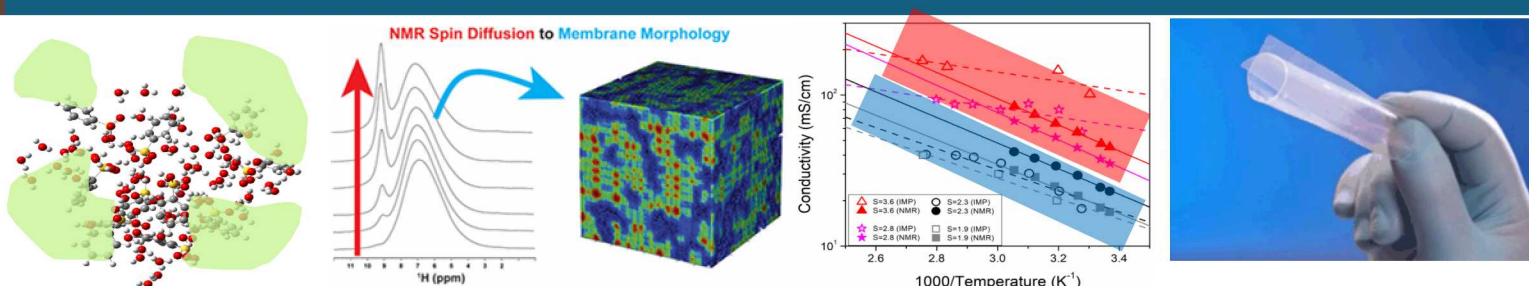
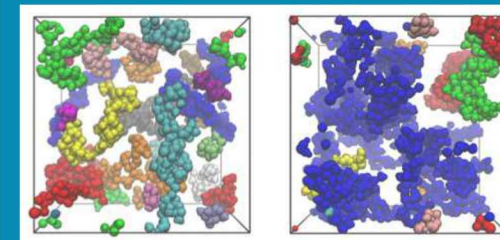


Structure and Dynamics in Sulfonated Polyphenylenes from Atomistic and Coarse-Grained Simulations



Amalie L. Frischknecht

2018 AIChE Annual Meeting
October 31, 2018



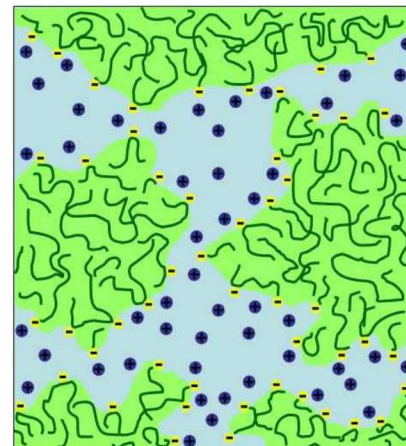
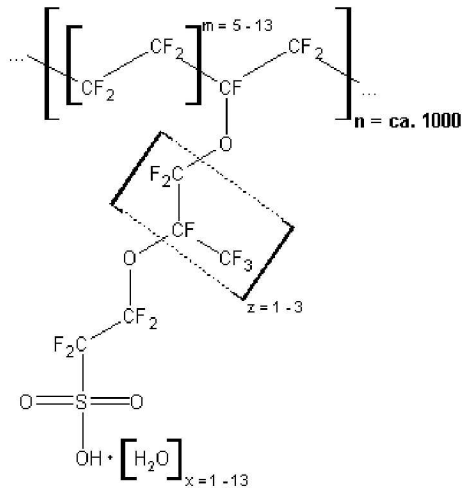
Sandia National Laboratories is a multimission laboratory managed and operated by National Technology & Engineering Solutions of Sandia, LLC, a wholly owned subsidiary of Honeywell International Inc., for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA0003525.

Proton Exchange Membranes (PEMs)

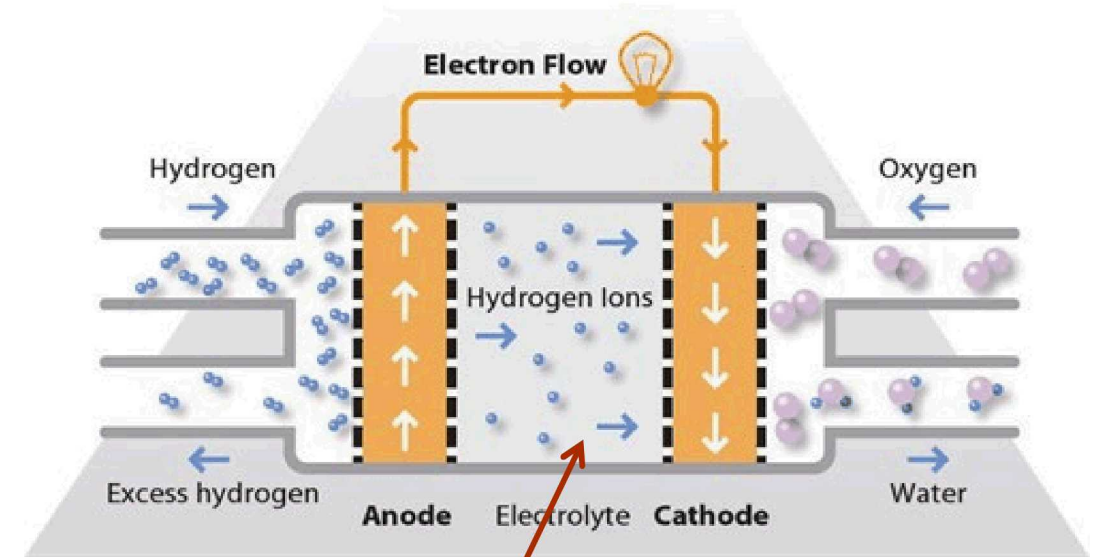
ion-selective membranes
typically in water

- water purification
- fuel cells

State of the art: Nafion™



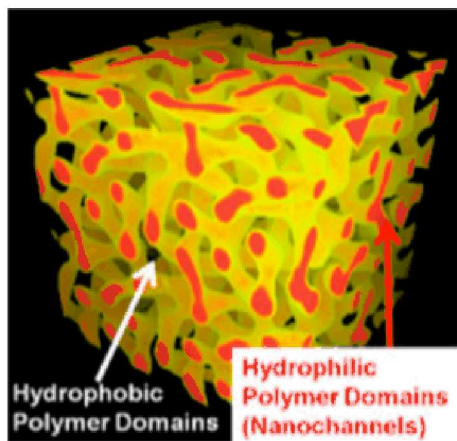
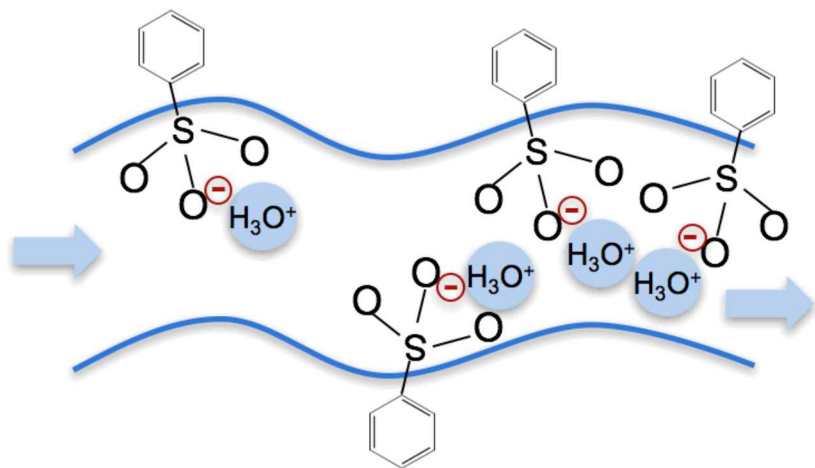
K. D. Kreuer, 2003



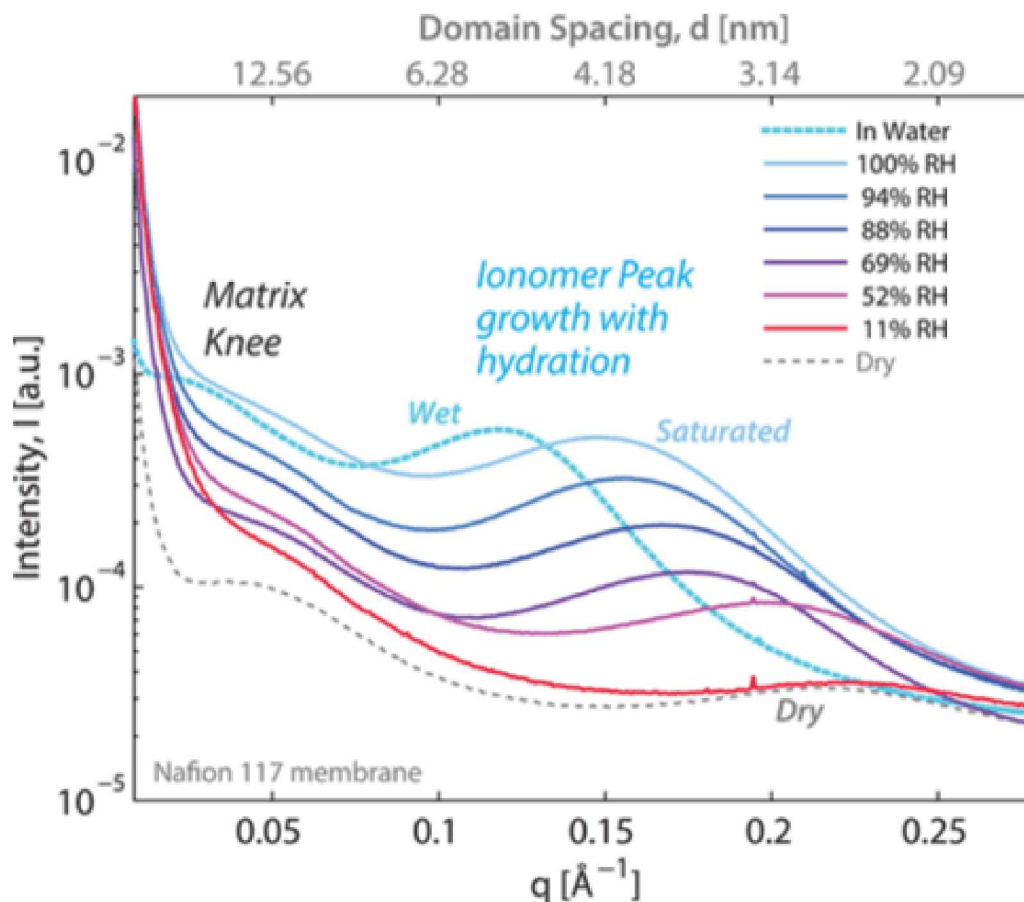
polymer membrane

Nanophase Morphology in PEMs

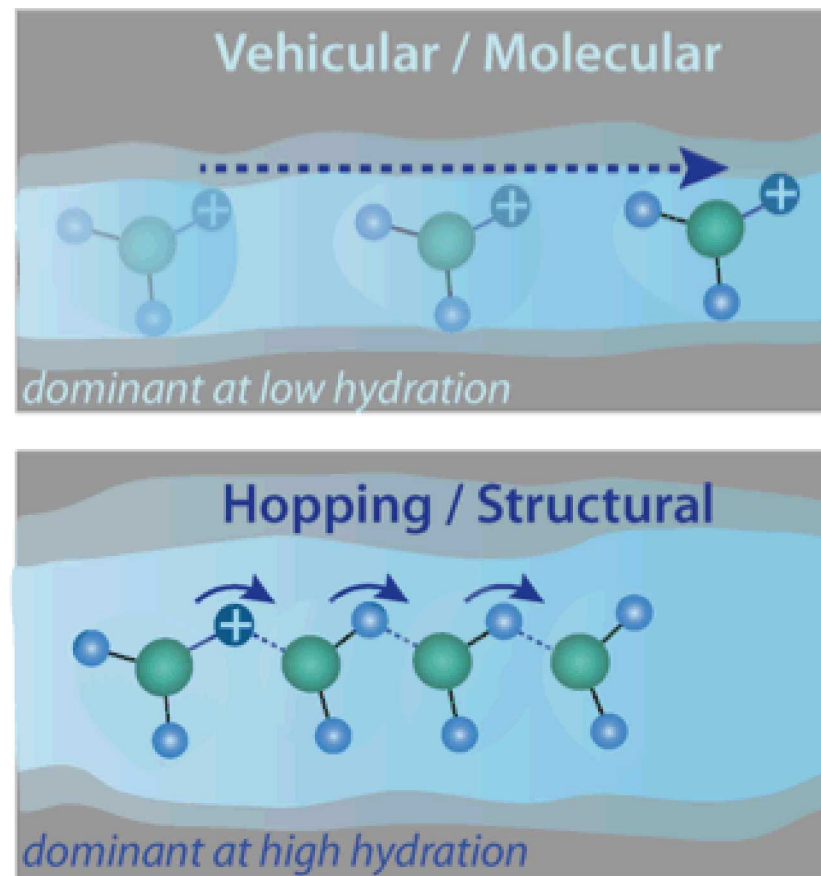
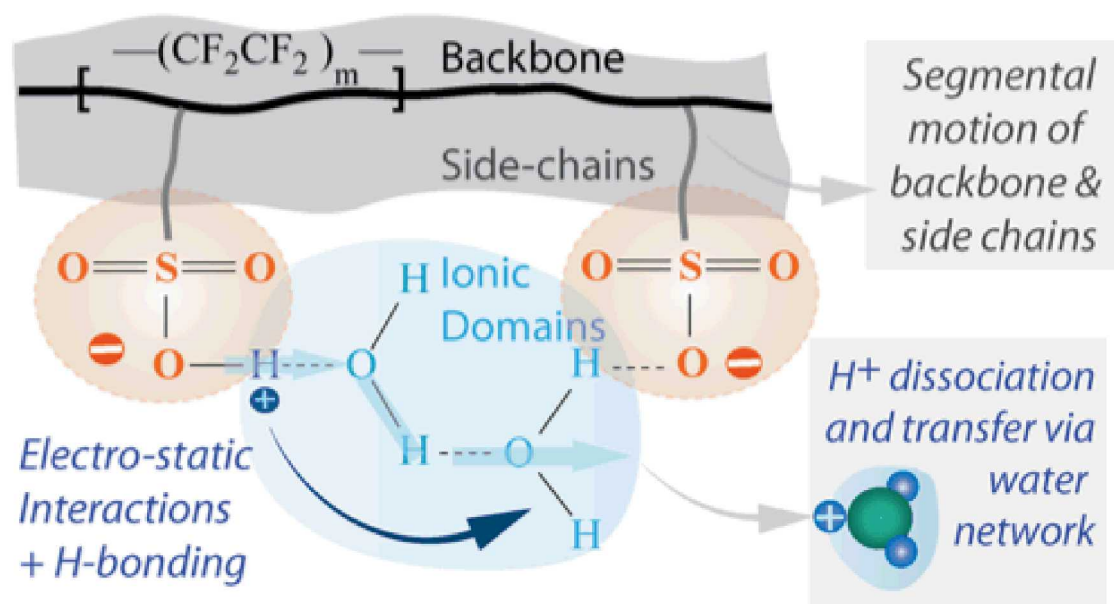
hydrated: get hydrophilic domains



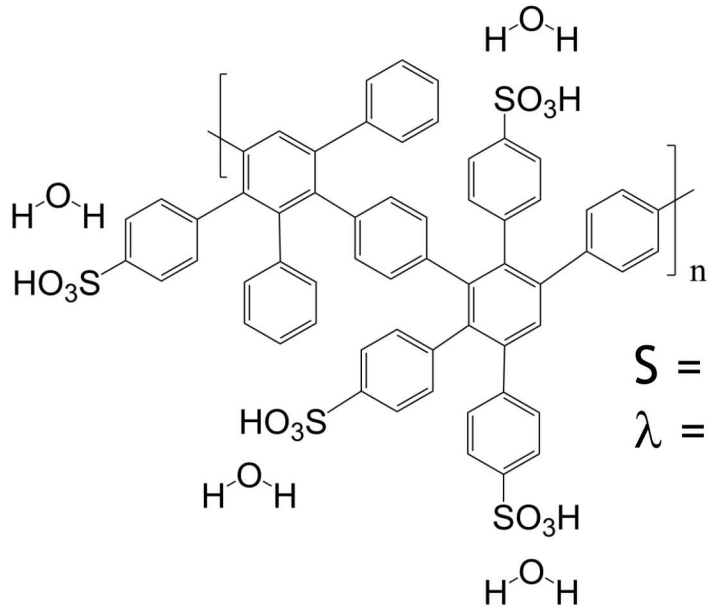
“ionomer peak” in x-ray scattering



Proton Transport Mechanisms

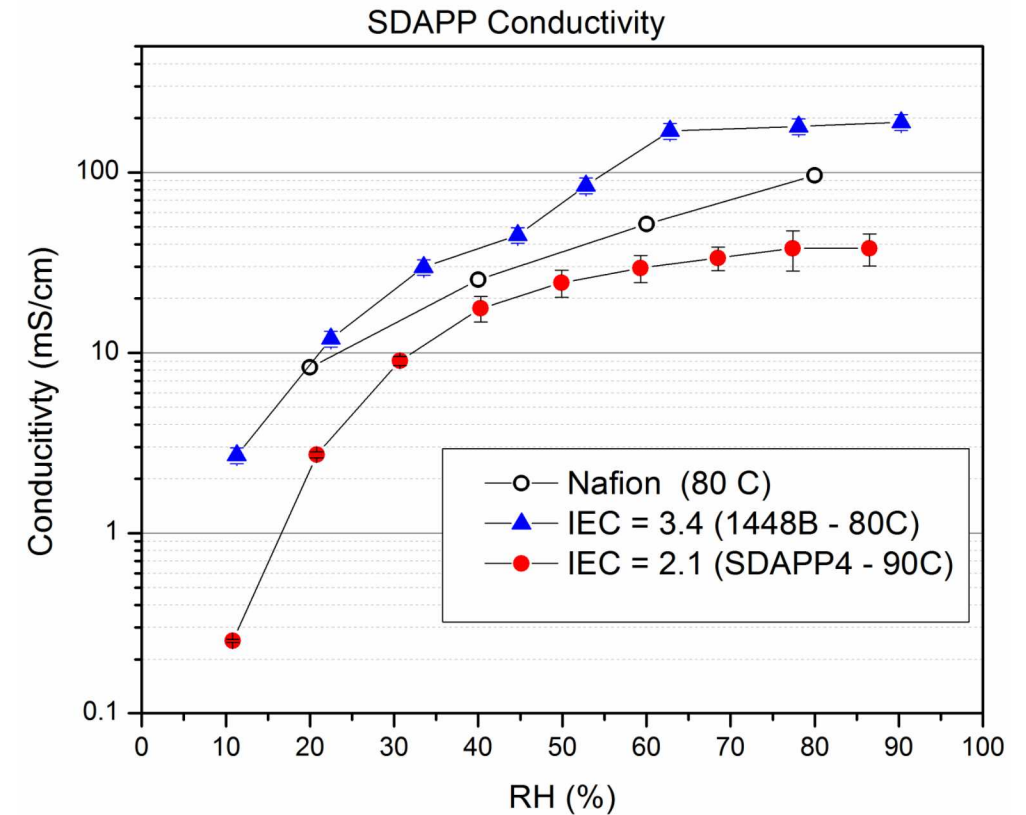


Sulfonated Diels-Alder Poly(phenylene) (SDAPP)



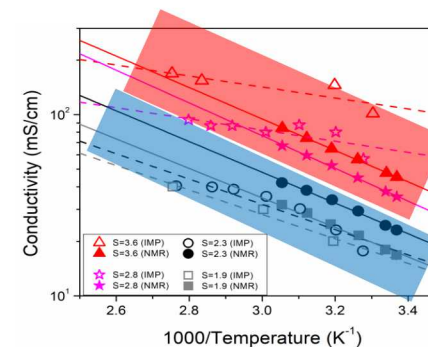
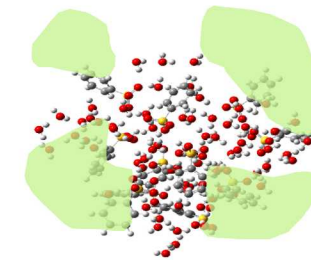
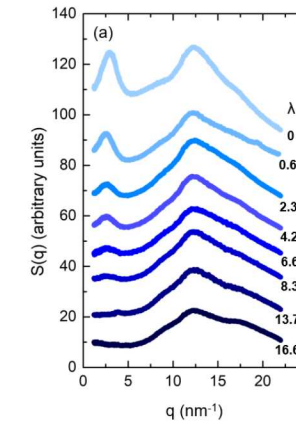
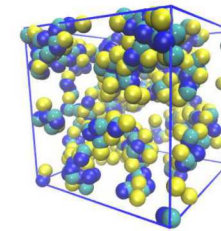
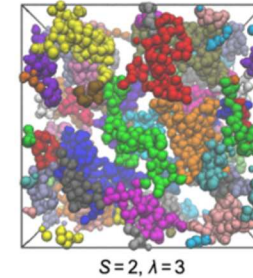
$S = \# \text{ sulfonic acids/monomer}$
 $\lambda = \# \text{ waters/sulfonic acid}$

- high T_g
- high modulus
- high thermomechanical stability
- high conductivity



what is the morphology?
 can we understand conductivity?

