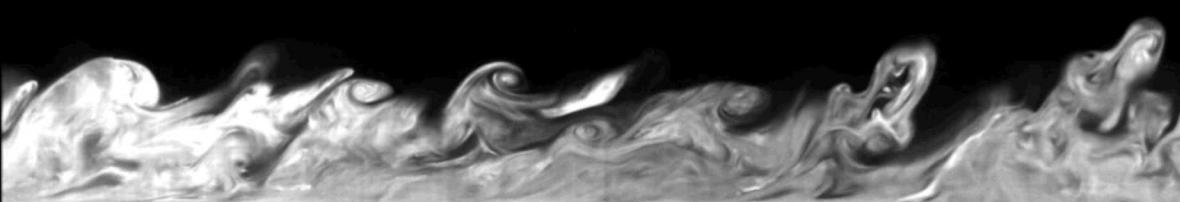


# Hairpin Vortex Packets in Oscillating Wall Turbulence



Lee, J. H., Kwon, Y. S., Hutchins, N., and Monty, J. P. (2012). Spatially developing turbulent boundary layer on a flat plate. *arXiv preprint arXiv:1210.3881*.

PRESENTED BY

Dr. Blake Lance, [blance@sandia.gov](mailto:blance@sandia.gov)

Penn State Fluid Dynamics Research Consortium

25 October 2018



SAND2018-12232PE



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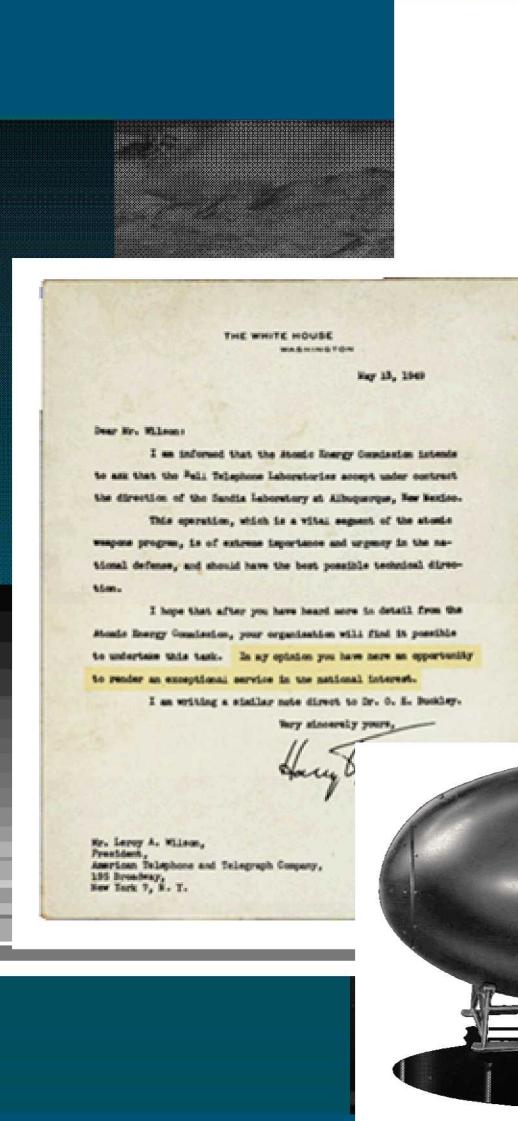


# Sandia National Lab's history is traced to the Manhattan Project



*...In my opinion you have here an opportunity to render an exceptional service in the national interest.*

- July 1945  
Los Alamos creates Z Division
- Nonnuclear component engineering
- November 1, 1949  
Sandia Laboratory established
- AT&T: 1949–1993
- Martin Marietta: 1993–1995
- Lockheed Martin: 1995–2017
- Honeywell: 2017–present



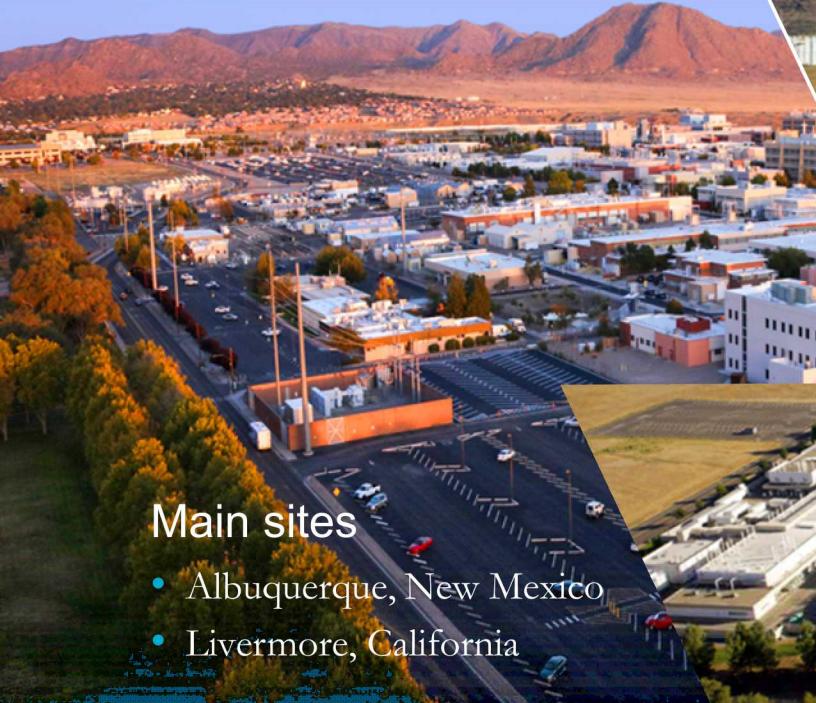
Sandia is a federally funded research and development center managed and operated by

National Technology & Engineering Solutions of Sandia, LLC, a wholly owned subsidiary of Honeywell International Inc.: 2017 – present

Government owned, contractor operated



## Sandia has facilities across the nation



### Main sites

- Albuquerque, New Mexico
- Livermore, California



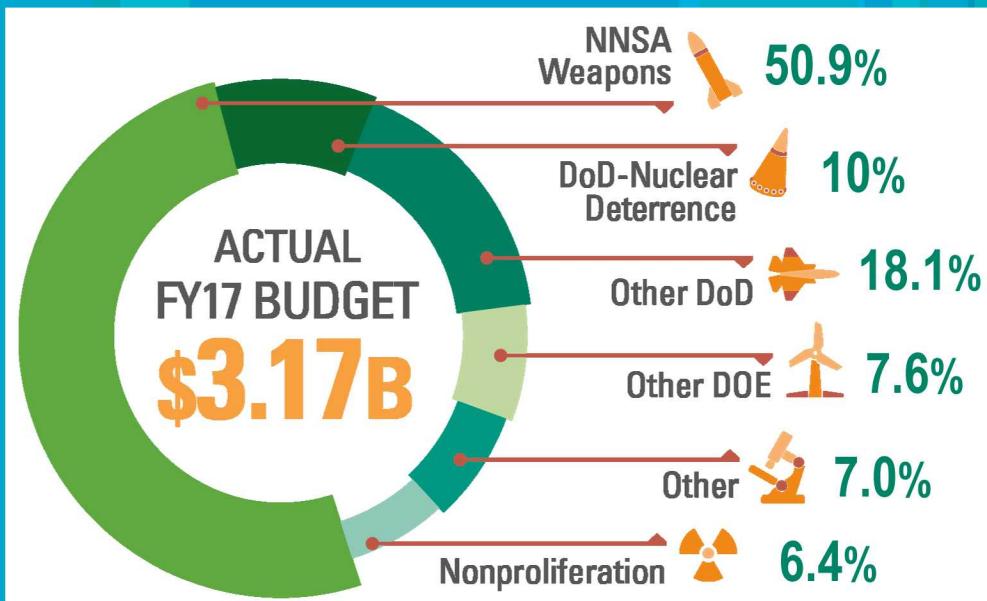
### Activity locations

- Kauai, Hawaii
- Waste Isolation Pilot Plant, Carlsbad, New Mexico
- Pantex Plant, Amarillo, Texas
- Tonopah, Nevada



Sandia develops  
advanced technologies  
to ensure global peace

# Sandia's budget covers a broad range of work



## OTHER

Department of Homeland Security  
Other federal agencies | Nonfederal entities  
CRADAs, licenses, royalties | Inter-entity work



## DoD

Air Force | Army | Navy  
Defense Threat Reduction Agency  
Ballistic Missile Defense Organization  
Office of the Secretary of Defense  
Defense Advanced Research Projects Agency  
Intelligence Community



## OTHER DOE

Science  
Energy Efficiency and Renewable Energy  
Nuclear Energy  
Environmental Management  
Electricity Delivery and Energy Reliability  
Other DOE

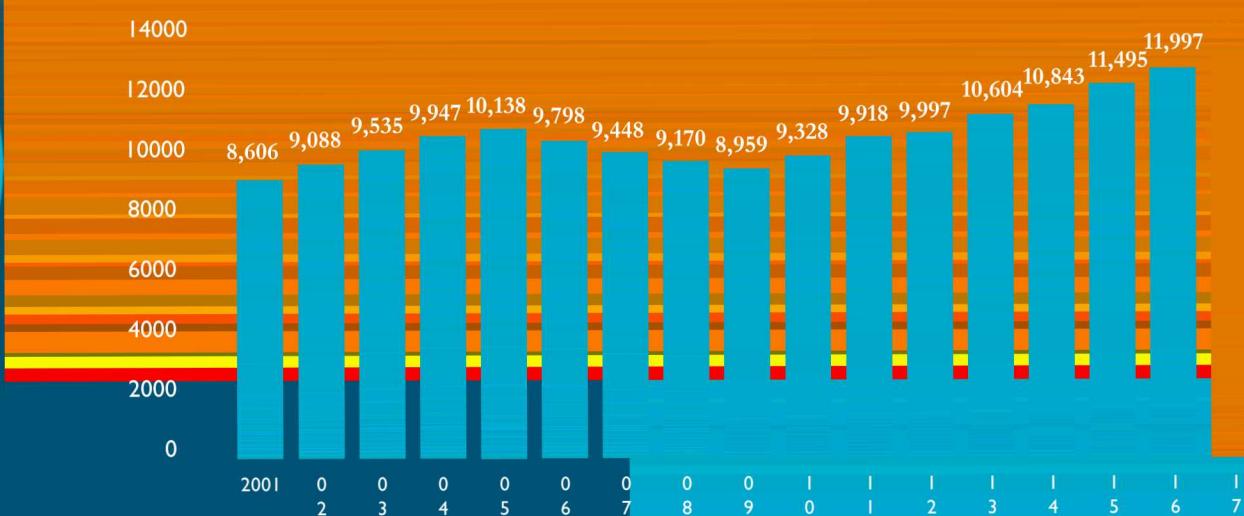


## NONPROLIFERATION

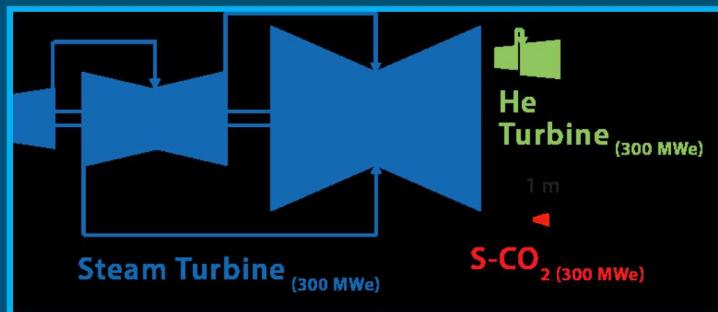
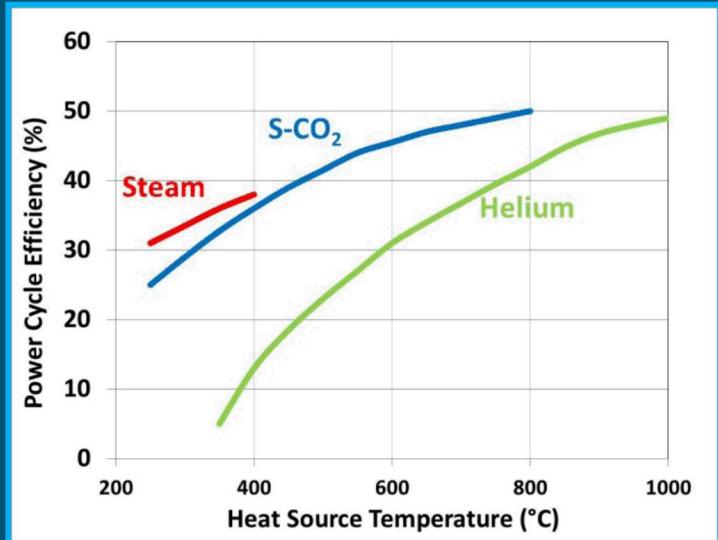
NNSA/NA20 | State Department

## 7 Sandia's workforce is growing

Staff has grown by over 3,000 since 2009 to meet all mission needs



# Supercritical CO<sub>2</sub> Brayton cycles have the potential for high efficiency and low cost energy conversion (heat to electricity)

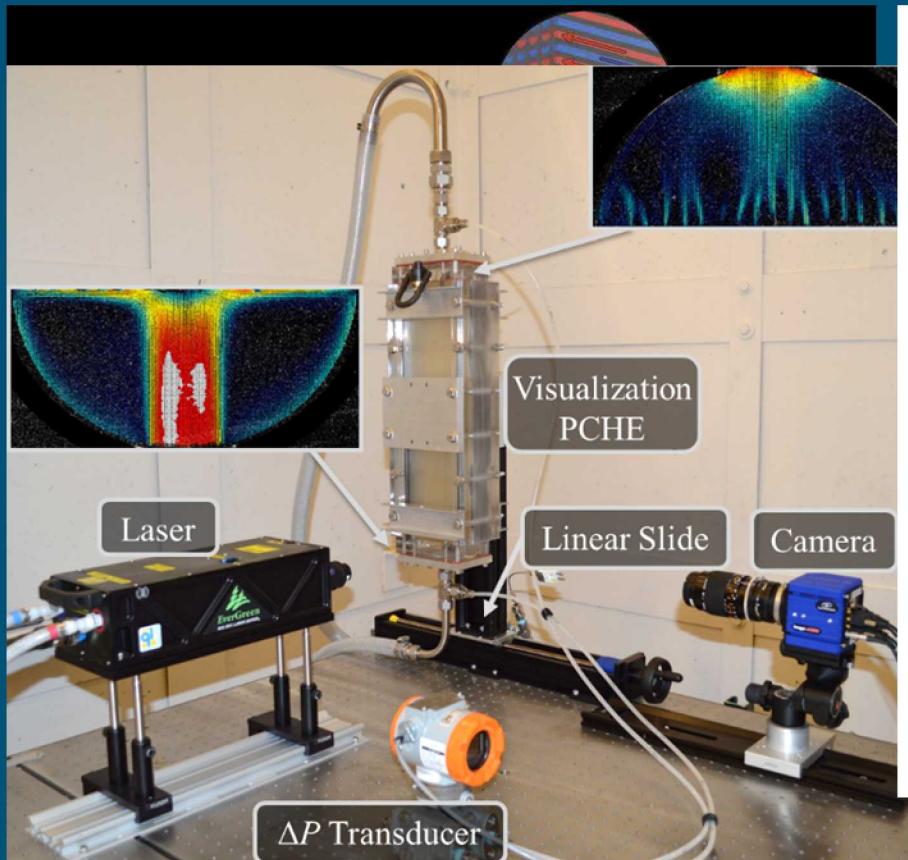


## Microchannel heat exchangers are a critical technology

Brayton cycles use a large amount of heat recuperation or recycling

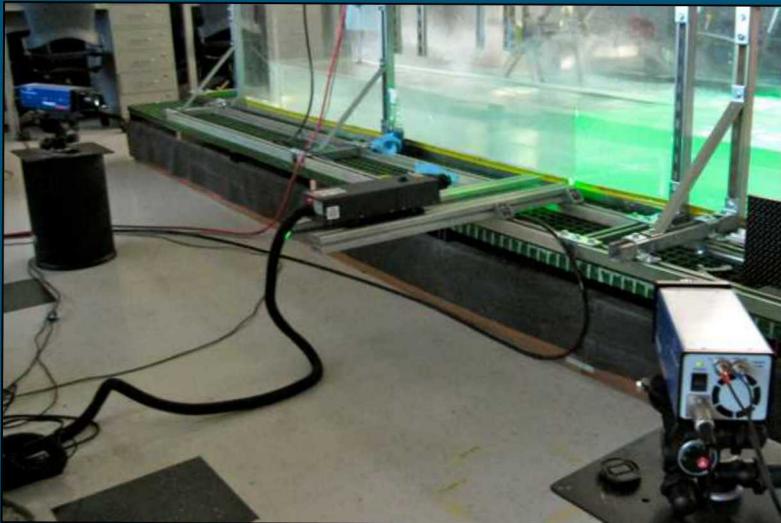
Microchannel heat exchangers are cheaper and smaller than typical shell and tube for high pressures

