

Analytical modelling of propagation velocity in electron transparent nanolaminates

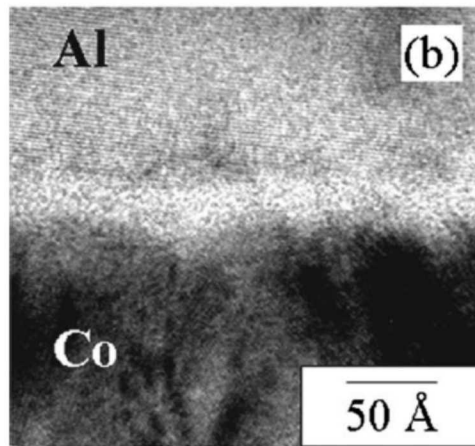
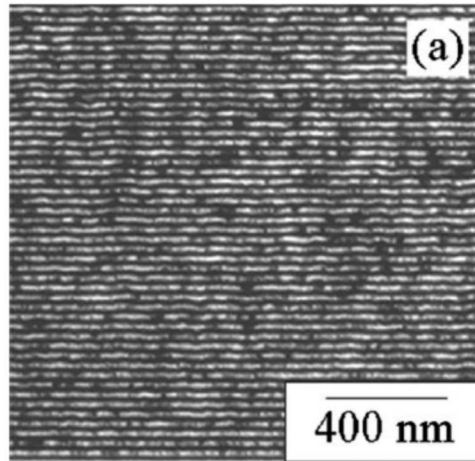
Michael J. Aberer, Garth C. Egan, and David P. Adams

Self-propagating reactions in Co/Al nanolaminates

25 nm Bilayer, 6 m/s

15 μ s per frame, played at 5 fps

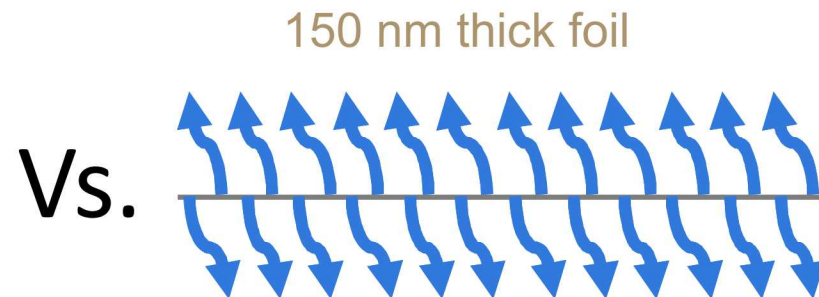
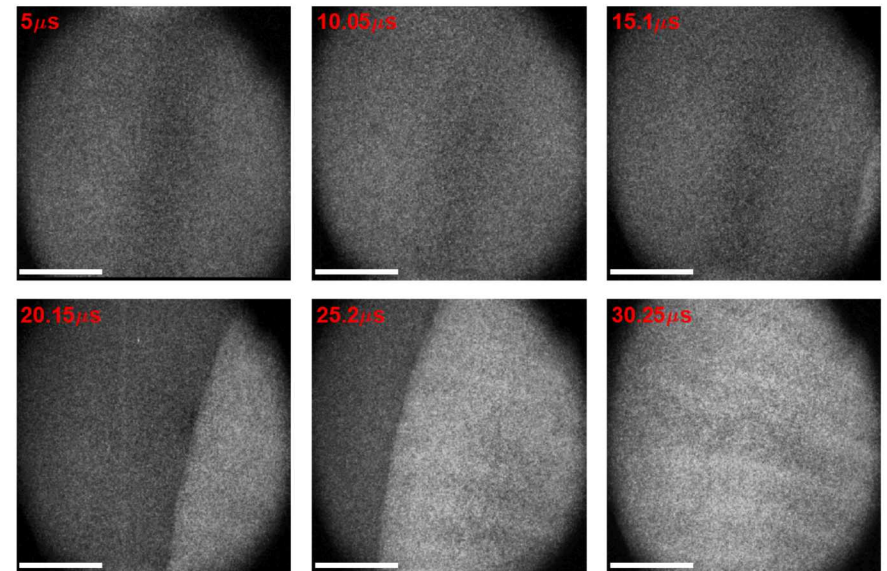
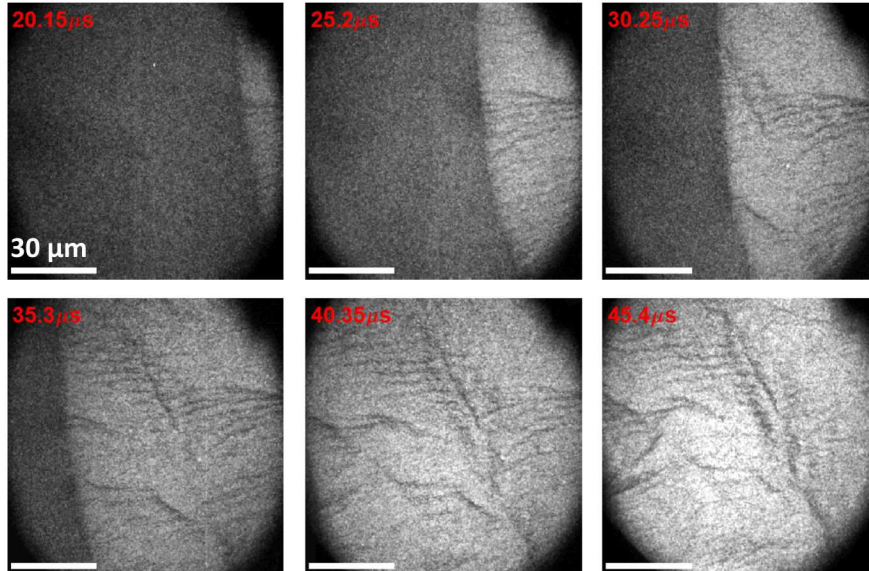
1 mm



