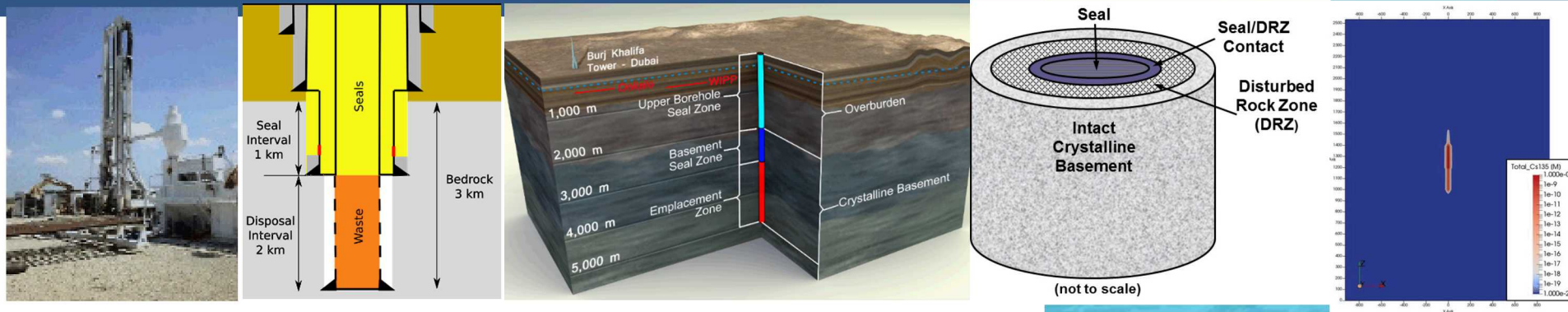


# Thermo-Hydro-Mechanical Evaluation of Critical Mass in Repository Far-Field



PRESENTED BY

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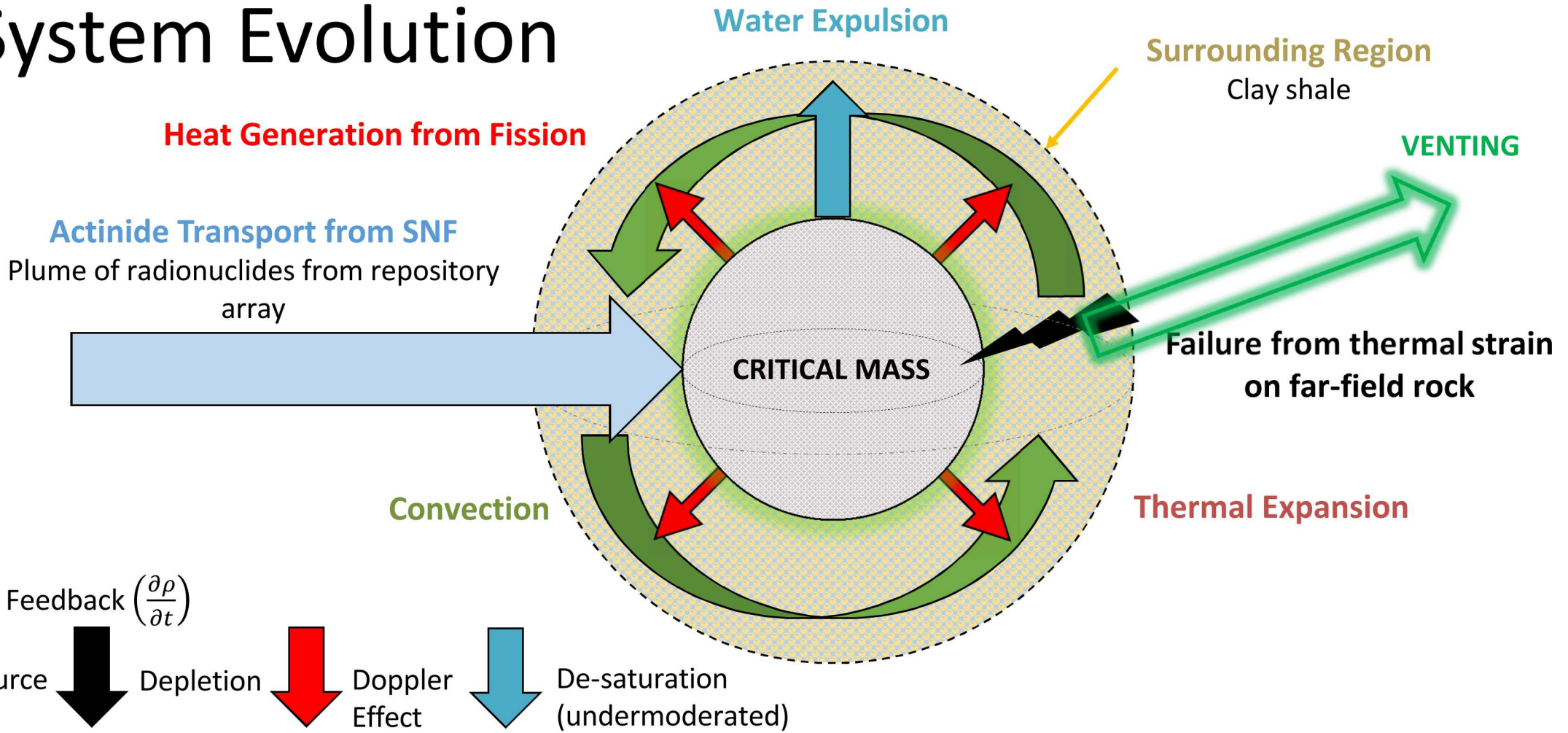
OECD/NEA 15<sup>th</sup> Information Exchange Meeting on Actinide and Fission Product Partitioning and Transmutation, Manchester, UK, 3 October 2018



