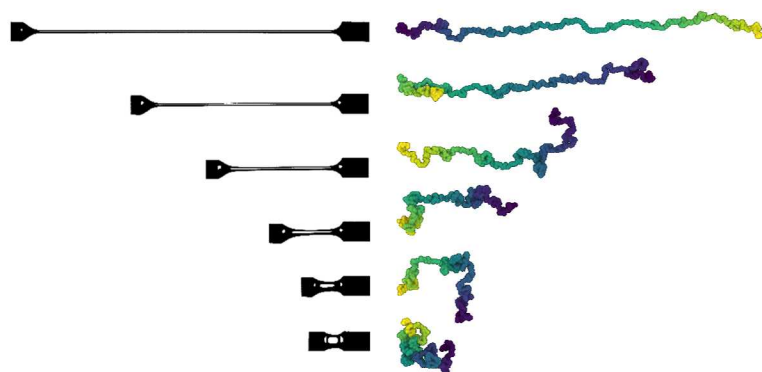


# Unexpected Extensional Rheology in Ring Polymer Melts



PRESENTED BY

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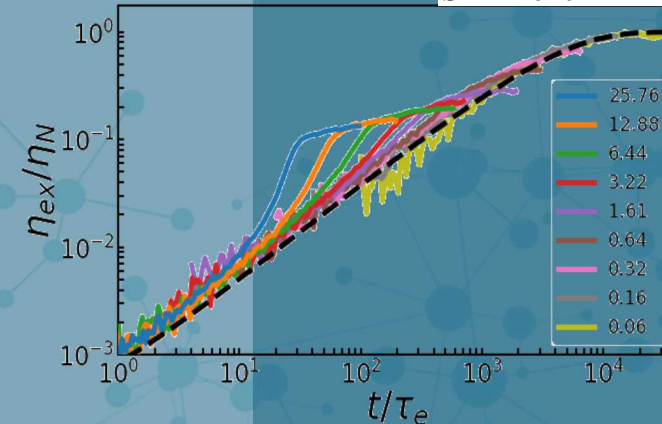


Gary S. Grest (SNL),

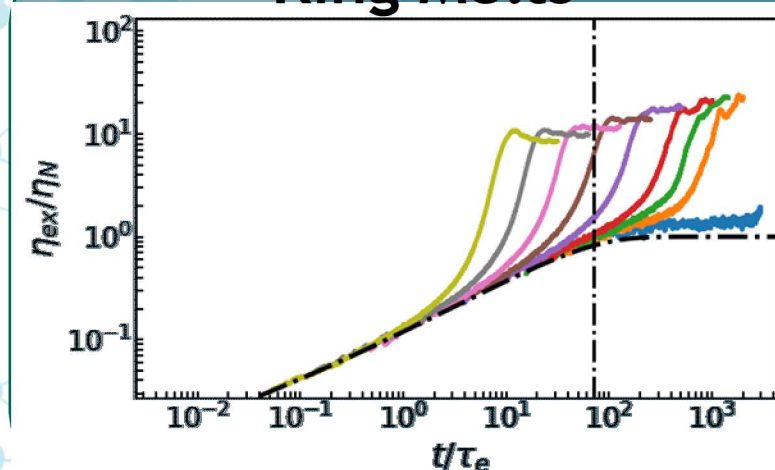
Ting Ge, Michael Rubinstein (DUKE)

## Linear Melts

SAND2019-2214C

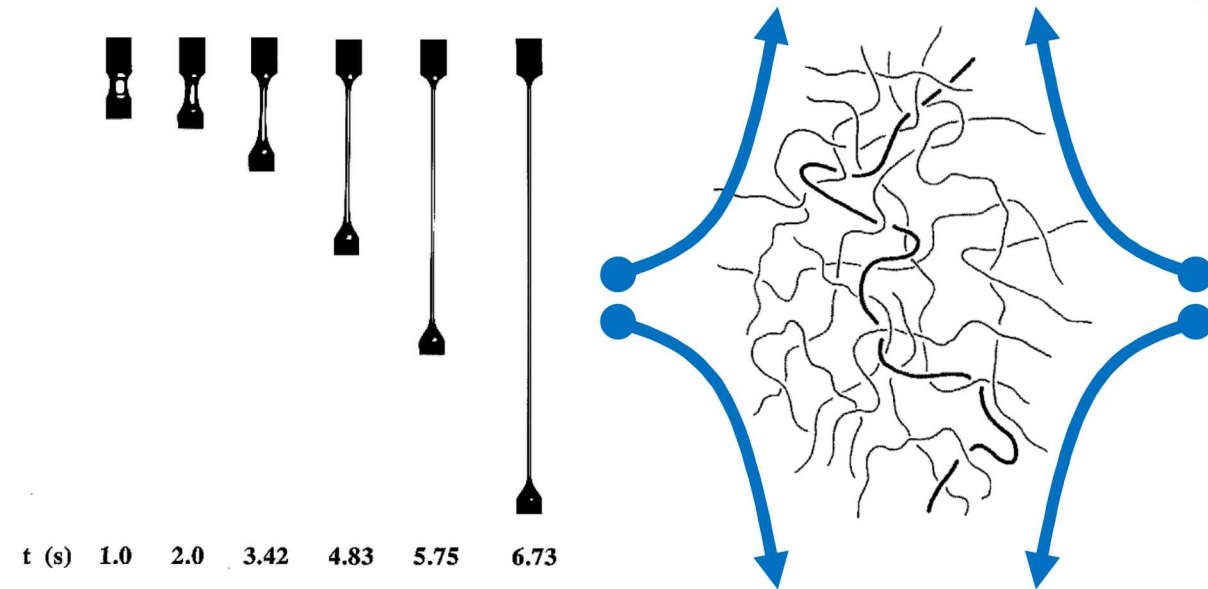


## Ring Melts



# Nonlinear Extensional Flows Alter Chain Conformation

Uniaxial extension flows stretch liquids exponentially in time. Rate of elongation set by the **strain rate**  $\dot{\epsilon} \equiv \frac{\partial \log(\lambda)}{\partial t}$



