



Full configuration interaction simulations of exchange coupled donors in silicon in an effective mass theory framework

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Abstract

Multi-qubit quantum logic gates are the final step to demonstrate the viability of donor spin qubits in silicon for quantum computation applications. Proposed two-qubit gates rely on the electron-electron exchange interaction which is highly sensitive to the relative placements of the donors in the silicon lattice¹. For two proximal phosphorus donors an inversion of the hierarchy of the valley-orbital split states has been observed, i.e. the crossing of the bonding combination of T2 states below that of the antibonding A1². Here, we use a full configuration interaction method within an established multivalley effective mass theory framework³ to model the two-electron wavefunction for different donor configurations. Specifically, we investigate the exchange interaction and valley population along different lattice orientations.

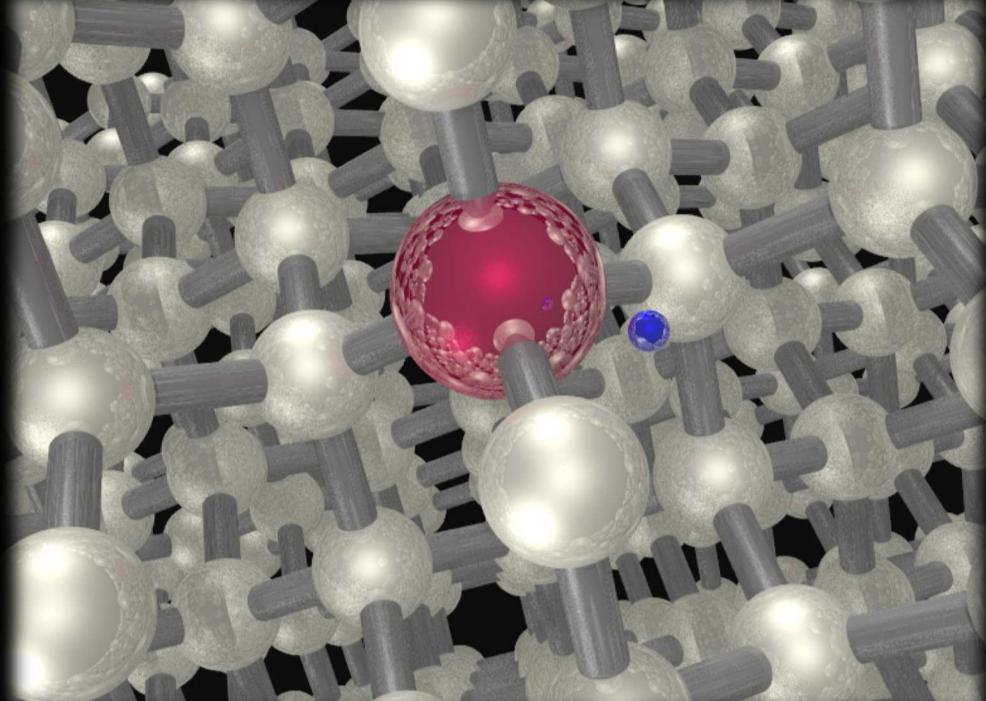
[1] R. Kalra, Phys. Rev. X 4(2), 021044 (2014)

[2] J.P. Dehollain, Phys. Rev. Lett. 112(23), 236801 (2014)

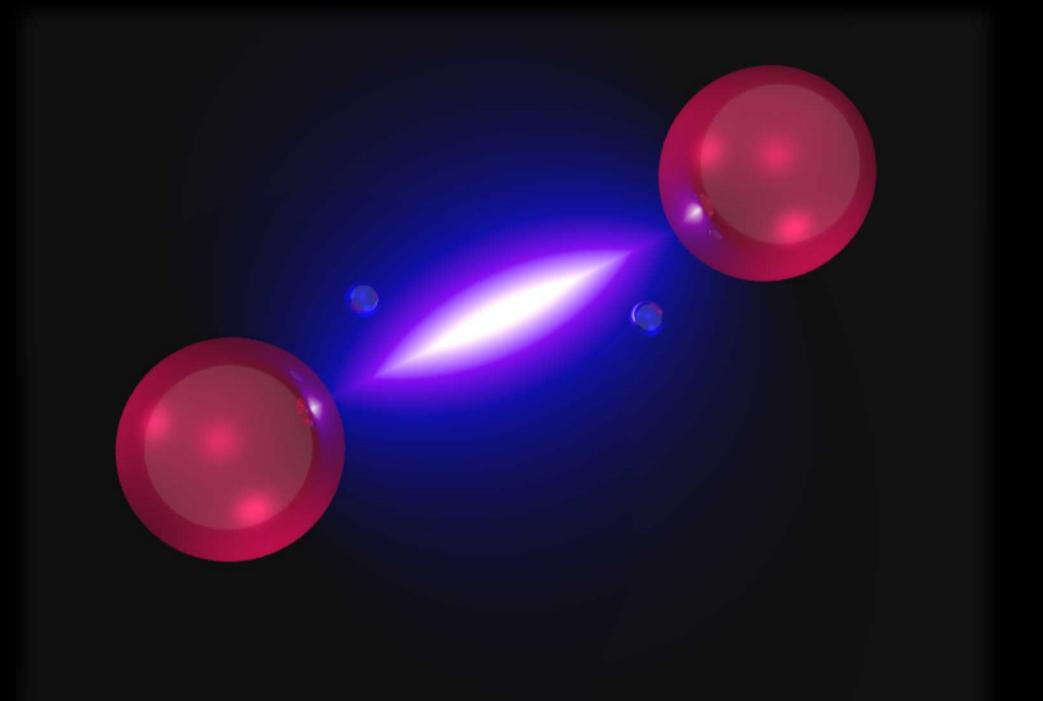
[3] J.K. Gamble, Phys. Rev. B 91(23), 235318 (2015)

