



This paper describes objective technical results and analysis. Any subjective views or opinions that might be expressed in the paper do not necessarily represent the views of the U.S. Department of Energy or the United States Government.

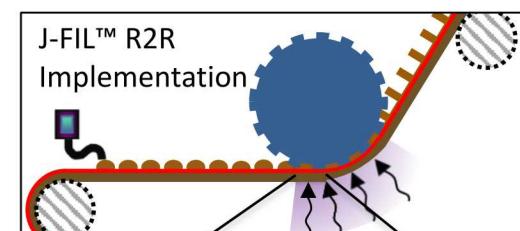
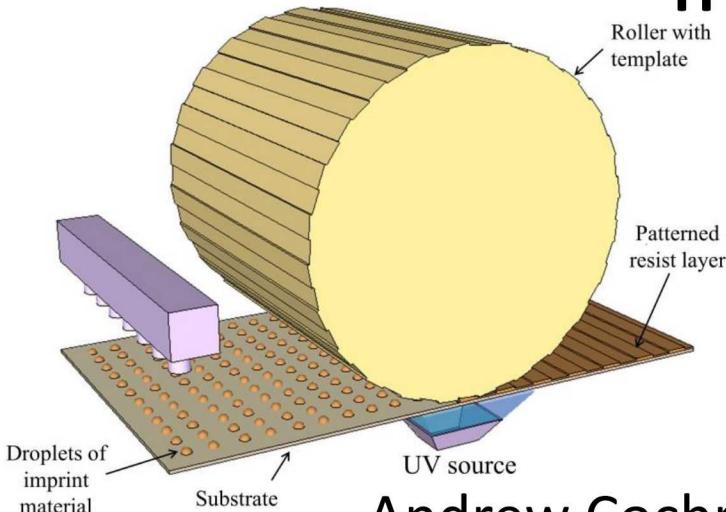


THE UNIVERSITY OF  
NEW MEXICO.



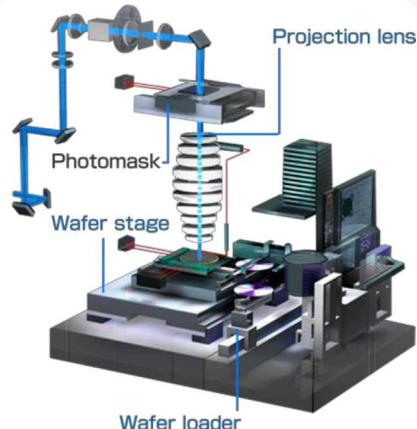
SAND2018-11560C  
**TEXAS**  
The University of Texas at Austin

# Two-phase flow and structural deformation models for nanoimprint lithography

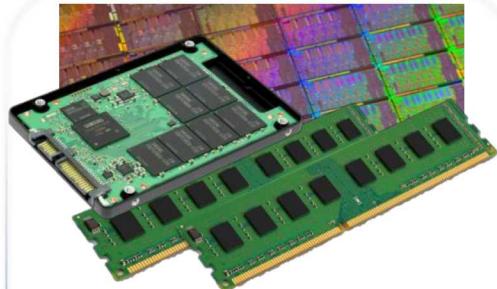


Andrew Cochrane, Kristianto  
Tjiptowidjojo, Roger T.  
Bonnecaze, P. Randall Schunk\*

# Manufacturing Nano-Featured Materials



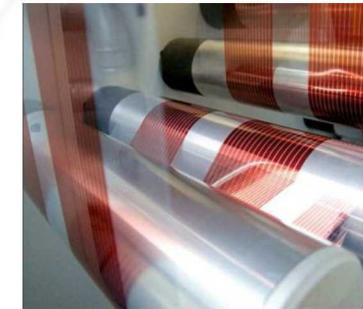
Optical Lithography



CPU, SSD, RAM

High Price Point  
High Volume

- Simpler processing steps
- More product



Roll-to-Roll Nanoimprint

Transparent Electronics



Flexible Batteries



Flexible Displays



Flexible Polarizers



Flexible Solar Cells

Lower Price Point  
Higher Volume

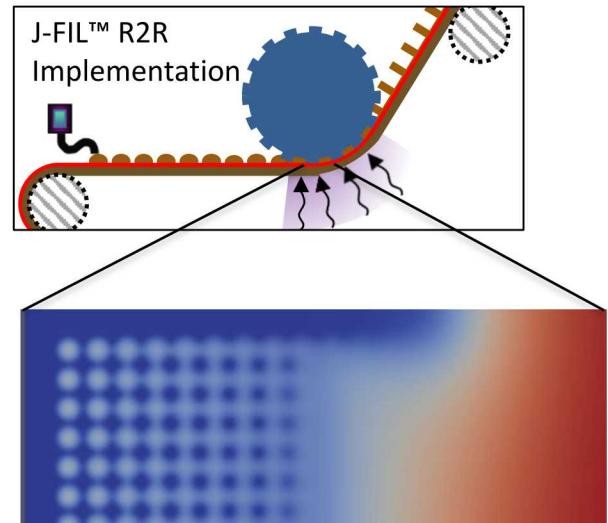
# Process Configuration of Jet and Flash Imprint Lithography (J-FIL™)



Dispense Photo-Polymer (Resist) via Ink-Jet  
Inkjet - reduces resist volume, viscous  
resistance and layer thickness  
- allows resist delivery to features