Flow uniformity and failure modes are being studied

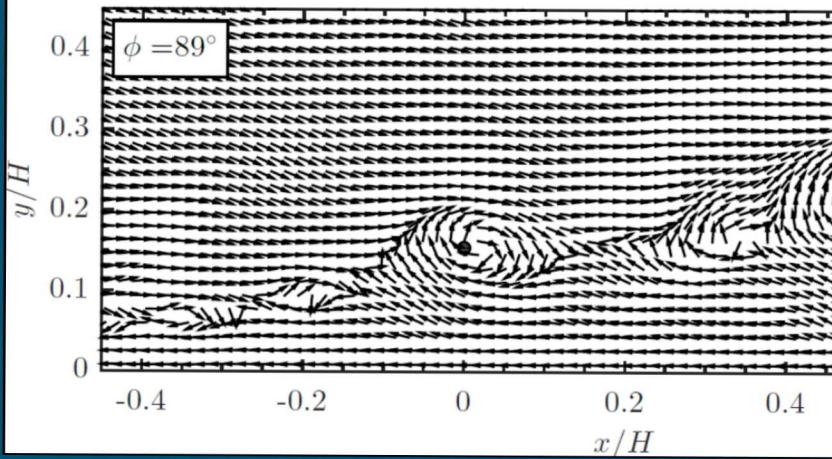


I've completed three previous fluid dynamics experiments

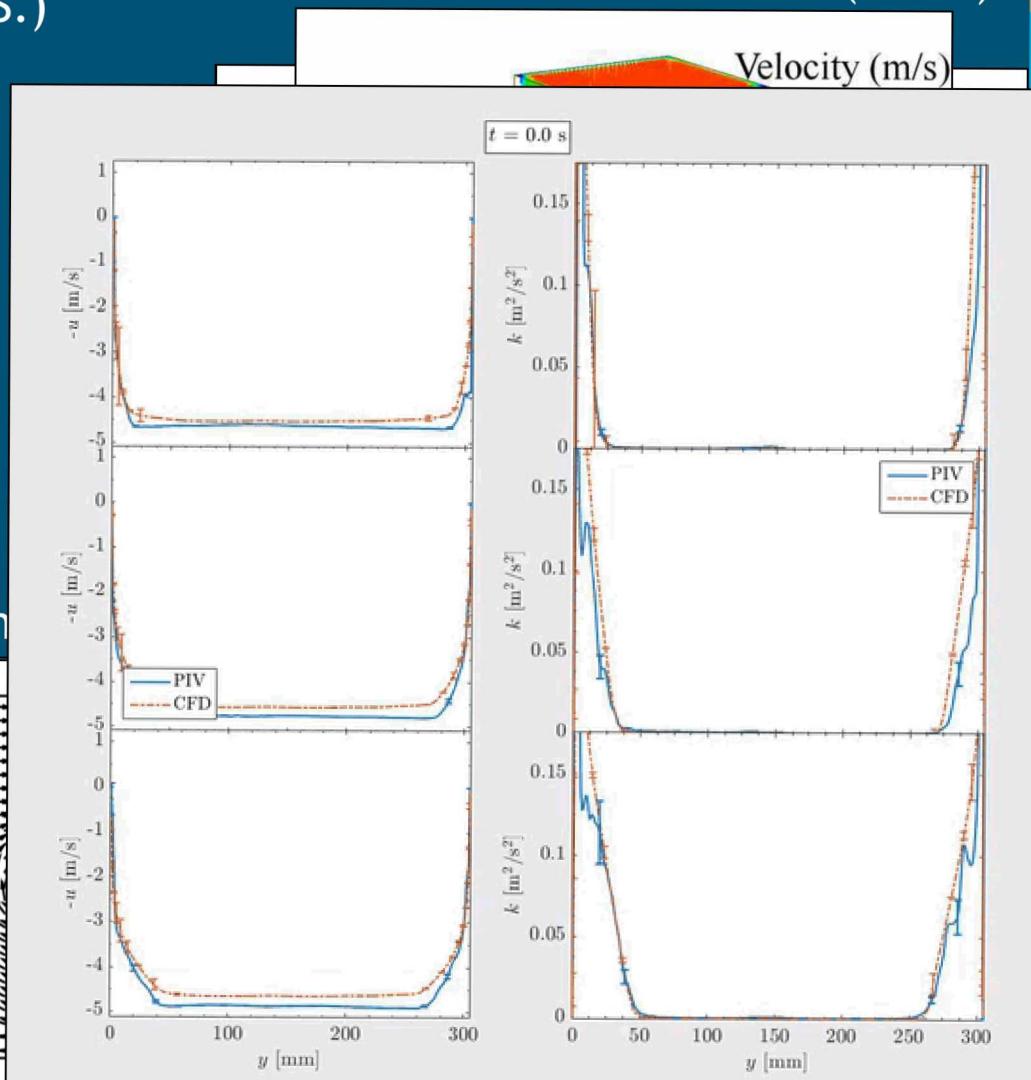
### Algal Raceway Mixing Optimization (M.S.)



### Oscillating Channel Flow (Sandia Intern)



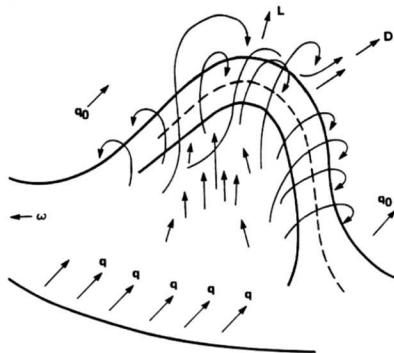
### Transient Mixed Convection (Ph.D.)



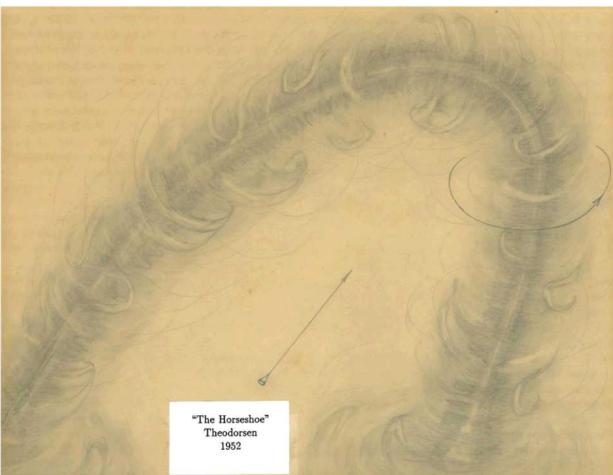
Solution Time 0 (s)

# Coherent structures have been measured in steady turbulent boundary layers, but what about for oscillating flow?

(a)



(b)



PHYSICS OF FLUIDS 19, 041301 (2007)

## Hairpin vortex organization in wall turbulence<sup>a)</sup>

Ronald J. Adrian

Laboratory for Energetic Flow and Turbulence, Department of Mechanical and Aerospace Engineering, Arizona State University, Tempe, Arizona 85287

(Received 31 October 2006; accepted 13 February 2007; published online 18 April 2007)

Coherent structures in wall turbulence transport momentum and provide a means of producing turbulent kinetic energy. Above the viscous wall layer, the hairpin vortex paradigm of Theodorsen coupled with the quasistreamwise vortex paradigm have gained considerable support from multidimensional visualization using particle image velocimetry and direct numerical simulation experiments. Hairpins can autogenerate to form packets that populate a significant fraction of the boundary layer, even at very high Reynolds numbers. The dynamics of packet formation and the ramifications of organization of coherent structures (hairpins or packets) into larger-scale structures are discussed. Evidence for a large-scale mechanism in the outer layer suggests that further organization of packets may occur on scales equal to and larger than the boundary layer thickness. © 2007 American Institute of Physics. [DOI: [10.1063/1.2717527](https://doi.org/10.1063/1.2717527)]

### I. INTRODUCTION

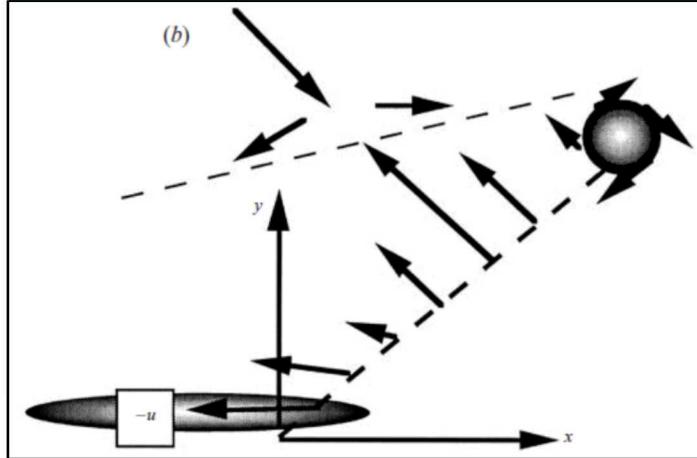
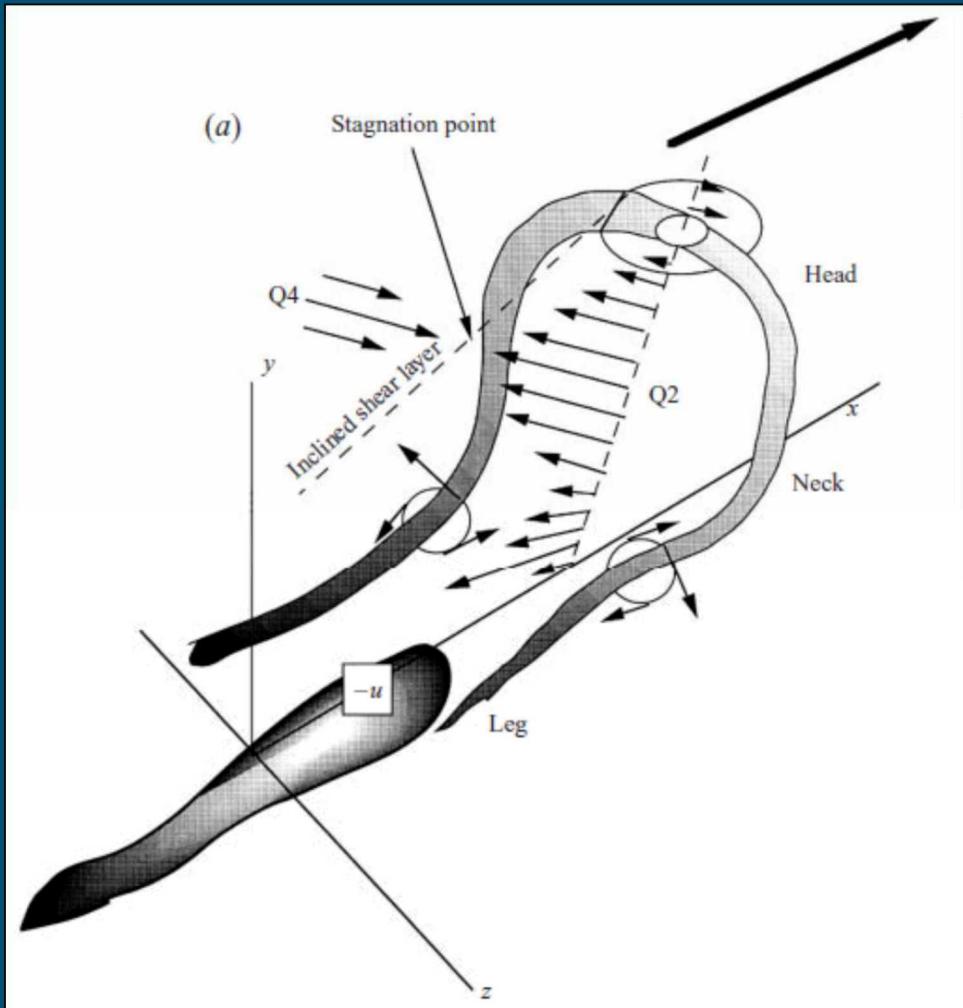
One of the principal schools of thought in the study of turbulence seeks to break the complex, multiscaled, random fields of turbulent motion down into more elementary organized motions that are variously called *eddies*<sup>1</sup> or *coherent structures*.<sup>2</sup> These motions can be thought of as individual entities if they persist for long times, i.e., if they possess *temporal coherence*. By virtue of fluid continuity, all motions possess some degree of spatial coherence, so coherence in space is not sufficient to define an organized motion. Only motions that live long enough to catch our eye in a flow visualization movie and/or contribute significantly to time-averaged statistics of the flow merit the study and attention we apply to organized structures. The kinematic properties of such motions (size, scaling properties, shape, vorticity, energy) and the dynamic properties (origin, stability, growth, genesis into new forms, and contribution to averages) are all of interest.

This paper is concerned with the structure of organized motion in the canonical forms of wall turbulence: steady, fully developed, incompressible, smooth-walled pipe and channel flow and the zero pressure gradient boundary layer. While these are the simplest possible wall flows, they exhibit most of the phenomena that are needed to understand turbulent flow over surfaces in more general cases. They contain

vance the development of ideas for scaling, manipulating and controlling wall turbulence. Less practically, but perhaps more satisfactorily, understanding the forms of the eddies, their origins, and their roles in creating stress and transporting energy in these canonical flows would go far toward answering some of the most tantalizing and long-standing questions in turbulence.

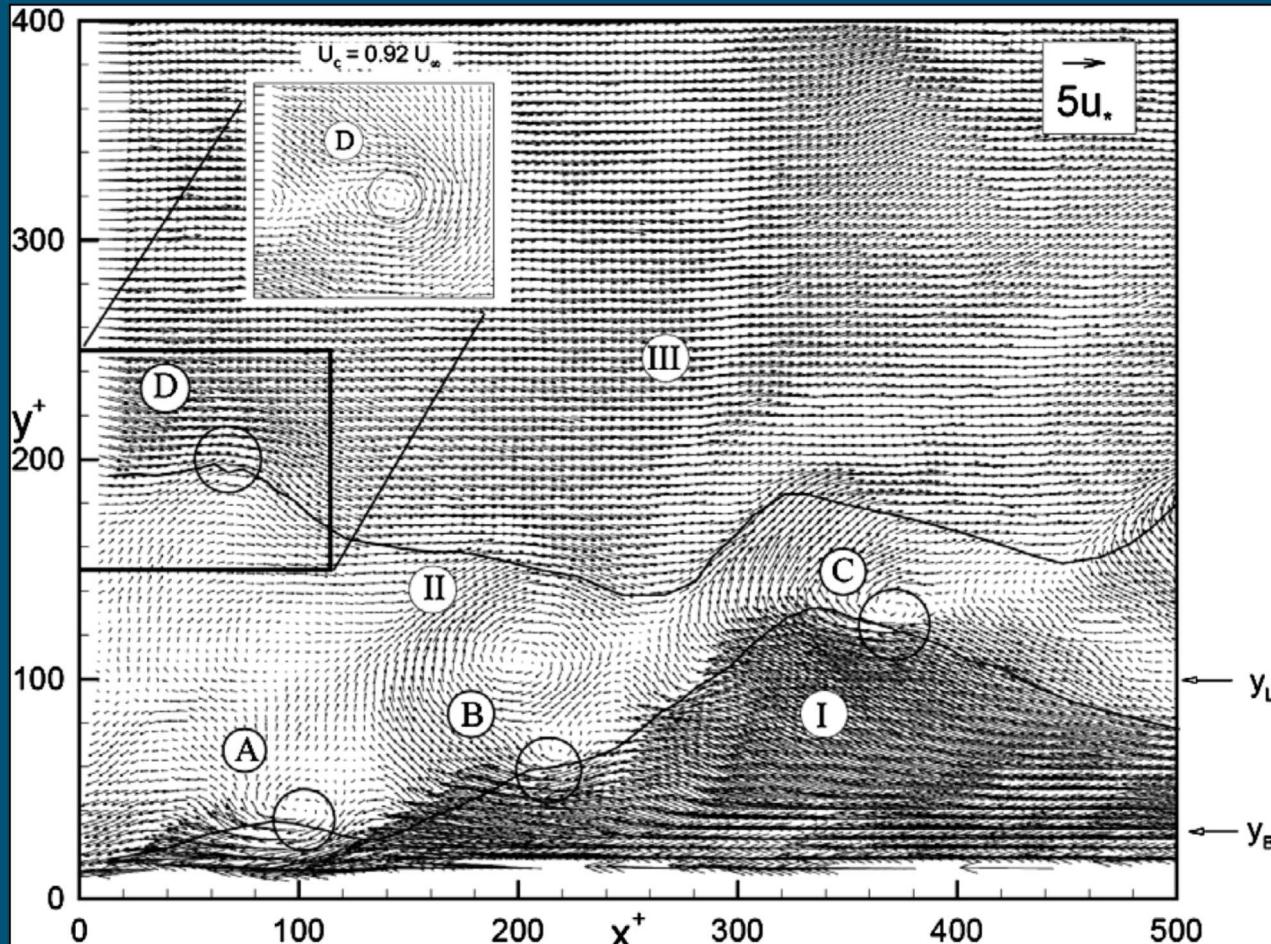
To begin, it is useful to summarize briefly the essential elements of wall turbulence, mainly to establish notation and define terms. Much of what we know can be inferred from the simple observation that the effect of turbulence on the mean flow is to flatten the profile relative to the parabolic profile that occurs in pipe and channel flow or the Blasius profile that occurs in the zero-pressure gradient laminar boundary layer, Fig. 1. The total shear stress is a sum of the Reynolds shear stress  $-\rho\bar{u}\bar{v}$  and the viscous stress,  $\tau(y) = -\bar{p}\bar{u} + \mu dU/dy$ . In fully developed pipe flow and channel flow, the absence of streamwise acceleration requires the stress to decrease linearly from the value at the wall,  $\tau_w = \tau(y=0) = \mu(dU/dy)_0$ , to zero at the centerline, where symmetry requires that  $-(\bar{u}\bar{v})_{\delta_0}$  and  $(dU/dy)_{\delta_0}$  each vanish. Consequently,  $\tau(y) = \tau_w(1 - y/\delta_0)$ . (The streamwise mean velocity is  $U$ , the streamwise and wall-normal velocity fluctuations about the mean are  $u$  and  $v$ ,  $y$  is distance from the wall,  $\rho$  is density, and  $\mu$  and  $\nu = \mu/\rho$  are the dynamic and kinematic viscosity, respectively.) The flattening of the mean velocity

# Hairpin Vortices have unique features



(a) Schematic of a hairpin vortex attached to the wall and the induced motion. (b) Signature of the hairpin vortex in the streamwise-wall-normal plane. The signature is insensitive to the spanwise location of the plane, until it intersects the concentrated core forming either side of the hairpin.

