

Exceptional service in the national interest



Combined computational and experimental study of zirconium tungstate

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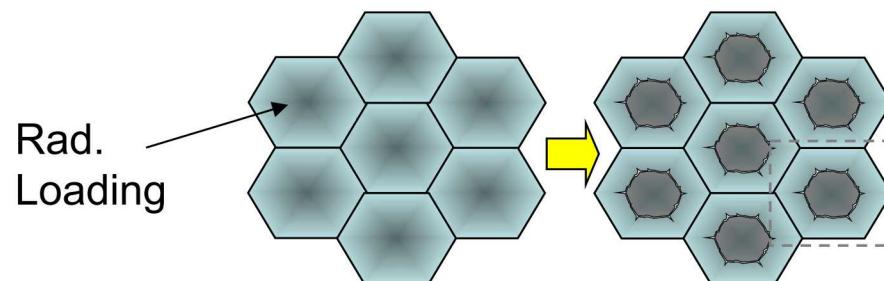
Nuclear waste forms

- Radioactive materials:
 - 34 tons of weapons-grade Pu metal from the US weapons program
 - *Long-lived isotope of technetium, ^{99}Tc ($t_{1/2} = 2.1 \times 10^5$ years, $\beta^- = 0.294$ MeV; 6% of the fission yield for ^{235}U)*
- *Chemical and physical waste forms for immobilizing radionuclides* (e.g., U, Pu, Tc):
 - Pu-waste form to isolate the radionuclides for extended periods of time needed
 - No effective Tc waste form identified yet (e.g., *highly mobile* as soluble TcO_4^- , volatile at elevated temperatures such as vitrification)
- Ideal radioactive material waste forms:
 - Low solubility
 - Ability to isolate radionuclides from the environment for long periods of time
 - Resistant to radiation damage that can lead to expansion, crumbling, increased exposed surface area, thus more rapid dissolution
- Ceramic waste forms (e.g., Zr-W-O and/or Zr-W-P-O).

Ceramic waste forms: ZrW_2O_8

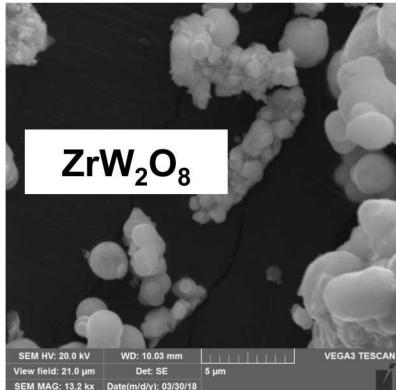
- Negative thermal expansion (NTE)
 - Contract upon heating
 - Naturally-occurring Zr minerals
 - Readily incorporate radionuclides (e.g., U, Tc, Pu) through substitution
- Radiation induced amorphization
- Zoned waste forms
 - No pressure exerted on the shell
 - No rupture of individual grains, mitigating the effect of amorphization on radionuclide release
 - Easy to maintain isolation of the radionuclide for long periods of time

Good candidate for radiation resistant waste forms!

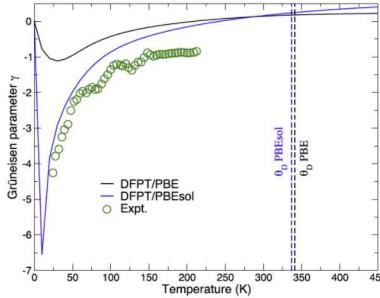
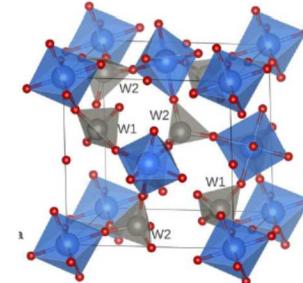


Combined computational-experimental strategy

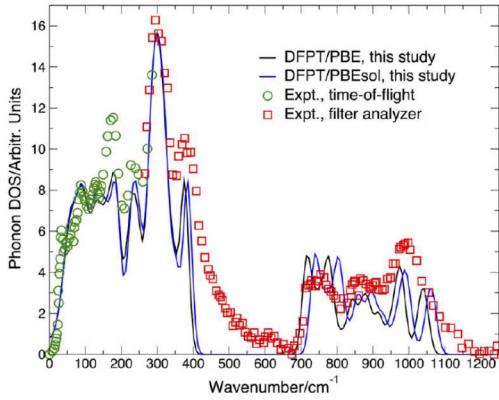
Synthesis (cubic ZrW_2O_8 and $\text{Zr}_2\text{P}_2\text{WO}_{12}$)



