

Developing Consistent Models for Matter in Extreme Conditions

S. Hansen, T. Nagayama, T. Gomez, A. Baczewski, and A. Cangi

Sandia National Laboratories

APS-DPP/GEC Meeting

Portland, OR

November 4 – 9, 2018

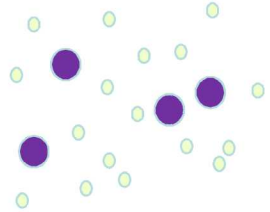
SAND2018-ZZ



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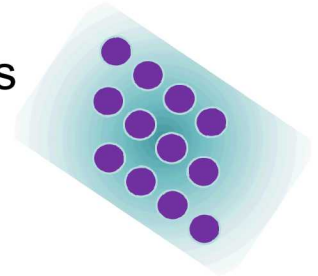
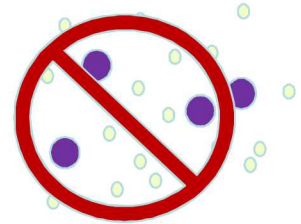
What's so difficult about modeling extreme conditions?

- HED plasmas are (usually) not well described by classical plasma models
 - Partial ionization / complex screening
 - Degeneracy effects
 - Density effects on electronic structure
 - Strongly coupled ions



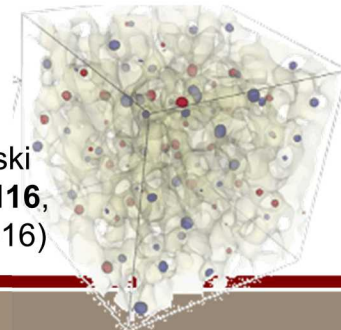
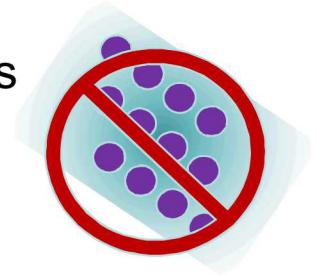
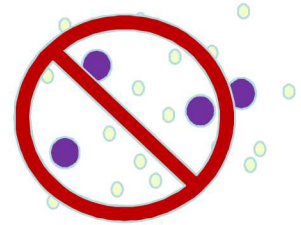
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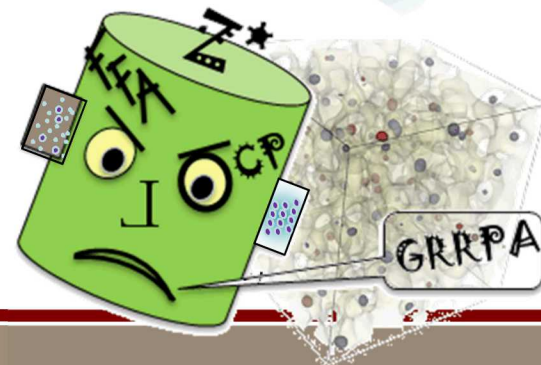
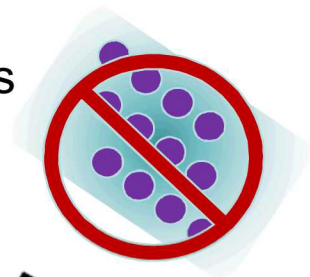
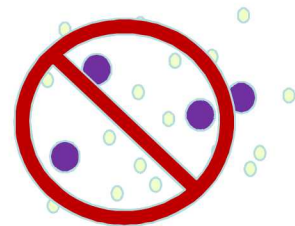
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- Rigorous and reliable models exist:
 - Quantum Molecular Dynamics (QMD)
 - Time-dependent Density Functional Theory (TD-DFT)
 - But these are expensive and can be difficult to extend to high temperatures, low densities, and complex ions



A. Baczewski
et al, PRL **116**,
115004 (2016)

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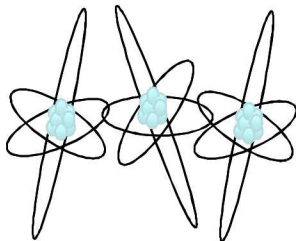


Central question: What happens to material when you squish it very hard and/or heat it quite a lot?

Experiments/Observables

Measurements from small, short-lived lab plasmas and large, distant astrophysical objects are inherently challenging

Observables (yields, images, spectra) can be difficult to interpret; may require both models and simulations



Simulations

Simulations help to design experiments and interpret data from laboratory and astrophysical plasmas

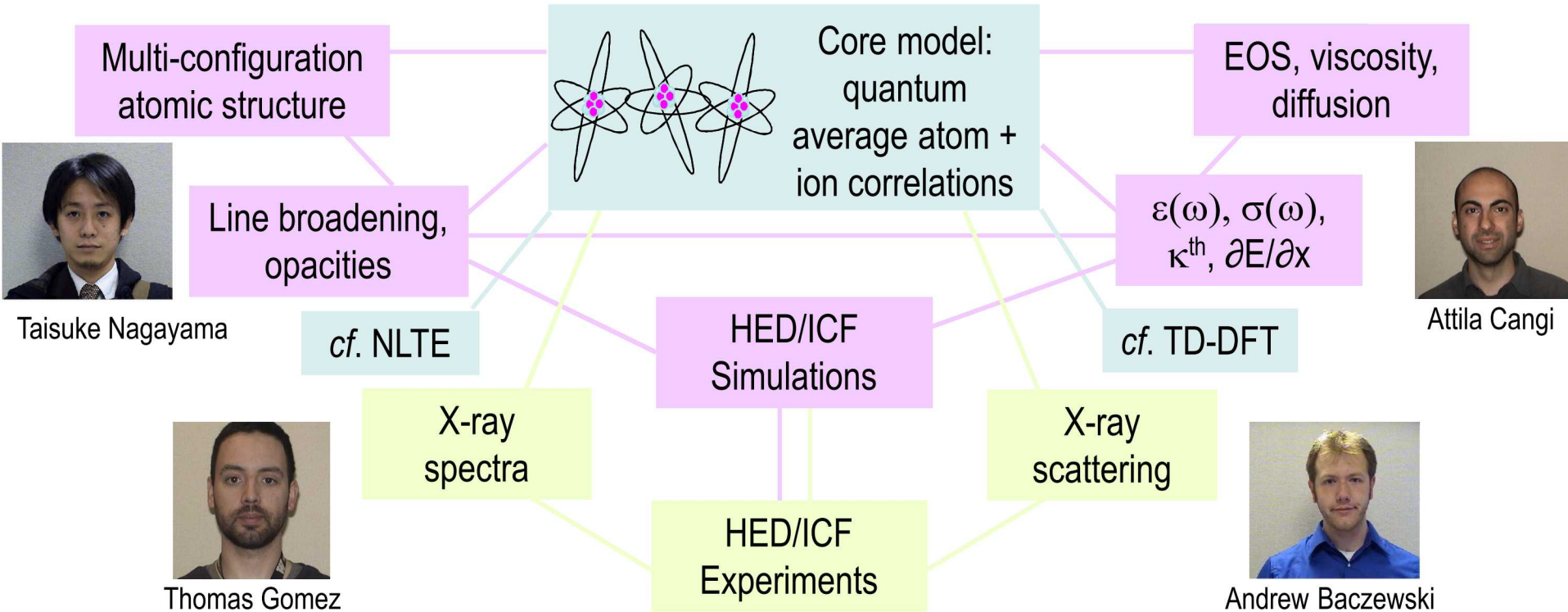
Rad-hydro simulations themselves require extensive input from adequate material models (EOS, transport, opacity)

Additional questions:

How can we tell if our models are right?

