

# WEC Design Practices and Tools



*37th International Conference  
on Ocean, Offshore and  
Arctic Engineering  
Madrid, Spain, June 17-22, 2018*



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**June 16, 2018**

Yi-Hsiang Yu (NREL)

# Agenda

1. Introduction
2. WEC fundamentals
3. Ocean waves
4. Numerical methods
5. Experimental methods
6. WEC control
7. Extreme response and fatigue

# Introduction

Presented by Ryan Coe

# Introductions

- Who are we?
  - Ryan Coe
  - Yi-Hsiang Yu
  - Kelley Ruehl
- Who are you?
- What are our goals for today?



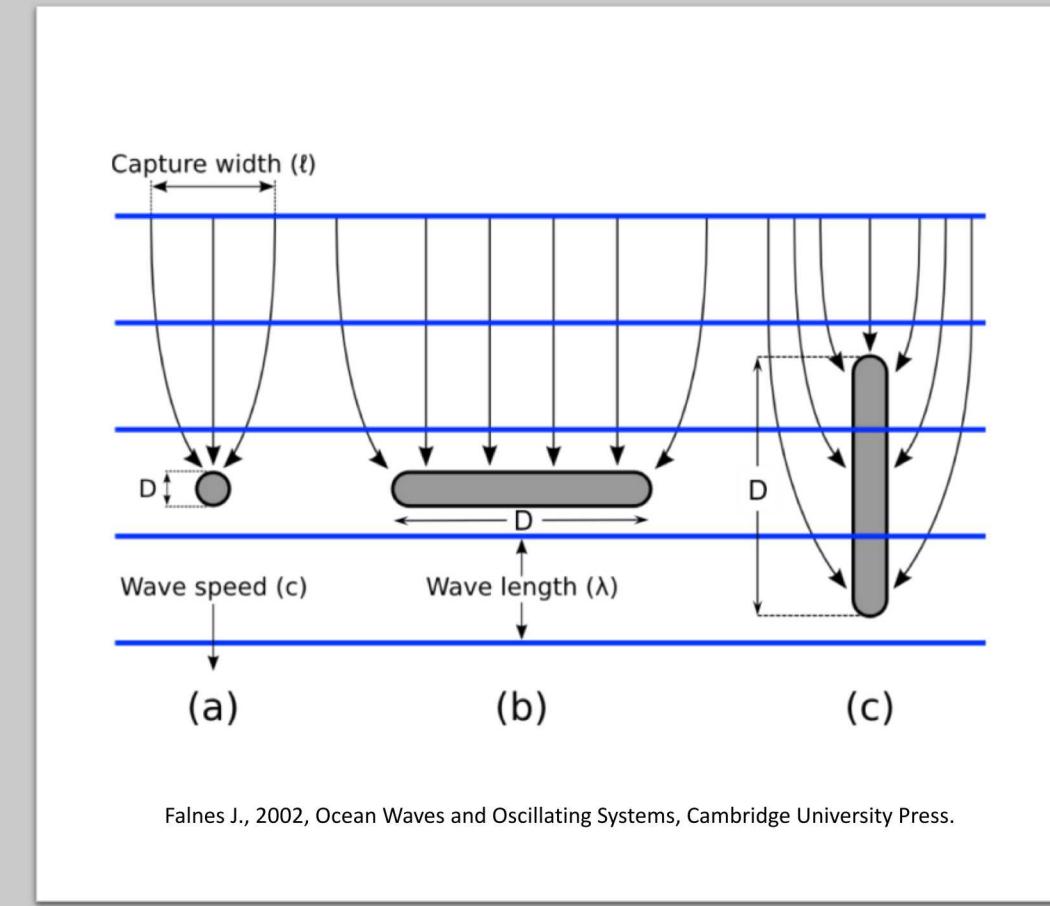
# WEC fundamentals

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Presented by Yi-Hsiang Yu

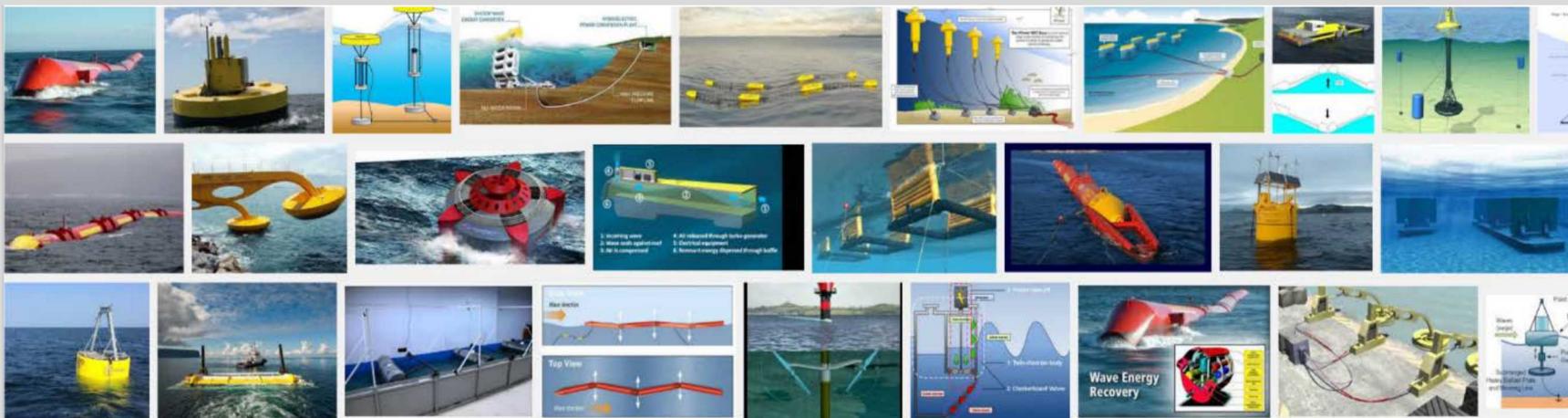
# Typical WEC Descriptions

- WEC devices extract energy contained within ocean surface waves and convert it to useful electric power.
- Traditionally, these devices are typically divided into three categories

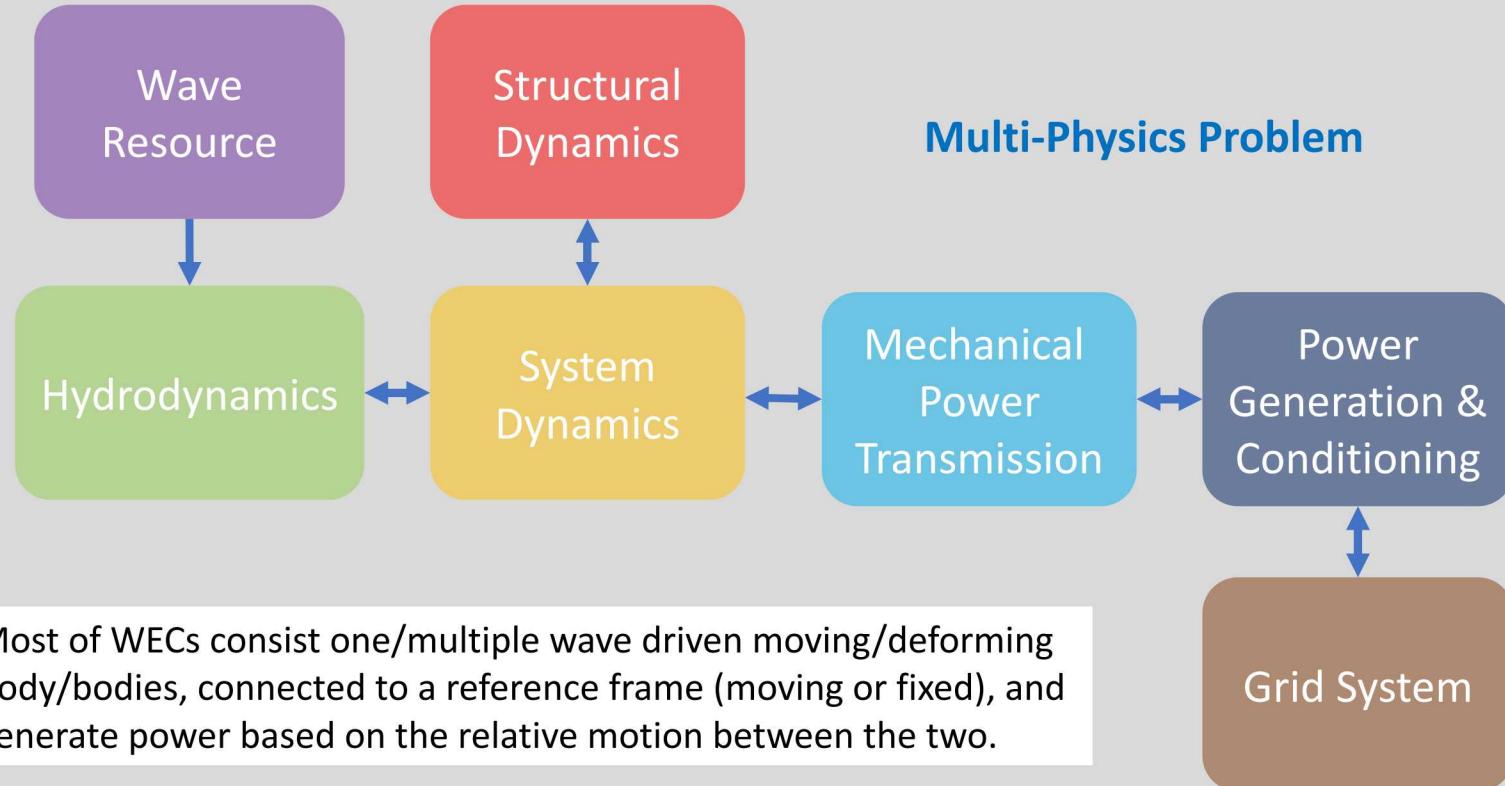


# What is a WEC?

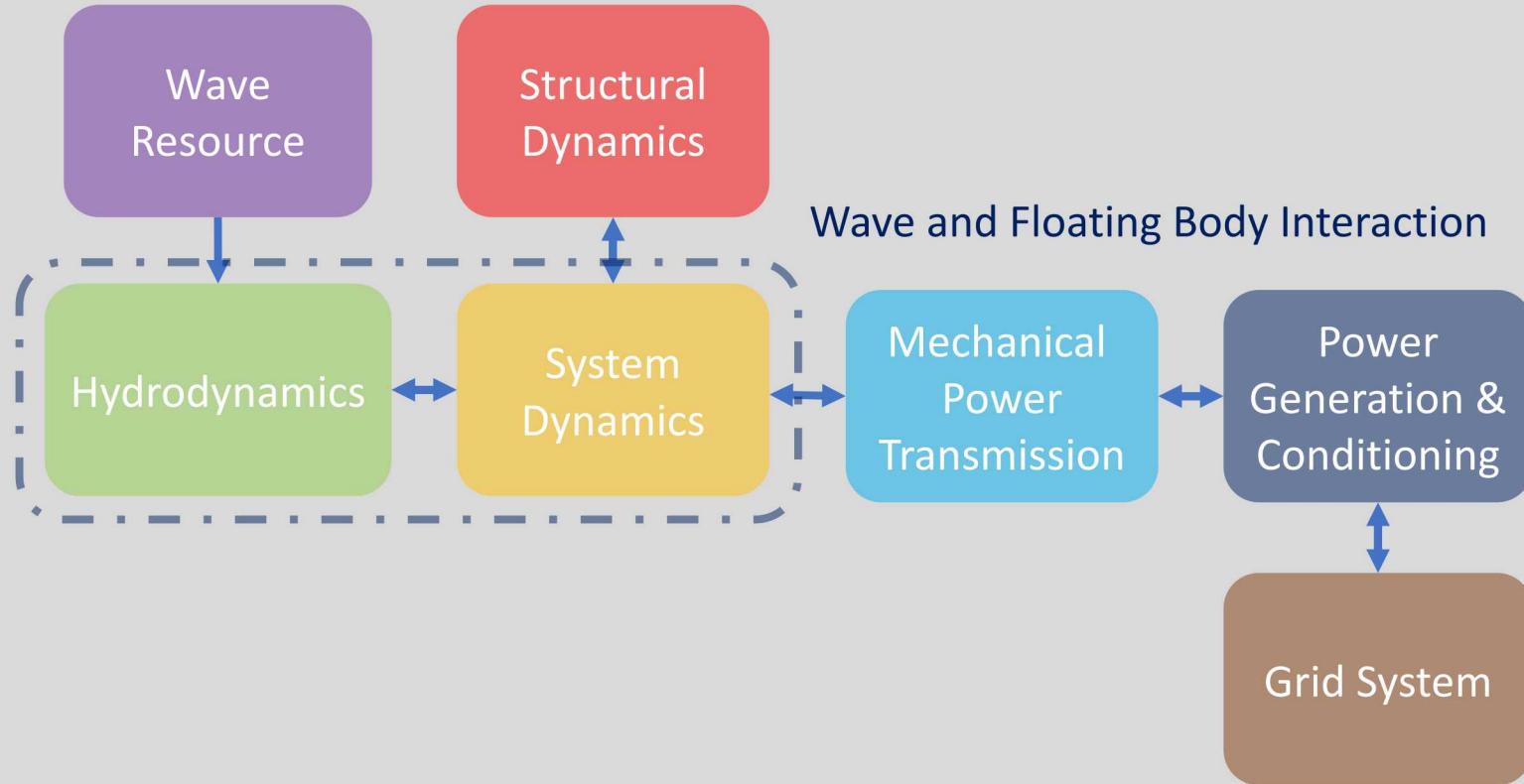
- A wide variety of WEC design concepts



# WEC Analysis

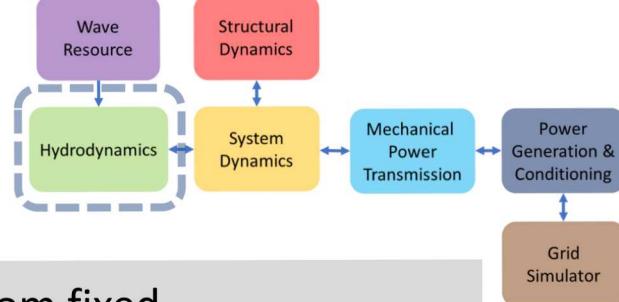
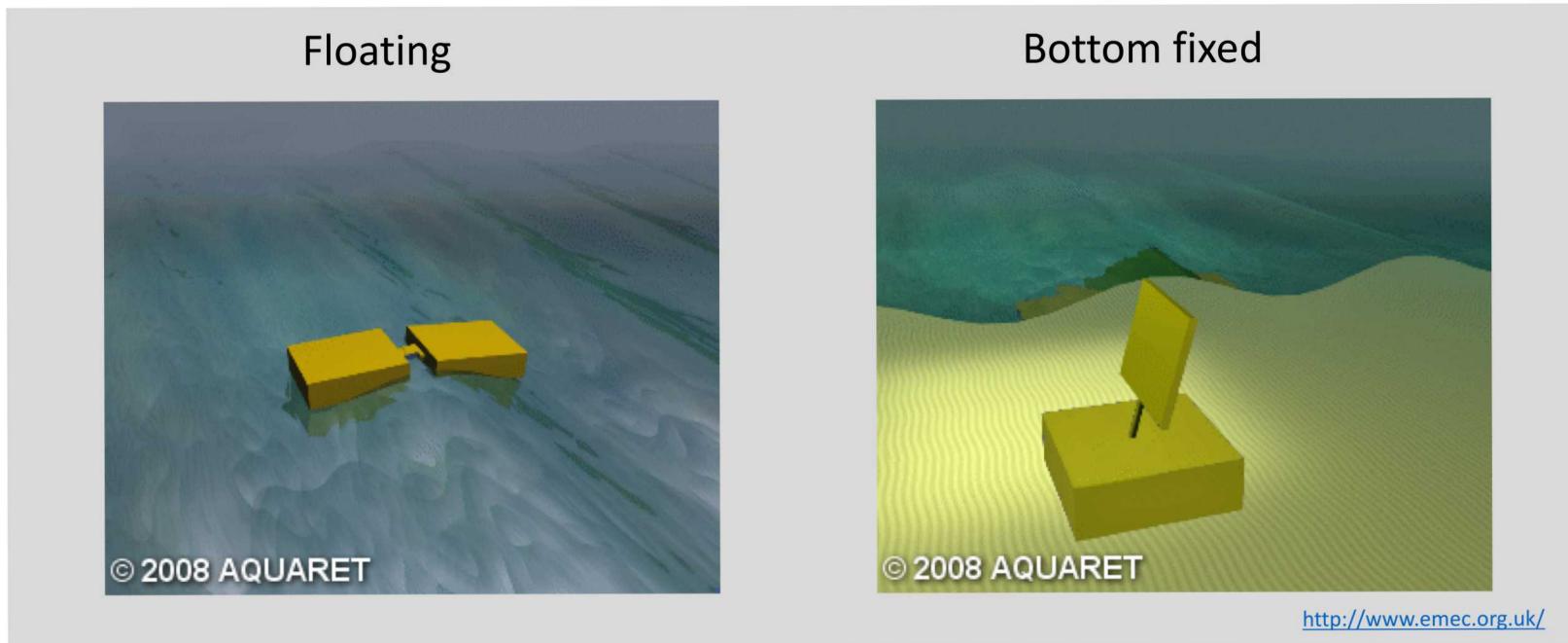


# WEC Analysis



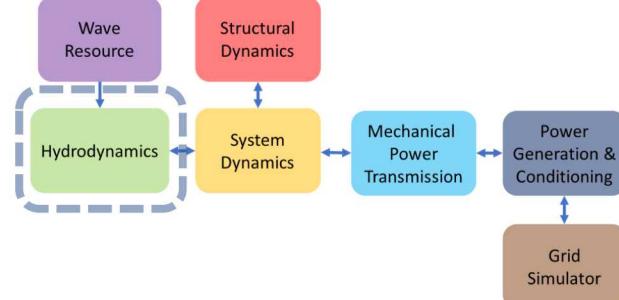
# WEC Classification

- From hydrodynamics prospective:

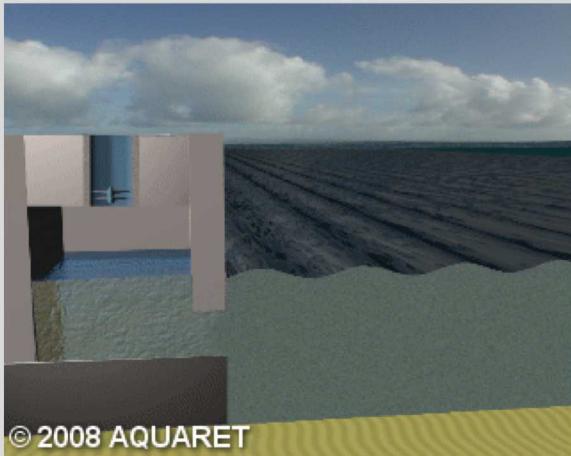


# WEC Classification

- From hydrodynamics prospective:



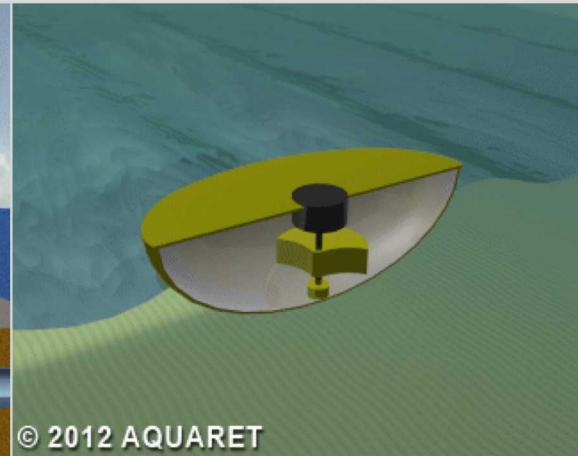
Oscillating water Column



Overtopping device



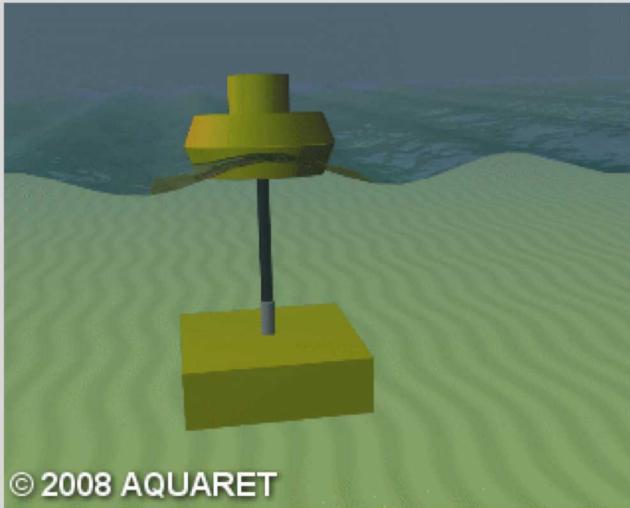
Gyroscopic device



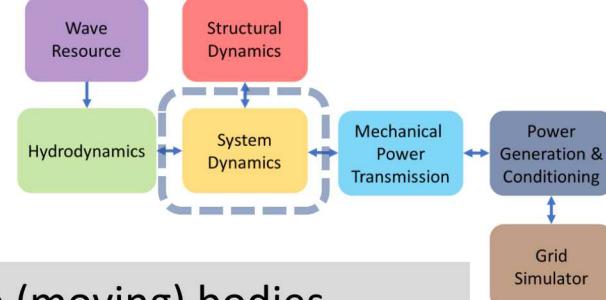
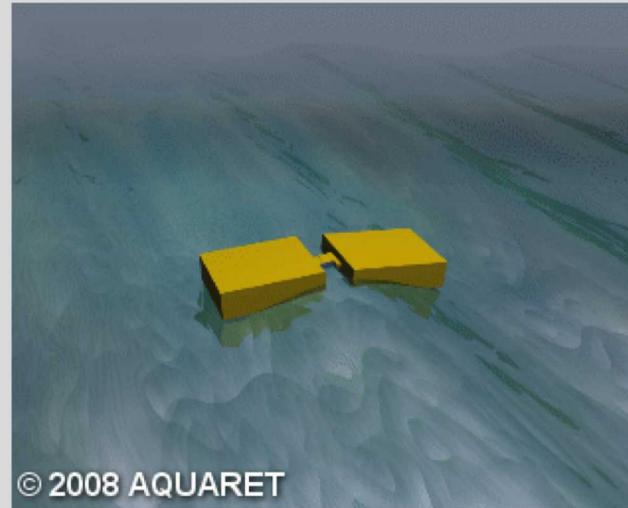
# WEC Classification

- From system dynamics:

Single (moving) body

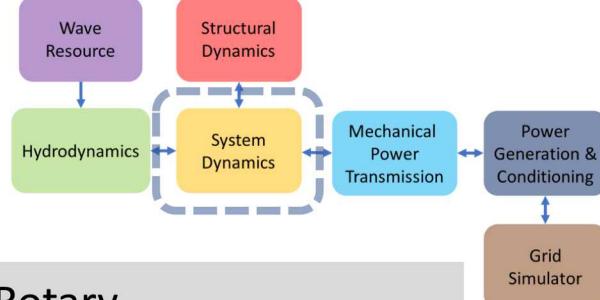
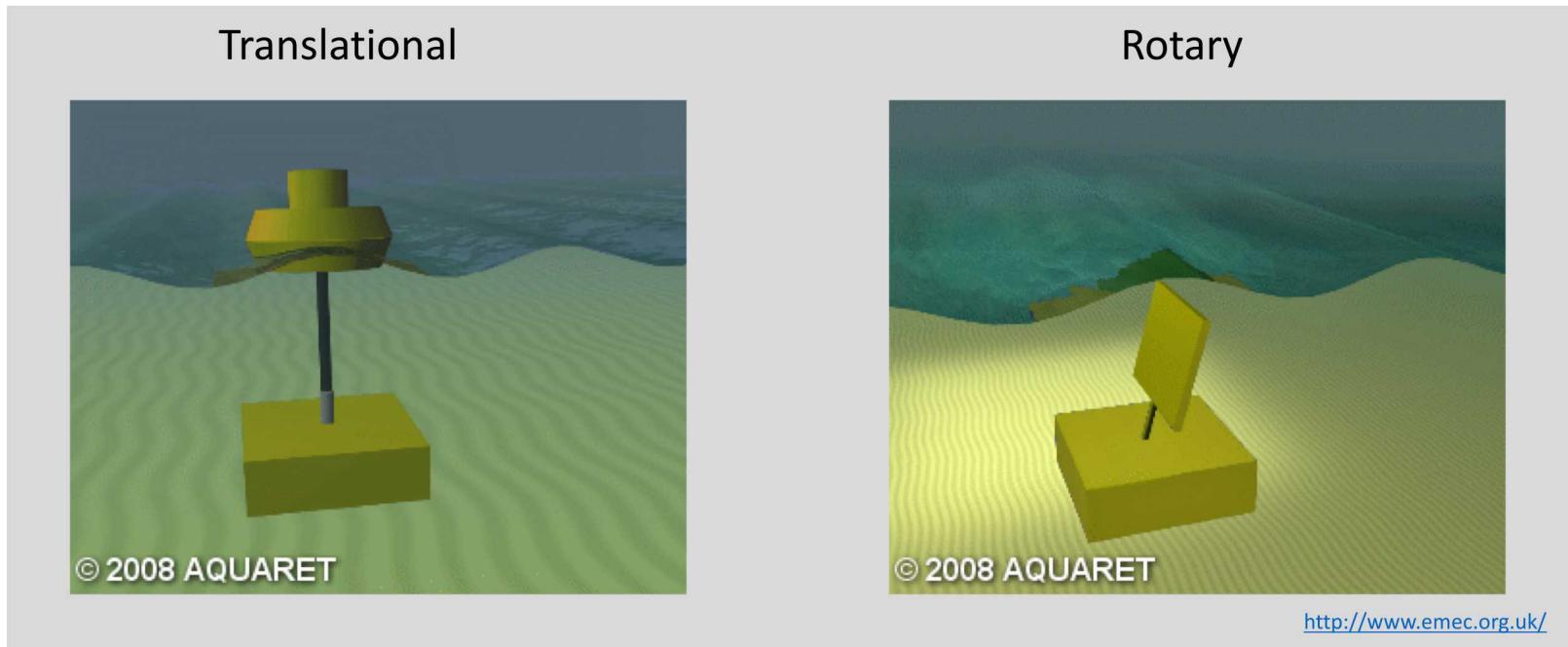


Multiple (moving) bodies

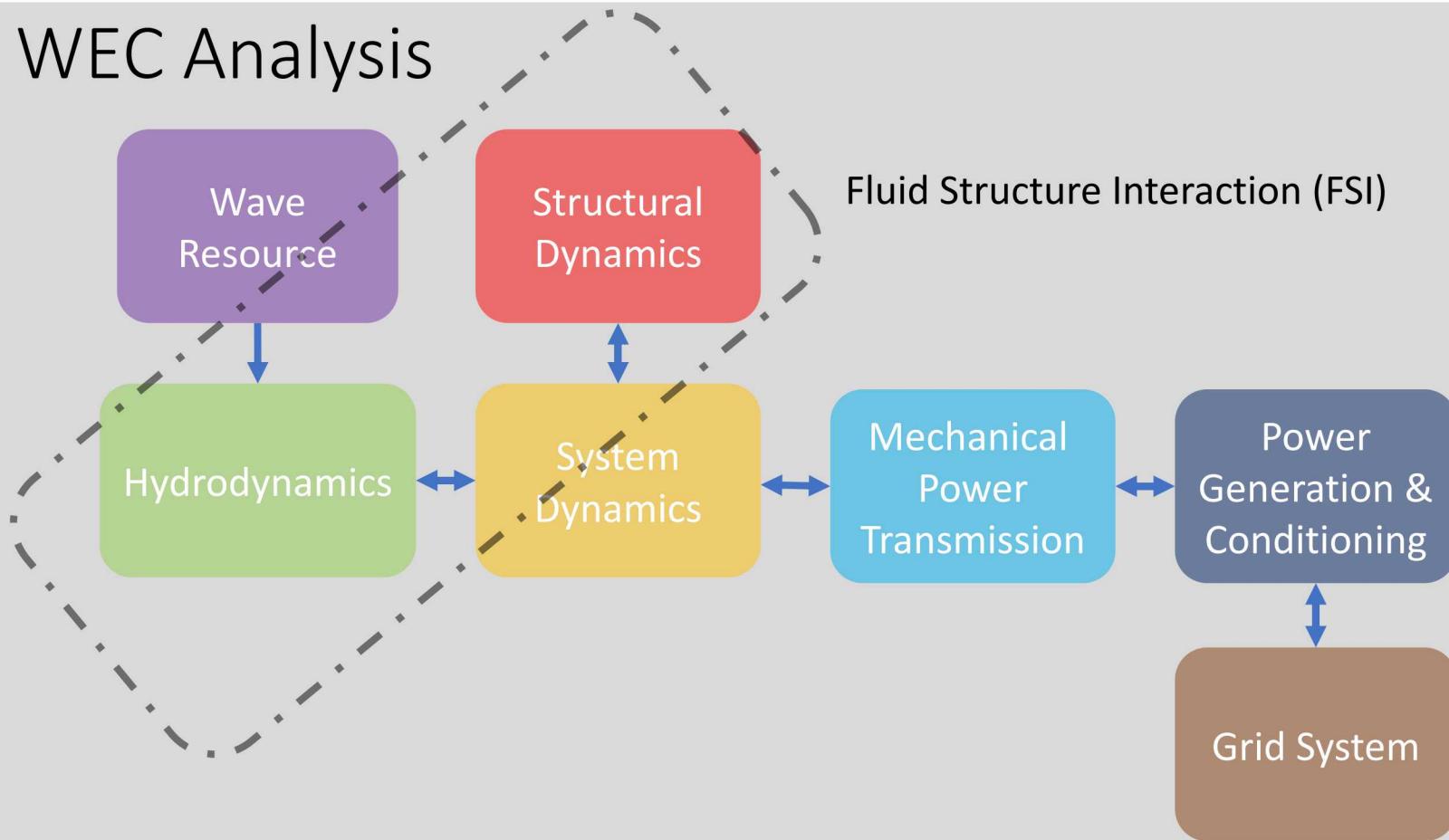


# WEC Classification

- From system dynamics:

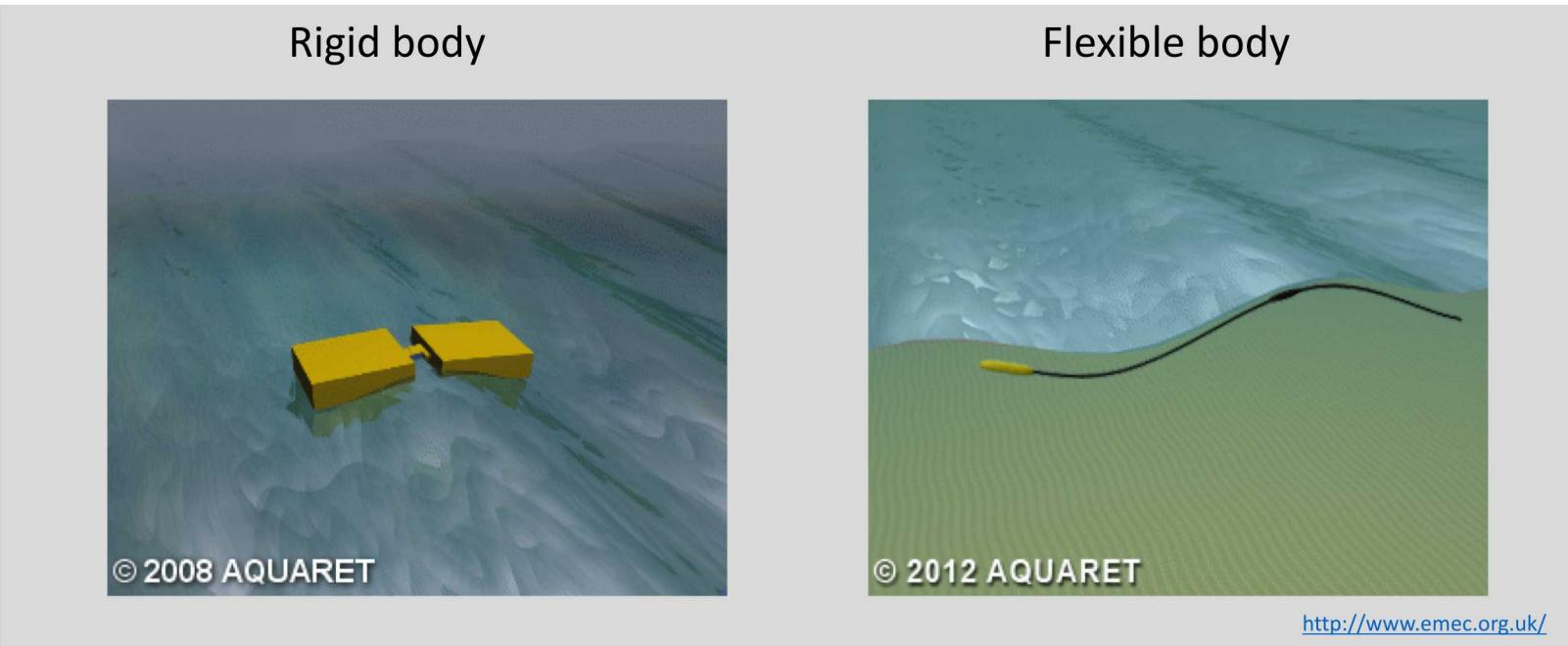


# WEC Analysis

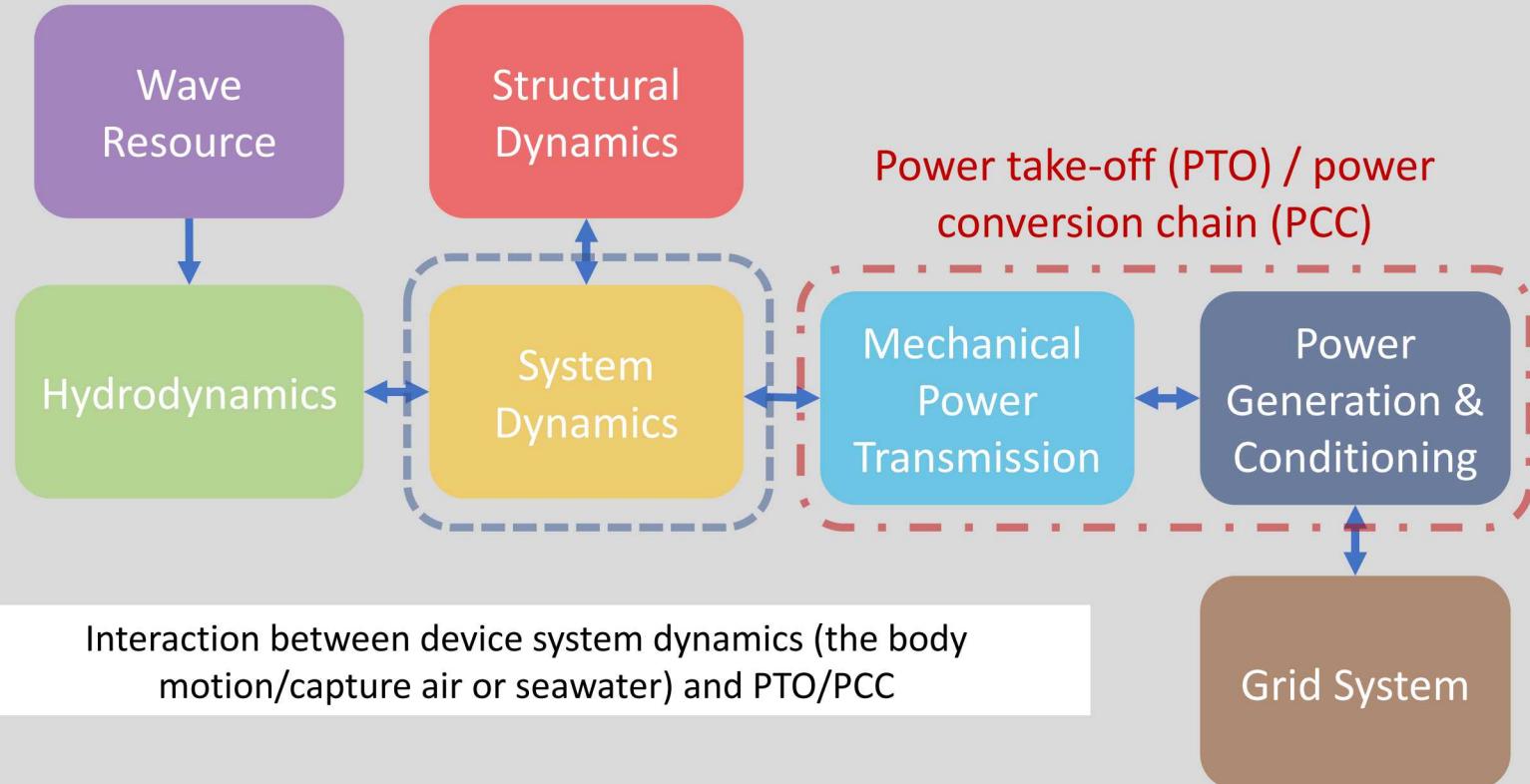


# WEC Classification

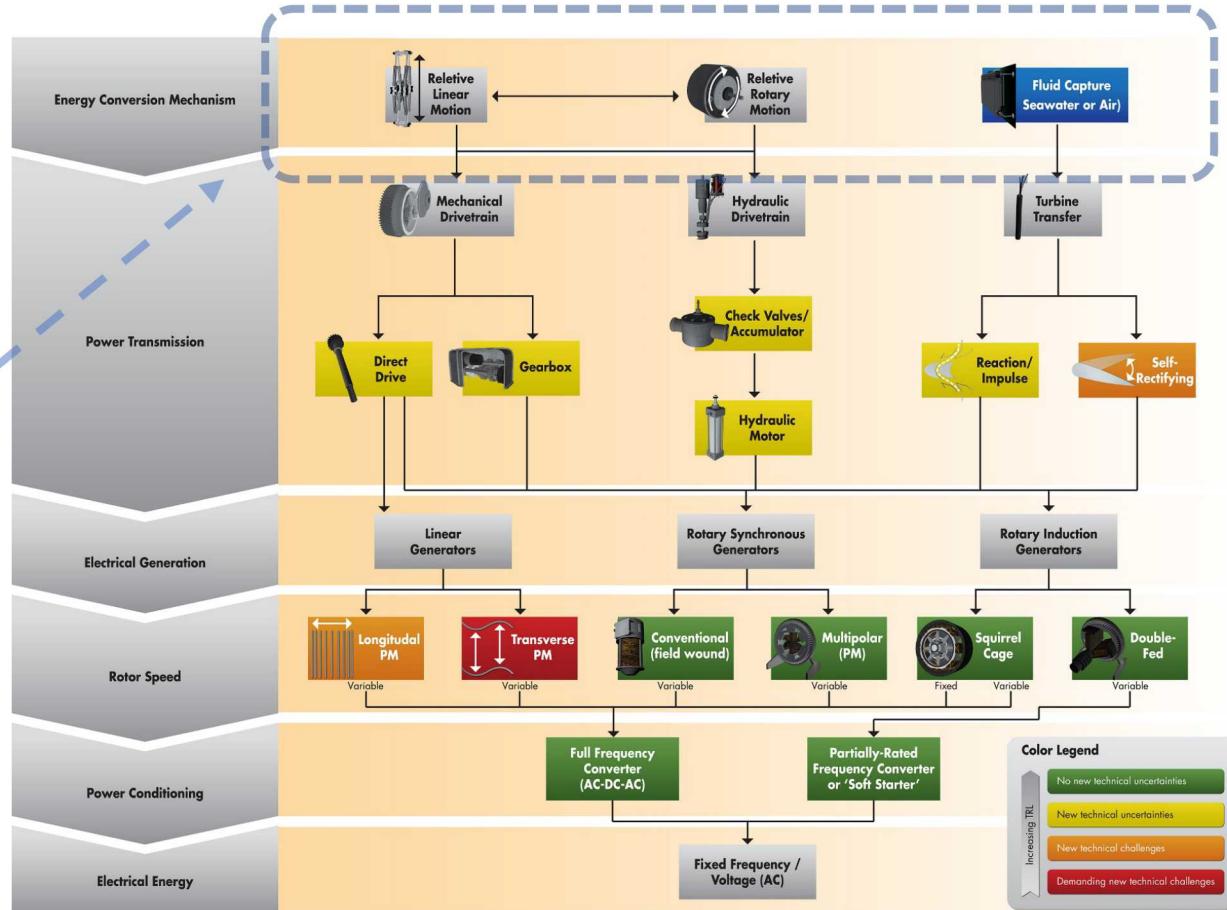
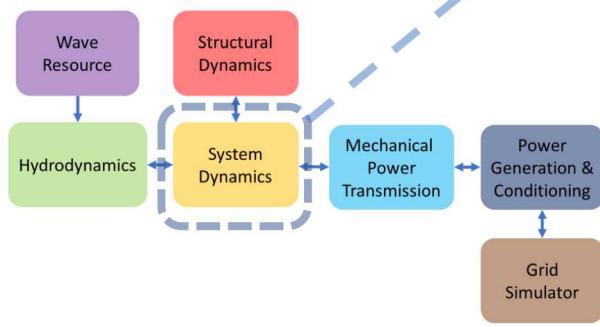
- From structural dynamics:



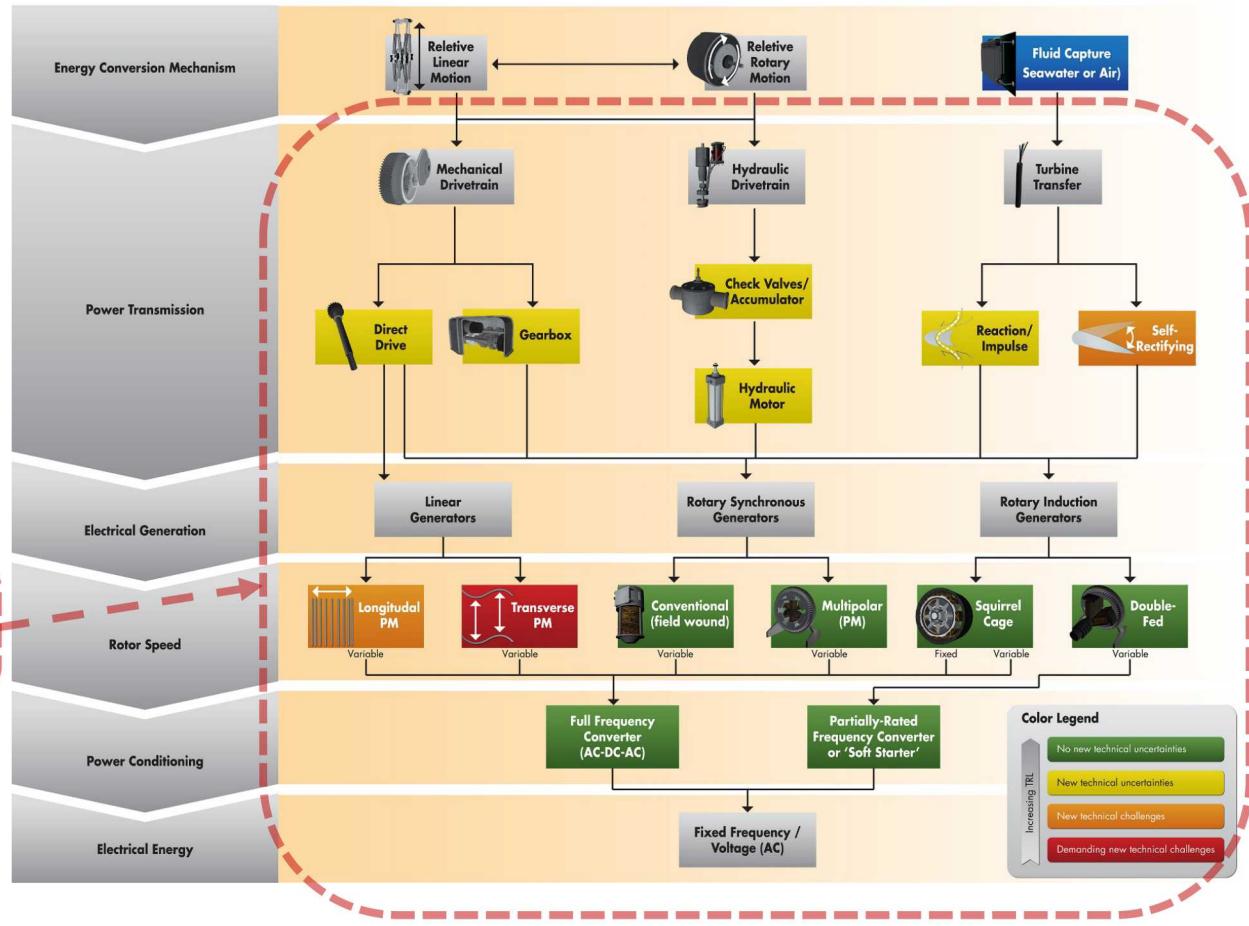
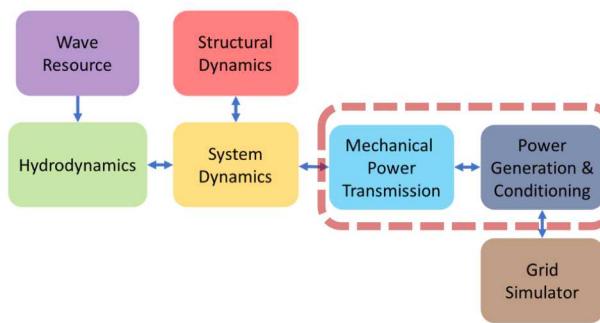
# WEC Analysis



# Power capture mechanisms

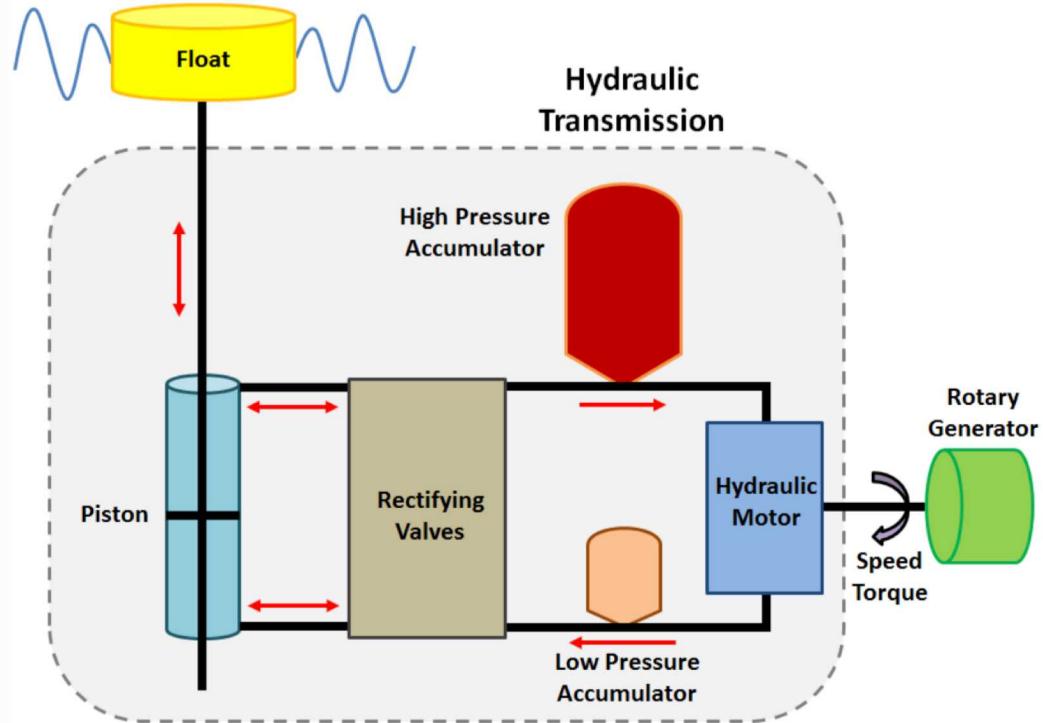


# Power capture mechanisms



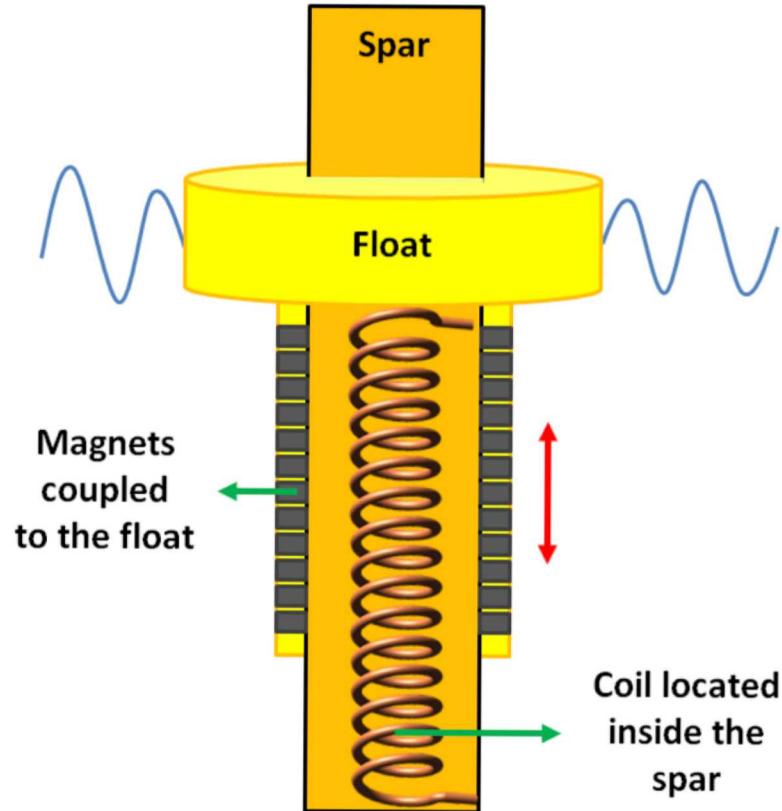
# Power capture mechanisms: Hydraulic System

Hydraulic PTO

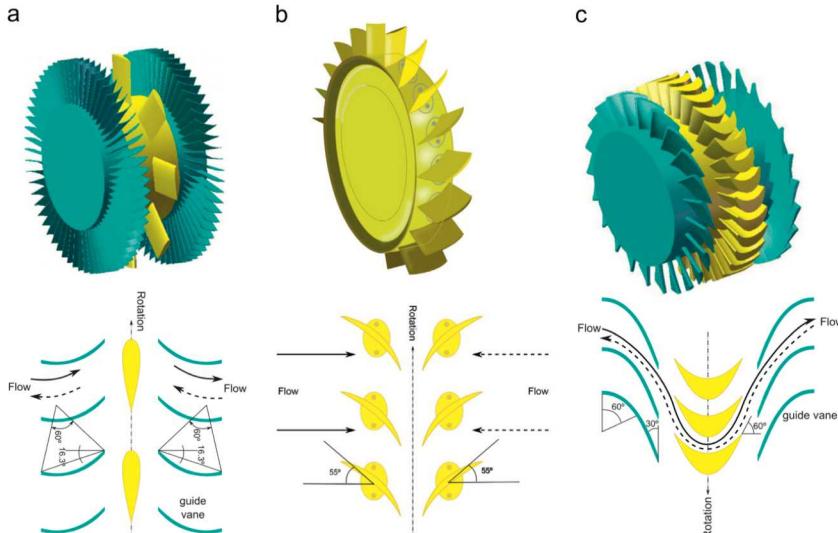


# Power capture mechanisms: Mechanical System

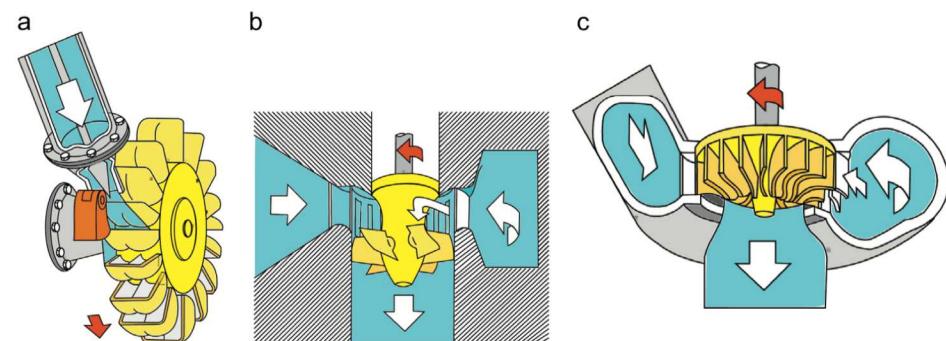
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# Power capture mechanisms: Air and Hydraulic Turbines



Air turbines for WECs. (a) Wells turbine, (b) Denniss–Auld turbine and (c) impulse turbine.

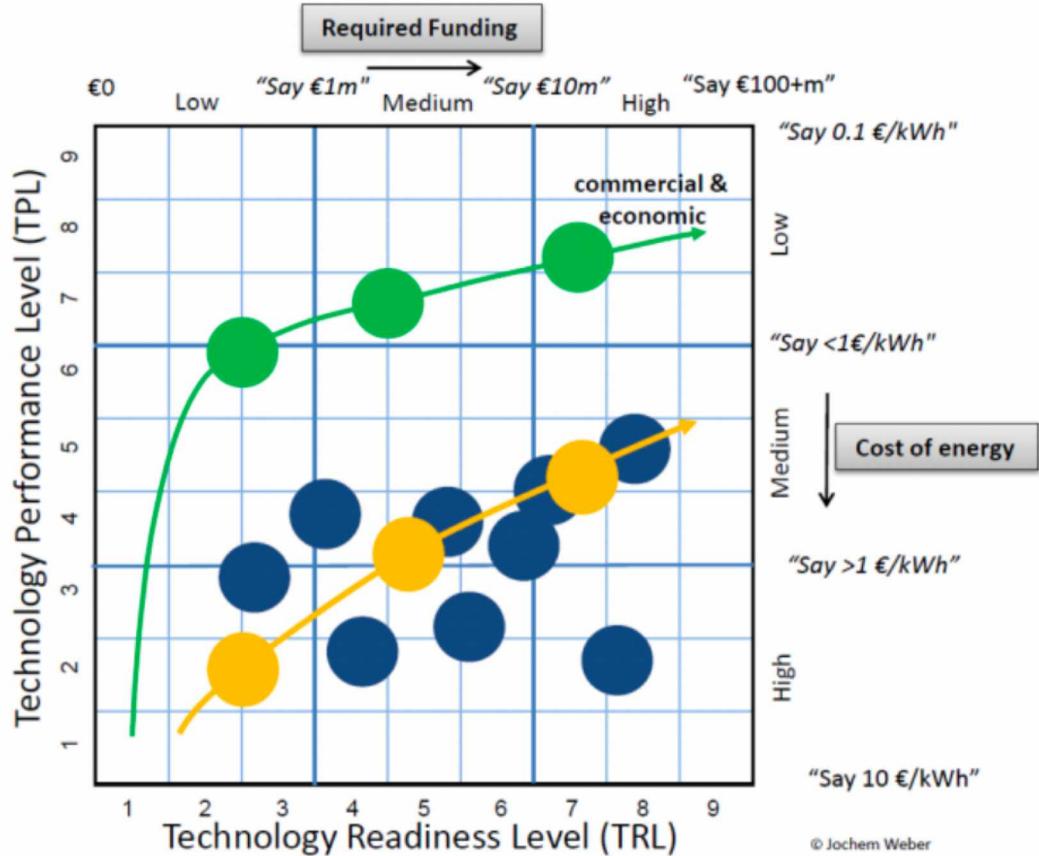


Hydro turbines for WECs. (a) Pelton turbine, (b) Kaplan turbine and (c) Francis turbine.

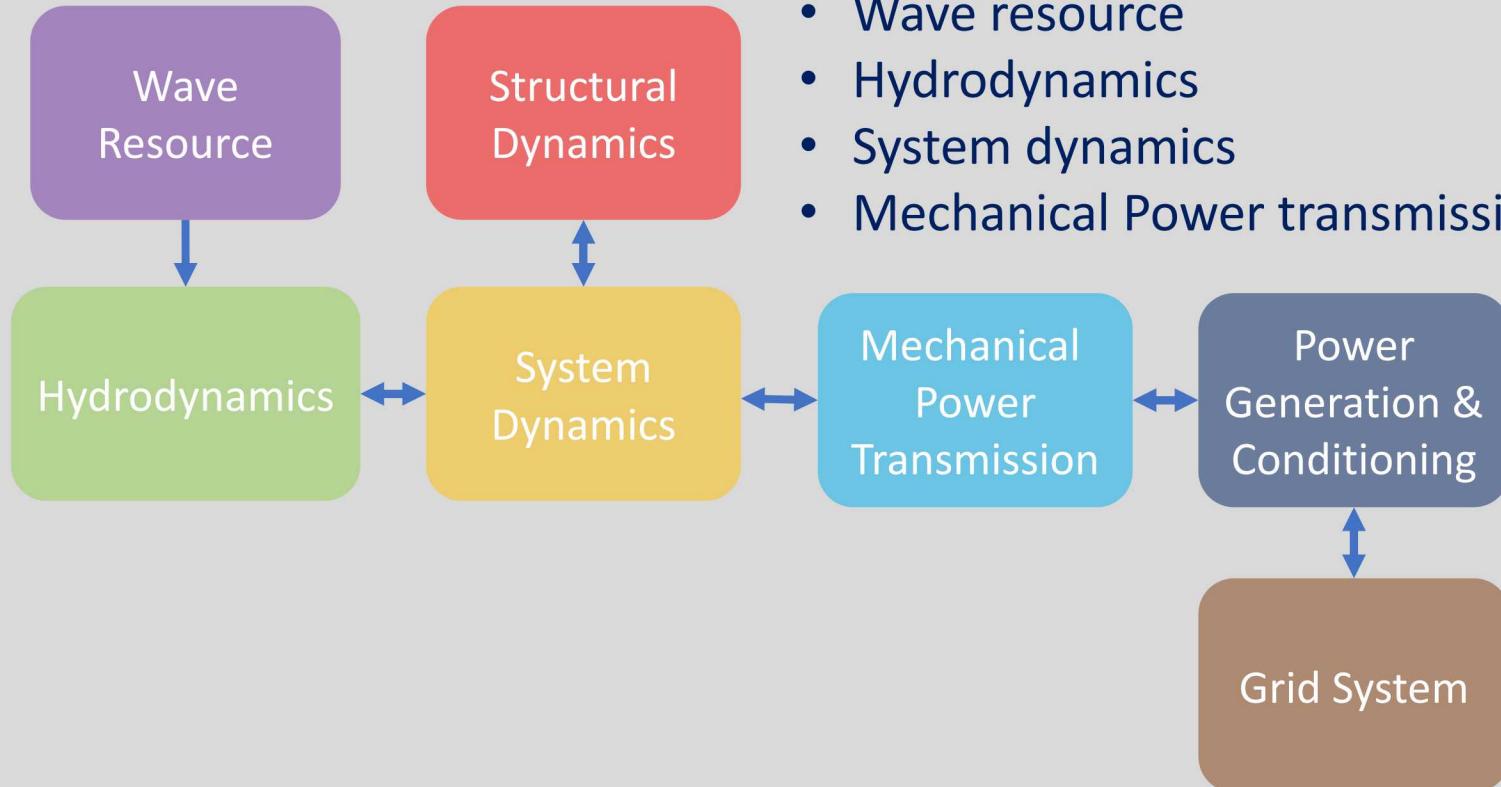
López I., Andreu J., Ceballos S., Martínez de Alegría I., and Kortabarria I., 2013, "Review of wave energy technologies and the necessary power-equipment," *Renew. Sustain. Energy Rev.*, **27**, pp. 413–434.