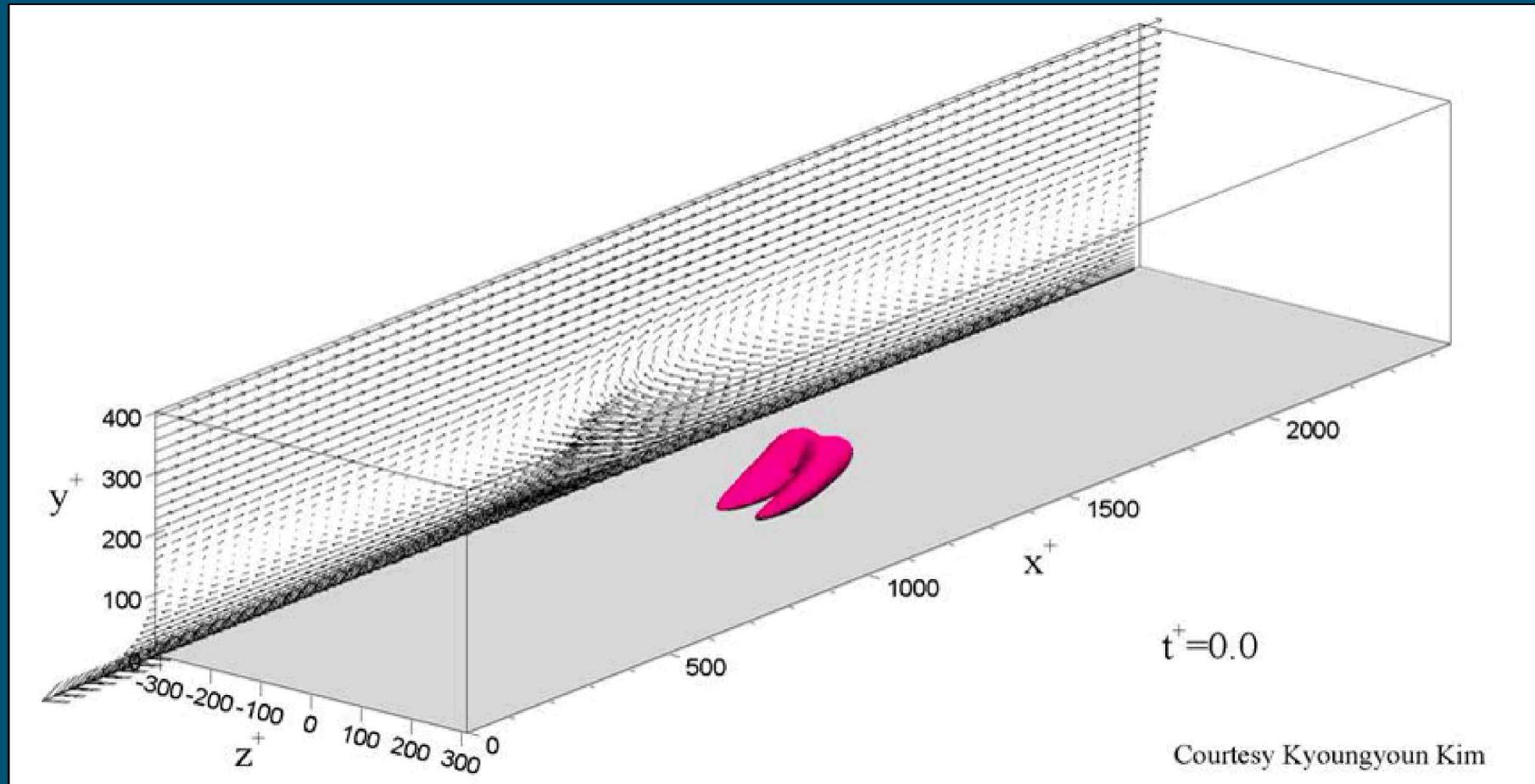
# Instantaneous vector fields have regions of uniform momentum



Hairpin vortex signatures in a PIV measurement of flow in the streamwise-wall-normal plane of a turbulent boundary layer,  $Re_\theta = 930$ . The heads of the hairpins are labeled A, B, C, and D. Note the correspondence between the flow patterns below and behind each head with the hairpin signature. Zones of uniform momentum are labeled I, II, and III. The reference frame for the vectors is translating at 80% of the free-stream velocity.

R. J. Adrian, C. D. Meinhart, and C. D. Tomkins, "Vortex organization in the outer region of the turbulent boundary layer," *J. Fluid Mech.* **422**, 1 (2000).

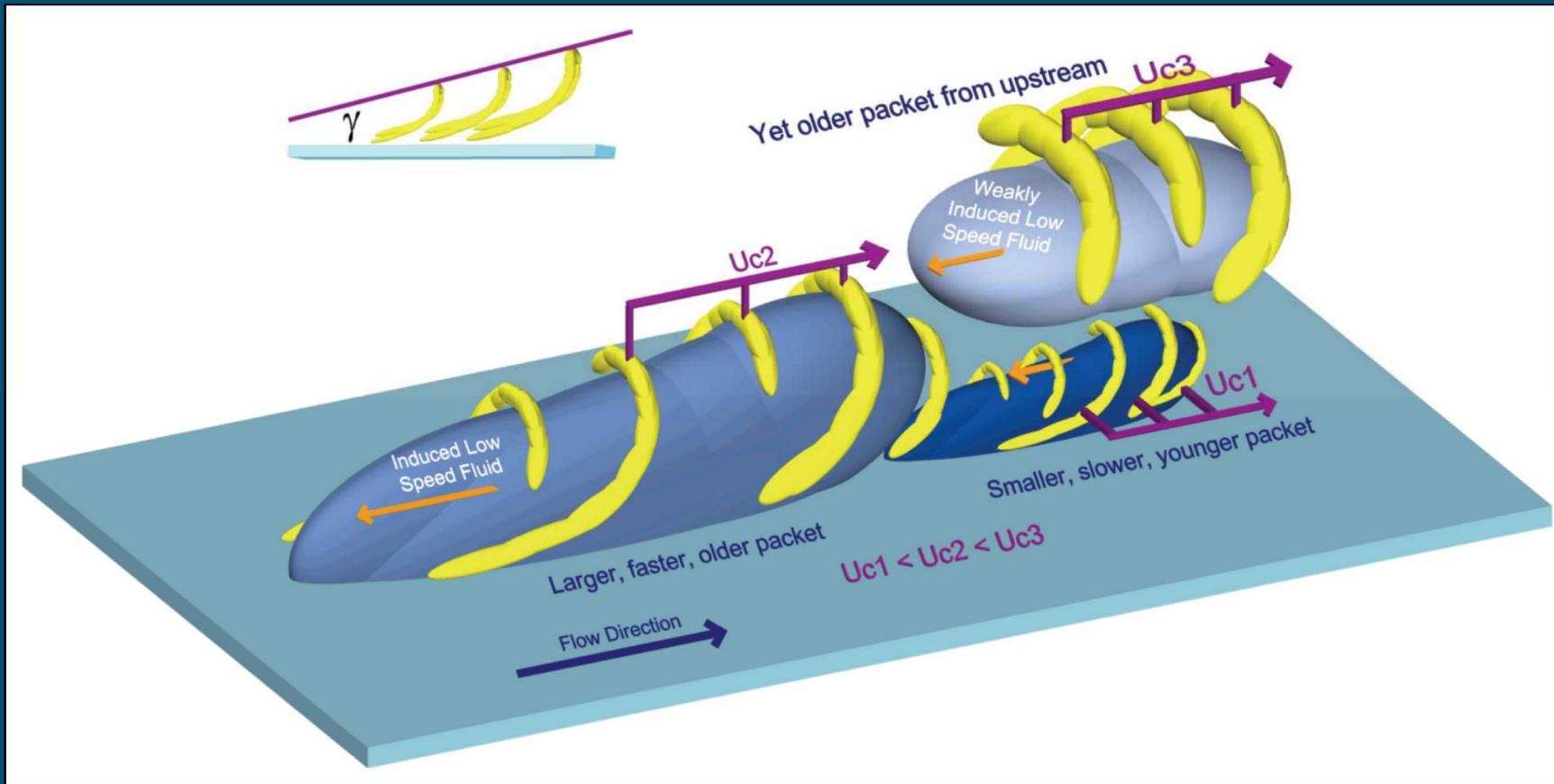
# Hairpin Vortices have been predicted with DNS in boundary layers



Courtesy Kyoungyoun Kim

Evolution of a packet of hairpins from a conditional Q2 event. Surface is an isosurface of swirling strength. The Reynolds number is  $Re_\tau = 395$ .

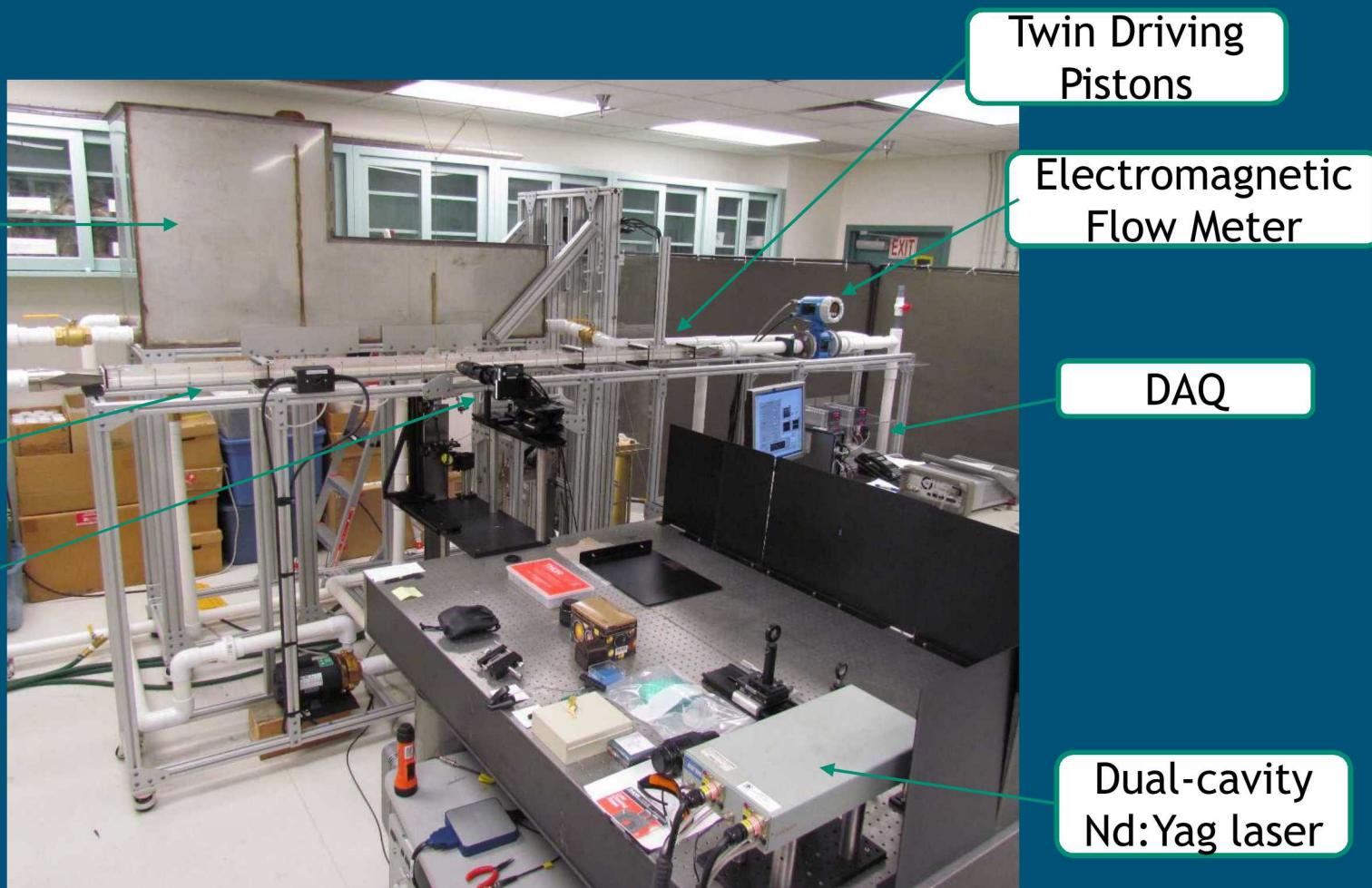
# Hairpin Vortices come in packets and have scales that depend on their age



Conceptual scenario of hairpins attached to the wall and growing in an environment of overlying larger hairpin packets

Our coherent structures experimental facility is called the SEAWOLF

# Sediment Erosion Actuated by Wave Oscillations and Linear Flow



# Oscillating flow was driven by a pair of piston-cylinders

Servomotors

Lead Screws

Pistons



Dual 10" pistons  
driven by  
servomotors to  
produce oscillating  
flow

The PIV system was assembled from borrowed parts with LabVIEW used for timing and image acquisition



Infinity Microscope and RedLake CCD digital camera

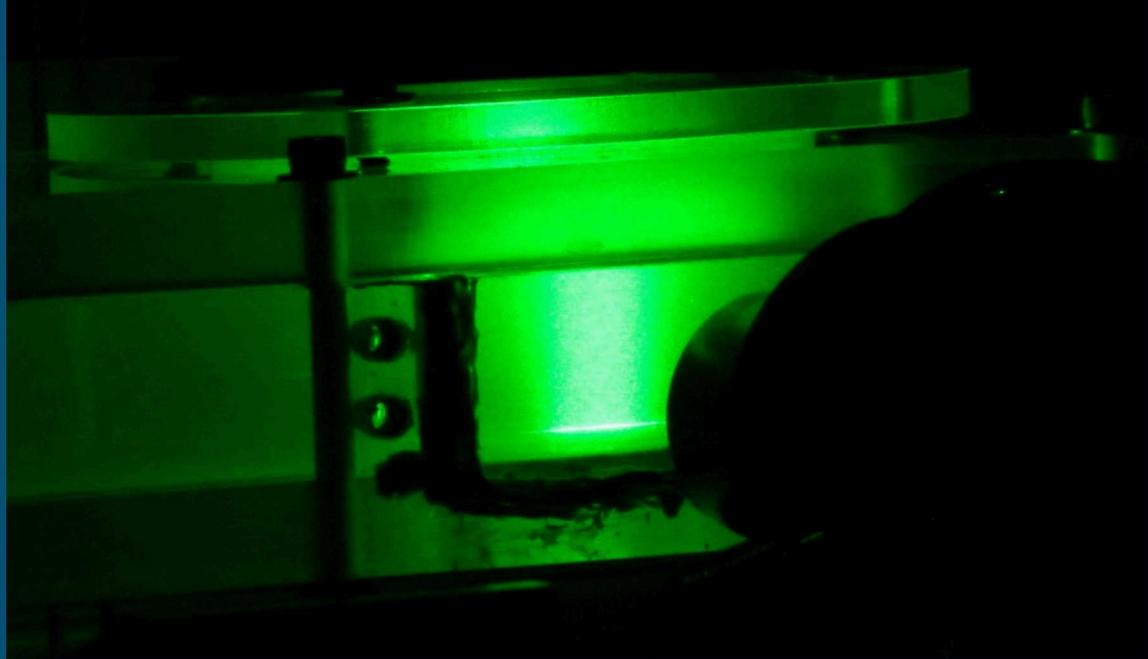
Test Section

CCD Camera

Microscope

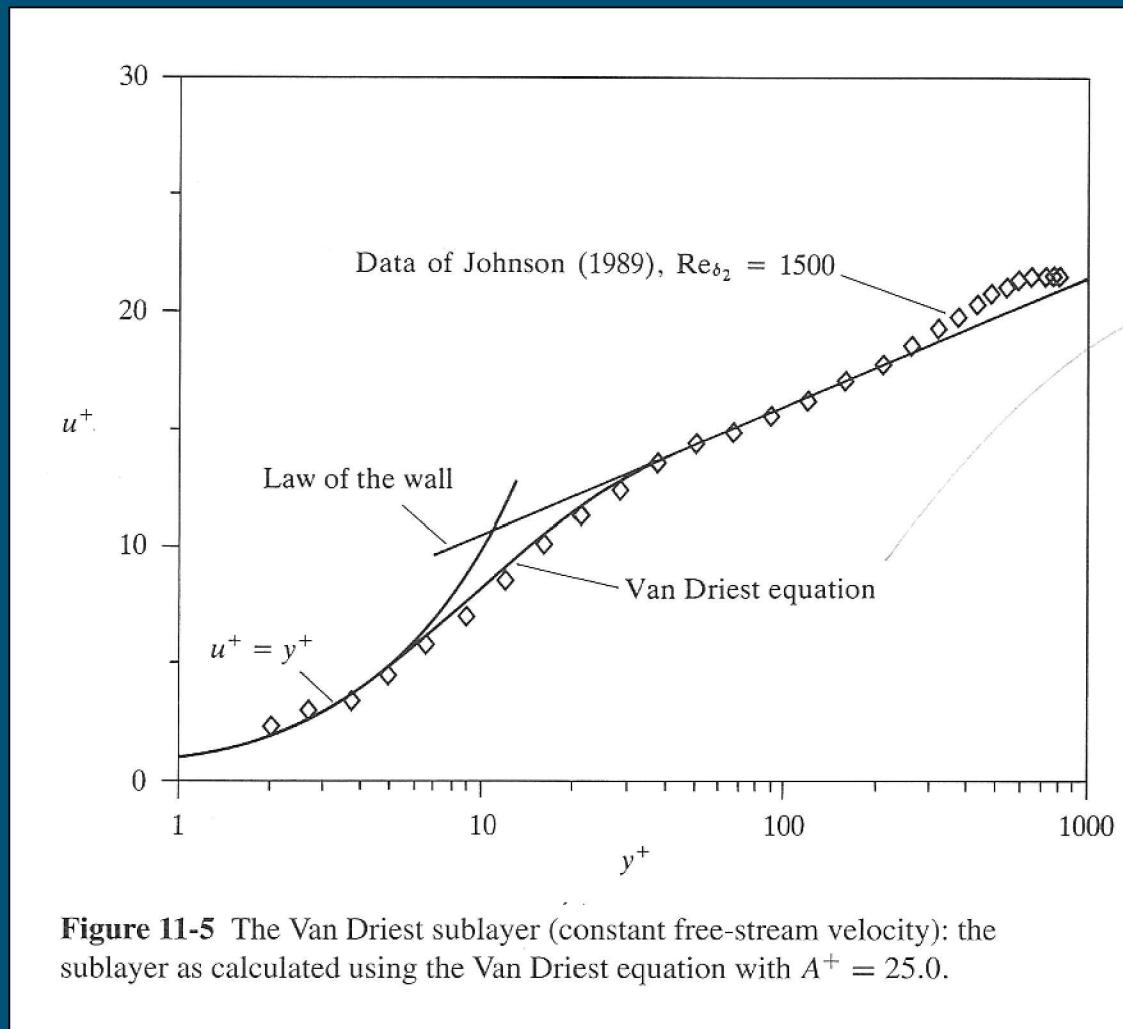
Laser Sheet  
Optics





- Flow seeded with  $10 \mu\text{m}$  diameter hollow glass spheres
- Seed particles illuminated by laser sheet
- Commercial software (DaVis) computes the cross-correlation

## So far you have seen the turbulent boundary layer time-mean velocity in wall coordinates



**Figure 11-5** The Van Driest sublayer (constant free-stream velocity): the sublayer as calculated using the Van Driest equation with  $A^+ = 25.0$ .

