

1                    Pilot-scale open raceway ponds and flat-panel  
2                    photobioreactors maintain well-mixed conditions under a  
3                    wide range of mixing energy inputs

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17  
18 Short running title:

19 Pilot photobioreactors maintain well-mixed conditions

22 **Abstract**

23           Turbulent mixing in pilot-scale cultivation systems is hypothesized to influence the  
24 productivity of photoautotrophic cultures. We studied turbulent mixing by applying particle  
25 image velocimetry (PIV) and acoustic doppler velocimetry (ADV) to pilot scale flat-panel  
26 photobioreactors and open raceway ponds. Mixing energy inputs were varied from 0.03 to 1.97  
27  $\text{W}\cdot\text{m}^{-3}$ . The experimental results were used to quantify turbulence and to validate computational  
28 fluid dynamics (CFD) models, from which Lagrangian representations of the fluid motion in  
29 these reactors was derived. The results of this investigation demonstrate that differences in  
30 mixing energy input do not significantly impact the structure of turbulence in the reactors, nor  
31 the frequency of photoautotrophic microorganisms' motions within the reactors. The  
32 experimental and computational results of our research demonstrate that well-mixed conditions  
33 exist in pilot flat-panel photobioreactors and open raceway ponds, even at relatively low mixing  
34 energy inputs.

35

36 *Keywords:*

37 Mixing energy, dark/light cycles, open raceway pond, flat-panel photobioreactor, fluid  
38 mechanics

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43 1. Introduction

44 Photoautotroph-based biofuels are considered one of the most promising renewable fuels to  
45 meet the global energy requirements for transportation systems (Y. Chisti, 2007). Long-term  
46 research and development has resulted in demonstrations of microalgae areal oil productivities  
47 that are higher than crop-based biofuels, about 10 times that of palm oil and about 131 times that  
48 of soybean (Brune, Lundquist, & Benemann, 2009; Y. Chisti, 2007; Lardon, Helias, Sialve,  
49 Steyer, & Bernard, 2009; Rodolfi et al., 2009). Cyanobacteria is reported to have ~4 times the  
50 areal productivity of microalgae on an equivalent energy basis (Robertson et al., 2011).  
51 Downstream of this cultivation process, cyanobacterial biomass and bioproducts can be supplied  
52 to biorefineries producing feed, biomaterials, biosynthetic chemicals, and biofuels (Wijffels,  
53 Kruse, & Hellingwerf, 2013). As such, cyanobacteria-based biofuel systems may be a significant  
54 contributor to more sustainable energy and material production systems.

55 Turbulent cultivation environments have been demonstrated to induce physiological  
56 responses in photoautotrophic microorganisms in open raceway ponds and photobioreactors  
57 (Fadlallah et al., 2016; Havens, James, East, & Smith, 2003; Kumar, Dasgupta, Nayak, Lindblad,  
58 & Das, 2011; Michels, van der Goot, Norsker, & Wijffels, 2010; Mirón et al., 2003; Moisander,  
59 Hench, Kononen, & Paerl, 2002; Nguyen & Hoang, 2016; Xiao, Li, Li, Zhang, & Guo, 2016).  
60 For example, recent efforts studied the effects of turbulence dissipation rates ranging from 0 to  
61  $8E^{-2} \text{ m}^2 \cdot \text{s}^{-3}$  simulated at laboratory scale conditions (1-liter cultures) (Xiao et al., 2016). This  
62 work concluded that despite no alteration of photosynthesis activity (as measured by chlorophyll  
63 a), there is a systematic increase in the growth rates of the strain *Microcystis flos-aquae* as a  
64 function of the turbulent dissipation rate, and a decrease in the growth rate of the strain  
65 *Anabaena flos-aquae* at high turbulence. These authors identified that a maximum phosphorous

66 uptake rate in these cyanobacteria strains occurs at turbulence dissipation rates of  $2.26E^{-2} \text{ m}^2 \cdot \text{s}^{-3}$ ,  
67 suggesting that turbulence plays an important role in the biological adaptation of cyanobacteria  
68 by influencing nutrient uptake (Xiao et al., 2016). In other recent research, the effects of shear  
69 environments were studied for the cyanobacteria and microalgae strains *Synechocystis sp.* and  
70 *Chlamydomonas reinhardtii*, in 150 ml cultures (Fadlallah et al., 2016). In this study, the growth  
71 rate of *Synechocystis sp.* was independent of shear stress (0 to  $0.18 \text{ N} \cdot \text{m}^{-2}$ ) and *Chlamydomonas*  
72 *reinhardtii* growth rate increased linearly with shear stress. It is an open question as to whether  
73 these research results under laboratory scale environments (<1L cultures) are representative of  
74 industrial-scale (>1000L) cultivation conditions.

75 Detrimental impacts of turbulent mixing have also been demonstrated, with inhibition  
76 attributed to cell disruption from shear stress (Chalmers, 2015; Han & Yuan, 2004; Kunnen,  
77 Malas, Semeins, Bakker, & Peters, 2017; Richardson, Lannigan, & Macara, 2015; Sieck et al.,  
78 2014; Sieck et al., 2013; Wang, Lü, Mao, & Long, 2014; Yi et al., 2010). For example,  
79 hybridoma cells suffer apoptosis at mixing energy inputs of  $1.87E^3 \text{ W} \cdot \text{m}^{-3}$  (Al-Rubeai, Singh,  
80 Goldman, & Emery, 1995; Chalmers, 2015). Other studies observed 51% lower recombinant  
81 protein production, 42% higher glucose uptake, and 50% lower lactate production in cells  
82 exposed to mixing energy inputs of  $6.4E^2 \text{ W} \cdot \text{m}^{-3}$  (Chalmers, 2015; Keane, Ryan, & Gray, 2003).  
83 In general, these inhibitory effects are reported at mixing energy inputs above  $1E^6 \text{ W} \cdot \text{m}^{-3}$  and  
84 Kolmogorov microscales less than or equal to 2.4 micrometers for mammalian cells (Chalmers,  
85 2015). In photobioreactors, small bubbles are reported to cause cell damage (Barbosa & Wijffels,  
86 2004; Mirón et al., 2003), colliding with photoautotrophic cells and contributing to a high shear  
87 environment. The growth of the microalgae strain *Phaeodactylum tricornutum*, for instance, was  
88 inhibited at air rates of  $0.567 \text{ m}^3_{\text{air}} \cdot \text{min}^{-1} \cdot \text{m}^{-3}_{\text{reactor}}$ , and carboxymethyl cellulose (CMC, a

89 viscosity increaser) supplied into the medium had the effect of mitigating shear-induced damage  
90 in parallel experiments (Mirón et al., 2003). Other sparged photobioreactors cultivating  
91 *Dunaliella tertiolecta* and *D. salina* reported increases in the culture decay rates as a function of  
92 gas velocity, observing the highest death rates at 8.91 and 13.37 m<sup>3</sup><sub>air</sub>.min<sup>-1</sup>.m<sup>-3</sup><sub>reactor</sub> (Barbosa &  
93 Wijffels, 2004). There is no research reported in the literature concerning the biological system  
94 response due to shear stress on cyanobacteria cells, particularly on the biofuels-relevant strains of  
95 *Synechocystis sp.* PCC6803. Moreover, most of the previous research was conducted at mixing  
96 energy inputs that are 30, 100, or thousands order of times higher than is considered cost-  
97 effective for industrial cultivation systems (Jones, Louw, & Harrison, 2017; Sánchez Mirón,  
98 Garcia Camacho, Contreras Gomez, Grima, & Chisti, 2000).

99         Industrial photobioreactors are used for large-scale cultivation of photoautotrophic  
100 microorganisms, the most common types being the open raceway ponds and flat panel  
101 photobioreactors (*Microalgal Biotechnology: Potential and Production*, 2013). Open raceway  
102 ponds are constructed in a configuration with channels, using paddlewheel mixers that promote a  
103 low shear environment (Oswald, 1988). Flat-panel photobioreactors are vertically translucent flat  
104 plates, illuminated on both sides and stirred by aeration (Little, 1953). Unlike outdoor raceways  
105 and outdoor photobioreactors, laboratory-scale experiments are rigorously controlled to create  
106 ideal conditions for growth including ideal mixing rates, optimum light intensities, and optimized  
107 media, which may lead to overestimation of photoautotrophic biomass and biofuels productivity  
108 at industrial scale (Rawat, Kumar, Mutanda, & Bux, 2013). The light regime experienced by  
109 photoautotrophic microorganisms under outdoor conditions is hypothesized to be one factor in  
110 this difference in the performance of industrial systems. For instance, the light saturation of  
111 *Synechocystis sp.* PCC6803 is at about 200 μmol photons.s<sup>-1</sup>.m<sup>-2</sup> (Kim, Vannela, Zhou, Harto, &

112 Rittmann, 2010; Kim, Vannela, Zhou, & Rittmann, 2011), whereas photoautotrophic  
113 microorganisms will face incident radiations of about  $2000 \mu\text{mol photons}\cdot\text{s}^{-1}\cdot\text{m}^{-2}$  at noon in  
114 locations such as Colorado (Quinn, Turner, & Bradley, 2012). Previous studies have estimated  
115 that the total photoconversion efficiency of algae varies from between 2.6% (at high light) to  
116 6.3% (at reduced light) (Weyer, Bush, Darzins, & Willson, 2010). These estimations assumed  
117 that 46% of the spectrum is in the photosynthetic active radiation (PAR) range of 400 to 700 nm,  
118 losses due to photon transmissions efficiency of 95%, photon utilization efficiency ranging from  
119 10% to 30%, biomass accumulation efficiency of 50%, and biomass energy content of  $21.9$   
120  $\text{kJ}\cdot\text{g}^{-1}$ . Low photoconversion efficiency in photoautotrophic microorganisms exposed to real-  
121 world light regimes is attributed to increased dark and photorespiration biomass losses (Drewry,  
122 Choi, An, & Gharagozloo, 2015; Edmundson & Huesemann, 2015; Gharagozloo et al., 2014).

