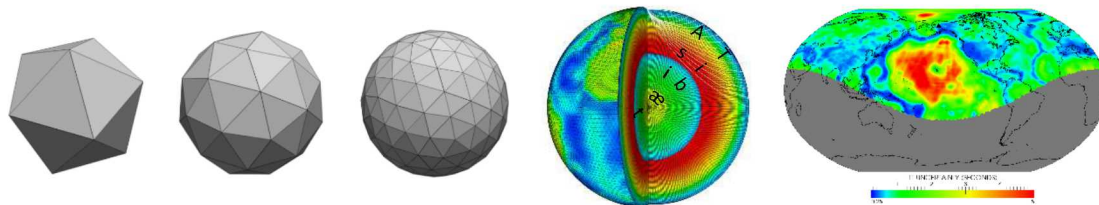
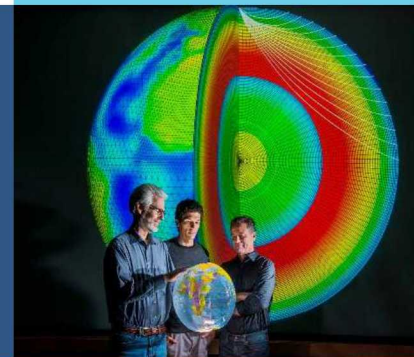


# SALSA3D



PRESENTED BY

Sandy Ballard



Sandia National Laboratories is a multimission laboratory managed and operated by National Technology & Engineering Solutions of Sandia, LLC, a wholly owned subsidiary of Honeywell International Inc., for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA0003525.

# **SALSA3D**

## **A Global 3D Velocity Model of the Earth's Mantle For Improved Seismic Event Location in Nuclear Explosion Monitoring**

Sandy Ballard<sup>1</sup>

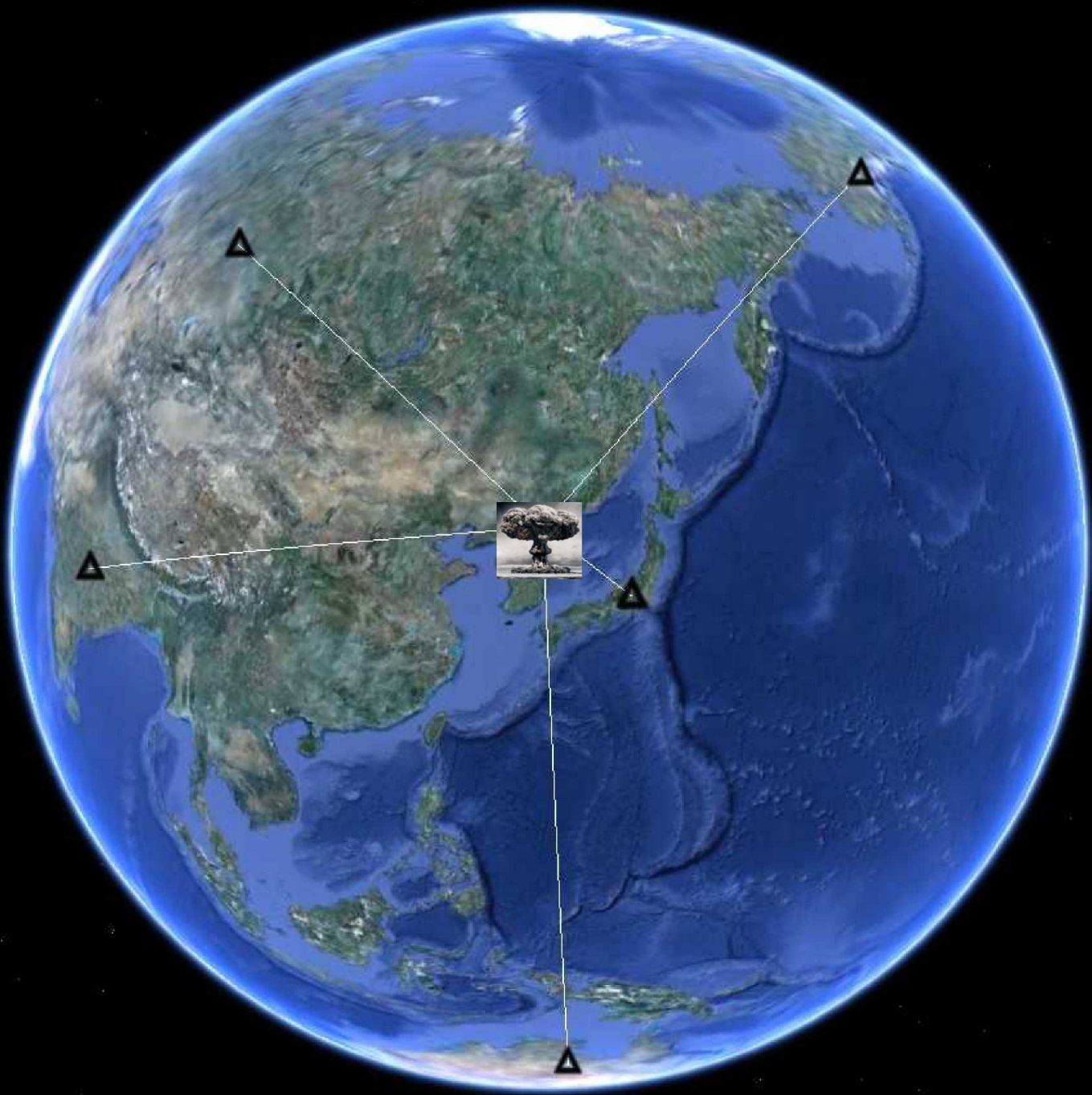
Mike Begnaud<sup>2</sup>, Jim Hipp<sup>1</sup>, Chris Young<sup>1</sup>,  
Andre Encarnacao<sup>1</sup>, Scott Phillips<sup>2</sup>

<sup>1</sup>Sandia National Laboratories

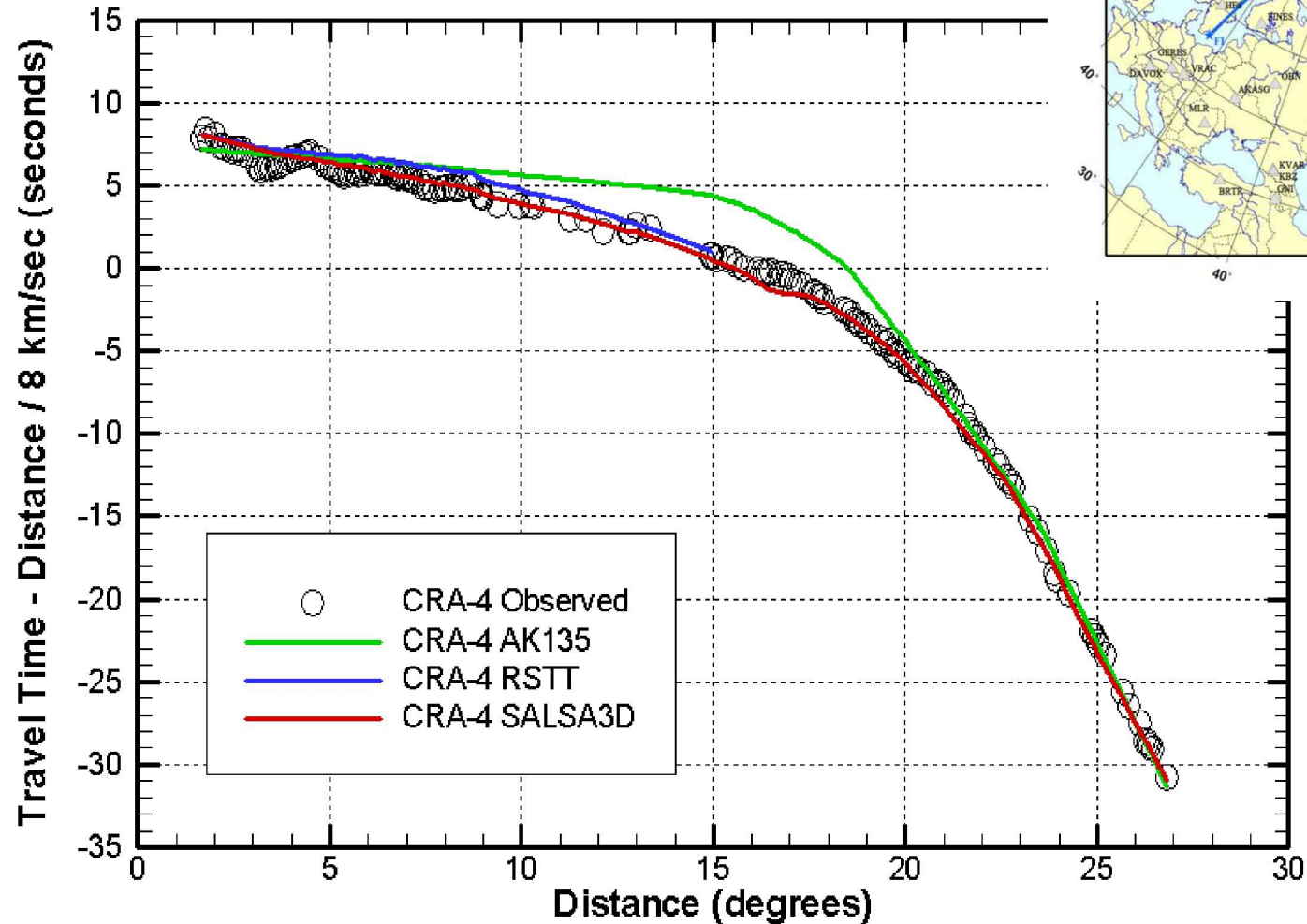
<sup>2</sup>Los Alamos National Laboratory

