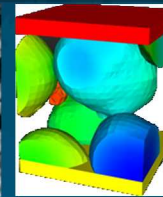
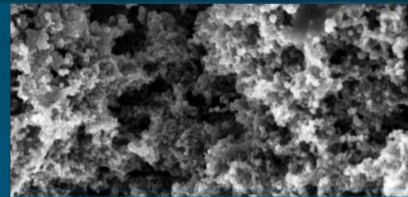
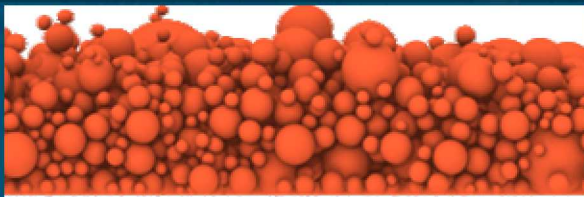
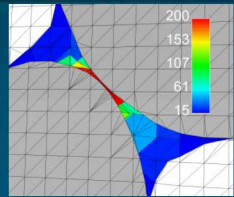
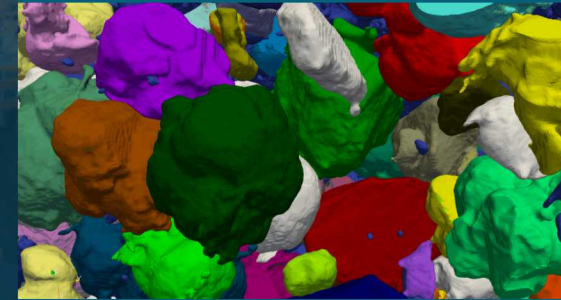


# Modeling Mesoscale Coupled Physics using Image Data: Batteries, Composites, and More



PRESENTED BY

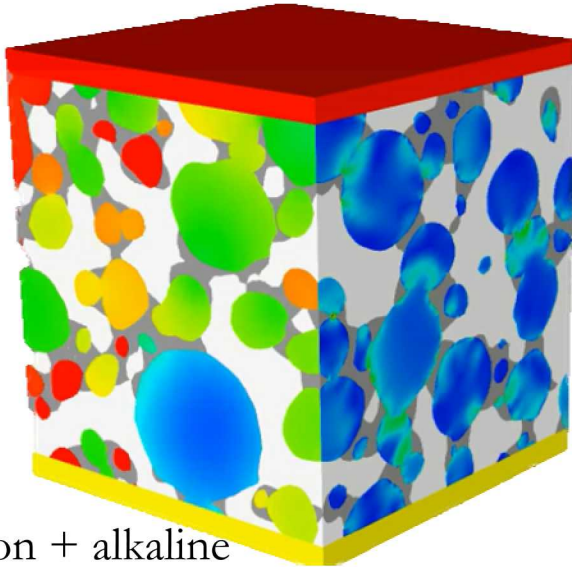
Scott A. Roberts, Ph.D.

October 2018

## 2 Roberts research efforts

Multi-physics, multi-scale applied modeling & simulation

- Lead teams comprised of 14 PhD staff members, 3 post-docs, 2 graduate students, and numerous summer interns
- \$3.4M in FY19 research funding



Li-ion + alkaline  
battery mesoscale

EM railgun launcher performance

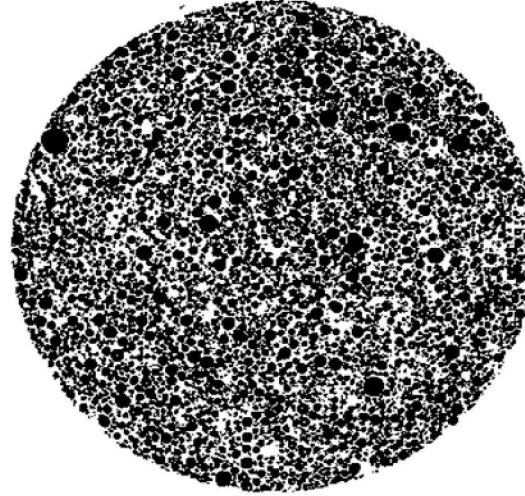
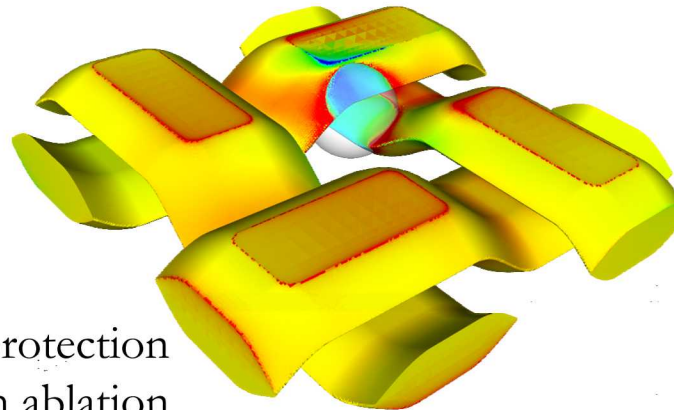
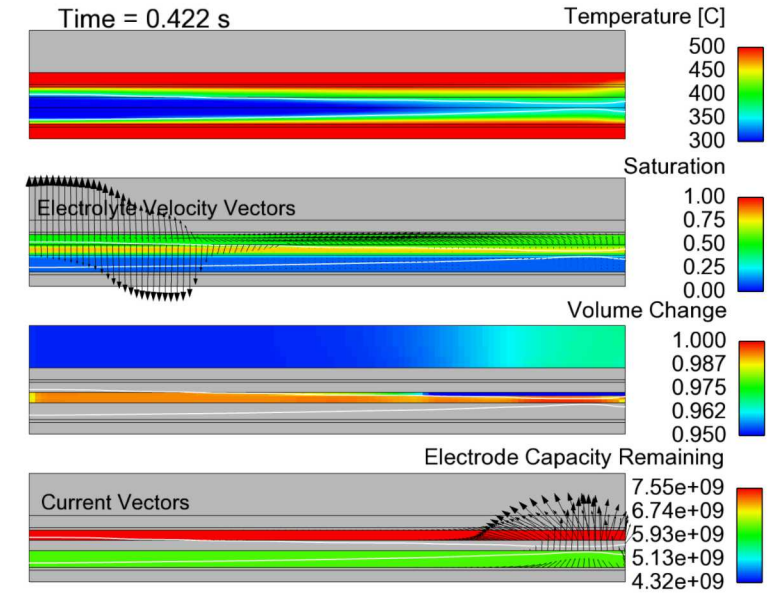


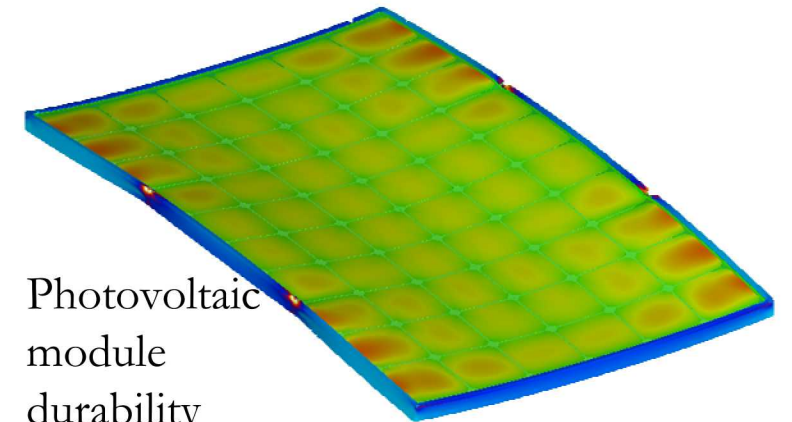
Image-to-mesh with ML/UQ



Thermal protection  
system ablation



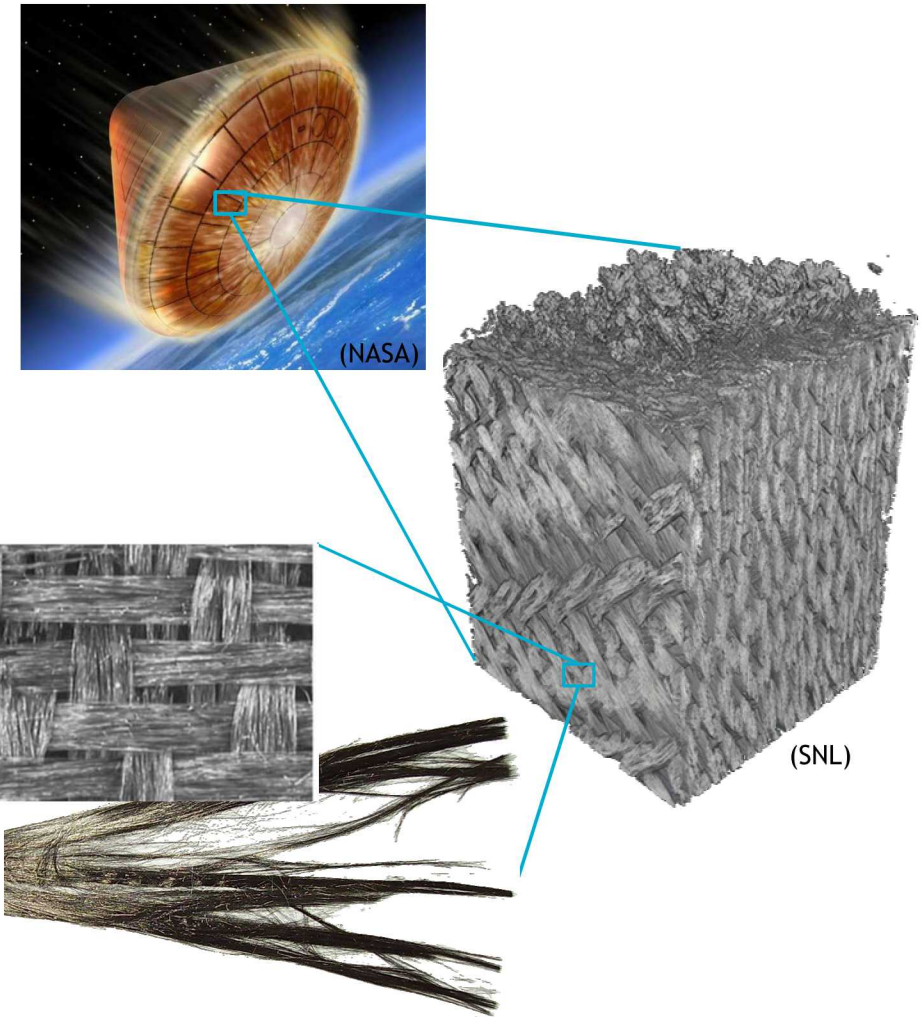
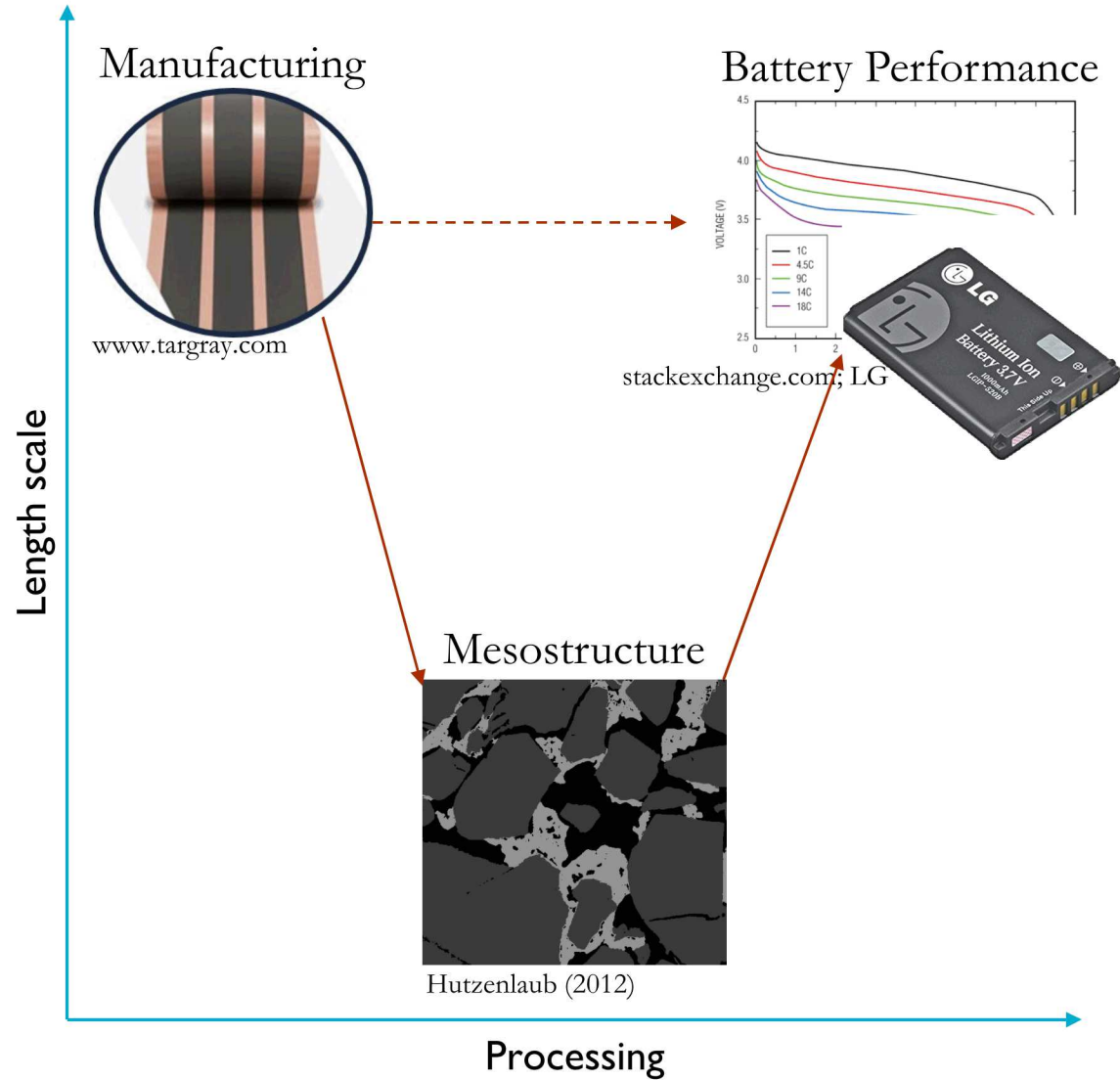
Thermal batteries



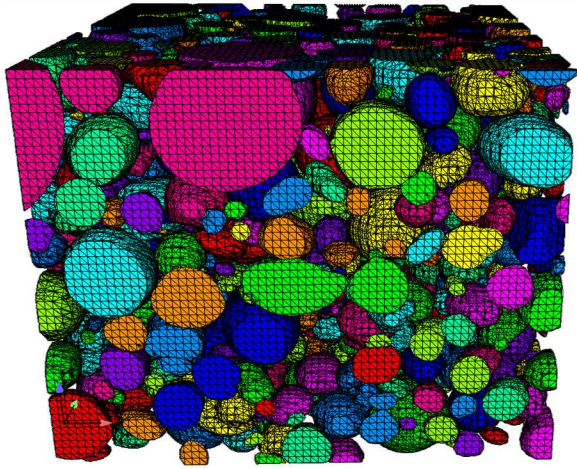
Photovoltaic  
module  
durability



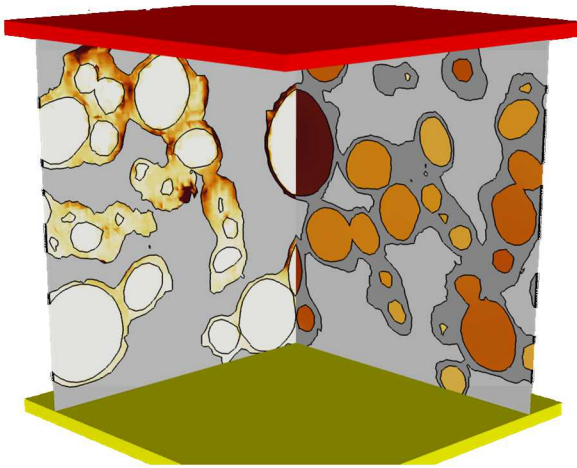
# Motivation



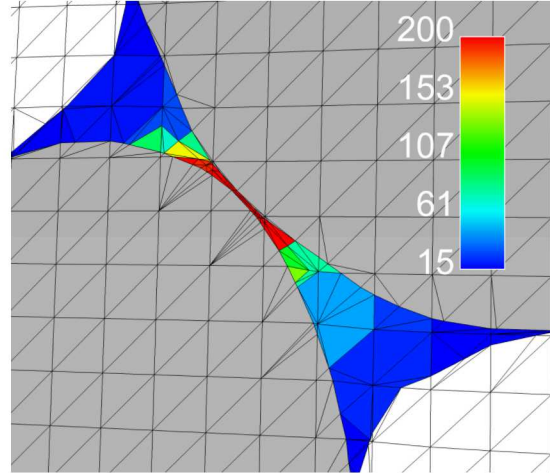
Coupled multi-physics effects at the mesoscale connect component manufacturing to performance



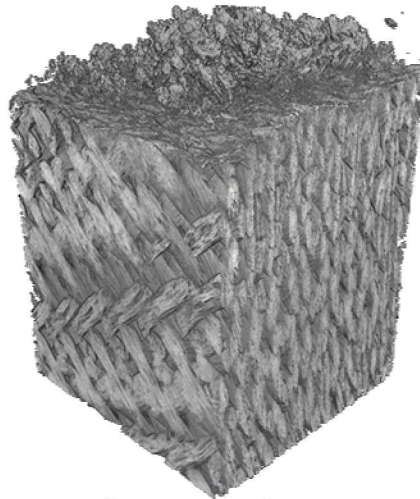
Computational representation of  
electrode mesostructures



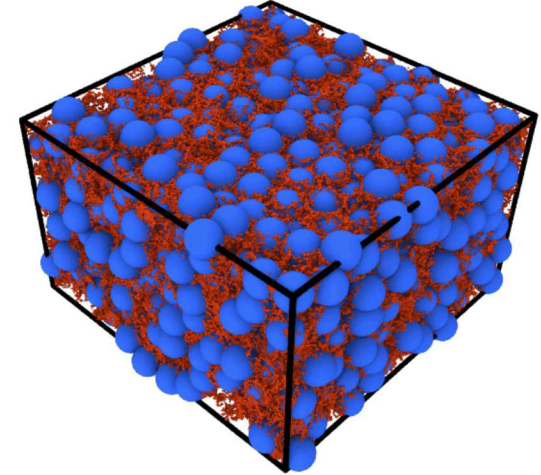
Electrochemical-mechanical  
discharge simulations



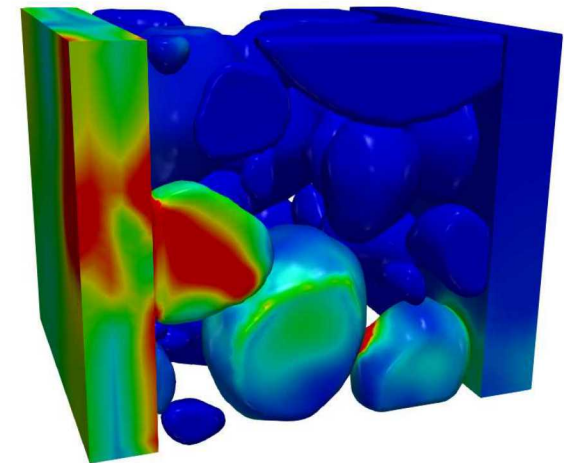
Representation and role of  
conductive binder morphology



