

 **Albany** : a Trilinos-based multi-physics partial differential equation research tool created using the AgileComponents code development strategy

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SIAM CSE 2019

Spokane, WA

Feb. 25-Mar. 1 2019



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Acknowledgements



“Father” of Albany, early advocate for AgileComponents strategy:

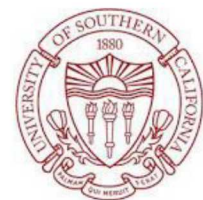
- Andy Salinger [SNL]

Albany contributors (58, from github):

- | | | |
|----------------------------|----------------------|-------------------------|
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| • G. Hansen [SNL] | • J. Robbins [SNL] | • J. Clough [USC] |
| • M. Perego [FSU/SNL] | • T. Smith [SNL] | • W. Sun [Columbia] |
| • L. Bertagna [FSU/SNL] | • R. Jones [SNL] | • Z. Wang [USC] |
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| • A. Salinger [SNL] | • Q. Chen [Clemson] | • M. Parks [SNL] |
| • D. Littlewood [SNL] | • P. Lindsay [SNL] | • J. Robbins [SNL] |
| • J. Foulk [SNL] | • J. Fike [SNL] | • M. Hoffman [LANL] |
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| • J. Overfelt [SNL] | • J. Redhorse [SNL] | • M. Bloomfield [RPI] |
| • E. Nielsen [SNL] | • S. Bova [SNL] | • G. Philipot [CalTech] |
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| • O. Guba [SNL] | • H. Yuan [Tokyo] | • J. Willenbring [SNL] |
| • M. Juha [U de La Sabana] | • C. Siefert [SNL] | • ... |



Rensselaer



Outline

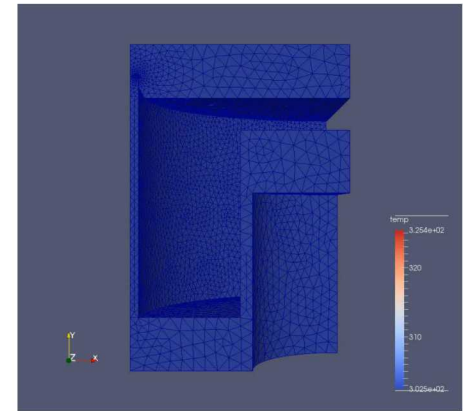
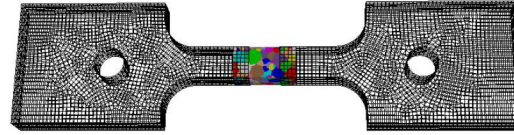


1. AgileComponents code-development strategy

2. What is Albany?

3. Albany code design

- Global discretization & libraries
- Problem abstraction & finite element assembly
- Nonlinear model abstraction & libraries
- Linear model abstraction & libraries
- Software quality tools



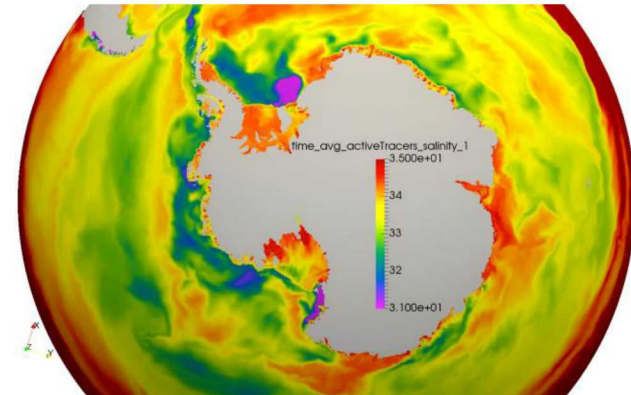
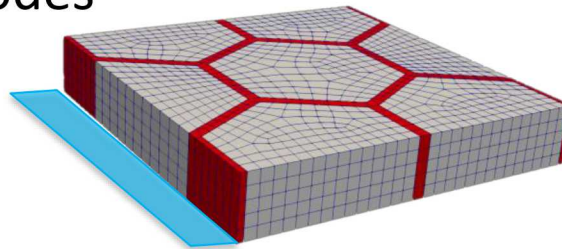
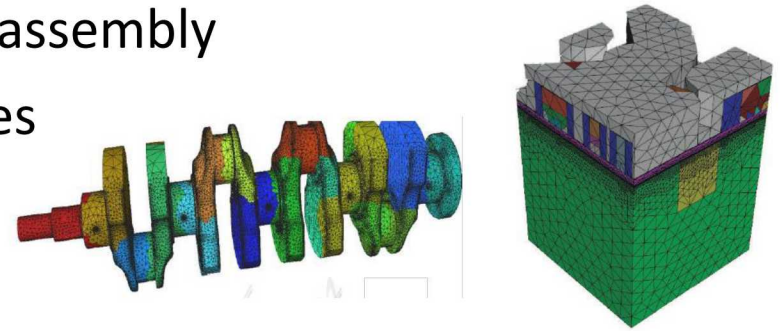
4. Applications hosted by Albany

5. Algorithmic projects hosted by Albany

6. Coupling with other codes

7. Work in progress

8. Summary



AgileComponents: a PDE code strategy

Strategic Goal: To enable the **rapid** development of new **production** codes embedded with **transformational** capabilities.

- **Technical strategy:** projects create, use, and improve a common base of modular, independent-yet-interoperable, software **components**
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Base of Software Components



AgileComponents: a PDE code strategy

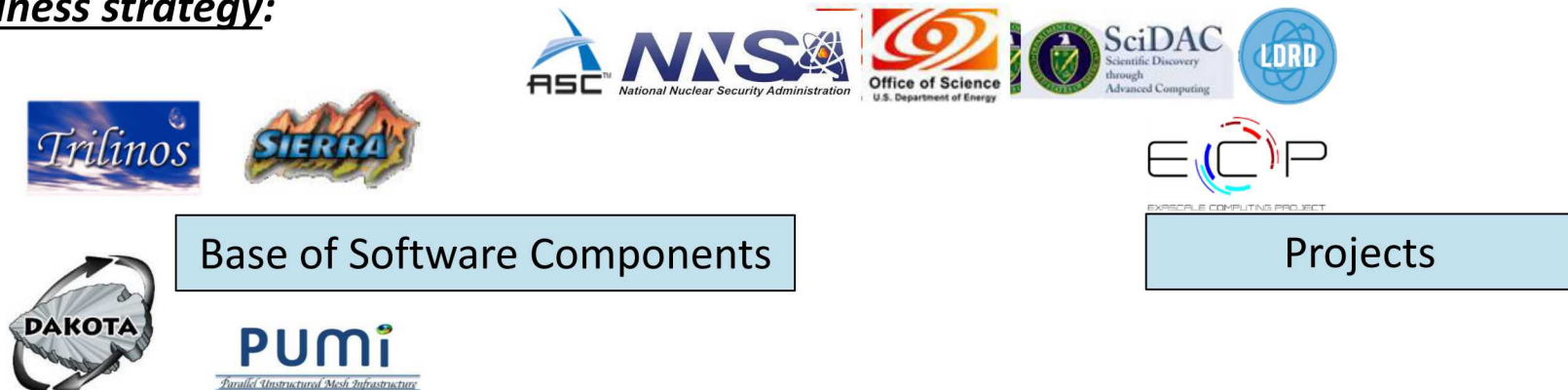
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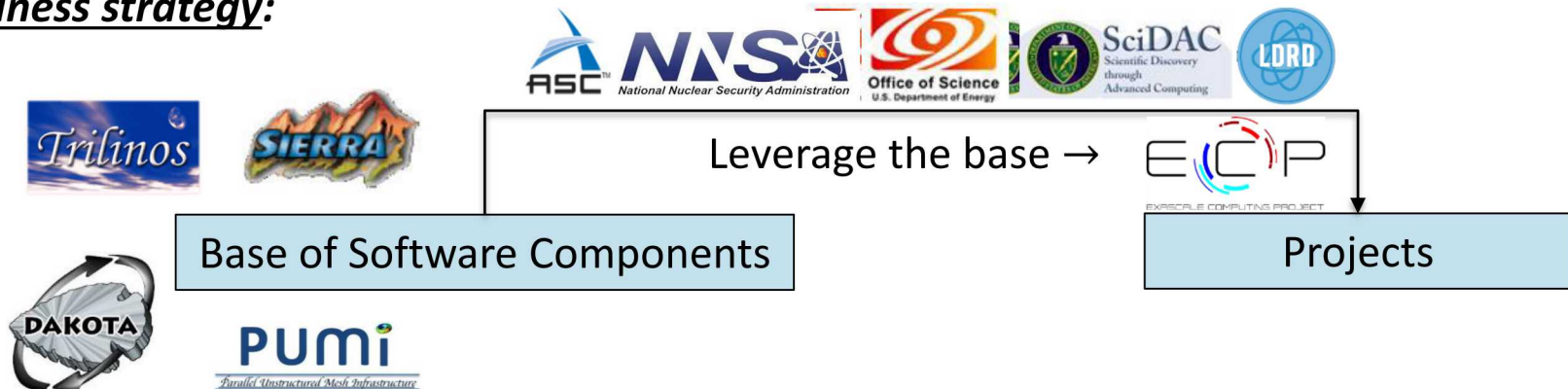
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What is Albany? (high-level description)

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☒ Interfaces ☒ **Demonstration Applications**

2008



What is Albany? (high-level description)

Albany: open-source*, parallel, C++, unstructured-grid, mostly-implicit multi-physics finite element code that demonstrates **AgileComponents** vision.

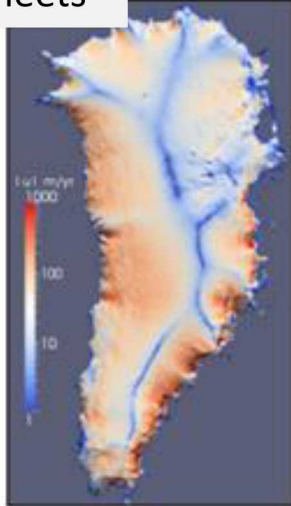
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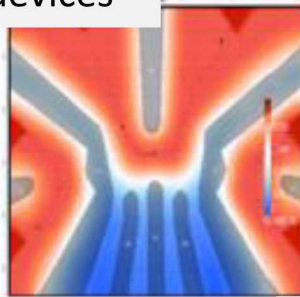
Distinguishing features of Albany:

- Houses a variety of **diverse algorithmic projects** and **applications**:

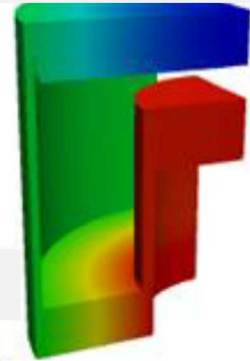
Ice sheets



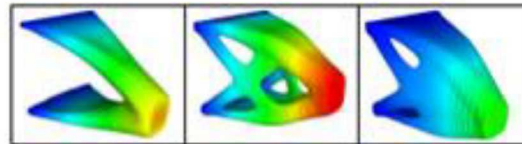
Quantum devices



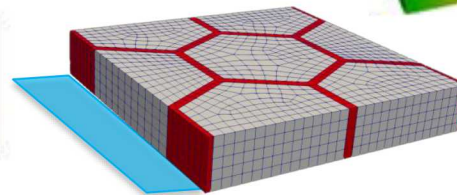
Computational mechanics



Additive manufacturing



Arctic coastal erosion



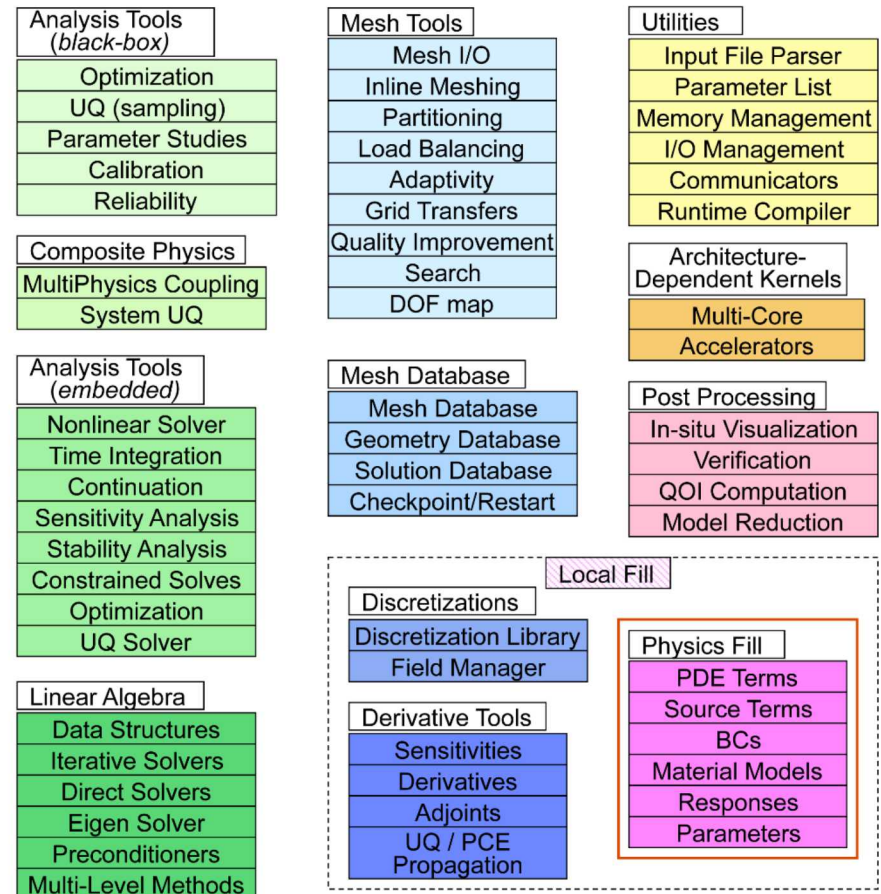
- Funded entirely by applications** residing within.
- Both a “**sand-box**” for prototyping **new algorithms/applications** and a **production** code.

The components effort: libraries & tools

Components in Albany = cutting-edge technology from Trilinos, SCOREC, SierraToolKit, DAKOTA, FASTMath, QUEST, Kitware, etc.

Many components are **Trilinos*** packages:

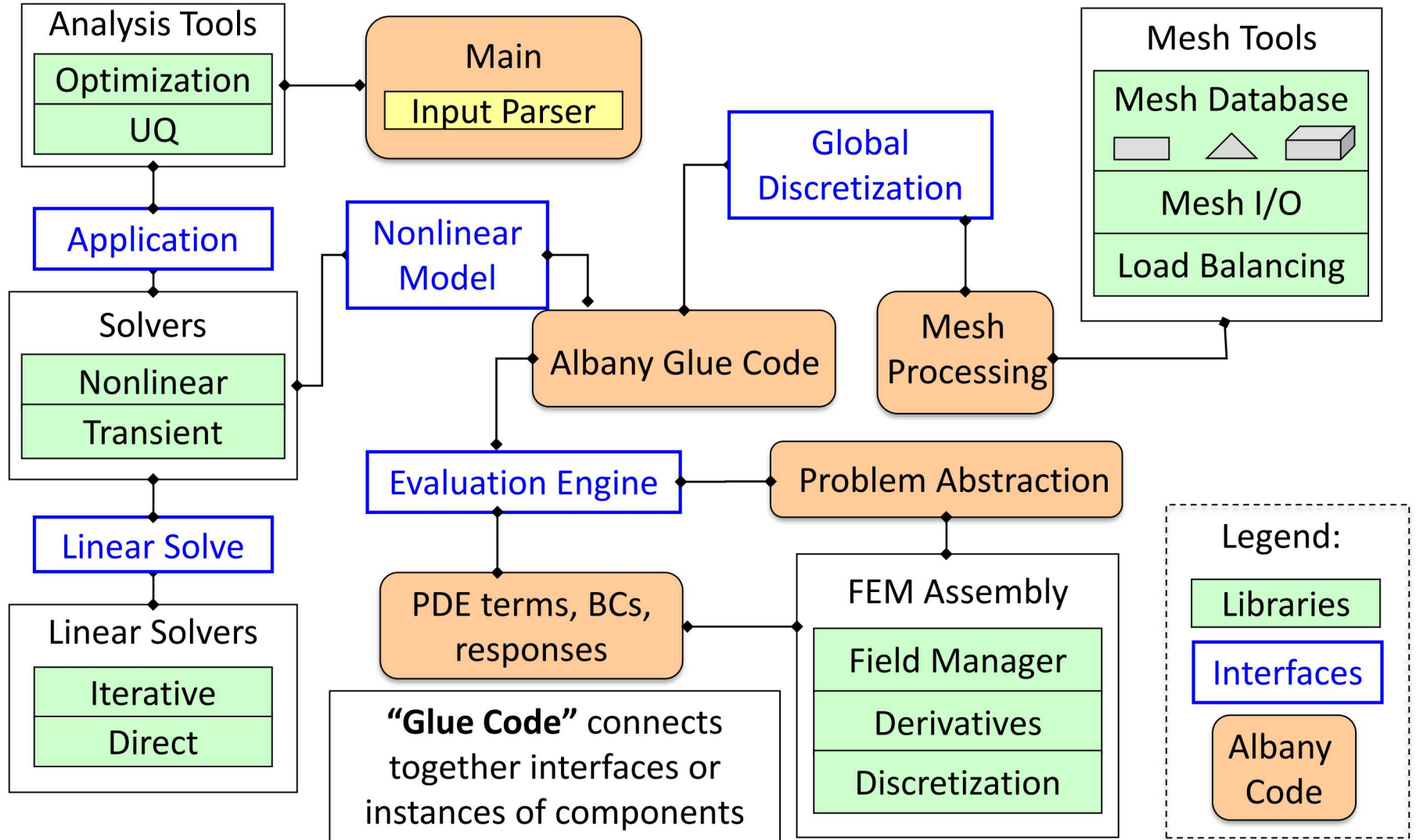
- Distributed linear algebra (*Tpetra*)
- Mesh tools (*STK*)
- Discretization tools (*Intrepid2*)
- Nonlinear solver (*NOX*)
- Linear solver (*Belos*)
- Preconditioners (*Ifpack2*)
- Automatic differentiation (*Sacado*)
- Shared memory parallelism (*Kokkos*)
- Optimization (*ROL*)
- *Many more...*



: 40+ packages; 120+ libraries

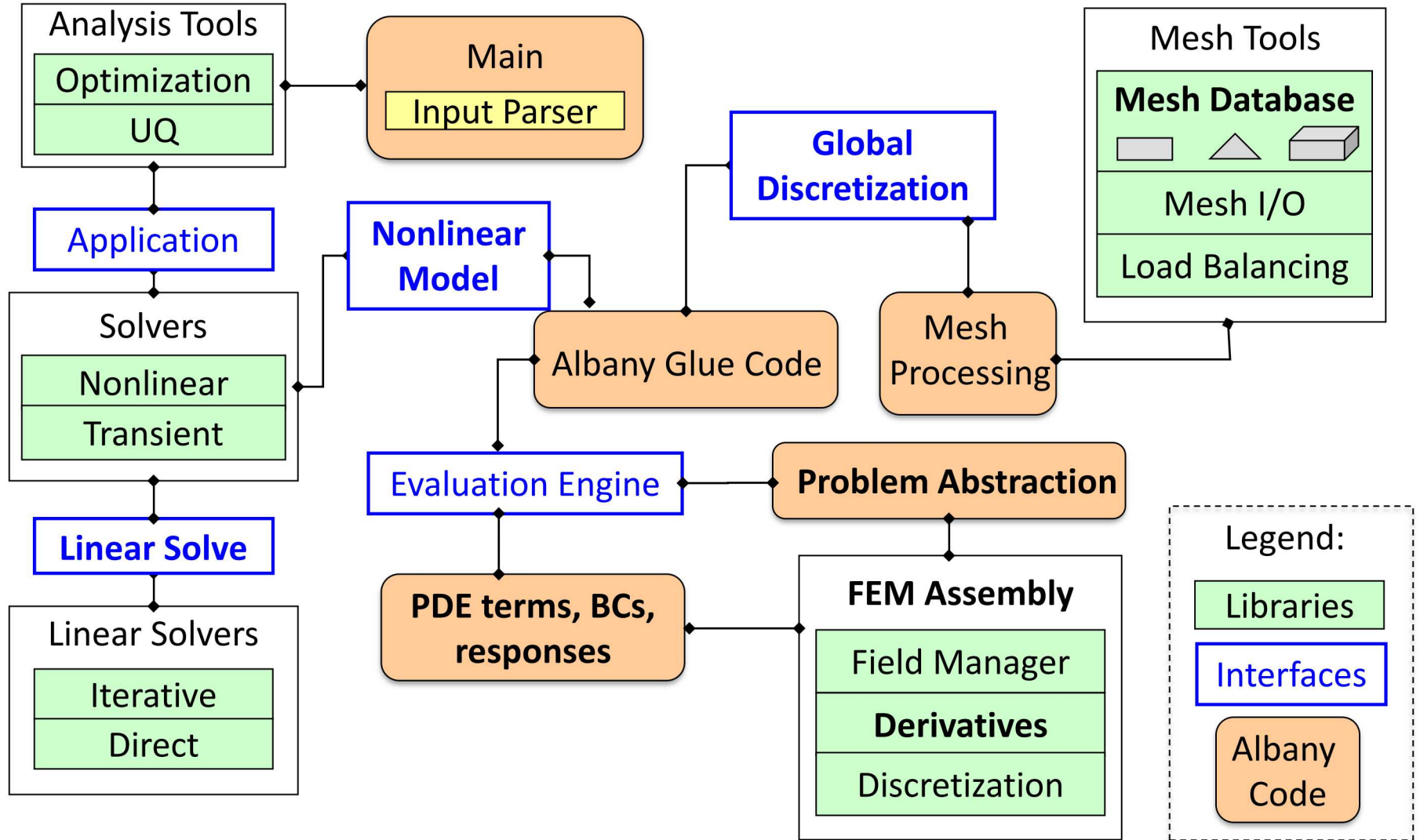
What is Albany? (under-the-hood)

Albany = Component Libraries + Abstract Interfaces + “Glue Code”