123         Some previous studies have investigated the effects of mixing rates on photoautotrophic  
124 biomass productivities in industrial scale systems (Jones et al., 2017; Quinn et al., 2012;  
125 Sompech, Chisti, & Srinophakun, 2012). Some of these efforts have identified optimum volumes  
126 of air flow rates per unit volume (VVM) of photobioreactors that might be industrially relevant  
127 for microalgae, generally between  $0.2$  to  $1.2 \text{ m}^3_{\text{air}}\cdot\text{min}^{-1}\cdot\text{m}^{-3}_{\text{reactor}}$  (Quinn et al., 2012). Many  
128 others have considered mixing energy inputs that are far outside the energy consumption that can  
129 be considered economic, or industrially relevant, ranging from  $8$  to  $633 \text{ W}\cdot\text{m}^{-3}$  (Jones et al.,  
130 2017; Sánchez Mirón et al., 2000). For raceway ponds, for instance, energy inputs from  $1$  to  $2$   
131  $\text{W}\cdot\text{m}^{-3}$  are utilized in the algae cultivation demonstrations performed to date (Sompech et al.,  
132 2012). Additionally, previous research states that mixing in industrial photobioreactors induces  
133 flashing or dark/light cycles (Janssen, Tramper, Mur, & Wijffels, 2003; Vejrazka, Janssen,  
134 Streefland, & Wijffels, 2011, 2012). For instance, by experimentally growing *Chlamydomonas*

135 *reinhardtii* under incident radiations fluctuating between 5 Hz and 100 Hz, growth rates were  
136 found to be linearly dependent on the light frequency. These previous efforts suggest that mixing  
137 in photobioreactors controls the light regimes experienced by single cells, impacting the bulk  
138 photosynthesis and biomass productivity of photoautotrophic microorganisms. However, other  
139 studies demonstrated no improvements in algal productivity at light fluctuations from 0.038 Hz  
140 to 1 Hz, modeled using a control timer to open and close a mini venetian blind device  
141 (Grobbelaar, 1991). The frequencies in these latter experiments ( $\ll 1$  Hz), are more consistent  
142 with the frequencies encountered in the circulation velocities for fermenters with a height to  
143 diameter ratio less than 3 ( $< 60$  seconds) and for airlift reactors with split-cylinders heights of  
144 6.02 m. (6.5 seconds) (M. Y. Chisti, 1989), perhaps suggesting that light fluctuations are a  
145 negligible component of the productivity benefits associated with highly mixed reactors.

146         Modelers and engineers have attempted to predict the fluid mechanics of raceway ponds,  
147 and photobioreactors via Computational Fluid Dynamics (CFD) approaches (Ali, Cheema, Yoon,  
148 Do, & Park, 2015; Labatut, Ebeling, Bhaskaran, & Timmons, 2015; Pires, Alvim-Ferraz, &  
149 Martins, 2017), but modeling of these systems is complex and a series of simplifications are  
150 generally required. For example, the conclusions from CFD models applied to investigate  
151 velocity and heat transfer are weakened because all studies to date use average velocities as  
152 boundary conditions (Sompech et al., 2012; Zhang, Qi, He, Yu, & Ruan, 2017), missing the  
153 dynamics of the flow downstream of the paddlewheel. Similarly, turbulence intensity and the  
154 impact of the difference in mixing energy inputs in open raceway ponds are not fully understood.  
155 Turbulence intensities used in previous CFD applications for open raceway ponds have been  
156 documented at 3.84% (Labatut et al., 2015), and at the default values recommended by  
157 commercial CFD codes (Drewry et al., 2015; Pires et al., 2017; Zhang et al., 2017), ranging from

158 5-10%. For the case of open channel flow, for instance, experimental turbulence intensities are  
159 reported at 2.8% (Nezu & Rodi, 1986). Other previous research studied particle tracking with  
160 neutrally buoyant particles in photobioreactors (Fernandes et al., 2017), but ignore the statistical  
161 and temporal nature of turbulence modeling. Previous efforts have demonstrated well-mixed  
162 conditions in open raceway ponds, but have considered paddlewheel speeds ranging from 15  
163 RPM to 28 RPM (Ali et al., 2015) equivalent to mixing energy inputs estimated at  $4.5 \text{ W.m}^{-3}$  to  
164  $30 \text{ W.m}^{-3}$  or two to 15 times higher than used for industrial cultivation (McGowen et al., 2017;  
165 Sompech et al., 2012). None of the reviewed studies have analyzed algae/cyanobacteria cell  
166 motion using modern experimental fluid mechanics tools, and CFD tools at industrially relevant  
167 mixing energy inputs.

168 Two modern methods for experimental fluid mechanics are particle image velocimetry  
169 (PIV) and Acoustic Doppler Velocimetry (ADV). PIV correlates the velocity of the fluid from  
170 the distance traveled in a short period of time by neutrally buoyant particles, captured by laser  
171 technology and high-resolution cameras (D. Adhikari & E. Longmire, 2012; Foeth, Van Doorne,  
172 Van Terwisga, & Wieneke, 2006; Jeon & Sung, 2011; Khalitov & Longmire, 2002; Kiger & Pan,  
173 2000). Biological applications include; for instance, aquatic predator-prey interactions (D.  
174 Adhikari & E. K. Longmire, 2012), hydrodynamics of fish in aquatic environments (Gemmell,  
175 Adhikari, & Longmire, 2014), and fluid transport by plankton aggregations (Wilhelmus &  
176 Dabiri, 2014). ADV correlates the velocity of the fluid from the speed of sound of an acoustic  
177 pulse (Kraus, Lohrmann, & Cabrera, 1994; Lohrmann, Cabrera, & Kraus, 1994). This technique  
178 has been widely used to understand turbulence in natural and engineered civil works including  
179 open channels (Blanckaert & Lemmin, 2006; Doroudian, Hurther, & Lemmin, 2007; García,  
180 Cantero, Niño, & García, 2007; Hurther & Lemmin, 2001; Nikora & Goring, 1998; Parsheh,

181 Sotiropoulos, & Porté-Agel, 2010; Rusello & Cowen, 2011). A previous study utilized ADV to  
182 describe the velocity field of raceway ponds (Chiaramonti et al., 2013), but did not consider the  
183 timescales and turbulence conditions of these reactors. In general, there is a poor understanding  
184 of the turbulence of flat-panel photobioreactors and open raceway ponds, and the impact of  
185 turbulent mixing on the light and dark oscillations experienced by photoautotrophic  
186 microorganisms is not conclusive.

187 Based on this understanding of the literature we seek to understand the role of turbulent  
188 mixing on the fluid mechanics experienced by photoautotrophic microorganisms during  
189 cultivation. Therefore, we conducted (i) pilot-scale fluid mechanics experimentation in open  
190 raceway ponds and flat-panel photobioreactors at industrially relevant mixing energy inputs, and  
191 (ii) applied computational fluid dynamics modeling and validation. By studying turbulence as a  
192 function of mixing energy input in open raceway ponds and flat-panel photobioreactors, we aim  
193 to understand the role turbulence plays in the motion of photoautotrophic microorganisms in  
194 pilot-scale systems.

## 195 2. Materials and Methods

196 To evaluate the implications of turbulent mixing on the fluid mechanics experienced by  
197 photoautotrophic microorganisms in pilot scale open raceway ponds and flat-panel  
198 photobioreactors, we must understand the connections between fluid mechanics and  
199 photoautotrophic microorganisms motion under different mixing energy inputs. The workflow,  
200 illustrated in Figure 1, integrates parallel but complementary experimental and computational  
201 fluid mechanics efforts. By incorporating laboratory experiments at industrially relevant mixing  
202 conditions, we can generate comparison and validation between laboratory and industrial scale  
203 modeling and experimentation.

## 204 2.1 Flat-Panel Photobioreactors Configuration

205 To validate the CFD models, we performed experimental work under various mixing  
206 energy inputs to the flat-panel photobioreactor. As illustrated in Figure 2, fluid mechanics  
207 experimentation was carried out in one replicate of 1L flat-panel photobioreactors made in  
208 acrylic with the surface to volume ratio of  $112 \text{ m}^2 \cdot \text{m}^{-3}$ . The experiments were at water depths of  
209 20 cm. The systems were mixed by sparged air at the bottom of the flat-panel photobioreactors at  
210 industrially relevant mixing inputs of 0.7, 0.35, and  $0.17 \text{ m}^3$  of air per minute per cubic meter of  
211 the reactor, commonly referred as VVM (Quinn et al., 2012). The equivalent mixing energy  
212 inputs used in the flat-panel photobioreactors experiments were 1.94, 0.97, and  $0.47 \text{ W} \cdot \text{m}^{-3}$ .

