

## Radionuclide Source Term Inter-Comparison Study: GDSA Framework and RepoTREND

Jennifer M. Frederick, Emily R. Stein, and S. David Sevougian

*Sandia National Laboratories, Albuquerque, New Mexico, USA*

### Summary

*Code inter-comparison studies are useful exercises to verify and benchmark independently developed software to ensure proper function, especially when the software is used to model high-consequence systems which cannot be physically tested in a fully representative environment, such as modelling a performance assessment of a deep geologic nuclear waste repository. Sandia National Laboratories and Gesellschaft für Anlagen- und Reaktorsicherheit (GRS) are jointly embarking on a code inter-comparison study between GDSA Framework and RepoTREND. GDSA Framework and RepoTREND are two suites of software used to model performance assessments of deep geologic repositories for nuclear waste. PFLOTRAN, one of the primary software components of GDSA Framework and partially developed at Sandia National Laboratories, USA, is an open source, massively parallel subsurface simulator that solves systems of generally nonlinear partial differential equations describing multiphase, multicomponent, and multiscale reactive flow and transport processes in porous media. RepoTREND, developed by GRS, Germany, is a compartmentally designed suite of modules (e.g., LOPOS, POSA, COFRAME, BioTREND, et al.) for the simulation of near-field, far-field, and biosphere domains, specifically developed to model processes in a deep geologic nuclear waste repository.*

*This paper describes the results of the first portion of the code inter-comparison between PFLOTRAN and RepoTREND, which compares the radionuclide source term used in a typical performance assessment simulation.*

SAND2018-xxxx

### Introduction

Code inter-comparison studies are useful exercises to verify and benchmark independently developed software to ensure proper function, especially when the software is used to model high-consequence systems which cannot be physically tested in a fully representative environment, such as modelling a performance assessment of a deep geologic nuclear waste repository.

GDSA Framework and RepoTREND are two suites of software used to model performance assessments of deep geologic repositories for nuclear waste. PFLOTRAN [Lichtner et al. 2018], one of the primary software components of GDSA Framework [Sevougian et al. 2018] and partially developed at Sandia National Laboratories, USA, is an open source, massively parallel subsurface simulator that solves systems of generally nonlinear partial differential equations describing multiphase, multicomponent, and multiscale reactive flow and transport processes in porous media. RepoTREND [Reiche 2017], developed by Gesellschaft für Anlagen- und Reaktorsicherheit (GRS), Germany, is a compartmentally designed suite of modules (e.g., LOPOS, POSA, COFRAME, BioTREND, et al.) for the simulation of near-field, far-field, and biosphere domains, specifically developed to model processes in a deep geologic nuclear waste repository.

Sandia National Laboratories and GRS are jointly embarking on a code inter-comparison study between GDSA Framework and RepoTREND. The study is being undertaken in two phases. The first phase compares the radionuclide source term used in a typical performance assessment, which represents the convolution of the

waste-package degradation and waste-form dissolution rates, as well as the solubility of radionuclides in the aqueous phase in contact with the waste form. The second phase consists of a simplified performance assessment of a small, mined repository containing spent nuclear fuel in a salt host rock.

This paper describes the results of the first phase of code intercomparison between PFLOTRAN and RepoTREND, which compares the radionuclide source term used in a typical performance assessment simulation.

### Radionuclide Source Term Set-Up

Common to all geological disposal system models, regardless of the geologic media or repository design, are the waste packages containing nuclear waste. For any geologic disposal system model, proper representation of waste package degradation and waste form dissolution is essential. The first step in the code intercomparison study was to compare the radionuclide source term, which represents the convolution of the waste-package degradation and waste-form dissolution rates, as well as the solubility of radionuclides in the aqueous phase in contact with the waste form.

The waste packages modeled are assumed to contain spent nuclear fuel. A total of 80 waste packages make up the total inventory for this comparison case. The waste packages are assumed to breach instantly, thus allowing waste form dissolution, and radionuclide release, at the beginning of the simulation. The waste form dissolution rate was set to a fractional rate of  $1\text{e-}7\text{ yr}^{-1}$ . This means that  $1/10000000^{\text{th}}$  of the remaining waste form volume dissolves each year. The modeled radionuclide inventory consists of the following decay chain:  $^{241}\text{Am} \rightarrow ^{237}\text{Np} \rightarrow ^{233}\text{U} \rightarrow ^{229}\text{Th}$  and  $^{129}\text{I}$ . These radionuclides are typically important contributors to potential biosphere dose for waste packages containing PWR spent fuel. The PWR inventory used in this comparison has a burn-up of 60 GW-d/MTHM and is assumed to be 100 yr out of reactor waste. It is emplaced in the repository as 12 PWR assemblies per waste package.