Thermal protection systems



Discrete element method  
mesostructure generation

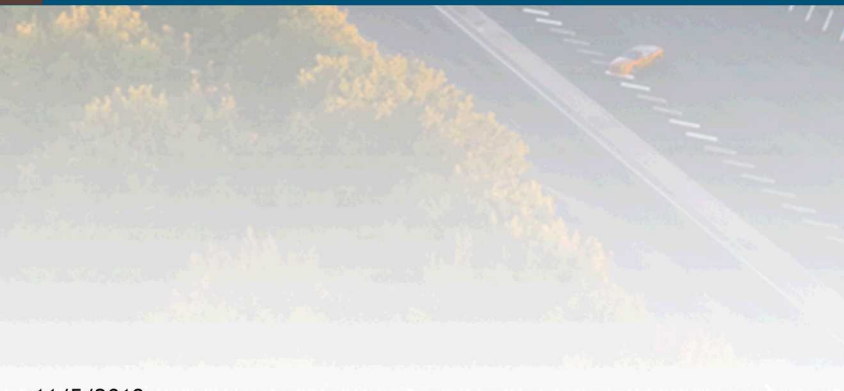


Future directions in  
credible image-based simulation

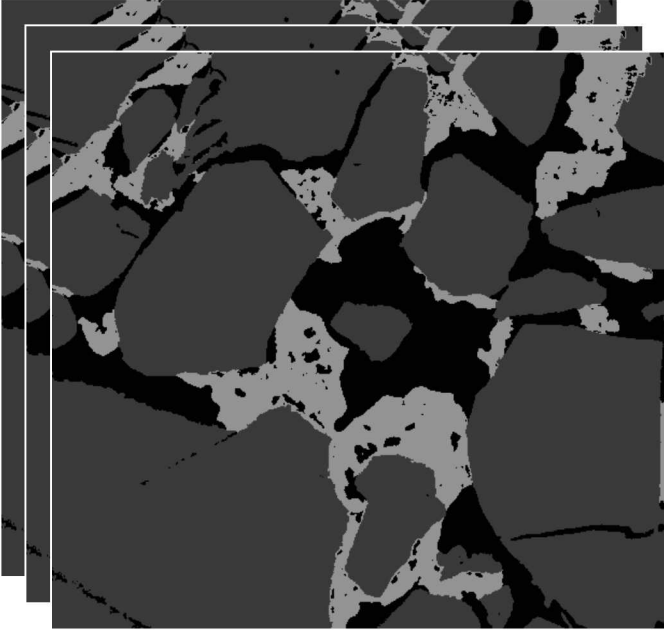




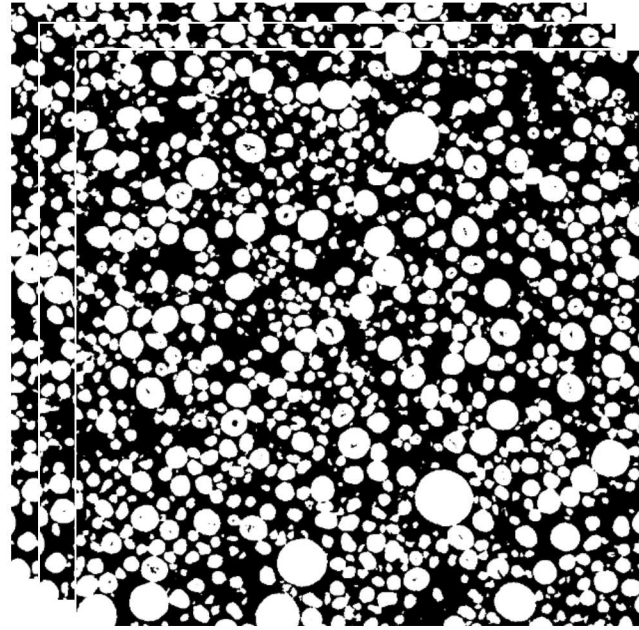
# Computational representation of electrode mesostructures



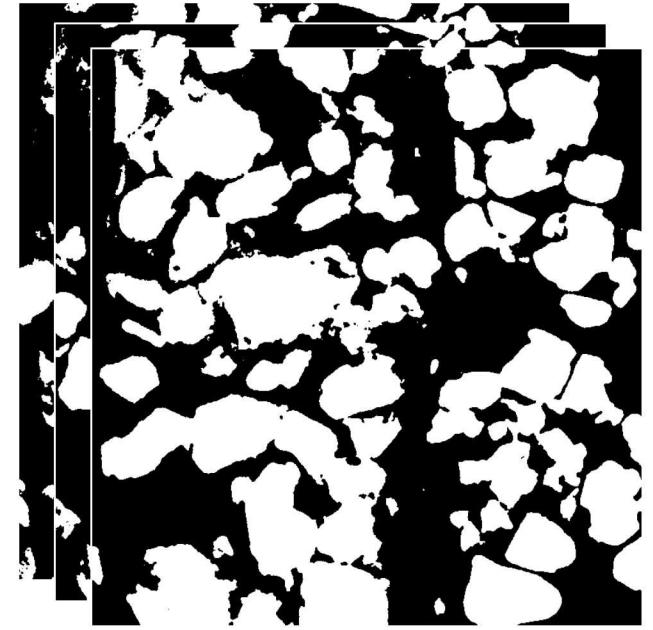
## Imaging of cathode mesostructures



LCO with binder from FIB/SEM,  
35 nm resolution,  
20  $\mu\text{m}$  domain.  
Hutzenlaub (2012)



NMC from XRCT,  
370 nm resolution,  
757  $\mu\text{m}$  domain.  
Ebner (2013)

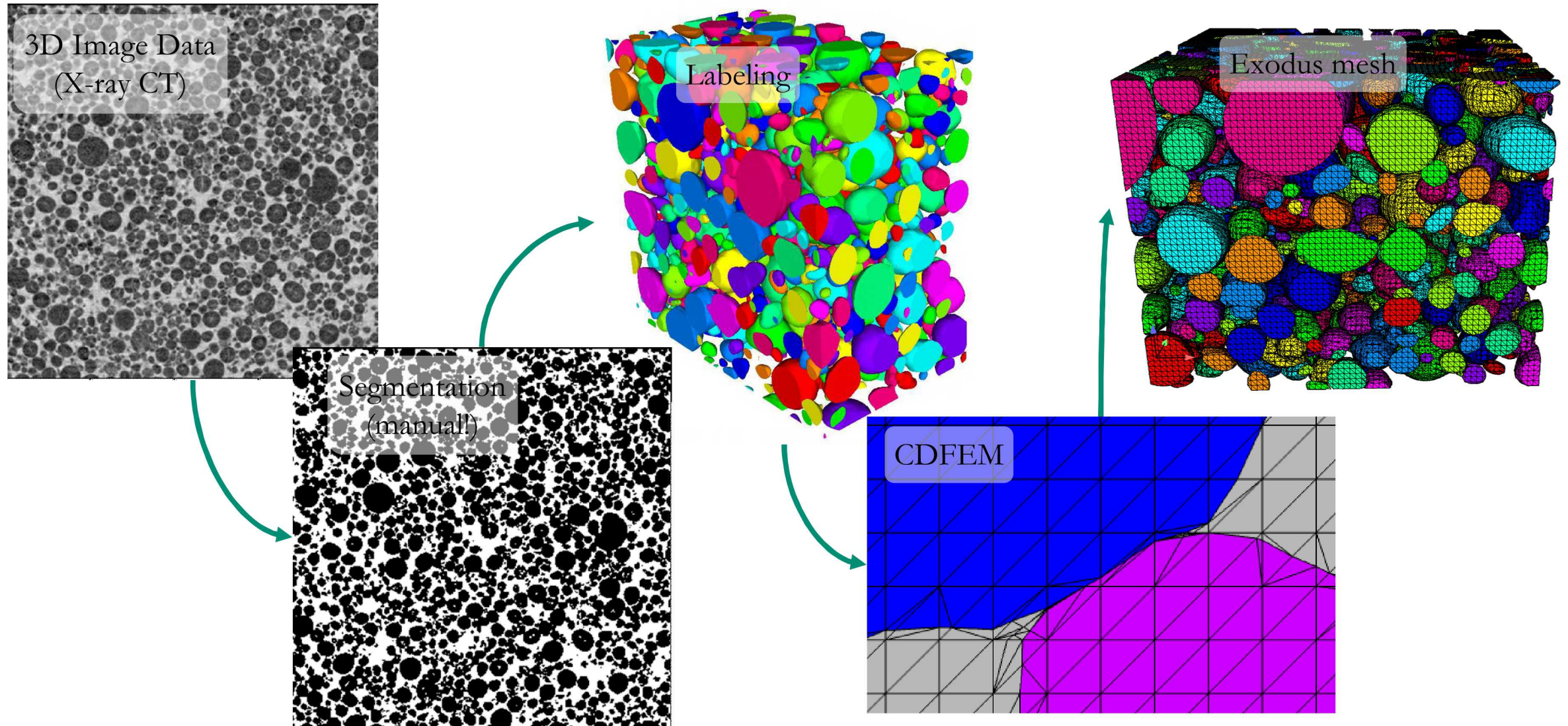


LCO from XRCT,  
64 nm resolution,  
22  $\mu\text{m}$  domain.  
Yan (2012)

Imaging reveals complex networks; binder can be difficult to detect at scale

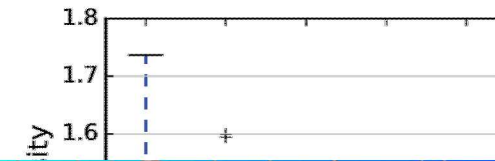
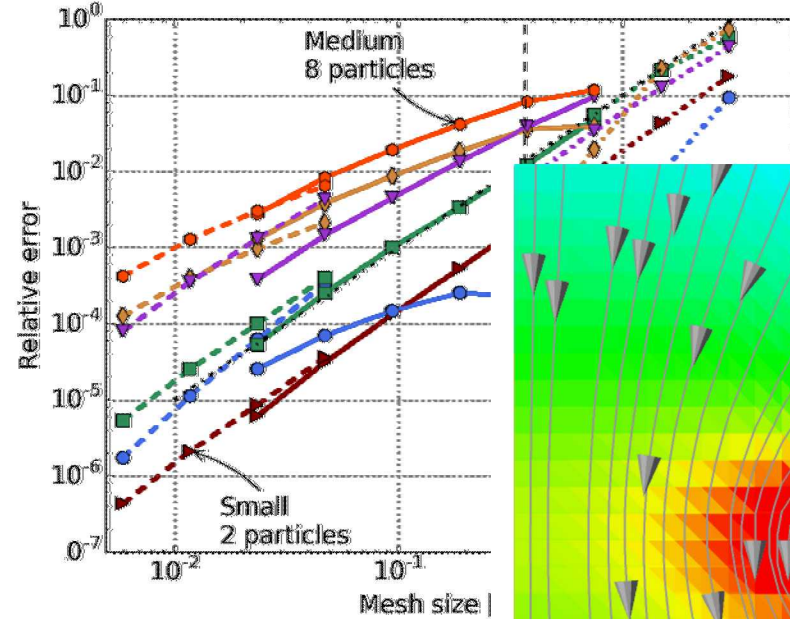
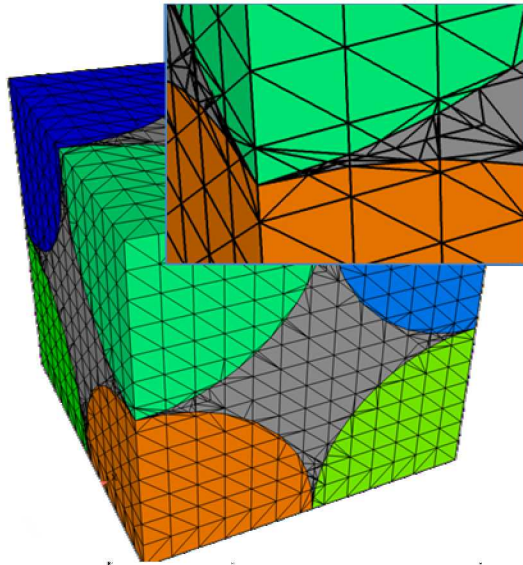


## 7 Mesoscale geometry from CT data using CDFEM

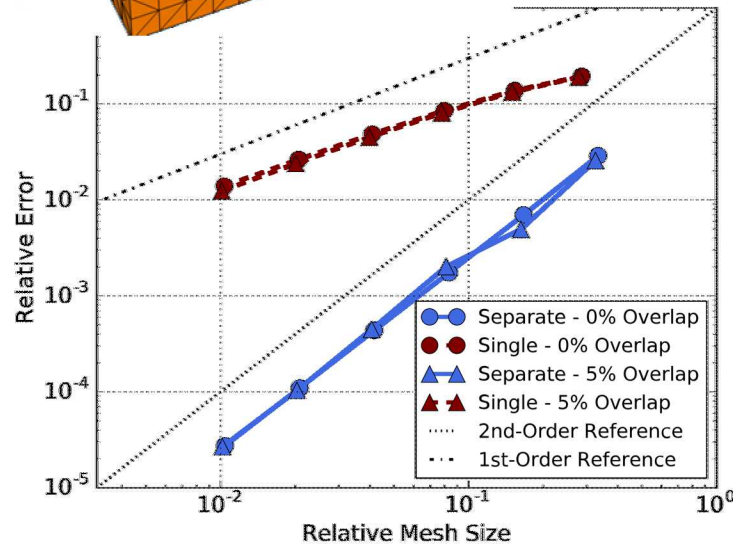


Detailed 3D reconstruction and image processing necessary to get usable mesostructure data



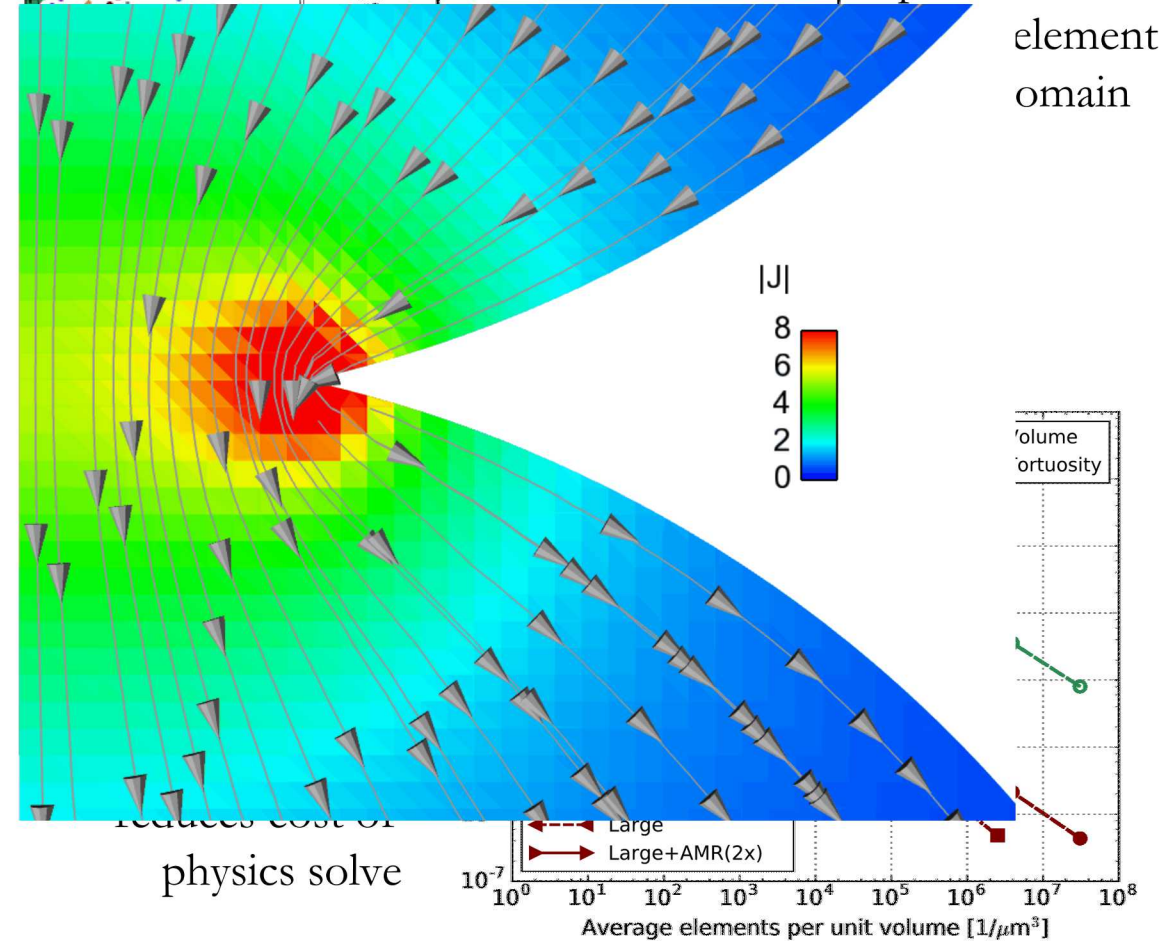


Quantify  
representative  
element  
domain



Understand mesh res  
for accurate pred

Separate particle  
representations  
required for  
optimal  
convergence



physics solve

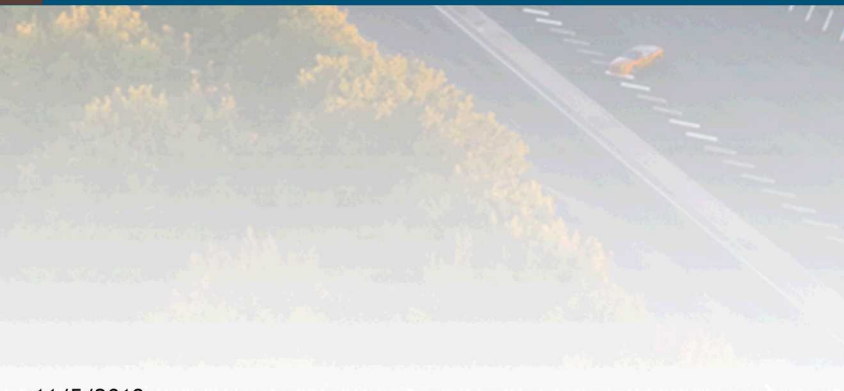
Large  
Large+AMR(2x)

Solution verification establishes simulation correctness and domain/mesh size requirements





# Representation and role of conductive binder morphology



# What about the conductive binder?

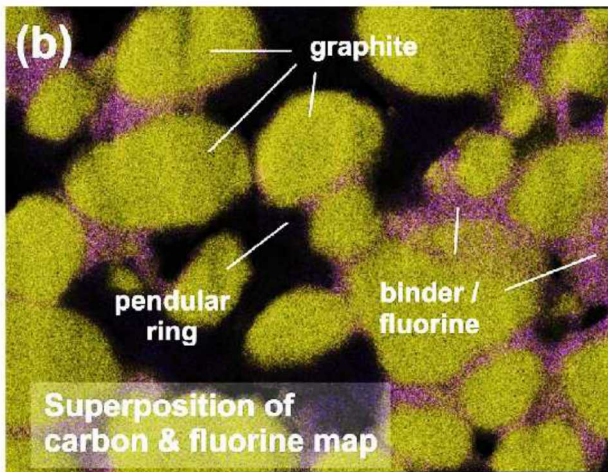
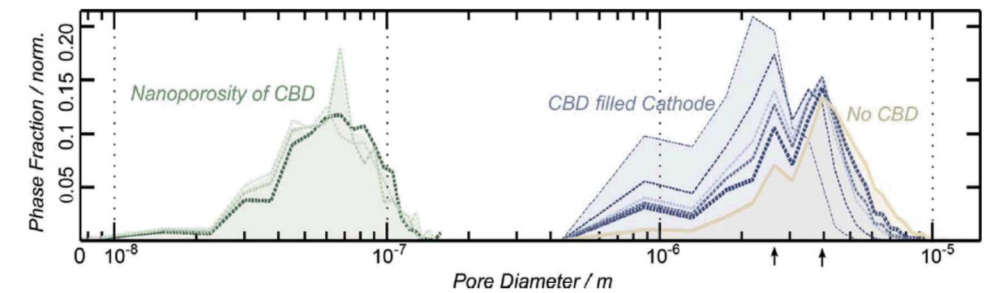
Resolving conductive binder in 3D imaging difficult