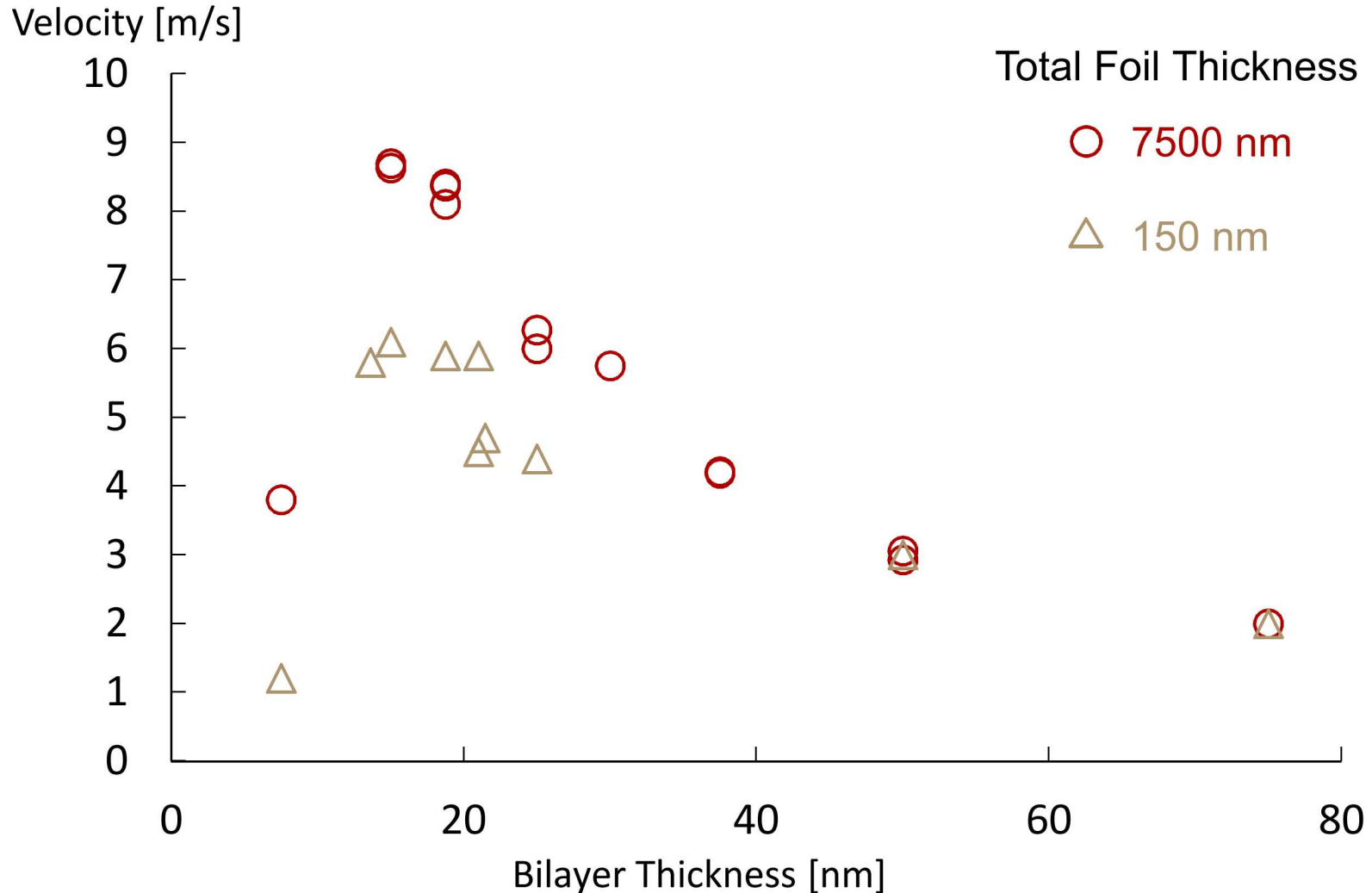
Dynamic TEM shows that foils still propagate at 150 nm total thickness

6 Bilayers (25.2 nm thick)

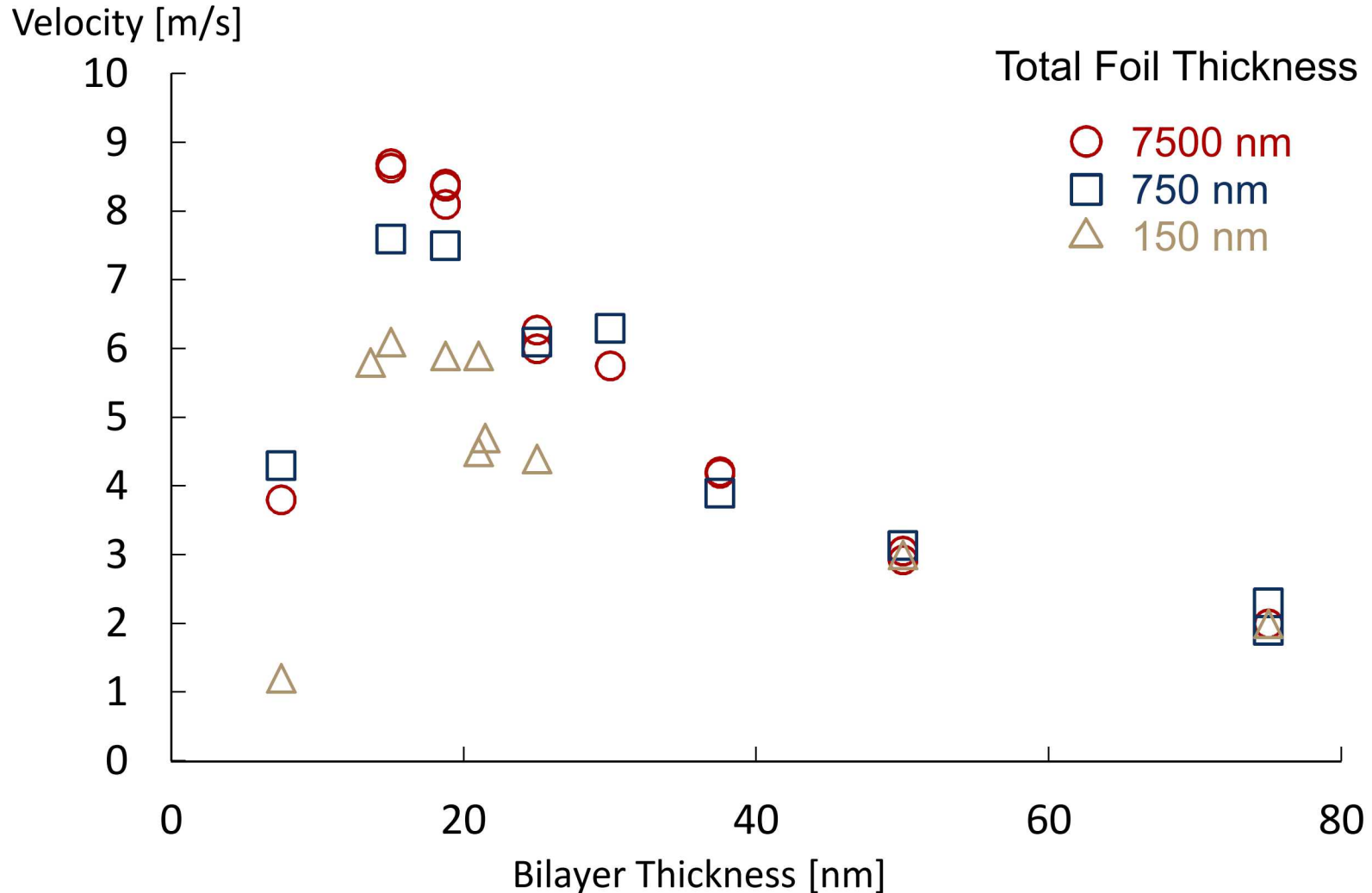
11 Bilayers (15 nm thick)



