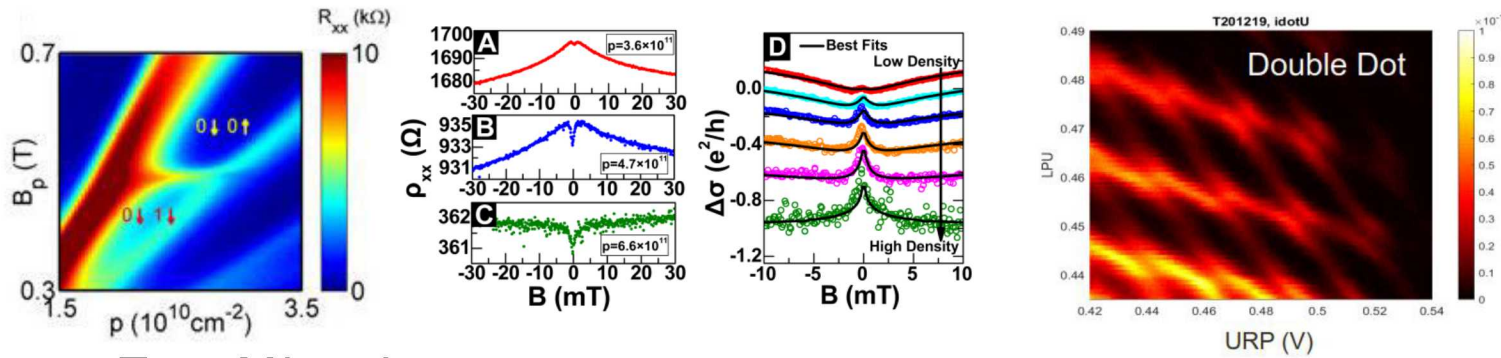
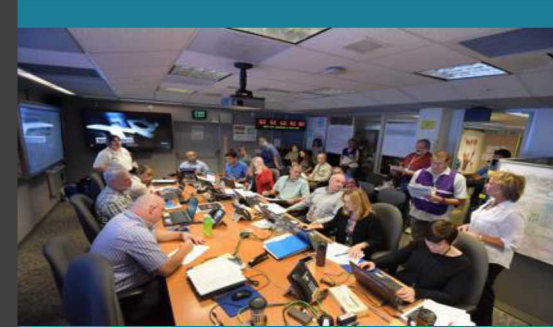




# Ge/SiGe quantum electronic devices



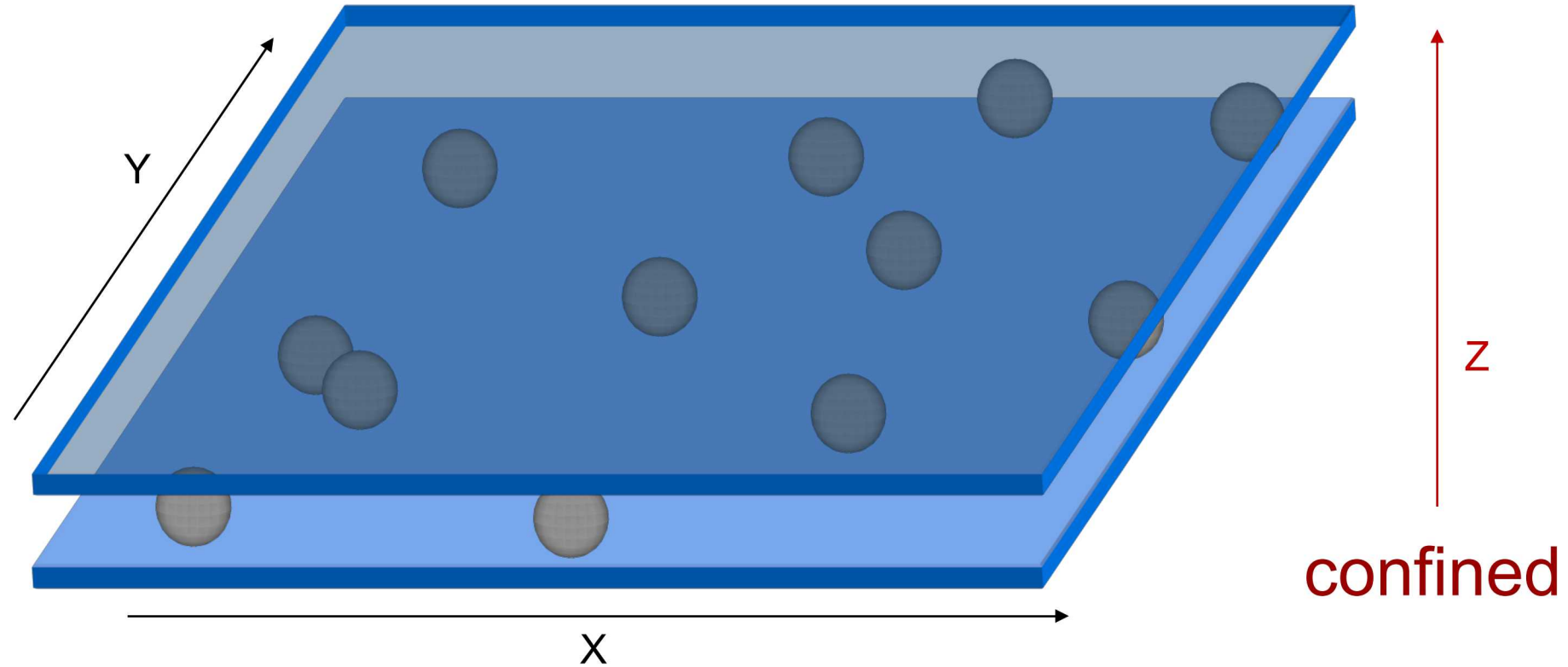
Tzu-Ming Lu

Department of Quantum Phenomena,  
Sandia National Laboratories, New Mexico

# Outline

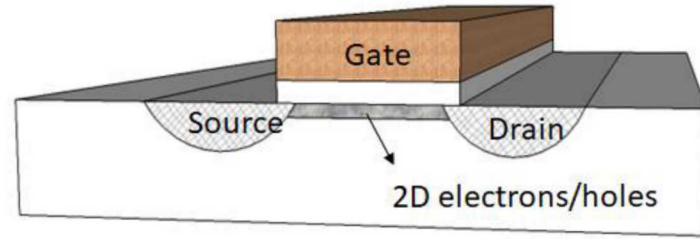
- Ge/SiGe heterostructures
- Device operation
- Properties of 2D holes in Ge/SiGe
- Quantum Hall ferromagnetic transition
- Spin qubits in Ge/SiGe
- Summary

## 2D electrons/holes

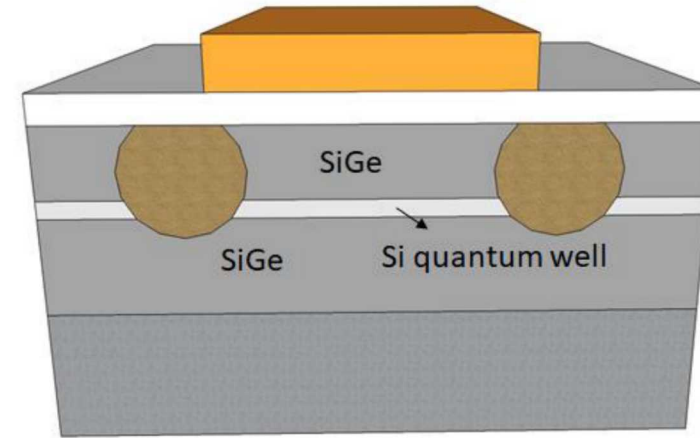


# 2D electrons in Si

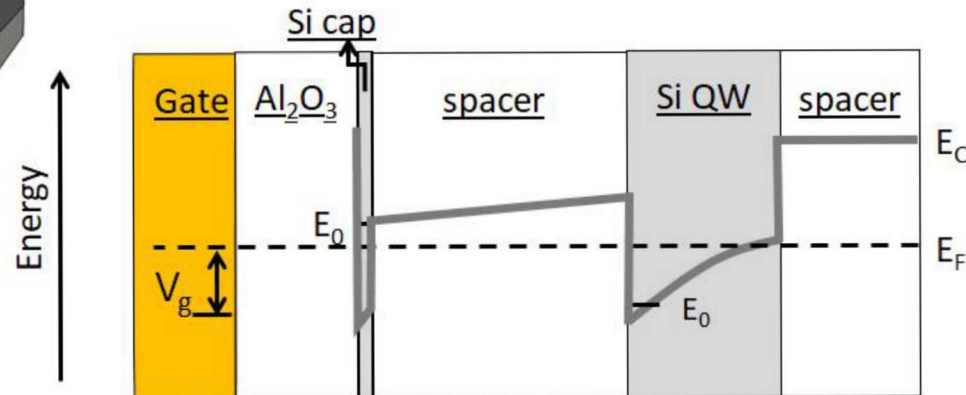
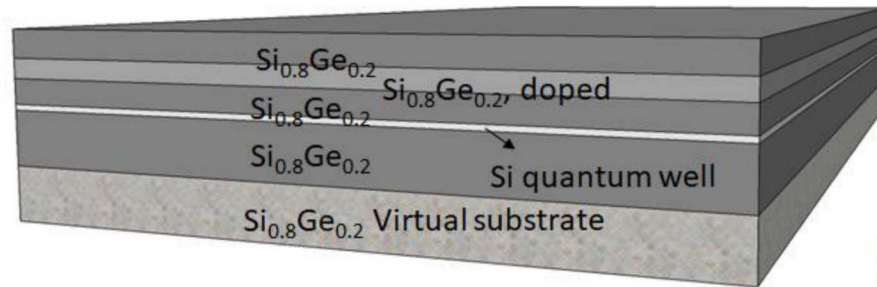
## Si MOSFET



