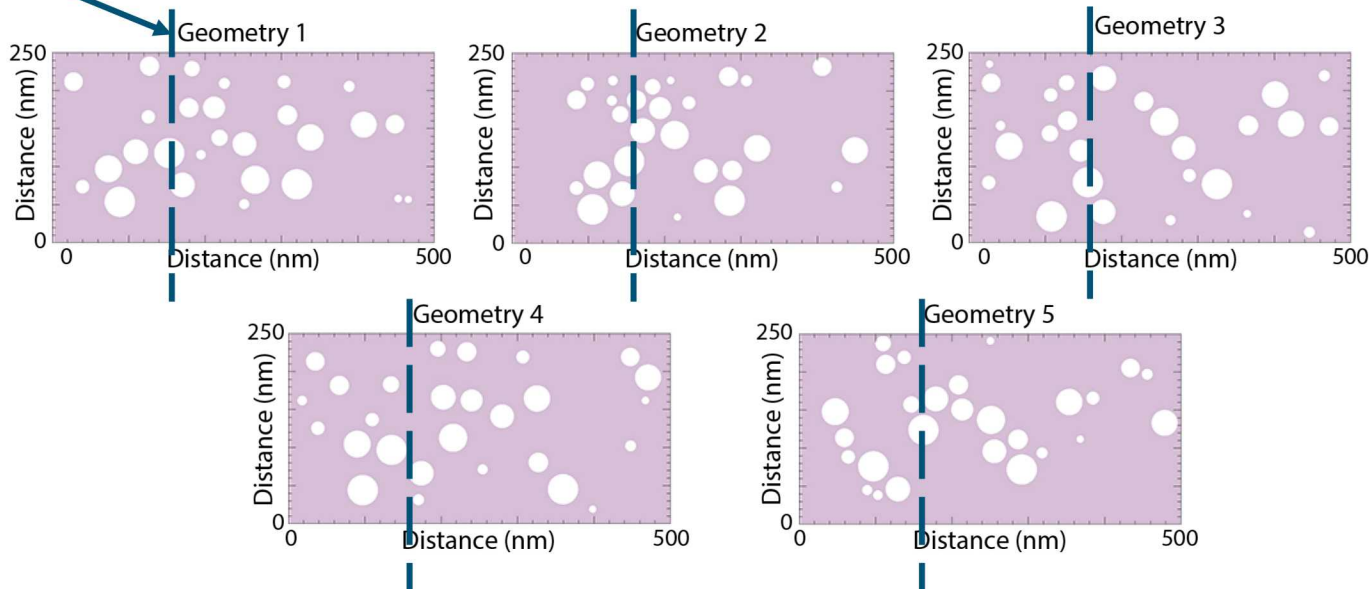
Hot Spots Related to Temperature Outliers



Gaussian
Distribution
Kurtosis = 3

Time = 50 ps

Approximate
shock wave
position

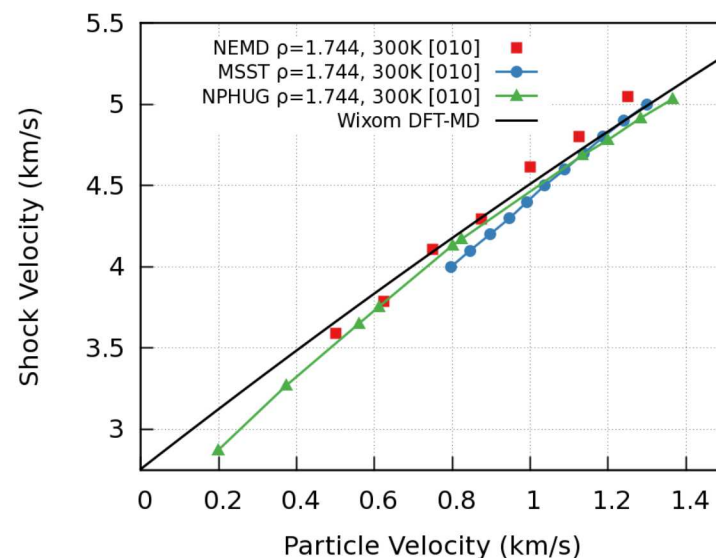
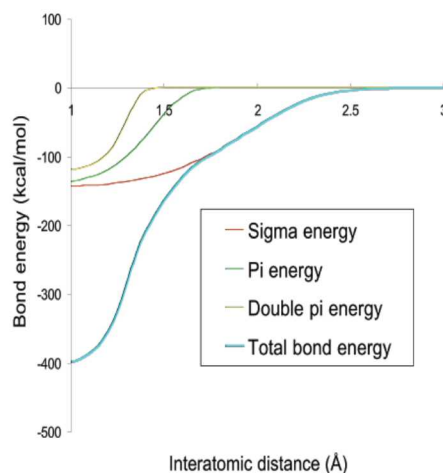
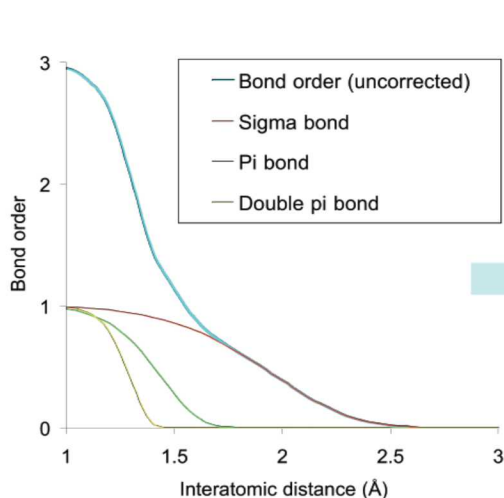