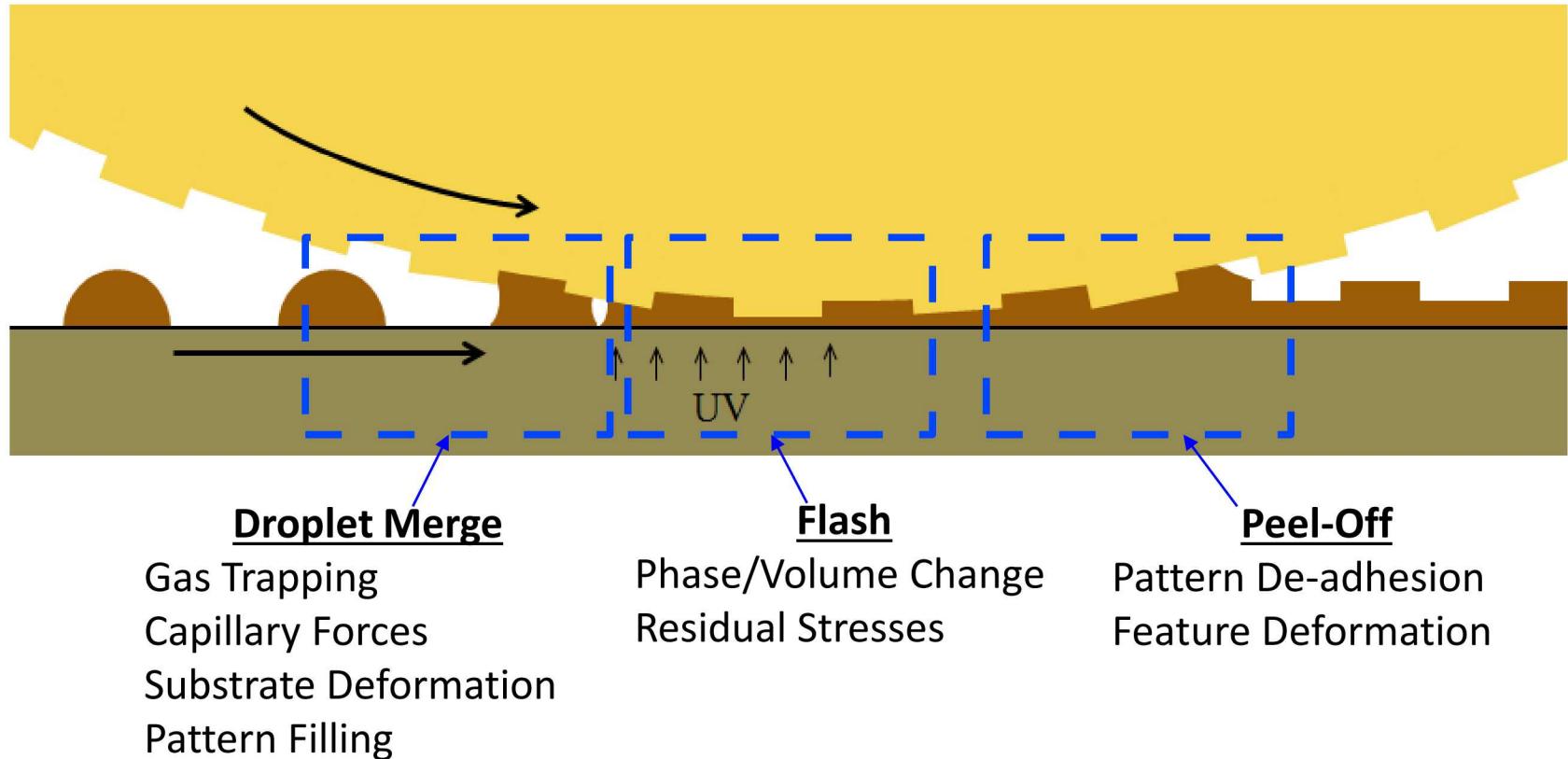
Resist fills template pattern  
Imprint

Resist is cured with light  
Flash



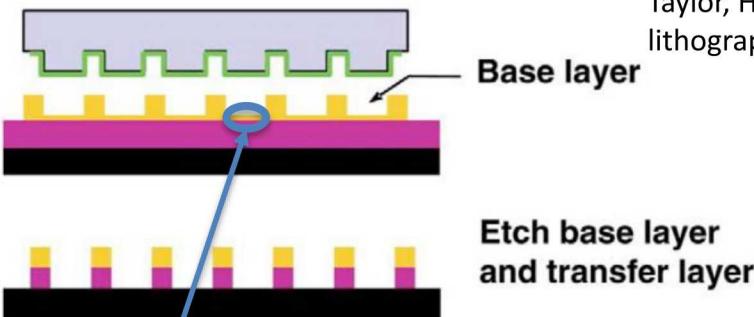
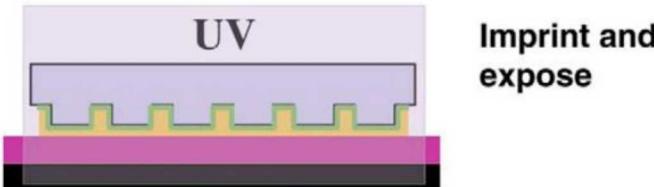
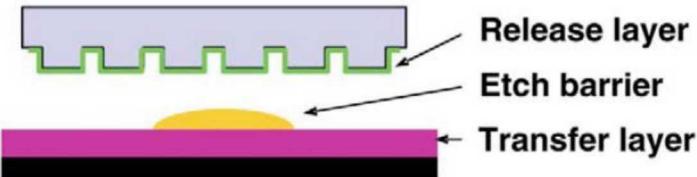
Many challenges arise when implementing this process

# Physics Regimes of Nanoimprint Lithography



Focus on processing barriers in the droplet merge regime

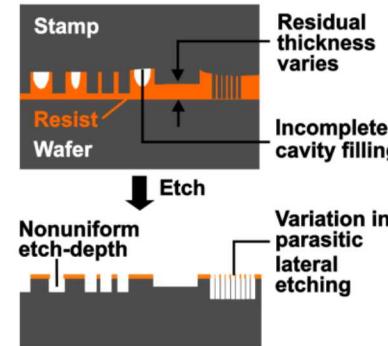
# Process Scaling Barriers



**Residual layer** is any resist that is not part of the pattern

## Non-Uniform Residual Layer Thickness

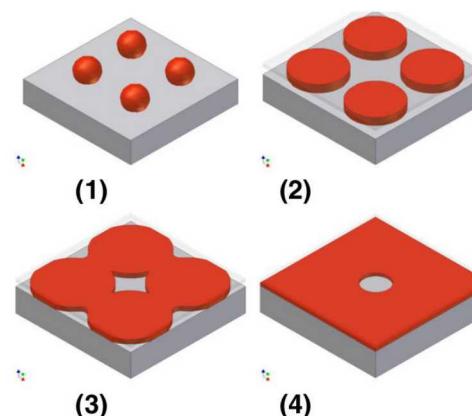
Results in non-uniform etch depth



Taylor, H., 2011, Simulation and mitigation of pattern process dependencies in nanoimprint lithography: Journal of Photopolymer Science and Technology, v. 24, n. 1, p. 47-55.