# Cost Effective WEC

TRL vs TRL

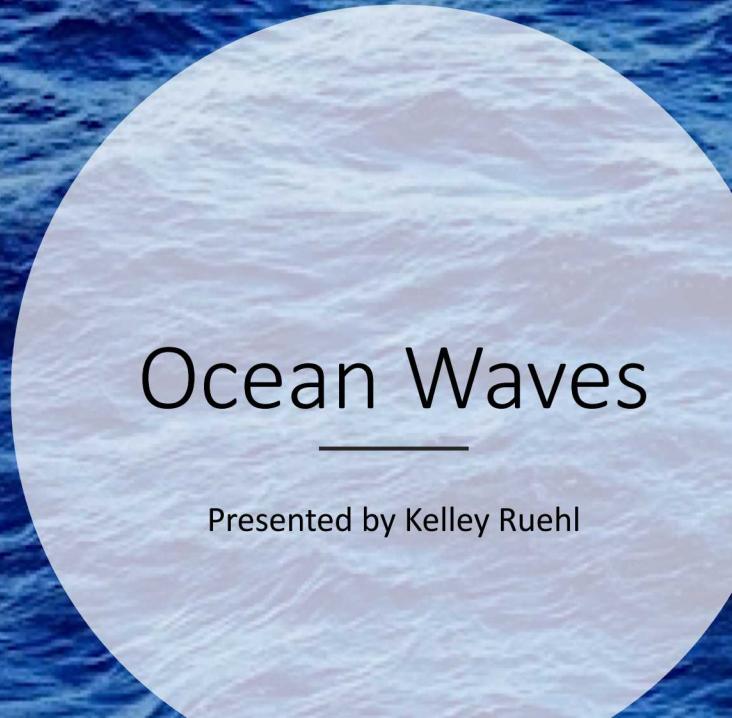


# WEC Analysis



## Focus of this OMAE Short Course

- Wave resource
- Hydrodynamics
- System dynamics
- Mechanical Power transmission



# Ocean Waves

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Presented by Kelley Ruehl

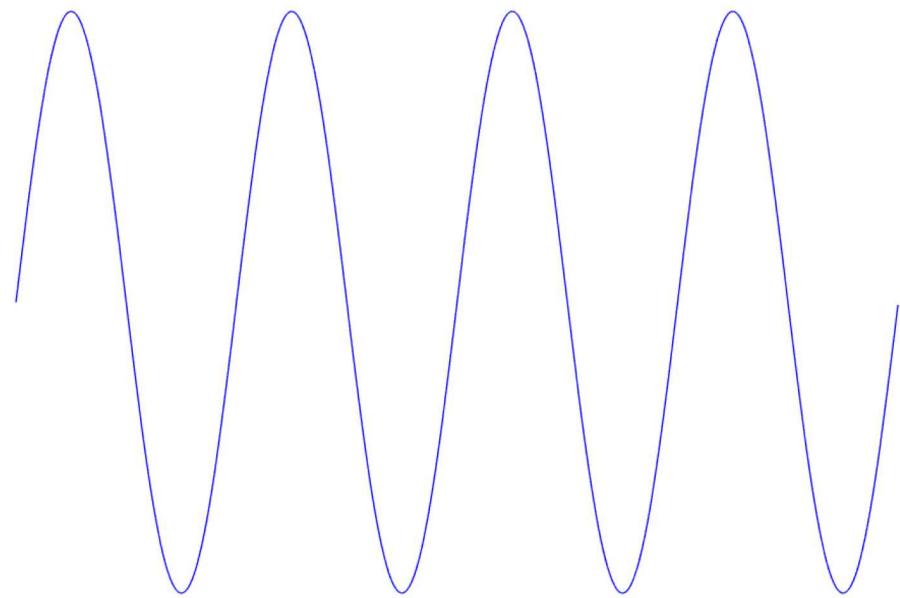
# Free Surface

- Still Water Line (SWL) refers to the undisturbed free surface, denoted by  $\nabla$
- Origin defined at SWL with  $+z$  up and  $+x$  to the right
- Water depth,  $h$  (seafloor at  $z = -h$ )





Harmonic  
Waves



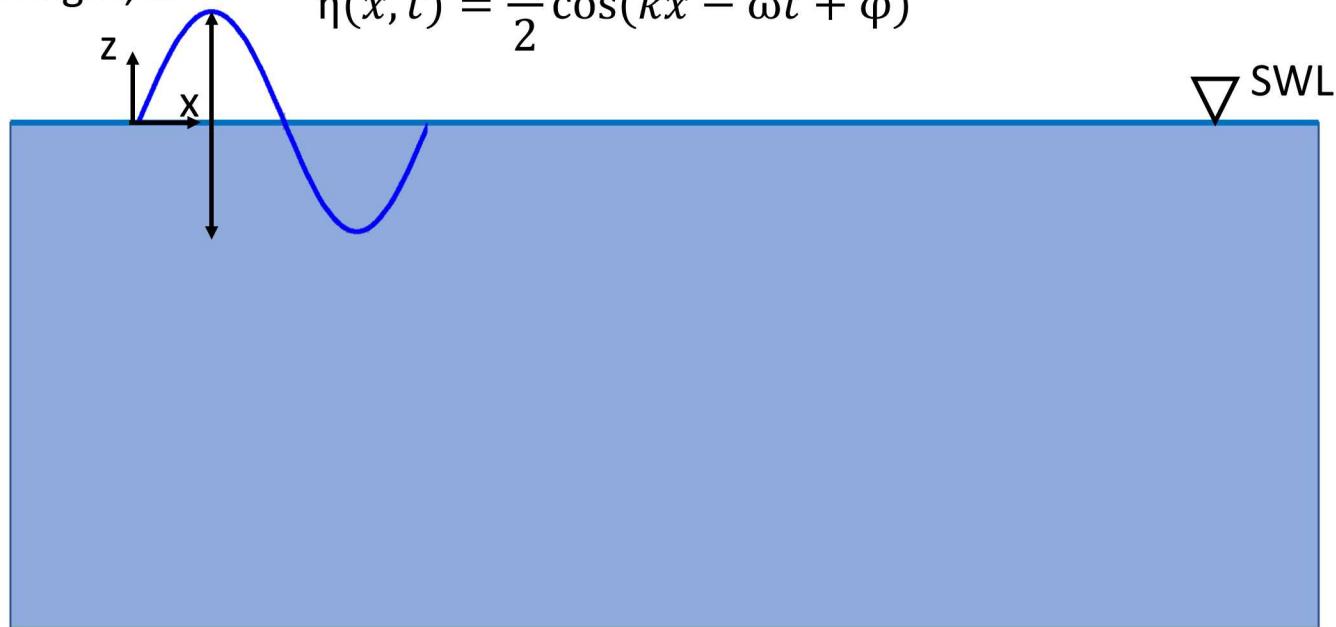
# Harmonic Waves (fixed in time)

Wave amplitude,  $A = \frac{H}{2}$

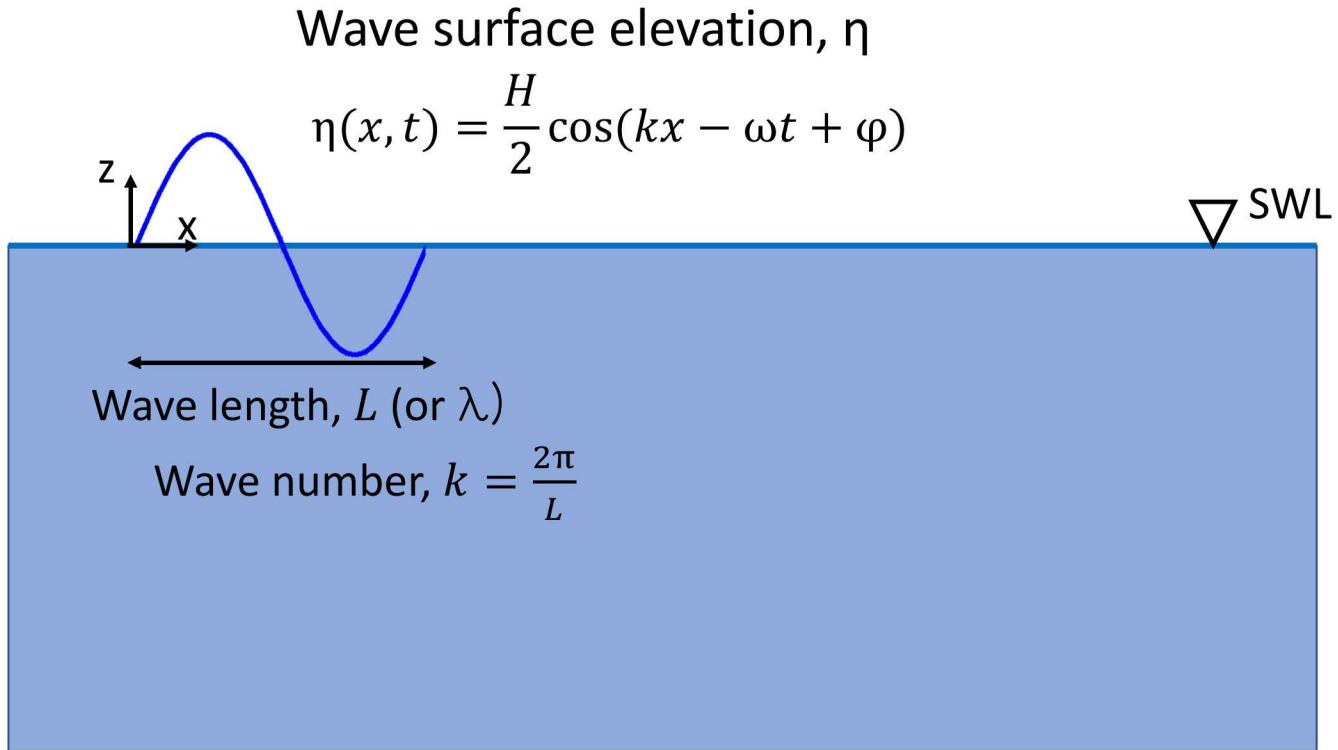
Wave surface elevation,  $\eta$

Wave height,  $H$

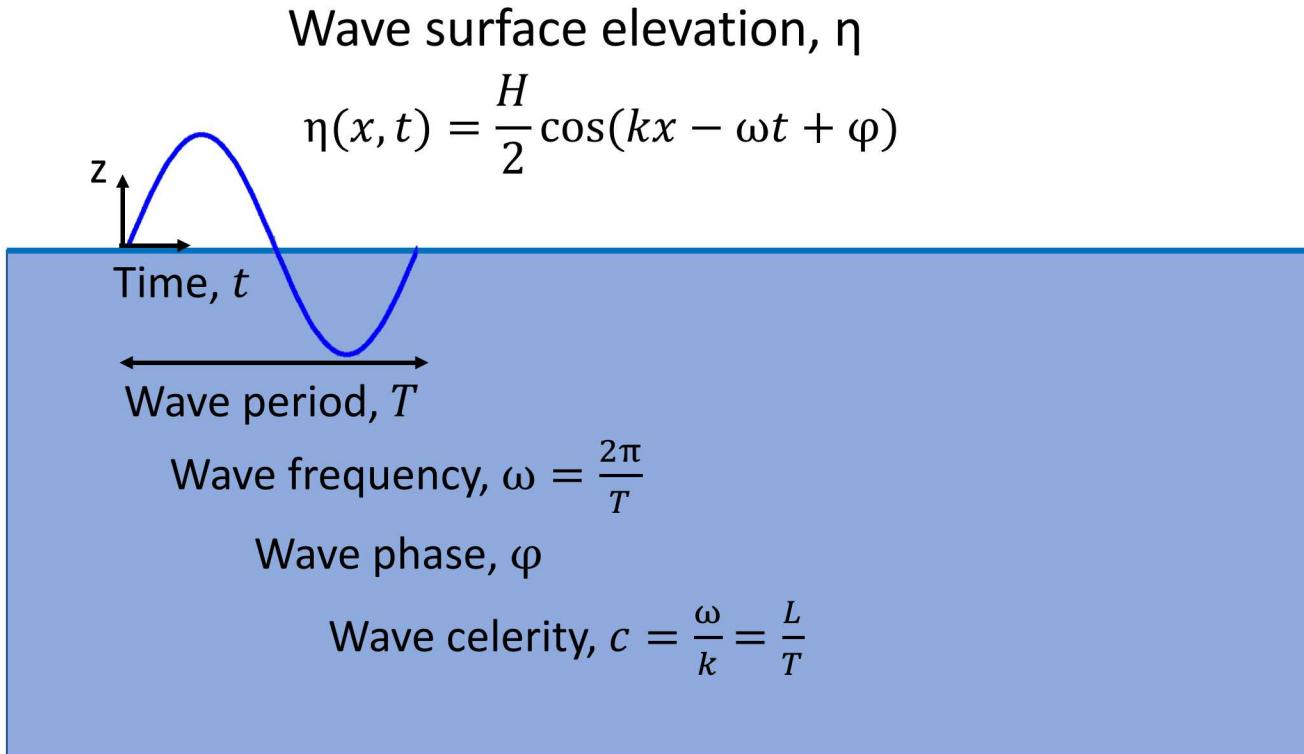
$$\eta(x, t) = \frac{H}{2} \cos(kx - \omega t + \varphi)$$



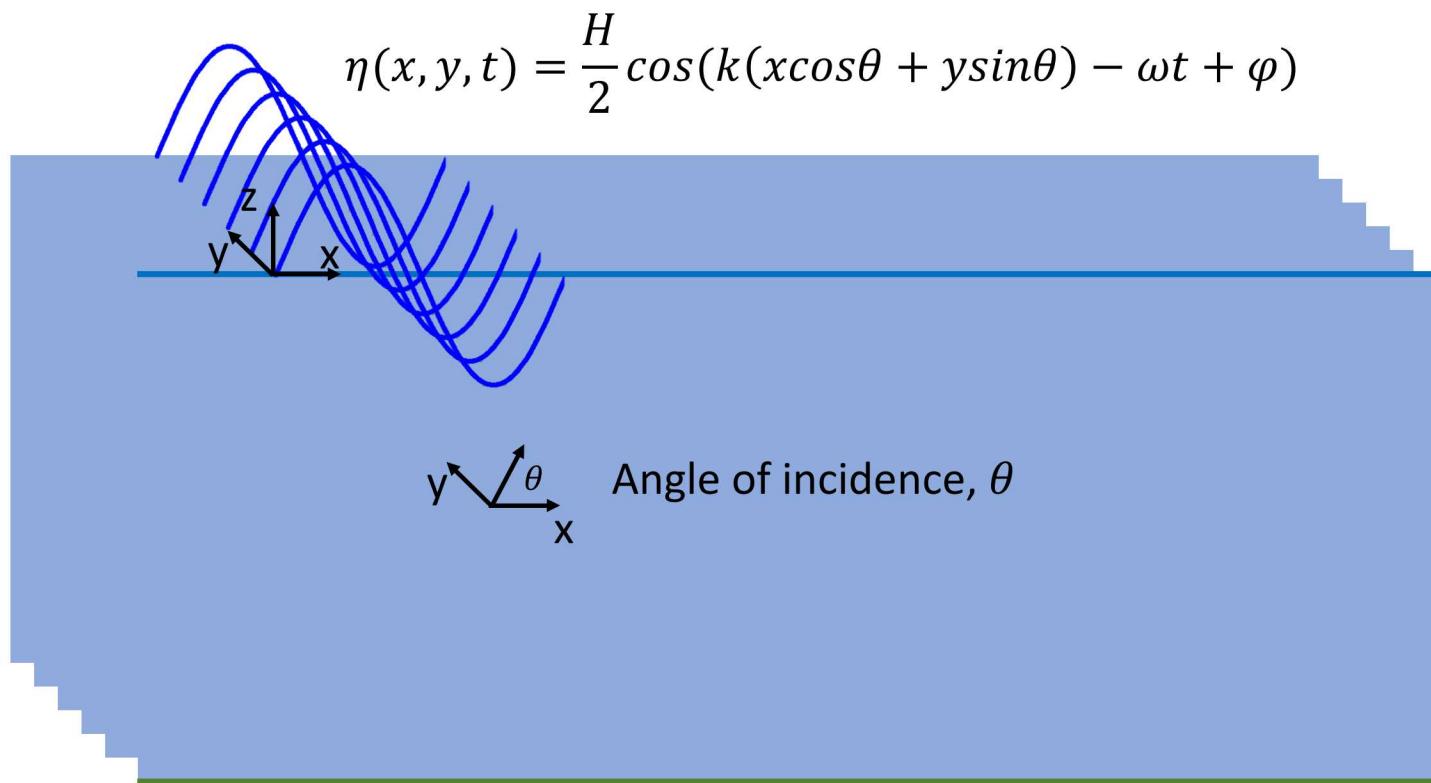
# Harmonic Waves (fixed in time)



# Harmonic Waves (fixed in space)

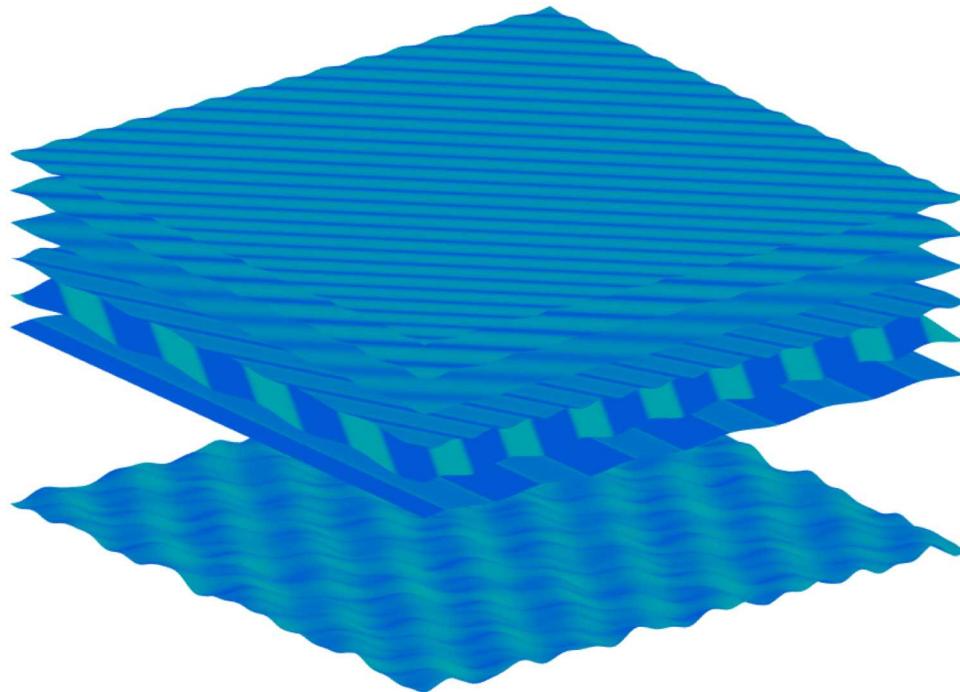


# Planar Harmonic Waves (fixed in time)



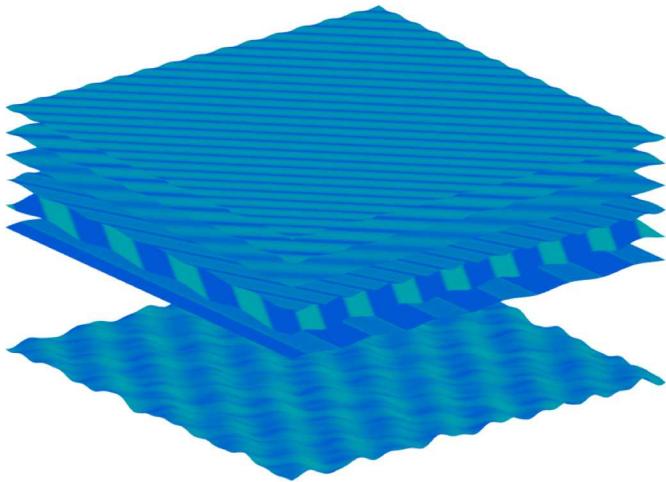


Ocean  
Waves



# Real Ocean Waves

$$\eta(x, y, t) = \sum_i \frac{H_i}{2} \cos(k_i (x \cos \theta_i + y \sin \theta_i) - \omega_i t + \varphi_i)$$



Real ocean waves are modeled as the **linear superposition** of a large number of **harmonic waves** at **different frequencies** and **angles of incidence**

Linear superposition is the basis of linear wave theory, which assumes

- **Small amplitude motion**
- **Inviscid fluid**
- **Irrational flow**

More on that later...

