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The SEARCH Software Suite Code Capabilities and Experimental Comparison

The 5th International Symposium - Supercritical CO₂ Power Cycles

March 28-31, 2016, San Antonio, Texas, USA

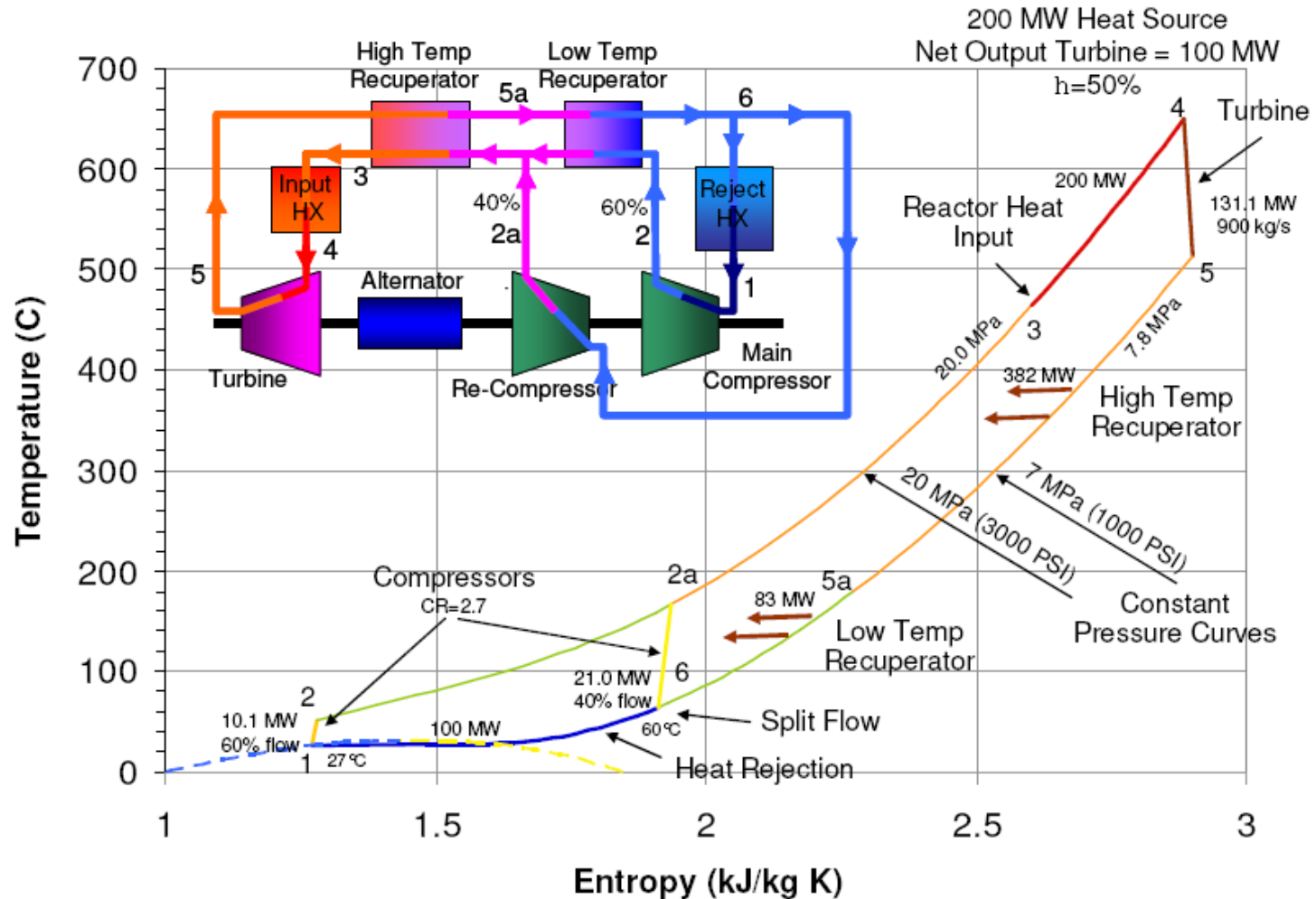
*Carlson, M. D, Bell, C., Schalansky, C., Fleming, D. F., Rochau, G.



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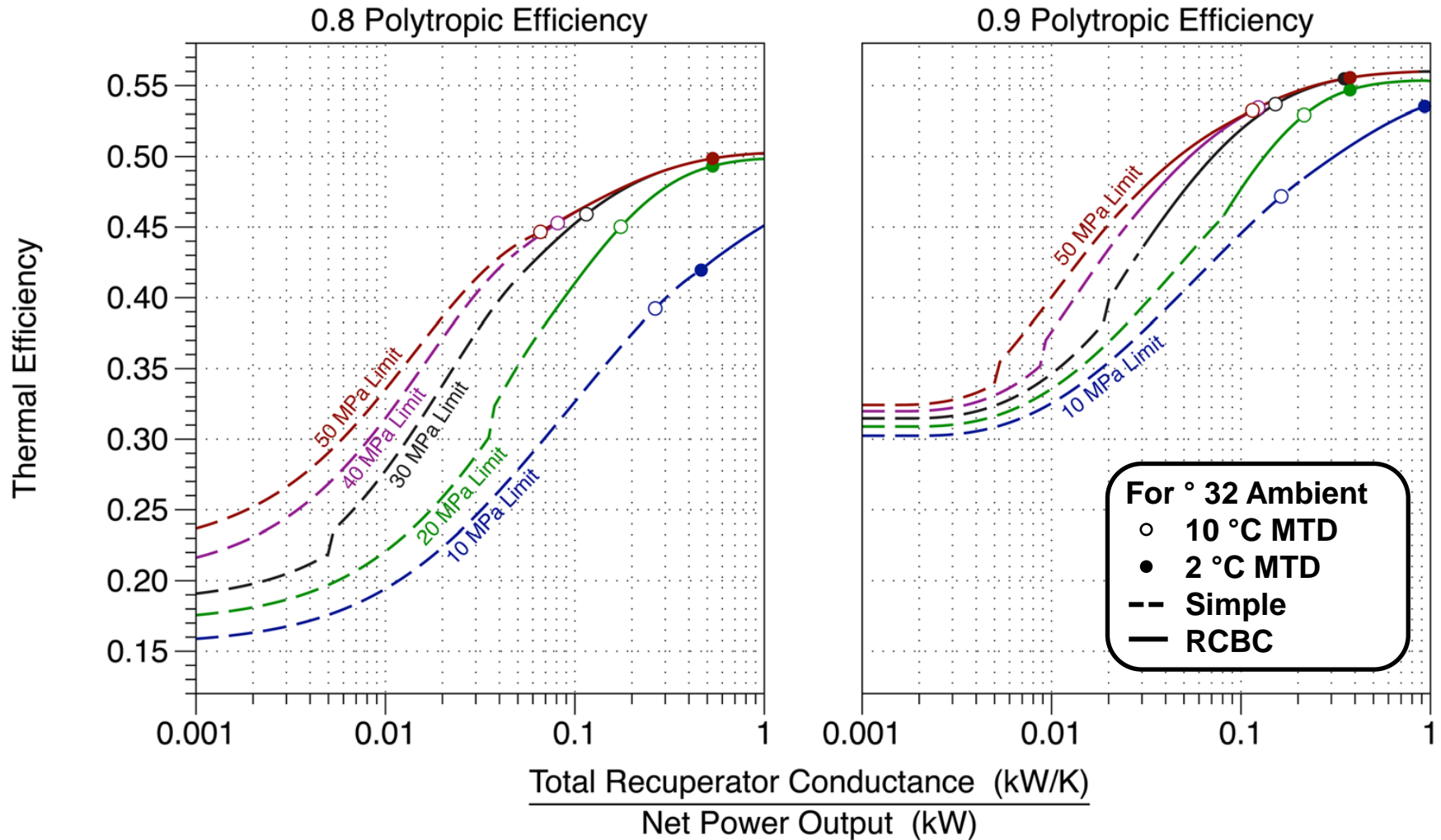
BACKGROUND

Supercritical CO₂ Brayton Cycle



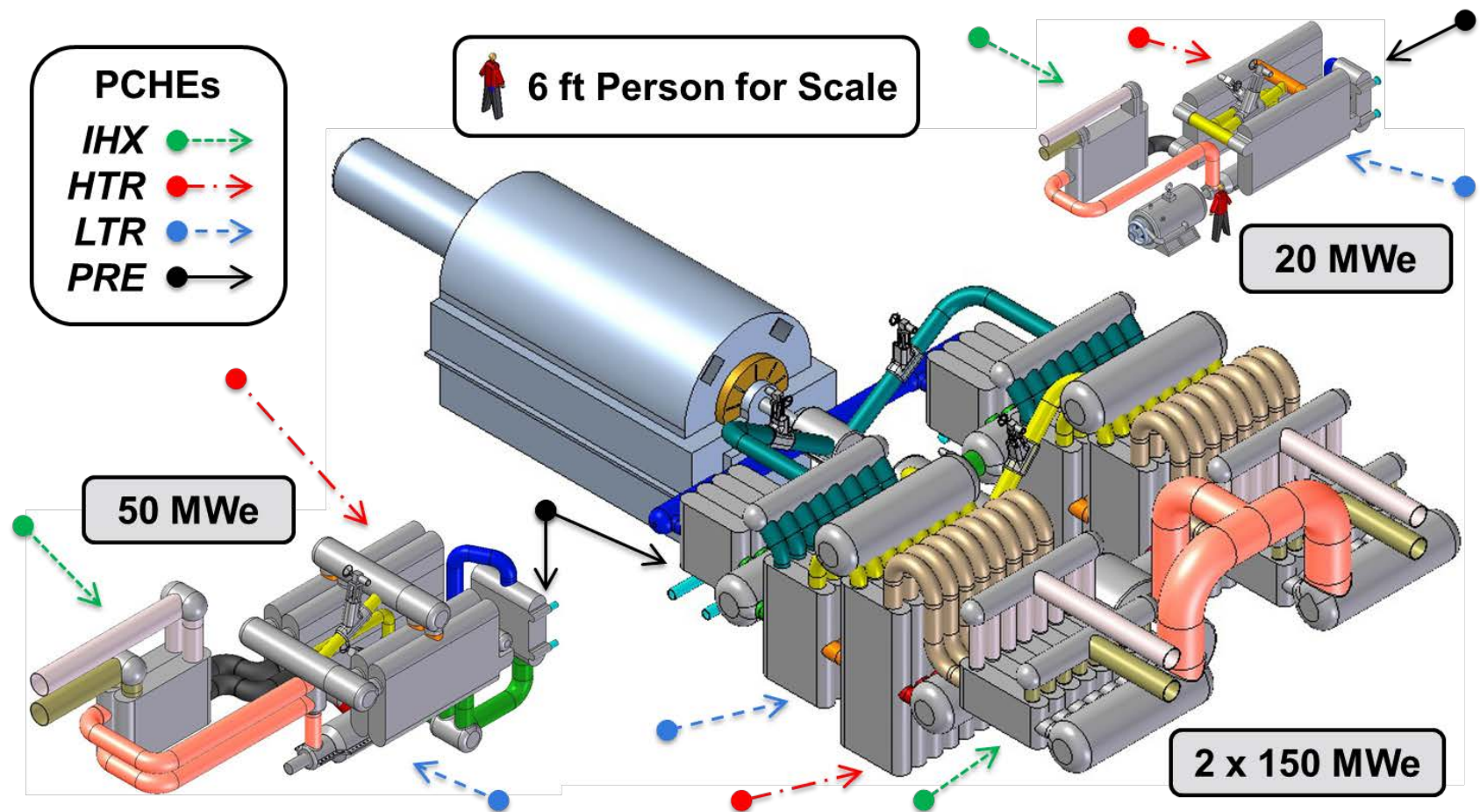
E. J. Parma, S. A. Wright, M. E. Vernon, D. D. Fleming, G. E. Rochau, A. J. Suo-Anttila, A. Al Rashdan, and P. V. Tsvetkov, "Supercritical CO₂ Direct Cycle Gas Fast Reactor (SC-GFR) Concept," Sandia National Laboratories, Albuquerque, NM, USA, SAND 2011-2525, May 2011.

sCO₂ Brayton Cycles Recuperation



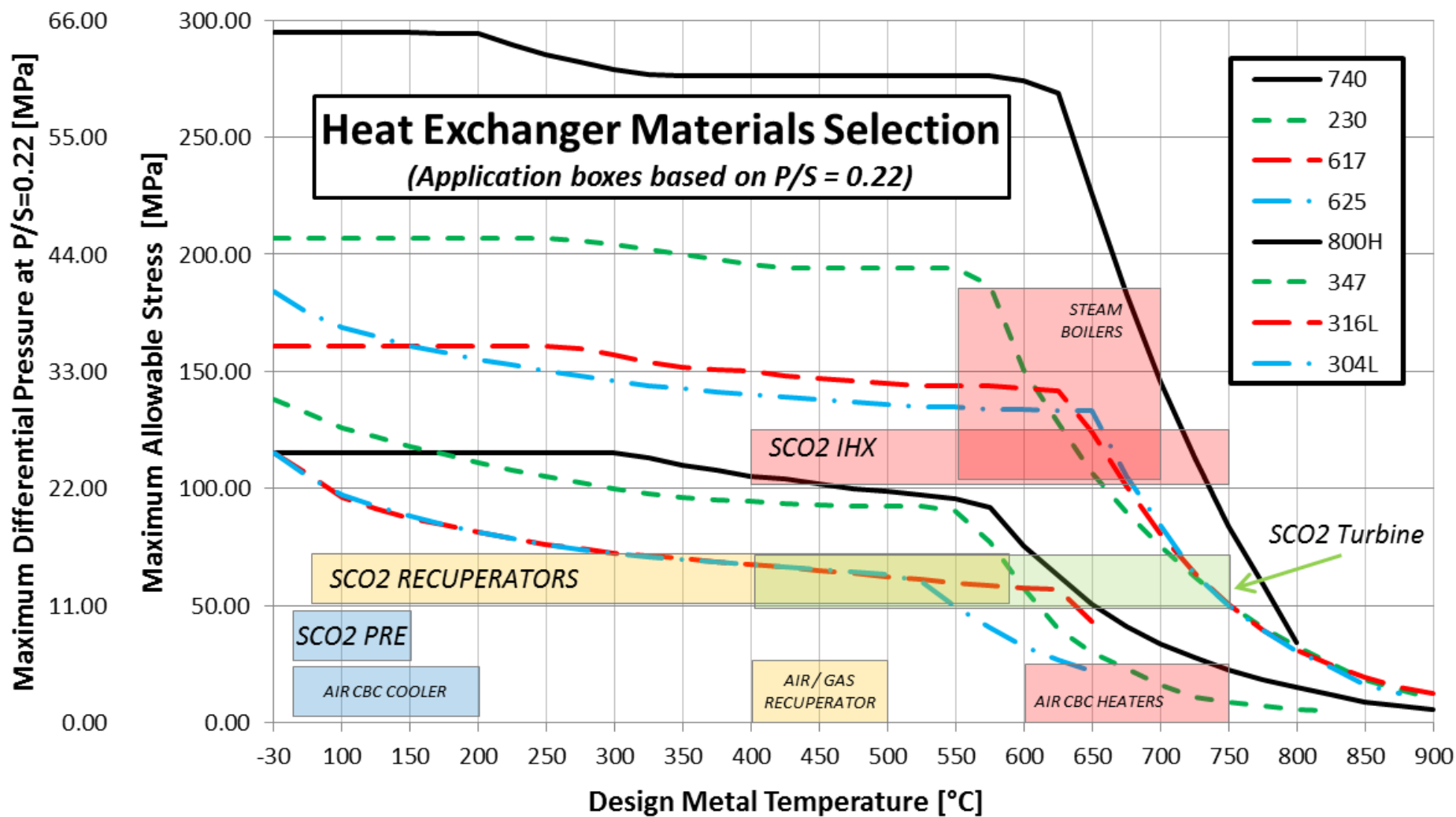
J. Dyreby, S. Klein, G. Nellis, and D. Reindl, "Design Considerations for Supercritical Carbon Dioxide Brayton Cycles With Recompression," *Journal of Engineering for Gas Turbines and Power*, vol. 136, no. 10, p. 101701, Jul. 2014.

Scalable SCO2 CBC Systems



J.P. Gibbs, P. Hejzlar, & M.J. Driscoll. (2006). *Applicability of Supercritical CO₂ Power Conversion Systems to GEN IV Reactors* (Topical Report No. MIT-GFR-037) (p. 97). Cambridge, MA: Center for Advanced Nuclear Energy Systems MIT Department of Nuclear Science and Engineering.