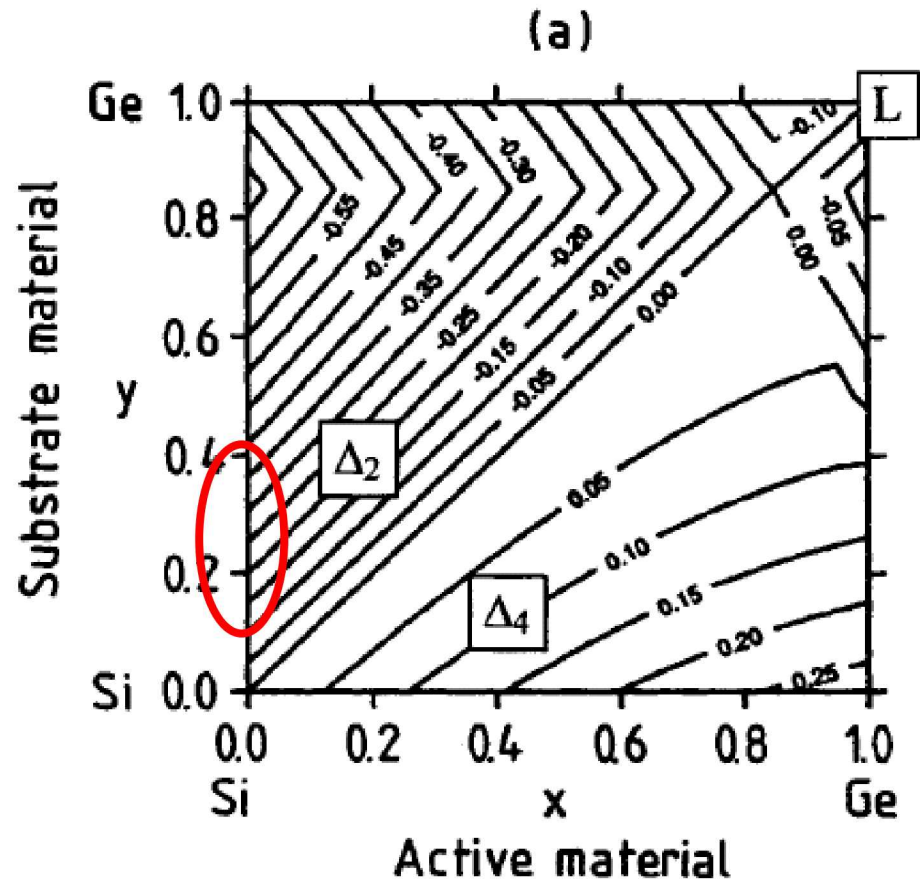
## Undoped Si/SiGe HFET



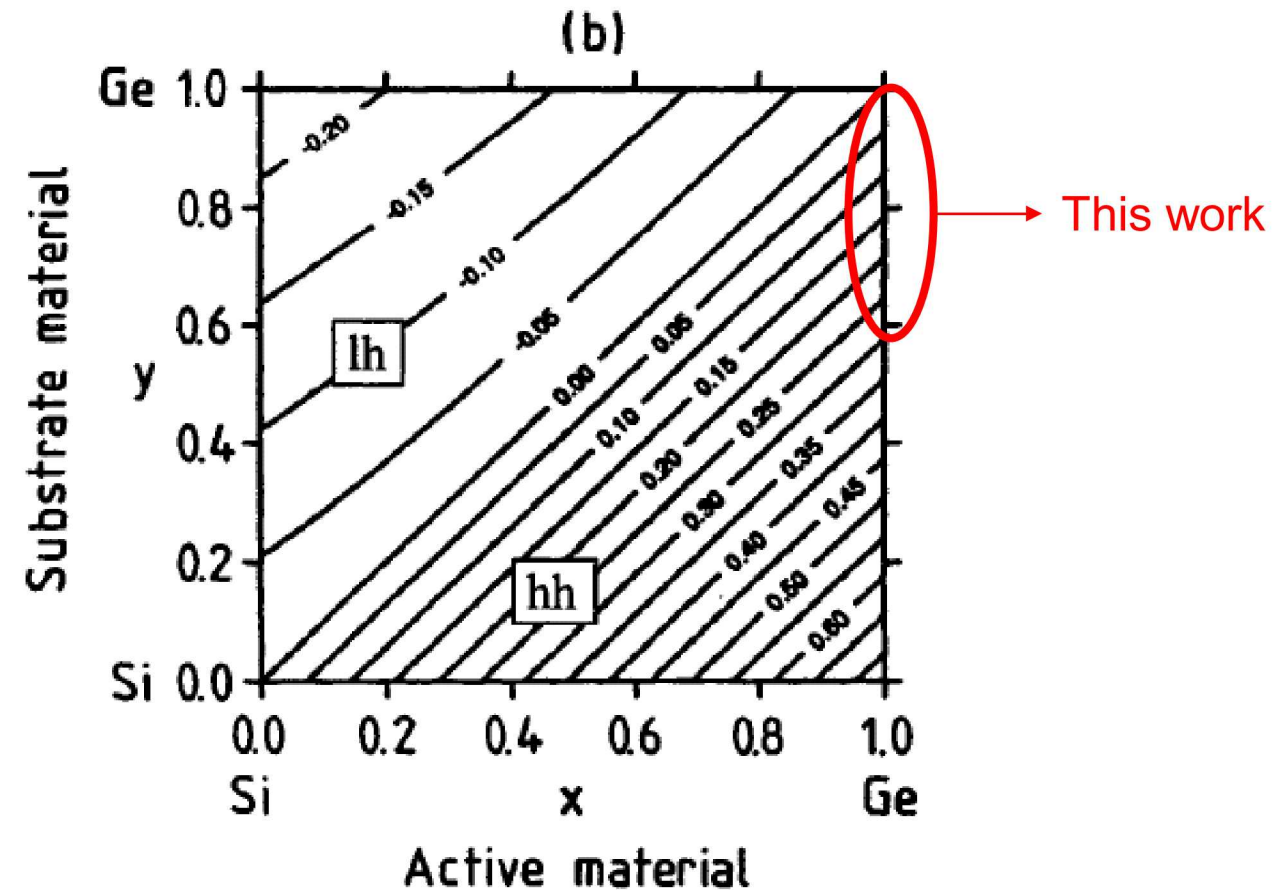
## Modulation doped Si/SiGe



# Band alignment of SiGe heterostructures

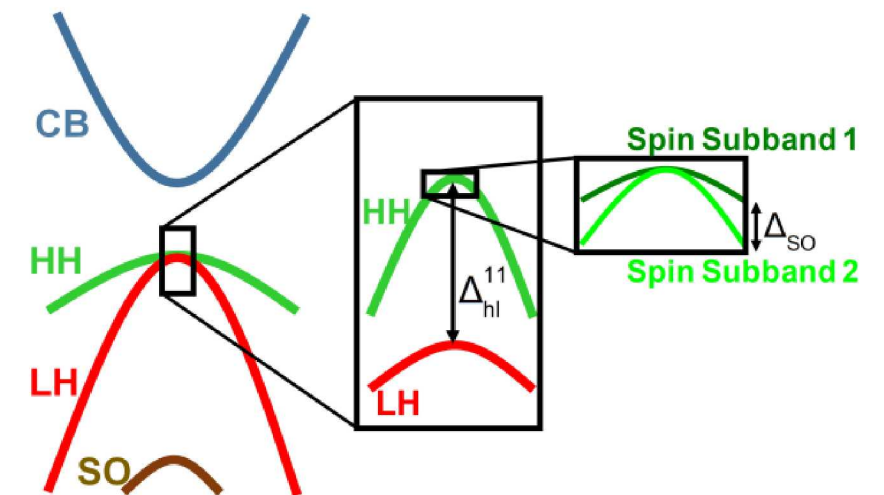
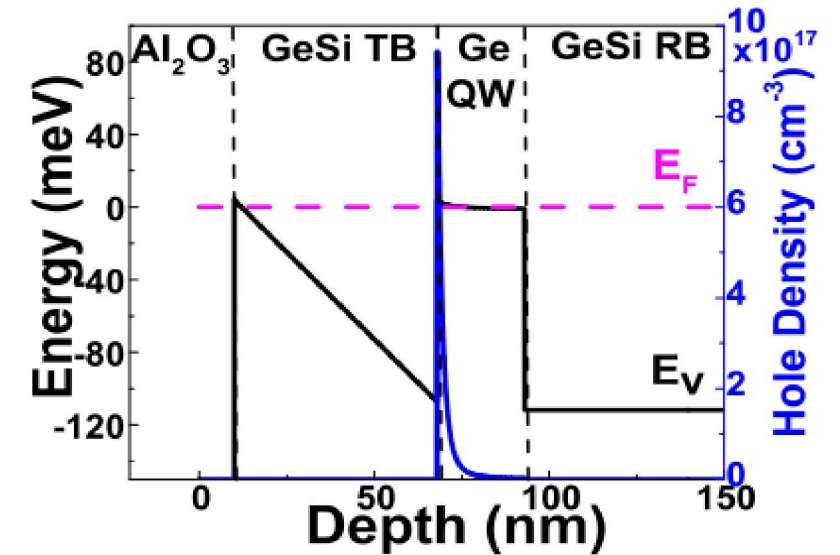
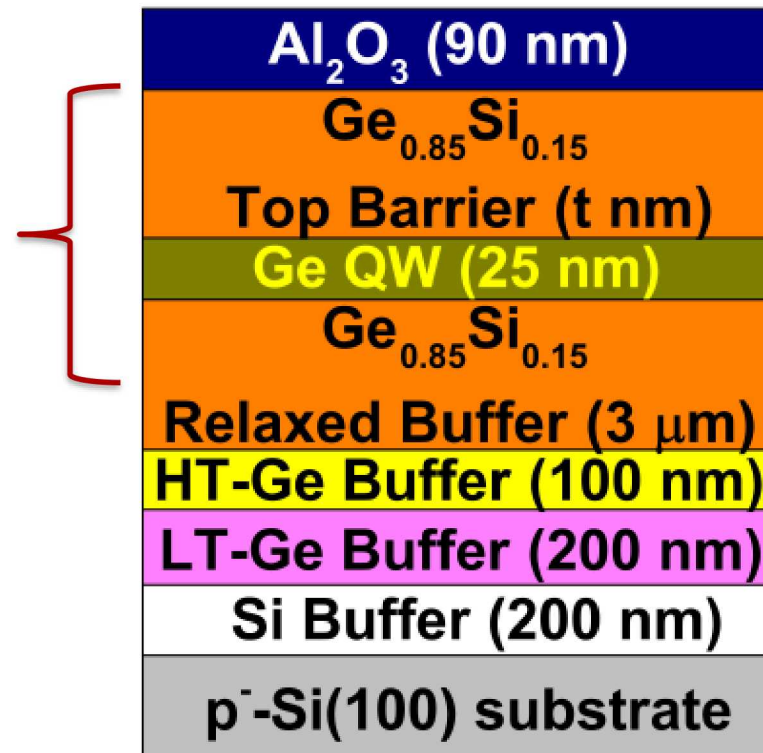
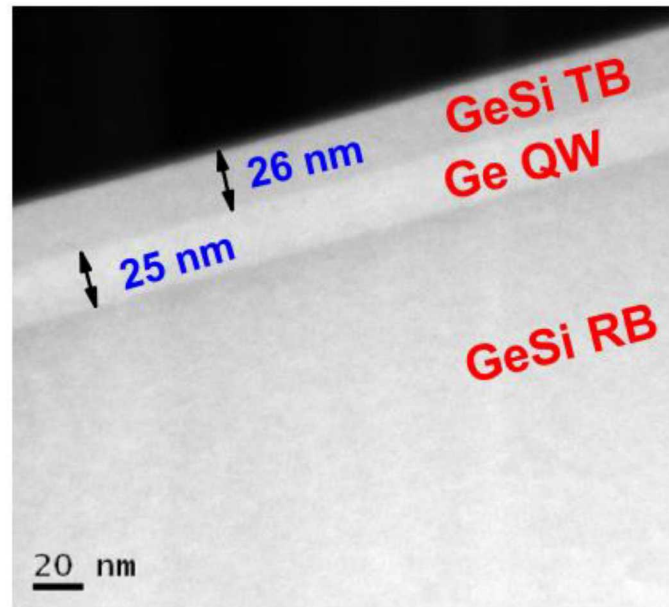


Conduction band  
2D electrons in Si quantum wells



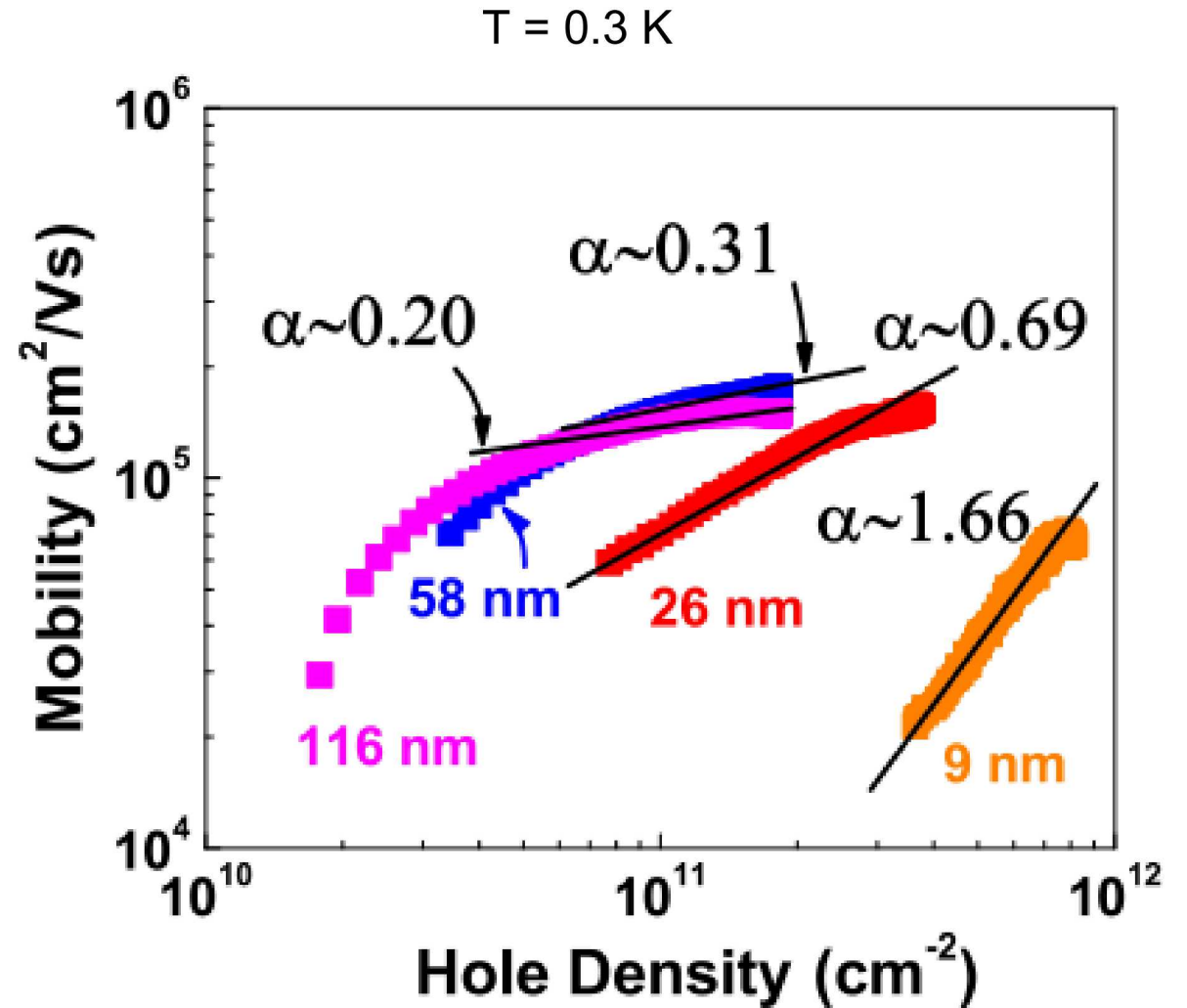
Valance band  
2D holes in Ge quantum wells