Entry #: V84181

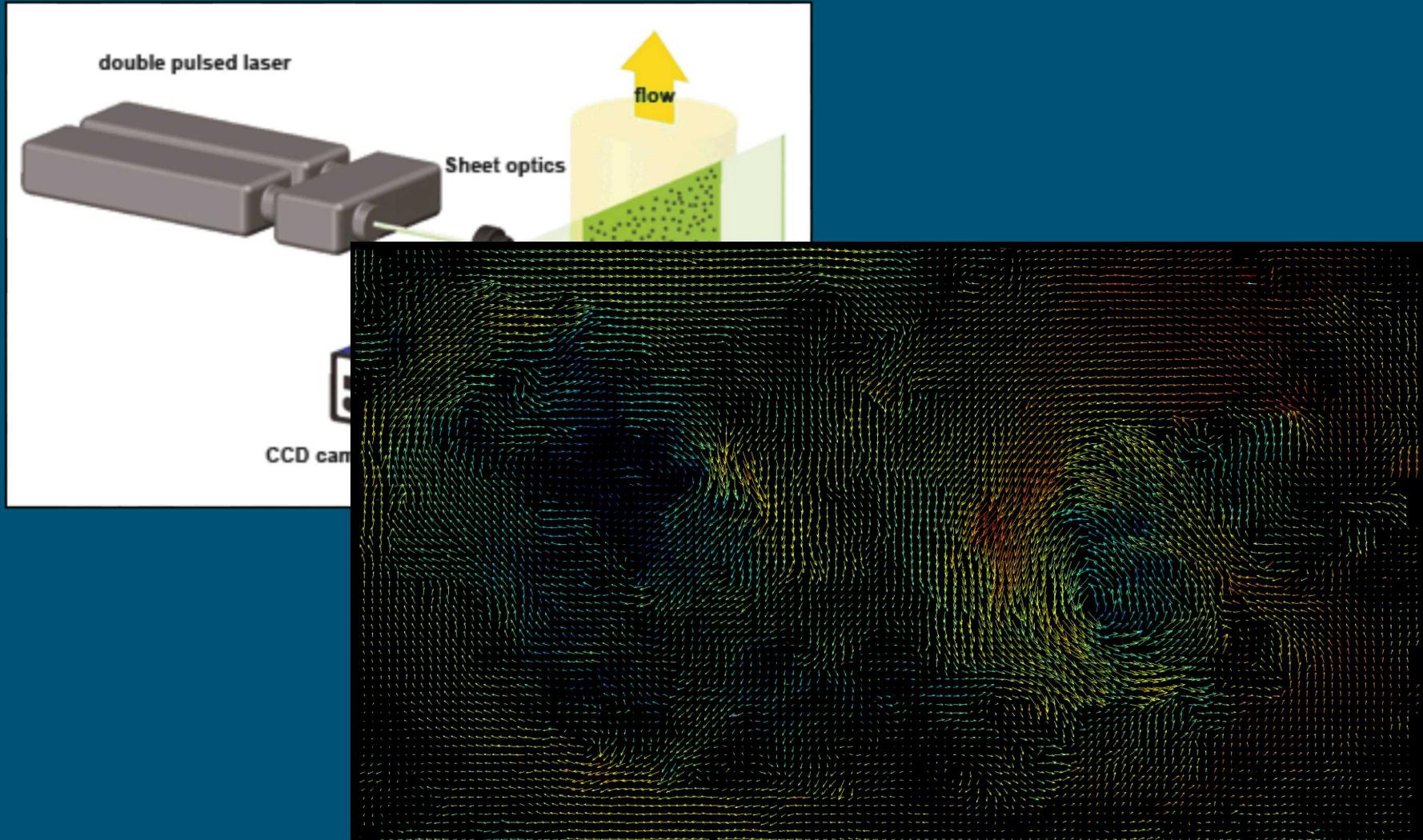
## Spatially developing turbulent boundary layer on a flat plate

J.H. Lee, Y.S. Kwon, N. Hutchins and J.P. Monty

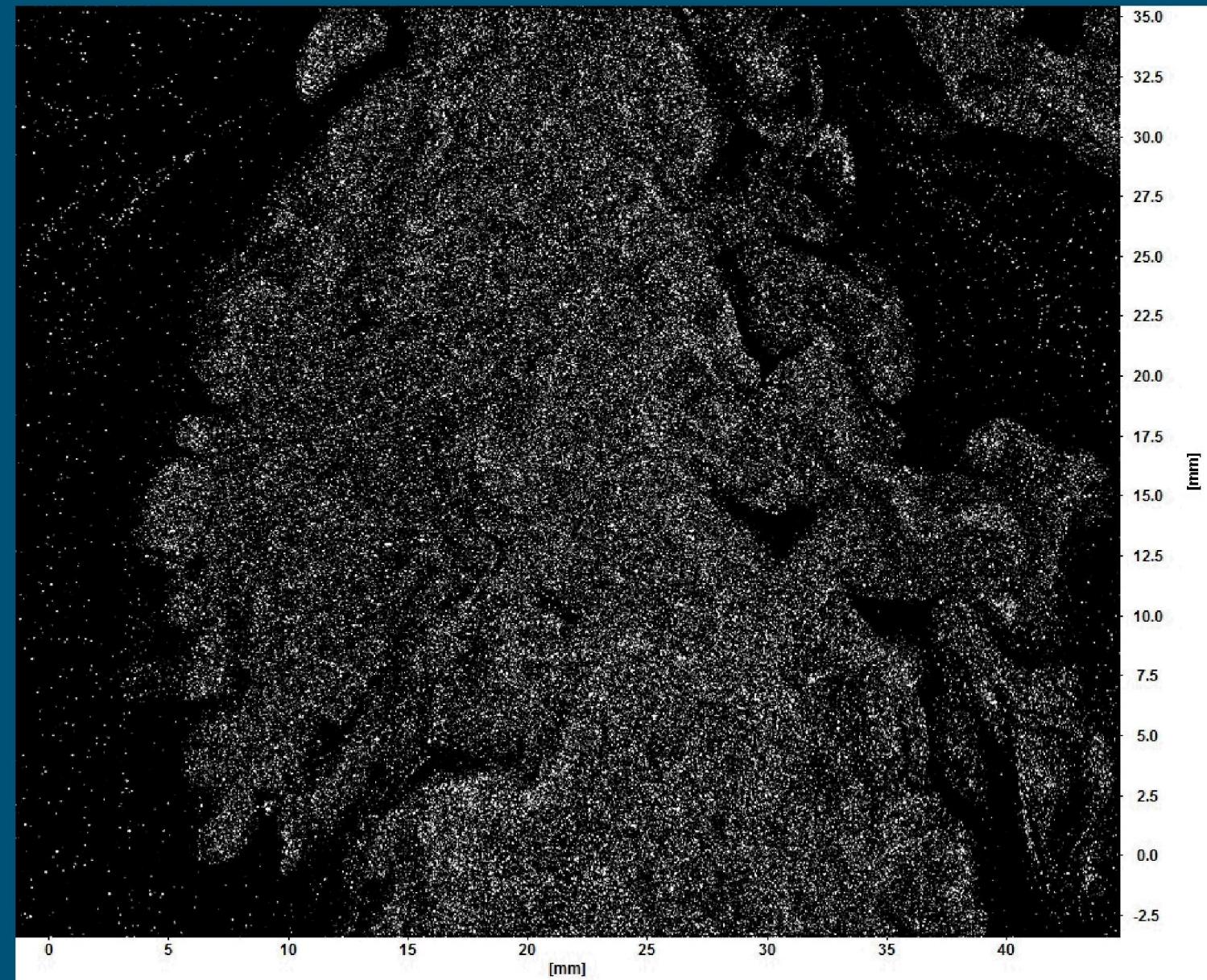
Department of Mechanical Engineering  
The University of Melbourne



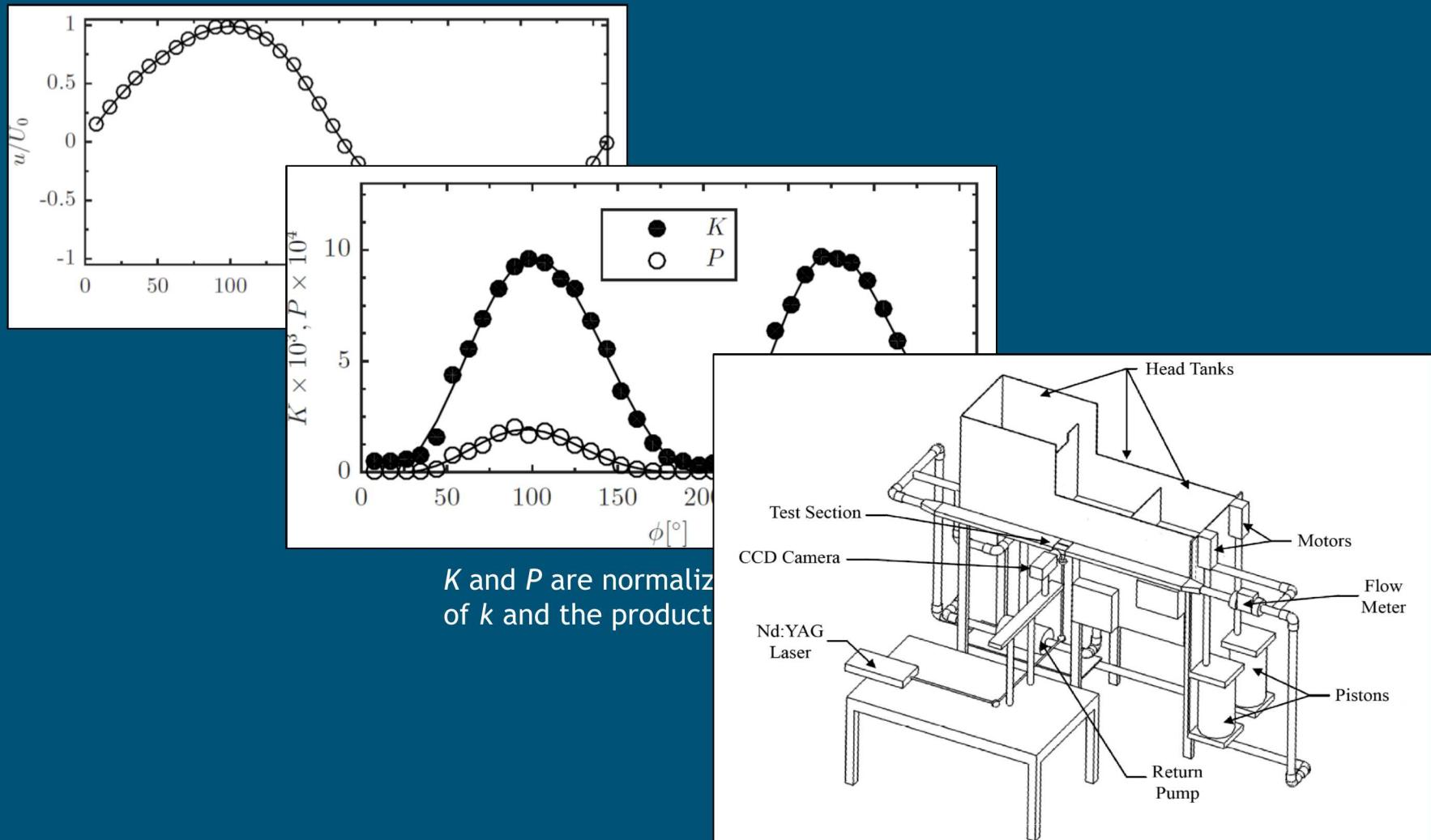
# Particle Image Velocimetry (PIV) is an excellent tool for measuring Coherent Structures



## Your eye can track the fluid motion in most PIV images

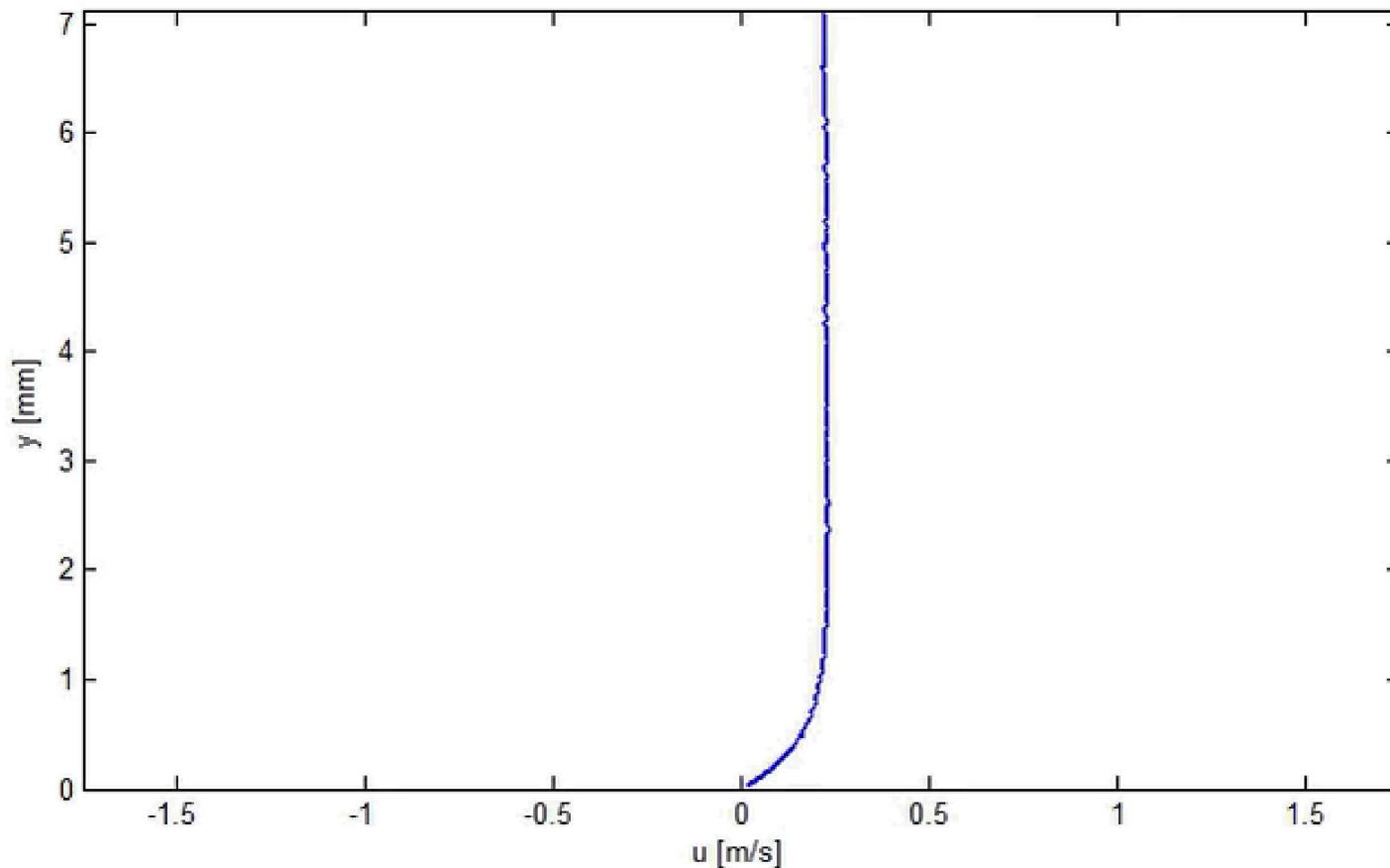


# Hairpin Vortices exist in steady turbulence, but what about oscillating turbulence?

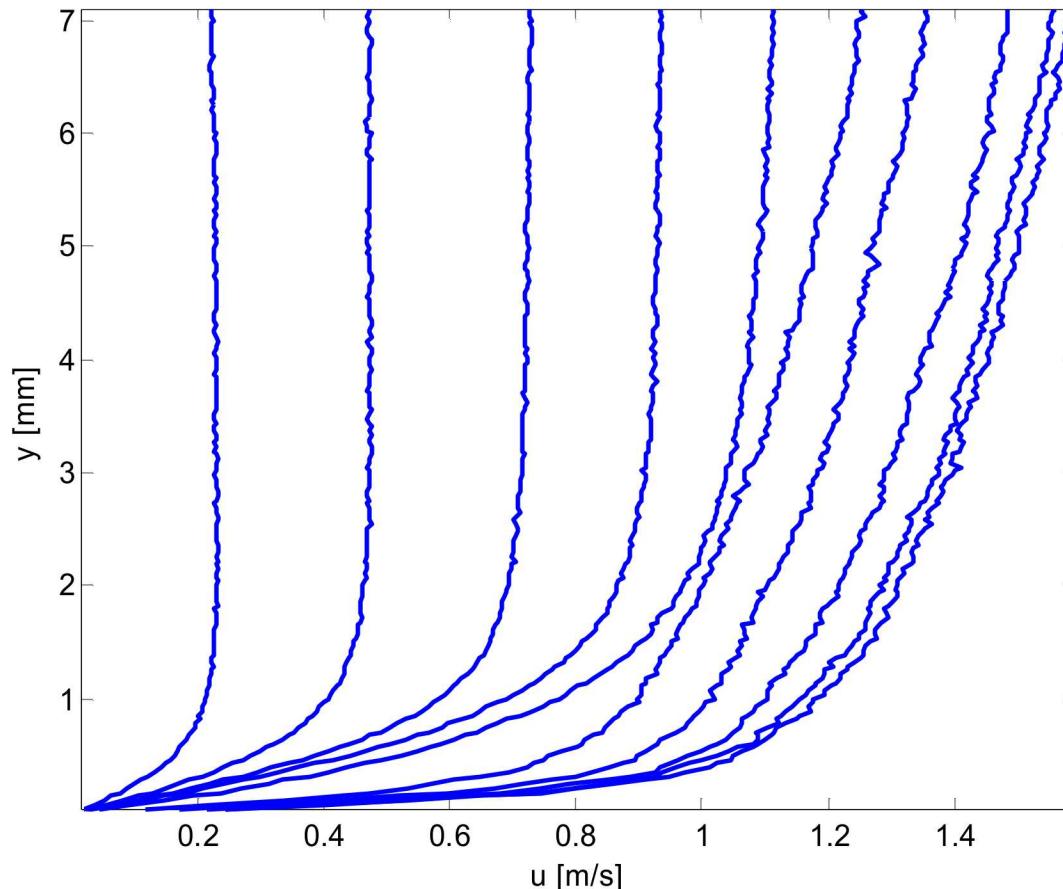


SEAWOLF at Sandia National Labs

The flow begins laminar, but transition to turbulence is observed as the velocity increases.



The flow begins laminar, but transition to turbulence is observed as the velocity increases.