Molecular Dynamics Simulations



❖ Use MD simulation to gain more physical insight into highly clustered microstructure configurations

ReaxFF Interatomic Potential  Detailed chemistry is incorporated in these MD potentials, hot spot evolution is captured naturally



Chenoweth, van Duin and Goddard, J. Phys. Chem. A, 112, 1040-1053 (2008)

Strachan *et al.* J. Chem. Phys. 122, 054502 (2005)

Castro-Marciano *et al.* Combustion and Flame 159(3) 1272-1285 (2012)

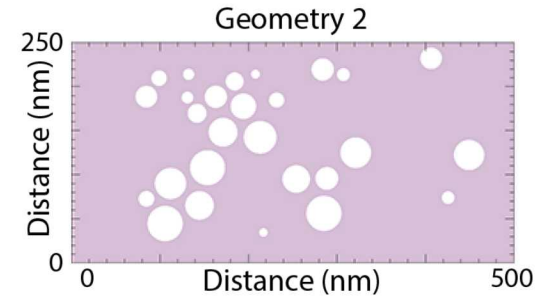
Wood, van Duin, Strachan, J. Chem. Phys. A 118, 885 (2014)

Rappe and Goddard, J. Phys. Chem 1991, 95, 3358-3363

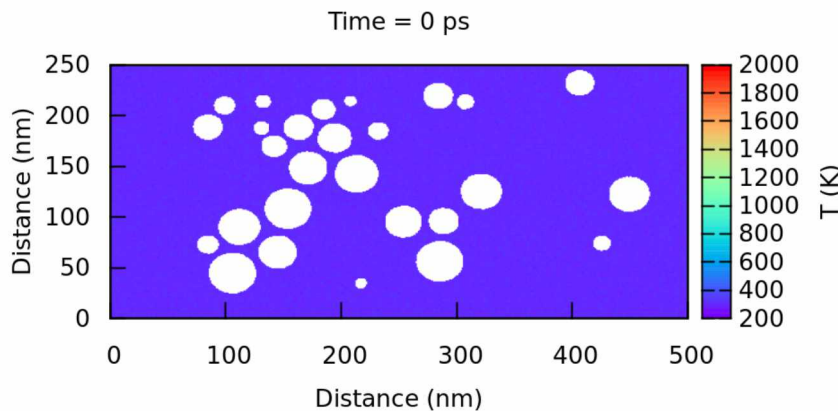


❖ Geometry 2:

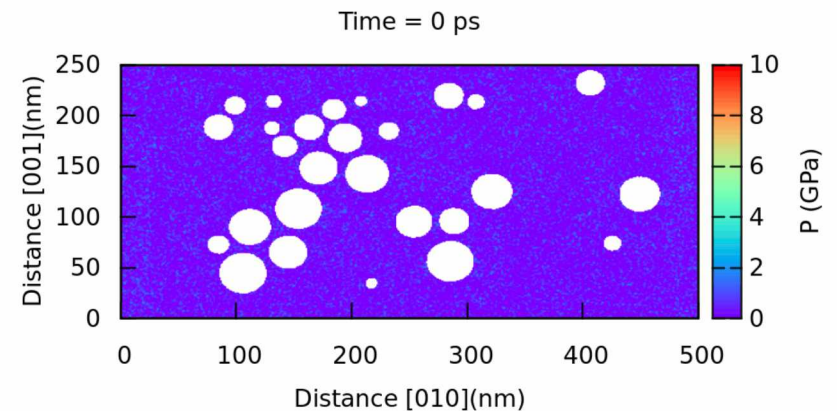
- ❖ Large pore cluster between 100-200 nm
- ❖ Temperature distribution with high skew and kurtosis



Temperature (K)



Pressure (GPa)