Heat Exchanger Requirements



Approximate Cost Scaling

$$Cost = C_{ESDU} F_{mat} F_p F_i U A_{sp} P_{elec}$$

C_{ESDU} is the UA-specific cost value [\$/((kW/K))]

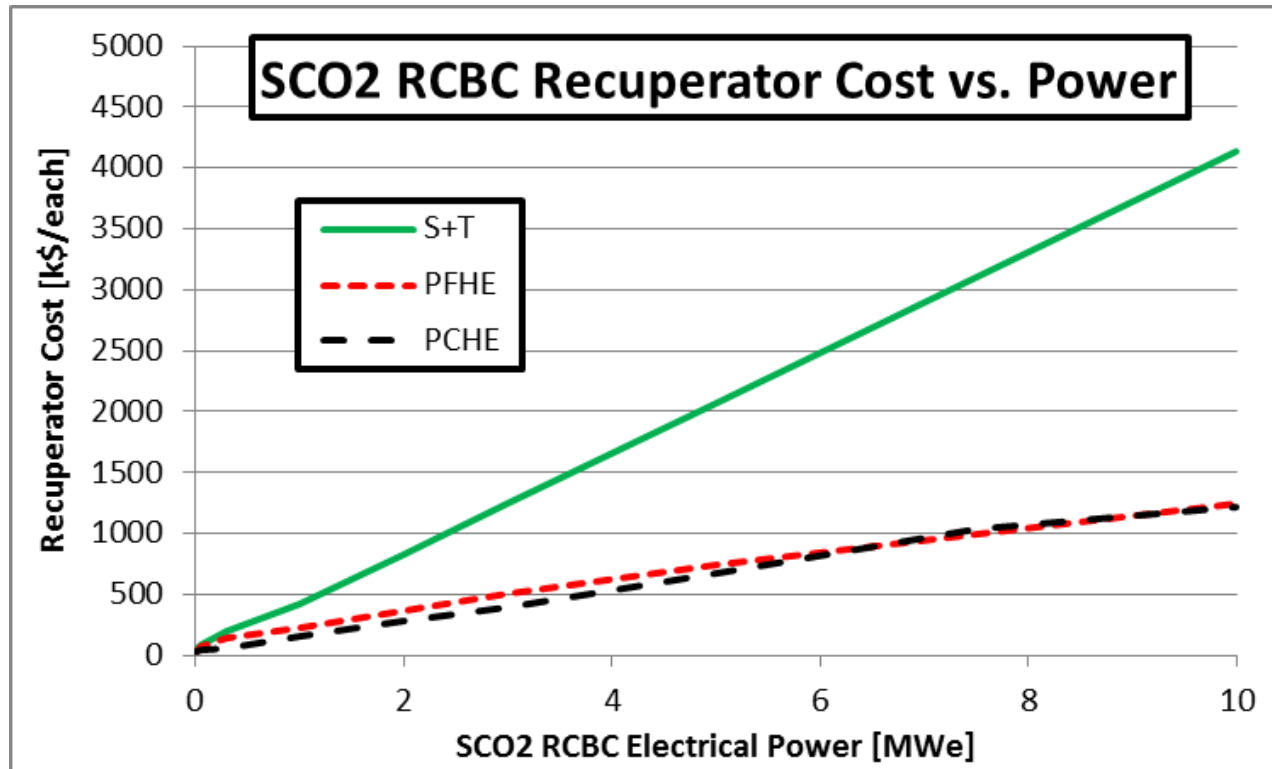
F_{mat} is a material cost factor

F_p is a pressure cost factor

F_i is an adjustment for inflation

$U A_{sp}$ is the cycle power-specific UA [kW/(K-MWe)]

P_{elec} is the cycle power level [MWe]

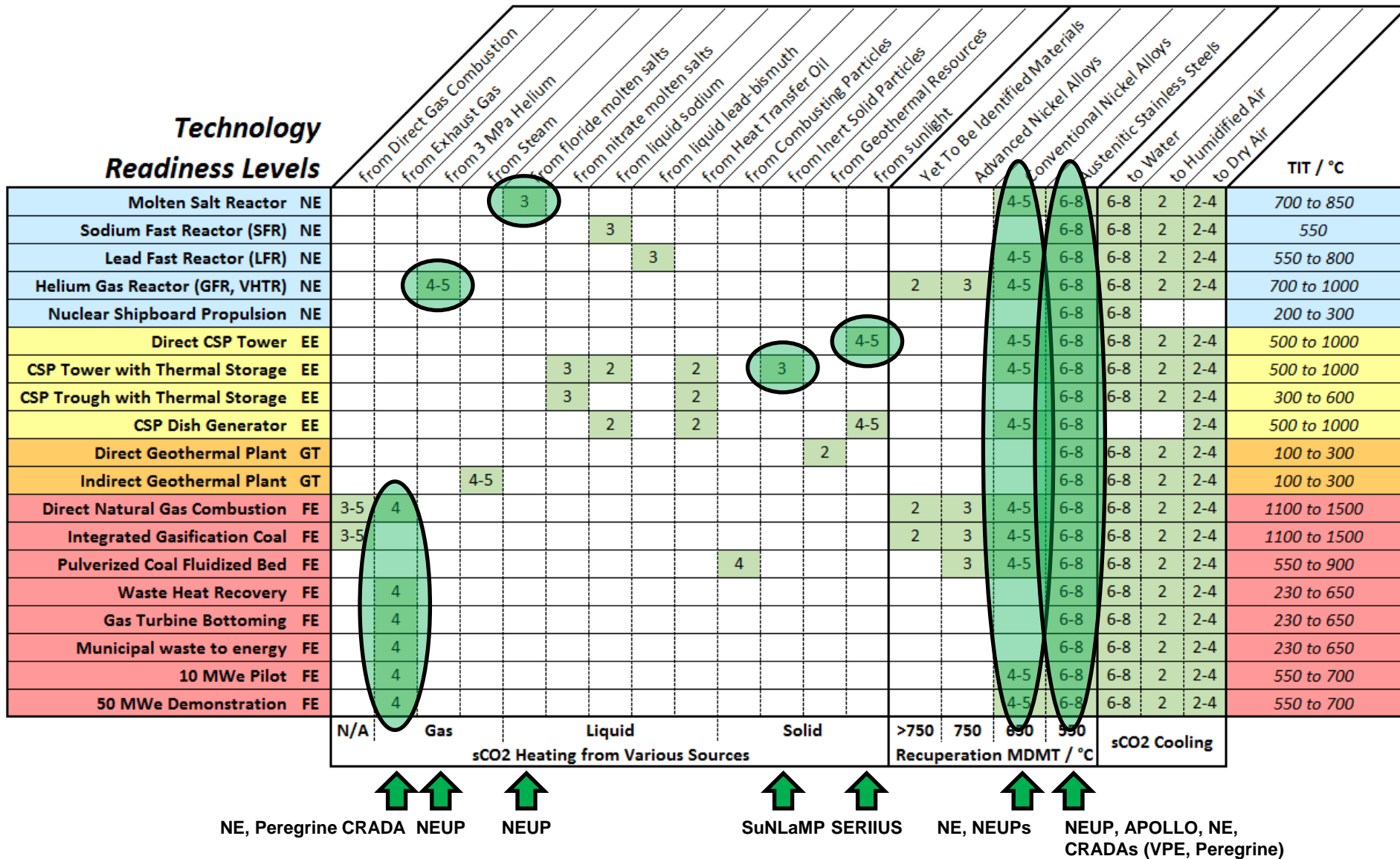


Heat Exchanger Development Gaps

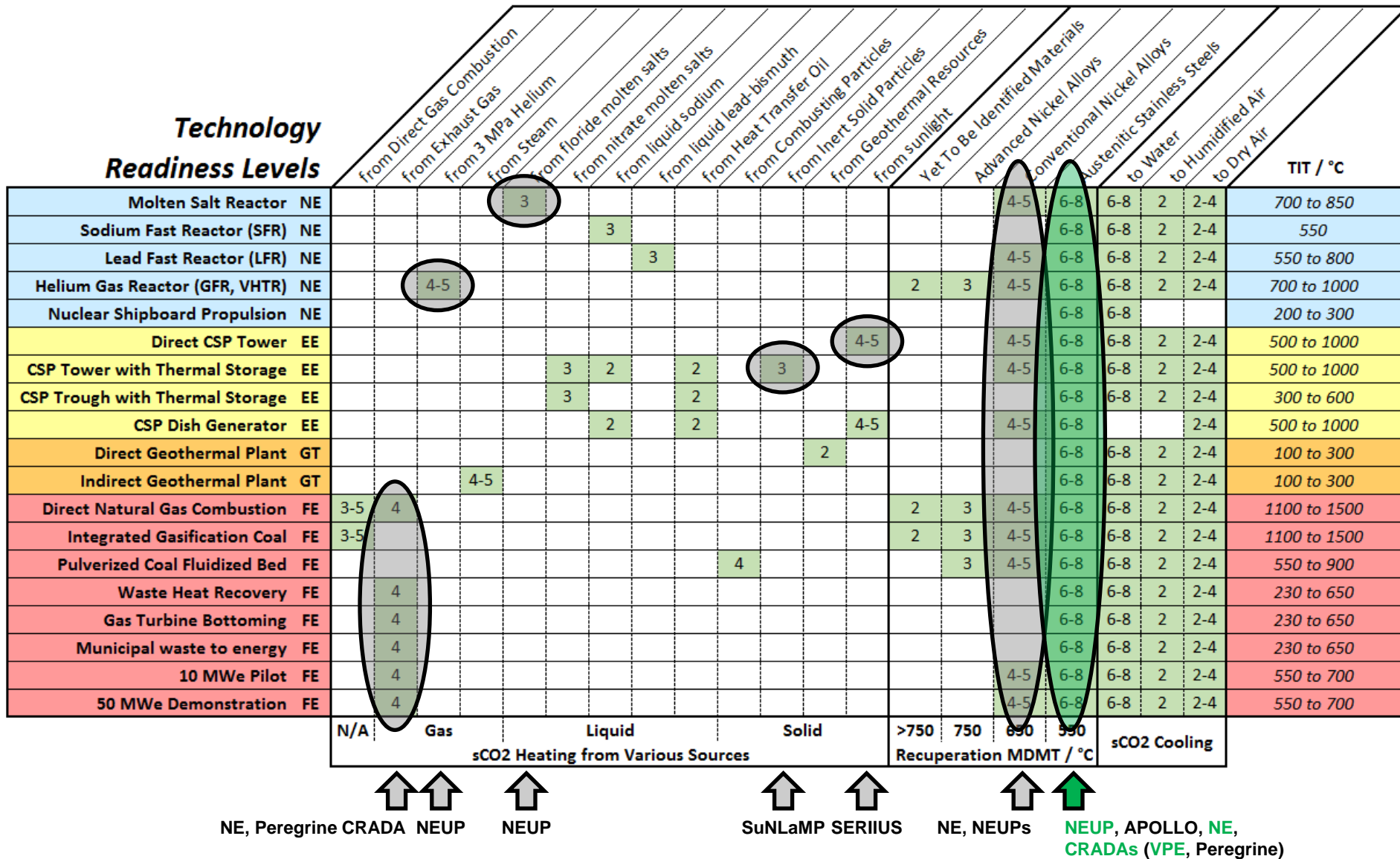
Technology Readiness Levels

Technology Readiness Levels		sCO ₂ Heating from Various Sources																TIT / °C					
		from Direct Gas Combustion	from Exhaust Gas	from 3 MPa Helium	from Steam	from fluoride molten salts	from nitrate molten salts	from liquid sodium	from Heat Transfer Oil	from Combusting Particles	from Inert Solid Particles	from Geothermal Resources	from sunlight	Yet To Be Identified	Advanced Nickel Materials	Conventional Nickel Alloys	Austenitic Stainless Steels			to Water	to Humidified Air	to Dry Air	
Molten Salt Reactor	NE					3										4-5	6-8	6-8	2	2-4	700 to 850		
Sodium Fast Reactor (SFR)	NE						3										6-8	6-8	2	2-4	550		
Lead Fast Reactor (LFR)	NE							3								4-5	6-8	6-8	2	2-4	550 to 800		
Helium Gas Reactor (GFR, VHTR)	NE			4-5									2	3		4-5	6-8	6-8	2	2-4	700 to 1000		
Nuclear Shipboard Propulsion	NE																6-8	6-8			200 to 300		
Direct CSP Tower	EE											4-5				4-5	6-8	6-8	2	2-4	500 to 1000		
CSP Tower with Thermal Storage	EE					3	2		2		3					4-5	6-8	6-8	2	2-4	500 to 1000		
CSP Trough with Thermal Storage	EE					3			2								6-8	6-8	2	2-4	300 to 600		
CSP Dish Generator	EE						2		2				4-5			4-5	6-8			2-4	500 to 1000		
Direct Geothermal Plant	GT										2						6-8	6-8	2	2-4	100 to 300		
Indirect Geothermal Plant	GT				4-5												6-8	6-8	2	2-4	100 to 300		
Direct Natural Gas Combustion	FE	3-5	4										2	3		4-5	6-8	6-8	2	2-4	1100 to 1500		
Integrated Gasification Coal	FE	3-5											2	3		4-5	6-8	6-8	2	2-4	1100 to 1500		
Pulverized Coal Fluidized Bed	FE									4				3		4-5	6-8	6-8	2	2-4	550 to 900		
Waste Heat Recovery	FE		4														6-8	6-8	2	2-4	230 to 650		
Gas Turbine Bottoming	FE		4														6-8	6-8	2	2-4	230 to 650		
Municipal waste to energy	FE		4														6-8	6-8	2	2-4	230 to 650		
10 MWe Pilot	FE		4													4-5	6-8	6-8	2	2-4	550 to 700		
50 MWe Demonstration	FE		4													4-5	6-8	6-8	2	2-4	550 to 700		
		N/A	Gas	Liquid			Solid			>750			750	650	550	sCO ₂ Cooling							
		sCO ₂ Heating from Various Sources																Recuperation MDMT / °C					

Development Gaps Addressed



Development Gaps Addressed

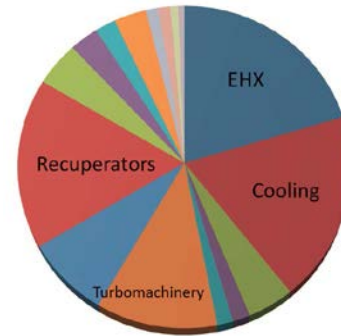


Key Development Metrics

■ Economics

- How do we optimize designs and reduce fabrication costs?
 - Efficiency vs. Effectiveness
 - Efficiency vs. pressure drop
 - Manufacturing techniques

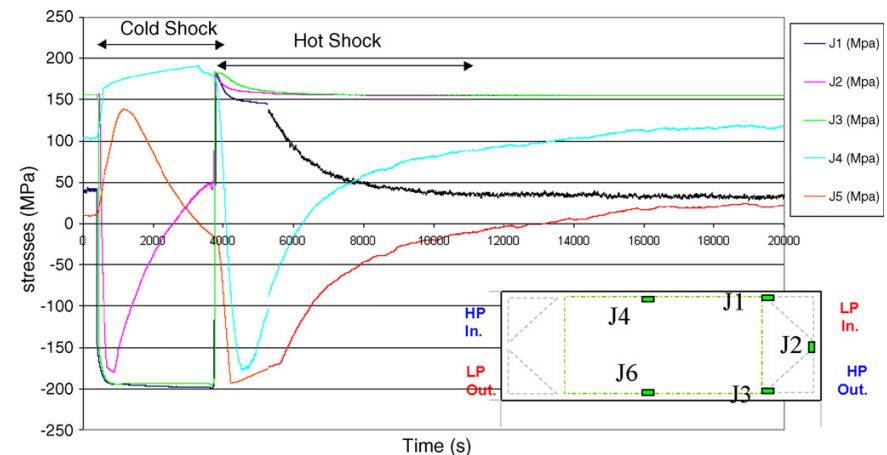
Echogen



“[A] 30% reduction in HX cost would have [a] meaningful impact on system cost.”

■ Failure Modes

- How do we accommodate thermal stress and fatigue?
 - Pressure containment (material vs. geometry)
 - Higher Temperatures
 - Corrosion and fouling



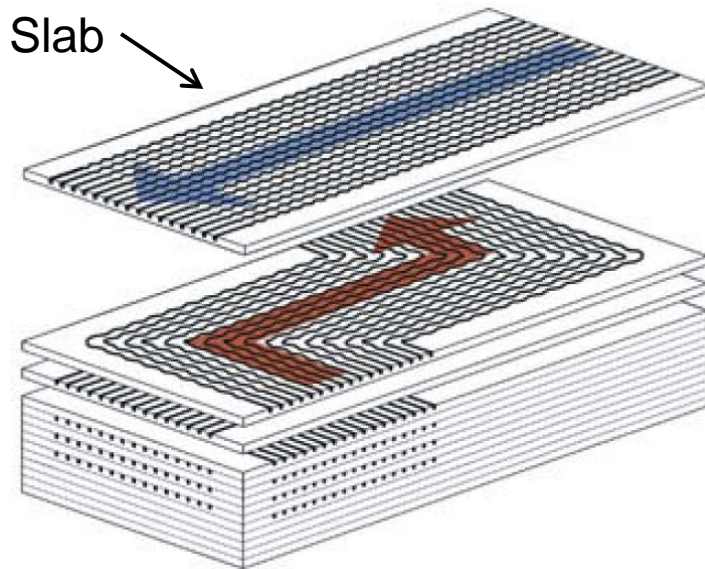
[1] T. Held, “Performance & cost targets for sCO₂ heat exchangers,” presented at the National Energy Technology Laboratory - EPRI Workshop on Heat Exchangers for Supercritical CO₂ Power Cycles, San Diego, CA, USA, 15-Oct-2015.