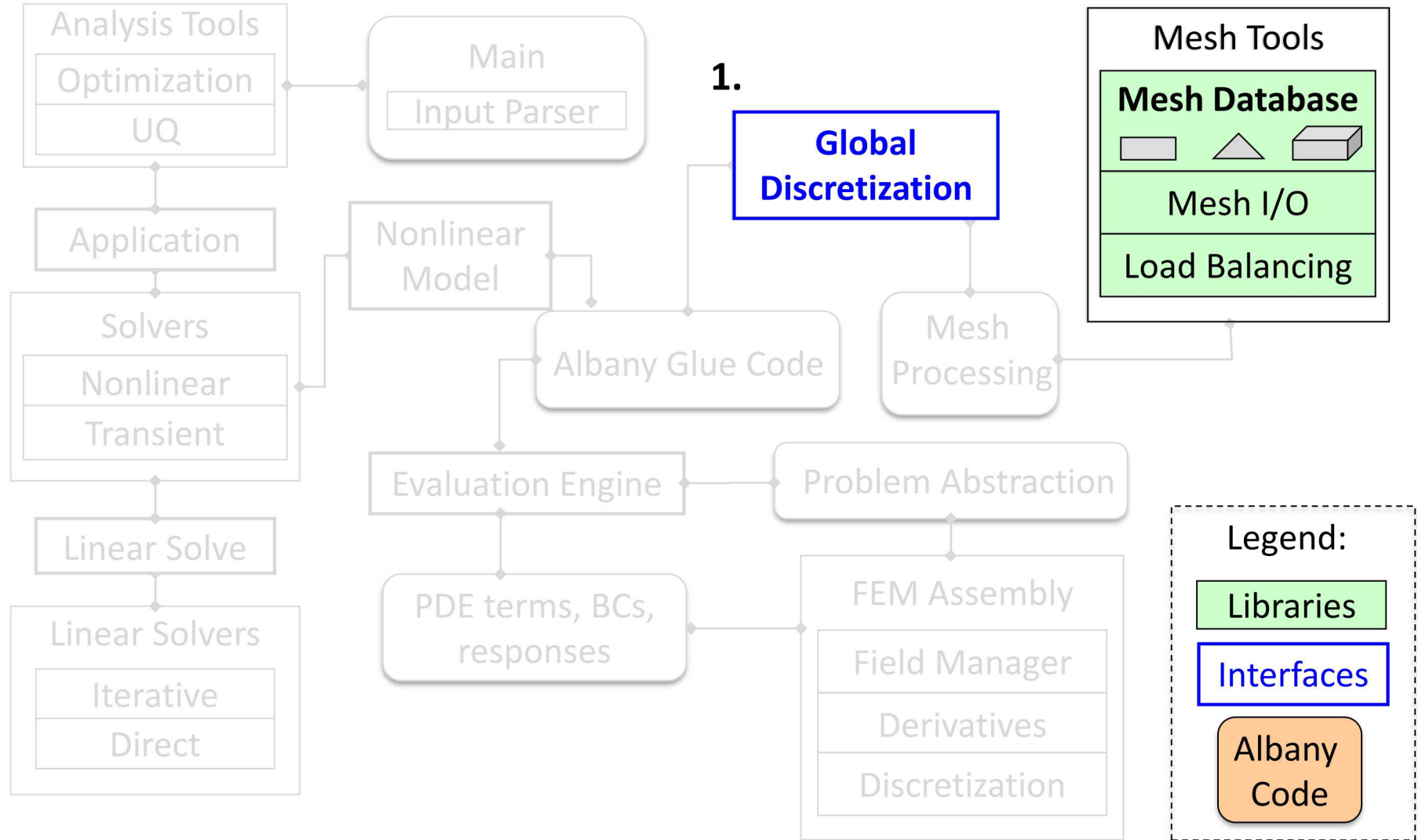
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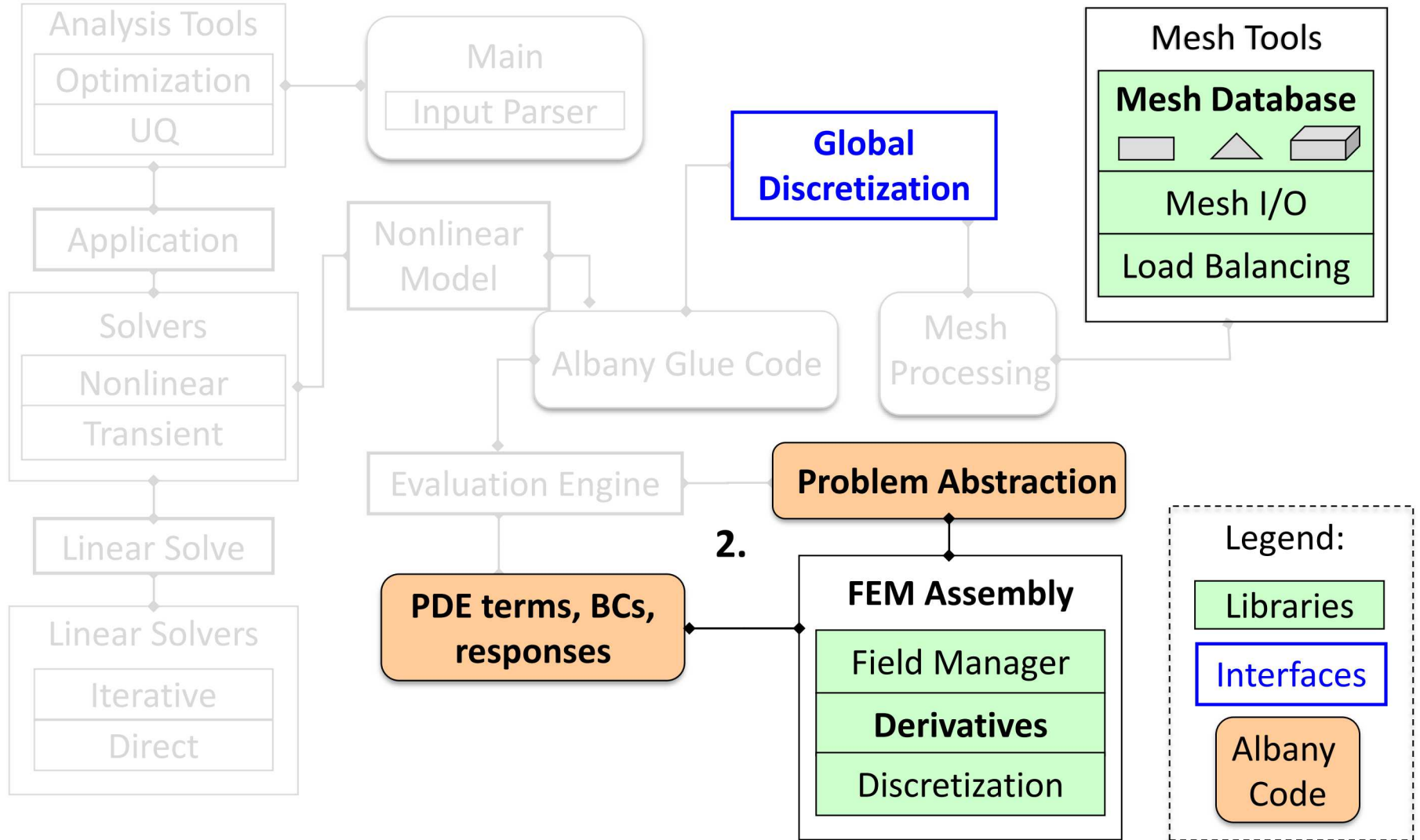
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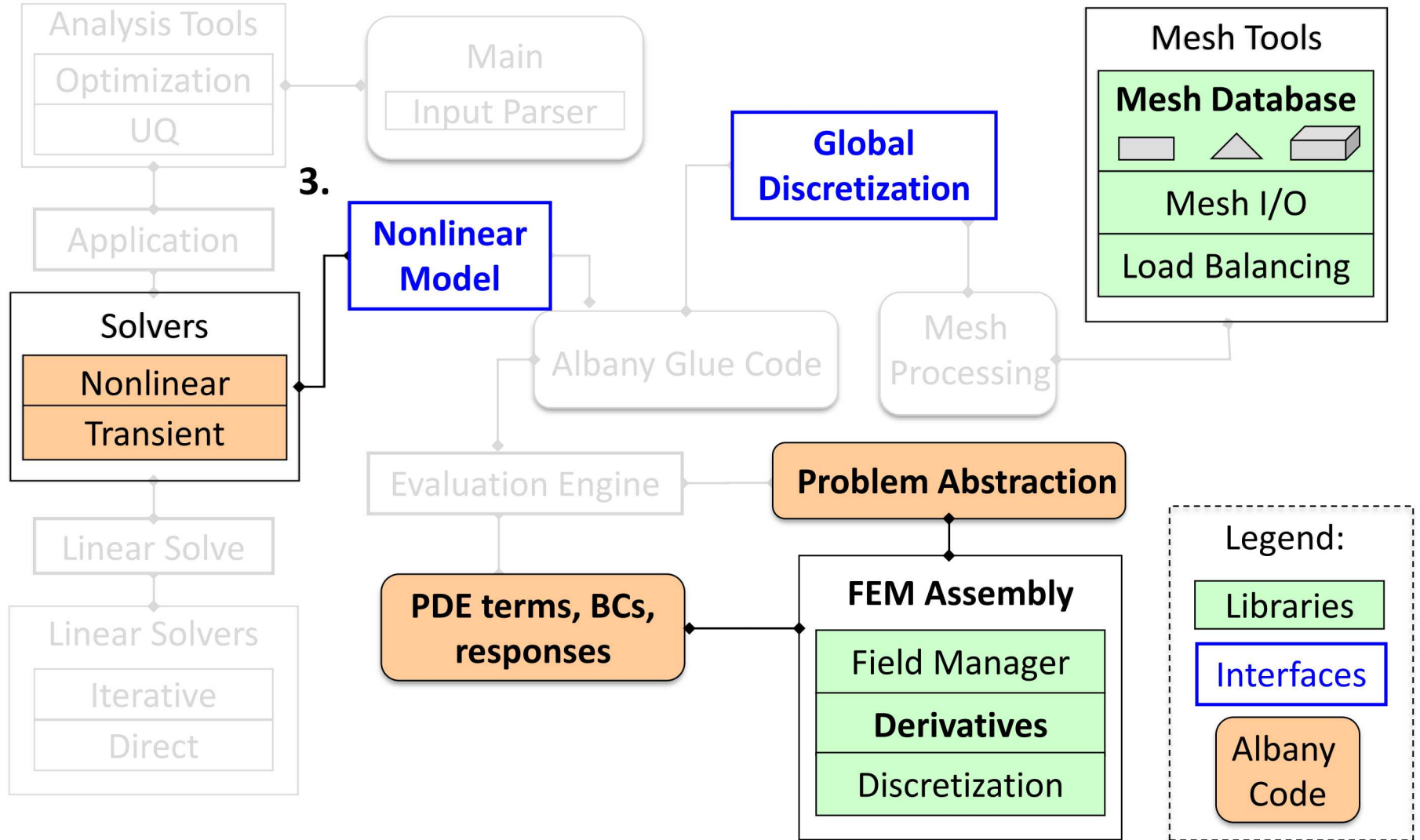
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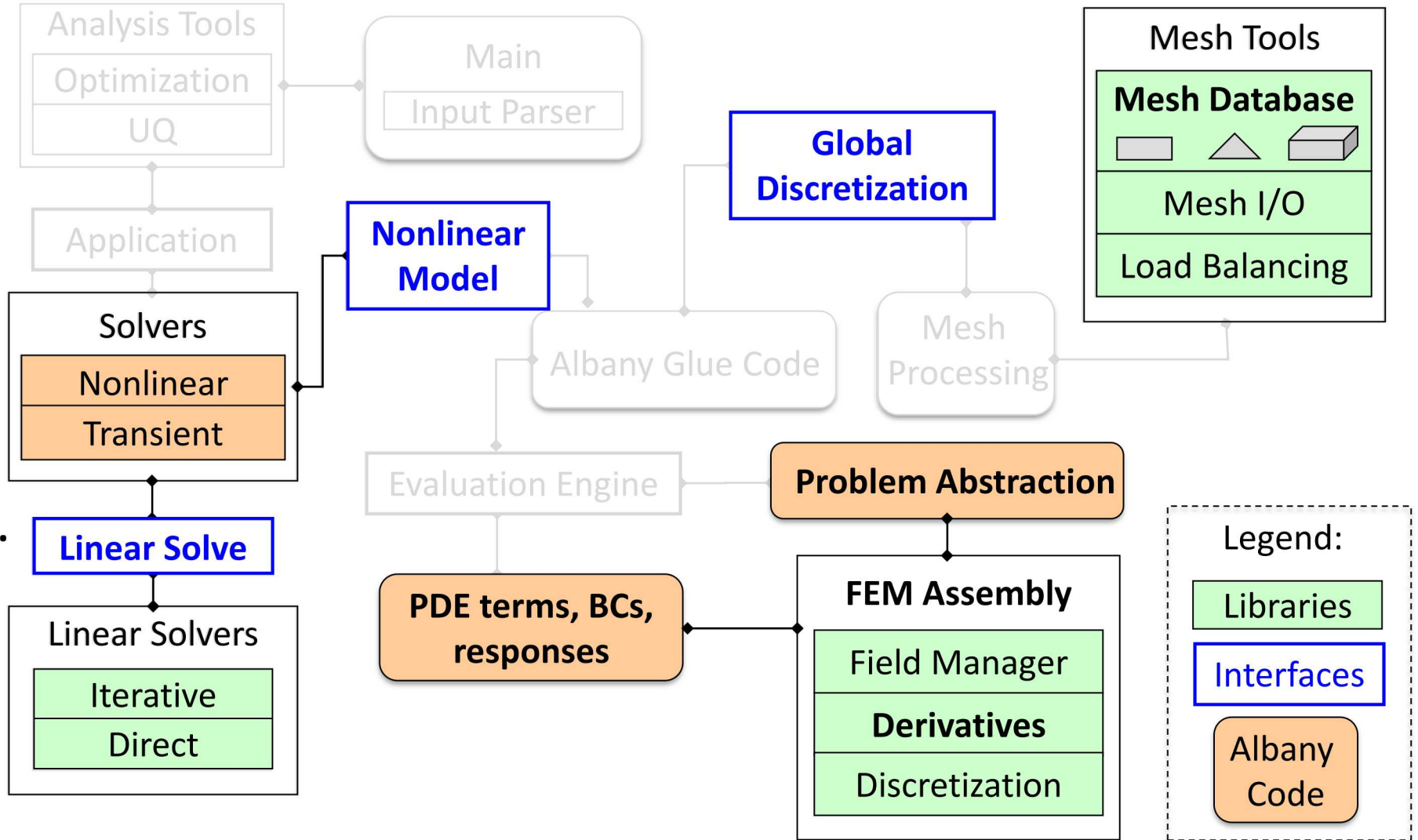
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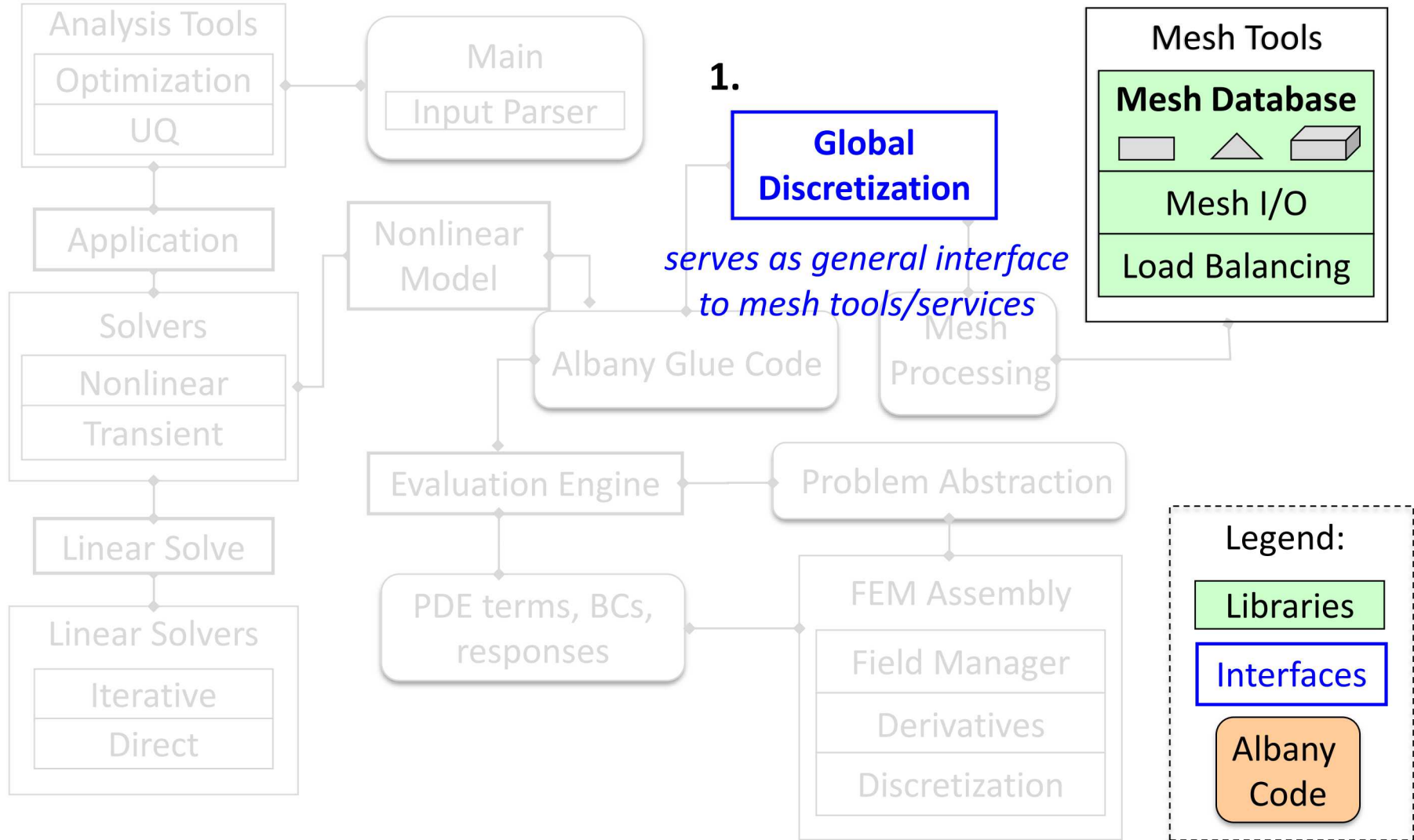
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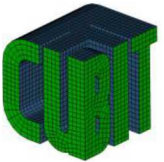
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Global discretization abstraction & libraries

Discretization interface: currently has *two independent implementations*

1. **SierraToolKit (STK)** package in Trilinos.
 - Supports reading in **Exodus** mesh files (e.g., from CUBIT), **inline meshing** via Pamgen, **simple rectangular meshes** constructed in Albany.
 - Meshes can be **structured/unstructured** but are **static**.
2. **Parallel Unstructured Mesh Interface (PUMI)** package, developed at the Scientific Computation Research Center (SCOREC) at RPI.
 - Supports **VTK mesh files** (generated by Symmetrix).
 - Goal-oriented generalized **error estimation** and **in-memory mesh adaptation**.

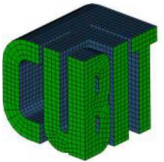


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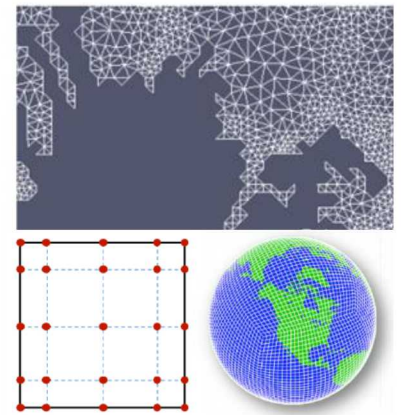
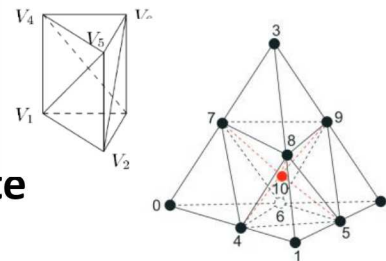
Parallel Unstructured Mesh Infrastructure

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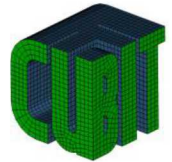
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- Goal-oriented generalized **error estimation** and **in-memory mesh adaptation**.

Element types: variety of element types supported, with basis functions/quadrature routines from *Intrepid2* Trilinos library:

- **Isoparametric** elements (tet, hex, wedge, ...).
- 2D **spectral elements** of arbitrary orders.
- Some physics-specific elements, e.g., **composite 10-node tetrahedron** for solid mechanics.



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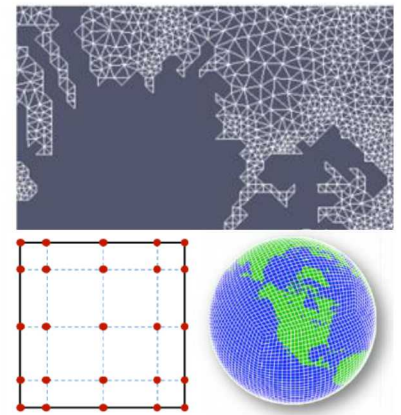
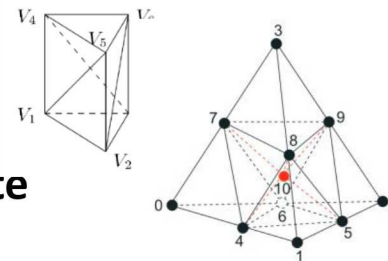
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Albany is a **Continuous Galerkin (CG)** unstructured grid finite element code.

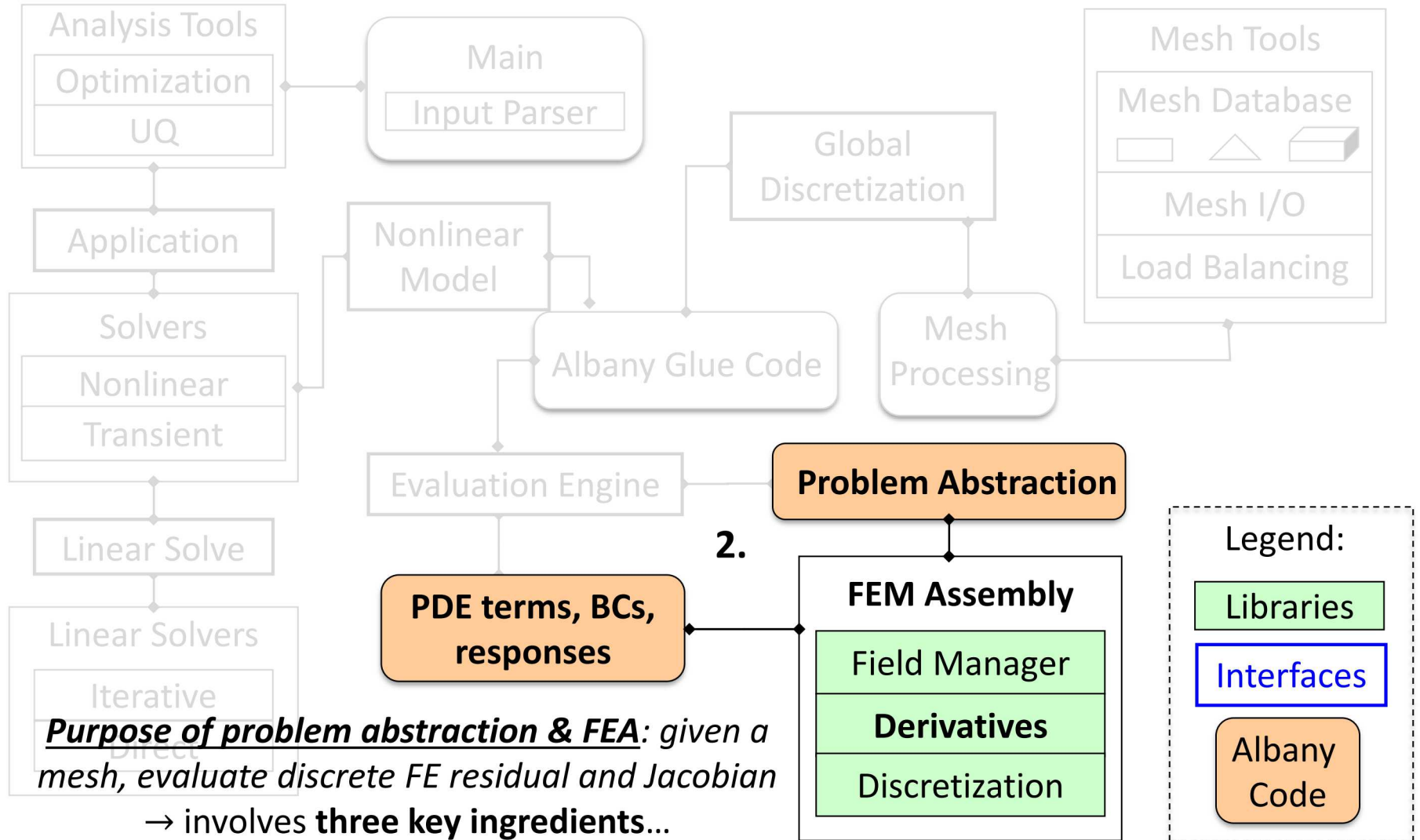
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What is Albany? (under-the-hood)

Albany = Component Libraries + Abstract Interfaces + “Glue Code”



1. Templated-based automatic differentiation

Automatic differentiation (AD) provides exact derivatives without time/effort of deriving and hand-coding them.

- Template equation implementation on scalar type.
- Libraries (Sacado) provides new scalar types that **overload the math operators** to propagate embedded quantities via chain rule.
 - Derivatives: `DFad<double>`
 - Hessians: `DFad<SFad<double,N>>`
 - Stochastic Galerkin resid: `PCE<double>`
 - Stochastic Galerkin Jac: `DFad<PCE<double>`
 - Sensitivities: `DFad<double>`

No finite difference truncation error!

- Great for **multi-physics codes** (e.g., many Jacobians) and **advanced analysis** (e.g., sensitivities, optimization)

double	DFad<double>
Operation	Overloaded AD impl
$c = a \pm b$	$\dot{c} = \dot{a} \pm \dot{b}$
$c = ab$	$\dot{c} = a\dot{b} + \dot{a}b$
$c = a/b$	$\dot{c} = (\dot{a} - c\dot{b})/b$
$c = a^r$	$\dot{c} = ra^{r-1}\dot{a}$
$c = \sin(a)$	$\dot{c} = \cos(a)\dot{a}$
$c = \cos(a)$	$\dot{c} = -\sin(a)\dot{a}$
$c = \exp(a)$	$\dot{c} = c\dot{a}$
$c = \log(a)$	$\dot{c} = \dot{a}/a$

