

# Performance Subtask: Update from Sandia National Laboratories

Irina Tezaur and Jerry Watkins

SNL Staff: L. Bertagna, M. Perego, I. Tezaur (subtask lead), R. Tuminaro, J. Watkins

Sandia National Laboratories, Livermore, CA 94587



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# Summary of performance subtask

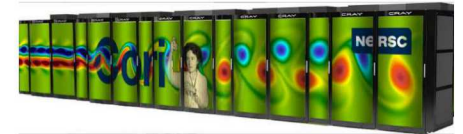


## Sub-project focus:

- **Performance** of Albany Land-Ice (ALI) stress-velocity: solver must be scalable, fast, robust.
  - ALI diagnostic solve is comprised of **finite element assembly (FEA)** and **linear solve**. Each takes ~50% of CPU time.
- **Performance portability** of ALI solver stress-velocity: solver must run correctly and efficiently on up-and-coming and future architectures (e.g., multi-core, many-core, GPU, Intel Xeon Phi, etc.)
  - SNL's strategy for performance portability focuses on **Kokkos**: C++ open-source library that provides performance-portability across diverse devices with different memory models using MPI+X
- Task includes **improved time-stepping methods** for e.g., temp.-velocity coupling in MALI.

## Importance/broader ties:

- For initialization, UQ, and predictive dynamic runs, solver needs to run as fast as possible.
- Running on up-and-coming architectures (e.g., Summit, Aurora) is critical.
- ALI is the basis of MPAS-Albany-Land-Ice (MALI) dynamical core.
- Pieces developed (e.g., linear solvers implemented in Trilinos) could be useful to other dycores.



# Year 1 and 2 SNL tasks/deliverables

Year	Task	Institutions	Joint with subgroup	Status
1	Finish Kokkos ALI FE refactor for velocity; port/optimize for current GPU/Phi	SNL		mostly complete
2	Kokkos ALI FE refactor for temperature & hydrology; port/optimize for current GPU/Phi	SNL		deferred to year 3
1	Deliver robust solvers/preconditioners for temperature model	SNL		in progress
2	Improve time-stepping method for thickness evolution (implicit/obstacle formulation)	SNL, LBNL, LANL	Other development*	deferred to year 3

## More Detailed Status

### ***Performance portability via Kokkos [J. Watkins, I. Tezaur]:***

- Kokkos refactor/optimization of FEA in stress-velocity solver: **mostly complete**
- Kokkos refactor of FEA for temperature/hydrology: **deferred to year 3**

### ***Linear solver performance [R. Tuminaro, I. Tezaur, M. Perego]:***

- Robust solvers/preconditioners for temperature model: **in progress**
- Performance improvements of semi-coarsening-based AMG preconditioner in MueLu for stress-velocity solver (remnant from PISCEES): **in progress**

### ***Improved time-stepping method for thickness evolution [M. Perego, L. Bertagna, I. Tezaur, R. Tuminaro]:*** **deferred to year 3**

- Infrastructure work in Albany to enable multi-physics/block preconditioning: **in progress**

\* Albany infrastructure work to enable modular multi-physics and block preconditioning (SNL, Yrs 1-2)

# Performance portability via Kokkos

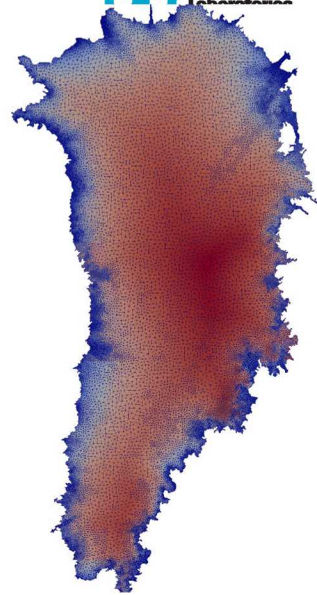
SNL staff: J. Watkins, I. Tezaur

**Task 1 [yr 1]:** Finish Kokkos ALI FE refactor for velocity; port/optimize for current GPU/Phi

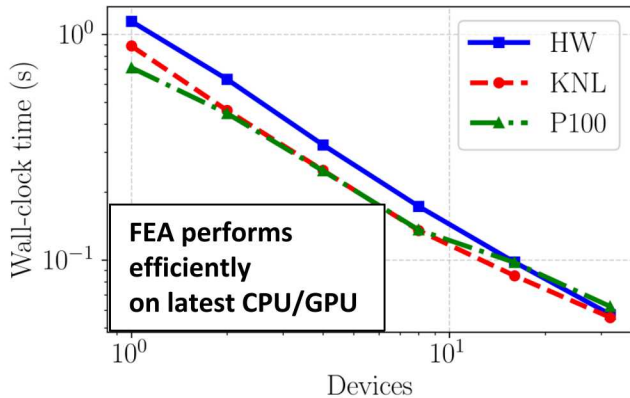
**Task 2 [yr 2]:** Kokkos ALI FE refactor for temperature & hydrology

