



# Full configuration interaction simulations of exchange coupled donors in silicon in an effective mass theory framework

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## Abstract

Multi-qubit quantum logic gates are the final step to demonstrate the the viability of donor spin qubits in silicon for quantum computation applications. Proposed two-qubit gates rely on the electron-electron exchange interaction which is highly sensitive to the relative placements of the donors in the silicon lattice<sup>1</sup>. For two proximal phosphorus donors an inversion of the hierarchy of the valley-orbital split states has been observed, i.e. the crossing of the bonding combination of T2 states below that of the antibonding A1<sup>2</sup>. Here, we use a full configuration interaction method within an established multivalley effective mass theory framework<sup>3</sup> to model the two-electron wavefunction for different donor configurations. Specifically, we investigate the exchange interaction and valley population along different lattice orientations.

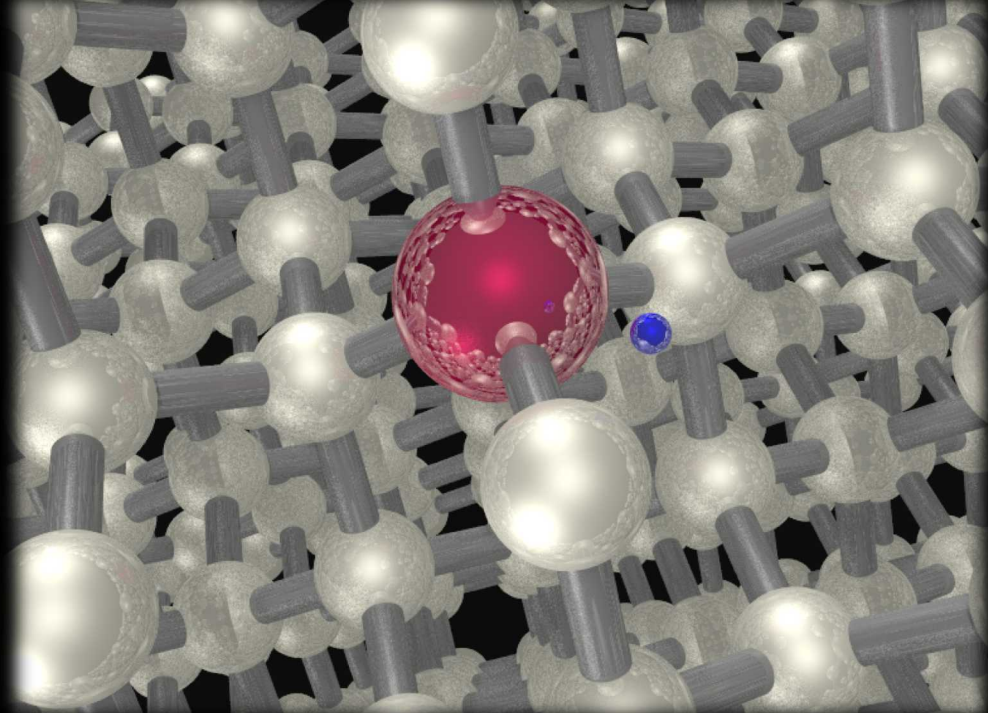
[1] R. Kalra, Phys. Rev. X **4**(2), 021044 (2014)

[2] J.P. Dehollain, Phys. Rev. Lett. **112**(23), 236801 (2014)