Introduction

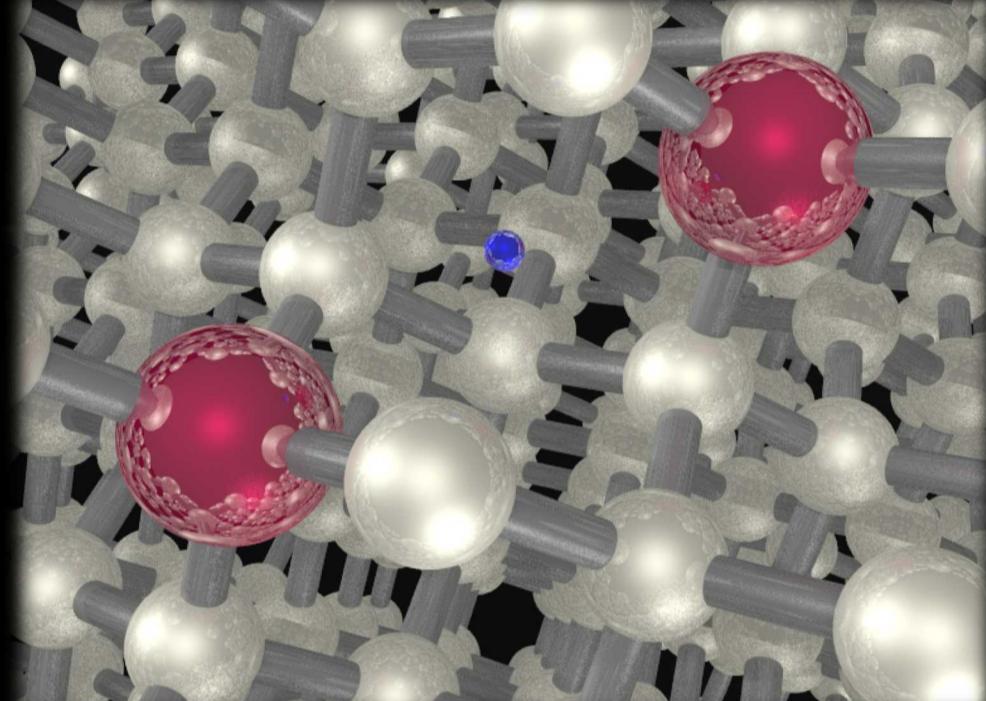
1. Single neutral donor



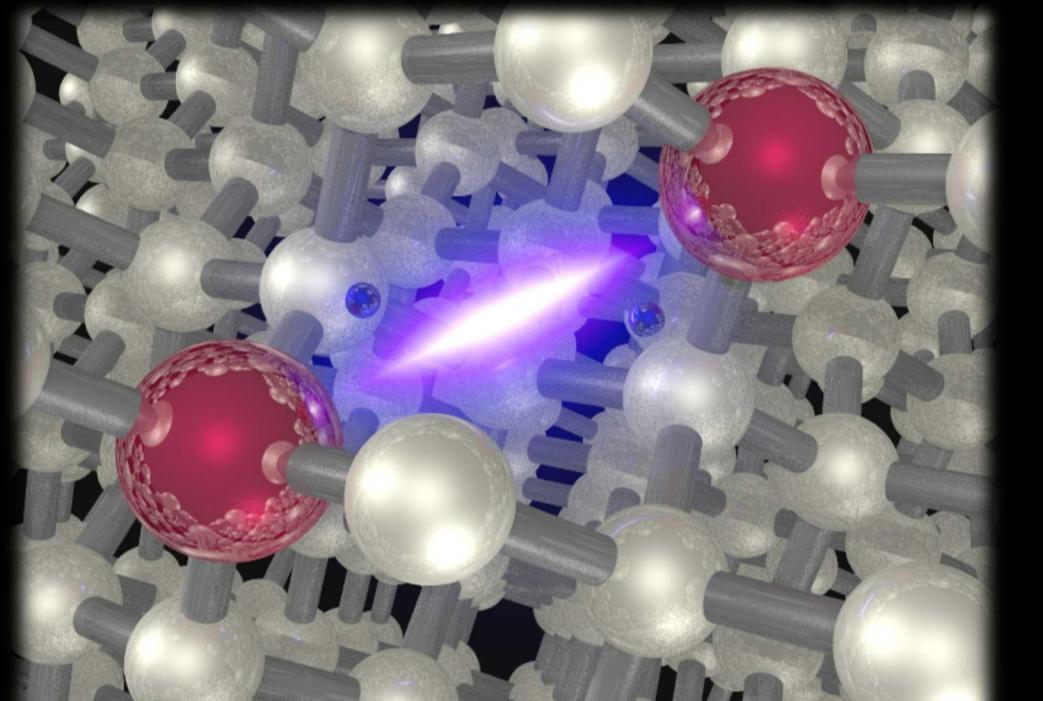
3. Hydrogen Molecule (H₂)



2. Two donors one e (P₂⁺)



4. Two neutral donors (P₂)



1. Multivalley Effective Mass Theory

Ansatz:

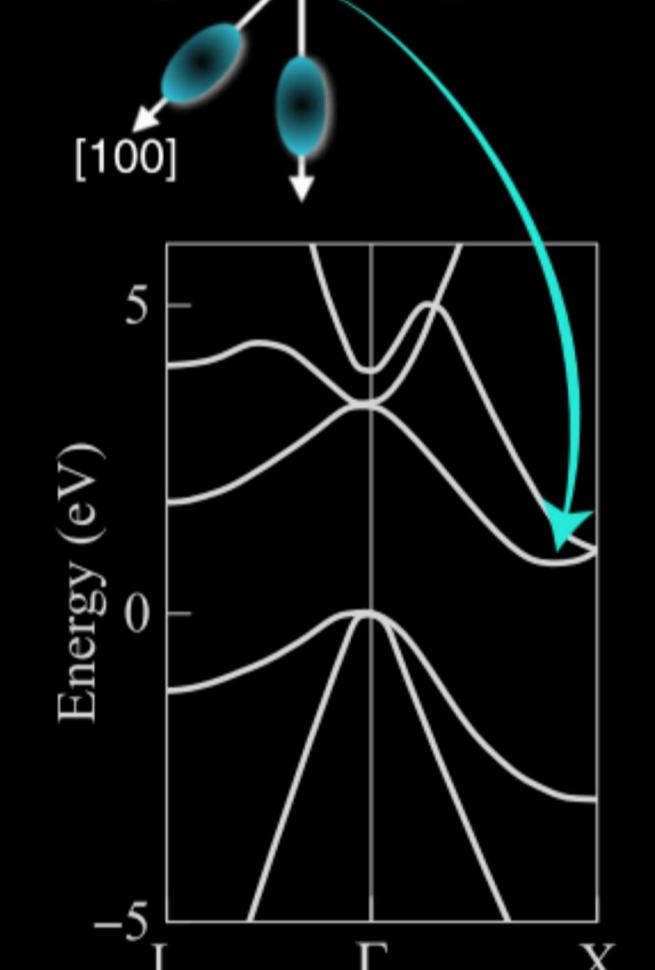
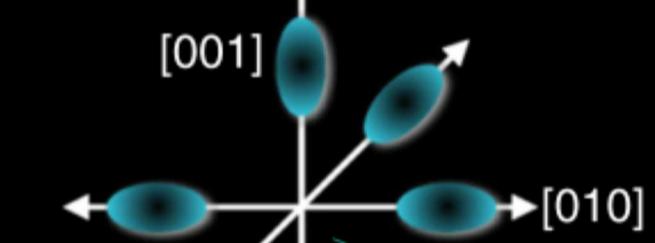
$$\psi(\vec{r}) = \sum_{j=1}^6 F_j(\vec{r}) \phi_j(\vec{r})$$