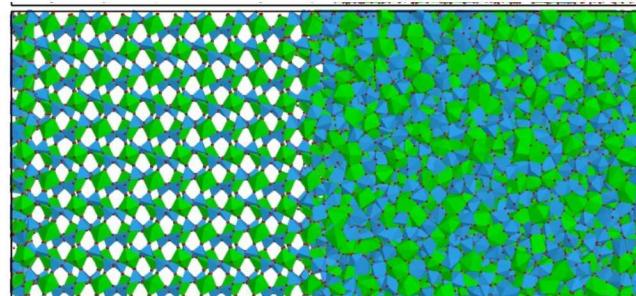
DFT/DFPT calculations (structure, vibrational, thermodynamics, and thermo- mechanical properties, etc)



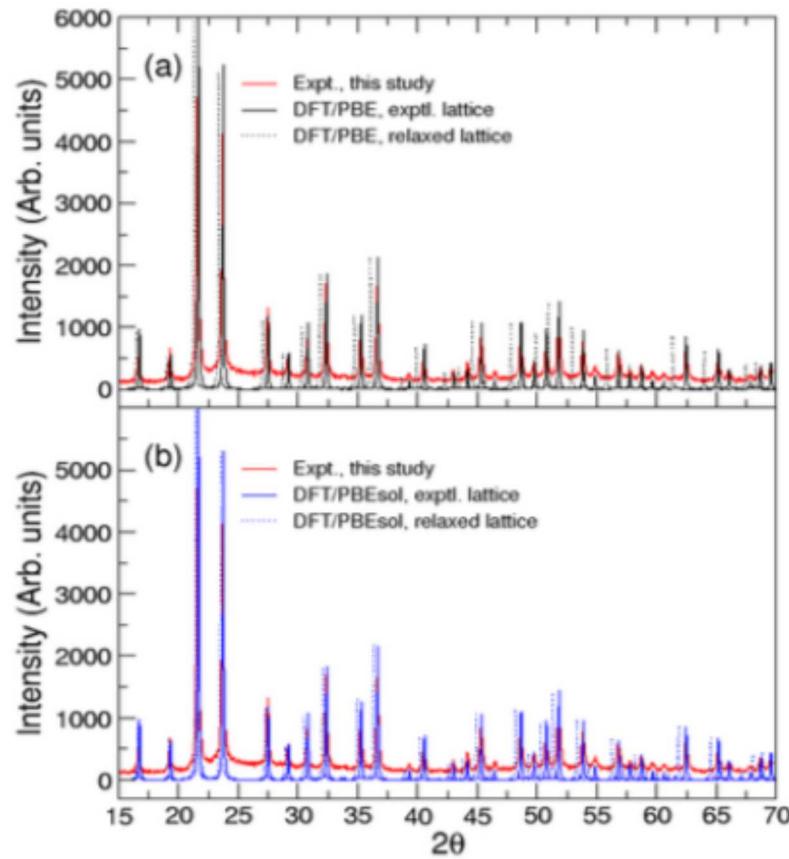
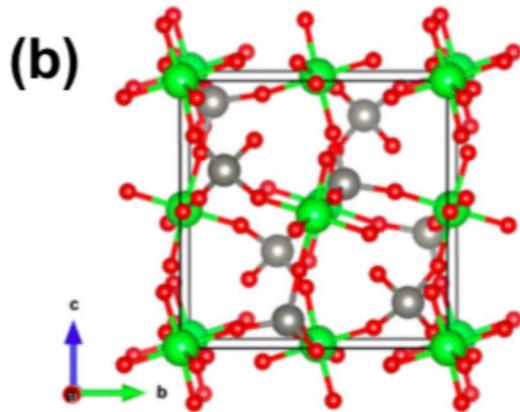
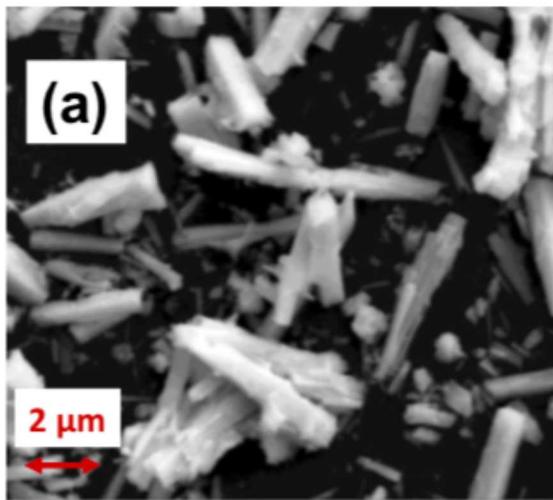
Characterization (XRD, mid/far-IR, Raman)



LAMMPS simulations (MD models for amorphization, crystal/ amorphous material boundary)