Typically the Reynolds number for oscillating flow is  $Re_\delta$

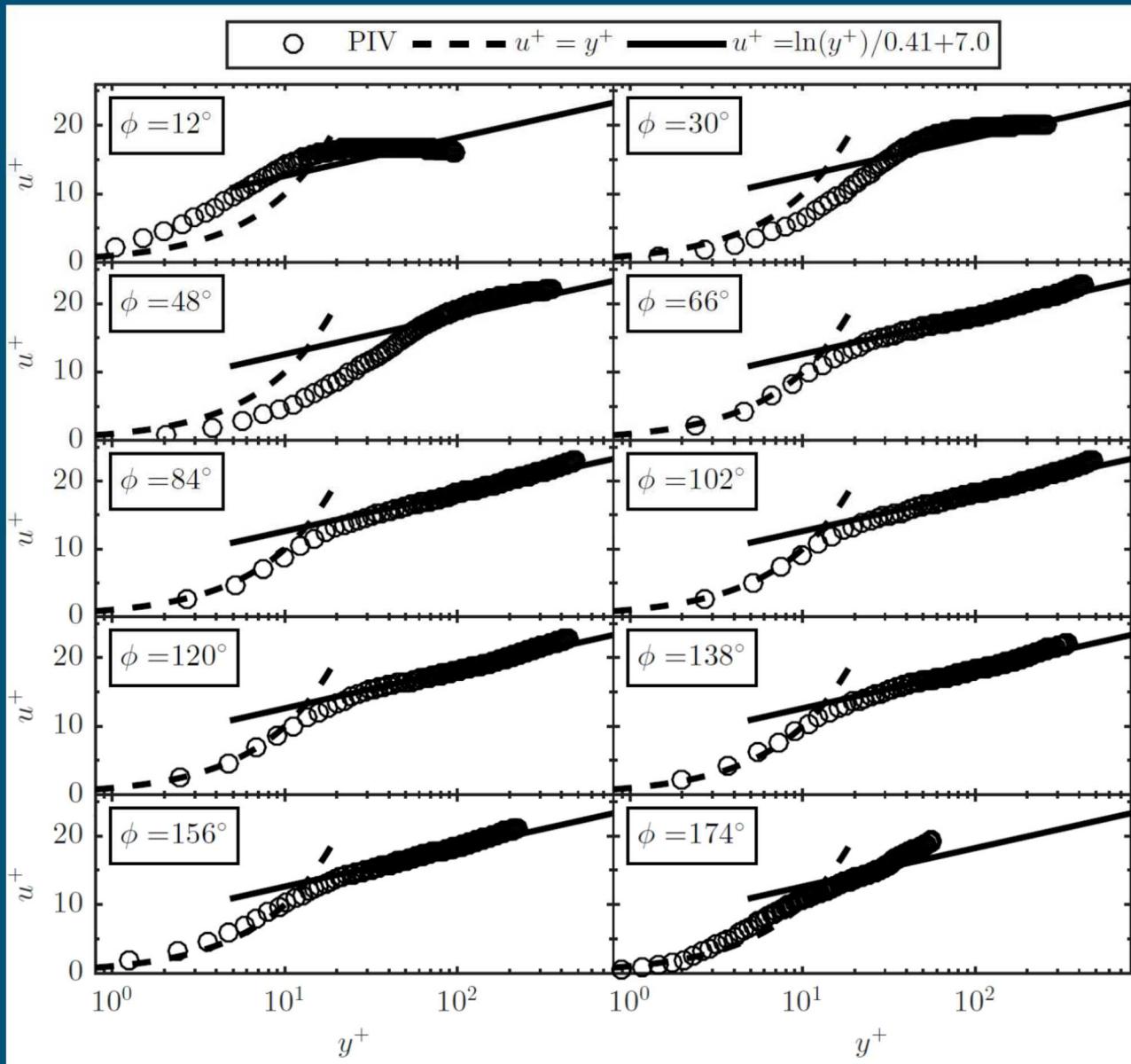
$$Re_\delta = \frac{U_0 \delta}{\nu}$$

$U_0$ [m/s]	$Re_\delta$
0.81	1440
1.35	2400
1.89	3360

The Stokes-layer thickness is given by  $\delta$

$$\delta = \sqrt{\frac{2\nu}{\omega}}$$

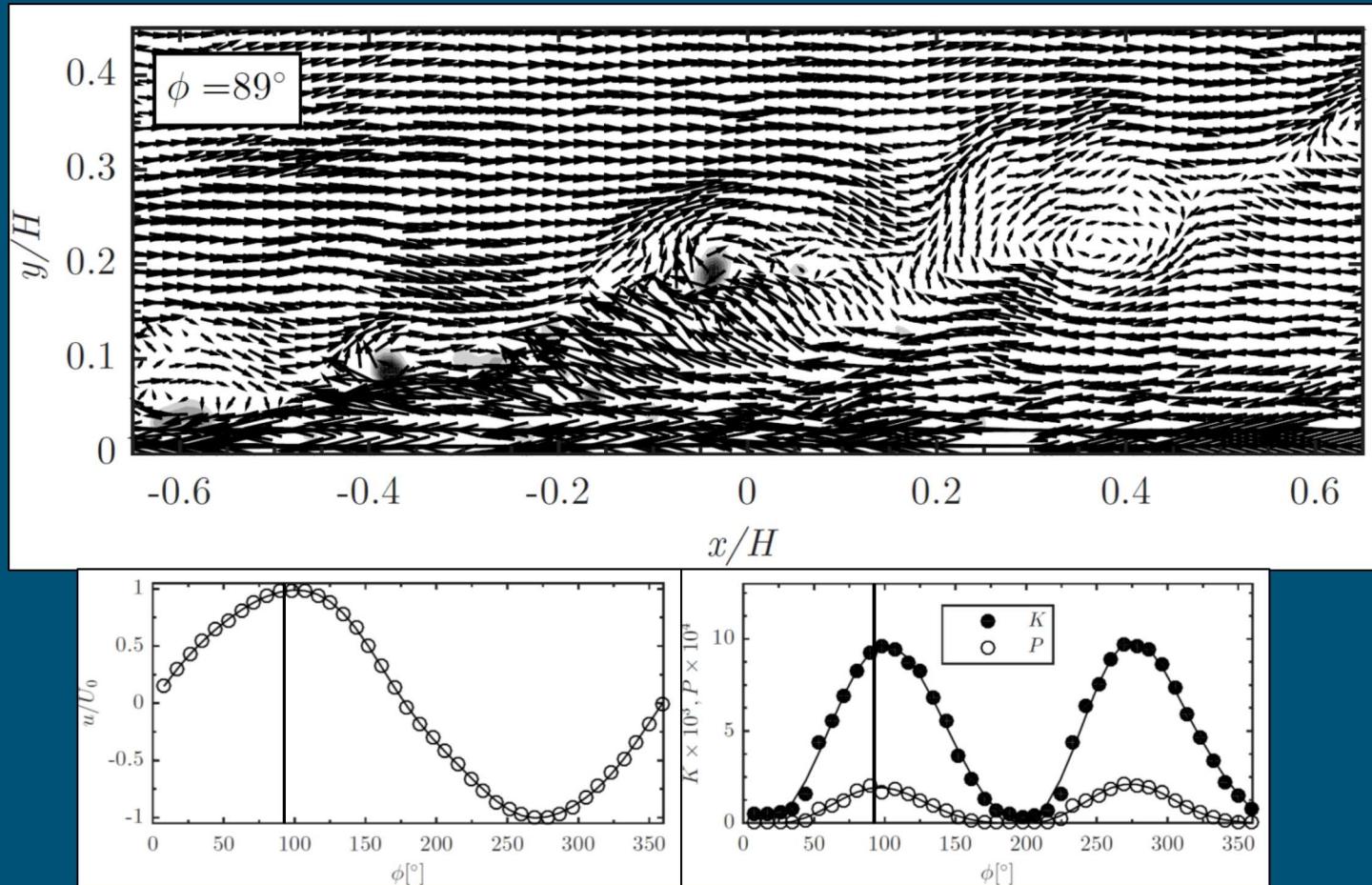
# Nondimensional velocity profiles at turbulent phases are similar to those of steady flow



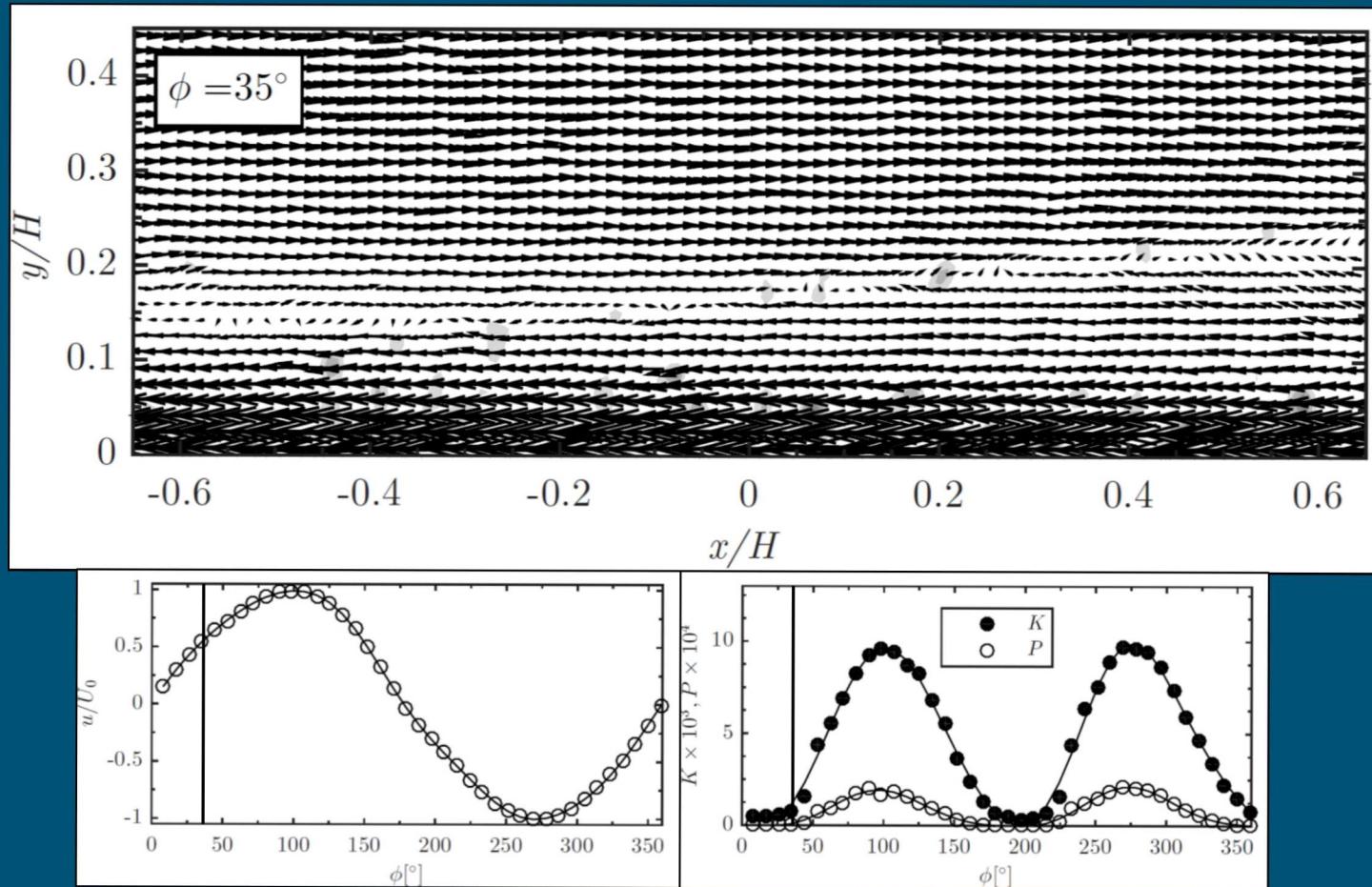
## They do exist for oscillating flow



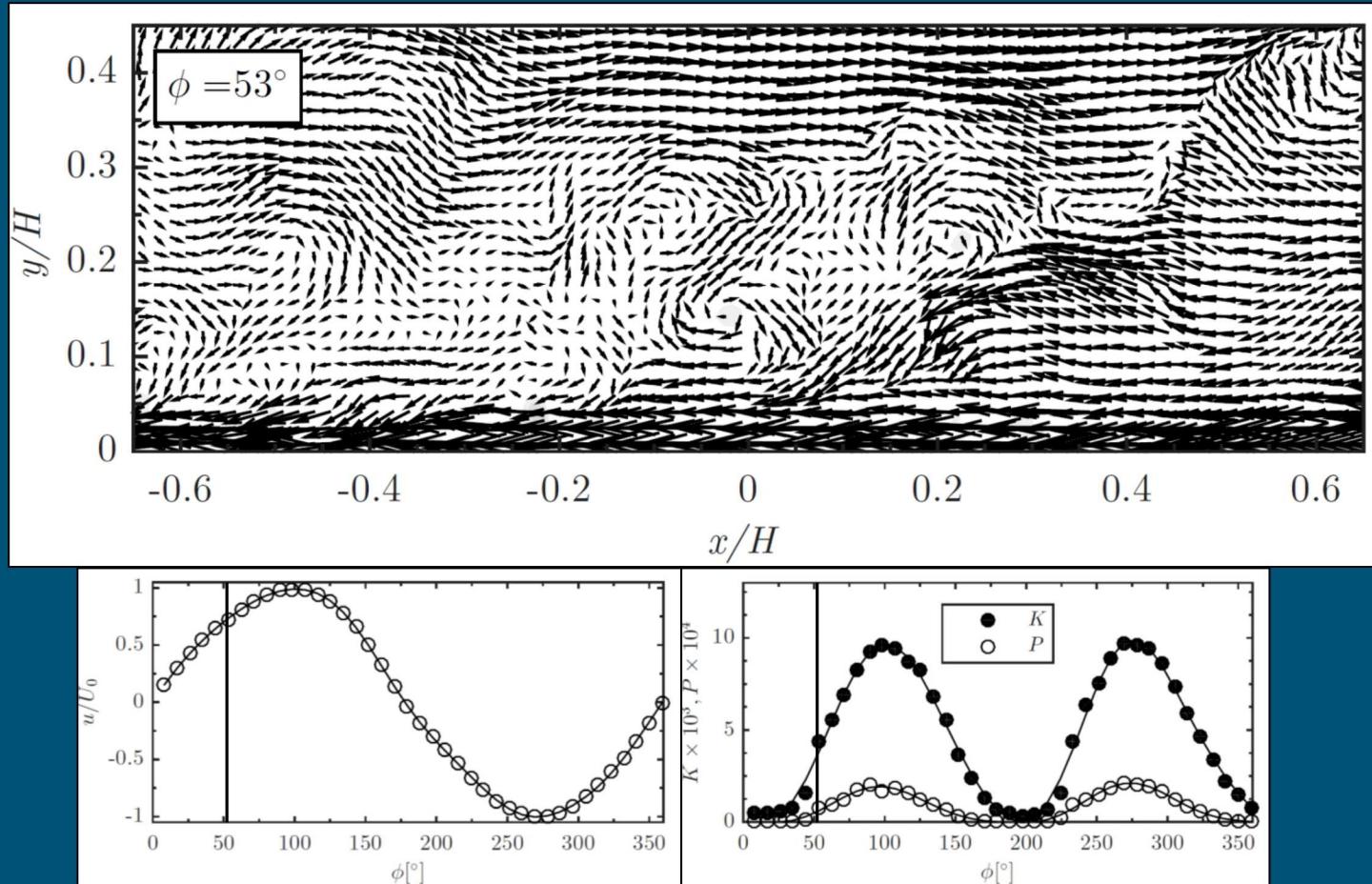
Instantaneous velocity fields with 90% of the mean streamwise subtracted and swirl strength in the background to highlight vortex cores