- Binder often neglected, assuming non-active void space is electrolyte
- Limited imaging results can hint at binder location

Amorphous binder is significantly nanoporous

- 47% Zielke (2015); 45% Grillet (2016)
- 5% ionic conductivity of pure electrolyte

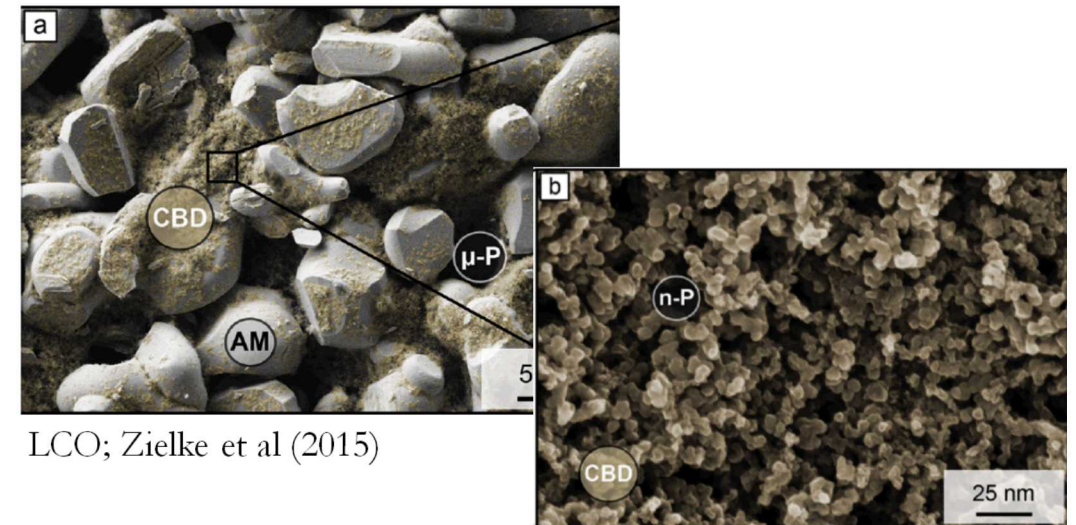
Binder weight fraction	Dense volume binder:particle	Porous volume binder:particle
0.04	0.10	0.15
0.06	0.16	0.23
0.08	0.22	0.31
0.10	0.28	0.40



Graphite; Jaiser et al. (2017)



LCO; Komini Babu et al (2015)

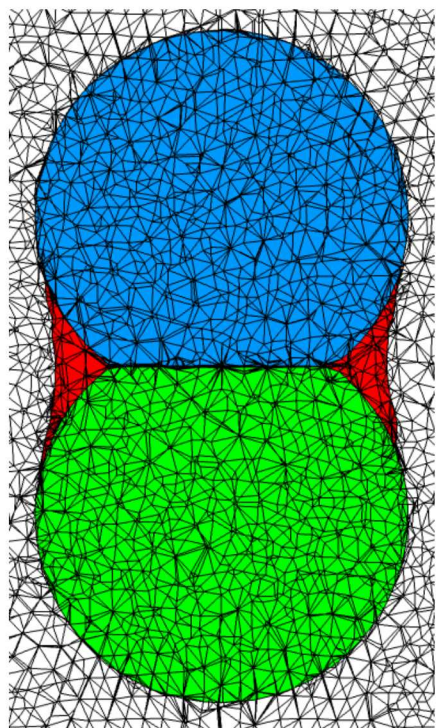


LCO; Zielke et al (2015)

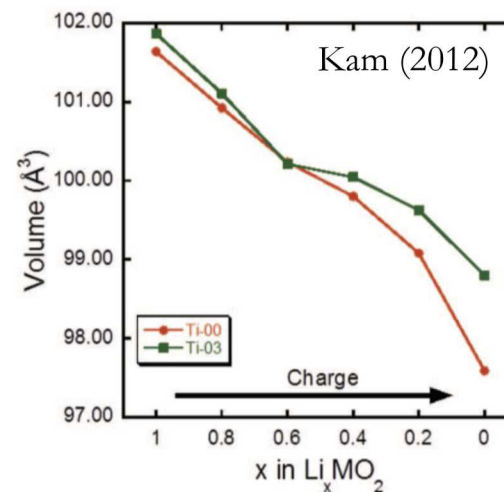
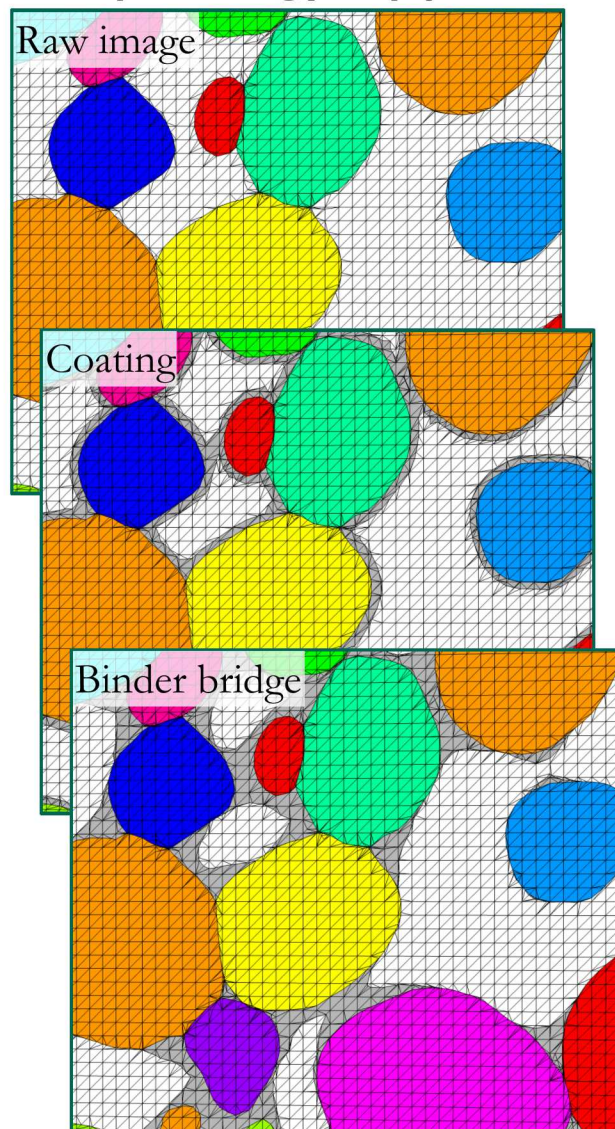
How are electrode-scale properties affected by the inclusion of binder? How does the morphology matter?



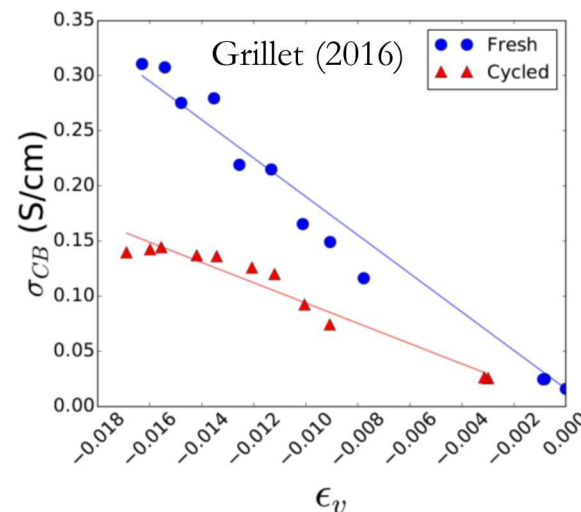
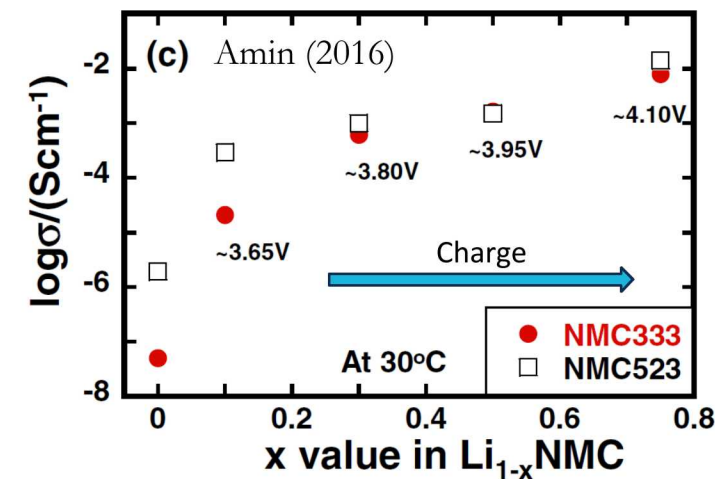
# Binder bridge morphology approach



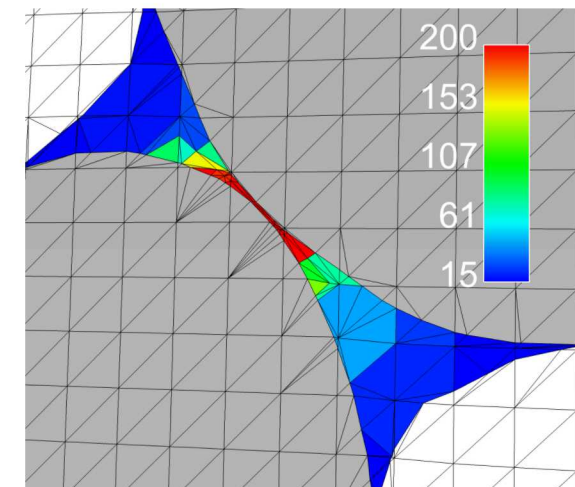
Mathematical description of "binder bridges"



NMC swells on lithiation, compressing binder



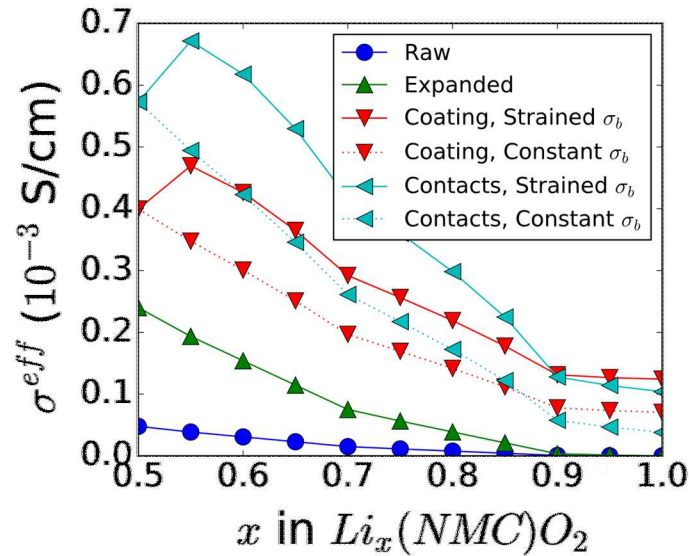
Binder has strain- (e.g. lithiation-) dependent properties



Binder bridge mimics experimental observations; properties are lithiation-dependent

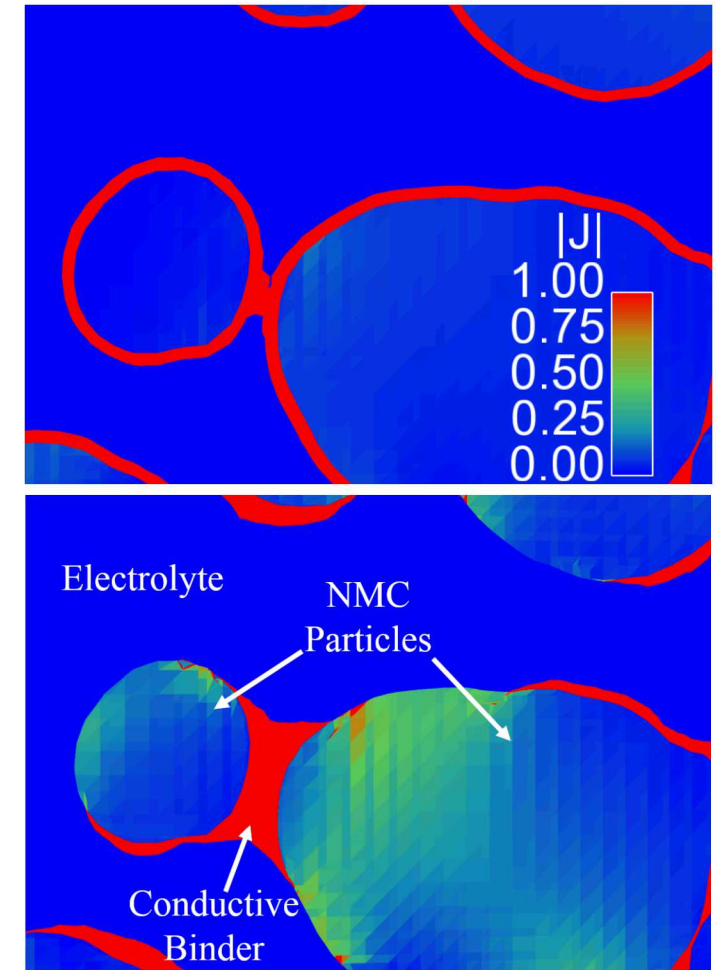
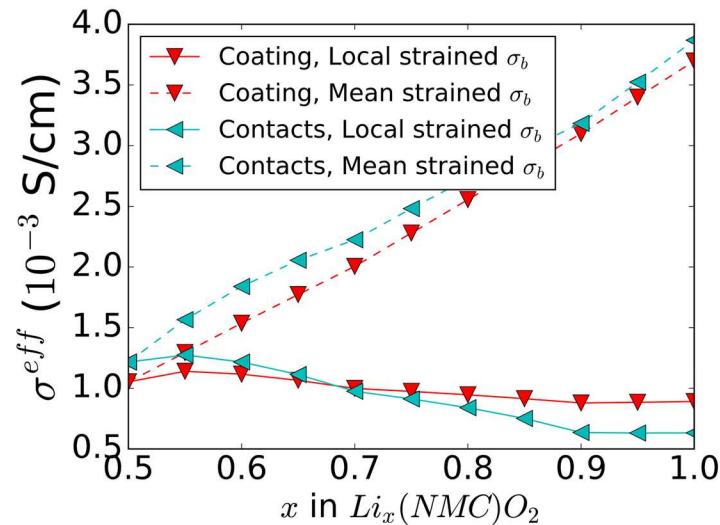
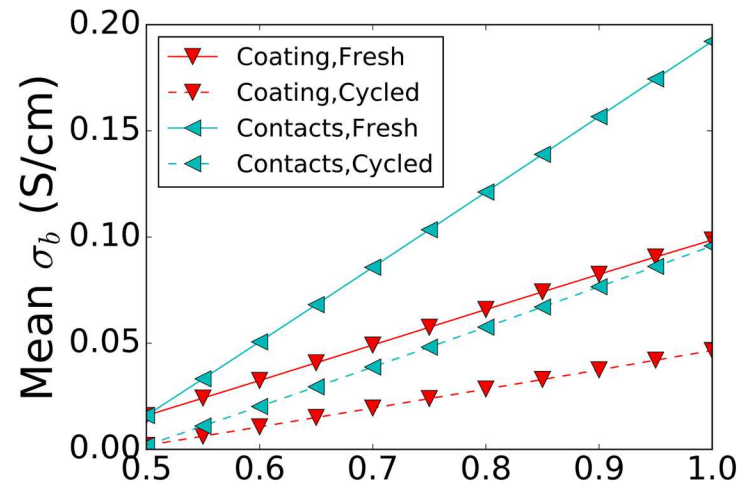


# Effect of including binder on effective properties



Presence of binder increases electrical conductivity. Mechanics further increase conductivity.

Binder morphology and current localization matters. Binder bridge forces current flow through particles.



Binder morphology and mechanical coupling have a significant impact on effective properties; localization matters!



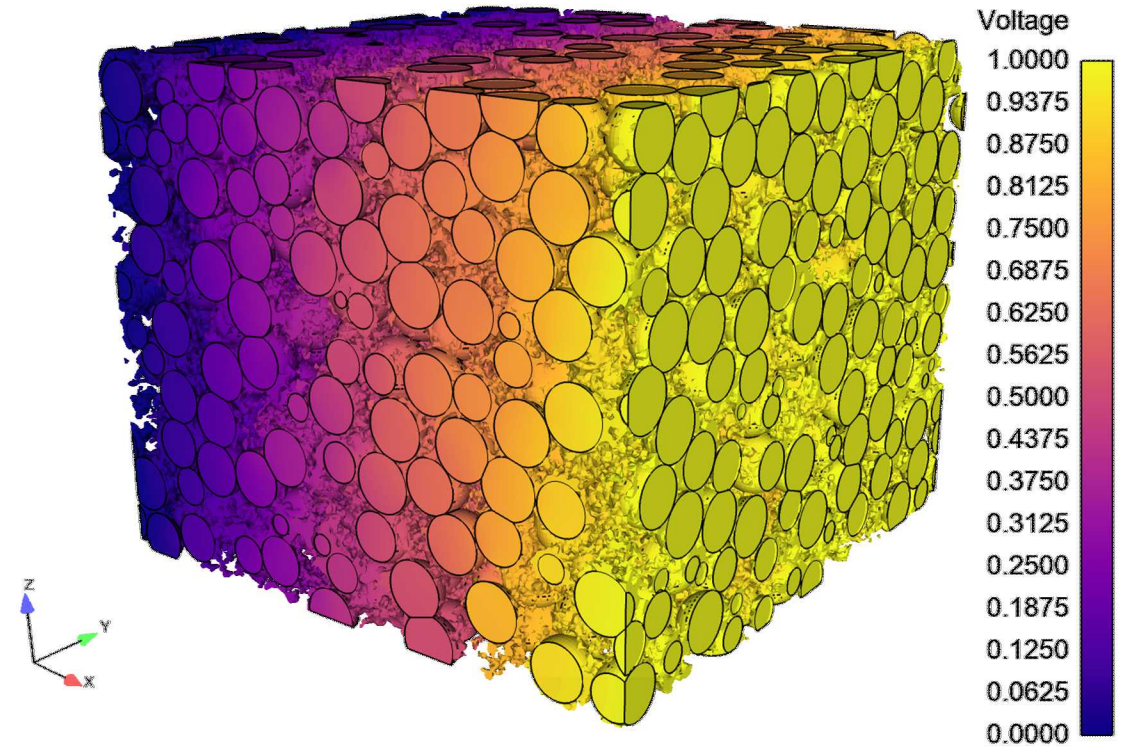
# Effective electrode property calculations