- atomistic MD simulations
 - clustering
 - comparison to X-ray scattering
- DPD model and simulations
- local hydrogen-bond environment
- conductivity

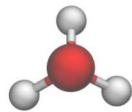
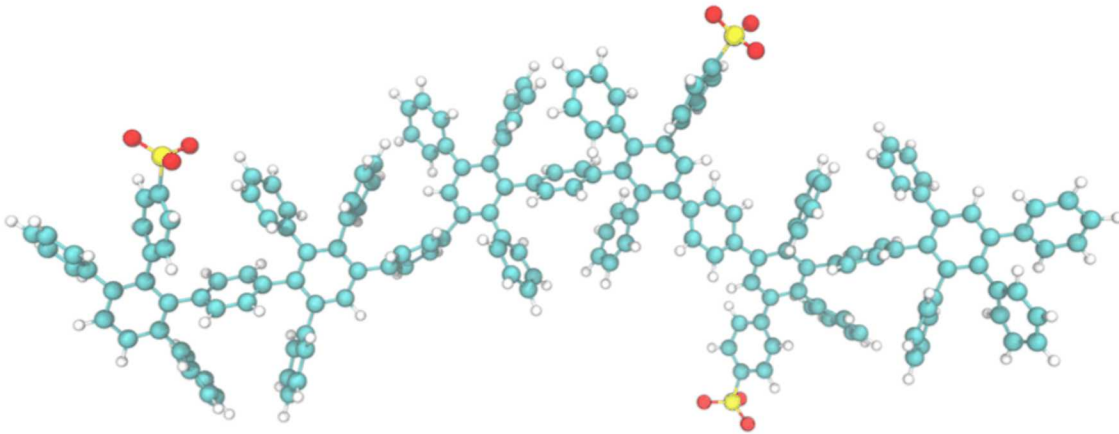


short SDAPP chain

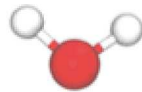
70 chains

3 monomers/chain

box size about 60Å



H_3O^+



H_2O

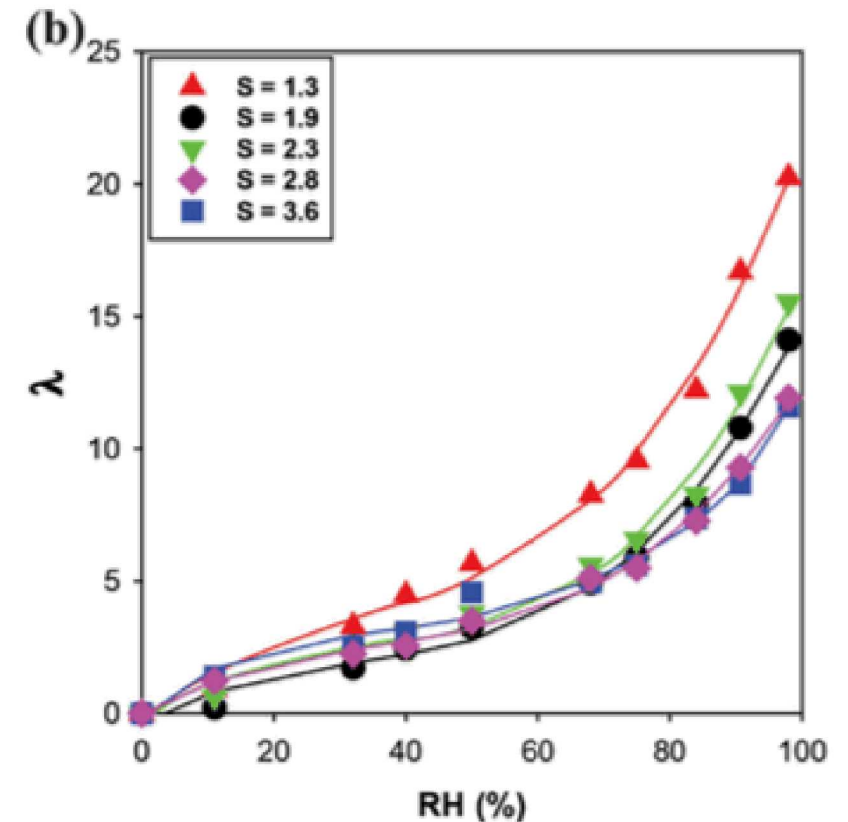
yellow = sulfur
red = oxygen
cyan = carbon
white = hydrogen

sulfonic acids/monomer:

$S = 1, 2, 4$

waters/sulfonic acid

$\lambda = 3, 5, 10, 20$



Simulation Details

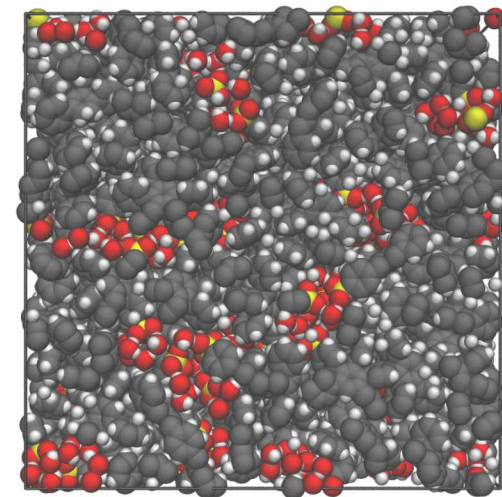
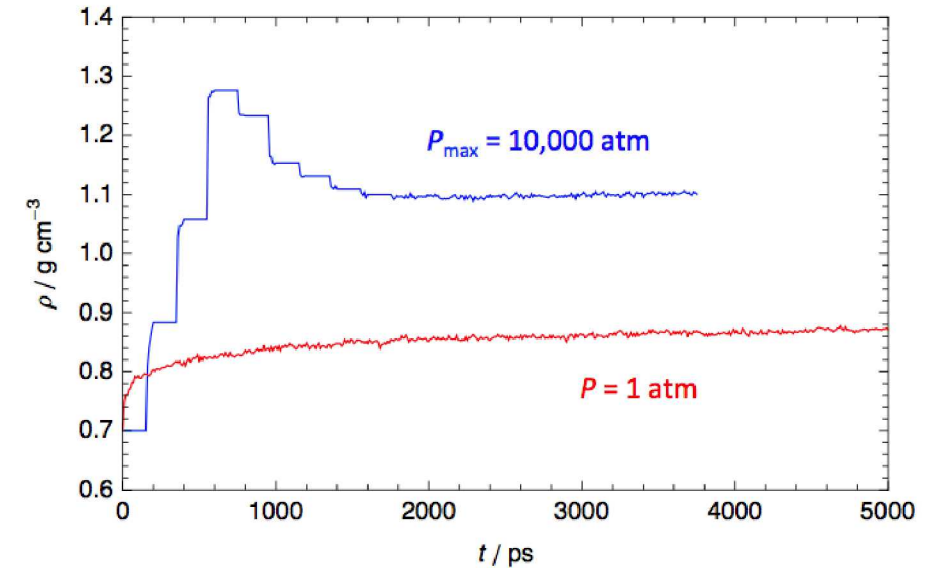
initial configurations: Monte Carlo simulation
5 boxes with different initial conditions/system

Simulation details:

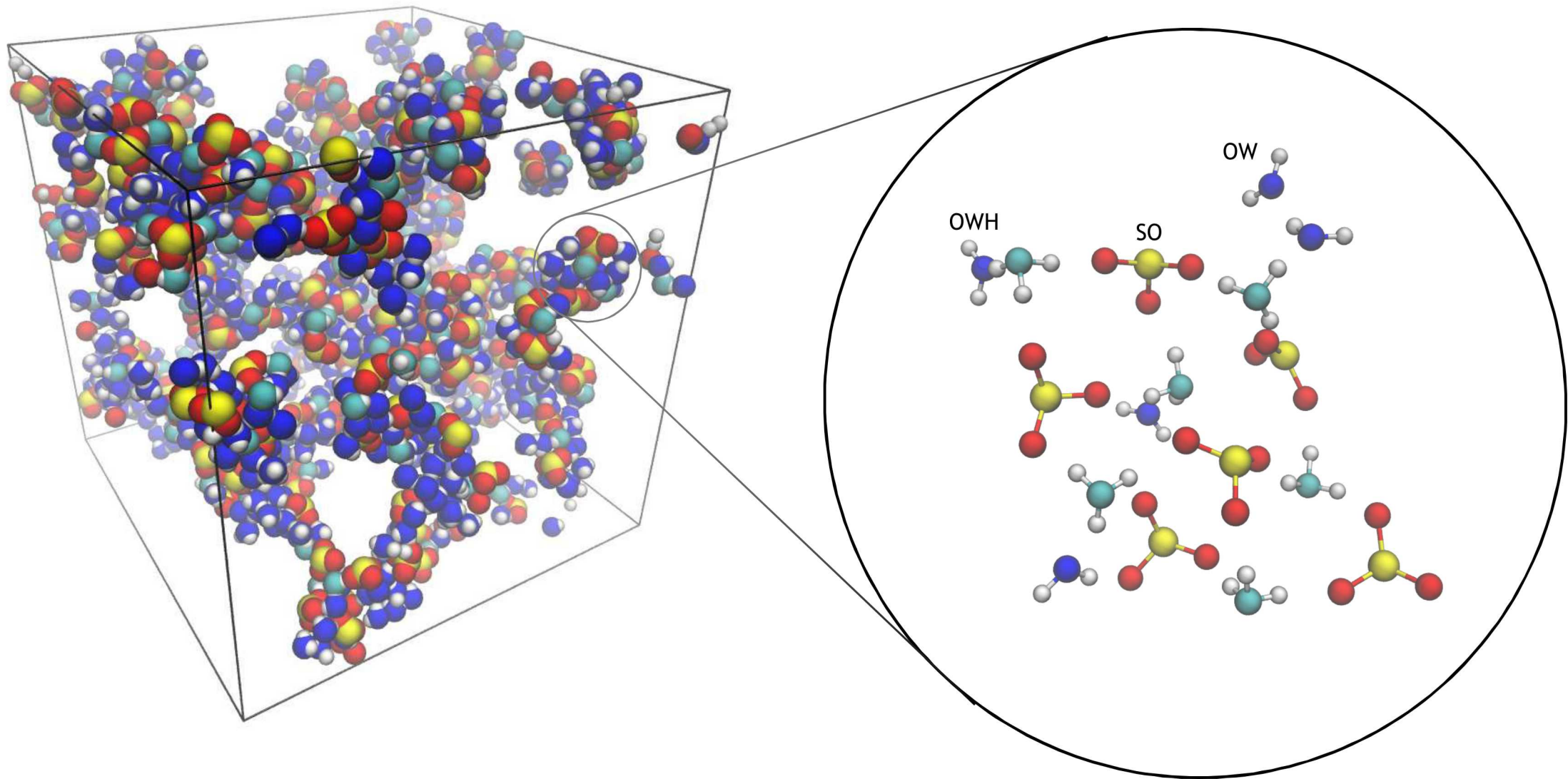
- Final box sizes of 66 to 91 Å
- OPLS force field with updates for biaryl and sulfonate
- TIP4P/2005 water model, flexible hydronium ion model
- MD simulations in LAMMPS, 1 fs timestep
- Nosé-Hoover thermostat and barostat
- 12 Å short range cutoff, long range with PPPM

final densities match experiment: $\approx 1.2 \text{ g/cm}^3$

pressure annealing



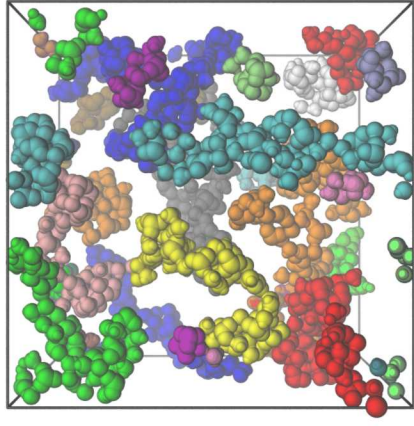
9 Ion/Water Aggregates Formed



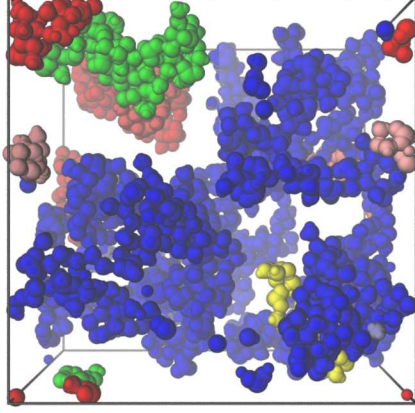
Nanoscale Morphology from MD Simulations

$S = 1$ sulfonic
acid/monomer

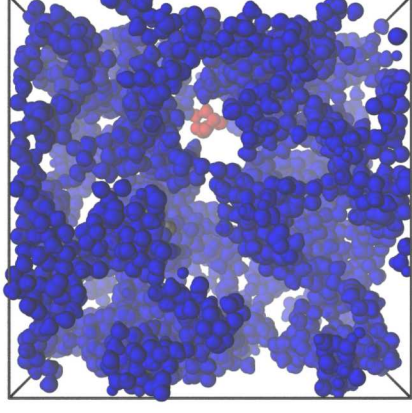
$\lambda = 3$



$\lambda = 3$

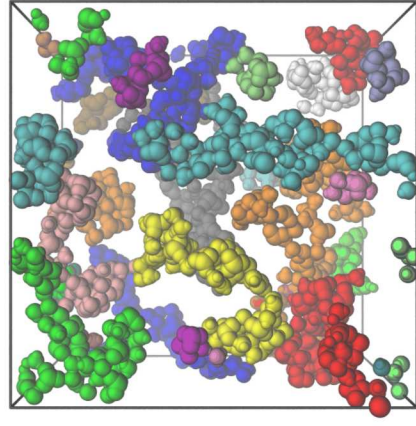


$\lambda = 5$

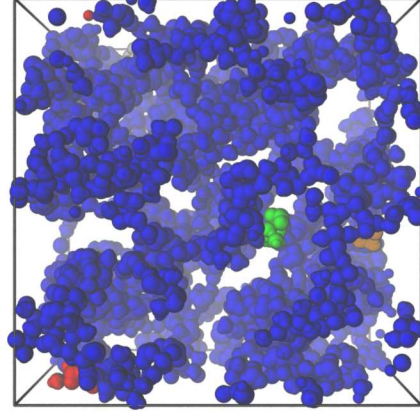


$\lambda = 10$

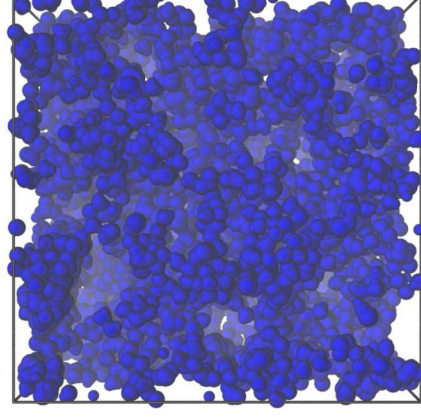
increasing water



$S = 1$



$S = 2$



$S = 4$

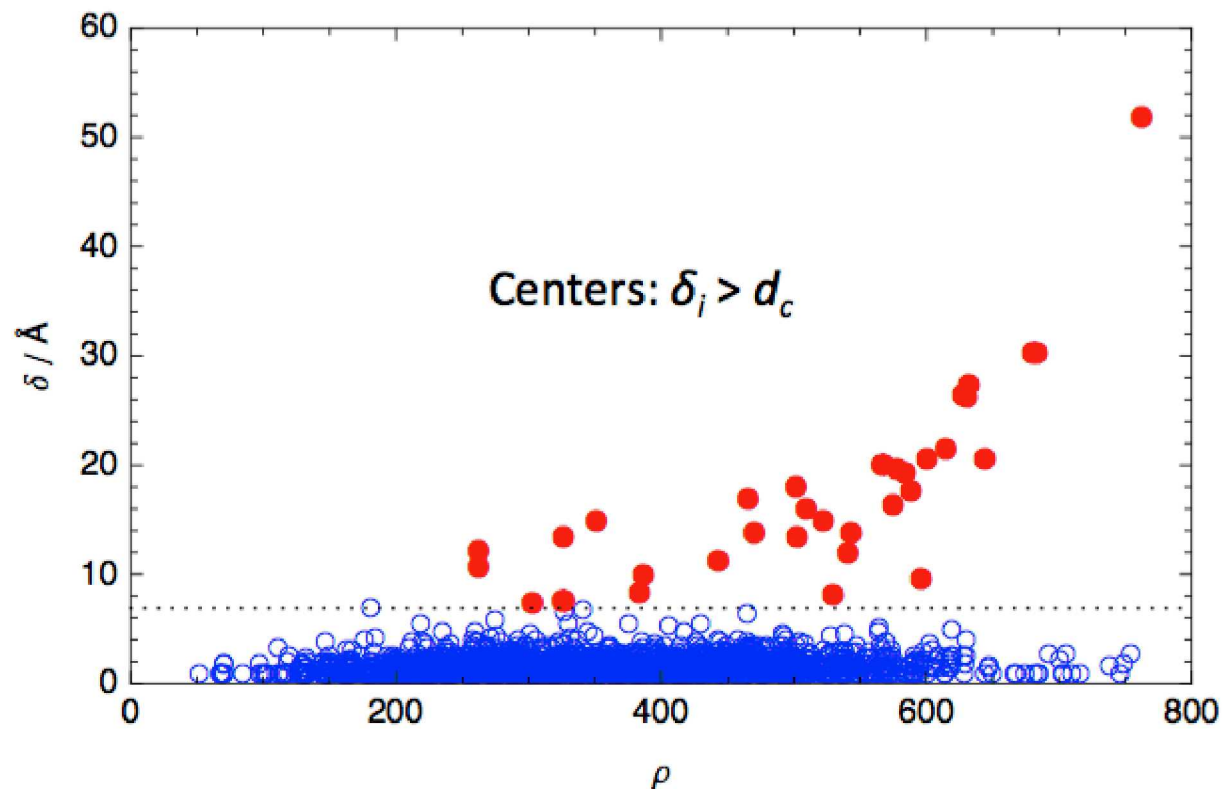
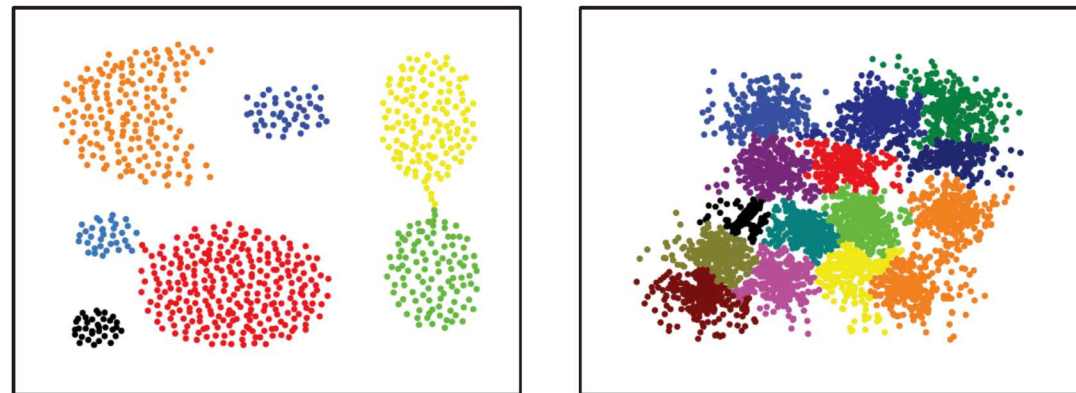
increasing sulfonation level

Density-based clustering

Algorithm:

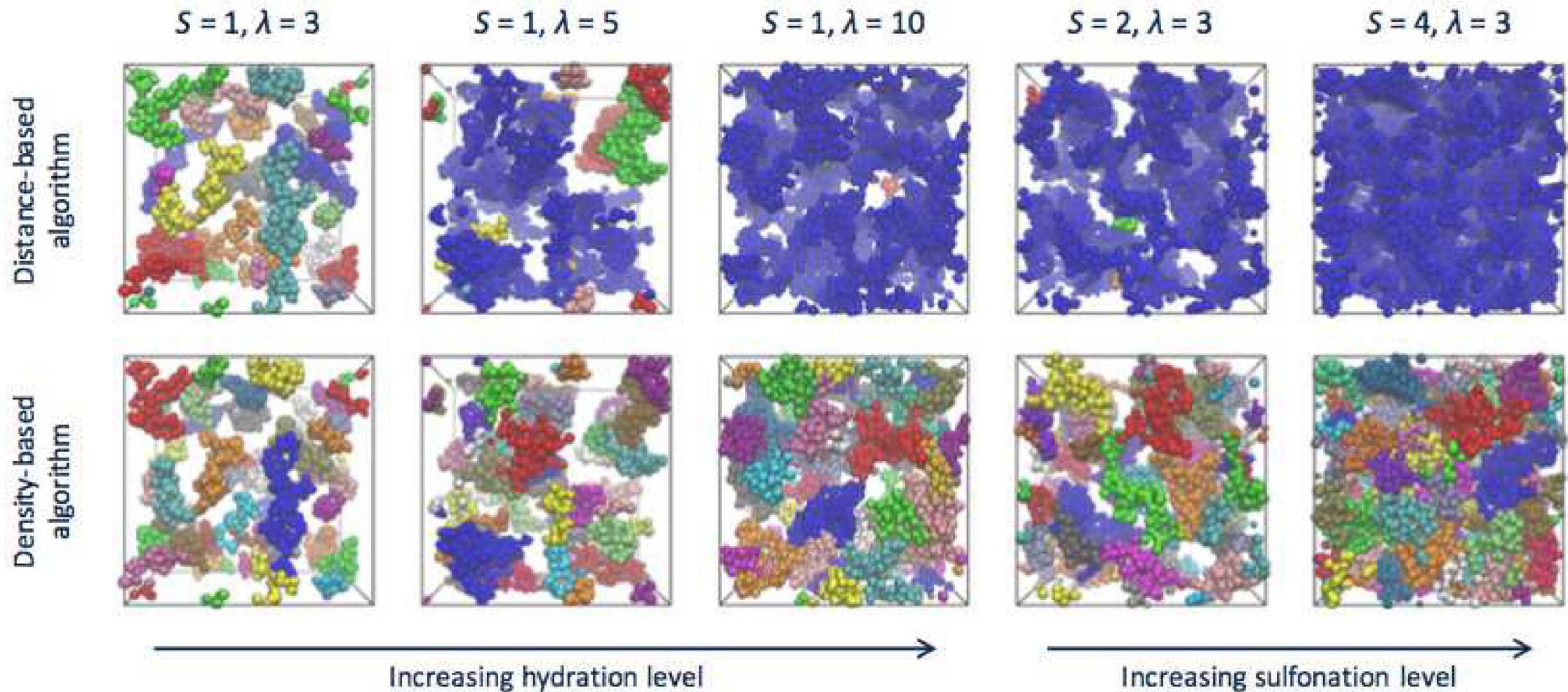
1. Each atom is assigned parameter ρ : the local density of atoms within a given cutoff distance r_c
2. Each atom is assigned parameter δ : the minimum distance from an atom of higher density
3. Cluster centers are chosen as atoms with highest density ($\delta_i > \delta_{\min}$)
4. Remaining atoms assigned to the same cluster as their nearest neighbor of higher density

Rodríguez, A., & Laio, A. (2014). Clustering by fast search and find of density peaks. *Science*, 344(6191), 1492–1496.