## 213 2.2 Open Raceway Pond Configuration

214 As illustrated in Figure 3, the open raceway pond fluid mechanics experimentation was  
215 carried out in one replicate 700L fiber-reinforced plastic raceway at water depths of 20 cm. The  
216 system included a paddlewheel provided with a 90V DC Gearmotor with a rated torque of 33 in.-  
217 lb, controlled by an IronHorse DC drive to mix the cultures. The mixing energy inputs used in  
218 the open raceway pond experiments were  $2.1 \text{ W} \cdot \text{m}^{-3}$  and  $0.7 \text{ W} \cdot \text{m}^{-3}$ . We conducted additional  
219 experiments at  $0.10 \text{ W} \cdot \text{m}^{-3}$ , an order of magnitude lower than reported in the literature for  
220 industrial systems (Sompech et al., 2012).

## 221 2.3 Experimental and Computational Fluid Mechanics Methods

222 To understand the physics of the open raceway ponds and flat-panel photobioreactors we  
223 applied a variety of fluid mechanics tools including Particle Image Velocimetry (PIV), Acoustic  
224 Doppler Velocimetry (ADV), and CFD.

225        2.3.1        Flat-panel photobioreactors fluid characterization by PIV

226                The velocity field of flat-panel photobioreactors was measured in 2-dimensions (x-  
227 velocity and y-velocity components) using PIV. We used mixing energy inputs at  $0.47 \text{ W.m}^{-3}$ ,  
228  $0.97 \text{ W.m}^{-3}$ , and  $1.94 \text{ W.m}^{-3}$  in the study of the flat photobioreactor. The study utilized 20 mm  
229 PMMA Rhodamine-B particles, Nd:YLF Single Cavity Diode Pumped Solid State High  
230 Repetition Rate, laser with 0.2 mm thick measurement plane, double frame CMOS camera,  
231 DaVis software for processing 999 samples at 500 hz, and 32x32 double pass followed by a  
232 12x12 single pass interrogation window. Turbulence characterization is described in detail in the  
233 next section.

234        2.3.2        Open raceway pond fluid characterization by ADV

235                The velocity field in the open raceway pond was measured in 3-dimensions (x-velocity,  
236 y-velocity, and z-velocity components) using ADV. We measure fluid velocities at three  
237 different cross sections (CS): (i) downstream of the paddlewheel, (ii) at the first turn, and (iii) at  
238 the straight channel. At each cross-section, we collected data in a 5X5 matrix with a Vectrino  
239 plus firmware + NORTEK. We collected 60,000 ADV samples at 50 Hz at each point. We  
240 repeated the experiment at mixing energy inputs of  $2.1 \text{ W.m}^{-3}$ ,  $0.7 \text{ W.m}^{-3}$ , and  $0.1 \text{ W.m}^{-3}$ . We  
241 describe turbulence by Reynolds decomposition, which includes the steady mean velocity ( $U$ )  
242 and the fluctuating component ( $u'(t)$ ) from the experimental data (Eq. 1) (Pope & Pope, 2000).  
243 The mean fluctuating components in 3-dimensions was used to compute turbulence kinetic  
244 energy ( $k$ ) (Eq. 2) (Pope & Pope, 2000). Lastly, turbulence intensities, defined as the ratio of the  
245 velocity fluctuations ( $u'$ ) to the mean velocity ( $U$ ) were computed from the experimental data  
246 (Eq. 3) (Russo & Basse, 2016; Schlichting & Gersten, 2016).

247  $u(t) = U + u'(t)$  Eq. 1

248  $k = 1/2 * (u'_x{}^2 + u'_y{}^2 + u'_z{}^2)$  Eq. 2

249  $I \equiv \frac{w'}{U}$  Eq. 3

250 2.3.3 Characterizing cell motion by CFD

251 To understand the frequency of photoautotrophic microorganism's motion in flat-panel  
252 photobioreactors and open raceway ponds, we obtained particle tracks from the CFD models in a  
253 Lagrangian representation of the flow. We computed the length and time scales from  
254 Kolmogorov microscales (Pope & Pope, 2000; Tennekes & Lumley, 1972; Versteeg &  
255 Malalasekera, 2007). The smallest length scales of motion ( $\eta$ ) are computed by dimensional  
256 analysis as a function of the largest length scale ( $l$ ) and the Reynolds number ( $Re$ ) (Eq. 4), and,  
257 the smallest time scales ( $\tau$ ) are a function of the largest time scale ( $T$ ) and the Reynolds number  
258 (Eq. 5). The viscous sub-layer in contact with a smooth wall is computed from a linear  
259 relationship between the mean velocity ( $U$ ), wall shear stress ( $\tau_w$ ), viscosity ( $\mu$ ), and the distance  
260 from the wall ( $y$ ) (Eq. 6) (Pope & Pope, 2000; Versteeg & Malalasekera, 2007).

261  $\eta = \frac{l}{Re^{3/4}}$  Eq. 4

262  $\tau = \frac{T}{Re^{1/2}}$  Eq. 5

263  $y = \mu \frac{U}{\tau_w}$  Eq. 6

264 The characteristic length of the flat-panel photobioreactor and open raceway pond are 0.20  
265 m. and 0.46 m., respectively. The Reynolds number of the flat-panel photobioreactors for mixing  
266 energy inputs of 0.03 W.m<sup>-3</sup>, 0.47 W.m<sup>-3</sup>, and 0.97 W.m<sup>-3</sup> are 2.9E<sup>2</sup>, 3.6E<sup>2</sup>, and 4.1E<sup>2</sup>,  
267 respectively. For the case of the open raceway pond, the Reynolds number at 0.1 W.m<sup>-3</sup>, 0.7  
268 W.m<sup>-3</sup>, and 2.1 W.m<sup>-3</sup> are 3.5E<sup>4</sup>, 6.8E<sup>4</sup>, and 9.3E<sup>4</sup>, respectively. The wall distance at 0.1 W.m<sup>-3</sup>,  
269 0.7 W.m<sup>-3</sup>, and 2.1 W.m<sup>-3</sup> are 0.0009 m, 0.0005 m, and 0.0002 m, respectively. We designed the

270 meshes of the flat-panel photobioreactor and open raceway pond at length scales of 0.0008 m.  
271 and 0.002 m., respectively, in Trelis 16.3. We developed CFD models in ANSYS Fluent 16.1 for  
272 the flat-panel photobioreactor and open raceway pond. The inlet velocity measured from PIV and  
273 ADV (Sections 2.3.1 and 2.3.2), and the turbulence intensities, were used as boundary conditions  
274 for the flat-panel photobioreactor and open raceway pond. The finite volume method was  
275 selected to guarantee conservation of mass, and Direct Numerical Simulation (DNS) was applied  
276 (Moin & Mahesh, 1998; Versteeg & Malalasekera, 2007). The time steps used for flat-panel  
277 photobioreactors CFD simulations were 0.02 seconds for mixing energy inputs of  $0.03 \text{ W.m}^{-3}$ ,  
278  $0.47 \text{ W.m}^{-3}$ , and  $0.97 \text{ W.m}^{-3}$ . We performed CFD simulations for the case of the open raceway  
279 pond, at  $0.1 \text{ W.m}^{-3}$ ,  $0.7 \text{ W.m}^{-3}$ , and  $2.1 \text{ W.m}^{-3}$  at time steps of 0.2, 0.1, and 0.05 seconds,  
280 respectively. We validated the CFD results against experimental velocity in x-velocity data. This  
281 validation was accomplished by comparing the experimental and CFD results as illustrated for  
282 the open raceway pond in the Supplementary Material (Figure A5). In figure A5, we represent  
283 the height ( $y$ ) of the reactor normalized to half the water column ( $H/2$ ) as a function of the  
284 normalized velocity, defined as the final velocity normalized to the velocity at half the water  
285 column.

286 To understand the influence of turbulent mixing on the motion of photoautotrophic  
287 microorganisms, we computed artificial particle tracks in the flat-panel photobioreactor and open  
288 raceway pond by integrating the CFD velocity field (Pope & Pope, 2000). Using particle tracks  
289 to model the paths of the cyanobacteria cells in the raceway or photobioreactor assumes that the  
290 cells are neutrally buoyant and that inertial forces dominate over gravity and buoyancy forces.  
291 From the particle tracks ( $x(n), x(n - 1)$ ), we computed the frequency of motion of these  
292 particles in the depth or  $y$ -axis of the reactors with respect to the moving average of each particle

293 position. The moving average ( $y(n)$ ) is computed as the mean value by considering an equal  
 294 number of data points at each side of the central value, known as the sample window (SW) (Eq.  
 295 7) (Schafer & Oppenheim, 1989). The sample window for the flat-panel photobioreactor and  
 296 open raceway pond are 100 and 1000 points. Lastly, the natural frequency ( $f$ ) is computed as the  
 297 number of oscillations ( $n$ ) cyanobacteria cells pass by the top of the chamber, divided by the  
 298 time length ( $L_T$ ). The time length of the flat-panel photobioreactors and the open raceway pond  
 299 are 60 seconds and 15 seconds.. The moving average and frequency were computed from five  
 300 samples for the flat-panel photobioreactor and open raceway pond.

