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George E. Orient and Lisa A. Deibler

Problem Schematic

$$m = 306 \text{ lb}$$

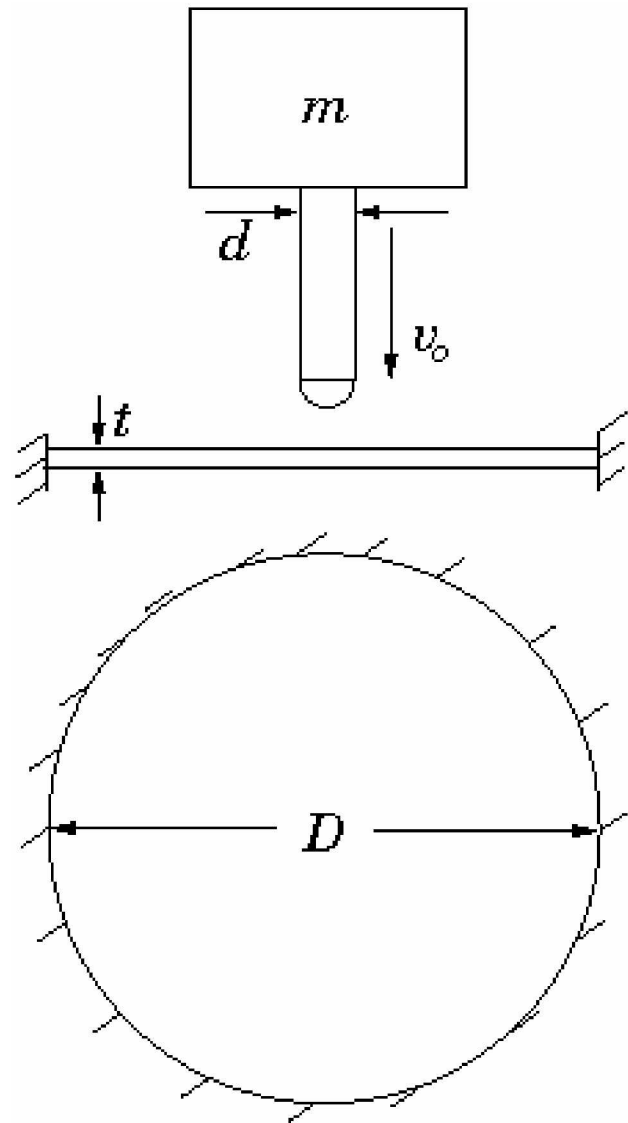
$$d = 0.5 \text{ in}$$

$$t = 0.5 \text{ in}$$

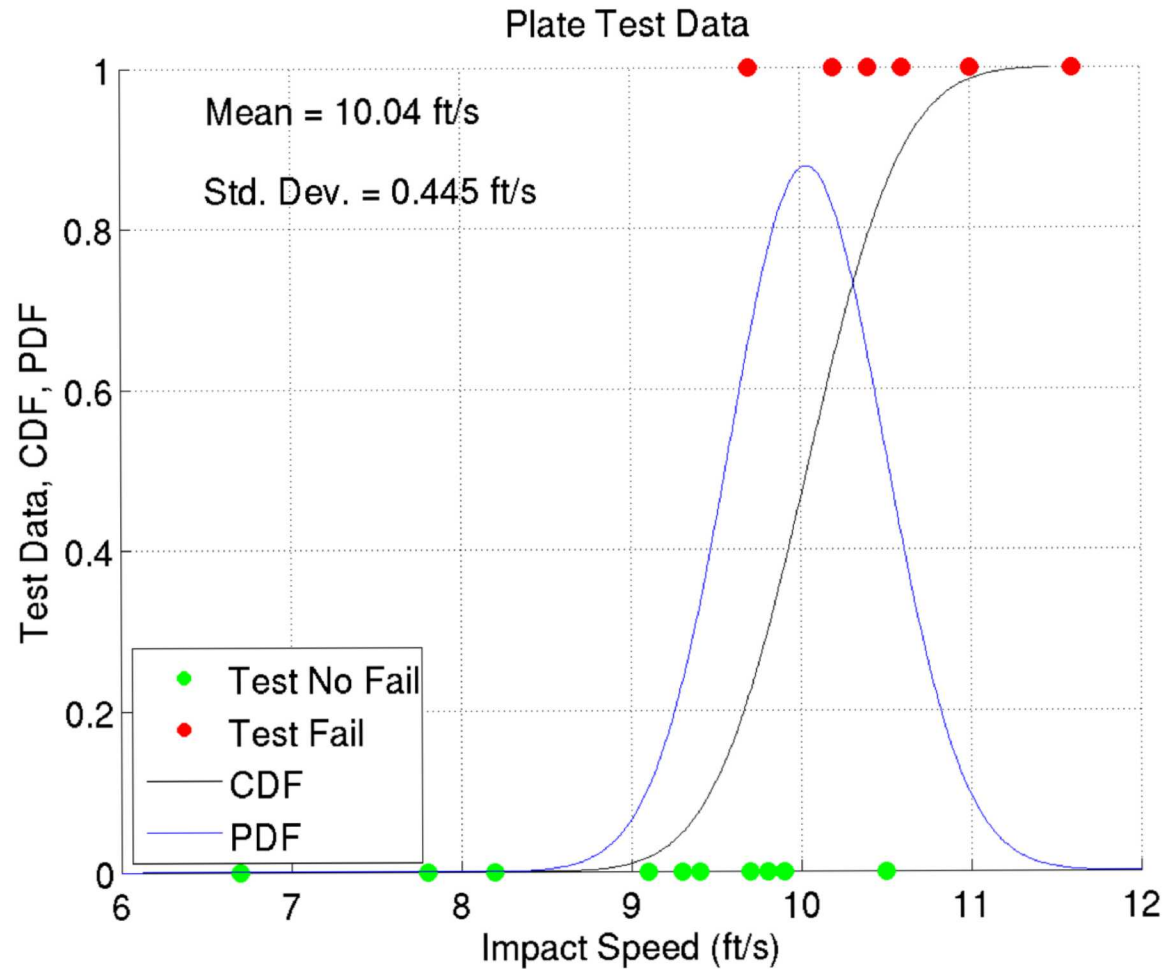
$$D = 6.75 \text{ in}$$

Al 7075-T651

- Determine threshold velocity
- Observe failure mode



Experimental Results



Threshold velocity: [9.7, 10.5] ft/s

Puncture Video Record



Johnson-Cook Material Choice

- Initial results overestimated threshold puncture velocity by 60%
- Searched for a model that:
 - Accounts for temperature and strain rate effects on material response/failure
 - Triaxiality dependence of failure strain can be adjusted
 - Has been implemented in a finite element code
- Johnson-Cook model met all the criteria.
- It has also been used by others in puncture applications (Borvik, Weirzbicki) and reported good results.

Johnson-Cook Material Characterization

J_2 Isotropic hardening, “Strength” Model:

$$\sigma_e = \left[A + B \left(\varepsilon_e^p \right)^n \right] \left[1 + C \ln \left(\frac{\dot{\varepsilon}_e^p}{\dot{\varepsilon}_o} \right) \right] \left[1 - \hat{T}^m \right]$$

$$\hat{T} = \frac{T - T_r}{T_m - T_r}$$

Five parameters to calibrate:

$$A, B, n, C, m$$

Auxiliary parameters that need values:

$$\dot{\varepsilon}_o, T_r, T_m$$

Johnson-Cook Material Characterization

Failure Model:

$$\varepsilon_{ef}^p = \left[d_1 + d_2 e^{d_3 \eta} \right] \left[1 + d_4 \ln \left(\frac{\varepsilon_e^p}{\varepsilon_o} \right) \right] \left[1 + d_5 \hat{T} \right]$$

$$\eta = \frac{\sigma_m}{\sigma_e}$$

Five parameters to calibrate:

$$d_1, d_2, d_3, d_4, d_5$$

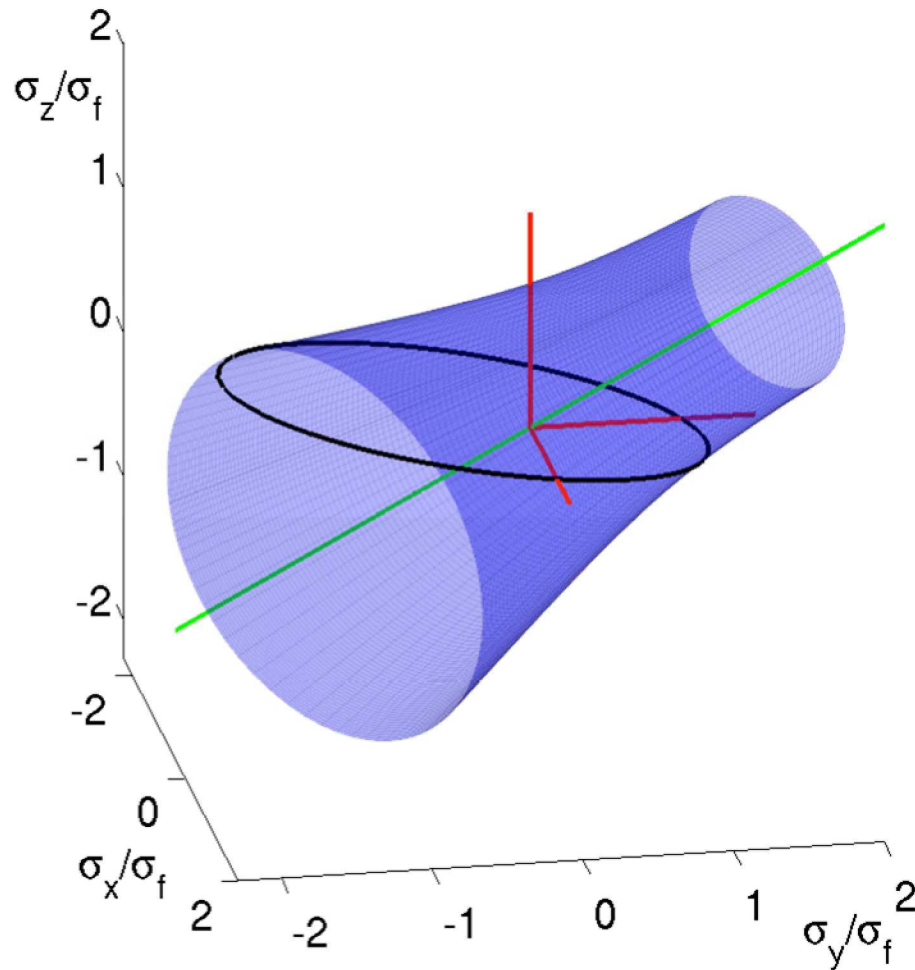
Damage accumulation:

$$\bar{D} = \int \frac{d\hat{\varepsilon}_e^p}{\varepsilon_{ef}^p(\eta, \dot{\varepsilon}/\dot{\varepsilon}_o, \hat{T})}$$