[2] F. Pra, P. Tochon, C. Mauget, J. Fokkens, and S. Willemsen, “Promising designs of compact heat exchangers for modular HTRs using the Brayton cycle,” *Nuclear Engineering and Design*, vol. 238, no. 11, pp. 3160–3173, Nov. 2008.

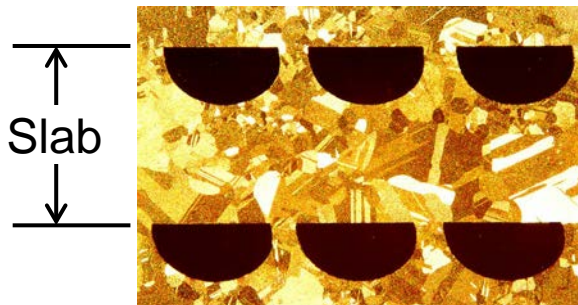
MCHE DESIGN ALGORITHM

The Printed Circuit Heat Exchanger

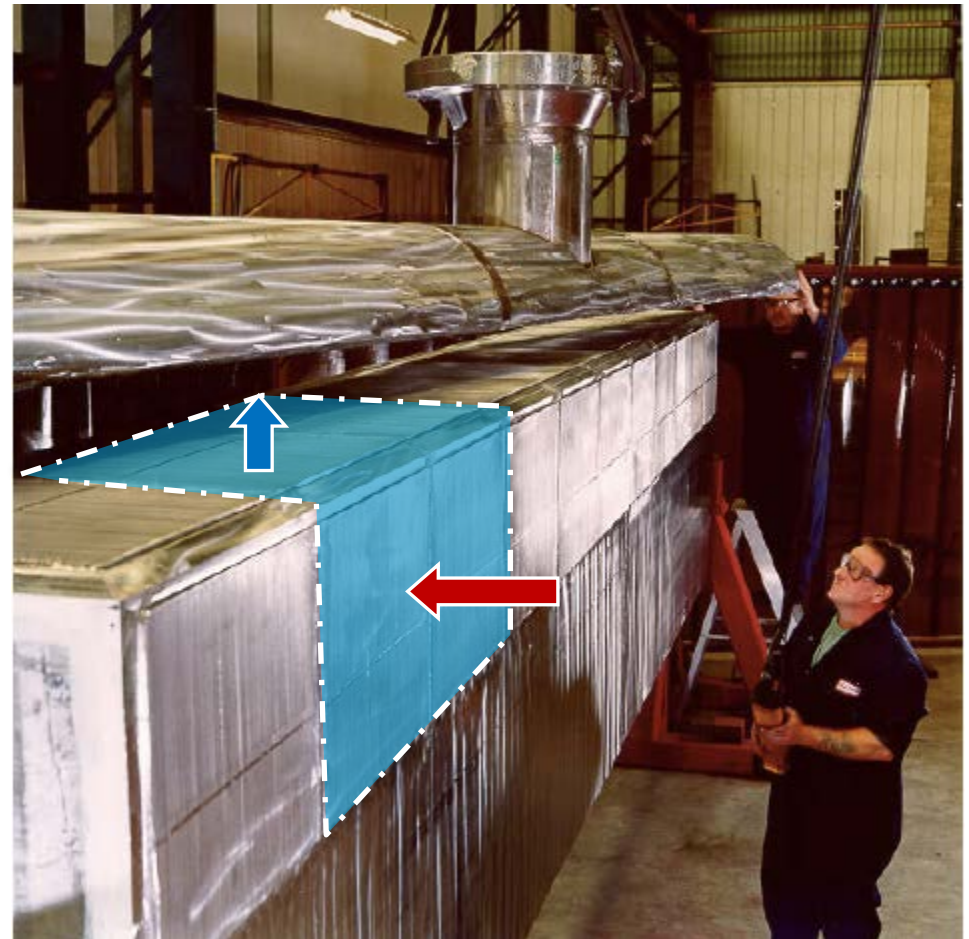
Heat Exchanger Core



Diffusion Bonding



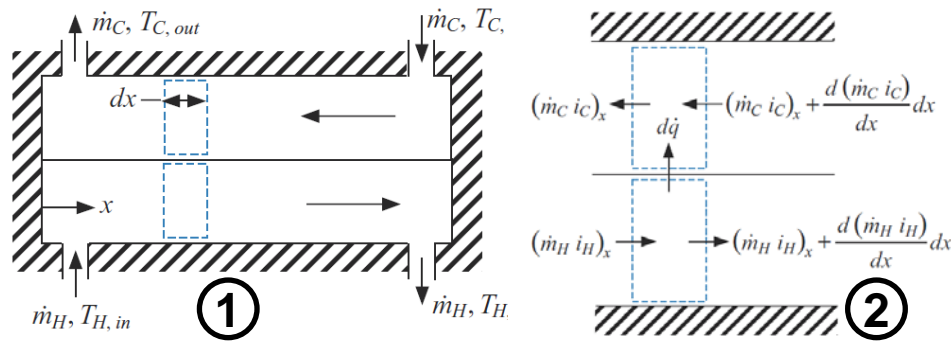
Core and Manifold Assembly



Methods of Heat Exchanger Design

- Effectiveness – NTU / LMTD Methods
 - Uses analytical solutions to various heat exchanger configurations
 - Explicit solution method with reasonable accuracy
- Compact Heat Exchanger Correlations
 - Correlations developed from experimental data for several geometries
 - Explicit accurate solution but for a limited number of correlations
- Sub-Heat Exchanger Method
 - Implements method 1 multiple times to capture property variations
 - Implicit solution needing fewer nodes / iterations than 1D solutions
- 1D Channel Solutions
 - Simulates channels identically or in parallel to determine performance
 - Iterative, intensive solution with the highest accuracy and flexibility
- More complex methods also exist (2D, 3D, CFD)

Effectiveness - NTU Derivation



$$\textcircled{3} \quad \frac{dT_H}{dx} = -\frac{UA}{L\dot{m}_H c_H} (T_H - T_C)$$

$$\textcircled{3} \quad \frac{dT_C}{dx} = \frac{UA}{L\dot{m}_C c_C} (T_H - T_C)$$

$$\textcircled{4} \quad \ln \left(\frac{T_{H,out} - T_{C,in}}{T_{H,in} - T_{C,out}} \right) = -UA \left(\frac{1}{\dot{C}_H} - \frac{1}{\dot{C}_C} \right)$$

$$\textcircled{5} \quad NTU = \begin{cases} \frac{\ln \left[\frac{1 - \varepsilon C_R}{1 - \varepsilon} \right]}{1 - C_R} & \text{for } C_R < 1 \\ \frac{\varepsilon}{1 - \varepsilon} & \text{for } C_R = 1 \end{cases}$$

1. Assume:

- Externally adiabatic
- Incompressible flow
- Constant specific heat capacity
- Enthalpy independent of pressure

2. Finite difference method

- Establish control volumes

3. Coupled differential equations

- Hot and cold-side temperatures

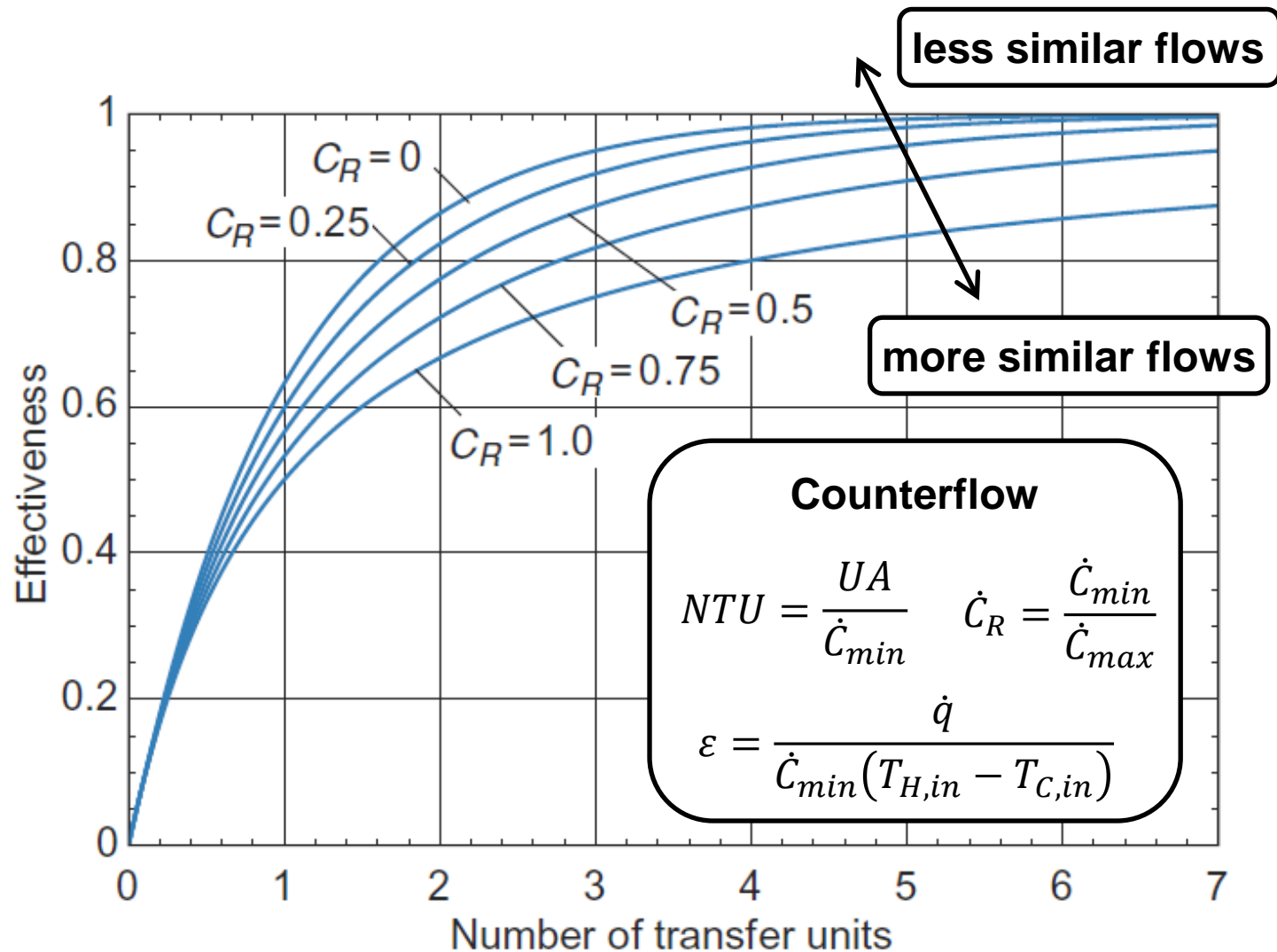
4. General solution

- Relate temperatures, UA, \dot{C} 's

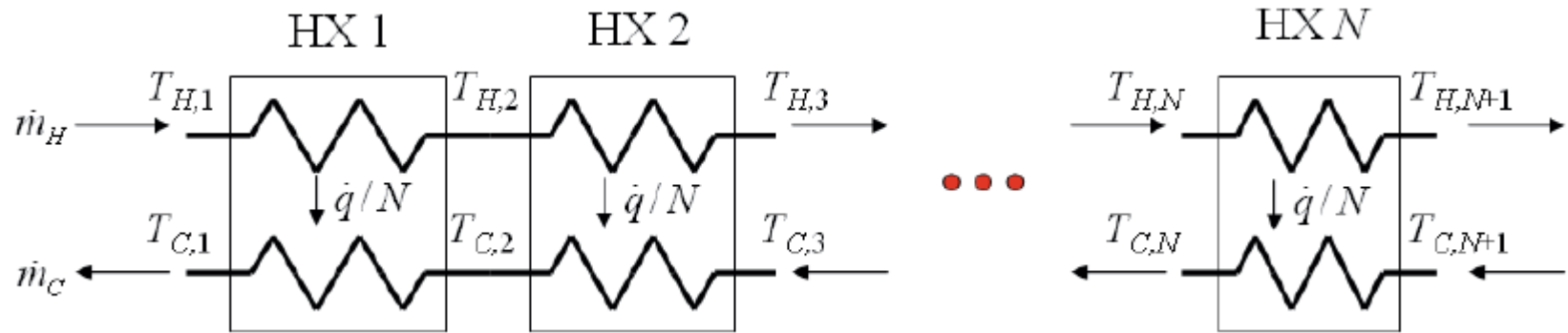
5. Effectiveness-NTU formulation

- $NTU = \frac{UA}{\dot{C}_{min}}$, and $\dot{C}_R = \frac{\dot{C}_{min}}{\dot{C}_{max}}$
- $\varepsilon = q / [\dot{C}_{min}(T_{H,in} - T_{C,in})]$

Effectiveness - NTU Solution



Sub-Heat Exchanger Method



$$\dot{C}_i = \dot{m} \frac{h_i - h_{i+1}}{\text{MAX}(1\text{e-}4 [\text{K}], |T_i - T_{i+1}| \text{SIGN}(h_i - h_{i+1}))}$$

$$\varepsilon_i = \frac{\dot{q}_i}{\text{MIN}(\dot{C}_{A,i}, \dot{C}_{B,i})(T_{A,i} - T_{B,i+1})}$$

$$NTU_i = \begin{cases} \frac{\ln \left[\frac{(1 - \varepsilon C_R)}{1 - \varepsilon} \right]}{1 - C_R} & \text{for } C_R < 1 \\ \frac{\varepsilon}{1 - \varepsilon} & \text{for } C_R = 1 \end{cases}$$

$$UA_i = NTU_i \text{MIN}(\dot{C}_{A,i}, \dot{C}_{B,i})$$

- Divide into a series of HXers
- Extends e-NTU method
- Assumptions apply to each sub-heat exchanger (Δx)
- Best method to obtain UA accurately and quickly with variable property flows

ASME BPVC Design Equations

$$S_{m,stay} = \frac{Ph}{2t_4} \left[\frac{6 + K(11 - \alpha^2)}{3 + 5K} \right]$$

$$S_{m,1} = \frac{Ph}{2t_1} \left[3 - \frac{6 + K(11 - \alpha^2)}{3 + 5K} \right]$$

$$S_{m,2} = \frac{PH}{2t_2}$$

$$S_{b,stay} = 0$$

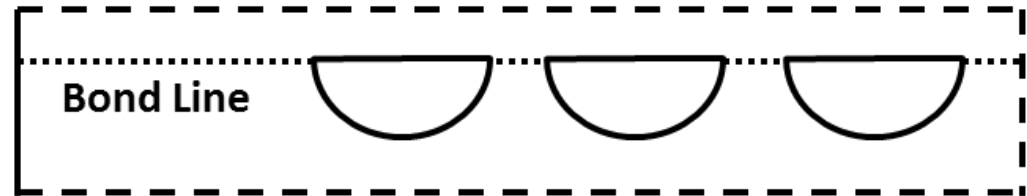
$$(S_{b,1})_{at N} = \frac{Pc_1}{24I_1} \left[-3H^2 + 2h^2 \left(\frac{3 + 5\alpha^2 K}{3 + 5K} \right) \right]$$

$$(S_{b,1})_{at Q} = \frac{Ph^2 c_1}{12I_1} \left(\frac{3 + 5\alpha^2 K}{3 + 5K} \right)$$