# Outline

- Motivation
- Data Set
- Tomographic Procedure
- Model Resolution and Adaptive Gridding
- Velocity Model and Uncertainty
- Predicted Travel Times and Uncertainty
- Location Accuracy Improvement



# Deep Seismic Sounding (DSS) Lines



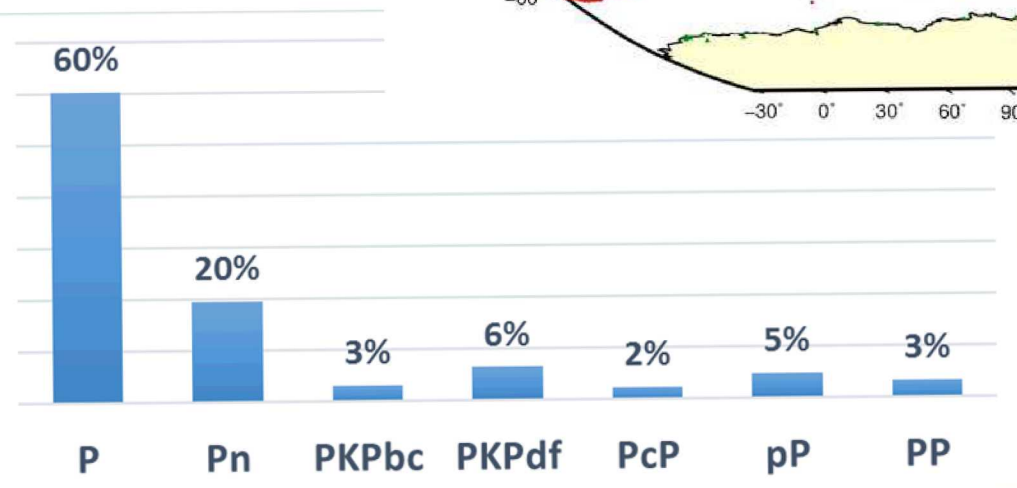
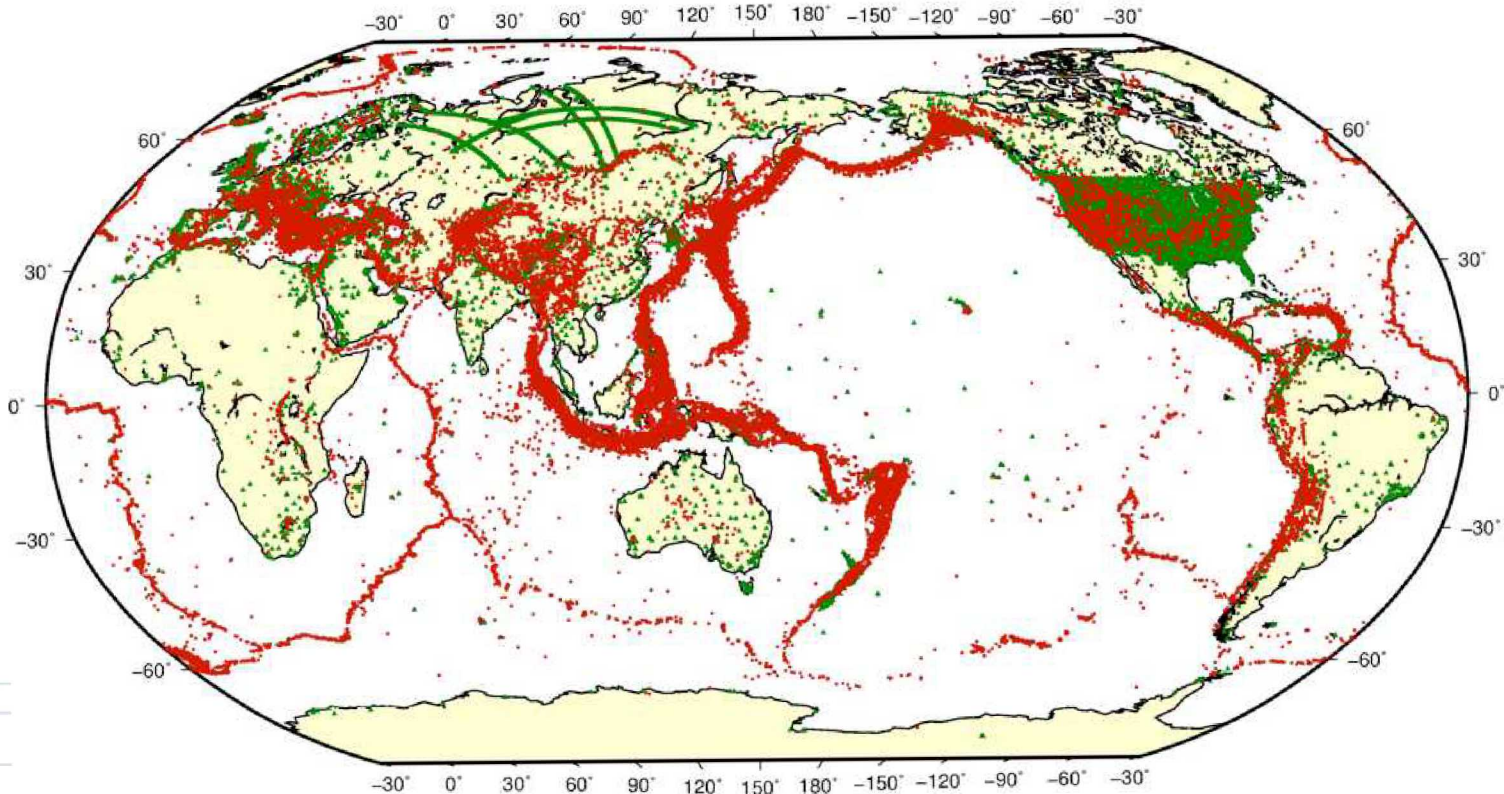