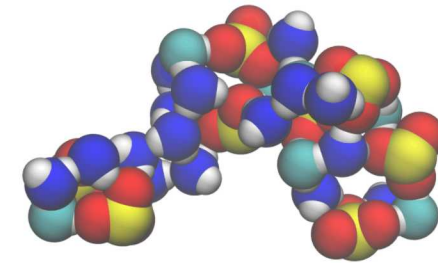
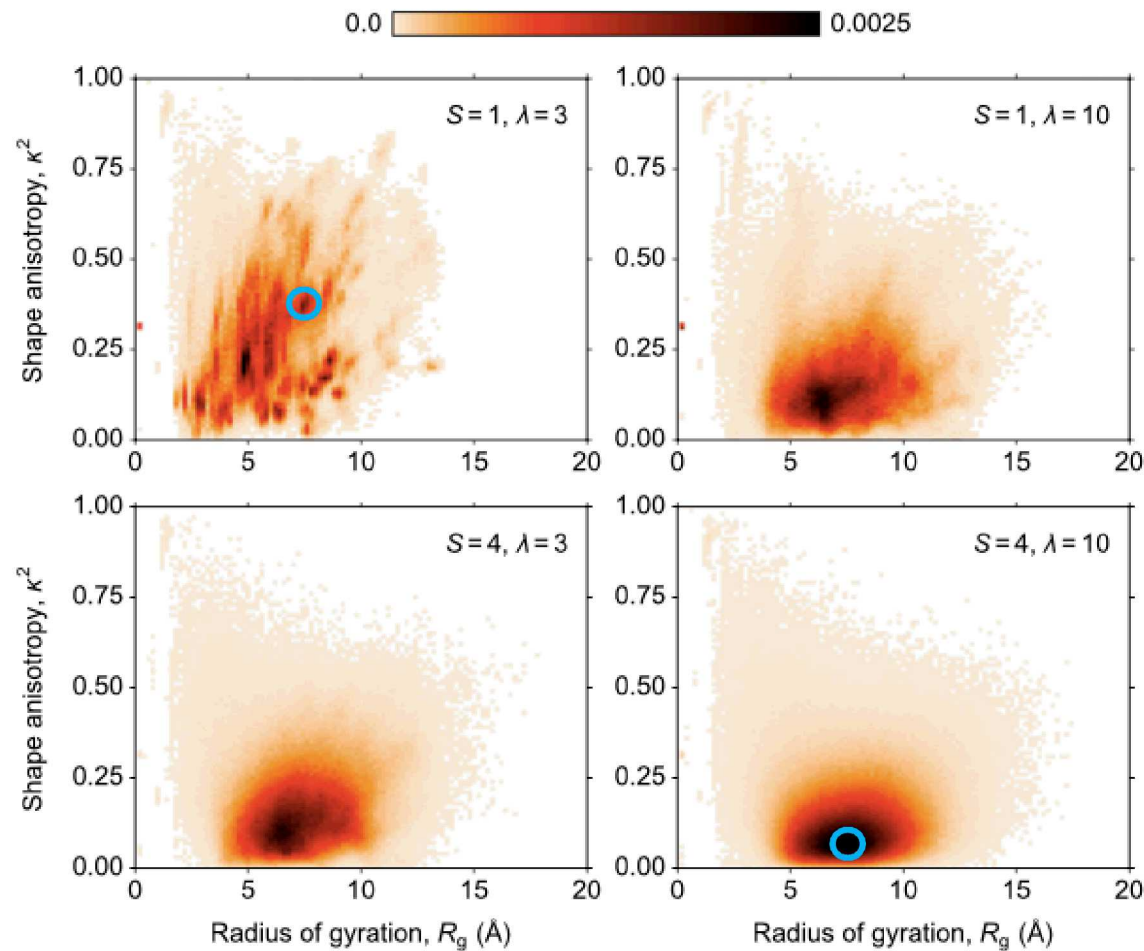


SDAPP Clusters

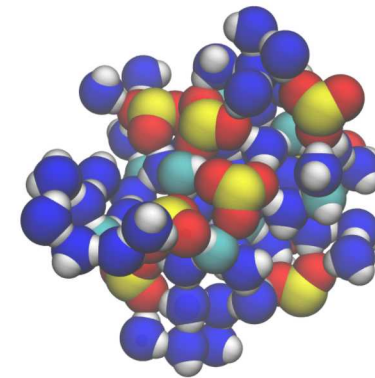
density-based algorithm resolves differences in percolated systems



$$R_g^2 = \lambda_1 + \lambda_2 + \lambda_3 \quad \kappa^2 = 1 - 3(\lambda_1\lambda_2 + \lambda_1\lambda_3 + \lambda_2\lambda_3)/R_g^4$$

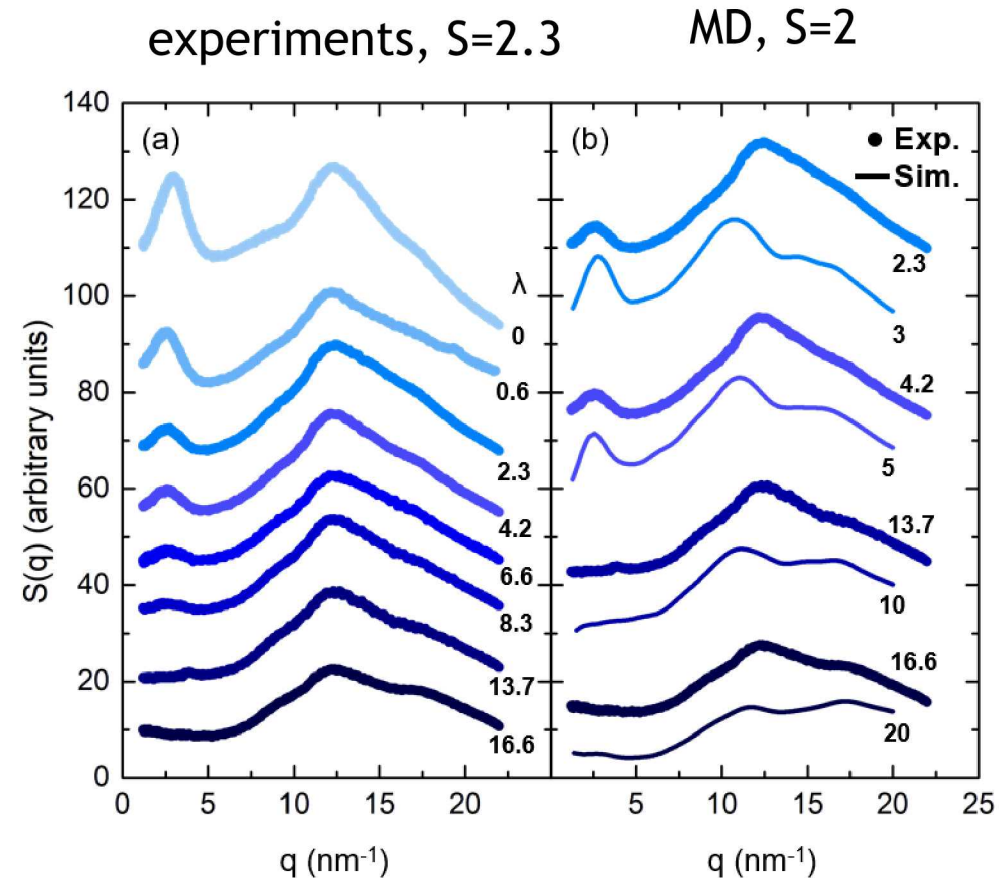
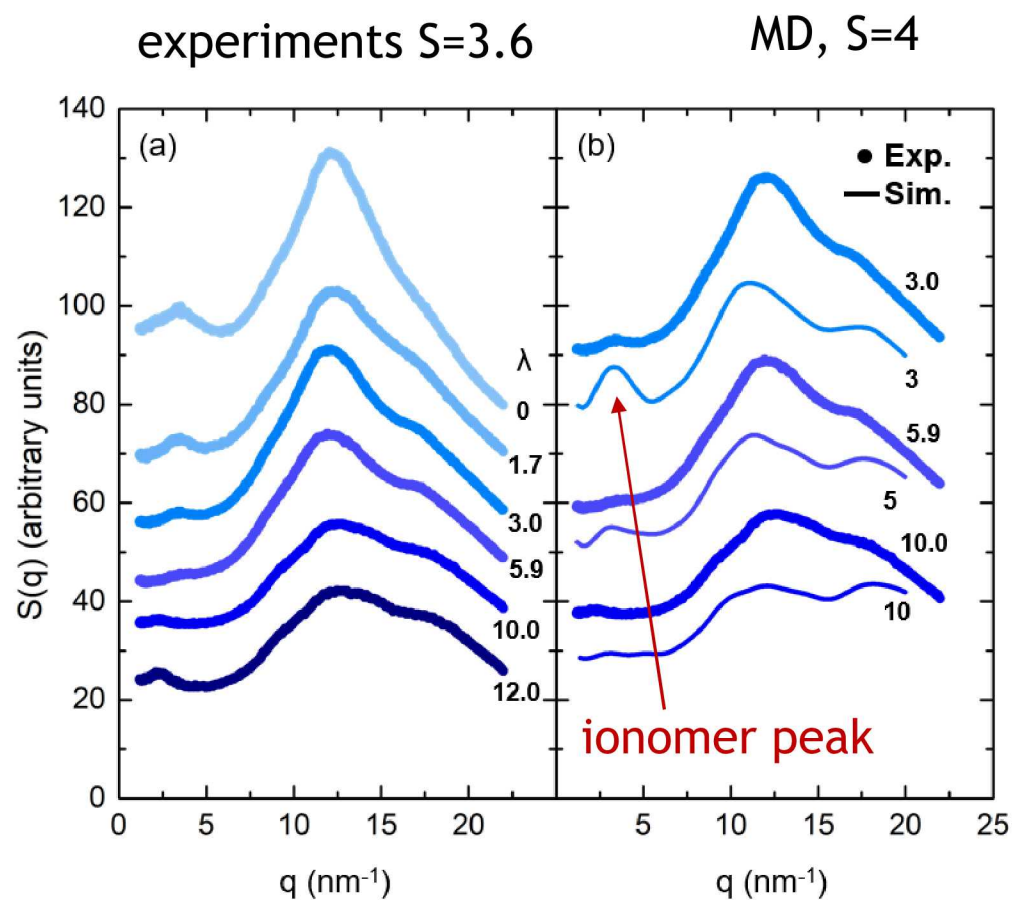


$$S = 1, \lambda = 3, \kappa^2 = 0.4$$



$$S = 4, \lambda = 10, \kappa^2 = 0.05$$

X-Ray Scattering from SDAPP

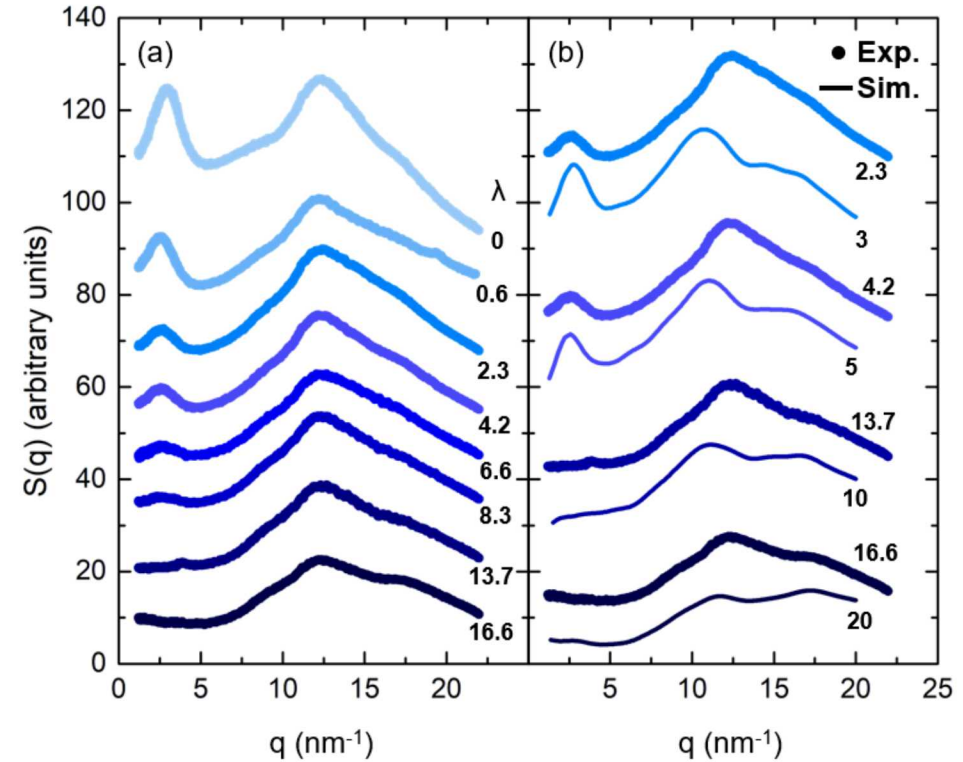
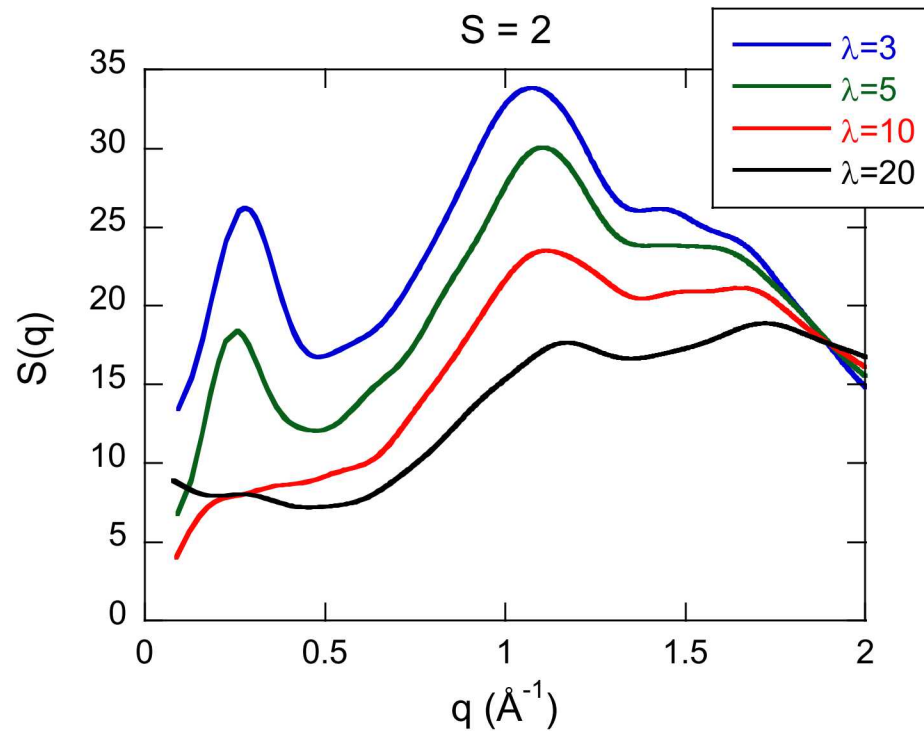


$$S(q) = \sum_i c_i f_i^2 + 4\pi\rho \int_0^\infty \frac{\sin(qr)}{qr} r^2 \sum_{i,j} c_i c_j f_i f_j (g_{ij}(r) - 1) dr$$

f_i = known x-ray atomic scattering function for each atom

Why Does the Ionomer Peak Disappear?

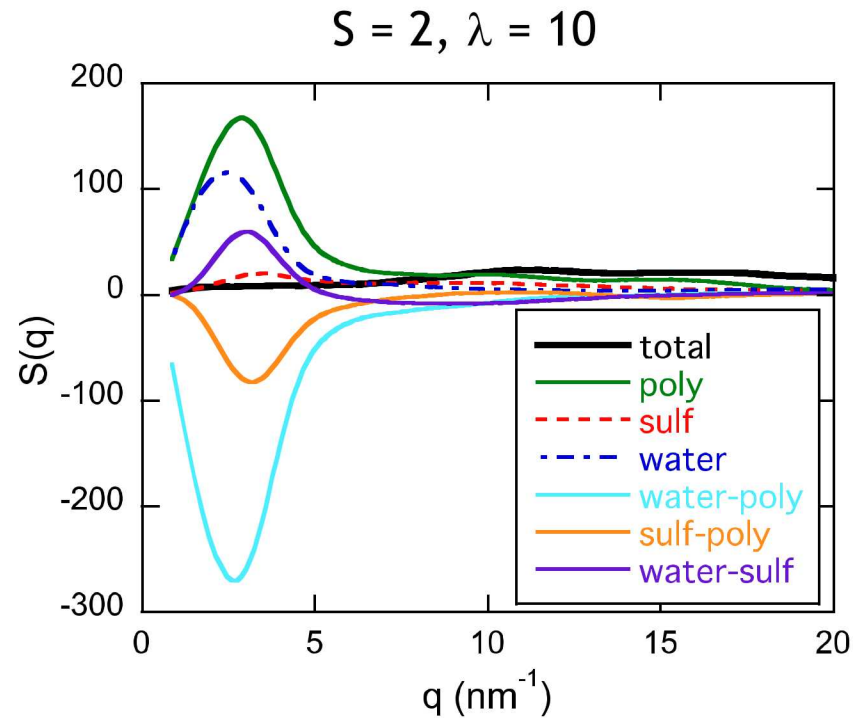
total $S(q)$



does this mean the water and sulfonic acids are no longer phase segregated?

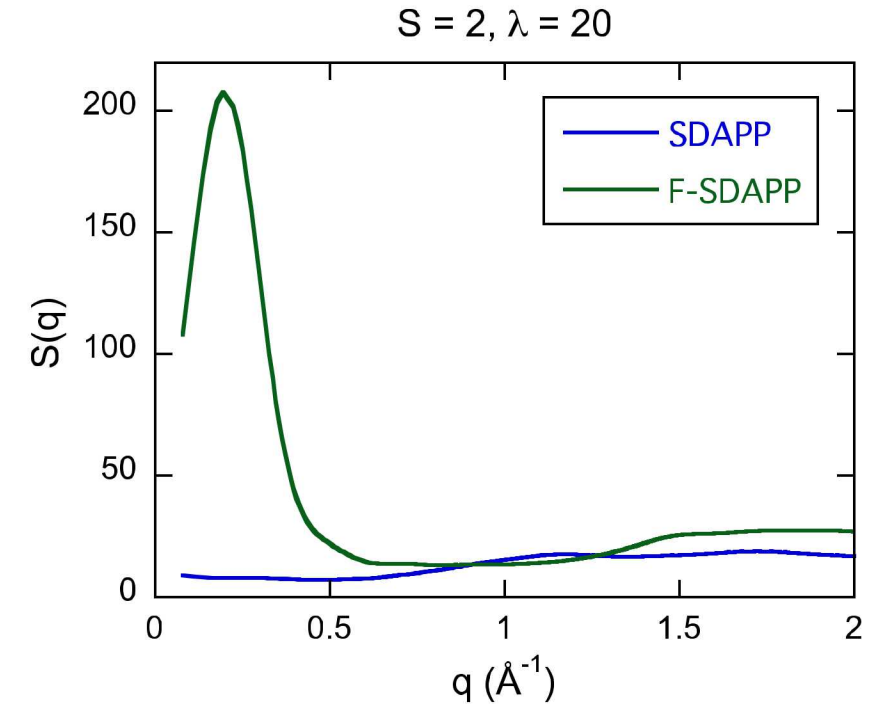
Further Understanding $S(q)$

$$S_{\text{total}} = S_{\text{polymer}} + S_{\text{sulfonic}} + S_{\text{water}} + S_{\text{water-poly}} + S_{\text{sulf-poly}} + S_{\text{water-sulf}}$$



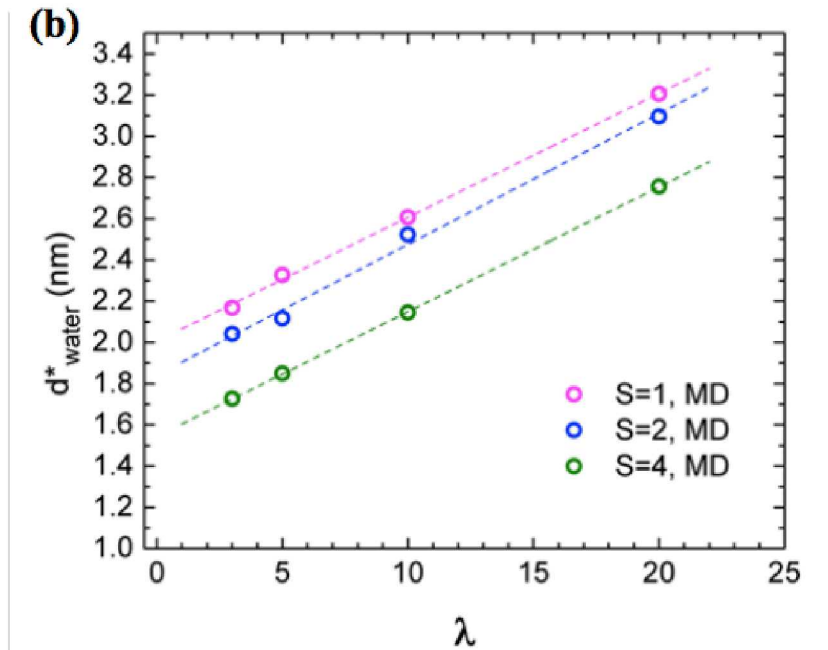
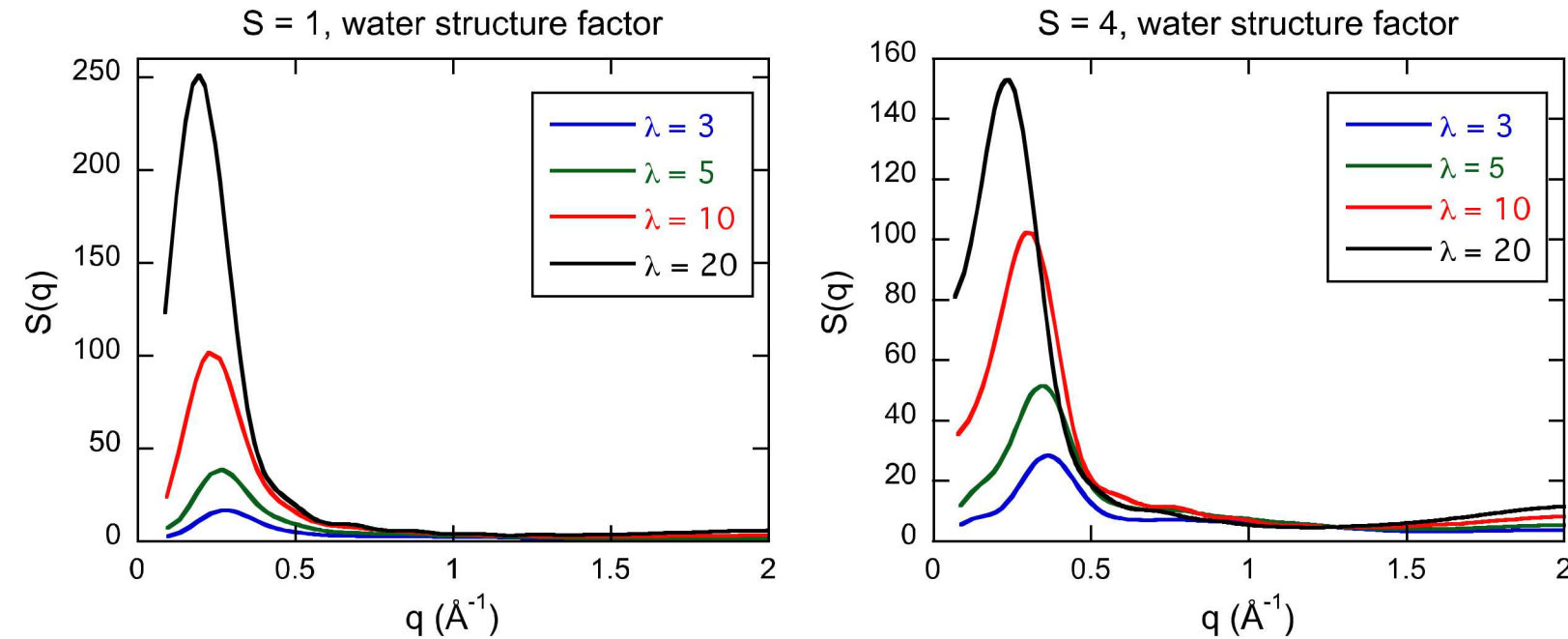
water-polymer cross-correlations cancel other peaks

what if SDAPP was fluorinated?



large ionomer peak!