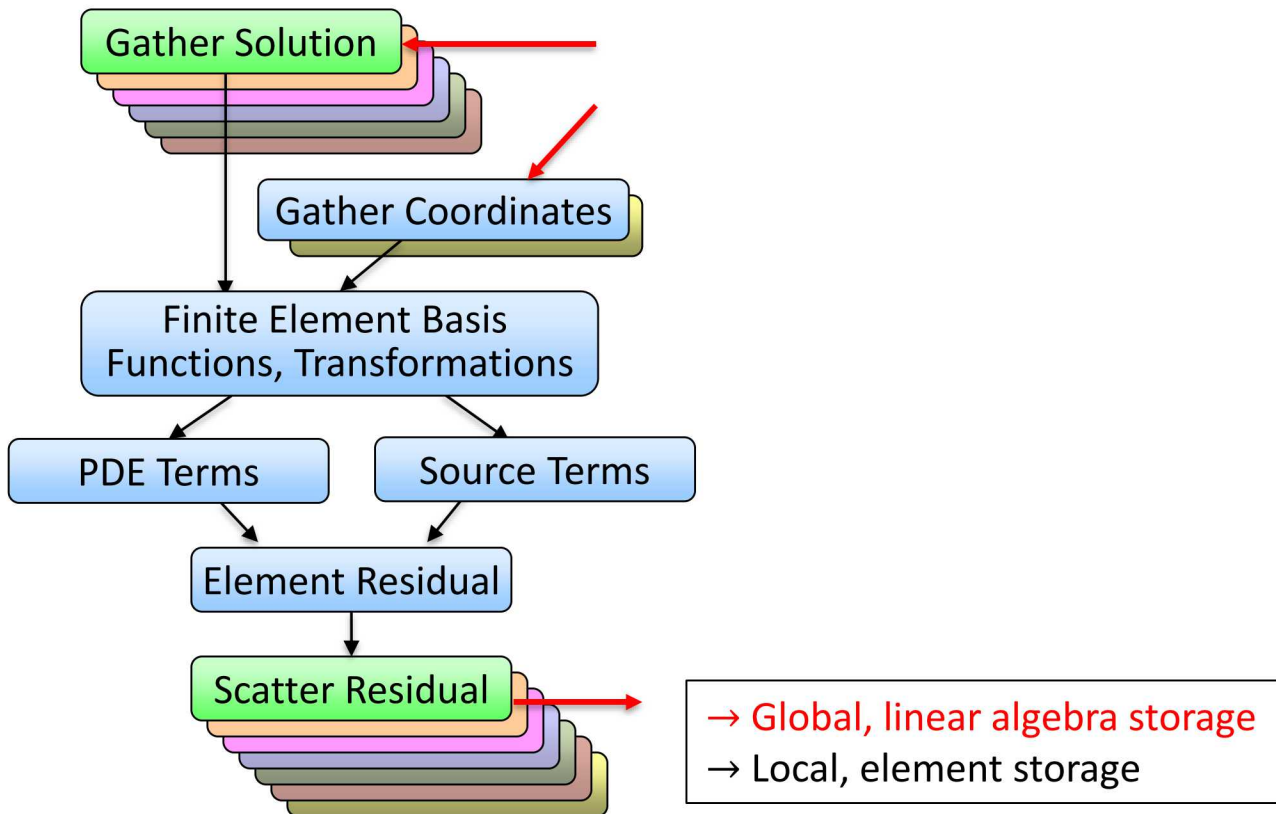
```
template <typename ScalarT>
void computeF(ScalarT* x, ScalarT* f)
{
    f[0] = 2.0 * x[0] + x[1] * x[1];
    f[1] = x[0] * x[0] * x[0] + sin(x[1]);
}
```

```
double* x;
double* f;
...
computeF(x, f);
```

```
DFad<double>* x;
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```

2. Template-based generic programming (TBGP) Sandia National Laboratories

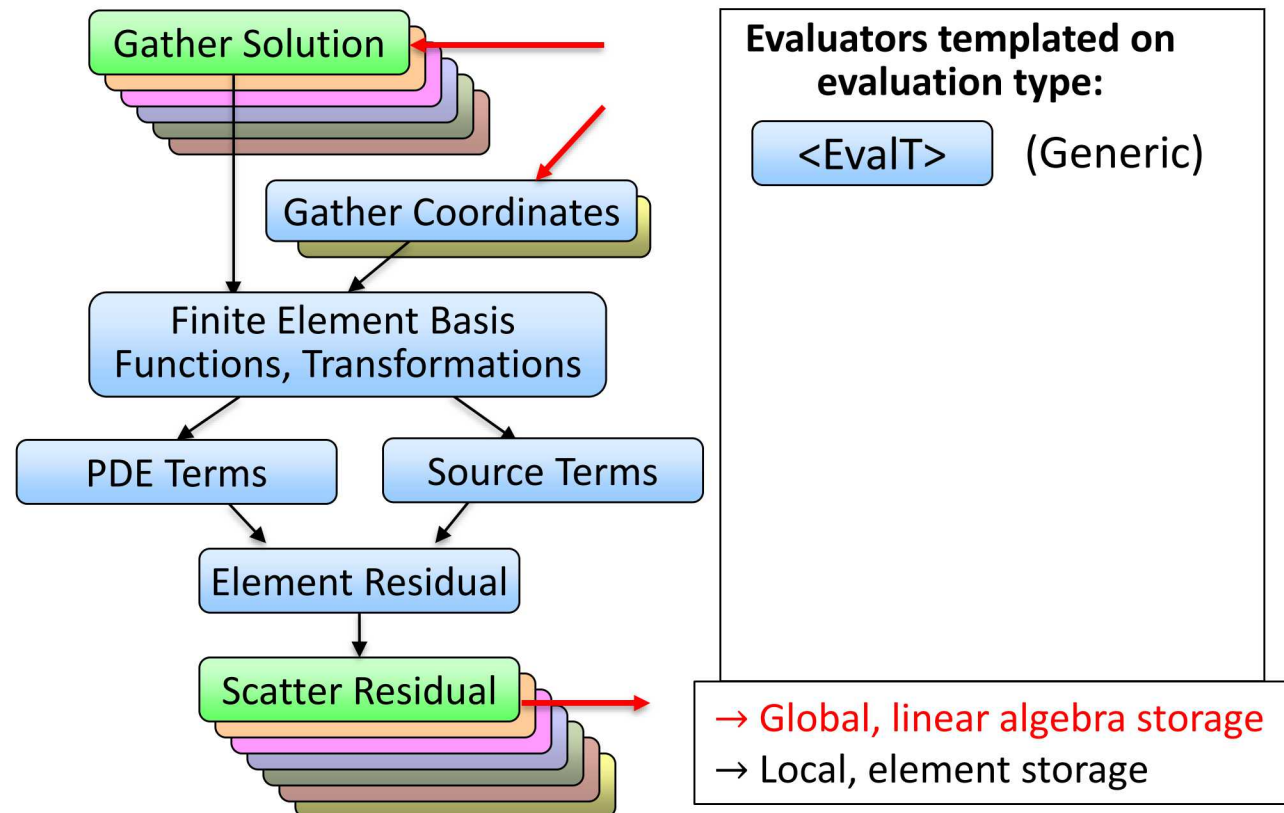
Albany Finite Element Assembly (FEA):



- **Gather Solution** extracts values from global structures, puts in element local structures
- **Evaluators** operate on element local data structures
- **Scatter** adds local contributions to global structures

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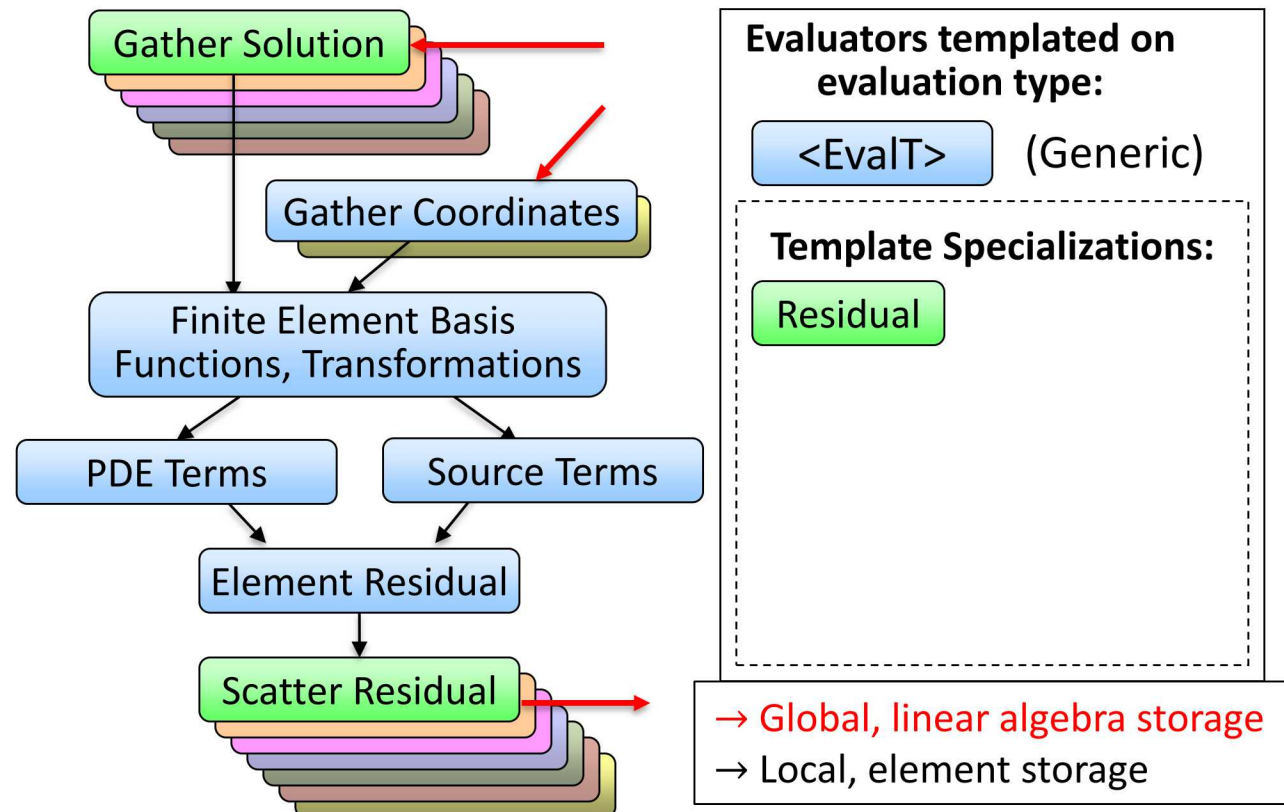
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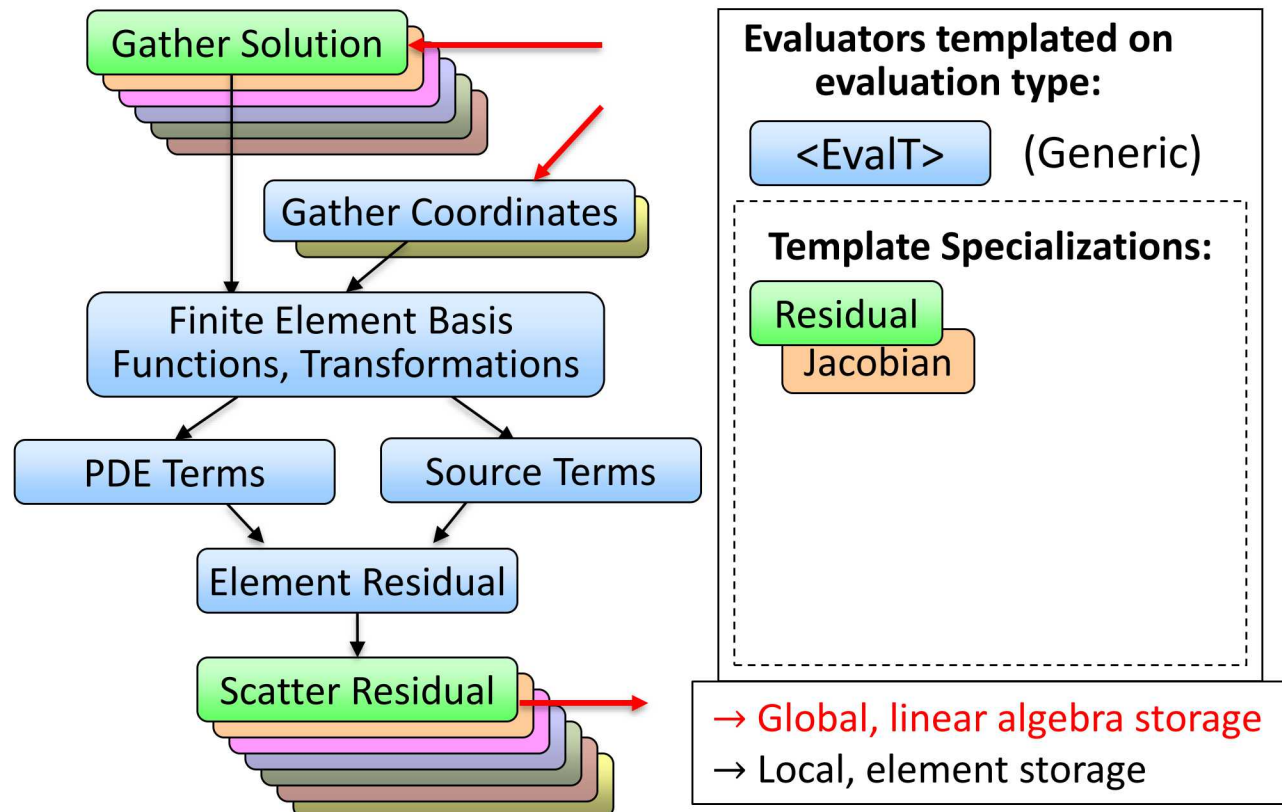
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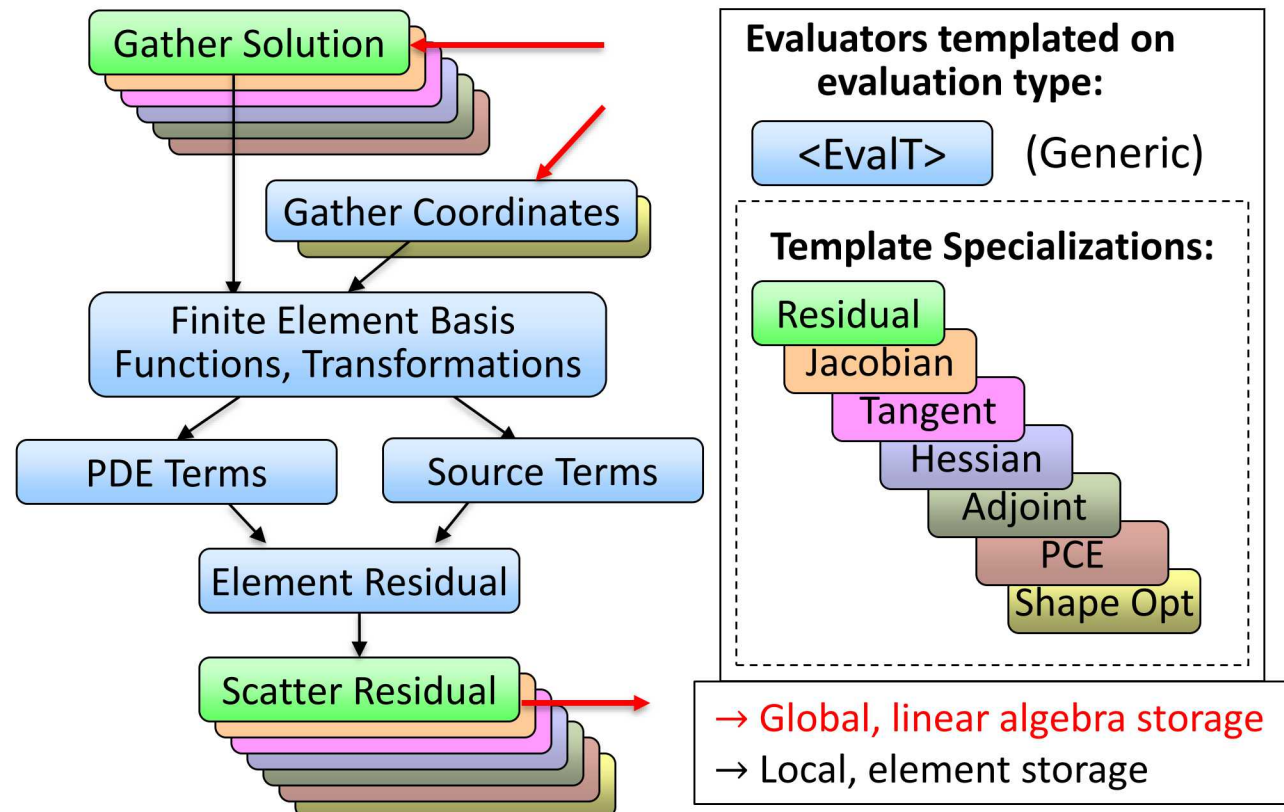
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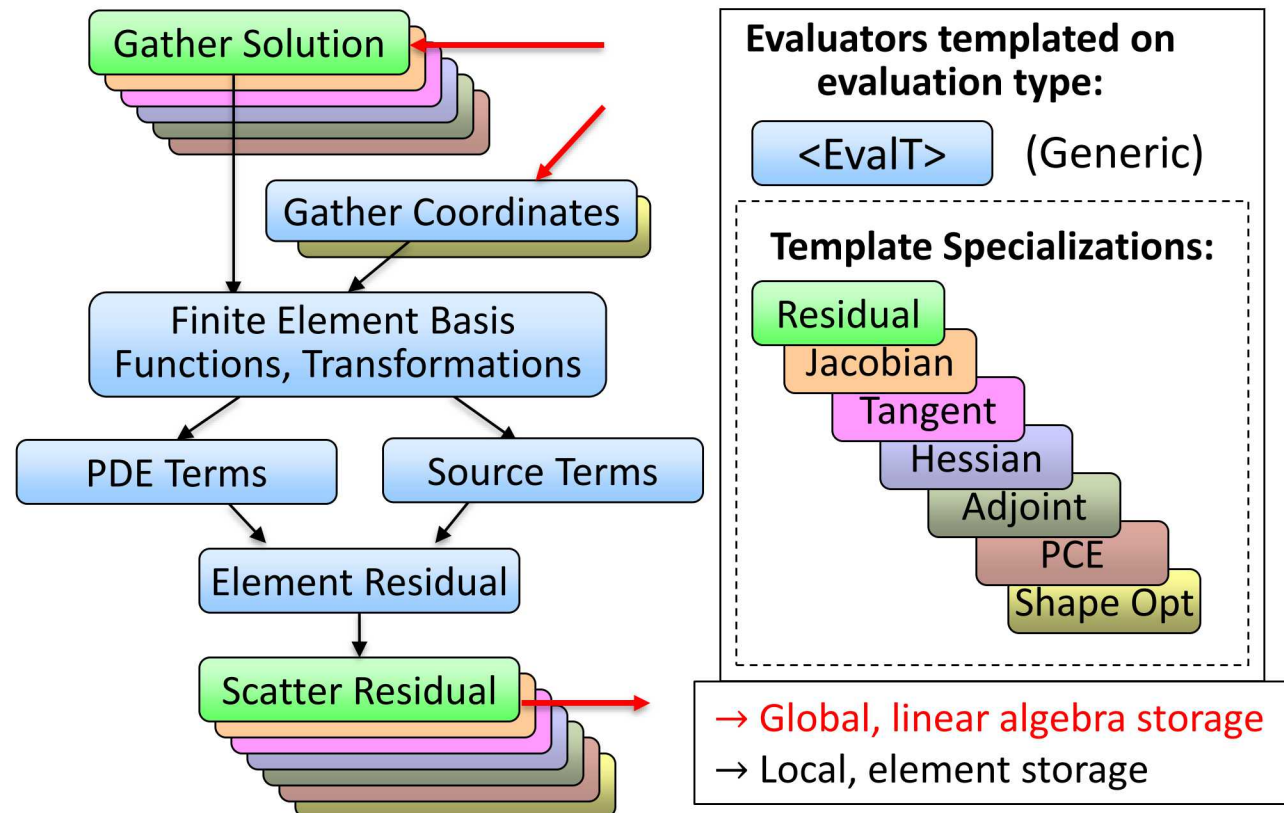
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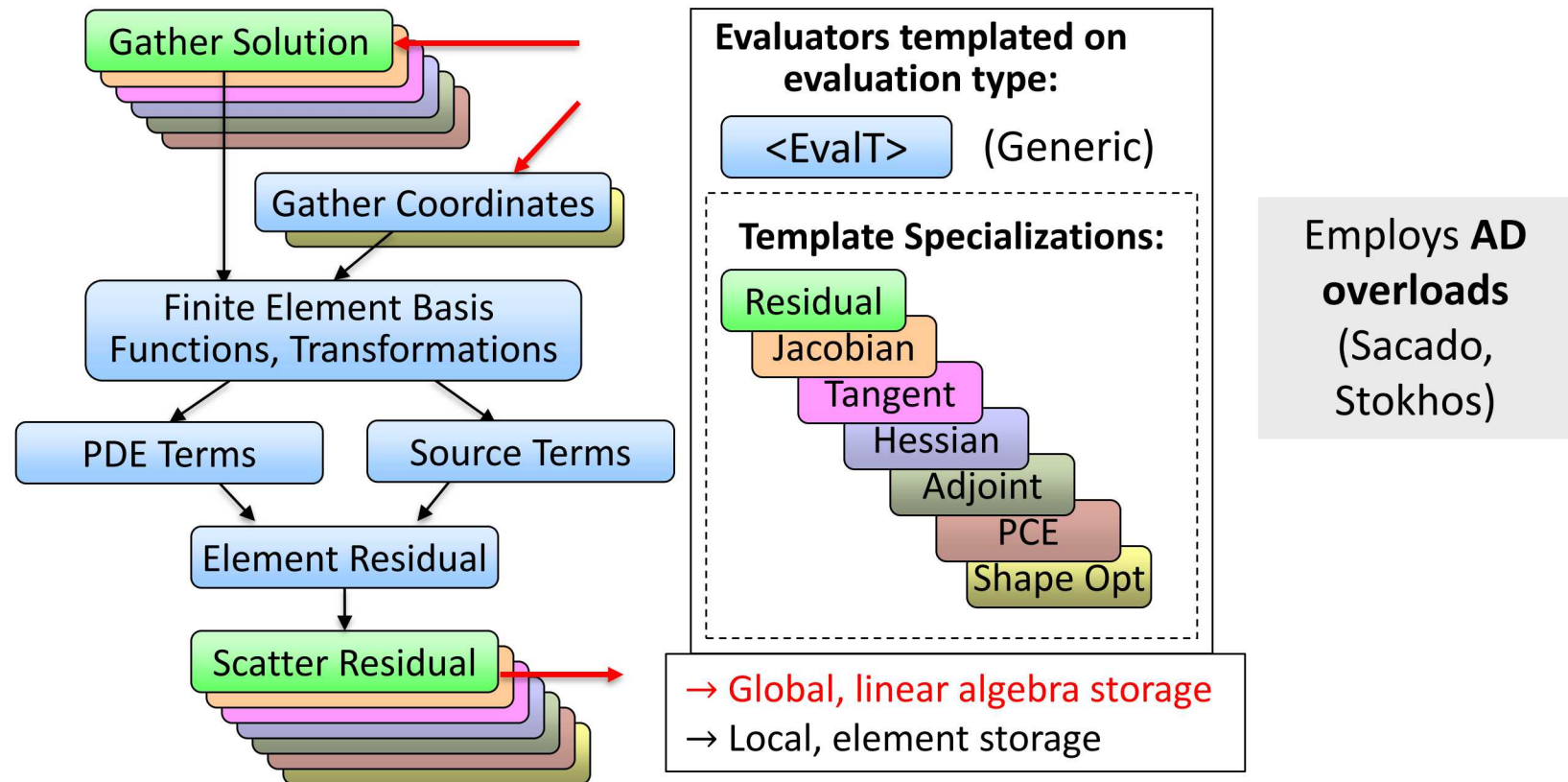


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Enables **advanced analyses**
(sensitivities, optimization, ...)

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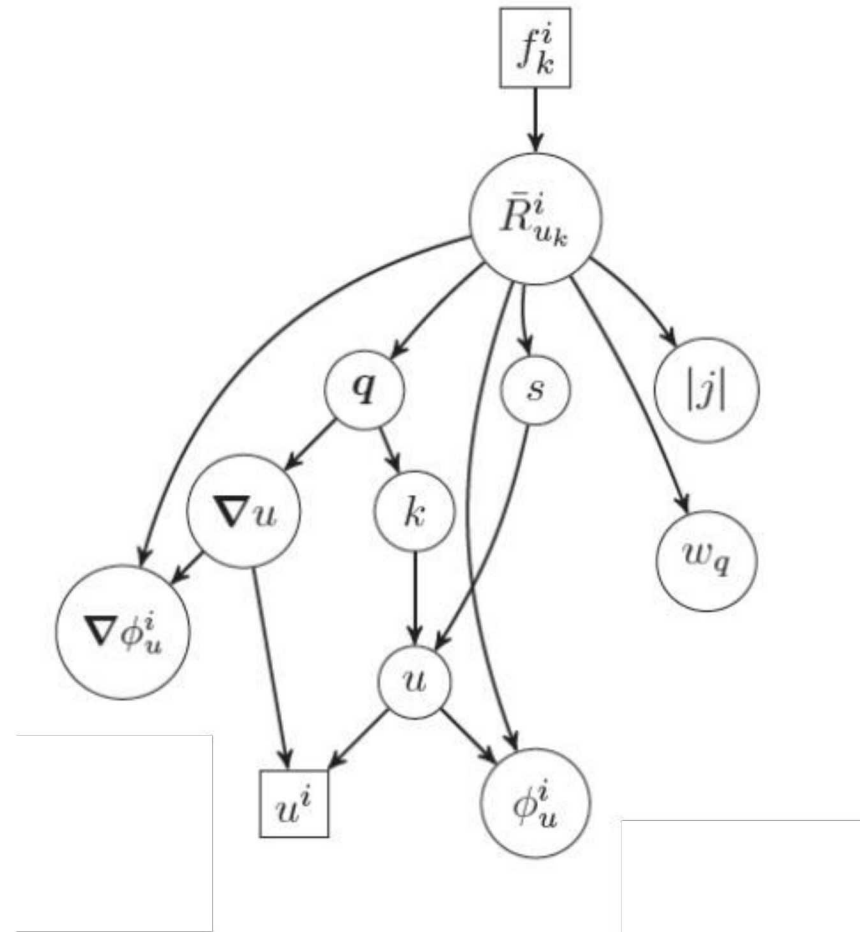
3. Graph-based finite element assembly (FEA)

Assembly of physics pieces comes down to the evaluation of a **directed acyclic graph (DAG)** of computations of field data.

Phalanx package: Local field evaluation kernel designed for assembly of arbitrary equation sets (i.e. evaluating residuals/Jacobians).

- **Decomposes** a complex model into a graph of **simple kernels** (functors)
- A node in the graph evaluates one or more **temporary fields**
- **Runtime** DAG construction of graph
- Achieves **flexible multi-physics assembly**

$$R_u^i = \int_{\Omega} [\phi_u^i \dot{u} - \nabla \phi_u^i \cdot \mathbf{q} + \phi_u^i s] \, d\Omega$$



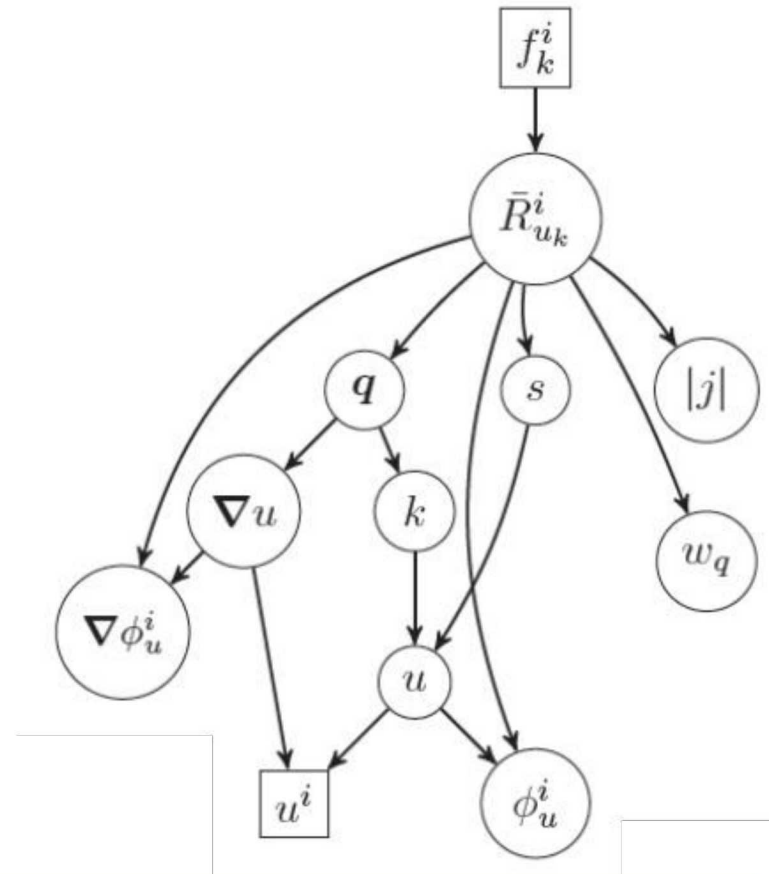
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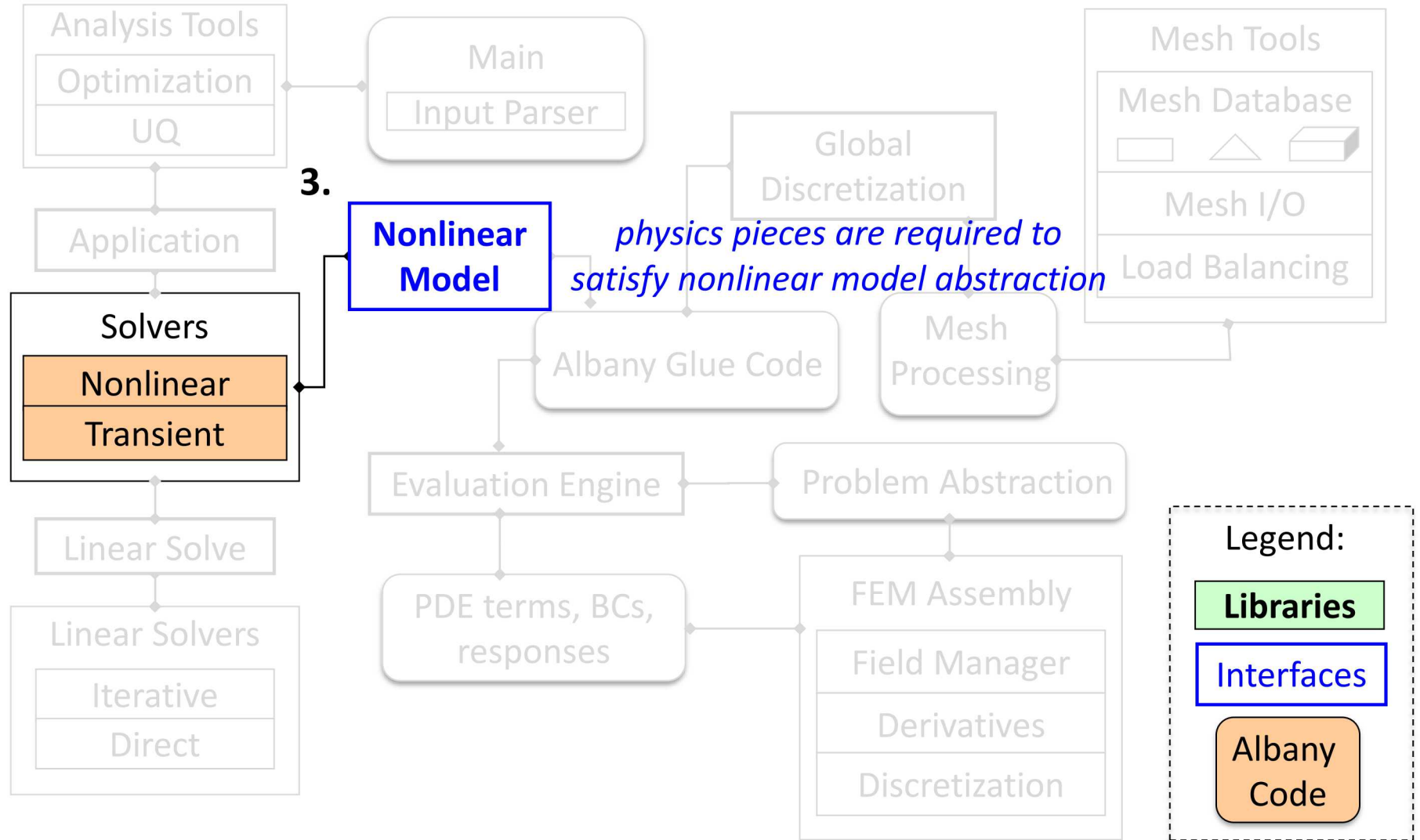
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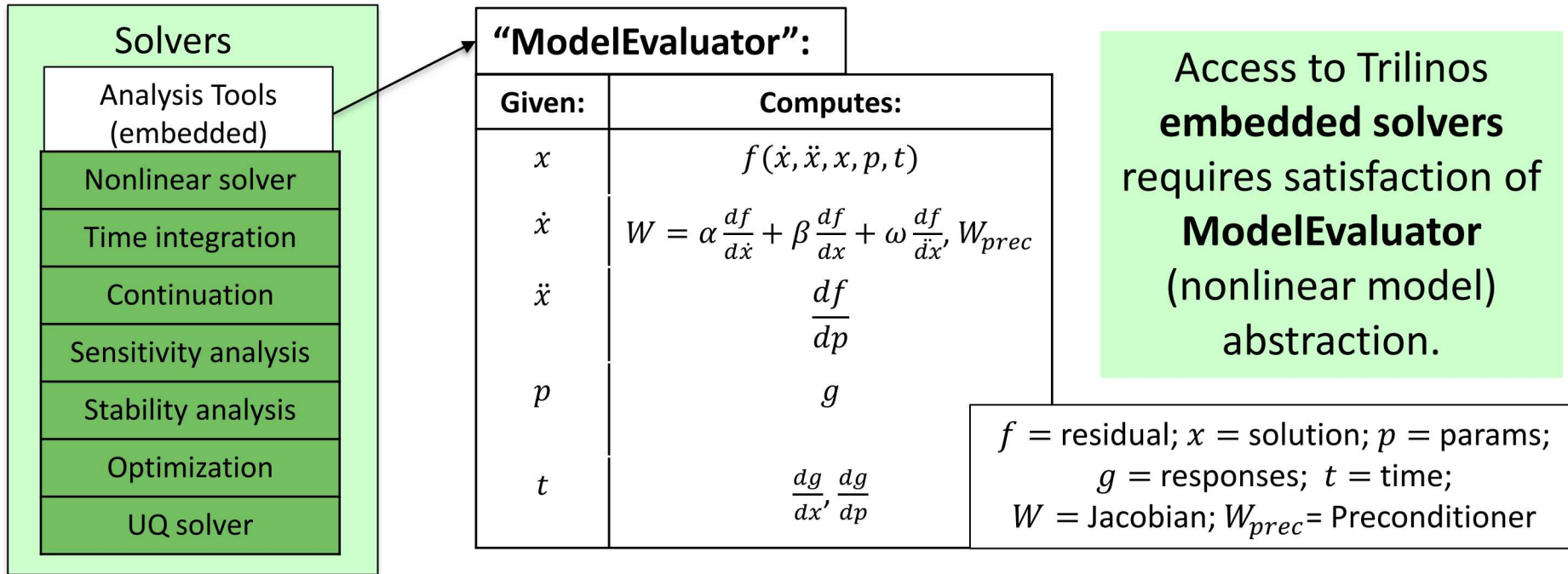
DAG-based assembly enables **flexibility, extensibility, rapid development:** to add new PDE, all you need to code is problem-specific residual R_u^i !

What is Albany? (under-the-hood)

Albany = Component Libraries + Abstract Interfaces + “Glue Code”



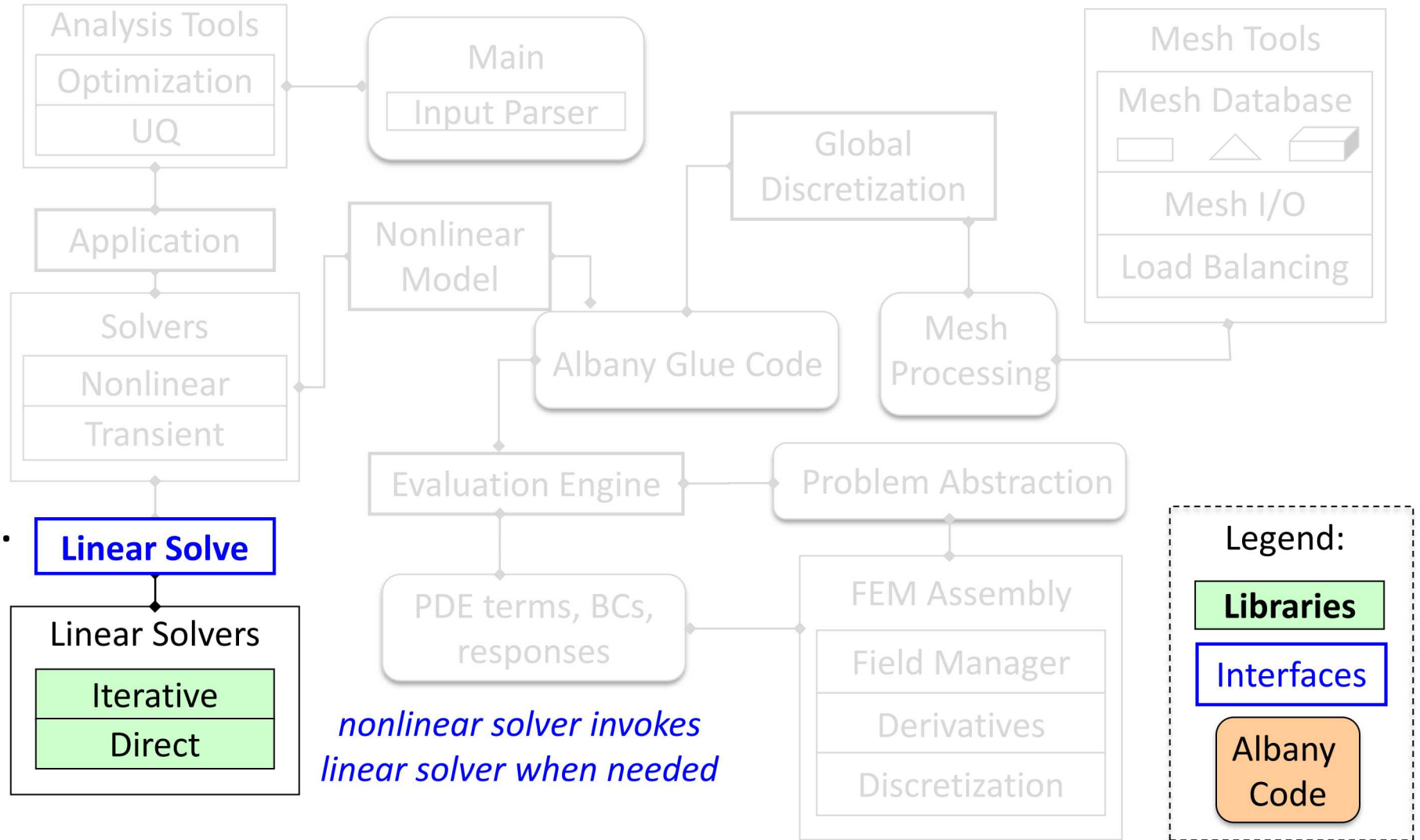
Nonlinear model abstraction & libraries



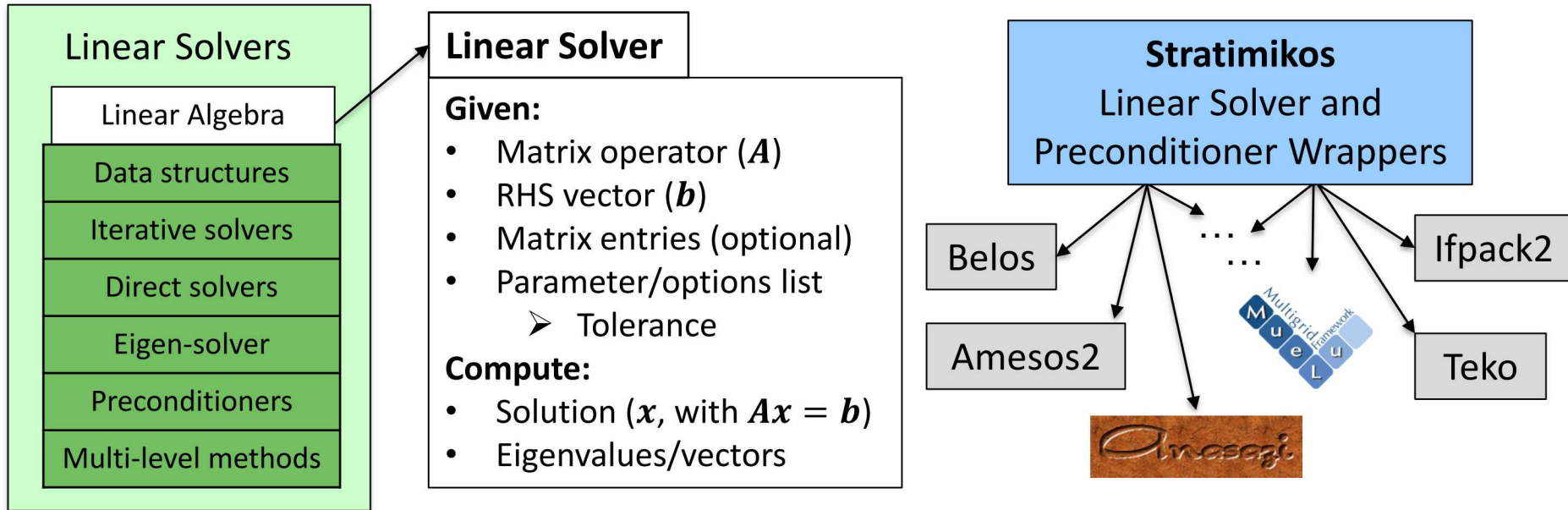
- Interface is **general** to accommodate computation of Jacobians, user-defined preconditioners, and stochastic Galerkin expansions.
- Enables “**beyond-forward analysis**”: analysts/physics experts are not burdened with analysis algorithm requirements, i.e., programming sensitivities for implicit solvers, optimization, stability, bifurcation analysis.
 - **Advanced capabilities**: optimization (ROL), homotopy continuation (LOCA), embedded UQ (Stokhos).

What is Albany? (under-the-hood)

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Linear solver abstraction & libraries



- **Linear solver abstraction** provides full access to all Trilinos linear solvers (direct and iterative), eigensolvers and preconditioners through Stratimikos interface.
- **Factory class** supports run-time solution configuration through input file options.
- **Available direct solvers**: Amesos, Amesos2 (UMFPACK, MUMPS, SuperLU, SCALAPACK, etc.).
- **Available iterative solvers**: AztecOO, Belos (CG, GMRES)
- **Available preconditioners**: Ifpack, Ifpack2 (ILU); ML, MueLu (AMG); Teko (block)
- **Eigensolvers**: Anasazi

Software quality tools & processes



Repository*	Nightly test harness	Mailing lists
Version control	Unit tests	Issue tracking
Build system	Verification tests	Web pages
Config mgmt	Code coverage	Licensing
Regression tests	Performance tests	Release process

Performance monitored via
CDash nightly testing on a
 variety of architecture including
 GPU (P100, V100), Xeon Phi,
 Skylake, ARM platforms.

<div> Login All Dashboards </div> <div> <div> Albany </div> <div> Dashboard Calendar Previous Current Next Project </div> </div>									
Project									
Project	Error	Configure Warning	Pass	Error	Build Warning	Pass	Test		
Albany	0	18	24	1	20	4	Not Run	Fail	Pass
							0	6	3201
SubProjects									
Project	Error	Configure Warning	Pass	Error	Build Warning	Pass	Not Run	Fail	Pass
Peridigm	0	0	1	1	1	0			
TrilinosIntel	0	1	1	0	1	0			
AlbanyIntel	0	0	1	0	0	1	0	1	347
IKTCismAlbany	0	1	1	0	1	0	0	0	5
IKTCismAlbanyEpetra	0	1	1	0	1	0	0	0	5
IKTAIbanyFunctorOpenMP	0	1	1	0	1	0	0	0	278
Trilinos	0	1	1	0	1	0			
TrilinosClang	0	1	1	0	1	0			
Albany64BitClang	0	0	1	0	1	0	0	1	166
IKTRideTrilinosCUDA	0	1	1	0	1	0			
IKTRideAlbanyCUDA	0	2	2	0	2	0	0	2	186
albany_cluster-toss3_skybridge-login5_serial-intel-release	0	1	1	0	0	1	0	1	288
Albany64Bit	0	0	1	0	1	0	0	1	317
IKTAIbany	0	1	1	0	1	0	0	0	372
IKTAIbanyNoEpetra	0	1	1	0	1	0	0	0	261
TrilinosDbg	0	1	1	0	1	0			
Albany64BitDbg	0	0	1	0	0	1	0	0	225
trilinos_cluster-toss3_skybridge-login5_serial-intel-release	0	1	1	0	1	0			
IKTMayerARMTTrilinos	0	1	1	0	1	0			
IKTMayerARMTAlbany	0	0	1	0	0	1	0	0	294
IKTWatmanTrilinosCUDA	0	1	1	0	1	0			
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IKTAIbanyFPECheckDbg	0	1	1	0	1	0	0	0	363