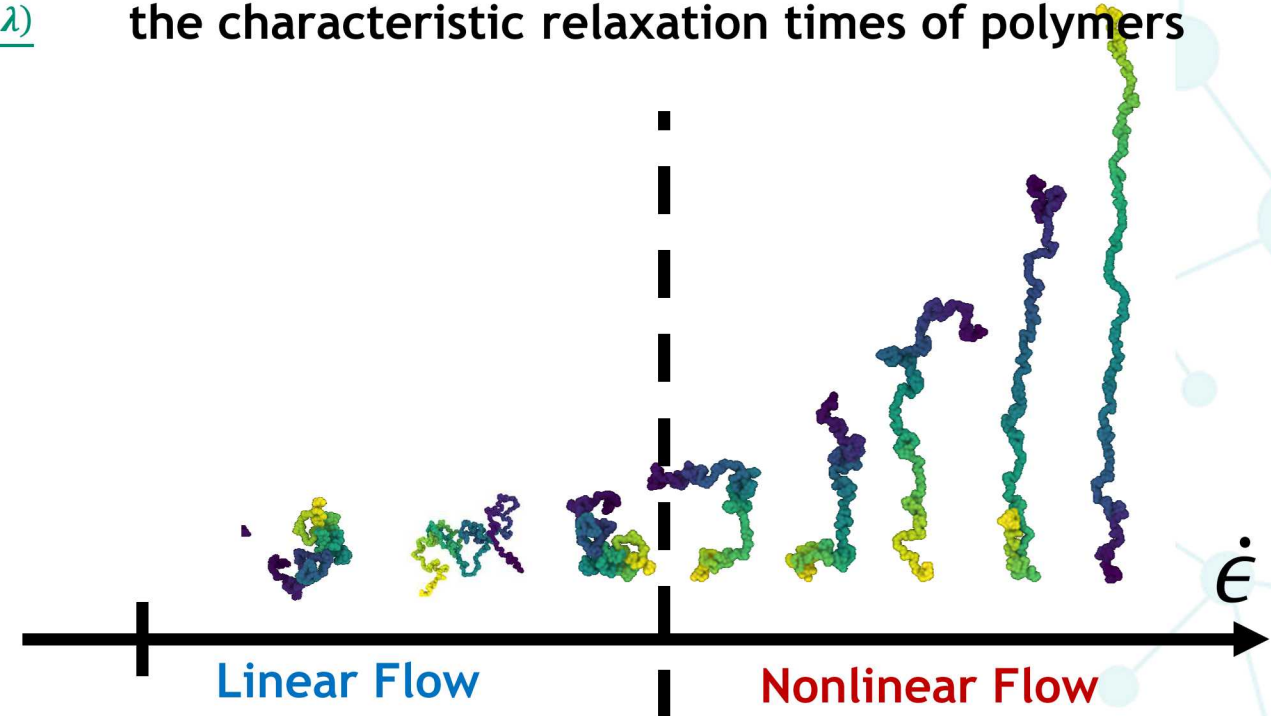
Measure flow strength with a Weissenberg number:

$$Wi_R = \dot{\epsilon} \tau_R$$

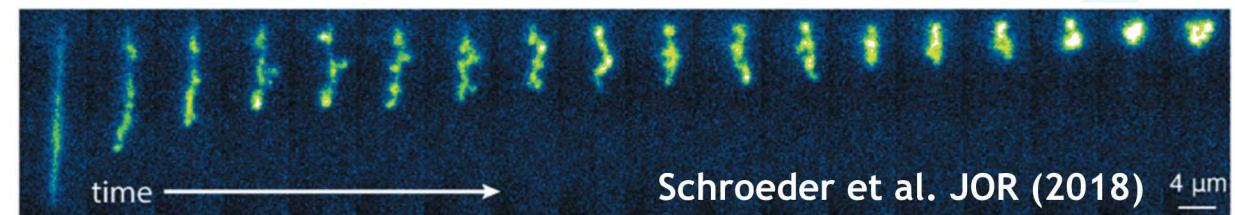
$Wi_R \rightarrow 0$  Newtonian

$Wi_R > 1$  Elongation

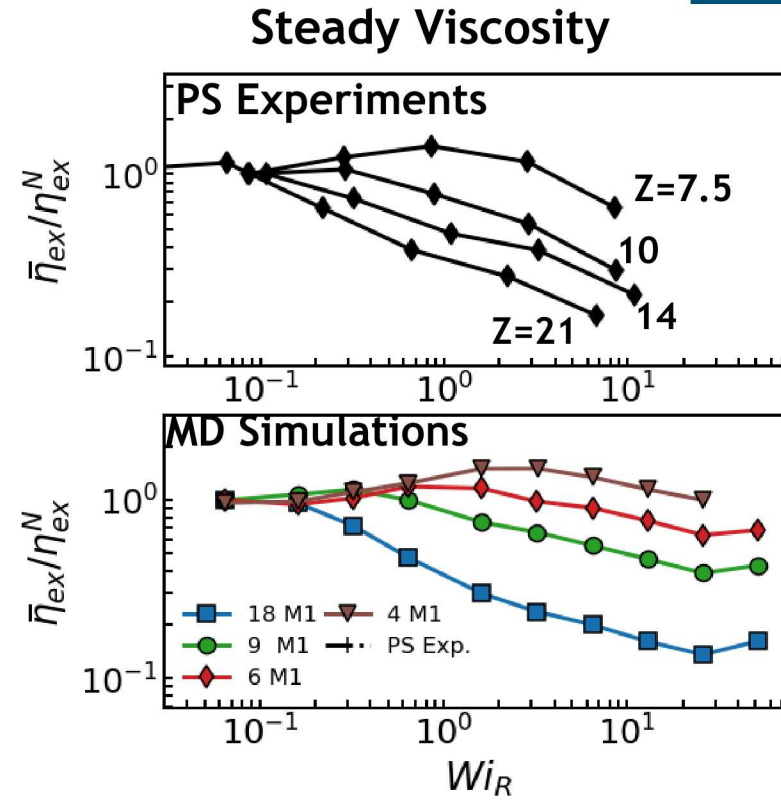
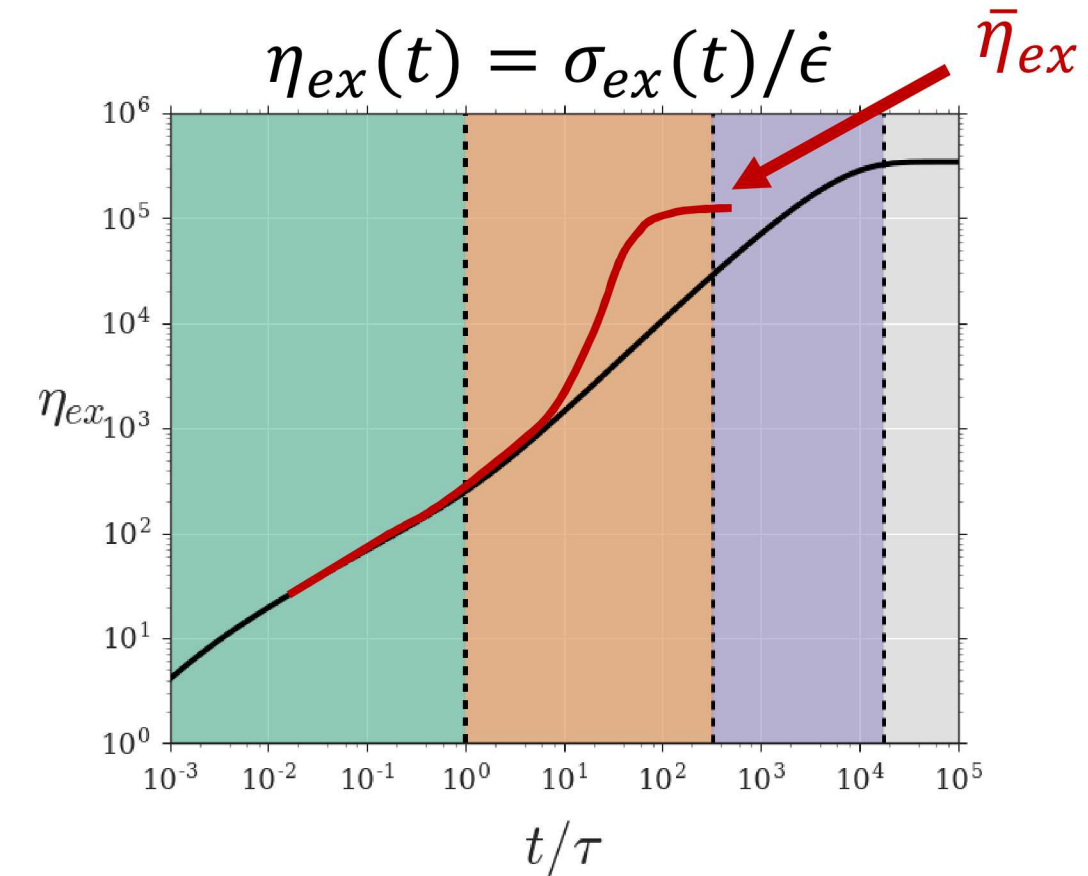
Nonlinear behavior occurs when  $\dot{\epsilon}$  is faster than the characteristic relaxation times of polymers



Linear chains relax stretch over the **Rouse time**  $\tau_R \sim N^2$



# MD Captures Nonlinear Dynamics and Rheology



*O'Connor, Alvarez, Robbins, PRL (2018)*

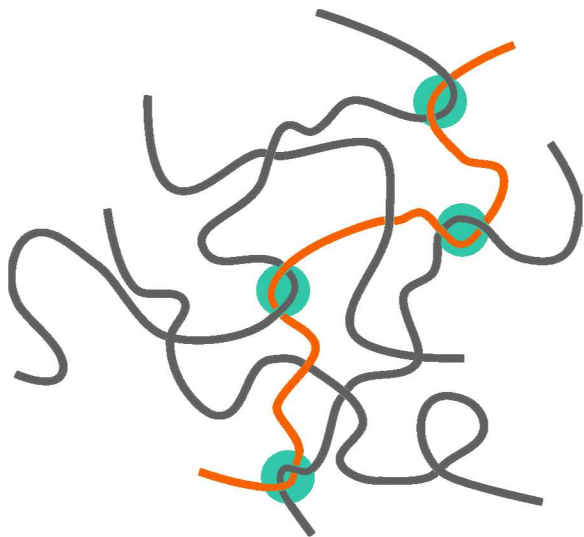
## Weak Linear Flows ( $Wi \rightarrow 0$ ):

- Viscosity evolves along a limiting curve (LVE), and plateaus to Newtonian viscosity.
- Controlled by equilibrium chain dynamics - very different for linear & ring polymers.