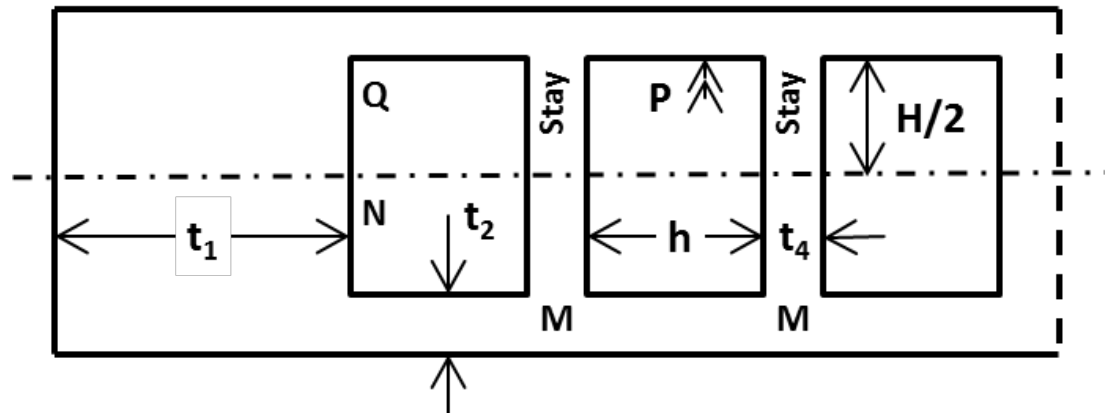
$$(S_{b,2})_{at M} = \frac{Ph^2 c_2}{12I_2} \left[\frac{3 + K(6 - \alpha^2)}{3 + 5K} \right]$$

$$(S_{b,2})_{at Q} = \frac{Ph^2 c_2}{12I_2} \left(\frac{3 + 5\alpha^2 K}{3 + 5K} \right)$$

Section of a printed circuit heat exchanger



Vessel sketch from the ASME BPVC VIII-1-13-2(a)(8)



Non-Dimensionalized Equations

$$\frac{P}{SE} \leq \left(\frac{1}{wf} - 1 \right)$$

$$\frac{P}{S} \leq 2 \left(\frac{1}{df} - 1 \right)$$

$$\frac{P}{S} \leq 3 \left(\frac{df}{1-df} + \frac{1}{AR^2} \left(\frac{df}{1-df} \right)^2 \right)^{-1}$$

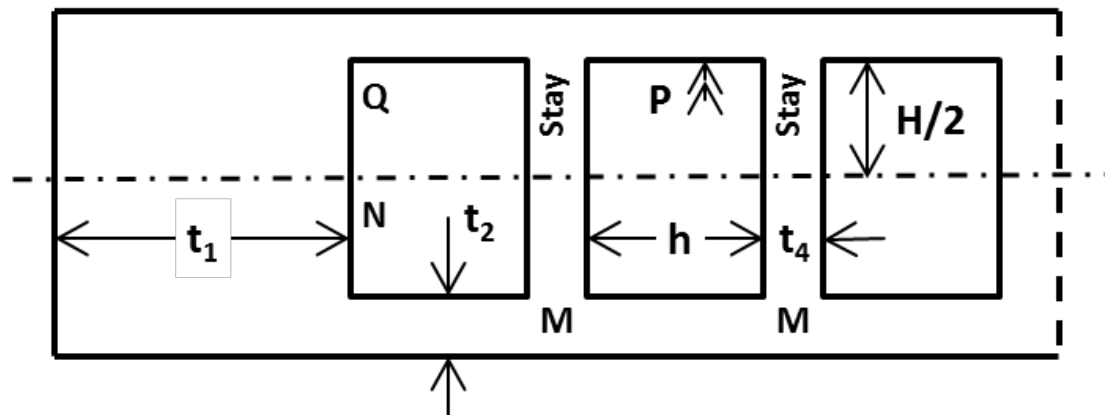
$$wf = \frac{h}{h + t_4}$$

$$df = \frac{H}{H + t_2}$$

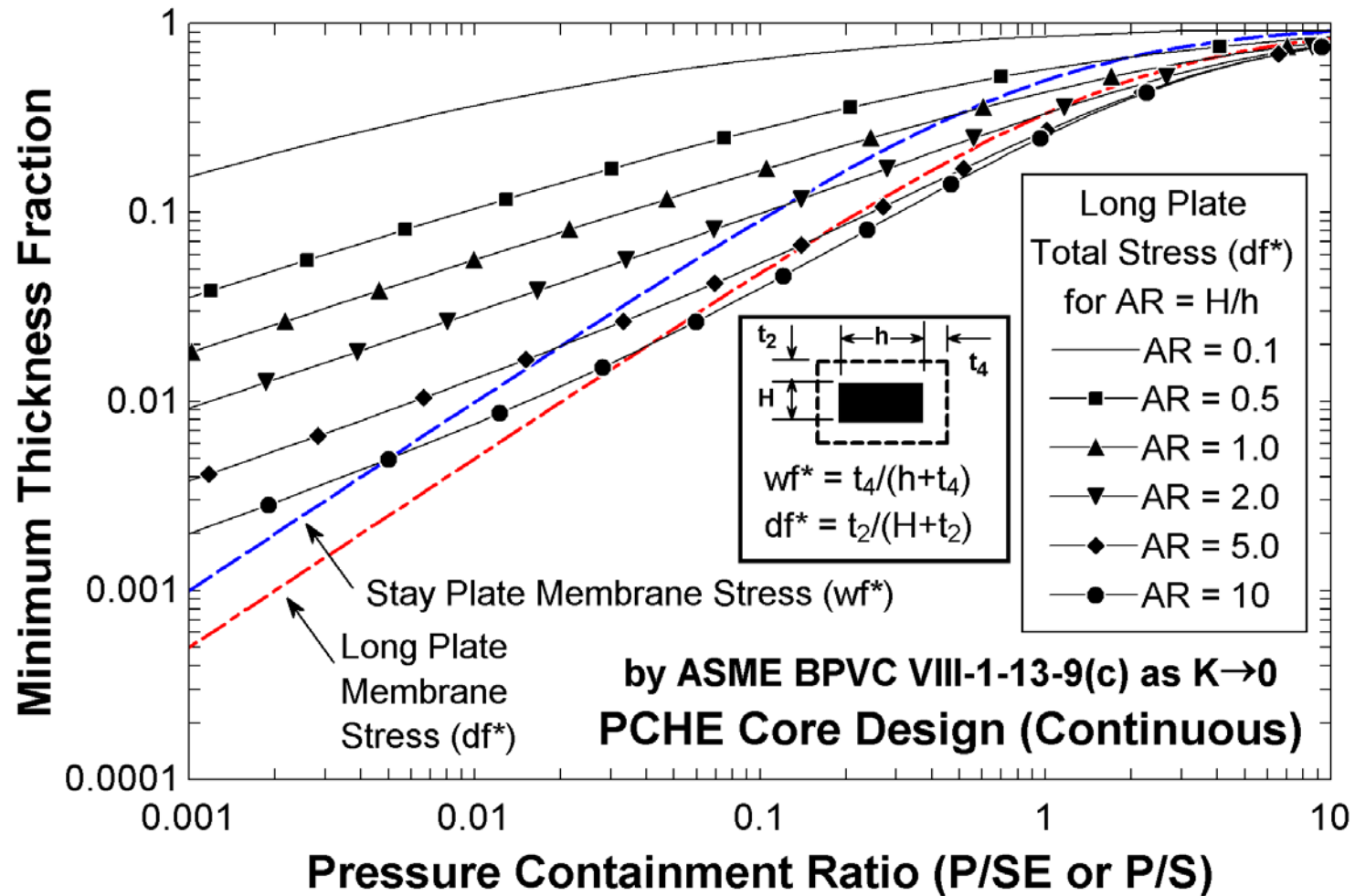
Section of a printed circuit heat exchanger



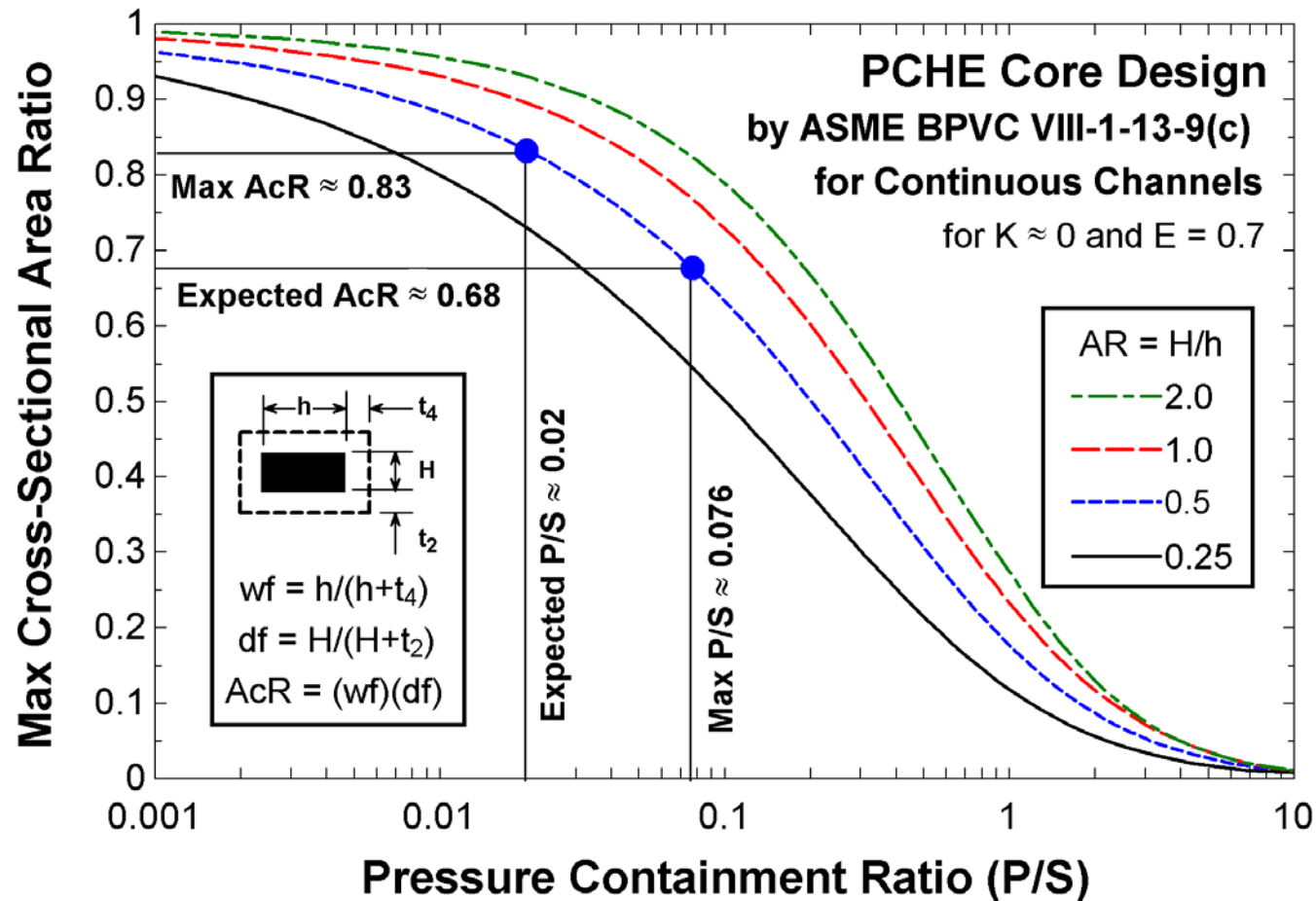
Vessel sketch from the ASME BPVC VIII-1-13-2(a)(8)



PCHE Core Pressure Containment

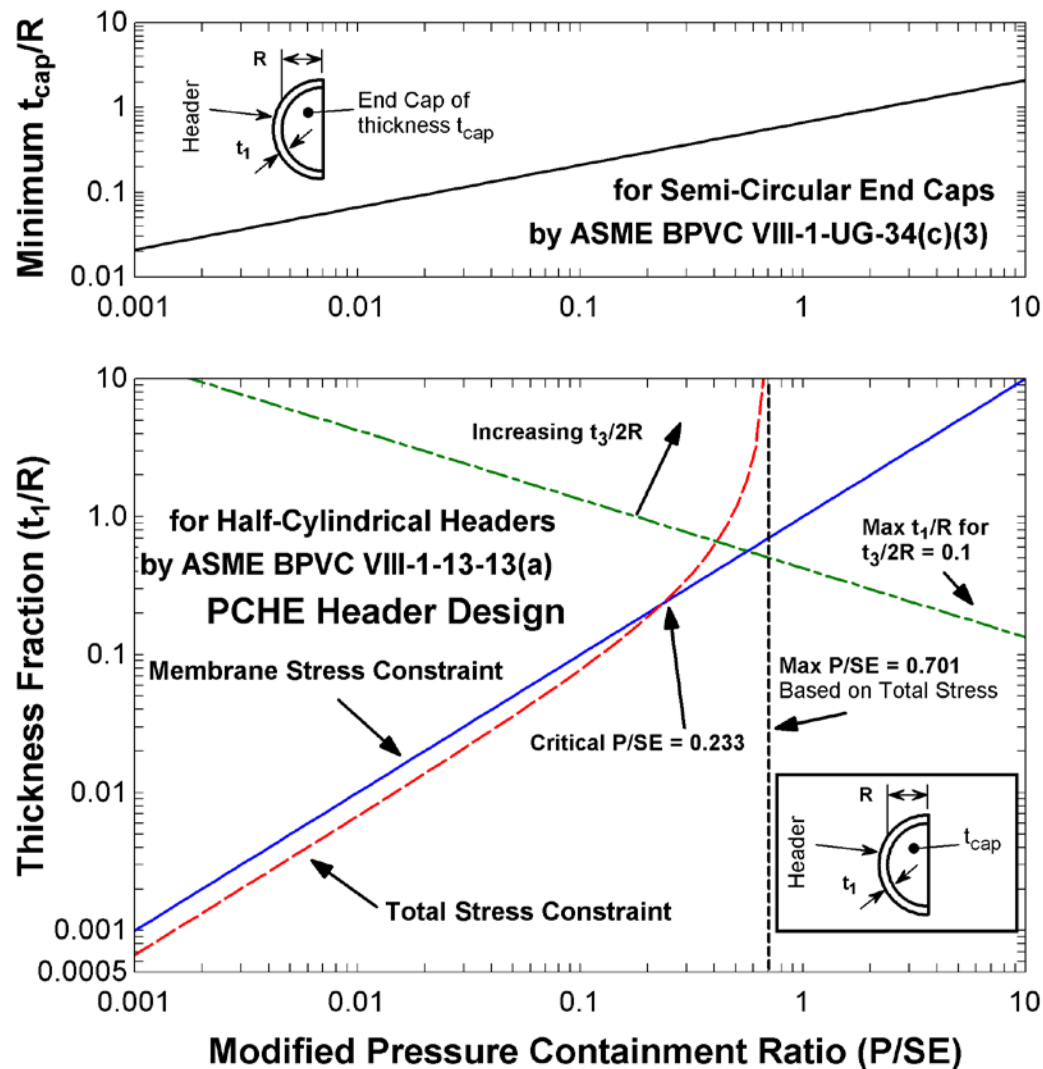


PCHE Core Pressure Containment



Carlson, M. (2012). *Measurement and Analysis of the Thermal and Hydraulic Performance of Several Printed Circuit Heat Exchanger Channel Geometries* (Master of Science). University of Wisconsin - Madison, Madison, WI.