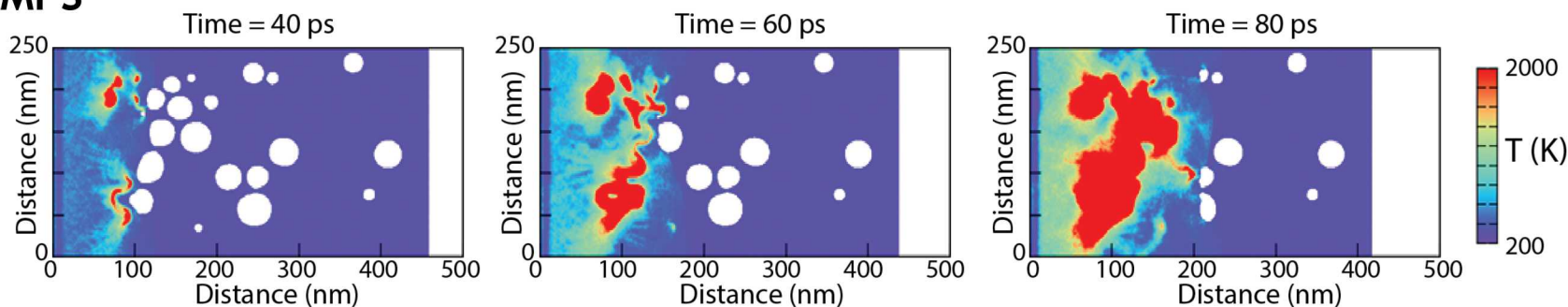


Comparison of MD vs CTH with reaction

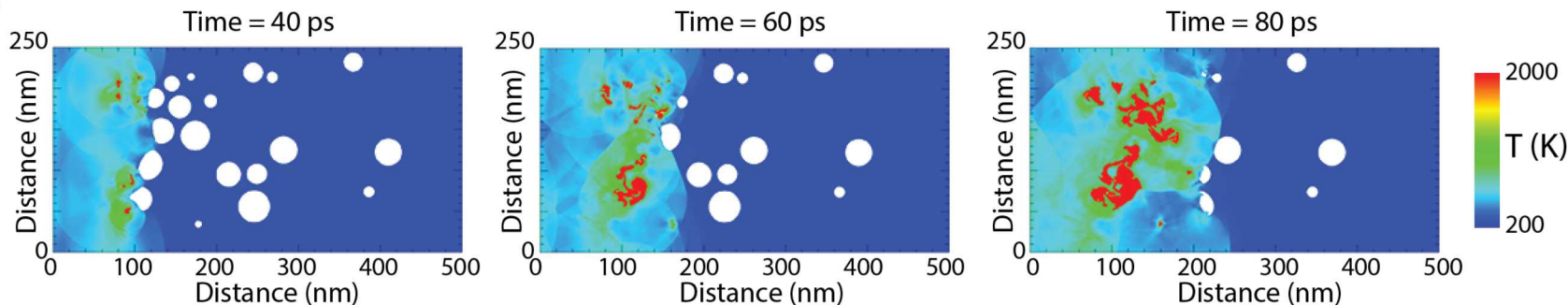


- ❖ Good qualitative agreement in spatial temperature fields
- ❖ Shock wave front well resolved in both codes
- ❖ Temperature magnitude in reacting areas higher in MD

LAMMPS



CTH





- ❖ Skew and kurtosis of instantaneous temperature distribution provide information of how many high temperature outliers are present
 - ❖ May be good indicator for hot spots
- ❖ Pore clustering seems to be a driver for more high temperature outlier events
- ❖ Evolution of temperature distribution with time is a complex function of chemistry and microstructure features

Future Work

- ❖ Characterize evolution of statistical metrics over time
- ❖ Better quantitative match of temperature predictions between MD and CTH



Thank You!

19 Time-Evolution of Temperature Distributions



CTH Conservation Equations



❖ Real material behavior comes from an **accurate equation-of-state (EOS)** plus a **constitutive model** with parameters fit to the appropriate, dynamic regime.

- ❖ spherical part is the equation of state $P = f(\rho, E)$
- ❖ deviatoric part is the constitutive model $\boldsymbol{\sigma} = f(\text{strain}, \dots)$
- ❖ numerical part is the artificial viscous stress $\mathbf{Q} = f(\text{velocity and } c_s)$

Mass $\frac{d\rho}{dt} = -\rho \nabla \cdot \vec{V}$

Momentum $\rho \frac{d\vec{V}}{dt} = -\nabla P - \nabla \cdot [\boldsymbol{\sigma} + \mathbf{Q}(\vec{V}, c_s)]$

Energy $\rho \frac{dE}{dt} = -P \nabla \cdot \vec{V} - [\boldsymbol{\sigma} + \mathbf{Q}(\vec{V}, c_s)] \cdot \nabla \vec{V}$

$$-\mathbf{S} = P\mathbf{I} + \boldsymbol{\sigma} + \mathbf{Q}(\vec{V}, c_s)$$

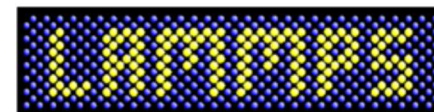
Stress Tensor

Spherical
Part

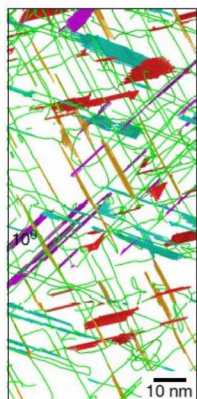
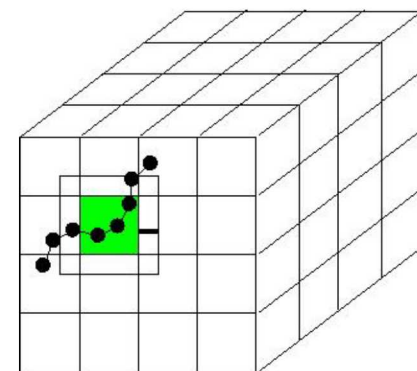
Deviatoric
Part

Artificial
Viscosity

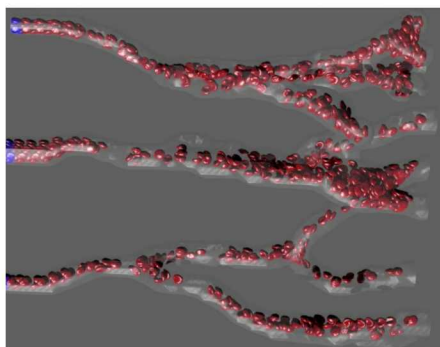
What is LAMMPS?