# Wave Spectra

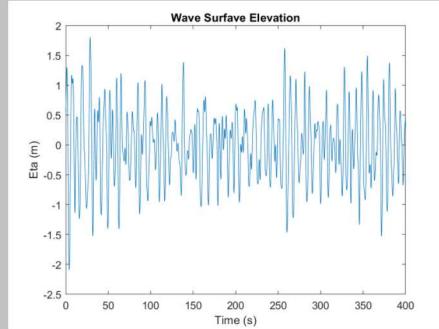
## Time-domain

- Waves are defined as wave surface elevation as a function of time and space

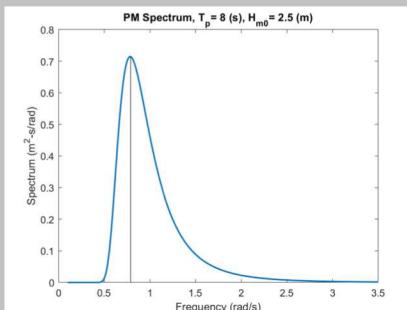


## Frequency-domain

- Waves are defined by energy content as a function of wave frequency
- Spectra proportional  $H^2$



$$\eta(x, y, t) = \sum_i \frac{H_i}{2} \cos(k_i (x \cos \theta_i + y \sin \theta_i) - \omega_i t + \varphi_i)$$



$$\overline{\eta^2(x, y, t)} = \int_0^{\infty} S(f) df$$

# Wave Spectra

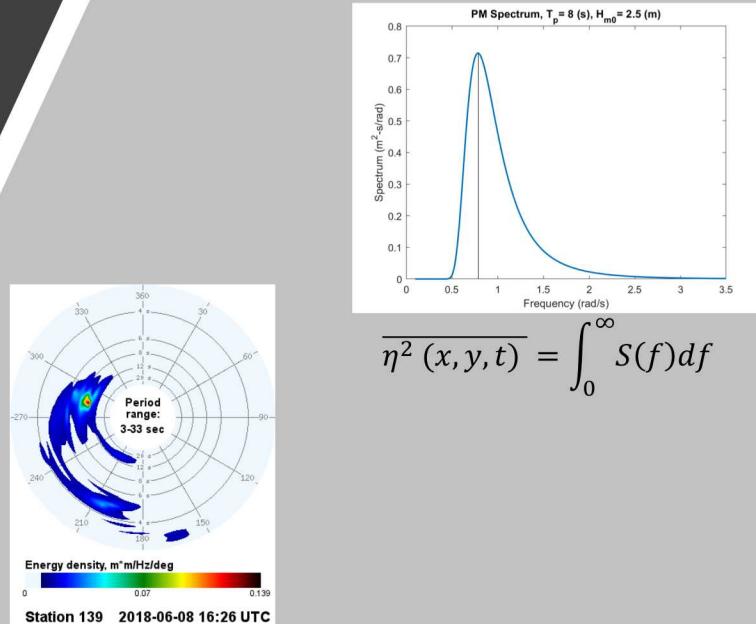
## Frequency Spectra

$$m_k = \int_0^\infty f^k S(f) df \quad H_{m0} = 4\sqrt{m_0}$$

- $H_{m0}$  = significant wave height
- $T_p$  = peak period

## Directional Spectra

- Real Ocean waves are often represented by wave spectra
- Used to determine **peak period, significant wave height and dominant wave direction**
- $\Theta$  = incident wave direction



$$S(f) = \int_{-\pi}^{\pi} S(f, \theta) d\theta$$

$$\overline{\eta^2(x, y, t)} = \int_0^\infty S(f) df$$

# Wave Spectra Formulations

## Pierson–Moskowitz

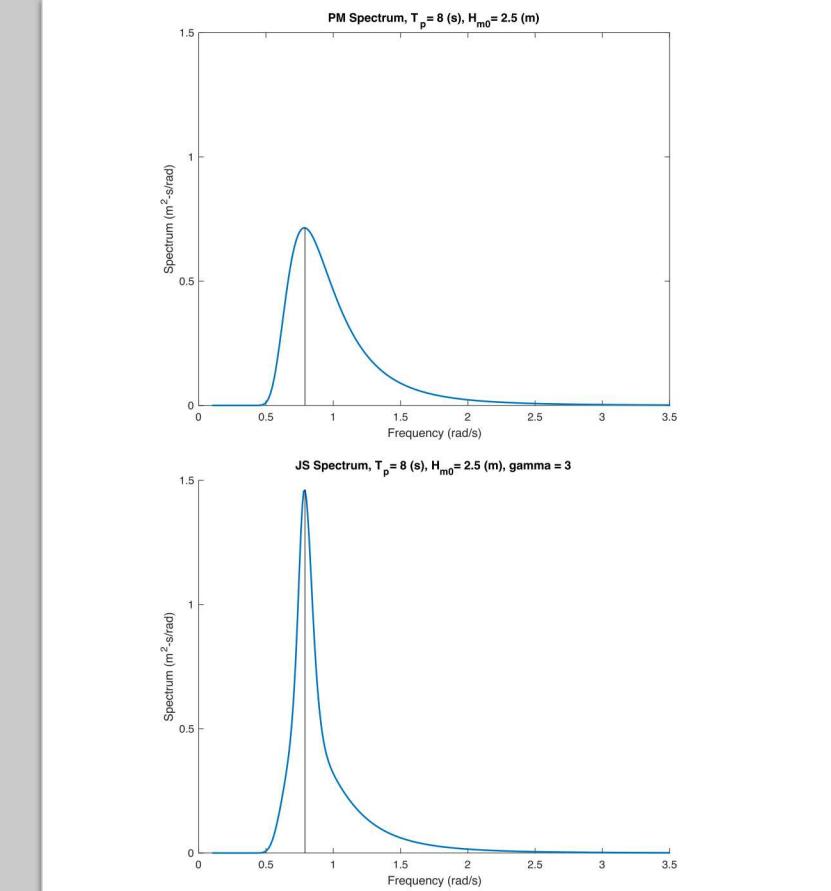
- Assumes wind blows steadily for a long time over a large area
- Fully developed seas

## JONSWAP

- Joint North Sea Wave Project
- JONSWAP is a Pierson-Moskowitz spectrum multiplied by an extra peak enhancement factor  $\gamma$

## Bretschneider

- 2 parameter spectrum based on peak period and significant wave height



# Wave Data Buoys

- National Data Buoy Center (NDBC)  
<http://www.ndbc.noaa.gov/>
- Coastal Data Information Program (CDIP)  
<http://cdip.ucsd.edu/>

## Data Collected

- Wave Height ( $H_s$ )
- Wave Period ( $T_p$ )
- Wave Direction ( $\theta$ )
- Wind data ( $U_{mean}$ ,  $U_{max}$  and  $\theta$ )
- Wave Spectra (energy content)
- And more...



CDIP Wind Buoy

<http://cdip.ucsd.edu/>



NDBC Directional Buoy

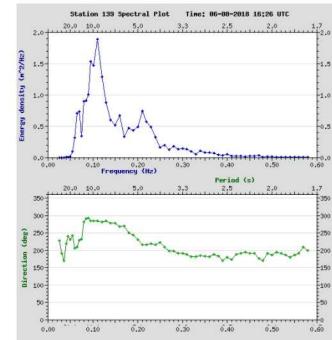
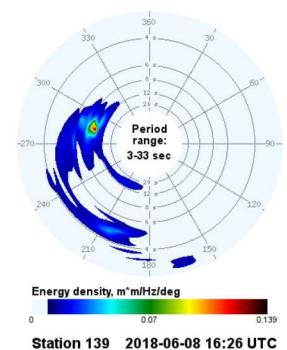
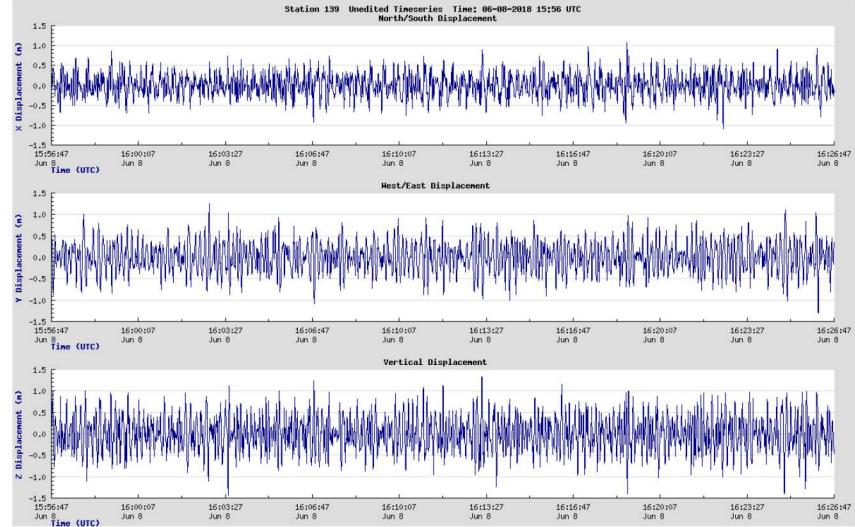
<http://www.ndbc.noaa.gov/>

# Umpqua Offshore, OR

## CDIP 139

- Maintains time-series of data buoy
- Generates wave spectra and wave rose

<http://cdip.ucsd.edu/?nav=historic&stn=139>



# Umpqua Offshore, OR

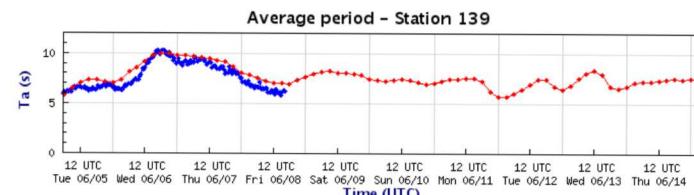
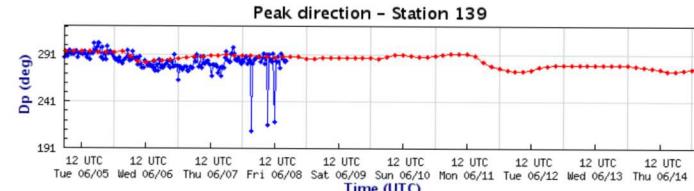
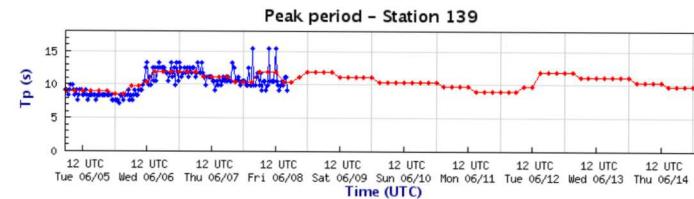
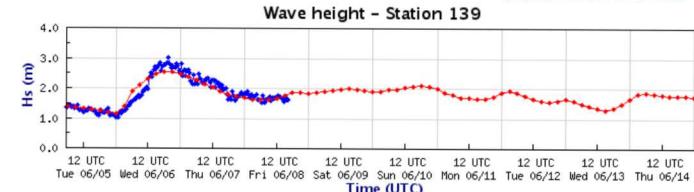
## CDIP 139

- Maintains time-series of data buoy
- Generates wave spectra and wave rose
- Compares data to WW3 Forecast

<http://cdip.ucsd.edu/?nav=historic&stn=139>

### Umpqua Offshore, OR Conditions + Forecast

Observations: CDIP buoy 139  
Forecast : NOAA WW3 46229

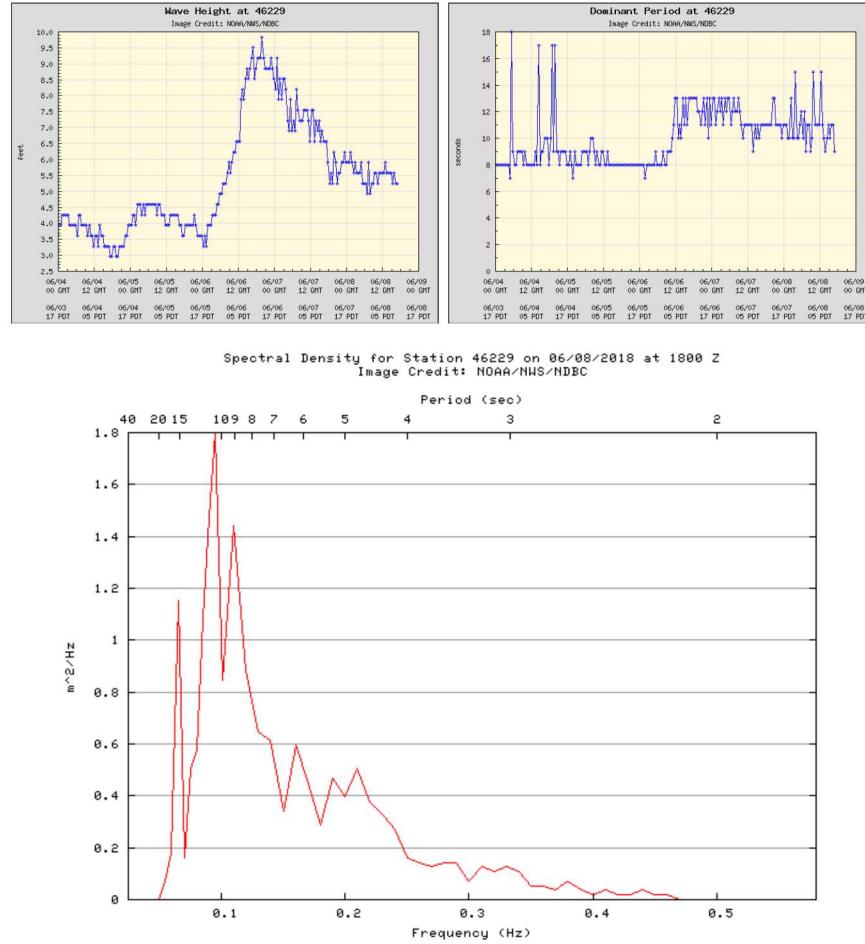


# Umpqua Offshore, OR

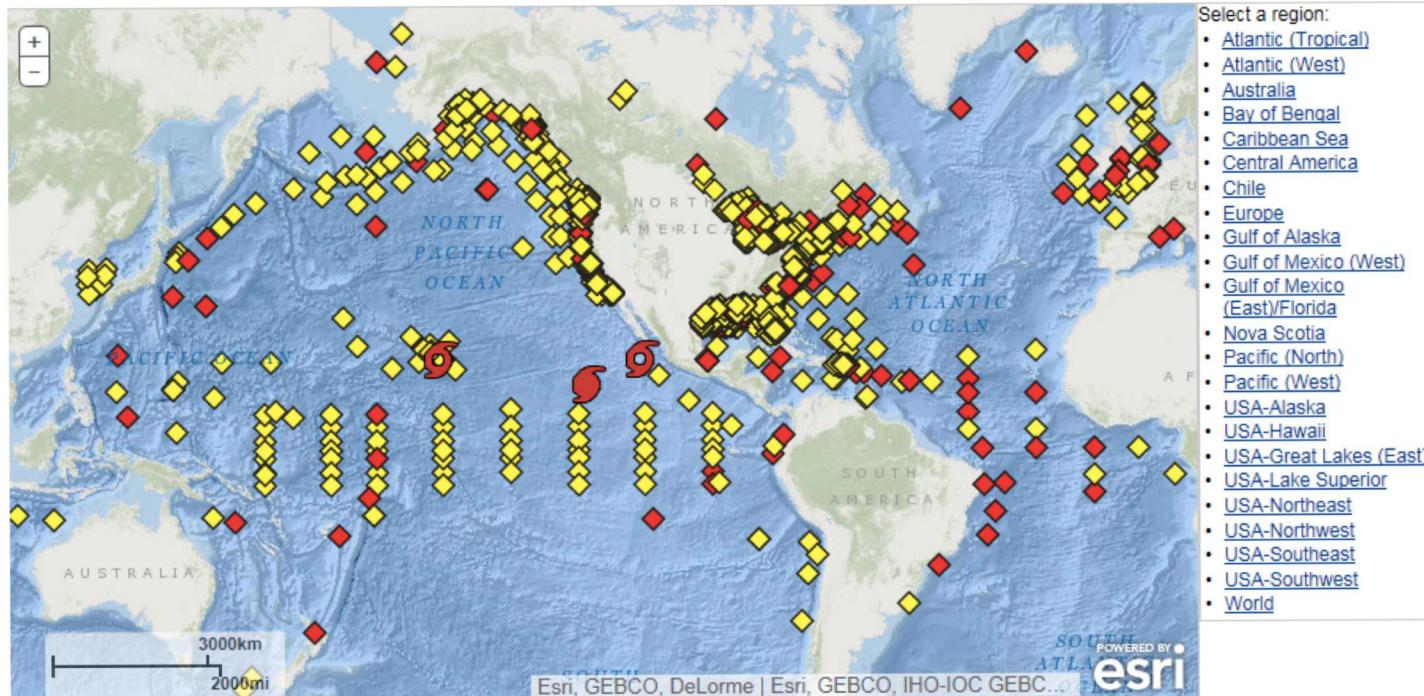
## NDBC 46229

- Data binned every 30min
- Maintains wave statistics
  - Peak Period
  - Significant Wave Height
  - Spectral Energy Content
- Generates data plots

[http://www.ndbc.noaa.gov/station\\_page.php?station=46229](http://www.ndbc.noaa.gov/station_page.php?station=46229)

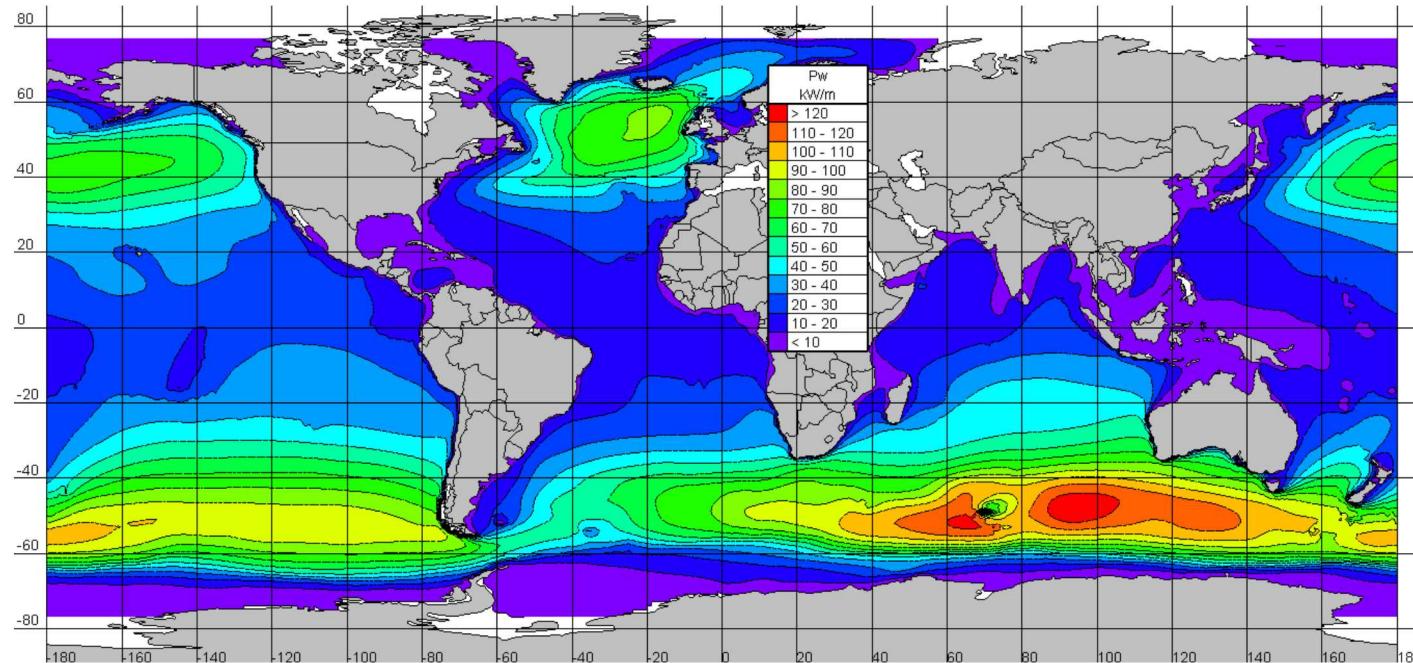


# NDBC Worldwide Buoy Map



<http://www.ndbc.noaa.gov/>

# Wave Energy Resource



Cornett, Andrew. (2008). A Global Wave Energy Resource Assessment.  
In: Proceedings of the eighteenth international offshore and polar conference, 50.