Half-Cylindrical Headers



Thermal-Hydraulics

$$\Delta x_i = UA_i \left(\underbrace{\frac{1}{h_{A,i} N_{ch,A} p_{ch,A}}}_{(1)} + \underbrace{\frac{R_{f,A,i}}{N_{ch,A} p_{ch,A}}}_{(2)} + \underbrace{\frac{t_m}{k_{m,i} W}}_{(3)} + \underbrace{\frac{1}{h_{B,i} N_{ch,B} p_{ch,B}}}_{(4)} + \underbrace{\frac{R_{f,B,i}}{N_{ch,B} p_{ch,B}}}_{(5)} \right)$$

1. Sub-heat exchanger length
2. Sub-heat exchanger conductance-area product
3. Convective thermal resistances
4. Conductive thermal resistance
5. Fouling thermal resistances

PCHE Design Software

- Sub-hxer model
- ASME BPVC
- Single, two-phase, supercritical flows
- Over 400 fluids

Document Number: RC1		Revision Number: 1		Heat Exchanger Data Sheet	
Side A (straight)			Side B (Z-side)		
Step 1. Side A and B Stream Compositions (by mass %)					
Choose the fluid set: Refprop Fluid(s)			Refprop Fluid(s)		
First 8 fluid components:					
100 (%) WATER.FLD			100 (%) R1233ZD.FLD		
0 (%) ACETONE.FLD			0 (%) 1BUTENE.FLD		
0 (%) Nitrogen.fld			0 (%) 1BUTENE.FLD		
0 (%) co2.fld			0 (%) 1BUTENE.FLD		
0 (%) Propane.FLD			0 (%) 1BUTENE.FLD		
0 (%) BUTANE.FLD			0 (%) 1BUTENE.FLD		
0 (%) IPENTANE.FLD			0 (%) 1BUTENE.FLD		
0 (%) HEXANE.FLD			0 (%) 1BUTENE.FLD		
Fouling (val A, val B)			CO2 vapor		
Fouling Factor: $R_{f,A} = 0.0001 \text{ [m}^2\text{]}$			Fouling Factor: $R_{f,B} = 0.0001 \text{ [m}^2\text{]}$		
Step 2. Specify Fluid Flow Rates					
Flow Rate (mass A, mass B)					
$\dot{m}_A = 80.4 \text{ [kg/s]}$			$\dot{m}_B = 34.9 \text{ [kg/s]}$		
$\dot{V}_A = \text{'''''' [m}^3\text{/s]}$			$\dot{V}_B = \text{'''''' [m}^3\text{/s]}$		
Step 3. Specify Inlet State for Sides A and B					
Inlet States (T_A, P_A, T_B, P_B)					
Inlet Pressure			$P_A = 7.170E+06 \text{ [Pa]}$		
Inlet Temperature			$T_{A,in} = 572.8 \text{ [K]}$		
Inlet Quality ($\pm 100 = \text{sup or sub}$)			$Q_{A,in} = \text{''''}$		
Outlet Pressure			$P_{B,out} = 2.330E+07 \text{ [Pa]}$		
Outlet Temperature			$T_{B,in} = 378.1 \text{ [K]}$		
Outlet Quality ($\pm 100 = \text{sup or sub}$)			$Q_{B,in} = \text{''''}$		
			$P_{A,out} = \text{'''''''' [Pa]}$		
			$T_{A,out} = \text{'''' [K]}$		
			$T_{B,out} = 564.2 \text{ [K]}$		
			$Q_{A,out} = \text{''''}$		
			$Q_{B,out} = \text{''''}$		
Step 4. Specify the Allowable Pressure Drop					
Pressure Drop			$dP_{sum,A} = \text{'''''' [Pa]}$		
Drop / Operating Pressure			$dP_{B,\%} = \text{'''''' [%]}$		
			$dP_{sum,B} = \text{'''''' [Pa]}$		
			$dP_{B,\%} = \text{'''''' [%]}$		
Step 5. Specify Header Orientations					
Header Axis Orientation			Vertical		
Step 7. Specify Core Channel Geometry					
Channel Width			$w_A = 0.001289 \text{ [m]}$		
Channel Depth			$w_B = 0.001289 \text{ [m]}$		
			$d_A = 0.000763 \text{ [m]}$		
			$d_B = 0.000763 \text{ [m]}$		
solutionScope= All design steps (mech, thermo, TH)					
<div>Calculate</div> <div>Save Inputs</div> <div>Load Inputs</div>					
Summary of PCHE Design					
Job Number RC1					
Run Date					
Job Title Test					
Code Used ASME Code Section VIII Division 1 - 2013					
Core Length (bet. headers) $L = \text{'''''' [m]}$					
Core Width (bet. headers) $W = \text{'''''' [m]}$					
Core Height $H = \text{'''''' [m]}$					
Core Cross-Section (H x W) $A_c = \text{'''''' [m}^2\text{]}$					
Side A Surface Area $As_A = \text{'''''' [m}^2\text{]}$					
Side B Surface Area $As_B = \text{'''''' [m}^2\text{]}$					
Wetted Volume (core + hders) $Vol_{wet} = \text{'''''' [m}^3\text{]}$					
Metal Mass (core + hders) $M = \text{'''' [kg]}$					
Heat Transfer Rate (Duty) $\dot{Q} = \text{'''''' [W]}$					
Conductance-Area Product $UA_{sum} = \text{'''''' [W/K]}$					
Side A MAWP $MAWP_A = \text{'''''' [Pa]}$					
Side B MAWP $MAWP_B = \text{'''''' [Pa]}$					
MAWT (same as MDMT) $MAWT = \text{'''' [K]}$					
Number of Etched Plate Pairs $N_{rows} = \text{'''' [-]}$					
Side A Channels per Plate $N_{chp,A} = \text{'' [-]}$					
Side B Channels per Plate $N_{chp,B} = \text{'' [-]}$					
Number of Un-etched Plates $N_{ex} = \text{'' [-]}$					
Step 9. Other Controls					
Max Active core volume width $W_{ACV,max} = 0.1597 \text{ [m]}$					
Max Active core volume height $H_{ACV,max} = 2.5 \text{ [m]}$					
Extra width provided $W_{extra} = 0 \text{ [m]}$					
Extra height provided $H_{extra} = 0 \text{ [m]}$					
Step 6. Specify the Performance Measure					
Choose Measure Type Side B Outlet Temperature					
Diffusion Bonding Joint Efficiency $E_{DB} = 0.7 [-]$					
Header Cylinder Joint Efficiency $E_{cyl} = 0.7 [-]$					

PROTOTYPE PCHE DESIGN

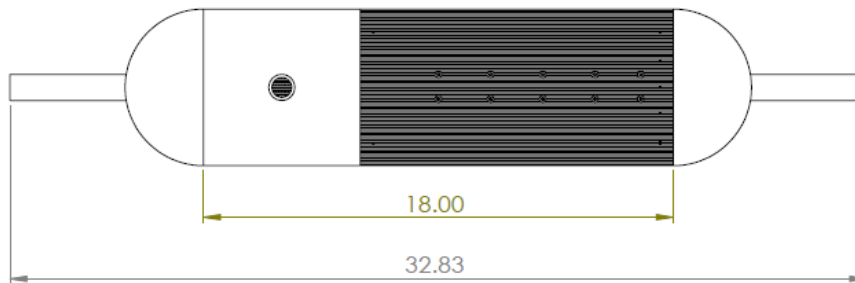
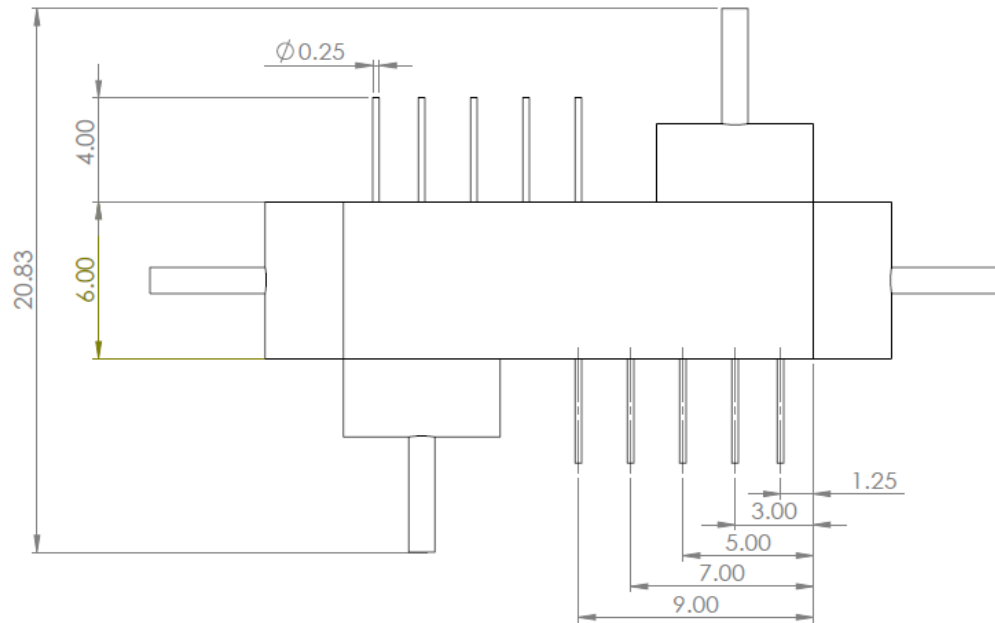
Heat Exchanger Data Sheet

Parameter	Unit	Side A (Straight)	Side B (Z)
<i>Fluid</i>	-	water	water
<i>Mass Flow Rate</i>	kg/s (lbm/hr)	1.5 (12000)	1.5 (12000)
<i>Volumetric Flow Rate</i>	m ³ /s (gpm)	1.5e-3 (24)	1.5e-3 (24)
<i>Inlet Temperature</i>	°C (°F)	82 (180)	37 (98)
<i>Inlet Pressure</i>	kPa (psi)	300 (44)	300 (44)
<i>Pressure Drop</i>	kPa (psi)	55 (7.9)	62 (9.0)
<i>Fouling Factor</i>	m ² -K/W	8e-5	8e-5
<i>MAWP</i>	MPa (psi)	20 (2900)	
<i>MAWT</i>	°C (°F)	550 (1000)	
<i>Duty</i>	kW _{th} (Btu/hr)	103 (350000)	
<i>Height x Width x Length</i>	m (in)	0.15 x 0.15 x 0.46 (6 x 6 x 18)	
<i>Active Surface Area</i>	m ² (in ²)	1.2 (13)	
<i>Material</i>	-	316L Stainless Steel	

Design for Multiple Phases

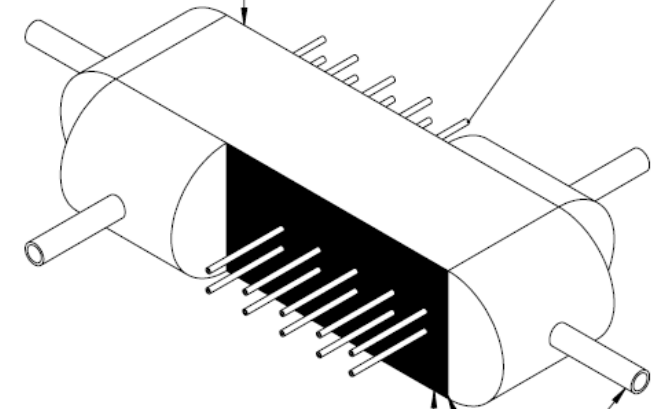
1. Pressure Containment
 - Evaluated by hydrostatic pressure testing
2. Single-phase Thermal Hydraulics
 - Evaluated in the NESL water test loop
3. Supercritical Thermal Hydraulics
 - Evaluated in the NESL sCO₂ loop
4. Fatigue Lifetime (to failure)
 - Tested by thermal cycling under pressure

Instrumentation



4.000 Long 0.25 ϕ 0.065 Thickness Swagelok 316L Tube (sim.)

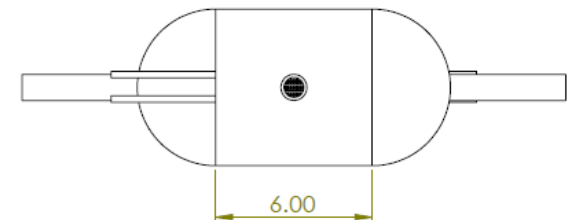
5 Pairs of holes w/o tubes



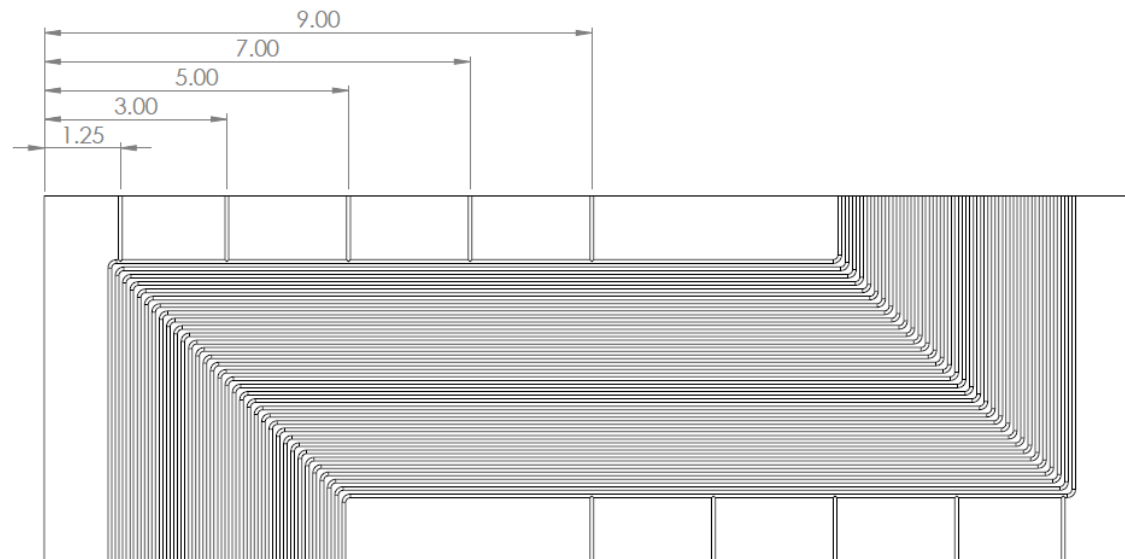
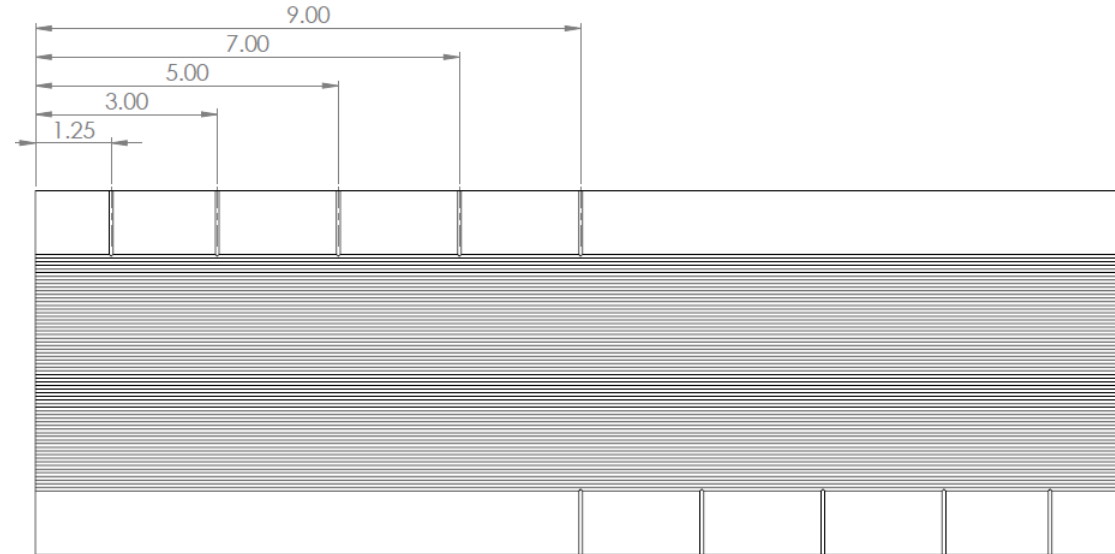
5 Pairs of holes w/o tubes

Support from base when handling and mounting.

1.000 ϕ 0.120 Thickness Swagelok 316L Tube (sim.)