- Large-scale Atomical/Molecular Massively Parallel Simulator
<http://lammps.sandia.gov>
- Open source, highly portable C++, free under GPL license
- Well documented with many examples, easily extendable for user specific needs
- Variety of boundary conditions, constraints, ensemble sampling methods etc.
- Parallelism through spatial decomposition of simulation domain
- Short and long ranged interactions allowed/included
- CPU cost is (N/P) and communication is $(N/P)^{2/3}$

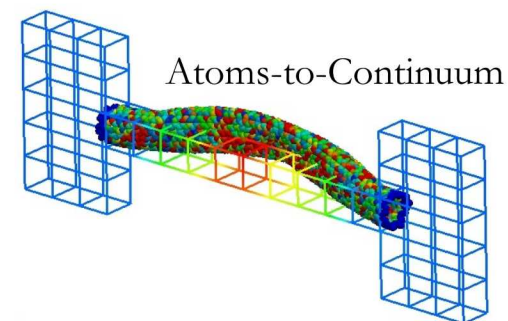
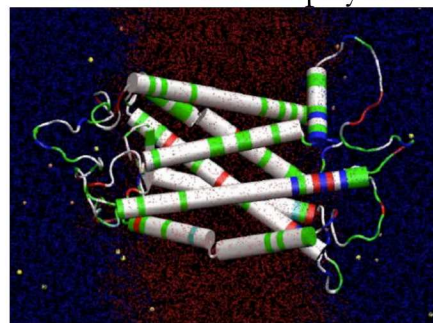