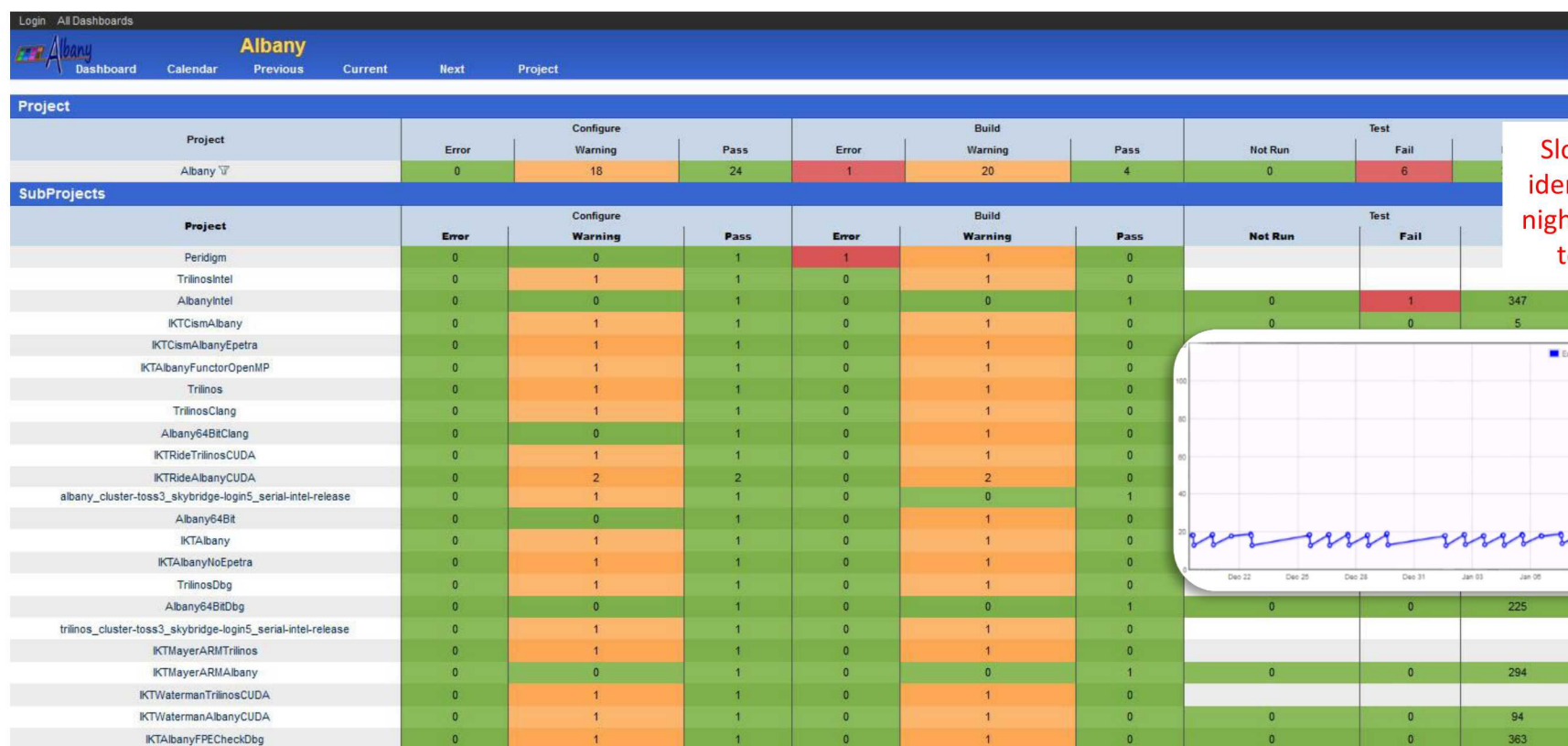
* Albany github repo: <https://github.com/SNLComputation/Albany>.

Software quality tools & processes



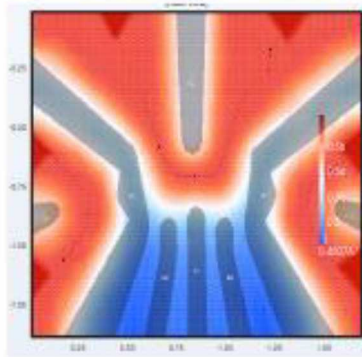
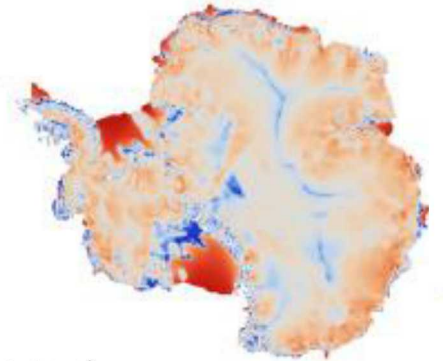
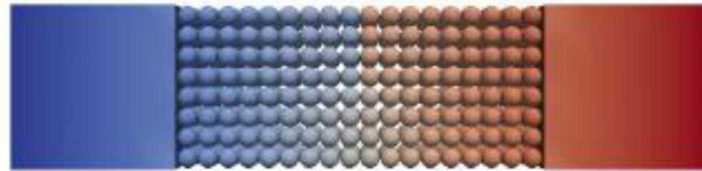
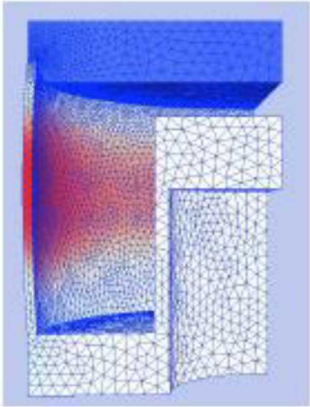
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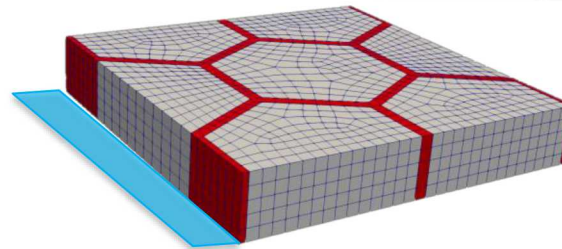
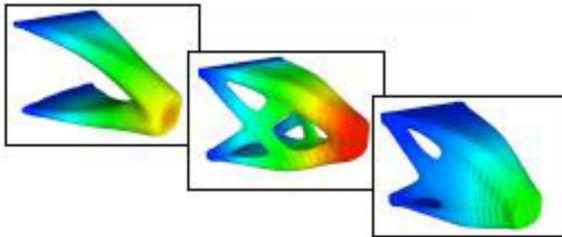
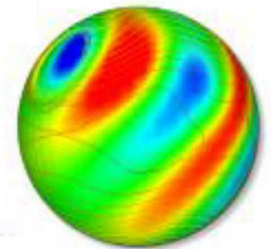


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Applications hosted by Albany



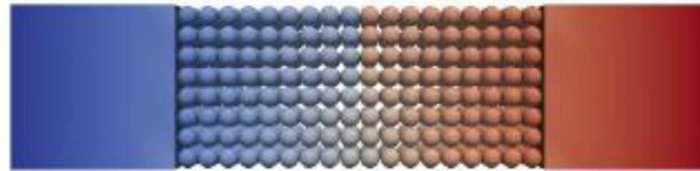
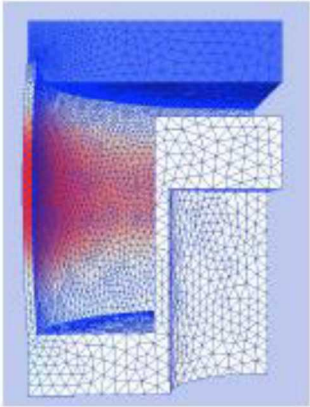
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- Ice Sheets (Albany Land-Ice)
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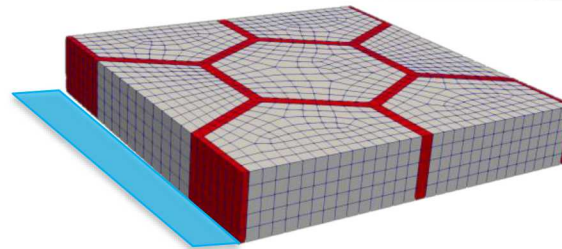
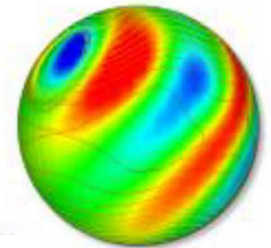
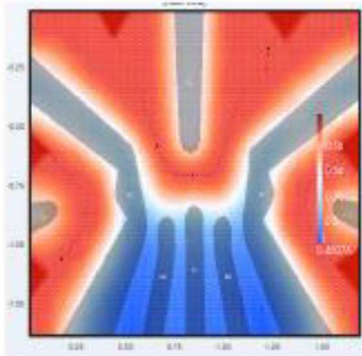
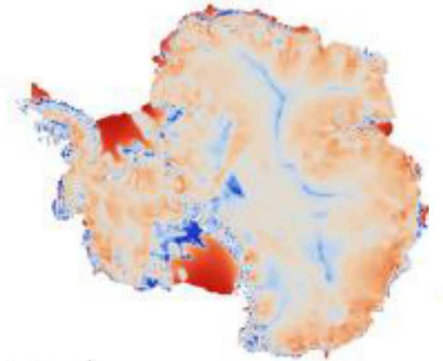
Blue: under active
development

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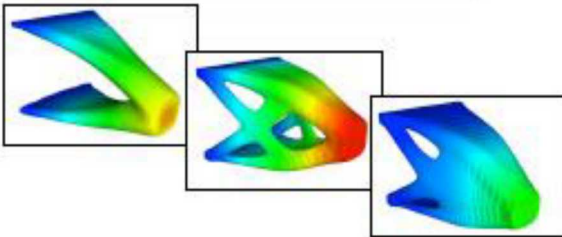
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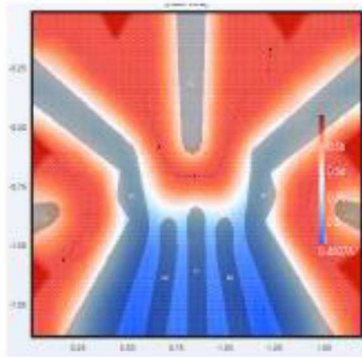
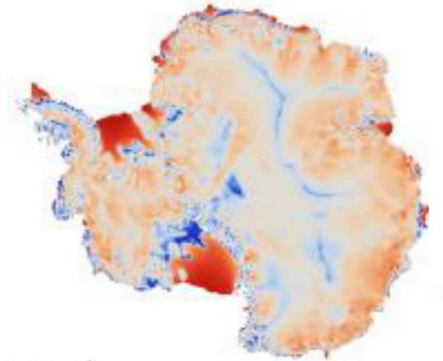
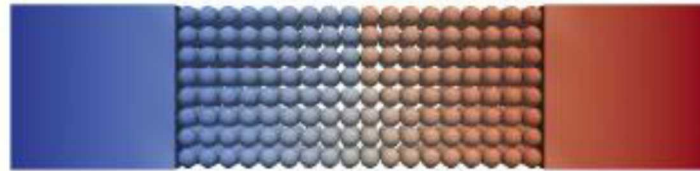
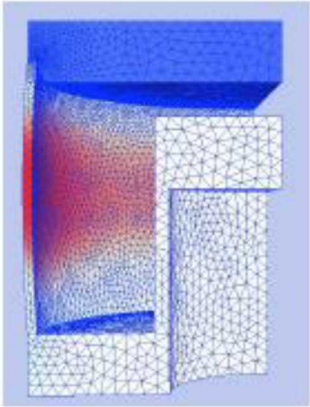


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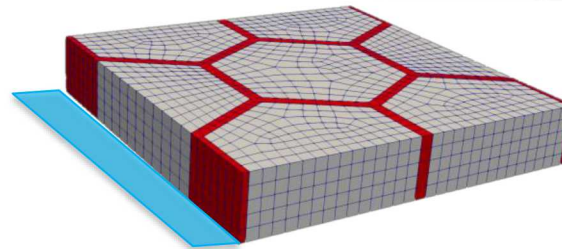
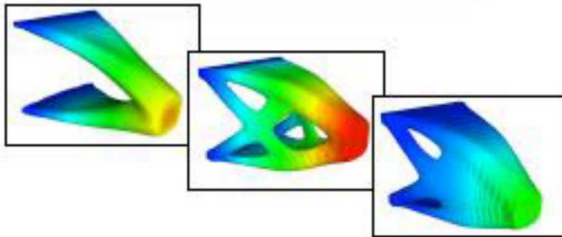
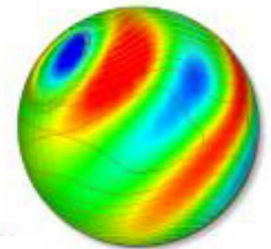


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Algorithmic projects hosted by Albany

Algorithms and software are matured directly on applications.

Algorithmic projects within Albany:

- Scalable multi-level solvers (PISCEES/ProSPect) – R. Tuminaro, I. Tezaur.
- Nonlinear solvers (FASTMath) – R. Pawlowski, M. Perego
- In-memory mesh adaptation (FASTMath) – M. Sheppard, M. Bloomfield (RPI), A. Oberai, J. Smith (USC), D. Ibanez, B. Granzow, G. Hansen
- Multi-scale coupling via Schwarz (P&EM) – A. Mota, I. Tezaur, C. Alleman, G. Phlipot (CalTech)
- Stabilized mechanics (FASTMath) – A. Bradley, J. Ostien, G. Hansen
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- Optimization-based coupling (ASCR) – M. Perego, M. D’Elia, D. Littlewood, P. Bochev
- UQ workflow (PISCEES) – J. Jakeman, I. Tezaur, M. Perego
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- Performance portable FEM (PISCEES/ProSPect/ATDM) – I. Demeshko (LANL), E. Phipps, R. Pawlowski, E. Cyr, I. Tezaur, A. Bradley, J. Watkins
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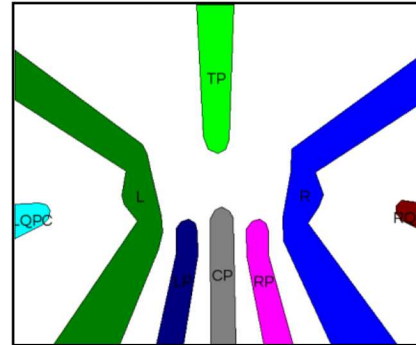
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Quantum device modeling (QCAD)

Albany enabled the rapid stand-up of a world-class **quantum device design tool**.

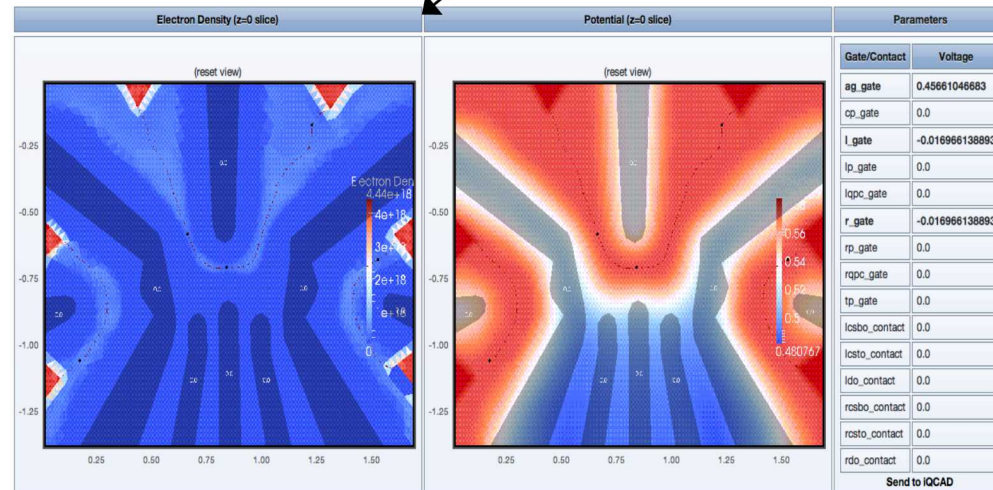
- **Application:** quantum computing
- **Objective:** simulation/optimization of semiconductor quantum double dots
 - Provide fast feedback on which device layouts are most likely to lead to **few-electron** behavior
- **Key to QCAD's success:** interfaces
 - Various **multi-physics couplings** of Poisson + Schrodinger
 - DAKOTA* for **optimization**.
- QCAD is used by experimentalist in Sandia's **world-class experimental facilities (CINT)** as design tool for quantum **device fabrication**

QCAD least squares optimization Run



QCAD = "Quantum Computer Aided Design"

1. Solid Model
2. GUI



Capacitances (in aF)

X. Gao, et al., J. Appl. Phys. 2013

	AG	CP	L	LP	LQPC	R	RP	RQPC	TP
Left dot electrons	11.3395131644	1.9579675685	4.3250030564	1.42889427277	0.0609931170611	1.12872609211	0.709234221893	0.0288086239542	3.59196174454
Right dot electrons	12.9310981401	2.29560838582	1.31135293202	0.812287188824	0.0392736392797	4.61207359466	1.61977770795	0.054532655725	3.3402953333

Ice sheets: Albany Land-Ice (ALI)

Albany enabled the **rapid development** of a production **land-ice dycore** for providing **actionable predictions** of **21st century sea-level rise** as a part of the DOE Energy Exascale Earth System Model (E3SM).

Capabilities:

- **Unstructured grid** finite elements.
- **Scalable, fast** and **robust**
- **Verified** and **validated**.
- **Advanced analysis:** inversion, UQ.
- **Portable** to new/emerging architecture machines (multi-core, many-core, GPU)
- **Multi-physics:** velocity-temperature, velocity-thickness, velocity-hydrology.

**MS121: Theoretical & Computational Advancements
in Ice Sheet Modeling (Tues. Feb. 26)**

Ice sheet modeling of Greenland, Antarctica helps predict sea-level rise

Michael Padilla

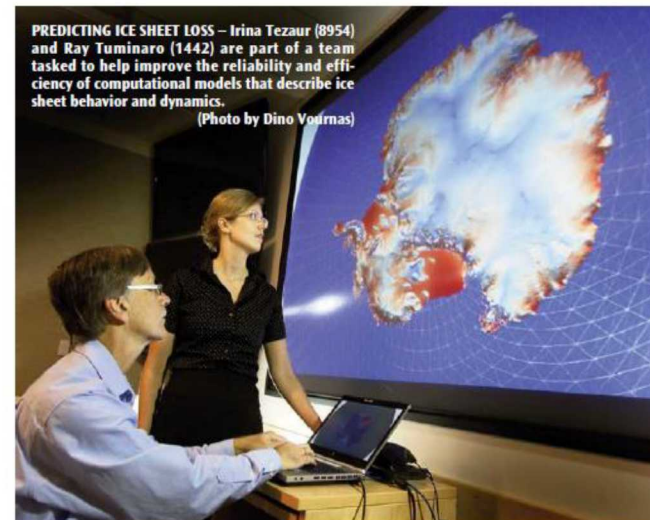
The Greenland and Antarctic ice sheets will make a dominant contribution to 21st century sea-level rise if current climate trends continue. However, predicting the expected loss

Computing (SciDAC) program. PISCEES is a multi-lab, multi-university endeavor that includes researchers from Sandia, Los Alamos, Lawrence Berkeley, and Oak Ridge national laboratories; the Massachusetts Institute of Technology; Florida State University; the University of Bristol; the University of

Texas Austin; the University of South Carolina; and New York University.

Sandia's biggest contribution to PISCEES has been an analysis tool: a land-ice solver called Albany/FELIX (Finite Elements for Land Ice eXperiments). The tool is based on equations that simulate ice flow over the Greenland and Antarctic ice sheets and is being coupled to Earth models through the Accelerated Climate for Energy (ACME) project.