Failure when $\bar{D} = 1$

Johnson-Cook Failure in Principal Stress

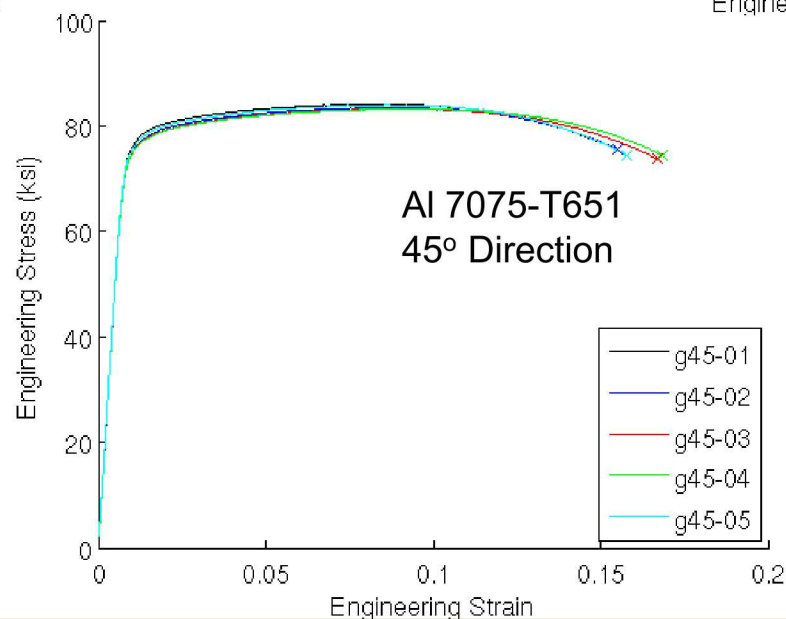
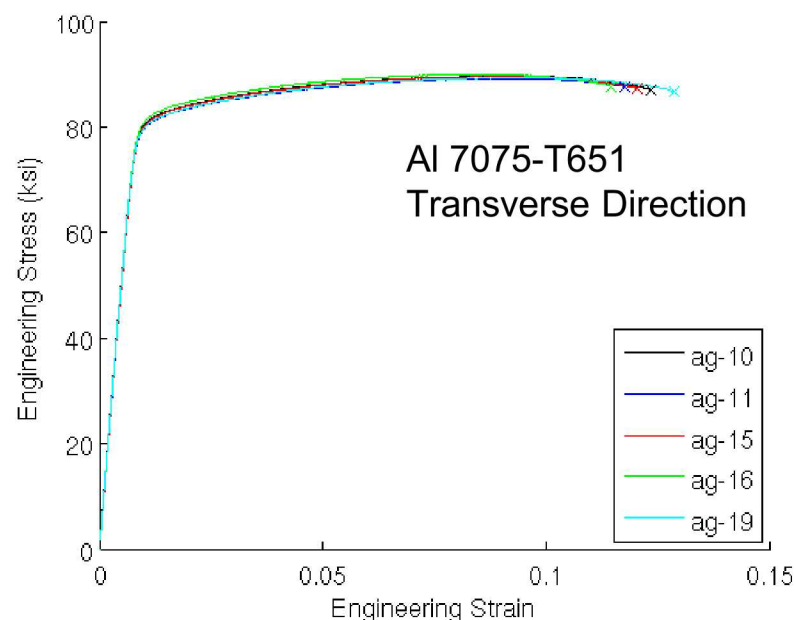
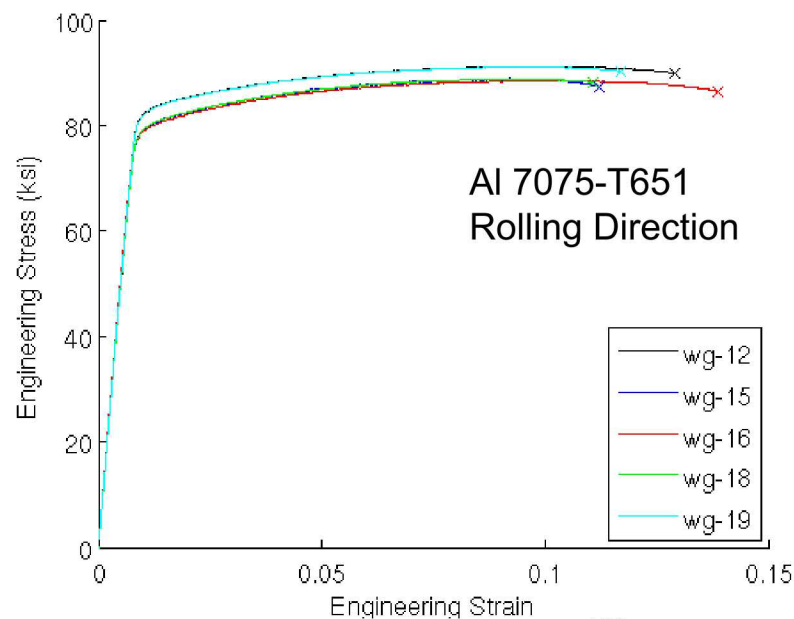
$$\begin{aligned}d_1 &= 0.005 \\d_2 &= 0.34 \\d_3 &= -1.5\end{aligned}$$



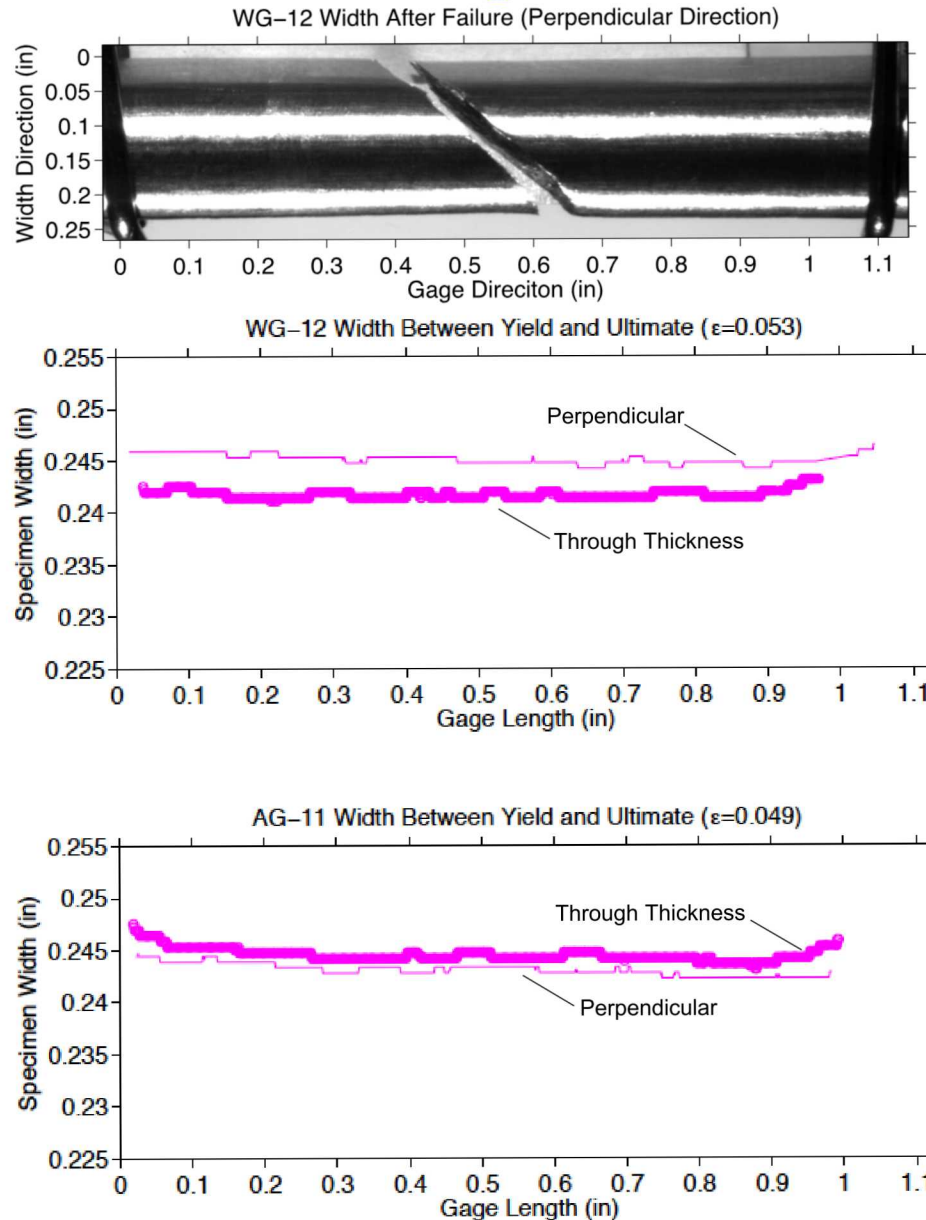
Special case:

$$\begin{aligned}T &= T_r \\ \dot{\epsilon}_e^p &= \dot{\epsilon}_o \\ \dot{\eta} &= 0\end{aligned}$$