Dislocations in Materials

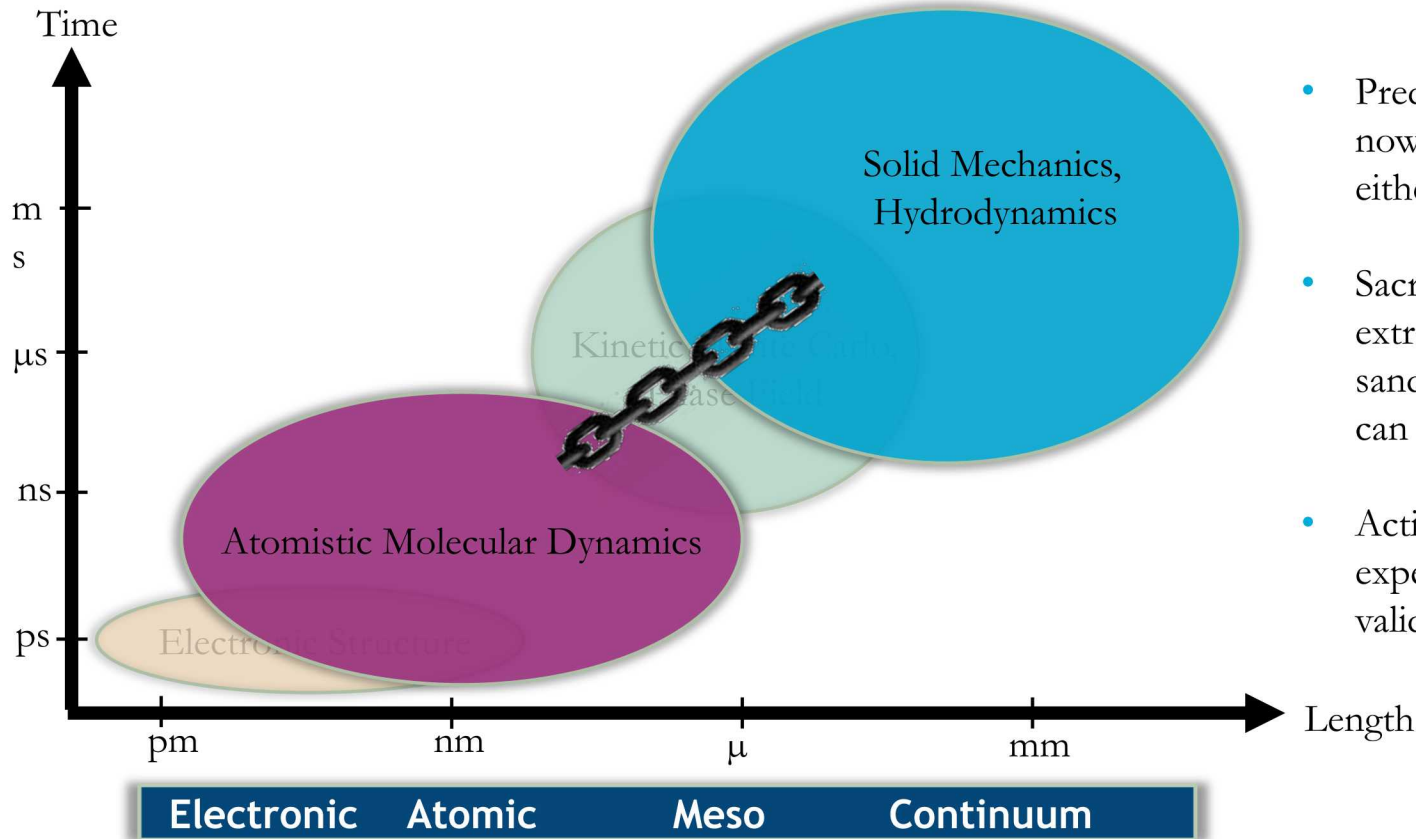


Blood Flow

Proteins and Biophysics

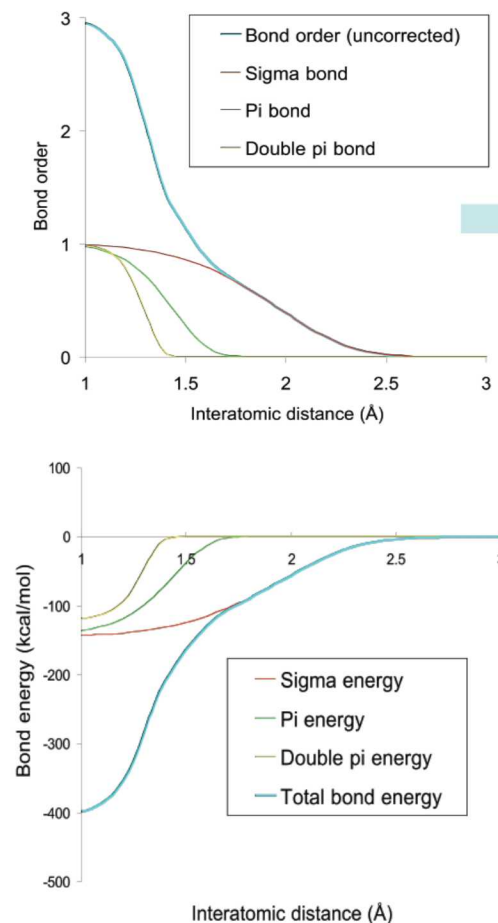
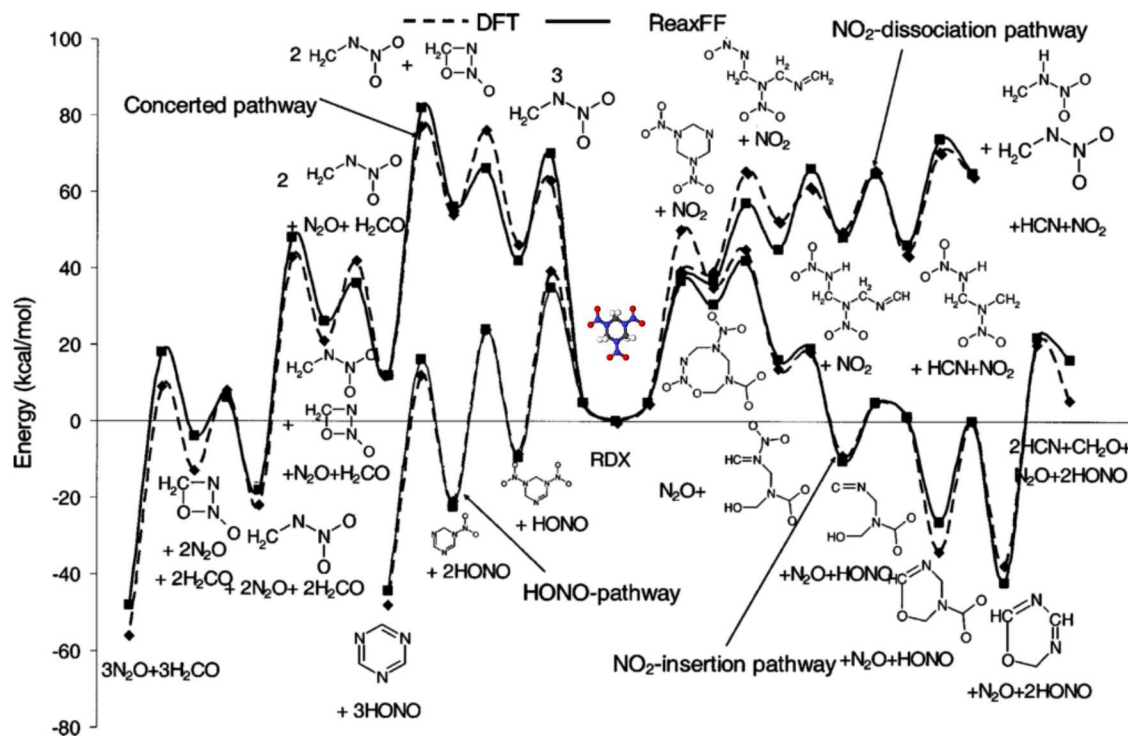