It is noted that PFLOTRAN and RepoTREND treat the waste form radionuclide inventory differently. In PFLOTRAN, each waste form can be explicitly represented, and thus a radionuclide inventory can be defined per waste form in terms of grams-radionuclide per gram-bulk (g/g). However, in RepoTREND, the entire waste inventory is lumped into one value, in terms of g-radionuclide (g). For this reason, radionuclide inventory is given on a waste form basis, as well as a total inventory value representing all 80 modeled waste forms. This 80-package radionuclide inventory is shown in **Error! Reference source not found..**

**Table 1: Source term radionuclide inventory**

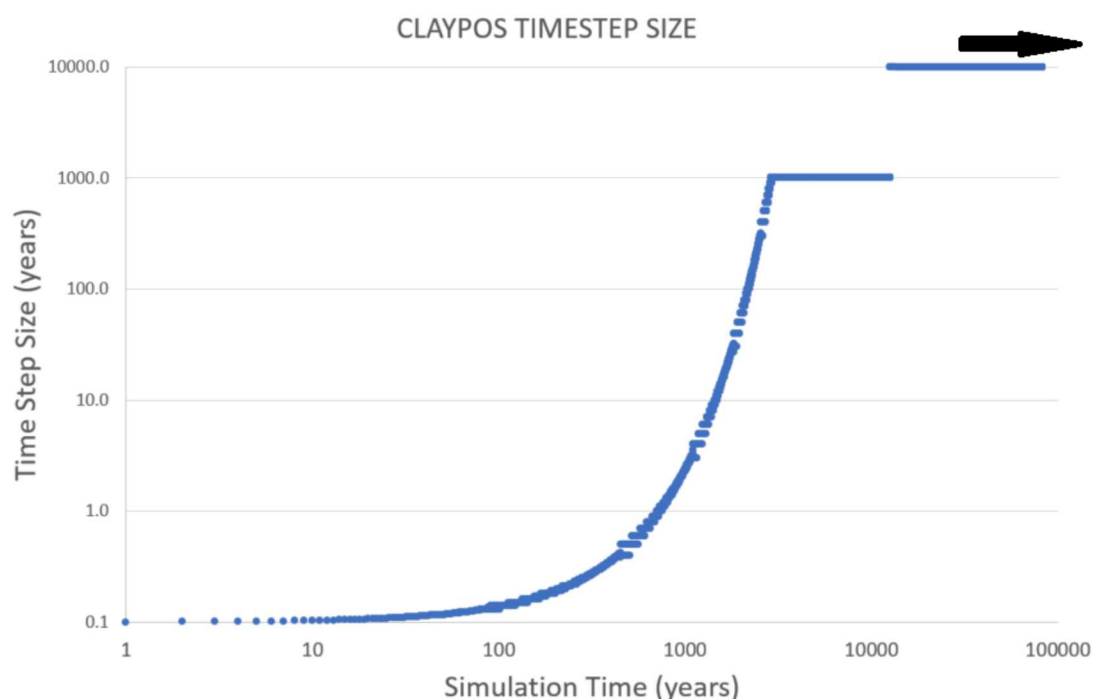
	$^{129}\text{I}$	$^{241}\text{Am}$	$^{237}\text{Np}$	$^{233}\text{U}$	$^{229}\text{Th}$
<b>Decay rate [1/s]</b>	1.29e-15	5.08e-11	1.03e-14	1.38e-13	2.78e-12
<b>Mass fraction in waste form [g/g]</b>	2.17e-4	1.01e-3	9.72e-4	3.01e-8	1.03e-11
<b>Total inventory (g)</b>	1.3e5	6.07e5	5.85e5	1.81e1	6.19e-3

### Comparison Results

The radionuclide source term was compared between PFLOTRAN and RepoTREND for a simulation time of  $1\text{e}^8$  yr. Both codes calculate the source term as the product of the remaining radionuclide inventory (in grams or moles) and the waste form dissolution rate ( $\text{yr}^{-1}$ ) at each time step of the simulation as it runs. For the results presented here, the PFLOTRAN results were extracted from the simulation after a careful time stepping scheme was chosen, but the RepoTREND results were generated separately (not as part of the RepoTREND simulation) using a time step size that ramps up as time proceeds, because extracting the source term value from the output of RepoTREND was too difficult at the time. The value of the time step size used in the CLAYPOS calculations is shown in Figure 1. The CLAYPOS time step ramps up slowly to  $1\text{e}^3$  years, staying

constant at  $1e^3$  years until approximately  $13e^3$  years, where it then jumps to  $1e^4$  years until the end of the simulation time. This time stepping scheme is not necessarily consistent with what would occur during a RepoTREND performance assessment simulation.