Experimentally Measured Velocities



Experimentally Measured Velocities



The relationship between physical parameters and propagation velocity

From Mann, Gavens, Reiss, Van Heerden, Bao, and Weihs, J. Appl. Phys. 1997:

Fick's Second Law

$$\frac{dC}{dt} - \nabla \cdot D \nabla C = 0$$

Heat Equation

$$c_p \rho \frac{dT}{dt} - c_p \rho \lambda \nabla^2 T = \frac{dQ}{dt}$$

Solved for the case of a
moving wave

$$v_x^2 = \left(\sum_{n=odd} \frac{k_n^2}{\alpha_n^2} \right)^{-1} \frac{4\lambda_x^2 R T_f^2 D}{E_A \lambda_y (T_{ad} - T_0)} \exp \left(\frac{-E_A}{R T_f} \right)$$

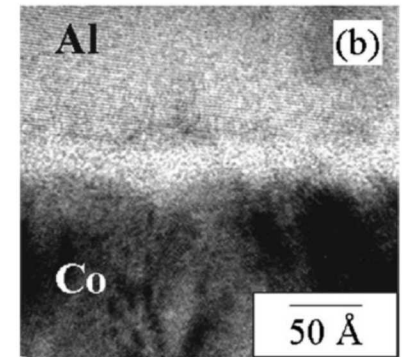
Values for model parameters are informed by experimental data

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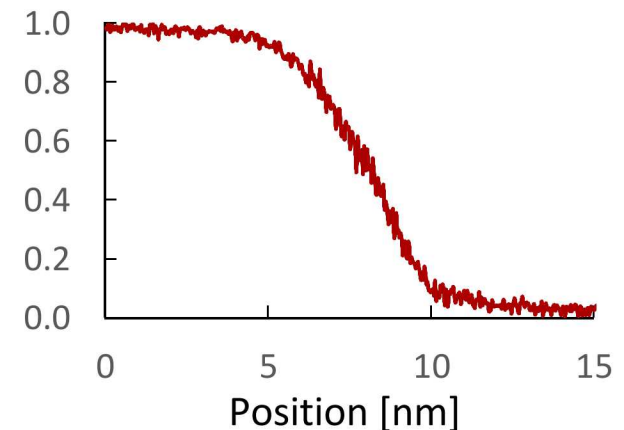
Series of eigenvalues, α_n , and Fourier coefficients, k_n , account for the chemical potential lost to imperfect interfaces as a function of initial concentration, $C_0(y)$, for quarter period δ .

$$\alpha_n = \frac{n\pi}{2\delta} \quad k_n = \frac{1}{2\delta} \int_{-2\delta}^{2\delta} C_0(y) \sin(\alpha_n y) dy$$