# Undoped Ge/SiGe heterostructure field-effect transistors



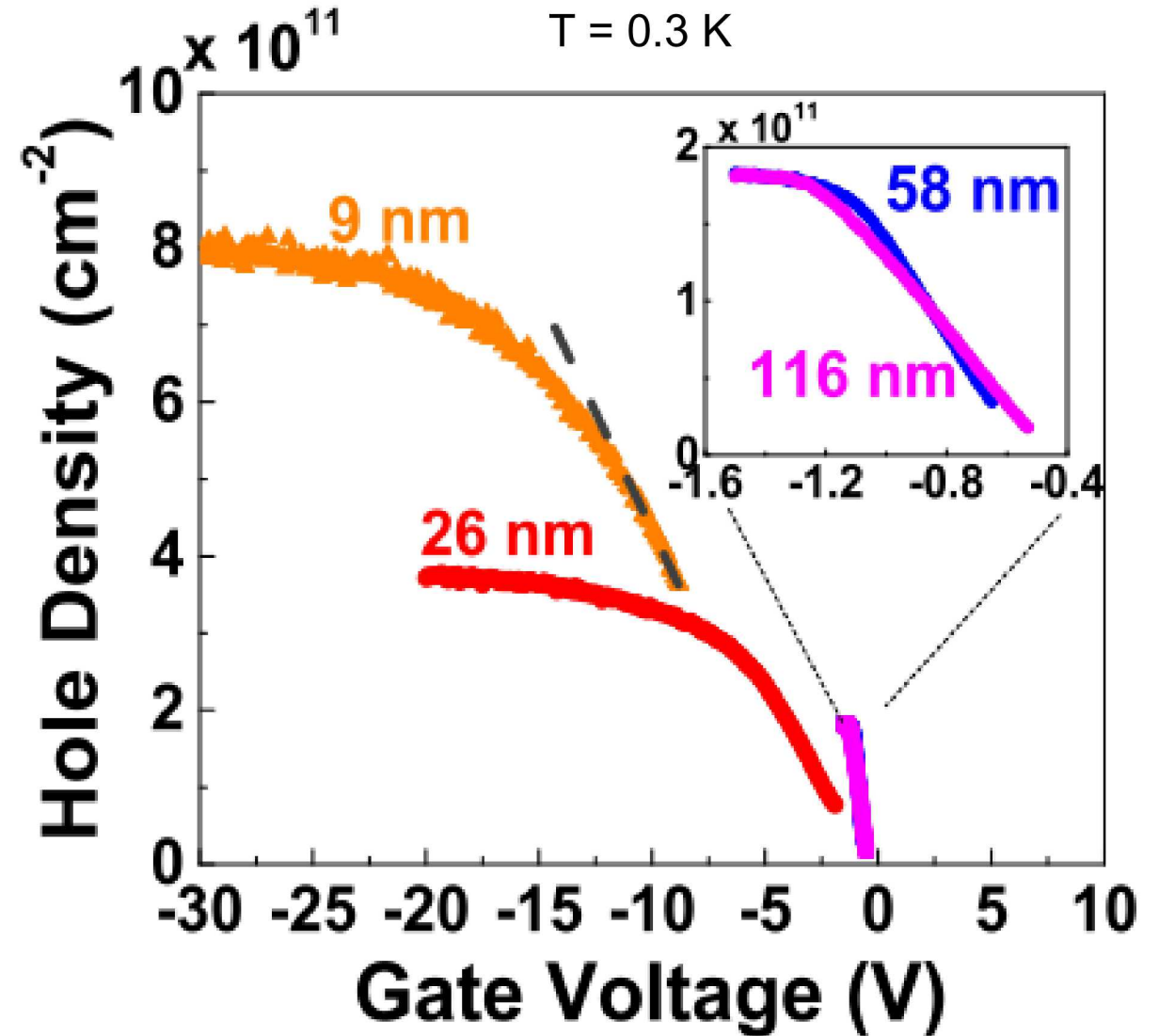
# Device operation – mobility

- Mobility on the order of  $2 \times 10^5$   $\text{cm}^2/\text{Vs}$  achievable
- Mobility increases with density  
=> screening
- Shallower channels have lower mobilities  
=> oxide/GeSi interface is disordered

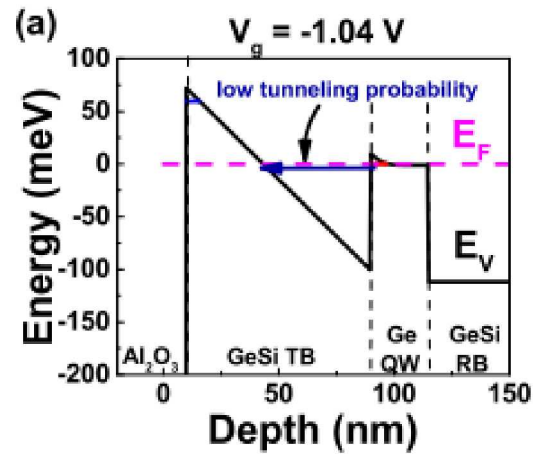


# Device operation – 2D hole density

- The 2D hole density saturates.
- Shallow channels
  - High saturation densities, depth dependent.
  - Small slopes (capacitances)
- Deep channels
  - Low saturation densities, depth independent.
  - Large slopes (capacitances)



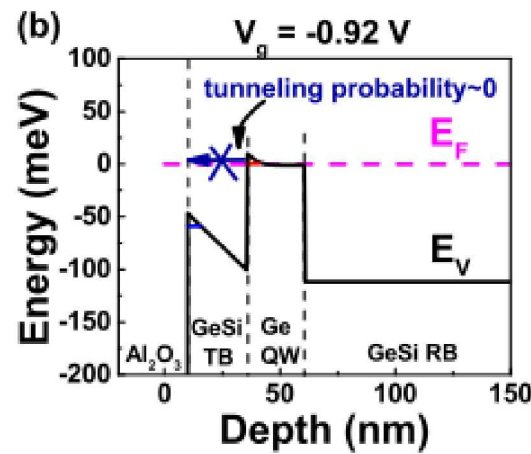
# Device operation – 2D hole density



## Deep channels

The tunnel rate is limited by triangular barrier (set by Si%) and is depth independent.

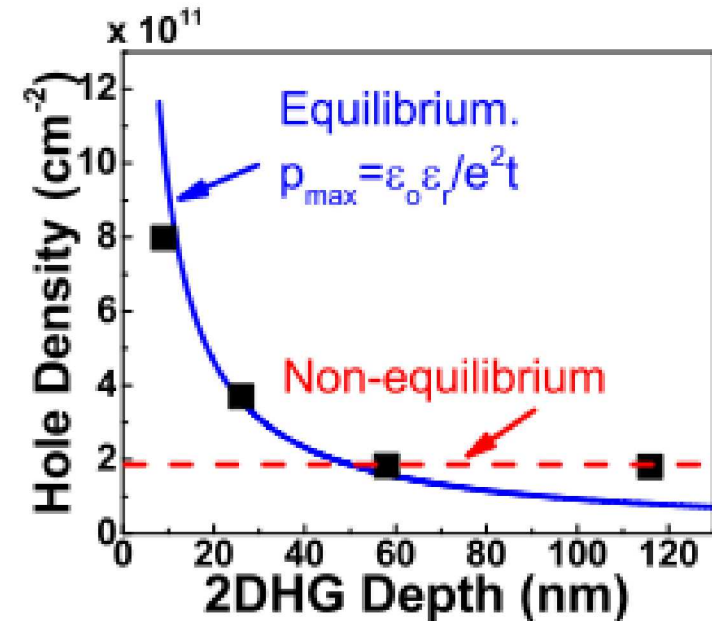
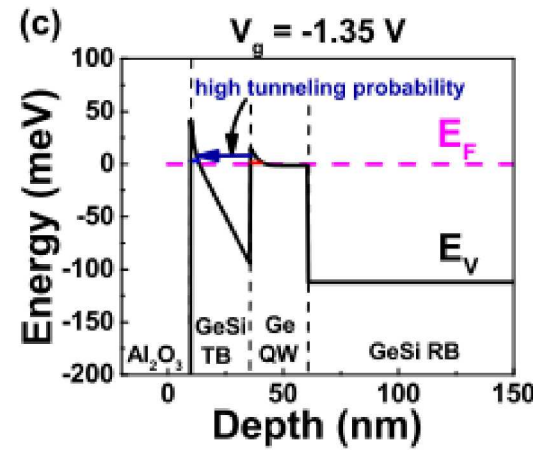
The tunnel rate can be so low that the density only slowly decreases and never reaches equilibrium at low temperatures!



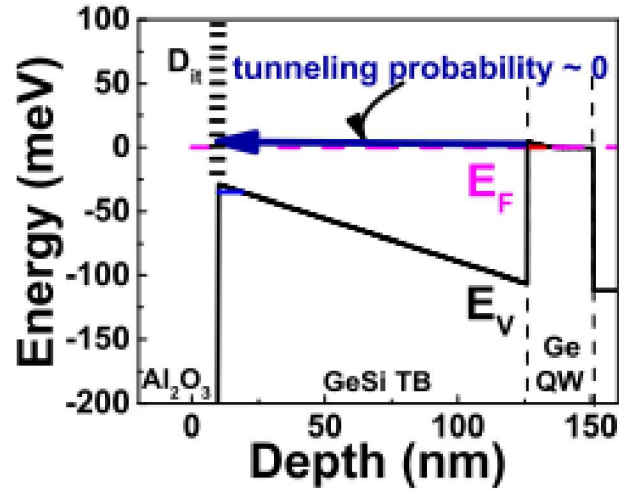
## Shallow channels

The tunneling rate is high (compared to experiment time scales).

The density probed by the Hall effect approaches the equilibrium case.



# Device operation – 2D hole density

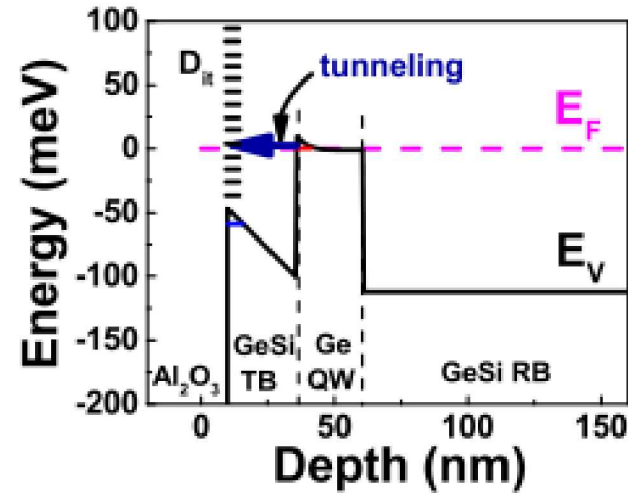


Deep channels

The tunnel rate is low.

The traps at the oxide/GeSi interface do not (need to) get filled.

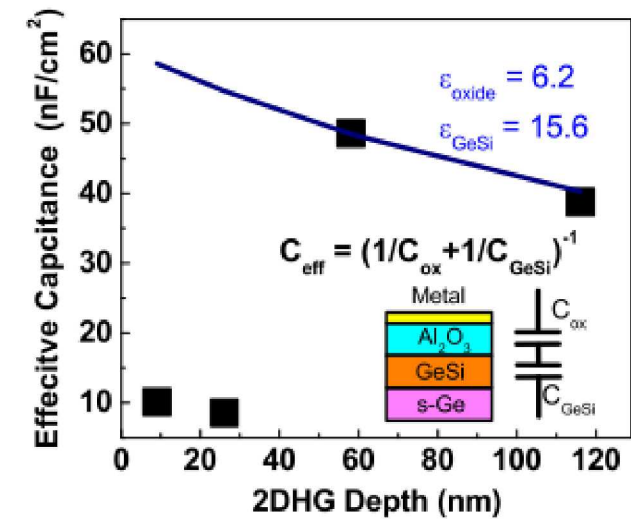
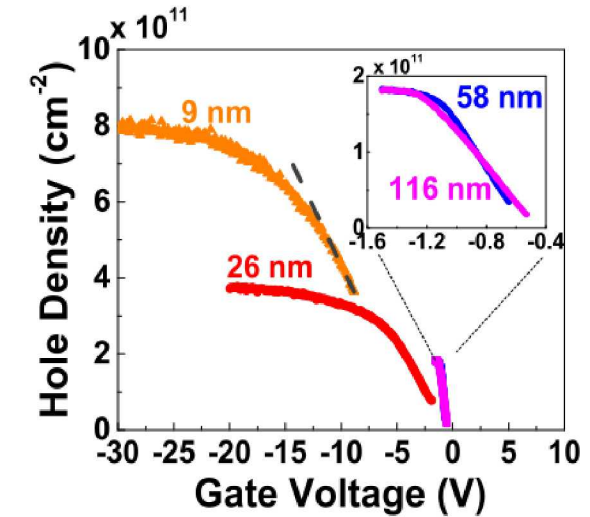
$$C_{\text{eff}} \sim C_{\text{geometric}}$$



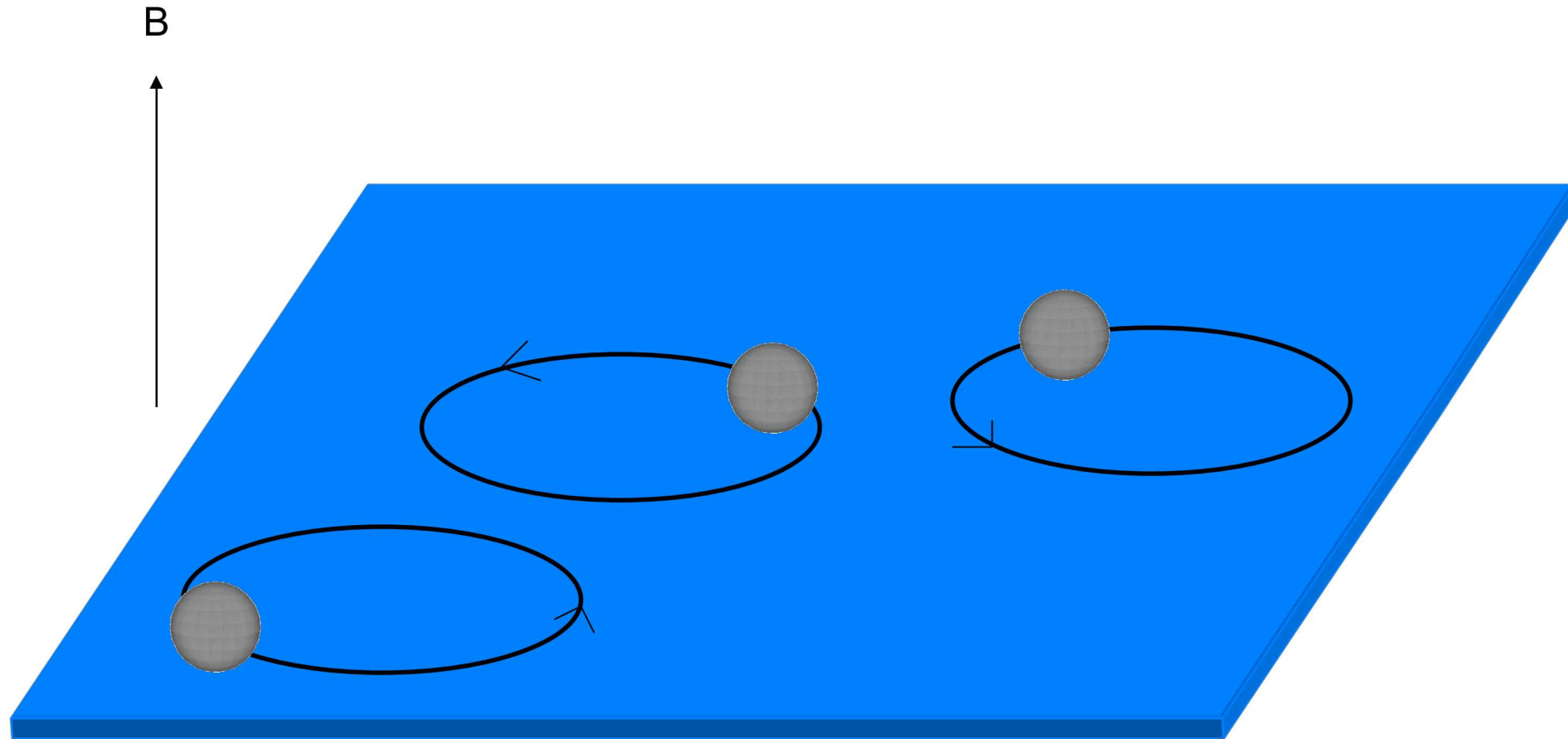
Deep channels

The tunnel rate is high.