Atoms-to-Continuum



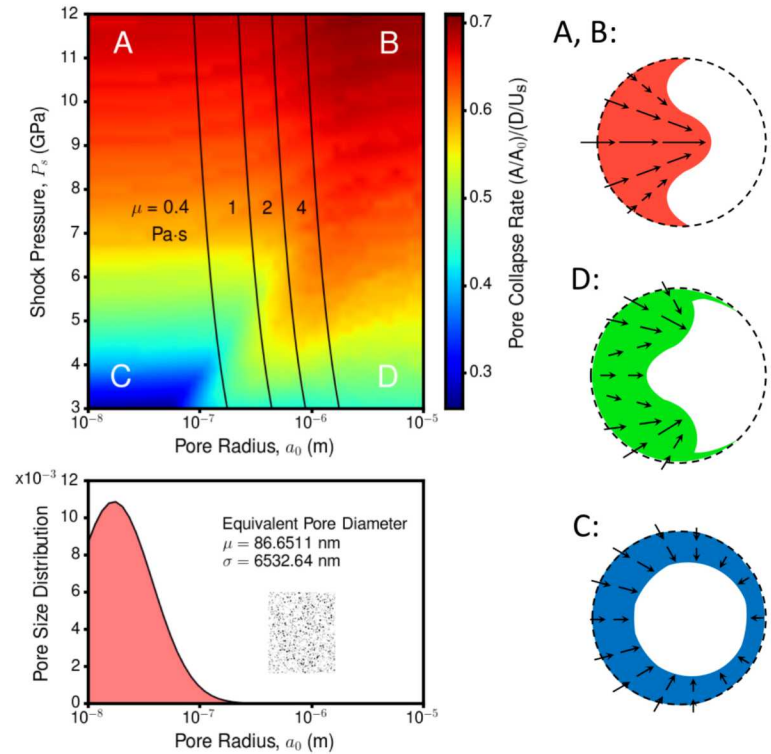
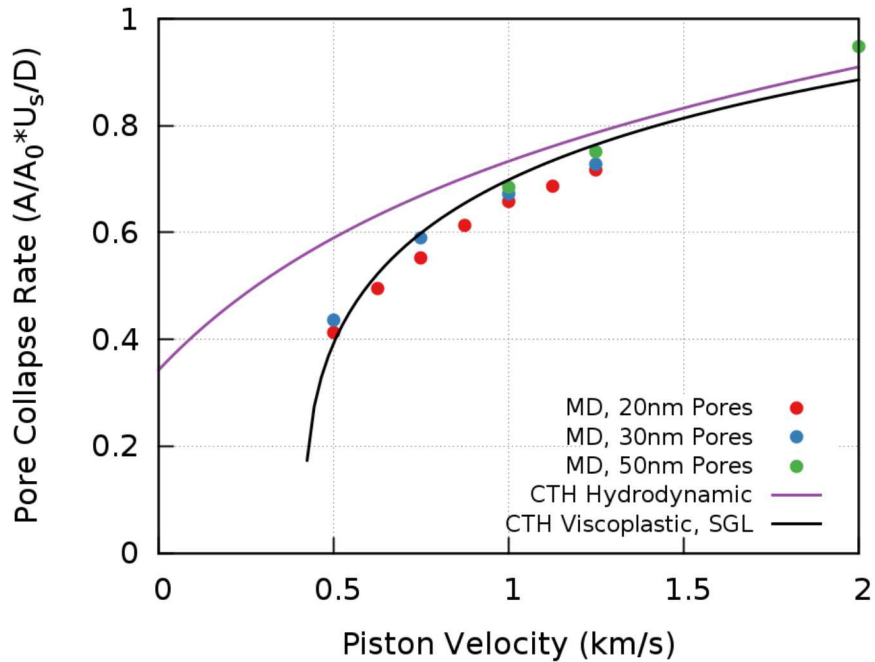
- Predictions at the mesoscale now share approximations of either model
- Sacrificed some ability to extrapolate, but have built a sandbox reality where much can be learned
- Actively looking for experimental integration as validation

Reactive Potentials in MD (the approximation)



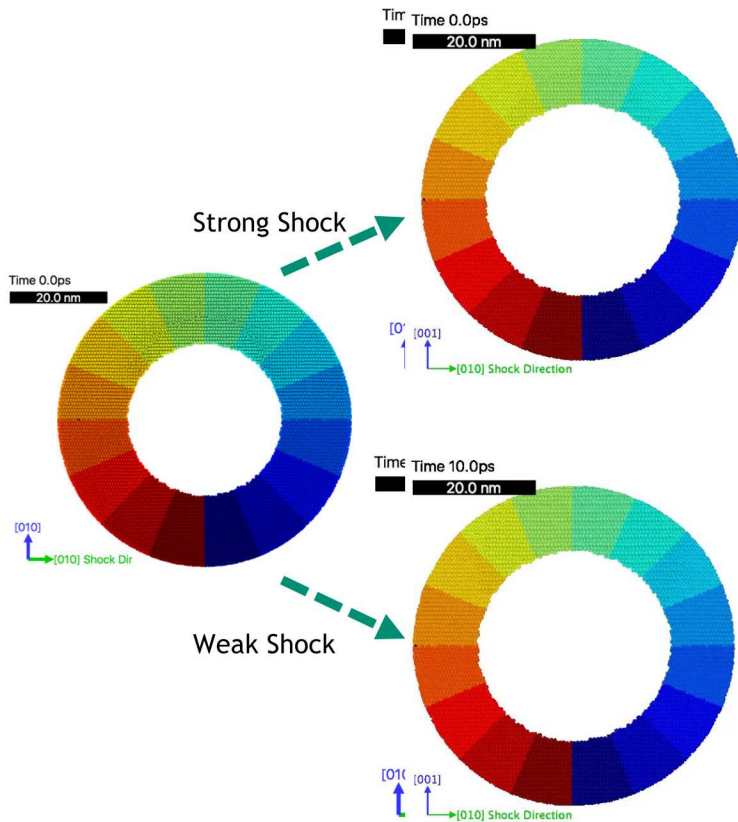
Chenoweth, van Duin and Goddard, J. Phys. Chem. A, 112, 1040-1053 (2008)
 Castro-Marciano *et al.* Combustion and Flame 159(3) 1272-1285 (2012)
 Rappe and Goddard, J. Phys. Chem 1991, 95, 3358-3363