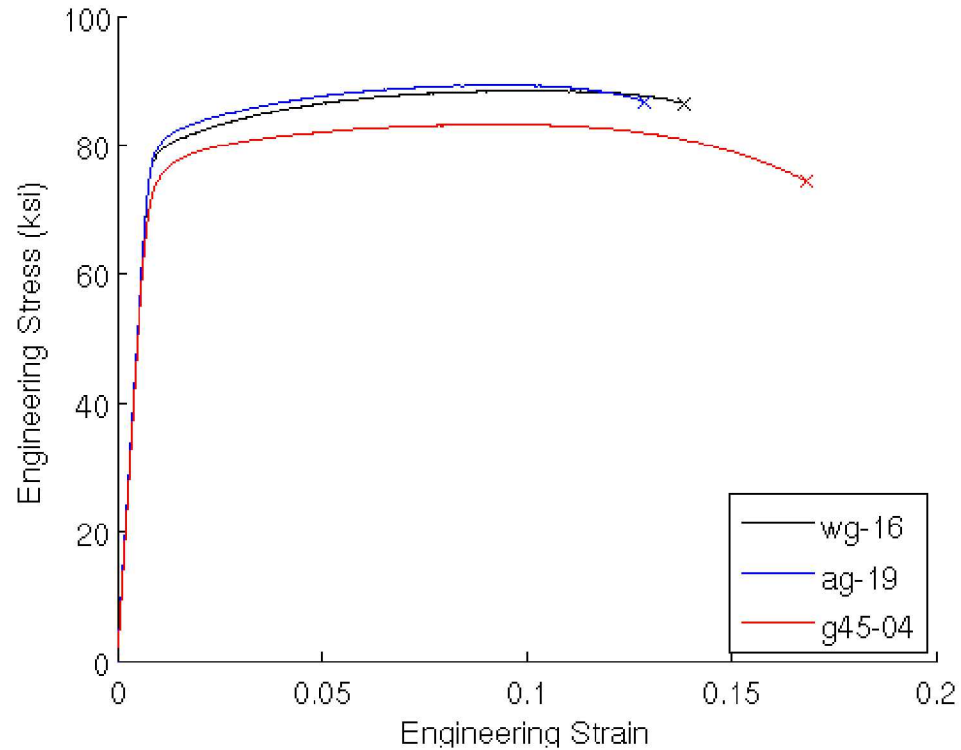
Uniaxial Tension Test Data



Uniaxial Tension Edge Detection Data



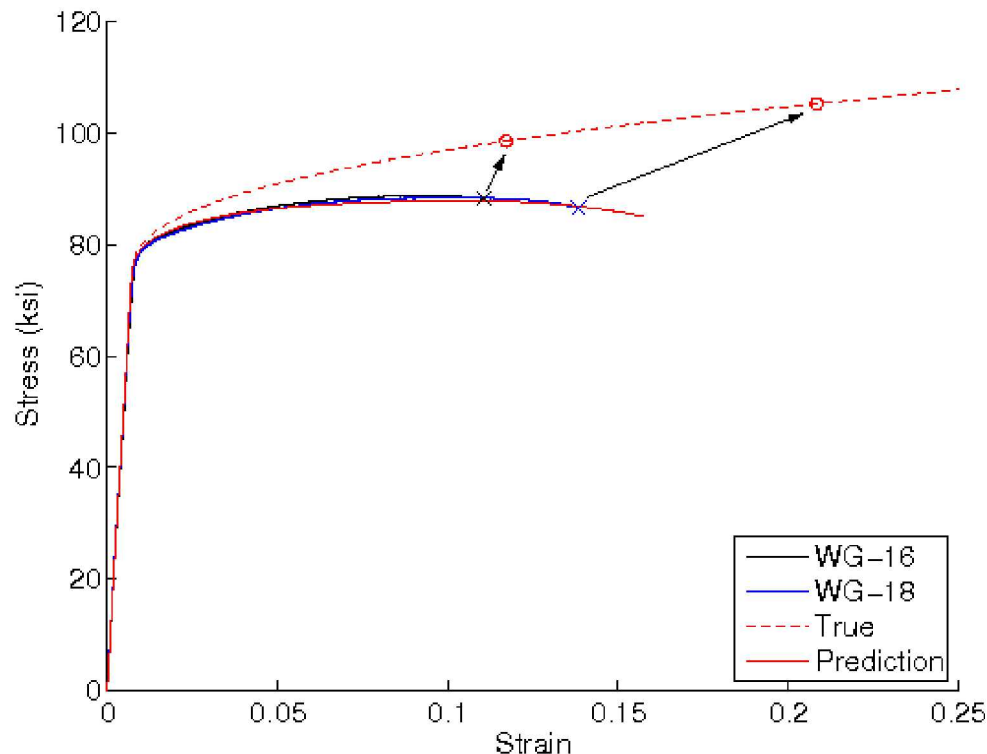
Uniaxial Tension Test Data Summary



Choice of stress-strain curve to fit: Highest strain to failure

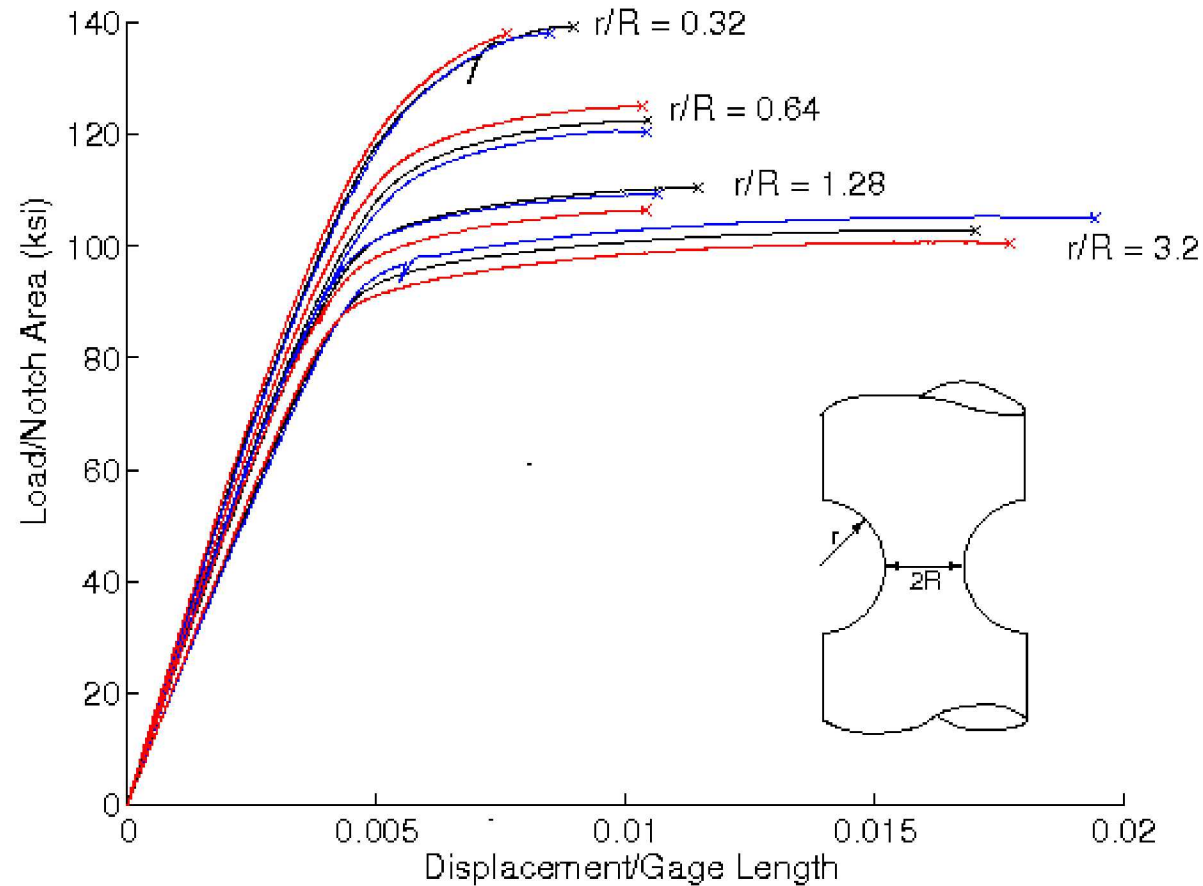
Fitting Procedure

- Make finite element model of tension test specimen
- Guess values for A , B , n
- Simulate the tension test
- Compare the predicted engineering stress-strain curve to measured one
- Iterate as necessary
- Note the true plastic strain at failure



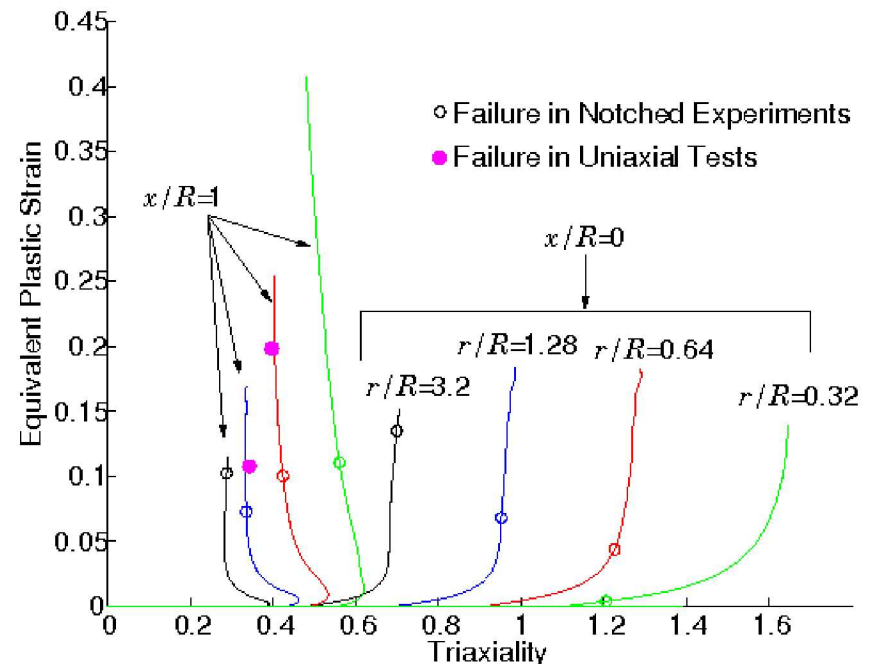
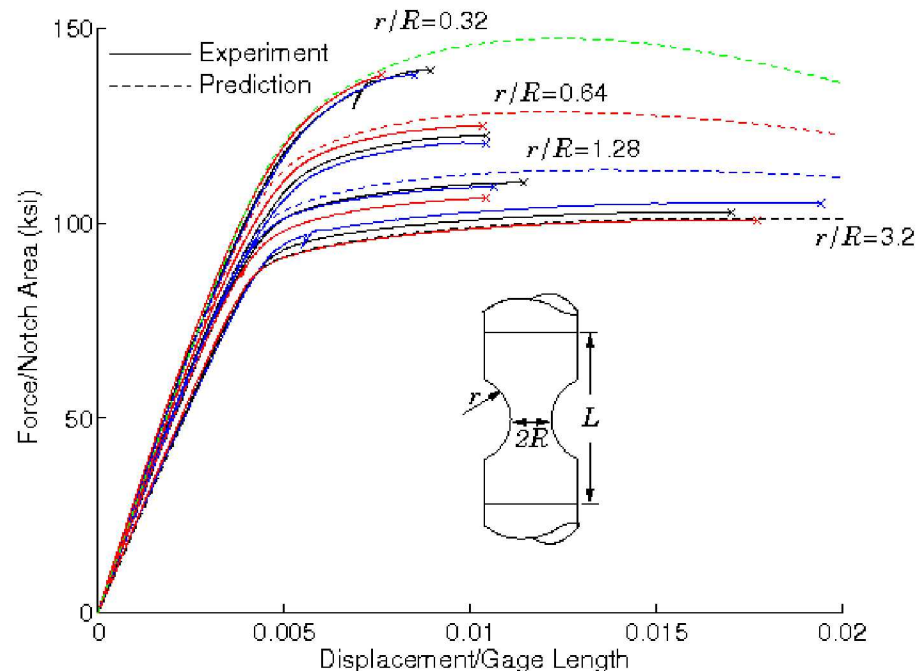
A, B, n, C, m
 d_1, d_2, d_3, d_4, d_5