Instrumentation – Tap Locations

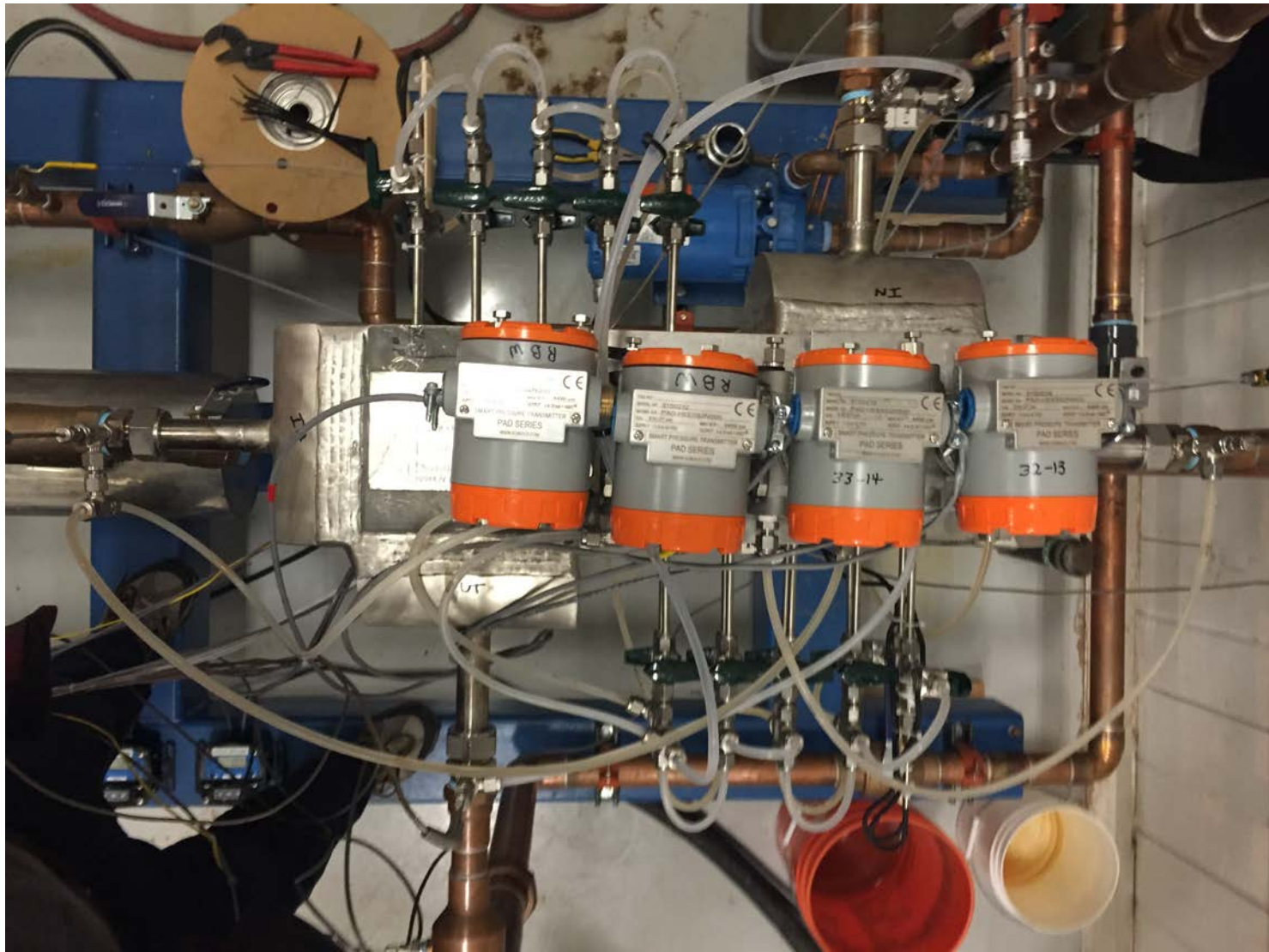


HEAT EXCHANGER TEST PLATFORM

Test Platform Configuration

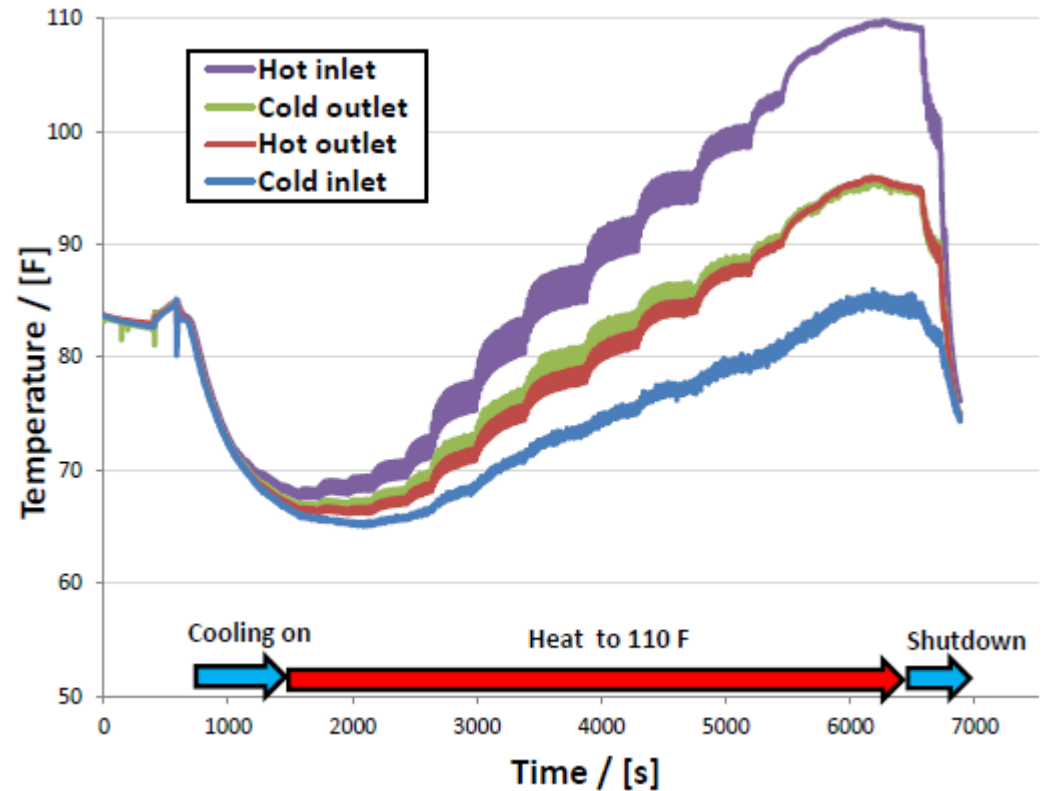


PCHE Instrumentation



PCHE PERFORMANCE COMPARISON

Performance Testing



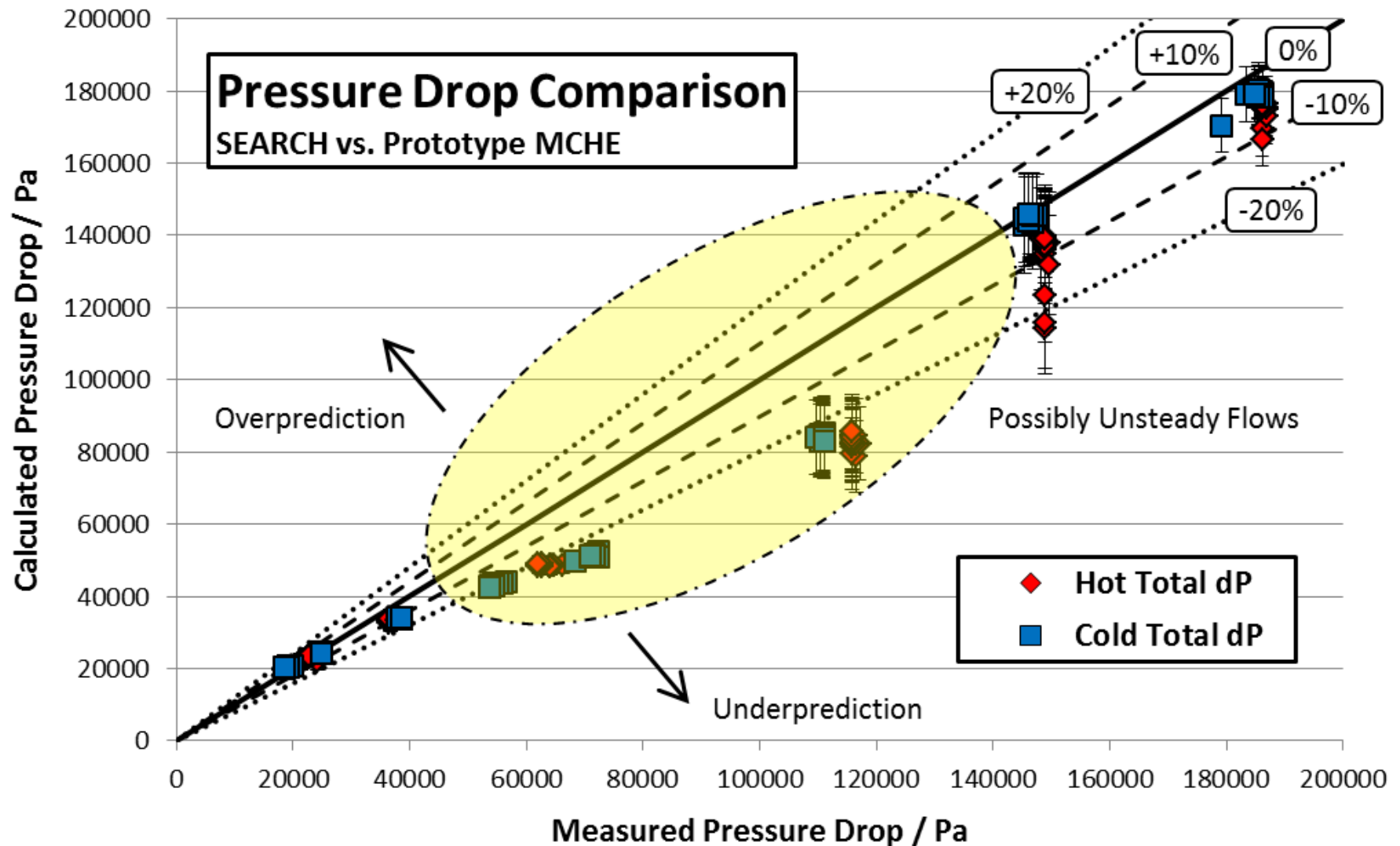
SEARCH appears conservative by at least 10% on q , UA , effectiveness

Performance Comparison

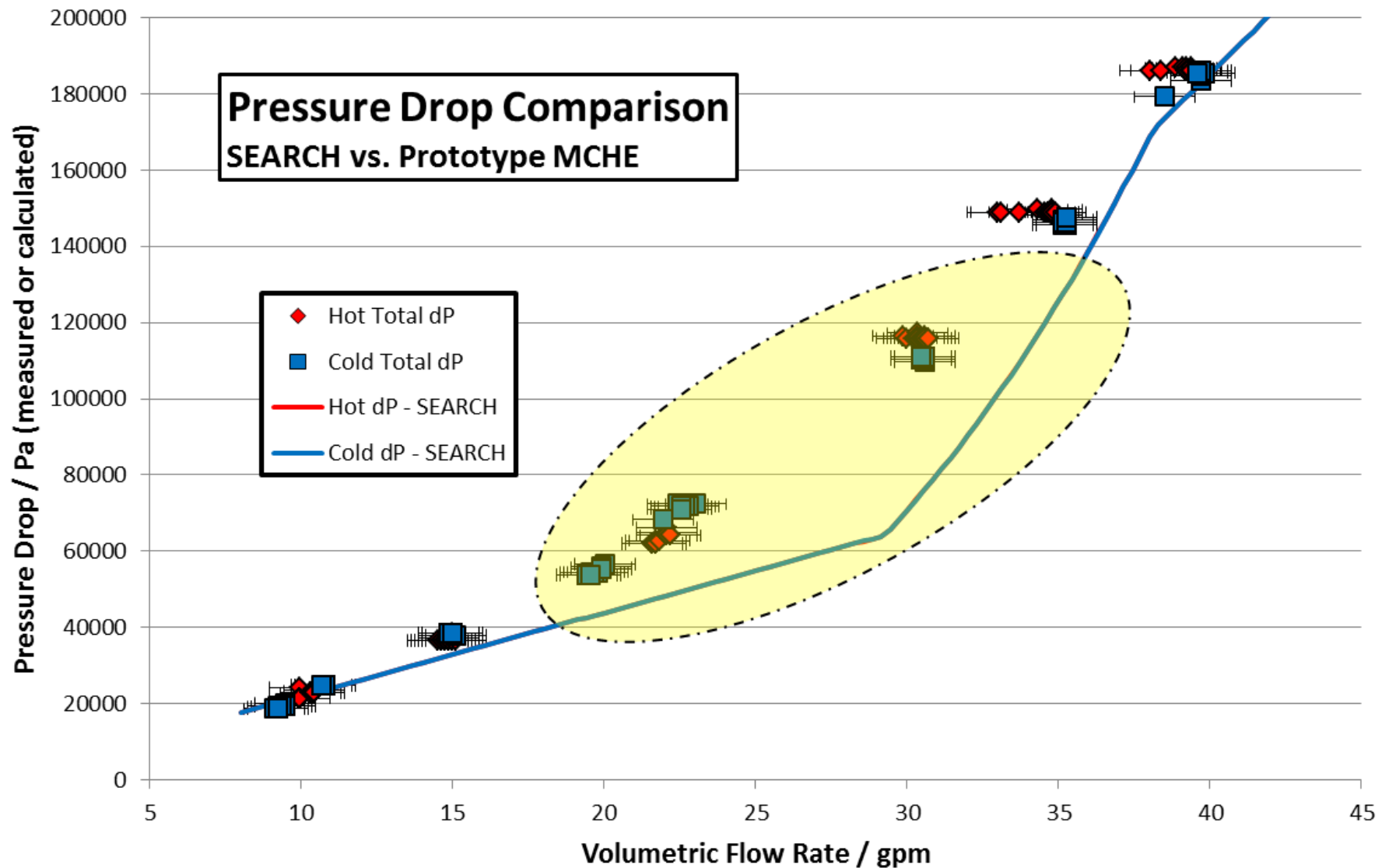
Time Range	Description
0-750	Baseline, prepare to start test. Hot flow started first, wait to reach steady state.
750-1500	Start cooling flow; keep at maximum rate until loop below 70°F.
1500-6500	Increased heater power gradually (5-10% increments) to 100% = 110°F.
6500-7000	Shut off heater power, cooling remains on.

Time / s	\dot{q} / W		$UA / (W/K)$		ε	
	SEARCH	Measured	SEARCH	Measured	SEARCH	Measured
4200	44000	+7%	8100	+13%	43%	+6%
4700	44000	+12%	8200	+23%	43%	+11%
5100	54000	+13%	8400	+26%	43%	+12%
5400	61000	+14%	8500	+28%	44%	+13%
5700	67000	+14%	8600	+27%	44%	+13%
6260	67000	+16%	8700	+32%	44%	+15%

Calculated vs. Meas. Pressure Drop



Pressure Drop Prediction Capability



Conclusions

- Based on our first set of tests:
 - SEARCH is within 25% accuracy on key metrics
 - Thermal performance is predicted conservatively
 - Pressure drop is under-predicted in some regimes
- These results have already been applied
- Testing is planned after loop upgrades
 - Additional thermal-hydraulic observations
 - Intermediate state (T & P) profiles
 - Future test phases (sCO₂, fatigue)

BACKUP SLIDES

The Argument for SCO₂ Brayton

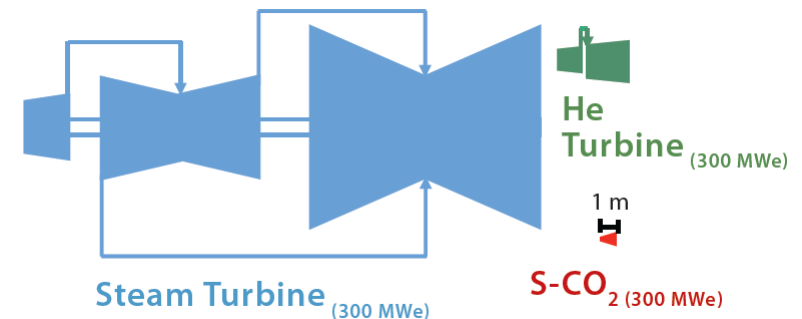
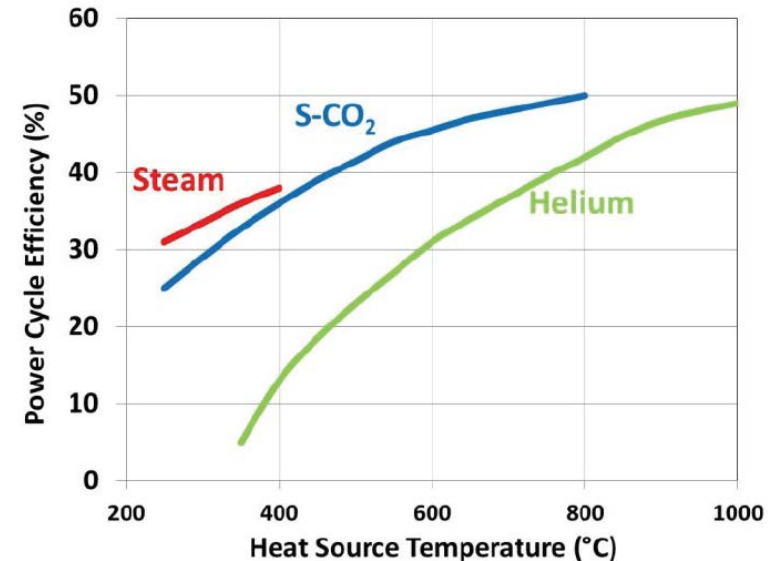
Versus Helium and Steam

1. Higher efficiency

- Sodium Fast Reactor operating at 550 °C
- Concentrated Solar Power up to 700 °C
- CCS Gasified Coal and Natural Gas up to 1150 °C

2. Compact turbomachinery

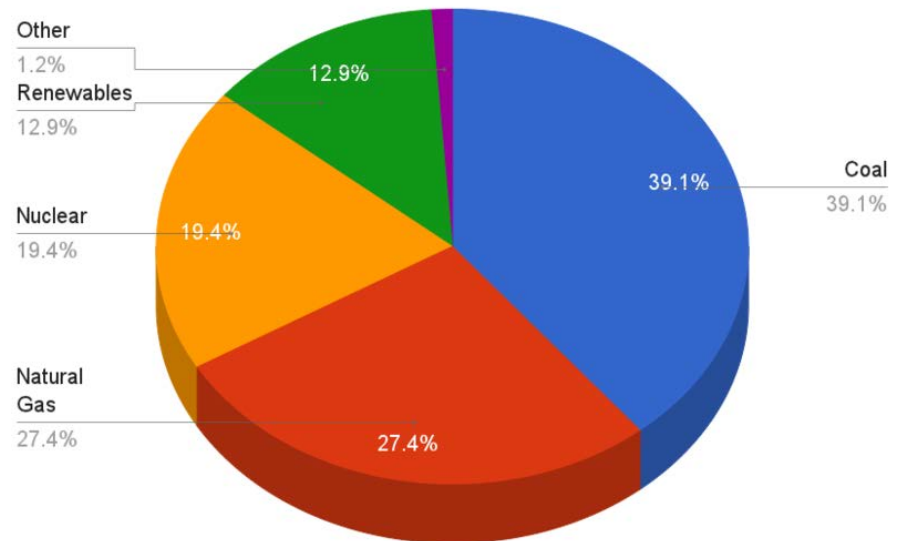
- Smaller system footprint
- Possibly reduced cost