**Figure 1: Time step size for the RepoTREND (labelled as CLAYPOS) source term calculation results.**



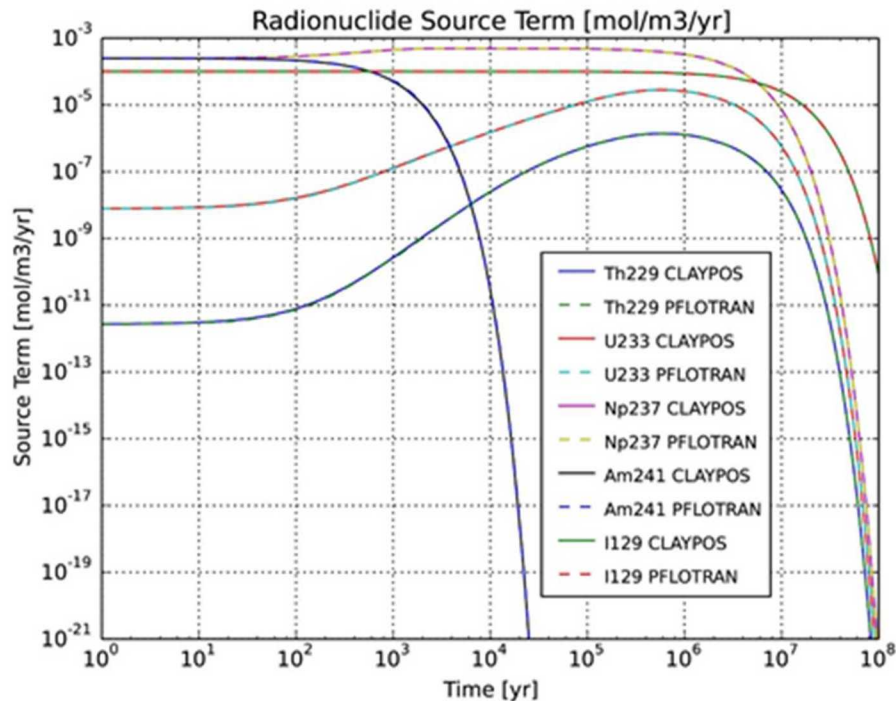
Additional differences between the two codes include the algorithm used to solve the partial differential equations that govern radionuclide decay and ingrowth. In PFLOTRAN, the system of equations can be solved for any number of generations iteratively and implicitly in time using Newton's method and LU decomposition. However, for simple decay chains that involve three radionuclide generations or less, and zero initial daughter concentration, PFLOTRAN can use an analytical solution, which is exact. For the results presented here, the analytical solution approach was chosen for the PFLOTRAN source term calculations, unless otherwise indicated. In RepoTREND, it is assumed that each parent radionuclide decays into a single unique daughter. Under this assumption, the decay equation is solved analytically, beginning with the uppermost level in the decay chain and inserting the solution recursively into the next level of the decay chain.

Figure 2 presents the results of the source term comparison between PFLOTRAN and RepoTREND. The RepoTREND results are labeled as CLAYPOS, because that is the name assigned to the module in RepoTREND responsible for calculating the radionuclide source term. The two codes produce identical values for the radionuclide source term as a function of time, and therefore compare exceptionally well, as long as time step size is similar between the two codes and the analytical solution approach is used in PFLOTRAN.

### Time Stepping Issues

Initial attempts at the source term comparison showed that the source term calculation is sensitive to the choice of time step. This is because of two main reasons. The first reason is time truncation error in the iterative numerical algorithm that solves the set of partial differential equations that describe decay and ingrowth (labeled as Type I error). The analytical solution does not suffer from time truncation error, but it is limited to simple decay chains. The second reason is that the source term is a rate which is held constant over the time step. Therefore, taking several small time steps means the code is updating the source term rate more often than if it took fewer, larger time steps (labeled as Type II error). This second reason applies to both the implicit, iterative solution method, as well as the analytical solution approach.