Concentration at each 1 Å wide mesh point comes from STEM-EDS to solve $C_0(y)$



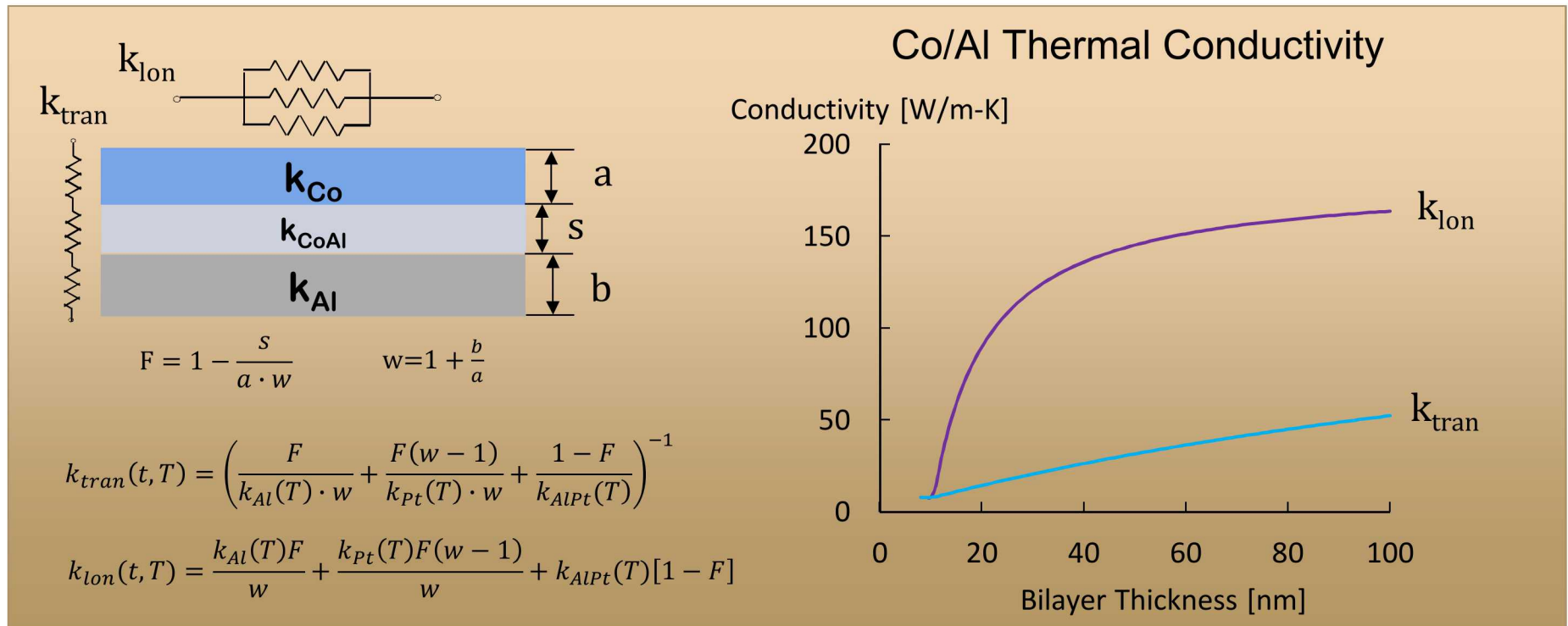
Concentration



Thermal Conductivity in a three-parameter fit of velocity data

$$v_x^2 = \left(\sum_{n=odd} \frac{k_n^2}{\alpha_n^2} \right)^{-1} \frac{4\lambda_x^2 RT_f^2 D}{E_A \lambda_y (T_{ad} - T_0)} \exp\left(\frac{-E_A}{RT_f}\right)$$

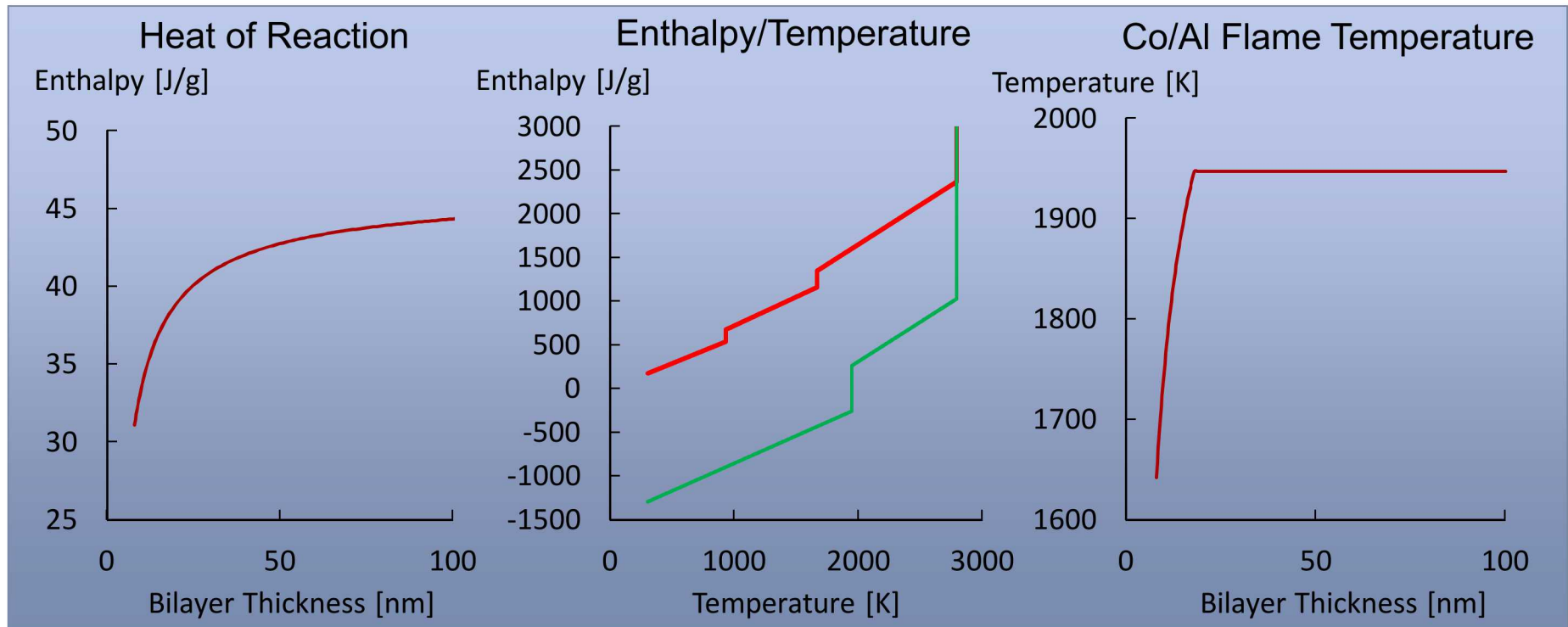
Heat of reaction from calorimetry and enthalpy-temperature diagrams allow for the calculation of adiabatic and flame temperatures



Values for model parameters are informed by experimental data

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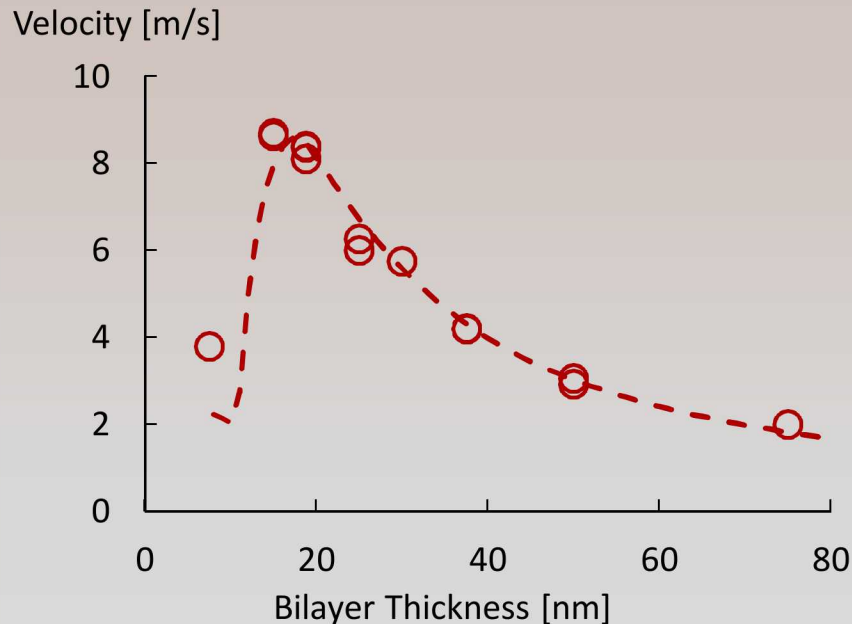