## Status:

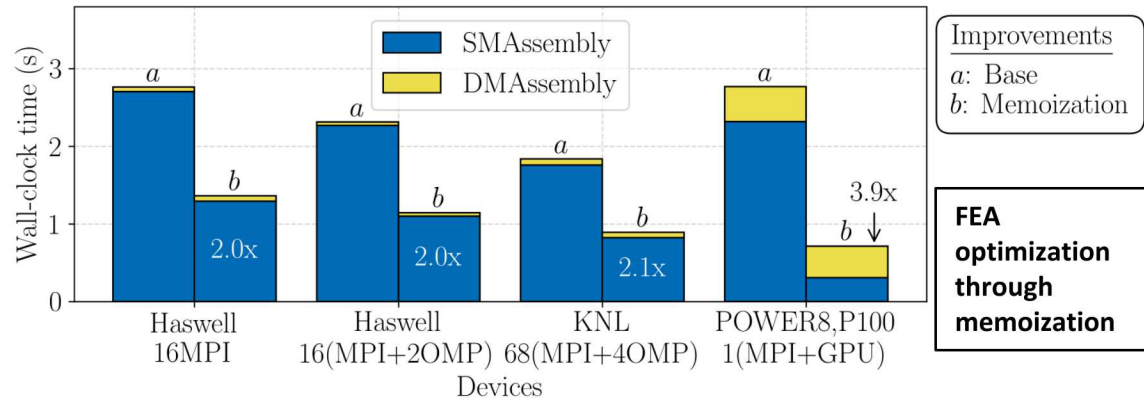
- Task 1 is complete\* (see figures) but still needs work:
  - Boundary conditions need to be refactored to work well on GPUs and future CPUs.
  - Optimization strategies need to be generalized for more flexibility.
- Task 2 deferred to year 3, as temperature and hydrology solvers are not mature yet.



### Strong Scalability



### Single CPU/GPU Performance



Improvements  
a: Base  
b: Memoization

FEA optimization through memoization

# Performance portability via Kokkos

SNL staff: J. Watkins, I. Tezaur

**Task 1 [yr 1]**: Finish Kokkos ALI FE refactor for velocity; port/optimize for current GPU/Phi

**Task 2 [yr 2]**: Kokkos ALI FE refactor for temperature & hydrology



## **Challenges:**

- Task 1: Component based design makes it difficult to refactor/optimize
  - flexibility vs. performance
- Task 2: This task will share similar challenges as task 1



## **Mitigation strategy/next steps:**

- Task 1: Currently testing different strategies on miniapp (faster design cycle) to achieve good performance while still maintaining some flexibility
- Task 2: Performance optimization of the temperature and hydrology solvers will benefit from the optimization approach adopted for the velocity solver

## **Looking forward:**

- Task 3 [yr 3]: Port/tailor ALI code performance to Summit (GPU), Aurora (Xeon)
  - Tpetra – performance portable global matrix assembly (WIP – Q1, FY19)
  - Aurora shifted to 2021; hierarchical parallelism required for strong scaling
  - Trilinos – simd support for CPU optimization (WIP – Q3, FY19)

# Nightly testing

SNL staff: I. Tezaur

Performance monitored via **CDash** nightly testing on a variety of architectures.



Albany									
Dashboard Calendar Previous Current Next Project									
Project									
Project	Error	Configure Warning	Pass	Error	Build Warning	Pass	Not Run	Test Fail	Pass
Albany	0	18	24	1	20	4	0	6	3201
SubProjects									
Project	Error	Configure Warning	Pass	Error	Build Warning	Pass	Not Run	Test Fail	Pass
Peridigm	0	0	1	1	1	0			
TrilinosIntel	0	1	1	0	1	0			
AlbanyIntel	0	0	1	0	0	1	0	1	347
KTCismAlbany	0	1	1	0	1	0	0	0	5
KTCismAlbanyEpetra	0	1	1	0	1	0	0	0	5
IKTAlbanyFunciorOpenMP	0	1	1	0	1	0	0	0	278
Trilinos	0	1	1	0	1	0			
TrilinosClang	0	1	1	0	1	0			
Albany64BitClang	0	0	1	0	1	0	0	1	186
IKTRideTrilinosCUDA	0	1	1	0	1	0			
IKTRideAlbanyCUDA	0	2	2	0	2	0	0	2	186
albany_cluster-toss3_skybridge-login5_serial-intel-release	0	1	1	0	0	1	0	1	288
Albany64Bit	0	0	1	0	1	0	0	1	317
IKTAlbany	0	1	1	0	1	0	0	0	372
IKTAlbanyNoEpetra	0	1	1	0	1	0	0	0	261
TrilinosDbg	0	1	1	0	1	0			
Albany64BitDbg	0	0	1	0	0	1	0	0	225
trilinos_cluster-toss3_skybridge-login5_serial-intel-release	0	1	1	0	1	0			
IKTMayerARMTrilinos	0	1	1	0	1	0			
IKTMayerARMAlbany	0	0	1	0	0	1	0	0	294
IKTWatermanTrilinosCUDA	0	1	1	0	1	0			
IKTWatermanAlbanyCUDA	0	1	1	0	1	0	0	0	94
IKTAlbanyFPECkDbg	0	1	1	0	1	0			

P100 GPU

ARM V100 GPU

Albany									
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Project									
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SubProjects									
SubProject	Error	Configure Warning	Pass	Error	Build Warning	Pass	Not Run	Test Fail	Pass
EdisonTrilinos	0	1	0	0	1	0			
CoriTrilinos	0	1	0	0	1	0			
CoriAlbanyFELIX	0	1	0	0	1	0			
CoriCismAlbany	0	1	0	0	1	0			
EdisonAlbanyFELIX	0	1	0	0	1	0			
EdisonCismAlbany	0	1	0	0	1	0			
IKTBlakeTrilinosSerial	0	1	0	0	0	1			
IKTBlakeAlbanySerial	0	0	1	0	0	1	0	0	316
IKTBlakeTrilinosOpenMP	0	1	0	0	0	1			
IKTBlakeAlbanyOpenMP	0	0	1	0	0	1	0	0	292

NERSC (Cori, Edison)

Skylake

# Nightly testing

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P100 GPU

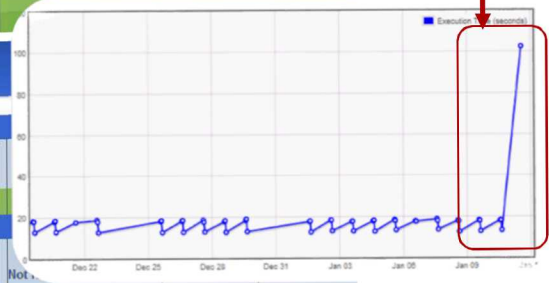
ARM V100 GPU

Slowdown identified by nightly CDash testing!