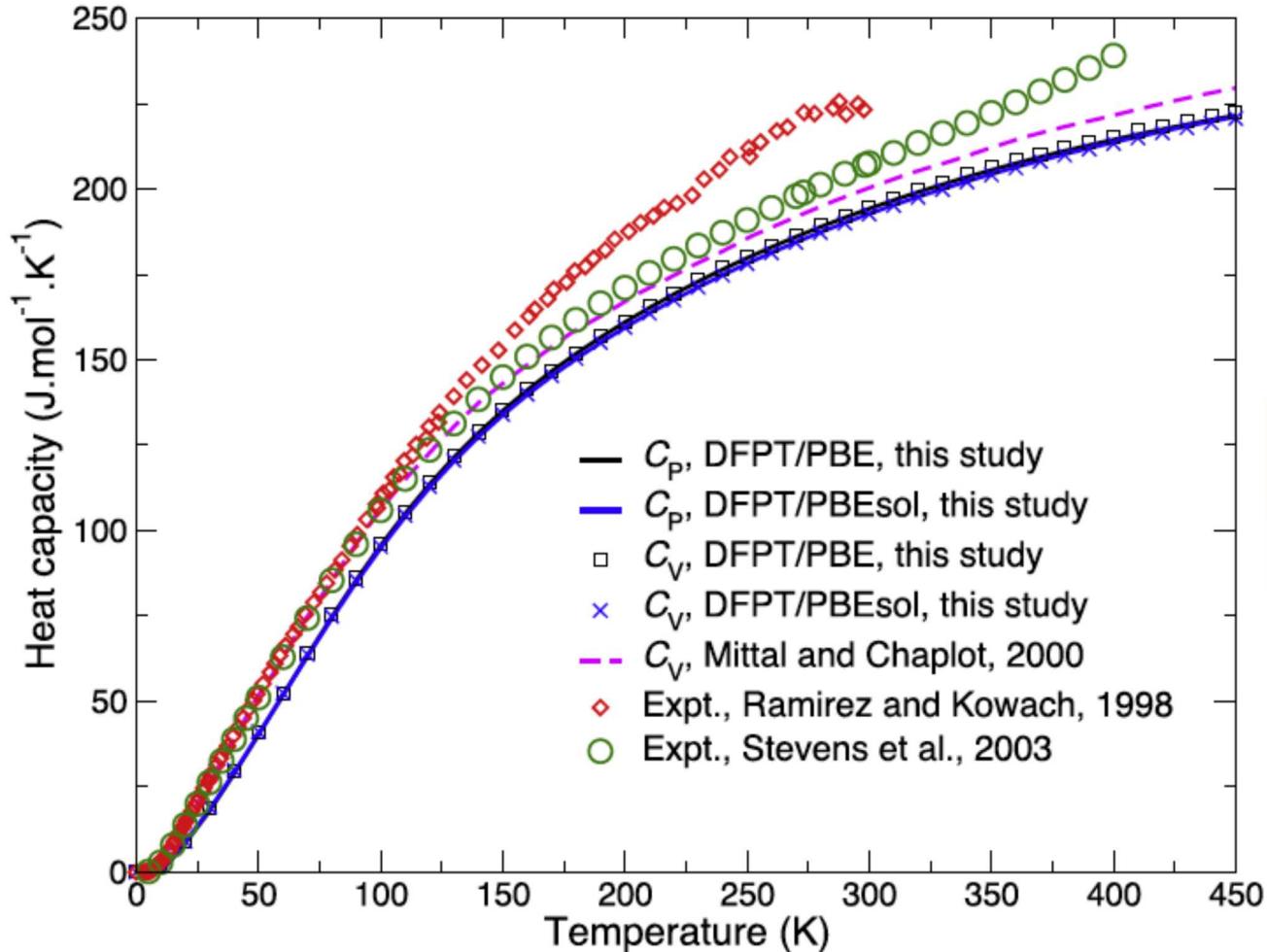
Zr Tungstate



	DFT		Expt.	
	PBE	PEBsol	This work	Evans et al.
a (\AA)	9.310	9.241	9.1493	9.1846

α -ZrW₂O₈ (space group P2₁3; IT No. 198; Z=4) with corner-sharing ZrO₆ octahedral and WO₄ tetrahedral coordination units [Weck et al., Chem. Phys. Lett. 698, 195 (2018)].