$$301 \quad y(n) = \frac{1}{SW} * (x(n) + x(n - 1) + \dots + x(n - (SW - 1))) \quad \text{Eq 7}$$

$$302 \quad f = \frac{n}{L_T} \quad \text{Eq 8}$$

303 To understand the spectrum and dissipation of eddies as a function of mixing energy inputs  
 304 in the open raceway ponds, we computed the spectral energy and turbulent dissipation rate (Pope  
 305 & Pope, 2000; Versteeg & Malalasekera, 2007). The calculation of the spectral energy ( $\varepsilon$ ) can  
 306 vary in the wavelength as denoted in equations 11 to 13, being a function of viscosity ( $\nu$ )  
 307 (Equation 9), turbulence kinetic energy ( $k$ ),  $\alpha \sim 1.5$ , wavenumber ( $\omega$ ) (Equation 10),  
 308 characteristic length ( $l$ ), and the mean velocity ( $u$ ) (Pope & Pope, 2000; Versteeg &  
 309 Malalasekera, 2007). The turbulent dissipation rate is a function of  $c_\mu \sim 0.09$ ,  $k$ , and  $l$  (Pope &  
 310 Pope, 2000). Spectral energy and turbulent dissipation rate were computed in the open raceway  
 311 pond at mixing energy inputs  $0.1 \text{ W.m}^{-3}$ ,  $0.7 \text{ W.m}^{-3}$ , and  $2.1 \text{ W.m}^{-3}$ .

$$312 \quad \nu = \mu / \rho \quad \text{Eq 9}$$

$$313 \quad \omega = 2 * \pi / \eta \quad \text{Eq 10}$$

$$314 \quad S = \nu^{5/4} * k^{1/4} \quad \text{For } \eta \leq 0.001 \quad \text{Eq 11}$$

$$315 \quad S = \alpha * \omega^{-5/3} * k^{2/3} \quad \text{For } l \geq \eta \geq 0.001 \quad \text{Eq 12}$$

316  $S = l * u^2$  *For  $\eta \geq l$*  Eq 13

317  $\varepsilon = c_{\mu}^{3/4} * \frac{k^{3/2}}{l}$  Eq 14

318 **3. Results and Discussion**

319 We synthesize the results of this research into three aspects. First, we present the flat-panel  
320 photobioreactor experimental fluid mechanics results and discuss the motion in these systems.  
321 Second, we present the open raceway pond experimental fluid mechanics results and focus the  
322 discussion on novel contributions to the field by understanding the turbulence intensities with  
323 differences in mixing energy input. Third, we evaluate the impact of differences in mixing  
324 energy inputs in the motion of photoautotrophic microorganisms by applying the validated CFD  
325 models to both flat-panel photobioreactors and open raceway ponds.

326 **3.1 Flat-panel photobioreactor flow characterization**

327 The velocity field of the flat-panel photobioreactor at low and high mixing energy inputs are  
328 illustrated in Figure 4. The mean velocity computed from PIV at mixing energy inputs of 0.47  
329  $\text{W.m}^{-3}$ , 0.97  $\text{W.m}^{-3}$  and 1.94  $\text{W.m}^{-3}$  are 0.015  $\text{m.s}^{-1}$ , 0.018  $\text{m.s}^{-1}$ , and 0.020  $\text{m.s}^{-1}$ , respectively.  
330 For mixing energy inputs of 0.47  $\text{W.m}^{-3}$ , 0.97  $\text{W.m}^{-3}$  and 1.94  $\text{W.m}^{-3}$  the turbulence intensities  
331 are 1.4%, 1.2%, and 1.0%, respectively. Turbulent dissipation for these mixing energy inputs are  
332  $1.3\text{E}^{-5} \text{ m}^2.\text{s}^{-3}$ ,  $1.7\text{E}^{-5} \text{ m}^2.\text{s}^{-3}$ , and  $1.5\text{E}^{-5} \text{ m}^2.\text{s}^{-3}$ .

333 These turbulence dissipation rates we obtained are from about four order of magnitudes  
334 smaller than those used by Xiao et al. (2016), in their measurements of maximized phosphorous  
335 uptake rates and growth decay in different cyanobacteria strains. These results demonstrate the  
336 significant differences in the fluid environments maintained under industrially relevant mixing  
337 energy inputs relative to laboratory conditions, impacting the biological responses of  
338 photoautotrophic microorganisms.

339 The buoyancy of air bubbles supplied by the air sparger drives the flow circulation in the  
340 pilot flat-panel photobioreactors. Buoyancy of an air bubble is a function of bubble size, and the  
341 orifice size primarily dictates the bubble sizes on the air sparger. This physics can be analytically  
342 described by Stokes Equation (Eq. 15). For small bubbles shaped as spheres due to surface  
343 tension, the bubble velocity is a function of gravity ( $g$ ), bubble diameter ( $d$ ), dynamic viscosity  
344 of liquid ( $\mu$ ), density of liquid ( $\rho_{Water}$ ), and the density of air bubble ( $\rho_{Air\ Bubble}$ ) (Stokes, 1880;  
345 Talaia, 2007). Because bubble buoyancy and therefore bubble velocity is relatively constant at  
346 all sparge rates, the velocity of the entrained fluid above the air sparger is relatively constant.  
347 The flow circulation in the flat-panel photobioreactors, as a result, is relatively constant over the  
348 span of industrially relevant mixing energy inputs studied in our research.

$$349 \text{ Velocity} = \frac{1}{18} * g * d^2 \left( \frac{\rho_{Water} - \rho_{Air\ Bubble}}{\mu} \right) \quad \text{Eq. 15}$$

350 This model explains how the experimentally measured mean velocity of the photobioreactors  
351 is relative constant, even under a 4x increase in mixing energy.

### 352 3.2 Pilot-scale open raceway pond flow characterization

353 By applying experimental ADV, we seek to understand turbulence as a function of  
354 industrially relevant mixing energy inputs in pilot open raceway ponds. The experimental  
355 velocity components (x, y, z) downstream of the raceway paddle wheel are illustrated for the 2.1  
356  $W.m^{-3}$  mixing energy input in Figure 5. The Supplementary Material (Figure A2) illustrates the  
357 instantaneous velocity measured at each point in the cross-section. We computed the velocity  
358 magnitude, turbulence dissipation rates, and turbulence intensities from these experimental data.  
359 Turbulence intensities, downstream from the raceway paddlewheel, are illustrated in Figure 6.

360 We used these experimental velocities and turbulence intensities as boundary conditions  
361 of the CFD models. We computed the velocity field of the fluid domain in the open raceway

362 pond by CFD models at mixing energy inputs  $0.1 \text{ W.m}^{-3}$ ,  $0.7 \text{ W.m}^{-3}$ , and  $2.1 \text{ W.m}^{-3}$  (Figure 7 and  
363 Figure A3). Figure 7 illustrates the velocity field of the CFD model at mixing energy inputs of  
364  $0.1 \text{ W.m}^{-3}$ . We validated the CFD models against experimental data measured at the 2nd and 3rd  
365 cross-section of the open raceway pond, located in the first turn and the straight channel as  
366 illustrated in the Supplementary Material (Figure A1 and A5).

367 These results demonstrate that previous studies applying CFD to open raceway ponds  
368 have overestimated boundary condition and mean turbulence intensities. At mixing energy inputs  
369 of  $0.1 \text{ W.m}^{-3}$ ,  $0.7 \text{ W.m}^{-3}$ , and  $2.1 \text{ W.m}^{-3}$  the velocity magnitudes computed from the experimental  
370 ADV data downstream of the raceway paddlewheel are  $0.08 \text{ m.s}^{-1}$ ,  $0.15 \text{ m.s}^{-1}$ , and  $0.21 \text{ m.s}^{-1}$ .  
371 Turbulence dissipation rates at these industrially relevant mixing energy inputs are  $6.1\text{E}^{-4} \text{ m}^2/\text{s}^3$ ,  
372  $2.8\text{E}^{-3} \text{ m}^2/\text{s}^3$ , and  $1.1\text{E}^{-2} \text{ m}^2/\text{s}^3$ . For example, turbulence dissipation rates at mixing energy  
373 inputs of  $0.1 \text{ W.m}^{-3}$  and  $0.7 \text{ W.m}^{-3}$  were found to be three and two order of magnitudes smaller  
374 than used by Xiao et al. (2016).

375 Turbulence intensities computed from our experimental work in a pilot open raceway  
376 pond at  $0.1 \text{ W.m}^{-3}$ ,  $0.7 \text{ W.m}^{-3}$ , and  $2.1 \text{ W.m}^{-3}$  are 1.02%, 1.05%, and 1.25%, respectively (Figure  
377 9.6). We observed low-quality data in the upper left point at a mixing energy input of  $0.1 \text{ W.m}^{-3}$ ,  
378 with a low signal-to-noise ratio (below ten with no significant implication for the average value  
379 calculation). The turbulence intensities used by Labatut et al. (2015) are about three to four times  
380 higher than what our research has measured at industrially relevant mixing energy inputs.. The  
381 turbulence intensities used by Drewry et al. (2015), Pires et al. (2017), and Zhang et al. (2017)  
382 are four to ten times higher than was found in our experimental work. Overestimated turbulence  
383 intensities, as a result, can impact the flow dynamics and turbulence in these open raceway  
384 ponds, leading to erroneous CFD results. By validating our CFD model with ADV data under

385 different mixing energy inputs, we have found that the results of the CFD models were sensitive  
386 to these boundary conditions, including velocity profiles and turbulence intensities. The  
387 Supplementary Material (Figure A5) illustrates the validation of the open raceway pond CFD  
388 model.

### 389 3.3 Differences in mixing energy have no significant impact on the frequency of cells motion

390 Finally, we observed that varying mixing energy inputs had no significant effect on the  
391 frequency of fluid motion in the flat-panel photobioreactors and open raceway ponds. By  
392 conducting experimental and computational fluid mechanics, we have demonstrated that the  
393 frequencies of light/dark cycling experienced by photoautotrophic microorganisms cultures in  
394 flat-panel photobioreactors and open raceway are not influenced at industrially relevant mixing  
395 energy inputs. We have demonstrated this by computing the frequency of this light/dark cycling  
396 (Figure 8) from randomly selected particles traveling in the flat-panel photobioreactor and open  
397 raceway pond (Figure A4).