**Figure 2: Radionuclide source term comparison results between PFLOTRAN and RepoTREND (labelled as CLAYPOS). The analytical solution approach is used in PFLOTRAN to solve for decay and ingrowth.**



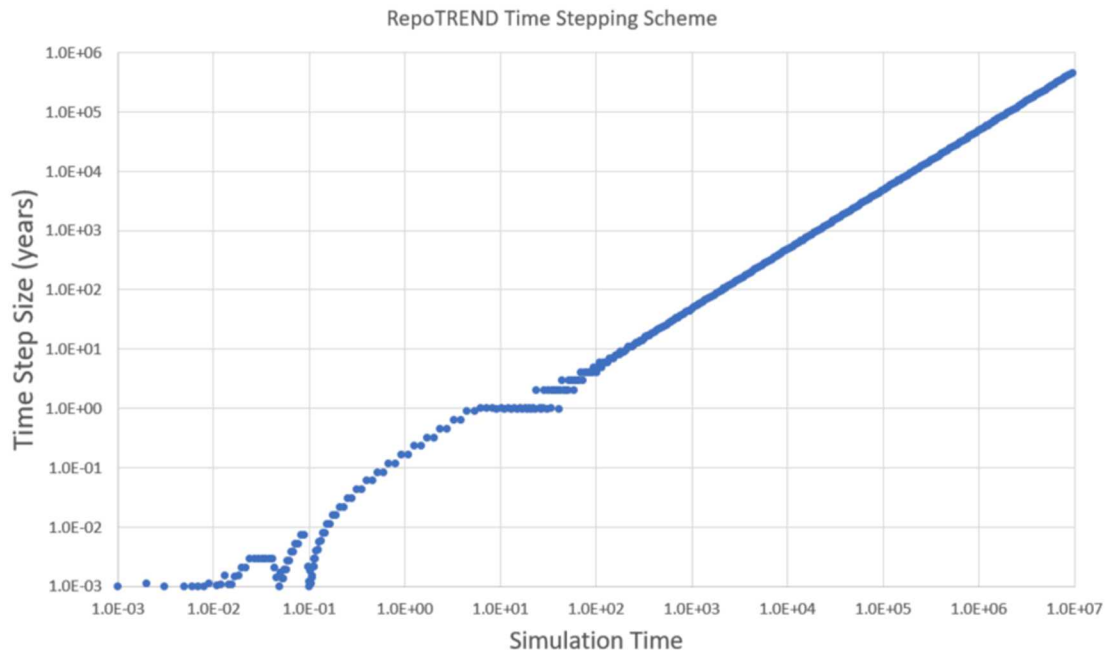
As previously noted, the RepoTREND results shown in Figure 2 were generated separately (not as part of the RepoTREND simulation) using several small ramped time steps because extracting the source term value from the output of RepoTREND was too difficult at the time. The CLAYPOS calculations, therefore, minimize the numerical error when time step ramps up slowly (both Type I and Type II), but the time step scheme presented may not necessarily be practical for a performance assessment simulation if the ramp-up rate is very slow. In other words, this particular time stepping scheme was not tested for a typical performance assessment simulation (a more typical RepoTREND time stepping scheme is shown in Figure 3). The PFLOTRAN results in Figure 2, on the other hand, were produced using the following time stepping scheme, which was chosen to minimize Type II error, but also represented a practical time stepping scheme that was tested for a typical performance assessment simulation (recall the analytical solution approach has no Type I error). In the following PFLOTRAN time stepping scheme, note that the time step size grows gradually, but not as gradually as the scheme chosen for CLAYPOS. Also note that the largest time step size is  $2e^3$  years for PFLOTRAN, but  $10e^3$  years for CLAYPOS.

```
TIME
  FINAL_TIME 1.0d8 y
  INITIAL_TIMESTEP_SIZE 1.d-6 y
  MAXIMUM_TIMESTEP_SIZE 1. y at 1. y
  MAXIMUM_TIMESTEP_SIZE 5. y at 10. y
  MAXIMUM_TIMESTEP_SIZE 10. y at 100. y
  MAXIMUM_TIMESTEP_SIZE 50. y at 1000. y
  MAXIMUM_TIMESTEP_SIZE 100. y at 10000. y
  MAXIMUM_TIMESTEP_SIZE 500. y at 100000. y
  MAXIMUM_TIMESTEP_SIZE 1000. y at 500000. y
  MAXIMUM_TIMESTEP_SIZE 2000. y at 700000. y
END
```