# Tomography Data

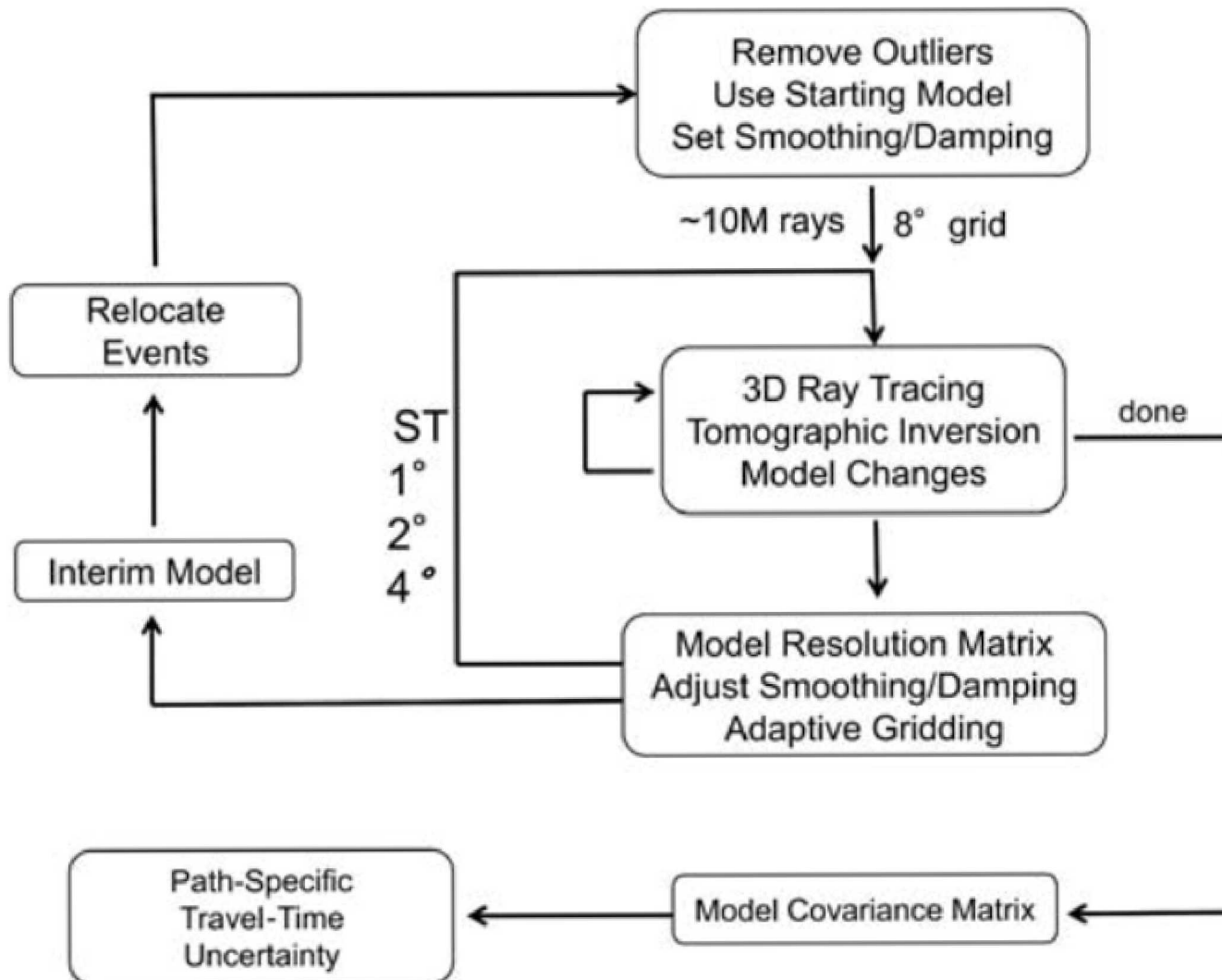
117K events

12K stations

12M rays



# Tomographic Procedure



# Travel Time Prediction Uncertainty

The standard least squares tomography solution seismic slowness,  $s$ , is formulated given an  $m \times n$  set of non-linear travel time path length weights,  $A(s)$ ; a vector of  $n$  associated path residuals,  $d$ ; an  $n \times n$  Bayesian inferred prior model covariance matrix,  $C_m$ . The Bayesian prior model parameters are used to constrain the solution in model regions possessing little or no data. This formulation can be written as

$$\begin{bmatrix} C_d^{-1/2} A(s_k) \\ \alpha C_m^{-1/2} \end{bmatrix} \Delta s^{k+1} = \begin{bmatrix} C_d^{-1/2} (d - A(s_k) s_k) \\ 0 \end{bmatrix} \quad s^{k+1} = \Delta s^{k+1} + s^k$$

Where  $C_d$  are the data variances associated with the travel time path weights,  $\alpha$  is a damping parameter applied to ensure solution stability, and the non-linear solution is updated in an iterative manner ( $k$ ) until convergence is obtained ( $\Delta s \approx 0$ ). Applying standard solution techniques, the posterior model covariance,  $\tilde{C}_m$ , and the model resolution,  $R_m$ , can be discovered and written as

$$\tilde{C}_m = [A^T C_d^{-1} A + C_m^{-1}]^{-1} \quad R_m = \tilde{C}_m A^T C_d^{-1} A = I - \tilde{C}_m C_m^{-1}$$

Given these definitions we can formulate the travel time and associated uncertainty of an arbitrary ray path,  $p$ , given its grid node vector of path length weights ( $W_p = \langle w_{pj} \rangle$ ) as

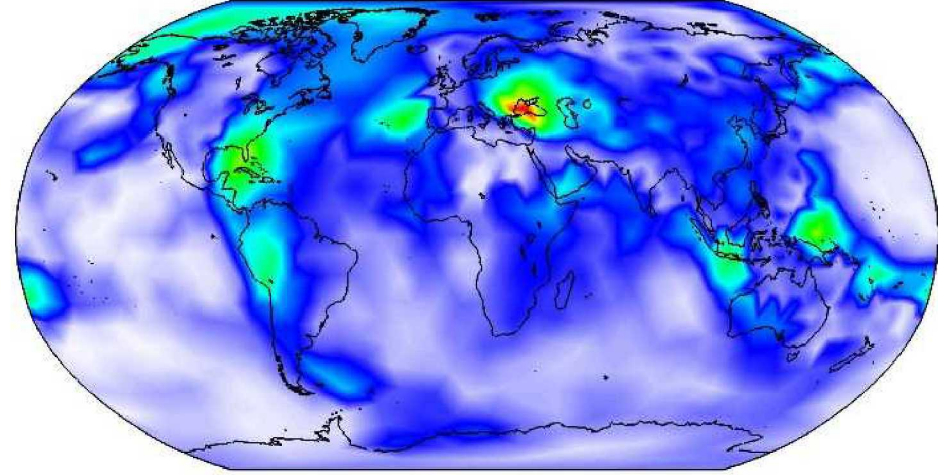
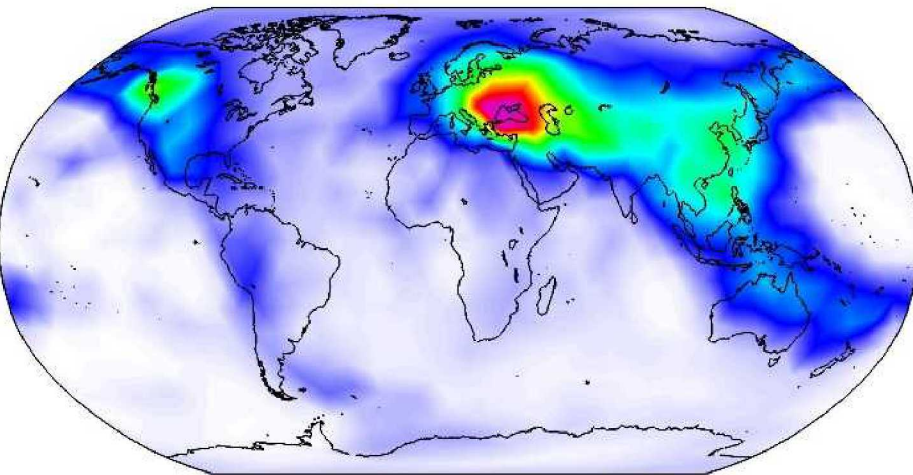
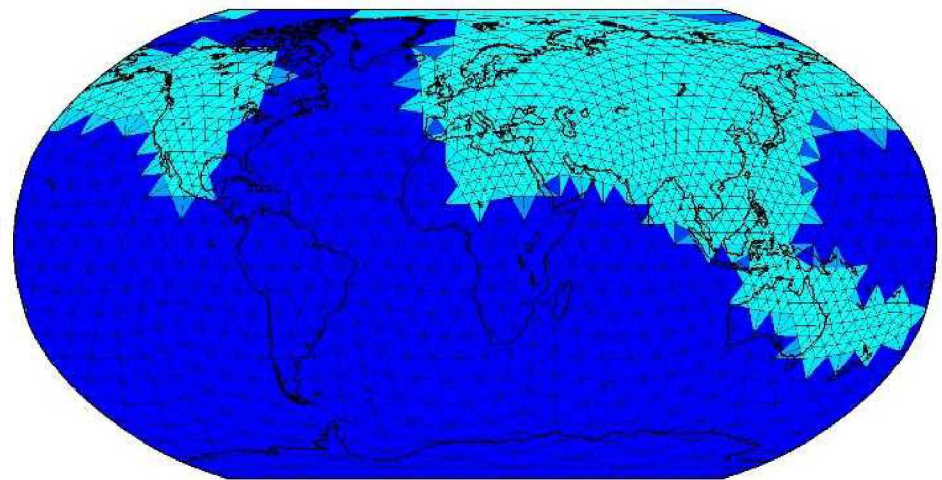
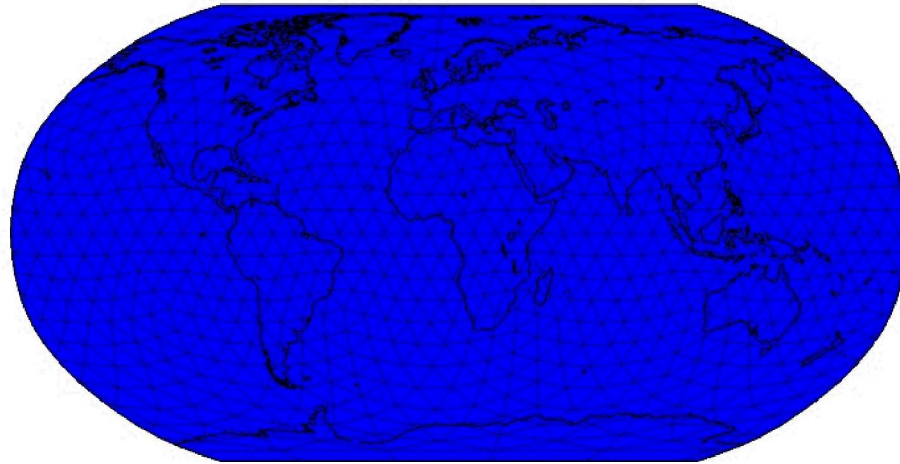
$$\tilde{t}_p = \sum_{j=0} w_{pj} \tilde{s}_j \pm \tilde{\sigma}_p \quad \tilde{\sigma}_p = \sqrt{W(\tilde{s}_m) \tilde{C}_m W^T(\tilde{s}_m) + W(s_m) C_m W^T(s_m)}$$