Valley orbit coupling

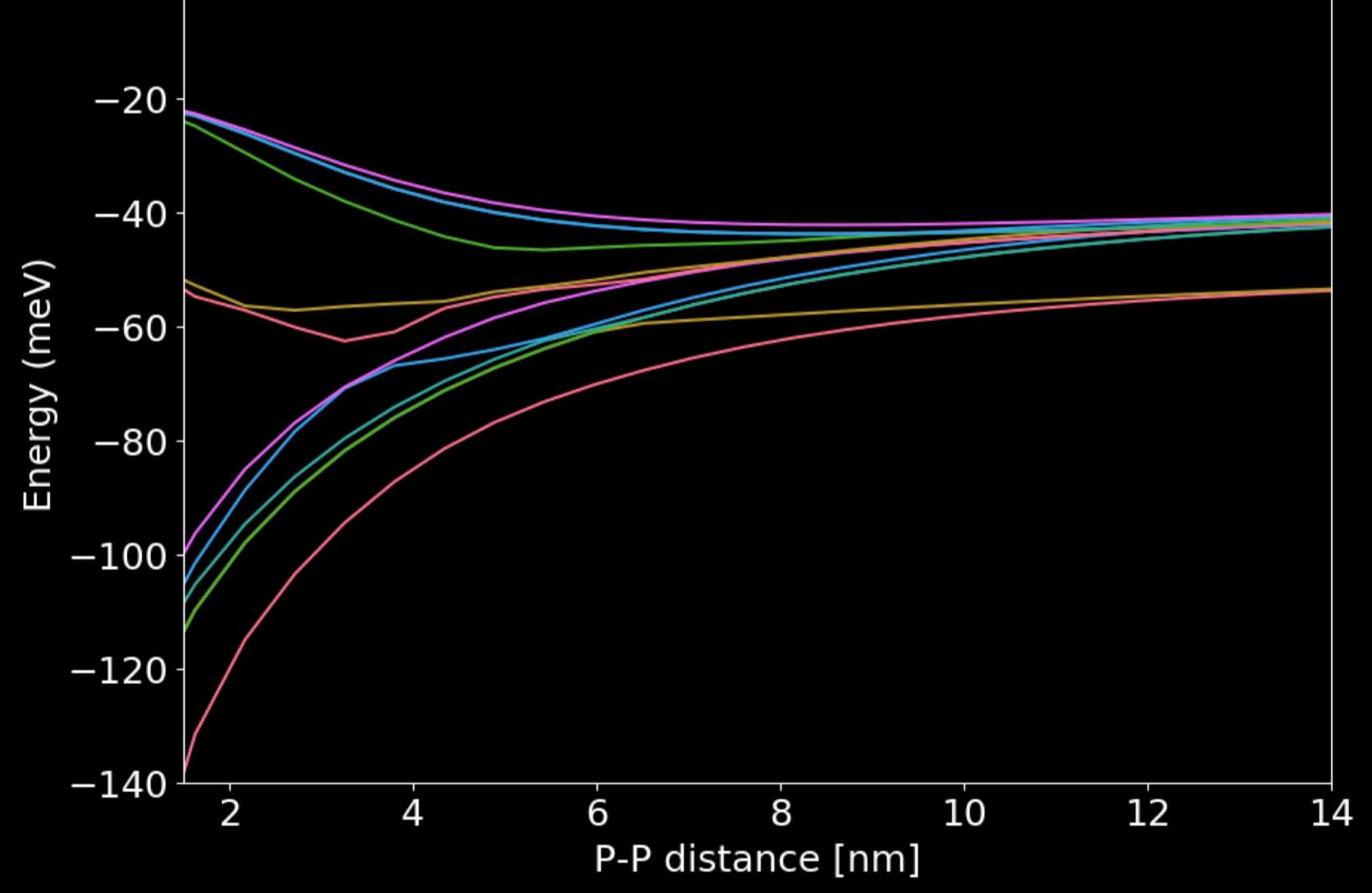
$$V_{i,j}^{VO}(\vec{r}) = \langle \phi_i | U(\vec{r}) | \phi_j \rangle$$