# Objective

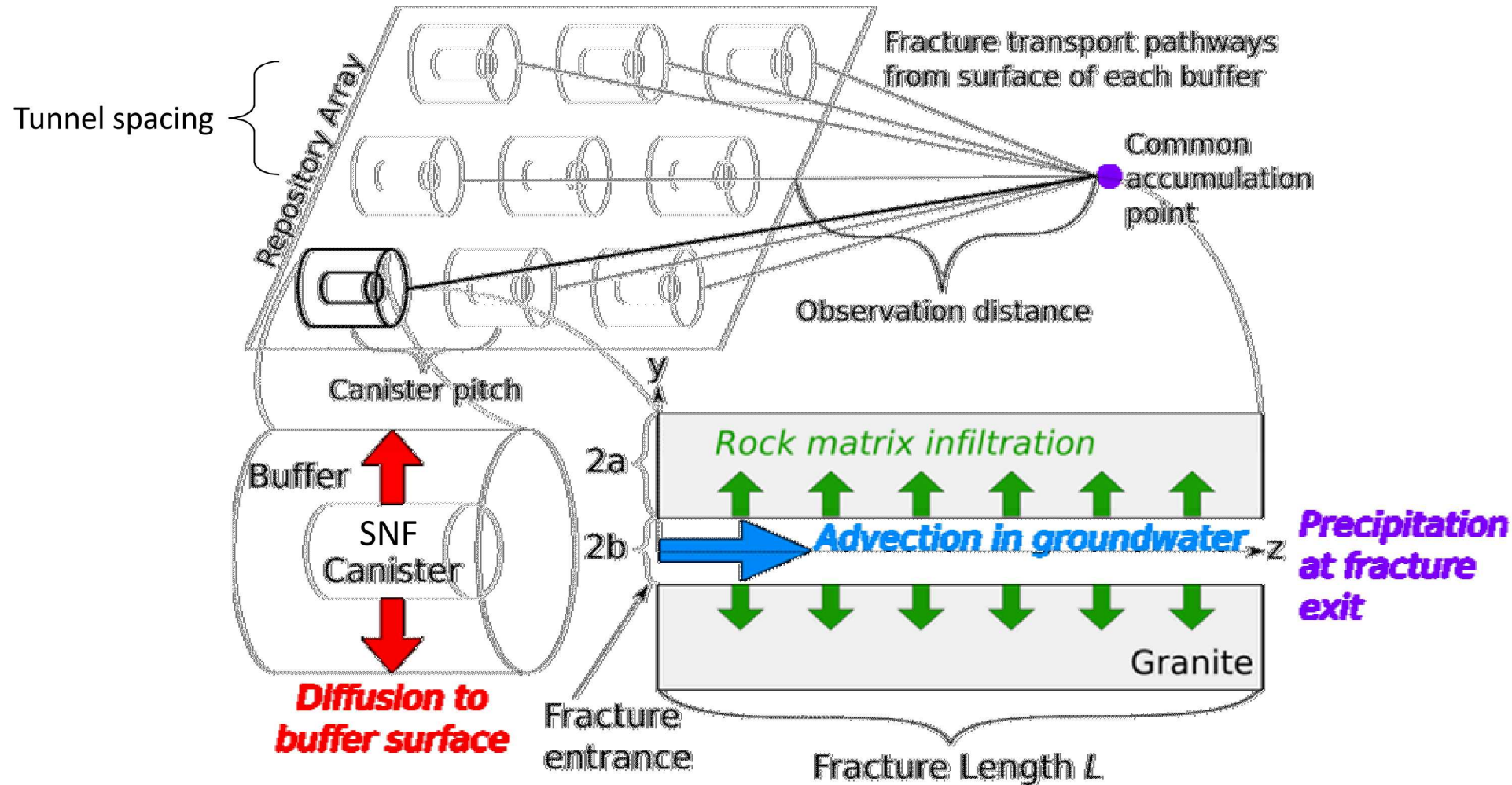
What are the long-term consequences of a heat-emitting critical mass deposited in the far-field of a repository?

# System Evolution



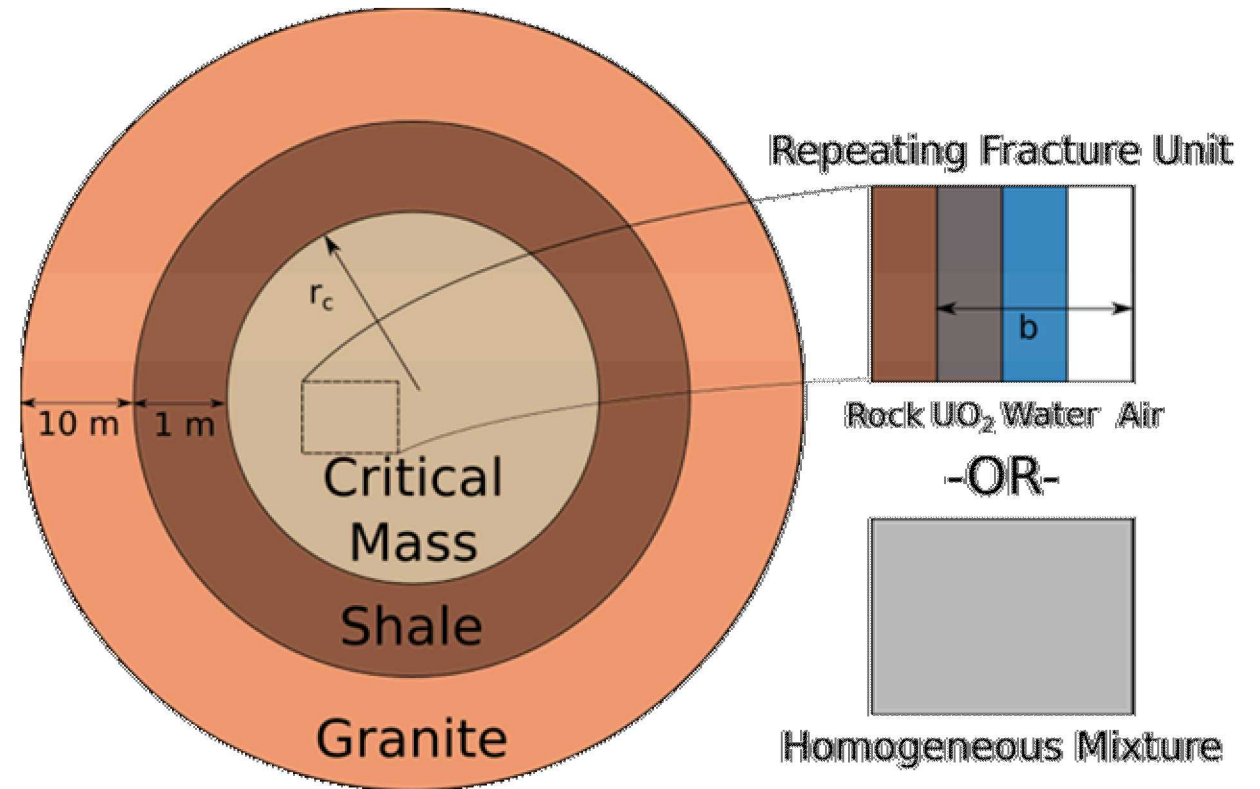
Critical mass in the far-field with hypothesized effects on reactivity