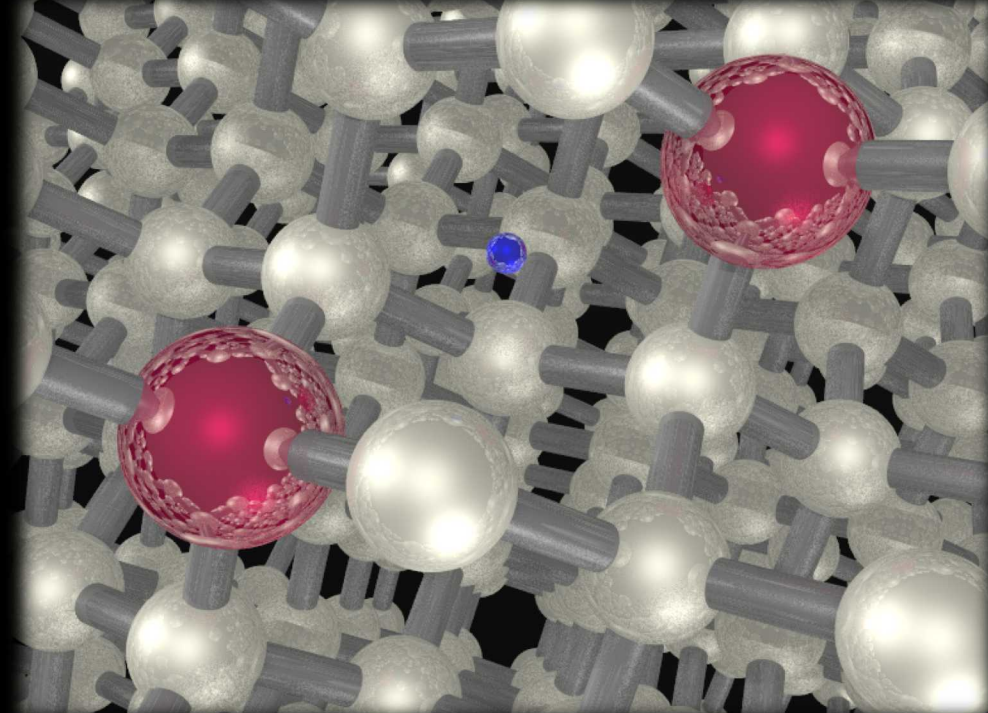
[3] J.K. Gamble, Phys. Rev. B **91**(23), 235318 (2015)