# Wave propagation models

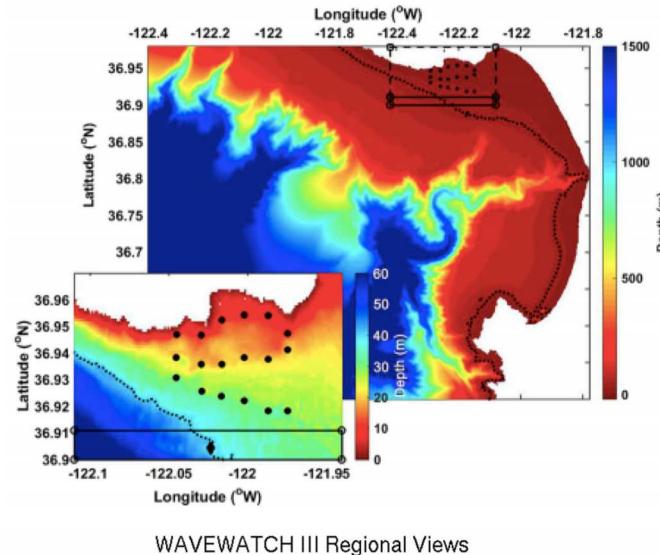
## Spectral Wave Models

- SWAN (Simulating WAves Nearshore)
- TOMAWAC

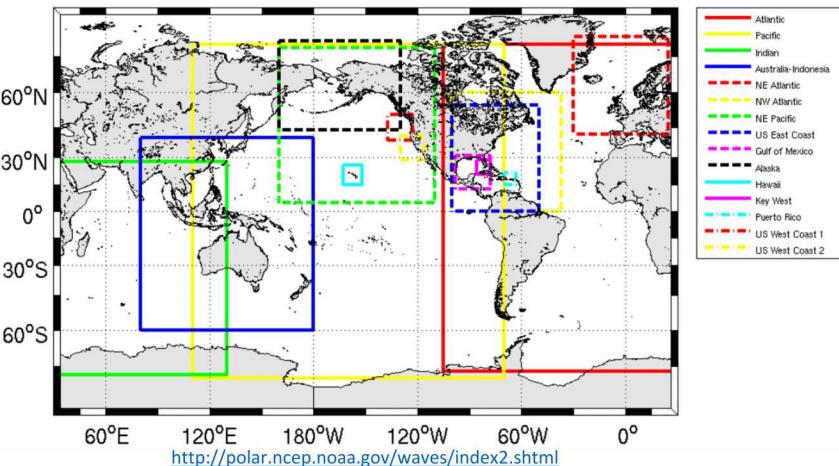
## NOAA WAVEWATCH III

- Maintains 30 year hindcast
- Generates forecast based on wind data

G. Chang, K. Ruehl, C. A. Jones, J. Roberts, and C. Chartrand, “[Numerical modeling of the effects of wave energy converter characteristics on nearshore wave conditions](#),” *Renewable Energy*, vol. 89, pp. 636–648, 2016.



WAVEWATCH III Regional Views



# Joint Probability Distribution

		Peak Period, Tp [sec]								
		5	7	9	11	13	15	17	19	22+
Significant Wave Height, Hs [m]	0.15	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.45	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.75	0.0	0.004	0.014	0.017	0.019	0.031	0.008	0.006	0.0
	1.05	0.008	0.021	0.034	0.044	0.024	0.048	0.017	0.012	0.0
	1.35	0.0	0.034	0.036	0.056	0.025	0.035	0.015	0.012	0.0
	1.65	0.0	0.018	0.029	0.050	0.028	0.024	0.010	0.010	0.0
	1.95	0.0	0.004	0.018	0.037	0.025	0.021	0.007	0.007	0.0
	2.25	0.0	0.0	0.008	0.020	0.017	0.016	0.005	0.005	0.0
	2.55	0.0	0.0	0.004	0.011	0.010	0.011	0.004	0.004	0.0
	2.85	0.0	0.0	0.0	0.006	0.006	0.008	0.003	0.0	0.0
	3.15	0.0	0.0	0.0	0.0	0.0	0.005	0.0	0.0	0.0
	3.45	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	3.75	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	4.05	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	4.35	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	4.65	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	4.95	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	5.25	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	5.55	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	5.85	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	6.15	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	6.45	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
		3.9	5.4	6.9	8.5	10.0	11.6	13.1	14.7	17.0
Average Period, Ta [sec] $2\pi(m_0/m_1)$										

Red Region Represents 95% of all possible sea conditions.

Red text depicts most common wave period for a given significant wave height.

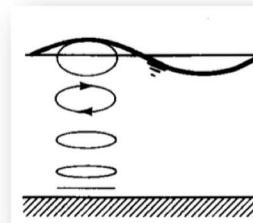
Using data summary products developed by CDIP for site

# Depth Regions (from Linear Wave Theory)

WEC Type?

## Shallow Water

- Water particle trajectories are elliptical
- Orbital size (energy content) is constant with depth

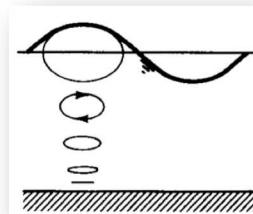


$$kh < \frac{\pi}{10}$$

$$\frac{h}{L} < \frac{1}{20}$$

## Intermediate Water

- Water particle trajectories are elliptical
- Orbital size (energy content) decays with increasing water depth

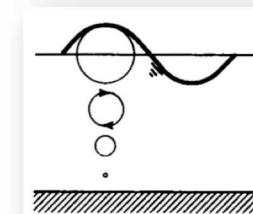


$$\frac{\pi}{10} < kh < \pi$$

$$\frac{1}{20} < \frac{h}{L} < \frac{1}{2}$$

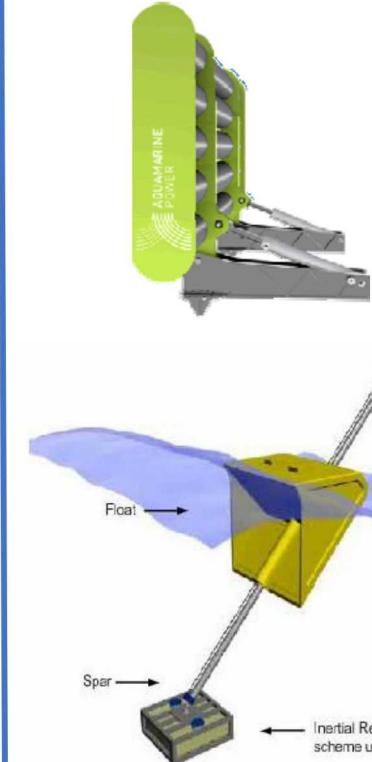
## Deep Water

- Water particle trajectories are circular
- Orbital size (energy content) decays with increasing water depth



$$kh > \pi$$

$$\frac{h}{L} > \frac{1}{2}$$

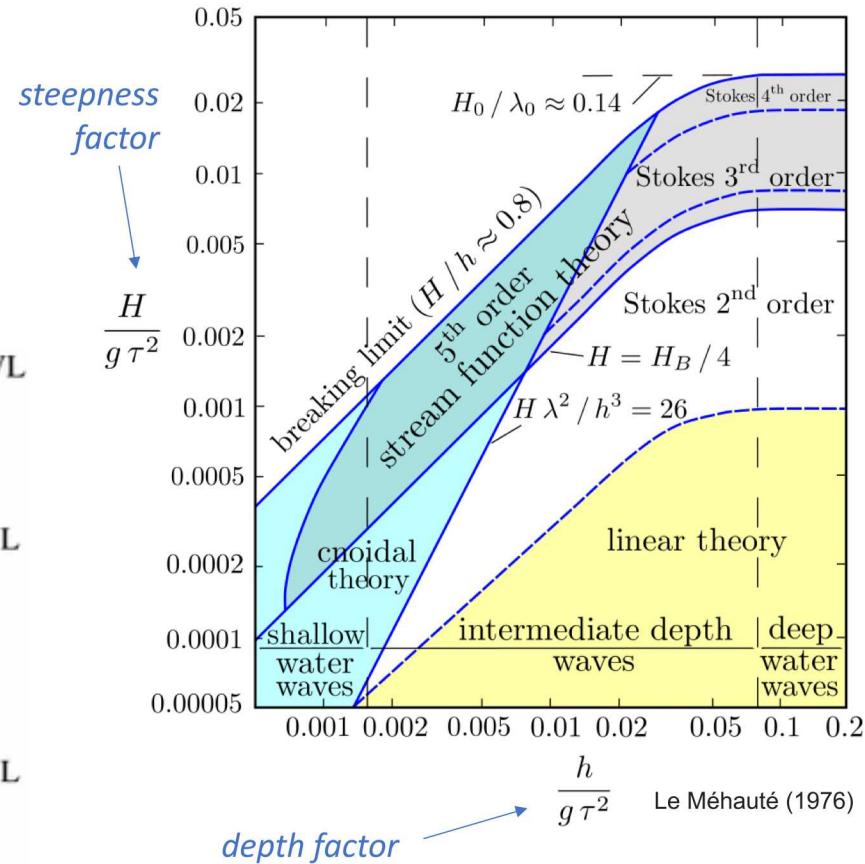
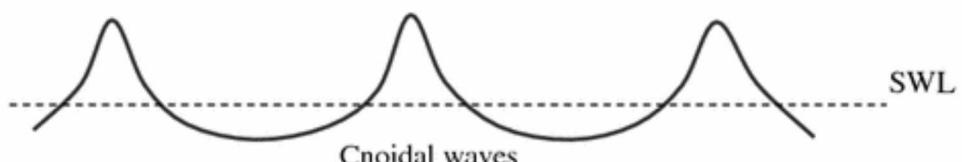
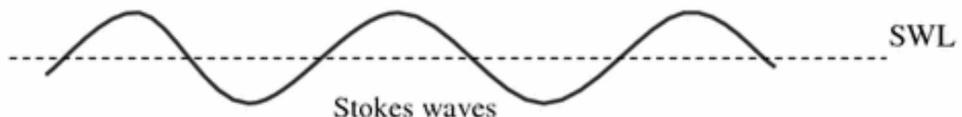
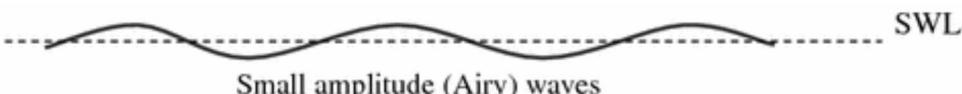


Depth region has implications on LWT formulation → shallow/deep water assumptions

# Wave Theory Formulations

*Real ocean waves are not sinusoids...*

*we use different representations  
based on some rough rules*



# WEC Design and Operation Requirement

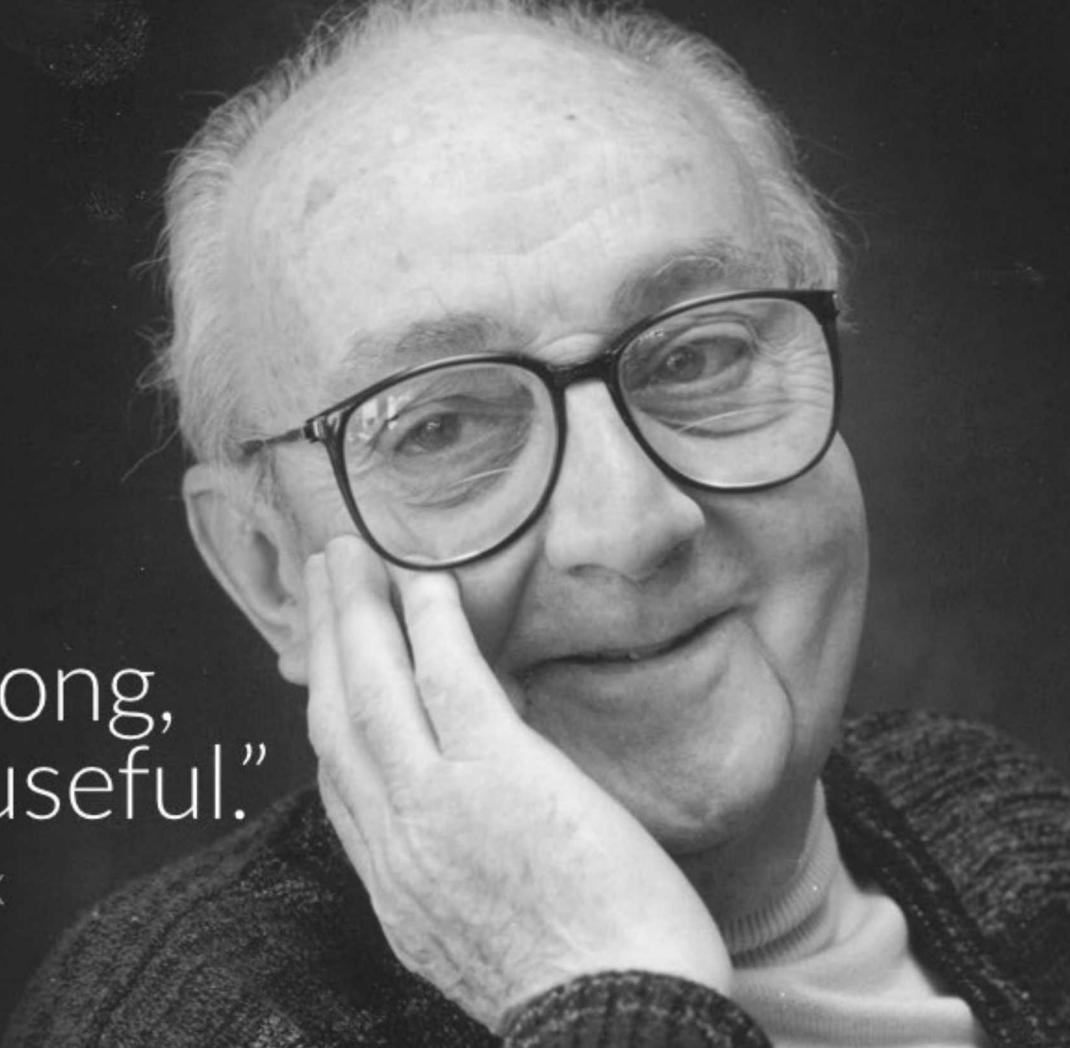
- WECs maximize energy capture and are often designed to resonate with waves (where viscous effects are essential).
- May result in large amplitude motion
- Need to survive in extreme, non-linear wave environments



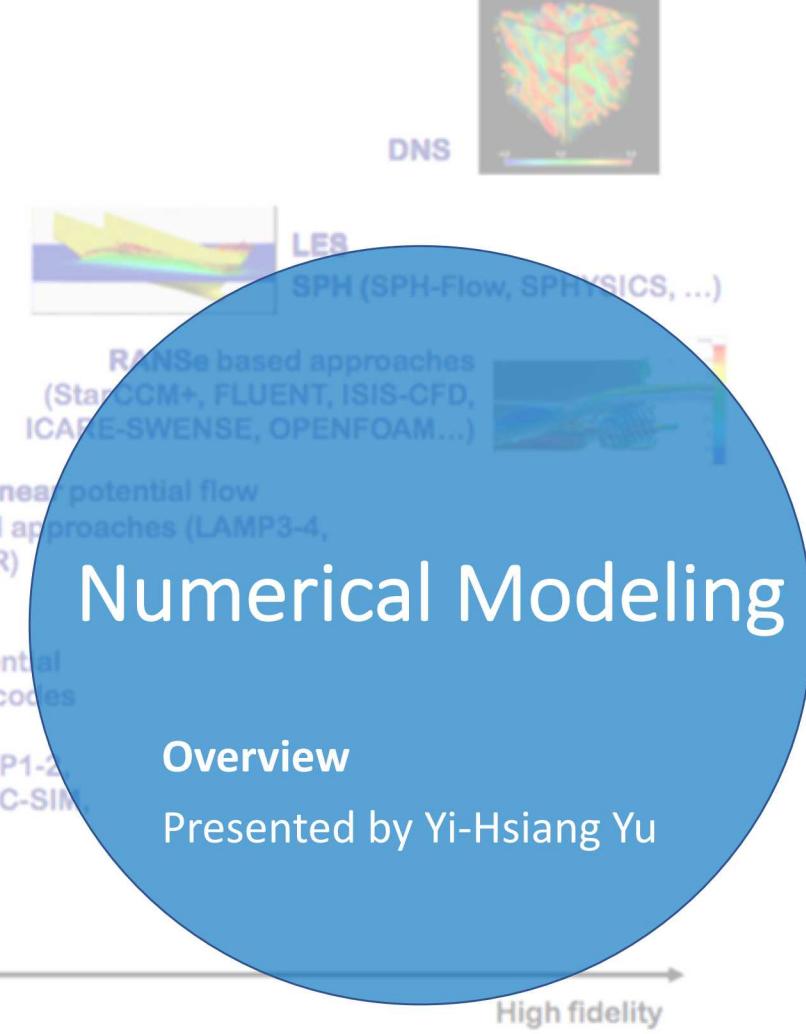
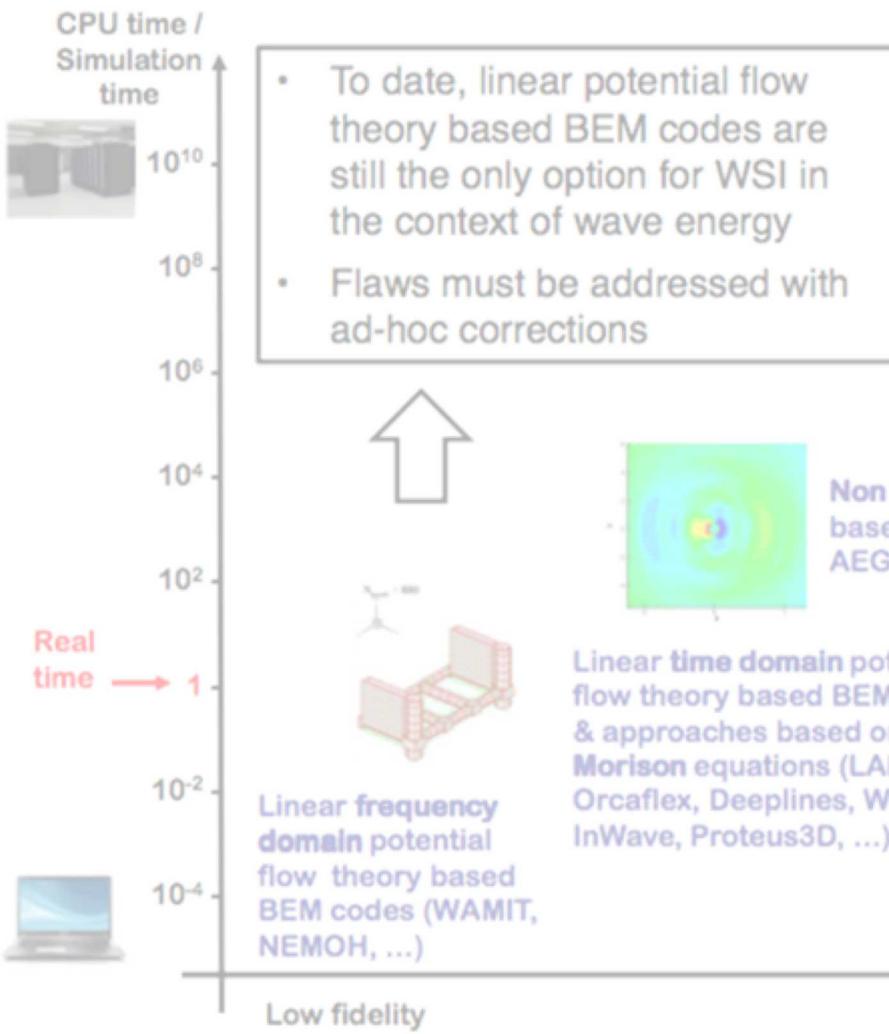
“

Essentially, all  
models are wrong,  
but some are useful.”