# Radionuclide Transport



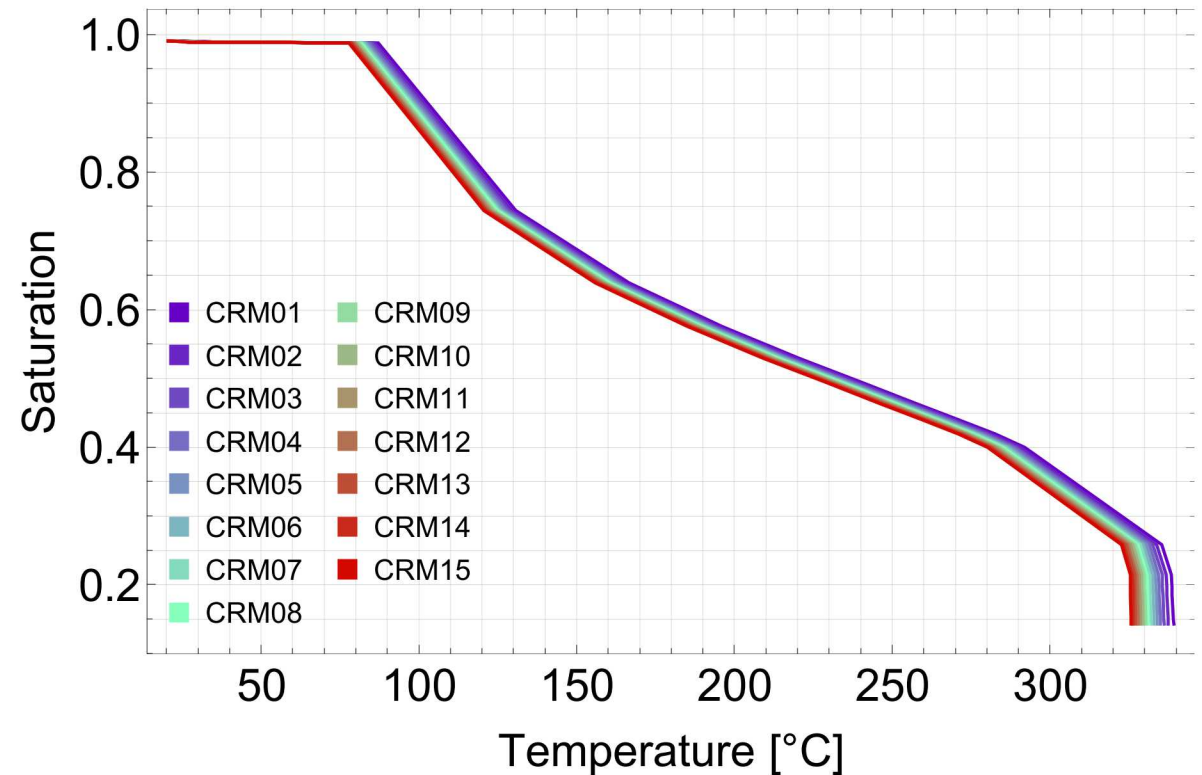
# Criticality

- Far-field precipitate is modeled as a sphere in a homogeneous or fractured geometry
- Shale serves as reducing sedimentary rock
- A parametric study based on the saturated porosity (VVF) and volume fraction of  $\text{UO}_2$  (HMVF) was performed to determine critical radius using MCNP6.1



# Unsaturated Heat and Mass Transfer

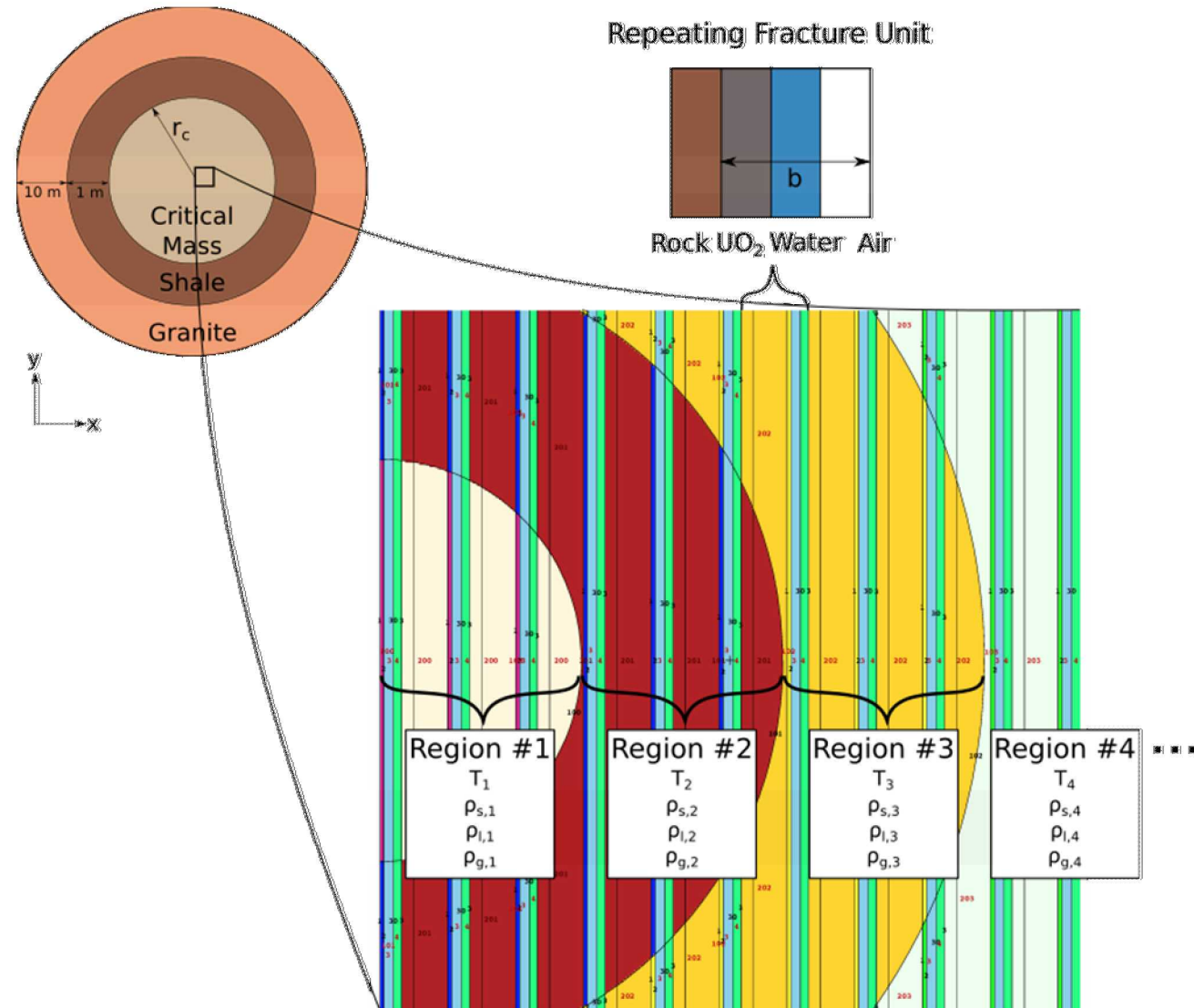
- The TOUGH2 code is used to evaluate the evolution of saturation and temperature in the critical deposition
- Van Genuchten-Mualem models are employed for capillary pressure and relative conductivity of pore fluid [1]
- Fission power distributions calculated by CINDER are employed as source terms