How important is model consistency?

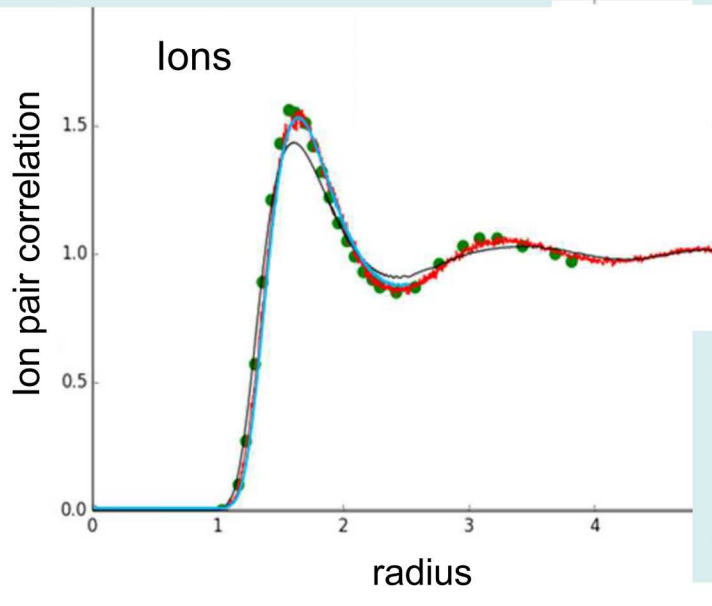
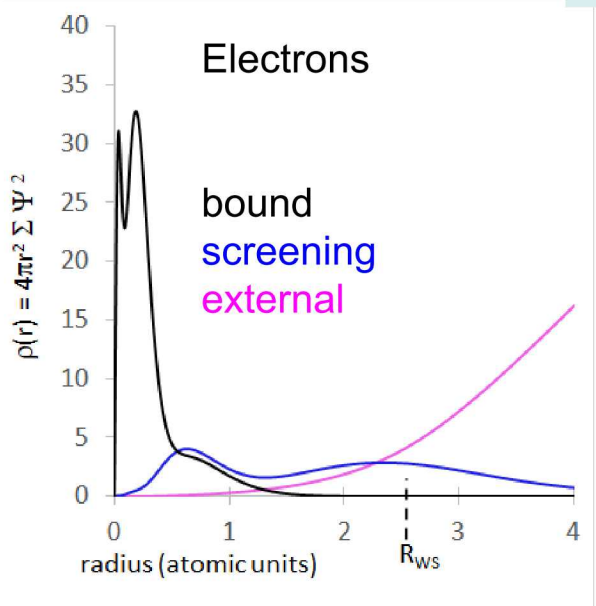
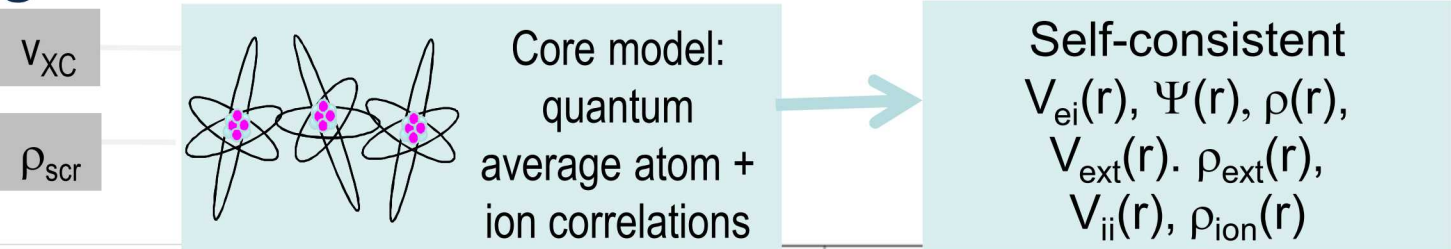
Our central goal: Develop a unified, tractable, and consistent model for matter in extreme conditions



Thanks to:
Charles Starrett, David Kilcrease (LANL), Carlos Iglesias, Brian Wilson, Phil Sterne, Paul Grabowski (LLNL), Richard More

Primary funding: U.S. DOE, Office of Science Early Career Research Program, OFES FWP-14-017426

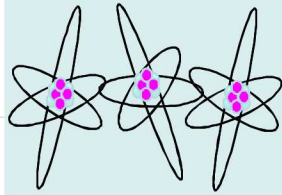
Fully self-consistent core model: Quantum average-atom + ion correlations



Observable and constitutive properties

- Spherical
- semi-relativistic
- + orthonormal $\Psi(r)$
- + runtime ~ 3 minutes

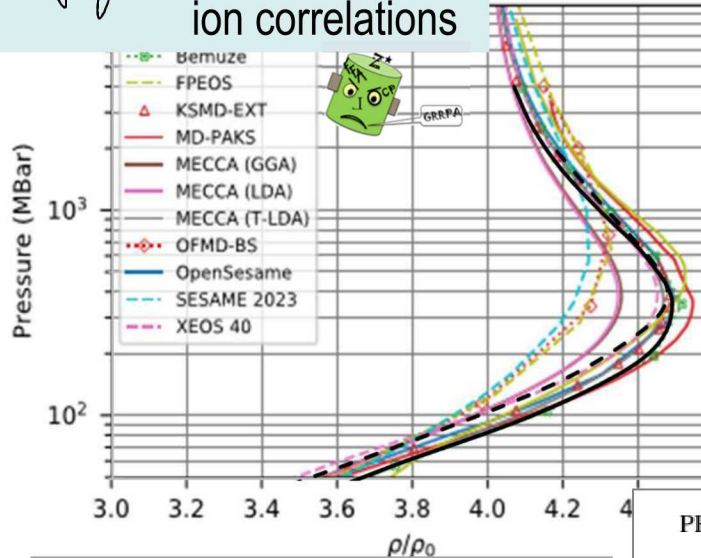
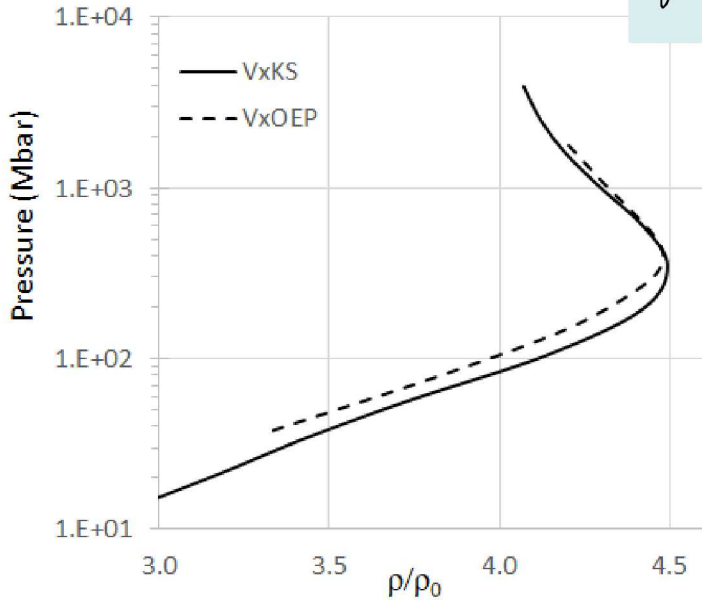
The model yields highly constrained Equations of State and ionic transport coefficients