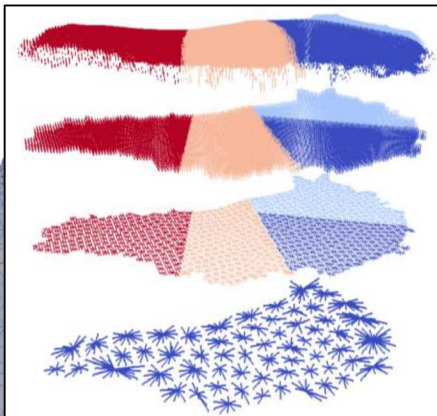
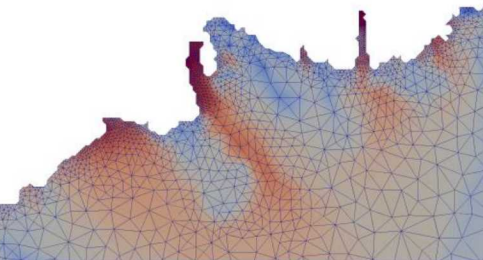
"One of the goals of PISCEES is to create a land-ice solver that is scalable, fast, and robust on continental scales," says computational scientist Irina Tezaur, a lead developer of Albany/FELIX. Not only did the new solver need to be reliable and efficient, but it was critical



PREDICTING ICE SHEET LOSS – Irina Tezaur (B954) and Ray Tuminaro (1442) are part of a team tasked to help improve the reliability and efficiency of computational models that describe ice sheet behavior and dynamics.
(Photo by Dino Vofrnas)

of ice sheet mass is difficult due to the complexity of modeling ice sheet behavior.

that the team develop a solver capable of running on new and emerging computers, and equipped with advanced



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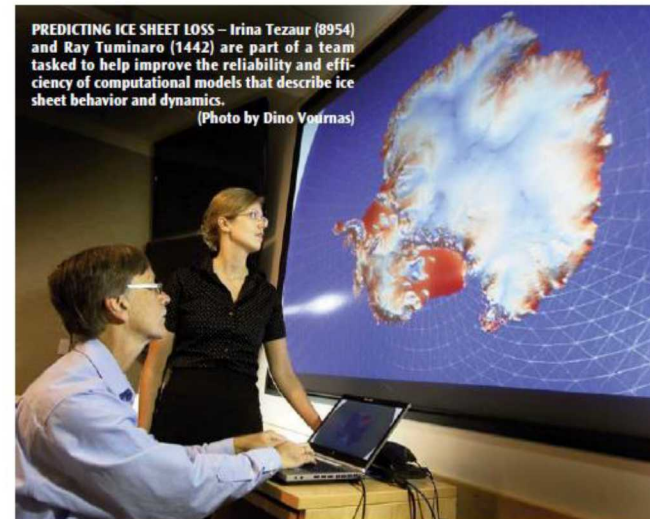
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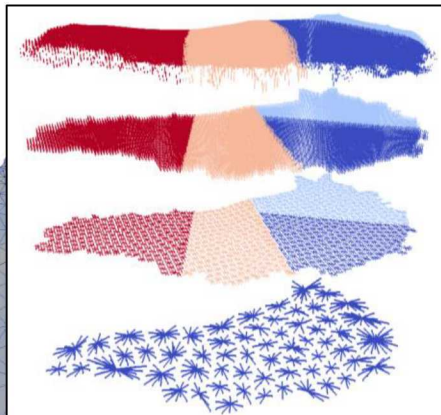
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Adjoint-based optimization/inversion



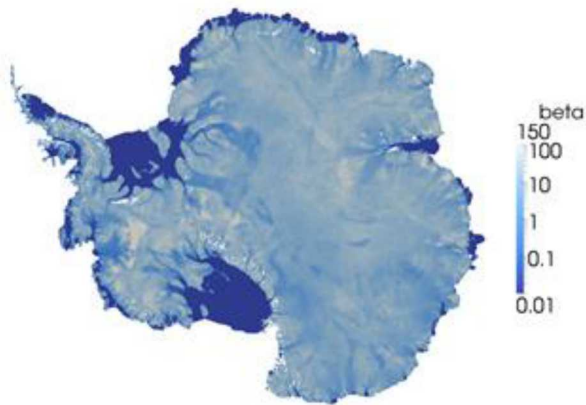
AD & TBGP in Albany enabled the efficient solution of **adjoint-based PDE-constrained optimization/inversion** problems.

Find p that minimizes $g(u, p)$
subject to $f(u, p) = 0 \leftarrow$ PDE

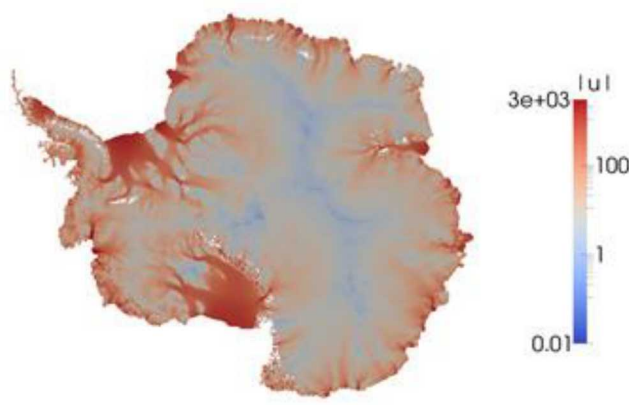
Inversion problem solved robustly for **$O(100K)$ parameters!**

Application: inversion for basal friction and ice thickness in Albany Land-Ice model to initialize dynamic simulation.

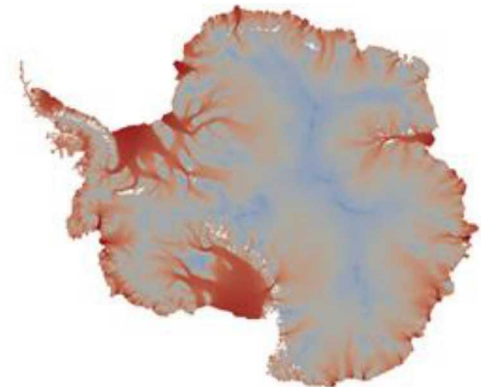
➤ Inversion approach **significantly reduces non-physical transients.**



β (kPa y/m) obtained through inversion



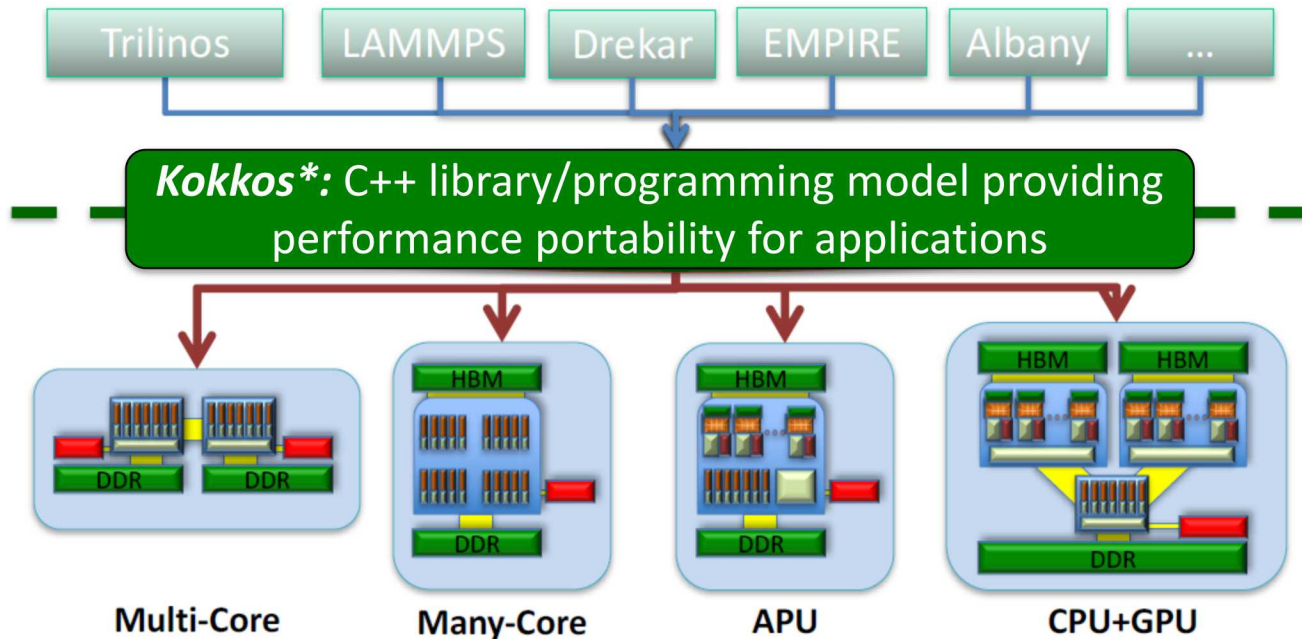
$|u|$ (m/yr) computed with estimated β



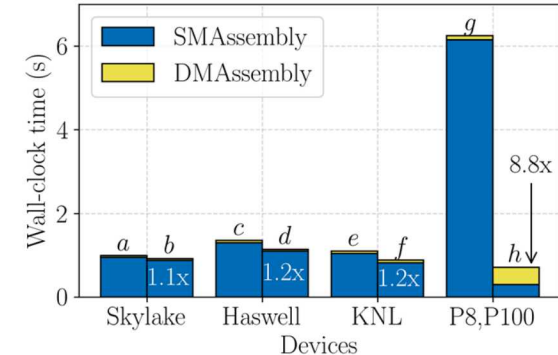
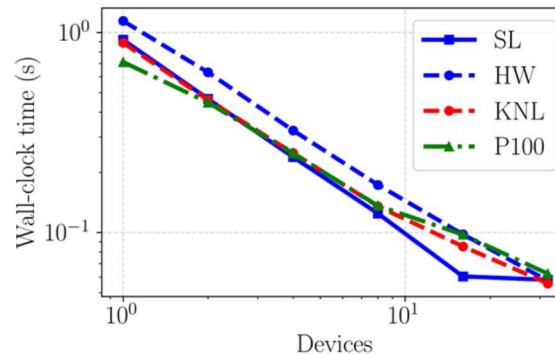
$|u|$ (m/yr) for observed surface velocity

Performance-portable FEM

Talk by J. Watkins,
MS 121, Tues. Feb. 26



- Provides **automatic access** to OpenMP, CUDA, etc.
- Abstracts **data layouts** for optimal performance

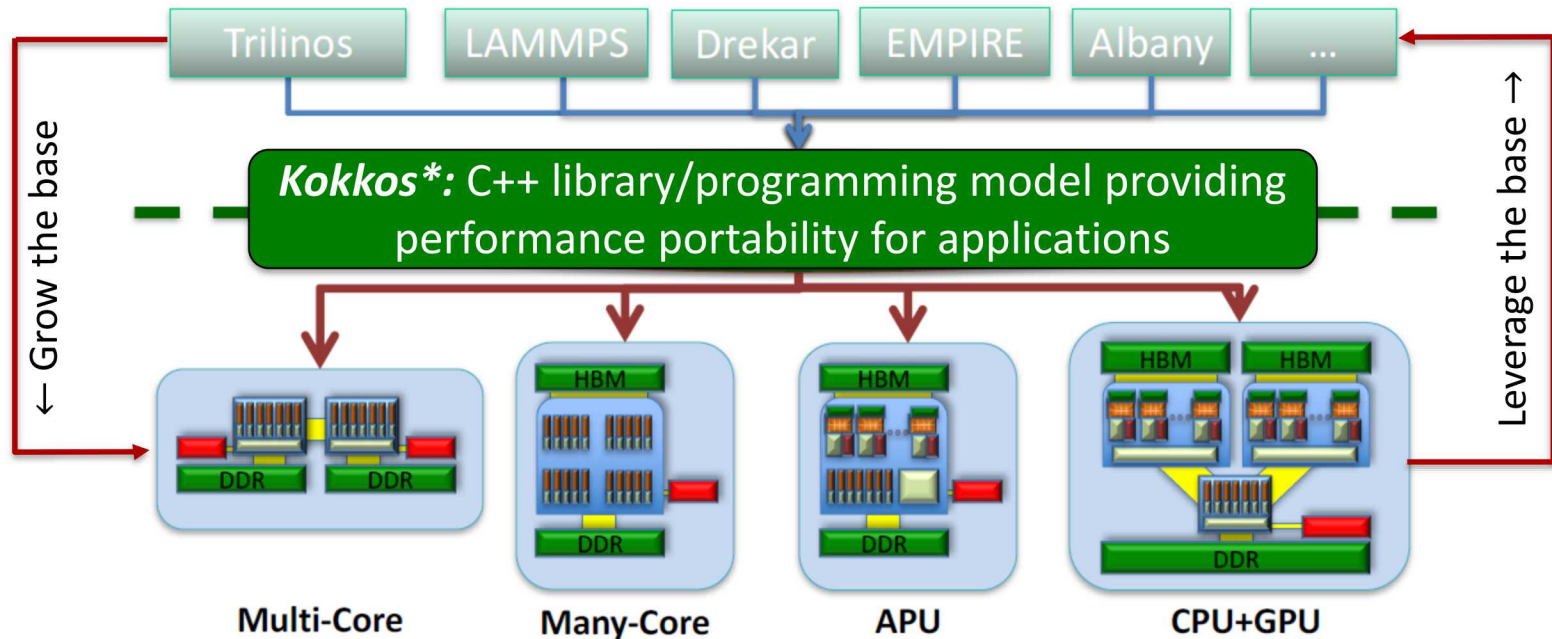


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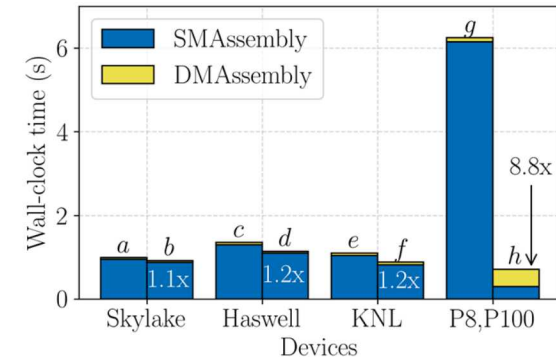
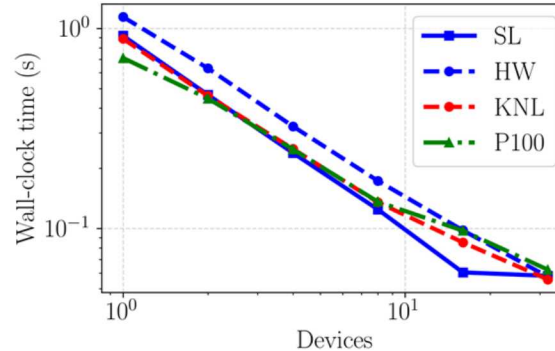
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Performance-portability of Albany FEA achieved using *Kokkos*;
Albany usage has in turn led to *Kokkos improvements*

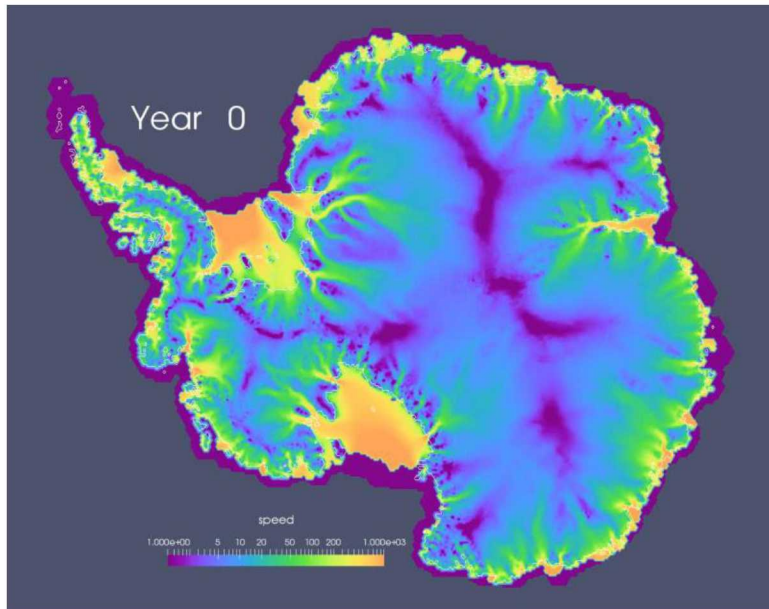


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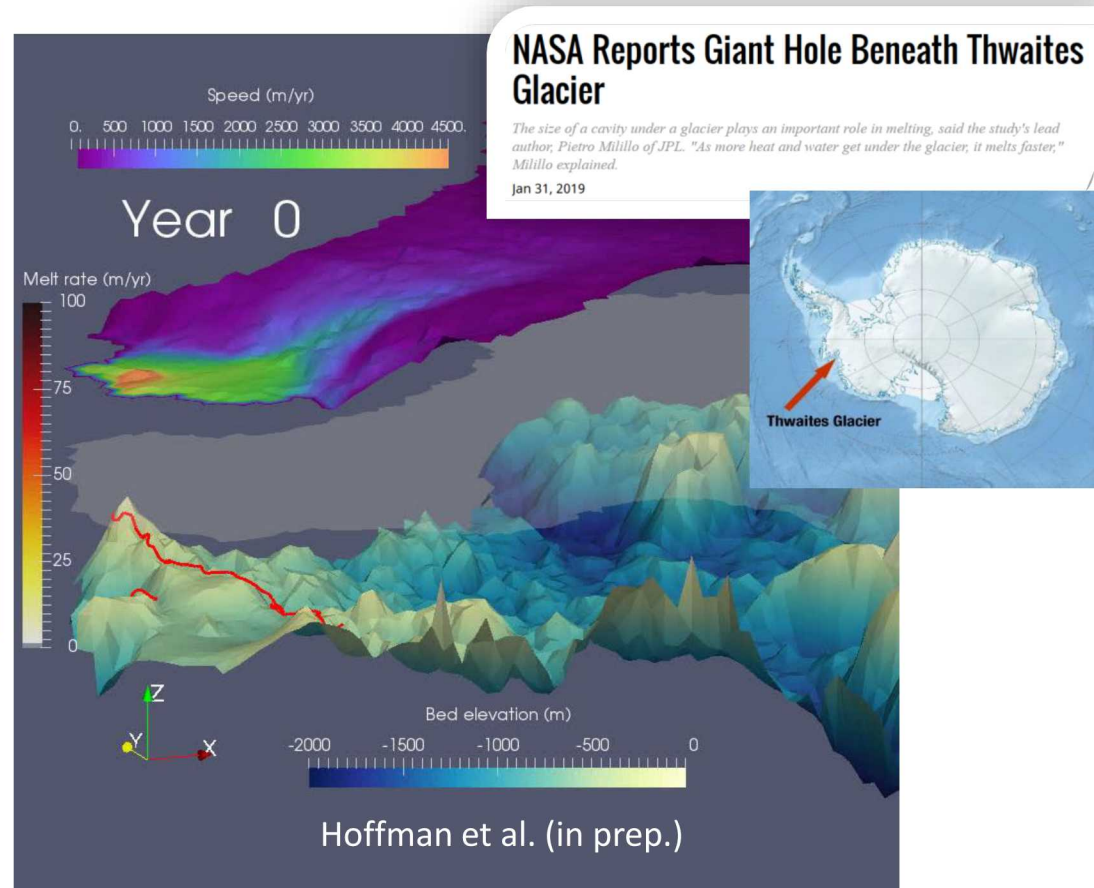


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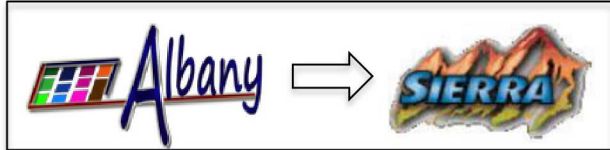


Above: ABUMIP-Antarctica experiment
Right: Thwaites glacier retreat under parametrized submarine melting.

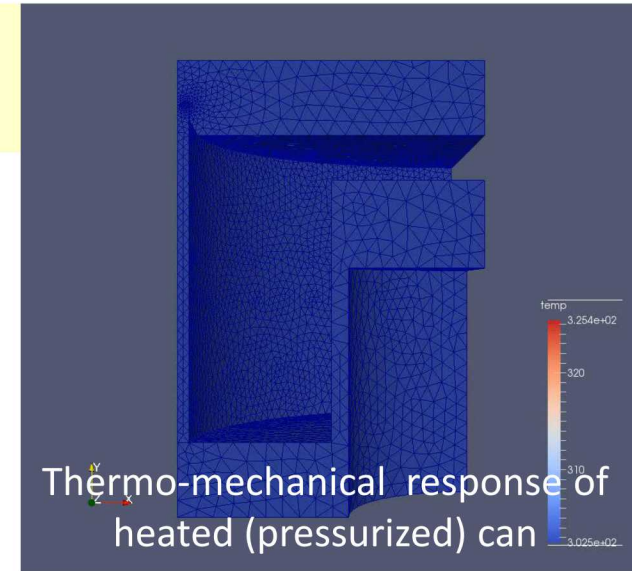


Laboratory for computational mechanics (LCM) Sandia National Laboratories

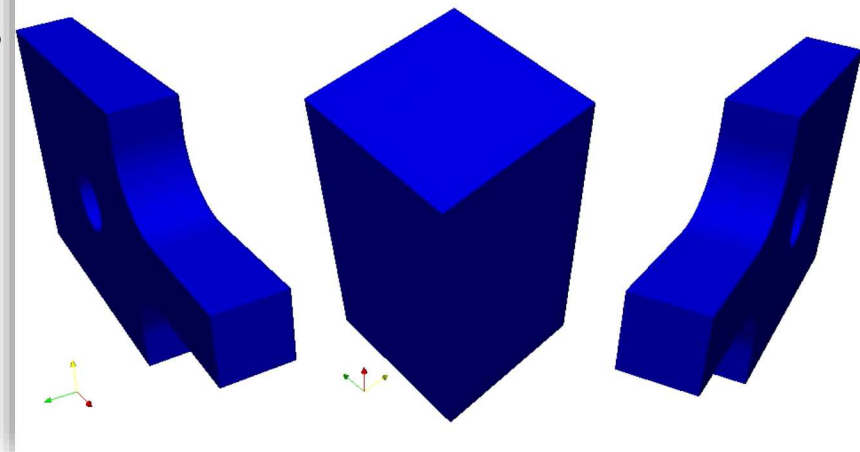
The Albany LCM suite contains sophisticated **material models**, **physics** and **technologies** for solid mechanics.



- **Models:** elasticity, Neohookean, J_2 plasticity, crystal plasticity, creep, elasto-visco-plastic, ...
- **Physics (PDEs):** mechanics, electro-mechanics, thermo-mechanics, unsaturated poro-elasticity, thermo-poro-mechanics, ...
- **Fracture and damage** simulation capabilities
- **“Sand-box”** for new algorithms/methods:
 - Composite 10-node tetrahedron
 - Pressure projection stabilization
 - Multi-scale coupling via Schwarz
 - In-memory mesh adaptation

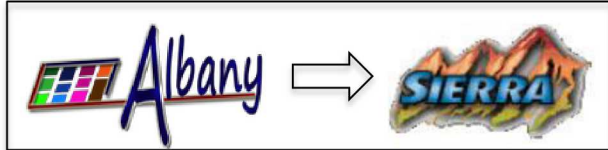


Tensile specimen with micro-structure in the middle

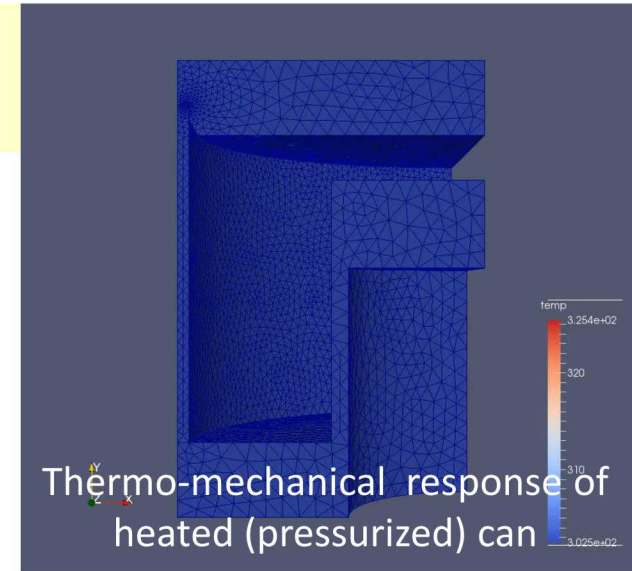


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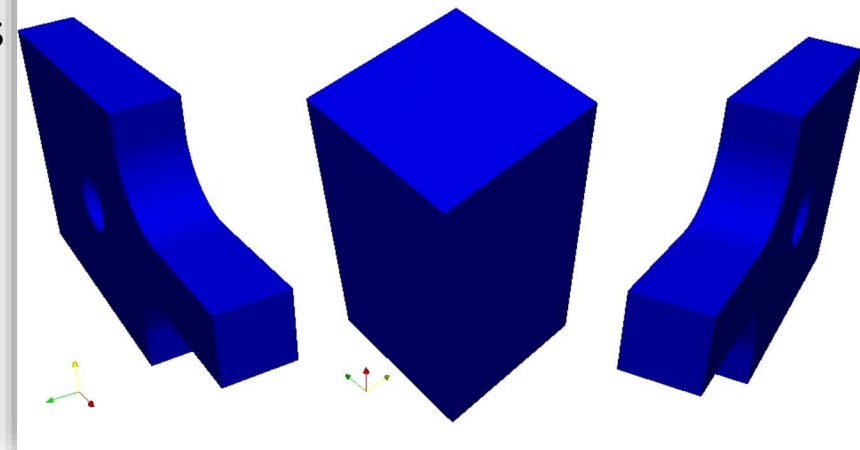
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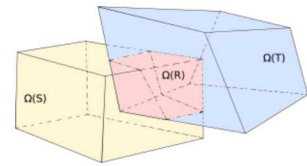
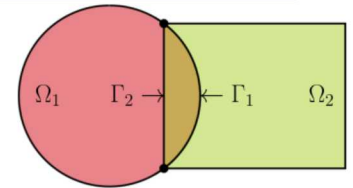
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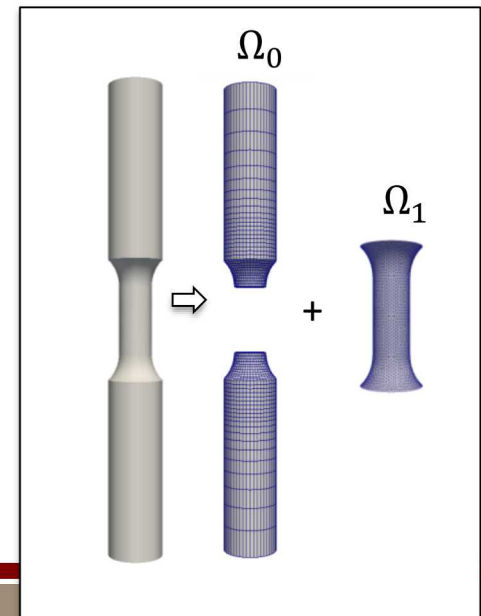
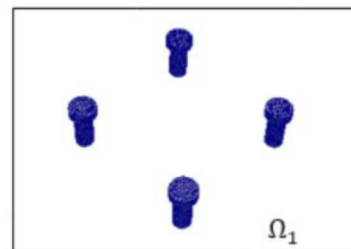
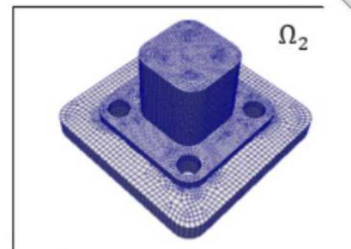
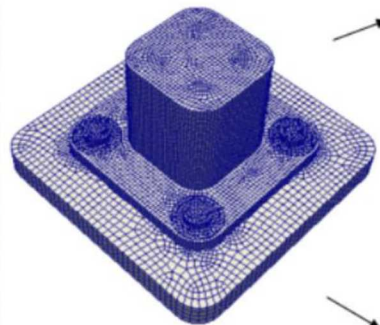
Multi-scale coupling via Schwarz

A **domain decomposition alternating-Schwarz**-based method has been developed in Albany for **concurrent multi-scale coupling** in solid mechanics.

- **Crux of Method**: use solutions in simple domains to iteratively build a solution for the more complex domain.
- **Targeted application**: failure of **bolted components**.
- **“Plug-and-play” framework**: simplifies meshing complex geometries!
 ➤ Couple regions with **different non-conformal meshes, element types, levels of refinement, solvers/time-integrators**.



<https://github.com/ORNLCES/DataTransferKit>



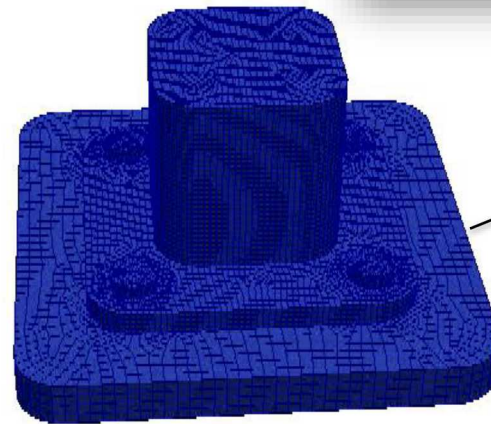
Multi-scale coupling via Schwarz

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See talk by A. Mota: MS 350, Fri. Mar. 1,
10:10-10:30AM, Room 302B



Single domain



Schwarz coupling of hex (parts) +
composite tet 10 (bolts) elements
(J_2 material model from LCM suite)



Future work:
extend method
for **multi-physics**
coupling

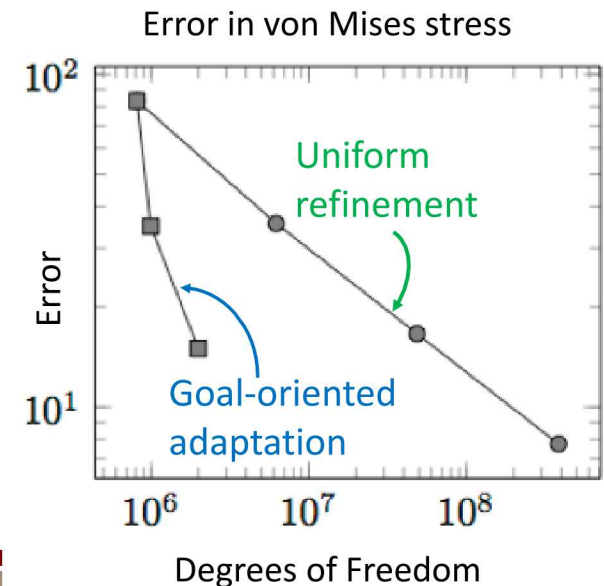
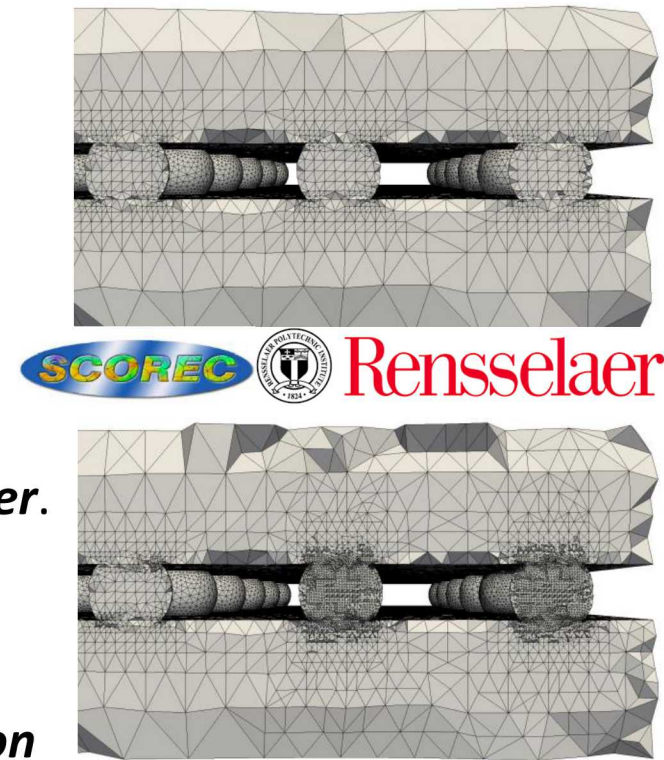
In-memory mesh adaptation