Here  $W(\tilde{s}_m)$  imply weights for nodes along the path  $p$  that lie in regions of the posterior model (the mantle), while  $W(s_m)$  define weights for nodes along the path that lie in prior model regions for which slowness updates were not computed (the crust).

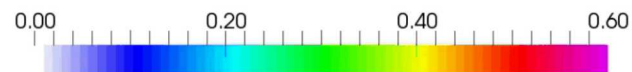


# Grid and Model Resolution

Triangle Edge Length (degrees)

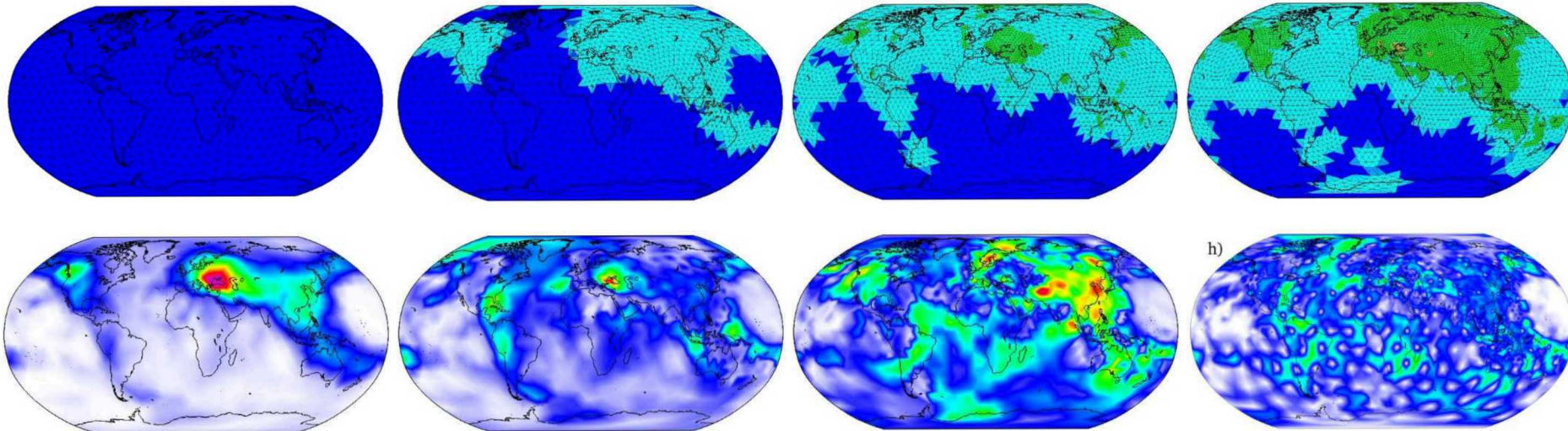


Model Resolution

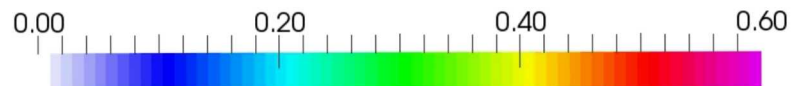


# Grid and Model Resolution

Triangle Edge Length (degrees)



Model Resolution



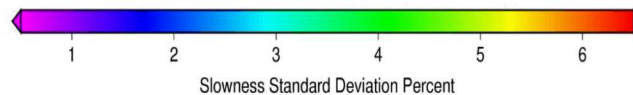
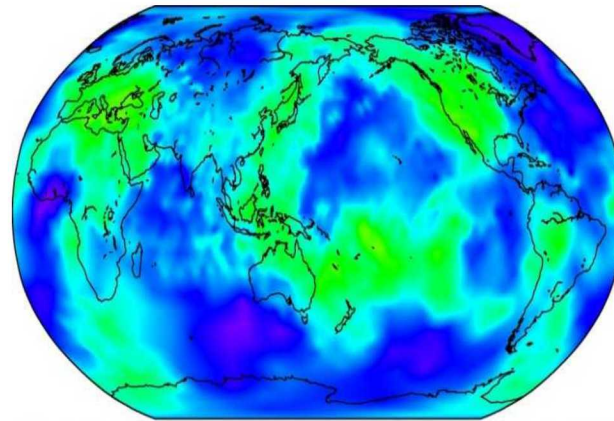
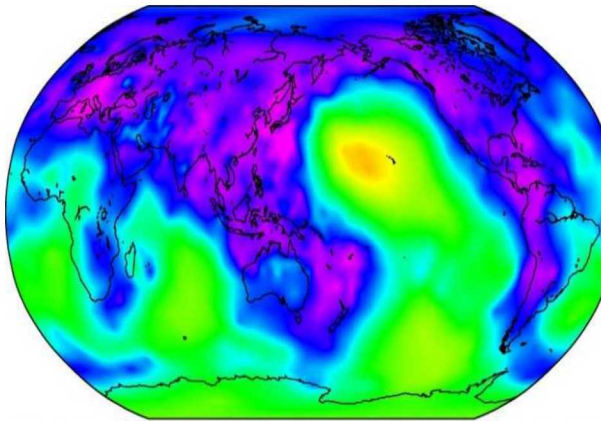
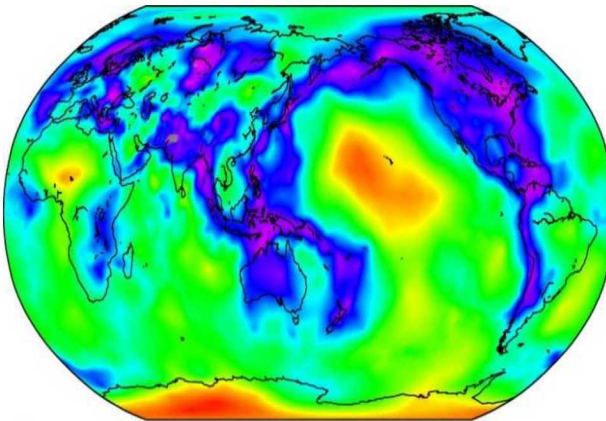
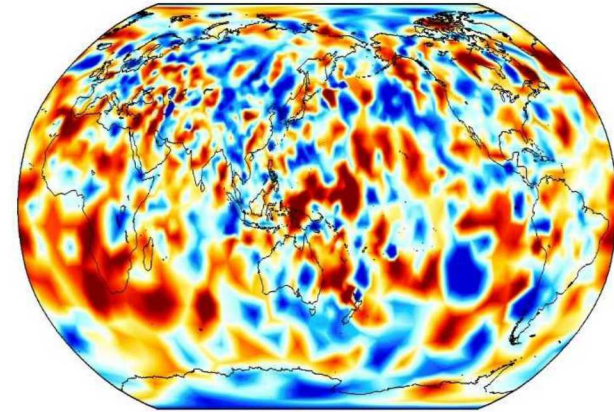
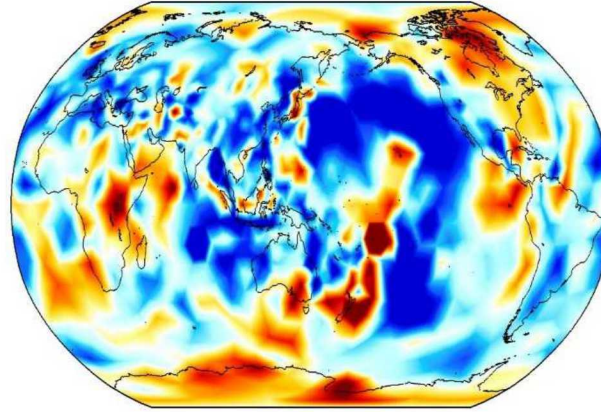
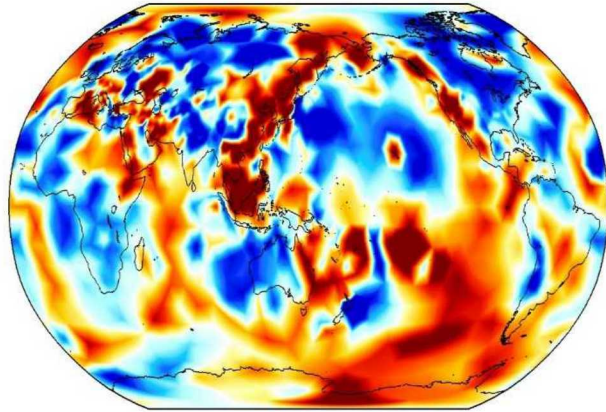