The behavior of saturation with temperature for each discrete region of the 5 MTU 2 wt% homogeneous critical mass ("CRM") as steady-state is reached for a dry environment at 0.1% saturation. The regions are numbered from the core outwards.

# Modification of MCNP cell densities

- The average temperature, saturation, and fluid densities from the TOUGH2 simulation are applied to discrete spherical shells of critical mass
- Saturation is varied in fractured geometry by modifying the volume of the air region in the repeating unit



# Temperature Evaluation at Quasi-Steady-State

- Quasi-steady-state (QSS) approach assumes fission power generation and heat dissipation from the critical system are in a relative steady state

$$\phi N_A \sum_{i \in TFM} E_{f,i} \sigma_{f,i} n_i(t) = MC_p \frac{d\Delta T}{dt} - hA\Delta T$$

- System remains critical until competing reactivity feedback mechanisms result in subcriticality

$$\alpha_T(T) \frac{\partial \Delta T}{\partial t} + \alpha_{25} (n_{25} - n_{25}^0) \frac{\partial n_{25}}{\partial t} + \alpha_{28} \frac{\partial n_{28}}{\partial t} + \alpha_R(\Delta T) f_R(\Delta T) \frac{\partial \Delta T(t)}{\partial t} = 0$$

# Nuclide inventories

- Fissile material

$$\dot{n}_{25}(t) = \dot{S}_{25} + \lambda_{49}n_{49}(t) + \phi(t)[- \sigma_c^{25}n_{25}(t) - \sigma_f^{25}n_{25}(t)]$$

$$\dot{n}_{49}(t)$$

$$= \dot{S}_{49} - \lambda_{49}n_{49}(t) + \phi(t)[\sigma_c^{28}n_{28}(t) - \sigma_c^{49}n_{49}(t) - \sigma_f^{49}n_{49}(t)]$$

- Fertile material

$$\dot{n}_{28}(t) = \dot{S}_{28} - \sigma_c^{28}n_{28}(t)\phi(t)$$

# Mechanical Failure Metric

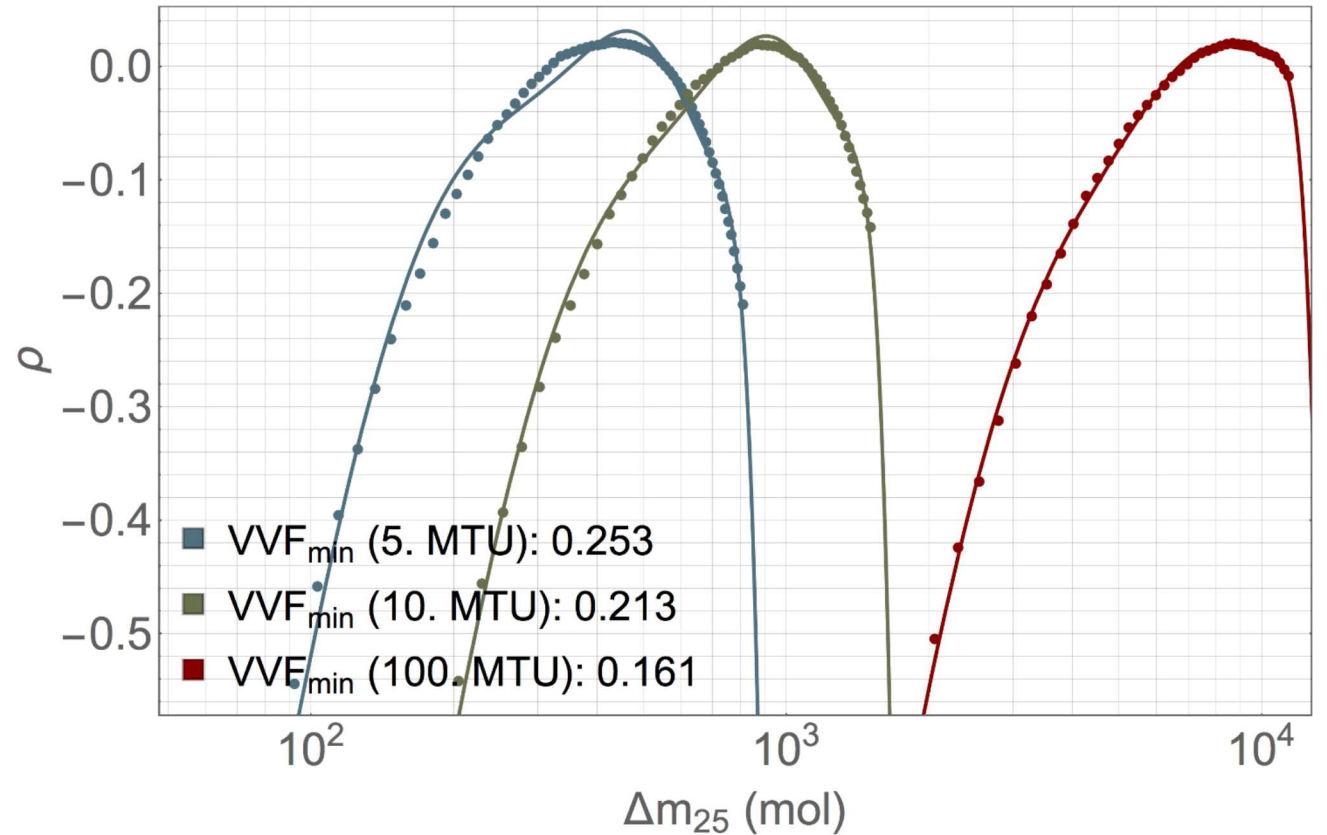
- The bedrock is assumed to fail via a steady-state thermal creep, which is governed by a power law relationship:

$$\epsilon = \begin{cases} \int_0^t A \left(\frac{\sigma}{G}\right)^n e^{-Q/R[T(\tau)+273.15]} d\tau & 150^\circ\text{C} \leq T < 1250^\circ\text{C} \\ 0 & T < 150^\circ\text{C} \end{cases}$$