Calculate effective transport properties for upscaling

- Particle specific surface area
- Electrical conductivity
- Tortuosity

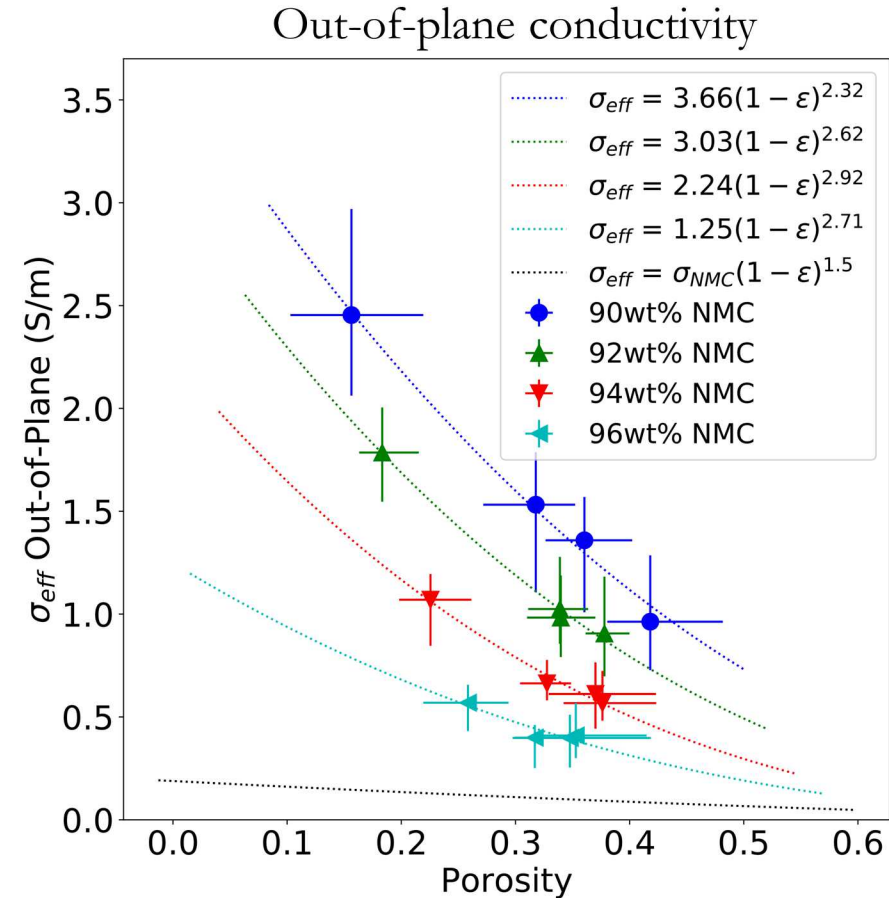
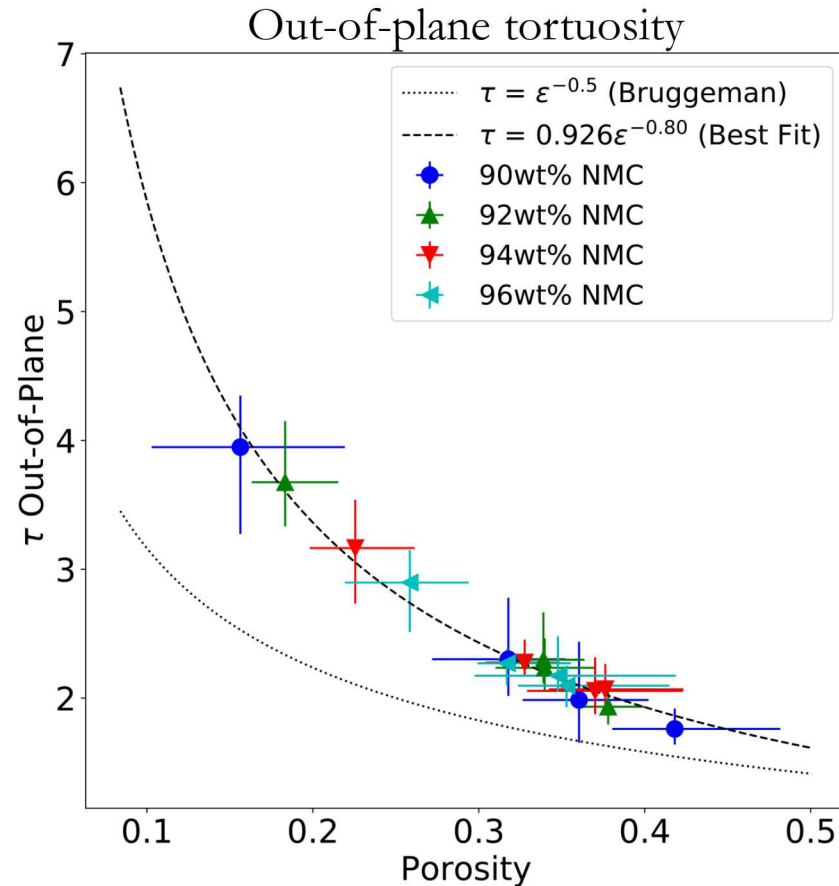
NMC image data from Ebner (2013)

- 90, 92, 94, 96 wt% NMC (remainder 1:1 CB:PVDF)
- 0, 300, 600 & 2000 bar calendering
- $100\text{ }\mu\text{m} \times 100\text{ }\mu\text{m} \times 60\text{ }\mu\text{m}$  domain (20 realizations eac
- Binder bridge (porous) morphology approach



Effective properties are an important first step for upscaling mesoscale data

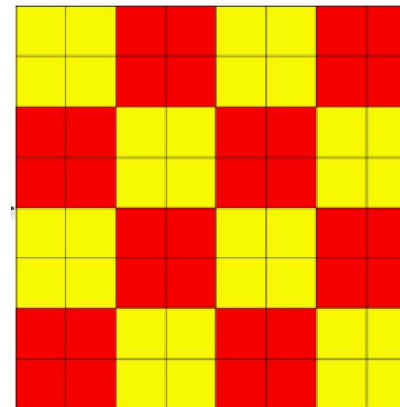
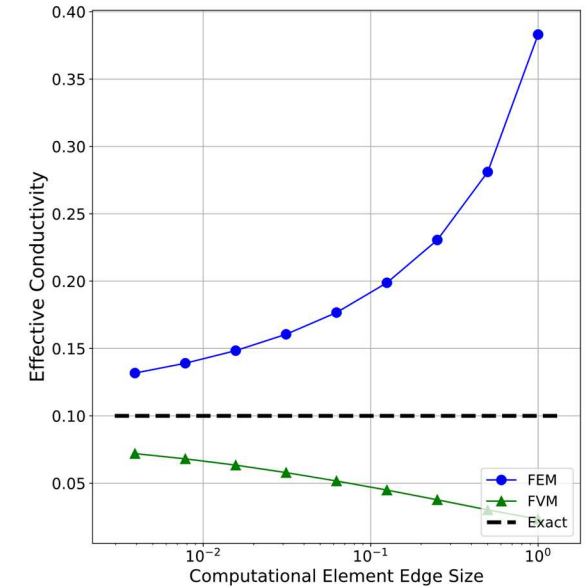
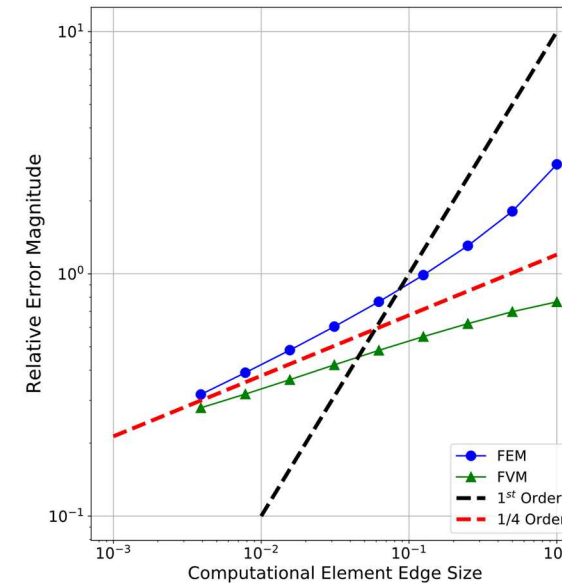
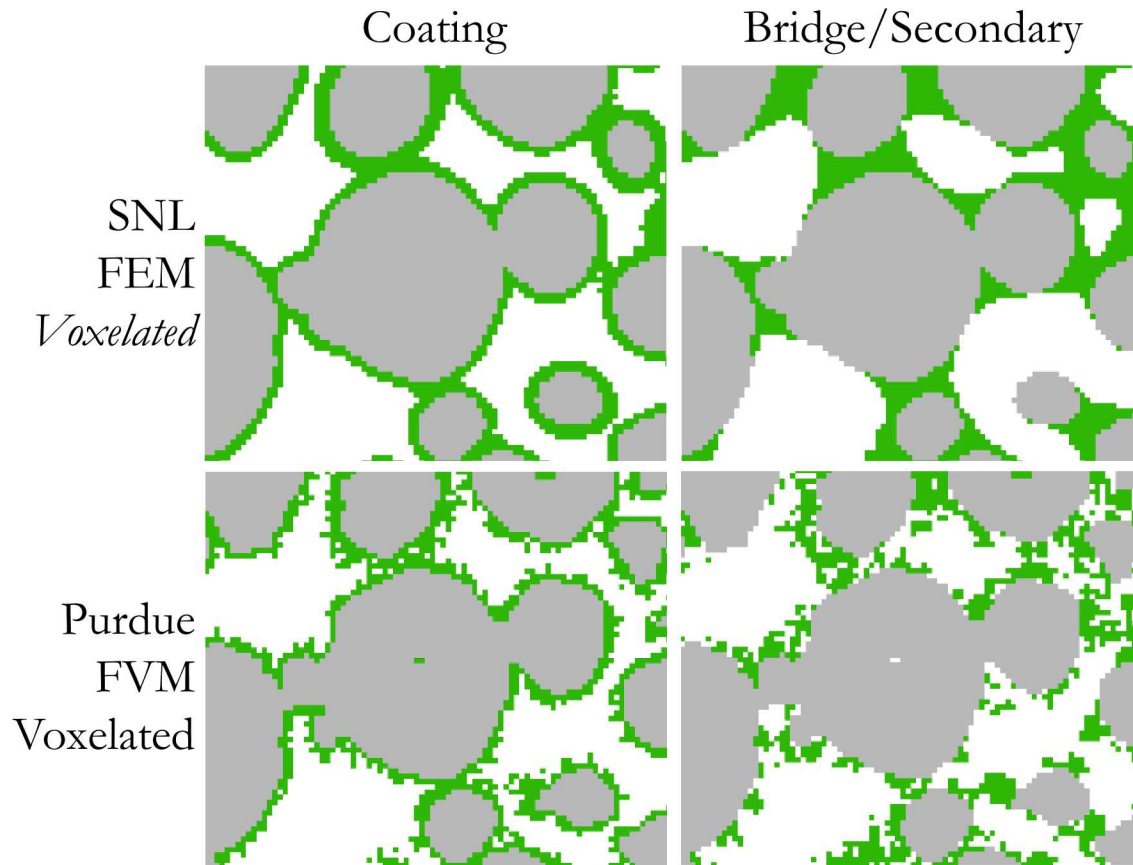
# Effective electrode property calculation results – Transport



Bruggeman relationships must be re-calibrated to fit simulated data



# What about other morphologies and numerical methods?

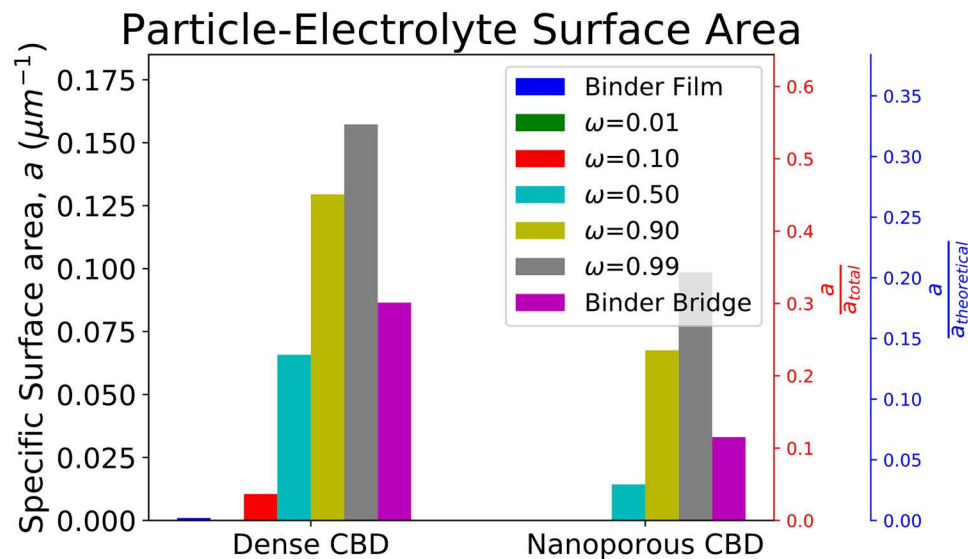


Both methods converge on voxelated meshes, but:

- At slow rates (1/4-order)
- From different directions
- Unrefined results 10x different

Care must be taken when comparing results generated using different numerical methods; likely not converged!

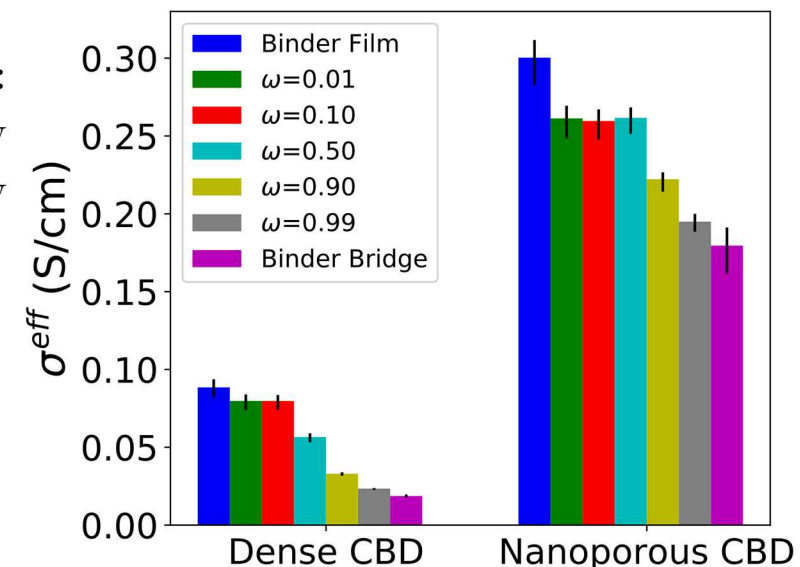
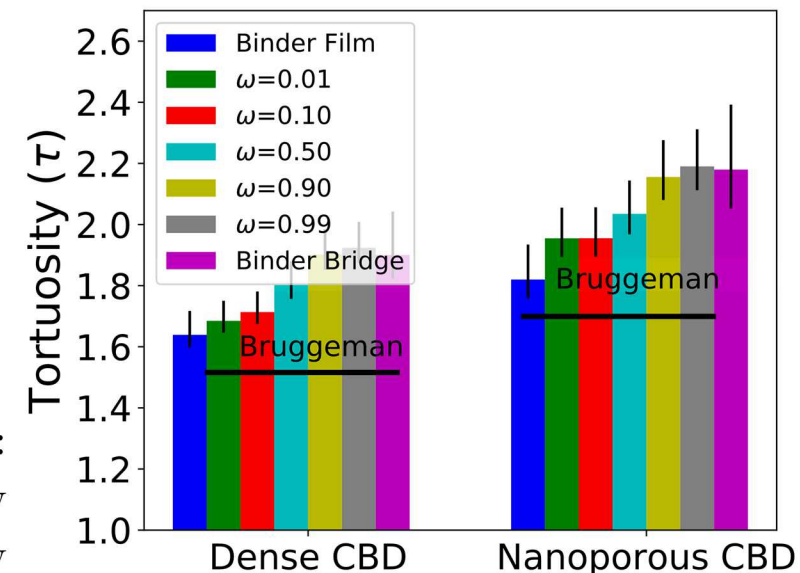
# Porous binder and morphology considerations



- More particle surface area available with non-uniform morphologies
- Nanoporous binder decreases bare particle surface area, but binder area is porous
- Surface area much less than theoretical

- Non-uniform binder:
- Increases tortuosity
  - Decreases conductivity

- Nanoporosity:
- Increases tortuosity
  - Increases conductivity

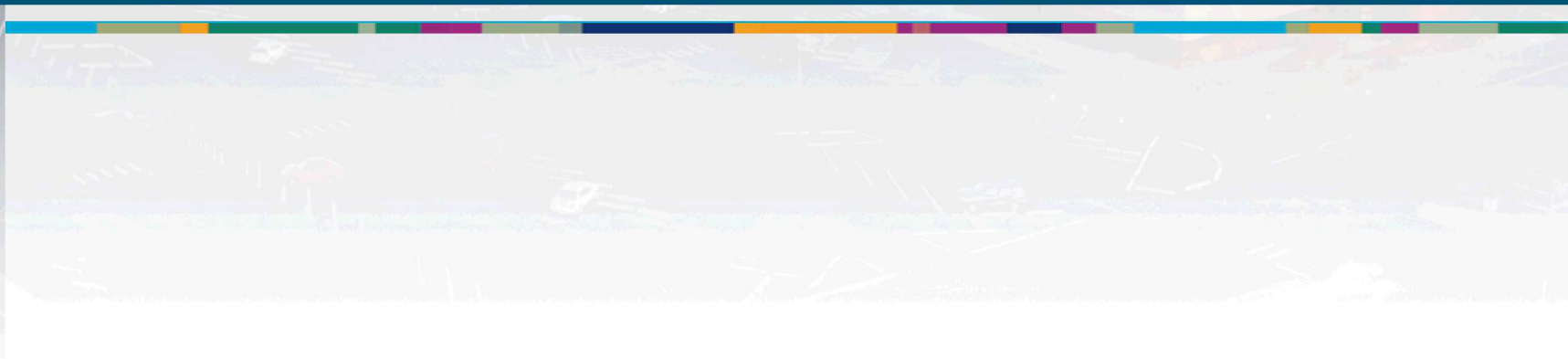
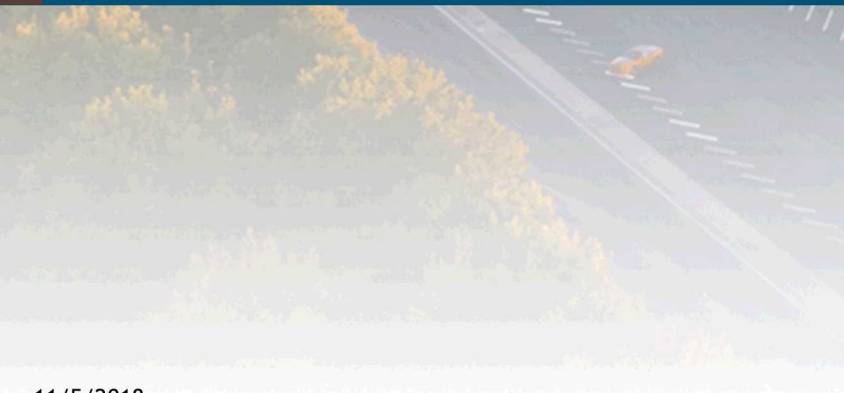


Limiting cases of both morphology methods show similar (but not identical) behavior; nanoporosity is important!