Strachan *et al.* J. Chem. Phys. 122, 054502 (2005)
Wood, van Duin, Strachan, J. Chem. Phys. A 118, 885 (2014)

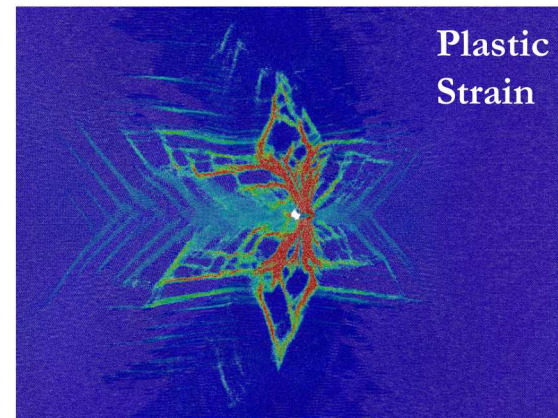
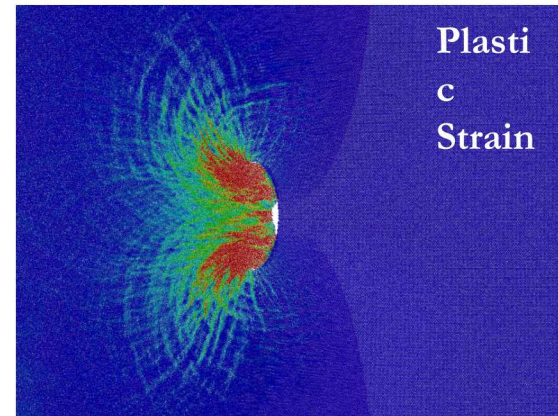


- Training data of collapsing pores from MD sent to CTH for strength model parameterization

Is the MD Model Useful?



OVITO : A. Stukowski, *Modelling Simul. Mater. Sci. Eng.* 18 (2010), 015012

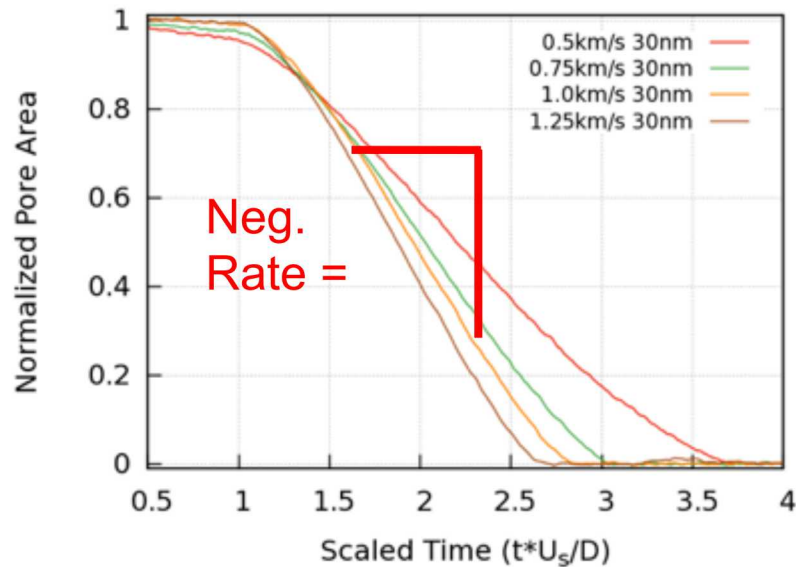




Metrics Passed from MD to CTH

Training Metric

- Collapse rate is used to calibrate strength models in CTH

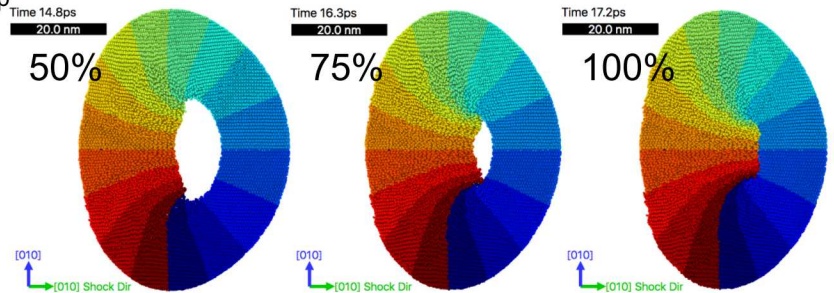


Quantitative post-processing was done using the OVITO code [10]

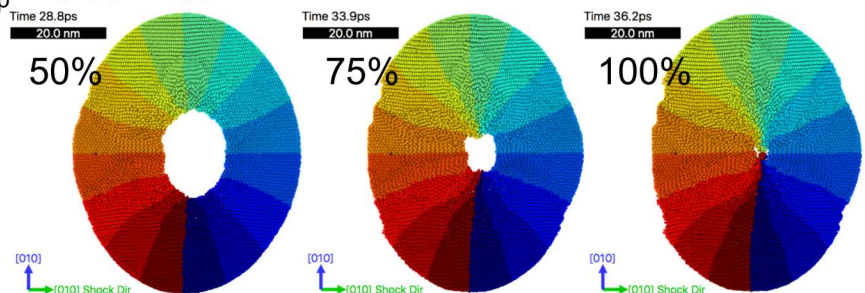
Comparison Metrics

- Radial distribution of plastic strain
- Temperature histograms
- Etc.