Thermal properties of $\alpha\text{-ZrW}_2\text{O}_8$



$$\begin{aligned}
 C_P(T, P) &= -T \frac{\partial^2 G(T, P)}{\partial T^2} \\
 &= T \frac{\partial V(T, P)}{\partial T} \frac{\partial S(T, V)}{\partial V} \Big|_{V=V(T, P)} \\
 &\quad + C_V[T, V(T, P)],
 \end{aligned}$$

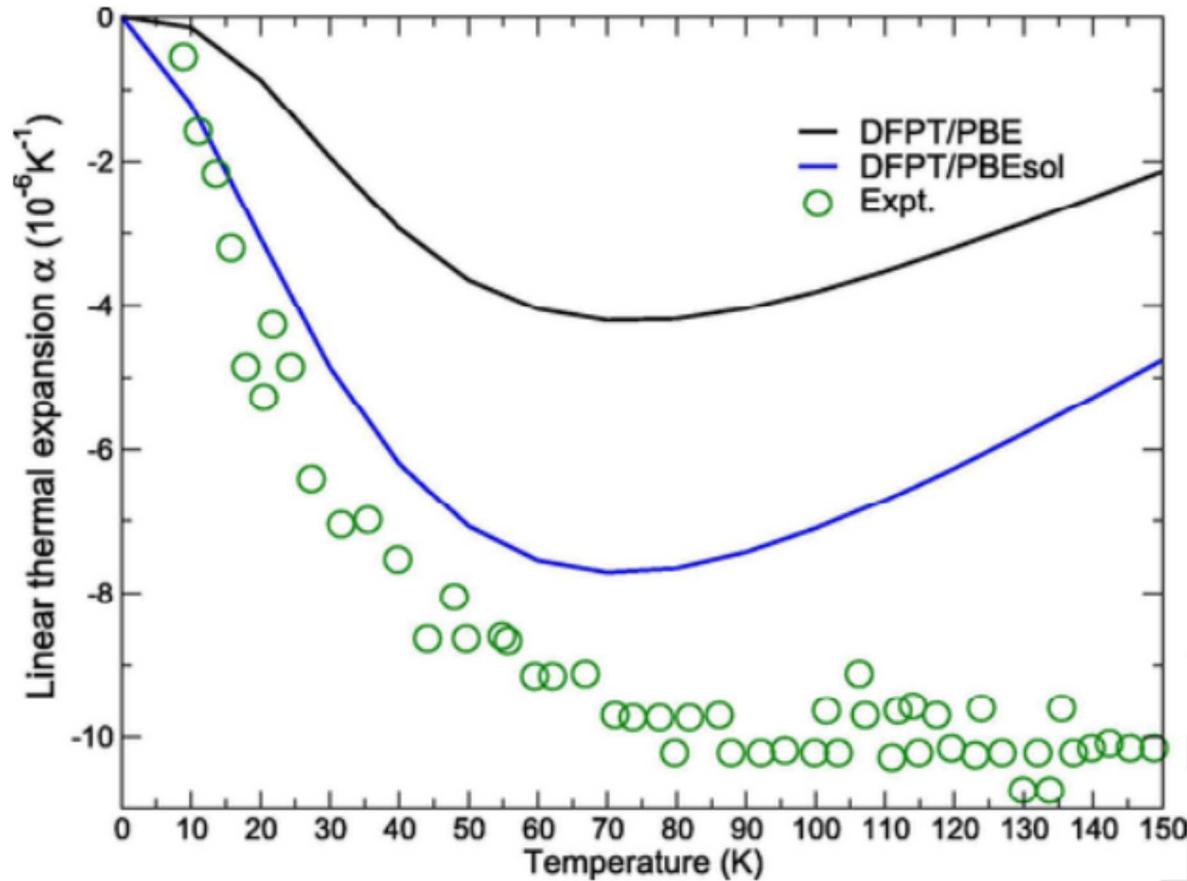
$$C_V = k_B \sum (\beta \hbar \omega)^2 \frac{e^{\beta \hbar \omega}}{[e^{\beta \hbar \omega} - 1]^2}$$

	C_P^0 ($\text{J}/\text{mol}/\text{K}$)
DFT	193.8 [1]
Expt	207.01[2]; 223.3 [3]

- [1] Weck et al., 2018.
 [2] Stevens et al., 2003.
 [3] Ramirez and Kowach, 1998.