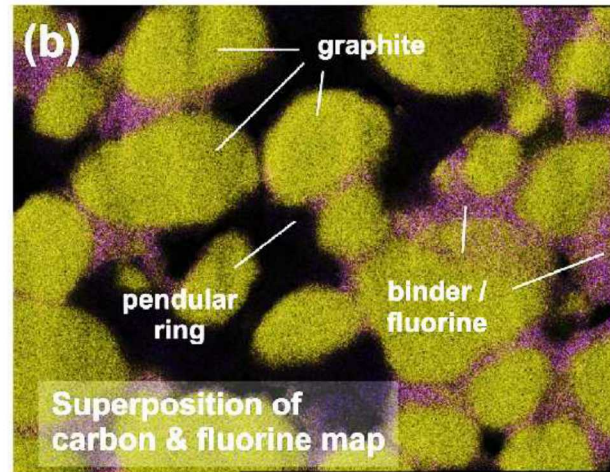
# Discrete Element Method Mesostructure Generation



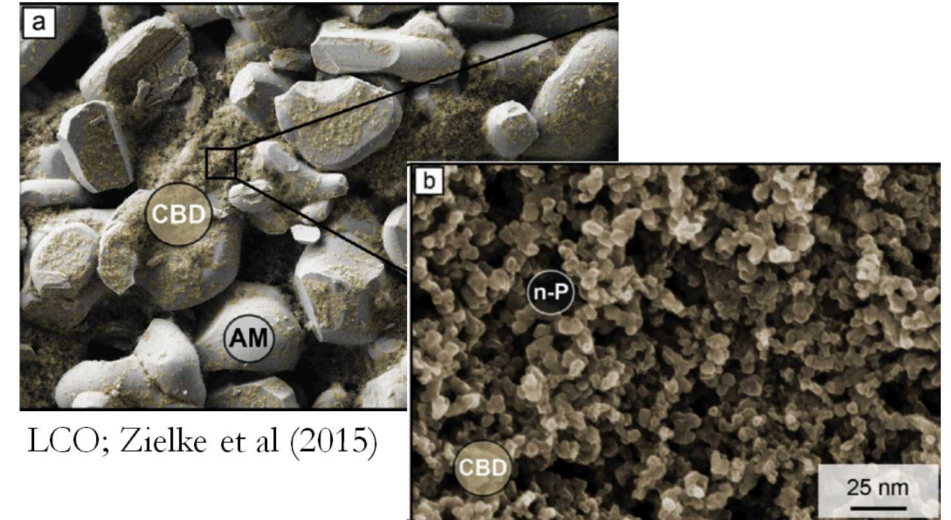
# Challenges with using CT mesoscale data

3D CT image data:

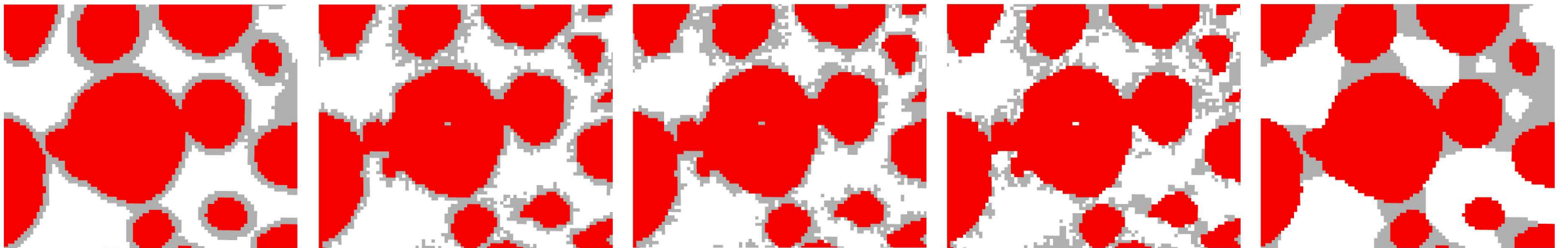
- Expensive
- Time consuming
- Conductive binder not visible



Graphite; Jaiser et al. (2017)



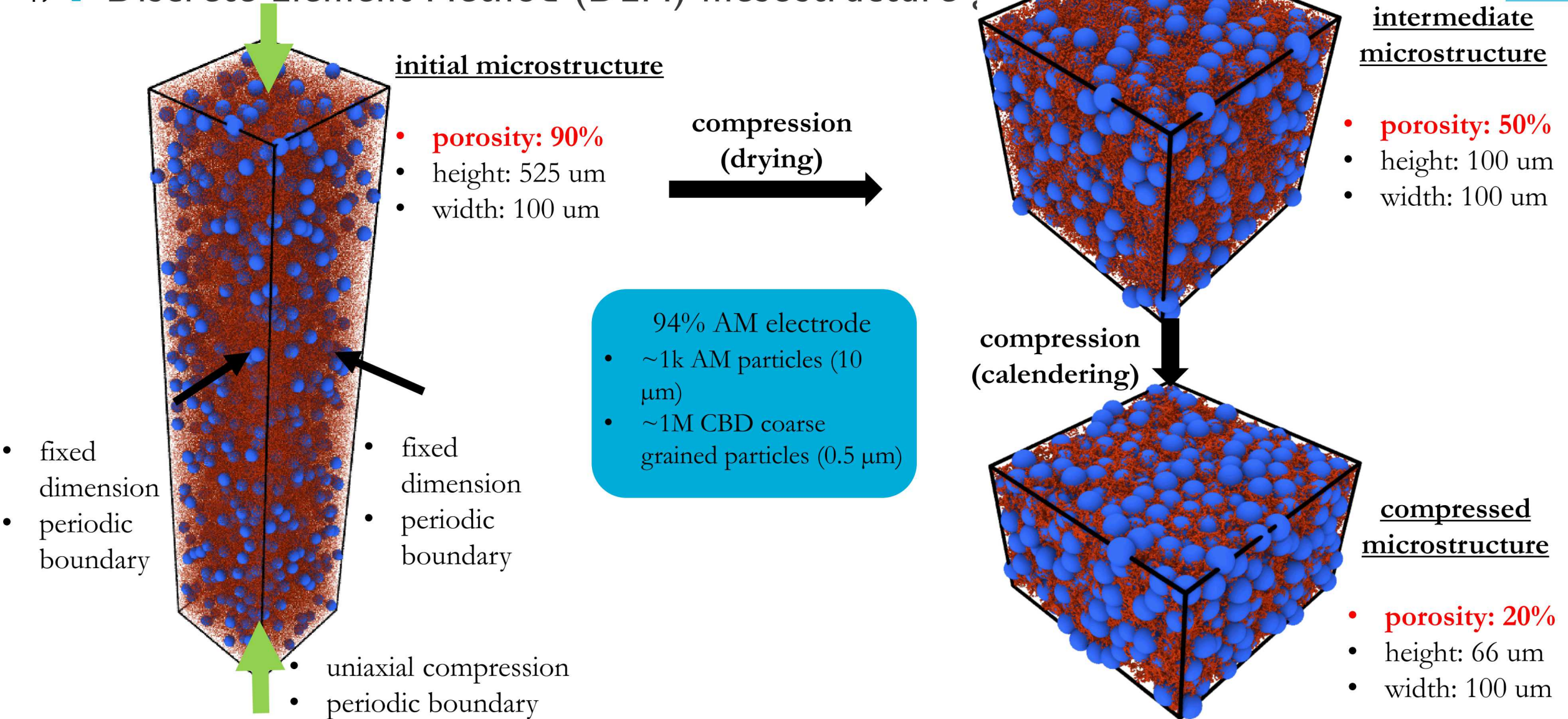
LCO; Zielke et al (2015)



Hypothesis: Use DEM simulations to create AM+CBD mesostructures and CDFEM for physics predictions



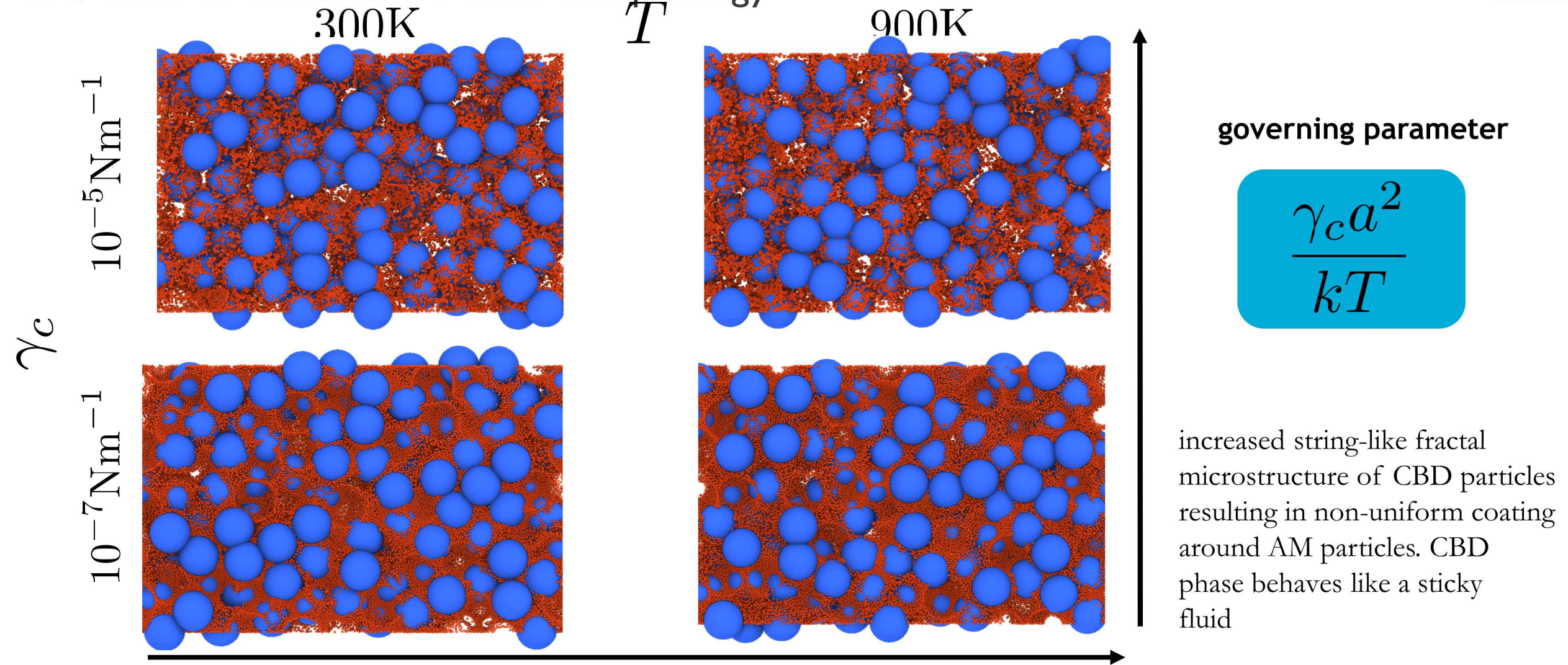
# Discrete Element Method (DEM) mesostructure



Uniaxial compression with granular and Brownian forces enable study of AM consolidation and CBD aggregation



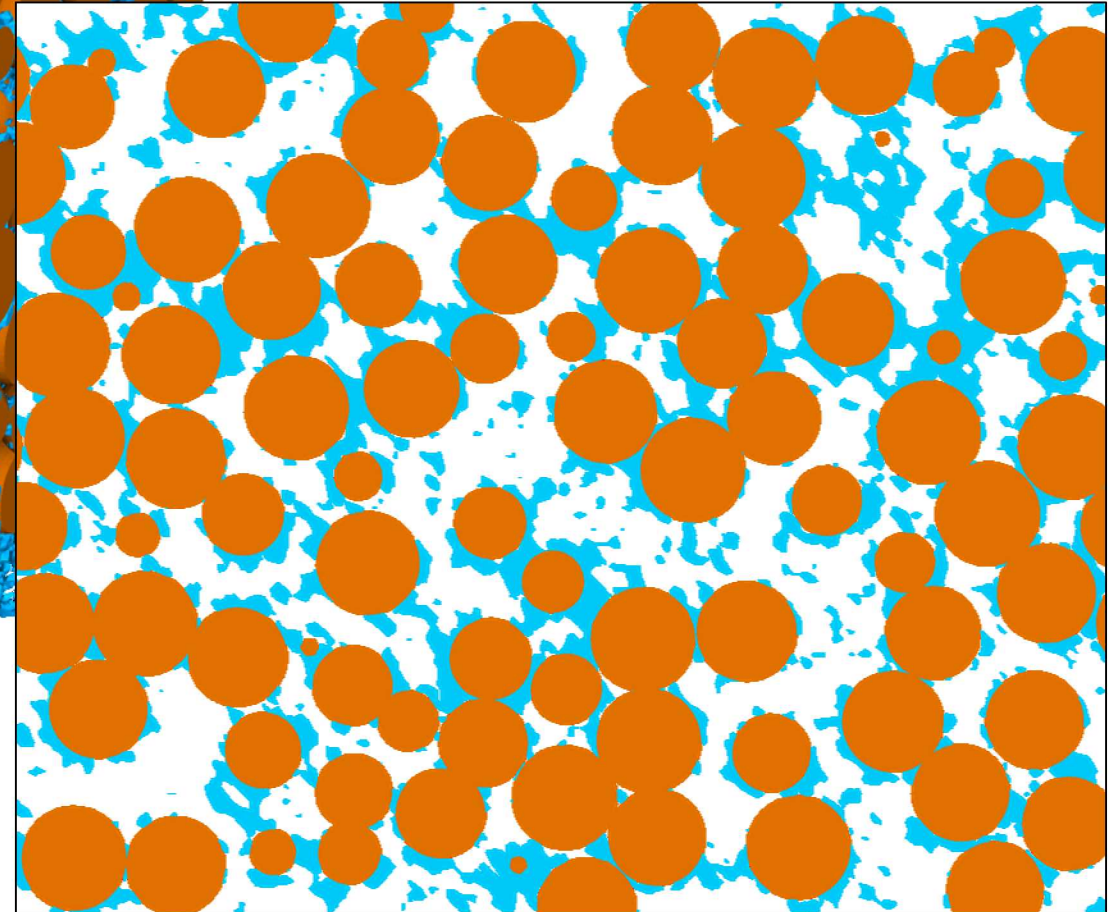
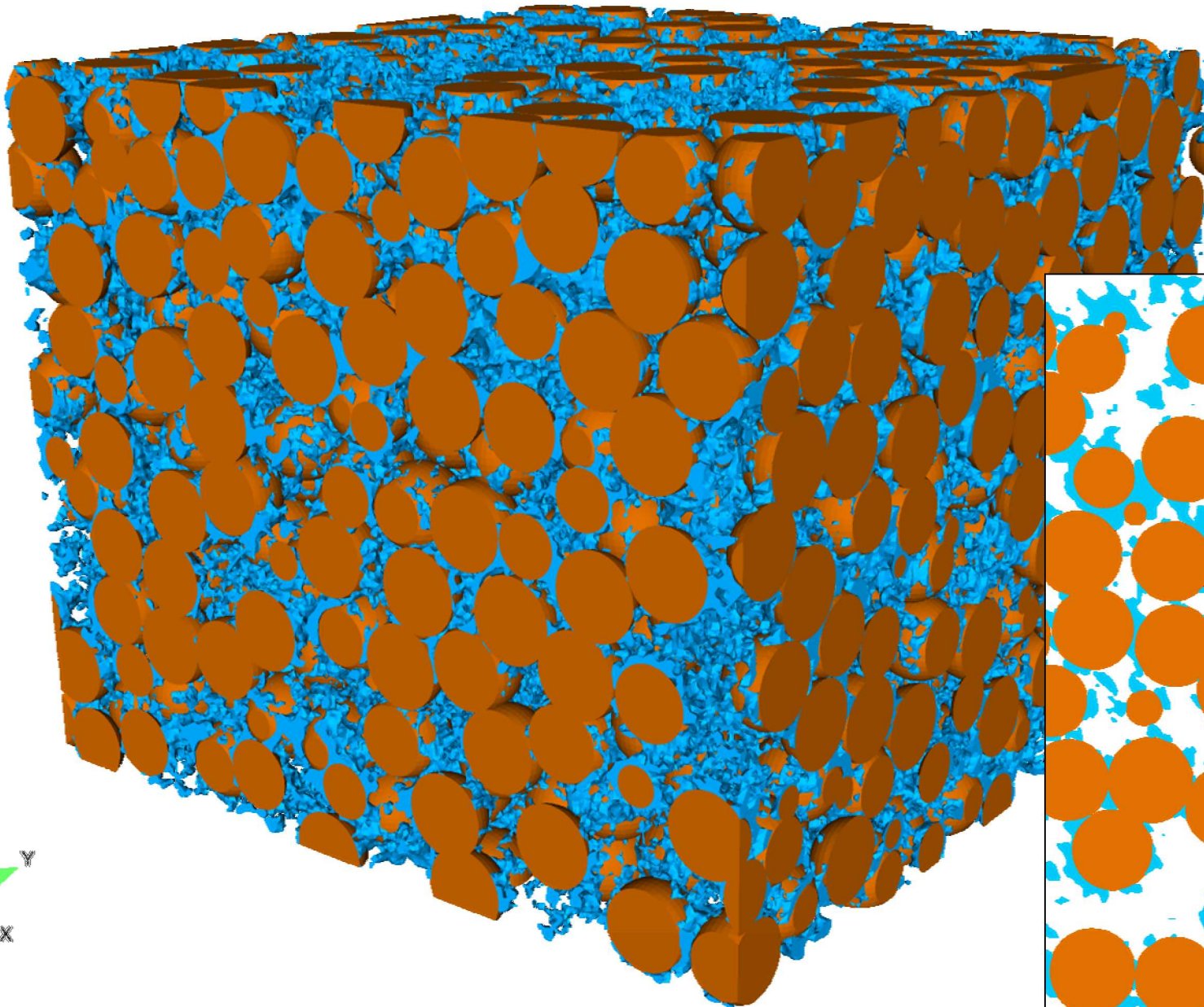
# Role of cohesion in CBD morphology