398 In the flat-panel photobioreactor, the frequency of motion of the photoautotrophic  
399 microorganisms is driven by the buoyancy of air bubbles, in which frequencies of this motion at  
400 mixing energy inputs of  $0.47 \text{ W}\cdot\text{m}^{-3}$ ,  $0.97 \text{ W}\cdot\text{m}^{-3}$ , and  $1.94 \text{ W}\cdot\text{m}^{-3}$  are 0.036 Hz, 0.032 Hz, and  
401 0.038 Hz, respectively. By performing a one-way analysis of variance (ANOVA), we conclude  
402 that differences in mixing energy inputs have no significant impact on the frequencies of fluid  
403 motion (and therefore organism light exposure), as illustrated in Figure 8. The frequencies of  
404 flashing lights used by Janssen, Tramper, Mur, & Wijffels (2003) and Vejrazka, Janssen,  
405 Streefland, & Wijffels (2011, 2012) are from about 13 to 300 times higher than observed in our  
406 experimental work at industrially relevant mixing energy inputs. Our frequencies of motion are  
407 consistent with the frequencies studied by Grobbelaar (1991) and the frequencies estimated for

408 fermenters by M. Y. Chisti (1989). Our results demonstrate that the buoyancy of air bubbles  
409 drives flow circulation in flat-panel photobioreactors, maintaining a relatively constant  
410 circulation in the reactor regardless of variation in mixing energy input.

411 In the pilot open raceway pond, the frequency of motion of the photoautotrophic  
412 microorganisms is not significantly impacted by changes in industrially relevant mixing energy  
413 inputs. Frequencies of motion at mixing energy inputs of  $0.1 \text{ W}\cdot\text{m}^{-3}$ ,  $0.7 \text{ W}\cdot\text{m}^{-3}$ , and  $2.1 \text{ W}\cdot\text{m}^{-3}$   
414 are 0.272 Hz, 0.364 Hz, and 0.358 Hz. By performing a one-way ANOVA of these frequencies,  
415 we found no significant impact due to differences in mixing energy input (Figure 8). Similar to  
416 the results for the photobioreactors, the frequencies of flashing lights used by Janssen, Tramper,  
417 Mur, & Wijffels (2003) and Vejrazka, Janssen, Streefland, & Wijffels (2011, 2012) are from  
418 about 1 to 40 order of magnitudes higher than observed in our experimental work at industrially  
419 relevant mixing energy inputs. Our frequencies of motion are consistent with the frequencies  
420 estimated for airlift reactors by M. Y. Chisti (1989). Since the light/dark cycling frequencies  
421 experienced by the photoautotrophic cells are not significantly impacted by mixing energy input,  
422 our research suggests that well-mixed conditions exist at the mixing energy levels used in  
423 industrial open raceway ponds, and that increased mixing rates do not improve cultivation  
424 productivity by changing the light regime of the culture.

425 The spectral energy computed for mixing energy inputs in a pilot open raceway pond at  
426  $0.1 \text{ W}\cdot\text{m}^{-3}$ ,  $0.7 \text{ W}\cdot\text{m}^{-3}$ , and  $2.1 \text{ W}\cdot\text{m}^{-3}$  (Figure 9) follows the vortex stretching process described  
427 in the turbulence literature including Pope & Pope (2000) and Versteeg & Malalasekera (2007).  
428 In this process, the largest eddies extract energy from the mean velocity, eddies are stretched as  
429 one end moves faster than the other end, and angular momentum is conserved as eddies are  
430 dissipated. Therefore, as eddies dissipate, the rotation of eddies increase and cross-section radius

431 of eddies decrease. Dissipation of energy occurs faster at higher mixing energy inputs, 0.7 W.m<sup>-3</sup>  
432 and 2.1 W.m<sup>-3</sup> as illustrated in figure 9, where turbulence kinetic energy and turbulent dissipation  
433 rate are higher. The characteristic length ( $L$ ) is theoretically constant regardless of mixing energy  
434 input, as it is theoretically a function of the open channel height ( $H$ ) and width ( $W$ ) of the open  
435 raceway pond (Eq. 16). The convective time scales, however, are reduced with increased mixing  
436 energy because increases in the input velocity magnitude ( $U$ ) increases the frequency of largest  
437 eddies in the system (Eq. 17). Although input velocity magnitudes at high mixing energy inputs  
438 (2.1 W.m<sup>-3</sup>) are about three times higher than at low mixing energy inputs (0.1 W.m<sup>-3</sup>), kinetic  
439 energy is dissipated about 18 times faster at mixing energy inputs of 2.1 W.m<sup>-3</sup> as illustrated in  
440 the experimental turbulence dissipation rates in section 3.2 and in the Supplementary Material  
441 (Figure A6). This analysis suggests that despite the increase of largest eddy frequency (Figure 9)  
442 at high mixing energy inputs, turbulence dissipation decreases the frequency of cell motion in  
443 open raceway ponds (Figure 8).

$$444 \quad L = \frac{4*H*W}{2*H+W} \quad \text{Eq. 16}$$

$$445 \quad \textit{Convective Time Scales} = \frac{L}{U} \quad \text{Eq. 17}$$

446 These results demonstrate that differences in mixing energy input have no significant impact  
447 on the overall light/dark cycling frequencies experienced by photoautotrophic cells in pilot flat-  
448 panel photobioreactors and open raceway ponds. These results provide evidence to disprove the  
449 hypothesis that light regime experienced by photoautotrophic organisms influences their  
450 productivity, over the range of industrially relevant mixing energies and mechanisms considered  
451 here. Alternative hypotheses, describing the effects of mixing energy input on the thermal,  
452 chemical, and biological response of these organisms is not addressed in this research.

#### 453 4. Conclusions

454 A combination of experimental and computational fluid mechanics measurements has been  
455 used to quantify the mixing conditions in pilot flat-panel photobioreactors and open raceway  
456 ponds. Our experimental and computational work has demonstrated that differences in mixing  
457 energy do not have a significant impact on the frequency of microorganisms' motion within the  
458 cultivation systems, and therefore do not influence the light/dark dynamics of the light regime  
459 experienced during cultivation. These measurements provide new boundary condition  
460 measurements as inputs for photobioreactor and raceway pond CFD practitioners, and  
461 demonstrate CFD results validated using a variety of experimental techniques.

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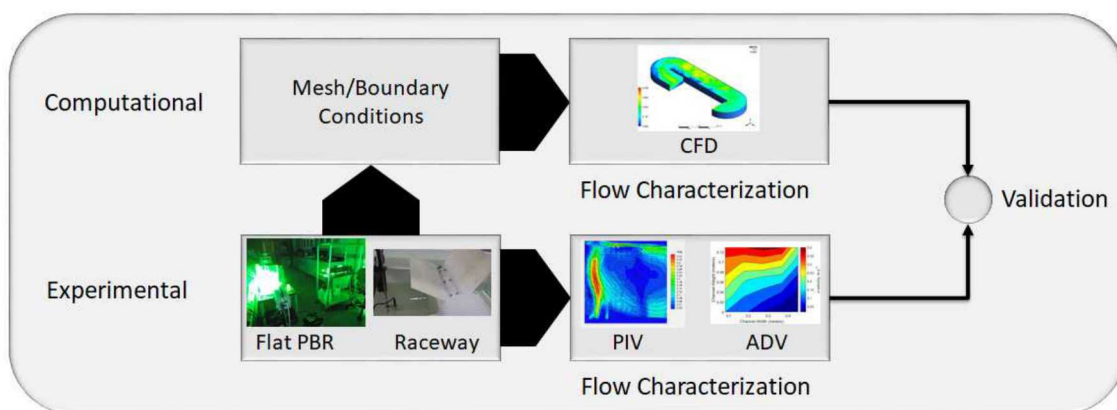
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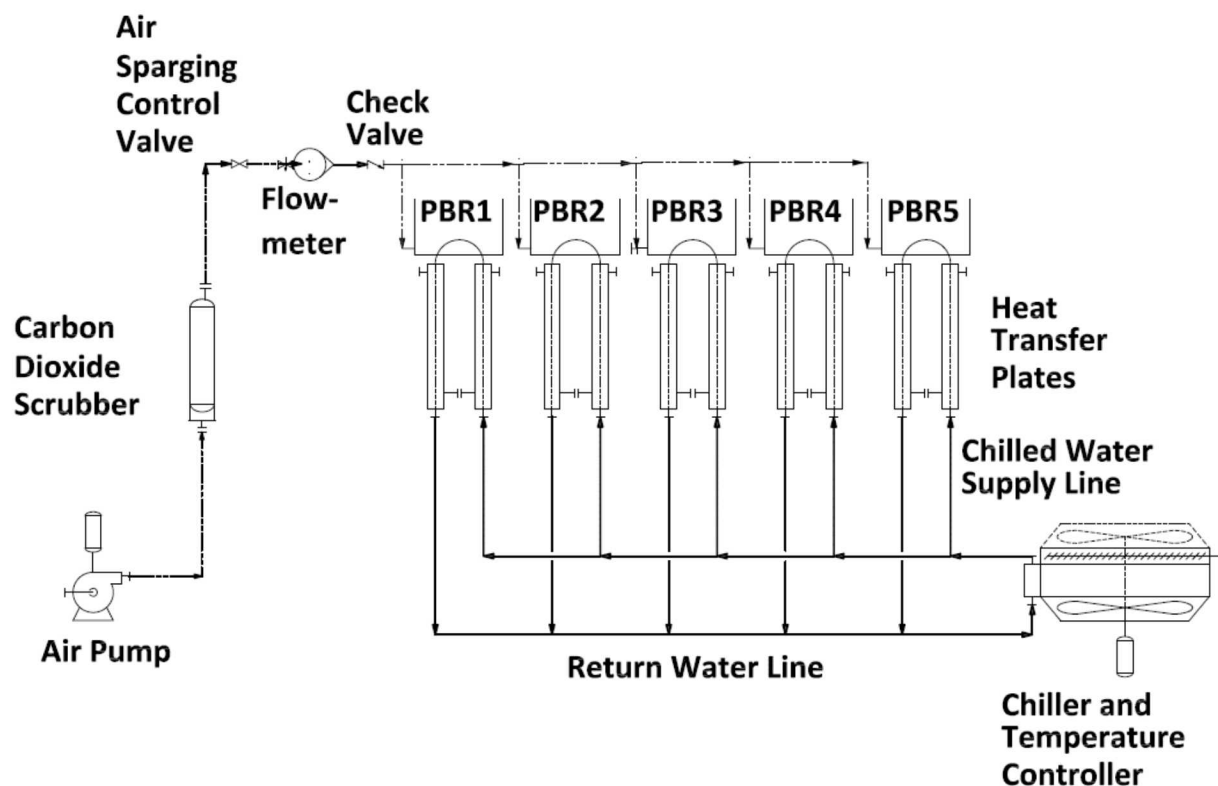