## Gas Trapping

Results in non-fill defects

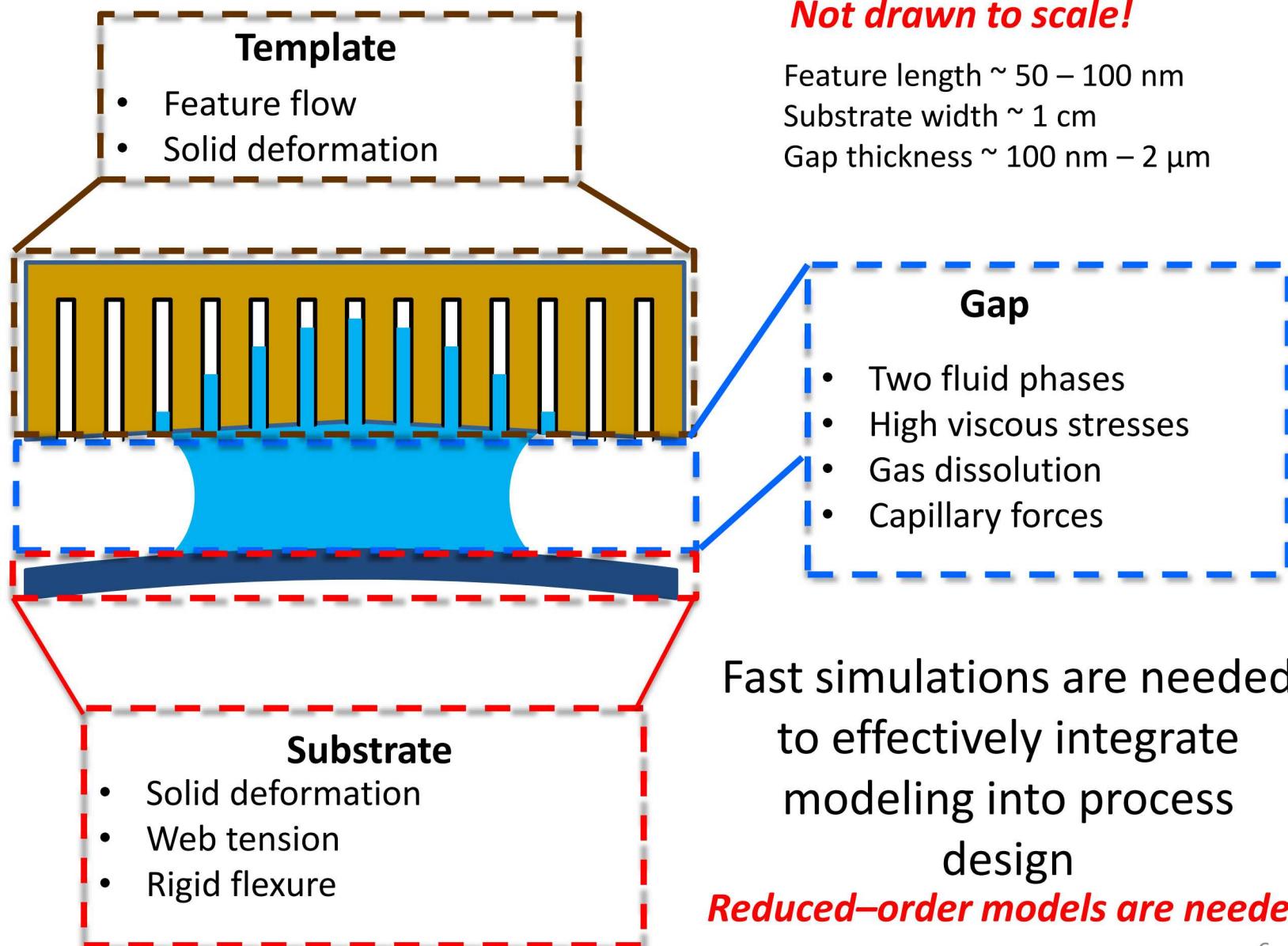


Model are used to optimize processes and minimize these barriers

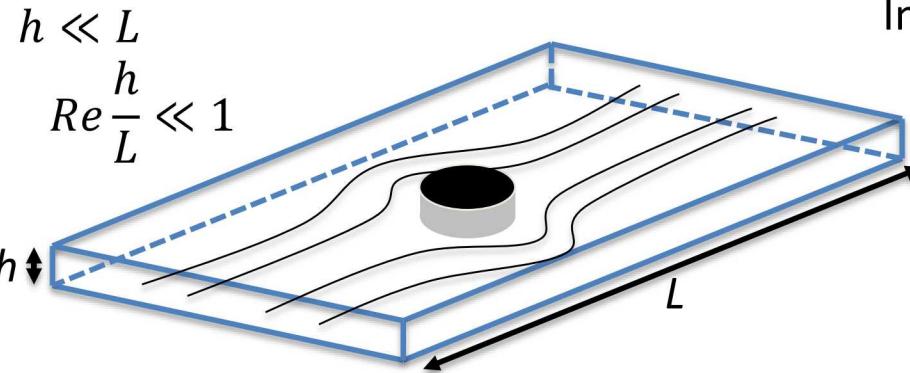
Resnick, D. J., Sreenivasan, S. V. and Wilson, G. C., 2005, Step & flash imprint lithography: Materials Today, February.

Liang, X., Tan, H., Fu, Z., Chou, S. Y., 2007, Air bubble formation and dissolution in dispensing nanoimprint lithography. Journal of Photopolymer Science and Technology, v. 24, n. 1, p. 47-55.

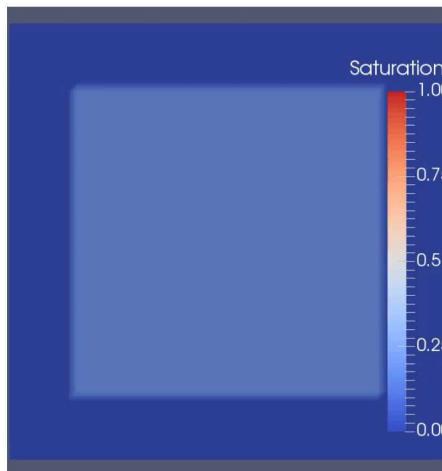
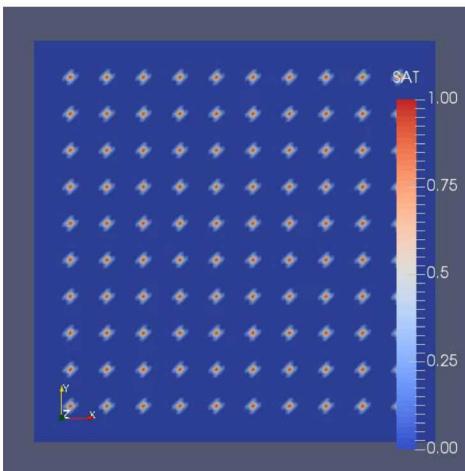
# Breaking Down the Droplet Merge Regime



# Reduced-Order Models for Thin Gap Multiphase Fluid Flow

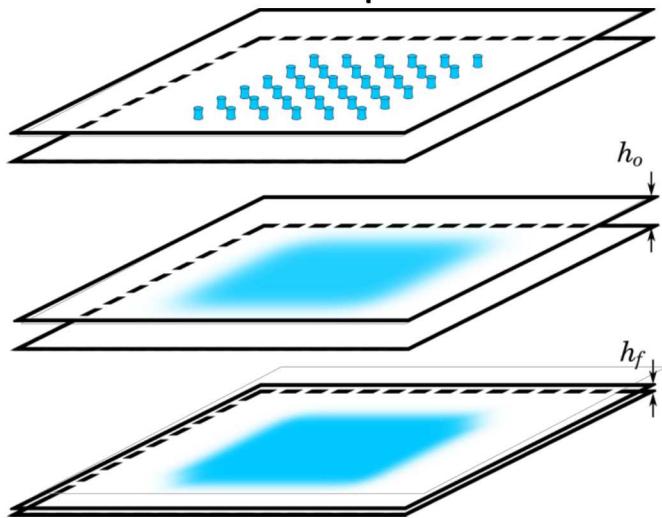


Reynolds, O., 1886, On the Theory of Lubrication and Its Application to Mr. Beauchamp Tower's Experiments, Including an Experimental Determination of the Viscosity of Olive Oil: Philosophical Transactions of the Royal Society of London, v. 177, p. 157-234.



In thin gaps momentum equations reduce to 2-D expression

$$\boldsymbol{v}_{II} = -\frac{h^2}{12\mu} \nabla_{II} P$$



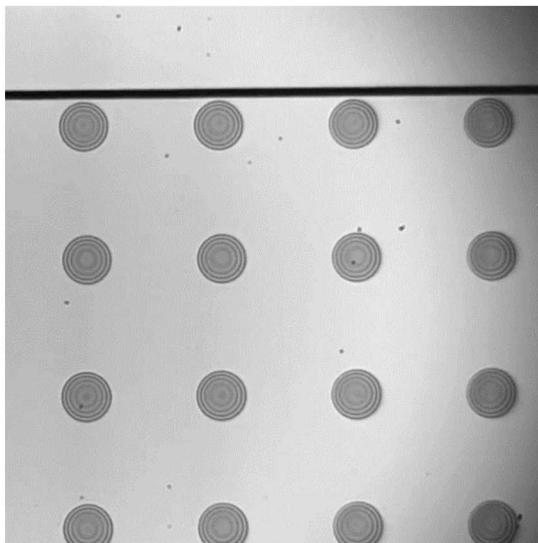
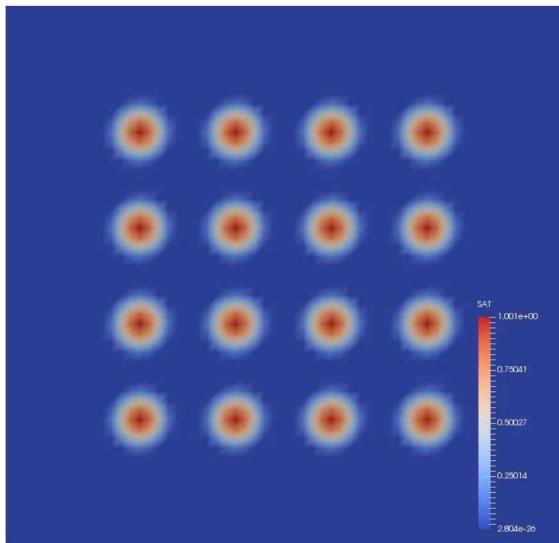
Relative Permeability