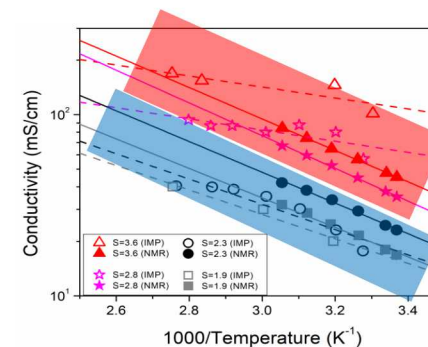
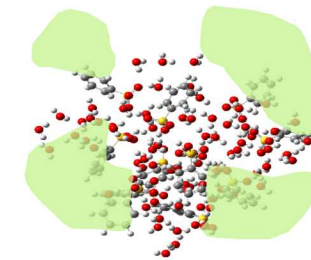
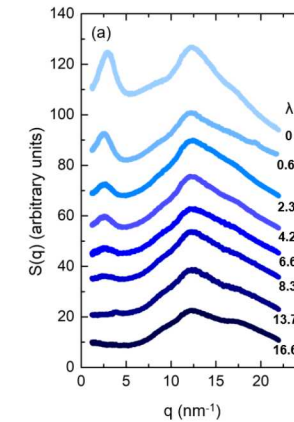
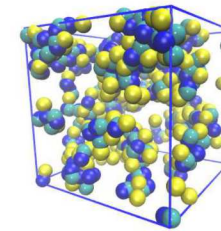
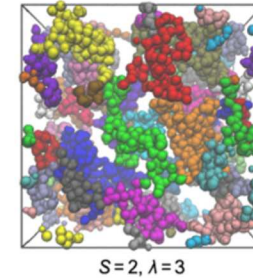
in hydrocarbon PEMs, loss of scattering contrast leads to loss of ionomer peak
still have nanoscale phase separation!



- water peak increases in intensity with increasing λ
- shifts slightly to the left (lower q , larger domains)

Rest of the Talk

- atomistic MD simulations
 - clustering
 - comparison to X-ray scattering
- DPD model and simulations
- local hydrogen-bond environment
- conductivity

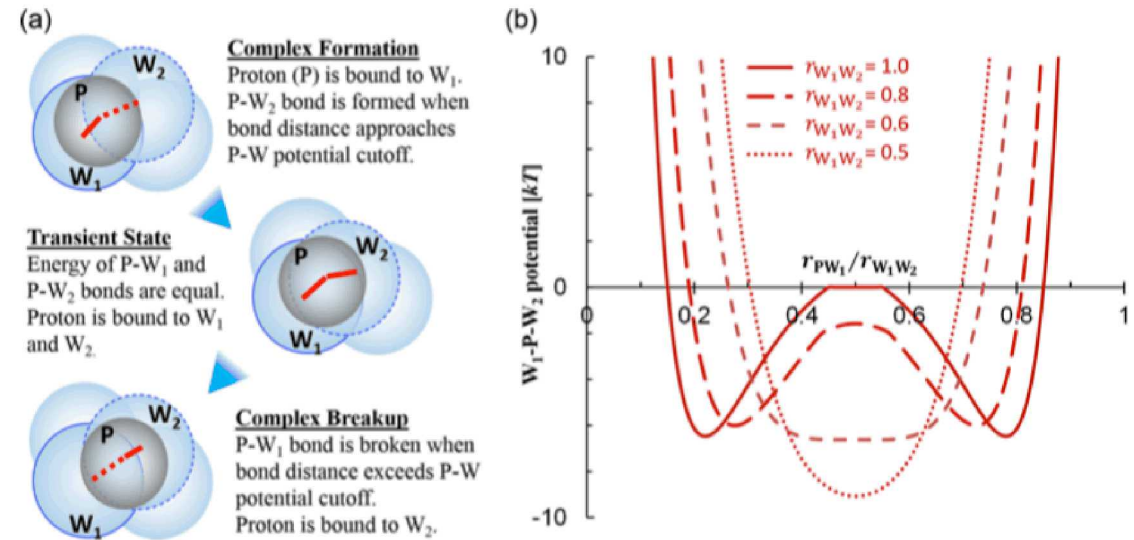
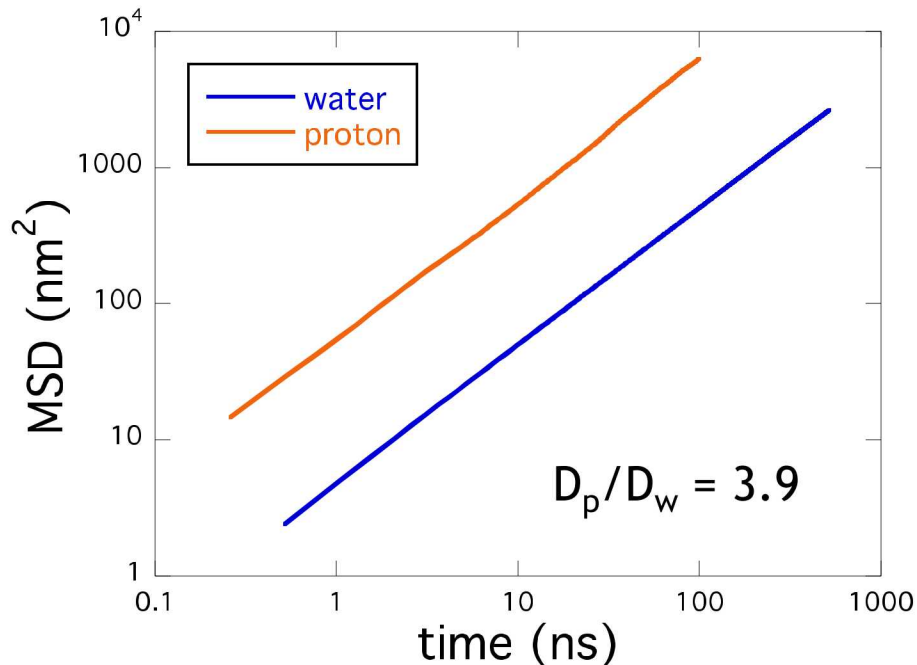


DPD Model for Protons in Water

based on work of Neimark et al

Morse bonds between protons and water

$$U_{ij}^{(M)}(r_{ij}) = K_{IJ}\{1 - \exp[\alpha_{IJ}(r_{ij} - r_{ij}^0)]\}^2 - K_{IJ}\{1 - \exp[\alpha_{IJ}(r_{ij}^M - r_{ij}^0)]\}^2$$



Lee, M.-T., Vishnyakov, A. & Neimark, A. V. *J Chem Theory Comput* **11**, 4395–4403 (2015)

3 water molecules/water bead
 proton mass 1
 water mass 54

$R_c = 6.65 \text{ \AA}$
 DPD $\tau = 10.8 \text{ ps}$

Experimental $D_p/D_w = 3.8$

DPD Model of SDAPP

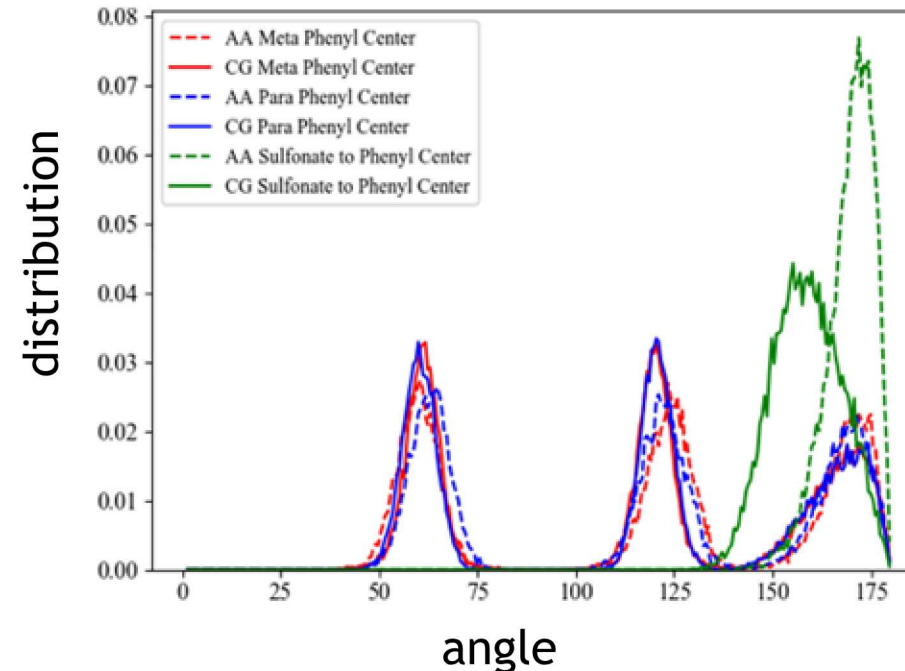
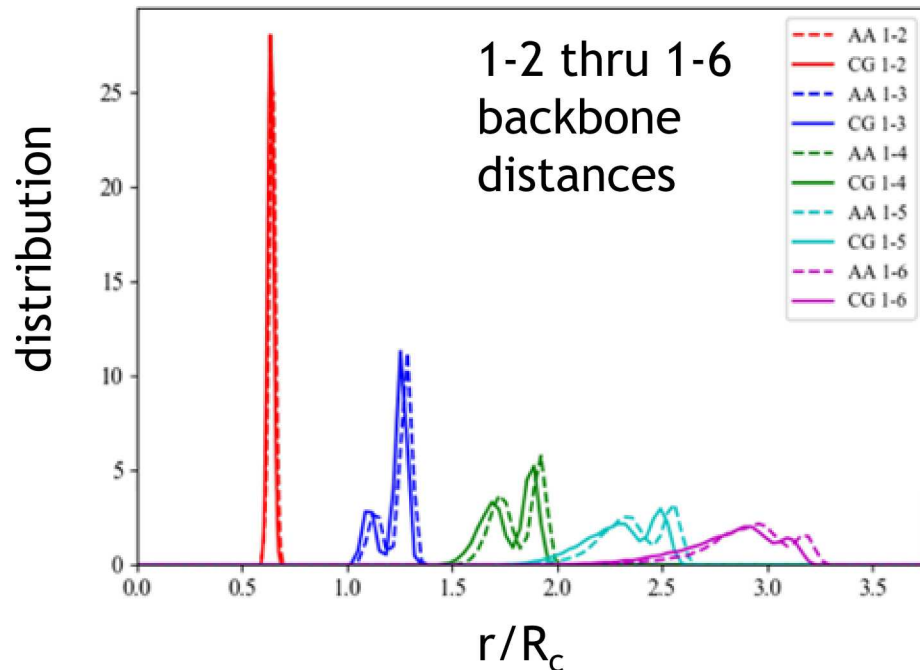
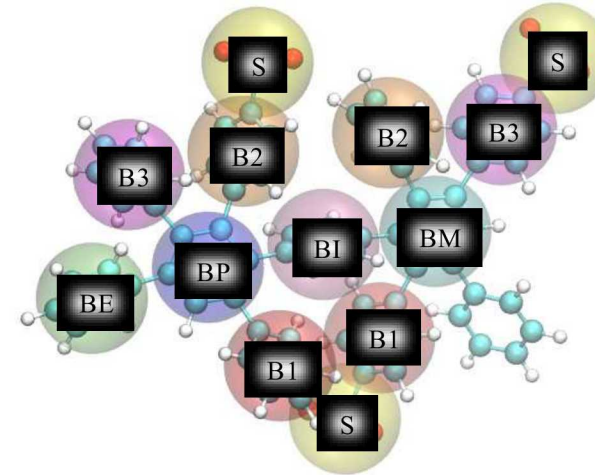
DPD forces

harmonic bonds, angles

smear charges for electrostatics

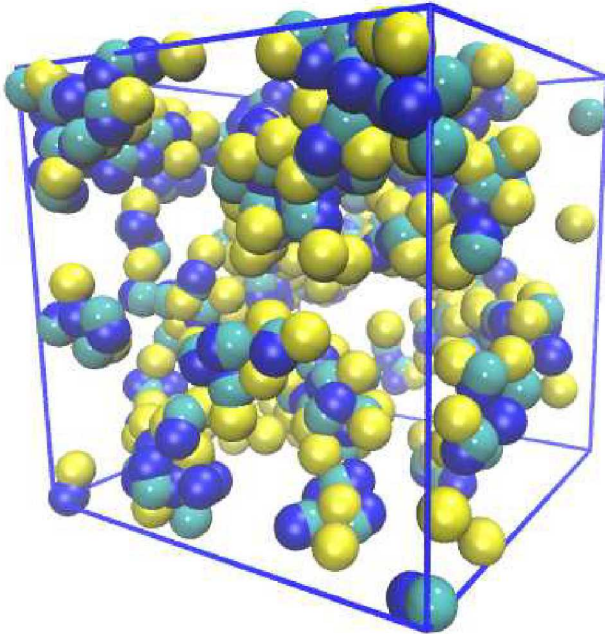
Morse bond for protons

Use inverse Boltzmann inversion to fit bonds, angles from atomistic simulations

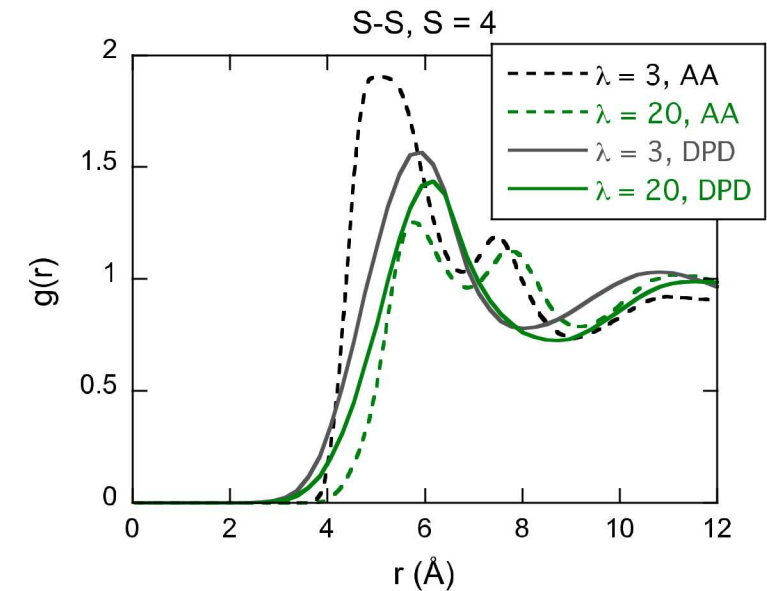
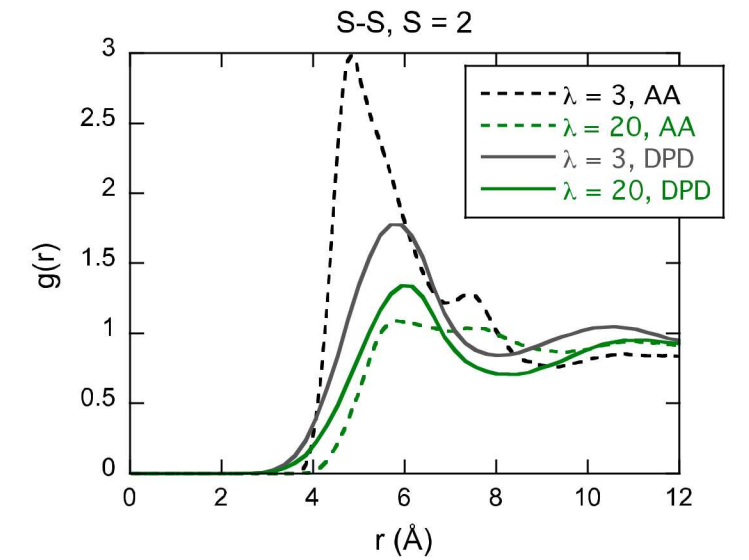
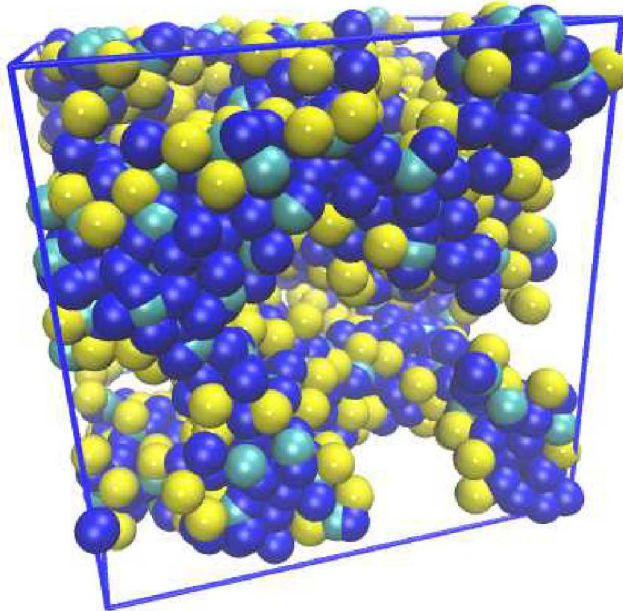


DPD Captures Structure and Morphology

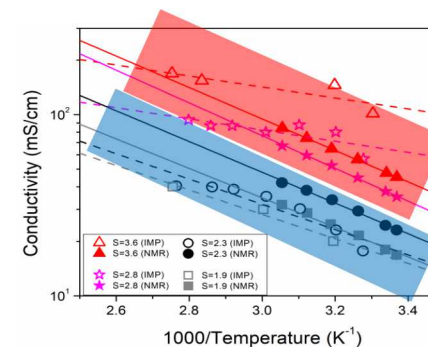
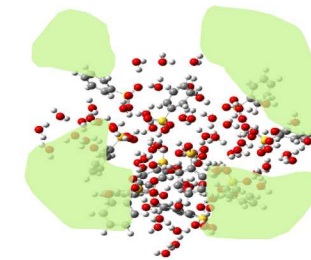
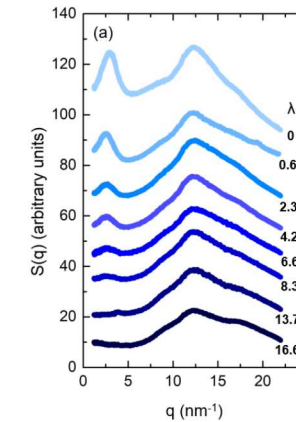
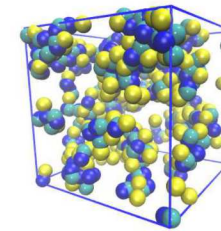
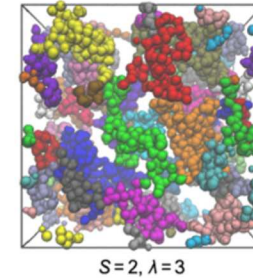
$S = 1, W = 3$