- The total strain is obtained through numerical integration over time using  $T(t)$  results of QSS model, where a 1.5% failure metric is employed

# Positive Feedback from U-235 is Limited

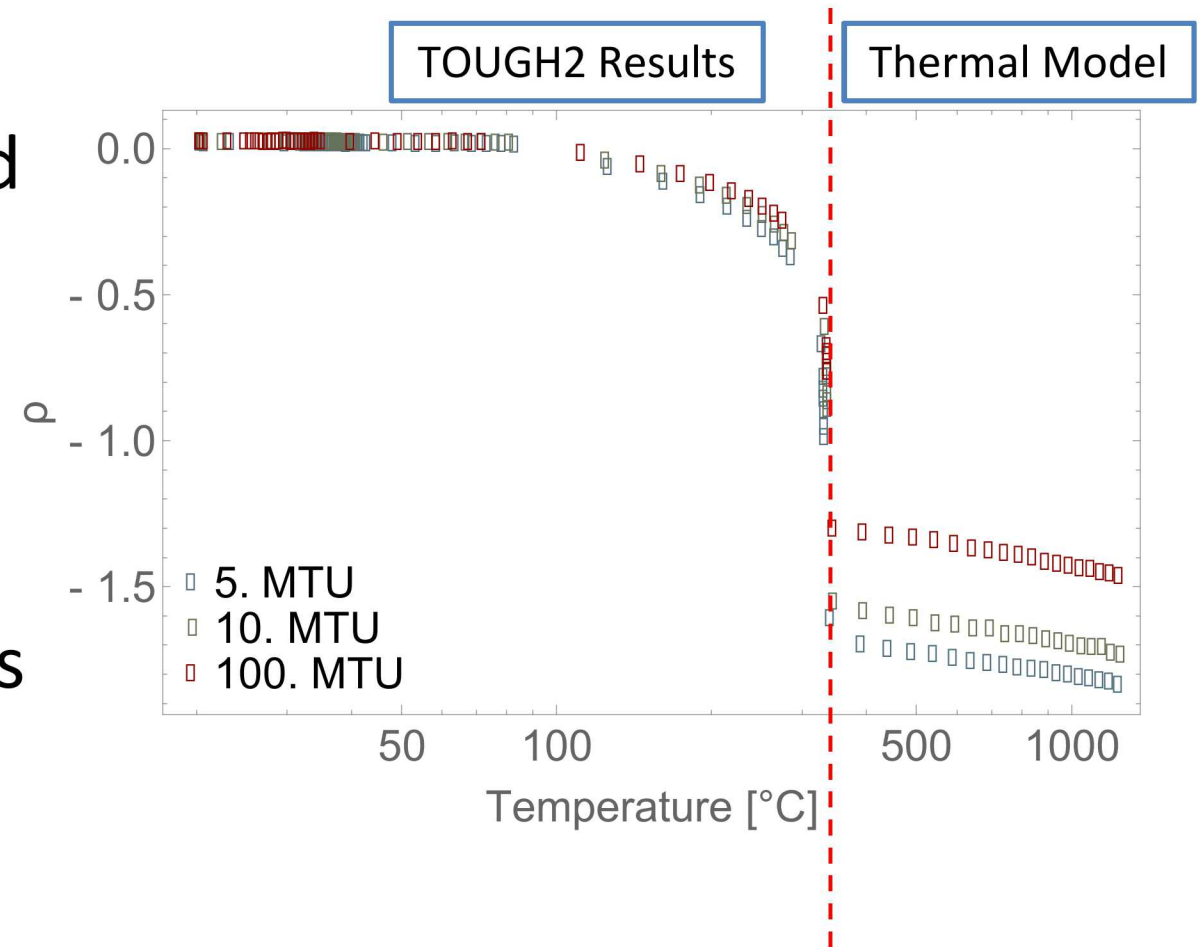
- After criticality is reached, the continued arrival of U-235 from the repository plume has limited positive reactivity ( $\rho$ ) feedback
- At some point, the system becomes undermoderated



Reactivity effect of displacing water with 2 wt%-enriched uranium in the void space of minimum critical masses, expressed in terms of moles of U-235. Shown with polynomial fit curves.