Notched Specimen Tension Test Data



Notched Specimen Tension Test Simulation

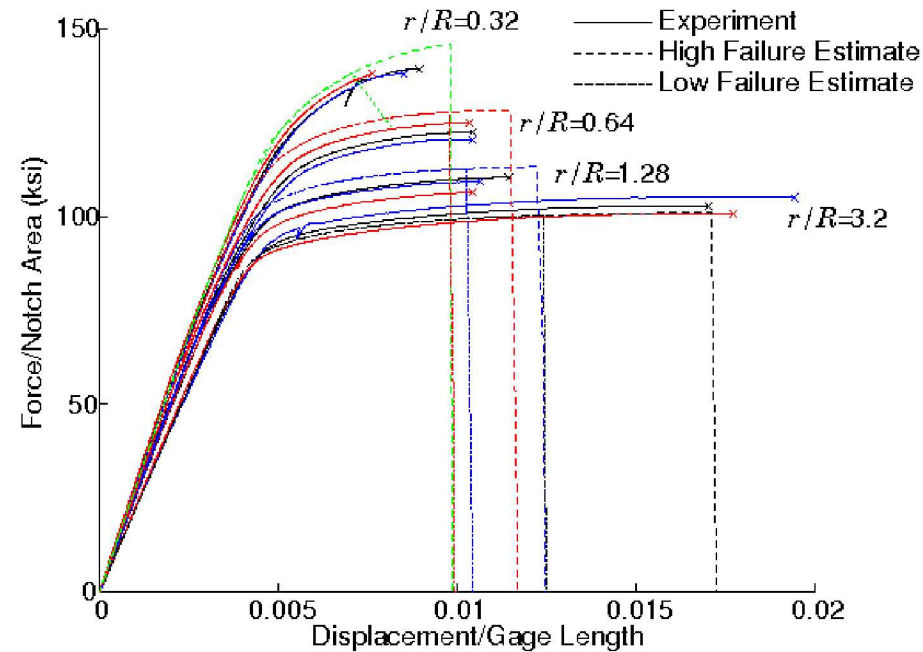
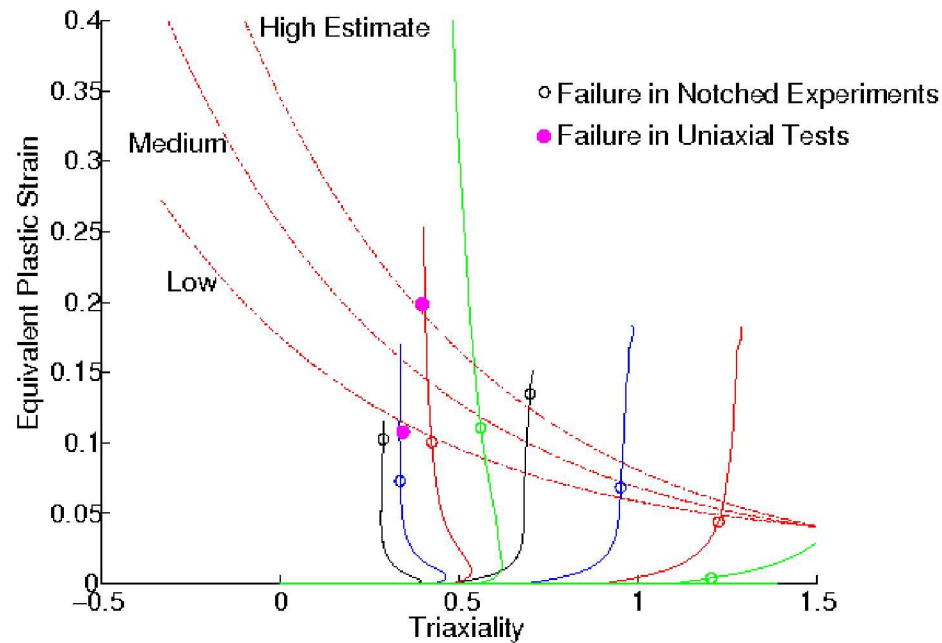
- Test performance of plasticity model under non-uniaxial conditions
- Obtain data to assess triaxiality dependence of the plastic strain to failure