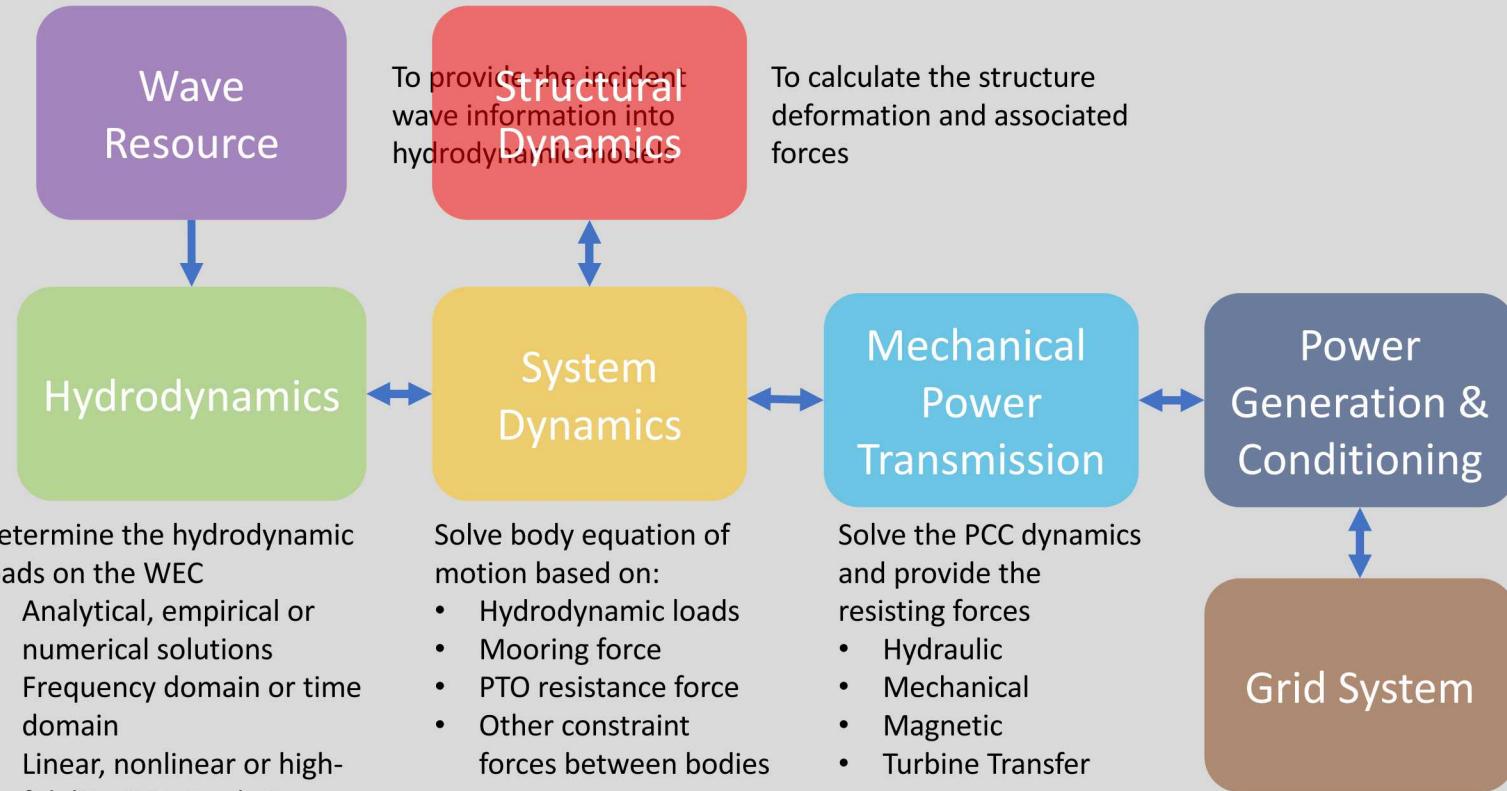
—George E. P. Box

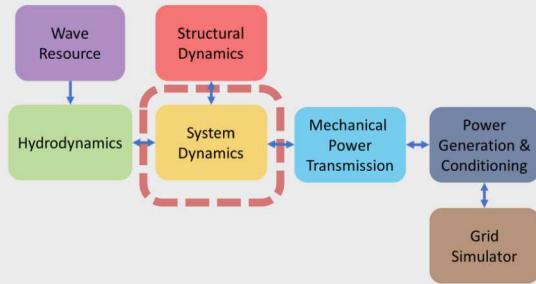


# Coffee Break (15 mins)



# WEC Simulations: Wave-To-Wire



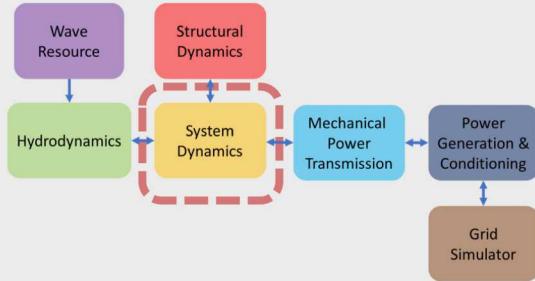


# System Dynamics: Equation of motion

$$m\ddot{x}(t) = f_{hd}(t) + f_{PTO}(t) + f_m(t) + f_c(t) + f_{st}(t)$$

PTO forces  
 Mooring force  
 Constraint forces between bodies/reference frame  
 Hydrodynamic loads  
 • Wave induced forces  
 • Body motion  
 • Gravity and buoyancy forces  
 • Including the effect of fluid viscosity

Forces from structure displacement



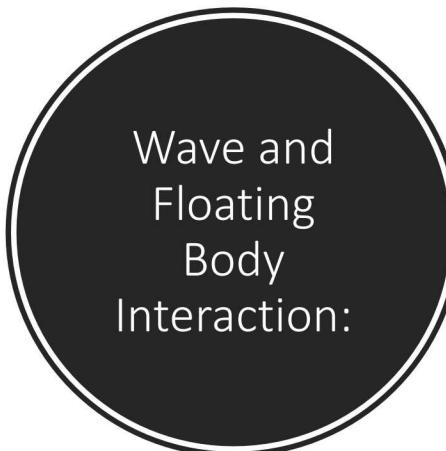
# System Dynamics: Equation of motion

The resulting governing equations for the flow, PTO and the structure displacement can be combined and solved simultaneously using a single solver or more often solved separately and coupled through iterations.

The iterative approach allows the use of more efficient numerical approaches for solving fluid dynamics and structural dynamics, such as different time step sizes and time marching methods.

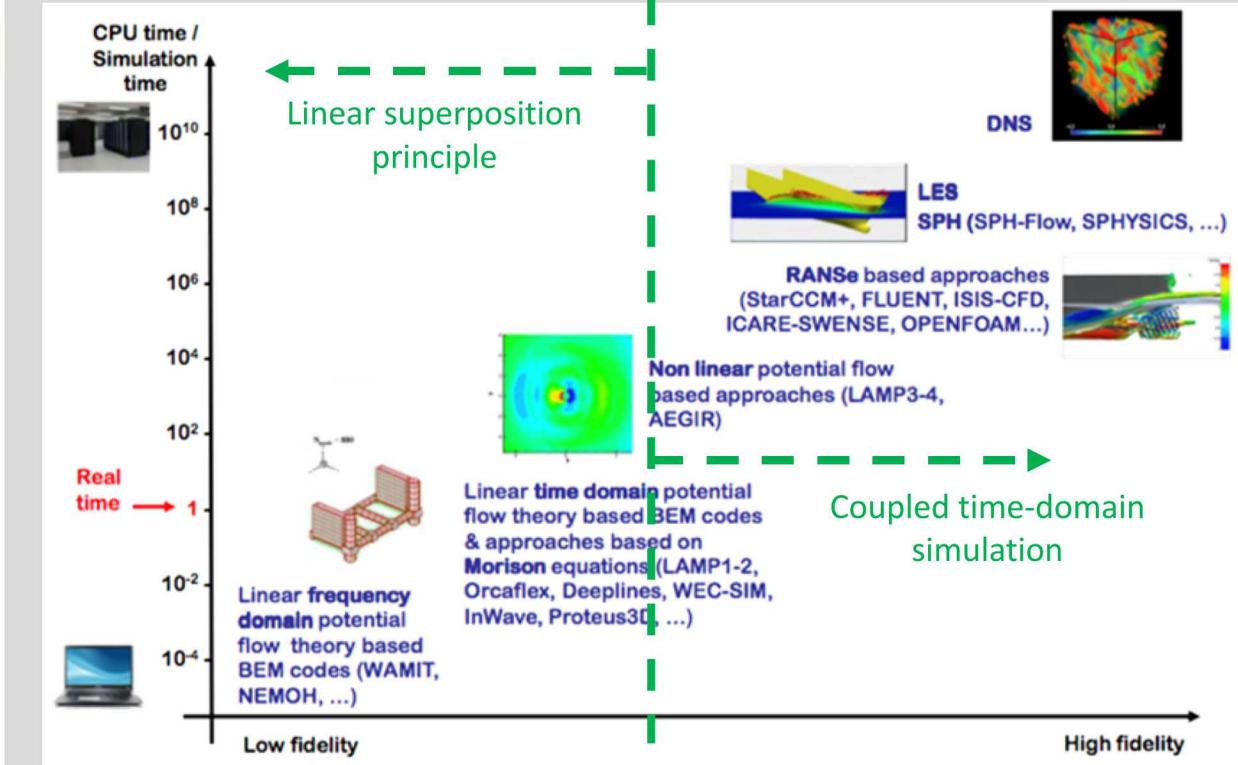
Wave  
Resource

Structural  
Dynamics



Linear superposition principle  
Vs  
Coupled time-domain  
simulation

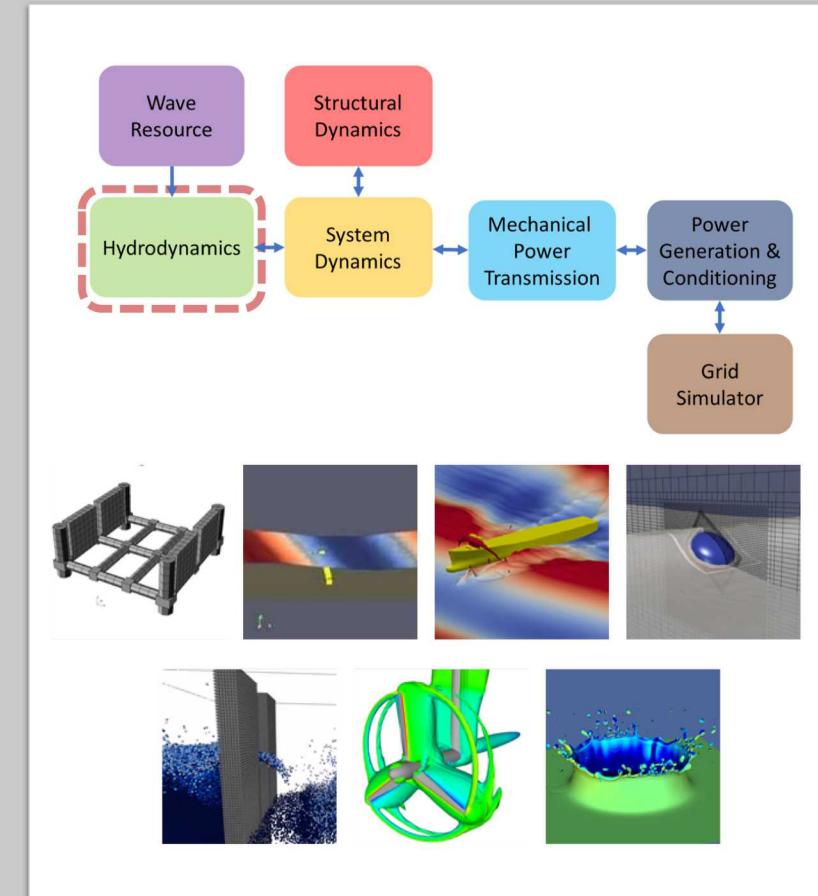
## Hydrodynamics and system dynamic model fidelity versus computational time



# Hydrodynamics Simulation

Determine the hydrodynamic loads on the WEC

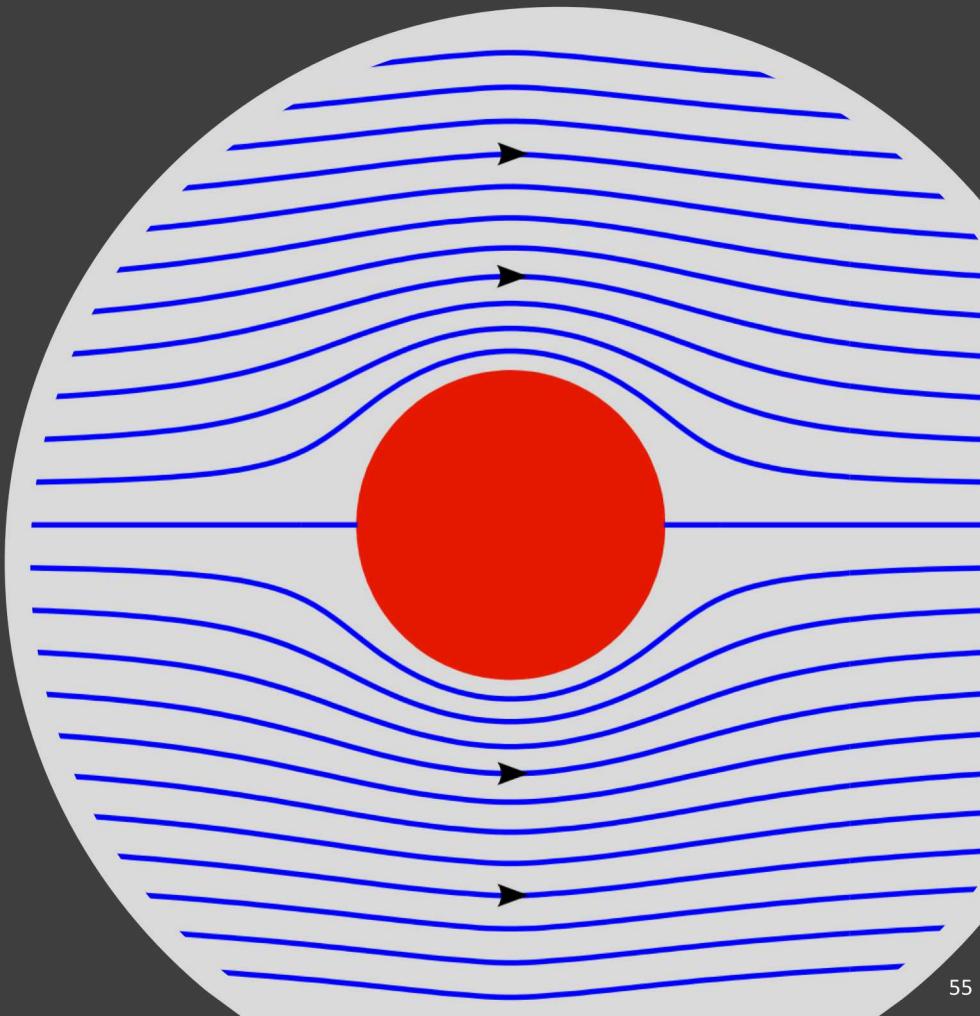
- Analytical, empirical or numerical solutions
- Frequency domain or time domain
- Linear, nonlinear or high-fidelity CFD simulations



Potential flow

Presented by Ryan Coe

# Hydrodynamics Simulation



# Potential flow

$\phi$  Scalar function describing flow kinematics (velocity)

$$u_i = \partial\phi/\partial x_i$$

$$\vec{v} = \nabla\phi$$

$$\nabla^2\phi = \frac{\partial^2\phi}{\partial x^2} + \frac{\partial^2\phi}{\partial y^2} + \frac{\partial^2\phi}{\partial z^2}$$

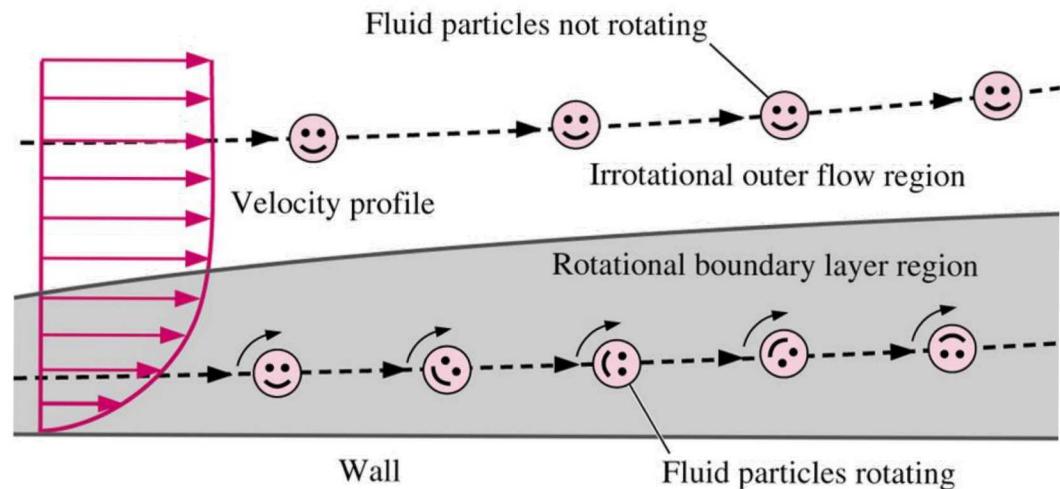
# Potential flow - Irrotational

$$\nabla \times \nabla \phi = 0$$



*True for any scalar*

$$\nabla \times \vec{v} = 0$$



*The internet (source unknown)*

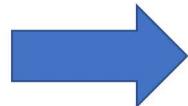
# Potential flow - incompressible

$$\nabla \cdot \vec{v} = 0$$

$$\nabla \cdot \nabla \phi = 0$$

$$\nabla^2 \phi = 0$$

*“continuity”*



**1 equation  
1 unknown**



*Also...*

***pressure is decoupled, so we can solve for it independently!***

$$p = f(\vec{v}) = f(\nabla \phi)$$

# Potential flow – Bernoulli's eq.

$$p = -\rho \left( \frac{\partial \phi}{\partial t} + \frac{1}{2} |\nabla \phi|^2 + \frac{p}{\rho} + gz \right) + F(t)$$



<https://en.wikipedia.org/wiki/Cavitation#/media/File:Cavitating-prop.jpg>



<https://en.wikipedia.org/wiki/Contrail#/media/File:A340-313X.jpg>



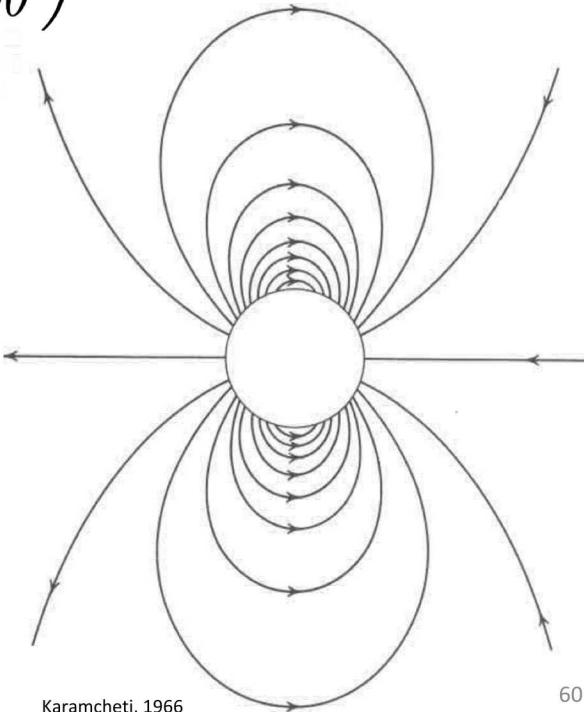
[https://commons.wikimedia.org/wiki/File:Cloud\\_over\\_A340\\_wing.JPG](https://commons.wikimedia.org/wiki/File:Cloud_over_A340_wing.JPG)

# Potential flow – simple problem

$$\nabla^2 \phi = 0 \rightarrow \frac{\partial}{\partial r} \left( r^2 \sin(\theta) \frac{\partial \phi}{\partial r} \right) + \frac{\partial}{\partial \theta} \left( \sin(\theta) \frac{\partial \phi}{\partial \theta} \right) = 0$$

$$\vec{v} = \nabla \phi \rightarrow \frac{\partial \phi}{\partial r} = -U \cos(\theta), \quad \text{on } r = a$$

$$\begin{aligned} \phi(r, \theta, t) &= \frac{U(t) a^3 \cos(\theta)}{2r^2} \\ &= -\frac{a \vec{U}(t) \cdot \vec{r}}{2r^3} \end{aligned}$$



# Potential flow – simple problem

$$p(a, \theta, t) = p_\infty + \frac{\rho}{2} \left( \frac{U^2(t)}{4} (9 \cos^2(\theta) - 5) - a \frac{dU}{dt} \cos(\theta) \right)$$