Pair of best fit for activation energy and diffusion coefficient

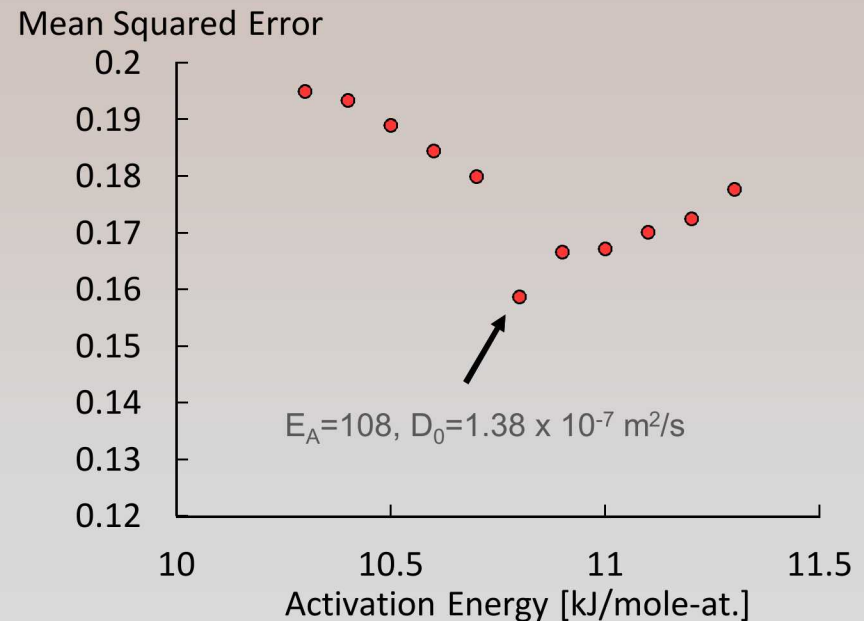
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Heat of reaction from calorimetry and enthalpy-temperature diagrams allow for the calculation of adiabatic and flame temperatures

Co/Al 7500 nm Total Thickness Velocity



Error Minimization for Pair of Best Fit

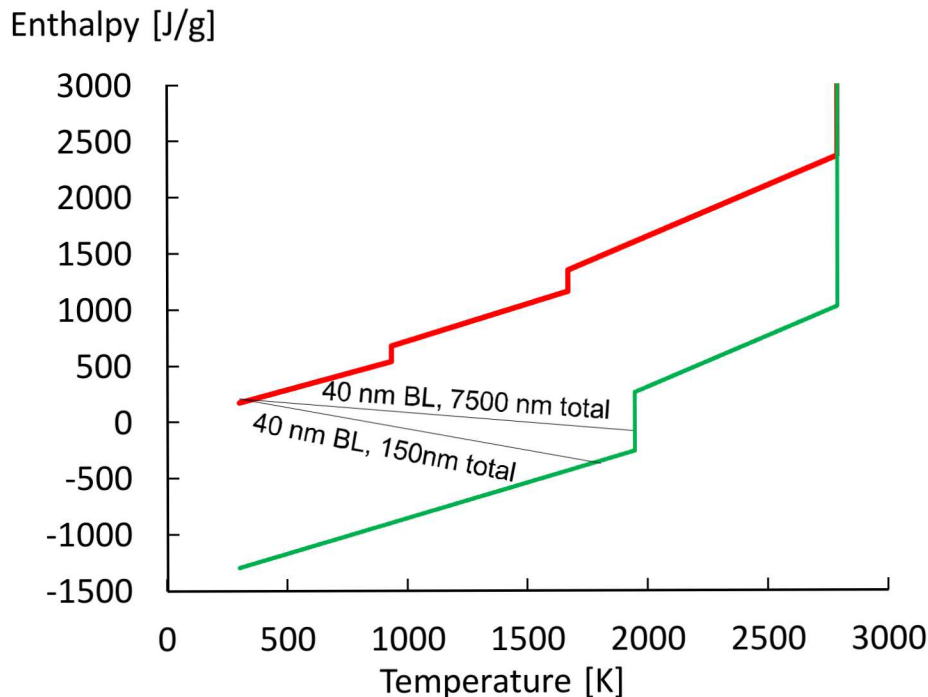


Accounting for Heat Loss in Model

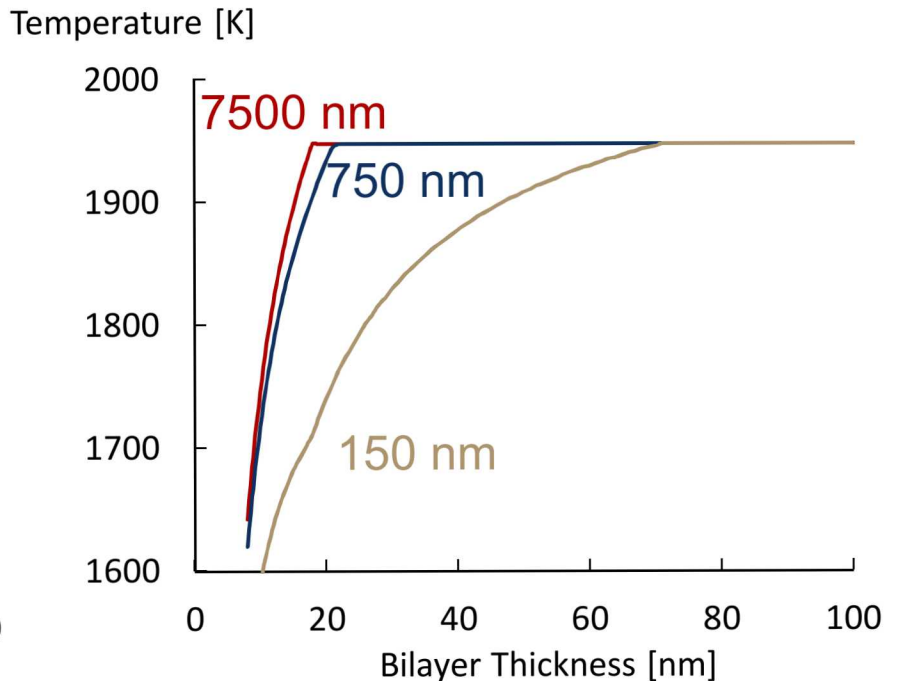
Flame temperature is determined based on the enthalpy/temperature diagram from the heat of reaction minus heat lost to radiation by:

$$Q_{rad}(T) = -\epsilon \frac{2\sigma(T^4 - T_0^4)}{b_{Total\ Thickness}}$$

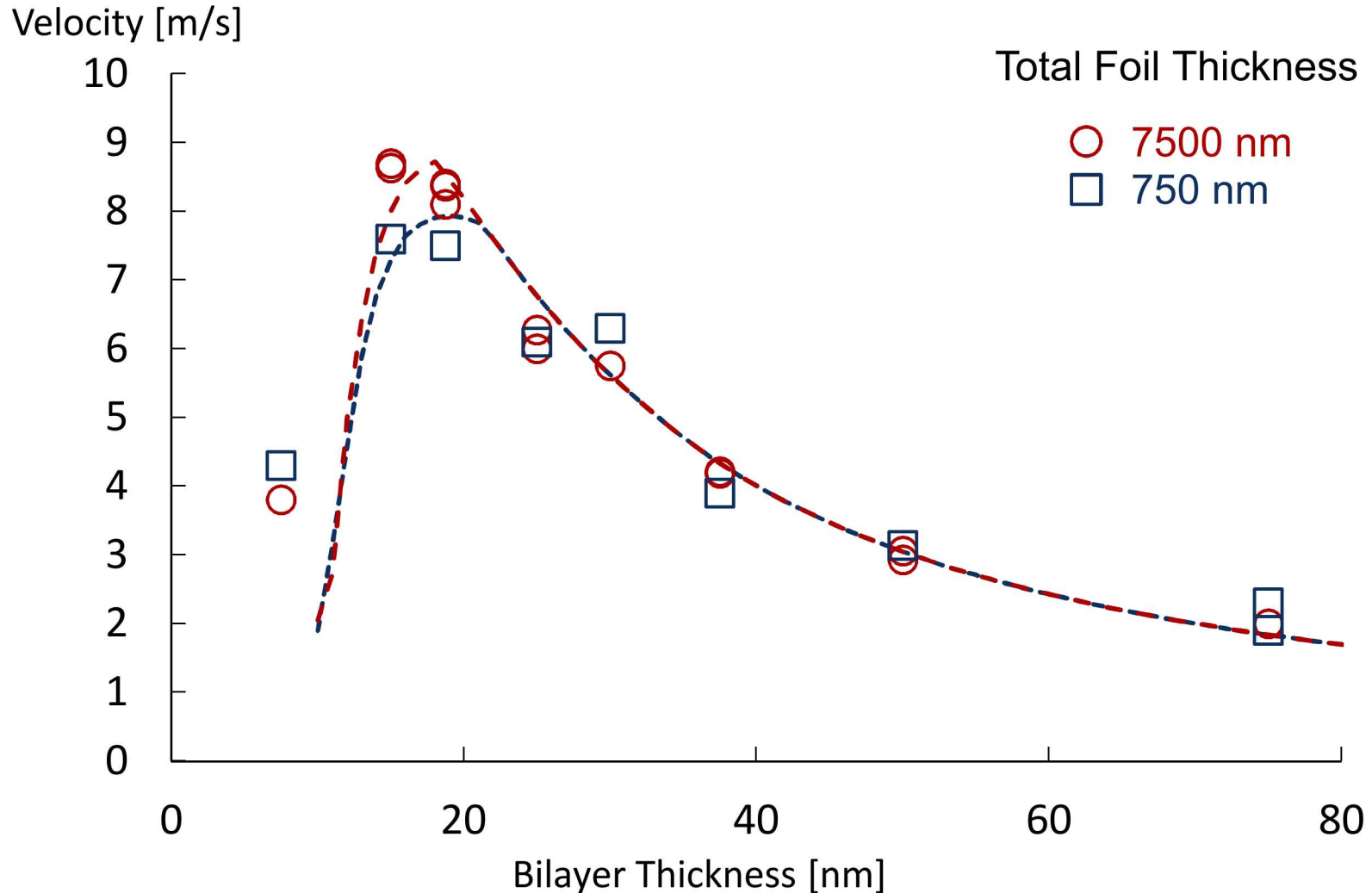
Enthalpy/Temperature



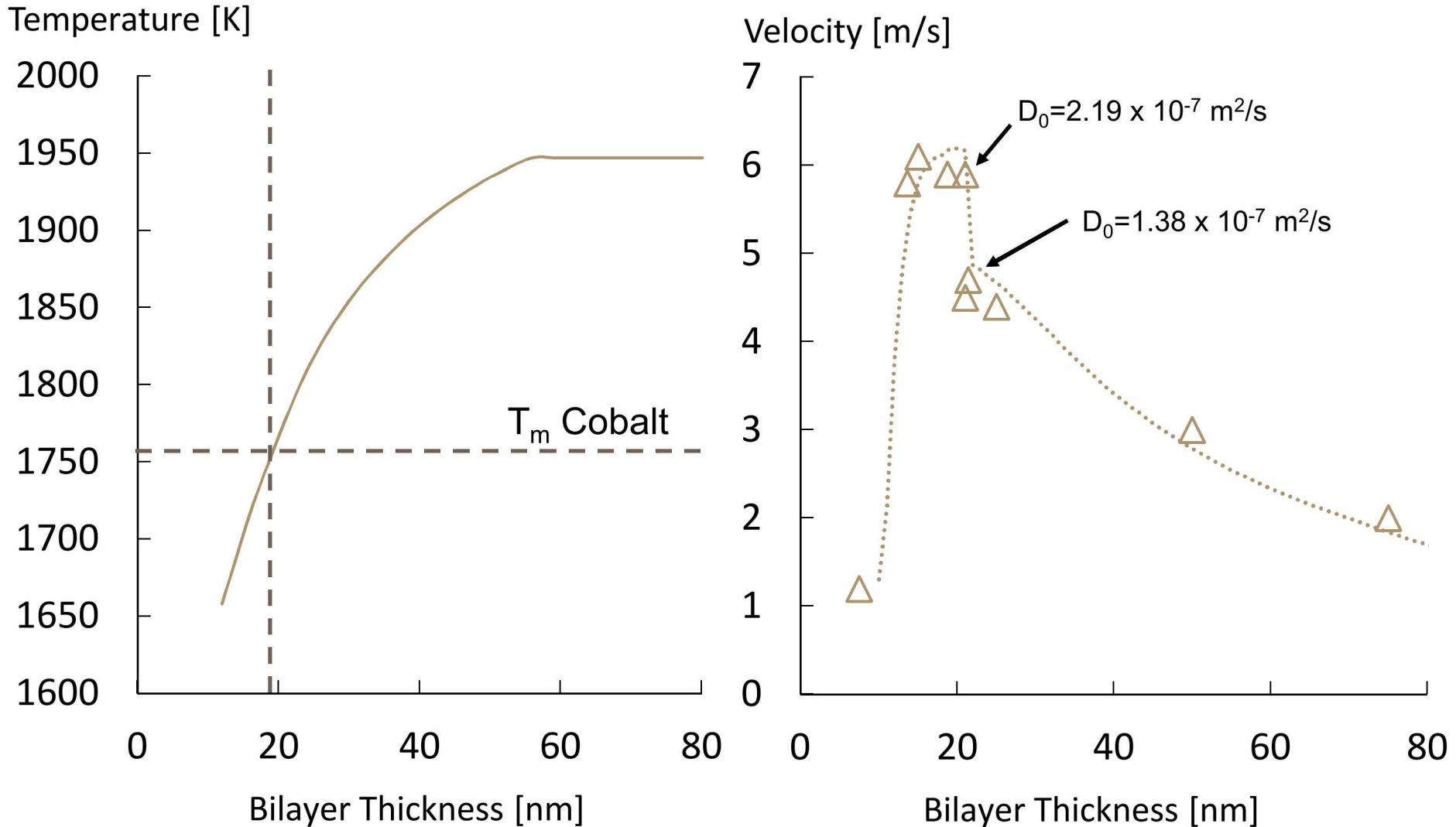
Co/Al Flame Temperature



Radiation loss in 750 nm thick foil reduces peak velocity

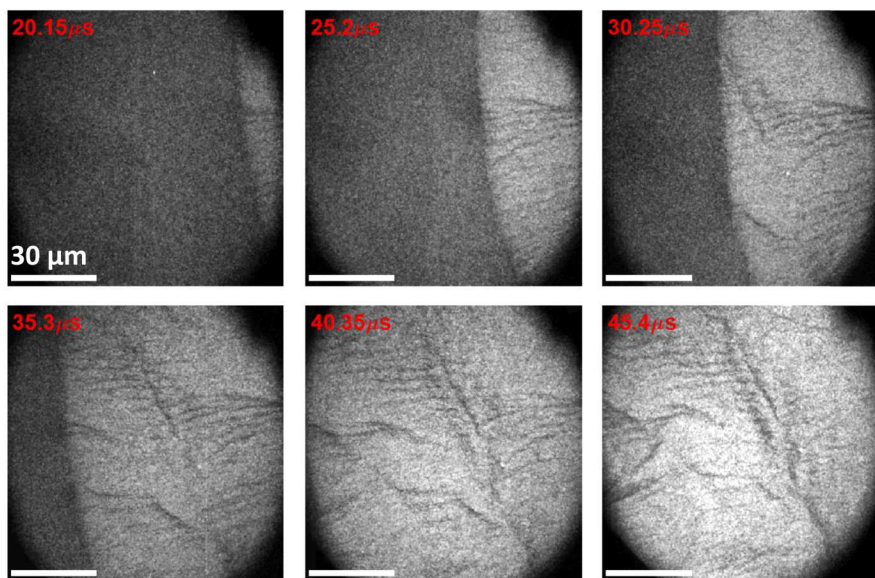


Mass transport rate is dependent on whether both reactants melt