The traps at the oxide/GeSi interface need to be filled before the Fermi level can move.



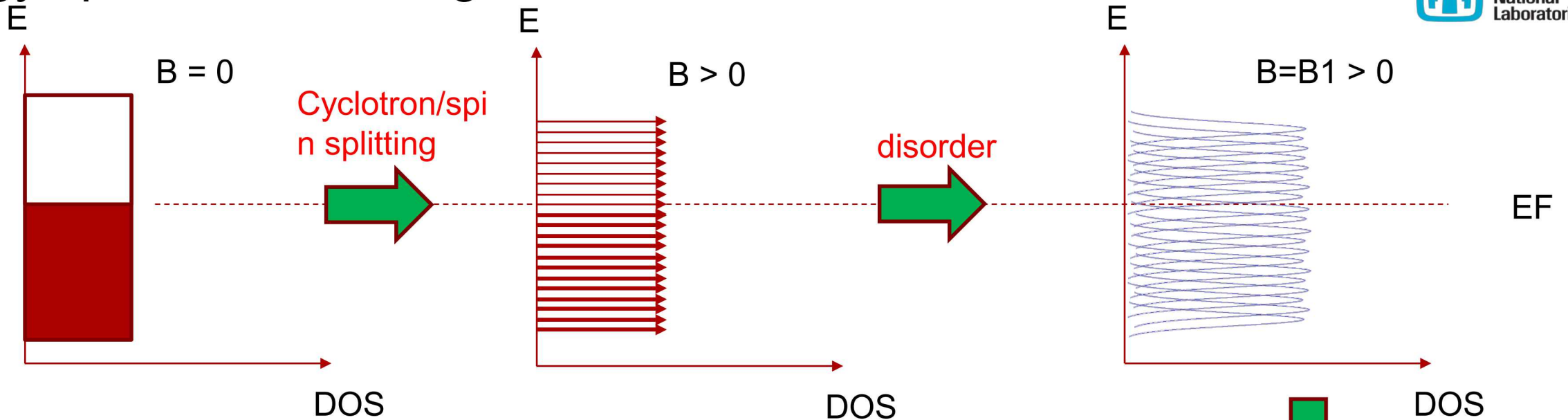
In a perpendicular magnetic field...



Cyclotron motion,  $E_c = \hbar e B_{\text{perp}} / m^*$

Spin splitting, gap  $E_z = g \mu B_{\text{total}}$

# Energy spectrum in a magnetic field



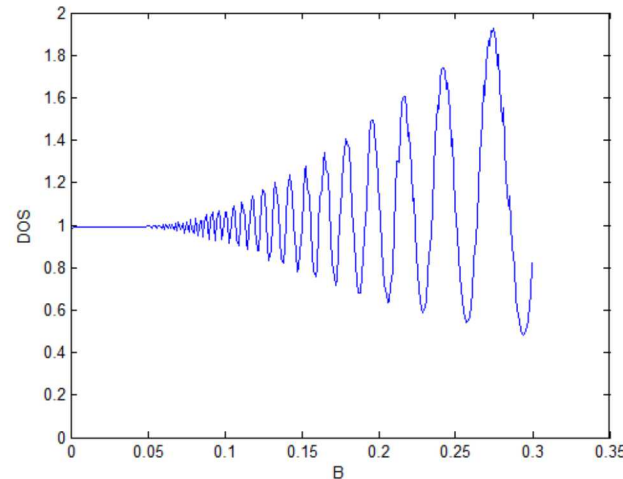
$$\frac{\Delta\rho}{\rho_0} \sim D(X) \frac{\Delta DOS}{DOS}$$

$$D(X) = X / \sinh X$$

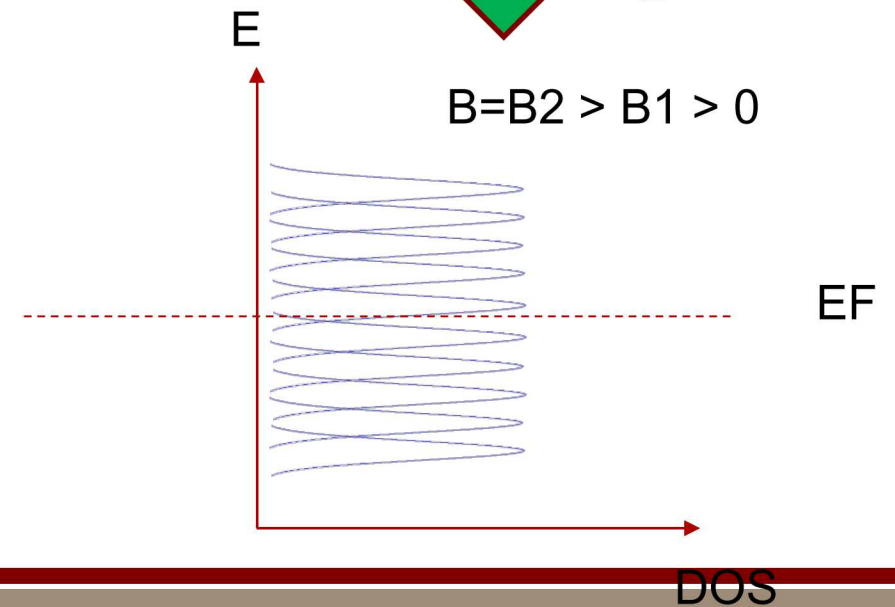
$$X = 2\pi kT / \text{Gap}$$

Temperature dependence  
 <=> Gap measurement  
 <=> cyclotron gap or spin gap

DOS at Fermi energy at a fixed density



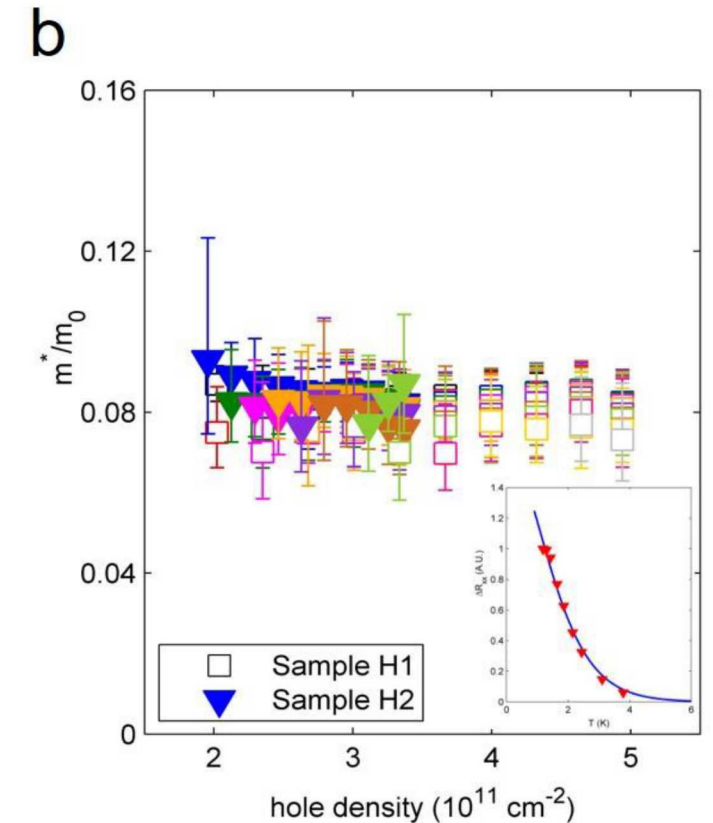
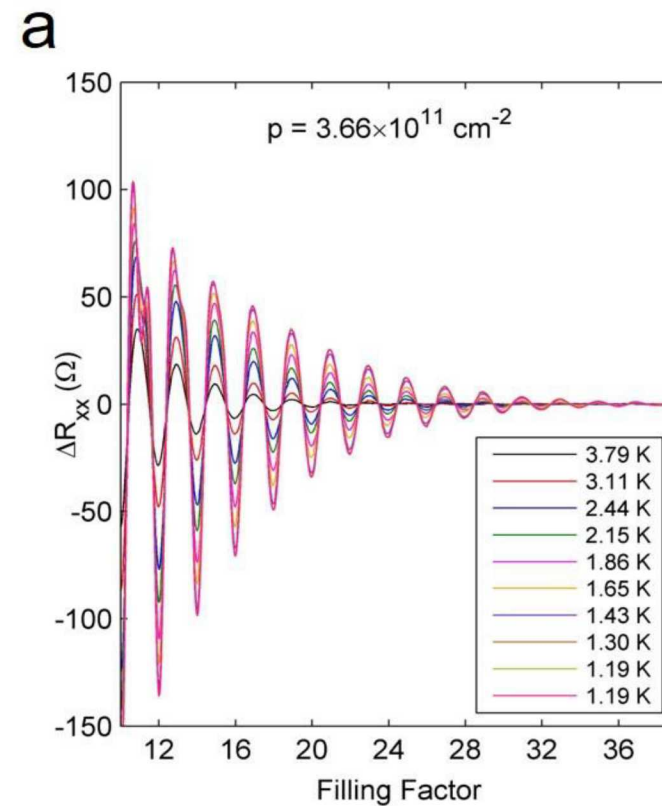
Higher field



DOS

# Physical properties – effective mass

- $\sim 0.08 m_0$ .
- $\sim$  density independent.
- This mass is small compared to the mass of electrons in Si (0.19), the mass of holes in GaAs (0.2-0.4), and is comparable to the mass of electrons in GaAs (0.07).
- Smaller mass  
=> more extended wave functions  
=> easier gate controls for nanostructures