## Strong Nonlinear Flows ( $Wi > 1$ ):

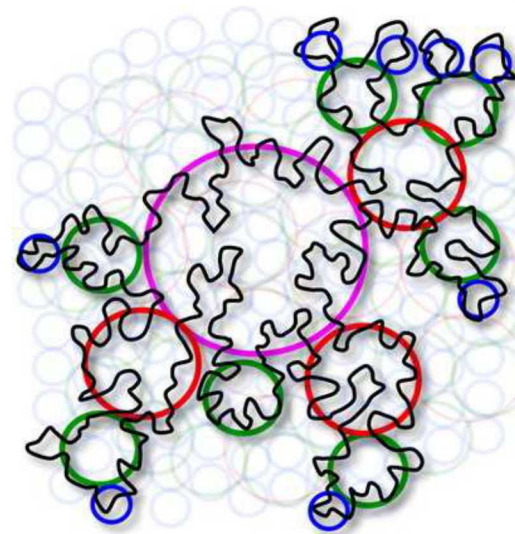
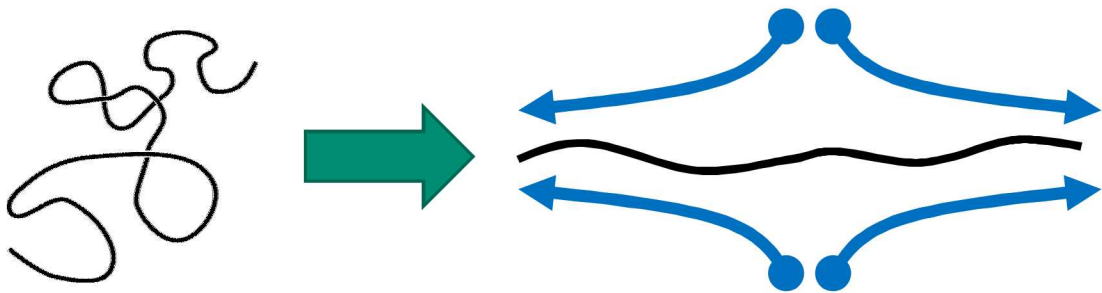
- Viscosity increases more rapidly than the LVE and plateaus to a nonlinear value  $\eta_{ex}(\dot{\epsilon})$ .
- MD reproduces nonlinear rate-dependence and relates to chain conformations: *O'Connor et al., PRL (2018)*

# Comparing Linear Melts and Ring Melts In Extensional Flow



Entanglements confine chains to a primitive path, & create a hierarchy of exponential relaxation times.

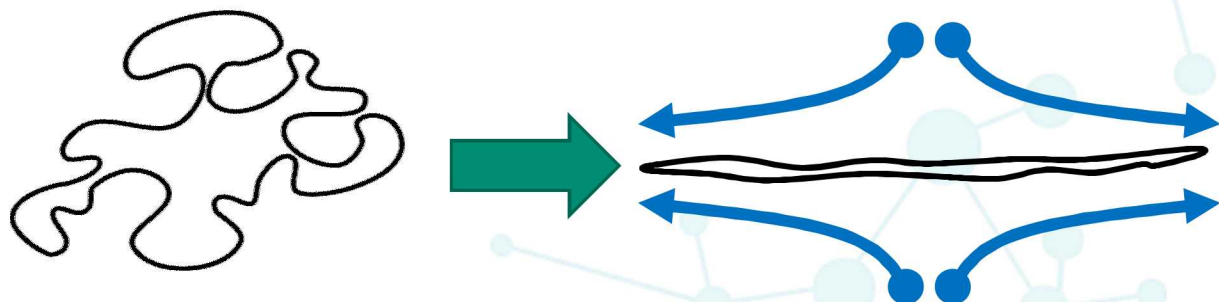
Longest relaxation time  $\tau_d \sim N^{3.4}$



T. Ge, M. Rubinstein,  
Macromol. (2016)

Fractal hierarchy of interpenetrating loops that gives a power-law viscoelastic relaxation

Longest relaxation time  $\tau \sim N^{2.33}$

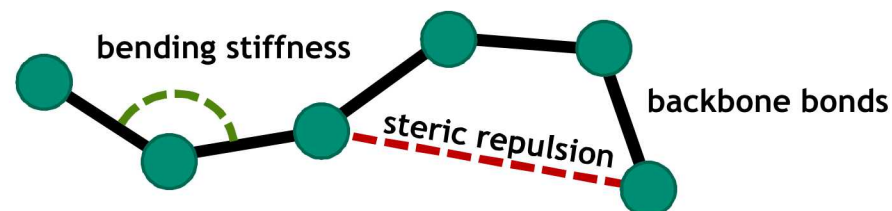


Equilibrium dynamics are very different, but elongated states are similar. Ring to linear crossover? 4

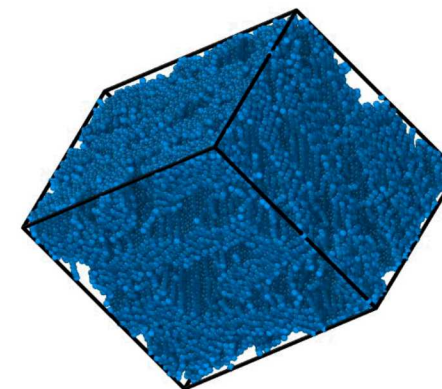
# Nonlinear Elongation of Ring Polymer Melts



## Model: Semiflexible bead-spring model



- linear properties well known ( $N_e \approx 28$  beads)
- Rings with  $N=200, 400, \& 800$  beads
- Compare to linears with  $N=100, 200, \& 400$  beads
- Same contour length at full extension