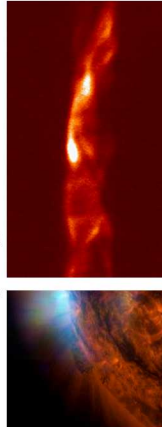
Core model:
quantum
average atom +
ion correlations

EOS, viscosity,
diffusion

Beryllium Hugoniot



Astrophysics & ICF



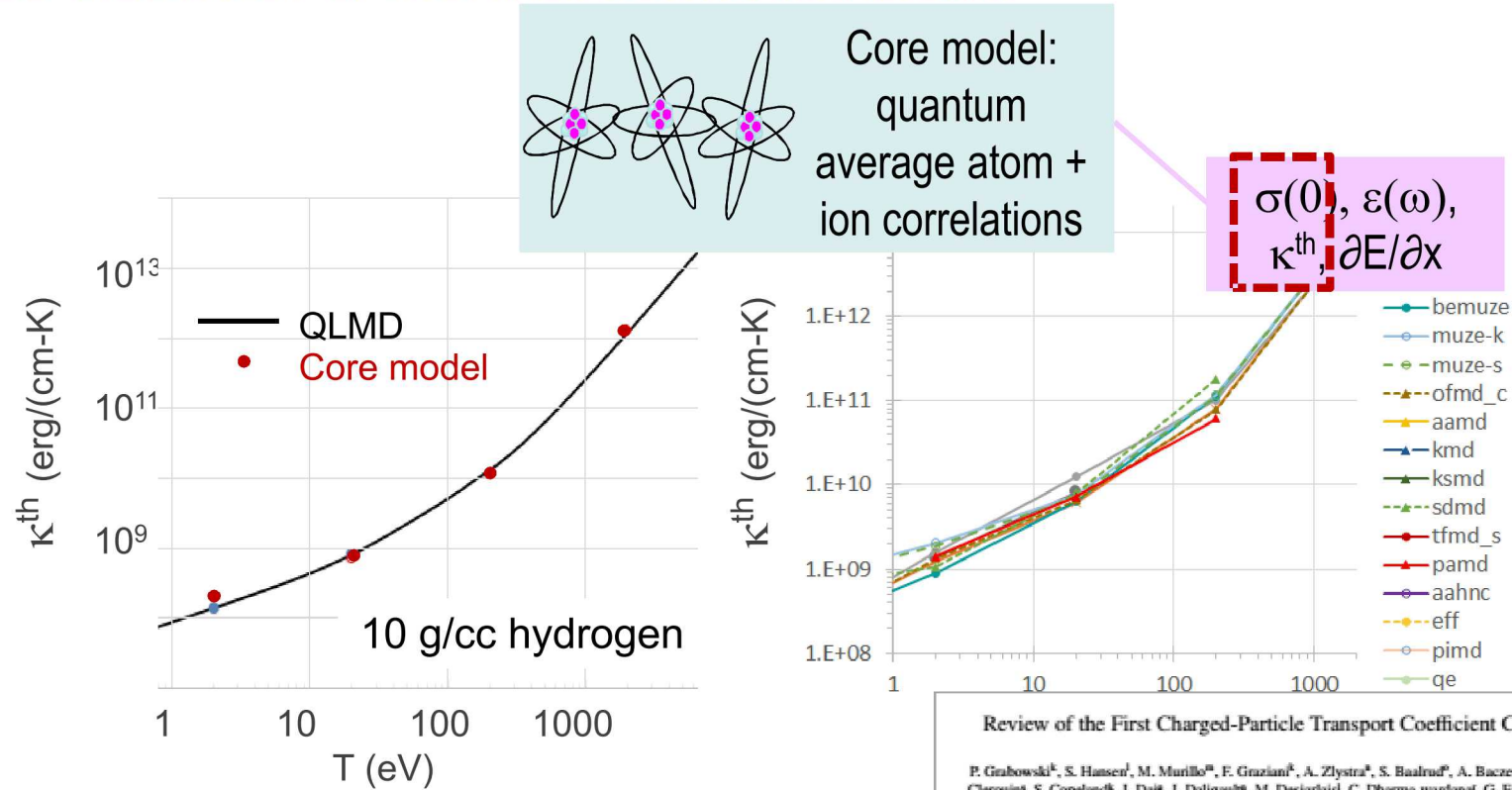
A Review of Equation-of-State Models for
Inertial Confinement Fusion Materials
J.A. Gaffney, S.X. Hu, P. Arnault, A. Becker, ... E. Zurek
*In Press, Accepted Manuscript, Available online 18 August
2018*

PHYSICAL REVIEW E **91**, 013104 (2015)

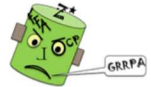
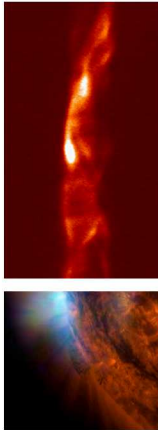
Pseudoatom molecular dynamics

C. E. Starrett,* J. Daligault, and D. Saumon

The electronic response from self-consistent wavefunctions yields electrical & thermal conductivities...