# Physical properties – effective mass (even filling factors)

## Theory

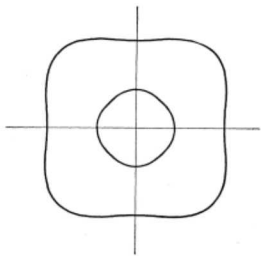
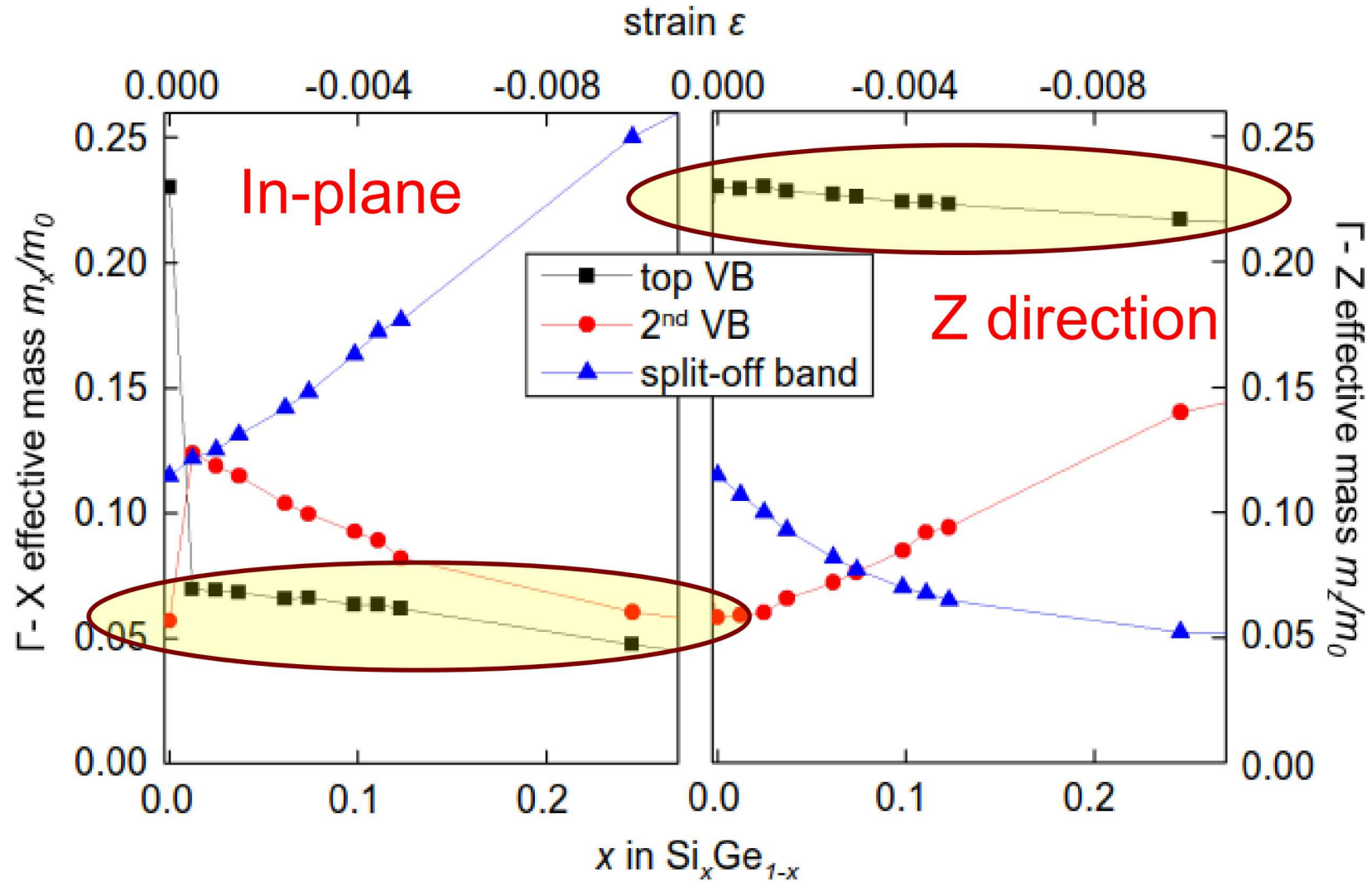
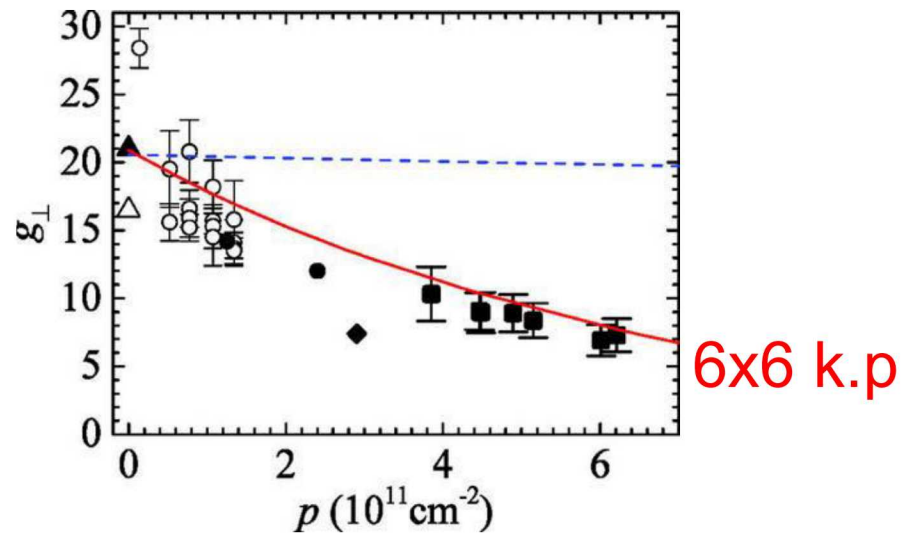


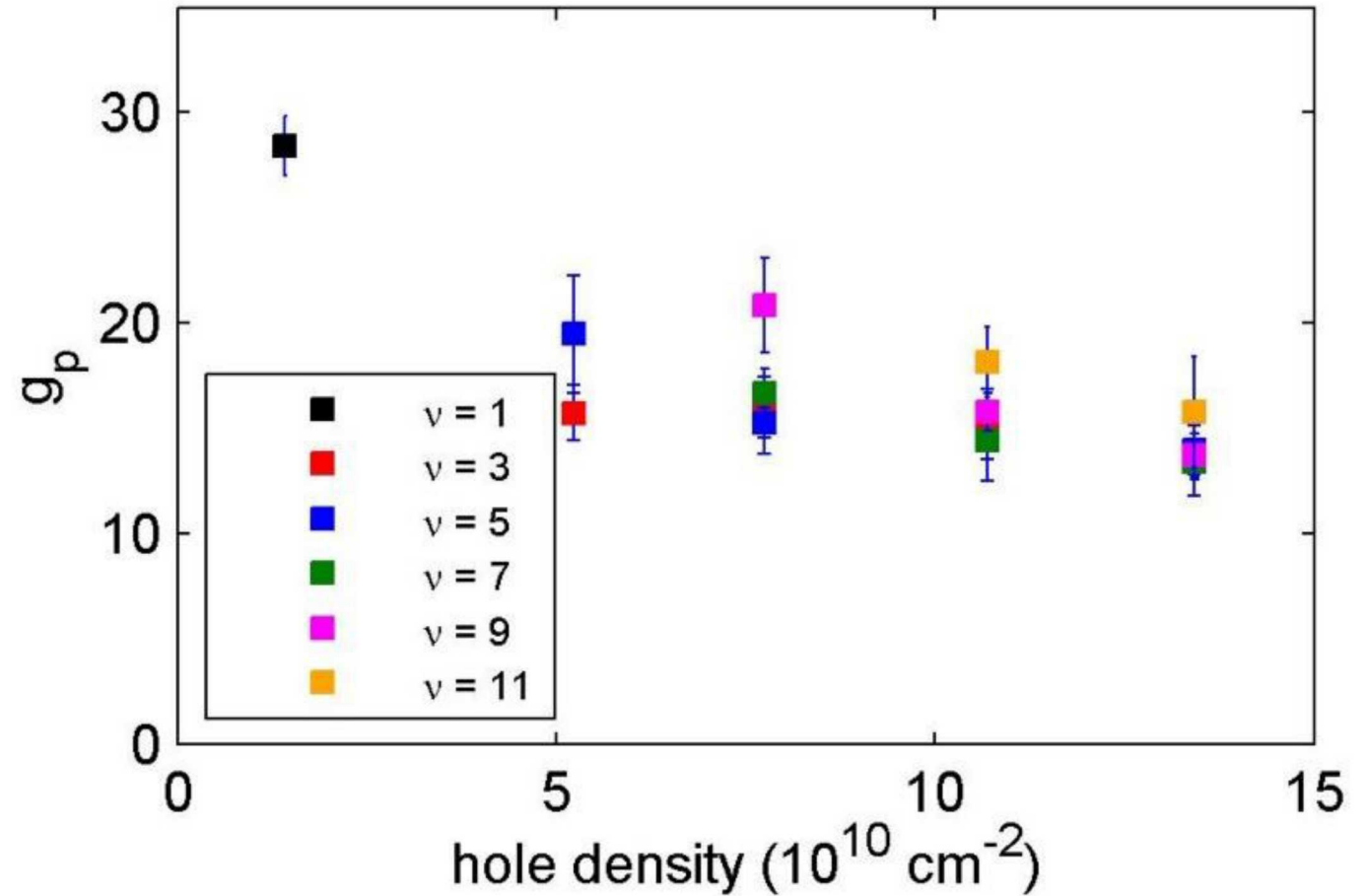
FIG. 8. Figures of constant energy in the (100) plane of  $k$ -space for the two fluted energy surfaces which are degenerate at the valence band edge; constants as for germanium.

# Physical properties – g factor (odd filling factors)

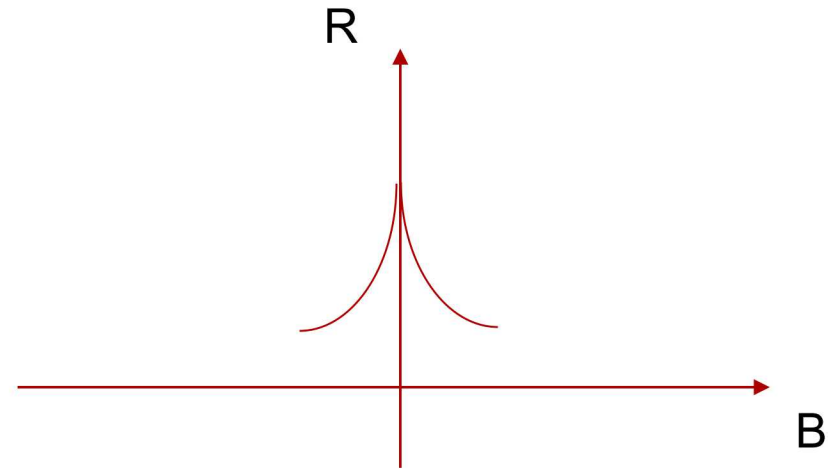
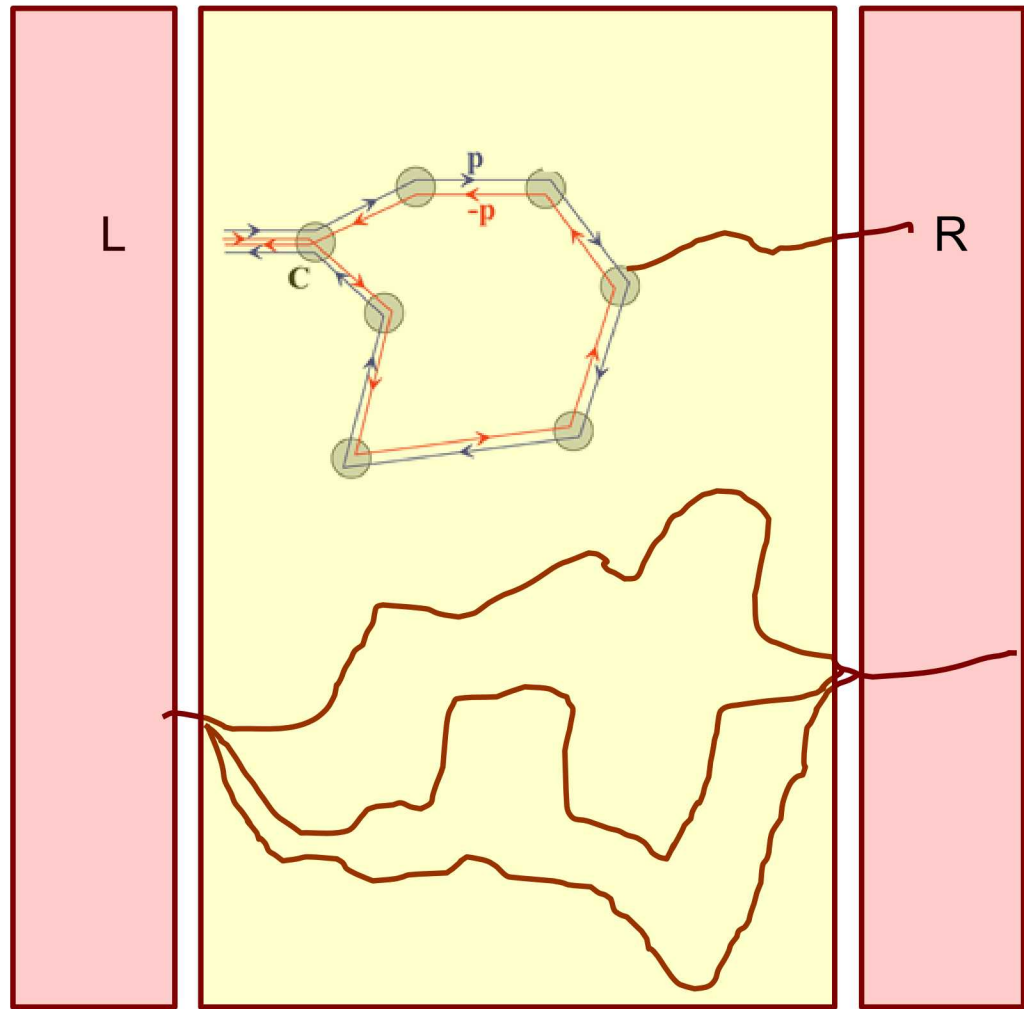
- $\sim 10 - 30$
- $\sim$  density dependent.
- The g factor is large compared to the g factor of electrons in Si ( $\sim 2$ ) and the g factor of electrons in GaAs ( $\sim 0.44$ ).