Notched Specimen Tension Test Calibration

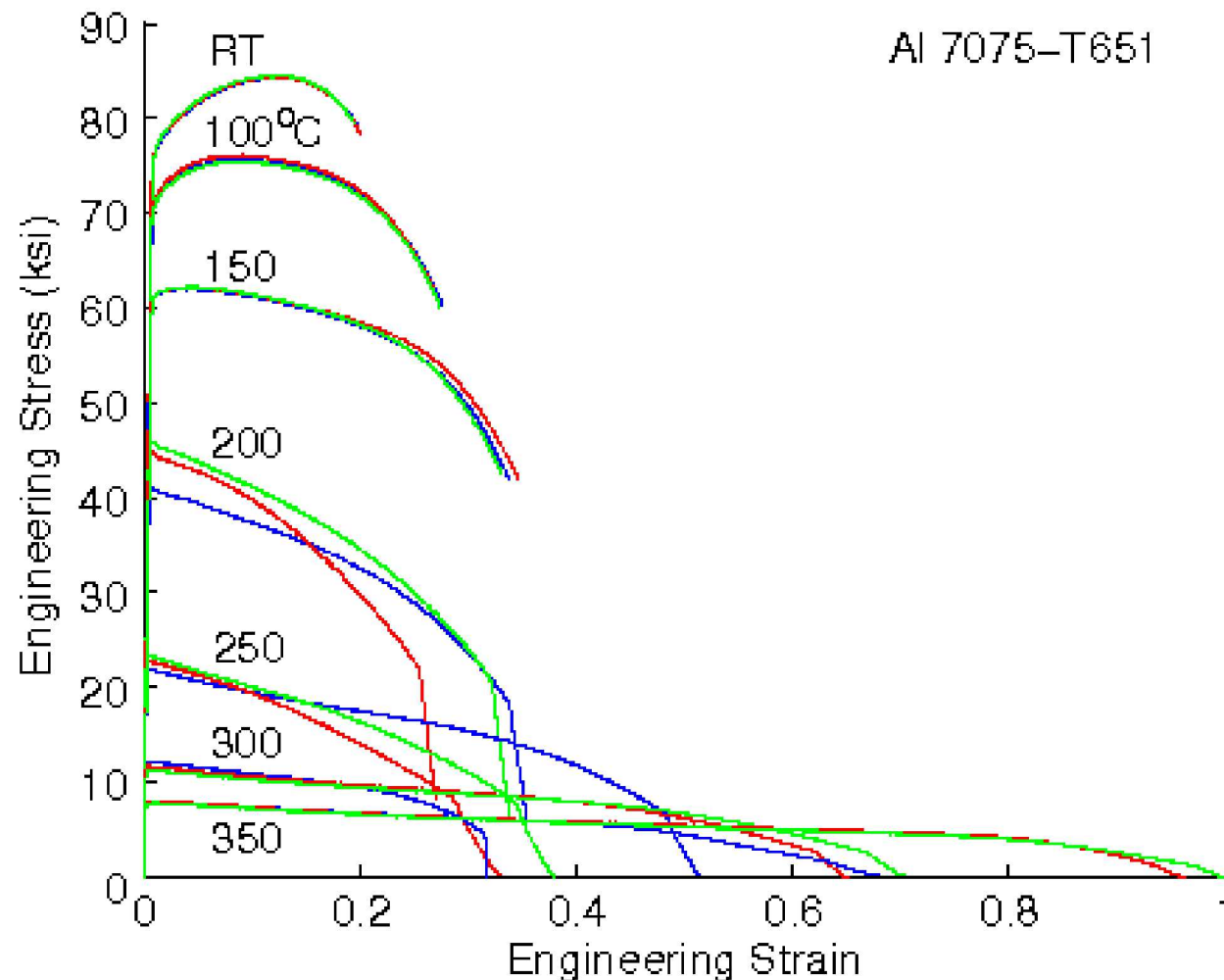
$$A, B, n, C, m$$

$$d_1, d_2, d_3, d_4, d_5$$



High Temperature Tension Test Data

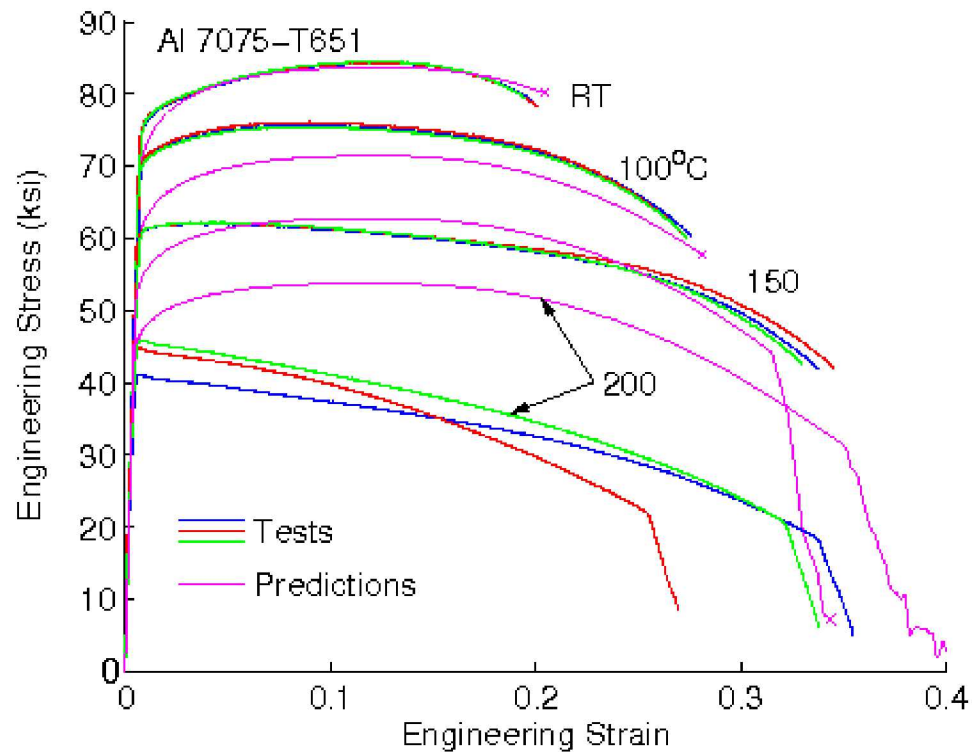
Determine values of temperature dependence parameters



High Temperature Tension Test Calibration

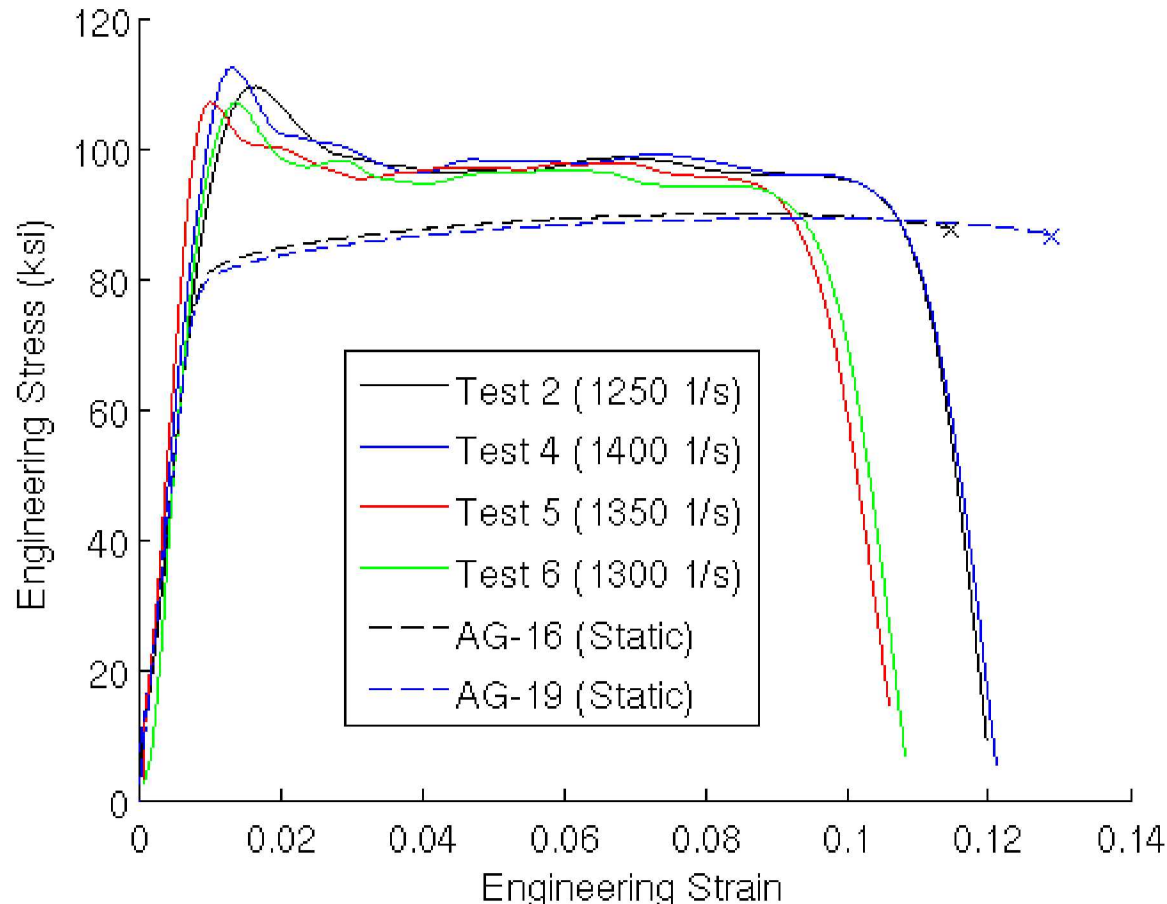
$$A, B, n, C, m$$

$$d_1, d_2, d_3, d_4, d_5$$



High Strain Rate Tension Test Data

Determine values of strain rate dependence parameters



Tensile Kolsky Bar Tests



High Strain Rate Tension Test Data

$$A, B, n, C, m$$

$$d_1, d_2, d_3, d_4, d_5$$

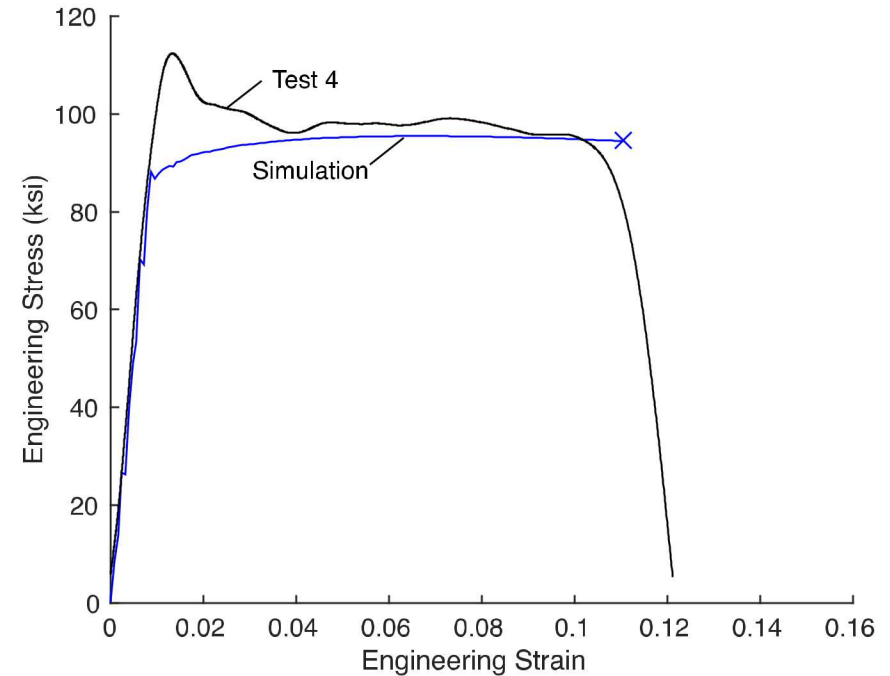
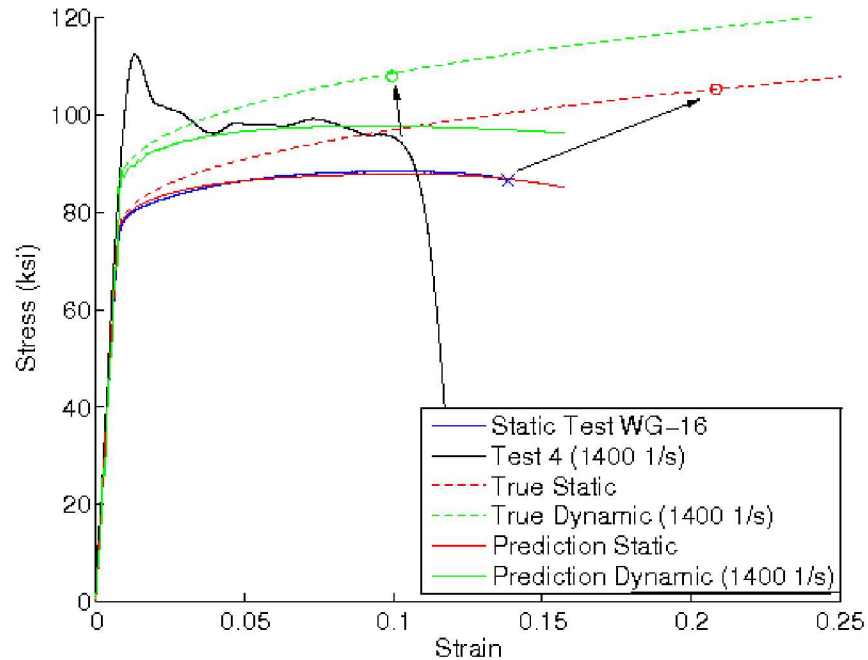