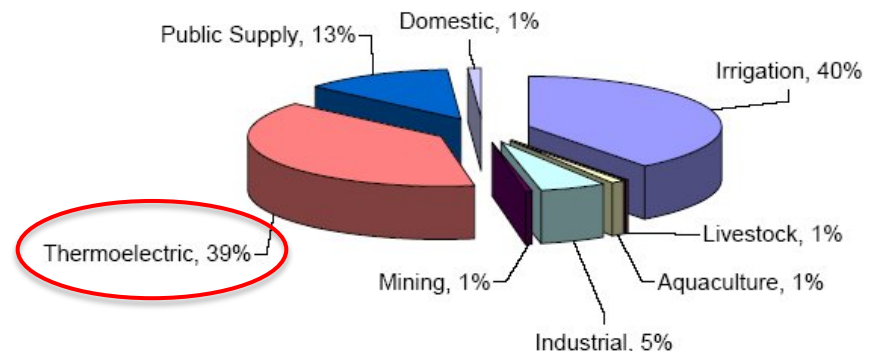
Current Electrical Generation

- Electrical Generation
 - Dominated by fossil
 - Nuclear is a critical part
 - Expected that natural gas and nuclear will grow; coal will shrink
- Two main technologies
 - Steam Rankine cycle
 - Coal, Nuclear, CCNG
 - Gas Brayton cycle
 - Natural gas

U.S. 2013 Electricity Generation By Type



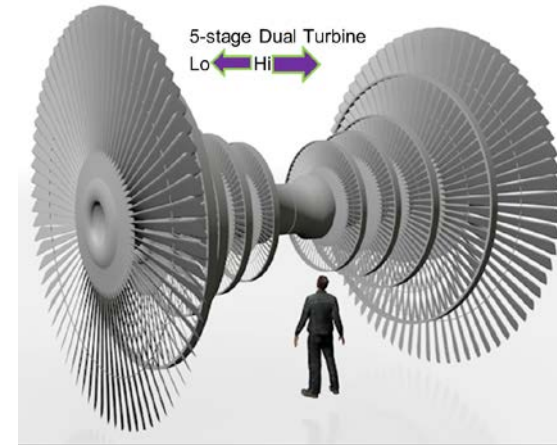
U.S. 2000 Water Withdrawals by Market



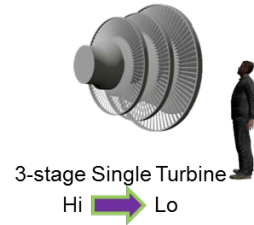
Supercritical CO₂ (sCO₂) Brayton Cycle

■ Key Advantages over Steam

- Smaller turbomachinery
- Single-phase fluid (no quality issues)
- Recuperation becomes practical



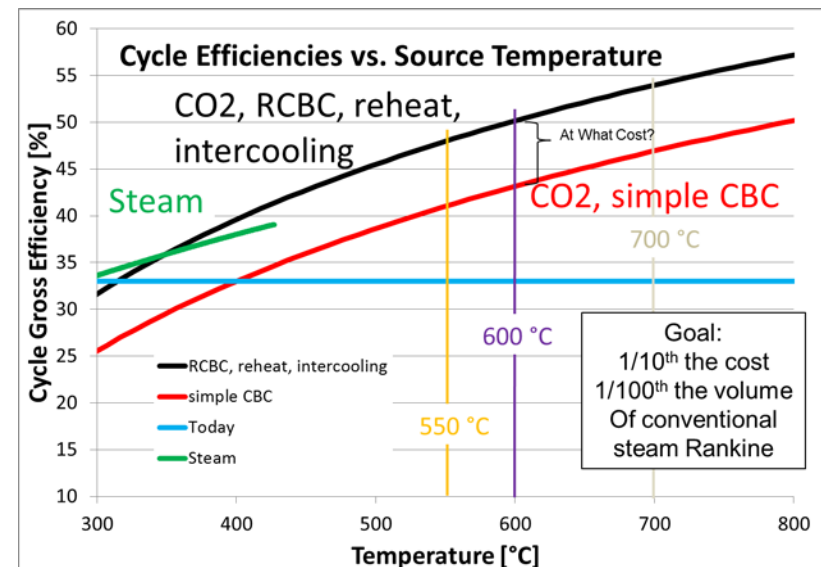
20 meter Steam Turbine (300 MWe)
(Rankine Cycle)



1 meter sCO₂ (300 MWe)
(Brayton Cycle)

■ Key Advantages over Gas

- High efficiency at low temperatures
- Lower compression work
- Smaller turbomachinery



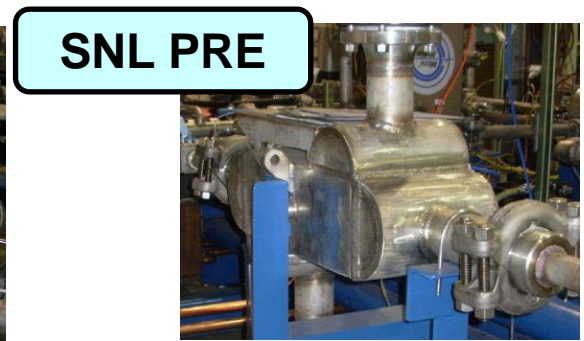
Current SCO₂ CBC HXers



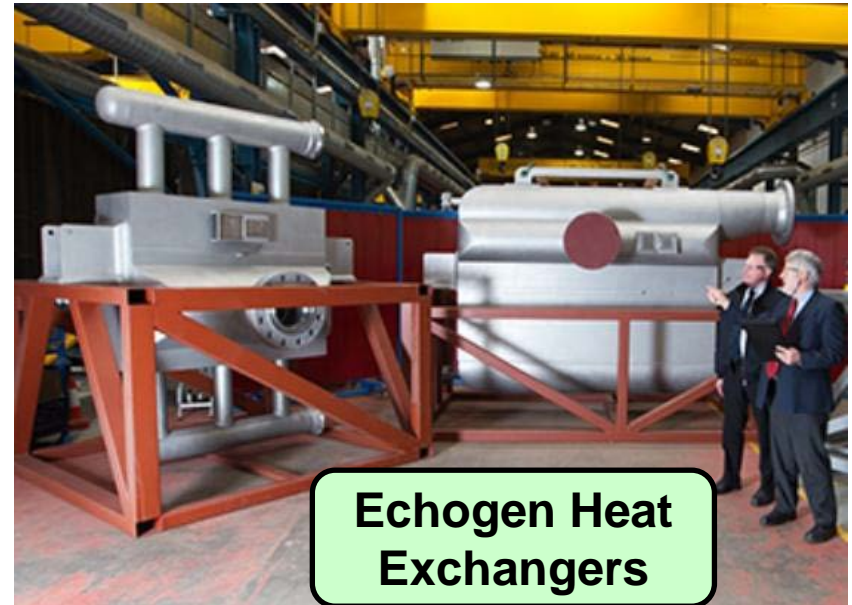
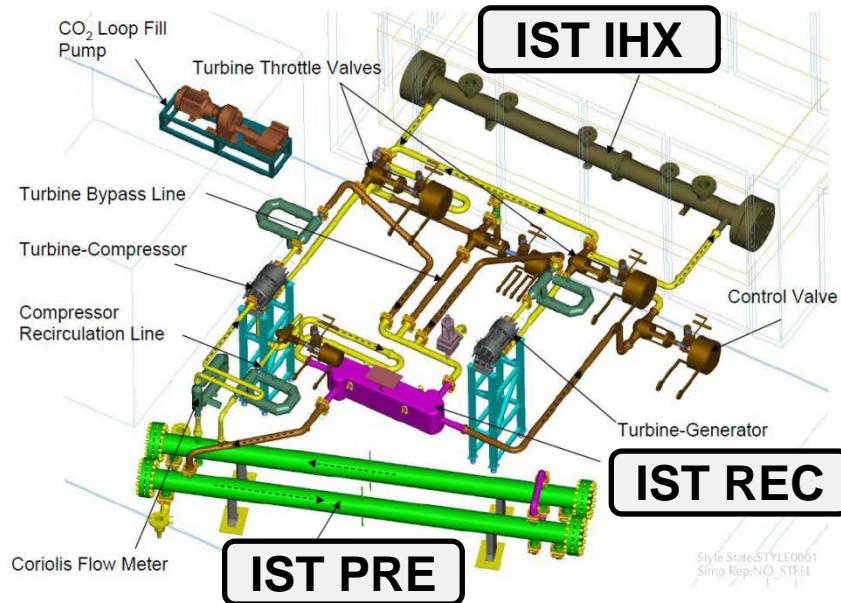
SNL HTR



SNL LTR



SNL PRE



**Echogen Heat
Exchangers**

G. O. Musgrove, C. Pittaway, D. Shiferaw, and S. Sullivan, "Tutorial: Heat Exchangers for Supercritical CO₂ Power Cycle Applications," San Antonio, Texas, USA, 03-Jun-2013.

Commercial Unit Potential

Key Requirements:

- ✓ High Pressure
- ✓ High Temperature
- ✓ Corrosion Resistant
- ✓ High Reliability
- ✓ Compact Geometry
- ✓ Scalable to 150 MWe

$$\beta = \frac{A_s}{V} = \frac{4\phi}{d_h}$$



Coil-Wound
10 to 300 [m²/m³]



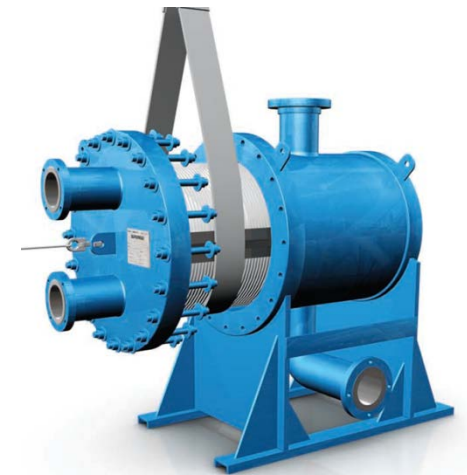
Shell and Tube
10 to 200 [m²/m³]



Plate-Fin
200 to 800 [m²/m³]

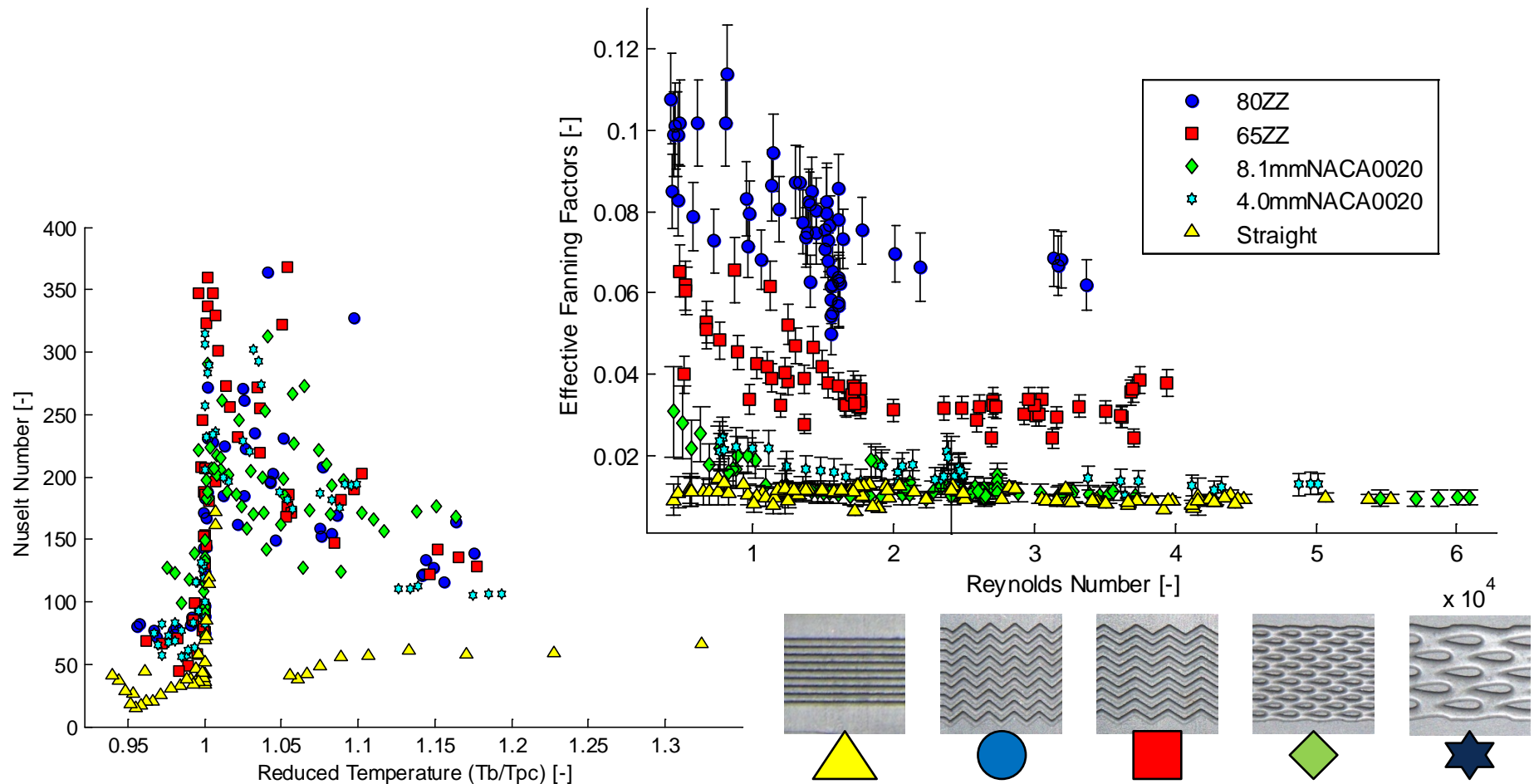


Printed Circuit
200 to 5000 [m²/m³]



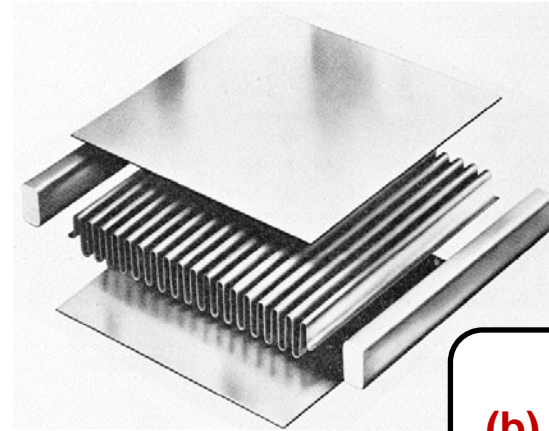
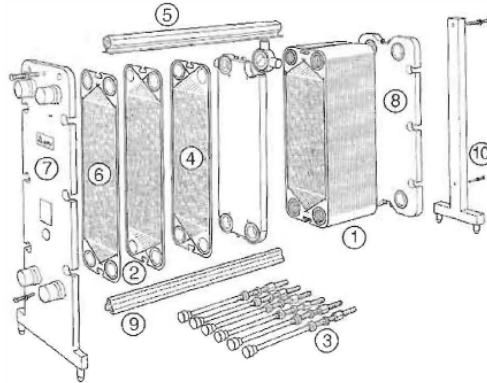
Shell and Plate
100 to 600 [m²/m³]

PCHE Thermal-Hydraulic Performance



Carlson, M. (2012). *Measurement and Analysis of the Thermal and Hydraulic Performance of Several Printed Circuit Heat Exchanger Channel Geometries* (Master of Science). University of Wisconsin - Madison, Madison, WI.