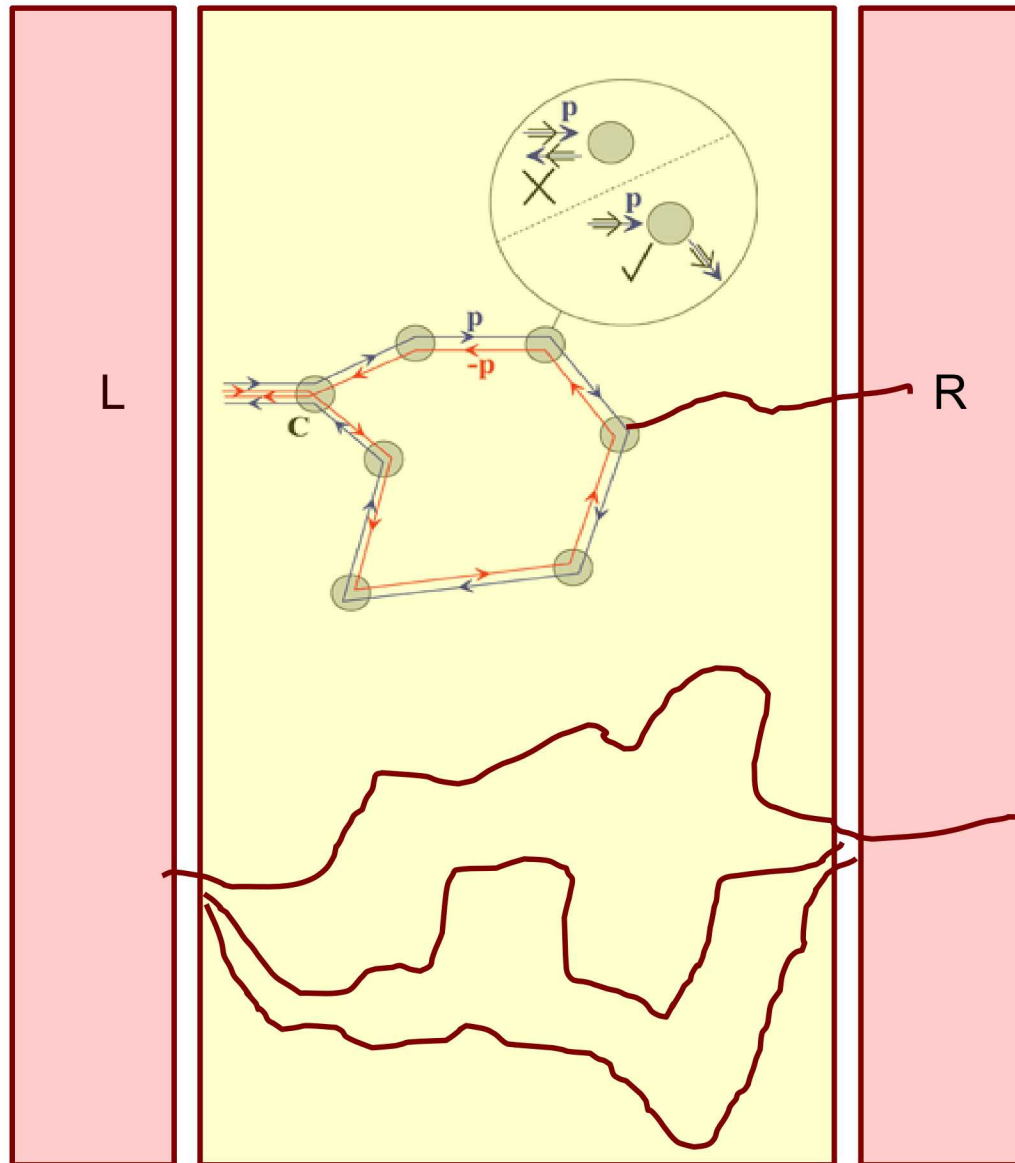
Drichko JAP 123, 165703



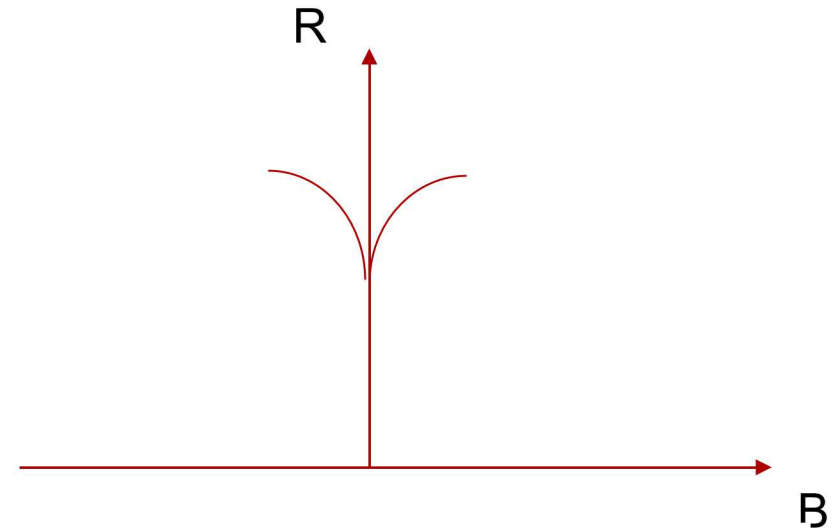
# Weak localization (no spin-orbit coupling)



# Weak anti-localization (spin-orbit coupling)



Spin and momentum are locked together.  
Back scattering is suppressed.



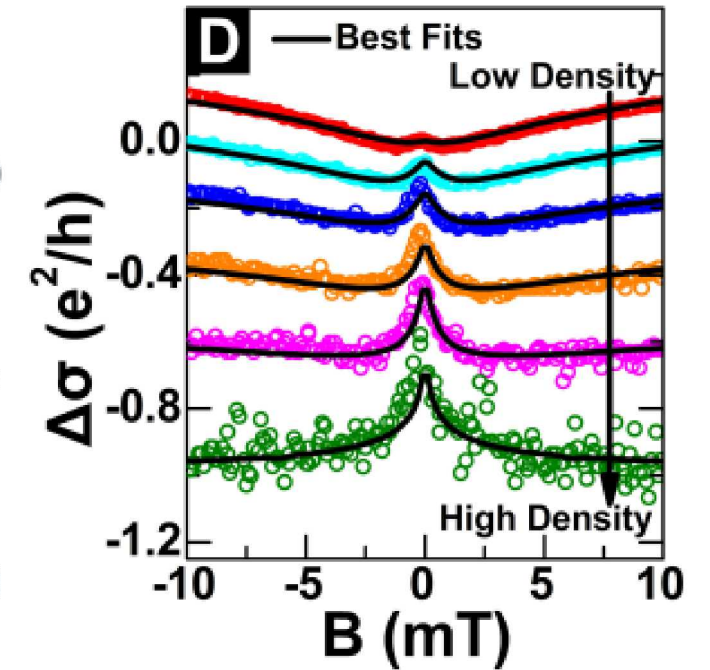
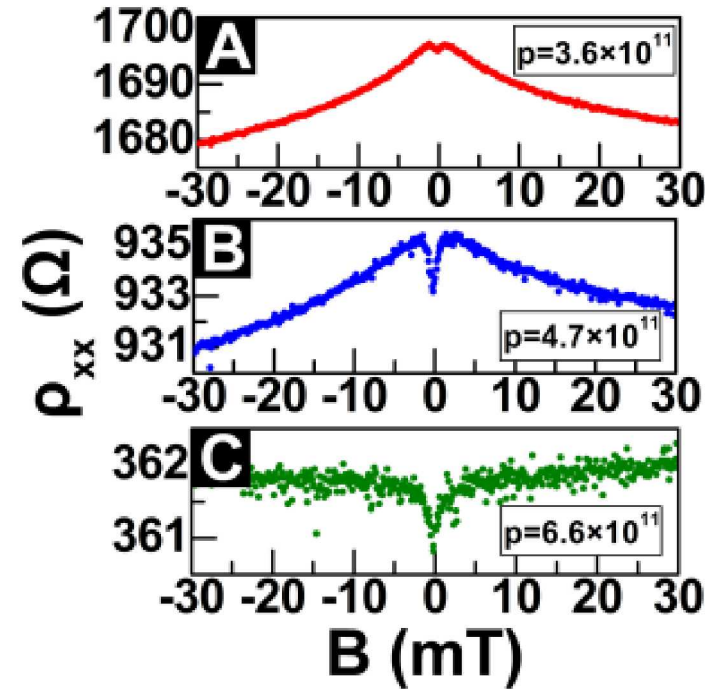
$$\Delta\sigma(B) - \Delta\sigma(0) = \frac{e^2}{2\pi^2\hbar} \left\{ \psi\left(\frac{1}{2} + \frac{H_\varphi}{B} + \frac{H_{SO}}{B}\right) + \frac{1}{2} \psi\left(\frac{1}{2} + \frac{H_\varphi}{B} + \frac{2H_{SO}}{B}\right) - \frac{1}{2} \psi\left(\frac{1}{2} + \frac{H_\varphi}{B}\right) - \ln\frac{H_\varphi + H_{SO}}{B} - \frac{1}{2} \ln\frac{H_\varphi + 2H_{SO}}{B} + \frac{1}{2} \ln\frac{H_\varphi}{B} \right\}$$

Hikami Prog. Theor. Phys. 63, 707

Adapted from McCann Physics 2, 98

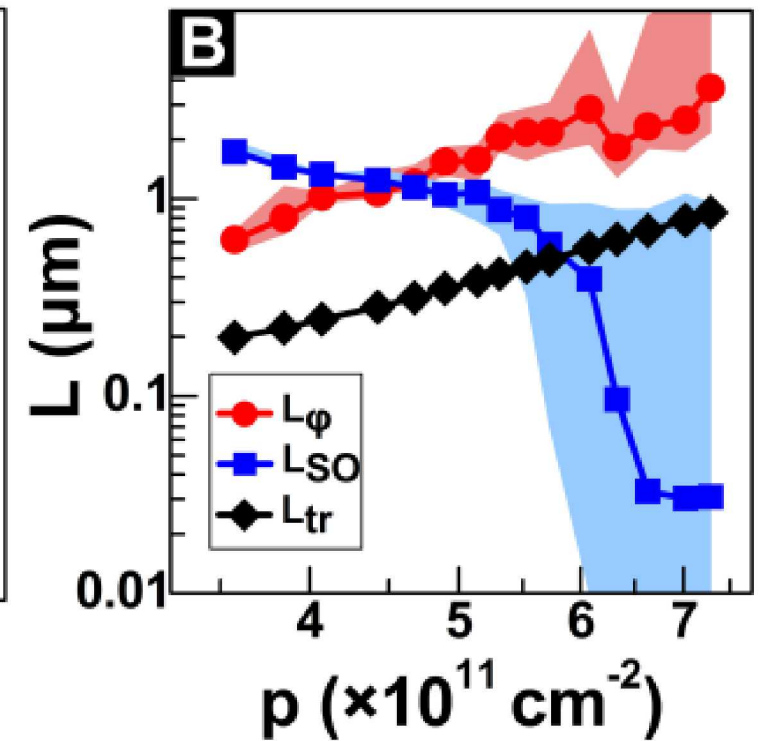
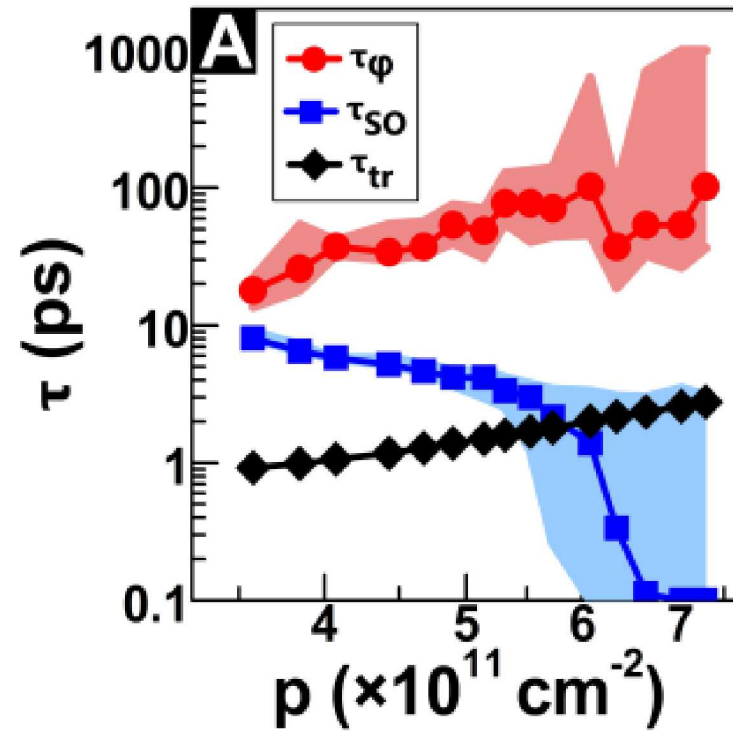
# Physical properties – spin-orbit coupling

- Low densities
  - Weak localization only
- Intermediate densities
  - Weak anti-localization on top of weak localization only
- High densities
  - Weak anti-localization only



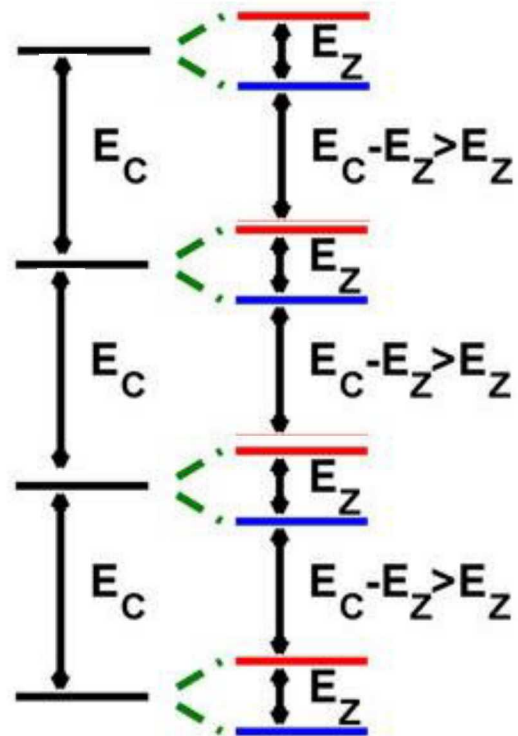
# Physical properties – spin-orbit coupling

- Spin-orbit length decreases with density and can be as short as 0.1  $\mu\text{m}$  ( $<$  mean free path), while the phase coherence length can be a few microns long ( $>$  mean free path)
- This means the hole spin can rotate at a high yet controlled rate, maintain its phase coherence, and suffer no scattering.