Collaboration with **SCOREC***: development of **mesh adaptation** capabilities in Albany to enable **multi-scale/multi-physics adaptive simulation**

PAALS (Parallel Albany Adaptive Loop with SCOREC)

- Fully-coupled *in-memory adaptation, solution transfer*.
- *Parallel mesh infrastructure* and services via **PUMI**.
- *Dynamic load balancing* (ParMetis/Zoltan, ParMA).
- Automated *parallel goal-oriented adaptive simulation*
 - Use **adjoint solution** to drive mesh adaptation
 - ~100× DoF-efficiency observed
 - Scaling out to at least 8K MPI ranks
- *Performance portability* to GPUs via **Kokkos**.
- *Applications*: 3D manufacturing, creep/plasticity in large solder joint arrays, coupled dislocation dynamics (Albany + ParaDis), ...

PUMI
Parallel Unstructured Mesh Infrastructure



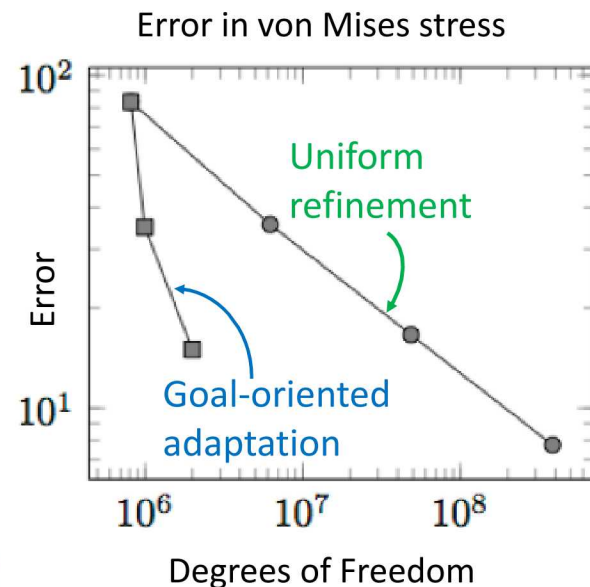
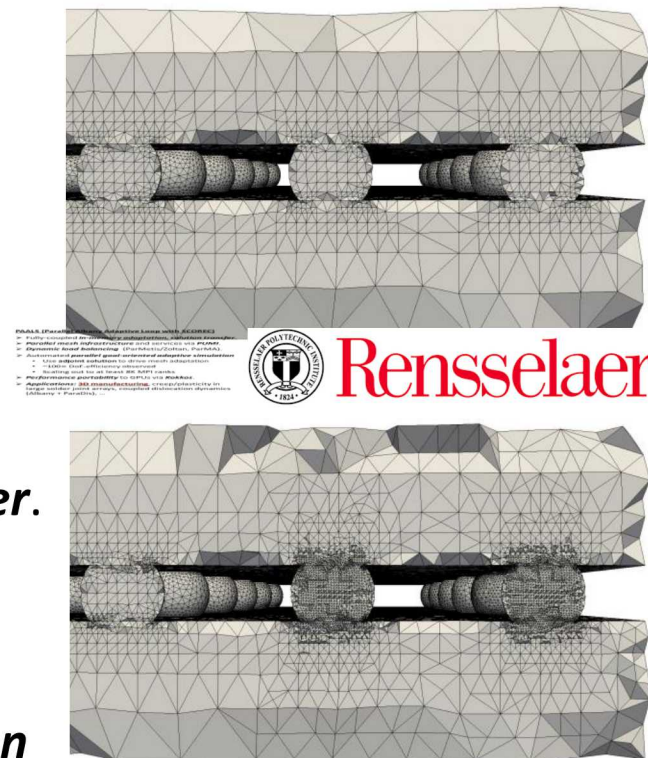
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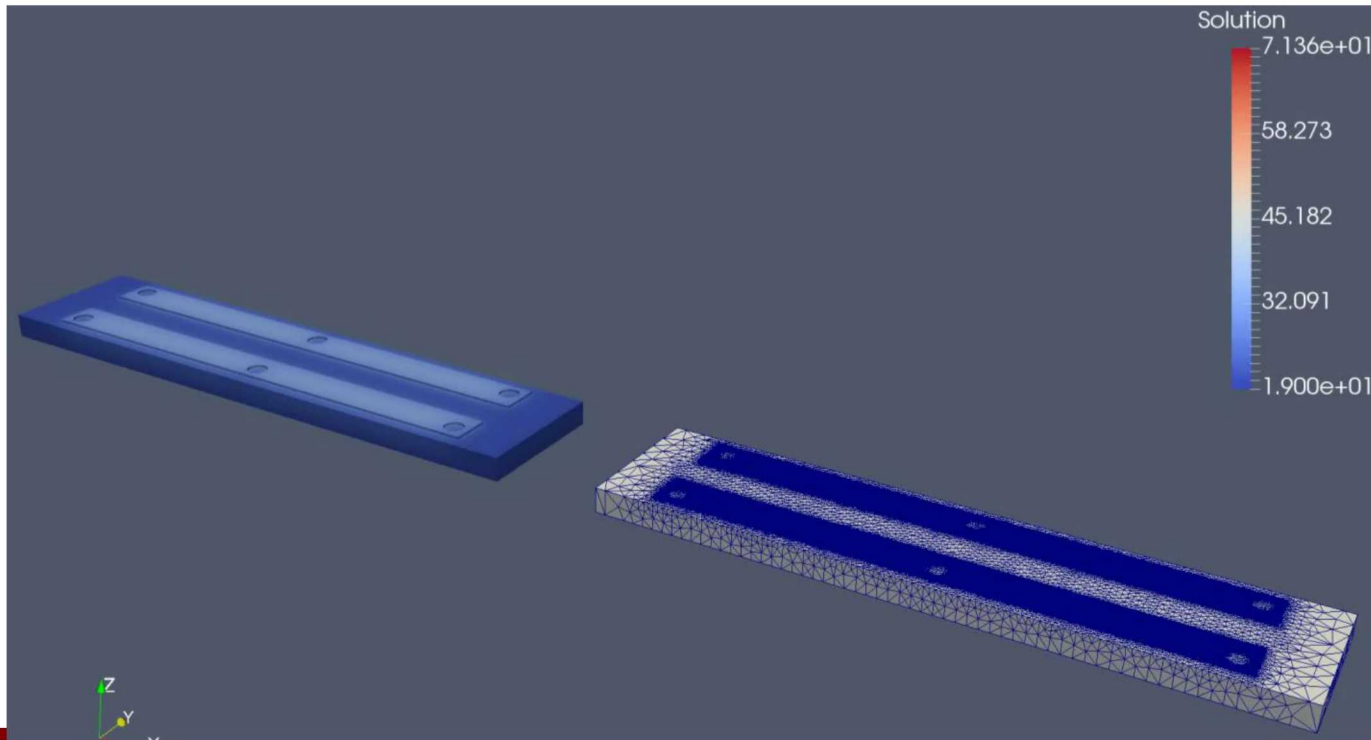
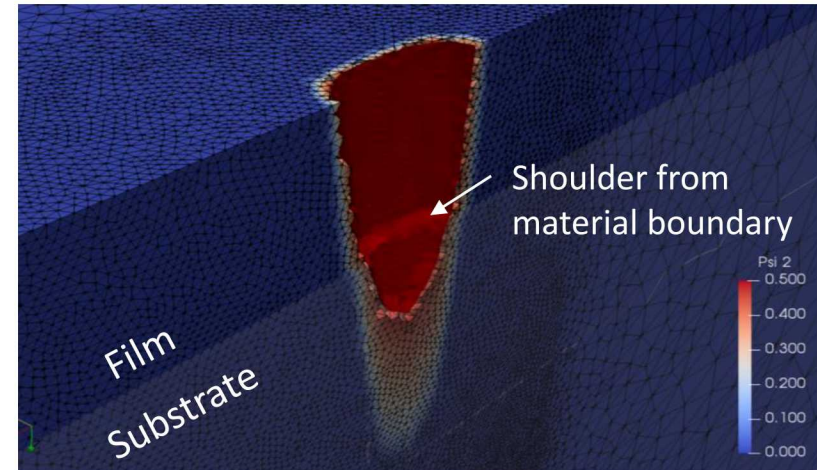
PUMI
Parallel Unstructured Mesh Infrastructure



3D manufacturing

- **Additive & subtractive** capabilities
- Employs **advanced adaptive meshing** and **evolving geometries**
- Coupling with **feedback control**

Right: simulation of subtractive manufacturing with picosecond laser*



Left: Additive manufacturing simulation showing temperature in evolving geometry

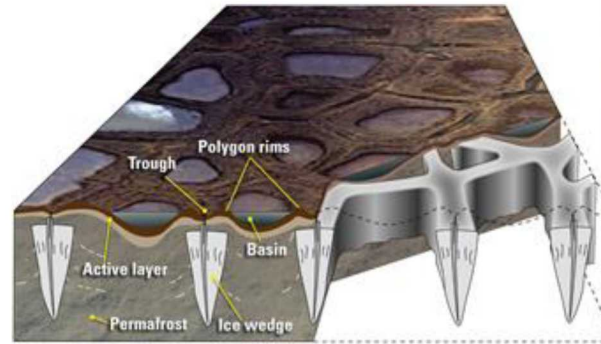
* Maniatty, et al., *Comp. Mech.*, 62:273, 2018.

Arctic Coastal Erosion (ACE)

Mechanistic modeling within Albany is **advancing state-of-the-art coastal erosion/permafrost modeling.**

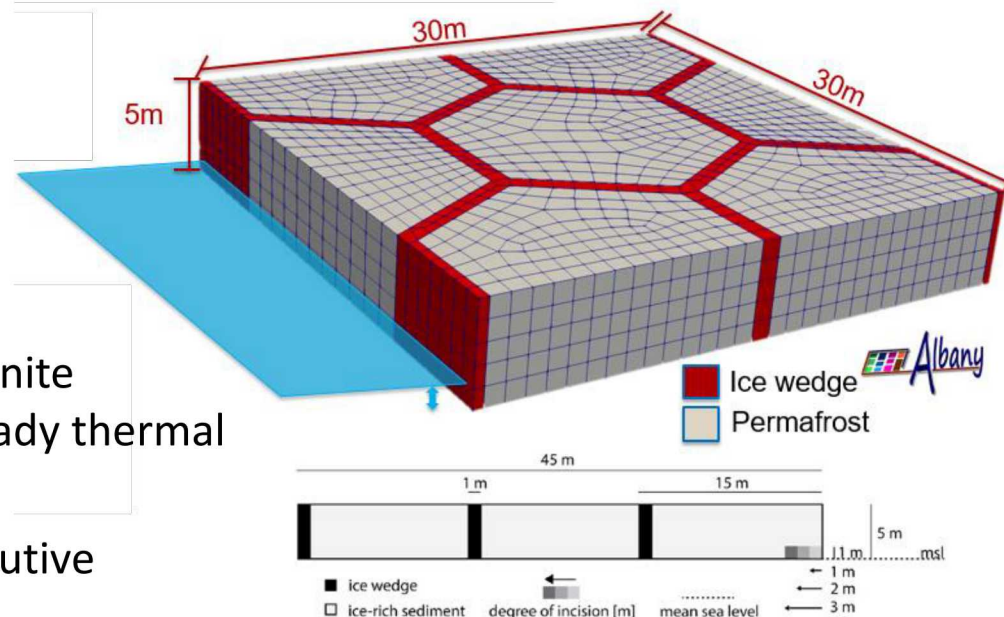
Permafrost modeling background:

- Predominant geomorphology is **ice-wedge polygons** (right).
- **State-of-the-art erosion modeling:** trend projection, empirical relationships, 1D steady-state heat flow, ...



Albany modeling of degradation:

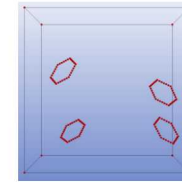
- **Leverages** years of LCM R&D.
- **Time-varying input variables** over the duration of a storm (water level, temperature, salinity)
- **Multi-physics FEM model of coastline:** finite deformation plasticity model + 3D unsteady thermal flow + chemical characteristics
 - **Failure modes** develop from constitutive relationships (**no empirical model!**)



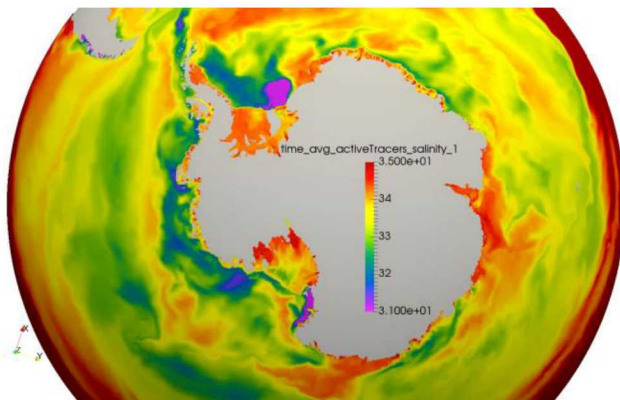
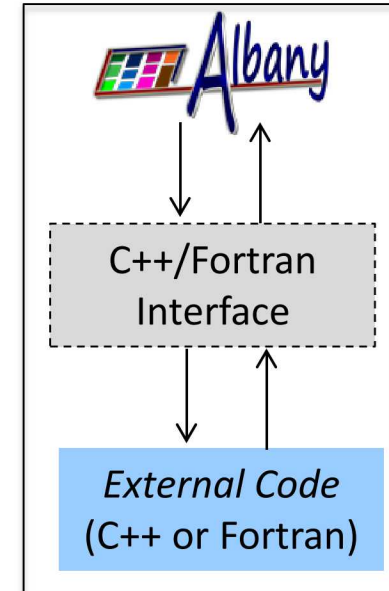
Coupling with other codes

Albany has been **interfaced/coupled** with a number of other codes.

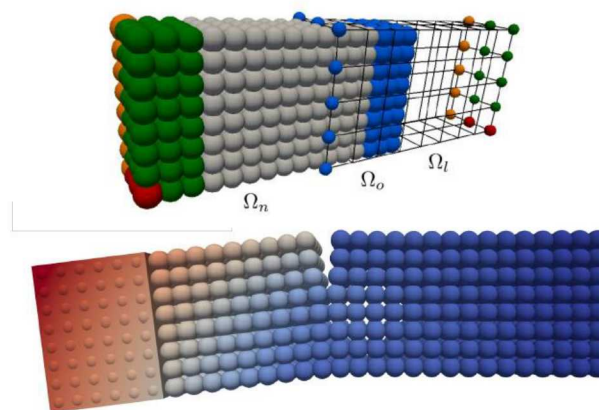
- **Albany-Peridigm**: local-nonlocal coupling of continuum mechanics + peridynamics
- **Albany-ParaDis**: coupled dislocation dynamics.
- **Albany-PLATO**: Advanced Topology Optimization (ATO)
- **MPAS-Albany-Land-Ice (MALI)**: ice sheets/coupling to E3SM
- **CISM-Albany-Land-Ice (CALI)**: ice sheets/coupling to CESM
- **Albany-PFLOTRAN (Albotran)**: coupled geomechanics problems



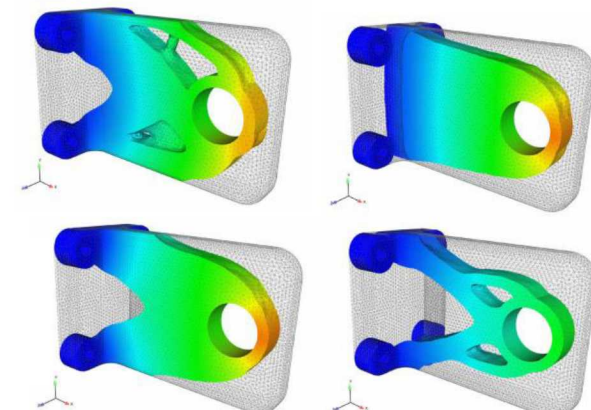
Albany-ParaDis



MPAS-Albany (MALI)



Albany-Peridigm



Albany-PLATO (ATO)

Work in progress

Performance portability:

- **Code optimizations** for finite element assembly
- Performance portable **solvers** [WIP by Trilinos team]



Infrastructure work:

- Refactor of code to use **block data structures** to facilitate **multi-physics** coupling
 - “**Plug-and-play**” different PDEs within Albany
 - Ability to use **block preconditioners** (Teko*)
- Add support for **mixed finite elements**
 - Can be accomplished via incorporation of **Panzer** and **DOFManager**.



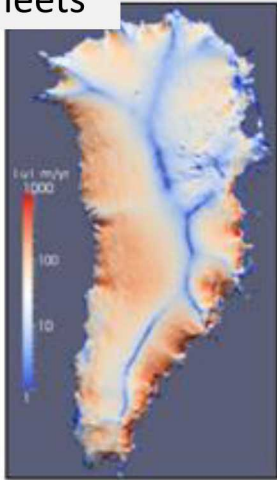
Application-driven development:

- Modeling of structural components in **hypersonic vehicles** with large mechanical and thermal loads (USC).
- Seeking funding for developing **solid-mechanics-based ice fracture/calving models** for improved ice sheet models.
- ***Much more...!***

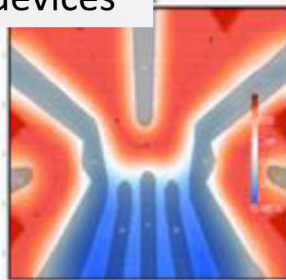
Summary

Albany: open-source, parallel, C++, unstructured-grid, mostly-implicit multi-physics finite element code that demonstrates **AgileComponents** vision and can enable **rapid development** of new physics/algorithms.

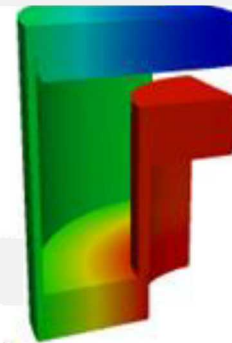
Ice sheets



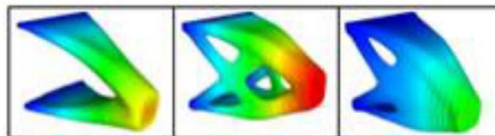
Quantum devices



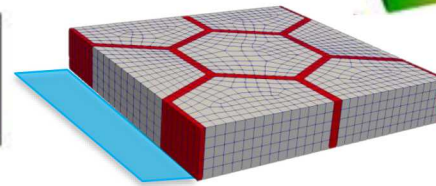
Computational mechanics



Additive manufacturing



Arctic coastal erosion



Github: <https://github.com/SNLComputation/Albany>

Paper: A. Salinger *et al.* "Albany: Using Agile Components to Develop a Flexible, Generic Multiphysics Analysis Code", *IJMCE* 14(4) (2016) 415-438.

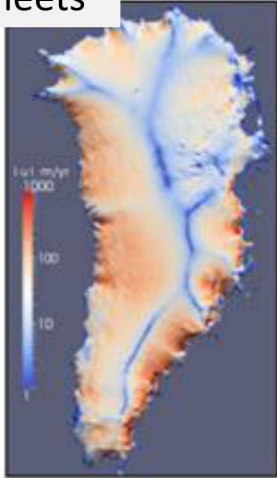
Albany User Meeting (AUM): every ~2 years (TBD)

Summary

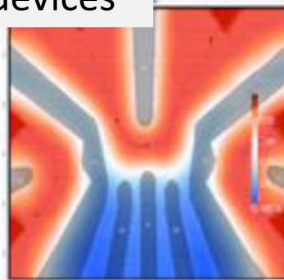
Thank you! Questions?

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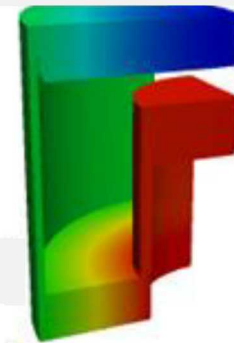
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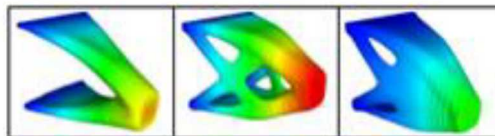
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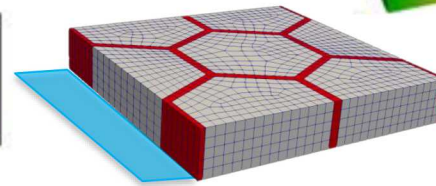
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- [2] M. Heroux *et al.* An overview of the Trilinos project, *ACM Trans. Math. Softw.*, vol. 31, no. 3, pp. 397–423, 2005.
- [3] I. Tezaur, M. Perego, A. Salinger, R. Tuminaro, S. Price. "*Albany/FELIX*: A Parallel, Scalable and Robust Finite Element Higher-Order Stokes Ice Sheet Solver Built for Advanced Analysis", *Geosci. Model Develop.* 8 (2015) 1-24.