causes the valley splitting

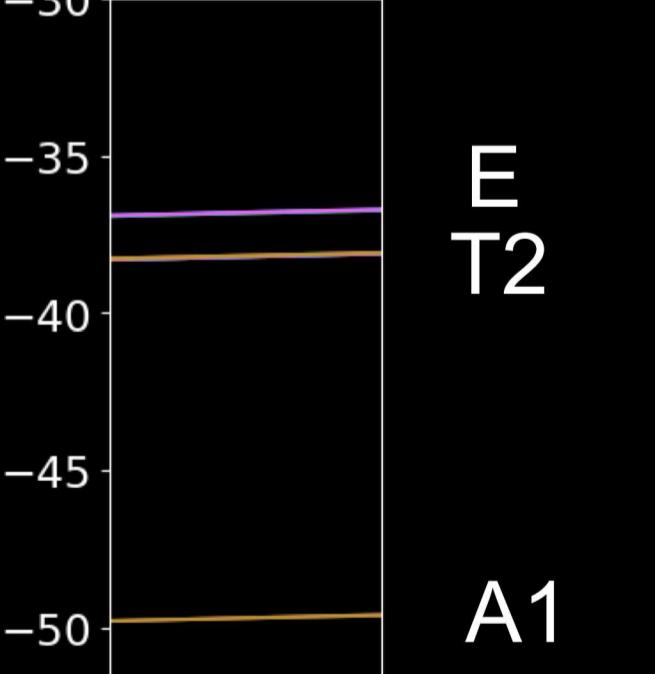


2. P₂⁺ Donor Cluster

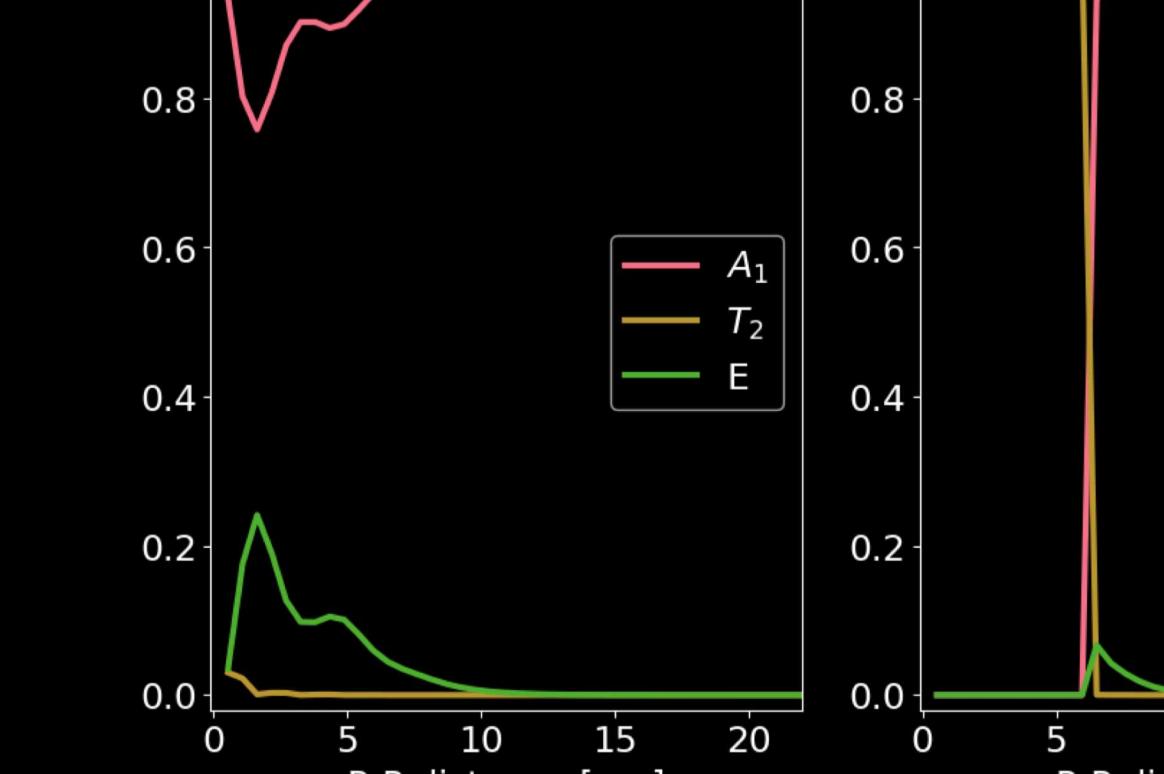
P₂⁺ Energies [100]