# The quantum Hall effect

In a perpendicular magnetic field, the spectrum of a 2D gas is a series of Landau levels:



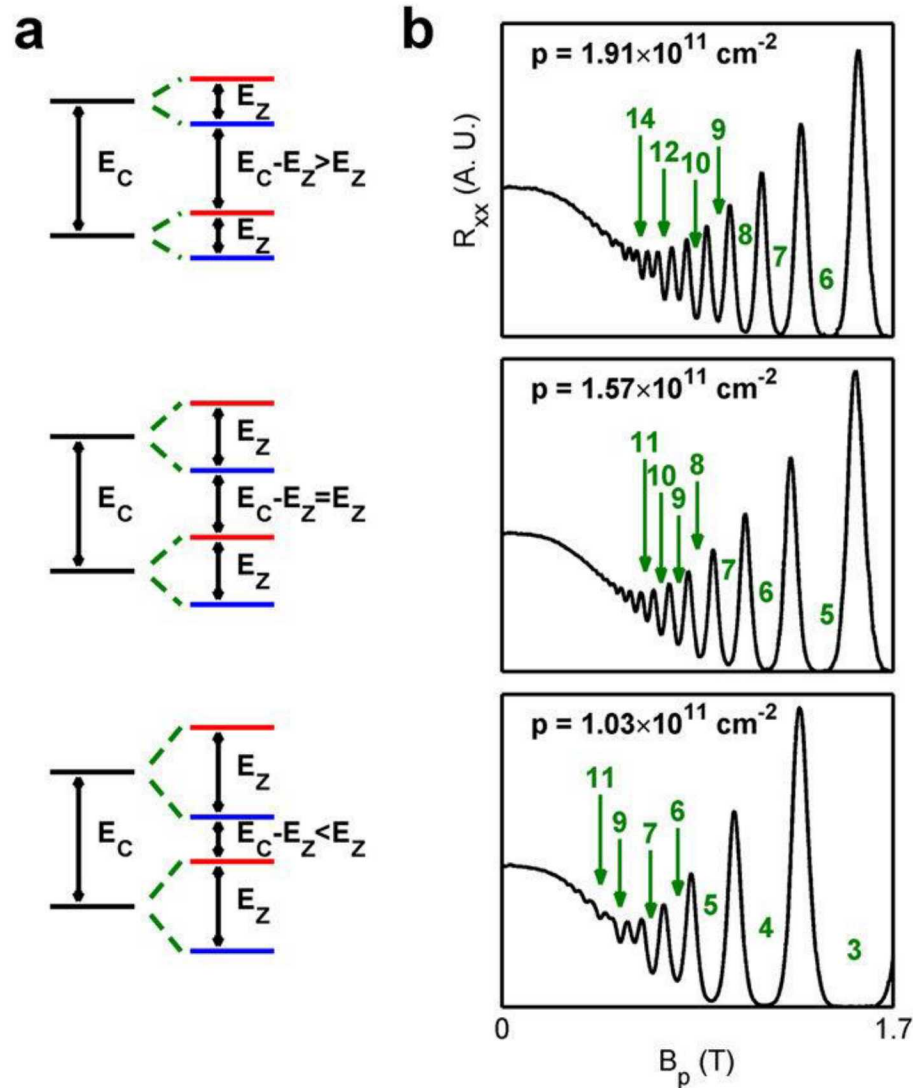
$E_C$  is cyclotron gap:  $\hbar eB/(2\pi m^*)$

$E_Z$  is Zeeman gap:  $g^* \mu_B$

$m^*$  and  $g^*$  are material parameters.

Landau level degeneracy (# electrons / area):  
 $eB/h$

# Quantum Hall ferromagnetic transition



In most cases,  $E_C \gg E_Z$

$\Rightarrow$  Strong even states, weak odd states

If  $E_C \sim 2E_Z$

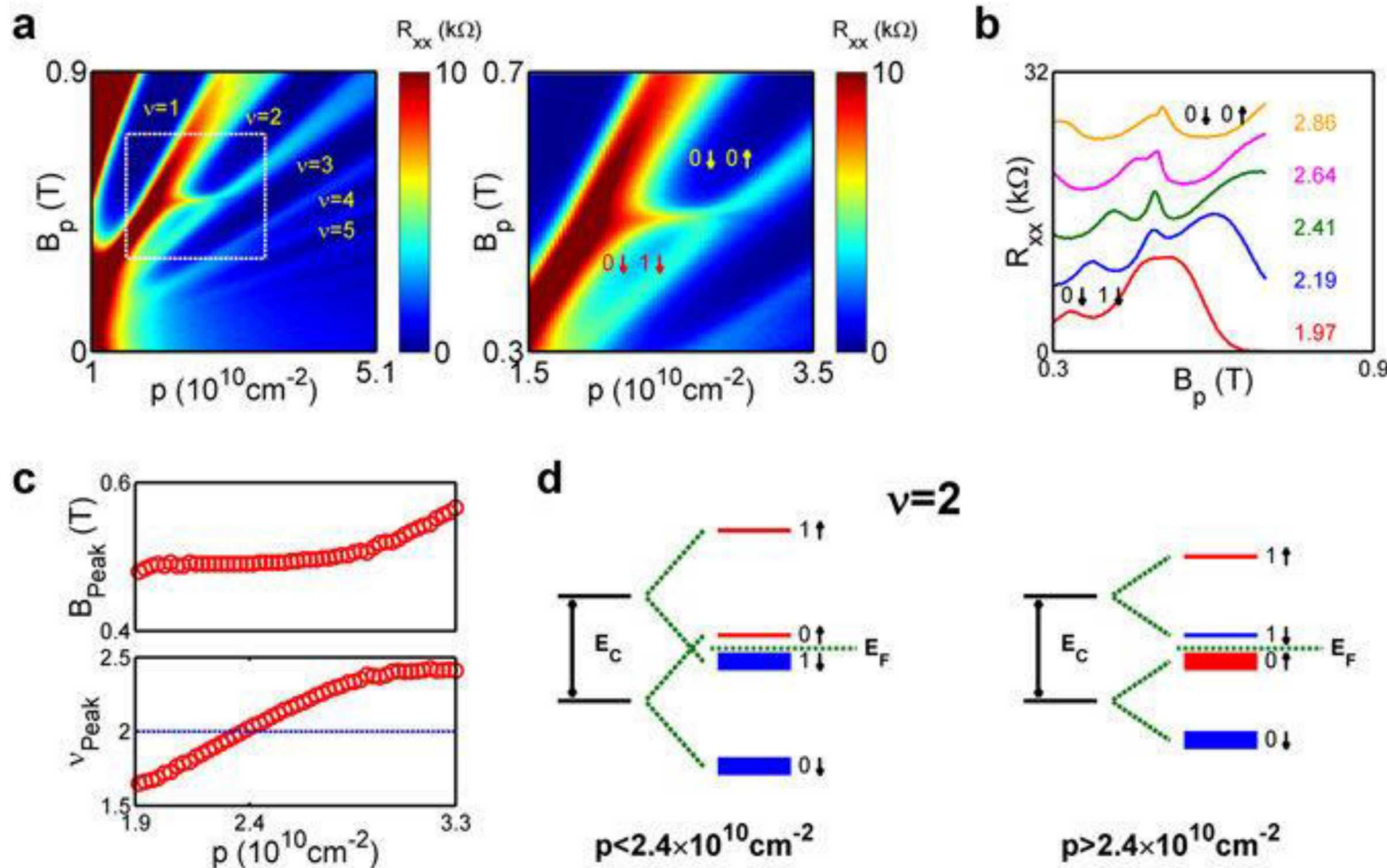
$\Rightarrow$  Strength of even states  $\sim$  strength of odd states

If  $E_C < 2E_Z$

$\Rightarrow$  Strong odd states, weak even states

$E_Z/E_C$  increases with decreasing density.

# Quantum Hall ferromagnetic transition



A spin transition (unpolarized  $\leftrightarrow$  polarized) at  $\nu=2$  occurs at  $p \sim 2.4 \times 10^{10}$  cm $^{-2}$ .

This transition marks the point where  $E_c \sim E_z$

$$\frac{\hbar e B}{(2\pi m^*)} = g^* \mu B$$

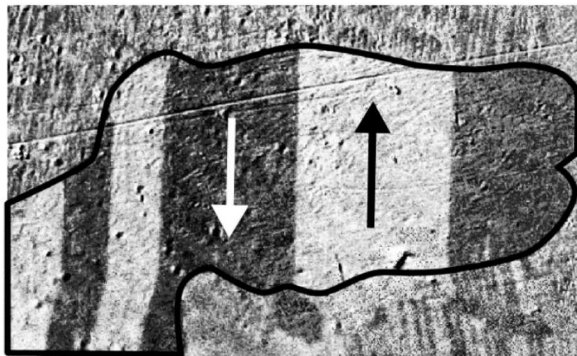
$$\Rightarrow m^* g^* = 2$$

# Quantum Hall ferromagnetic transition

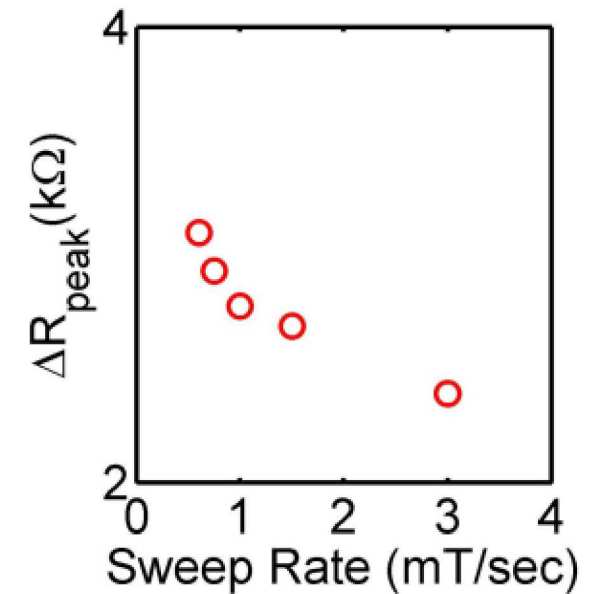
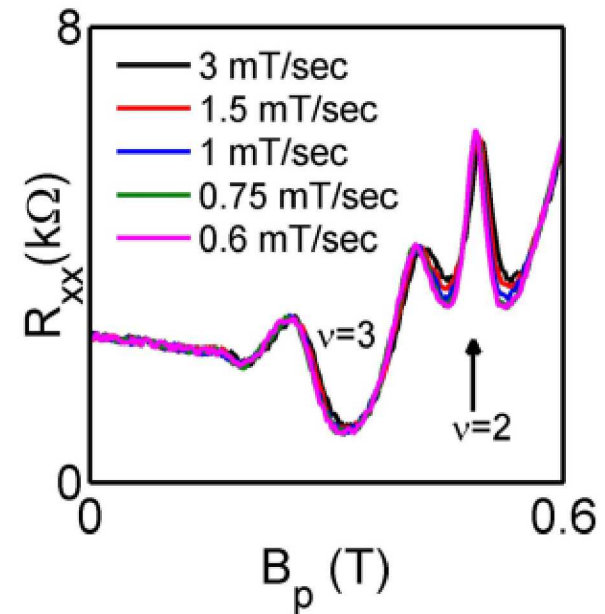
The physical picture of the system at the transition:

micro-domains of different spin configurations. Away from the transition, one spin configuration is preferred. Domains move and merge to minimize surface energy.

Evidence of micro-domains is found in the time dependence.

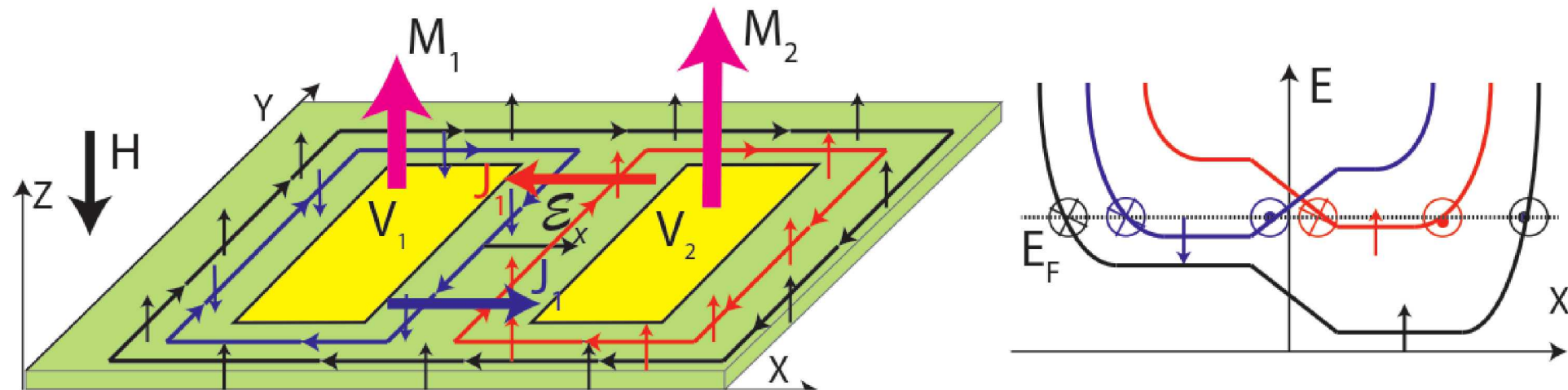


by S. Zurek, *E. Magnetica*, [CC-BY-3.0](https://creativecommons.org/licenses/by/3.0/)