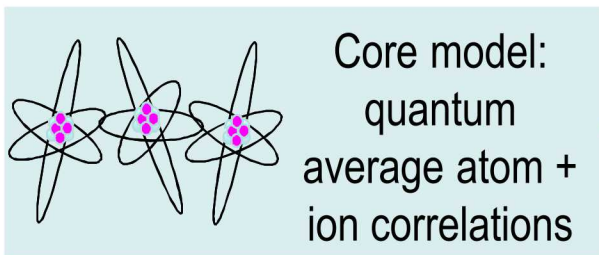
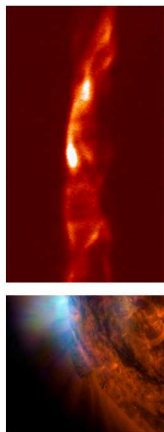
Astrophysics & ICF



M. Desjarlais *et al.* 2018

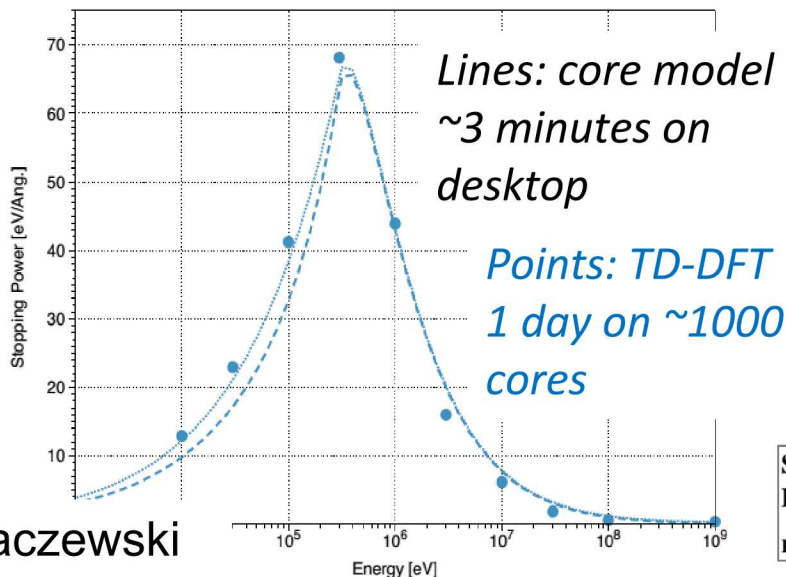
Review of the First Charged-Particle Transport Coefficient Comparison Workshop

P. Grabowski¹, S. Hansen¹, M. Murlis², F. Grazian³, A. Zlystra⁴, S. Baalrud⁵, A. Baczewski¹, L. Benedic⁶, O. Certik⁷, J. Clerouin⁸, S. Copeland⁹, J. Dai¹⁰, J. Dalgaard¹¹, M. Desjarlais¹, C. Dharma-wardana¹², G. Faussurier¹³, J. Haack¹⁴, S. Haan¹⁵, T. Haxhimali¹⁶, A. Hayes-Sterbenz¹⁷, Y. Hou¹⁸, S. Hu¹⁹, D. Jensen²⁰, D. Kang²¹, J. Kress²², Q. Ma²³, M. Marciani²⁴, E. Meyer²⁵, R. Rudd²⁶, D. Saumon²⁷, R. Singleton²⁸, L. Shulenburger²⁹, T. Sjostrom³⁰, L. Stanton³¹, C. Starren³², C. Ticknor³³



$$\sigma(\omega), \epsilon(\omega), \kappa^{\text{th}}, \partial E / \partial x$$

Protons
stopping in
10 g/cc
deuterium



Measurement of Charged-Particle Stopping in Warm Dense Plasma

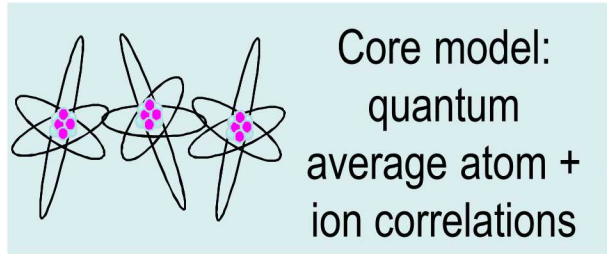
A. B. Zylstra, J. A. Frenje, P. E. Grabowski, C. K. Li, G. W. Collins, P. Fitzsimmons, S. Glenzer, F. Graziani, S. B. Hansen, S. X. Hu, M. Gatu Johnson, P. Keiter, H. Reynolds, J. R. Rygg, F. H. Séguin, and R. D. Petrasso
Phys. Rev. Lett. **114**, 215002 – Published 27 May 2015

Stopping of Deuterium in Warm Dense Deuterium from Ehrenfest Time-Dependent Density Functional Theory

R. J. Magyar*, L. Shulenburger, and A. D. Baczewski

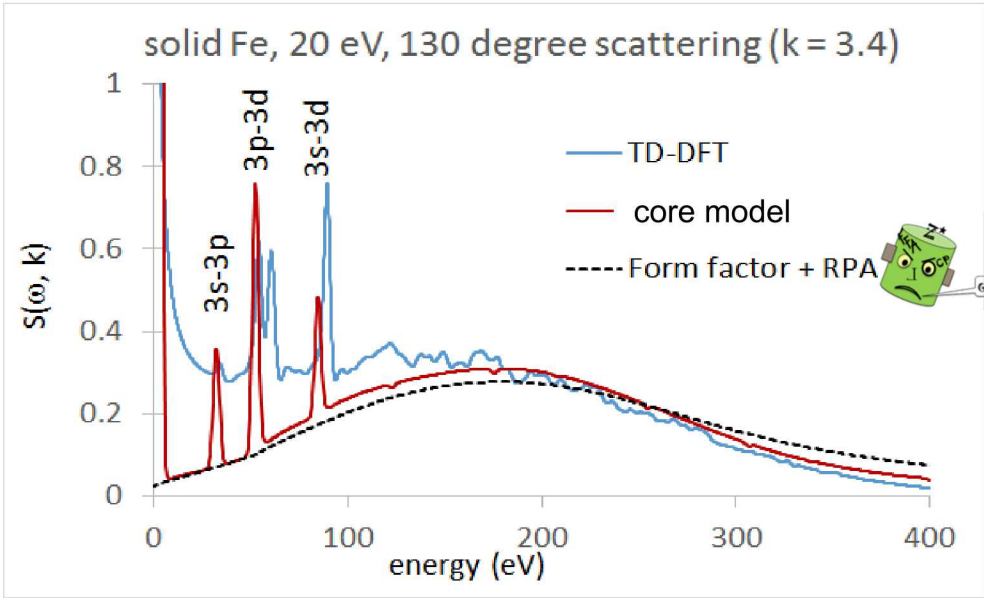
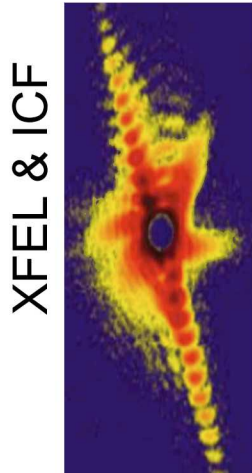
A. Cangi, A. Baczewski

... and x-ray scattering signals



$$\sigma(\omega), \epsilon(\omega), \kappa^{\text{th}}, \partial E / \partial x$$