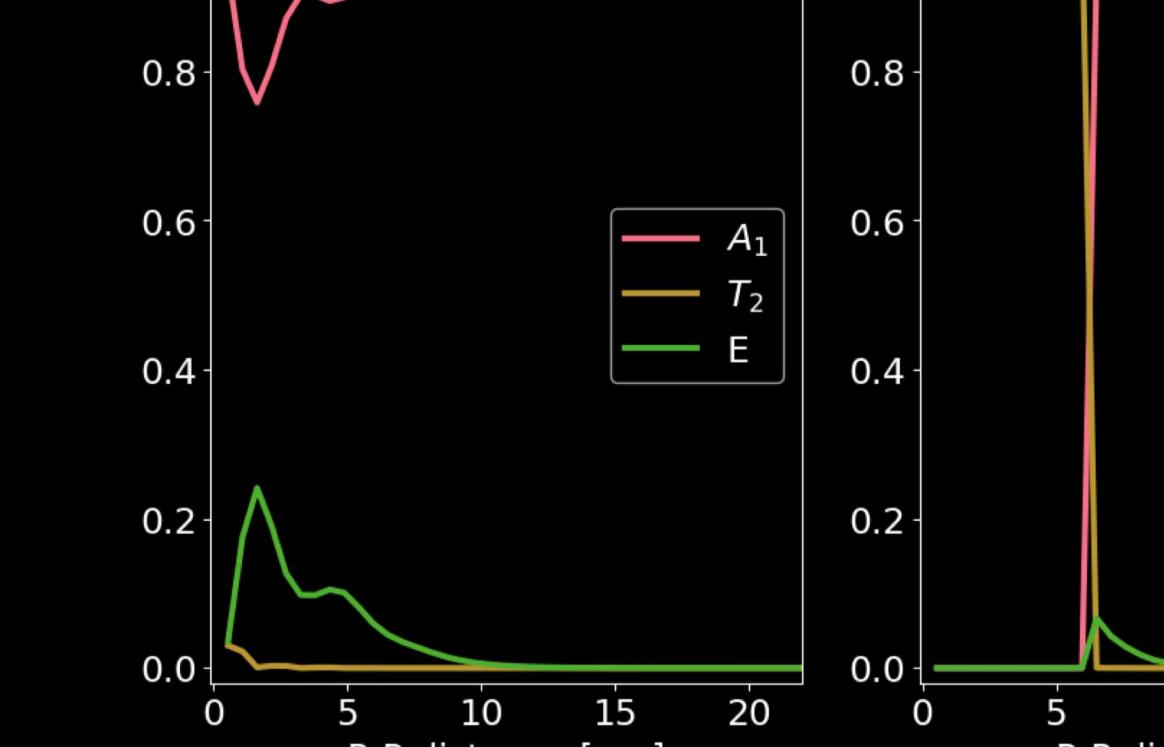
Large distance limit



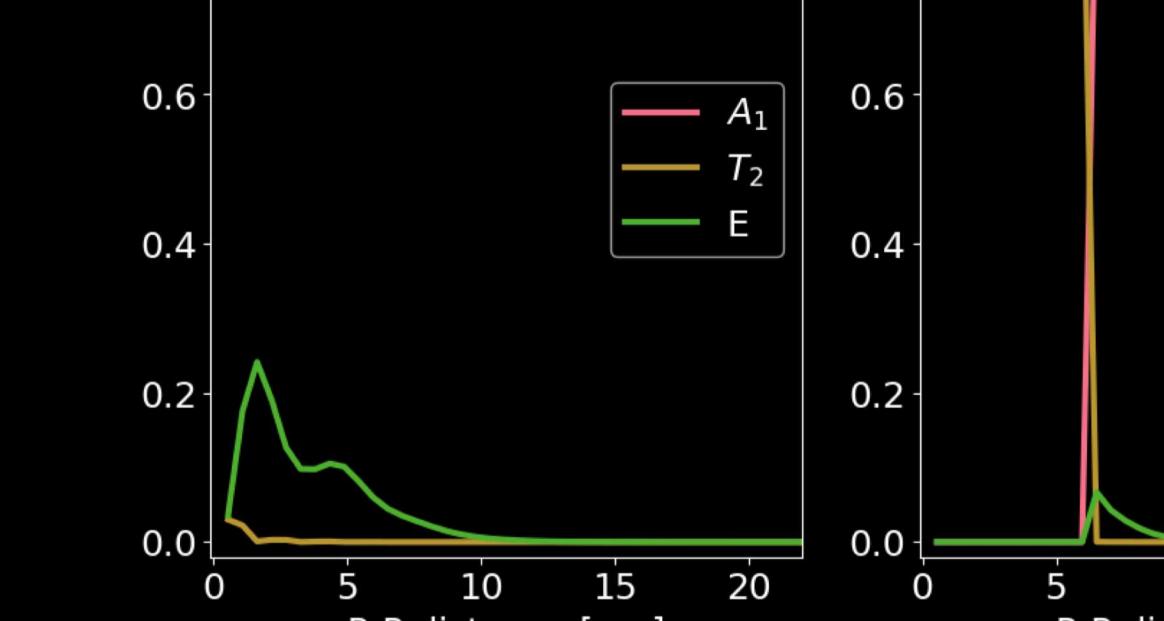
Valley configuration GS



Valley configuration 1st Ex



Valley configuration 2nd Ex



3. Hartree-Fock and Configuration Interaction

The Hartree-Fock Approximation:

$$\Phi = \frac{1}{\sqrt{2}} (|\psi_i \psi_j\rangle |\alpha\beta\rangle - |\psi_j \psi_i\rangle |\beta\alpha\rangle)$$

Energy of a SD

$$E = \langle \Phi | H | \Phi \rangle$$

Fock Operator

$$F_i \psi_i = \varepsilon_i \psi_i$$

minimize

Configuration Interaction:

Molecular Orbitals

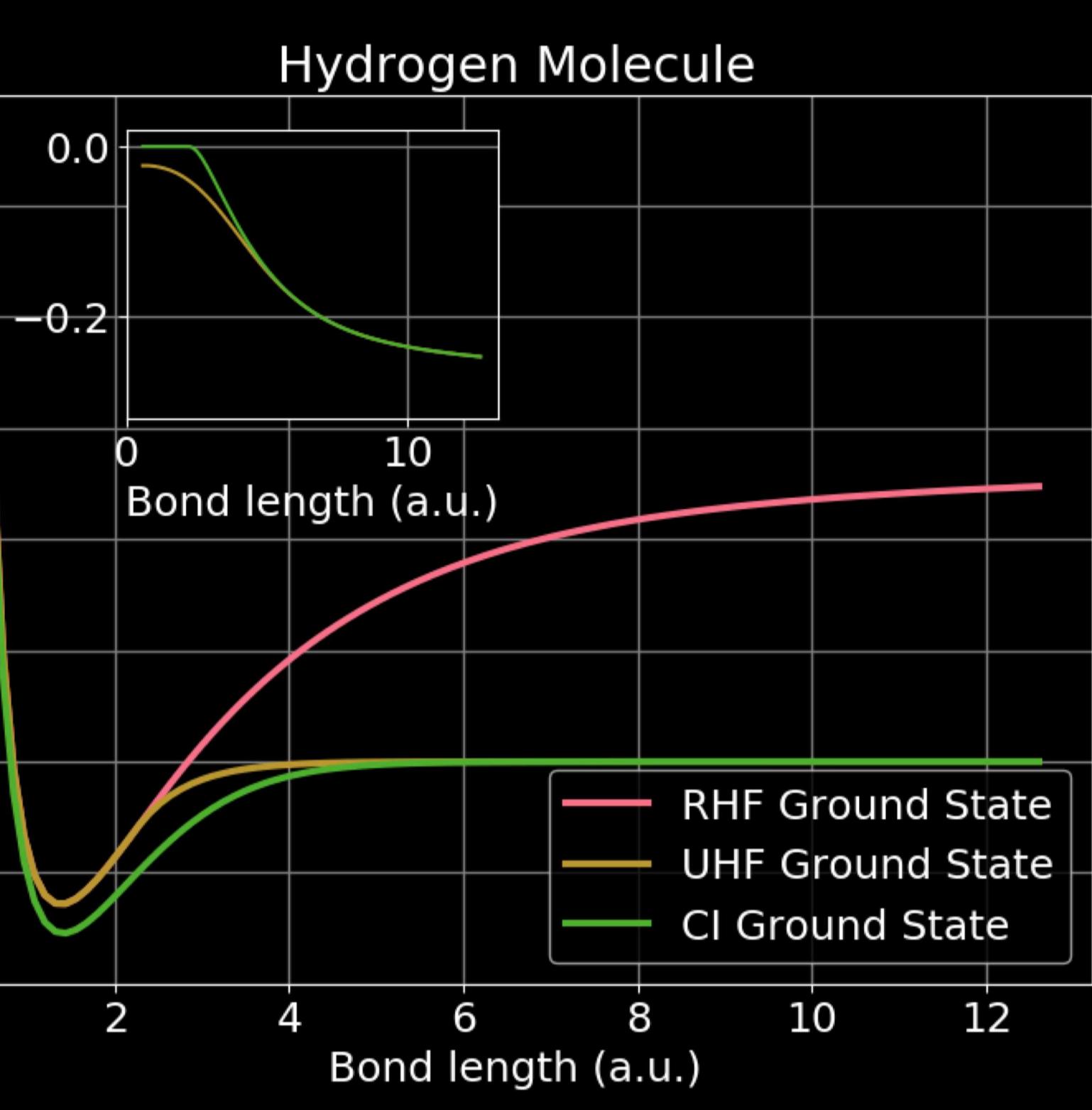
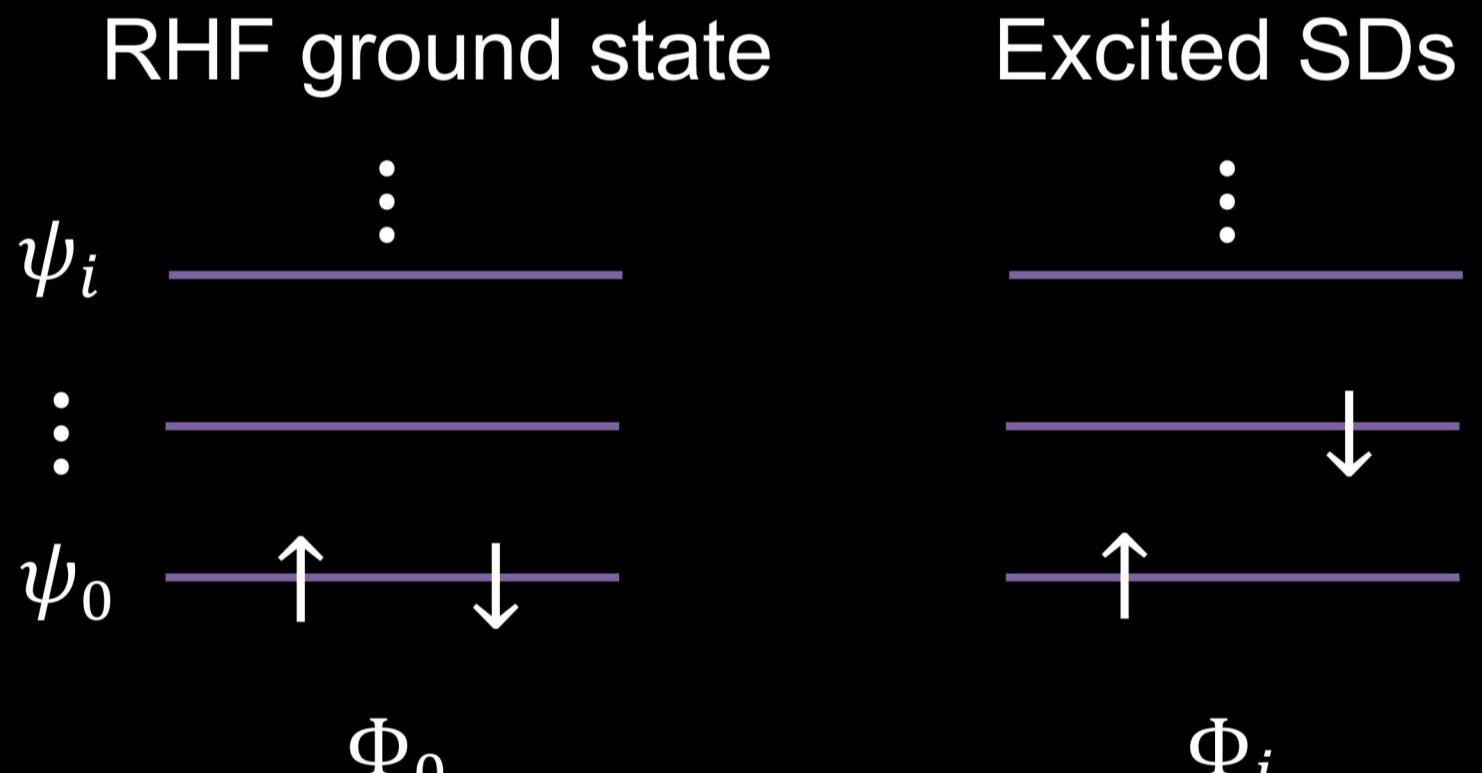
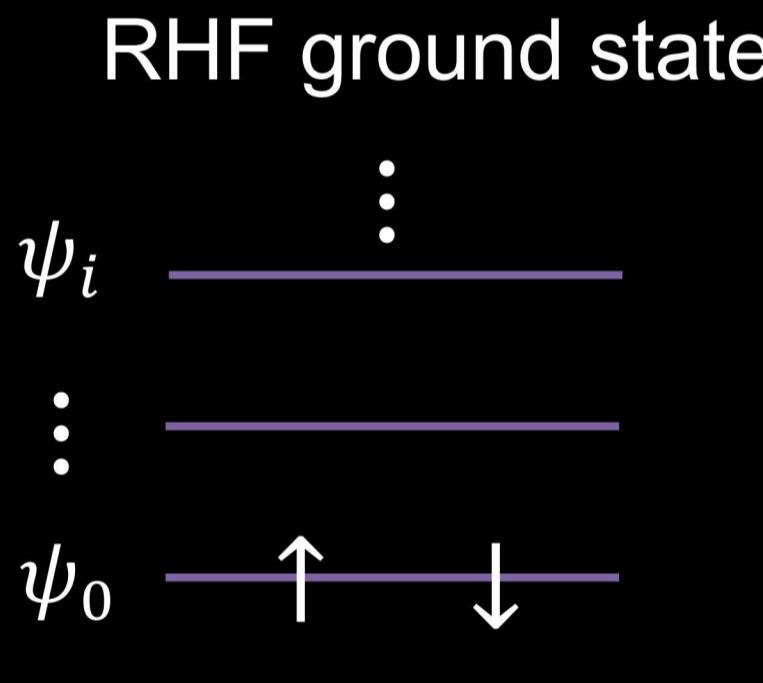
$$\psi_i \rightarrow$$