## Introduction

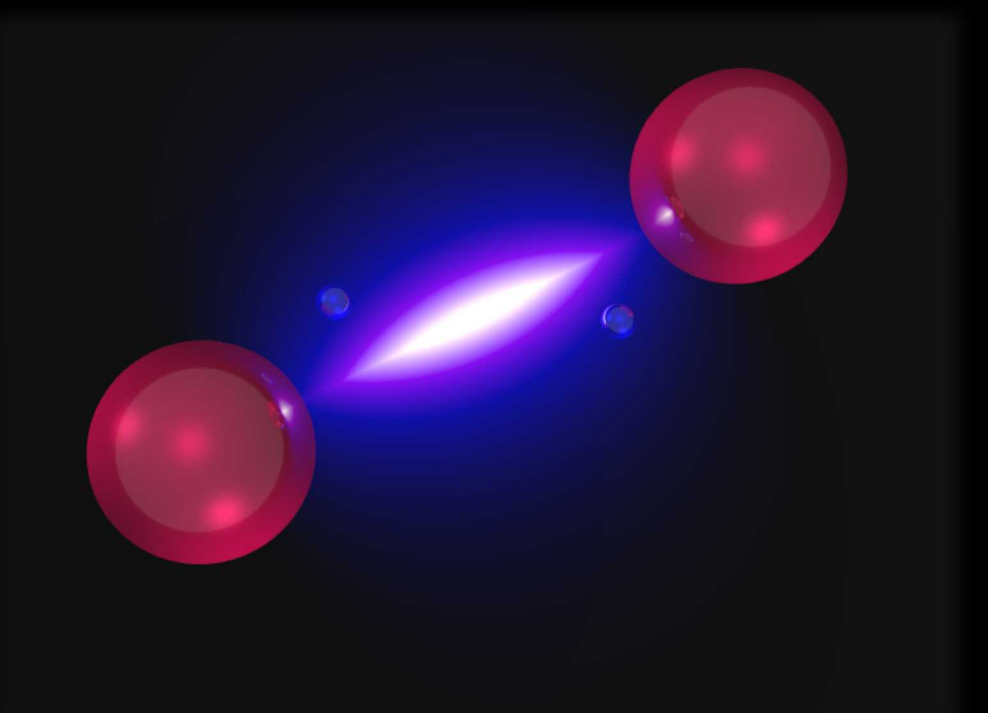
### 1. Single neutral donor



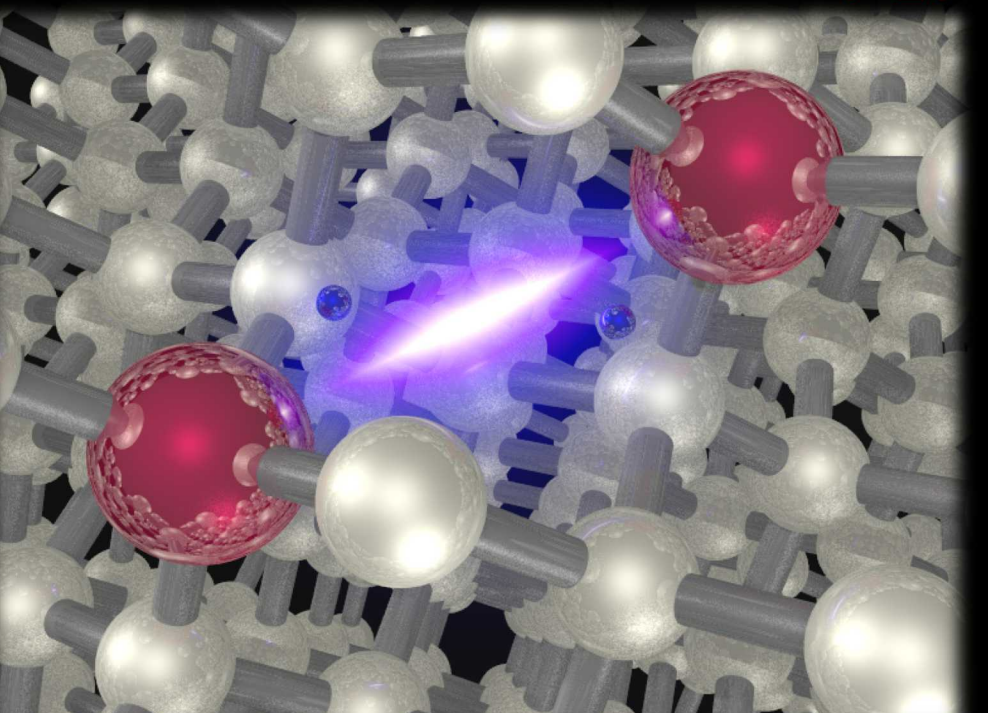
### 2. Two donors one e (P<sub>2</sub><sup>+</sup>)



### 3. Hydrogen Molecule (H<sub>2</sub>)



### 4. Two neutral donors (P<sub>2</sub>)



## 3. Hartree-Fock and Configuration Interaction

The Hartree-Fock Approximation:

$$\Phi = \frac{1}{\sqrt{2}}(|\psi_i\psi_j\rangle|\alpha\beta\rangle - |\psi_j\psi_i\rangle|\beta\alpha\rangle)$$