# Doppler Effect

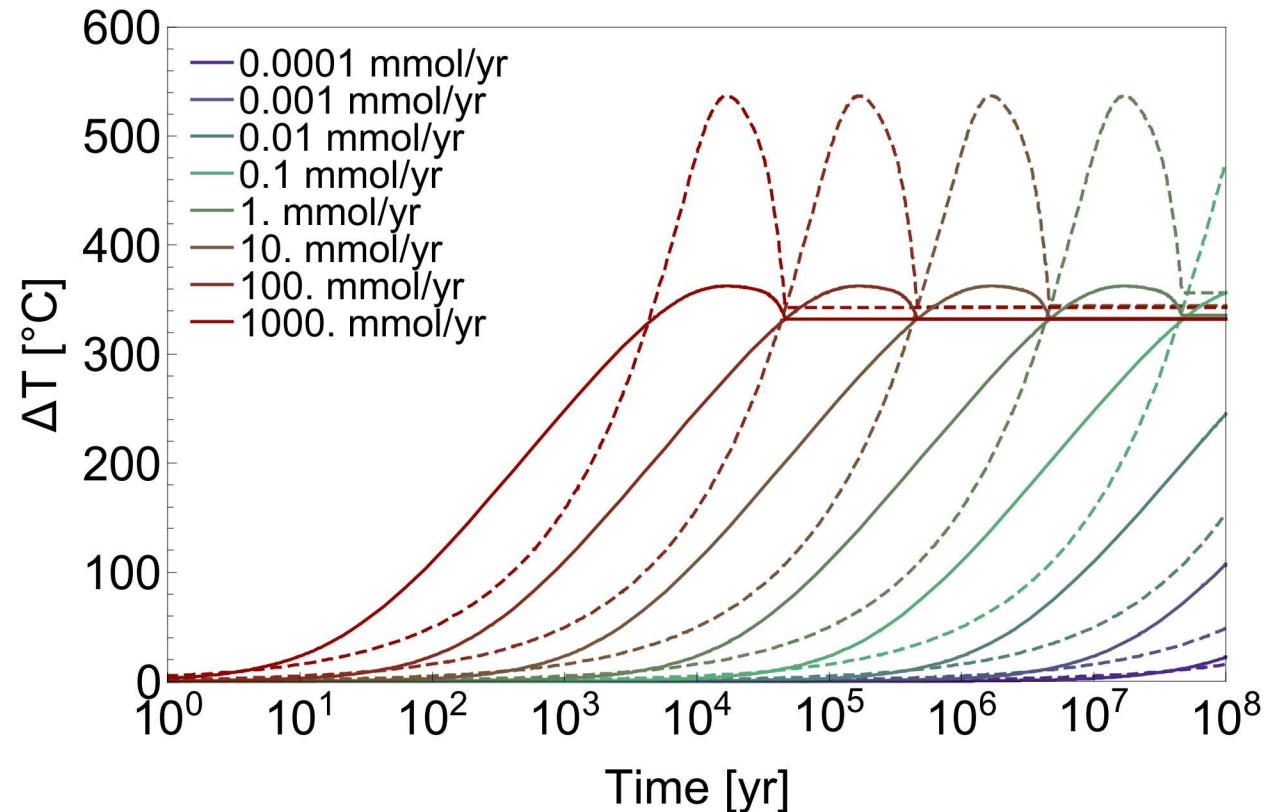
- Cross sections are modified based on average cell temperatures using the On-the-Fly Doppler Broadening code [2]
- Thermal resistance model extrapolates system temperatures to rock melting point ( $\approx 1250^{\circ}\text{C}$ )
- Regression is performed for temperature feedback coefficient



Reactivity feedback for fractured geometry at various critical masses of 2 wt% enrichment in the fractured configuration

# Lumped System Temperature

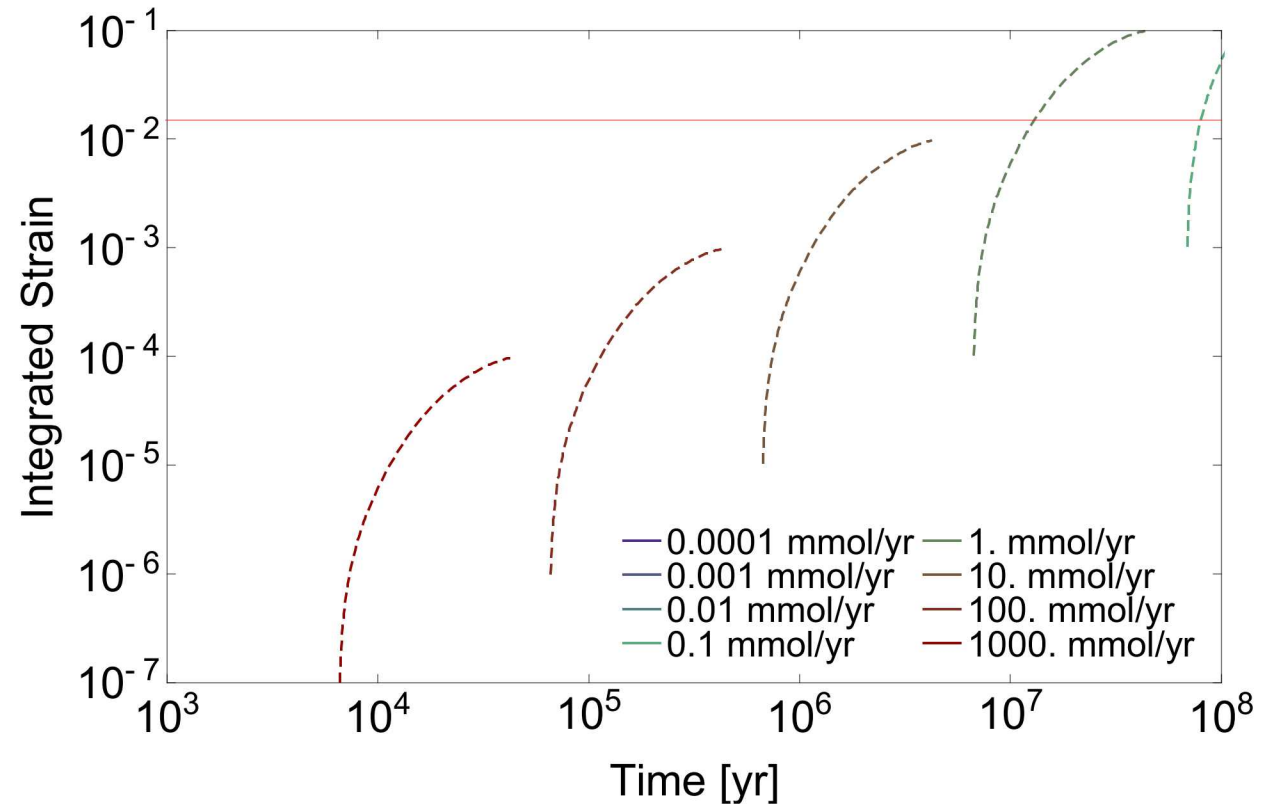
- A maximum  $\Delta T$  can be achieved before uranium fills the pore space, with a minimum uranium influx of 1 mmol/yr from the repository
- For reference, the Nopal I deposit at Peña Blanca (welded tuff) has dissolution rates of  $\sim 2 \text{ mmol/m}^3/\text{yr}$  within fractured zones [3]



The temperature change over time in the 5 MTU 2 wt% homogeneous critical mass as parametrized by the source term of uranium (in mmol/yr) for piecewise (solid) and Gaussian (dashed) fits of  $\alpha_T$ .

# Strain of Far-field Host Rock

- The time- and temperature-dependent creep relationship only allows for certain influxes to meet the failure metric
- The 1 mmol/yr source term allows for excessive strain to be reached at about  $10^7$  years post-formation
- Compare to 0.055 mmol/yr value observed in very conservative transport analysis [4]



The integrated creep strain over time in the 5 MTU 2 wt% homogeneous critical mass as parametrized by the source term of uranium (in mmol/yr) for a Gaussian fit of  $\alpha_T$ .