# Mantle Slowness and Slowness Uncertainty

100 km  
 $\pm 3\%$

500 km  
 $\pm 2\%$

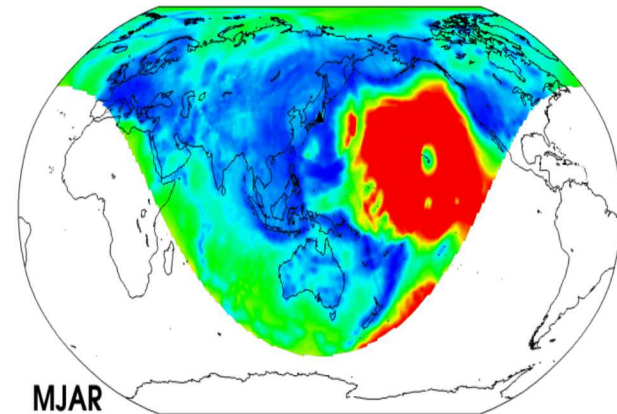
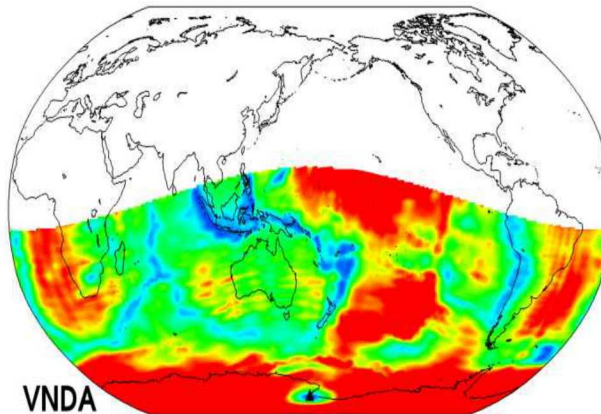
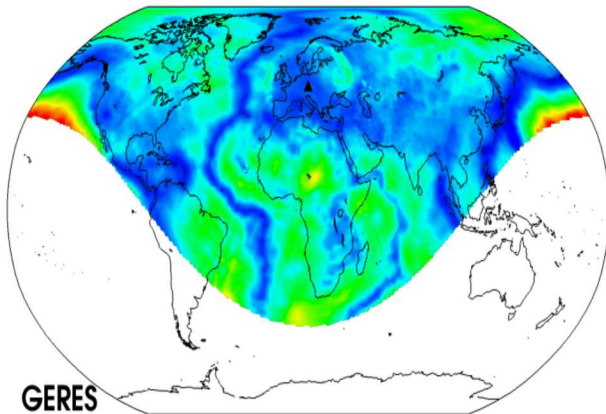
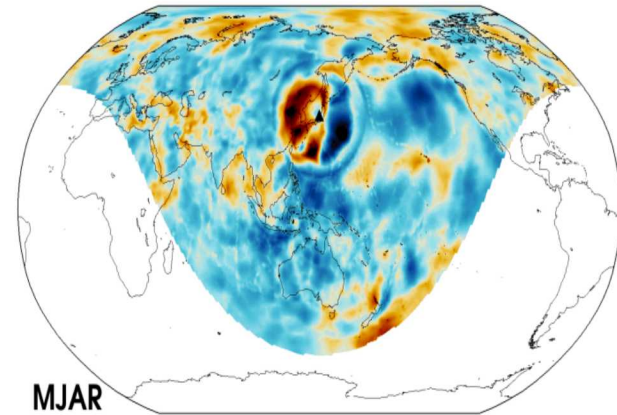
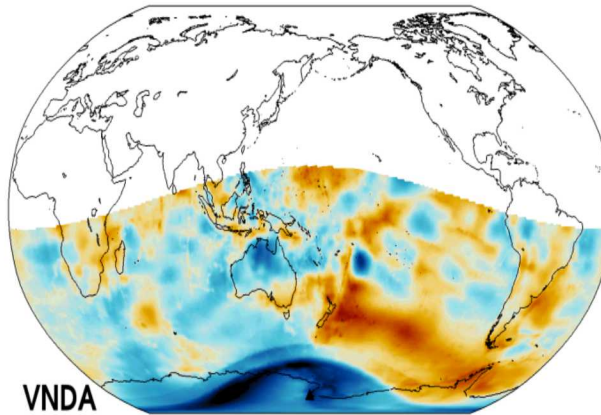
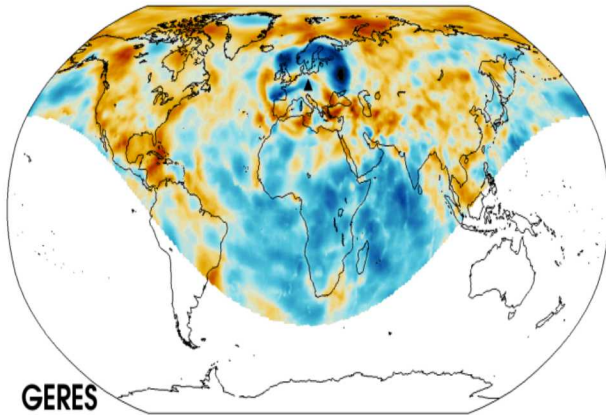
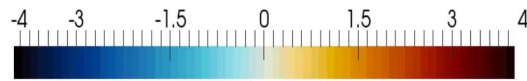
2500 km  
 $\pm 1\%$