# Quantum Hall ferromagnetic transition

Local gating to create counter-propagating edge states with opposite spins

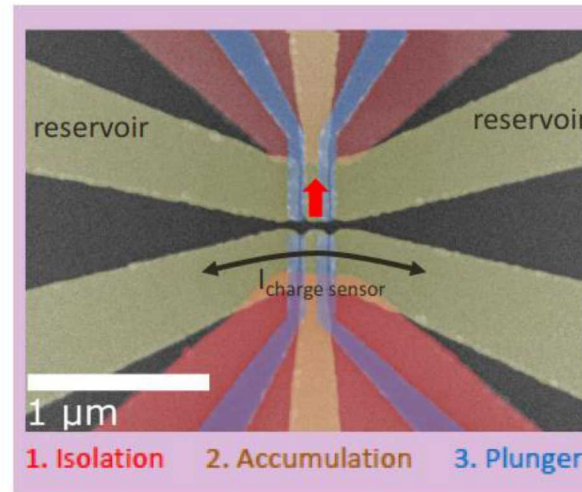


## Implications for Quantum Dots

- Low Disorder
  - Help Dot-Dot Coupling
- Small Effective Mass
  - Help Dot-Dot coupling
  - Easier Lithography
- Anisotropic g-factor
  - Large g-factor allows operation at smaller magnetic fields
  - Dot-to-Dot variation is possible
- Strong Spin-Orbit-Coupling
  - Natural mechanism for qubit control
  - Introduces additional noise channel

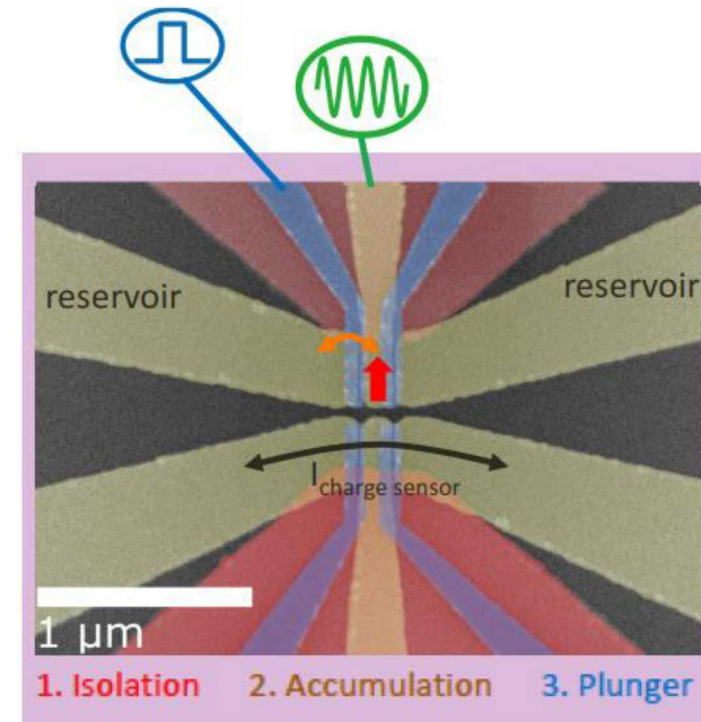
The effect of confinement on these properties remains largely unexplored

Surface electrodes used to laterally confine hole

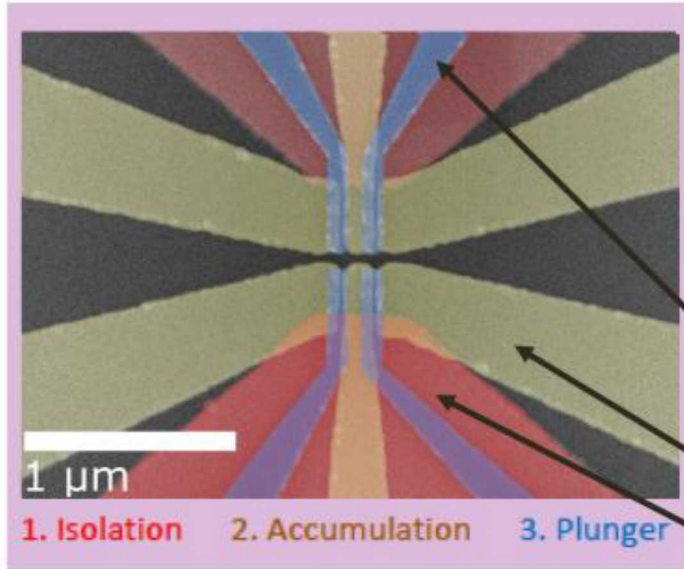


# Spin qubits in Ge/SiGe

- Single Hole confined to lateral quantum dot
- Spin Qubit States:  $m_j = \pm 3/2$
- Qubit readout and initialization through energy selective tunneling to reservoir
- Qubit Control through microwaves applied to gate
- Occupancy detected through nearby charge sensor



# Spin qubits in Ge/SiGe



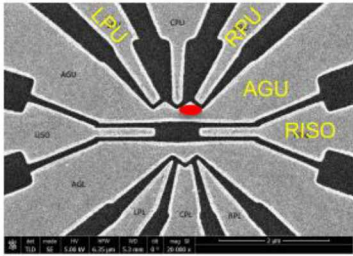
## Goals:

- Independent Control of occupation and tunnel barriers
- Tighter Confinement
- Low Capacitance for EDSR

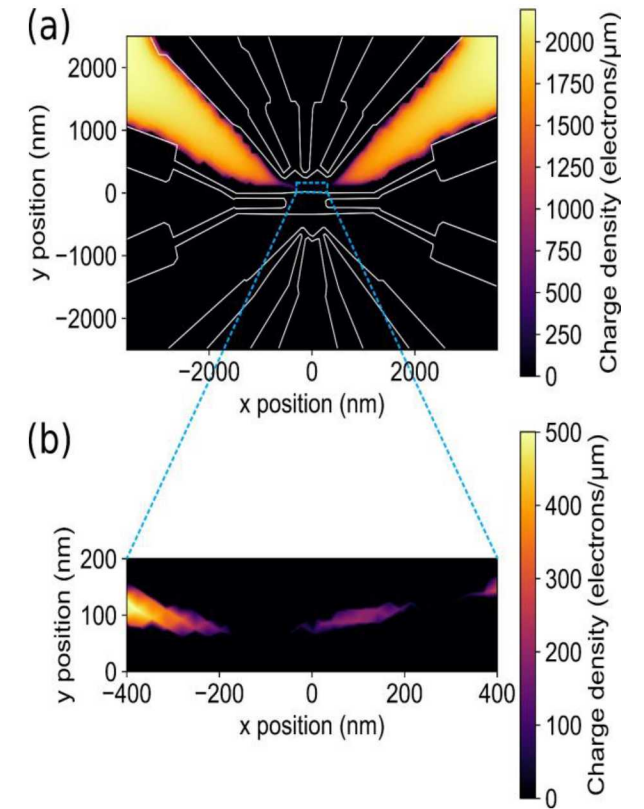
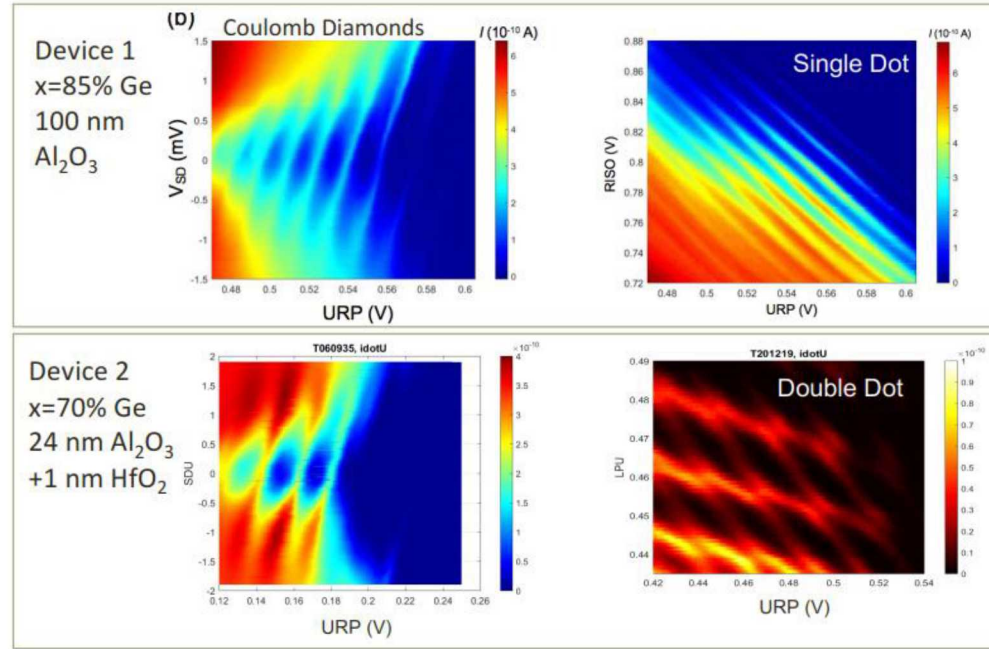
Ga implanted Ohmic contacts



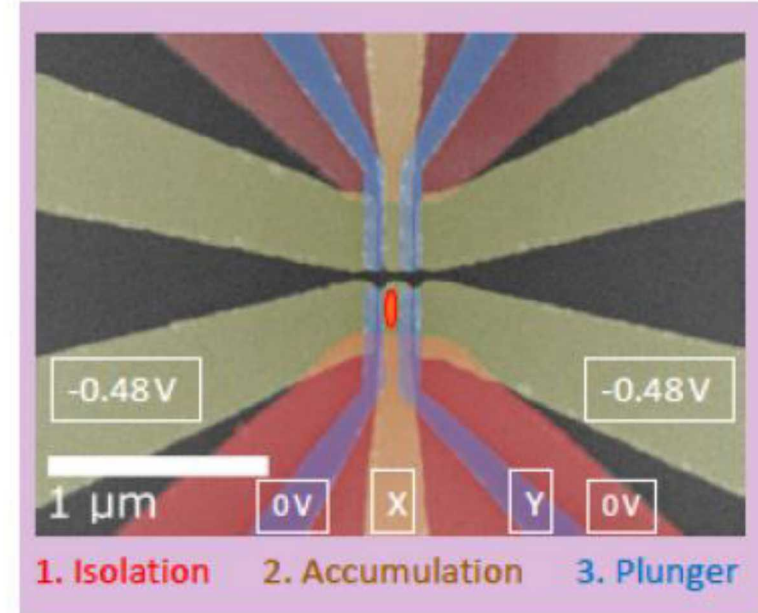
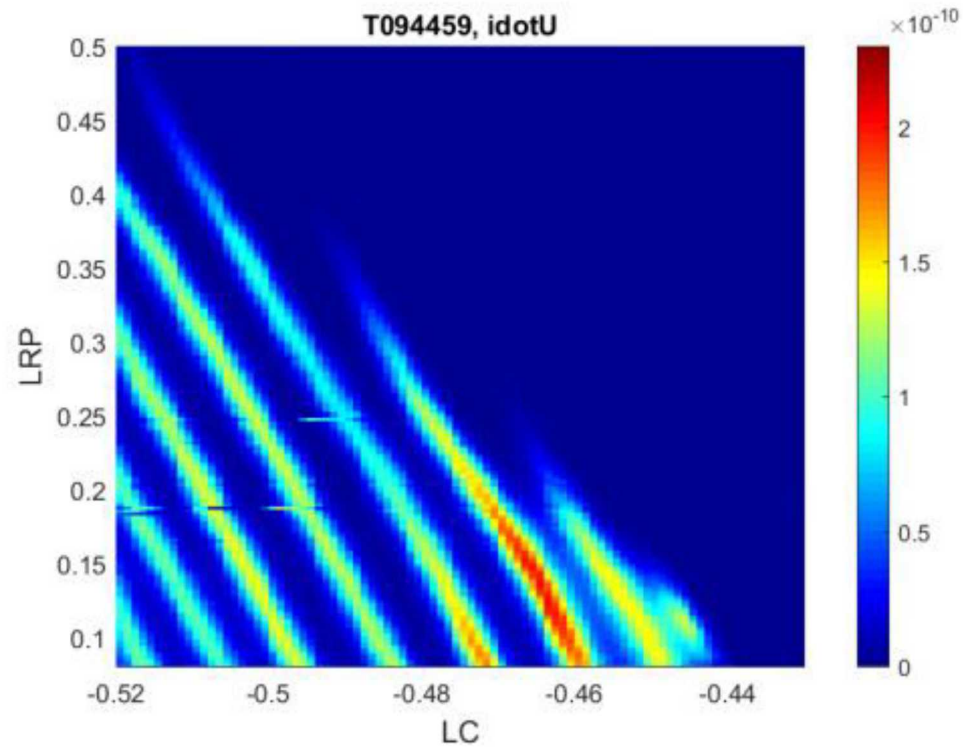
# Spin qubits in Ge/SiGe



Single Layer Devices can be tuned to low-hole regime in transport



## Three Metal Layer Device



Coulomb Blockade observed in the three-metal-layer devices

# Summary

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- Induced 2D holes in Ge/SiGe heterostructure field effect transistors demonstrated.
- Device behavior can deviate from thermal equilibrium.
- Physical properties (mass, g factor, spin-orbit coupling strength) characterized.
- Gate controlled quantum Hall ferromagnetic transition observed at low densities.
- Development of spin qubits in Ge/SiGe

# Acknowledgements

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- National Taiwan University: C. W. Liu, J.-Y. Li, C.-H. Lee, S.-H. Huang, Y. Chuang, Y.-H. Su, C.-T. Chou
- NHMFL

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