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696 Figure 1. Workflow for experimental and computational fluid mechanics (top flow) and  
697 photoautotrophic growth (bottom flow) to assess the impact of mixing energy inputs.

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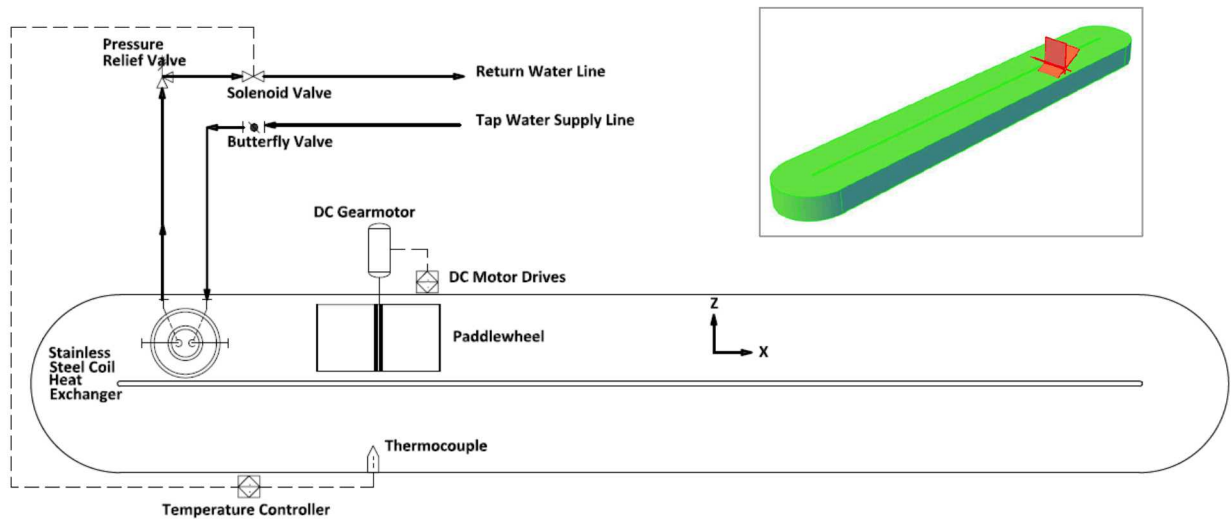


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701 Figure 2. Instrumentation Diagram of Flat-panel photobioreactors system for experimental and  
702 model-based analysis.

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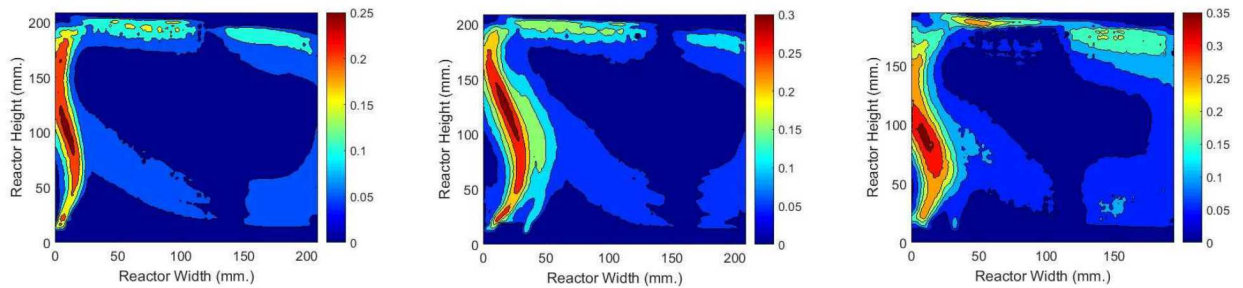
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706 Figure 3. Plan View and Instrumentation Diagram of Open raceway pond system for industrial  
707 scale experimental and model-based analysis. The 3D view in the upper right corner illustrates  
708 the Open Raceway Pond.

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711 Figure 4. Velocity field ( $\text{m}\cdot\text{s}^{-1}$ ) obtained from PIV of flat-panel photobioreactor at mixing energy  
712 inputs of  $0.47 \text{ W}\cdot\text{m}^{-3}$  (left figure),  $0.97 \text{ W}\cdot\text{m}^{-3}$  (middle figure), and  $1.94 \text{ W}\cdot\text{m}^{-3}$  (right figure).

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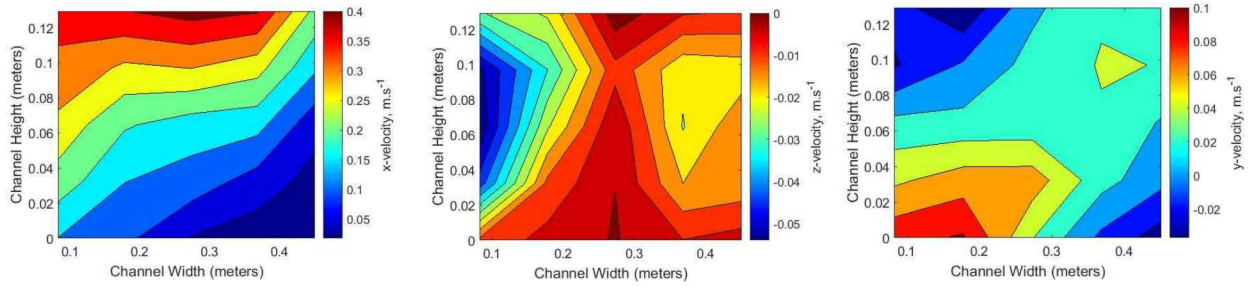
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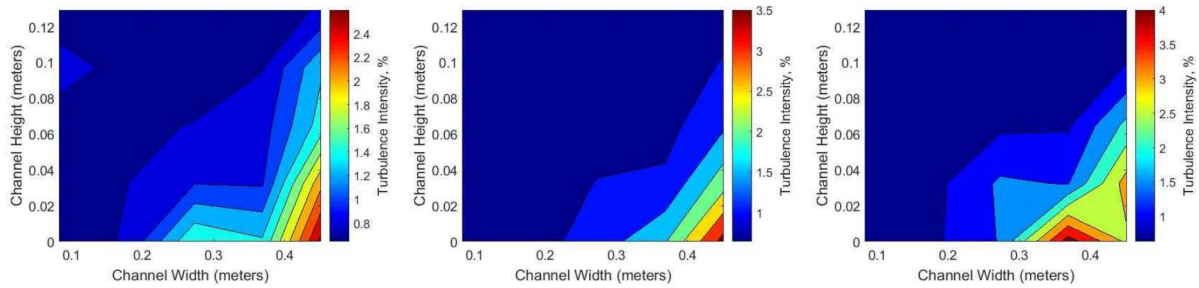
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725 Figure 5. First cross section (downstream paddlewheel) velocity components ( $\text{m.s}^{-1}$ ) of open  
726 raceway pond at mixing energy input of  $2.1 \text{ W.m}^{-3}$ . The left figure corresponds to the x-velocity,  
727 the middle figure corresponds to the y-velocity, and the right figure corresponds to the z-  
728 velocity.

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731 Figure 6. Turbulence intensities (%) of first cross section of open raceway pond at mixing energy  
732 inputs of  $0.1 \text{ W.m}^{-3}$  (left figure),  $0.7 \text{ W.m}^{-3}$  (middle figure) and  $1.94 \text{ W.m}^{-3}$  (right figure).