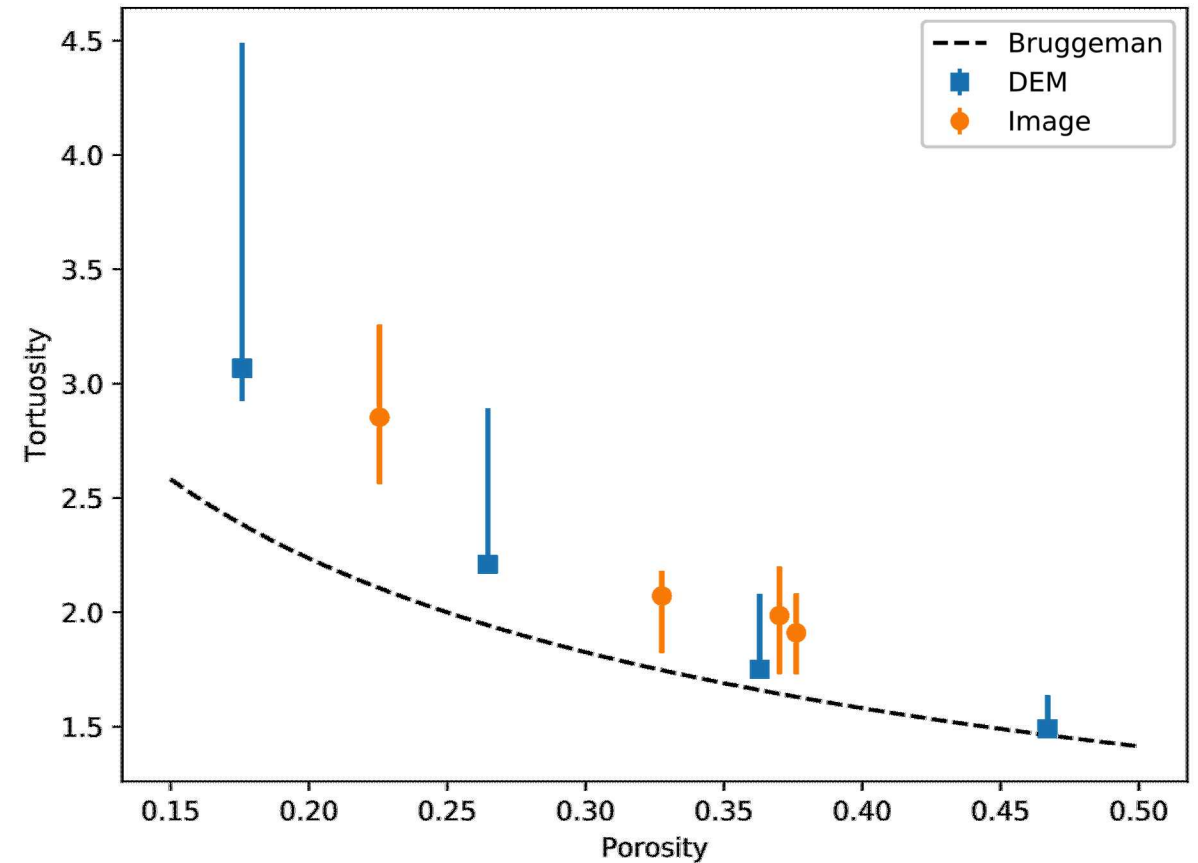
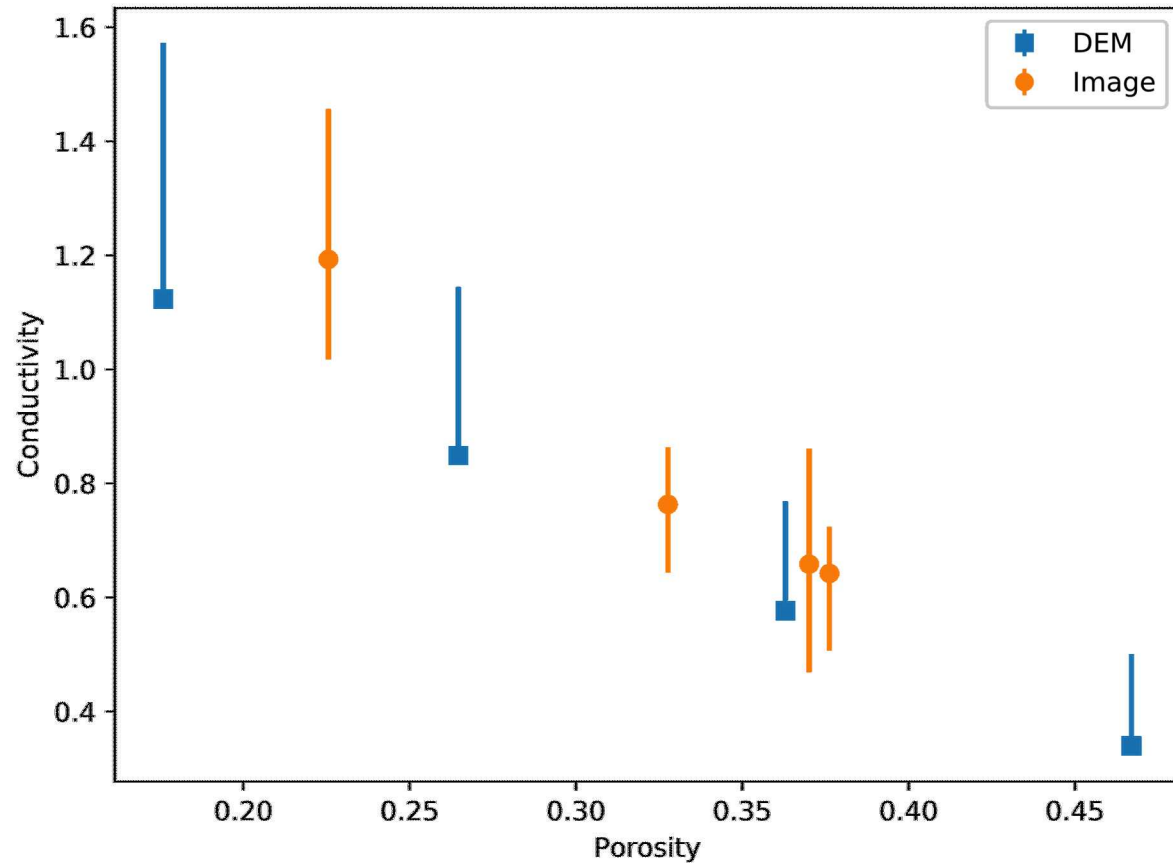
increased CBD diffusion results in a more uniform coating around AM particles

Cohesive surface energy drastically alters CBD morphology





# Comparison of image- and DEM-based mesostructures



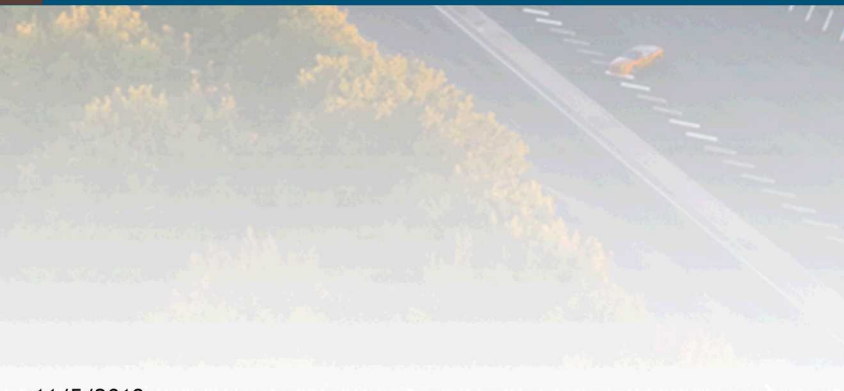
All simulations for  $T=600$ ,  $\gamma=10^{-5}$ , AM=94 wt%, 0 bar calendaring

Calendaring  $\rightarrow$  lower porosity  $\rightarrow$  more CBD connectivity  $\rightarrow$  higher conductivity and tortuosity





# Electrochemical-mechanical discharge simulations of NMC half-cells



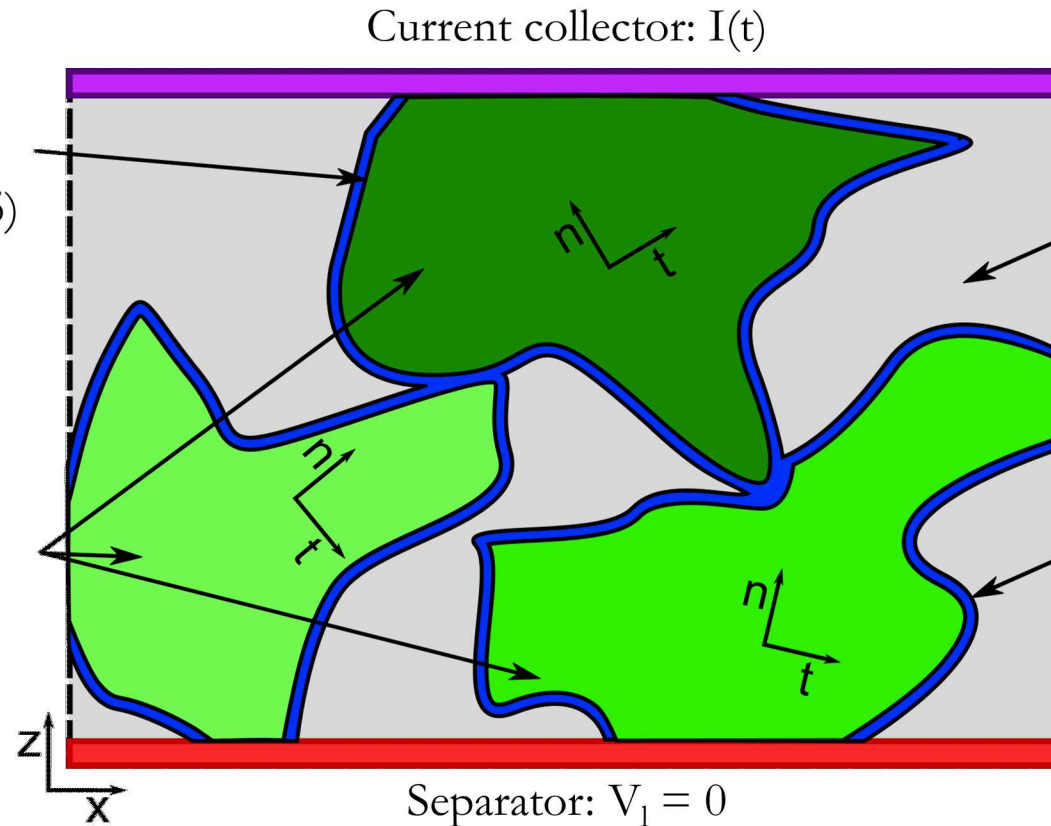
# Coupled electrochemical-mechanical half-cell discharge simulations

## Particle Interface:

- Butler-Volmer reaction
- OCV from Smekens (2015)

## Particles:

- Species – Li tr
  - Chemical
  - Stress pc
- Electrical –  $\phi$
- Mechanics -  $\mathbf{E}$ 
  - Li-induc



## Electrolyte:

- Species –  $\text{Li}^+$  transport
  - Nernst-Planck fluxes
  - Electroneutrality for  $\text{PF}_6^-$
- Current conservation

## Conductive binder:

- Species – Porous  $\text{Li}^+$  transport
- Electrical
  - Solid: Porous Ohm's law
    - Strain-dependent electrical conductivity
  - Liquid: Ionic conservation & electroneutrality
- Mechanics – Elastic

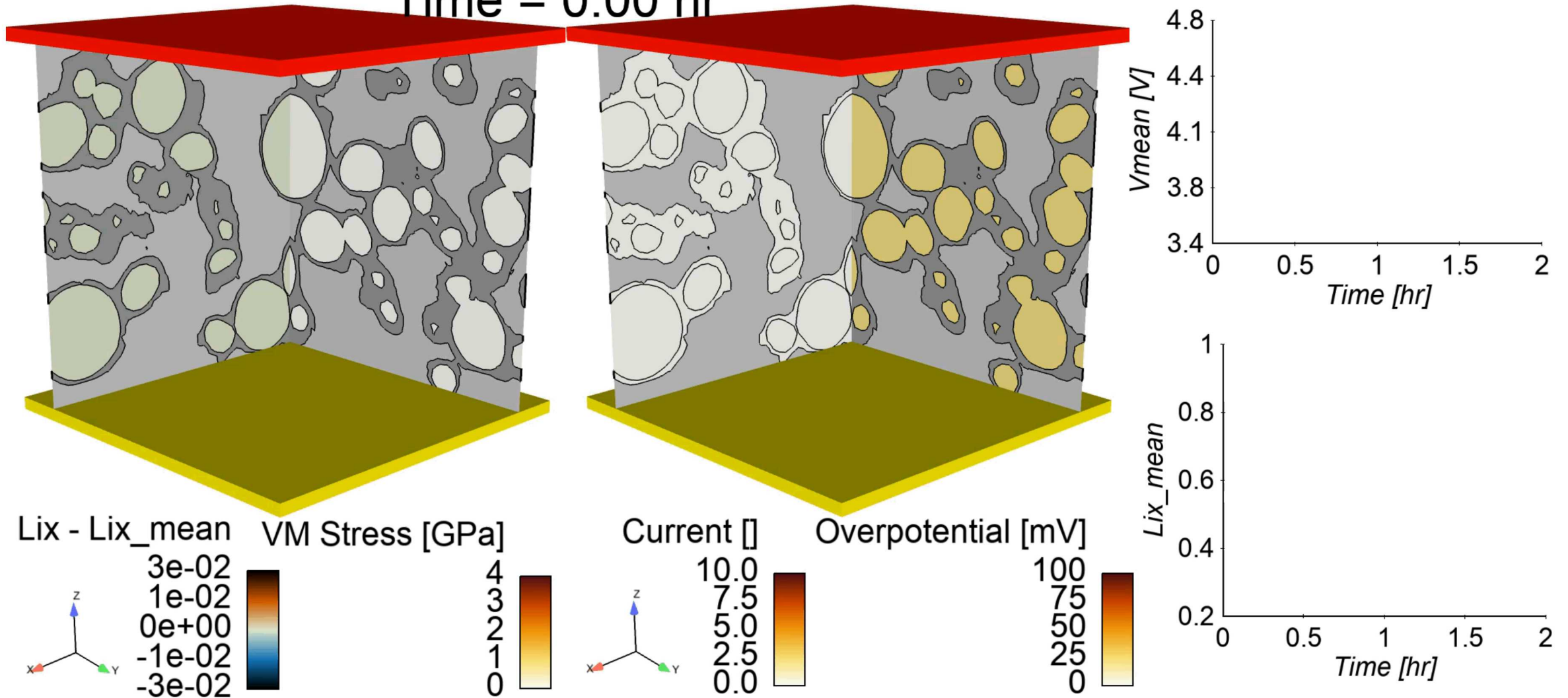
Mathematical formulation builds off of Mendoza (2016) LCO studies

Predictions of discharge curves, effects of mechanics, rate effects, and spatial variations in performance



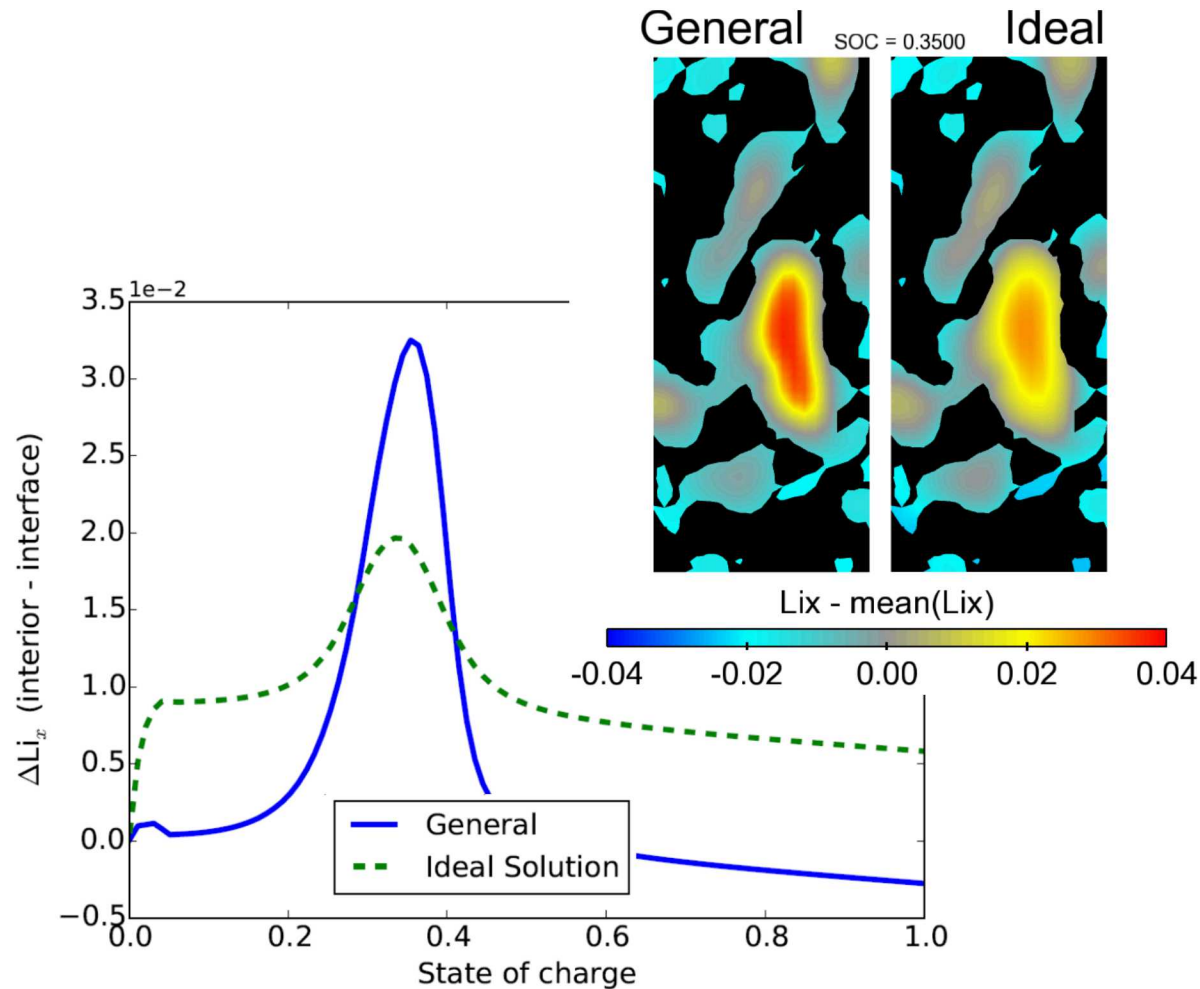
# Demonstration of NMC half-cell discharge simulation at C/2

Time = 0.00 hr

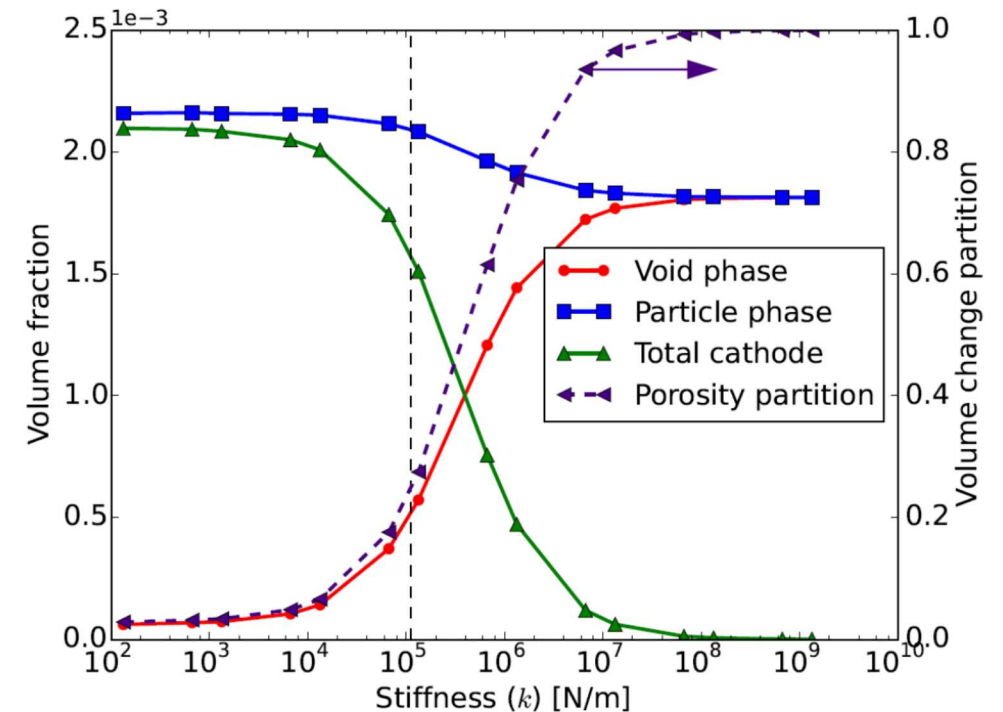


Coupled electrochemical-mechanical simulation yields detailed insight, predicts electrode-scale response

# What can you learn from coupled half-cell simulations? LCO



LCO is a non-ideal solution, gradients not as dominant as some believe



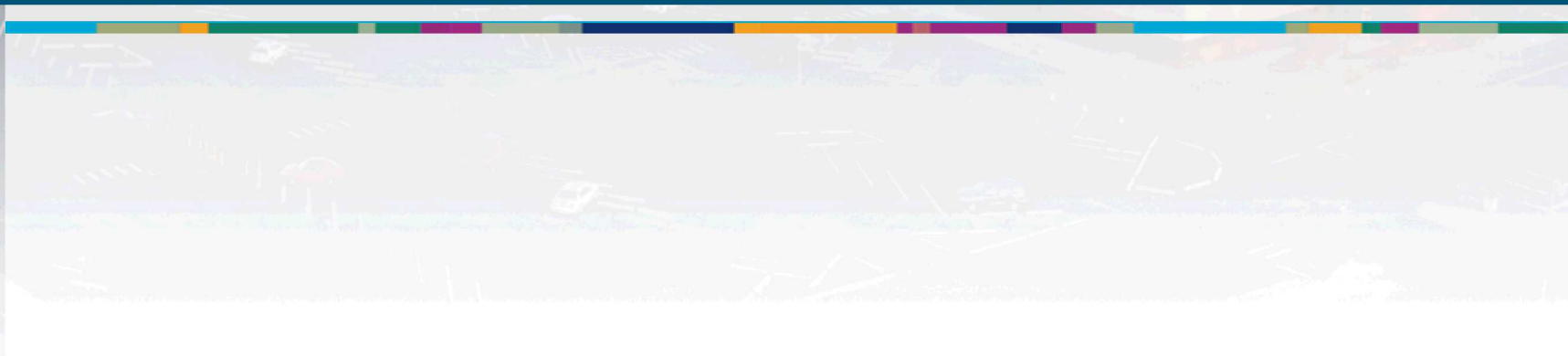
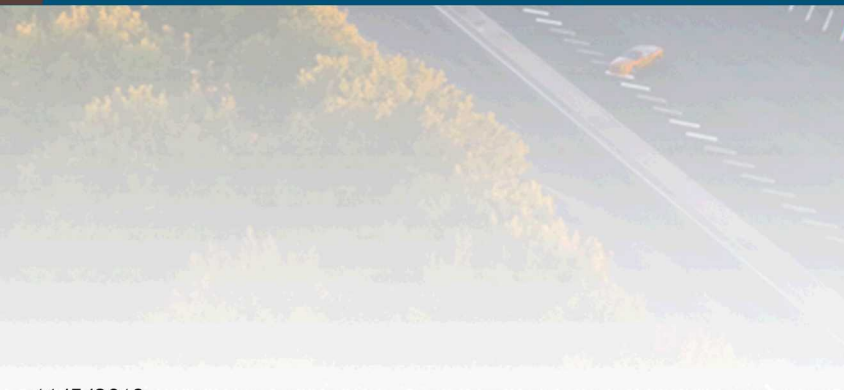
Separator/collector stiffness/boundary conditions influence electrode mesostructure evolution

Details at the mesoscale influence cell performance ... and vice versa!