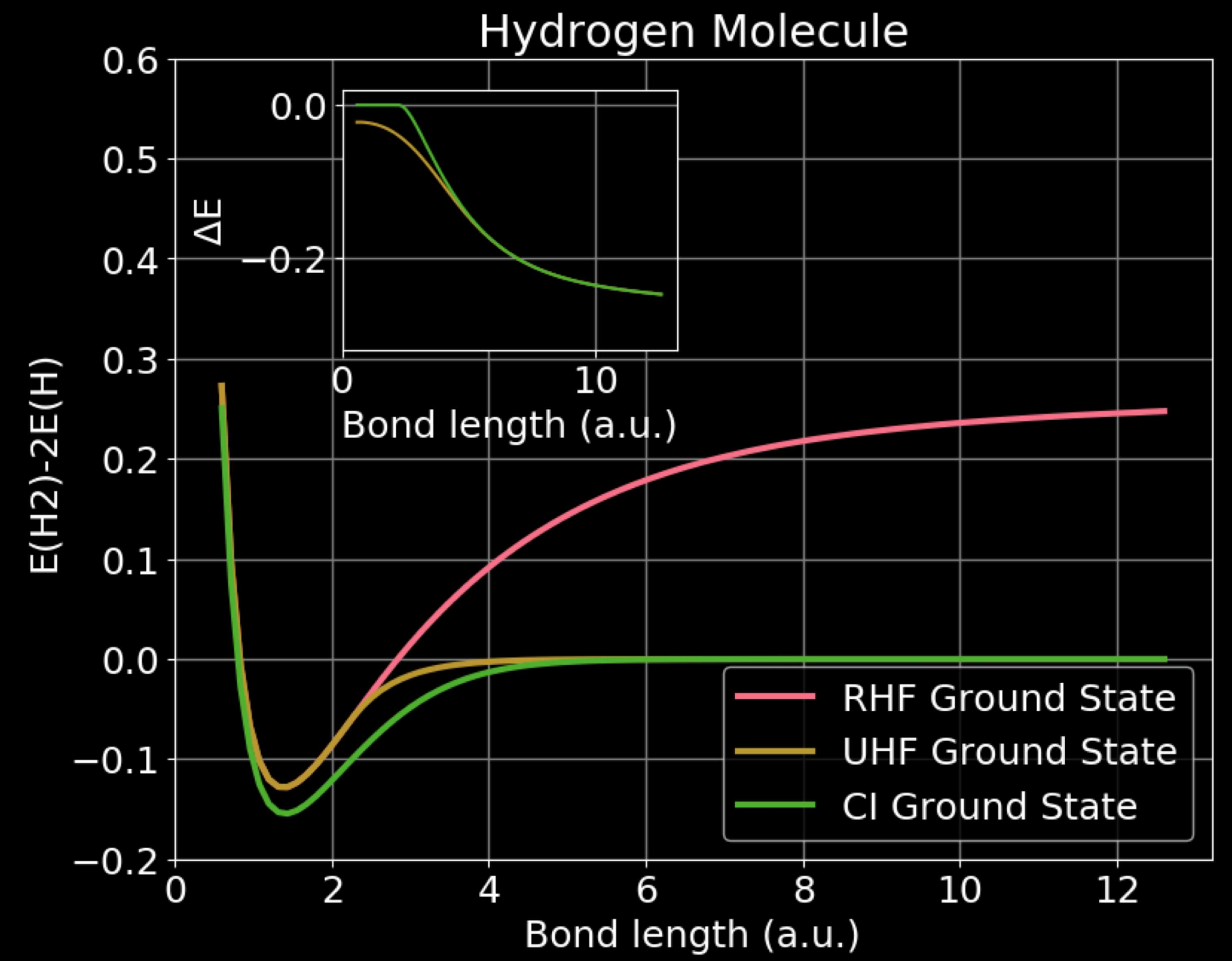
Energy of a SD

$$E = \langle\Phi|H|\Phi\rangle$$

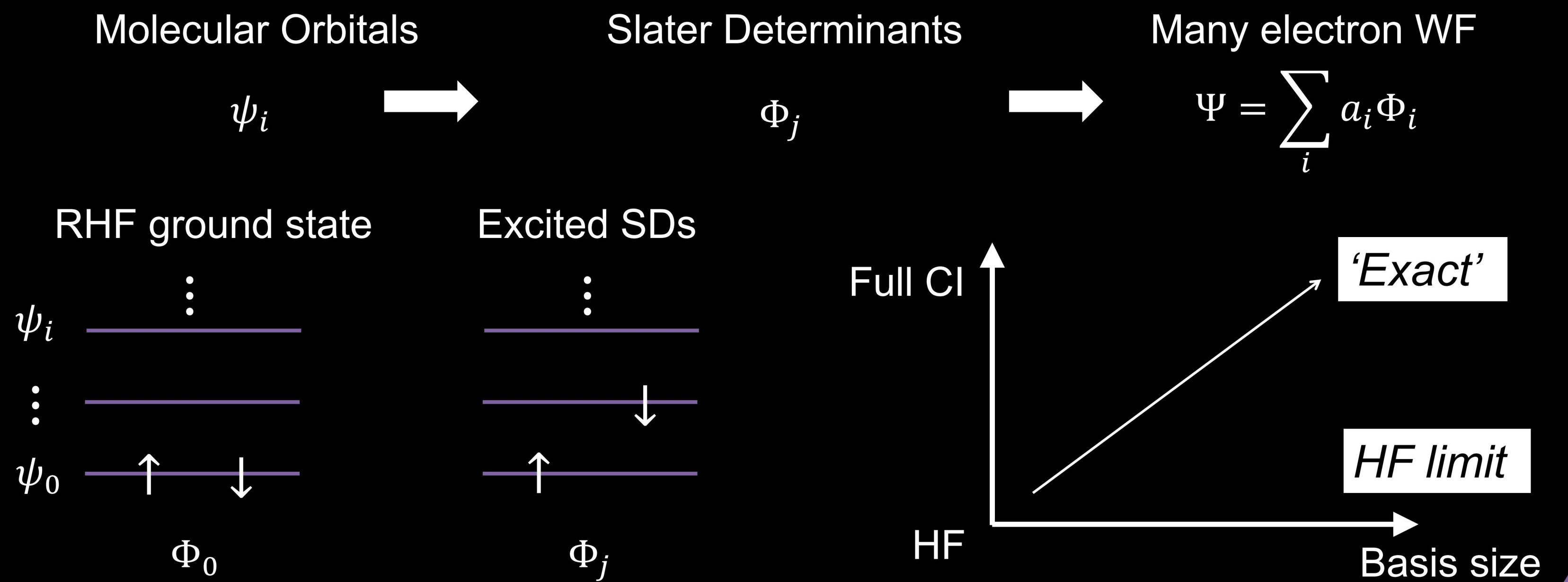
Fock Operator

$$F_i\psi_i = \varepsilon_i\psi_i$$

minimize