$$\boldsymbol{v}_\alpha = -\frac{h^2}{12\mu} k_{r\alpha} \nabla_{II} P$$

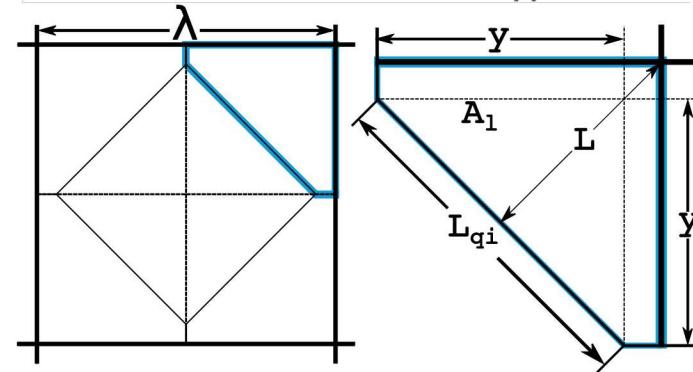
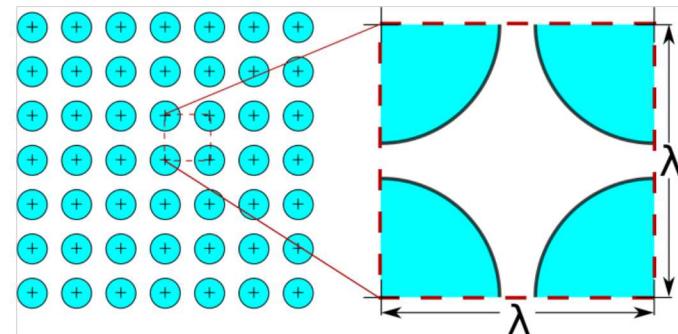
Disperse representation enables large area simulations with coarse discretization

# Gas Dissolution

Gas Mass Balance      
$$\frac{\partial((1-S)h\rho_g)}{\partial t} + \nabla_{II} \cdot (h\rho_g \mathbf{v}_g) + J = 0$$
  
 Ideal Gas Law      
$$\rho_g = \frac{M_g P}{RT}$$
  
 Lumped Parameter Dissolution Model      
$$J = h \frac{A_i}{V_G} \frac{D}{L} H(P - P_{atm})$$



Regular/known drop pattern

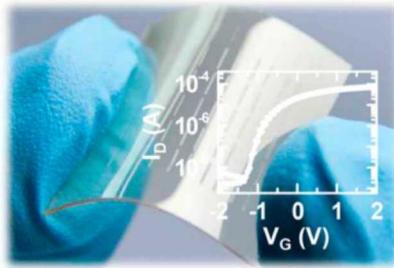
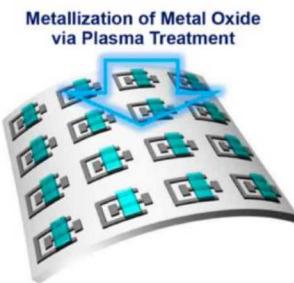


Analytic dissolution model

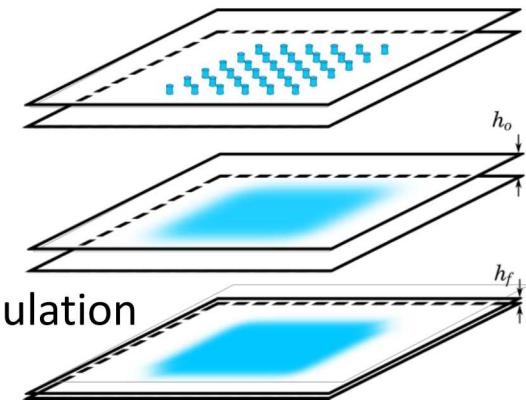
Reduced order models for two-phase, thin-gap, gas dissolving flow

# Drop Density Varied for Fill of Non-Uniform Pattern

Thin film transistor



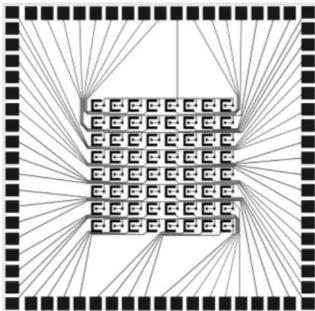
NIL processing model



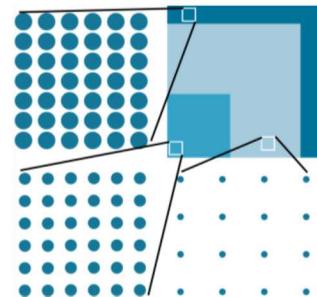
Disperse flow formulation

Choi, Y., W.-Y. Park, M. S. Kang, G.-R. Yi, J.-Y. Lee, Y.-H. Kim, and J. H. Cho, 2015, Monolithic metal oxide transistors, ACS Nano, p. 4288-4295.

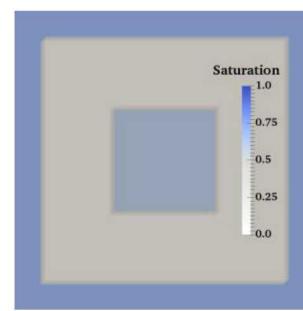
Pattern mask



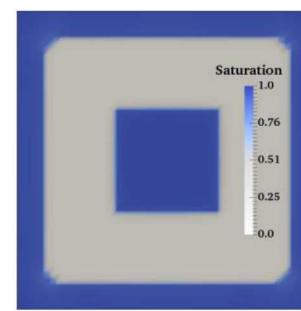
Regions require different amounts of resist



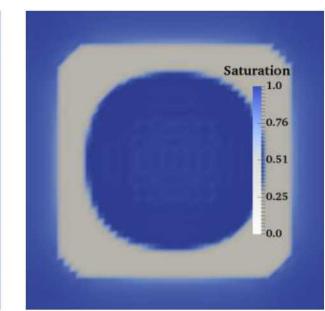
Liquid bridge formation



Full gap



Overfull gap



Model can represent varied density drop pattern by variation across initial saturation field