Albany									
Dashboard   Calendar   Previous   Current   Next   Project									
Project									
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NERSC (Cori, Edison)

Skylake



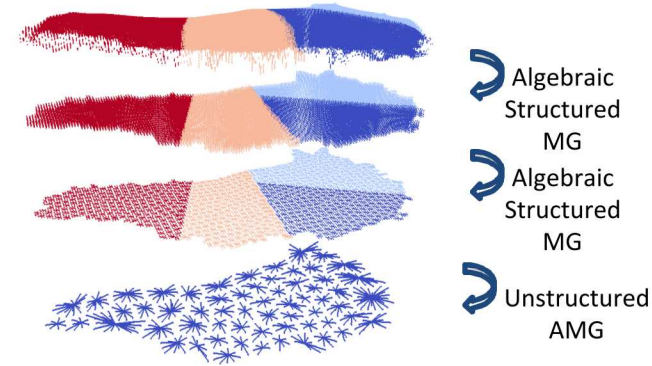
# Linear solver performance

SNL staff: R. Tuminaro, I. Tezaur, M. Perego



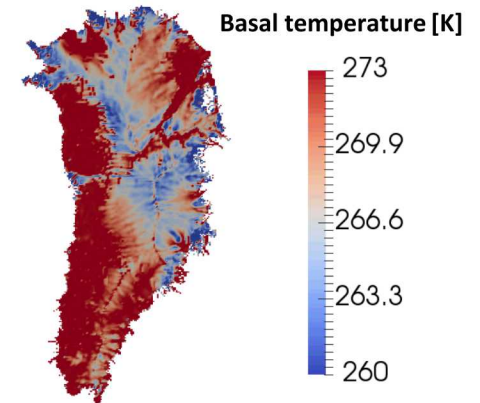
**Task 1 [yr 1]:** deliver robust solvers/preconditioners for temperature model in ALL.

**Task 2 [from PISCEES]:** for FO-Stokes solver, improve performance of MueLu implementation of aggressive-semi-coarsening-based AMG\* preconditioner.



## Status:

- Task 1 deferred to year 2 b/c Ray was unavailable in year 1
  - Some progress made on nonlinear solvers for temperature equation last year (presented at AGU 2017).
- Task 2 replaced Task 1 for year 1, and is in progress:
  - Inconsistencies b/w ML and MueLu have been resolved.
  - Seg faults/FPEs/overflow in MueLu have been resolved.
  - Total # of iterations b/w ML and MueLu are similar though not identical (right).
  - MueLu still runs  $\sim 2\times$  slower than ML (right) – culprit has been identified as banded relaxation line-smoothing in lfpack2.



	2km AIS/ 20 layers	ML	MueLu
Total Time (s)		413.3	513.6
Total Linear Solve Time (s)		97.1	190.6
# linear iters		426	400

\* R. Tuminaro, et al. "A matrix dependent/algebraic multigrid approach for extruded meshes with applications to ice sheet modeling", *SISC* 2016.

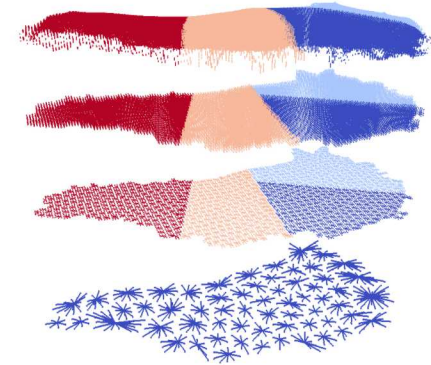
# Linear solver performance

SNL staff: R. Tuminaro, I. Tezaur, M. Perego

LABORATORIES

**Task 1 [yr 1]:** deliver robust solvers/preconditioners for temperature model in ALI.

**Task 2 [from PISCEES]:** improve performance of MueLu implementation of aggressive-semi-coarsening-based AMG\* preconditioner to make it comparable to ML.



- Algebraic Structured MG
- Algebraic Structured MG
- Unstructured AMG

## **Challenges:**

- Task 1: highly nonlinear and advection-dominated problems.
- Task 2: currently lacking manpower to speed-up relevant routine in Ipack2 (banded relaxation line-smoothing ).



## **Mitigation strategy/next steps:**

- Task 1: Ray + Mauro will start on this in FY19.
- Task 2: currently consulting with Ipack2/MueLu developers; hire summer student to work on Ipack2 improvements?



## **Looking forward:**

- Task 3 [yr 4]: study of Trilinos linear solvers performance on next generation architectures for ALI
  - Ipack2 and MueLu are designed for performance portability (integrate Kokkos), and are being matured for up-and-coming architectures by Trilinos team.