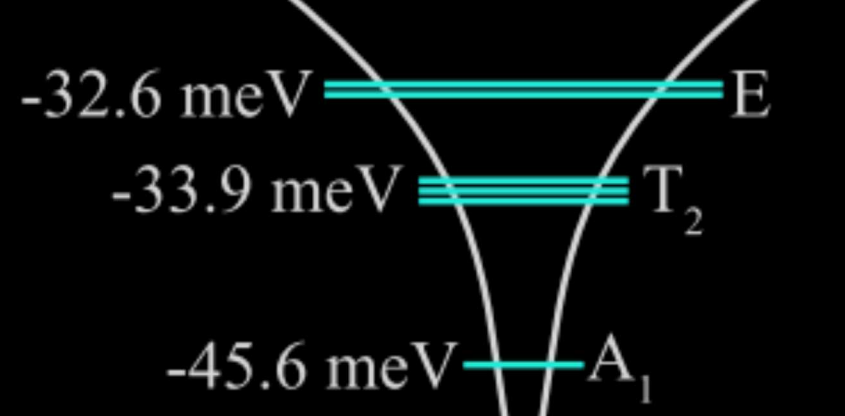
Configuration Interaction:



## 1. Multivalley Effective Mass Theory

Ansatz:

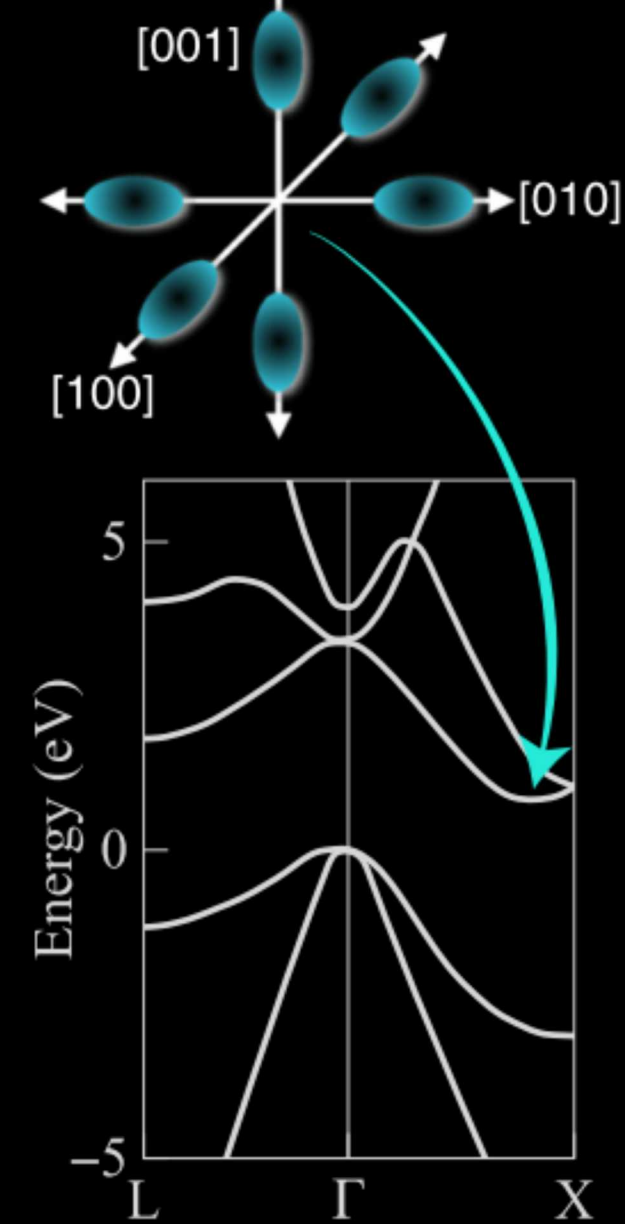
$$\psi(\vec{r}) = \sum_{j=1}^6 F_j(\vec{r})\phi_j(\vec{r})$$