PHE
120 to 660

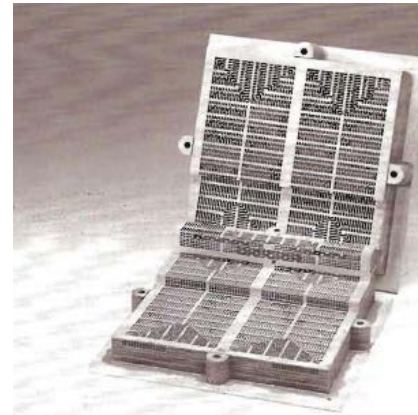


PFHE
(b) 800 to 1500
(d) 700 to 800

PCHE
(d) 200 to 5000



CBHE
(Marbond)
Up to 10000



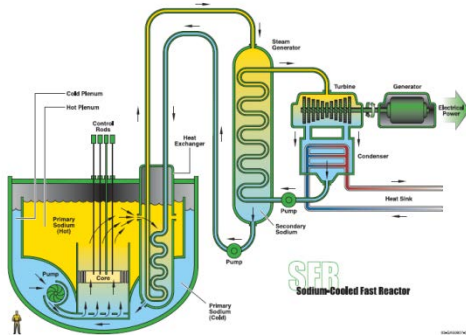
HEAT EXCHANGER COMPACTNESS

Surface Area Density: $\beta = \frac{A_s}{V} = \frac{4\phi}{d_h}$

Potential Applications



Coal / Nuclear
Steam Rankine



GenIV Nuclear
Sodium Fast Reactor



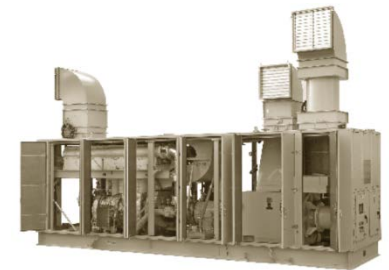
MARINE
Rolls-Royce WR-21
Type 45 Destroyer



VEHICULAR
Honeywell AGT1500
M1 Abrams Tank



Refrigeration
Commercial, Cryogenic



STATIONARY
Solar Turbines
Mercury 50

Effectiveness and Scaling Behavior

Heat Transfer Rate

Heat Transfer Surface Area

Temperature Differential

Hot Inlet

Cold Inlet

$$\dot{q} = UA\Delta T = \varepsilon(\dot{m}\bar{c}_p)_{\min}(T_{H,in} - T_{C,in})$$

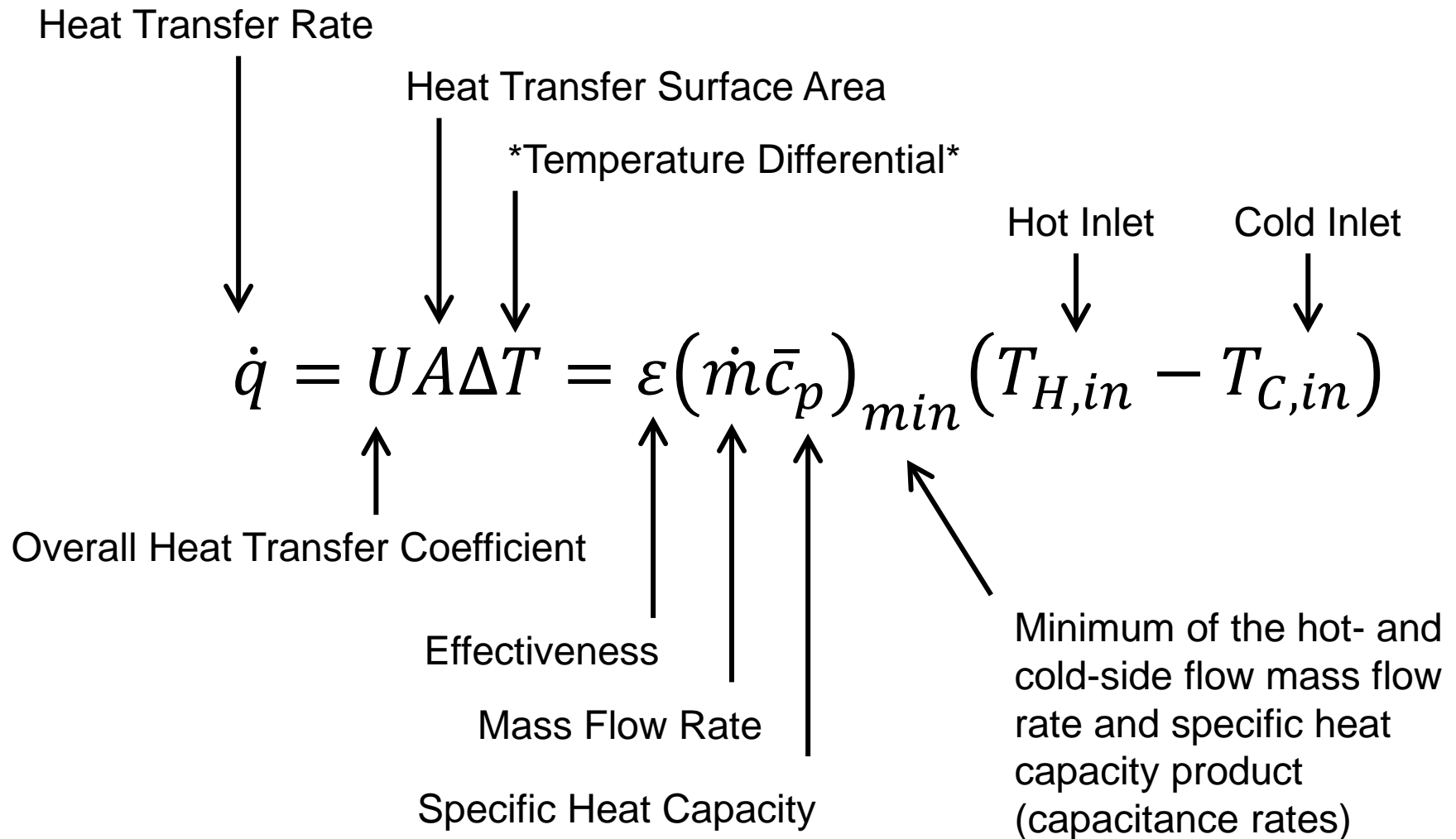
Overall Heat Transfer Coefficient

Effectiveness

Mass Flow Rate

Specific Heat Capacity

Minimum of the hot- and cold-side flow mass flow rate and specific heat capacity product (capacitance rates)



The diagram illustrates the heat transfer equation $\dot{q} = UA\Delta T = \varepsilon(\dot{m}\bar{c}_p)_{\min}(T_{H,in} - T_{C,in})$. Arrows point from descriptive labels to each term in the equation: 'Heat Transfer Rate' points to \dot{q} ; 'Heat Transfer Surface Area' points to U ; '*Temperature Differential*' points to ΔT ; 'Overall Heat Transfer Coefficient' points to ε ; 'Effectiveness' points to ε ; 'Mass Flow Rate' points to \dot{m} ; 'Specific Heat Capacity' points to \bar{c}_p ; 'Hot Inlet' points to $T_{H,in}$; 'Cold Inlet' points to $T_{C,in}$; and 'Minimum of the hot- and cold-side flow mass flow rate and specific heat capacity product (capacitance rates)' points to the $_{\min}$ subscript.

Fundamental Scaling Behavior

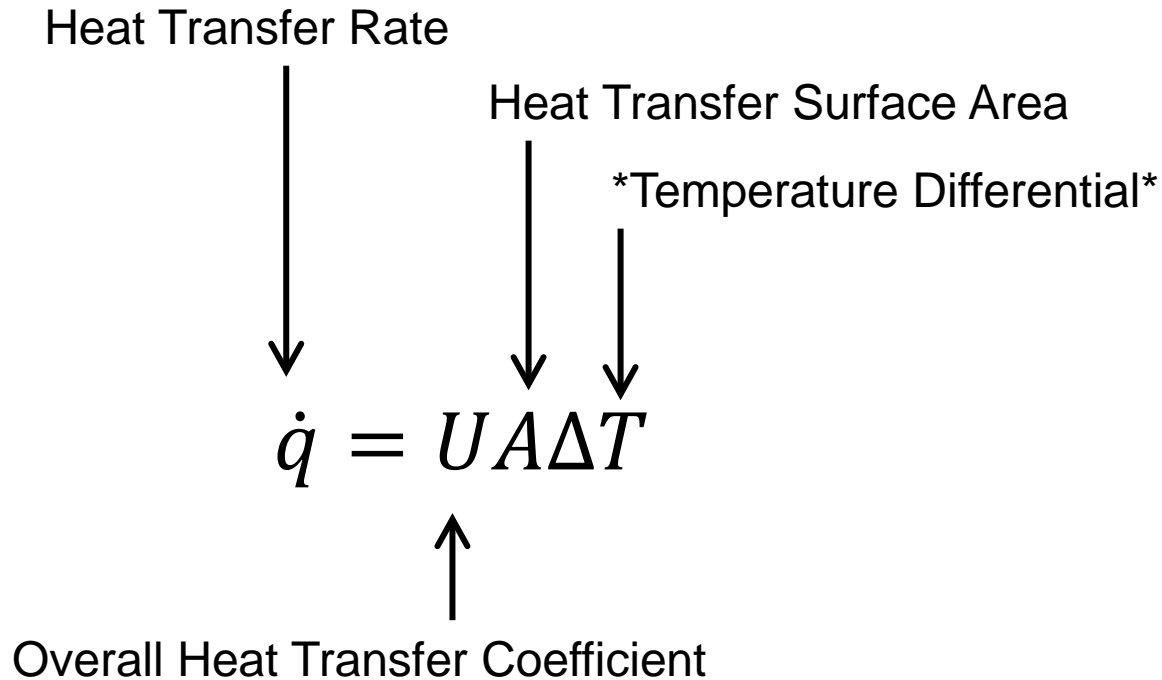
Heat Transfer Rate

Heat Transfer Surface Area

Temperature Differential

$$\dot{q} = UA\Delta T$$

Overall Heat Transfer Coefficient



Fundamental Scaling Behavior

$$\dot{q} = UA\Delta T$$

Fluid	Transmission Surface	Fluid	<u>Overall Heat Transmission Coefficient</u>	
			(Btu/ft ² hr °F)	(W/m ² K)
Water	Cast Iron	Air or Gas	1.4	7.9
Water	Mild Steel	Air or Gas	2.0	11.3
Water	Copper	Air or Gas	2.3	13.1
Water	Cast Iron	Water	40 - 50	230 - 280
Water	Mild Steel	Water	60 - 70	340 - 400
Water	Copper	Water	60 - 80	340 - 455
Air	Cast Iron	Air	1.0	5.7
Air	Mild Steel	Air	1.4	7.9
Steam	Cast Iron	Air	2.0	11.3
Steam	Mild Steel	Air	2.5	14.2
Steam	Copper	Air	3.0	17
Steam	Cast Iron	Water	160	910
Steam	Mild Steel	Water	185	1050
Steam	Copper	Water	205	1160
Steam	Stainless Steel	Water	120	680

Effectiveness and Scaling Behavior

Heat Transfer Rate

$$\dot{q} = UA\Delta T = \varepsilon (\dot{m} \bar{c}_p)_{\min} (T_{H,in} - T_{C,in})$$

Hot Inlet

Cold Inlet

Effectiveness

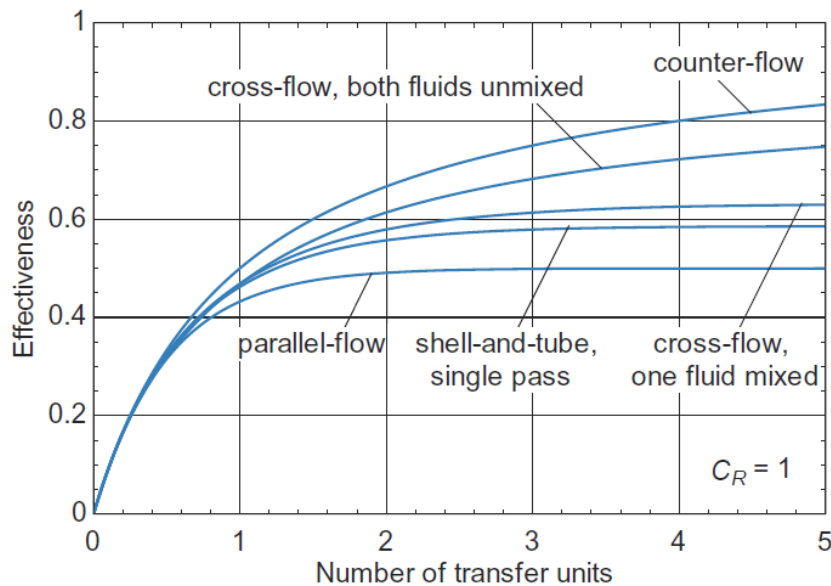
Mass Flow Rate

Specific Heat Capacity

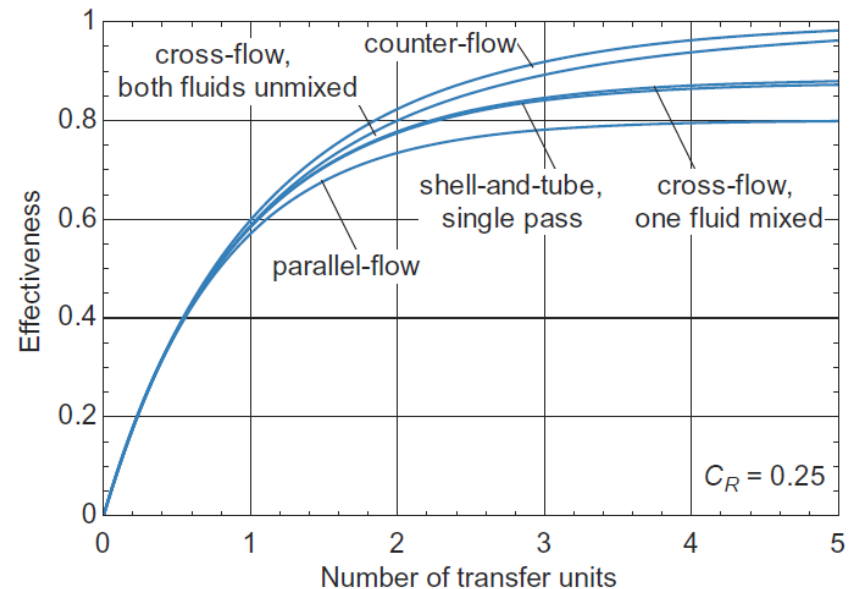
Minimum of the hot- and cold-side flow mass flow rate and specific heat capacity product (capacitance rates)

Other Useful e-NTU Scaling

- Configuration matters most for $C_R = 1$; counter-flow is best
- Effectiveness is asymptotic with NTU (size); 1 for counter-flow
- Configuration matters less as C_R approaches 0



$C_R = 1$



$C_R = 0.25$

Pressure Drop Correlations

$$\Delta P = \sum \Delta P_{friction} + \sum \Delta P_{local} + \sum \Delta P_{acceleration} + \sum \Delta P_{body\ forces}$$

■ Body Forces

$$\Delta P_{friction} = f \frac{L_s}{d_{hyd}} \frac{1}{2} \frac{G^2}{\rho}$$

$$\Delta P_{gravity} = g \left(\frac{i_{out} \rho_{out} + i_{in} \rho_{in}}{i_{out} + i_{in}} \right) L \sin(\theta)$$

Blasius

Kondrat'ev

$$f = 0.316 Re^{-0.25}$$



$$f = 0.188 Re^{-0.22}$$

■ Local Form Losses

$$\frac{\Delta P_{local}}{G^2/2\rho} = K_{loss} = f \left(\frac{L_{equivalent}}{d_{hyd}} \right)$$

Haaland

Filonenko

$$f = \frac{1}{\left(1.8 \log_{10} \left[\left(\frac{RR}{3.7} \right)^{1.11} + \frac{6.9}{Re} \right] \right)^2}$$



$$f = \frac{1}{(1.82 \log_{10} Re_b - 1.64)^2}$$

■ Acceleration Difference

$$\Delta P_{acceleration} = G^2 \left(\frac{1}{\rho_{out}} - \frac{1}{\rho_{in}} \right)$$

Colebrook Equation

$$\frac{1}{\sqrt{f}} = -2 \log_{10} \left(\frac{RR}{3.7} + \frac{2.51}{Re \sqrt{f}} \right)$$

Heat Transfer Correlations

Constant Property

Dittus-Boelter Correlation

$$Nu = C Re^n Pr^m$$



Supercritical Fluids

Jackson's Correlation

$$Nu = 0.0183 Re_b^{0.82} Pr_b^{0.5} \left(\frac{\rho_w}{\rho_b} \right)^{0.3} \left(\frac{\bar{c}_p}{c_{p,b}} \right)^n$$

Gnielinski Correlation

$$Nu = \frac{\left(\frac{f}{8} \right) (Re - 1000) Pr}{1 + 12.7 \sqrt{\frac{f}{8}} \left(Pr^{\frac{2}{3}} - 1 \right)}$$



Pitla Correlation

$$Nu = \left(\frac{Nu_w|_{Gnielinski} + Nu_b|_{Gnielinski}}{2} \right) \frac{k_w}{k_b}$$