# Sensitivity Analysis

## Relative Work Comparison

### Comparative Work Function

- No Surface Tension
- No Deformation

$$E = \int_0^{t_f} \int_A P dA \frac{dh}{dt} dt$$

### Base Case:

6 pL water drops in N<sub>2</sub>

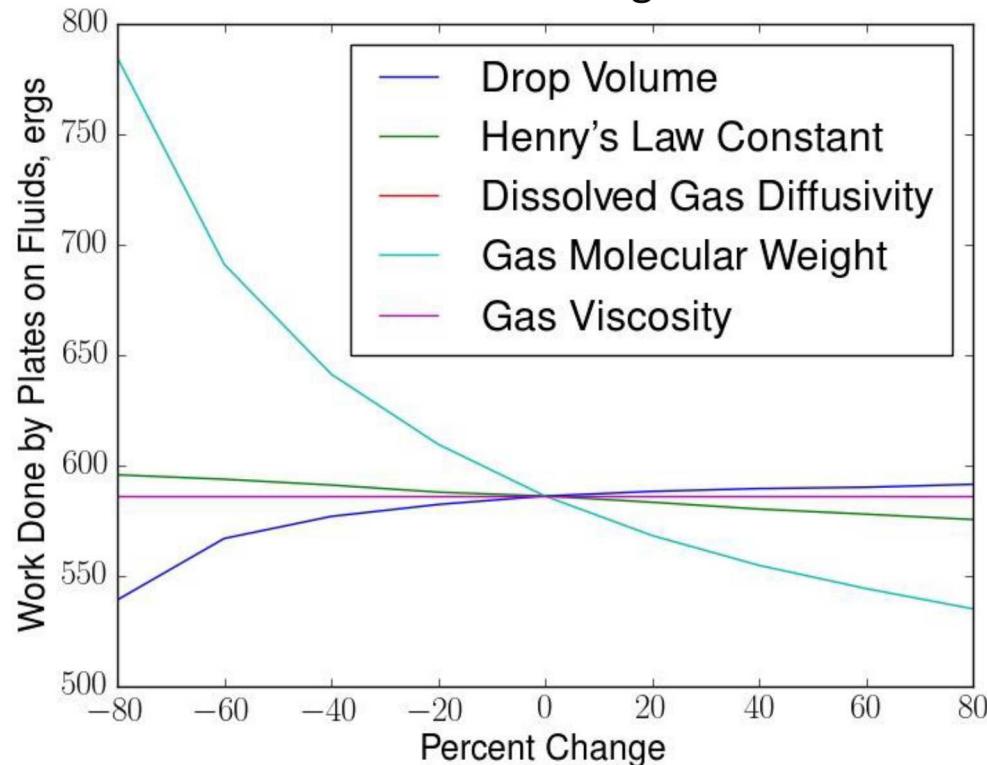
Squeezed from 1 micron to 100 nm

Is processing rate increased because  
viscous dissipation is high or because it  
takes a long time to dissolve the gas?

### Experimentally Realizable parameter adjustment

Reduce liquid viscosity 20% → Reduce Work by 9%  
Change N<sub>2</sub> to CO<sub>2</sub> → Reduce Work by 8%

Sensitivity of Work to Percent Change  
in Base Case Processing Parameter



Both viscous dissipation and gas  
dissolution can have an effect on  
processing rate

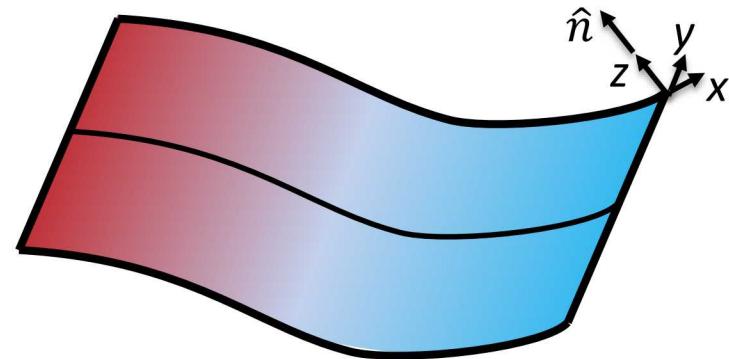
# Structural Model

## Membrane Mechanics

$$\nabla_{II} \cdot \overline{\overline{T}}_{II} + \tau_{II} = 0$$

$$T_{xx}\kappa_x + T_{yy}\kappa_y + P_s = 0$$

- Constitutive Relationship



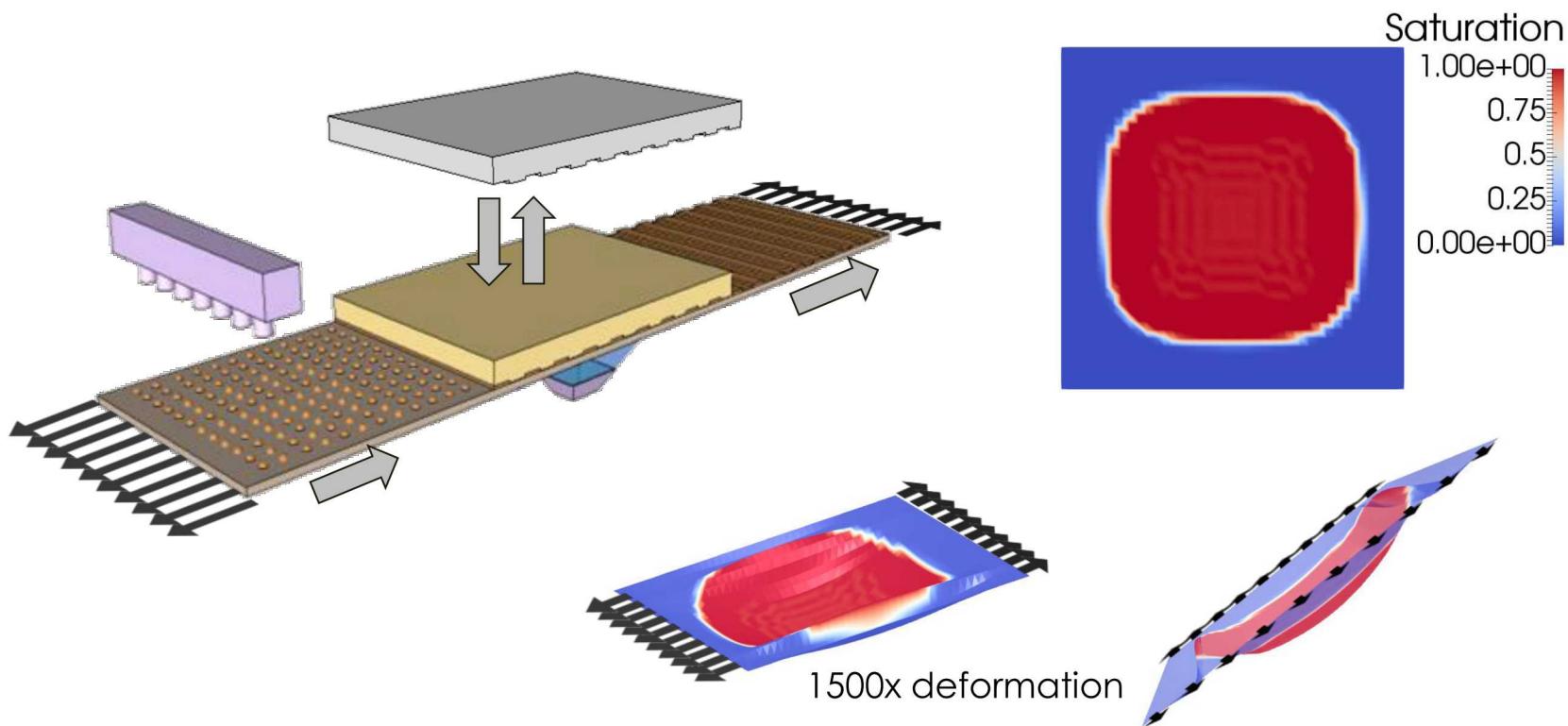
$$\begin{aligned} \boldsymbol{v}_{II} &= -\frac{h^2}{12\mu} \nabla_{II} P \\ P_s &= P + S\sigma\kappa \end{aligned}$$



Wrinkled membrane

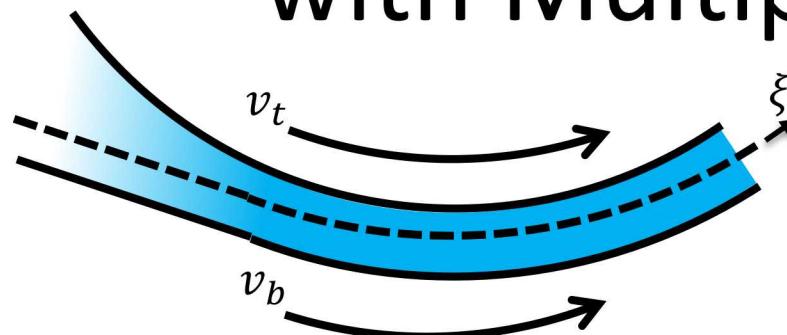
Reduced order model for web-structure mechanics