Plate Puncture Finite Element Model

- Explicit Dynamics
- Adiabatic

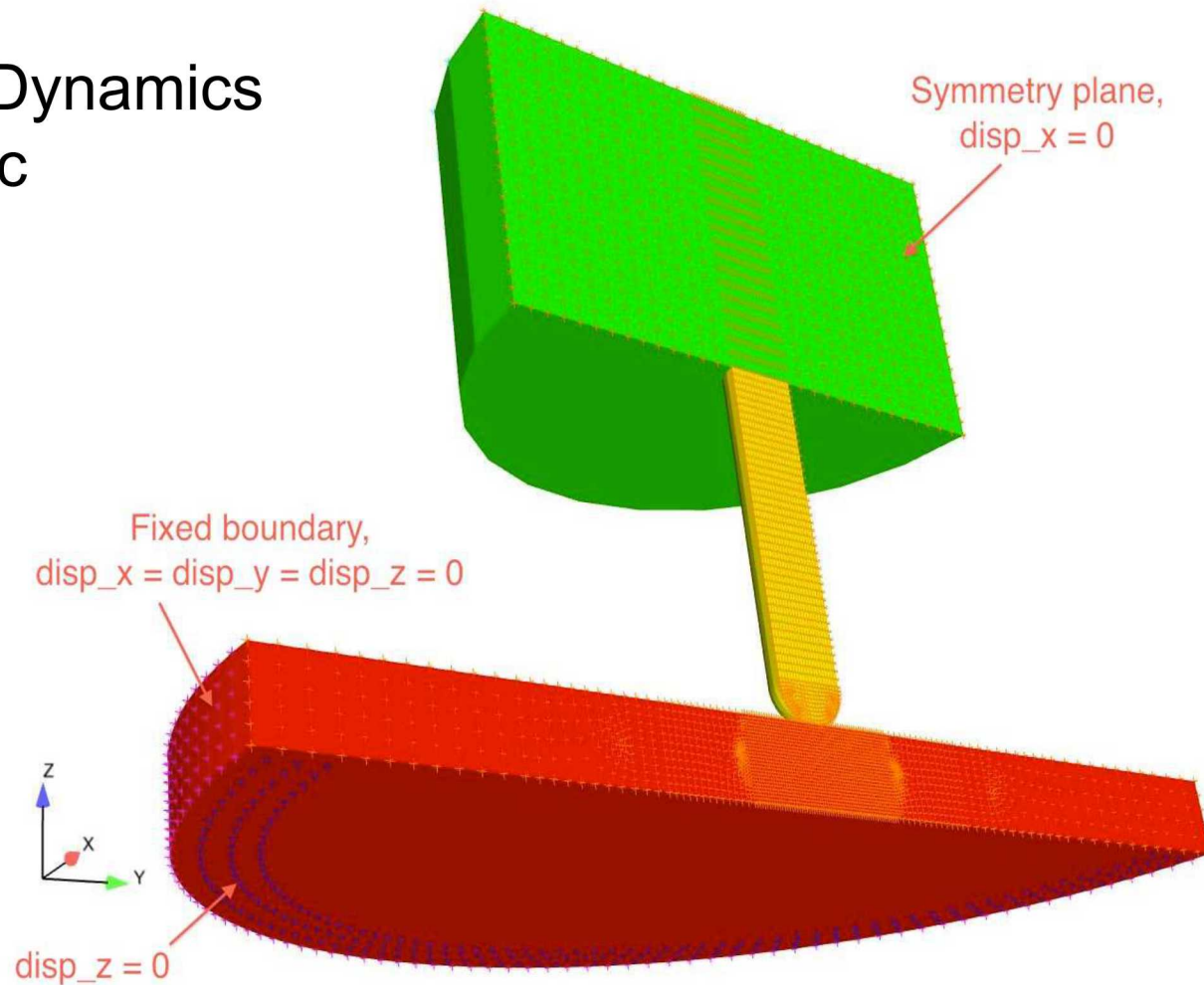
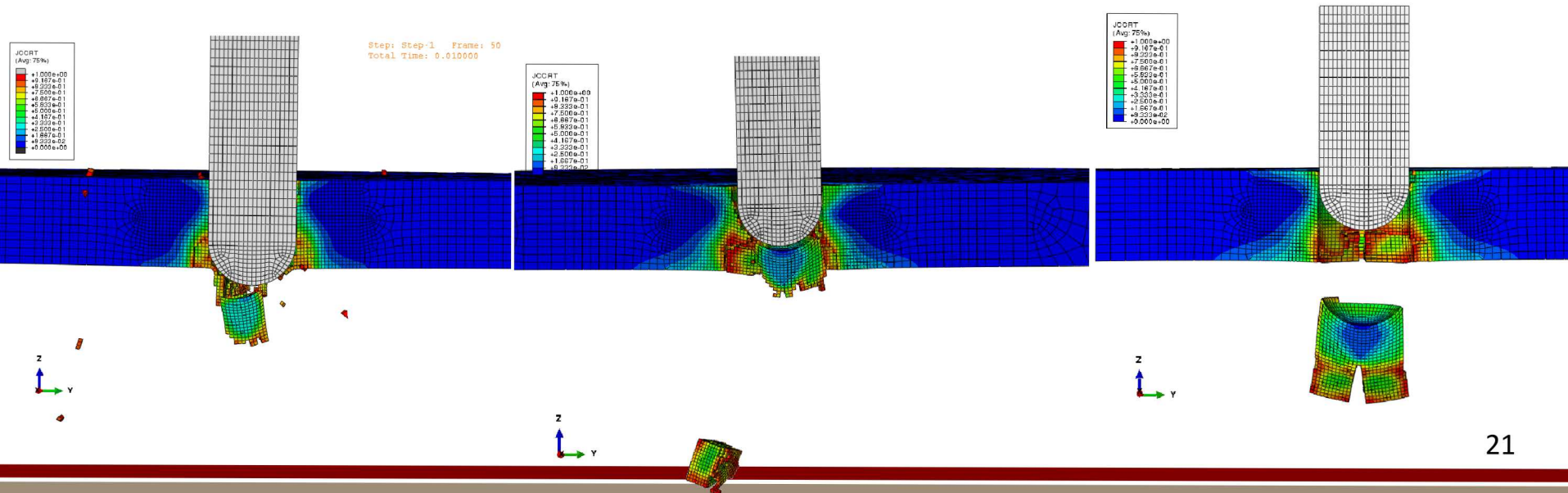


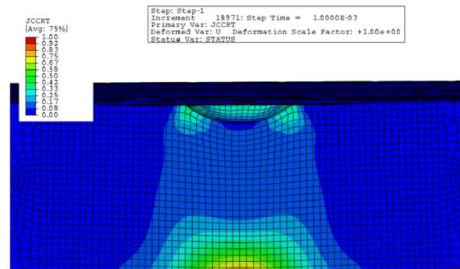
Plate Puncture Results

v_o , ft/s	Low	Medium	High
6	N		
6.5	N		
7	Y	N	
7.5	Y		
8	Y	N	
8.5	Y		N
9	Y	N	N
9.5	Y	N	N
10	Y	Y	N
10.5		Y	N
11		Y	Y
11.5		Y	Y
12			Y

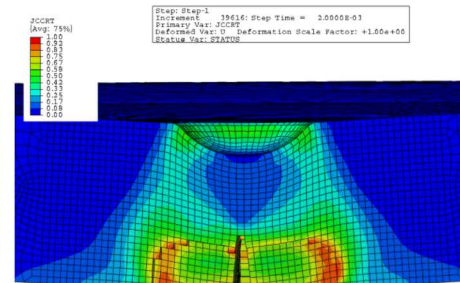


Evolution of Johnson-Cook Damage

1 ms



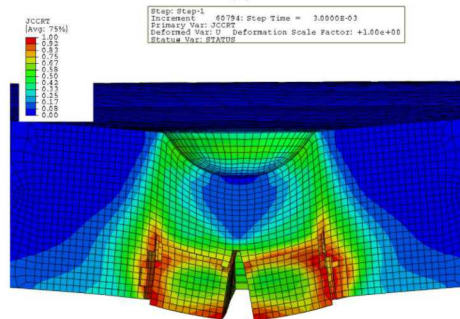
2 ms



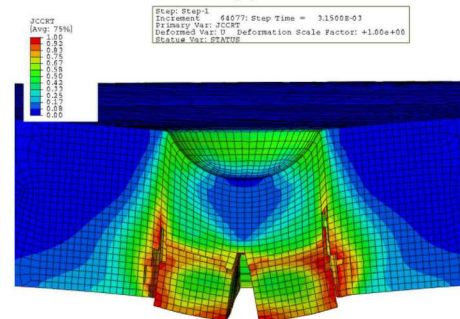
(a)

(b)

3 ms



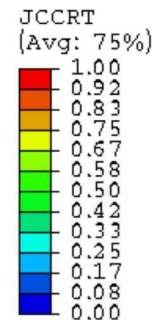
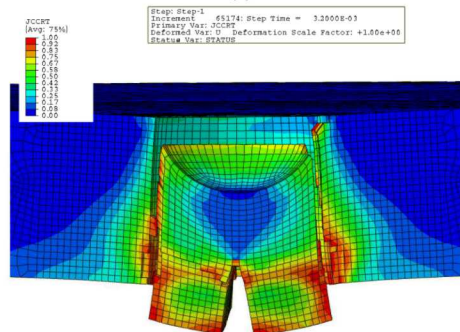
3.15 ms



(c)

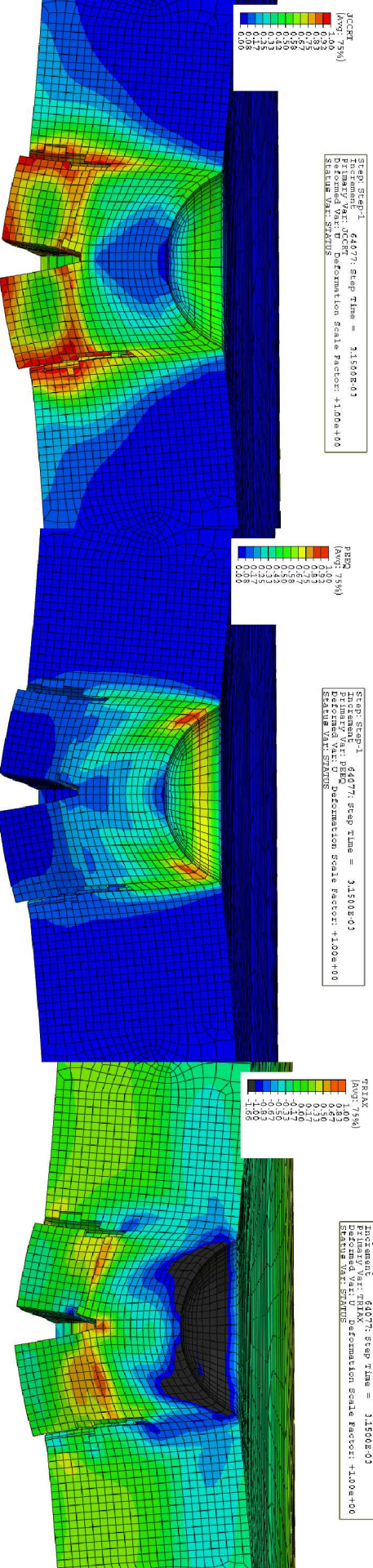
(d)