Slater Determinants

$$\Phi_j$$

Many electron WF

$$\Psi = \sum_i a_i \Phi_i$$



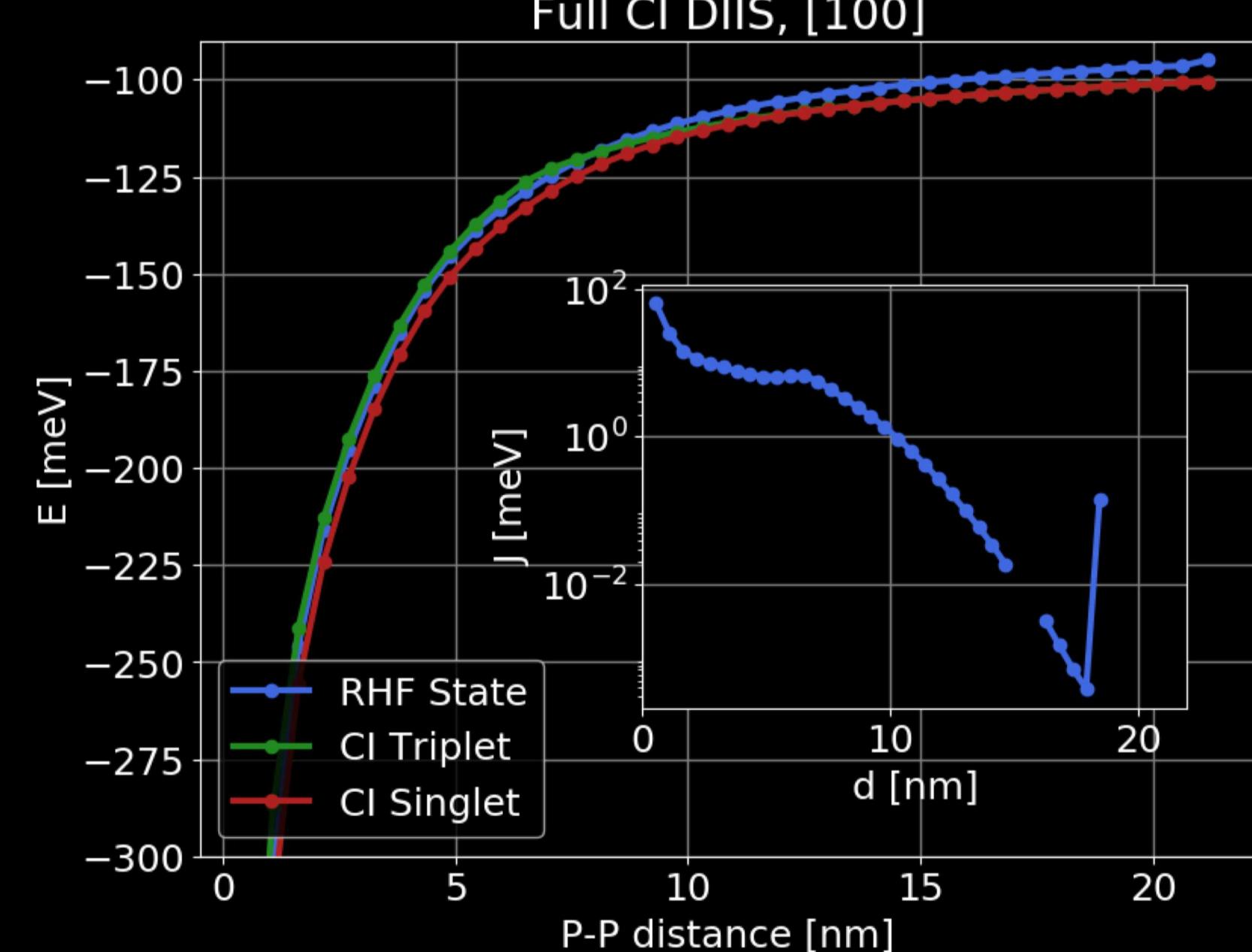
4. Exchange Coupled Donors

Notable features:

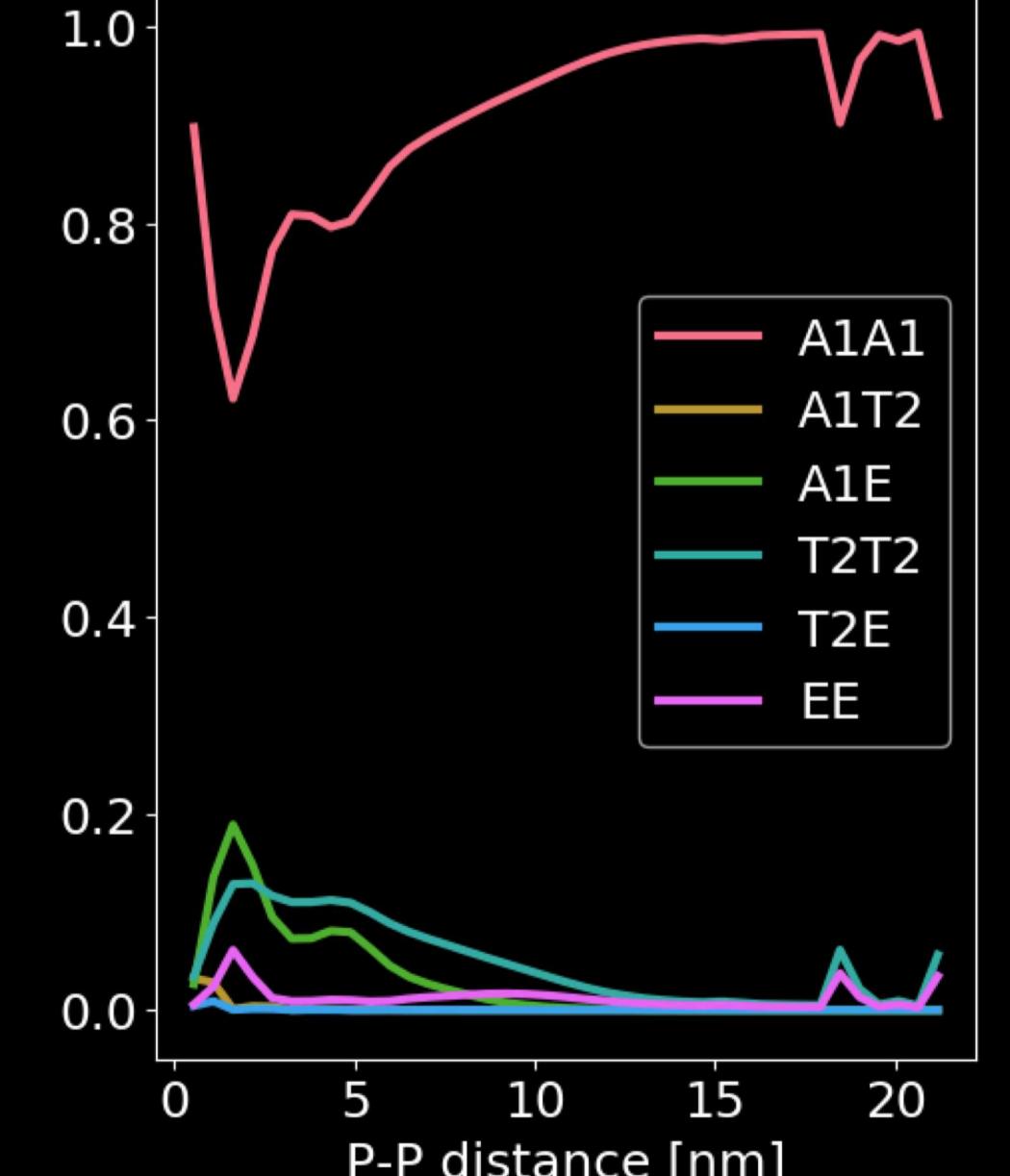
- For large donor distances S and T are A1-like (as expected)
- At 7nm the Triplet mixes in T2
- Below 7nm the exchange appears to evolve non-exponential
- RHF fails for large distances

Future Plans:

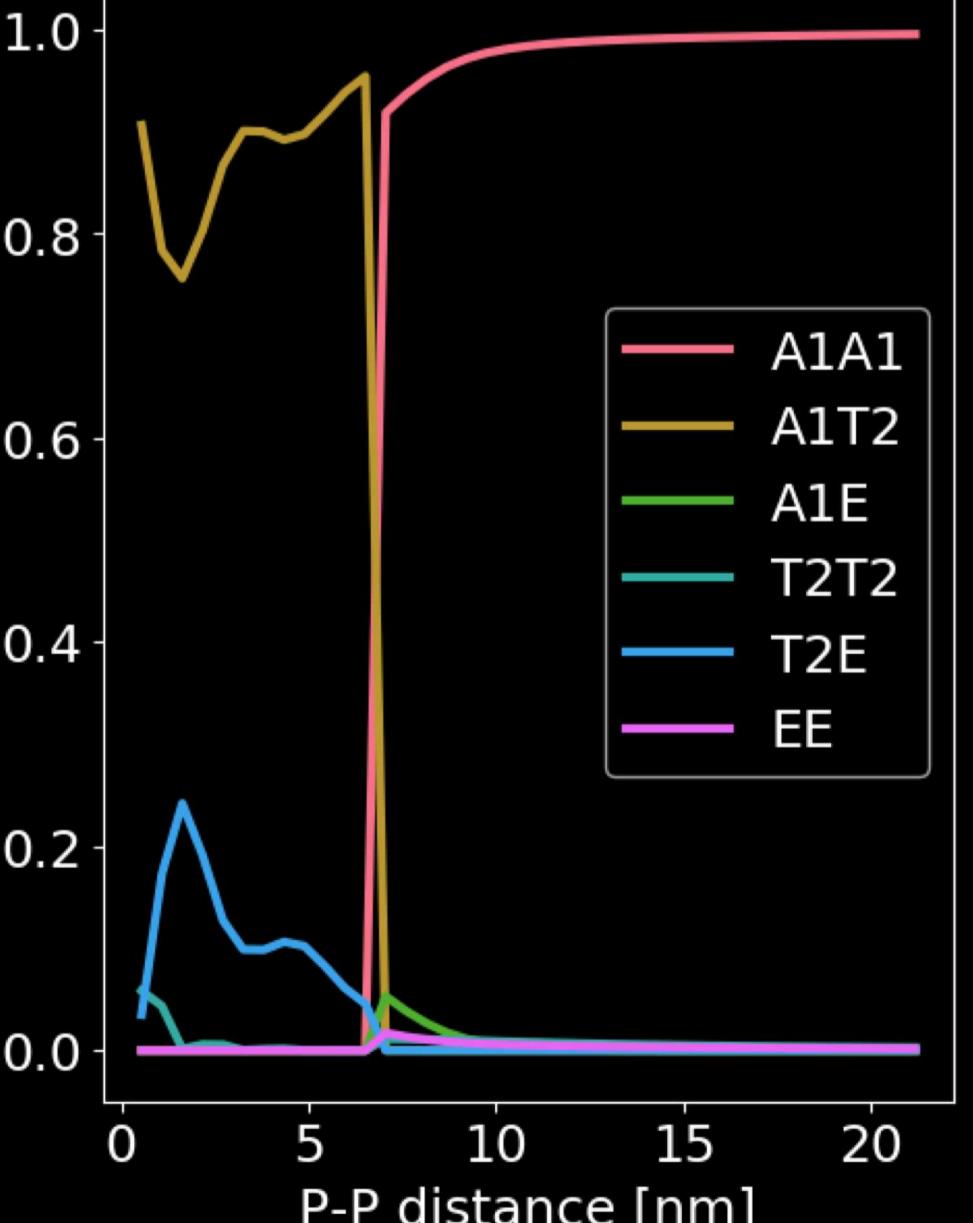
- Extend basis to D⁻-like states
- ...



Valley configuration Singlet



Valley configuration Triplet



Valley configuration RHF