# Membrane Mechanics Model Coupled with Disperse Flow Model



Pinch-off in crossweb direction suggests membranes  
are too pliant

# Cylindrical Shell Model Coupled with Multiphase Lubrication



Cylindrical Shells

## Tangential Force Balance

$$\frac{dT}{d\xi} + \kappa \frac{\partial}{\partial \xi} (\kappa D) + P_t = 0$$

## Normal Force Balance

$$-\kappa \frac{\partial^2}{\partial \xi^2} (\kappa D) + \kappa T + P_n = 0$$

## Geometry

$$\frac{d^2x}{d\xi^2} + \kappa \frac{dy}{d\xi} = 0$$

## Liquid Mass Balance

$$\frac{\partial(Sh)}{\partial t} + \frac{\partial}{\partial \xi} (h v_l) + \frac{\partial}{\partial \xi} (Sh v_a) - \frac{1}{2} S v_d \frac{\partial}{\partial \xi} h = 0$$

Pressure driven flow    Top/Bottom boundary motion terms

Pressure driven flow    Top/Bottom boundary motion terms

Pressure driven flow    Top/Bottom boundary motion terms

## Displacement-Gap Thickness Coupling

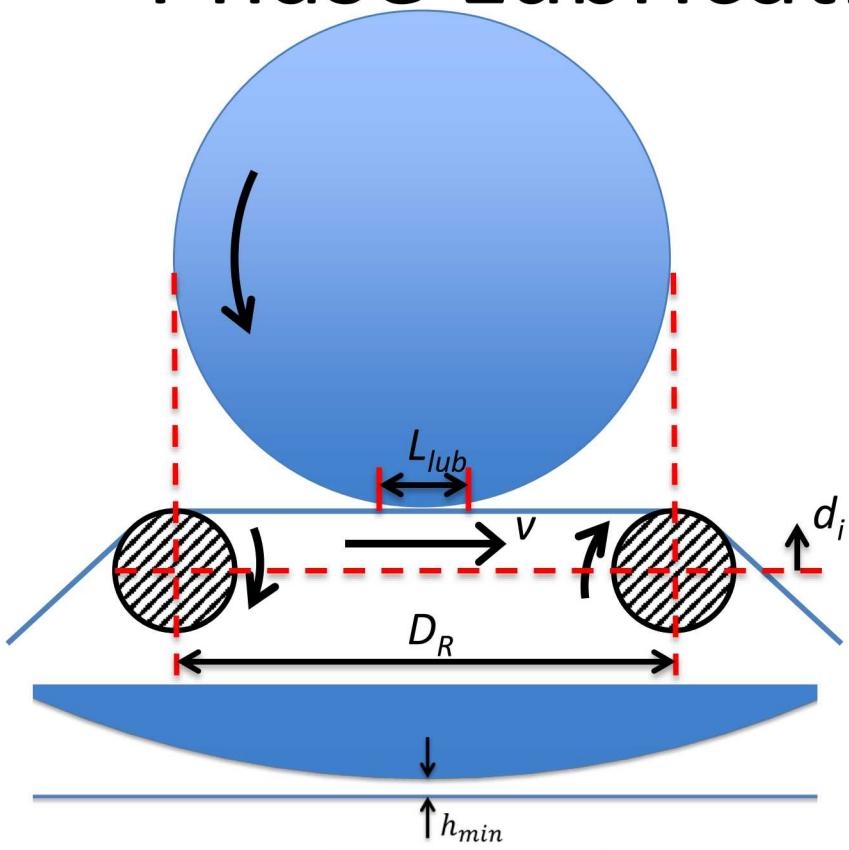
$$h = h_o - n \cdot \delta$$

## Lubrication-Normal Pressure Coupling

$$P_n = P - P_{\text{atm}}$$

With this coupled model we explore how bending stiffness affects web deformation in a closing nip

# Effects of Web Stiffness on Single Phase Lubrication Thickness Profile



$$L_{lub} = 6.6 \text{ mm}$$

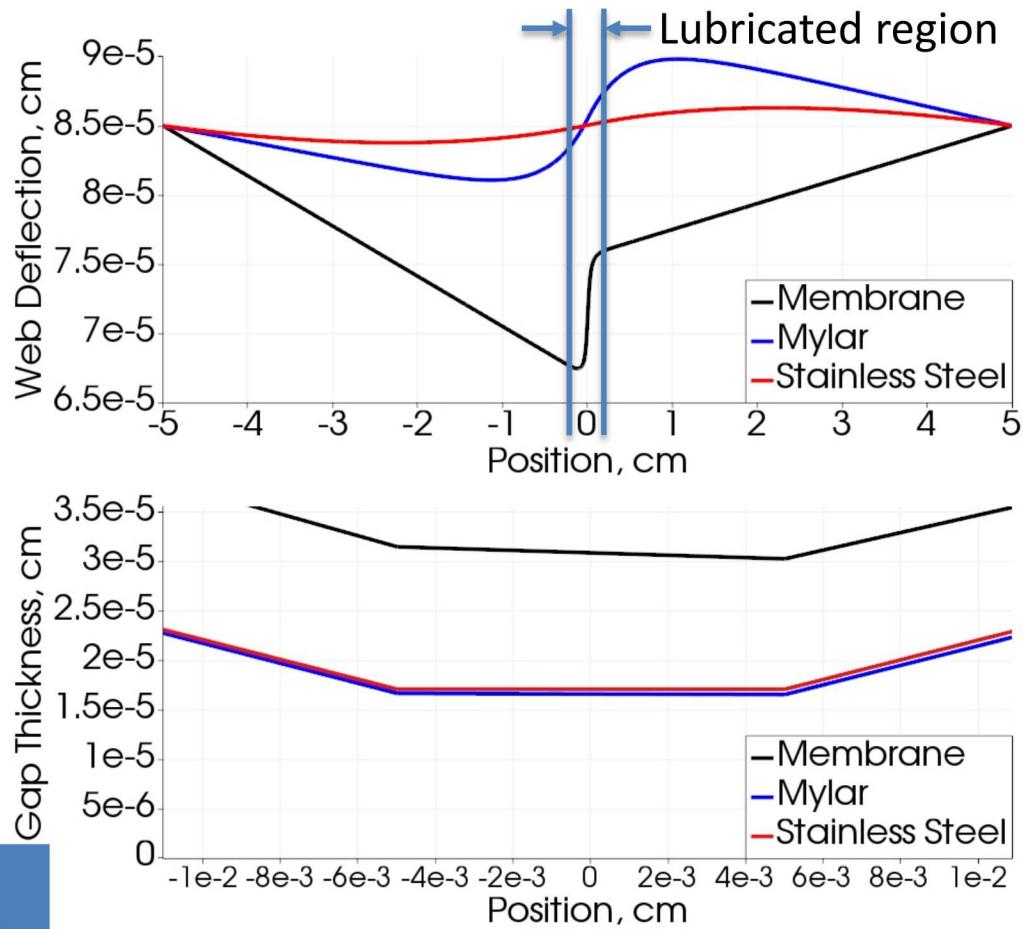
$$D_R = 10 \text{ cm}$$

$$v = 1 \text{ micron/s}$$

$$d_i = 850 \text{ nm}$$

$$h_{min} = 1 \text{ micron}$$

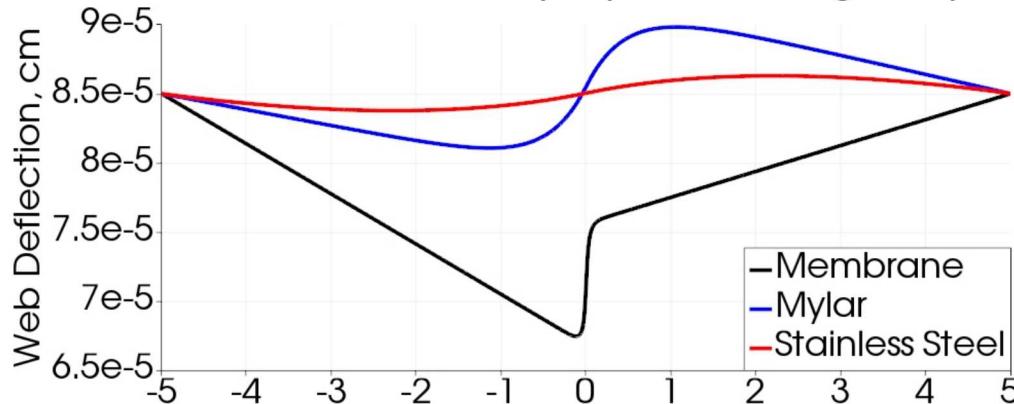
Material	Bending Stiffness, Nm
Membrane	0
Mylar	$0.21(10)^{-3}$
Stainless Steel	$7.7(10)^{-3}$