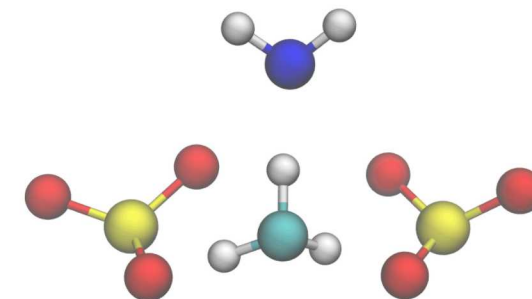
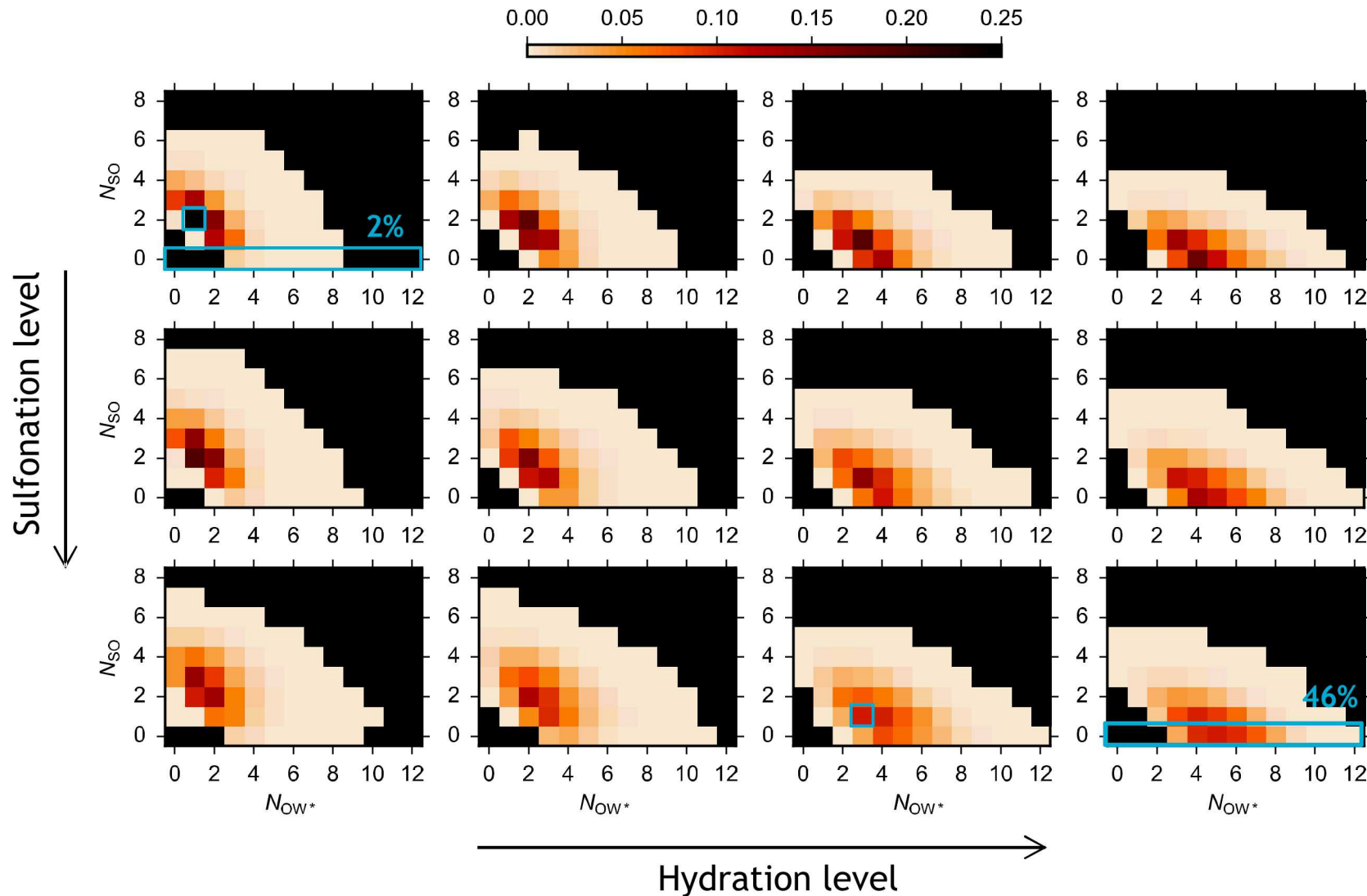
$S = 2, W = 9$



- atomistic MD simulations
 - clustering
 - comparison to X-ray scattering
- DPD model and simulations
- local hydrogen-bond environment
- conductivity

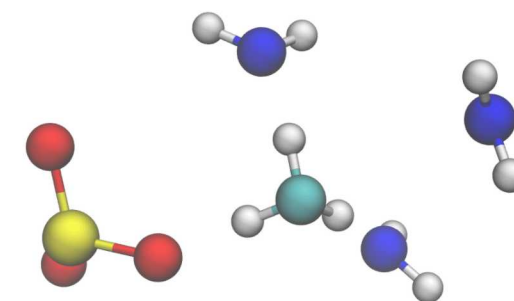


Hydronium Ion Coordination from MD



$$N_{OW^*} = 1, N_{SO} = 2$$

(25%)

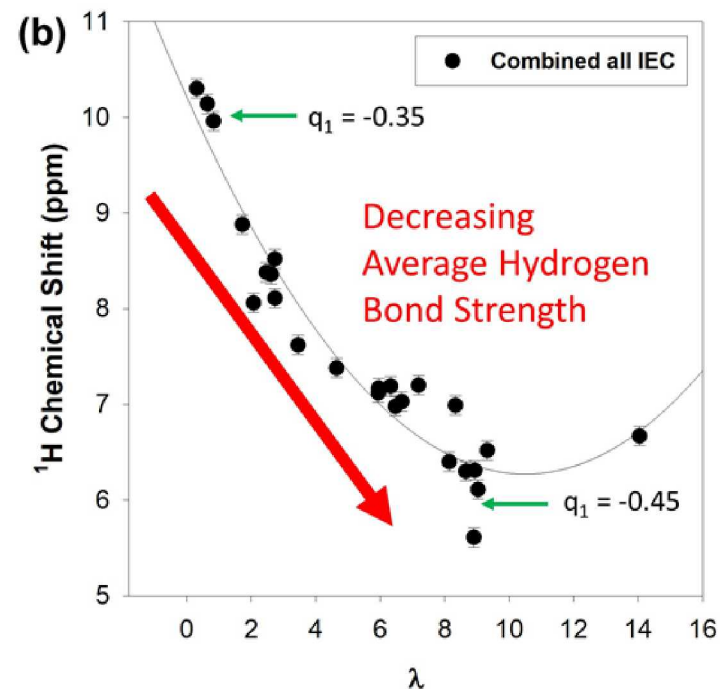
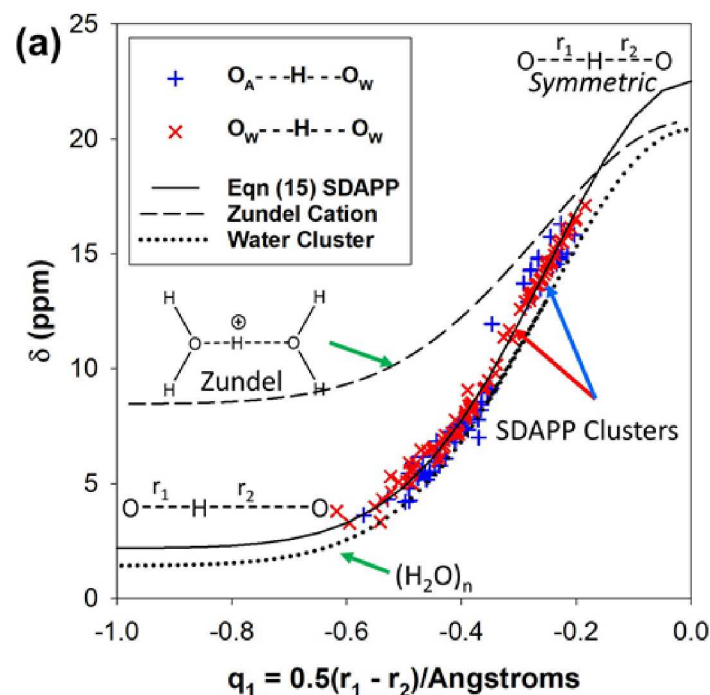
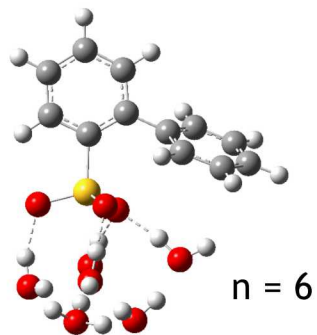
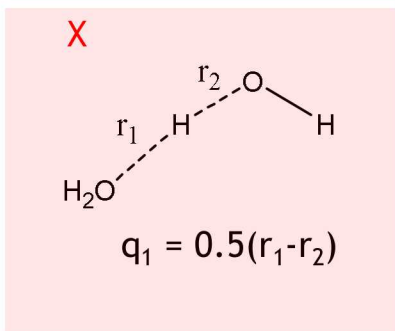
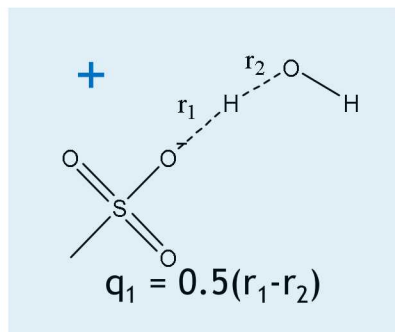


$$N_{OW^*} = 3, N_{SO} = 1$$

(11%)

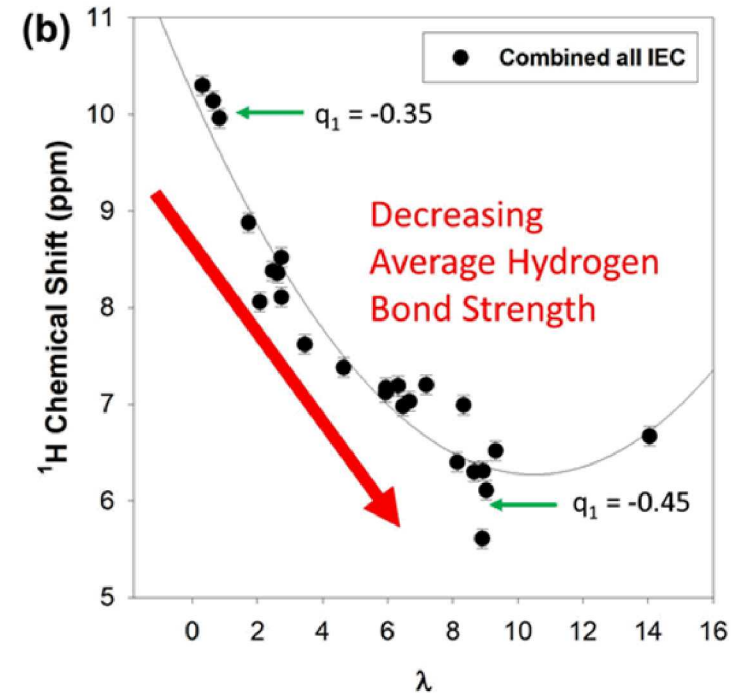
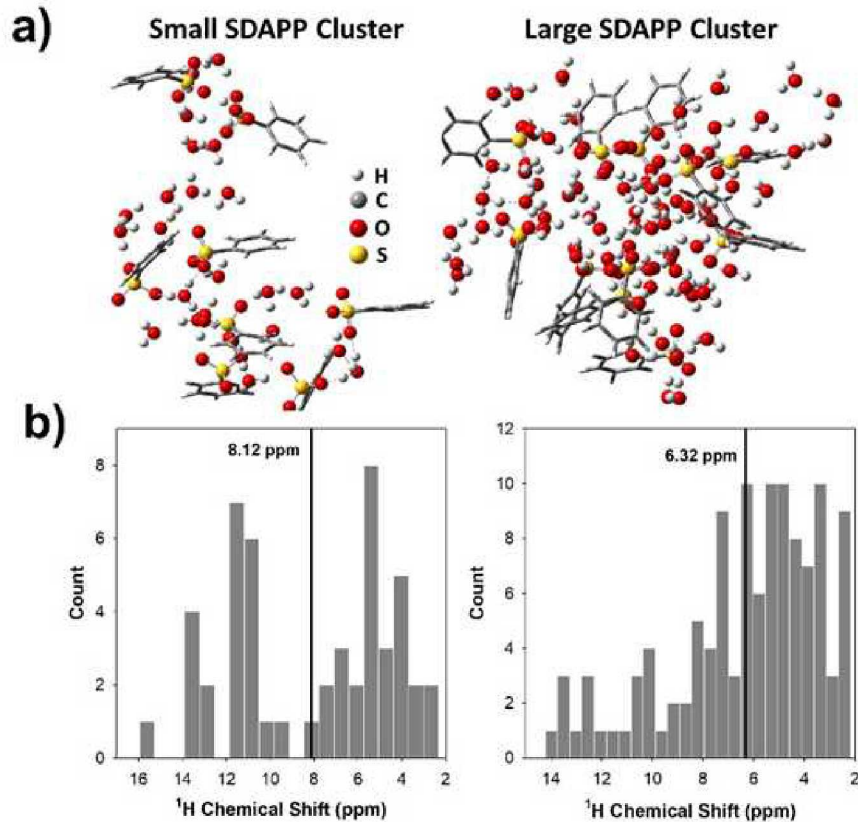
N_{SO} = number of SO_3 groups in first solvation shell of H_3O^+
 N_{OW^*} = number of H_2O and H_3O^+ in first solvation shell of H_3O^+

Local Hydrogen Bond Environment in SDAPP



- Correlations follow definition of Limbach et al $\delta(^1\text{H}) = a + b \exp[-cq_1^2]$
- Experiments are a dynamic average over all H environments
- Measure of the changing *average* hydrogen bond strengths with hydration
- Reduction in hydrogen bond strength $\rightarrow$ increase in Grotthuss mechanism

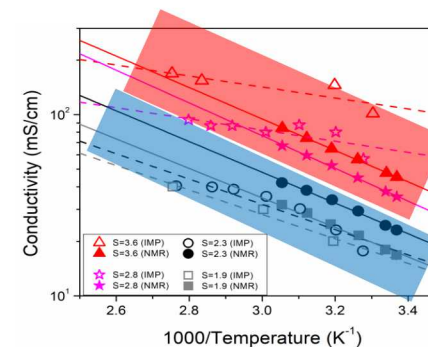
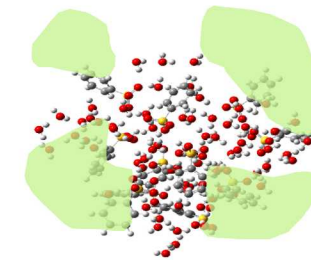
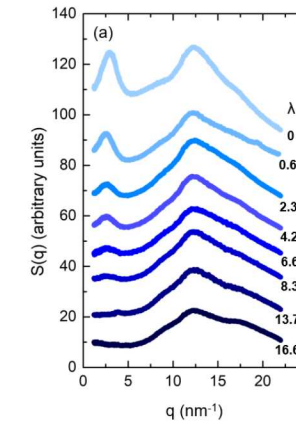
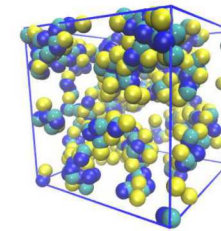
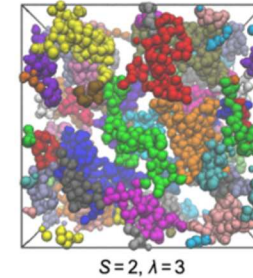
Hydrogen Bond Network in SDAPP



- Hydrophilic domains from MD simulations predict a reduction in the average HB strength.
- Lower RH increase HB strength tend to reduce Grotthuss mechanism - but higher S/V of SDAPP (vs. Nafion) increases cooperative effects in the energetics of CIP solvation.

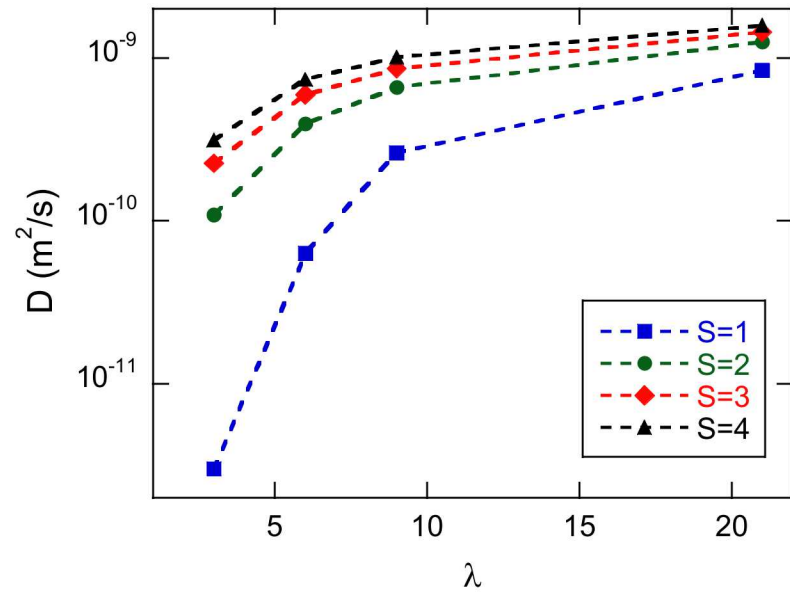
Rest of the Talk

- atomistic MD simulations
 - clustering
 - comparison to X-ray scattering
- DPD model and simulations
- local hydrogen-bond environment
- conductivity

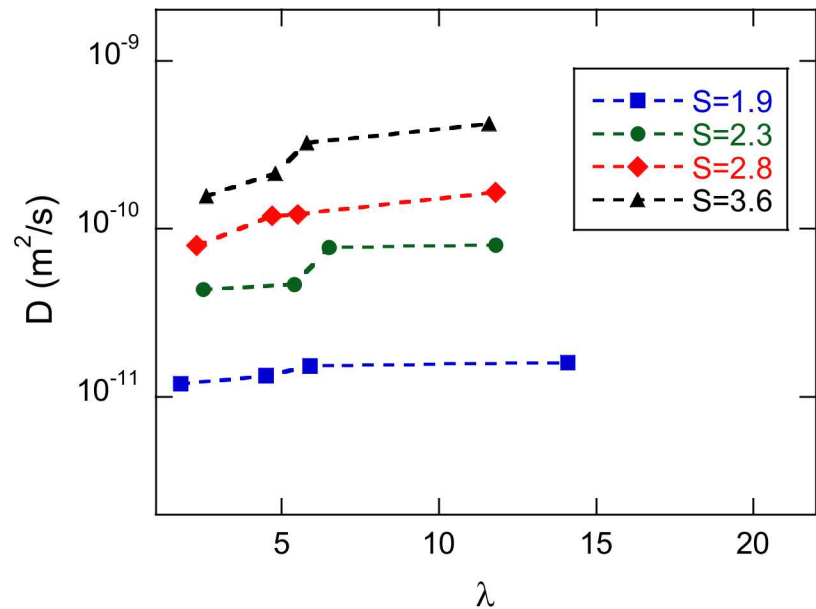


Water and Proton Diffusion: DPD

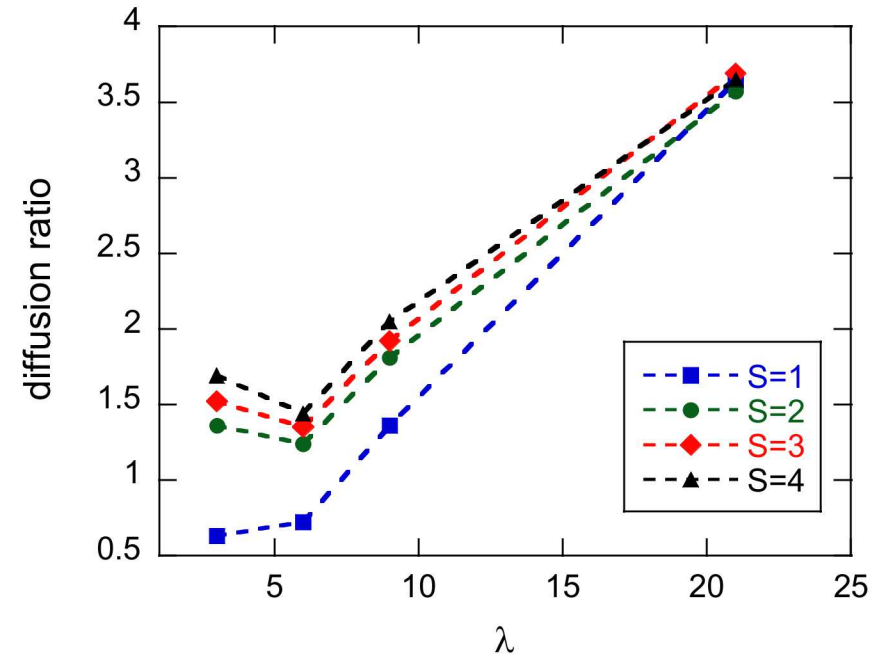
DPD



NMR

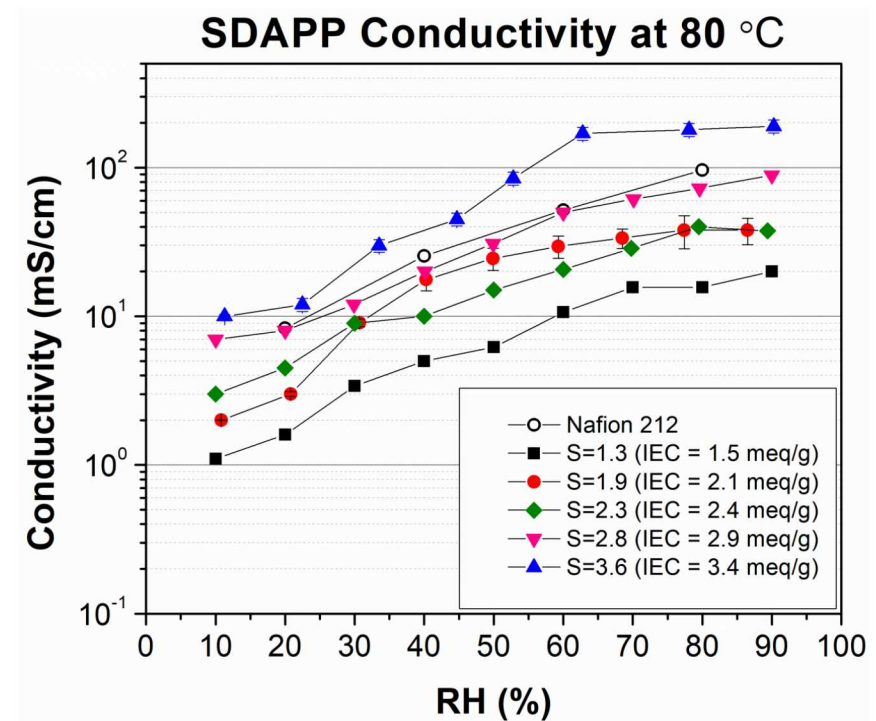
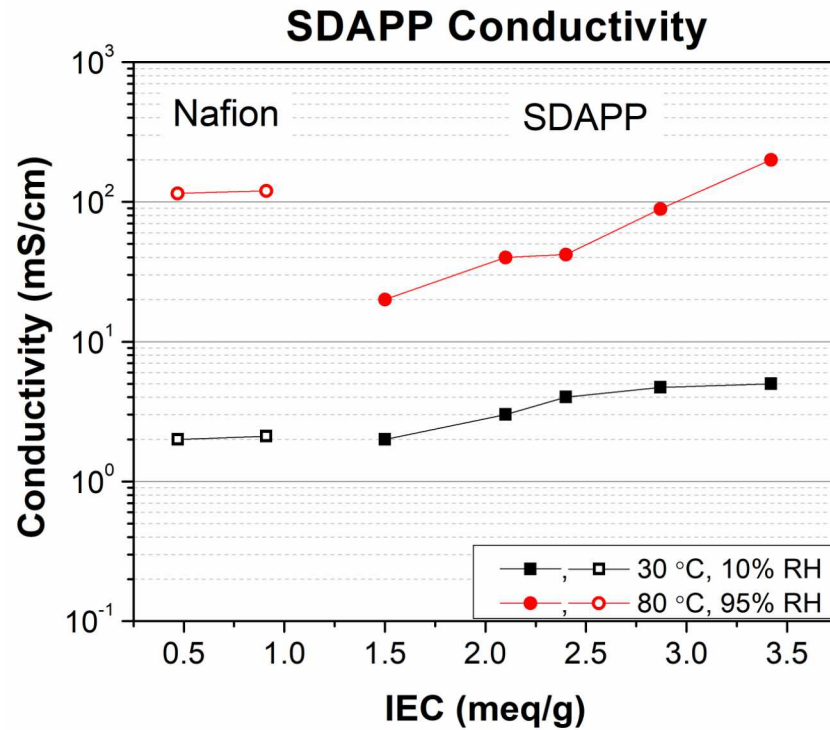