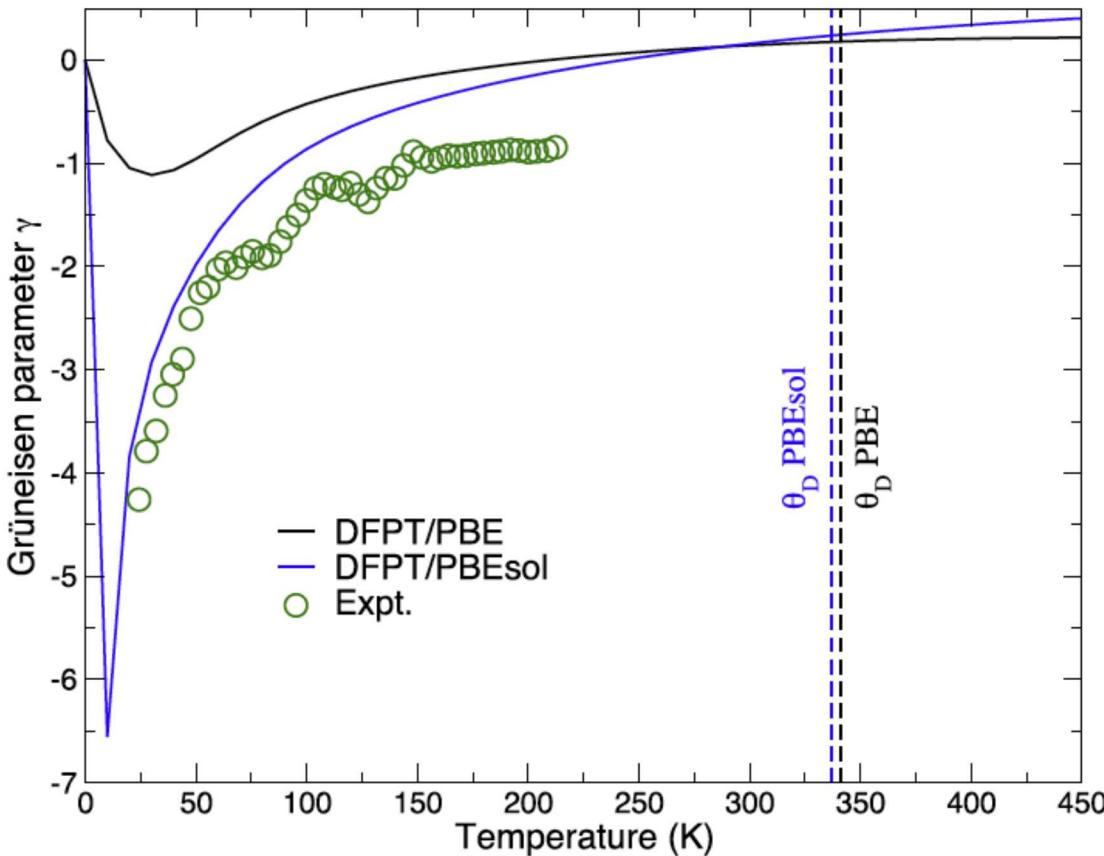
Thermal evolution of the molar isochoric (C_V) and isobaric (C_P) heat capacities of $\alpha\text{-ZrW}_2\text{O}_8$ calculated at constant atmospheric pressure using DFT at the GGA/PBE and GGA/PBEsol levels within the quasi-harmonic approximation.

Linear coefficient of thermal expansion (CTE) of $\alpha\text{-ZrW}_2\text{O}_8$



- The linear CTE computed using PBEsol is in very good agreement with the experimental data from the high-resolution neutron diffraction measurements of David et al. (1999) to $\sim 60\text{K}$
- The PBEsol linear CTE reaches an extremum of at $\sim 70\text{K}$
- Similar discrepancies were found above $\sim 60\text{K}$ between these experimental data [6] and the finite-displacement B3LYP calculations of Gava et al. (2012)