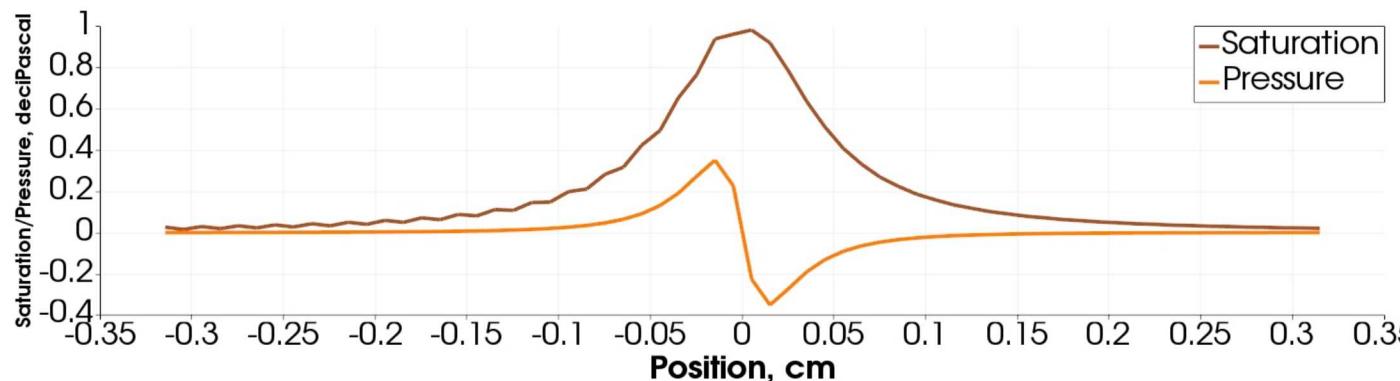
Even for pliant web material, bending stiffness has an effect on web deformation

# Conclusions & Future Work

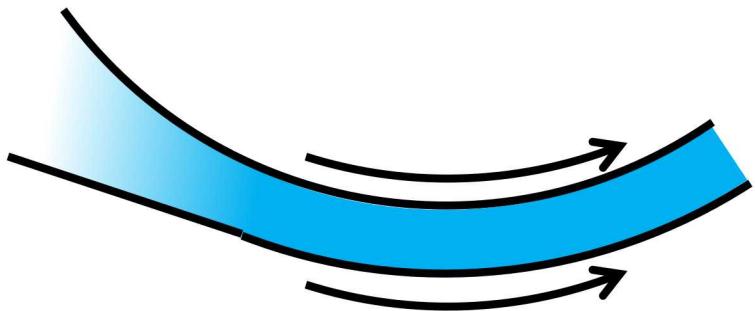
- In drop merger, both viscous dissipation and gas dissolution can effect processing rate
- Bending stiffness is an important physical aspect that needs to be included in simulations of web deformation
- Using coupled reduced order models many simulations can be iterated through quickly to determine effects of various properties in a given process



- Push forward with cylindrical shell model and two-phase flow



# Questions and Acknowledgements



Is the instability due to physical model,  
mathematical formulation or numerical  
implementation?

## Schunk Group:

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Kris Tjiptowidjojo  
Daniel Hariprasad  
Rich Martin  
Weston Ortiz

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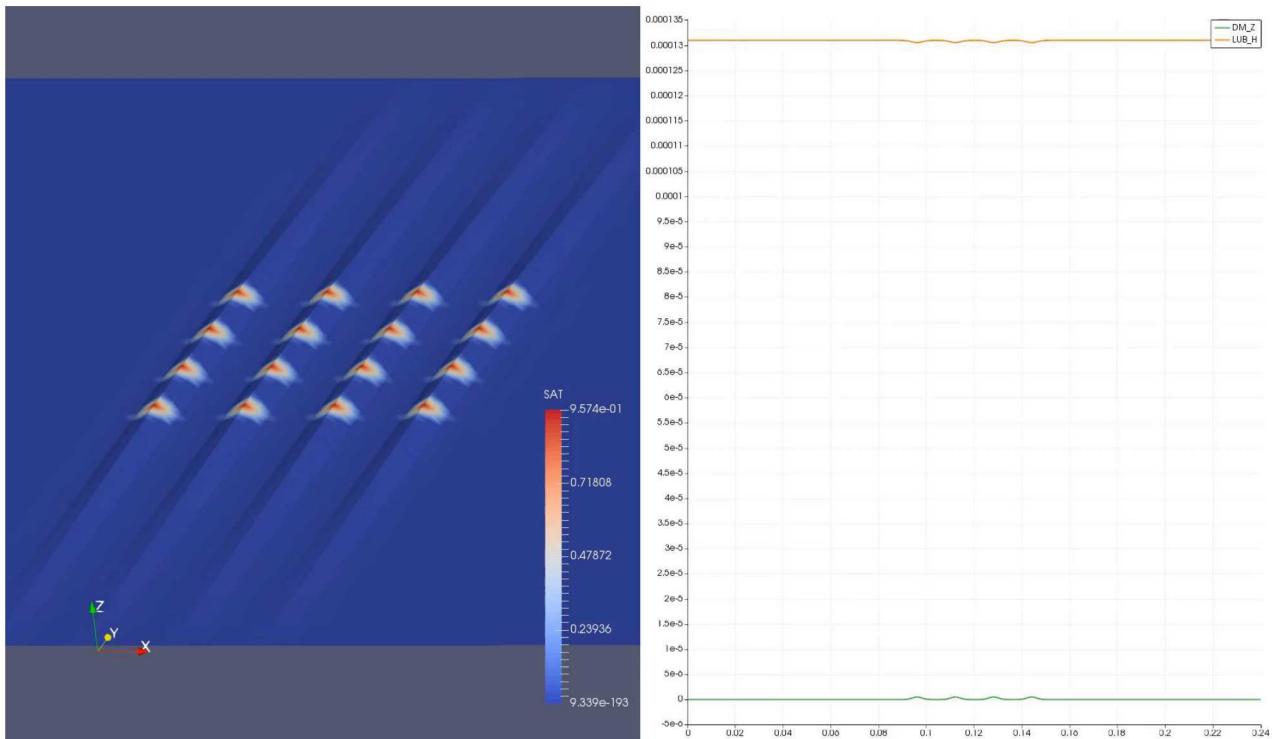
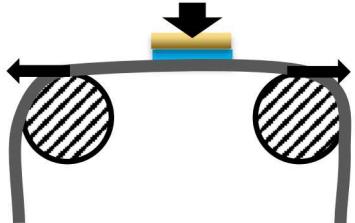
Stokes, G., 1898, Mathematical proof of the identity of the stream lines obtained by means of a viscous film with those of a perfect fluid moving in two dimensions: *Report of the British Association for the Advancement of Science*, p. 143-144.