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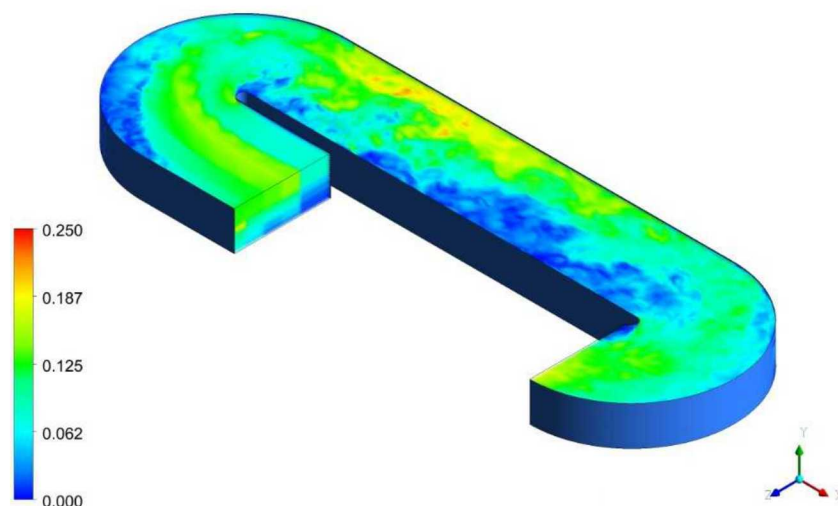


Figure 7. Velocity field ( $\text{m}\cdot\text{s}^{-1}$ ) from Direct Numerical Simulation-based CFD model of open raceway pond at mixing energy inputs of  $0.1 \text{ W}\cdot\text{m}^{-3}$ .

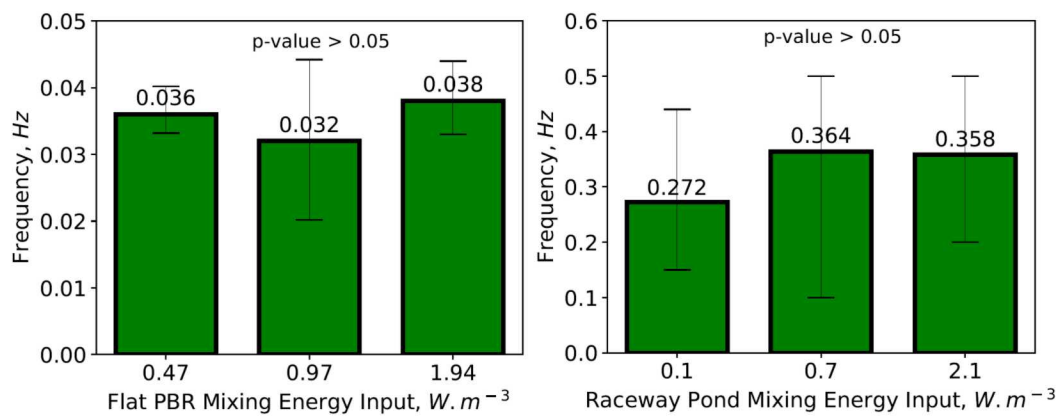
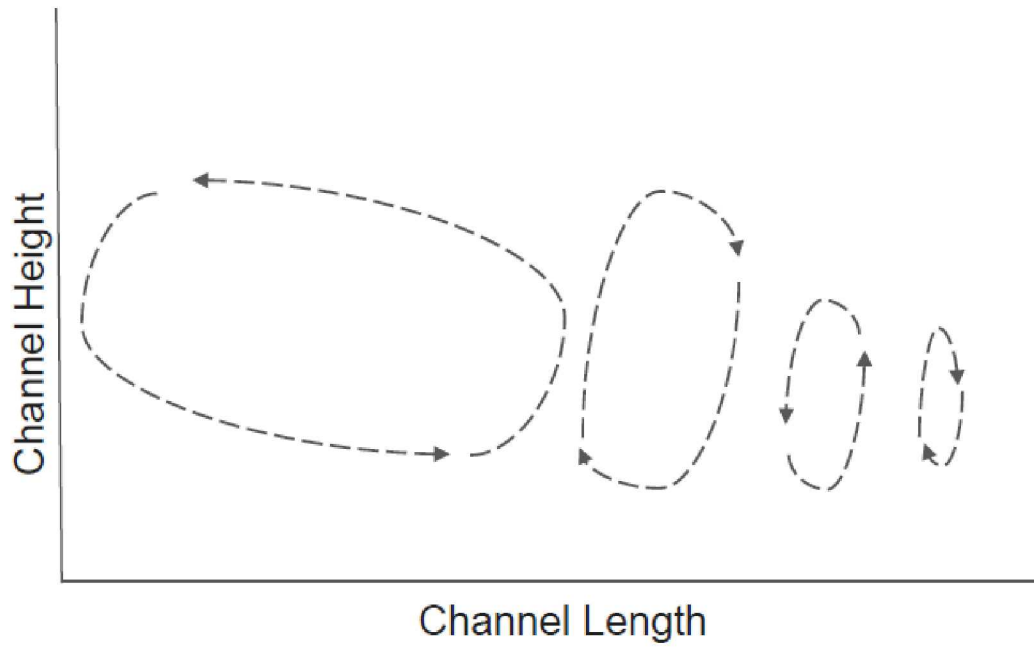
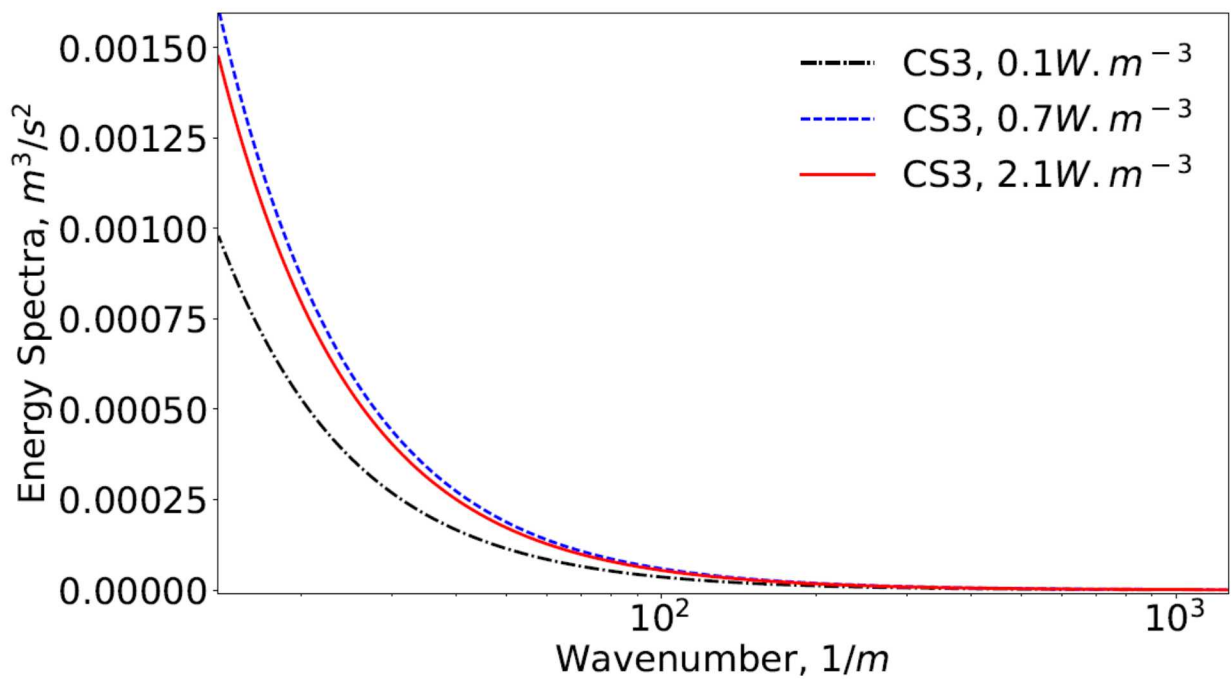


Figure 8. The frequency of photoautotrophic microorganism cell motion in flat-panel photobioreactor (left figure) and open raceway pond (right figure).

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770 Figure 9. Energy Spectra at the straight channel (CS3) in open raceway pond at mixing energy  
771 inputs of  $0.1 W \cdot m^{-3}$ ,  $0.7 W \cdot m^{-3}$ , and  $1.94 W \cdot m^{-3}$  computed from experimental ADV data.

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775 **Supplementary Material: Pilot-scale open raceway ponds**  
776 **and flat-panel photobioreactors maintain well-mixed**  
777 **conditions under a wide range of mixing energy inputs**

778

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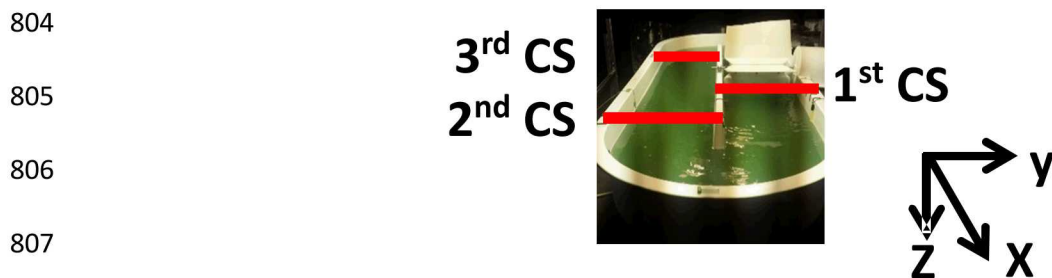
784 <sup>4</sup>Department of Biomedical Engineering, The Ohio State University, Columbus, OH 43210, USA

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786 1. [Experimental and Computational Fluid Dynamics of Open Raceway Pond](#)