X-ray
scattering



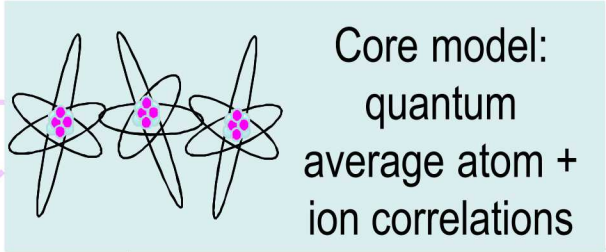
X-ray Thomson Scattering in Warm Dense Matter without the Chihara Decomposition

A. D. Baczewski, L. Shulenburger, M. P. Desjarlais, S. B. Hansen, and R. J. Magyar
Phys. Rev. Lett. **116**, 115004 – Published 18 March 2016

... and detailed opacities

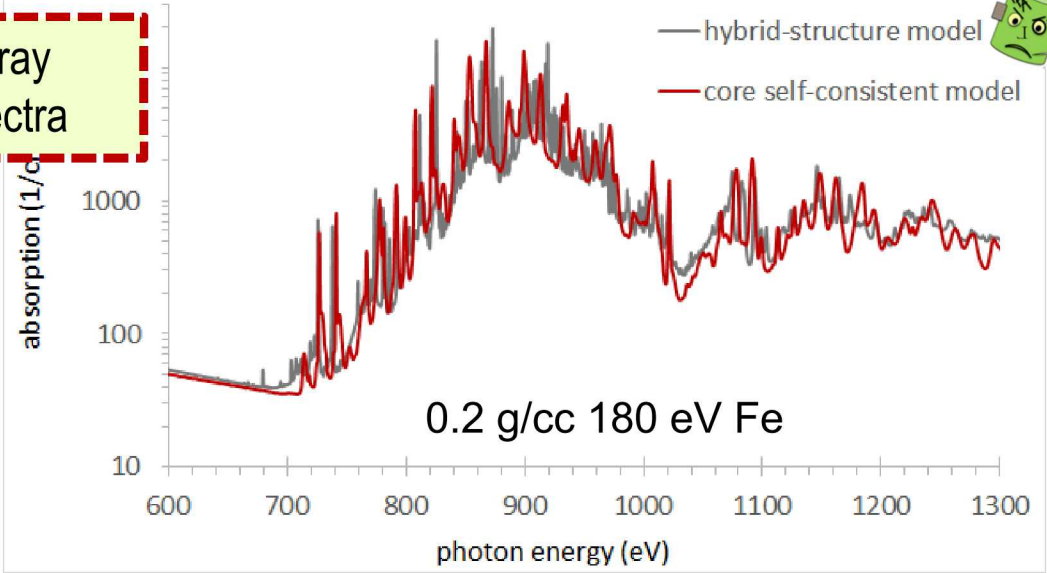
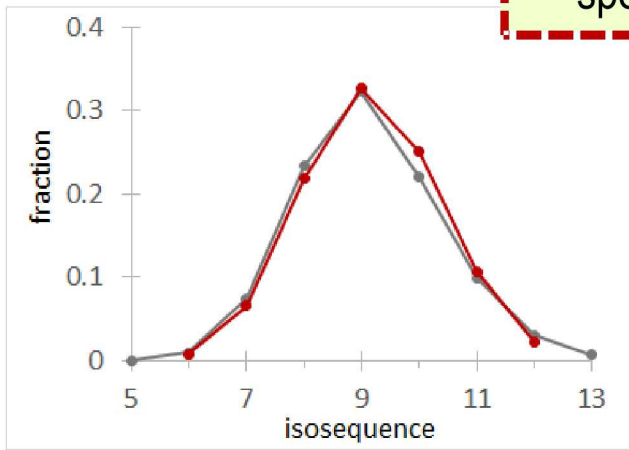
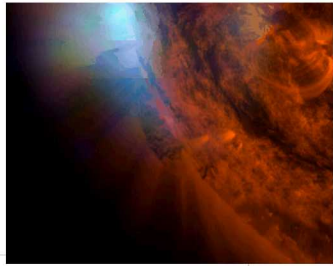
Multi-configuration atomic structure

Line broadening, opacities $\alpha(\omega)$



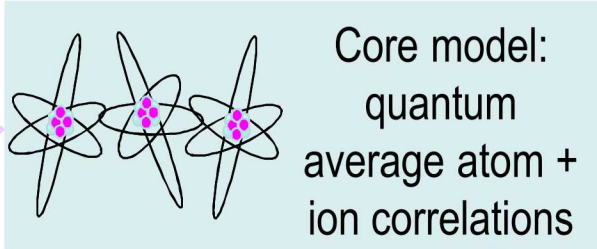
X-ray spectra

Solar physics

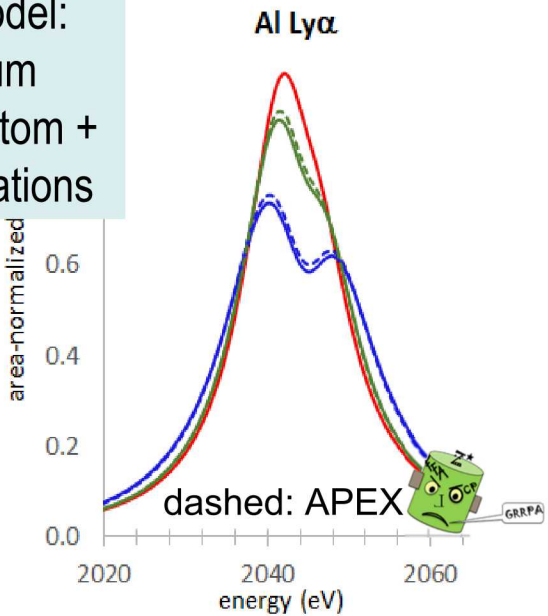
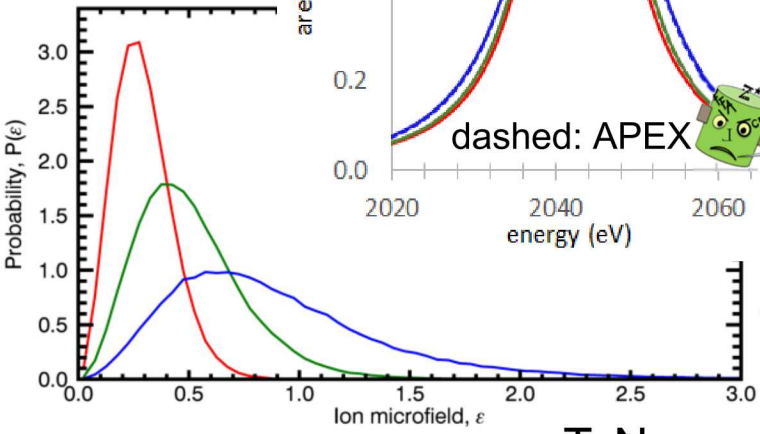
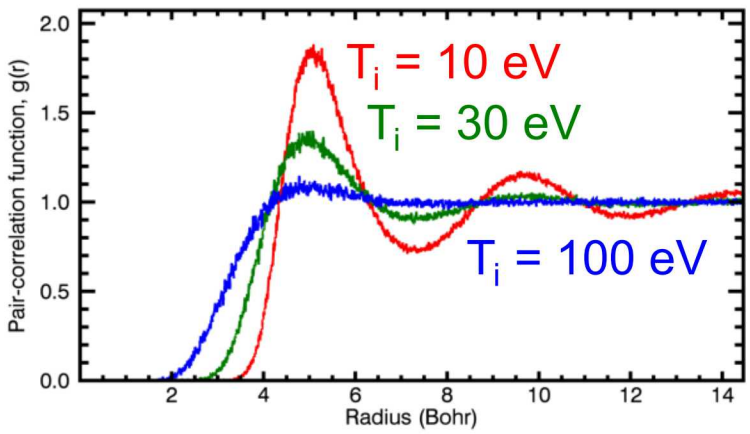