# Travel Time Prediction and Uncertainty

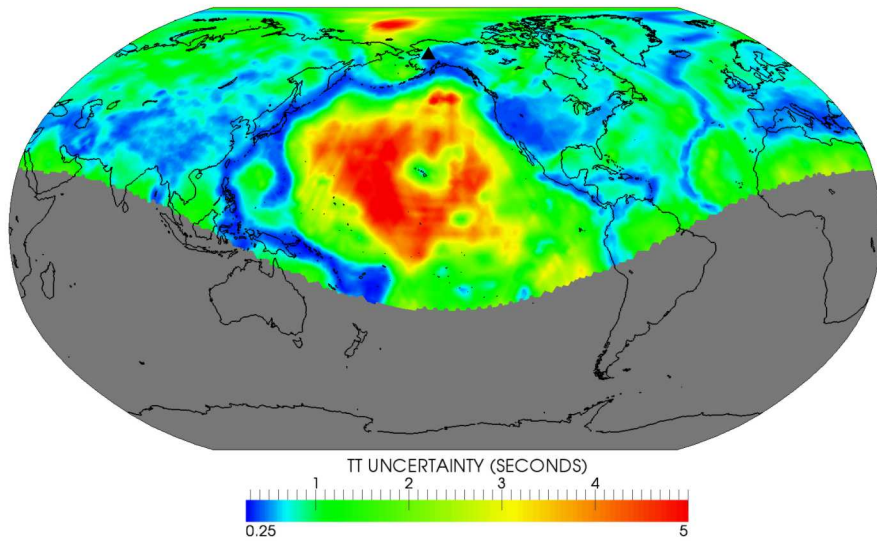
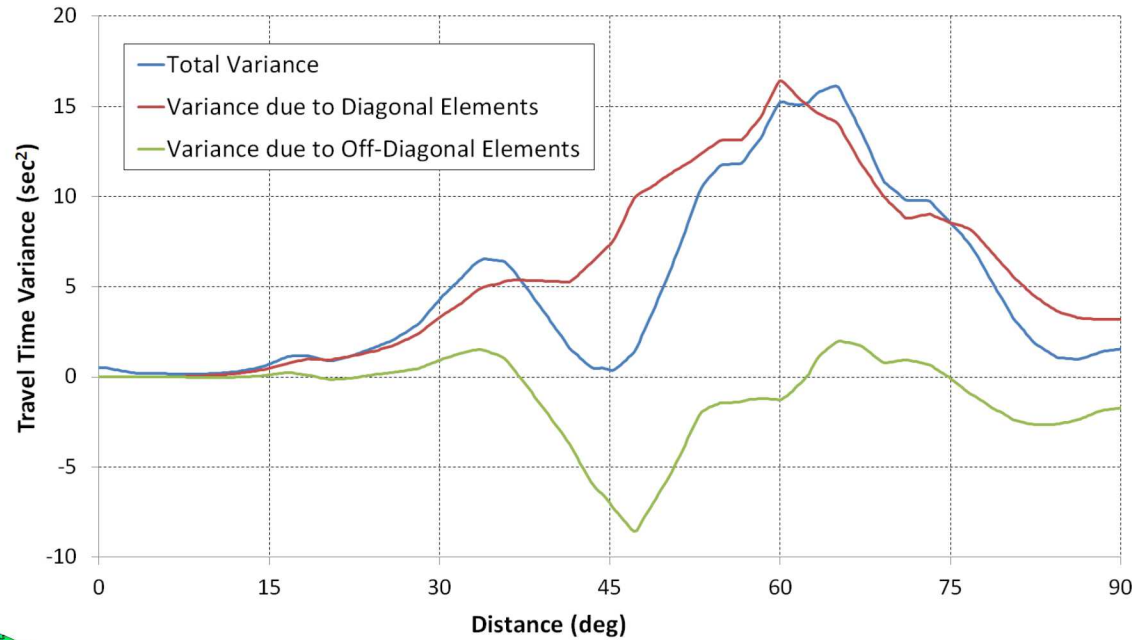
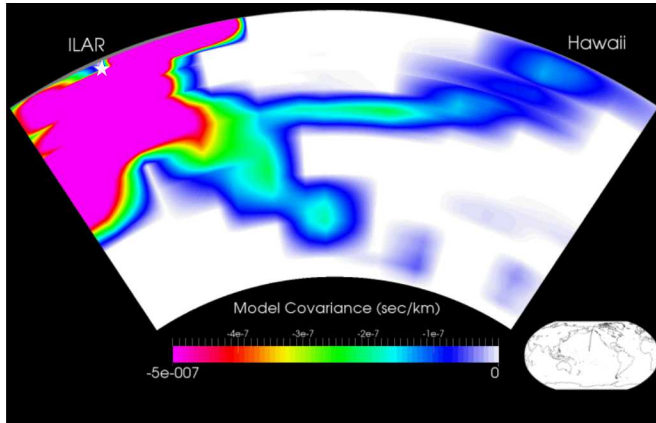
Travel Time Change from ak135 (seconds)



Travel Time Uncertainty (seconds)

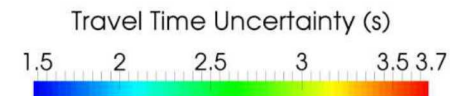
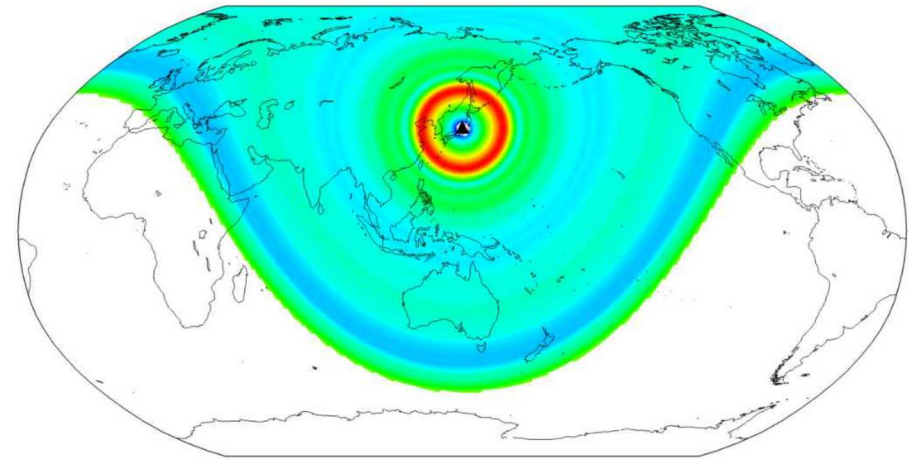
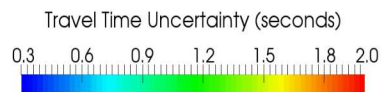
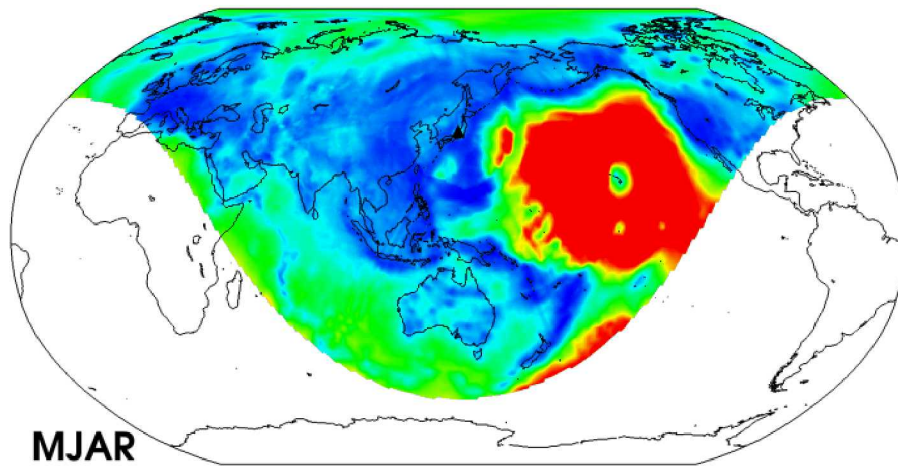
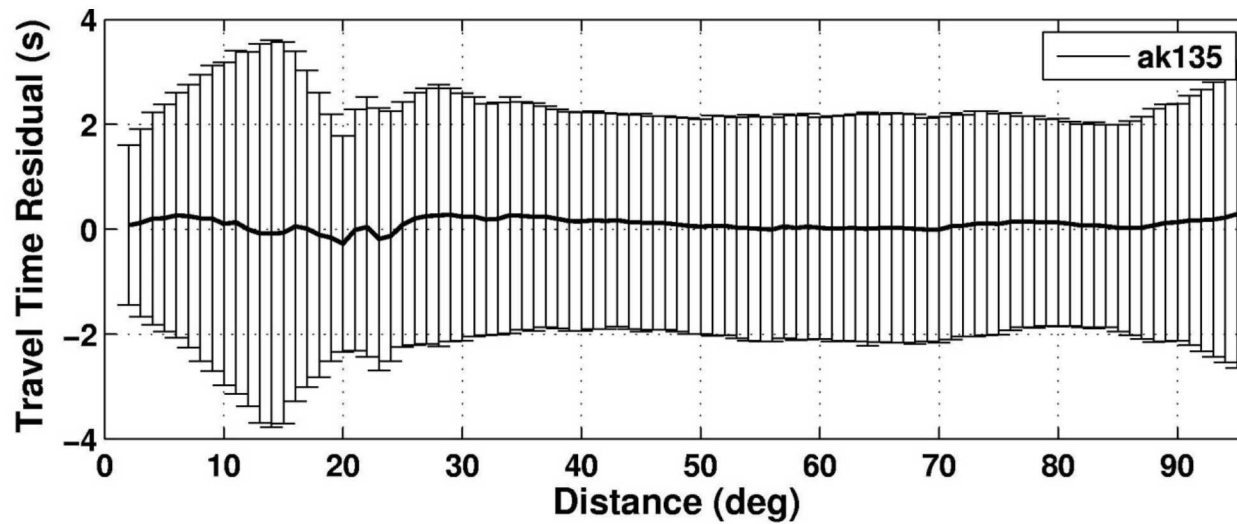