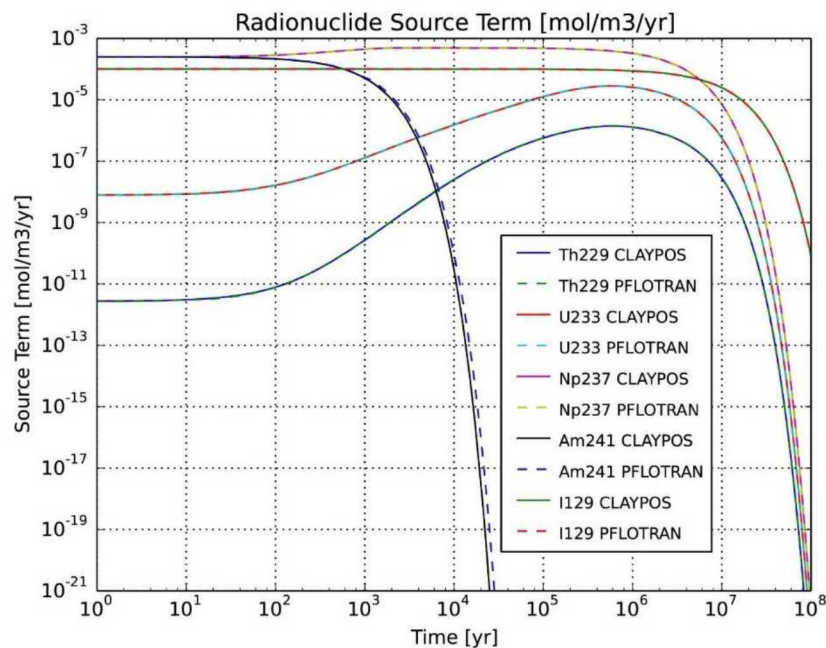


If in PFLOTRAN, the iterative, implicit solution approach is used instead of the analytical solution approach, then the comparison is slightly worse due to the introduction of Type I error. Figure 4 presents the source term comparison between PFLOTRAN and RepoTREND using the same time stepping scheme as shown above, but using the iterative, implicit solution approach. Note that the  $^{241}\text{Am}$  source term is slightly larger in PFLOTRAN than the RepoTREND results.

**Figure 3: Time step size for a typical RepoTREND performance assessment simulation.**



**Figure 4: Radionuclide source term comparison results between PFLOTRAN and RepoTREND (labelled as CLAYPOS). The implicit, iterative solution approach is used in PFLOTRAN to solve for decay and ingrowth.**



As a final example, Type II error is introduced if the time step is allowed to grow too large, too fast, and too suddenly. Using the following time stepping in PFLOTRAN demonstrates this rapid time step growth, and the results are shown in Figure 5.

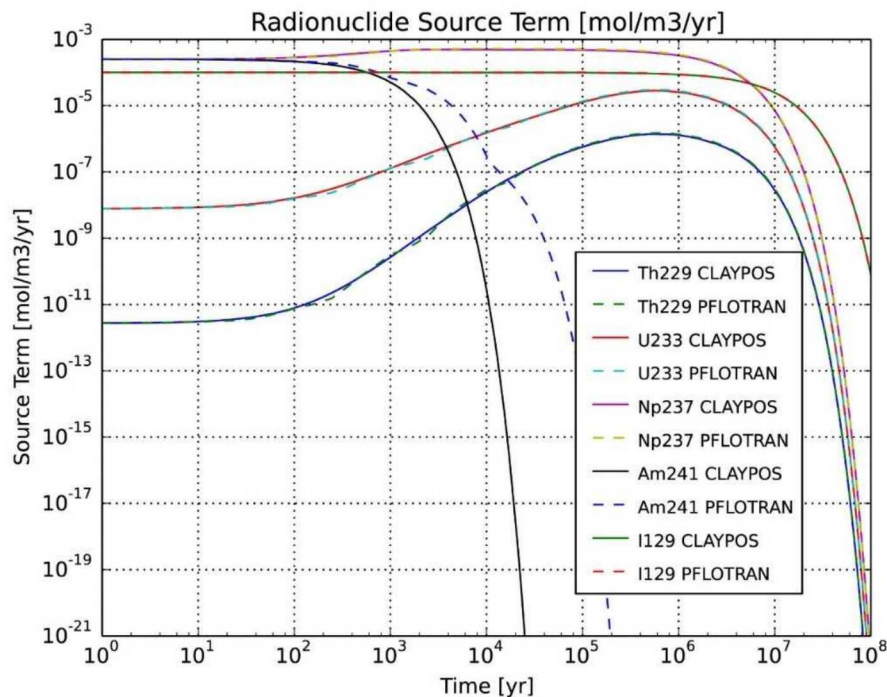
```

TIME
  FINAL_TIME 1.0d8 y
  INITIAL_TIMESTEP_SIZE 1.d-6 y
  MAXIMUM_TIMESTEP_SIZE 1. y at 1. y
  MAXIMUM_TIMESTEP_SIZE 10. y at 10. y
  MAXIMUM_TIMESTEP_SIZE 100. y at 100. y
  MAXIMUM_TIMESTEP_SIZE 1000. y at 1000. y
  MAXIMUM_TIMESTEP_SIZE 5000. y at 10000. y
END