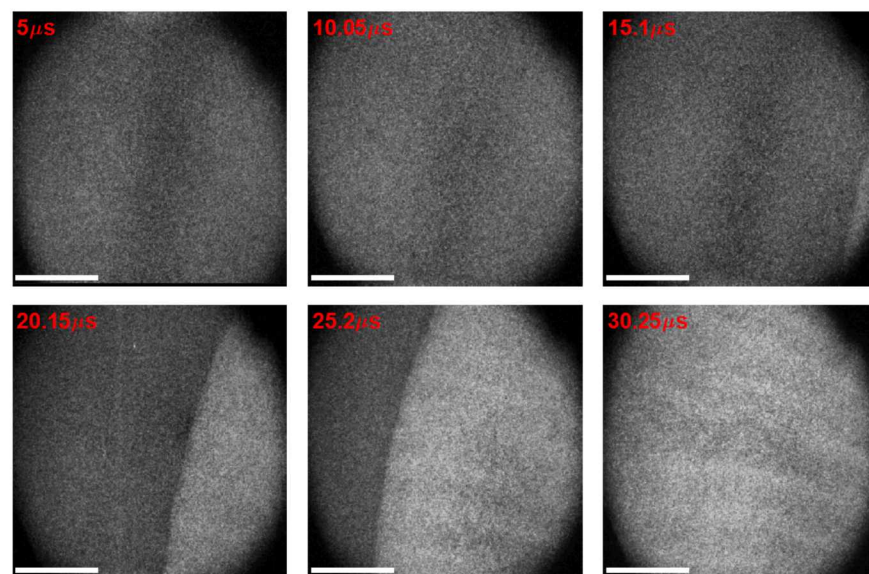


Reactant phase determines kinetic path to product formation

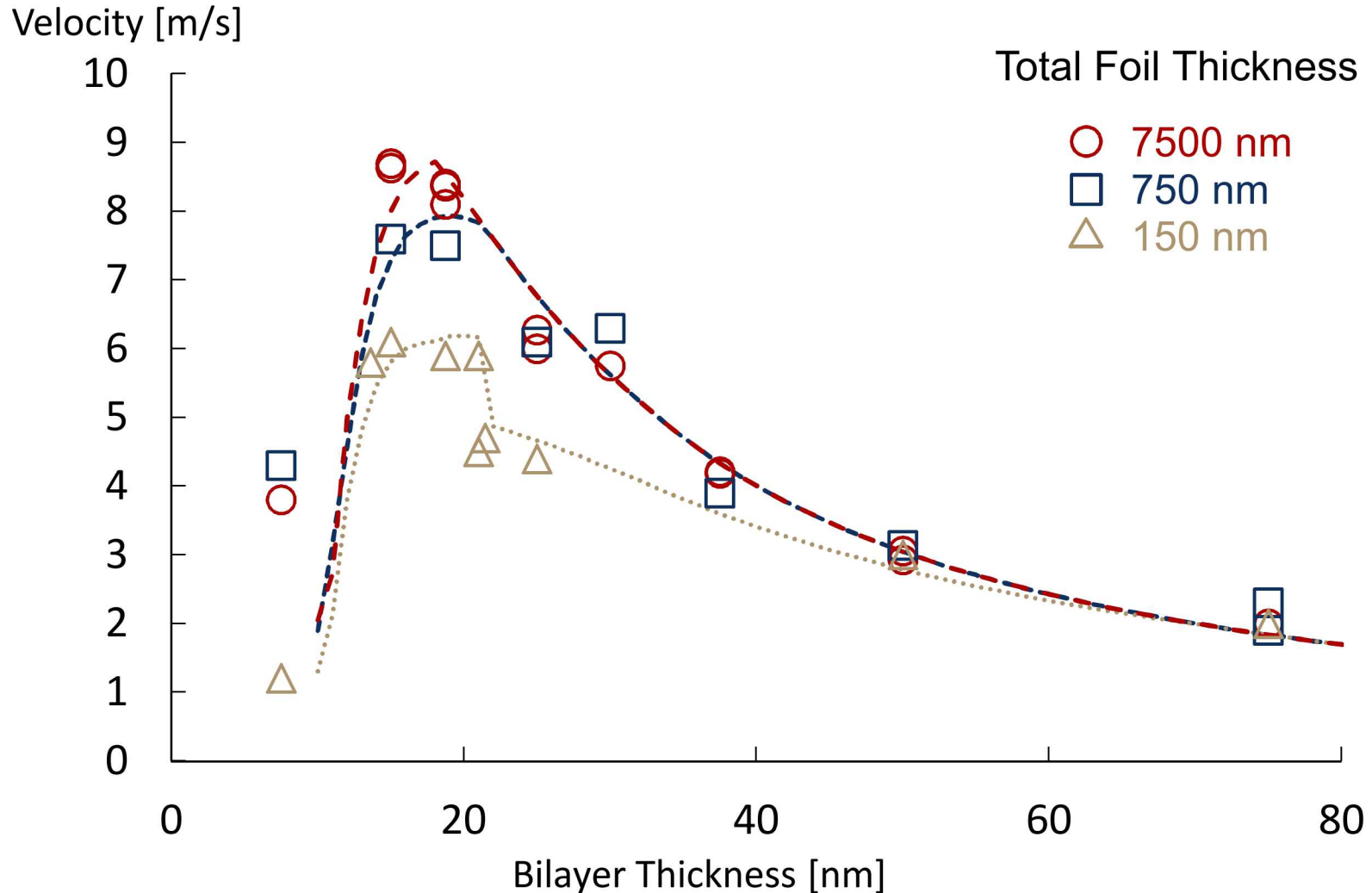
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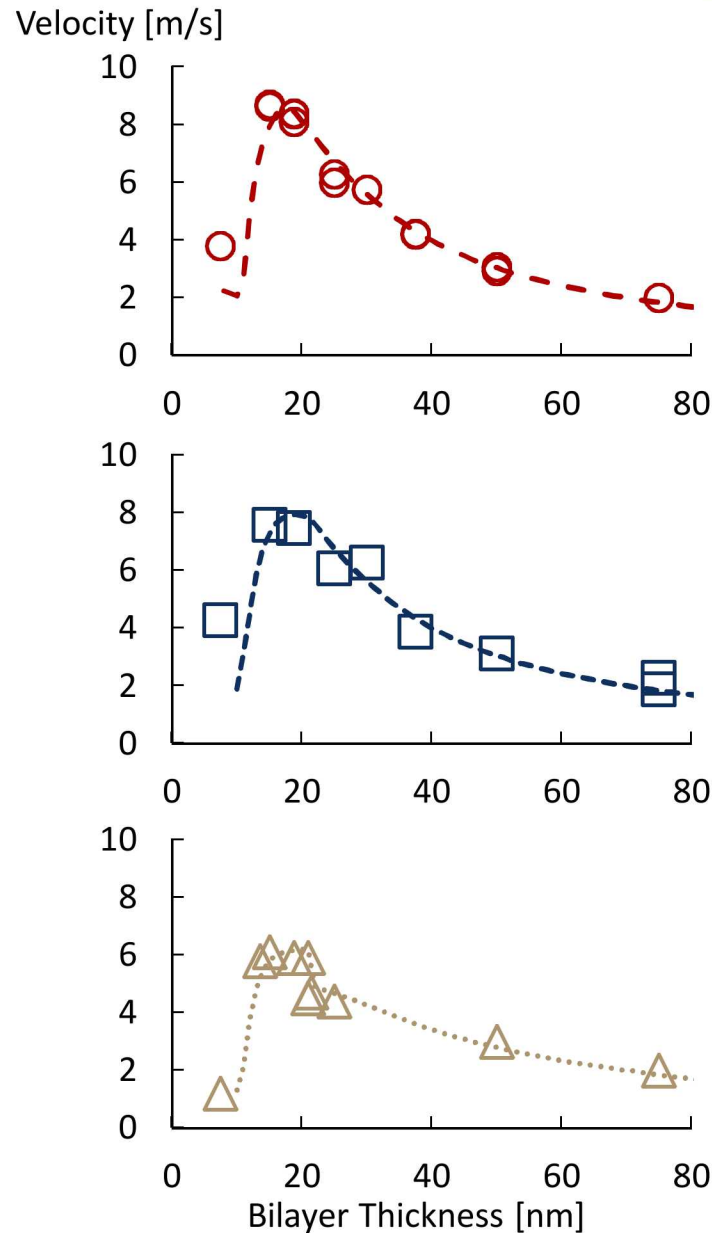
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Model Fits to Measured Velocities



Summary



We have populated the Mann model based on experimental data in order to fit values for activation energy and diffusion coefficient for Co/Al

Energy loss from radiation can lower flame temperatures for thin foils and bilayer designs with reduced heat of reaction due to premixing

The propagation velocity of electron transparent Co/Al samples is dependent both upon radiation effects and phase path dependent reaction kinetics