# Discussion

- The time scale needed for excessive plastic deformation from thermal creep exceeds a million years
- This comes with amplified source terms of heavy metal not likely to be observed in a reducing, water-saturated host rock even with heavily conservative assumptions
- This conservatism is compounded with the small window of applicability for creep strain to take place

# Conclusions

- The failure of natural barriers from a long-term, sustained criticality event is considered to be highly implausible for direct disposal
- Although steady-state creep was isolated as the performance metric of interest, previous studies with high-energy, explosive events were also considered to be very improbable, even with more enriched materials [5]

# Acknowledgments

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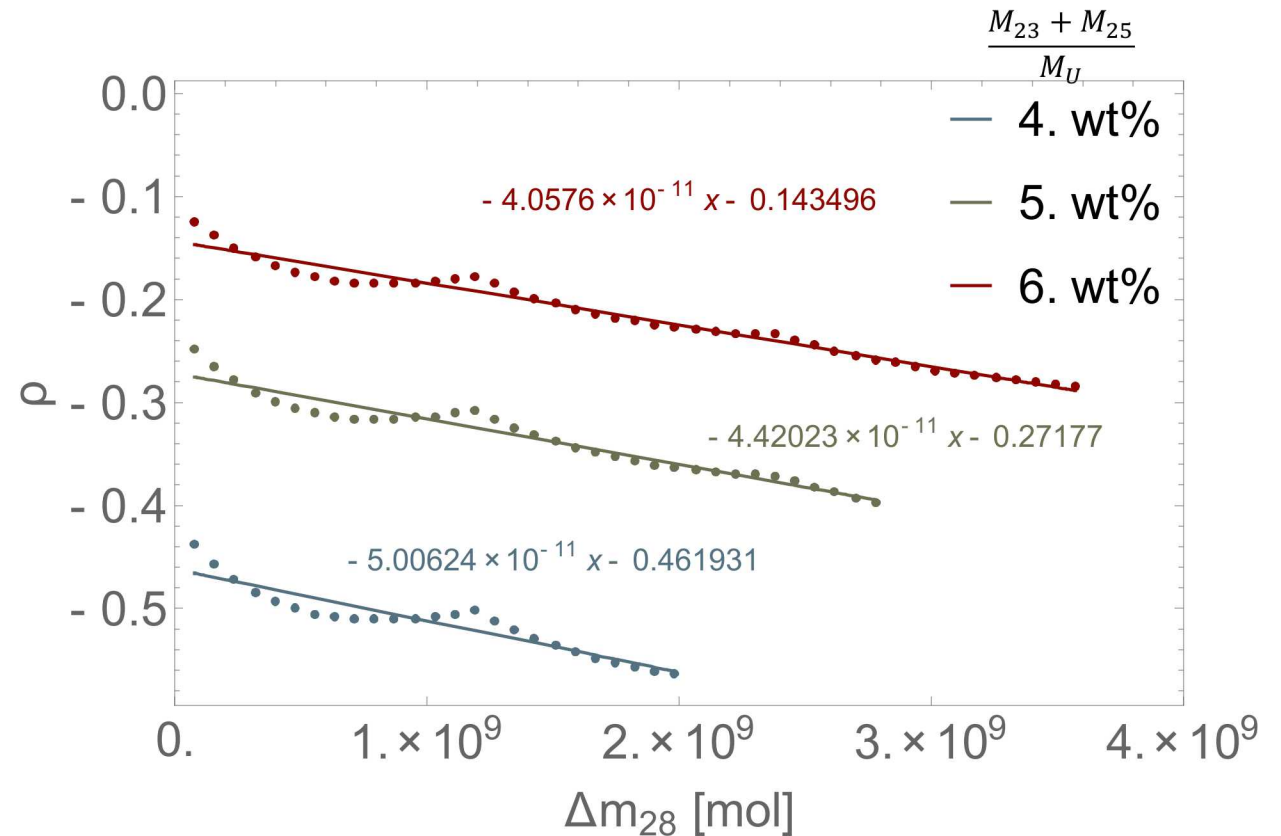
# References

- [1] M. T. Van Genuchten (1980), “A closed-form equation for predicting the hydraulic conductivity of unsaturated soils,” *Soil Sci. Soc. Am. J.*, 44[5], pp. 892–898.
- [2] F. B. Brown, W. R. Martin, G. Yesilyurt, and S. Wilderman (2012), “On-the-Fly Neutron Doppler Broadening for MCNP,” Los Alamos Natl. Lab.
- [3] S. J. Goldstein et al. (2010), “Uranium-Series Constraints on Radionuclide Transport and Groundwater Flow at the Nopal I Uranium Deposit, Sierra Peña Blanca, Mexico,” *Env. Sci. & Technol.*, 44[5], pp. 1579-1586.
- [4] A. Salazar (2018), “Criticality in the far-field of a granitic repository for used nuclear fuel,” University of California, Berkeley, Berkeley, CA.
- [5] Kastenbergh, et al (1996), “Considerations of Autocatalytic Criticality of Fissile Materials in Geologic Respositories”, *J. Nuc. Tec*, 115[3], pp. 298-310.

# BACKUP

# Effect from U-238 in the Plume

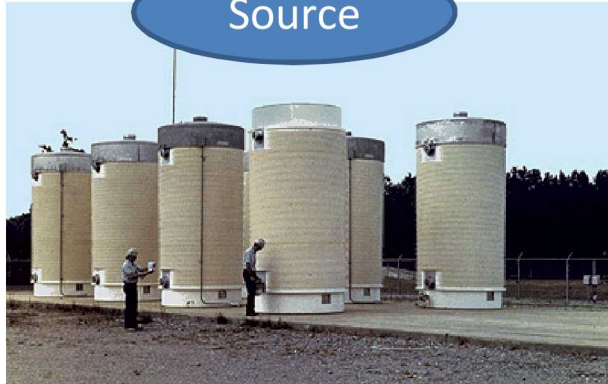
- Data for higher-enriched precipitates were interpolated to probe effect of U-238 influx
- The proportion of U-238 in the superposed uranium plume eventually becomes dominant and constitutes a negative reactivity feedback mechanism



Reactivity effect of displacing water with pure U-238 in the void space of precipitates at different initial enrichments, expressed in terms of moles of U-238. The heavy metals are assumed to be instantaneously mixed. Shown with linear best-fit curve.