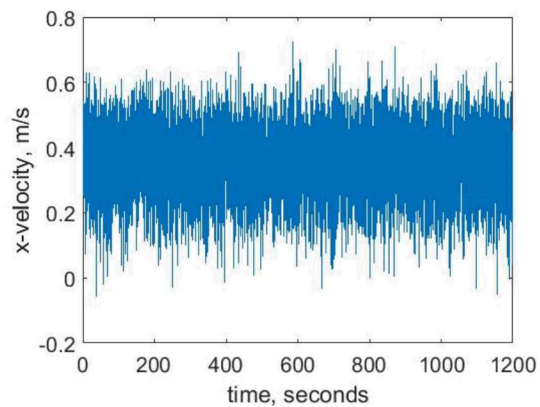
787 To understand the frequency of photoautotrophic microorganism's motion in flat-panel  
788 photobioreactors and open raceway ponds, we obtained particle tracks from the CFD models in a  
789 Lagrangian representation of the flow. The finite volume method was selected to guarantee the  
790 conservation of mass, and Direct Numerical Simulation (DNS) was applied to obtain precise  
791 details of turbulence (Moin & Mahesh, 1998; Versteeg & Malalasekera, 2007), influencing the  
792 motion of photoautotrophic microorganisms. We computed the velocity field of the fluid domain  
793 in the open raceway pond by CFD models at mixing energy inputs  $0.1 \text{ W}\cdot\text{m}^{-3}$ ,  $0.7 \text{ W}\cdot\text{m}^{-3}$ , and  $2.1$   
794  $\text{W}\cdot\text{m}^{-3}$  (Figure 7 and Figure A3). Figure 7 illustrates the velocity field of the CFD model at  
795 mixing energy inputs of  $0.1 \text{ W}\cdot\text{m}^{-3}$ . We validated the CFD models against experimental data

796 measured at the second and third cross-section of the open raceway pond, located in the first turn  
797 and the straight channel as illustrated in the Supplementary material (Figure A1 and A5). By  
798 integrating experimental and computational fluid mechanics, we have represented the physics in  
799 pilot scale environments, demonstrating the fluid dynamics in flat-panel photobioreactors and  
800 open raceway ponds do not influence the overall light experienced by photoautotrophic  
801 microorganisms cultures. We have demonstrated this by computing the frequency of this motion  
802 (Figure 8) from randomly selected particles traveling in the flat-panel photobioreactor and open  
803 raceway pond (Figure A4).



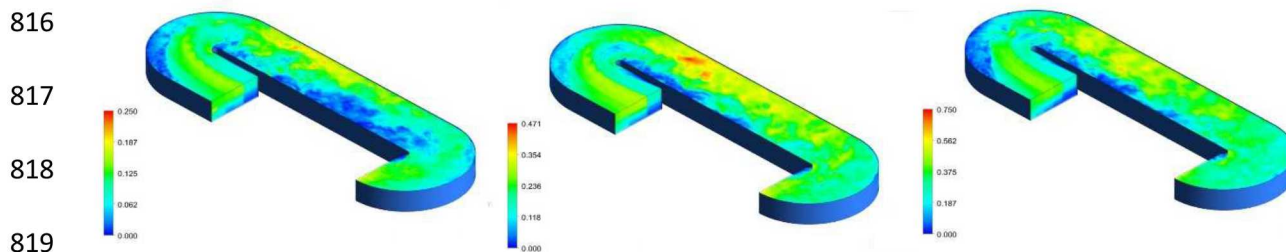
808 Figure A1. Open raceway pond Coordinates. The x-velocity follows the flow direction  
809 downstream the paddlewheel. The y-velocity points toward the vertical wall of the raceway  
810 pond. The z-velocity point towards the bottom of the raceway pond. The first cross-section (CS)  
811 is located downstream of the paddlewheel. The second CS is located on the first turn of the  
812 channel. The third CS is located in the straight channel behind the paddlewheel.

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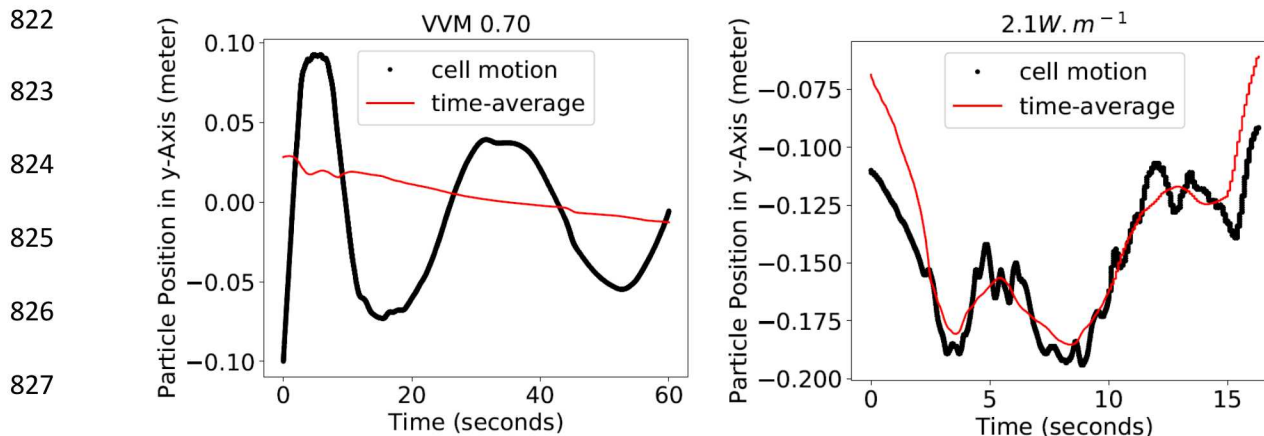
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815 Figure A2. Example of instantaneous velocity measured in open raceway pond by ADV.



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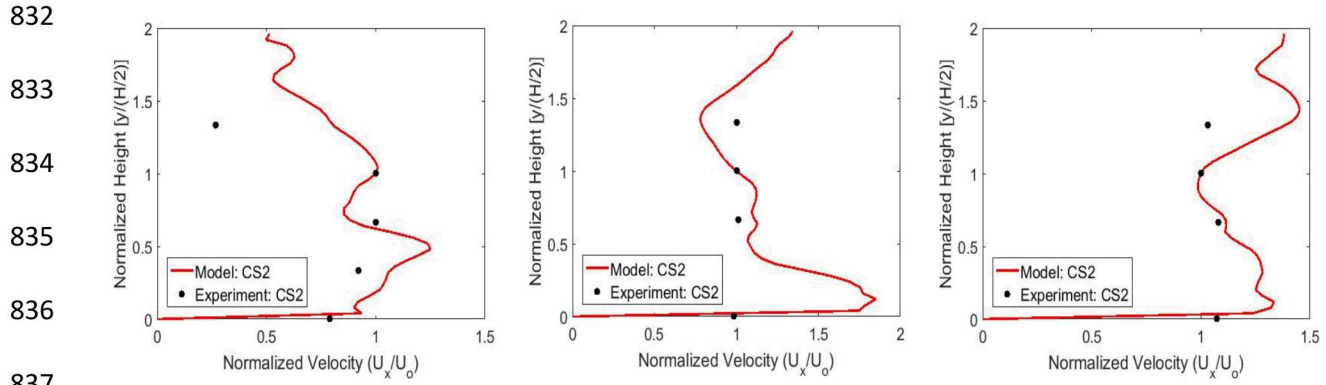
820 Figure A3. DNS based CFD model of open raceway pond at mixing energy inputs of  $0.1 \text{ W.m}^{-3}$   
 821 (left figure),  $0.7 \text{ W.m}^{-3}$  (middle figure) and  $1.94 \text{ W.m}^{-3}$  (right figure).



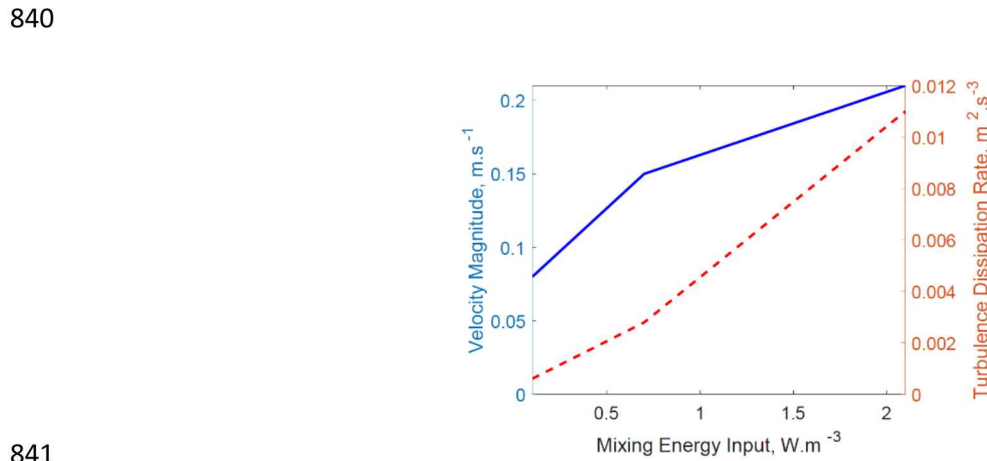
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829 Figure A4. Photoautotrophic microorganism cell motion open raceway pond at flat-panel  
 830 photobioreactor (left figure) and open raceway pond (right figure).

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838 Figure A5. Validation of DNS based CFD model of open raceway pond at mixing energy inputs  
 839 of 0.1 W.m-3 (left figure), 0.7 W.m-3 (middle figure) and 1.94 W.m-3 (right figure).



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842 Figure A6. Experimental input velocity magnitude and turbulence dissipation rate as a function  
 843 of mixing energy input in the open raceway pond.

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