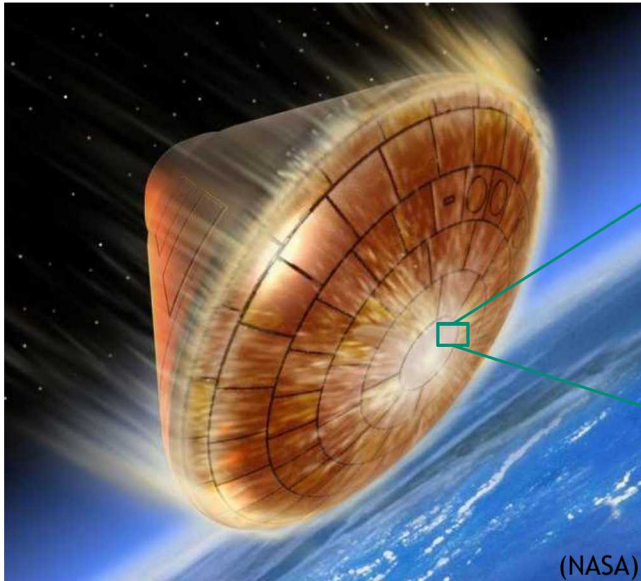




# Mesoscale modeling of TPS materials: Effective property calculations and sensitivity analysis

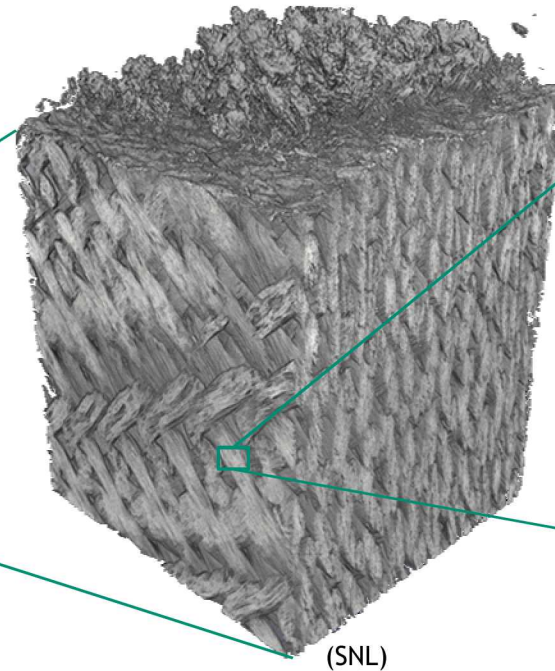


# TPS materials are hierarchical, multi-scale composites



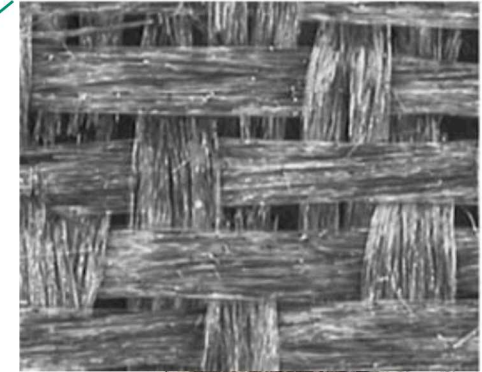
## Macroscale

Typical performance assessments and modeling.  
Composite properties required.



## Mesoscale

Woven fiber surrounded by phenolic resin. Governed by weave geometry, resin/tow properties.



## Microscale

Individual fiber filaments spun into yarns, impregnated with resin. Fiber arrangement affects tow properties.

TPS performance governed at the mesoscale and microscale, modeling those scales gives flexibility to CMA etc.



# Bulk properties depend on constituents

## Constituents

### Fiber properties

- Anisotropy

### Resin properties

### Filler properties

- Size distribution
- % mass

### Void space

- % vol.

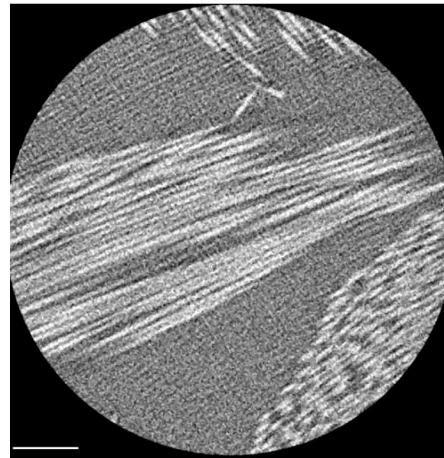
## Microscale

### Yarn model

- Filament packing
- Filament count
- Twist
- Shape/length

### Matrix model

- Effective medium
  - Bruggeman etc.
- Void/filler shape/size



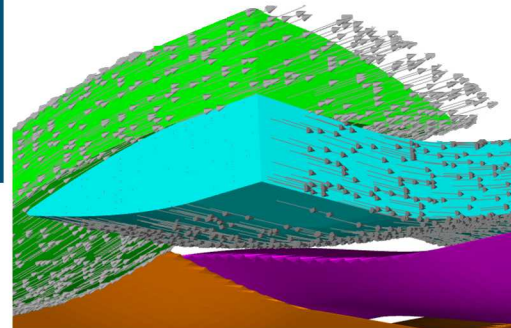
## Mesoscale

### Fabric geometry

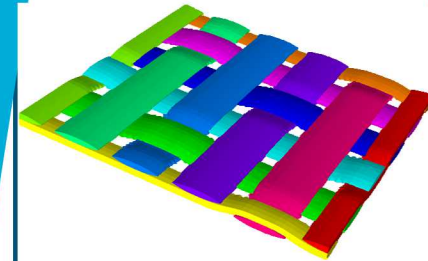
- Yarn Count
- Thickness
- Gaps in fabric
- “Waviness”

### Yarn properties

### Matrix properties



## RVE Model + FEM Model



## Macroscale

### Composite Effective Properties

### Properties

- $K$
- $C_p$
- $\rho$
- $E, G$
- $\nu$
- $CTE$

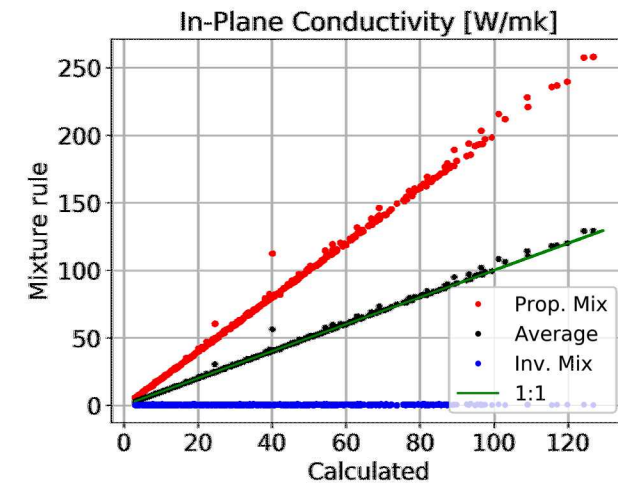
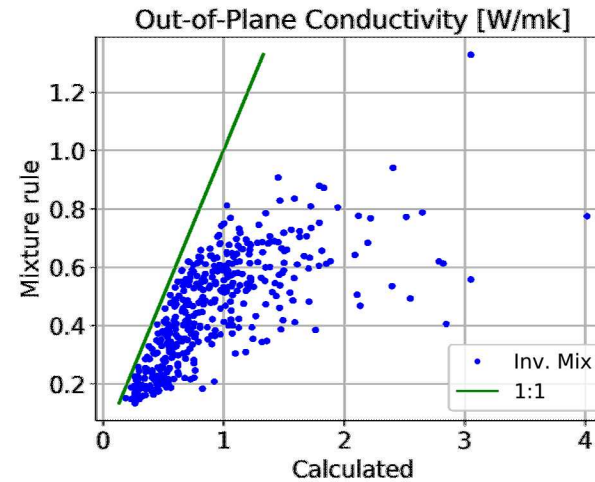
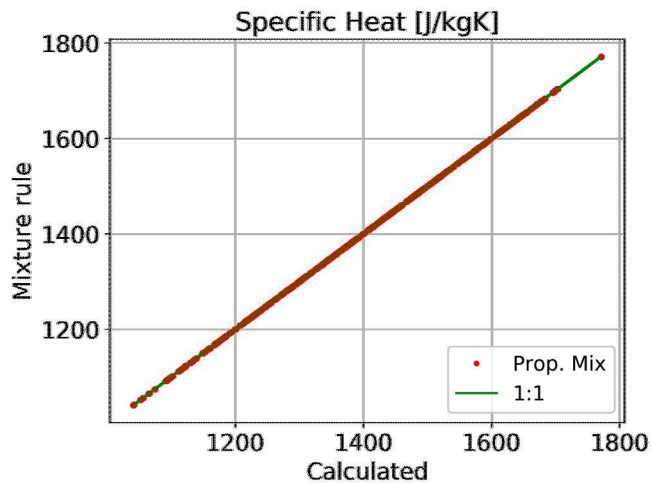
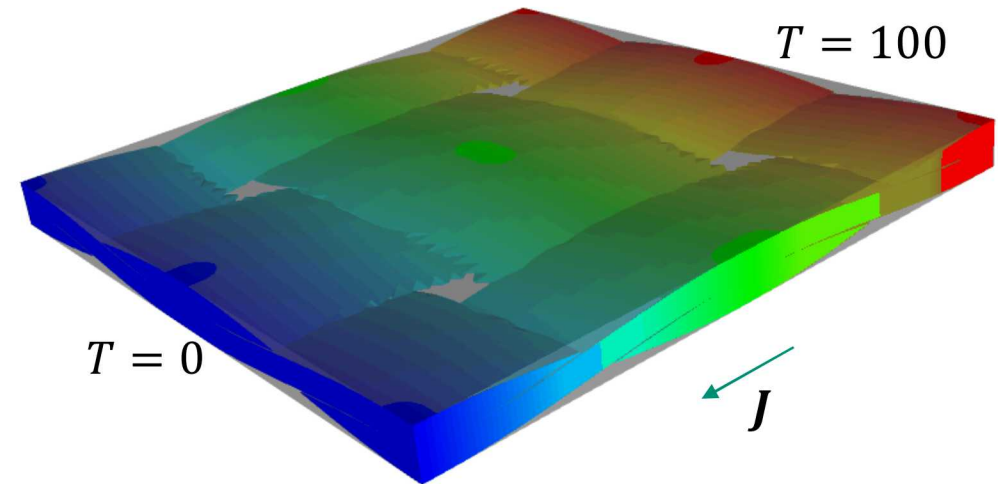
# Trends in thermal conductivity and distributions

Proportional mixture rule (axial, upper bound):

$$E_v^* = v_f E_f + (1 - v_f) E_m$$

Inverse mixture rule (transverse, lower bound):

$$E_r^* = \left( \frac{v_f}{E_f} + \frac{1 - v_f}{E_m} \right)^{-1}$$



Effect medium approximations are applicable only in certain situations



# Ablation is a transient process

Mesoscale is *not* static during ablation

- Surfaces recede
- Phases evolve (resin → char)
- Phases melt
- Phases deposit (coking)

Evolving geometries are necessary

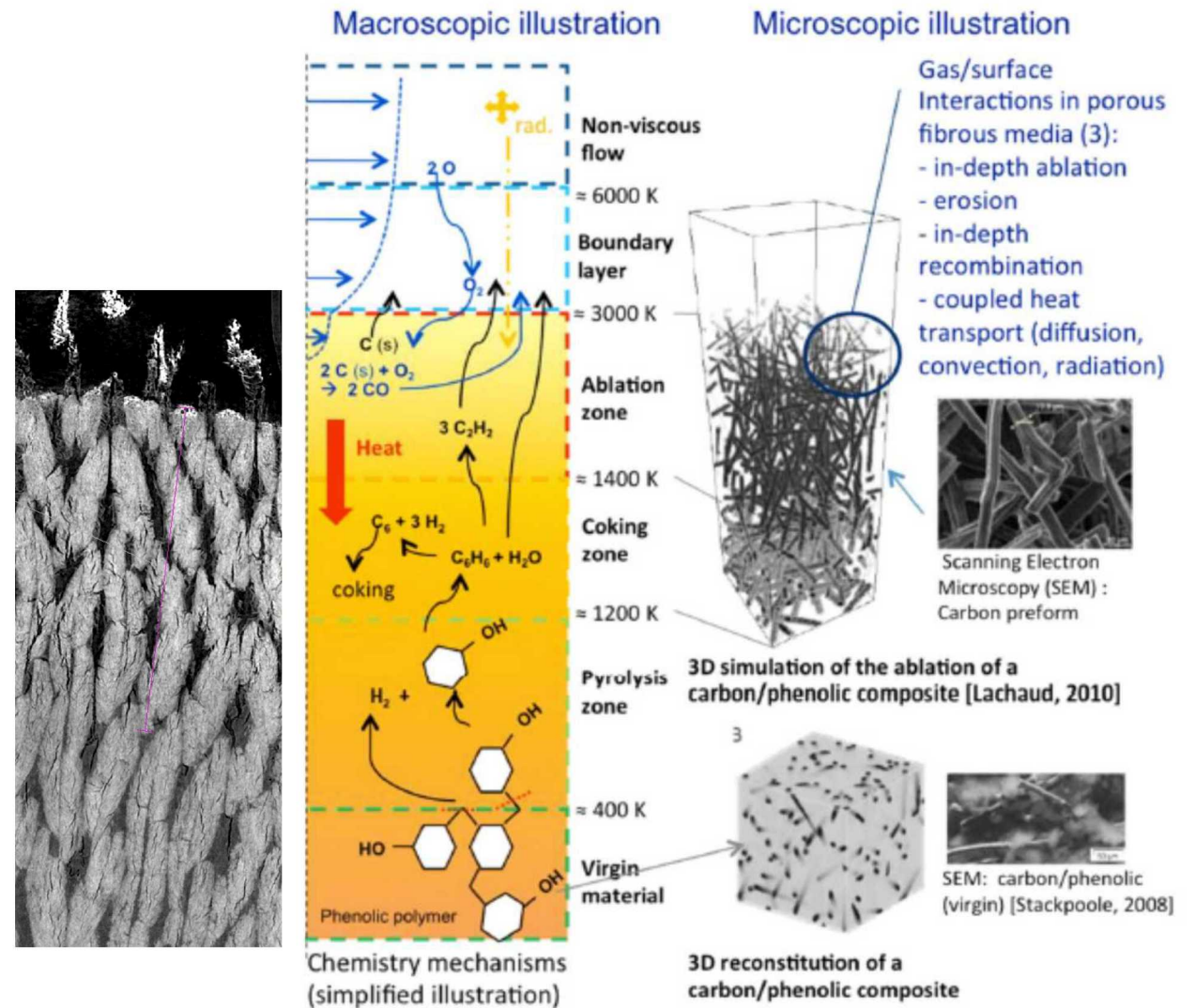
Analytic background

- System of sinusoid fabric descriptions

Moving resin interface

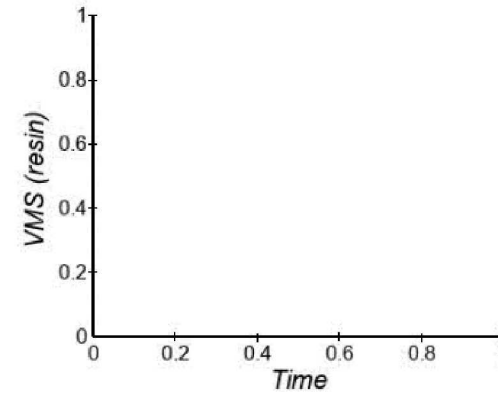
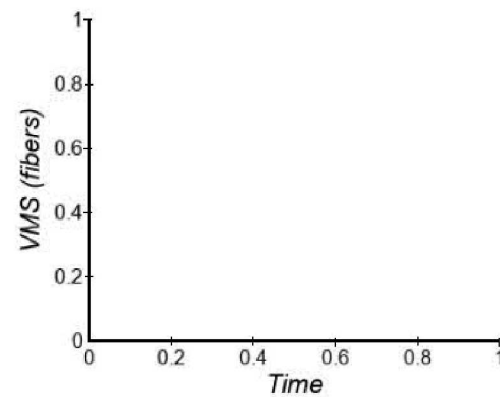
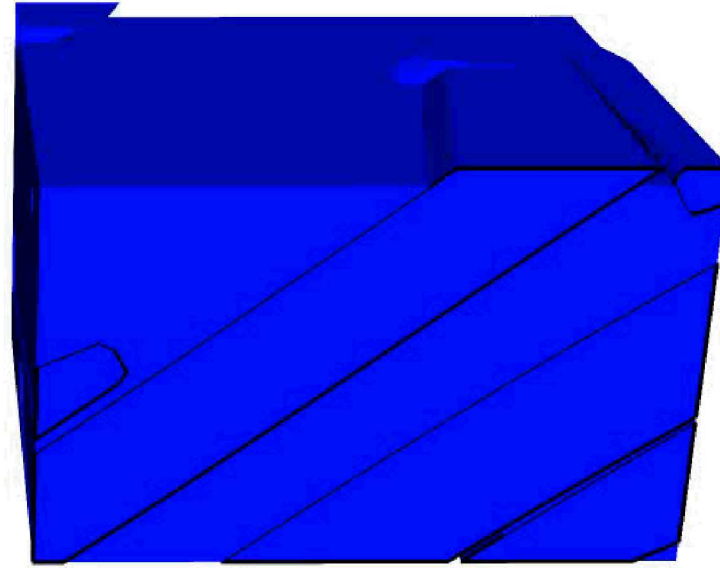
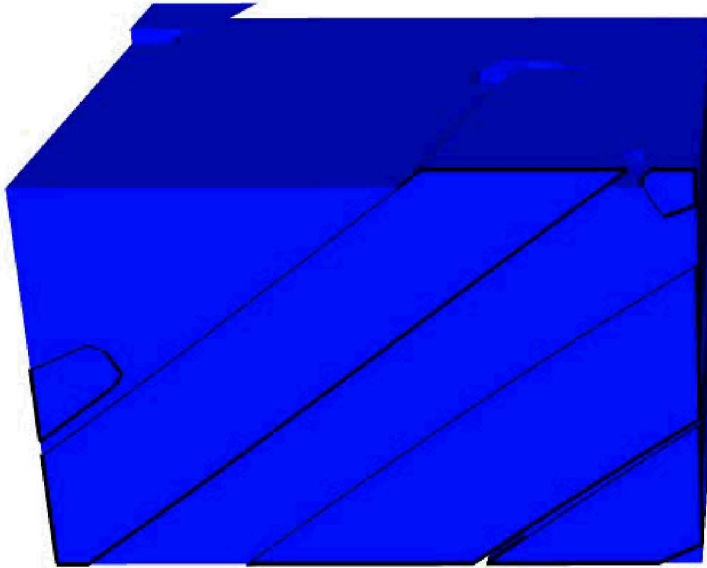
- Transient level set