# Improved time-stepping method for thickness evolution

SNL staff: L. Bertagna, M. Perego, I. Tezaur, R. Tuminaro

**Task 1 [yr 2]**: Improve time-stepping method for thickness evolution (implicit/obstacle formulation)



**Status**: deferred to year 2.

- We decided to focus on infrastructure (block data structure) work that is needed by the thickness evolution equation and temperature/hydrology couplings with FO solver
  - This will enable a variety of couplings and block solvers (Teko) for improved performance.

**Challenges**:

- Hard highly nonlinear free-surface problem on fixed mesh
- Albany is a complex code to refactor; we have limited manpower.

**Mitigation strategy/next steps**:

- Hiring post-doc to help with the task

**Looking forward**:

- Task 2 [yr 3]: All robust solvers/preconditioners for coupled thermo-mechanical model; scalability studies
  - Block data structures will enable block solvers for improved performance

# Summary/looking forward

Year	Task	Institutions	Joint with subgroup	Status
1	Finish Kokkos ALI FE refactor for velocity; port/optimize for current GPU/Phi	SNL		mostly complete
2	Kokkos ALI FE refactor for temperature & hydrology; port/optimize for current GPU/Phi	SNL		deferred to year 3
1	Deliver robust solvers/preconditioners for temperature model	SNL		in progress
2	Improve time-stepping method for thickness evolution (implicit/obstacle formulation)	SNL, LBNL, LANL	Other development*	deferred to year 3
3	ALI: robust solvers/preconditioners for coupled thermo-mechanical model; scalability studies	SNL		
3	Port & tailor ALI code performance to Aurora (Phi) & Summit (GPU) machines	SNL		
4	Study of Trilinos linear solvers performance on next generation architectures for ALI	SNL		
4	Numerical convergence study of ice evolution on simplified experiments	SNL, LBNL		
5	Kokkos refactor of remaining ALI evaluators; & optimize for new state-of-the-art HPC	SNL		

\* Albany infrastructure work to enable modular multi-physics and block preconditioning (SNL, Yrs 1-2)

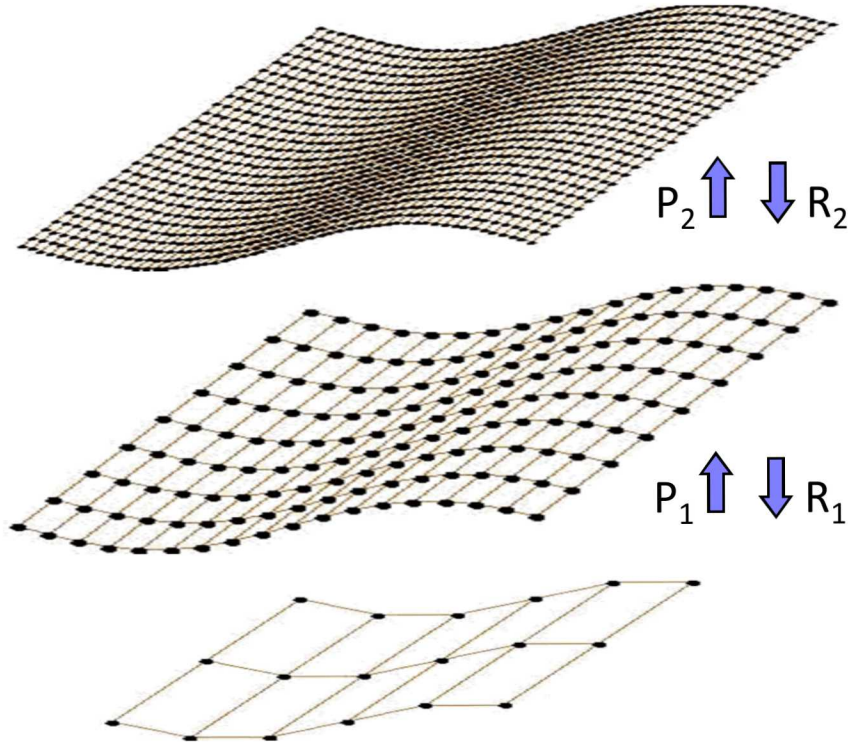
# Start of Backup Slides

# How Does Multi-Grid Work?

$$\text{Solve } A_3 u_3 = f_3$$

## Basic idea:

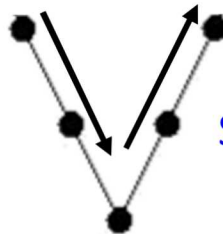
- Develop coarse approximations
- Accelerate convergence via coarse iterations to efficiently propagate information



Smooth  $A_3 u_3 = f_3$ . Set  $f_2 = R_2 r_3$ .

Smooth  $A_2 u_2 = f_2$ . Set  $f_1 = R_1 r_2$ .

Solve  $A_1 u_1 = f_1$  directly.



Set  $u_3 = u_3 + P_2 u_2$ . Smooth  $A_3 u_3 = f_3$ .