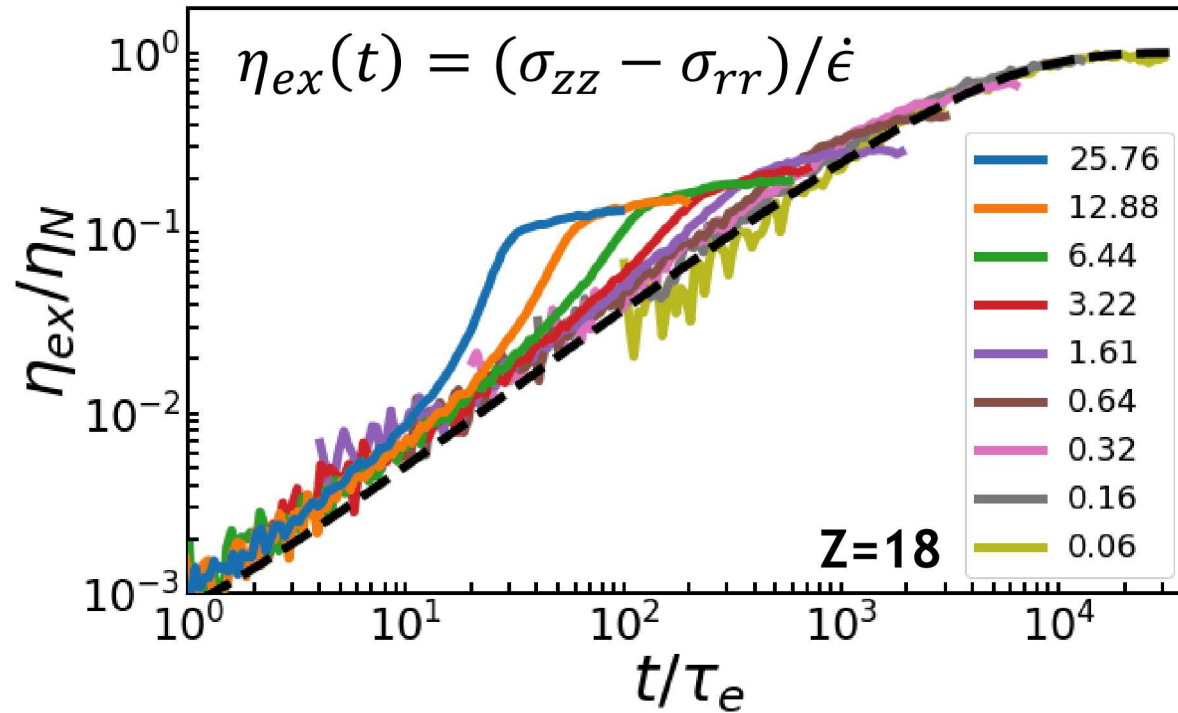
## Constant-rate uniaxial extensional flows

- Elongate to strain  $\epsilon > 6.0 \rightarrow$  resolve steady-state
- Vary  $Wi = \dot{\epsilon}\tau = 0.16 - 0.25$
- Linear:  $Wi = \dot{\epsilon}\tau_R$     Ring:  $Wi = \dot{\epsilon}\tau$
- Relate rate-dependence to chain dynamics

Rate dependence - do highly extended rings behave like linear chains?

Dynamics - how do rings elongate in the absence of entanglements?

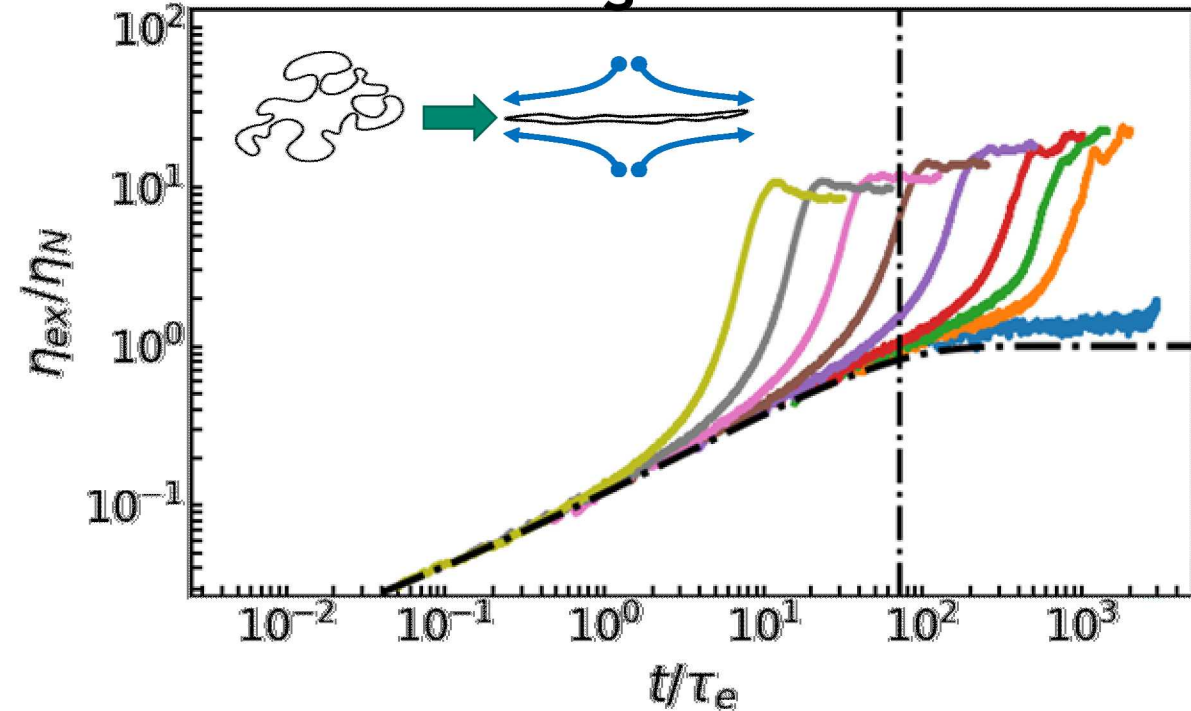
## N=200 Linear Melt Extension



$\eta_{ex}$  collapses onto LVE (dashed) as  $Wi \rightarrow 0$

Steady viscosity decreases with increasing  $Wi$ , typical of well-entangled melts.