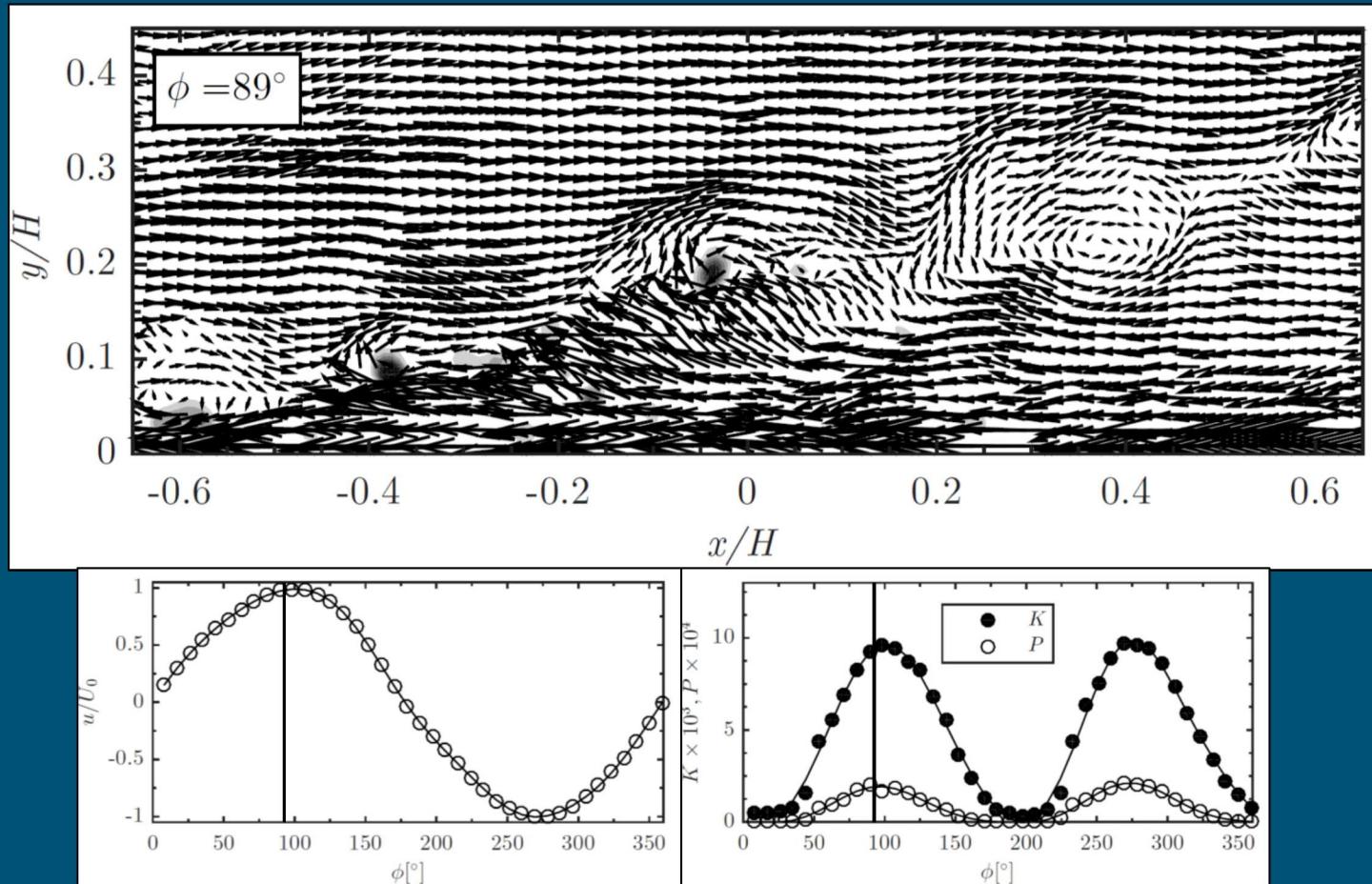
# They do exist for oscillating flow



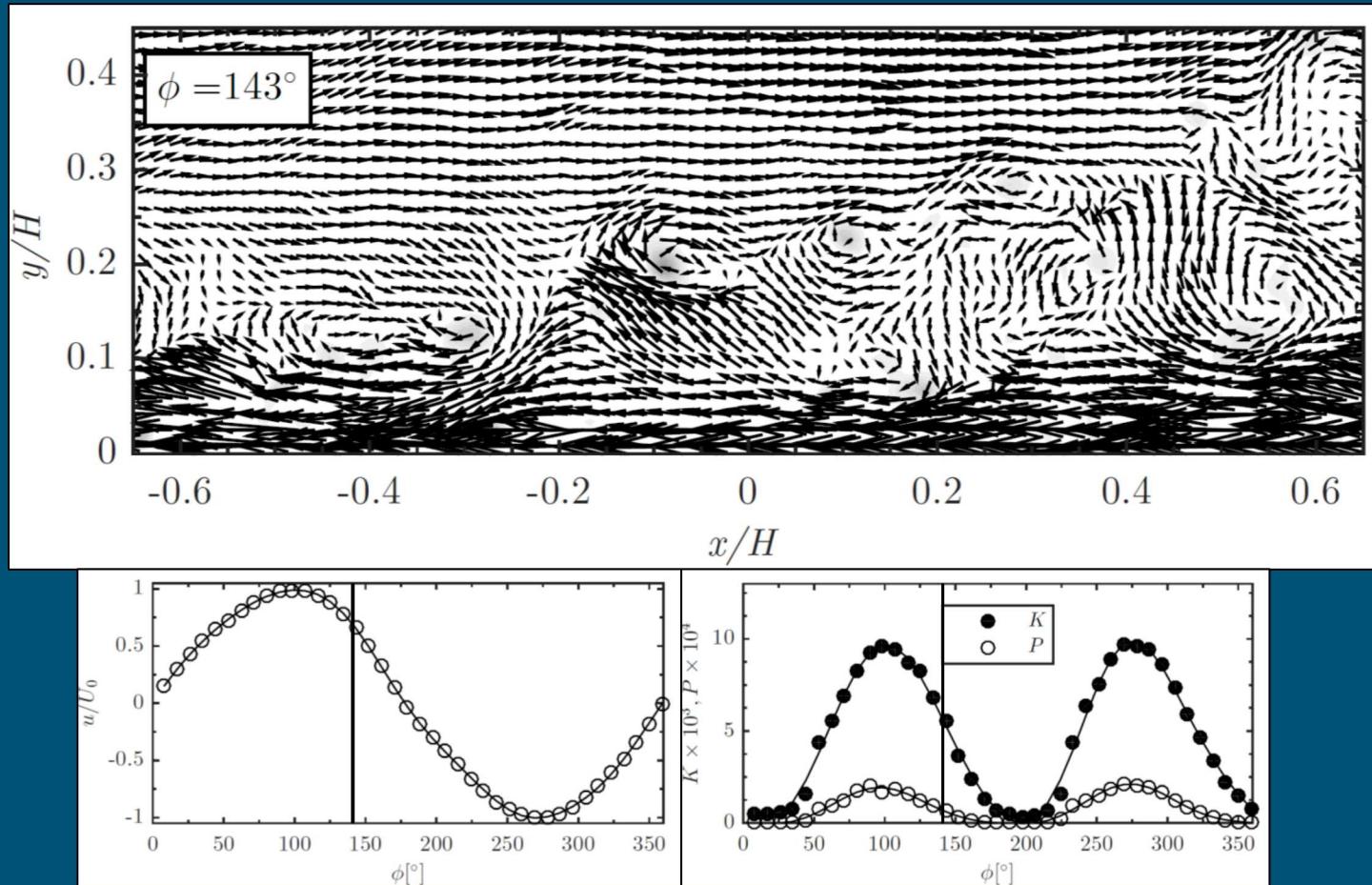
# They do exist for oscillating flow



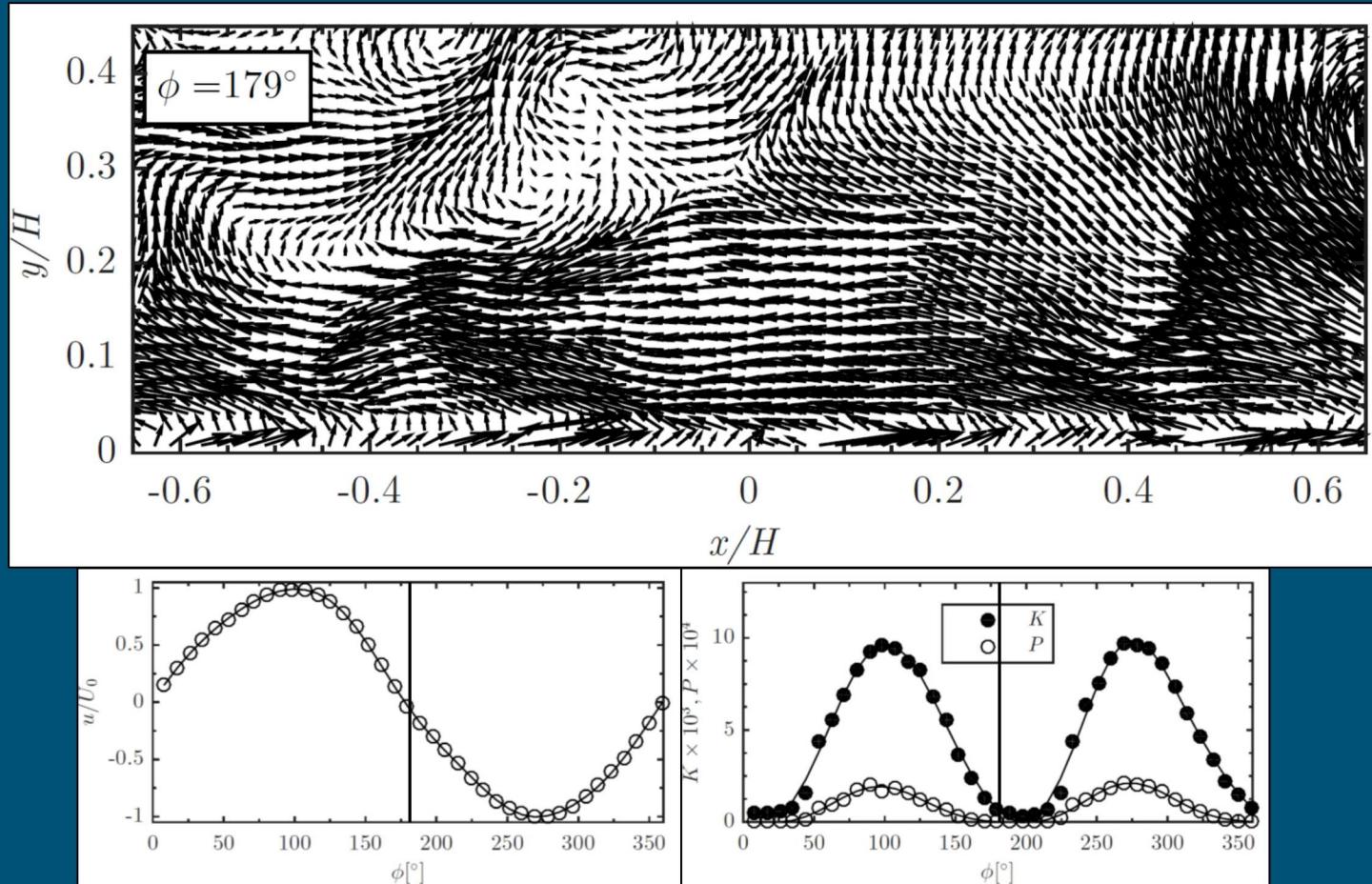
# They do exist for oscillating flow



# They do exist for oscillating flow



# They do exist for oscillating flow



# Christensen published a paper on conditional averaging to identify Hairpins



*J. Fluid Mech.* (2001), vol. 431, pp. 433–443. Printed in the United Kingdom  
 © 2001 Cambridge University Press

433

## Statistical evidence of hairpin vortex packets in wall turbulence

By K. T. CHRISTENSEN AND R. J. ADRIAN

Laboratory for Turbulence and Complex Flow, Department of Theoretical and Applied Mechanics, University of Illinois, Urbana, IL 61801, USA

(Received 14 October 2000 and in revised form 15 December 2000)

The structure of velocity in the outer region of turbulent channel flow ( $y^+ \gtrsim 100$ ) is examined statistically to determine the average flow field associated with spanwise vortical motions. Particle image velocimetry measurements of the streamwise and wall-normal velocity components are correlated with a vortex marker (swirling strength) in the streamwise–wall-normal plane, and linear stochastic estimation is used to estimate the conditional average of the two-dimensional velocity field associated with a swirling motion. The mean structure consists of a series of swirling motions located along a line inclined at  $12^\circ$ – $13^\circ$  from the wall. The pattern is consistent with the observations of outer-layer wall turbulence in which groups of hairpin vortices occur aligned in the streamwise direction. While the observational evidence for the aforementioned model was based upon both experimental and computational visualization of instantaneous structures, the present results show that, on average, the instantaneous structures occur with sufficient frequency, strength, and order to leave an imprint on the statistics of the flow as well. Results at  $Re_\tau = 547$  and 1734 are presented.

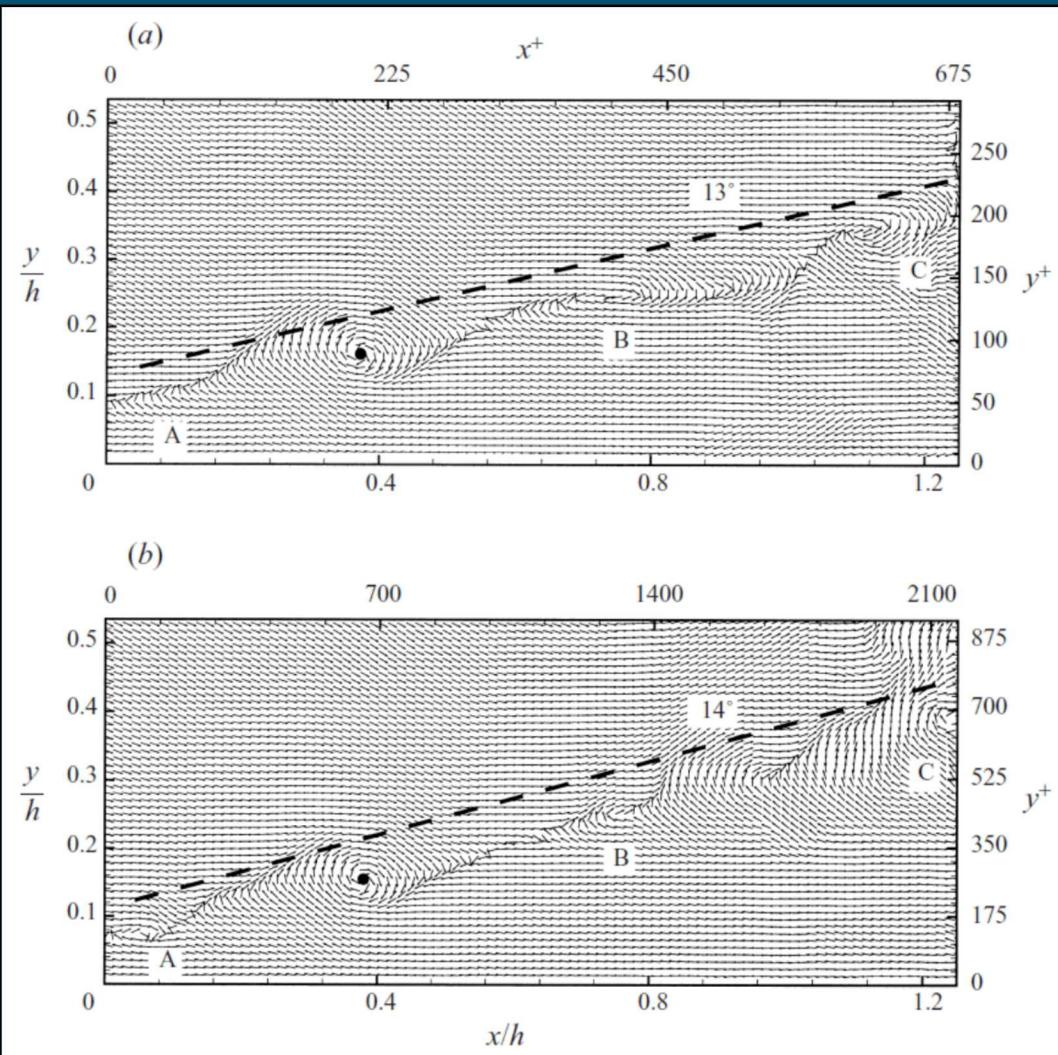


“Given the presence of a single spanwise vortex core (believed to be associated with the head of a hairpin vortex), what is the average fluctuating velocity field associated with this physical event? The best estimate of the average velocity field is the conditional average of the velocity field given the presence of a vortex core.”

### 1. Introduction

The structure of turbulent flow near a boundary has been studied extensively over the past decades (for a comprehensive review of this history, the reader should consult Robinson 1991 and, more recently, the collection edited by Panton 1997). Moreover, there is broad evidence that a vortical structure qualitatively similar to the ‘horseshoe

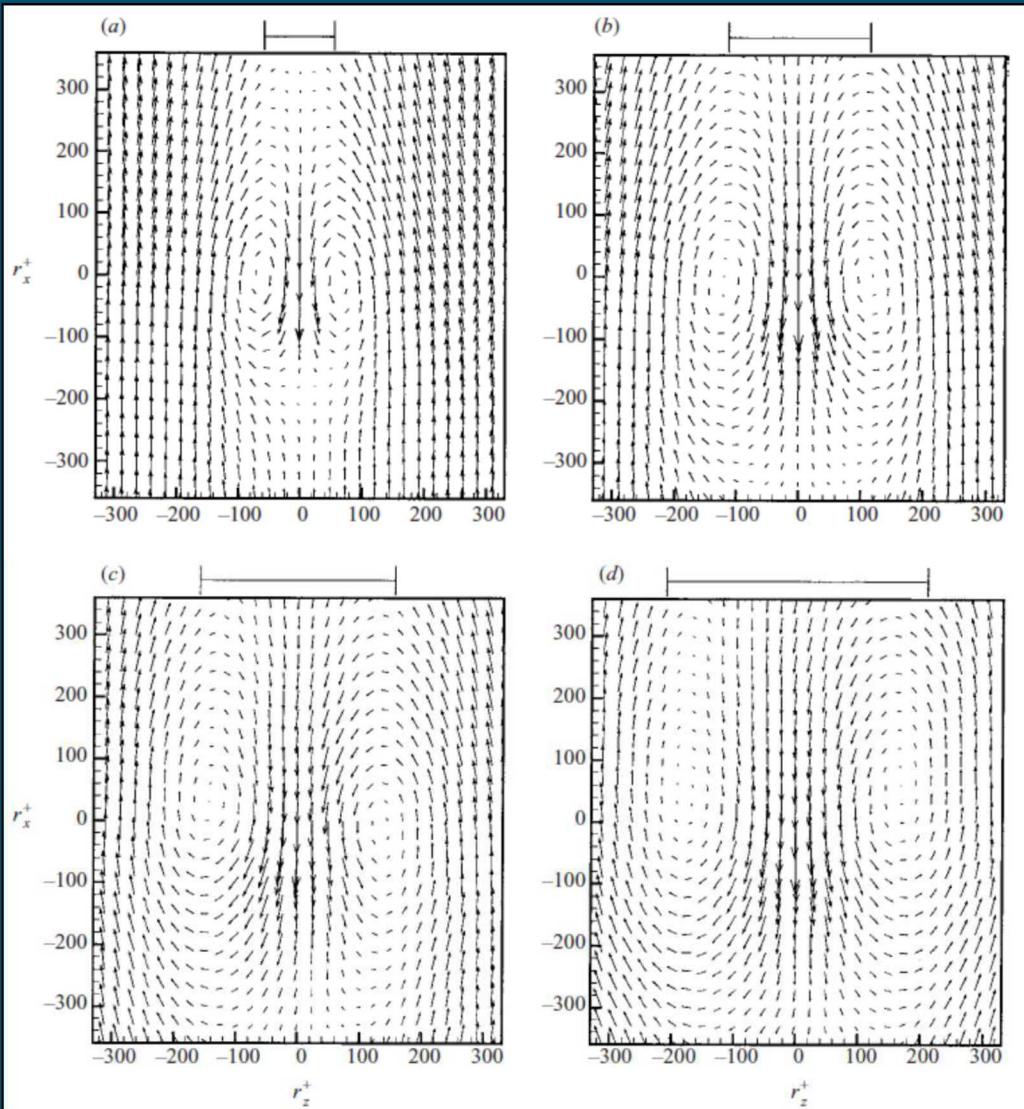
# Christensen published a paper on conditional averaging to identify Hairpins



Linear stochastic estimation. The location of the swirling strength event is indicated by a solid circle. (a)  $Re_\tau = 547$  ( $y^+_{ref} = 83.6$ ); (b)  $Re_\tau = 1734$  ( $y^+_{ref} = 256.0$ ). Vectors have been normalized to unity by their respective magnitudes to highlight swirling motions away from the event location.

Christensen, K. T. & Adrian, R. J. 2001 "Statistical evidence of hairpin vortex packets in wall turbulence." *J. Fluid Mech.* **431**, 433-443.