D_p/D_w in SDAPP



large increase in proton motion at high λ

Conductivity from Impedance Spectroscopy

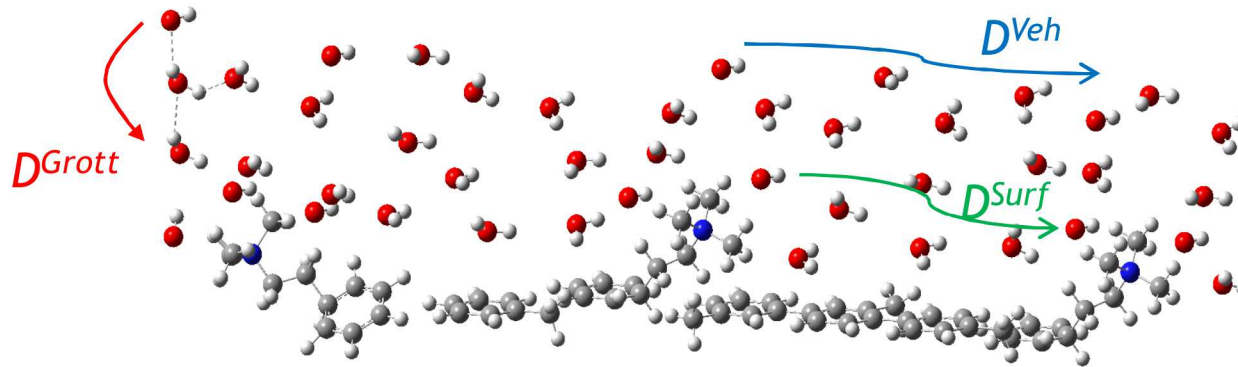


excellent conductivity at high sulfonation

Nernst-Einstein
Equation

$$\sigma = \frac{F^2 c (D_+ + D_-)}{RT} \xrightarrow{\text{Only involves H}^+} \sigma = \frac{F^2 c (D_+)}{RT}$$

$$\sigma = \frac{F^2}{RT} \left(\overset{\text{Surface}}{D_{\text{H}^+}^{\text{Surf}} C_{\text{H}^+}^{\text{Surf}}} + \overset{\text{Grotthuss}}{D_{\text{H}^+}^{\text{Grott}} C_{\text{H}^+}^{\text{Grott}}} + \overset{\text{Vehicular}}{D_{\text{H}^+}^{\text{Veh}} C_{\text{H}^+}^{\text{Veh}}} \right)$$



If we can measure diffusion individually, we can evaluate different contributions.

Conductivity

Connecting SDAPP Conductivity from Diffusivity

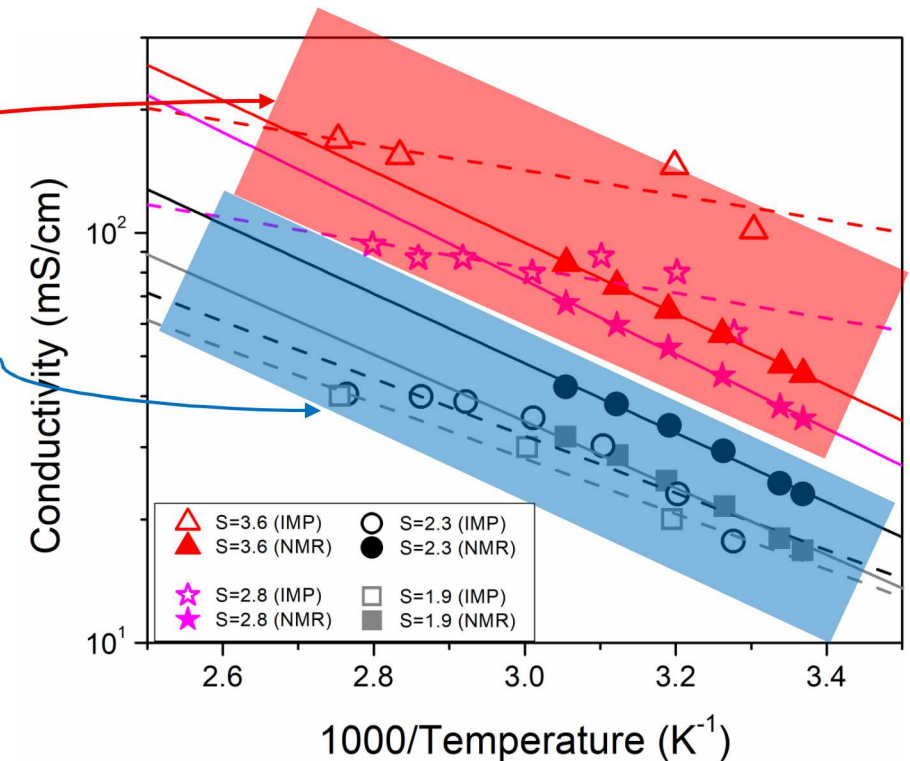
Nernst-Einstein Equation

$$\sigma = \frac{F^2 c(D_{\text{H}^+})}{RT} \iff \sigma_{\text{NMR}} = \frac{F^2 c(D_{\text{PFG}})}{RT}$$

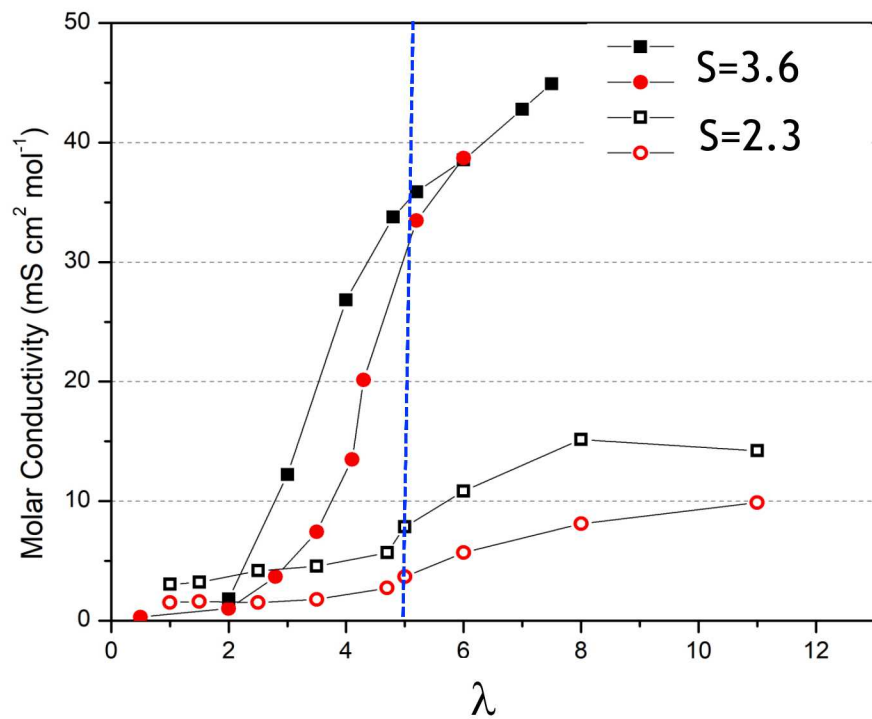
$$\sigma = \frac{F^2}{RT} \left(\overset{\text{Grotthuss}}{D_{\text{H}^+}^{\text{Grott}} C_{\text{H}^+}^{\text{Grott}}} + \underset{\text{Vehicular}}{D_{\text{H}^+}^{\text{Veh}} C_{\text{H}^+}^{\text{Veh}}} \right)$$

$$\sigma(T) = \frac{F^2 C_{\text{H}^+}}{RT} \left[D_0^{\text{Grott}} \exp(-E_a^{\text{Grott}} / RT) + D_0^{\text{Veh}} \exp(-E_a^{\text{Veh}} / RT) \right]$$

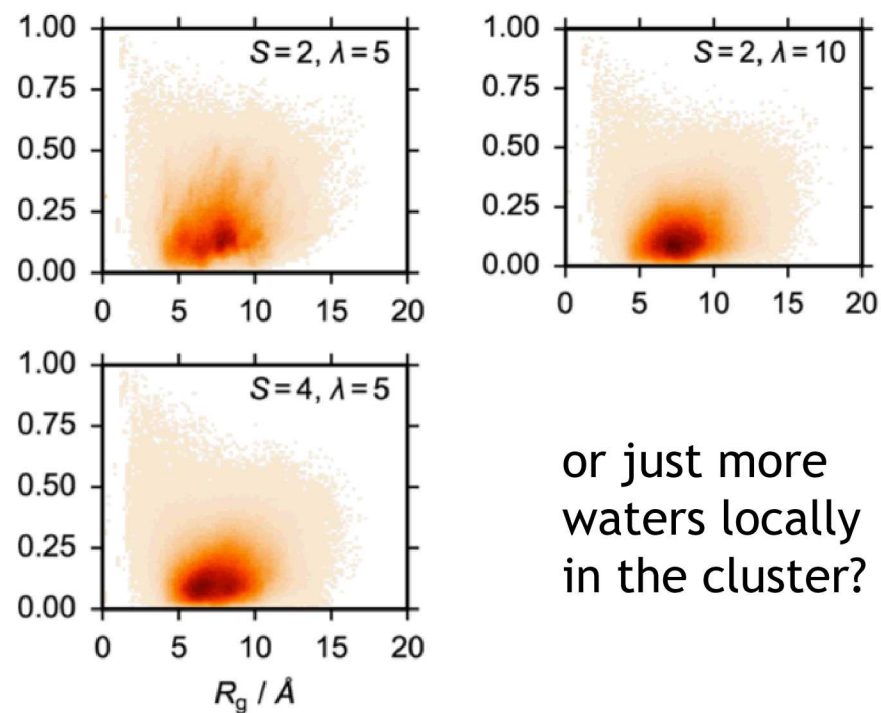
- at low-moderate S: proton conductivity controlled by water vehicular transport
- increasing S: Grotthuss mechanism becomes significant



Relate Conductivity to MD Morphology



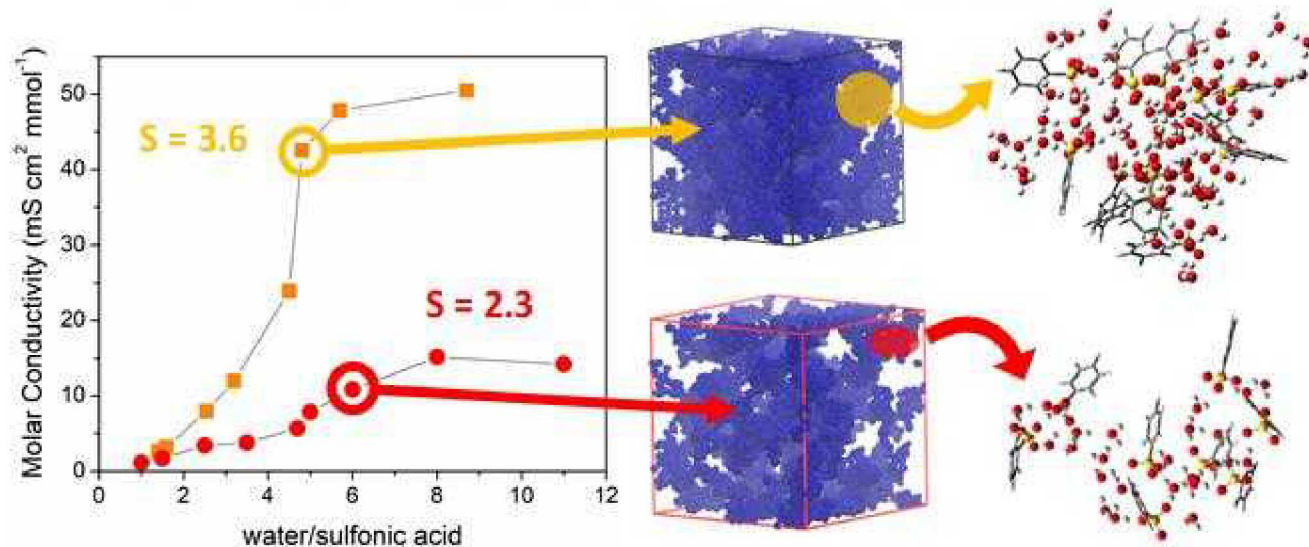
do more spherical cluster shapes
improve conductivity?



or just more
waters locally
in the cluster?

Relate Morphology/Hbond Network to Conductivity

SDAPP PEM Membrane Nanomorphology

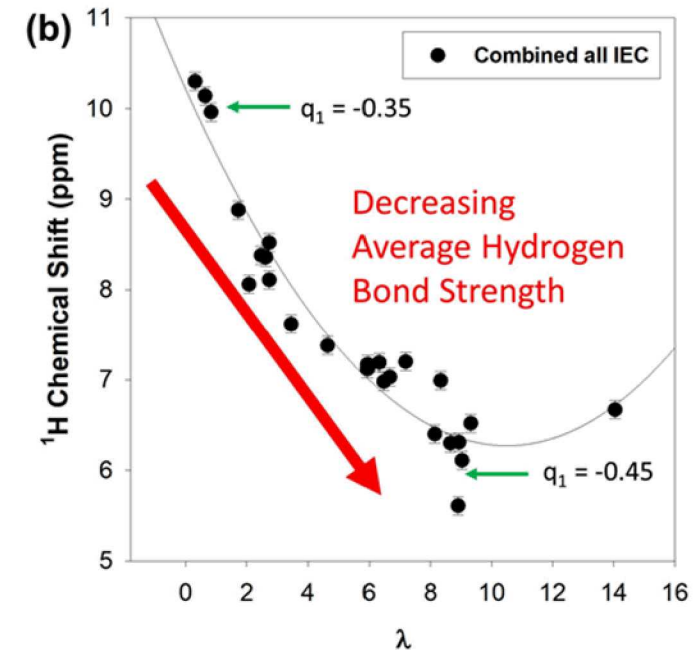


with increasing sulfonation and water content:

- percolated hydrophilic domains
- more bulk-like water domains
- weaker hydrogen bond network
- larger variety of proton coordination environments



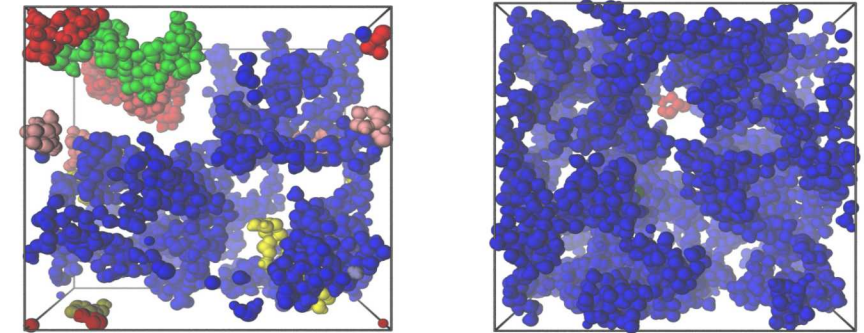
turn on of the Grotthuss mechanism and much higher conductivity



Summary

SDAPP morphology with increasing sulfonation, hydration:

- increasingly percolated domains
- more bulk-like water domains
- weaker H-bond network
- more heterogeneous H-bond network and coordination



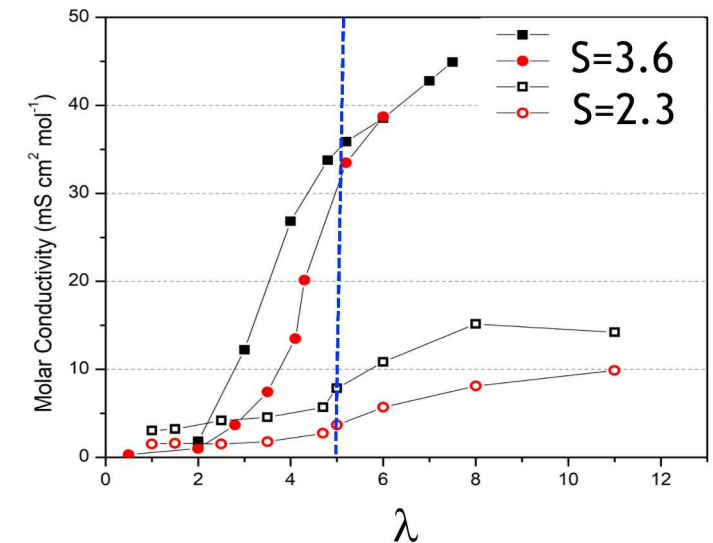
MD simulation agrees with X-ray, NMR

SDAPP proton conductivity with increasing sulfonation, hydration:

- Grotthuss mechanism turns on
- large increase in conductivity at highest S

DPD simulations

- qualitatively similar morphology
- increase in proton motion with λ



SDAPP promising PEM material
multiple modeling & experimental tools needed to understand

Acknowledgments

Sandia National Labs

Dr. Lauren Abbott: MD simulations

Jennifer Clark: DPD model/simulations

Dr. Eric Sorte: NMR, characterization

Dr. Todd Alam: NMR, characterization

Dr. Cy Fujimoto: synthesis



Lauren Abbott



Jen Clark



Todd Alam



Eric Sorte



Cy Fujimoto

University of Pennsylvania



Ben Paren: X-ray scattering

Prof. Karen Winey: X-ray, etc



Ben Paren



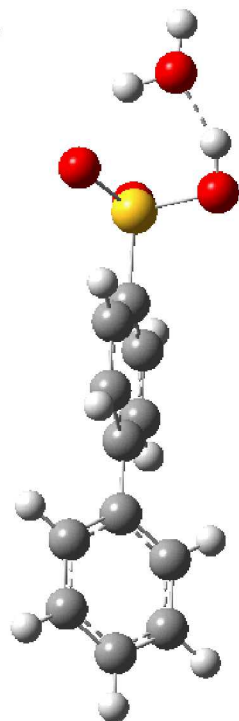
Karen Winey

Funding: Sandia LDRD
DOE/BES Center for Integrated Nanotechnologies



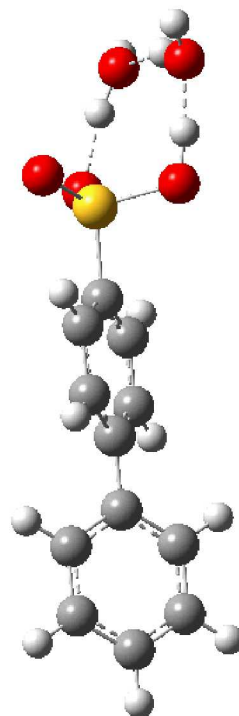
Quantum cluster calculations

DFT 6-311**



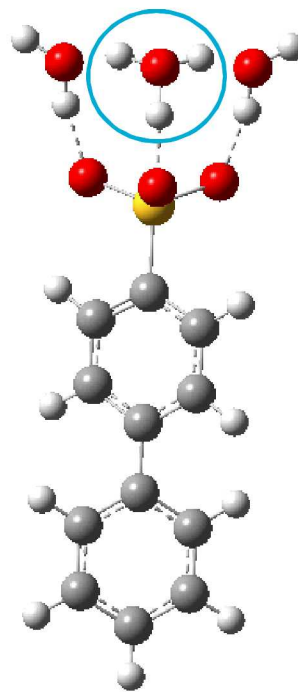
$\lambda = 1$

Hydrogen
bond



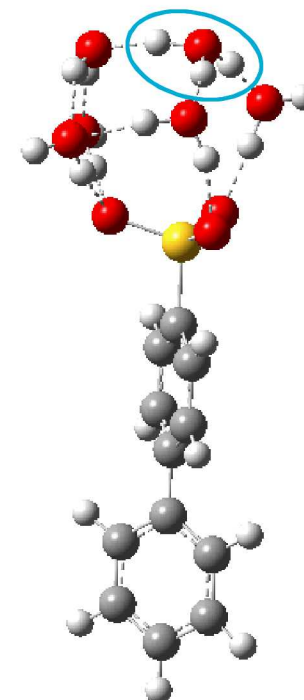
$\lambda = 2$

Hydrogen
bond



$\lambda = 3$

Contact ion
pair

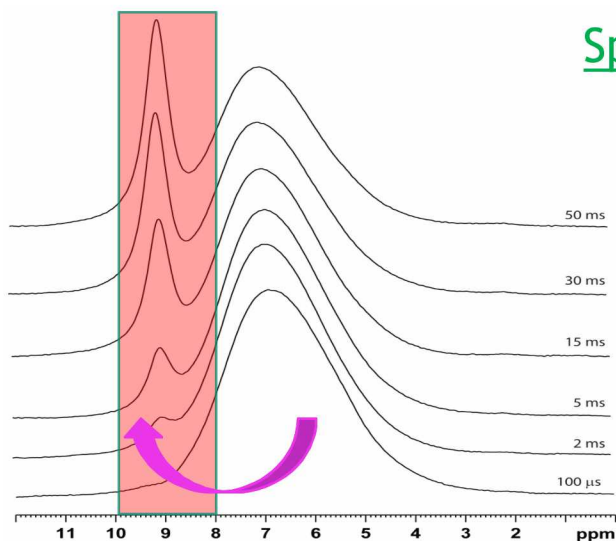
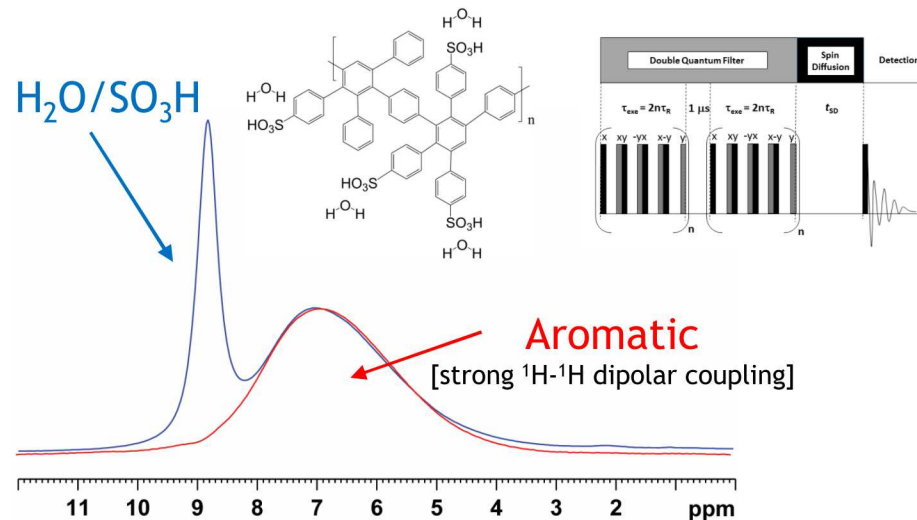