## N=400 Ring Melt Extension

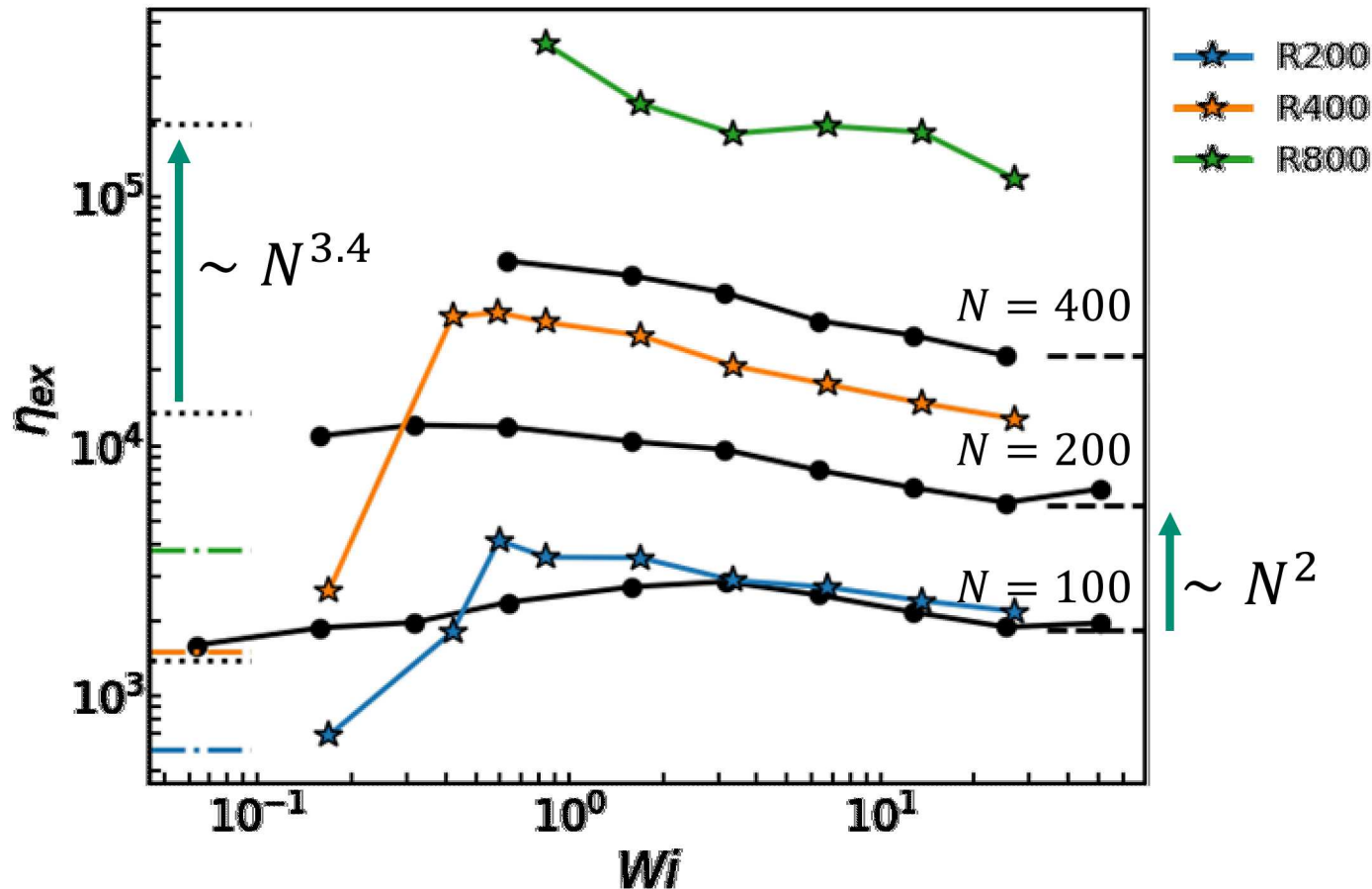


10x rise in viscosity at **ALL**  $Wi$  even  $Wi \ll 1$

Rise at low  $Wi$  *delayed* for many ring relaxation times (vertical dashed line)

Is dramatic viscosity rise due to elongated rings behaving like slower linear chains? <sub>6</sub>

## Steady-State Extensional Viscosity



## Linear melts with N=100,200,400

Newtonian viscosity  $\sim N^{3.4}$  tube theory

High Wi viscosity set by drag on highly extended chains  $\eta_{ex} \sim \zeta N^2$ .