... with self-consistent line broadening

Line broadening, opacities



Solid-density Al, $T_e = 250$ eV



Cosmology, Astrophysics & ICF



T. Gomez

T. Nagayama

We are working to build a self-consistent model of material at extreme conditions with:

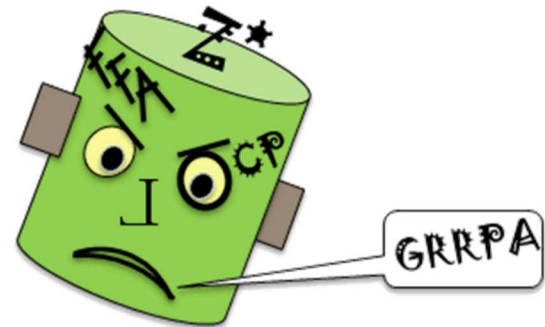
- Constitutive properties adequate for use in simulations
 - Enforced consistency can improve sensitivity studies & increase constraints
- Observable predictions adequate for comparison with experiment
 - Enforced consistency means that if part of this model is wrong, the whole thing is wrong – and its wrongness should be detectable

Conclusions

We are working to build a self-consistent model of material at extreme conditions with:

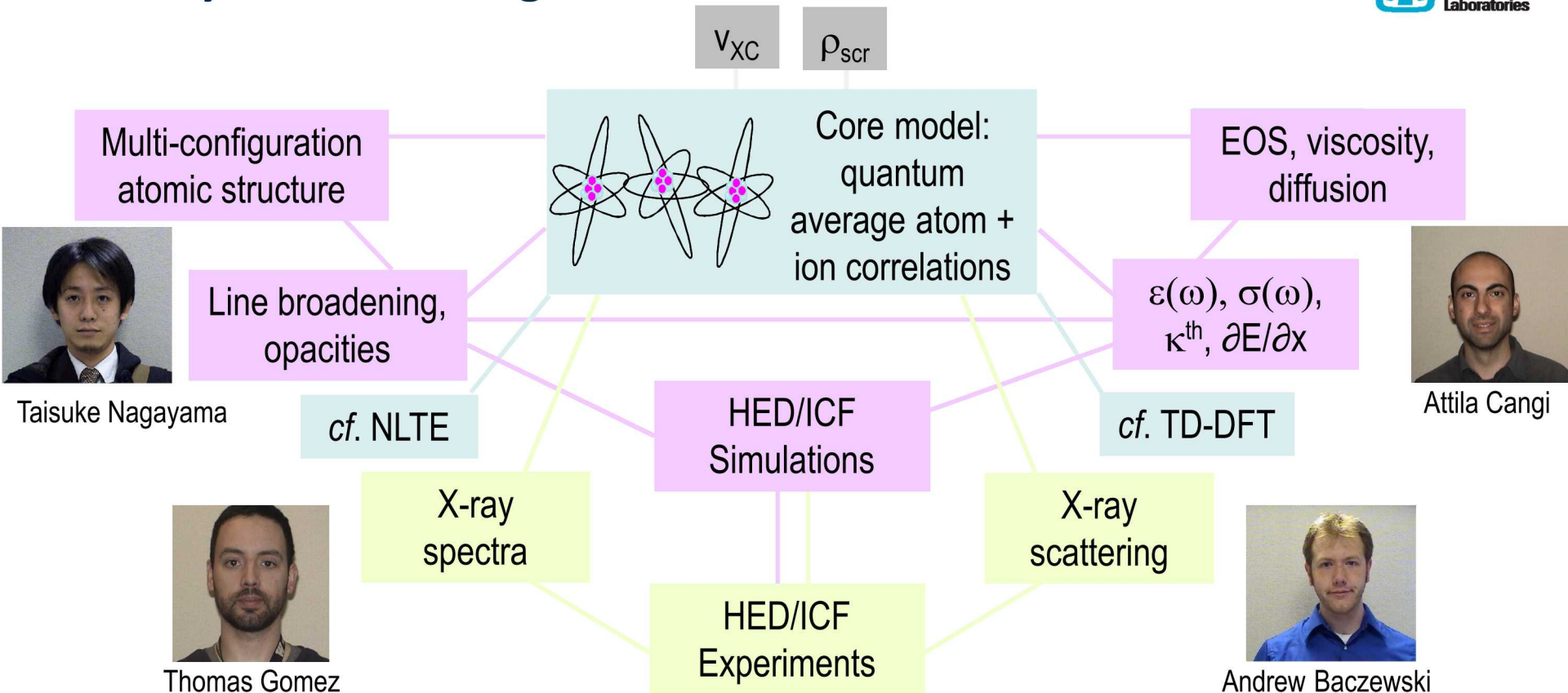
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For complex systems, internally consistent models that can be falsified by comparison to detailed data have more epistemic value than tunable models made to fit integrated data



Thank you!

Summary & acknowledgements



Thanks to:

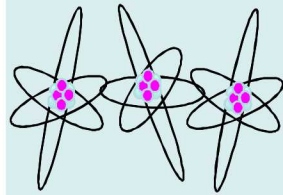
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Primary funding: U.S. DOE, Office of Science Early Career Research Program, OFES FWP-14-017426