```

Note that the difference in the  $^{241}\text{Am}$  source term is much larger, and each time PFLOTRAN suddenly increases the time step size, there is a bend, or hump in the curve. The bend is clearly seen for  $^{241}\text{Am}$  at  $1\text{e}^3$  years, but can also be seen for  $^{233}\text{U}$  and  $^{229}\text{Th}$  at early times. This is not ingrowth. Besides  $^{241}\text{Am}$ , which has a fast decay rate, the Type II error introduced at early times does not seem to affect source term values for later times when the radionuclide decay rate is very slow. Moreover, sudden increases in time step early-on in the simulation introduce much more error than when time step is increased later in the simulation.

**Figure 5: Radionuclide source term comparison results between PFLOTRAN and RepoTREND (labelled as CLAYPOS). The implicit, iterative solution approach is used in PFLOTRAN to solve for decay and ingrowth, with rapid increases in the time step size.**



## Conclusions

This summary describes the results of the first portion of the code inter-comparison between PFLOTRAN and RepoTREND, which compares the radionuclide source term used in a typical performance assessment. The two codes compare exceptionally well when time step size is ramped up in RepoTREND (CLAYPOS), and when PFLOTRAN uses slowly increasing time step size with the analytical solution approach.

However, initial comparison attempts showed that the radionuclide source term is sensitive to time step size in PFLOTRAN (and probably RepoTREND, although this has not been explicitly shown) due to Type I and Type II error. While the analytical approach to solve the partial differential equations that govern decay and ingrowth in PFLOTRAN can only suffer from Type II error, it is limited to simple decay chains that have three radionuclide generations or less. To model more complex decay chains, the implicit, iterative solution approach must be used, but it additionally suffers from Type I error as well.

In order to minimize both Type I and Type II numerical errors, it is important to carefully choose the time stepping scheme so that time step size slowly increases over the simulation time. This can be manually controlled in PFLOTRAN by setting the maximum time step size at pre-determined times in the simulation. In RepoTREND, an automatic time ramping scheme is used, which limits control over the time step size. Without precise control over time step size, the source term may suffer from numerical error. However this is overcome in RepoTREND because it uses an analytical solution approach to solve for decay and ingrowth.

Recall that the RepoTREND results shown in all figures were generated separately (not as part of the RepoTREND simulation) using a predetermined ramped time step size because extracting the source term value from the output of RepoTREND was too difficult at the time. A further study is required where the RepoTREND source term is calculated during the simulation and the results are extracted from the simulation output, with the time step size reported.

## References

- Lichtner, P. C., G. E. Hammond, C. Lu, S. Karra, G. Bisht, B. Andre, R. T. Mills, J. Kumar, and J. M. Frederick, PFLOTRAN User Manual, <http://www.documentation.pflotran.org>, 2018. [Lichtner et al. 2018]
- Reiche, T. (2017), "RepoTREND – A Program Package for Safety Analysis," Proceedings of the 2017 International High Level Radioactive Waste Management (IHLRWM) Conference, Charlotte, NC, USA, 9-12 Apr. [Reiche 2017]
- Sevougian, S. D., G. E. Hammond, P. E. Mariner, E. R. Stein, J. M. Frederick, and R. J. MacKinnon (2018), "GDSA Framework: High-Performance Safety Assessment Software to Support the Safety Case," Proceedings of the 2018 Integration Group for the Safety Case (IGSC) Symposium, Rotterdam, The Netherlands, 10-11 Oct. [Sevougian et al. 2018]