*O'Connor, Alvarez, Robbins, PRL (2018)*

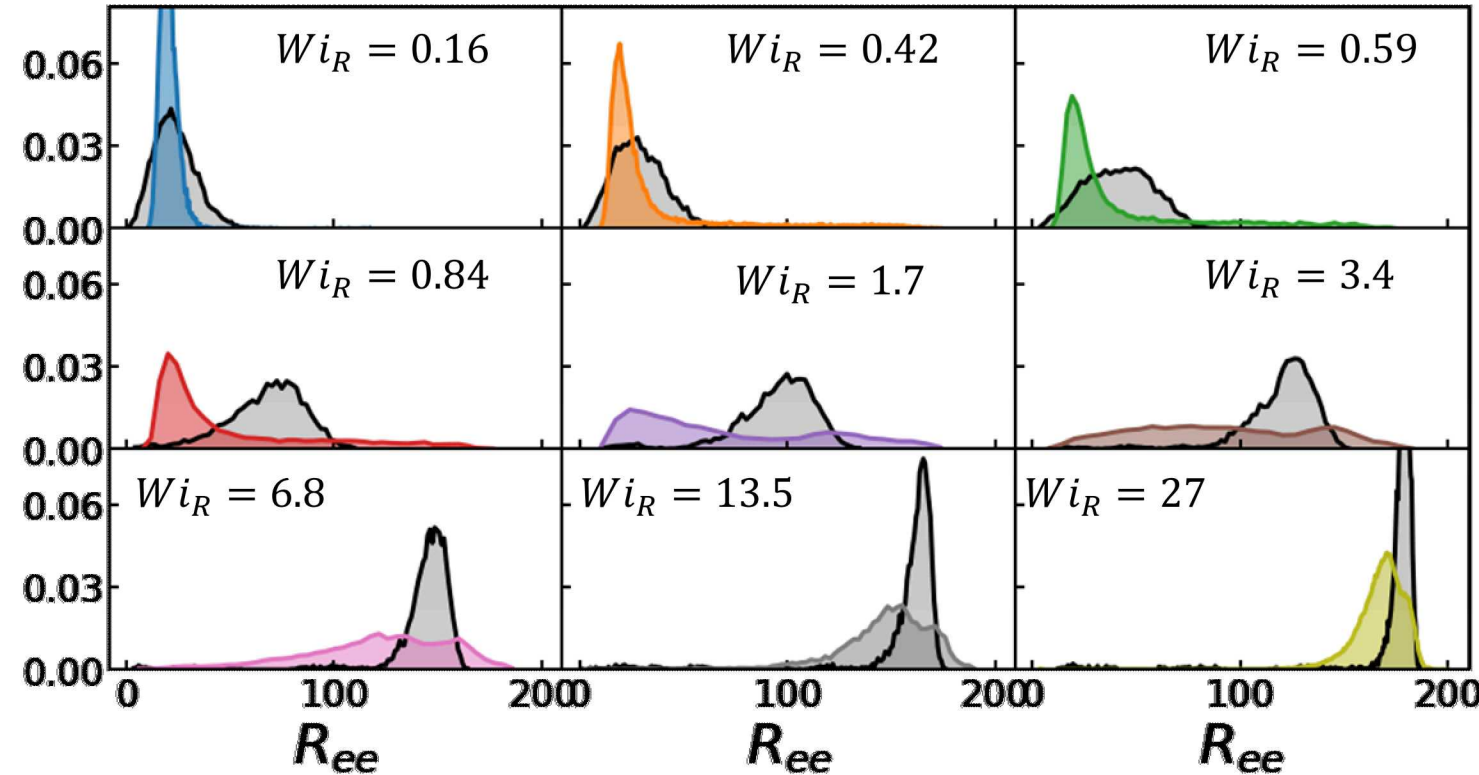
## Ring melts with N=200,400,800

N=200 ring viscosity appears to follow N=100 linear melt for  $Wi > 1$ .

Agreement breaks down as  $N$  increases.

Ring viscosity grows faster with  $N$  than it does for linear chains.

## Steady-State End-End Distributions



## Network Stretches Linear Chains ~Affinely

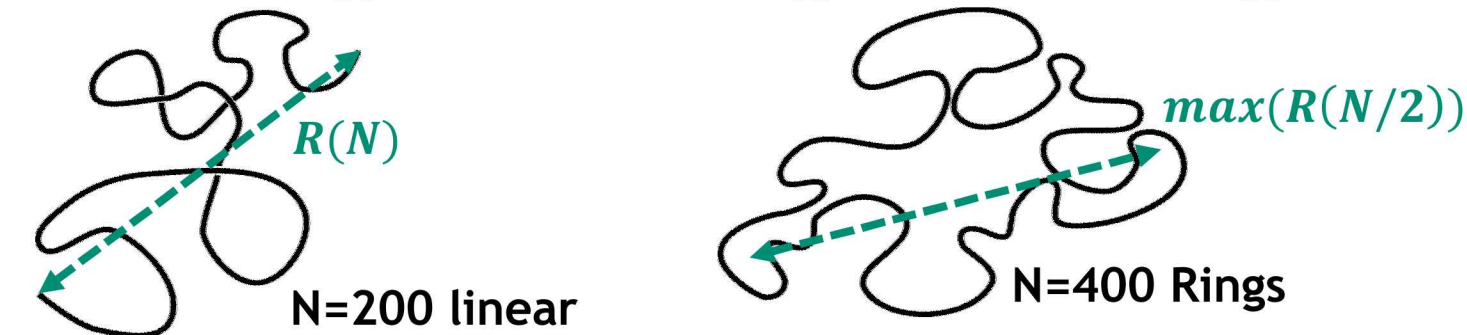
Chains stretch uniformly with single peak captured by average stretch  $\lambda$  in models