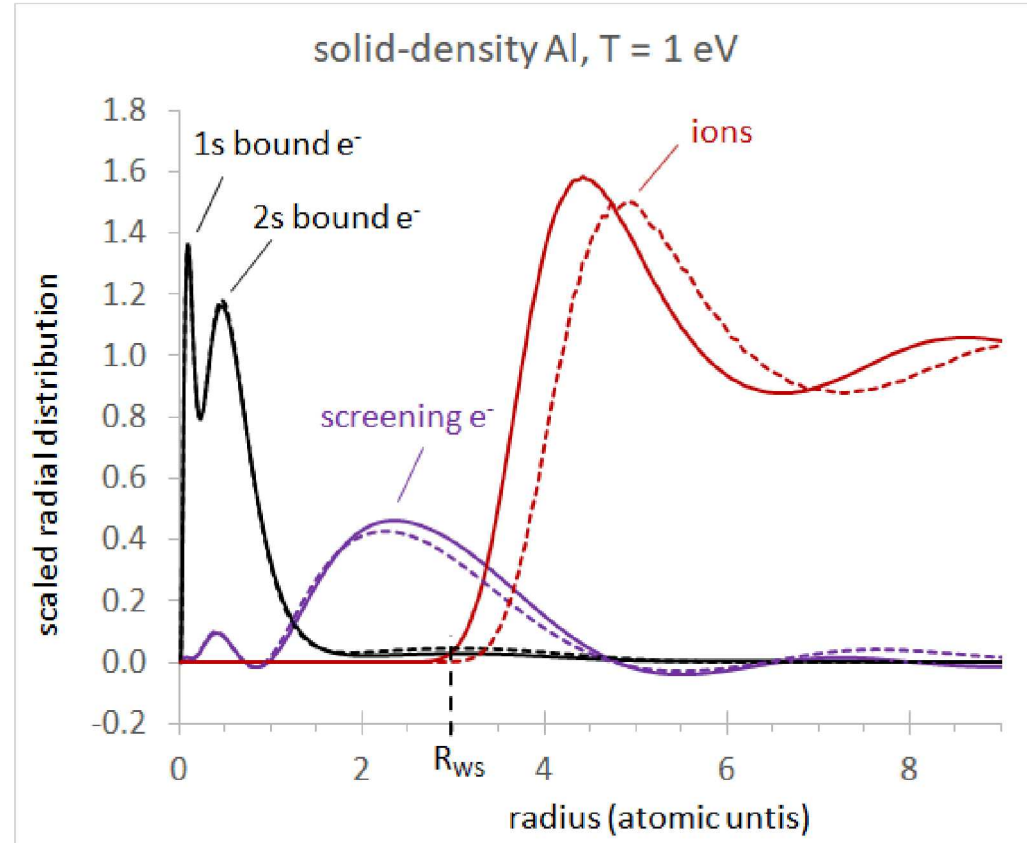
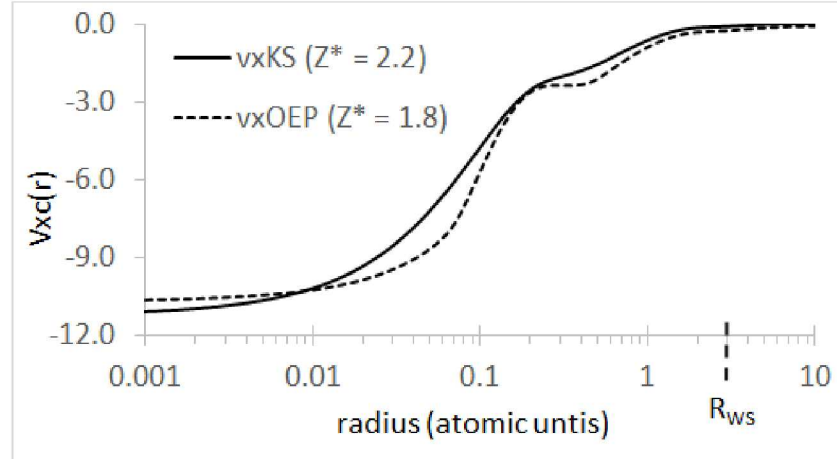
The core model is sensitive to the choice of exchange potential

V_{XC}

ρ_{scr}

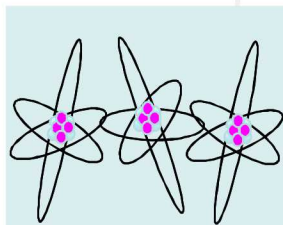


Core model:
quantum
average atom +
ion correlations

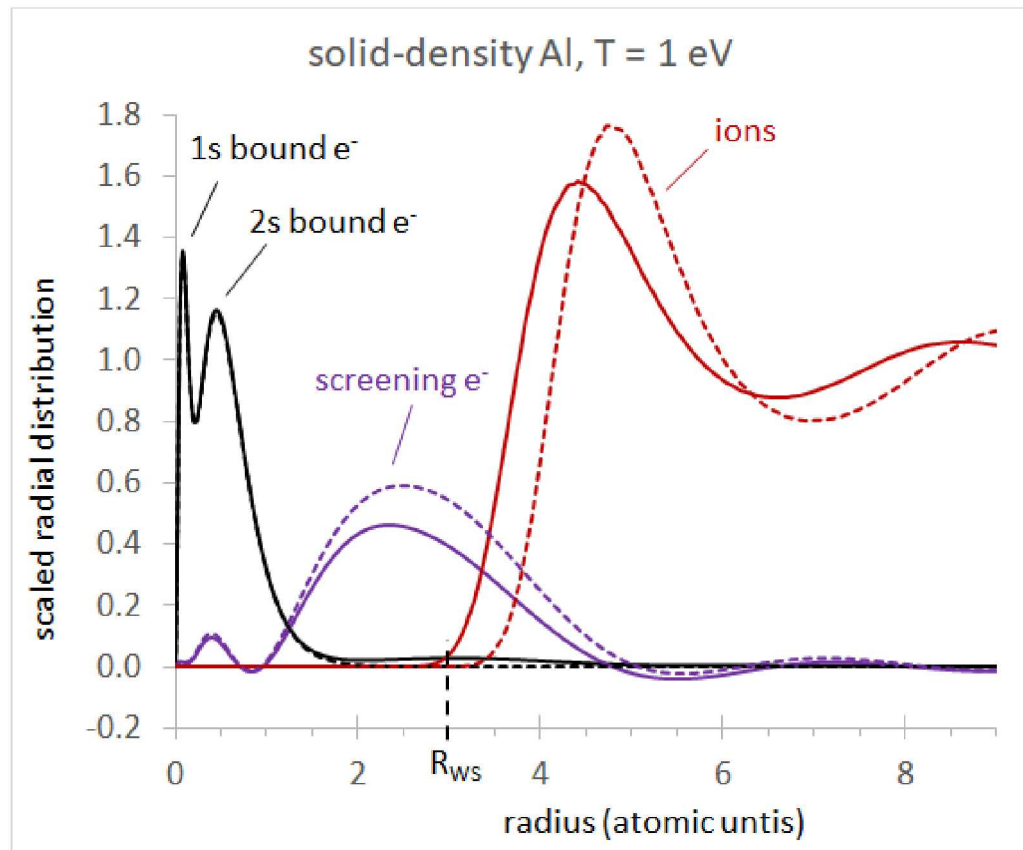
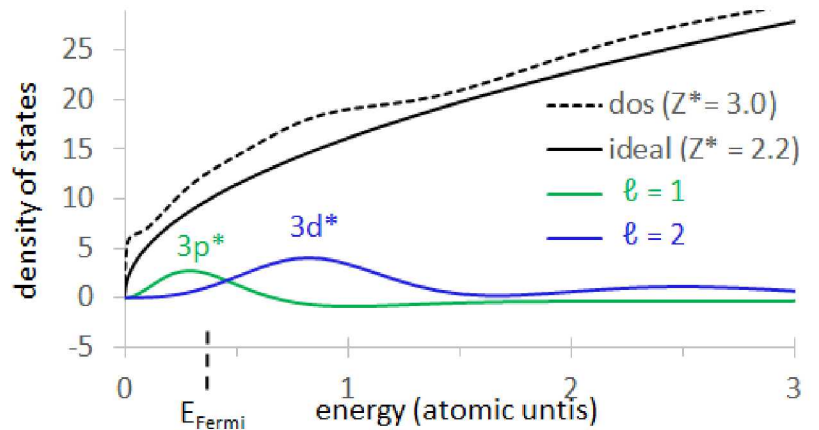