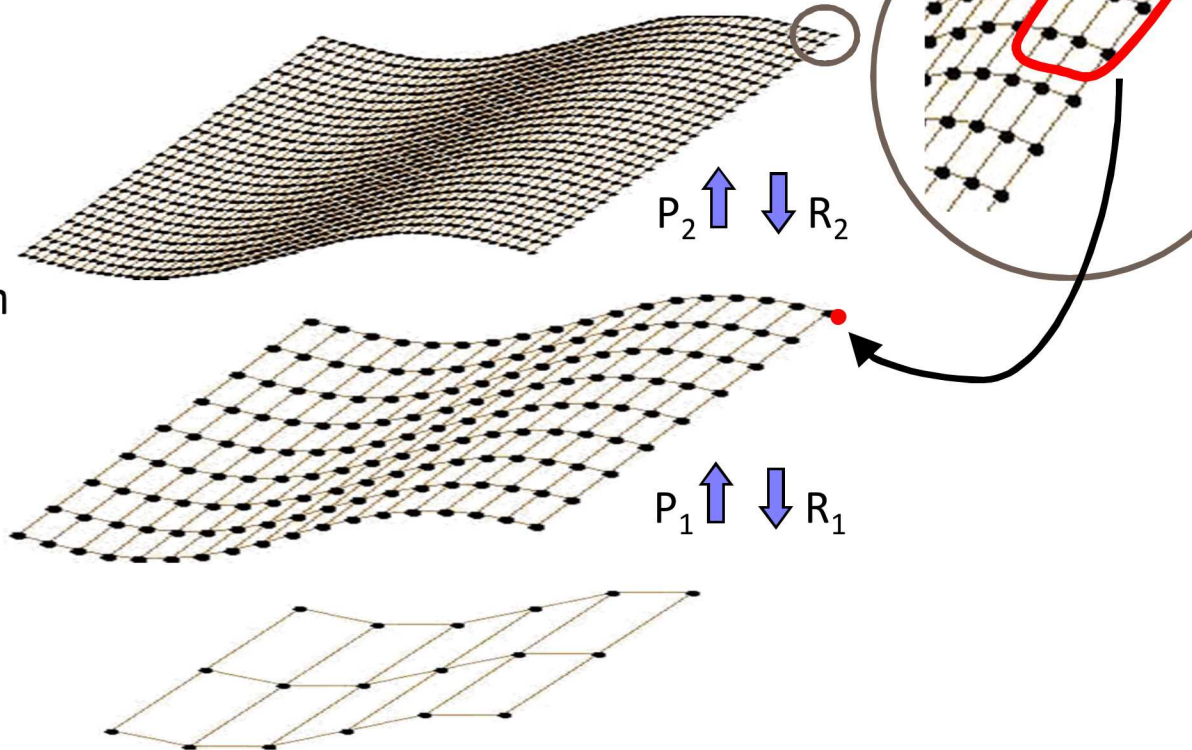
Set  $u_2 = u_2 + P_1 u_1$ . Smooth  $A_2 u_2 = f_2$ .

# How Does Algebraic Multi-Grid Work?

Solve  $A_3 u_3 = f_3$

**Basic idea:**

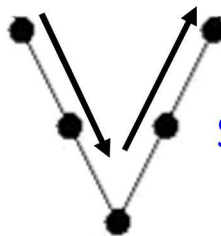
- Construct graph & coarsen
- Determine  $P_i$  &  $R_i$  sparsity pattern
- Determine  $P_i$  &  $R_i$ 's coeffs
- Project:  $A_i = R_i A_{i+1} P_i$



Smooth  $A_3 u_3 = f_3$ . Set  $f_2 = R_2 r_3$ .

Smooth  $A_2 u_2 = f_2$ . Set  $f_1 = R_1 r_2$ .

Solve  $A_1 u_1 = f_1$  directly.



Set  $u_3 = u_3 + P_2 u_2$ . Smooth  $A_3 u_3 = f_3$ .

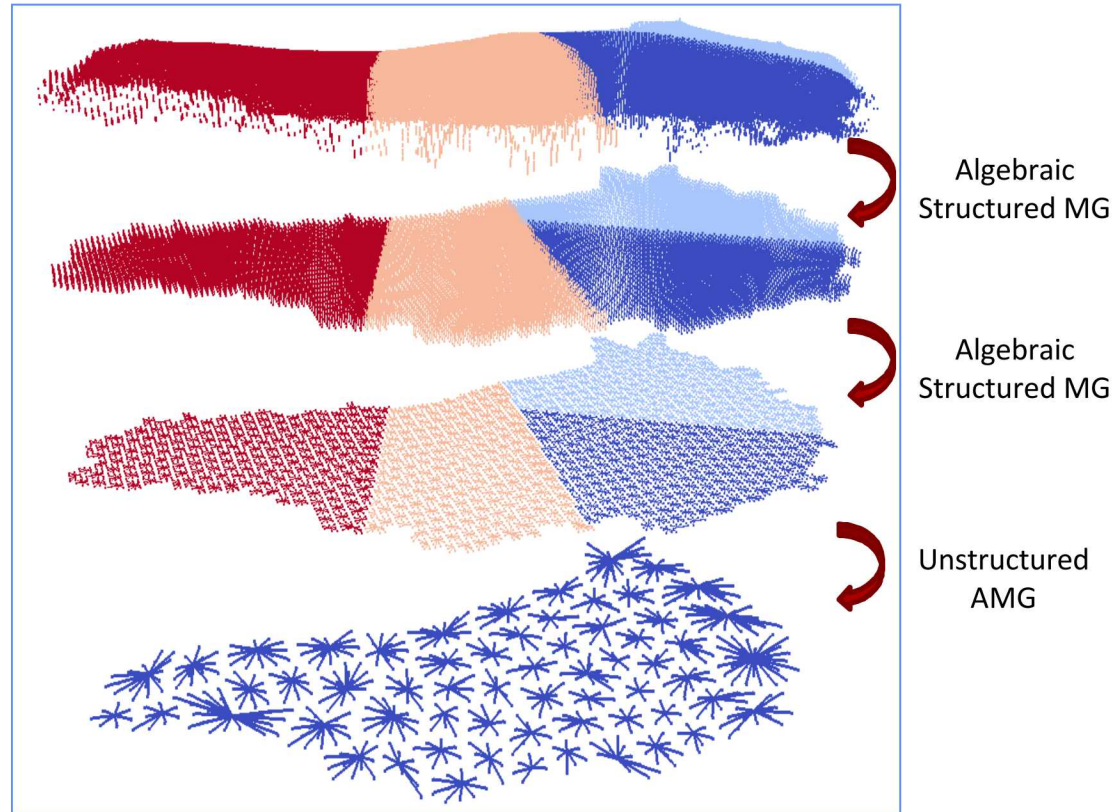
Set  $u_2 = u_2 + P_1 u_1$ . Smooth  $A_2 u_2 = f_2$ .