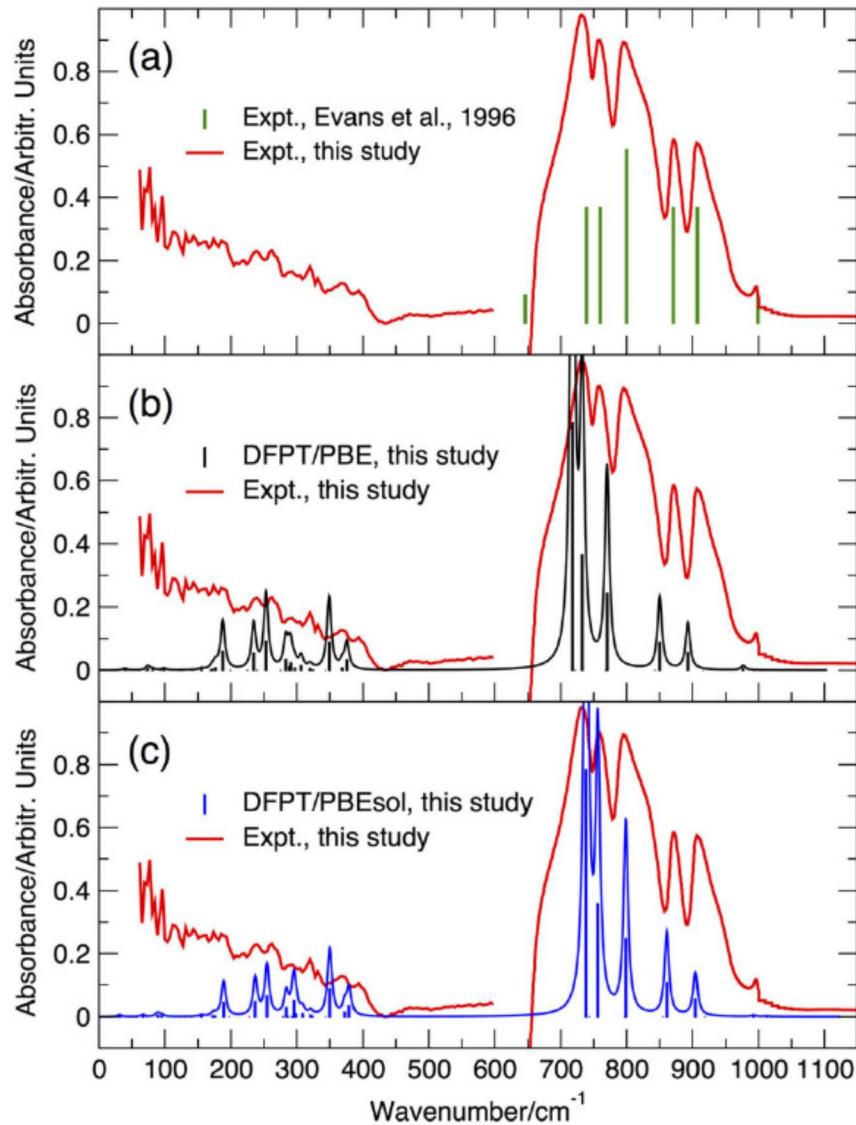
Grüneisen parameter of $\alpha\text{-ZrW}_2\text{O}_8$



- PBEsol results are in excellent agreement with the experimental Grüneisen parameter by Ernst et al. (1998) to 60K.
- The main contributions to NTE at low temperature stem from the two lowest-frequency optical phonons, predicted at 36 cm^{-1} (T_{irrep}) and 37 cm^{-1} (E_{irrep}).
- These modes are characterized by variations of intrapolyhedral bond angles O-M-O (M = W, Zr), achieved through combined librational and translational motions of WO_4 units.

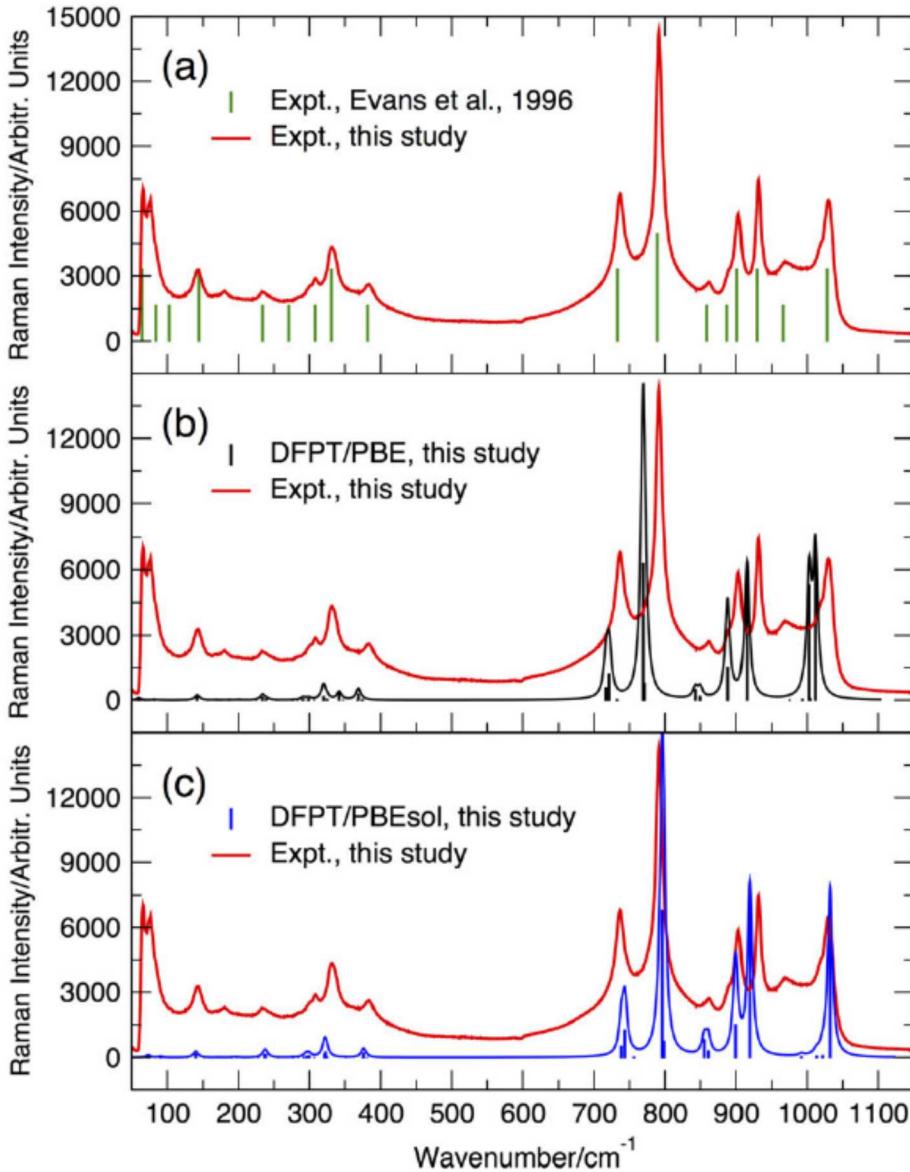
Thermal evolution of the Grüneisen parameter of alpha-ZrW₂O₈ calculated using DFT at the GGA/PBE and GGA/PBEsol levels within the quasi-harmonic approximation.