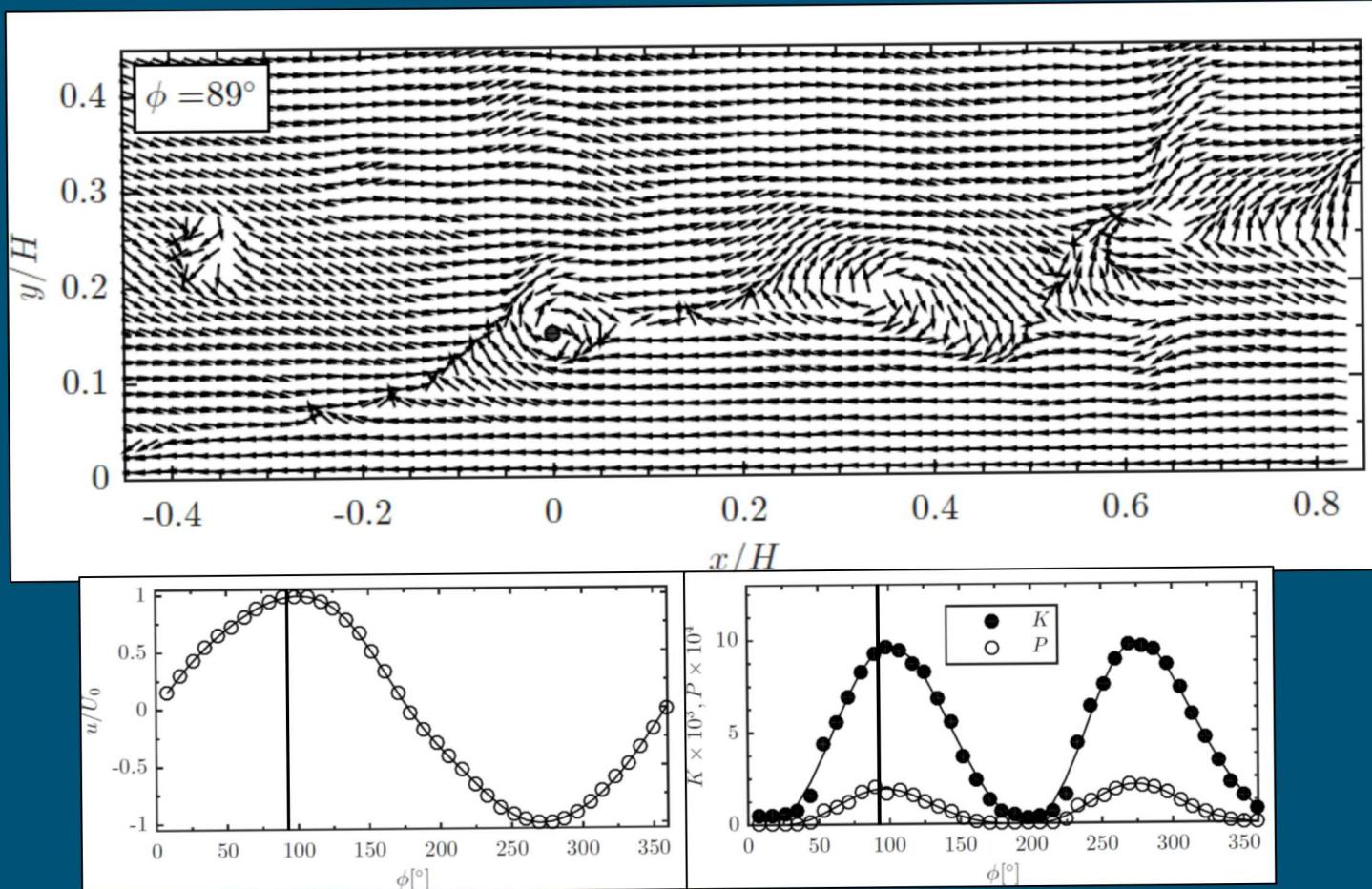
# Conditional velocity fields in the x-z plane show counter-rotating vortices with low momentum between them



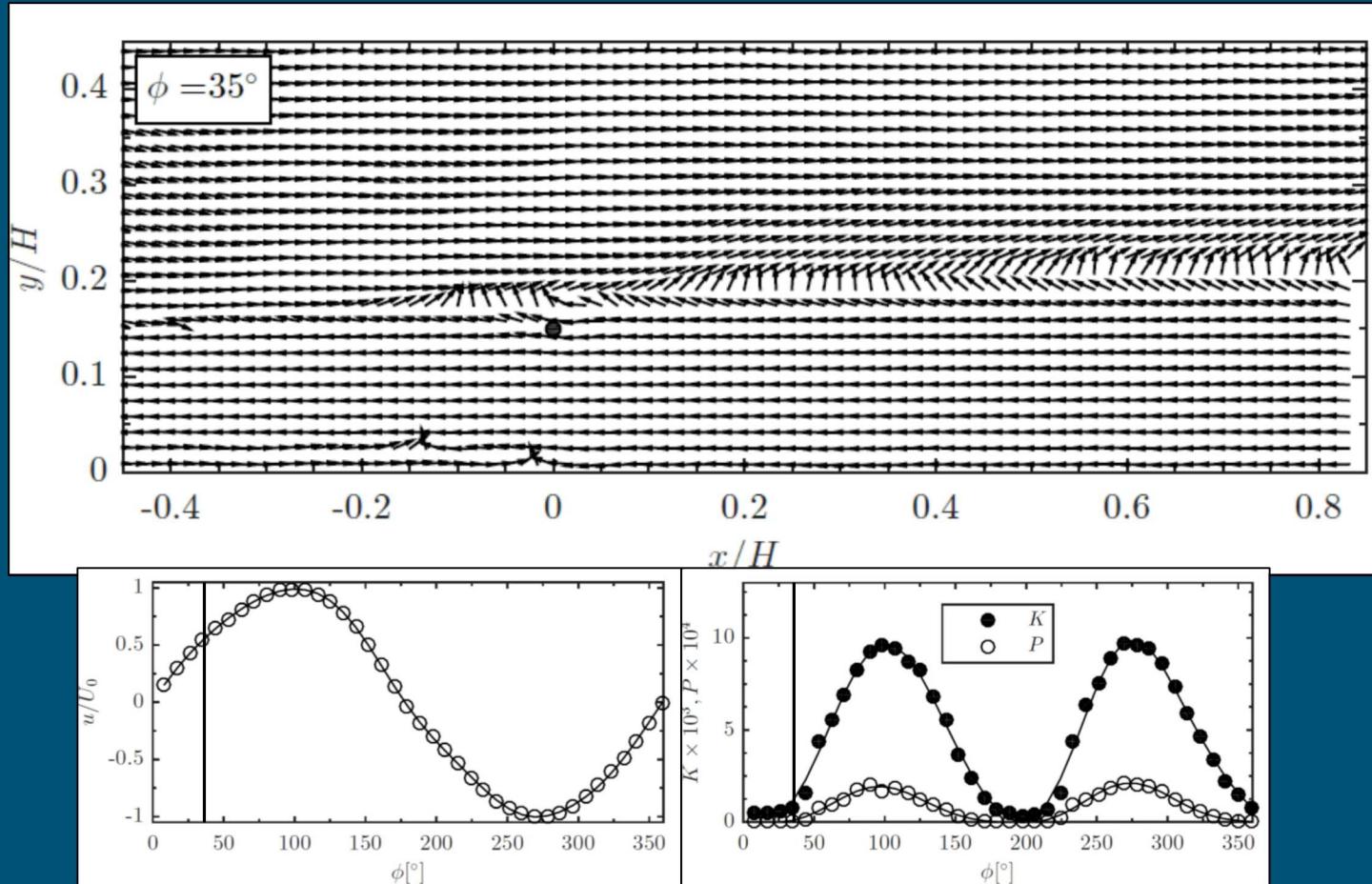
Conditionally averaged structure in the (x-z)-plane at  $Re_\theta = 7705$ . The specified event is a local  $u$ -minimum with  $u < 0.75U_\infty$ . (a)  $y^+ = 100$ ; (b)  $y^+ = 220$ ; (c)  $y^+ = 330$ ; (d)  $y^+ = 440$ .

C. D. Tomkins and R. J. Adrian, “Spanwise structure and scale growth in turbulent boundary layers,” *J. Fluid Mech.* **490**, 37 (2003).

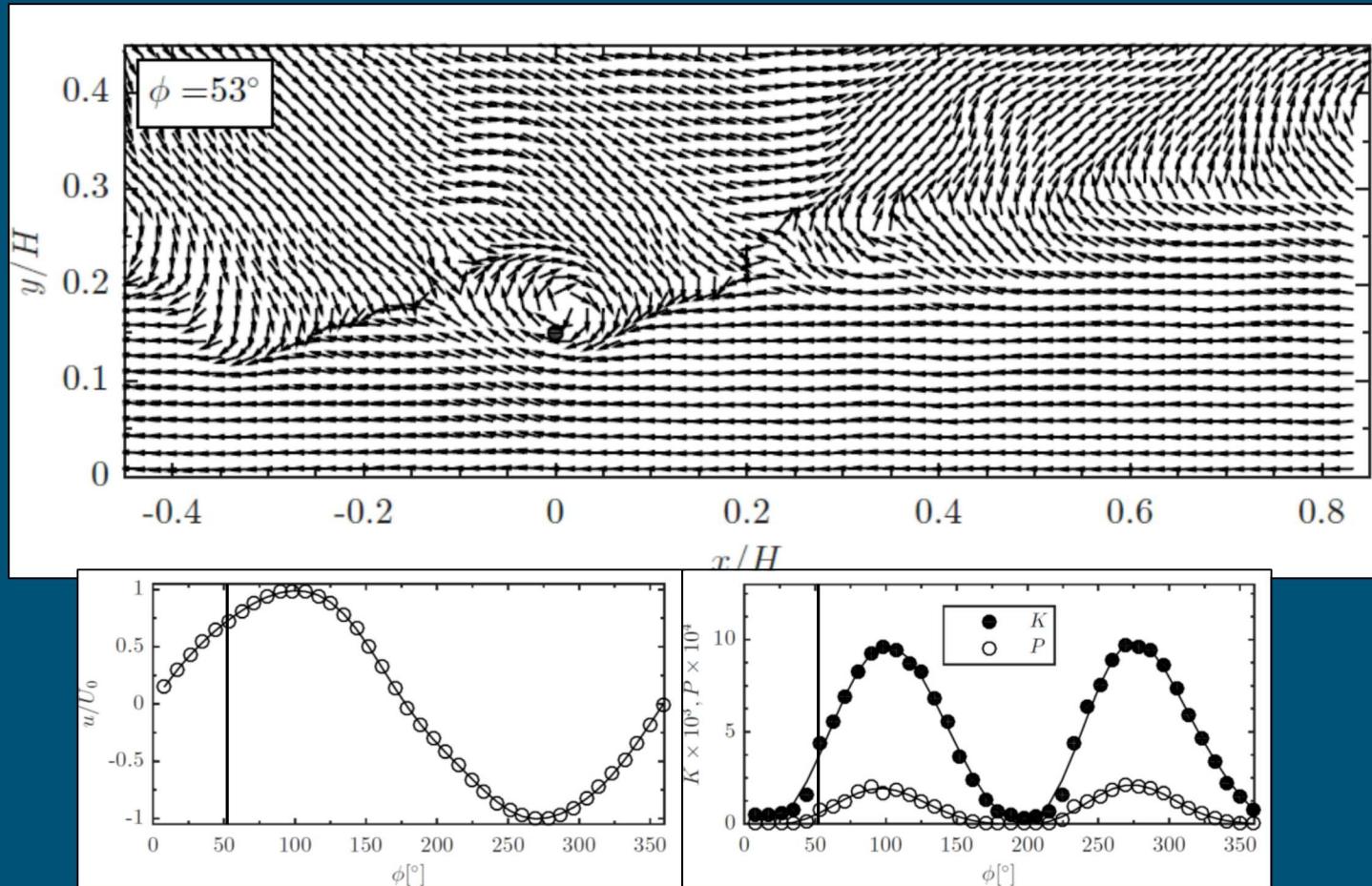
# We used Christensen and Adrian's method to find them in oscillating flow



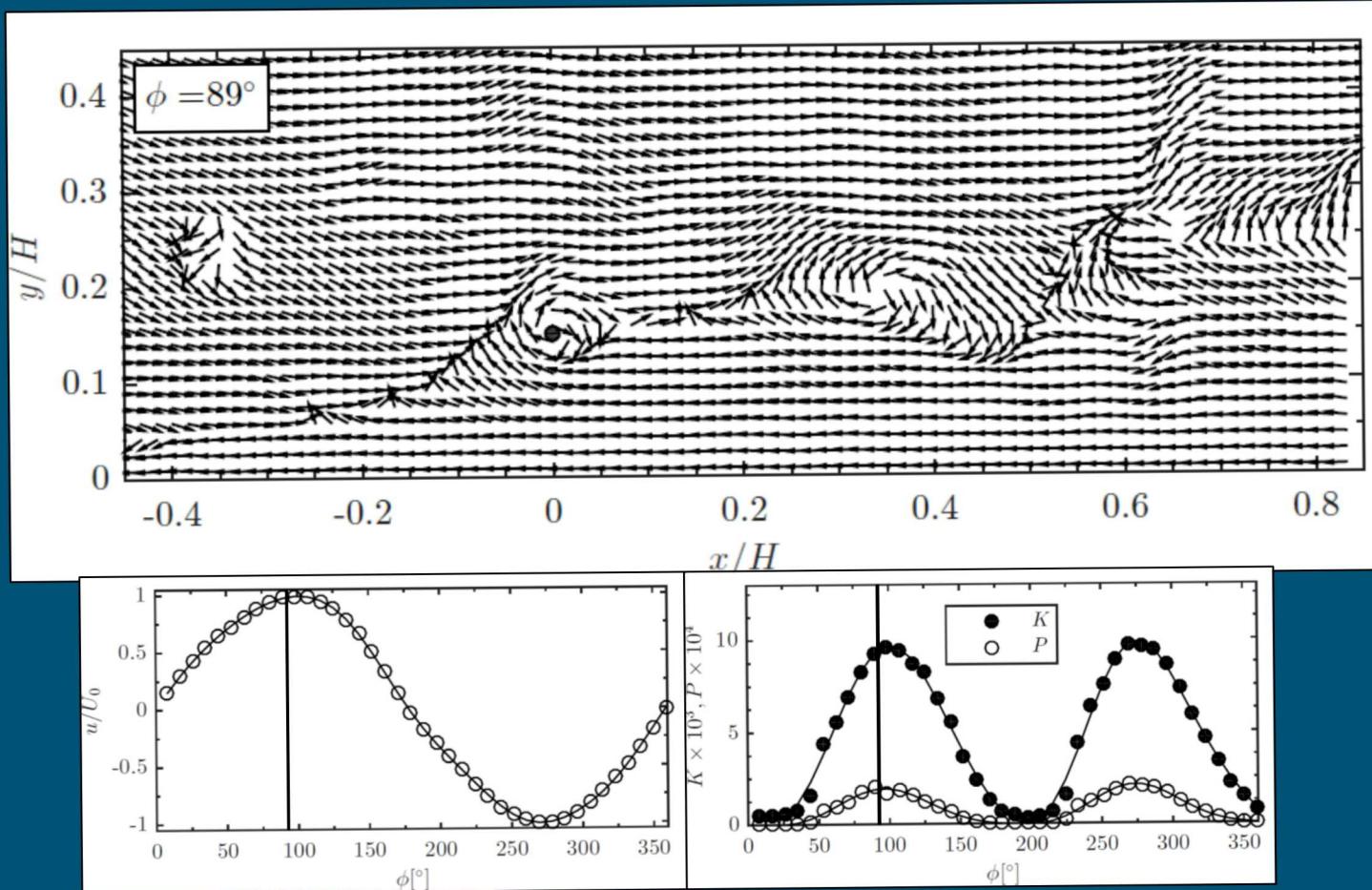
We used Christensen and Adrian's method to find them in oscillating flow