# Scalability via Algebraic Multi-Grid Preconditioning with Semi-Coarsening

Bad aspect ratios ( $dx \gg dz$ ) ruin classical AMG convergence rates!

- relatively small horizontal coupling terms, hard to smooth horizontal errors
- ⇒ Solvers (AMG and ILU) must take aspect ratios into account

We developed a **new AMG solver** based on aggressive **semi-coarsening** (available in *ML/MueLu* packages of *Trilinos*)

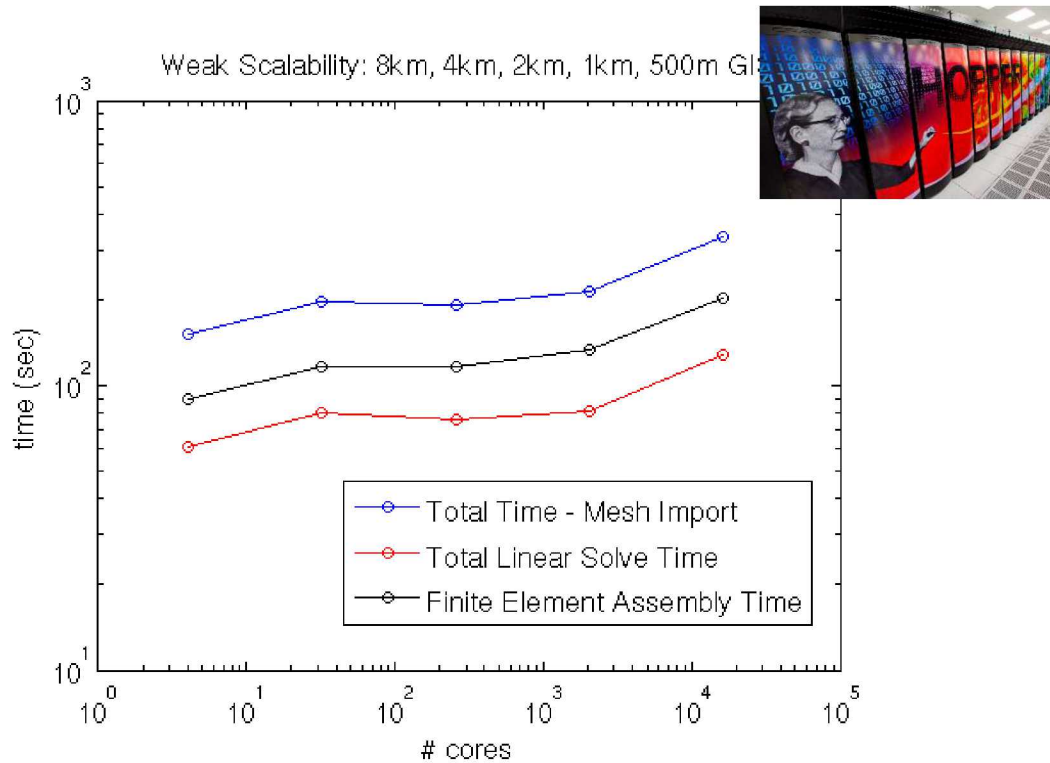


See (Tezaur *et al.*, 2015),  
(Tuminaro *et al.*, 2016).

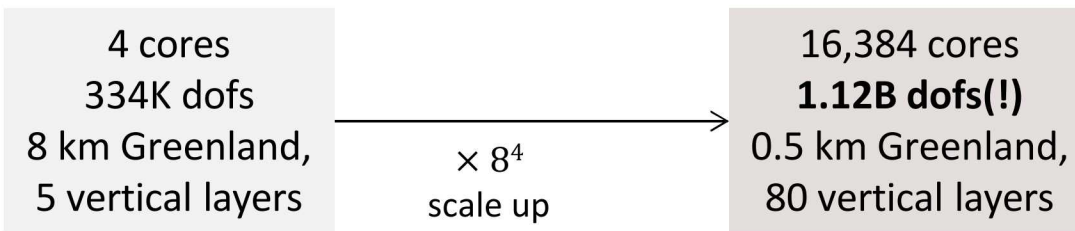
***Scaling studies (next slides):***  
New AMG preconditioner vs. ILU