IR spectrum of $\alpha\text{-ZrW}_2\text{O}_8$



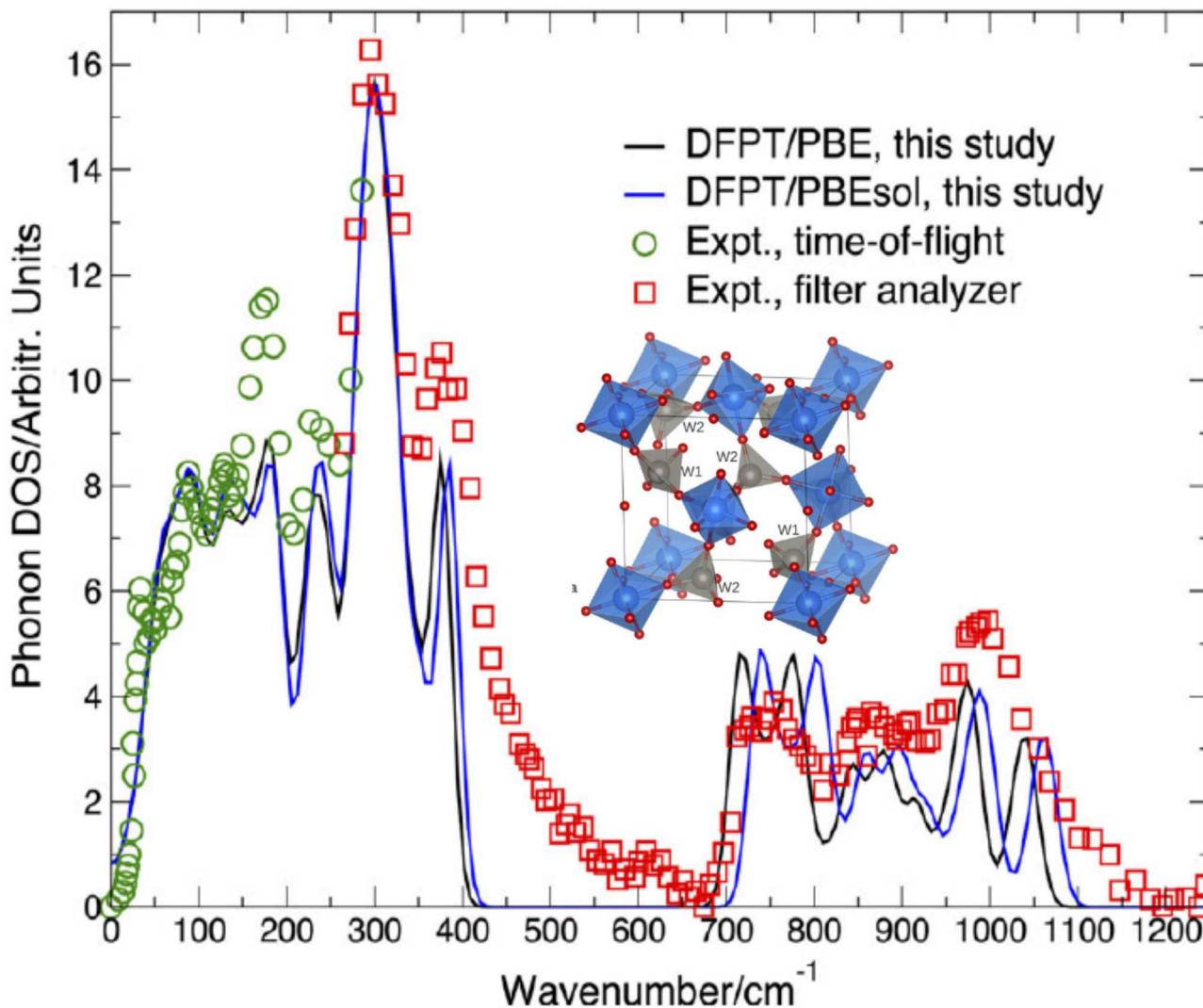
- Fourier transform infrared (FT-IR) spectra of $\alpha\text{-ZrW}_2\text{O}_8$ measured in this study at T = 298 K (red line) and observed IR band centers reported by Evans et al. (green lines), along with infrared spectra simulated from DFPT at the GGA/PBE (black) and GGA/PBEsol (blue) levels
- The IR spectrum simulated using PBEsol is in close agreement with experiments
- The IR-active wavenumber observed by Evans et al. at 646 cm⁻¹ along with several weak lines in the range 600–400 cm⁻¹ were not predicted by DFPT calculations, nor observed in the present experiments