- [4] M. Perego, S. Price, G. Stadler. "Optimal Initial Conditions for Coupling Ice Sheet Models to Earth System Models", *J. Geophys. Res.* 119 (2014) 1894-1917.
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- [6] J. Watkins, I. Tezaur, I. Demeshko. "A study on the performance portability of the finite element assembly process within the Albany land ice solver", *Lecture Notes in Computational Science and Engineering* (accepted).
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- [12] J. Ostien, et al., A 10-node composite tetrahedral finite element for solid mechanics, *Internat. J. Numer. Methods Engrg.* (ISSN: 1097-0207) 107 (2016) 1145–1170.
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- [17] H. Edwards, A. Williams, G. Sjaardema, D. Baur, W. Cochran, SIERRA toolkit computational mesh conceptual model. Tech. Rep. SAND2010-1192, Sandia National Laboratories, 2010.

Backup Slides



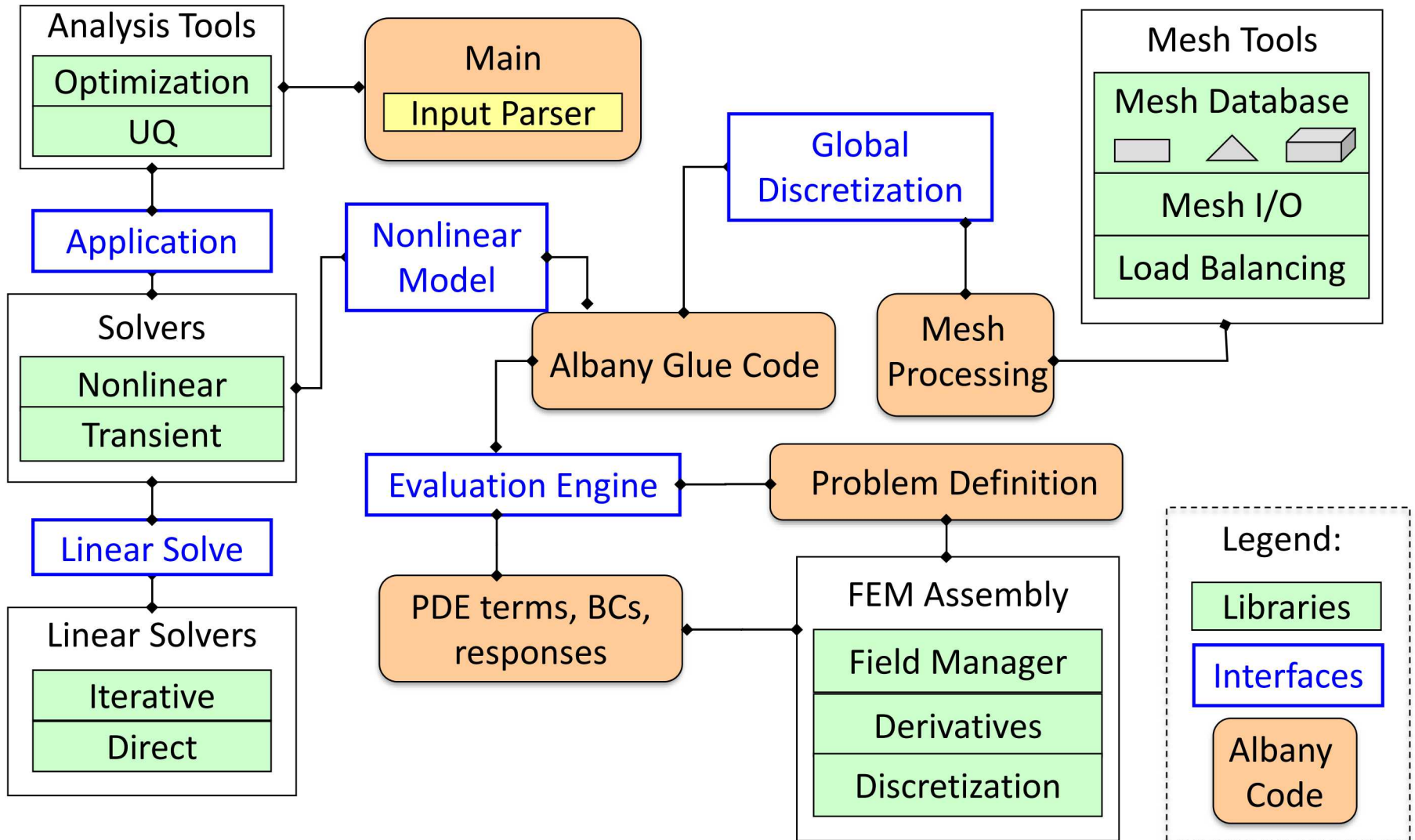
Albany : a component-based finite element code

2008

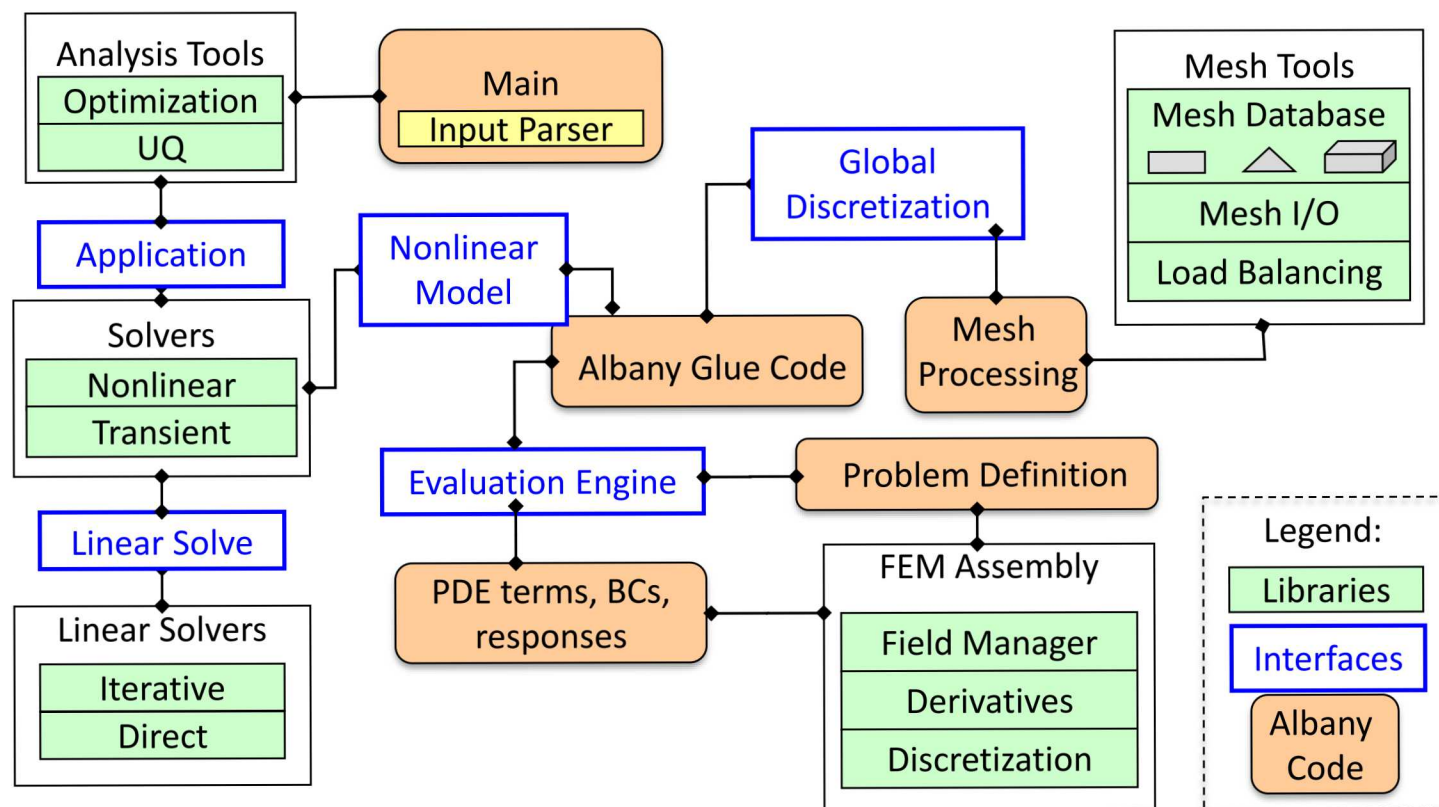
- Started by A. Salinger in 2008 as **first DemoApp** for AgileComponents code development strategy.
- During **next 10 years**, Albany became:
 - a friendly **early adopter** of cutting-edge technology from Trilinos, SCOREC, SierraToolKit, DAKOTA, FASTMath, QUEST, Kitware.
 - a model for a **Trilinos-based** and **Office of Science** application.
 - a demonstration of **transformational analysis** spanning template-based generic programming to optimization and UQ
- **11 years later**, Albany is:
 - an open-source parallel, mostly-implicit **unstructured-grid multi-physics finite element code** that demonstrates the AgileComponents vision by using, maturing, and spinning-off reusable libraries/abstract interfaces.
 - an **attractive environment** for the development of open-source application codes and research.
 - a Meso-App for maturation of **MPI+X programming model** for next generation architecture
 - the code base underlying a number of **research projects** and **applications**.

2019

Albany code design

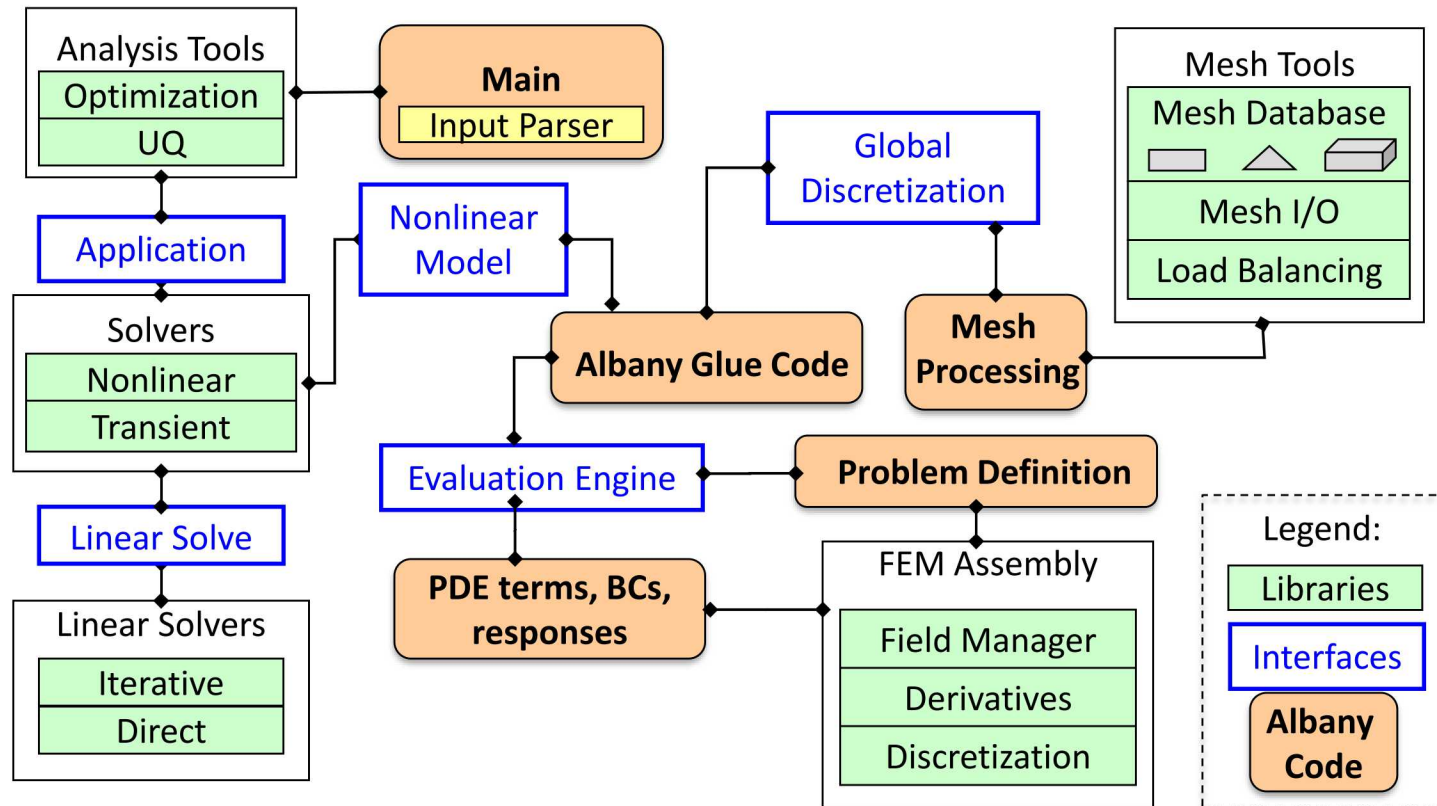


Albany code design



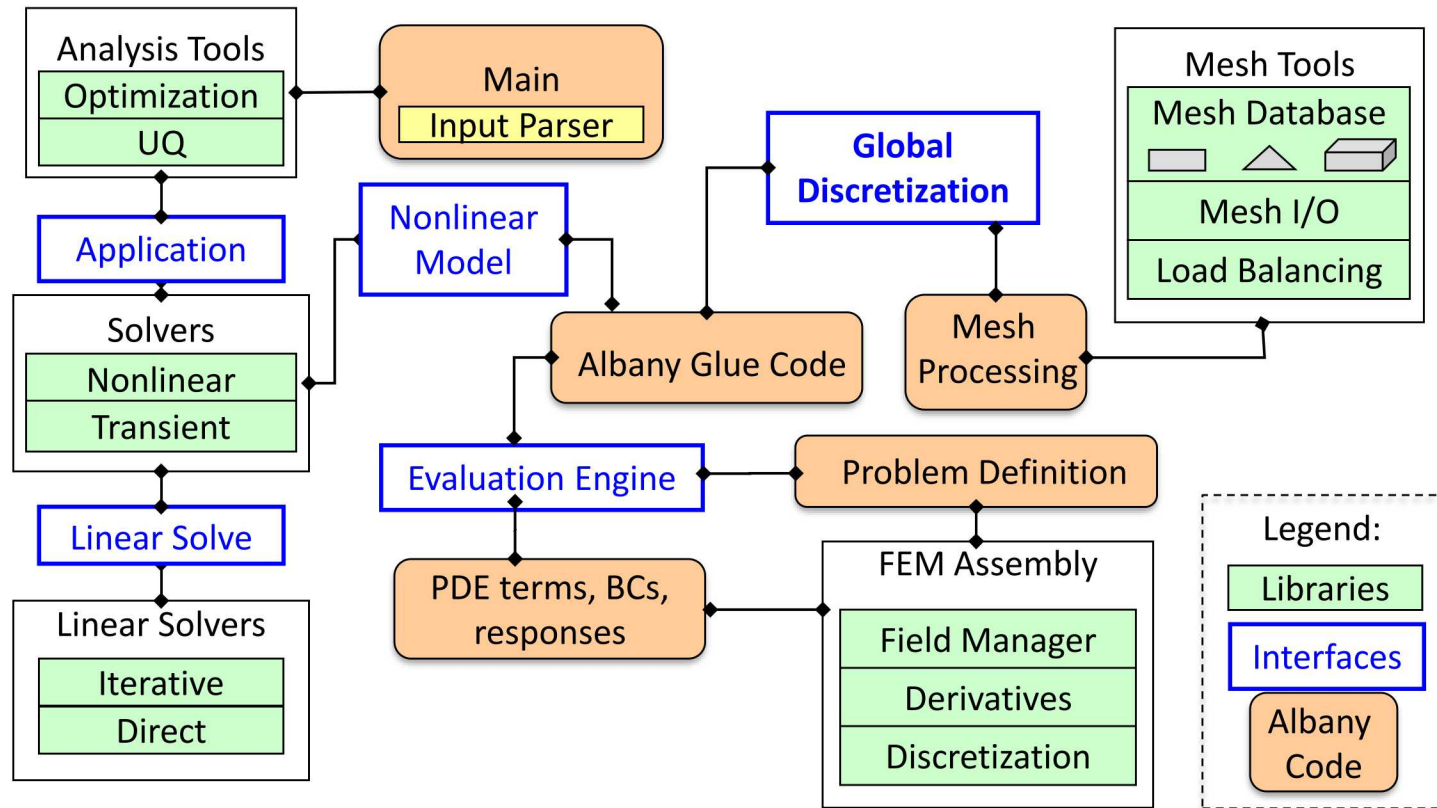
Albany “glue code”

“Glue Code”: driver code integrating components + providing overall capabilities



Albany “glue code”

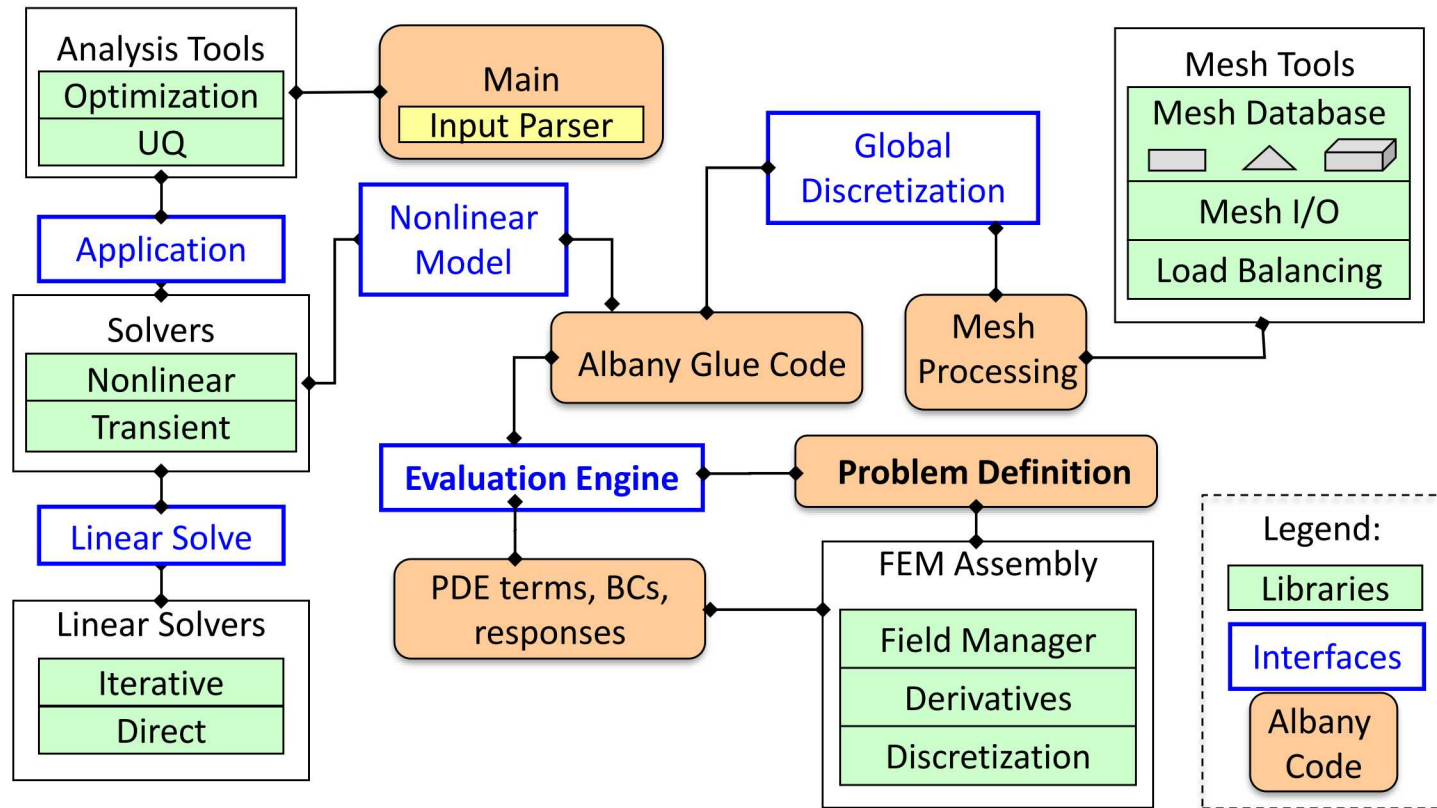
“Glue Code”: driver code integrating components + providing overall capabilities



- Depends on **discretization abstraction** (serves as general interface to a mesh service)

Albany “glue code”

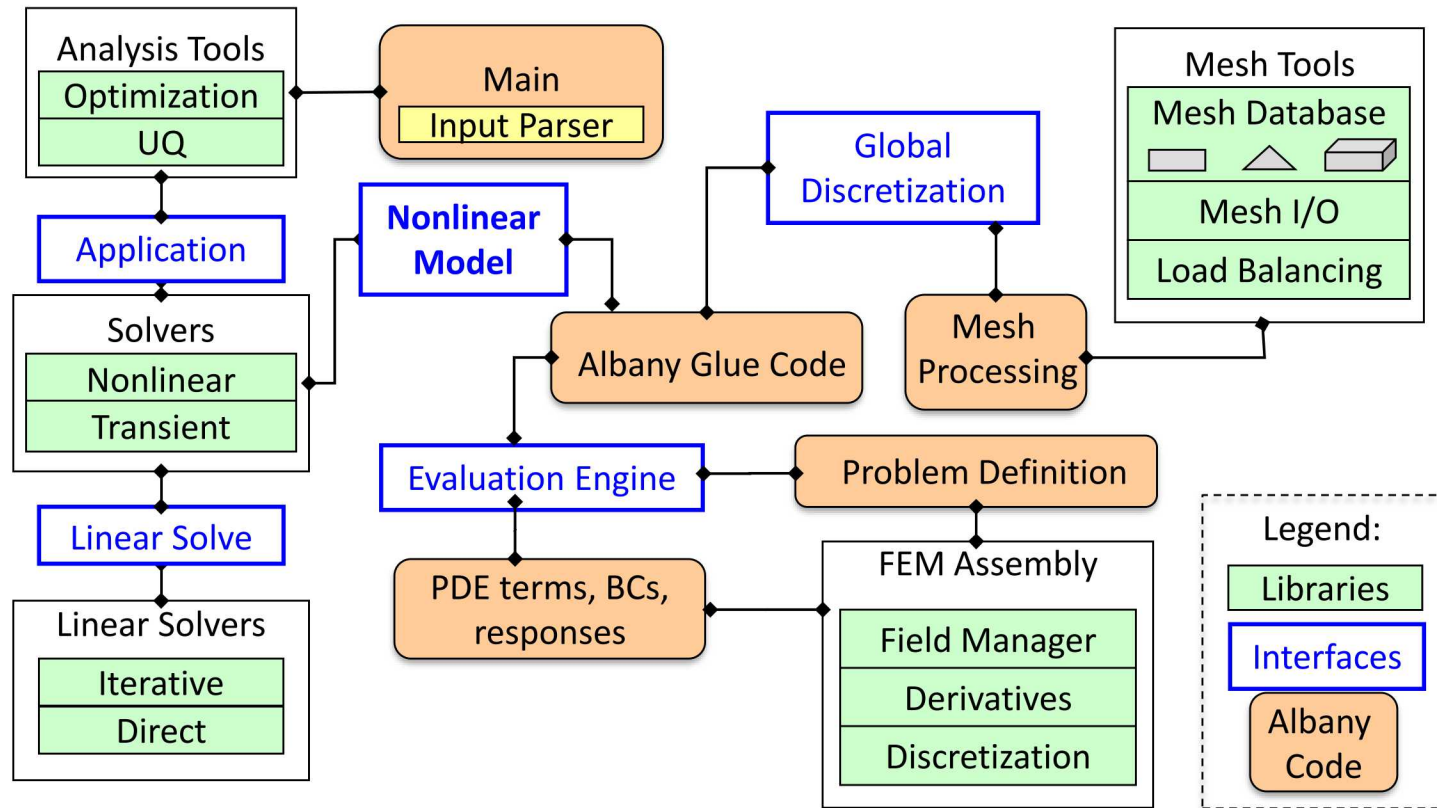
“Glue Code”: driver code integrating components + providing overall capabilities



- Depends on **discretization abstraction** (serves as general interface to a mesh service)
- Employs **evaluation engine** to construct PDEs, BCs, and response calculations

Albany “glue code”

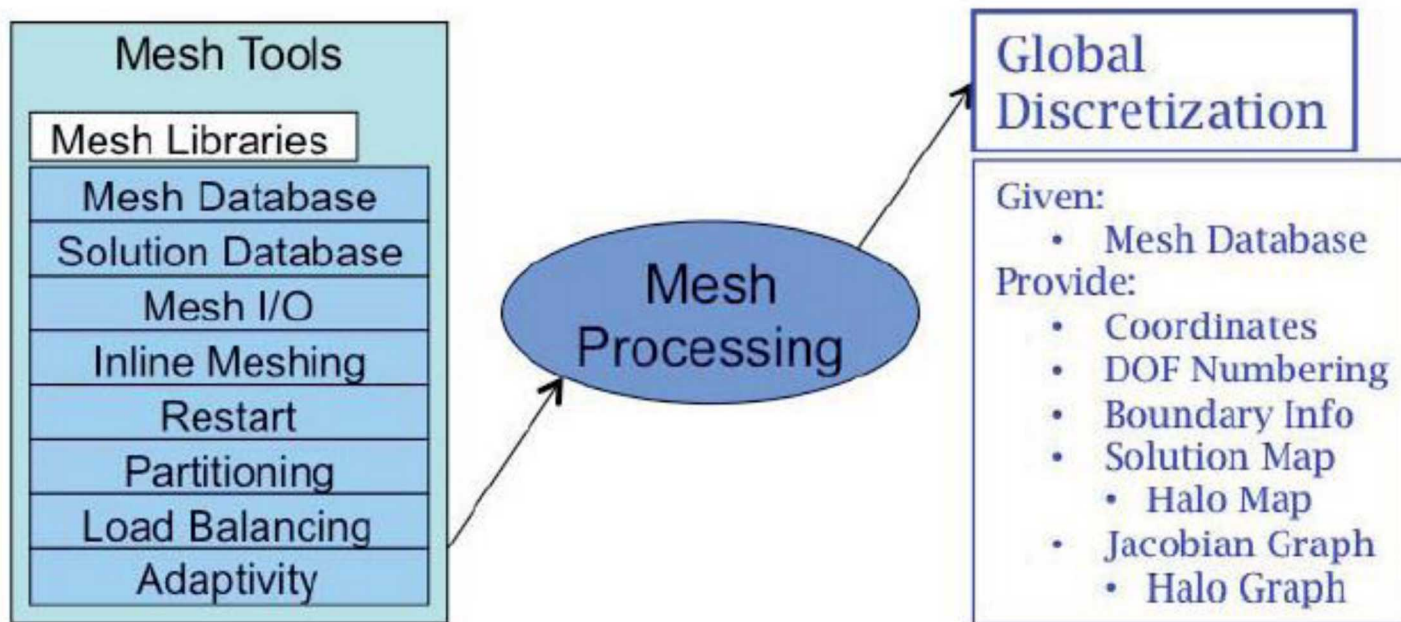
“Glue Code”: driver code integrating components + providing overall capabilities



- Depends on **discretization abstraction** (serves as general interface to a mesh service)
- Employs **evaluation engine** to construct PDEs, BCs, and response calculations
- Uses physics pieces to satisfy **nonlinear model abstraction** (e.g., compute resid/Jac)

Global discretization abstraction

- **Mesh framework:** defines geometry, element topologies, connectivities, boundary info, mesh-dependent fields.
- **Global discretization abstraction:** gives the finite element assembly process access to all of the data distribution information required by the linear algebra objects.
- Mesh info is contained in in-memory mesh database accessed through abstract **global discretization interface** class.

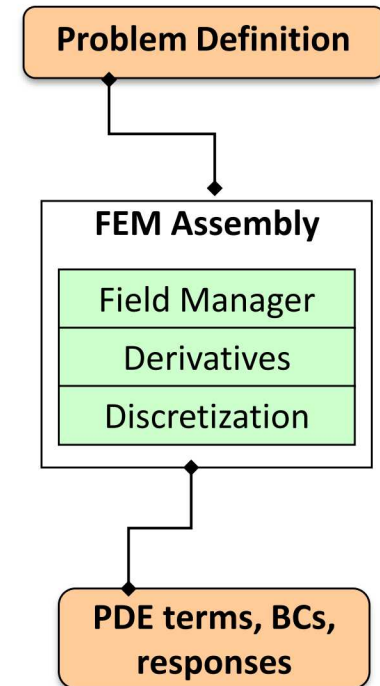
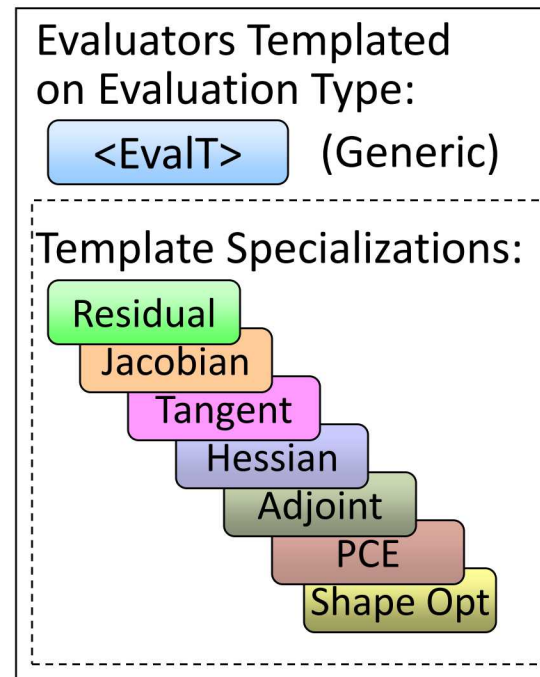


Problem abstraction & finite element assembly Sandia National Laboratories

Purpose of problem abstraction & finite element assembly: given a finite element mesh, evaluate discrete finite element residual, Jacobian, and (if applicable) parameter derivatives.

3 key ingredients facilitating multi-physics implementations in Albany:

1. Template-based generic programming (TBGP)
2. Graph-based finite element assembly (FEA)
 - Handled by Phalanx package
3. Templated-based automatic differentiation
 - Handled by Sacado package



Automatic differentiation via Sacado

Automatic Differentiation (AD) provides exact derivatives w/o time/effort of deriving and hand-coding them!

- How does AD work? → **freshman calculus!**
 - Computations are composition of simple operations (+, *, sin(), etc.)
 - Derivatives computed line by line then combined via chain rule.
- Great for **multi-physics codes** (e.g., many Jacobians) and **advanced analysis** (e.g., sensitivities)
- Albany uses Trilinos package **Sacado** for AD
 - AD accomplished via **operator overloading + templating**: floats/double data types replaced by AD types.

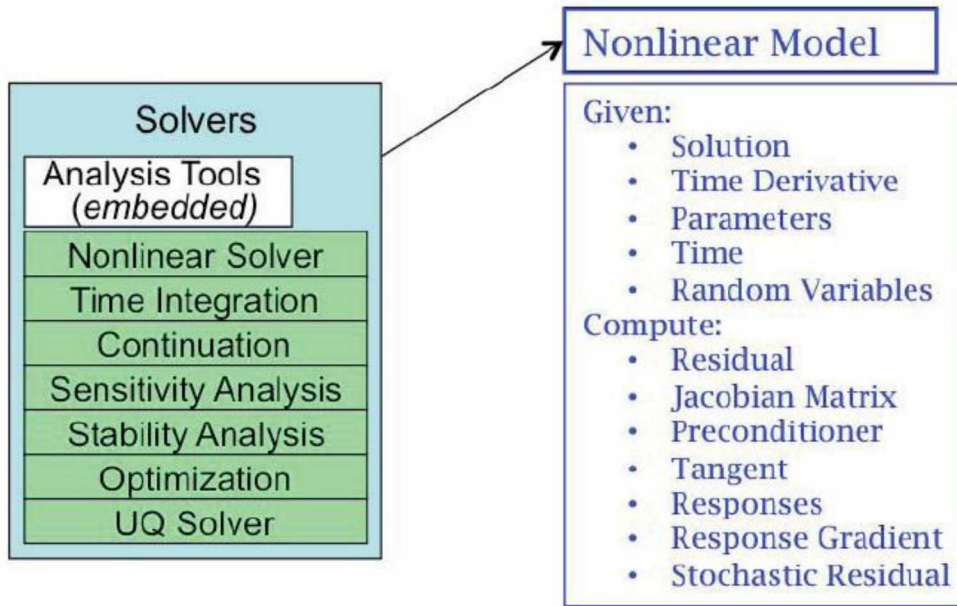
Automatic Differentiation Example:

$$y = \sin(e^x + x \log x), \quad x = 2$$

	$\frac{d}{dx}$
$x \leftarrow 2$	1.000
$t \leftarrow e^x$	7.389
$u \leftarrow \log x$	0.500
$v \leftarrow xu$	1.301
$w \leftarrow t + v$	8.690
$y \leftarrow \sin w$	-1.188

Derivatives are ***as accurate as analytic computation*** – no finite difference truncation error!

Nonlinear model abstraction & libraries



“ModelEvaluator” Abstraction:

Given:	Computes:
x	$f(\dot{x}, \ddot{x}, x, p, t)$