# Greenland Controlled Weak Scalability Study

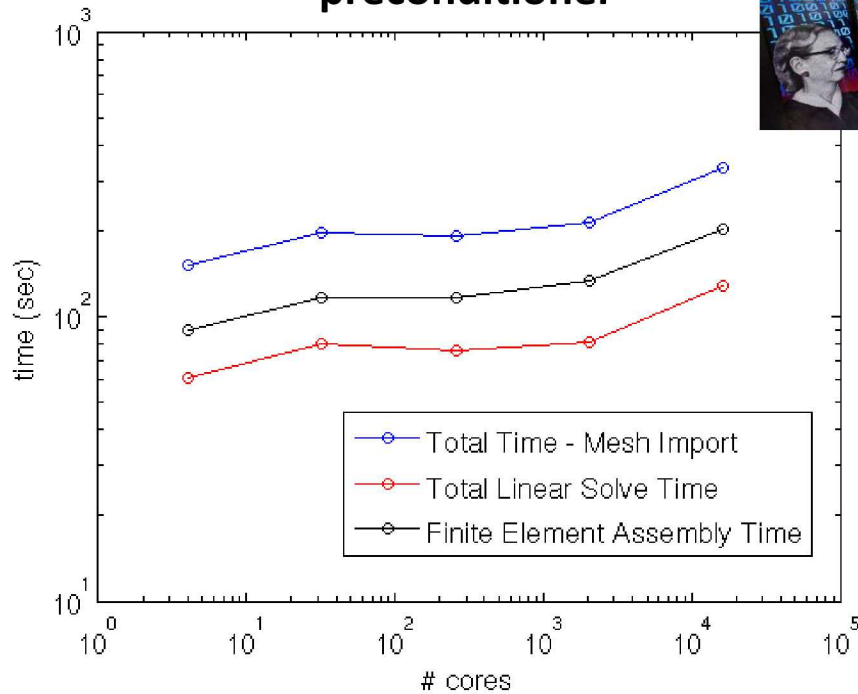


- Weak scaling study with fixed dataset, 4 mesh bisections.
- ~70-80K dofs/core.
- **Conjugate Gradient (CG) iterative method** for linear solves (faster convergence than GMRES).
- **New AMG preconditioner** developed by R. Tuminaro based on **semi-coarsening** (coarsening in z-direction only).
- **Significant improvement** in scalability with new AMG preconditioner over ILU preconditioner!

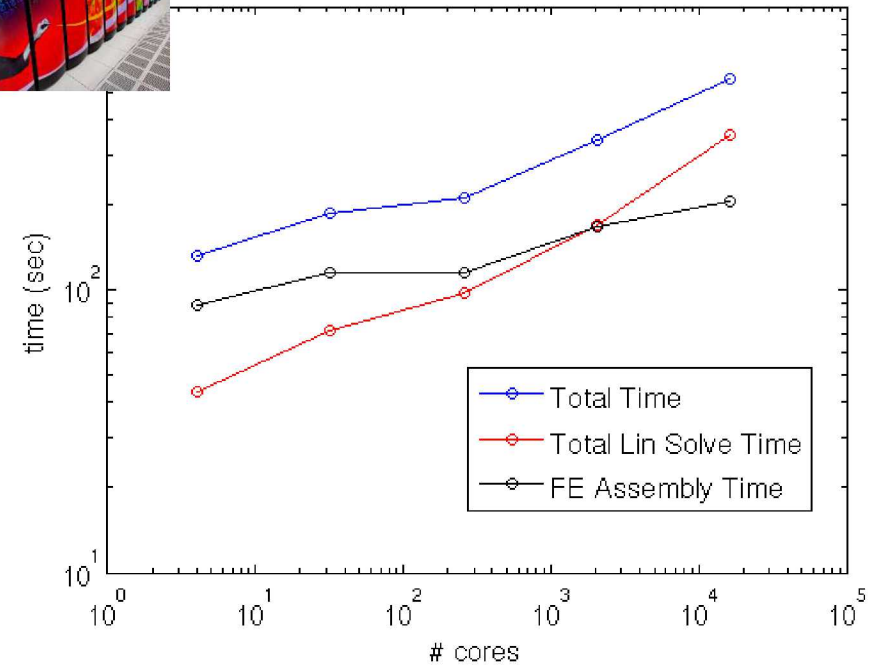


# Greenland Controlled Weak Scalability Study

## New AMG preconditioner preconditioner



## ILU preconditioner



4 cores  
334K dofs  
8 km Greenland,  
5 vertical layers

→  
× 8<sup>4</sup>  
scale up

16,384 cores  
**1.12B dofs(!)**  
0.5 km Greenland,  
80 vertical layers

- **Significant improvement** in scalability with new AMG preconditioner over ILU preconditioner!

# Moderate Resolution Antarctica Weak Scaling Study

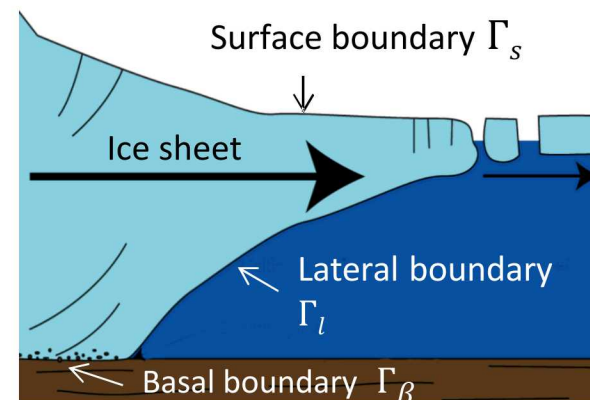
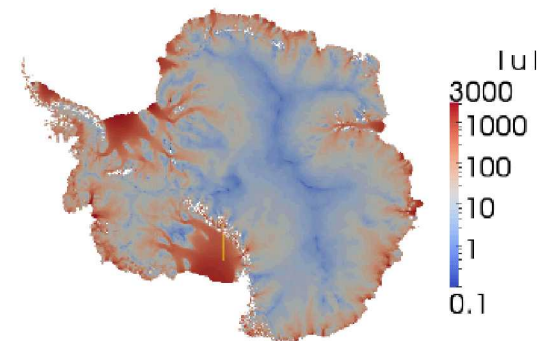
Antarctica is fundamentally different than Greenland: AIS contains large ice shelves (floating extensions of land ice).