# Significance of Off-Diagonal Terms

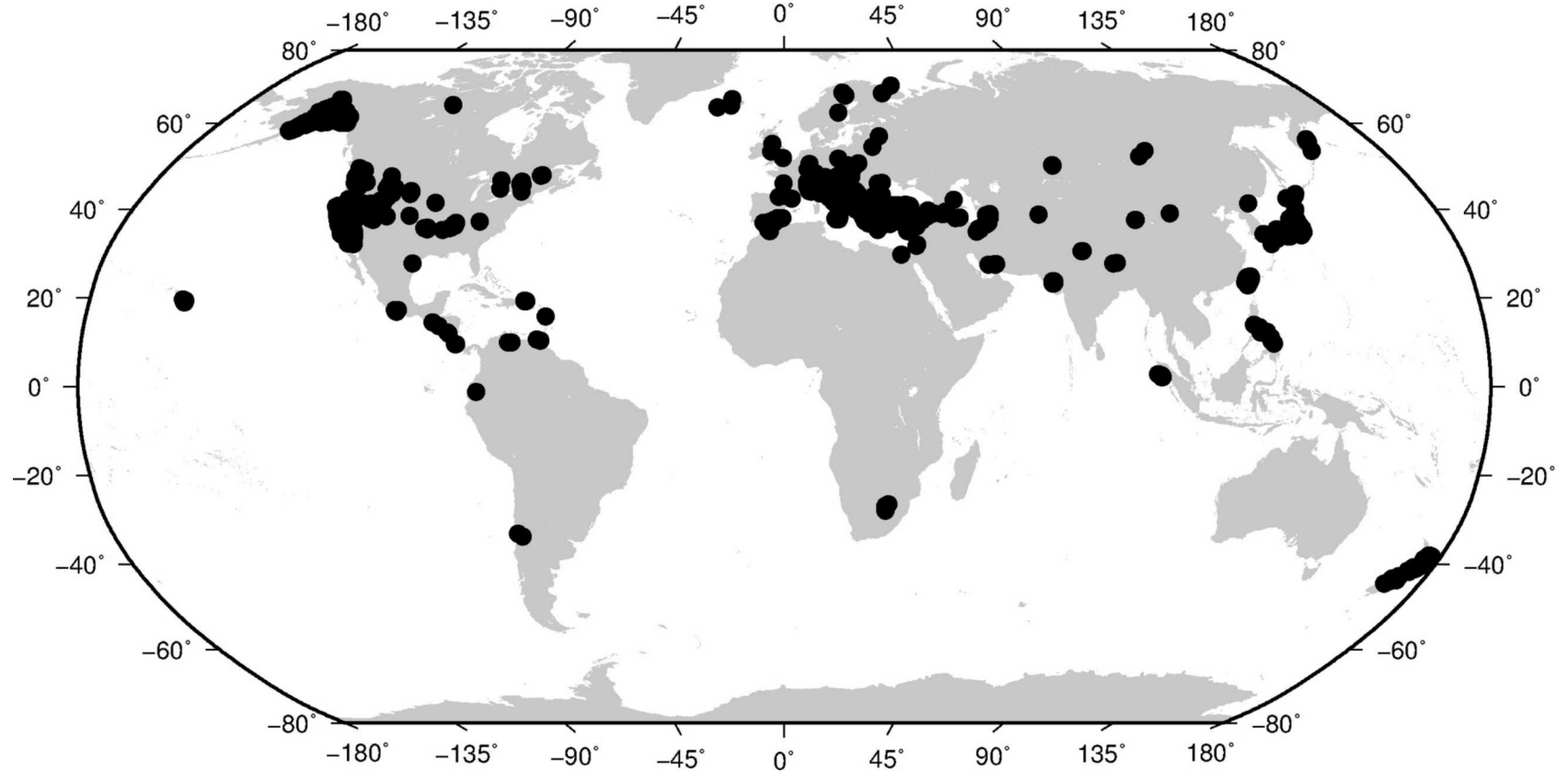




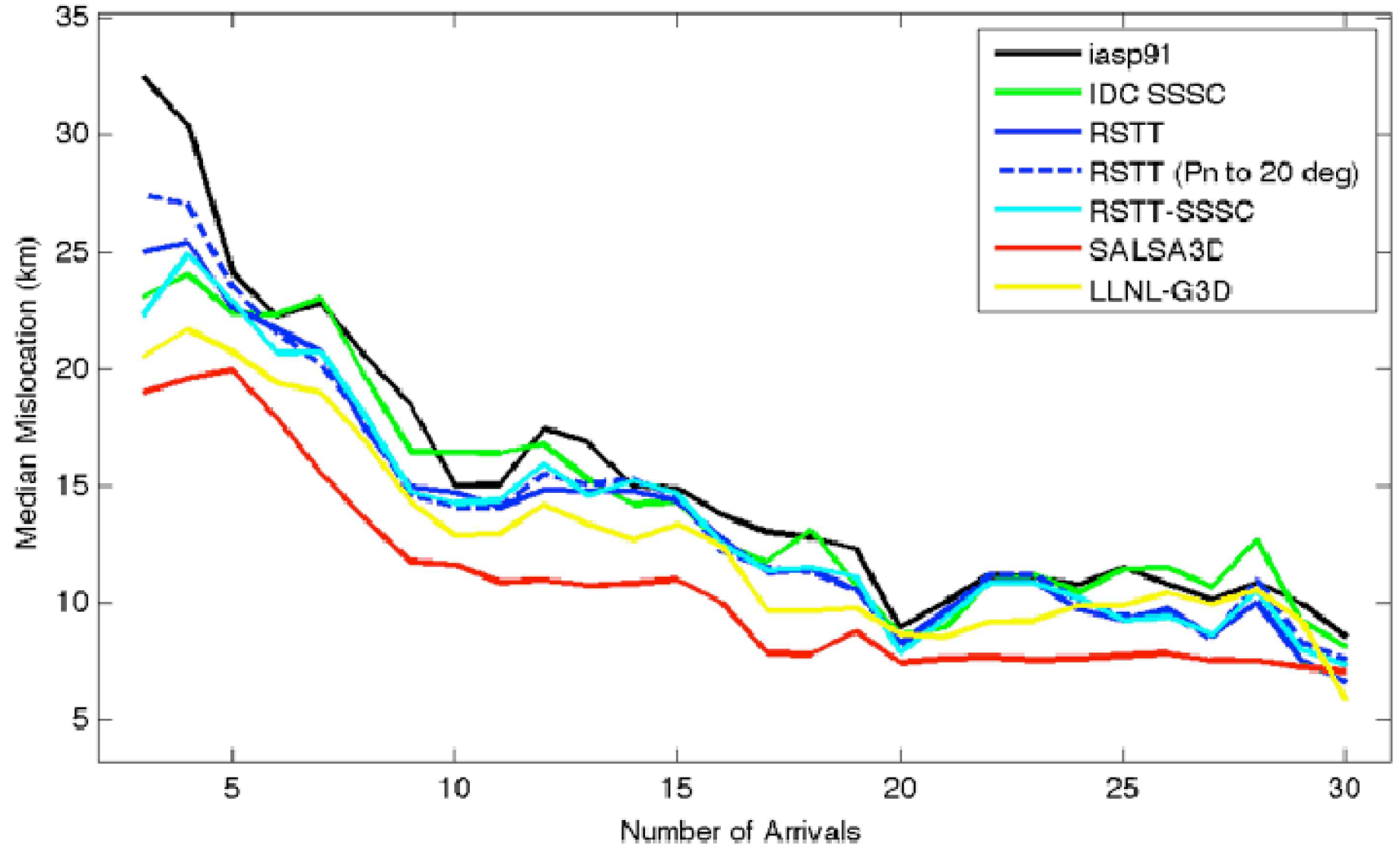
# Comparison with Standard Uncertainty



# Seismic Events Used for Validation

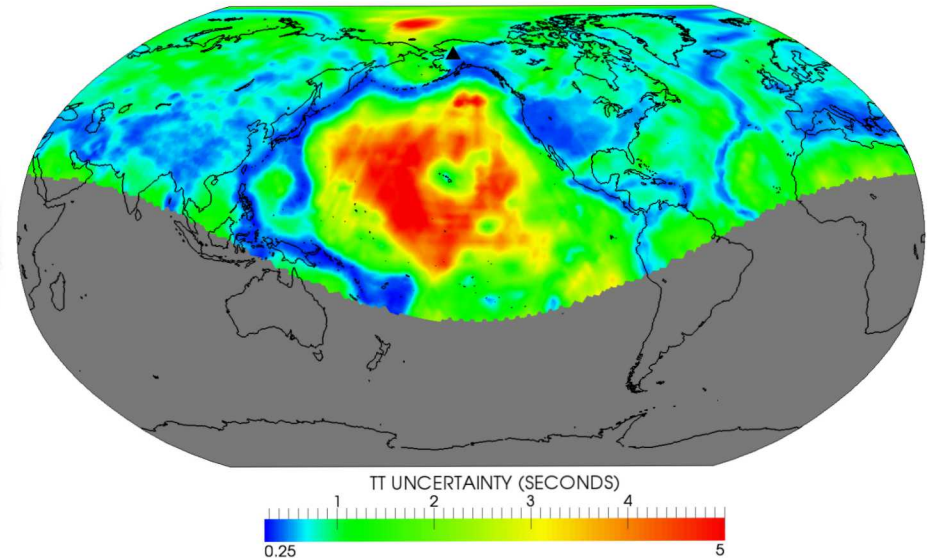
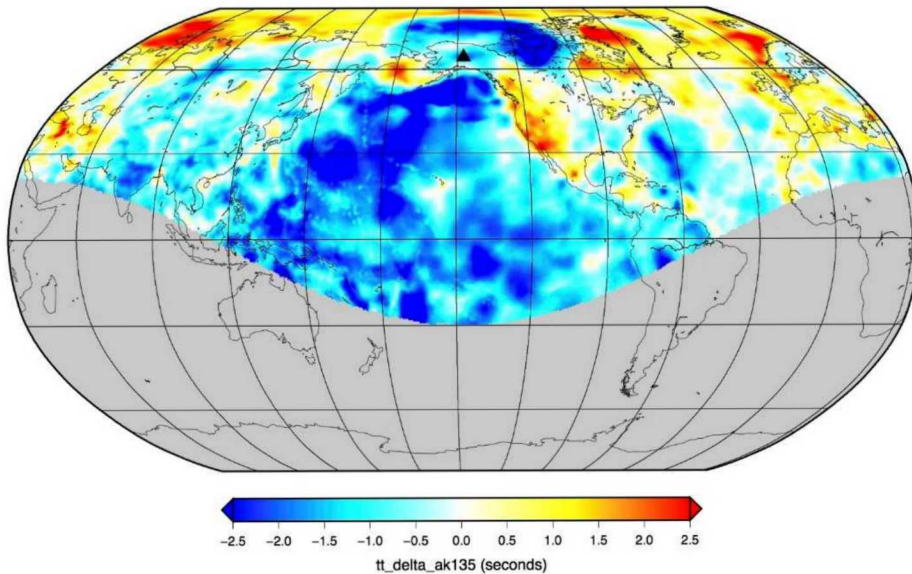
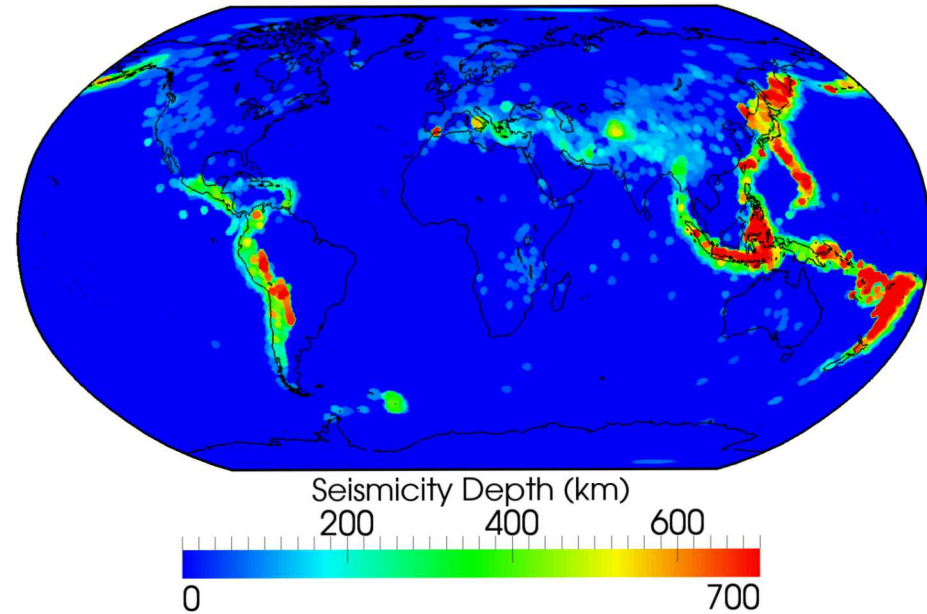


Mislocation Information



# GeoTess

- Station-phase specific travel time difference relative to ak135.
- Path-dependent travel time prediction uncertainty (model error).
- First-P lookup tables for the IMS primary and auxiliary network requires about 3GB of RAM.



# Summary

- We have developed a global 3D model of the seismic wave speed distribution in the Earth.
- We successfully computed the model covariance matrix for our model which allows us to calculate path-dependent travel time uncertainty estimates.
- The model significantly improves the accuracy and precision and seismic event locations.
- We have developed 3D travel time lookup tables for the IMS network to mitigate performance issues related to the use of 3D models in operational systems
- Our grid management software GeoTess has been released as open source software and can be accessed at [www.sandia.gov/geotess](http://www.sandia.gov/geotess)



# Future Work

- For SALSA3D, we did not invert for the crustal model. We are planning on creating a local crustal velocity model in near proximity of the state of Utah using arrivals provided by the UUSS in an effort to assess the applicability of our tomography approach to crustal tomography.