\dot{x}	$W = \alpha \frac{df}{d\dot{x}} + \beta \frac{df}{dx} + \omega \frac{df}{d\ddot{x}}$
\ddot{x}	$\frac{df}{dp}$
p	g
t	$\frac{dg}{dx}$
	$\frac{df}{dp}$

f = residual; x = solution vec;
 p = parameters; g = responses;
 t = time; W = Jacobian

- Access to the **embedded solvers** in Trilinos requires satisfaction of **ModelEvaluator** (nonlinear model) abstraction.
- Interface is **general** to accommodate computation of Jacobians, user-defined preconditioners, and stochastic Galerkin expansions.
- **Advanced capabilities:** embedded UQ (Stokhos), optimization (ROL), homotopy continuation (LOCA).




Core building blocks of Albany

- Component-based design.
- Template-based generic programming.
- Assembly/field evaluation via Phalanx.
- Automatic differentiation.
- Discretizations/meshes, mesh adaptivity.
- Solvers, time-integration schemes.
- Performance-portable kernels.
- Software quality tools: git cmake, ctest, CDash.

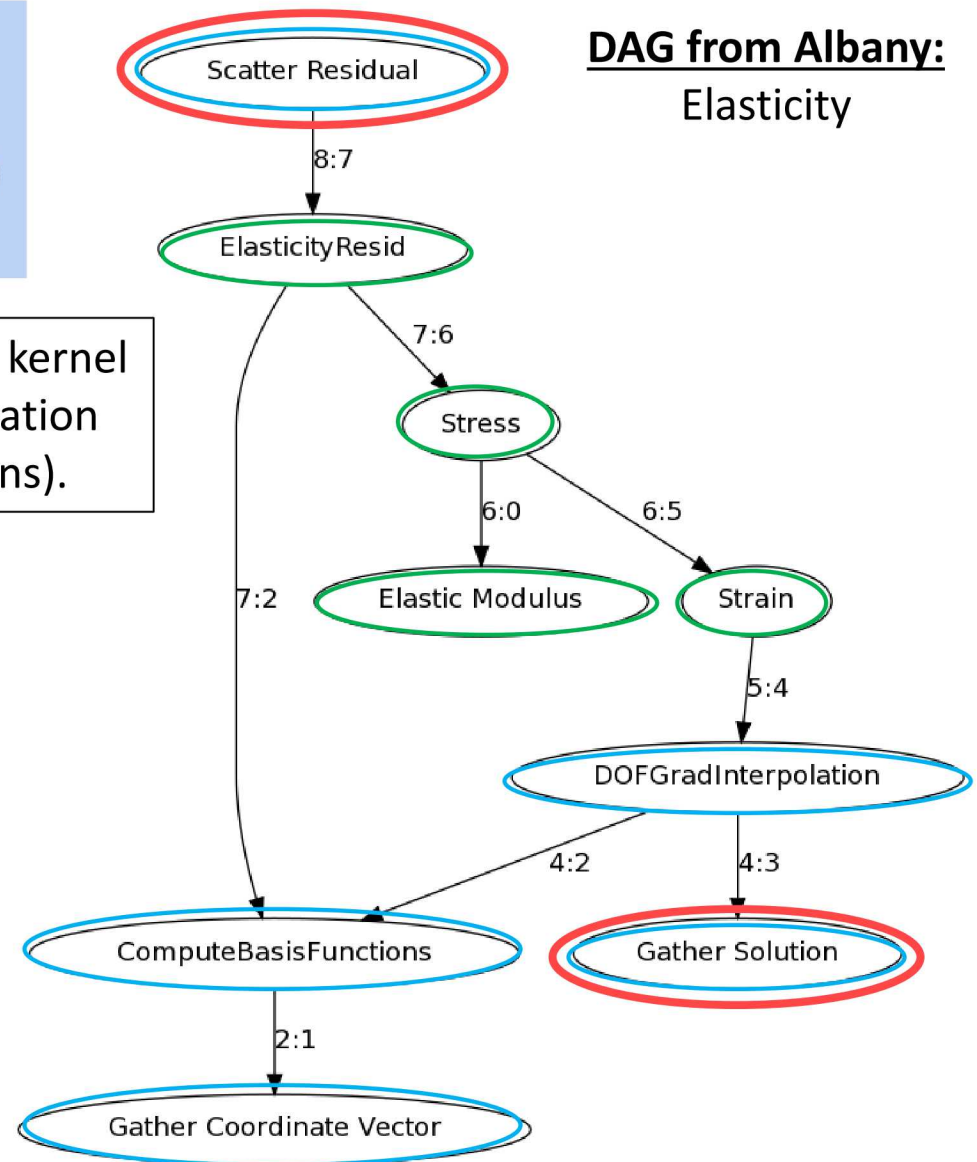
Graph-based finite element assembly (FEA)

Assembly of physics pieces comes down to the evaluation of a **directed acyclic graph (DAG)** of computations of field data.

Phalanx package: Local field evaluation kernel designed for assembly of arbitrary equation sets (i.e. evaluating residuals/Jacobians).

-  Template-specialized evaluators
-  Evaluator common to all FEAs
-  Problem-specific evaluator

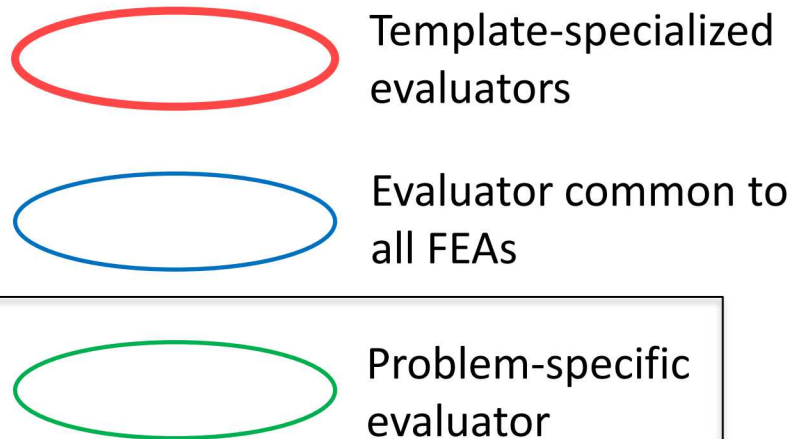
DAG from Albany:
Elasticity



Graph-based finite element assembly (FEA)

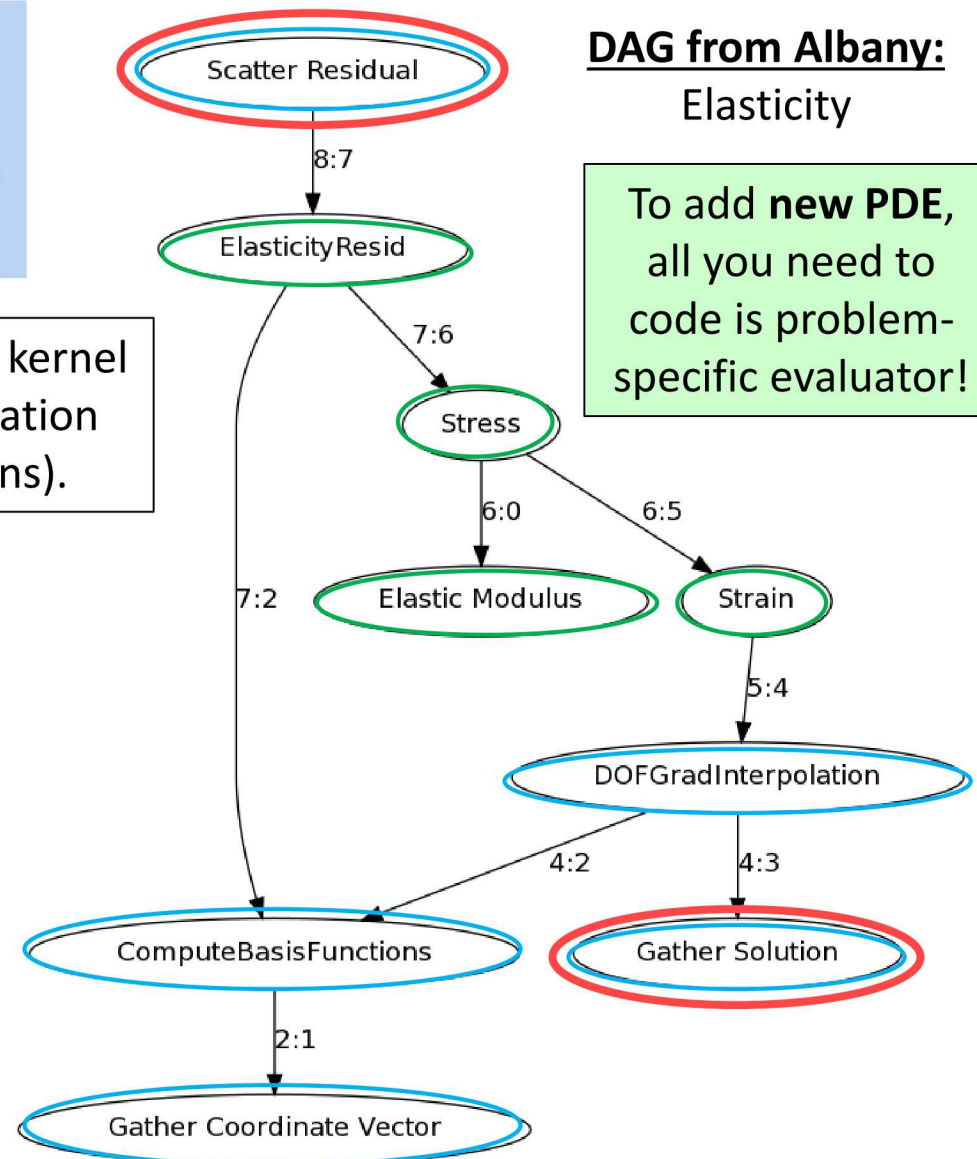
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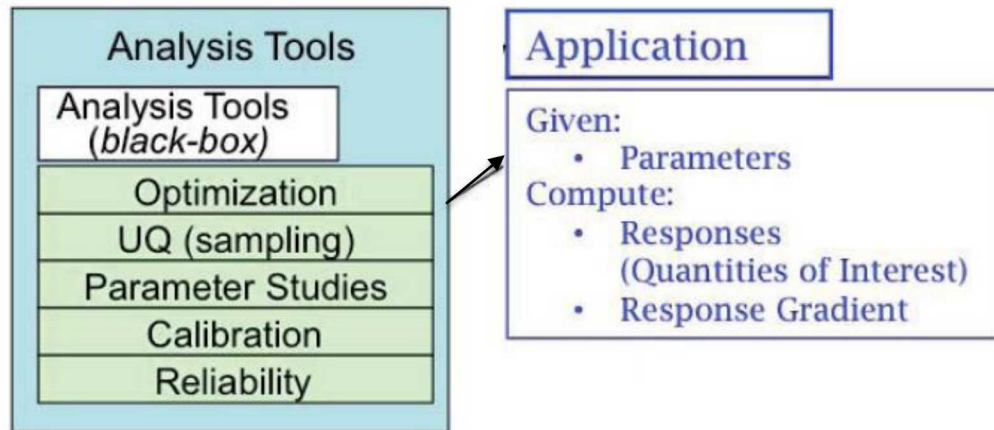


DAG from Albany:
Elasticity

To add **new PDE**, all you need to code is problem-specific evaluator!



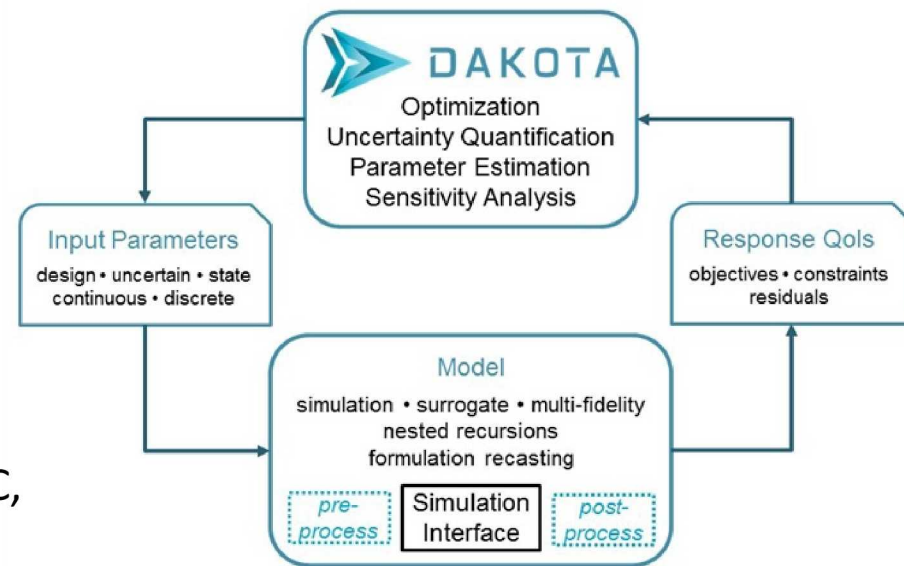
Analysis tools abstraction & libraries



“**Black box**” analysis tools at top level of software stack can perform a single forward solve, sensitivity analysis, parameter studies, bifurcation analysis, optimization, and UQ runs.

Optimization and **UQ** can be done through DAKOTA:

- **Optimization algorithms**: gradient-based local algorithms, pattern searches, and genetic algorithms, etc.
- **UQ algorithms**: Latin hypercube stochastic sampling, stochastic collocation, PCE, MCMC, etc.



Libraries/algorithms whose development was significantly aided by Albany

Libraries Developed in Albany:

- Piro
- TriKota
- MiniTensor
- Razor (MOR)
- buildAgainstTrilinos

Libraries Driven by Albany:

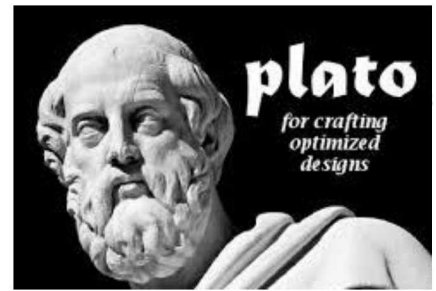
- Stokhos Embedded UQ
- Semi-Coarsening AMG
- PAALS
- Advanced Topological Opt
- Embedded Ensembles
- CUBIT Mesh-Morpher

Libraries Matured in Albany:

- Tempus
- Phalanx
- STK
- ModelEvaluator
- Stratimikos
- TPetra
- PUMI
- ROL
- DTK
- Intrepid2/Kokkos
- DynRankView
- *And counting...*

Advanced Topology Optimization (ATO)

Coupling of Albany code and **PLATO*** engine for **optimization-based topology optimization**.



Goals:

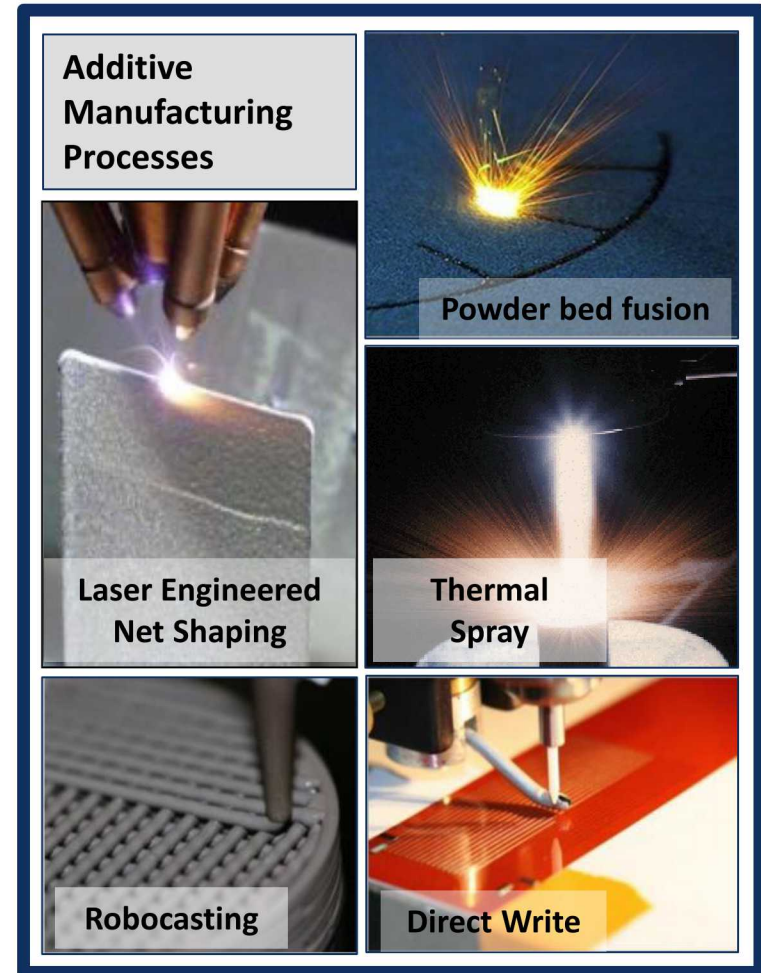
- **Qualification:** assure quality
- **Design:** effectively utilize AM

PDE-constrained optimization:

- **Physics:** elastostatics, Poisson
- **Objectives:** compliance, p-norm
- **Constraints:** volume/mass

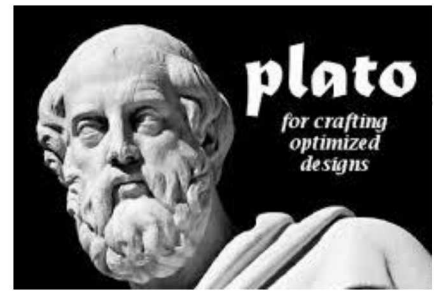
Multiple simultaneous Albany runs can inform a single design optimization by PLATO:

- Albany implements objective + gradient evaluation, optimization loop
- **New “meshless” ATO capability:** allows user to include arbitrarily many simultaneous load cases (linear thermal/electrical, mechanical)



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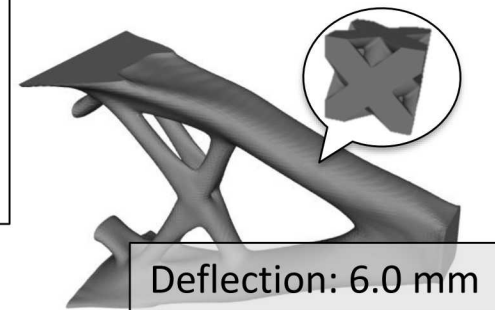
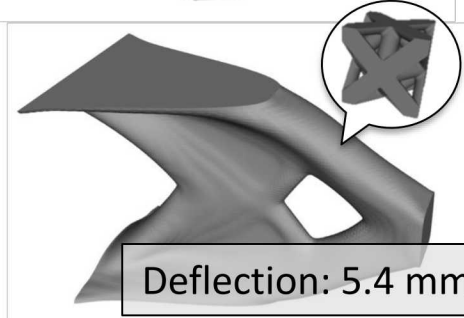
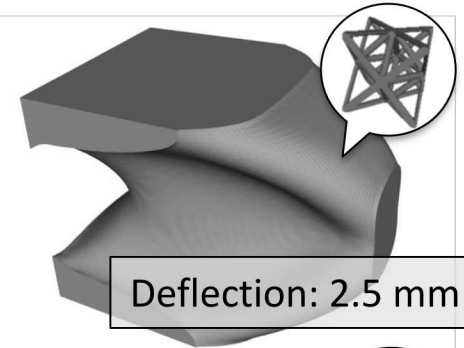
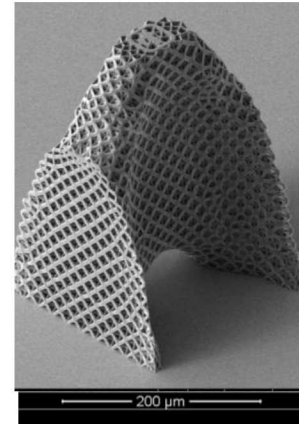
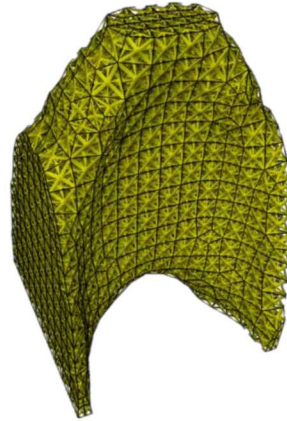
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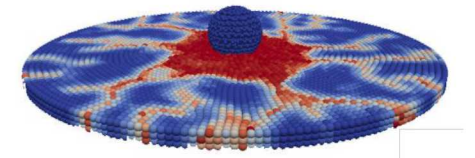
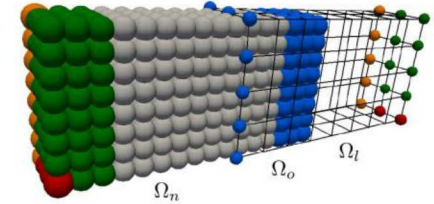
Right:
cellular
structures
with
optimized
stiffness

Albotran (Albany-PFLOTRAN)

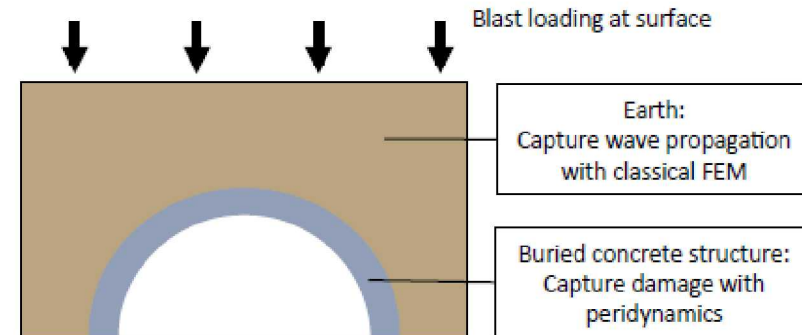
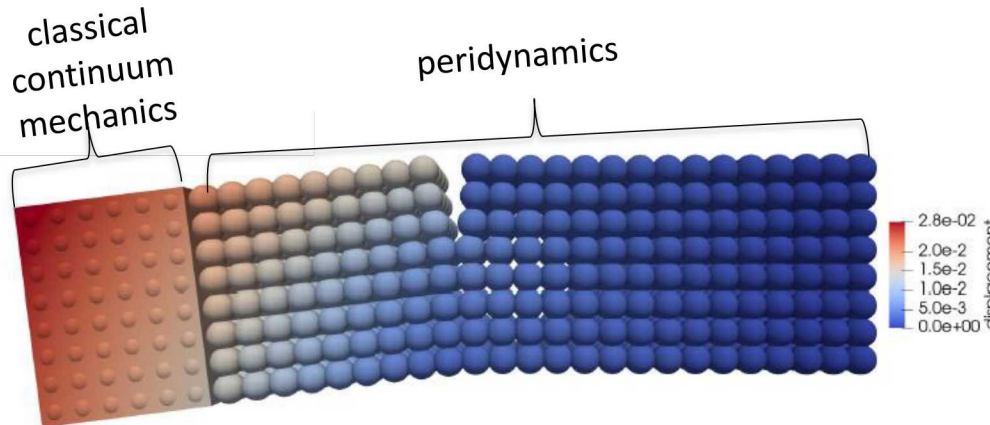
Albany-Peridigm

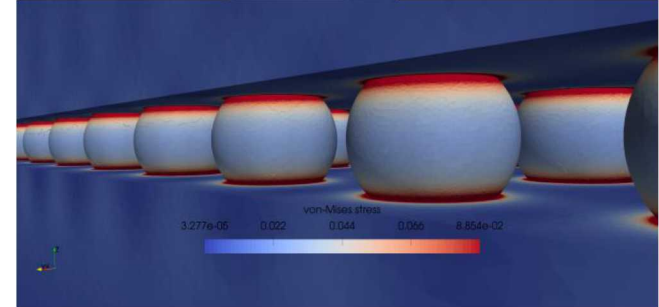
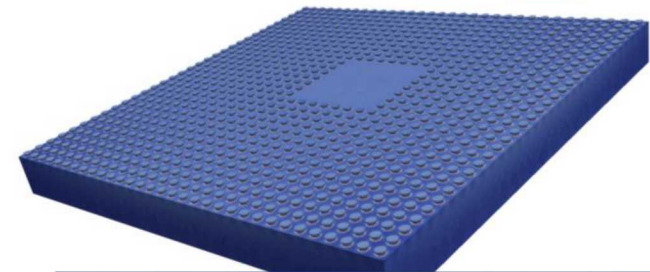


Local-nonlocal coupling for integrated fracture modeling & multi-physics peridynamics simulations



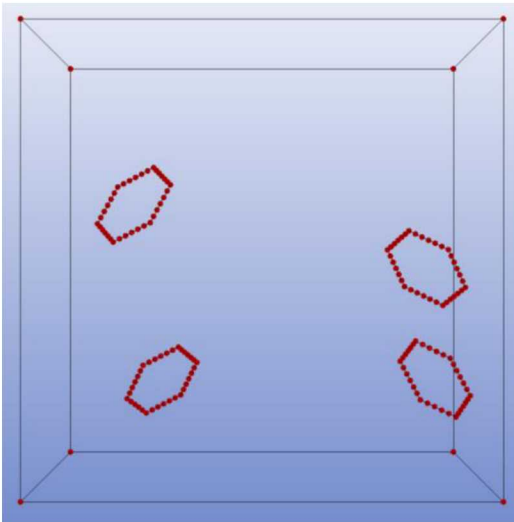
- **Peridynamics**: nonlocal extension of continuum mechanics that remains valid at discontinuities/cracks
- **Peridigm** = open-source* peridynamics code
 - **Nonlocal meshfree approach** (Silling *et al.*, 2005).
- “**Best of both worlds**” by combining FEM + peridynamics: peridynamics applied in regions susceptible to material failure, easy delivery to applications via FEM.
- **Optimization-based local-to-nonlocal coupling** using ROL (D’Elia *et al.* 2016).





Creep/Plasticity in Large Solder Joint Arrays*

- Strategic reliability process in semiconductor manufacturing
- Automated workflows with locally refined meshing
- Novel materials models
- Scaling out to 16K processors, 1B+ elements



Coupled Dislocation Dynamics

- Integrates Albany and ParaDis
- Computes dislocation dynamics (DD) in complex geometry
- Allows intersection of dislocations with free surfaces
- **Left**: prismatic dislocation loops in finite domain

* Li, et al. *Comp.Mech.*, 62:323, 2018. Bloomfield, et al. *Eng. with Comp.*, 33: 509, 2017.