- **Along ice shelf front:** open-ocean BC (Neumann).
- **Along ice shelf base:** zero traction BC (Neumann).

⇒ For vertical grid lines that lie within ice shelves, top and bottom BCs resemble Neumann BCs so sub-matrix associated with one of these lines is almost\* singular.

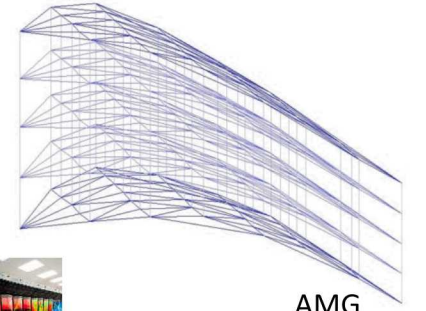
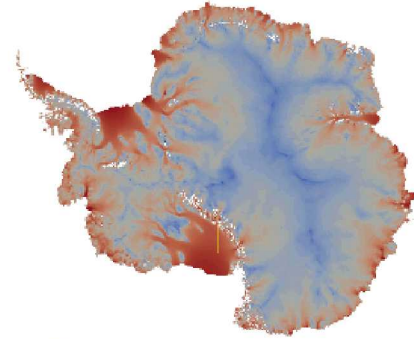
(vertical > horizontal coupling)  
+  
Neumann BCs  
=  
nearly singular submatrix associated with vertical lines

⇒ Ice shelves give rise to severe ill-conditioning of linear systems!



\*Completely singular in the presence of islands and some ice tongues.

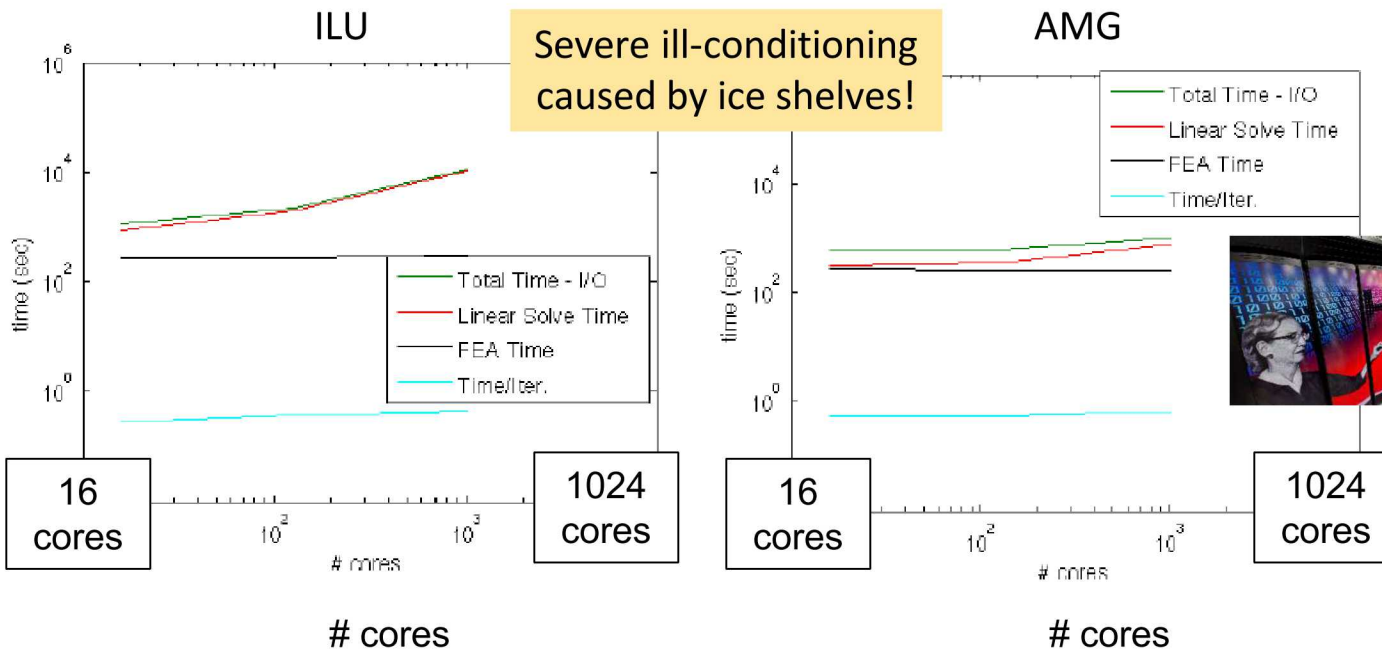
# Moderate Resolution Antarctica Weak Scaling Study



AMG preconditioner



- Weak scaling study on Antarctic problem (8km w/ 5 layers → 2km w/ 20 layers).
- Initialized with realistic basal friction (from deterministic inversion) and temperature field from BEDMAP2.
- **Iterative linear solver:** GMRES.
- **Preconditioner:** ILU vs. new AMG based on aggressive semi-coarsening.



(vertical > horizontal coupling)  
 +  
 Neumann BCs  
 =  
 nearly singular submatrix associated with vertical lines

AMG preconditioner less sensitive than ILU to ill-conditioning (ice shelves → Green's function\* with modest horizontal decay → ILU is less effective).

\* Tuminaro *et al.*, *SISC*, 2016.