$\lambda = 5$

Solvated contact
ion pair

need $\lambda = 3$ for deprotonation

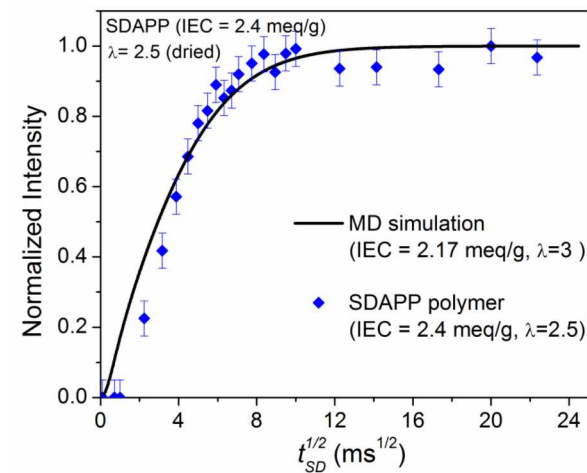
^1H NMR Spin Diffusion Experiments



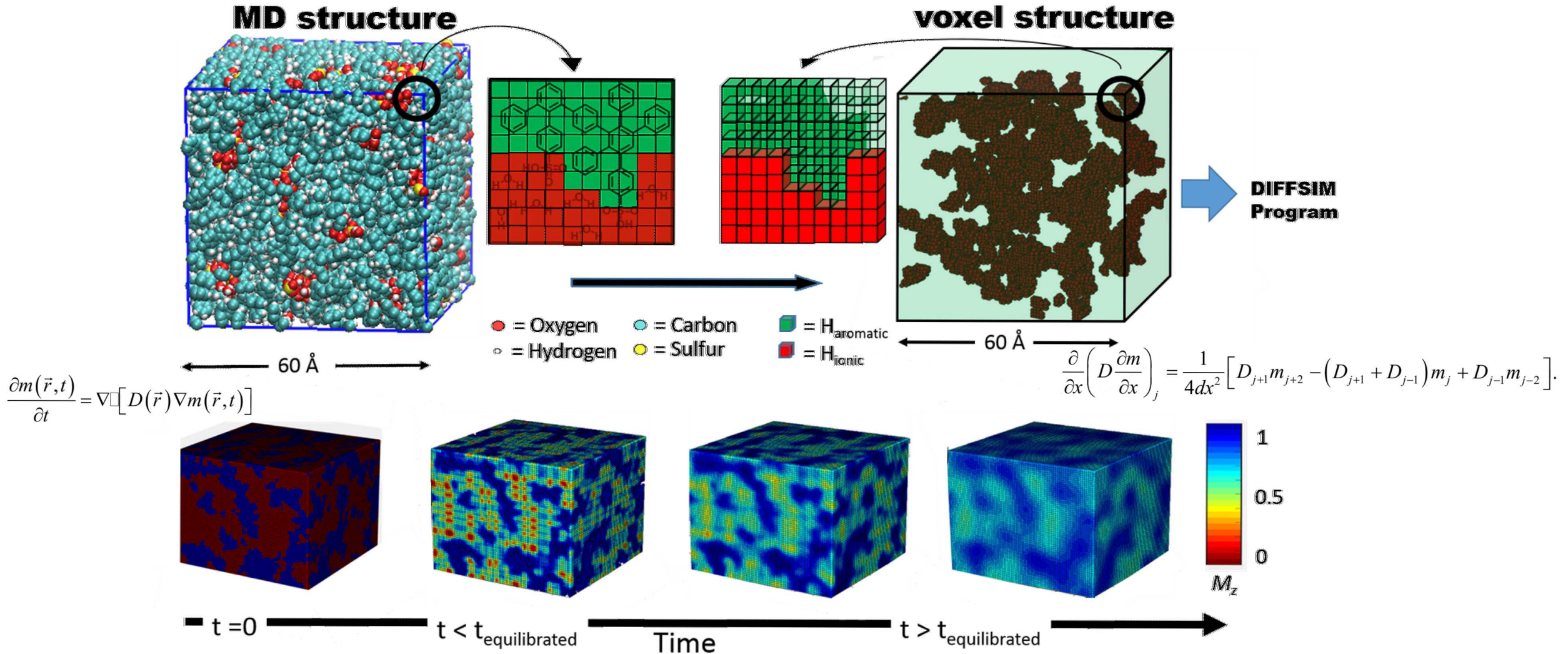
Spin Diffusion Experiment



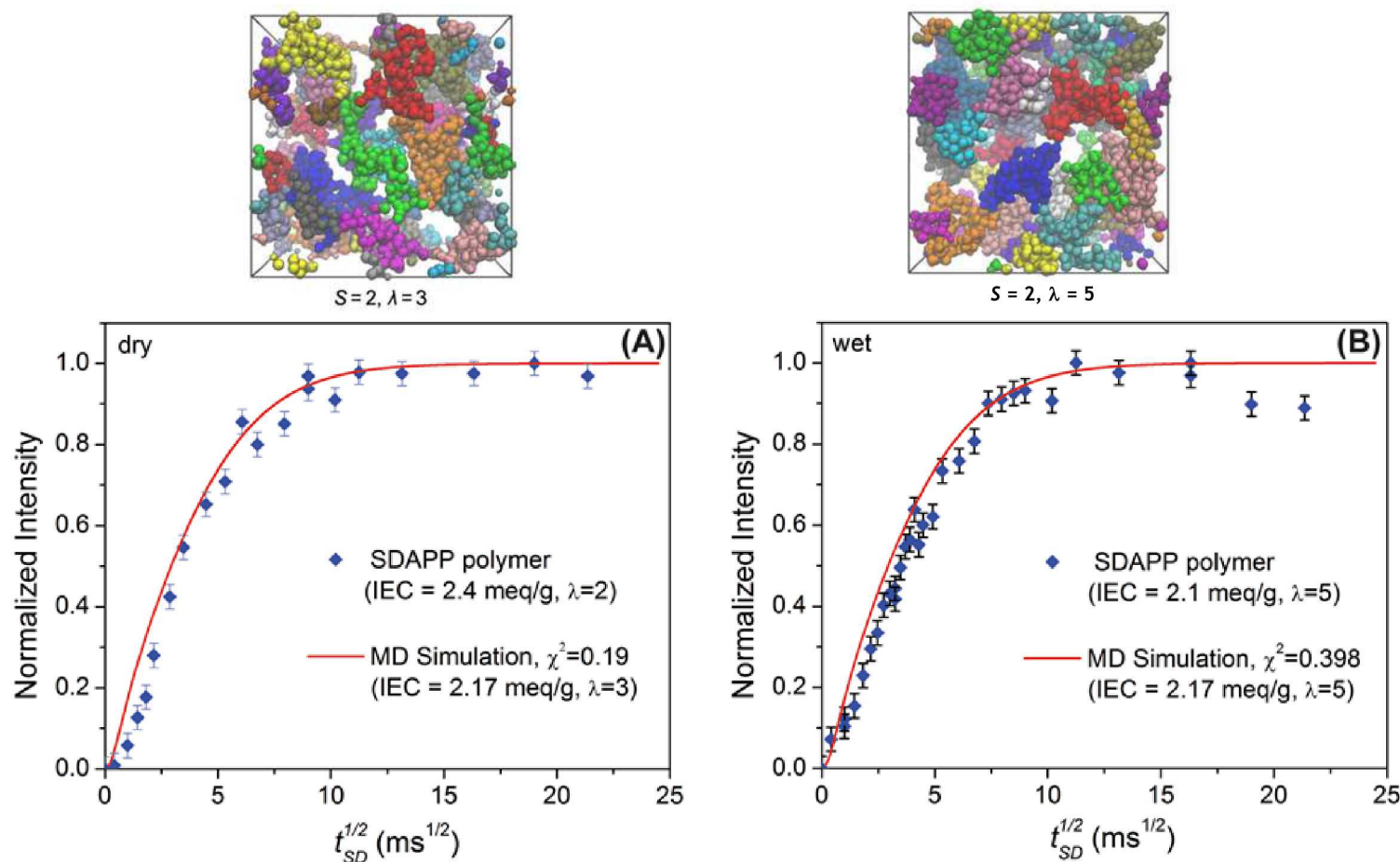
**“spin temperature”
Equilibration via
 ^1H - ^1H dipolar
mediated spin
diffusion**



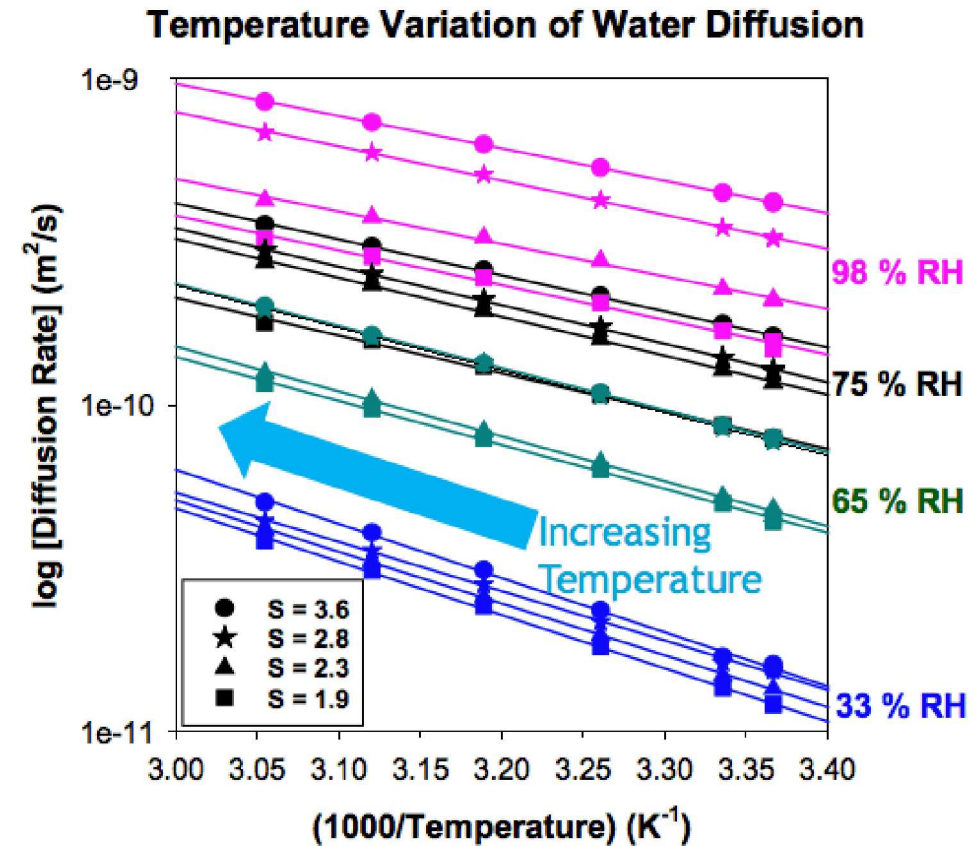
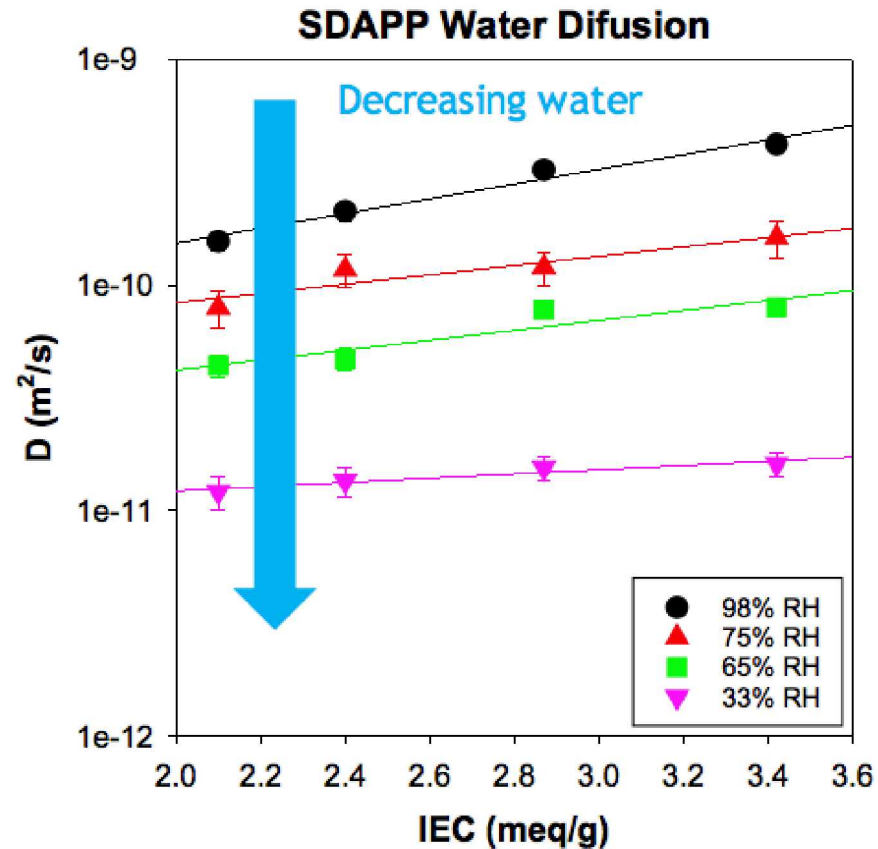
Simulating Spin Diffusion Experiments



Simulated Spin Diffusion from MD vs Experiment



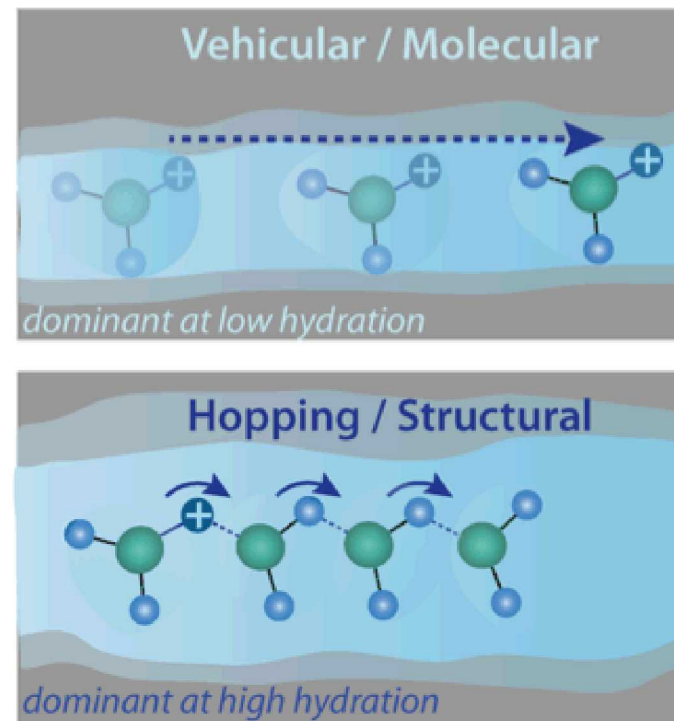
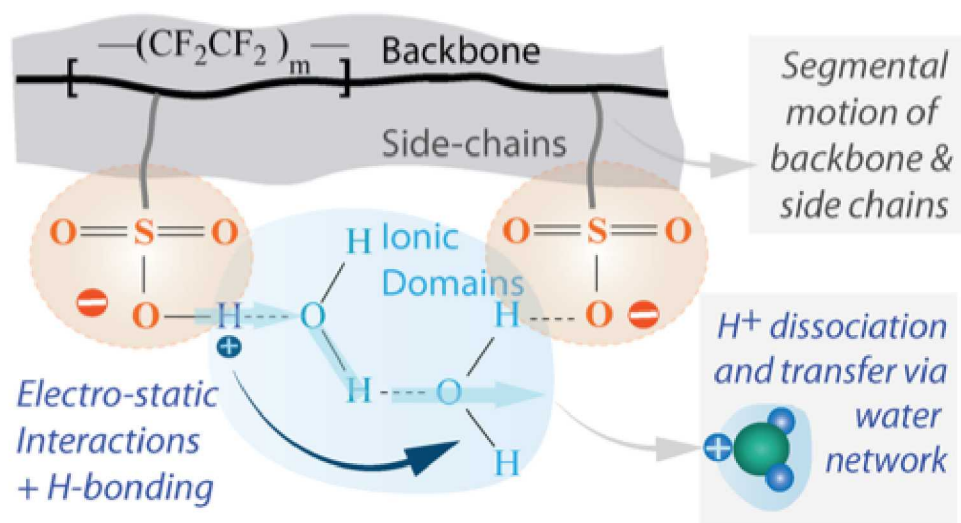
- MD structure (morphology from simulation)
- Spin diffusion constants (from line width), volume fractions, etc. are fixed.
- **No adjustable parameters in these fits!!!!**
- Deviations at higher hydration levels [finite simulation size? NMR relaxation?]



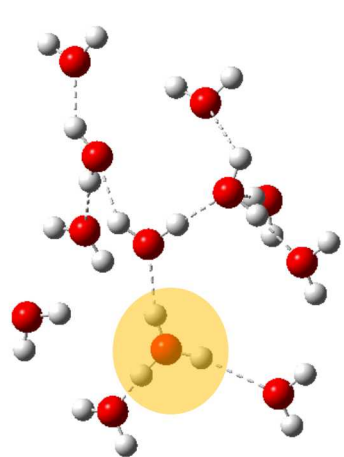
Sample	E_a (kJ/mol)			
	33%	65%	75%	98%
S = 1.9	31.3	25.8	22.2	20.4
S = 2.3	30.4	26.4	22.9	19.1
S = 2.8	29.0	24.7	22.6	20.1
S = 3.6	31.8	24.7	21.1	19.0

- E_a similar to other PEMs at higher hydration levels.
- At < 33% RH increasing E_a .
- PFG NMR not obtainable at very low RH%

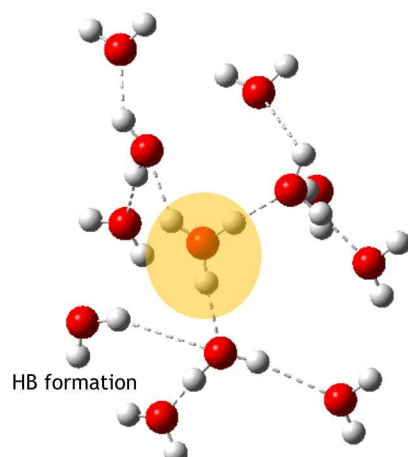
Proton Transport Mechanisms



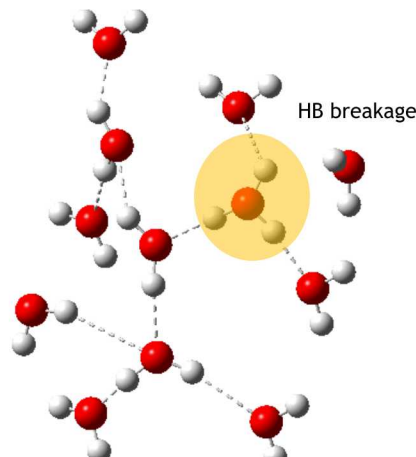
Kusoglu, A. & Weber, A. Z. *Chem Rev* **117**, 987–1104 (2017).