Ablation modeling



(Lachaud, 2014)

Dynamic geometry is necessary to model ablation

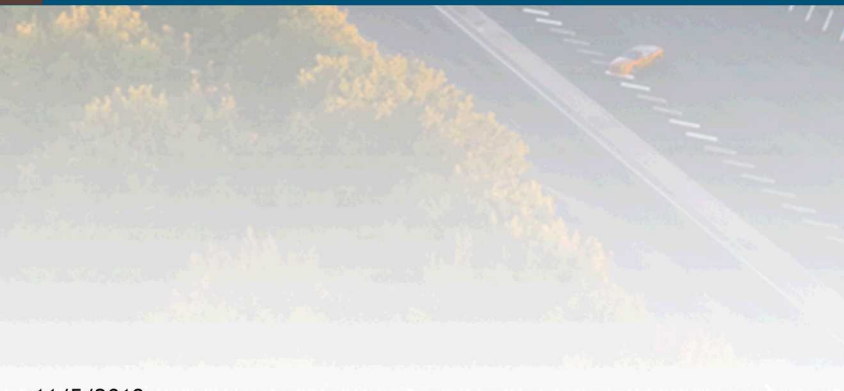


Coupled thermal and mechanical effects can identify failure mechanisms





# Credible Automated Meshing of Images



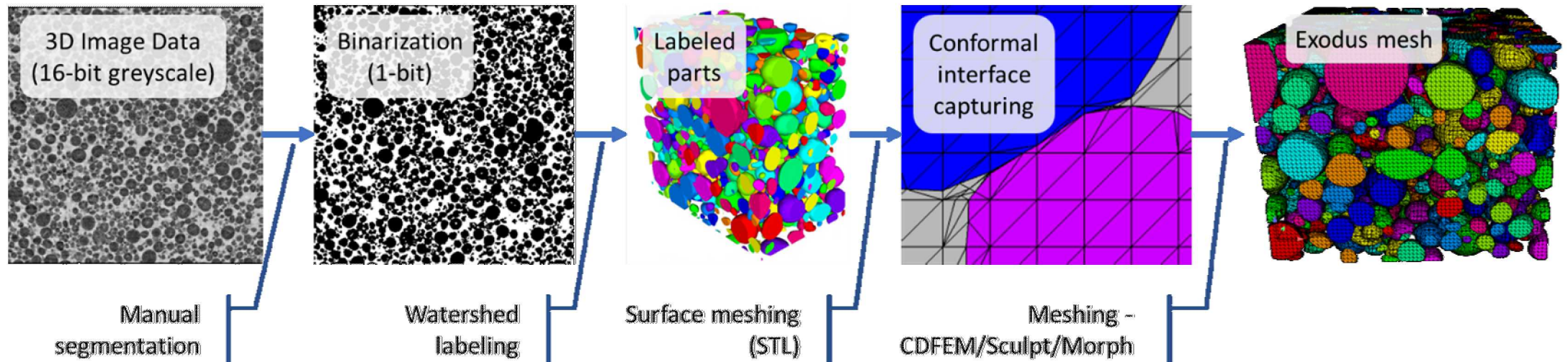
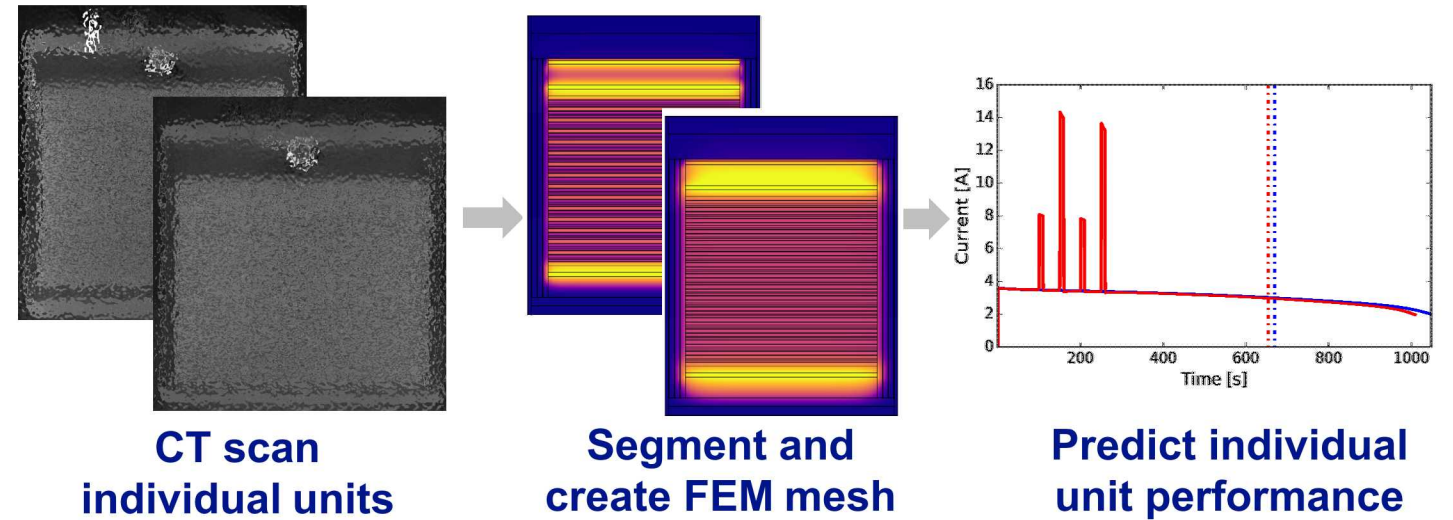
## Problem statement

Desire to perform FEM simulations directly from 3D tomographic imaging

- Enables “digital-twins”

Recent state-of-the-art processes are:

- Manual, SME-dependent
- Time-consuming
- Unknown credibility
- Don't capture all geometric features



Automated, credible CT-to-mesh would revolutionize engineering analysis workflows!

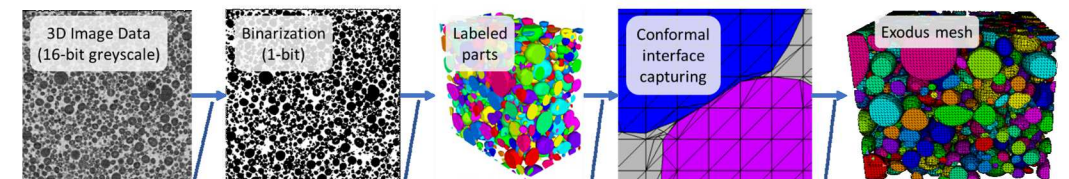
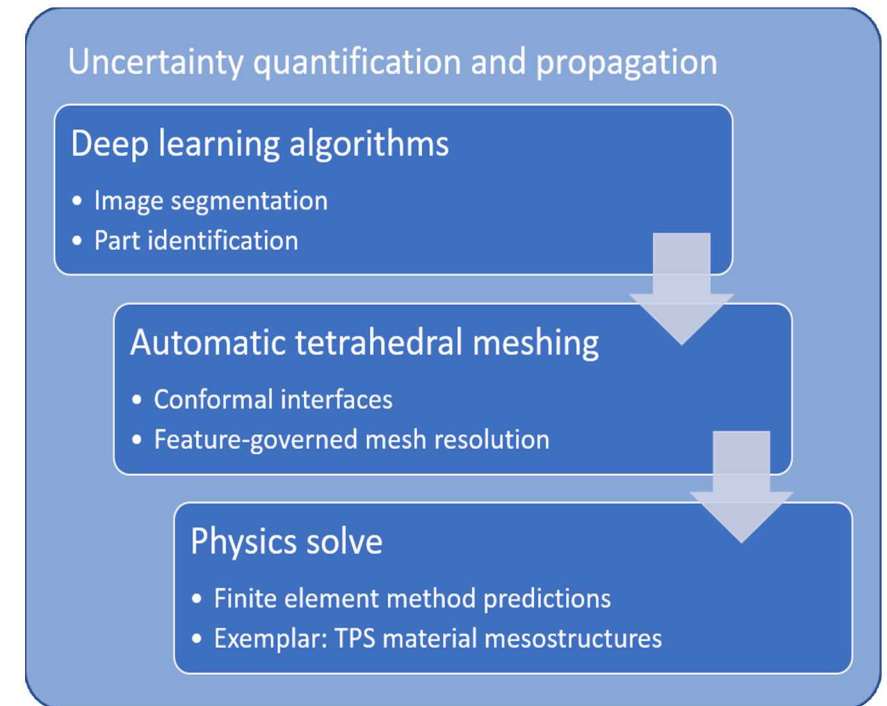


Hypothesis: We can develop an automated and credible image-to-mesh technology that can demonstrate the physics impact of per-unit variability on material, component, or system performance

Objective: We seek to develop a methodology for **automatically, efficiently, and reproducibly** creating **conformal** finite element meshes from **3D tomography** with **quantified uncertainty**.

Research thrusts – primary science questions:

- Deep machine learning algorithms (ML)
- Automatic conformal tetrahedral mesh creation (ATM)
- Uncertainty quantification and propagation (UQ)
- Application exemplar: Thermal protection system materials (TPS)



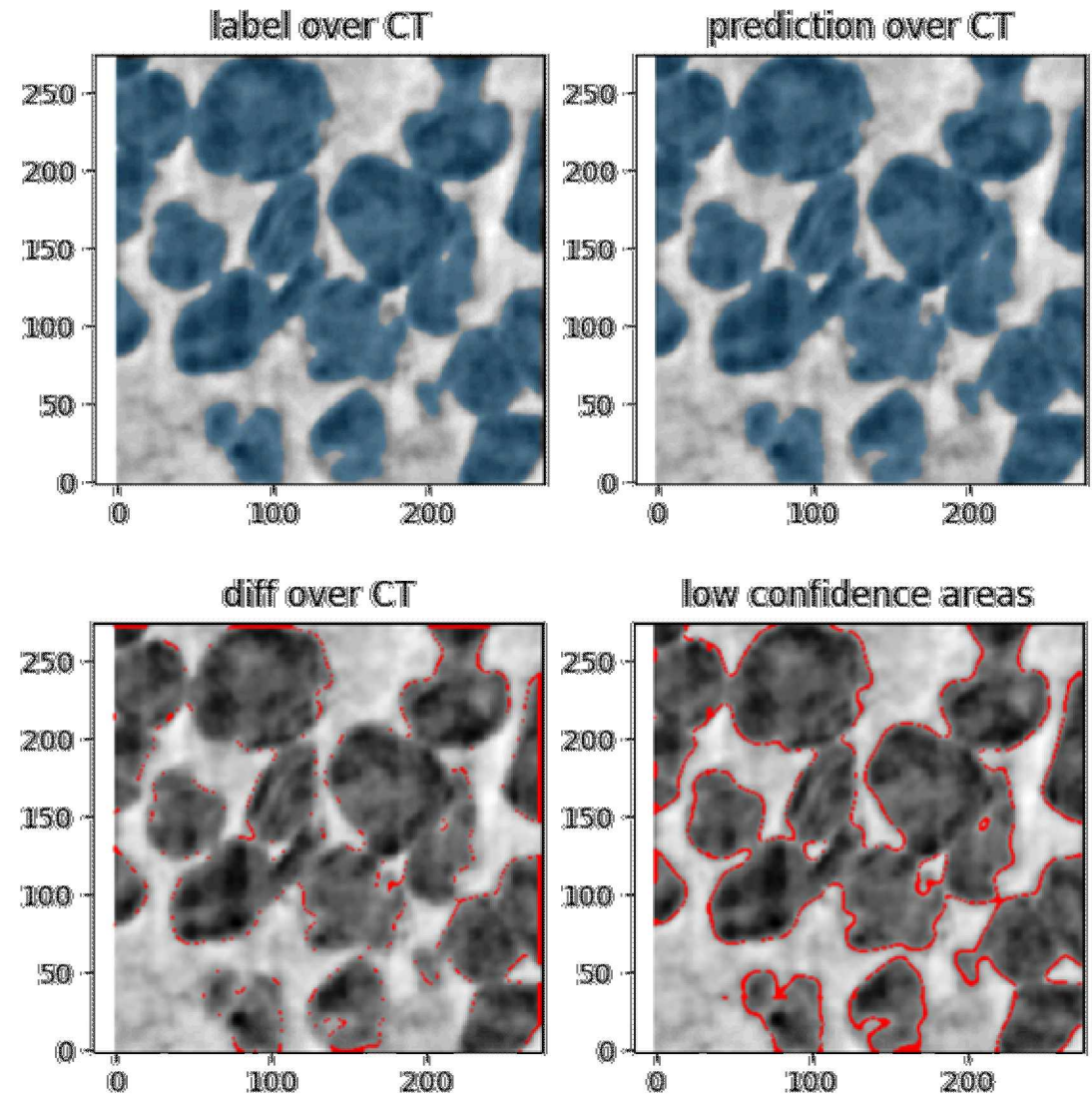
## Early demonstration of DL and UQ on graphite electrodes

DL trained with human labels to segment  
with  $> 99.9\%$  accuracy

Developing methodology to continuously assess  
per-voxel confidence in assessment and propagate  
through mesh

Upcoming challenges:

- Instance segmentation (particle labeling)
- Feature identification (edges/corners)
- Part orientation
- Mesh quality
- Verification of uncertainties (ground truth)

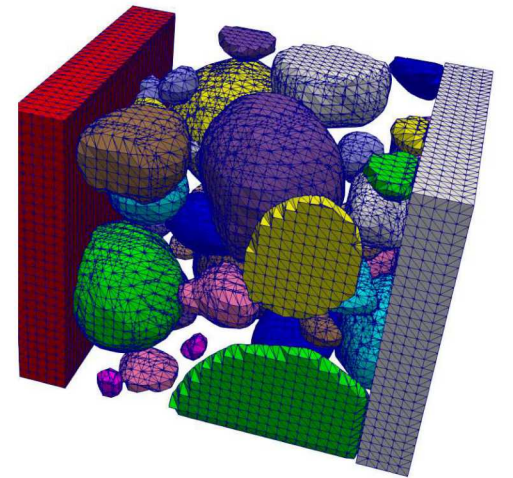
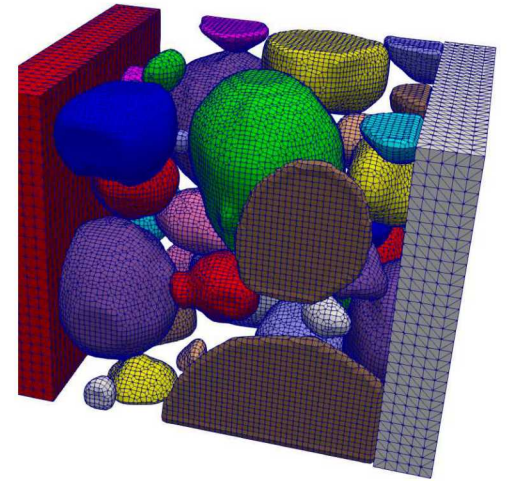
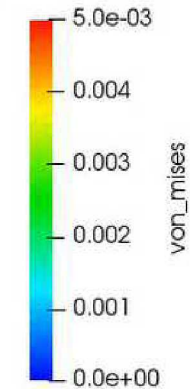
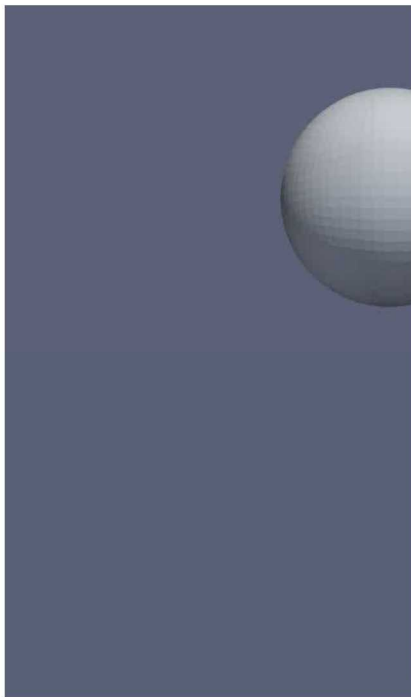


Deep learning shows huge promise in increasing throughput, repeatability, and credibility



Concept:

- Solid mechanics c
- Transport/electro
- Transfer displacer



Demonstrated two-way coupling between mechanics and transport codes; developing robust particle contact

We have developed a **unique image-to-mesh capability** to enable rapid analysis of as-manufactured parts

We have carefully **verified this approach**, identifying potential pitfalls and domain/mesh requirements

We have applied this technique to **lithium-ion battery cathode** mesostructures and have:

- Created and characterized the impact of conductive binder morphology
- Calculated and correlated effective properties
- Predicted coupled electrochemical-mechanicals effects during charge/discharge

We are developing **particle simulations** to carefully manufacture realistic mesostructures

We are applying these techniques to woven composites for **thermal protection systems**

We are beginning to improve the **credibility, reproducibility, and time required** to create high-quality meshed from 3D image data



## Publications

- Roberts *et al.*, “A Framework for Three-Dimensional Mesoscale Modeling of Anisotropic Swelling and Mechanical Deformation in Lithium-Ion Electrodes”, J. Electrochem. Soc. (2015) 10.1149/2.0081411jes
- Mendoza *et al.*, “Mechanical and Electrochemical Response of a LiCoO<sub>2</sub> Cathode using Reconstructed Microstructures,” Electrochim. Acta (2016) 10.1016/j.electacta.2015.12.224
- Roberts *et al.*, “Insights into lithium-ion battery degradation and safety mechanisms from mesoscale simulations using experimentally-reconstructed mesostructures,” J. Electrochem. En. Conv. Stor. (2016) 10.1115/1.4034410
- Trembacki *et al.*, “Mesoscale Effective Property Simulations Incorporating Conductive Binder,” J. Electrochem. Soc. (2017) 10.1149/2.0601711jes
- Roberts *et al.*, “A verified conformal decomposition finite element method for implicit, many-material geometries,” J. Comp. Phys (2018) 10.1016/j.jcp.2018.08.022
- Trembacki *et al.*, “Mesoscale Analysis of Conductive Binder Domain Morphology in Lithium-Ion Battery Electrodes,” J. Electrochem. Soc. (2018) 10.1149/2.0981813jes

## Data

- V. Wood Group – ETH Zurich
- S. Thiele Group – U. Freiburg
- L. Zhu Group – IUPUI

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- Sandia’s Laboratory Directed Research and Development (LDRD) program – 2013-2016, 2018-2021
- Computer Aided Engineering for Batteries (CAEBAT) program, DOE/EERE/VTO – 2015-2019



# Questions?

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