3.2 ms

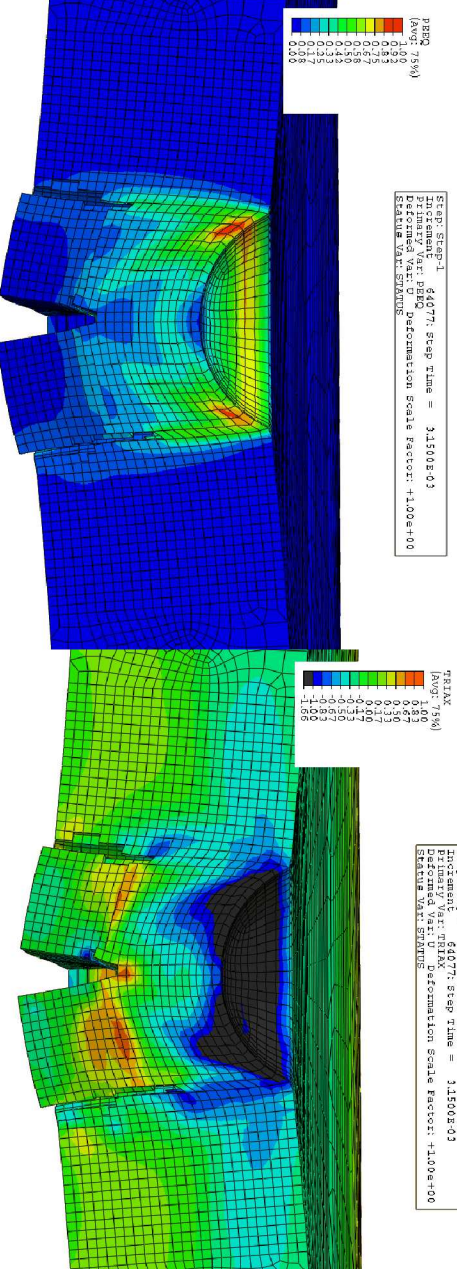


Just Prior to Plug Ejection (3.15 ms)