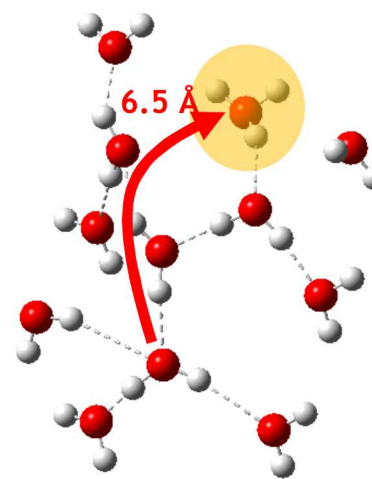
Eigen(1) → Zundel



Eigen(2)



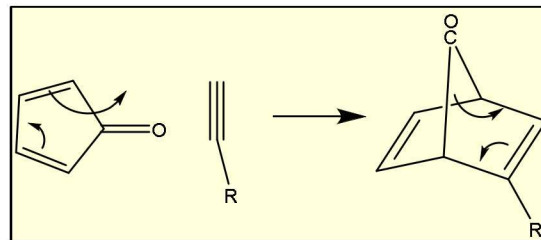
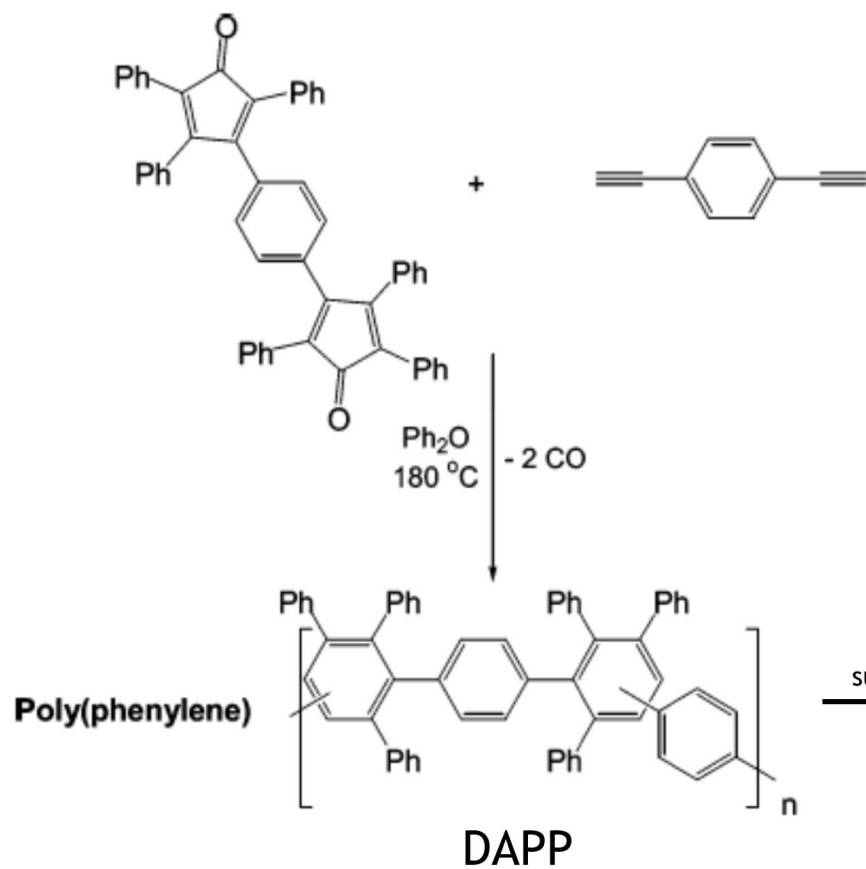
Eigen(3)



Eigen(4)

Grotthuss mechanism

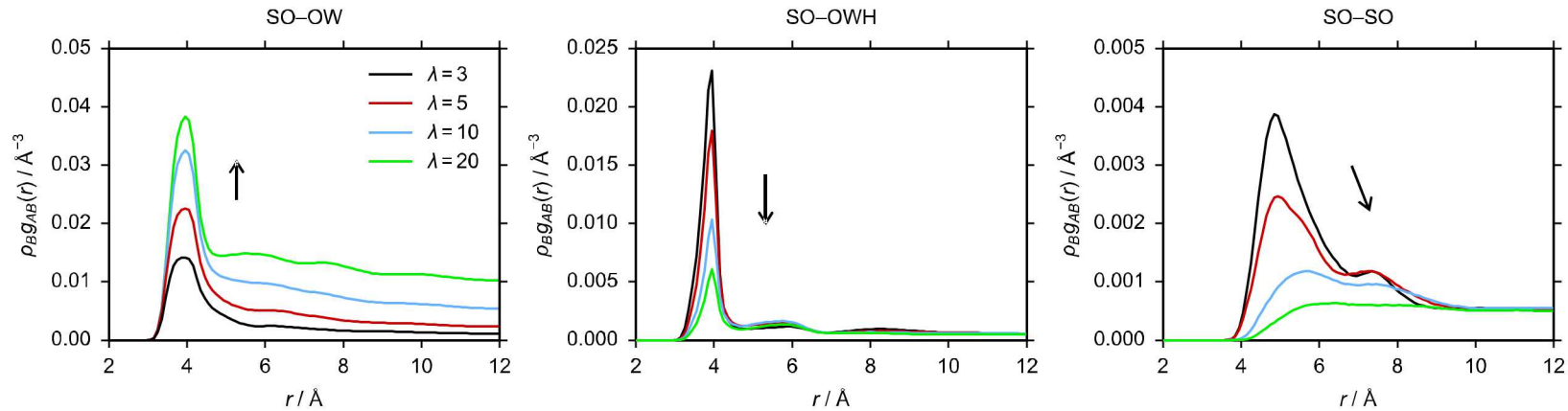
Diels-Alder Polymerization



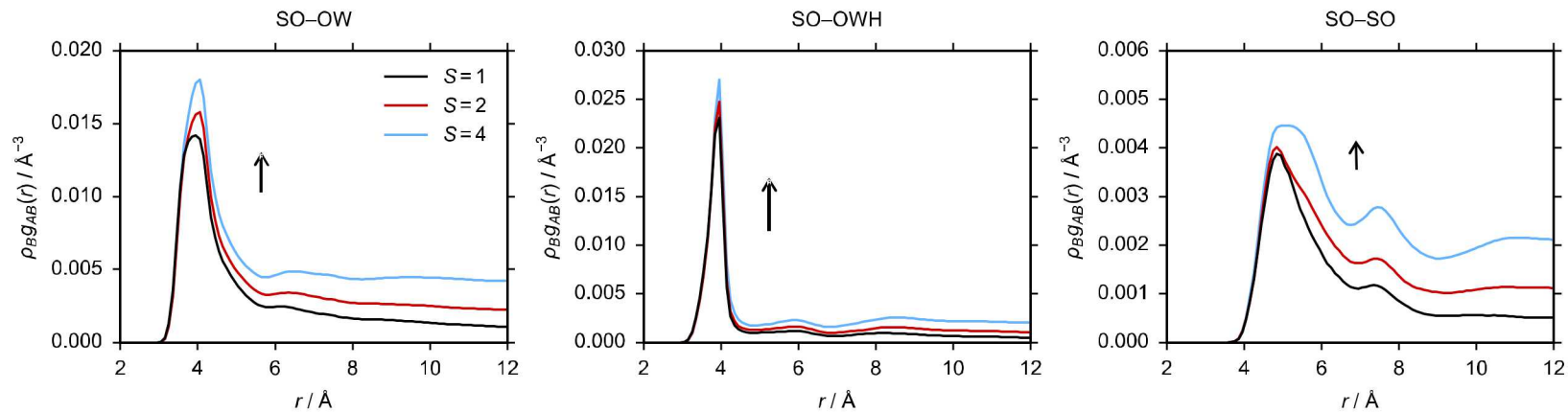
SDAPP

Sulfonate group more solvated at higher water contents

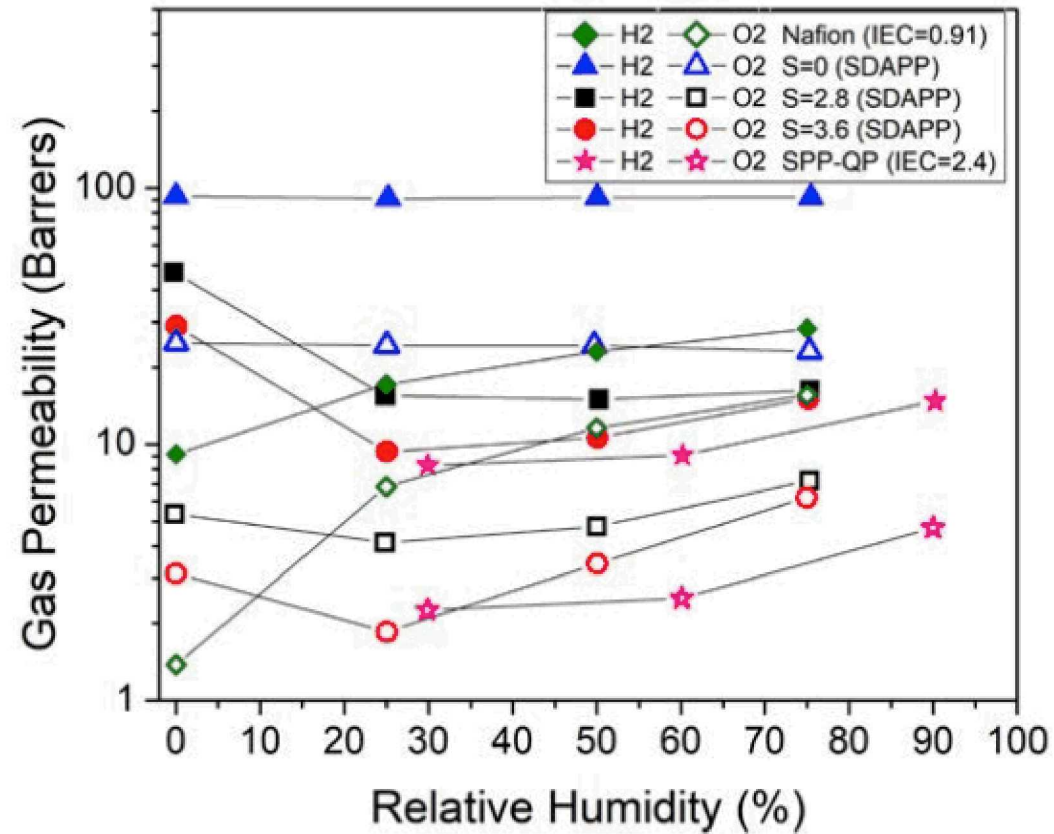
Increasing hydration level:



Increasing sulfonation level:

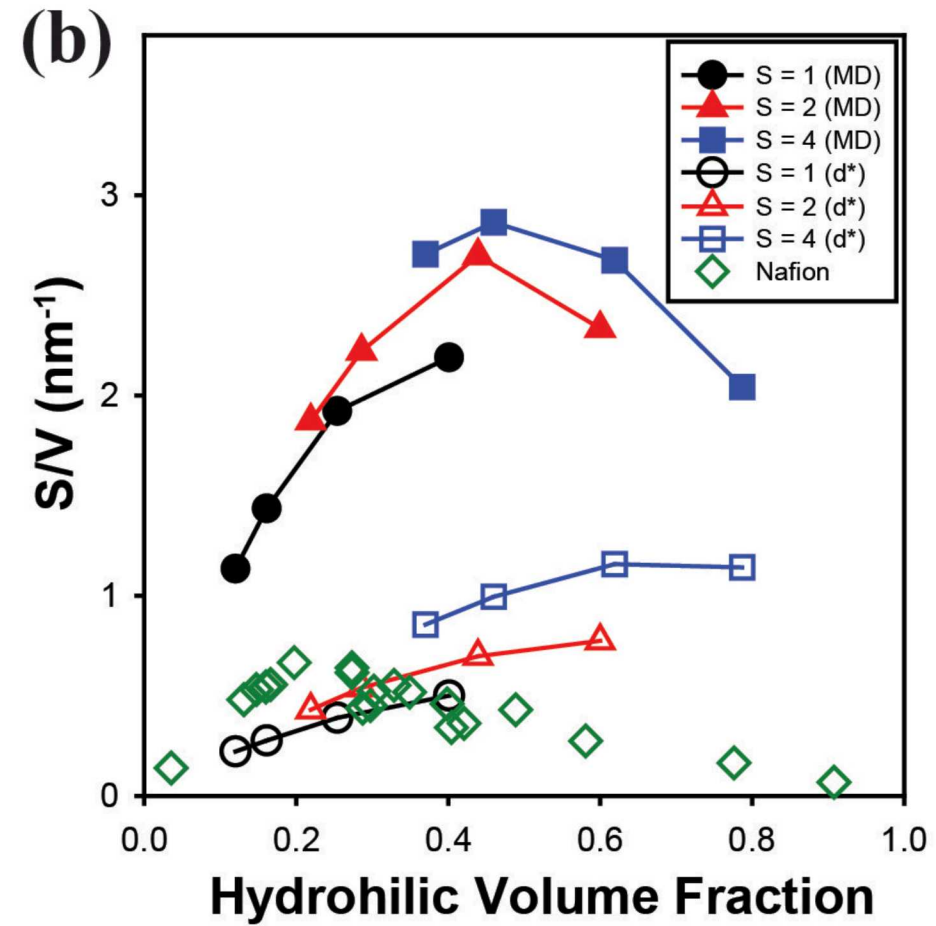
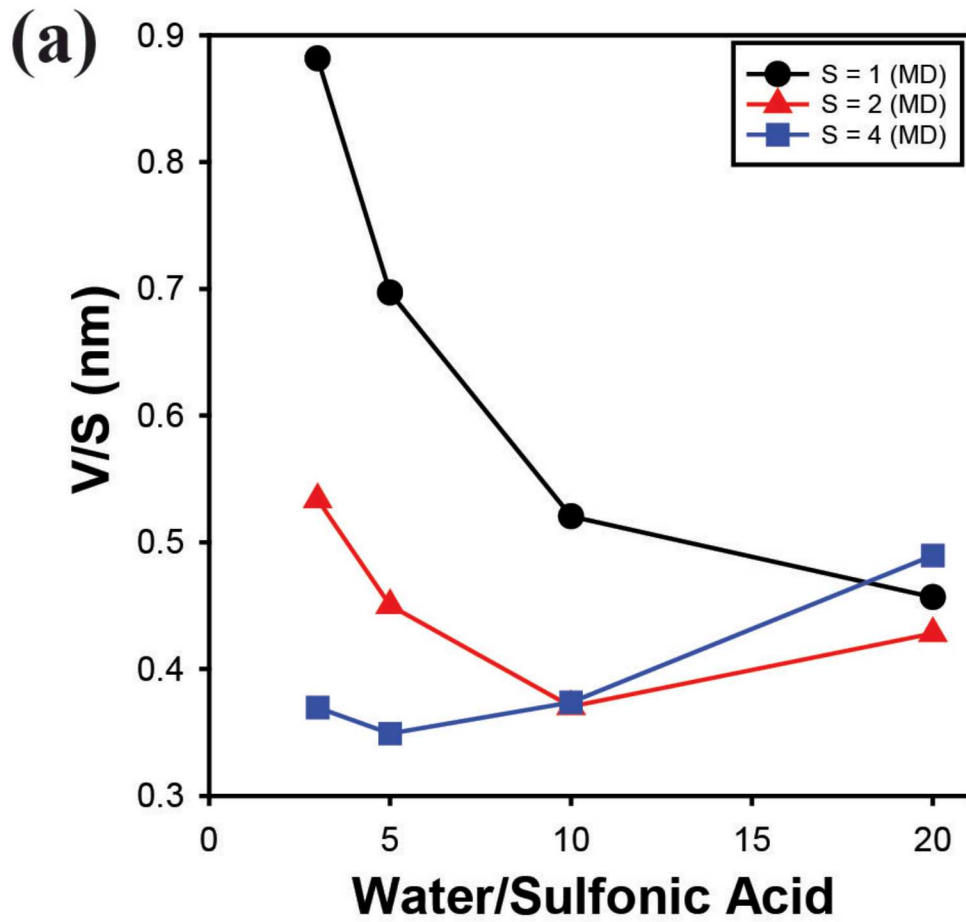


Gas permeability



Christina Rodriguez and Nate Lynd, UT Austin

Surface to volume of hydrophilic domains



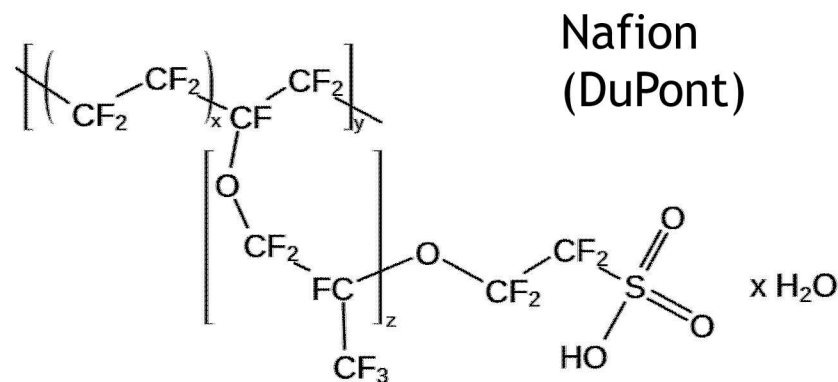
Desired Properties of Fuel Cell Membranes

- high conductivity, $\sigma \approx 0.1 \text{ S/cm}$
- low cost
- chemically stable
- mechanically stable
- mechanically strong (resist swelling)
- low gas crossover

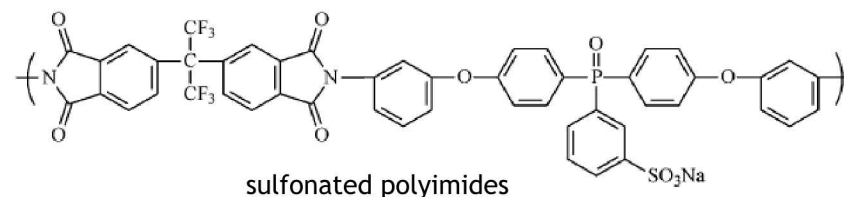
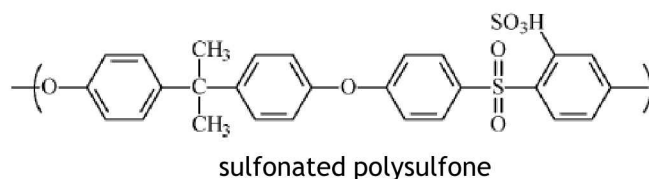
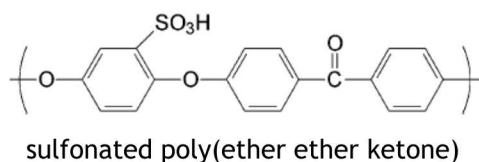
Shortcomings of perfluorosulfonic acid membranes:

- Low proton conductivity at high temperatures
- High methanol/gas diffusion
- Poor recyclability
- High manufacturing costs

Current industry standard:
perfluorinated sulfonic acid ionomers (PFSA)

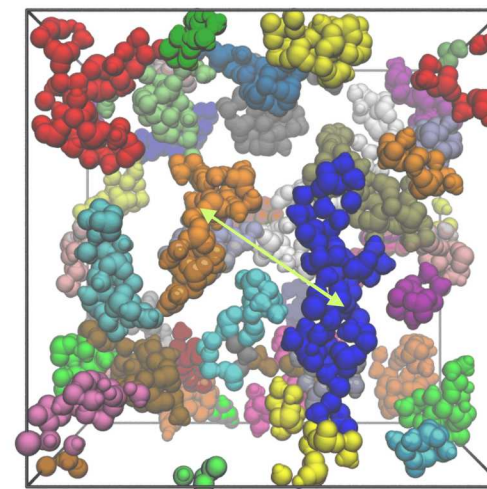
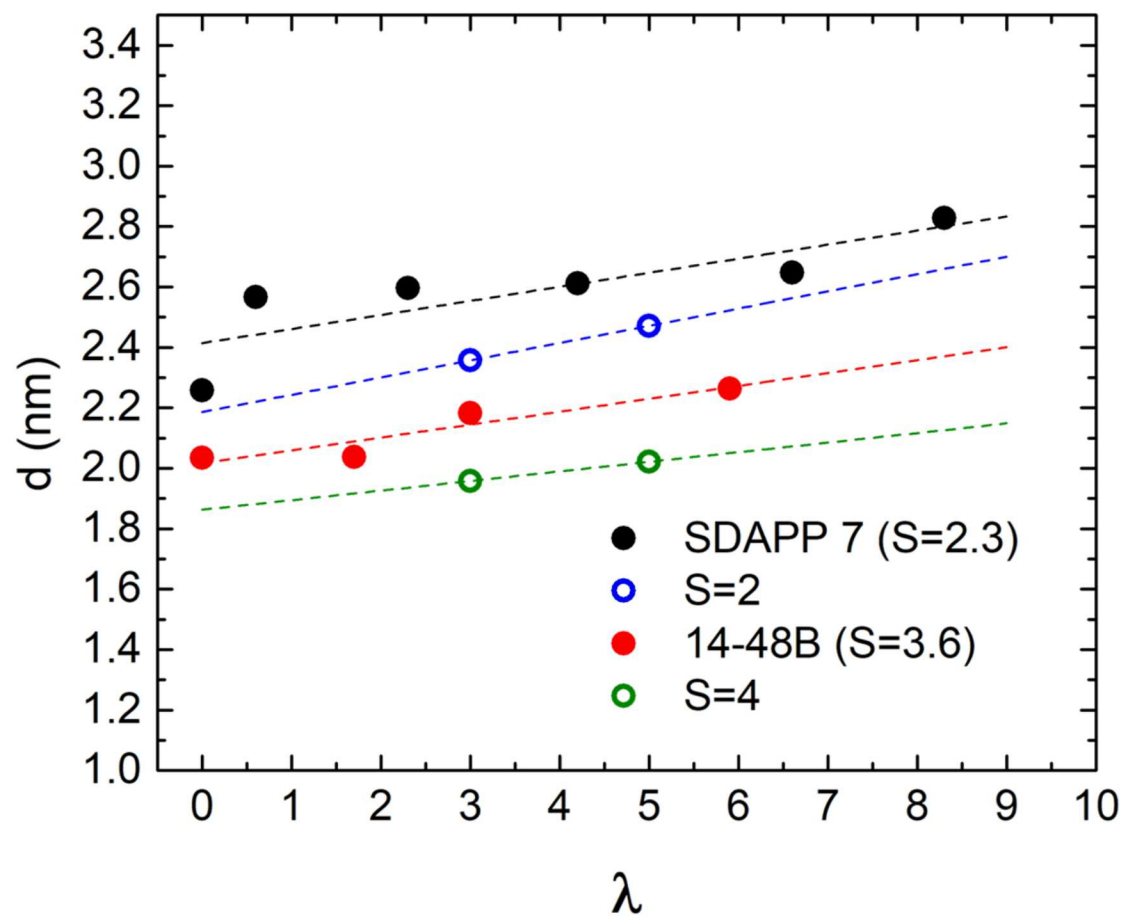


Alternatives: hydrocarbon-based proton-conducting polymers



Correlation Distance between Aggregates

$d = 2\pi/q^*$, q^* = ionomer peak location



$S=1, \lambda=3$

from real space snapshots, low λ :

$S = 2, d = 23 \text{ \AA}$

$S = 4, d = 19 \text{ \AA}$

MD consistent with X-ray