- We will extend the tomography campaign to include surface wave data for a better sampling of the crust and uppermost mantle.
- Similar to SALSA3D, we intend to develop a 3D velocity model for *S*-wave travel time prediction.
- We intend to develop velocity/attenuation models of the Earth's crust and mantle based on full waveform tomography methods.

# SALSA3D - References

- Ballard, S., J. R. Hipp, M. L. Begnaud, C. J. Young, A. V. Encarnacao, E. P. Chael, W. S. Phillips (2016) SALSA3D – A Tomographic Model of Compressional Wave Slowness in the Earth's Mantle For Improved Travel Time Prediction and Travel Time Prediction Uncertainty, Bulletin of the Seismological Society of America, Vol. 106, No. 6, pp. 2900-2916, December 2016, [doi: 10.1785/0120150271](https://doi.org/10.1785/0120150271).
- Ballard, S., J. Hipp, B. Kraus, A. Encarnacao, and C. Young (2016). GeoTess: A generalized Earth model software utility, Seismol. Res. Lett. 87, no. 3, [doi: 10.1785/0220150222](https://doi.org/10.1785/0220150222).
- Ballard, S., J. R. Hipp and C. J. Young (2009). Efficient and Accurate Calculation of Ray Theory Seismic Travel Time through Variable Resolution 3D Earth Models, Seismological Research Letters v 80, 6 [doi: 10.1785/gssrl.80.6.989](https://doi.org/10.1785/gssrl.80.6.989).