$U_p = 1.25 \text{ km/s}$



$U_p = 0.50 \text{ km/s}$



CTH Strain Rate Dependent Model – Steinberg, Guinan and Lund (1988)



- We believe that only a strain rate-dependent model can match MD results for viscoplastic pore collapse; EPPVM and Johnson-Cook are not up to the task.
 - Assume a constant shear modulus
 - Neglect work hardening
 - Assume linear variation of the Grüneisen parameter

Yield Strength:	$Y = \{Y_T(\dot{\epsilon}_p, T) + Y_A f(\epsilon_p)\}$
-----------------	--

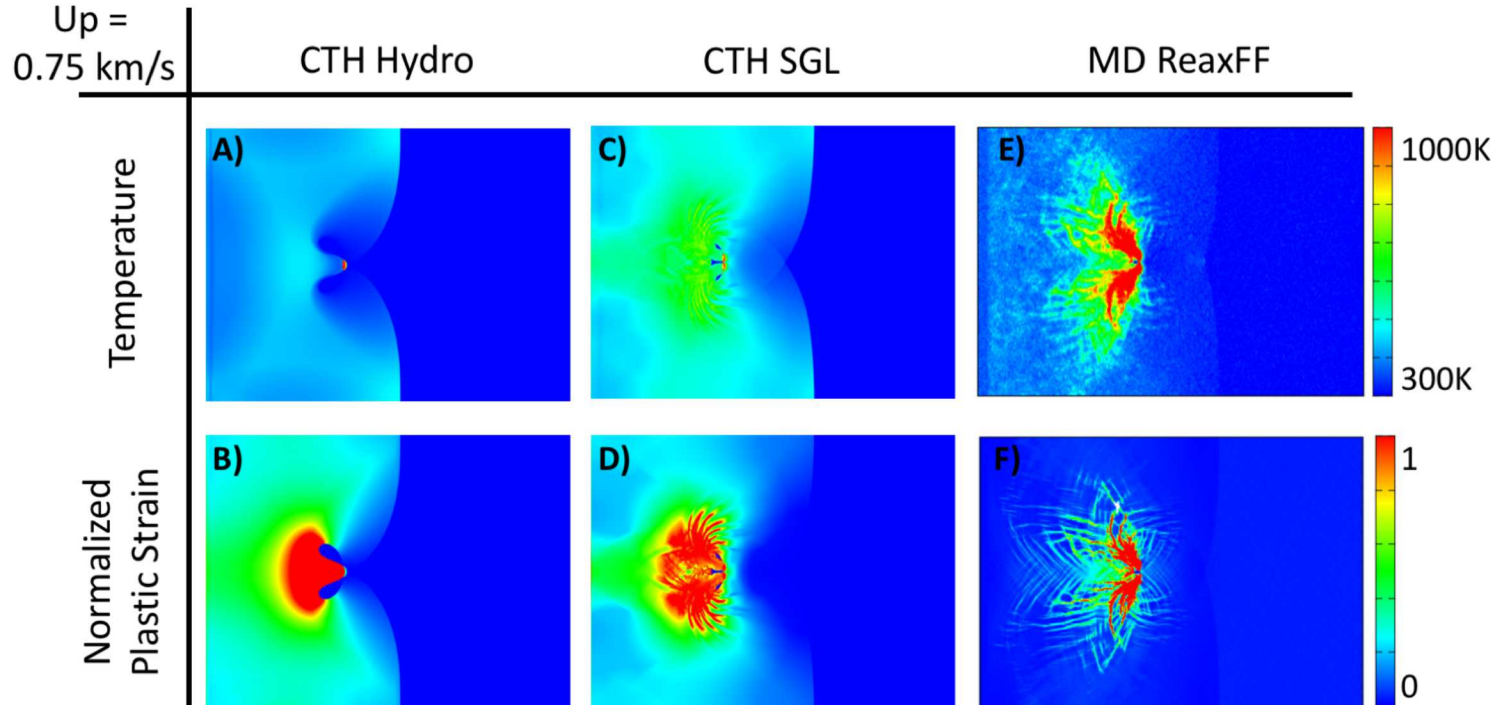
Shear Modulus:	$G(P, T) = G_0$
----------------	-----------------

Thermal Activation: (Implicit Equation)	$\dot{\epsilon}_p = \left\{ \frac{1}{C_1} \exp \left[\frac{2U_K}{kT} \left(1 - \frac{Y_T}{Y_P} \right)^2 \right] + \frac{C_2}{Y_T} \right\}^{-1}$	$Y_T \leq Y_P$
--	---	----------------

Melting Curve: ($Y = 0$ when $T \geq T_m$)	$T_m = T_{m0} \exp \{ 2a(1 - 1/\eta) \} \eta^{2(\gamma_0 - a - 1/3)}$
---	---

Grüneisen parameter:	$\gamma = \gamma_0 / (1 + \mu)$
----------------------	---------------------------------

Much Better Mechanical Agreement



CTH now predicts:

- A much more detailed strain field, viscoplastic deformation
- Correlation between temperature and regions of high strain