The core model is sensitive to whether the screening density includes the pressure-ionized “scars” of bound states

V_{XC} ρ_{scr}



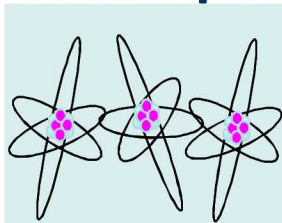
Core model:
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Examining the full dielectric function indicates a missing piece in the standard Chihara decomposition

Chihara decomposition:

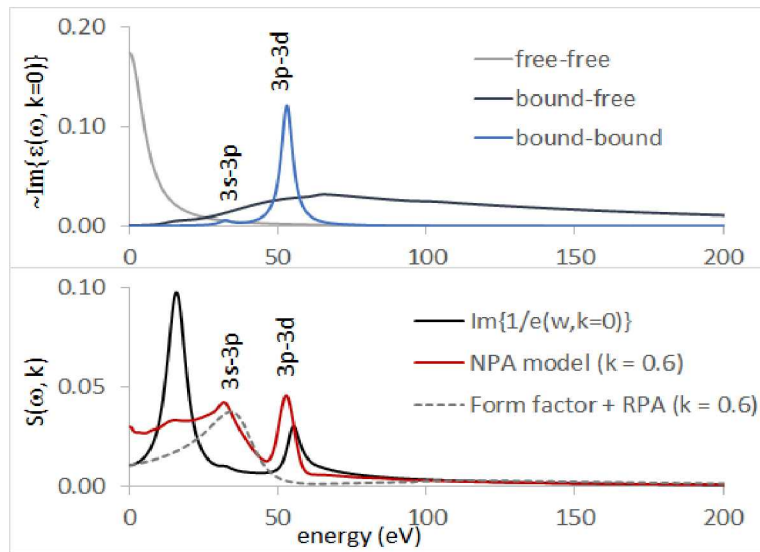
$$S(k, \omega) = \underbrace{|f_I(k) + q(k)|^2 S_{ii}(k, \omega)}_{\text{elastic}} + \underbrace{\bar{Z} S_{ee}(k, \omega)}_{\text{free-free}} + \underbrace{S_{bf}(k, \omega)}_{\text{bound-free}} + \underbrace{S_{bb}(k, \omega)}_{\text{bound-bound}}$$



Core model:
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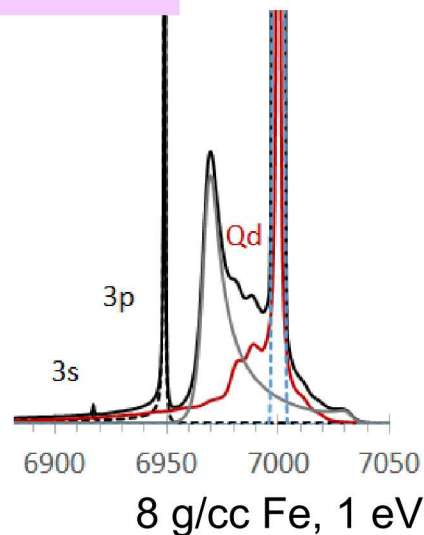
$$\sigma(\omega), \epsilon(\omega), \kappa^{\text{th}}, \partial E / \partial x$$

X-ray
scattering



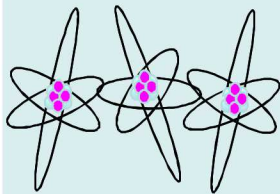
The bound-bound features in $\text{Im}\{1/\epsilon_{bb}(\omega)\}$ are reminiscent of sharp bound-free features previously noted by Johnson *et al.* and Souza *et al.**

5 g/cc Fe, 10 eV



*Johnson *et al.*, *PRE* **86**, 036410 (2012); Souza, Starrett *et al.*, *PRE* **89**, 023108 (2015)

Both the core model and TD-DFT capture bound-bound scattering features in $S(\omega, k)$

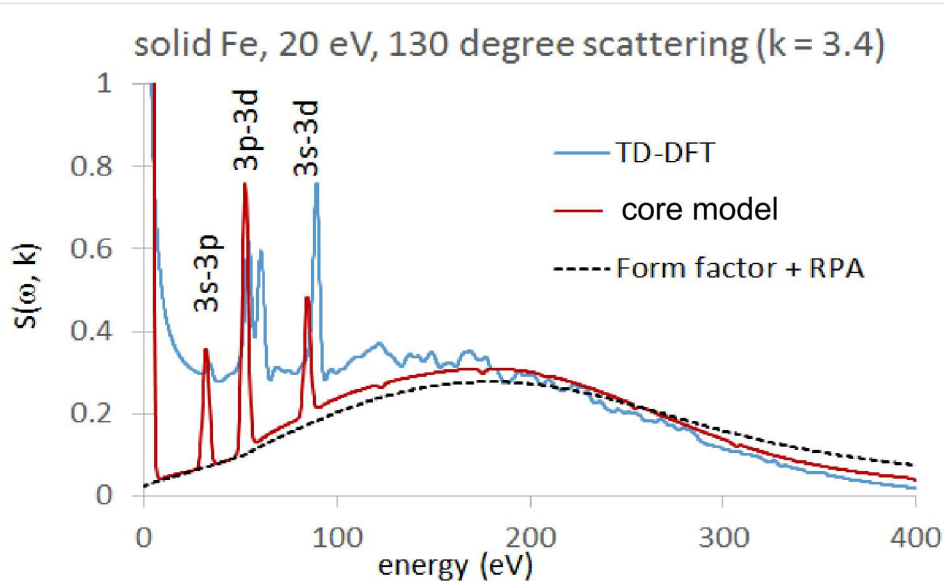


Core model:
quantum
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ion correlations

While $S(\omega, 0) \sim \text{Im}\{1/\epsilon(\omega, 0)\}$ roughly describes edges and line, a more general $S(\omega, k)$ can be obtained directly from core-model wavefunctions

X-ray
scattering

Experimental diagnostics benefit from consistent and complete atomic-scale models



A. Baczewski