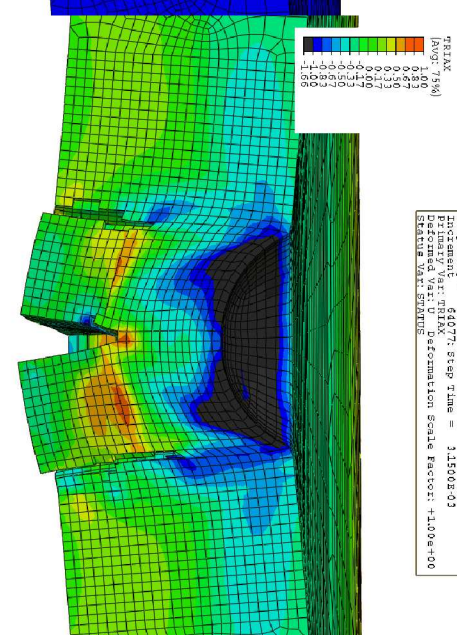
Damage



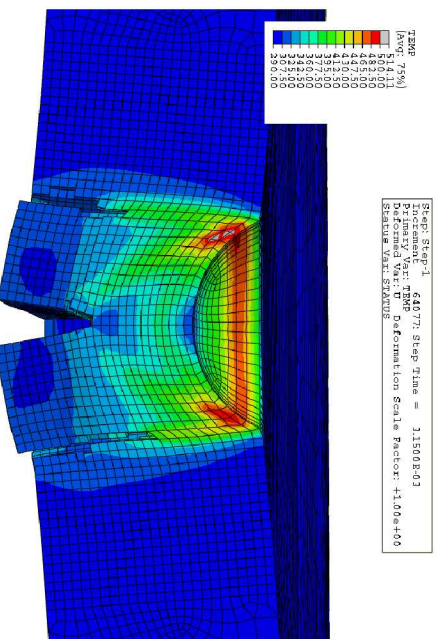
Equivalent Plastic Strain



Triaxiality

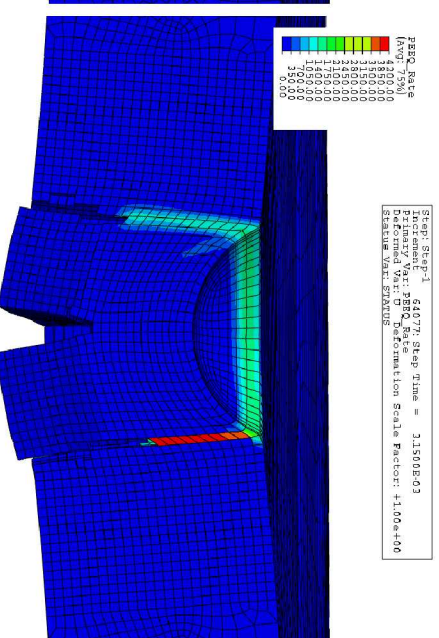


Temperature



Temperature

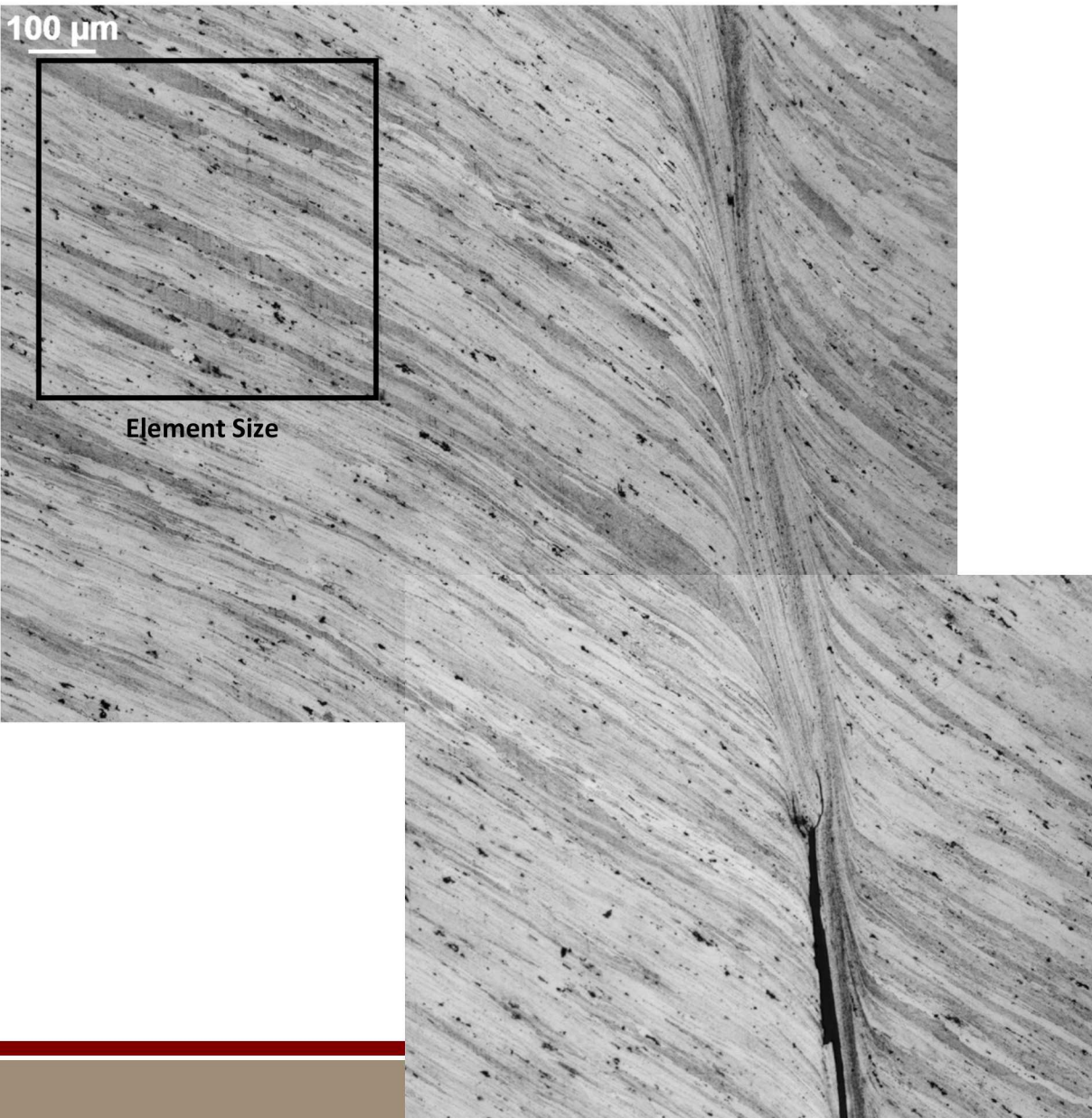
Equivalent Plastic Strain Rate



10.5 ft/s, No Failure

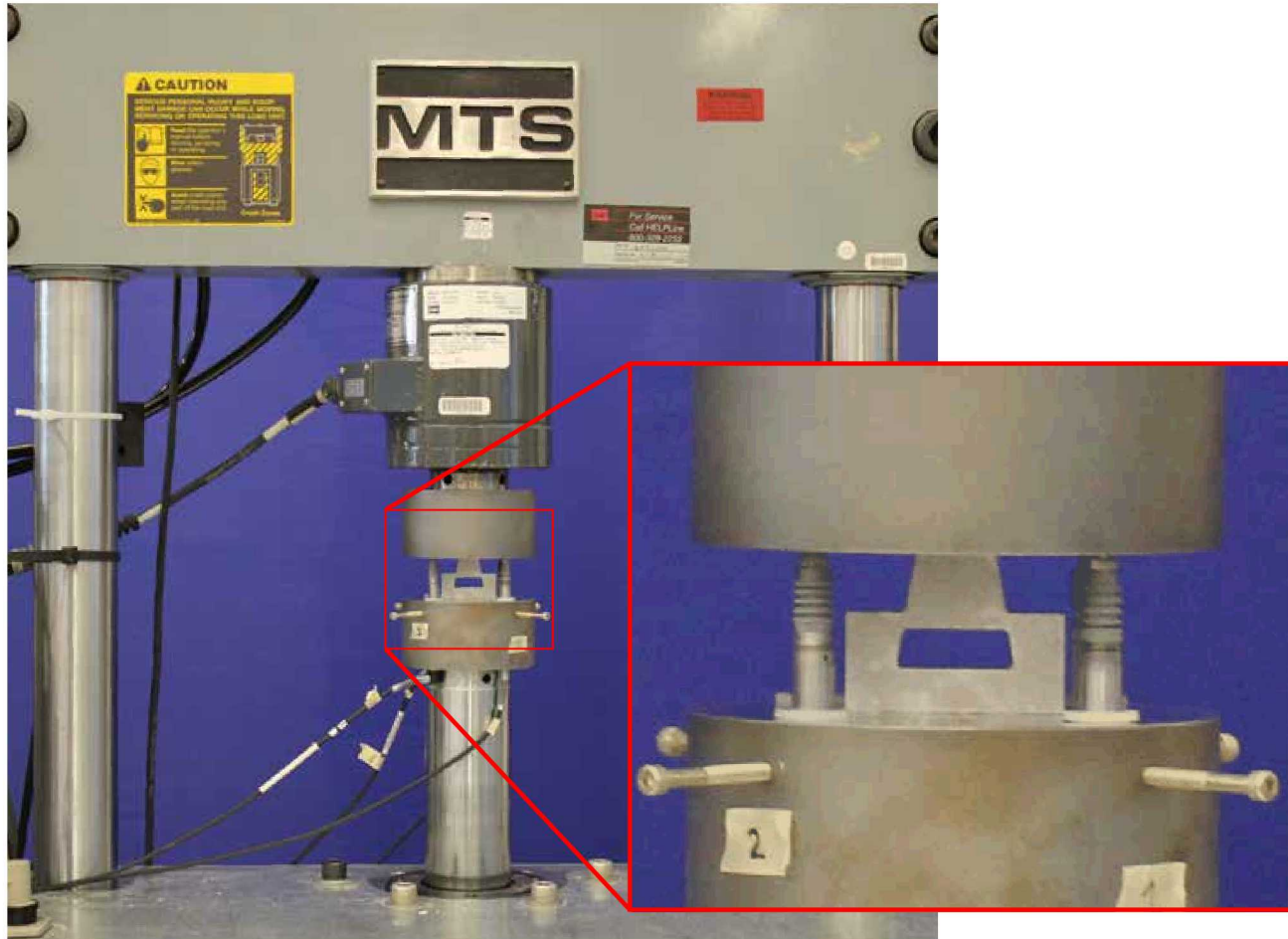


Microstructure of Plug Formation

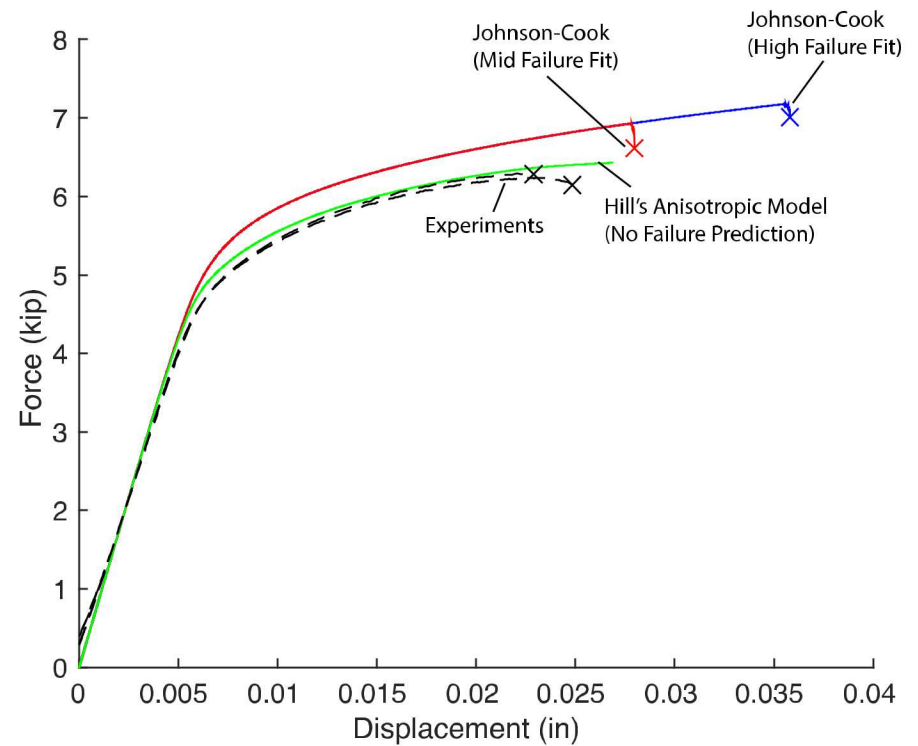
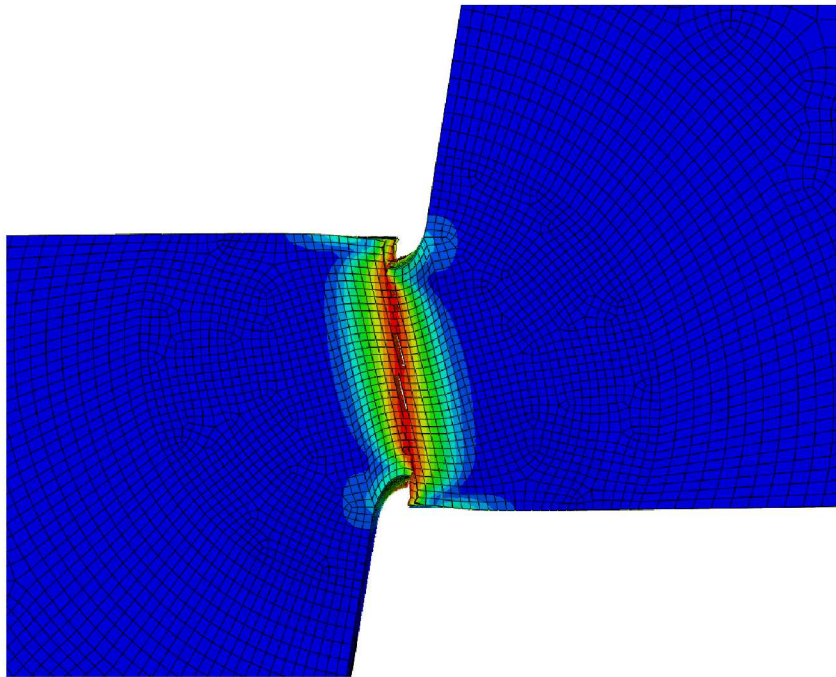


High Shear Test

Test predictions against test in high shear regime



High Shear Test Results and Predictions



Conclusions

Positive Outcomes:

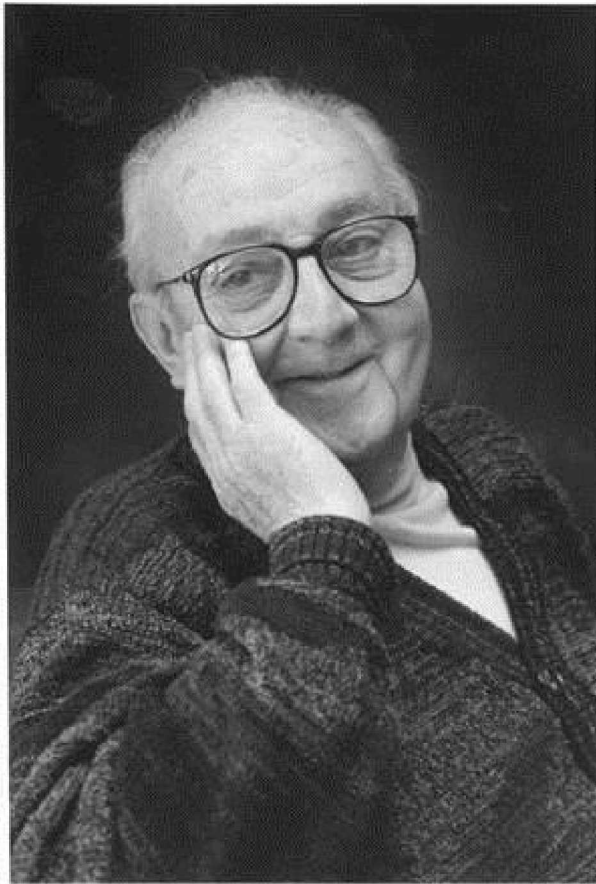
- Accomplished full calibration of Johnson-Cook strength and failure model
- Puncture predictions have high resemblance to experimental observations
 - Accurate prediction of threshold puncture velocity
 - Failure sequence leading to plugging reasonably reproduced

Deficiencies:

- Model neglects observed material anisotropy
- Model captures response at high temperature to a first order only
- High shear failure information is scarce
- Material properties in the thickness direction have not been measured
- The element size used in the puncture calculations is way too big compared to the observed shear bands. (Clearly, however, the model predicts the onset of a shear instability)
- We are still uncertain whether the very reasonable predictions by the model are due to good modeling or good luck.

Observations and Recommendations:

- The Johnson-Cook model provided a reasonable first-order representation of the observed material behavior, both for response and failure
- The puncture predictions were reasonable
- It is reasonable to use a properly calibrated Johnson-Cook model as an initial step in the simulation of similar problems.
- Use of the methods considered here in other problems will provide further experience and evidence of the soundness of the approach.



George E. P. Box (1919-2013)

British mathematician

Statistics professor at Univ. of WI

“Essentially, all models are wrong, but some are useful.”

“Remember that all models are wrong; the practical question is how wrong do they have to be to not be useful.”