## Rings Dominated By Large Fluctuations

Develop long tail at low  $Wi$  of few highly stretched and retracting rings

Grows into a broad distribution of highly fluctuating rings at  $Wi \sim 1$

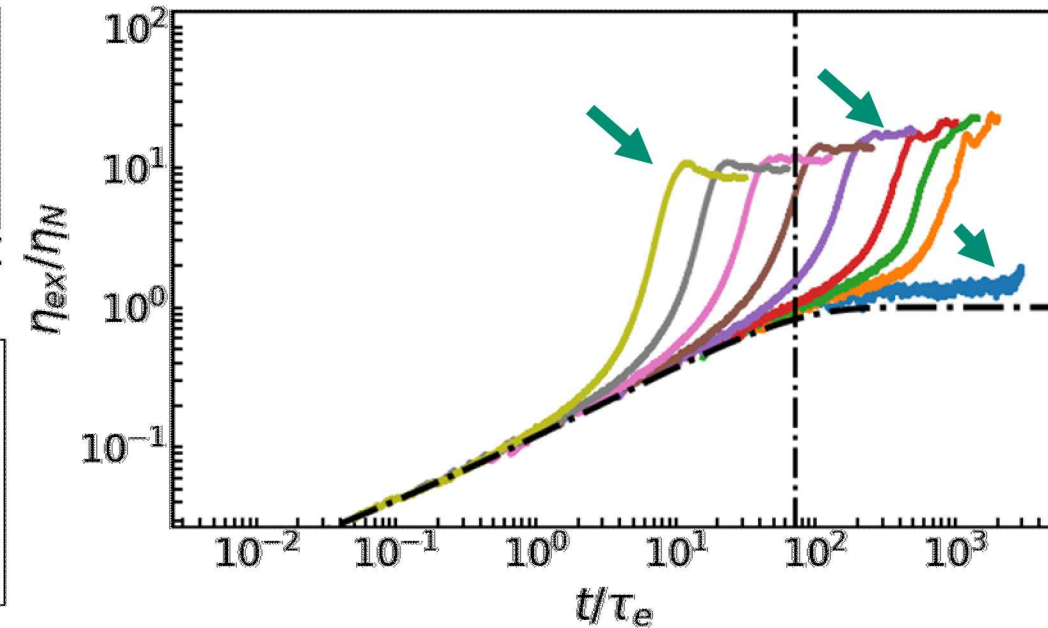
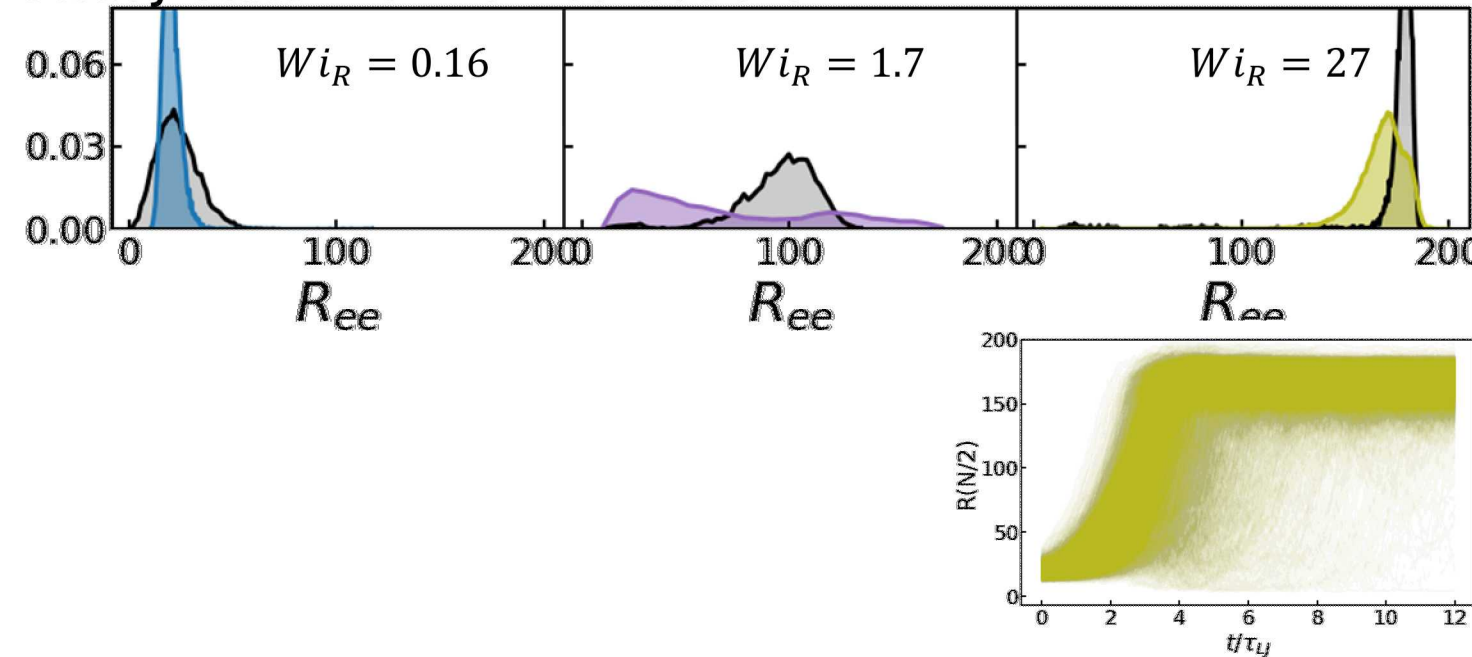
Large fluctuations cannot be described by averages



# Individual Chains Fluctuate Between Extended & Retracted



## Steady-State End-End Distributions



Individual chains only remain stretched at the highest  $Wi \sim 27$

$Wi=0.16$ : small fraction of highly stretched chains produce larger  $\eta_{ex}$  than fully stretched  $Wi=27$

Low & high  $Wi$  have qualitatively different distributions but similar nonlinear  $\eta_{ex}$

$Wi=0.16$ : small fraction of highly stretched chains produce larger  $\eta_{ex}$  than fully stretched  $Wi=27$

# Acknowledgements & Conclusions



## Collaborators:

Ting Ge, Michael Rubinstein (Duke)

Gary S. Grest (SNL)

## Funding:

Harry S. Truman Fellowship (SNL)

1. Simulations reveal unique extensional rheology for rings
2. Rings exhibit a massive and delayed rise in  $\eta_{ex}$ , even for  $Wi \ll 1$
3.  $Wi \ll 1$ : large  $\eta_{ex}$  from small # of stretched chains
4.  $Wi \sim 1$ : broad distributions, chains stretch and retract regularly
5. Large fluctuations cannot be captured by mean-field models