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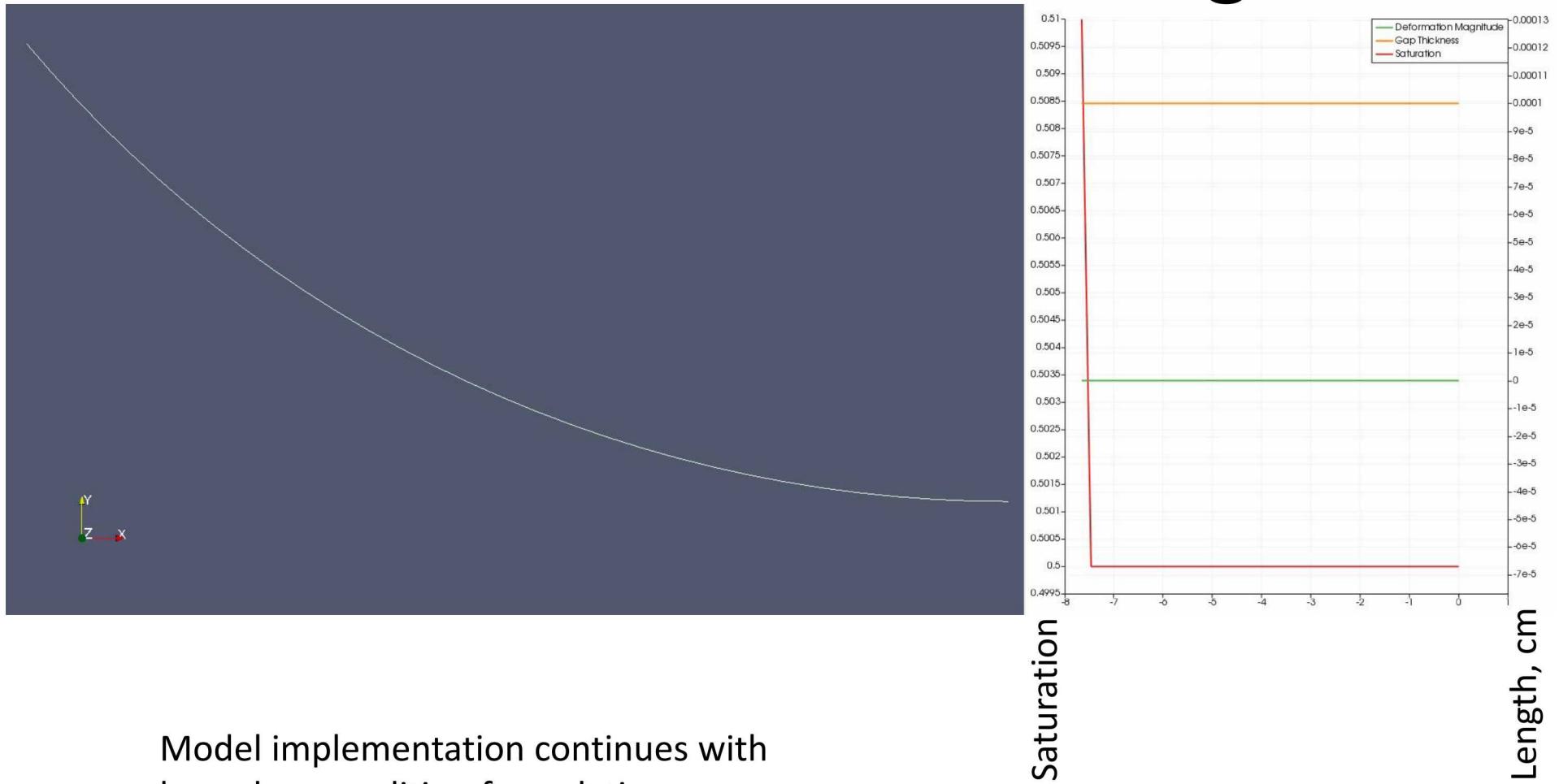
# Membrane + Reduced-Order, Separated Reynolds Lubrication

**Squeezing of liquid film**  
Membrane Deformation  
+ Reynolds Lubrication  
+ two-phase model



Demonstrated coupling of multiphase flow and  
structural mechanics

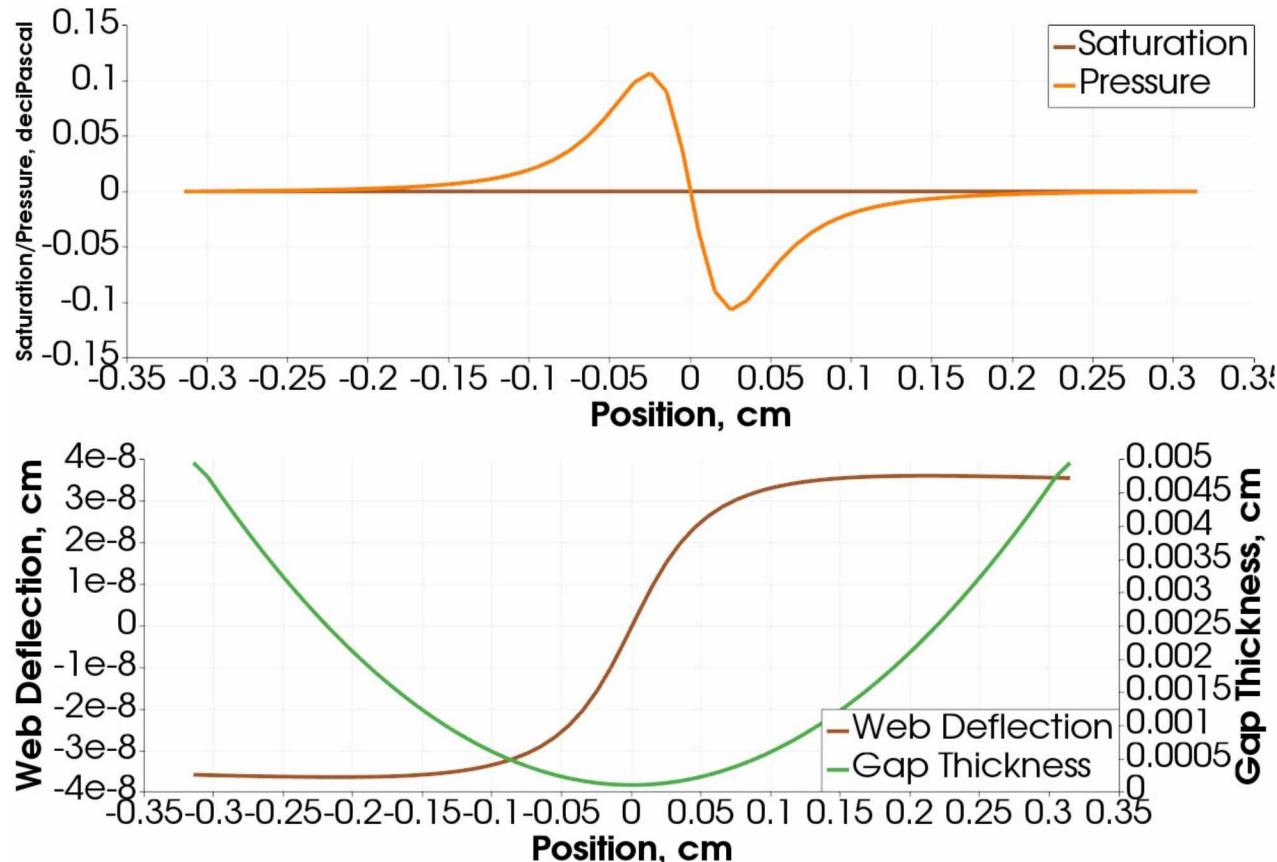
# Disperse Drop Merger Between Tensioned Web and Rotating Roller





$\uparrow h_{min}$

# Two Phase Lubrication Flow in Rolling Imprint Mode



The next challenge is to smooth out the intersection of partially saturated and fully saturated zones