# Integrated Modeling Approach

Source



[NRC]

Characterization of UNF source term in the United States

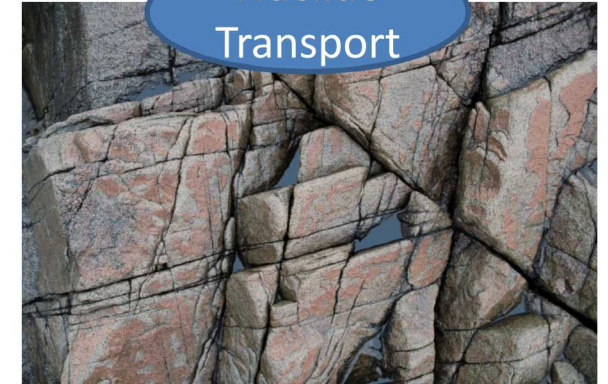
System



[POSIVA]

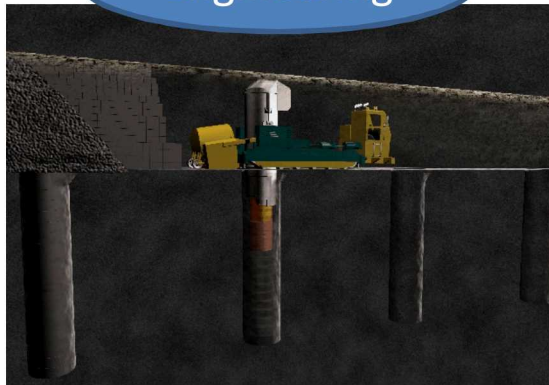
Canister and repository configuration

Nuclide Transport



Dissolution of UO<sub>2</sub> fuel and transport in granitic fractures

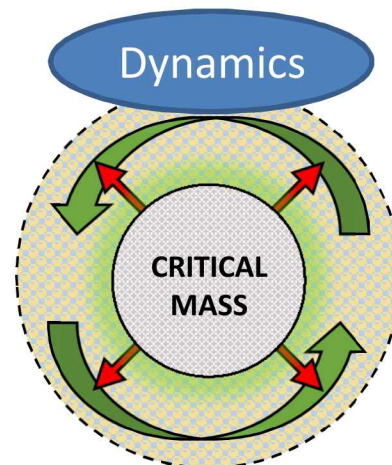
Engineering



[POSIVA]

Expanded view of criticality safety criteria for repository loading

Dynamics



Dynamic evaluation of heat and mass transfer with sustained criticality

Criticality

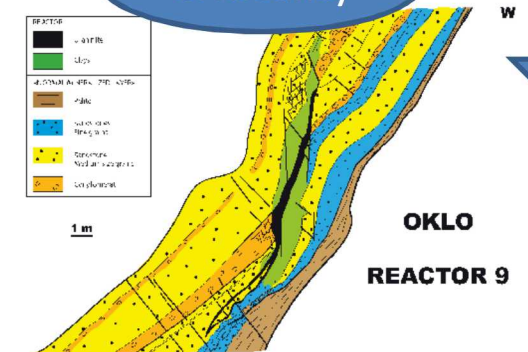


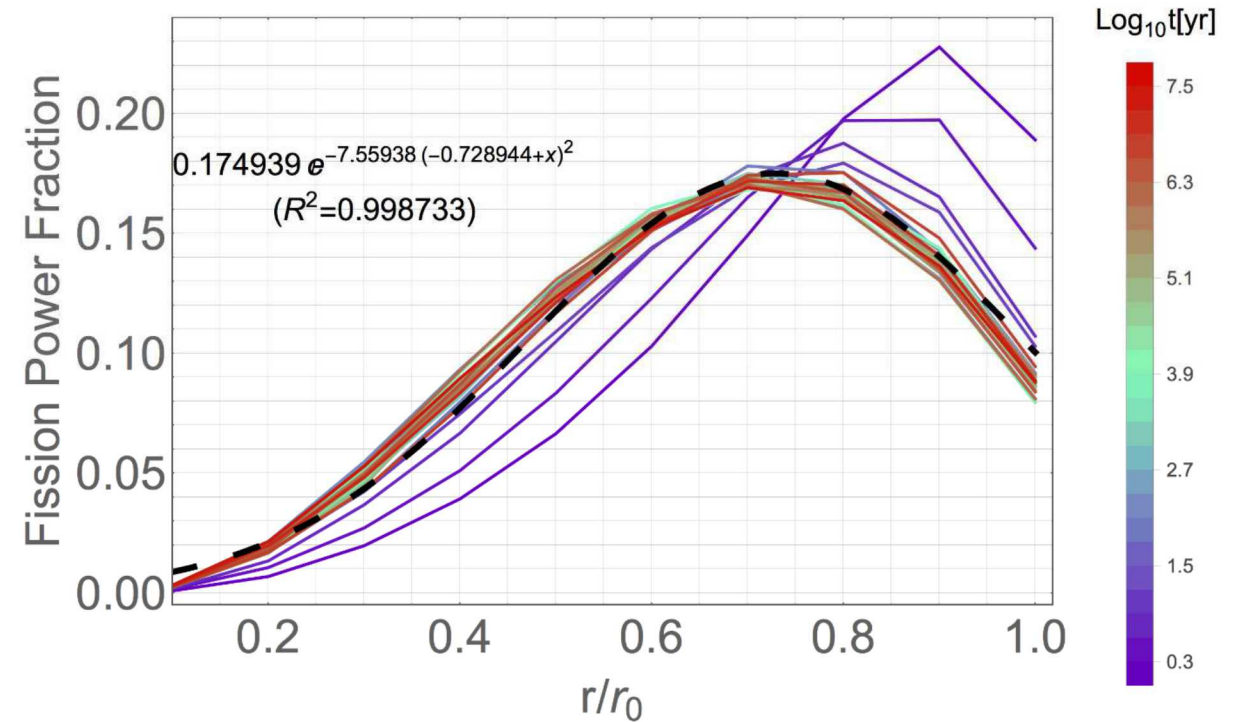
Fig. 2 East-West section of the R79 reactor area

Re-concentration of fissile material in reducing region of the far field

[Bentridi et al, 2011]

# Fission Power in Precipitate Varies Radially

- CINDER module in MCNP6.1 employed for depletion to probe the spatial distribution of fission reactions
- Gradual time steps leading up to  $10^8$  years
- Peaked fission power distribution from shale reflector



Fission power distribution in the critical mass for 100 MT Fractured geometry at  $10 \text{ kW}_t$  output for 2.25 wt% enriched precipitate