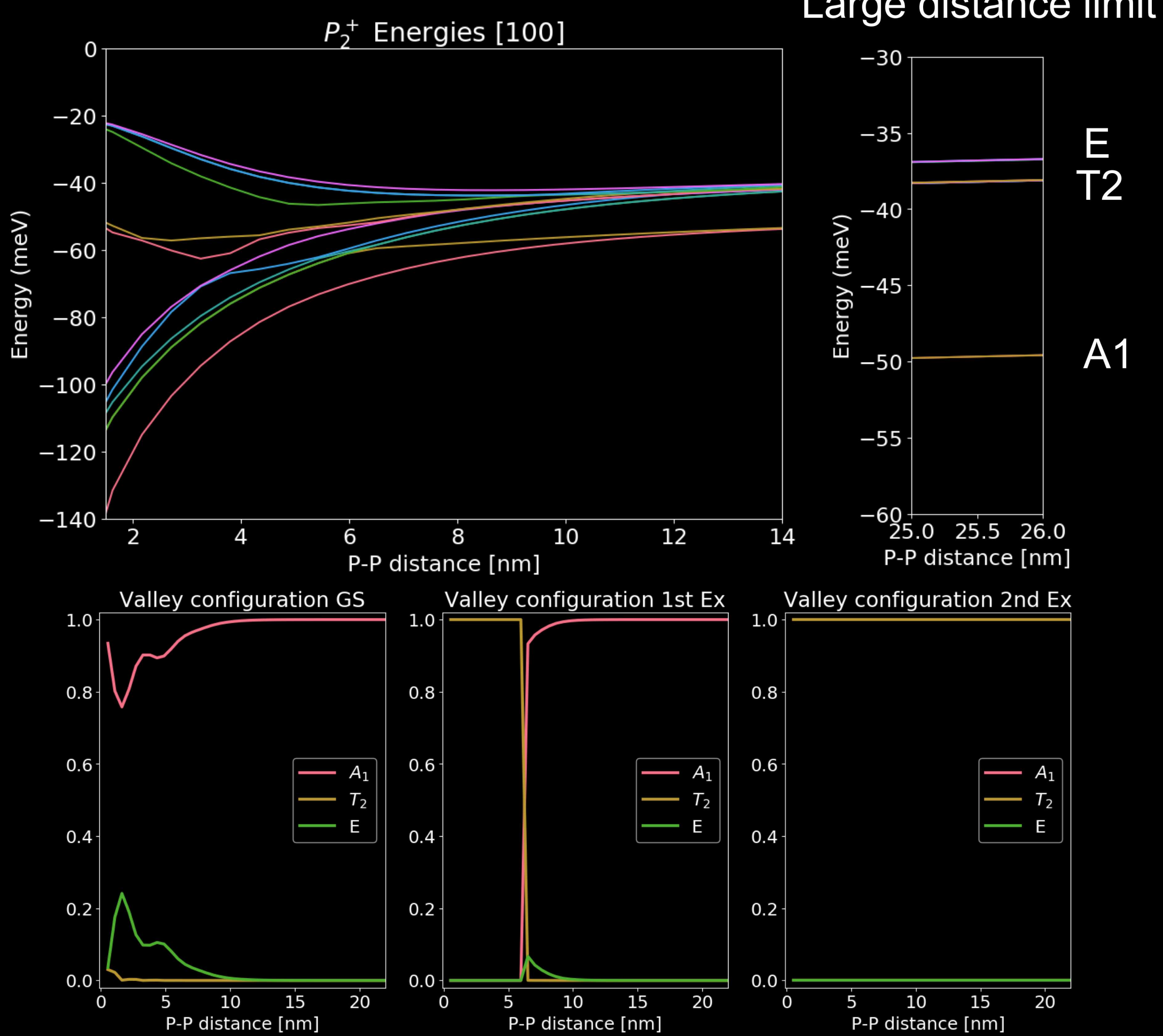
Valley orbit coupling

$$V_{ij}^{VO}(\vec{r}) = \langle\phi_i|U(\vec{r})|\phi_j\rangle$$

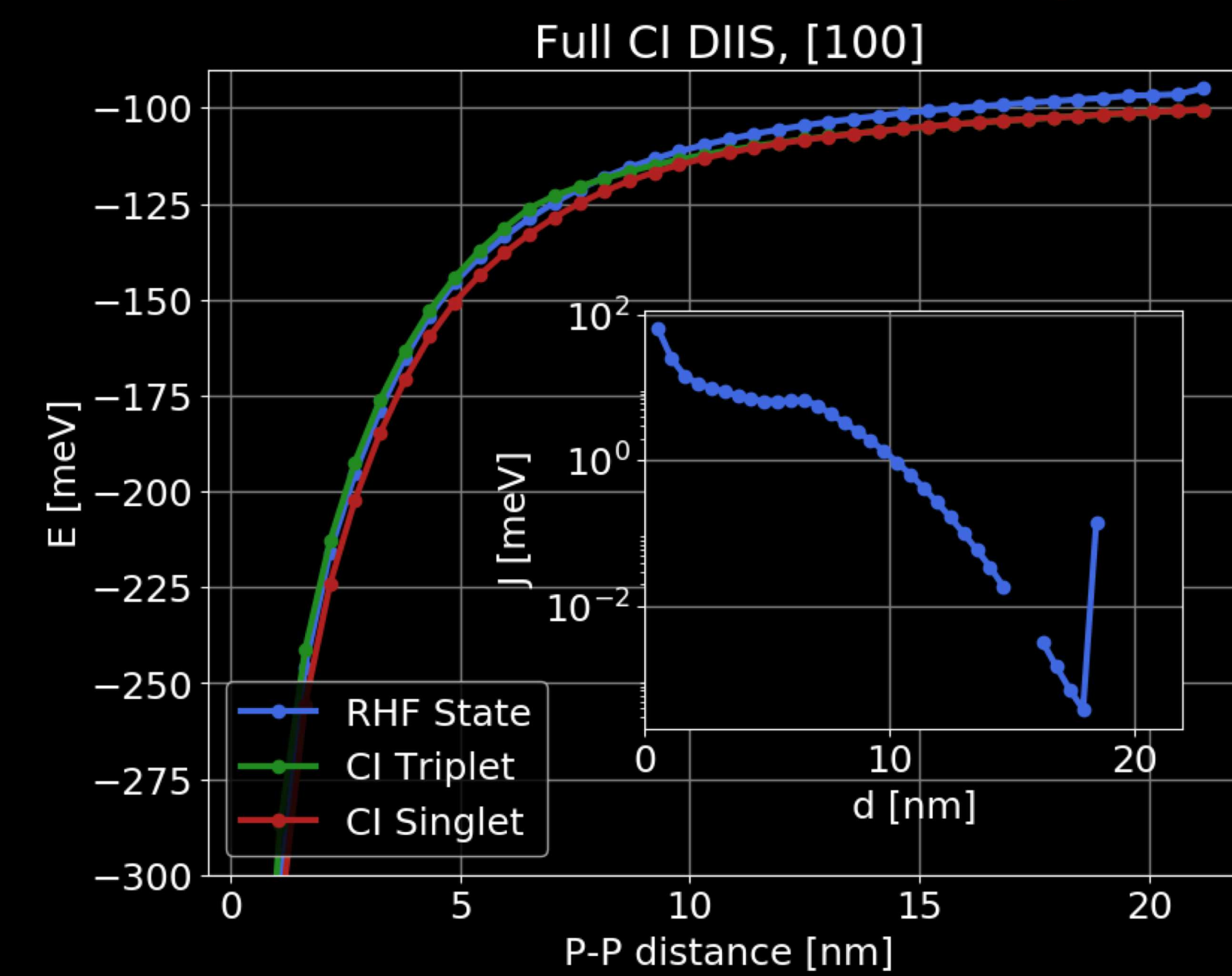
causes the valley splitting



## 2. P<sub>2</sub><sup>+</sup> Donor Cluster



## 4. Exchange Coupled Donors



Notable features:

- For large donor distances S and T are A1-like (as expected)
- At 7nm the Triplet mixes in T2
- Below 7nm the exchange appears to evolve non-exponential
- RHF fails for large distances

Future Plans:

- Extend basis to D<sup>-</sup>-like states
- ...