Raman spectrum of $\alpha\text{-ZrW}_2\text{O}_8$



- Raman spectrum of $\alpha\text{-ZrW}_2\text{O}_8$ measured in this study at T = 298 K (red) and observed and calculated Raman band centers reported by Evans et al. (green), along with Raman spectra simulated from DFPT-PBE (black) and DFPT-PBEsol (blue) levels
- No 855-628 cm⁻¹ peaks appear in the $\alpha\text{-ZrW}_2\text{O}_8$ Raman bands predicted with DFPT or measured in this study or by Evans et al
- No stable ZrO_2 or WO_3 present in the sample
- Similar to PDOS and IR DFPT calculations, no Raman active modes are predicted to occur in the ranges 381–739 cm⁻¹ and 374–717 cm⁻¹ with PBEsol and PBE, respectively

Phonon density of states (PDOS) of α -ZrW₂O₈



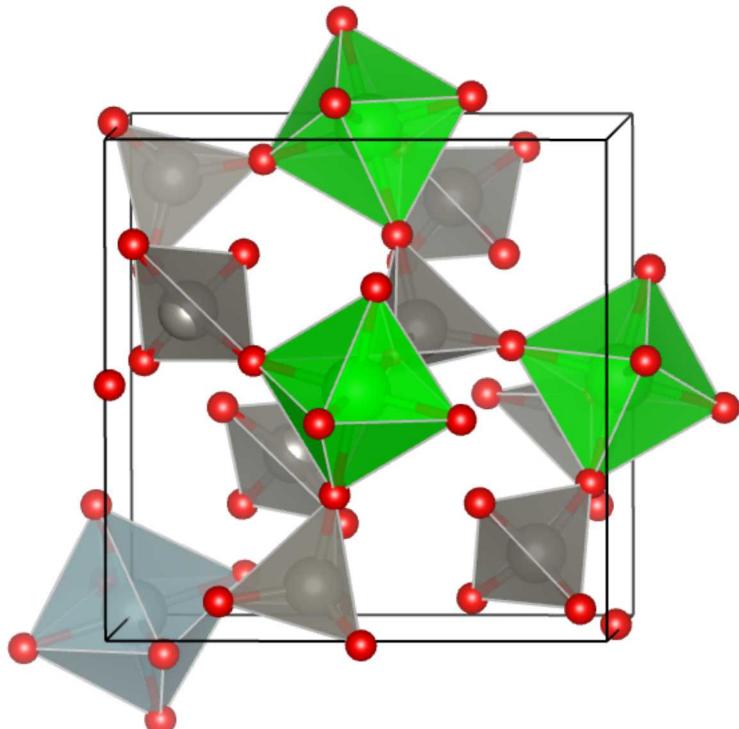
Phonon density-of-states (PDOS) spectra of α -ZrW₂O₈ simulated at T = 0 K using density functional perturbation theory (DFPT) at the GGA/PBE (black line) and GGA/PBEsol (blue line) levels. The generalized PDOS spectrum from inelastic neutron scattering data collected at T = 300 K using time-of-flight (green circles) and filter-analyzer (red squares) spectroscopy is shown for comparison

Conclusion

- DFPT calculations were conducted at the GGA/PBE and GGA/PBEsol levels of theory to systematically investigate the crystal structure, phonon, IR and Raman spectra, and vibrational properties of α -ZrW₂O₈
- DFPT calculations were able to correctly reproduce the NTE behavior, elastic/mechanical properties, and IR/Raman spectra of ZrW₂O₈
- The calculated thermodynamic/thermo-mechanical properties were validated with measured data
- Calculations for Zr₂P₂WO₁₂ are being finalized and also appear to reproduce available experimental data

Current/future research

1. U/Pu/Tc inclusion in α -ZrW₂O₈



2. DFT Modeling of Zr₂P₂WO₁₂