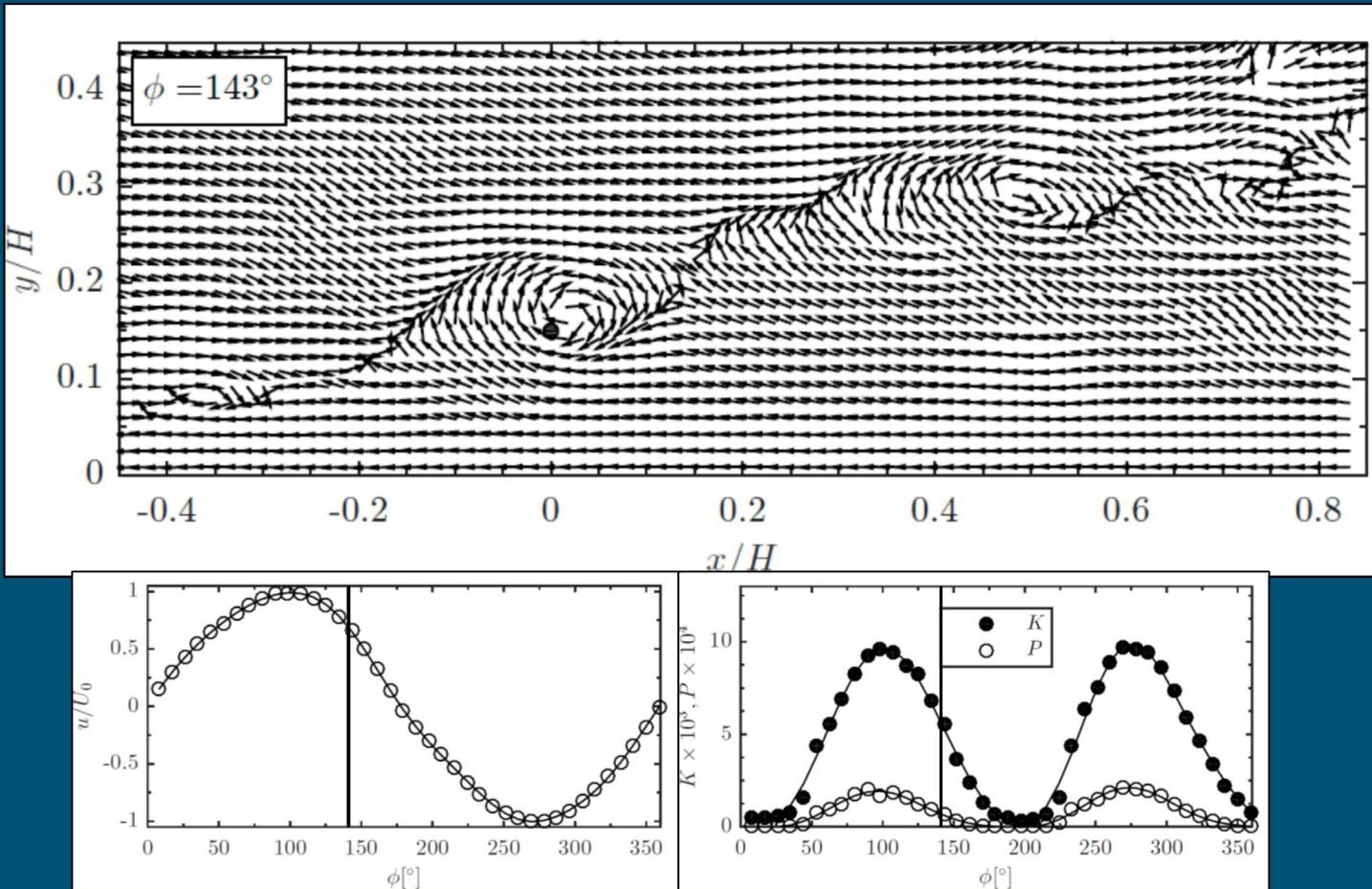
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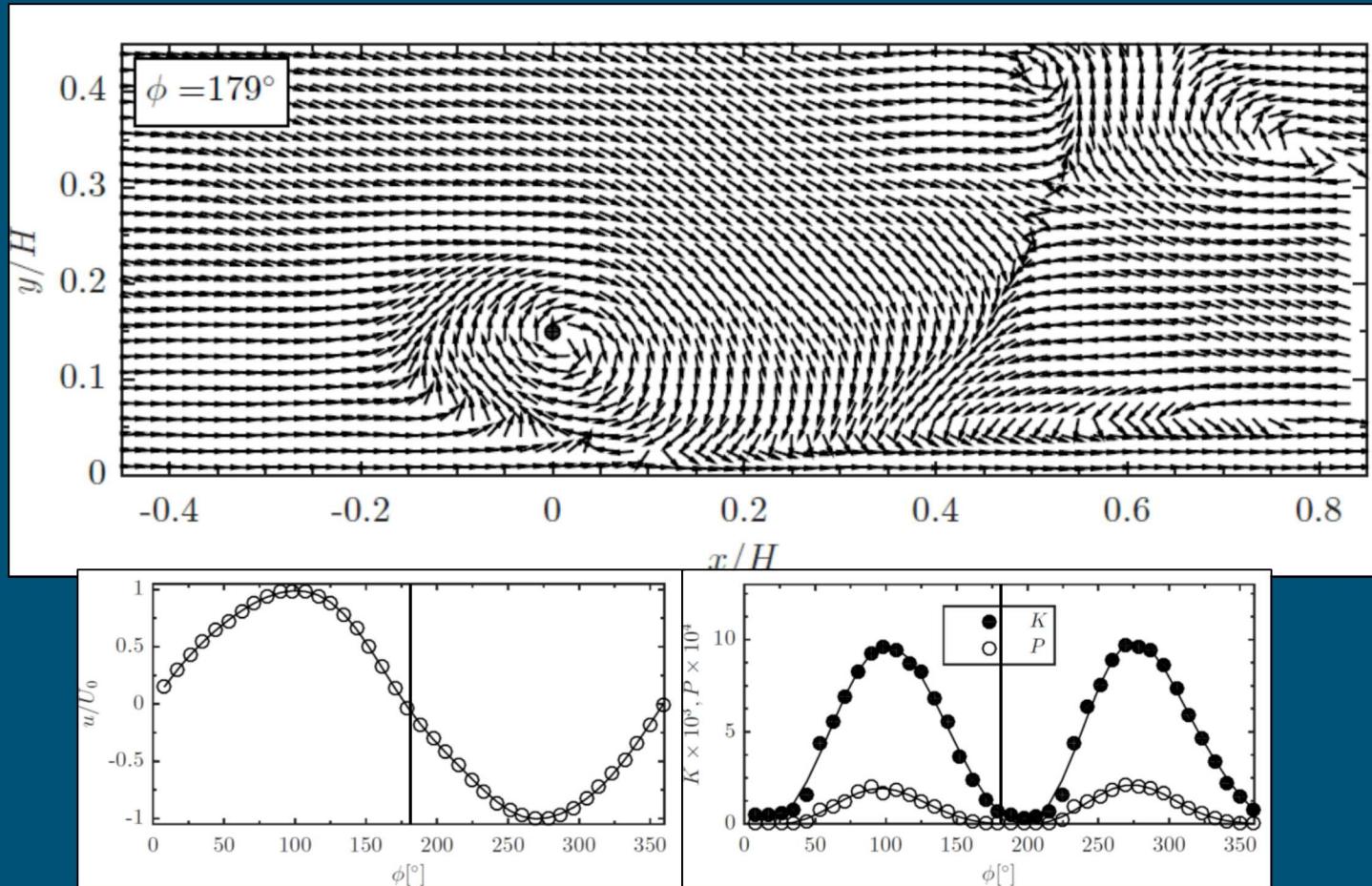
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# We used Christensen and Adrian's method to find them in oscillating flow

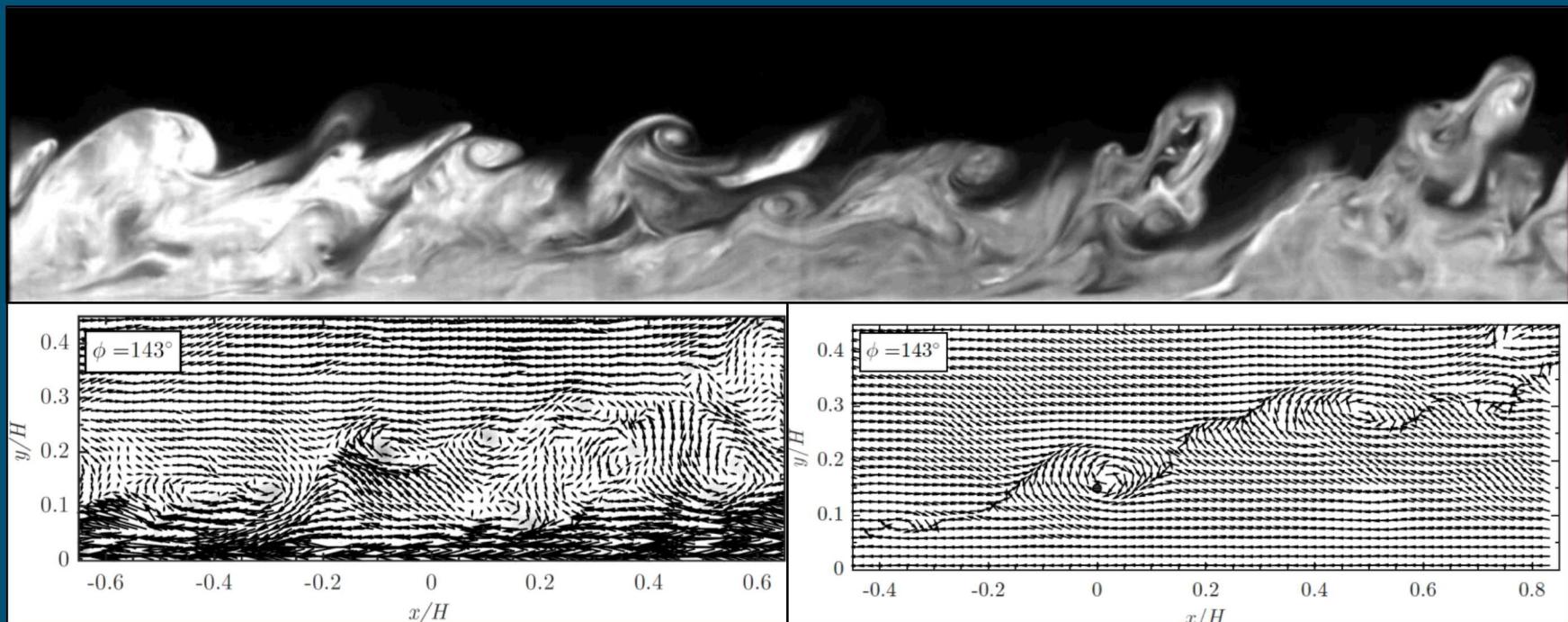


# We used Christensen and Adrian's method to find them in oscillating flow



# Hairpin Vortices are a fascinating feature of turbulent flow that can be identified with modern analysis

- They have been observed in steady boundary layer flow for several decades
- They have been identified with experiments as well as LES and DNS simulations
- We have identified them in oscillating flow and are writing a paper

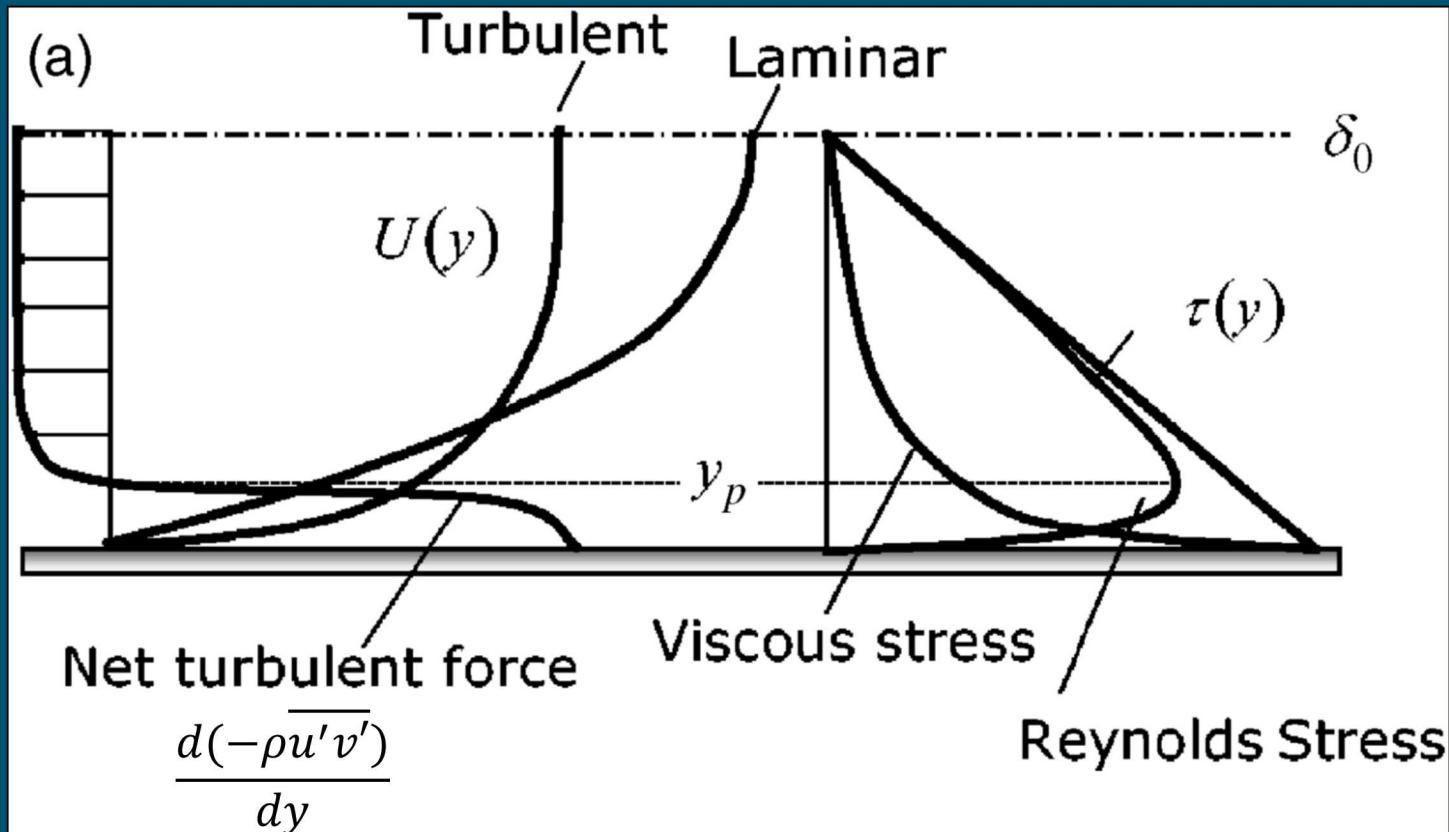


## Acknowledgements

- Jesse Roberts was the project PI
- Barton Smith setup the PIV equipment and configured the system
- Sean Kearney was the master behind the analysis
- Guilde Copeland built the flow system

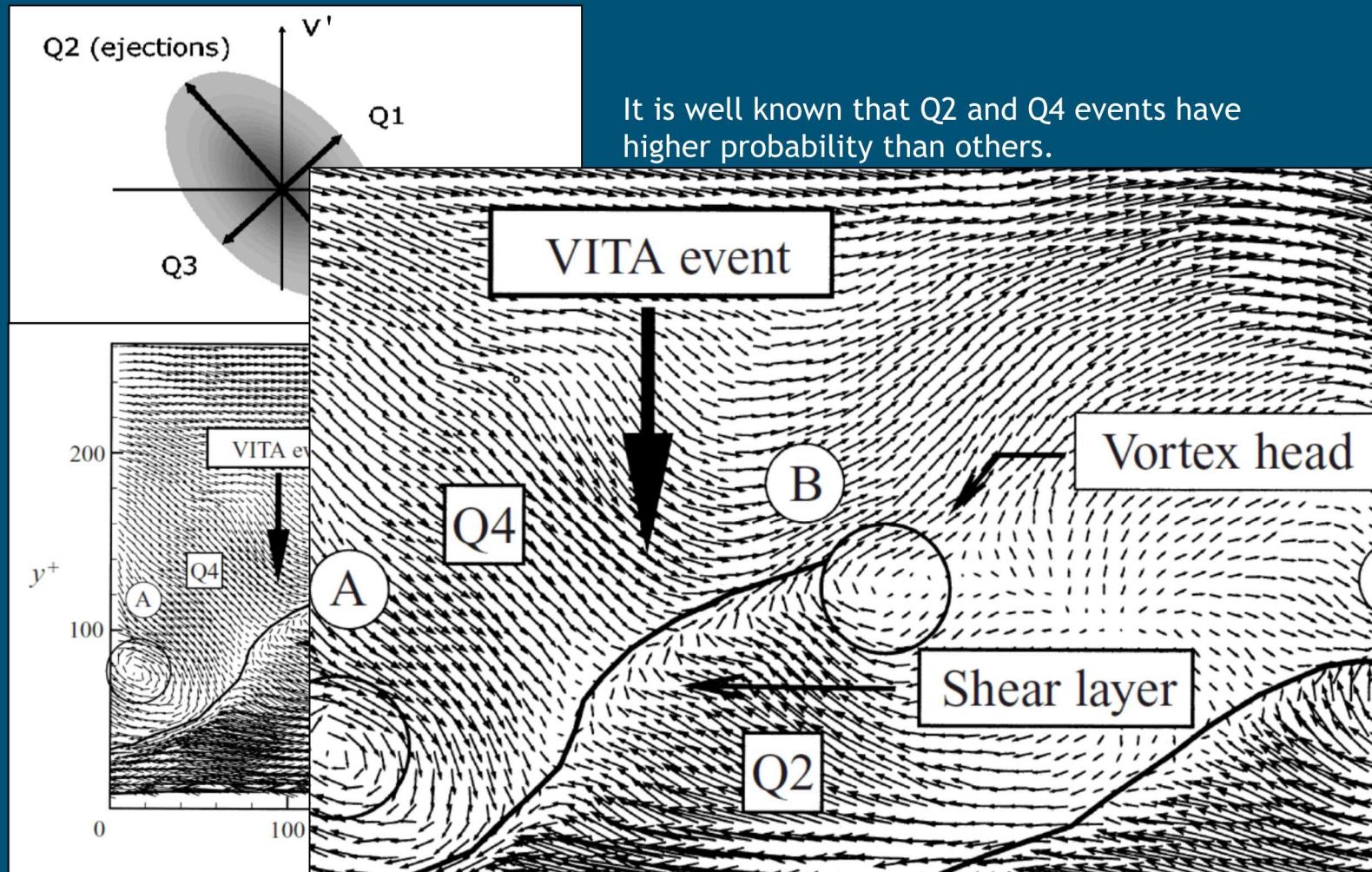
# Backup

Steady, incompressible, smooth-wall, external, turbulent flow with zero pressure gradient is simple but rich



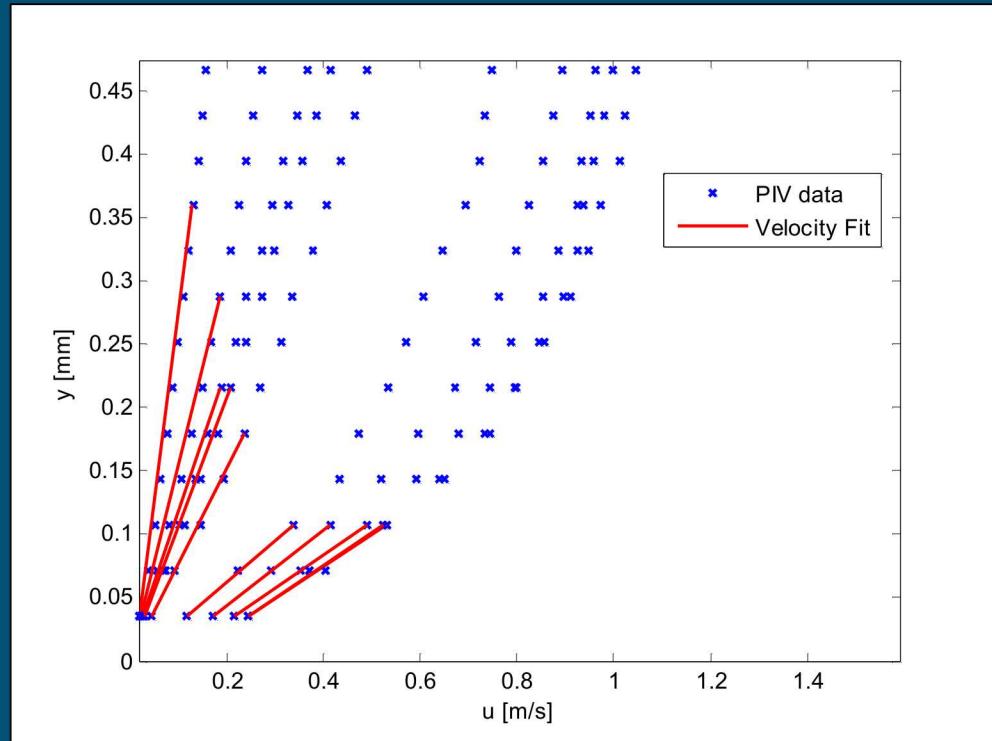
Adrian, R. J., 2007. "Hairpin vortex organization in wall turbulence". Physics of Fluids, 19, p. 041301.

# Before reviewing the work of others, we need to define turbulent events



## Shear Stress from PIV Data

- Streamwise velocity gradient within VSL is fit for each phase
- Only points within 7 viscous wall units ( $y^+ \leq 7$ ) are included
- A numeric solver converges on the number of points in the VSL.



$$\tau_s = \mu \partial u / \partial y \Big|_s$$

$$u_\tau = \sqrt{\frac{\tau_s}{\rho}} \quad y^+ = \frac{yu_\tau}{\nu}$$