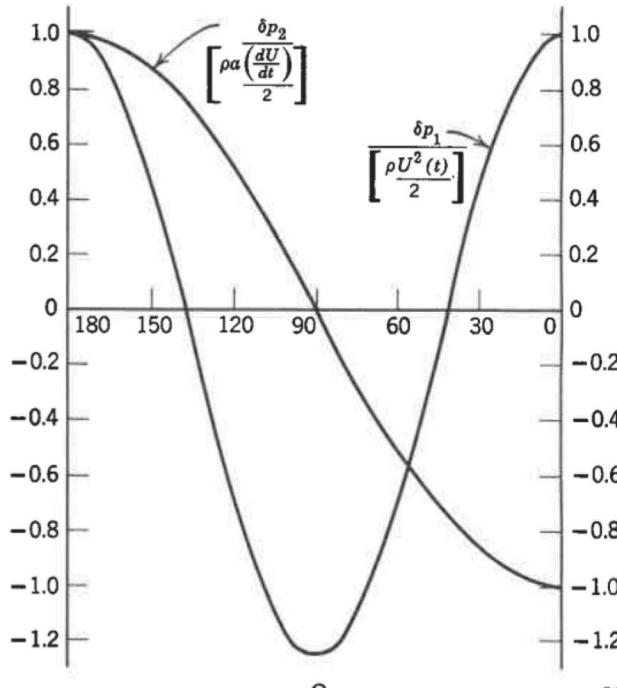
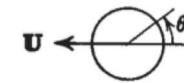
*Steady*                                    *Unsteady*

$$\vec{F} = \frac{\rho a}{2} \frac{dU}{dt} \int \int \hat{n} \cos \theta a^2 \sin \theta d\theta d\varphi$$

$$F_x = -\frac{2}{3} \pi a^3 \rho \frac{dU}{dt}$$



*Only force is caused by acceleration!*



# Potential flow – waves

**kinematic  
boundary  
condition**

at  $z = \eta(t)$

$$\frac{\partial \phi}{\partial z} = \frac{\partial \eta}{\partial t}$$

velocity of a particle at free surface interface

*Vertical velocity or free surface and particles are equal*

**dynamic  
boundary  
condition**

at  $z = \eta(t)$

$$\eta = -\frac{1}{g} \frac{\partial \phi}{\partial t}$$

*Pressure is constant across the free surface interface*

# Potential flow – waves, linearized

*kinematic  
boundary  
condition*

at  $z = 0$

$$\frac{\partial \phi}{\partial z} = \frac{\partial \eta}{\partial t}$$

*dynamic  
boundary  
condition*

at  $z = 0$

$$\eta = -\frac{1}{g} \frac{\partial \phi}{\partial t}$$

*Small waves!*

*(with wavelength much  
larger than amplitude)*



# Potential flow – waves, linear

***differentiating the dynamic boundary condition with time  
and combining with the kinematic boundary condition...***

at  $z = 0$

$$\frac{\partial^2 \phi}{\partial t^2} + g \frac{\partial \phi}{\partial z} = 0$$

# Potential flow – waves

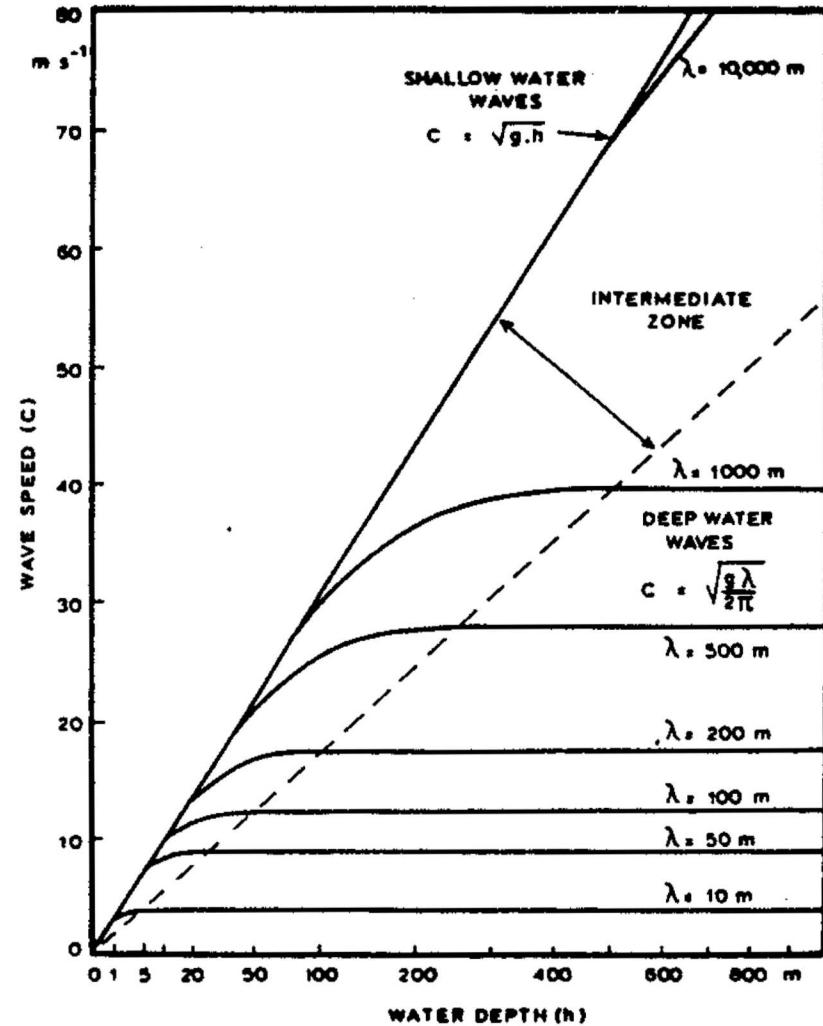
$$\frac{\partial^2 \phi}{\partial t^2} + g \frac{\partial \phi}{\partial z} = 0$$

the “dispersion relation”



$$\omega^2 = gk \tanh kh$$

**Phase speed**  $c = \frac{\omega}{k}$



# Potential flow – waves, energy

*Considering the energy in waves...*

*We can quantify the average energy passing through a plane*

$$P_p = \int_{-h}^0 \rho g z \frac{\partial \phi}{\partial x} dz$$

$$P = P_p + P_k = E c_g$$

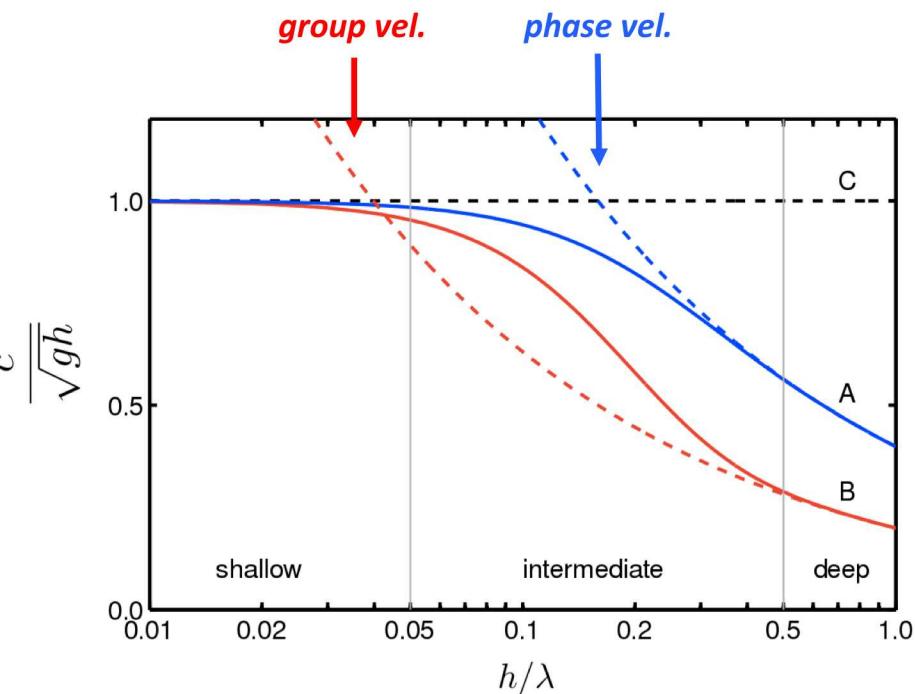
$$P_k = \int_{-h}^0 \frac{1}{2} \rho |\nabla \phi|^2 \frac{\partial \phi}{\partial x} dz$$

$$E = \frac{1}{2} \rho g A^2$$

Energy transport speed  
("group velocity")



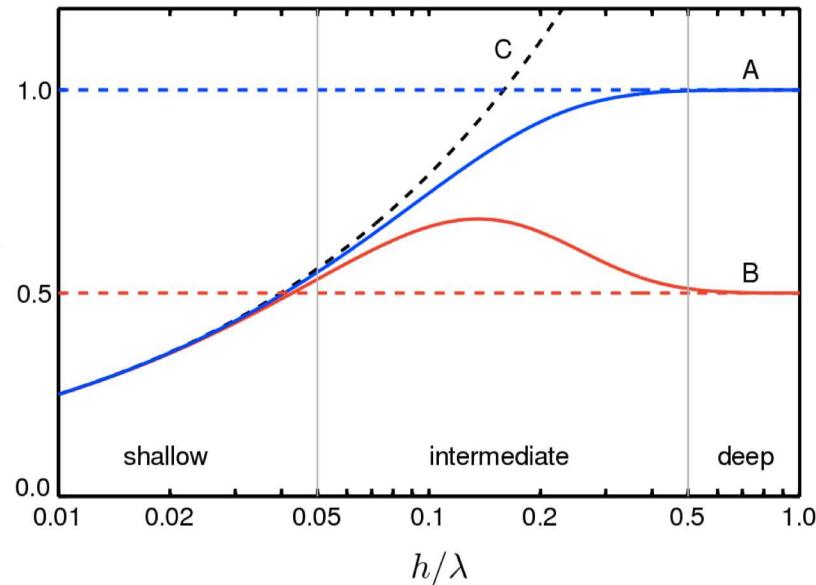
# Potential flow – waves, energy



*Group velocity*

$$c_g = \frac{1}{2} \frac{\omega}{k} \left( 1 + \frac{2kh}{\sinh 2kh} \right)$$

Phase velocity



# Potential flow – waves, energy

*In deep water...*

$$\begin{aligned}c_g &= \frac{1}{2}c \\&= \frac{1}{2}\omega k \\&= \frac{gT}{4\pi}\end{aligned}$$

*Energy in waves travels  
more slowly than the  
crests*

$$P = Ec_g$$

$$P = \frac{1}{8\pi}\rho g^2 A^2 T$$

# Boundary element model

## Linear (frequency domain)



- Small motion around mean position, small steepness
- Linearized boundary conditions
- Harmonic solutions (frequency domain)

## Nonlinear

- LAMP4
- AEGIR
- Xwave

- Various levels of nonlinearity
- Time-domain
- Limited to single solution (no wave breaking)

# Boundary element model - linear

- The free-surface and body-boundary conditions are linearized
- A harmonic time dependence is adopted for  $\phi$

$$\Phi = \operatorname{Re}(\varphi e^{i\omega t})$$

$$\varphi = \varphi_R + \varphi_D$$

$$\varphi_R = i\omega \sum_{j=1}^6 \xi_i \varphi_i$$

$$\varphi_D = \varphi_0 + \varphi_S$$

The linearization of the problem permits decomposition of  $\varphi$  into the ***radiation*** and ***diffraction*** components

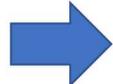


# Boundary element model - linear

***Now our free surface boundary condition simplifies to***

at  $z = 0$

$$\frac{\partial^2 \phi}{\partial t^2} + g \frac{\partial \phi}{\partial z} = 0$$

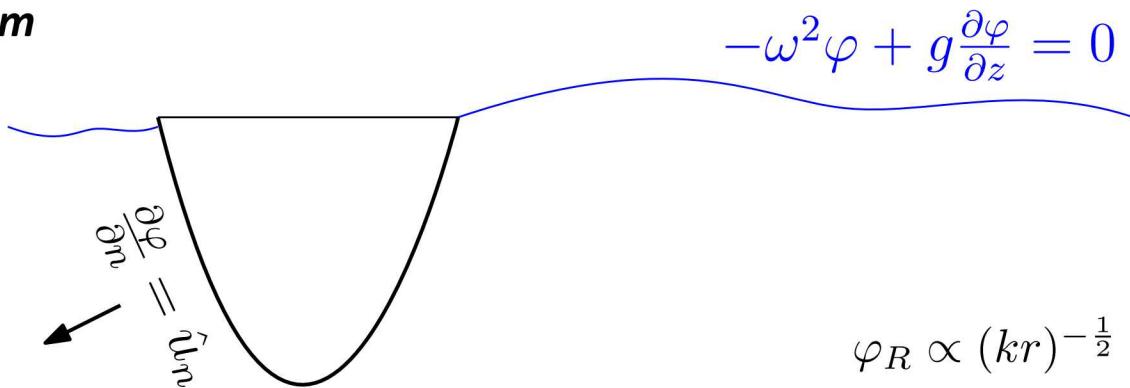


at  $z = 0$

$$-\omega^2 \varphi + g \frac{\partial \varphi}{\partial z} = 0$$

# Boundary element model - linear

**Boundary value problem**



$$\nabla^2 \varphi = 0$$

$$\frac{\partial \varphi}{\partial z} = 0$$

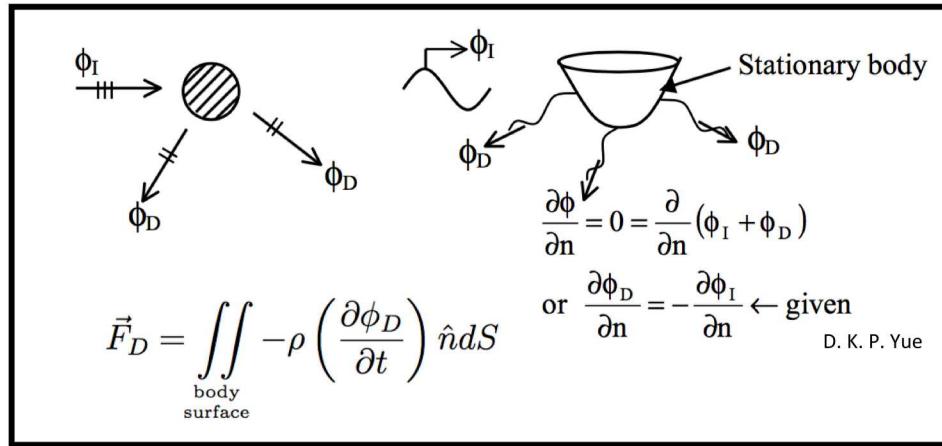
# Boundary element model - linear

## Diffraction

On the *undisturbed* position of the body boundary, the radiation and diffraction potentials are

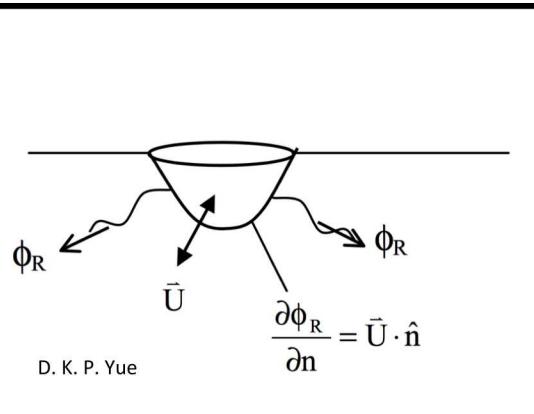
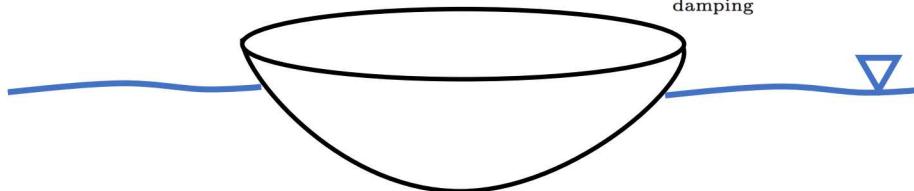
$$\varphi_{jn} = n_j,$$

$$\varphi_{Dn} = 0,$$



## Radiation

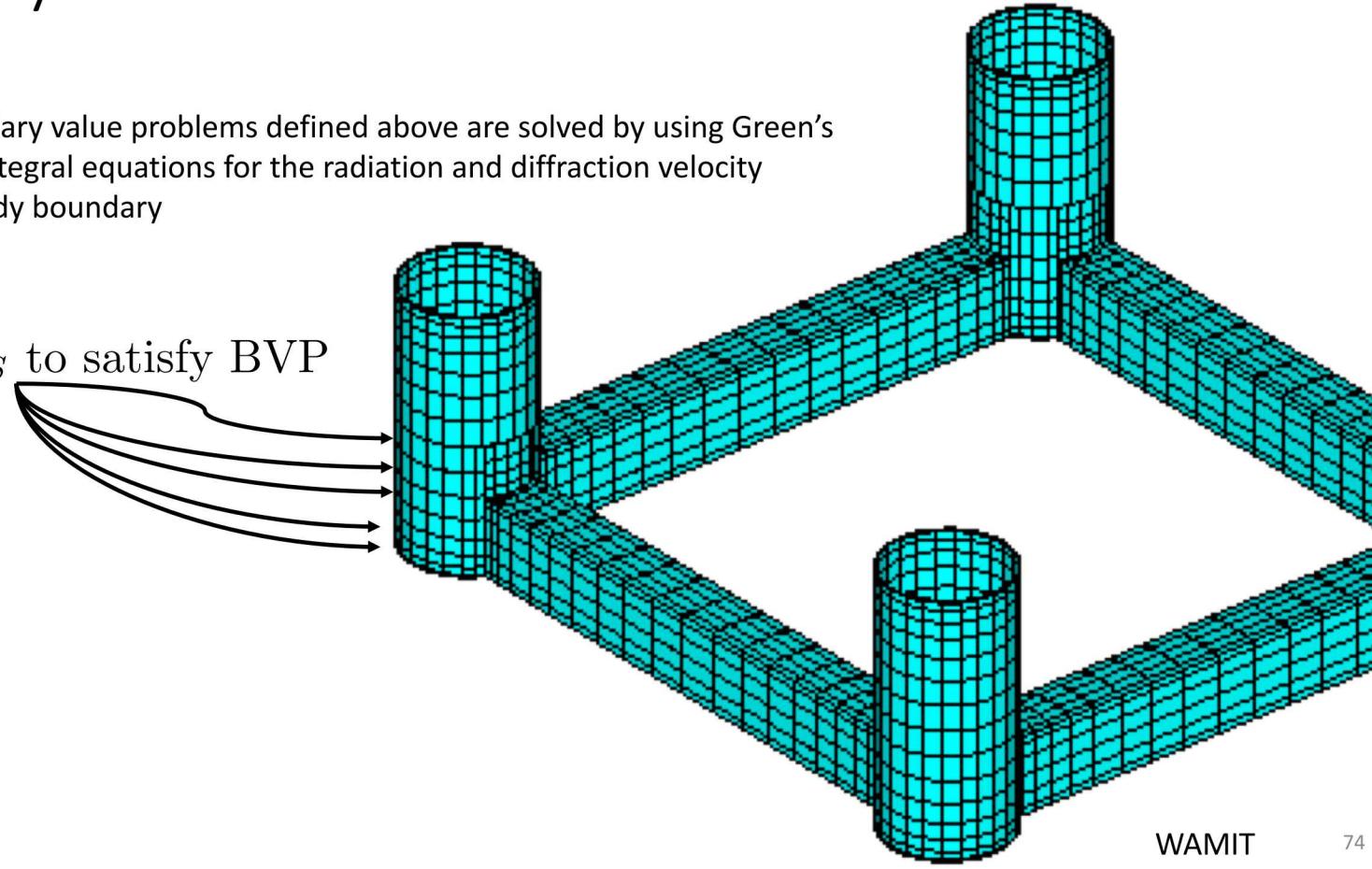
$$\vec{F}_R = \iint_{\text{body surface}} -\rho \left( \frac{\partial \phi_R}{\partial t} \right) \hat{n} dS = - \underbrace{m_{ij}}_{\text{added mass}} \dot{U}_j - \underbrace{d_{ij}}_{\text{wave radiation damping}} U_j$$



# Boundary element model - linear

In WAMIT the boundary value problems defined above are solved by using Green's theorem to derive integral equations for the radiation and diffraction velocity potentials on the body boundary

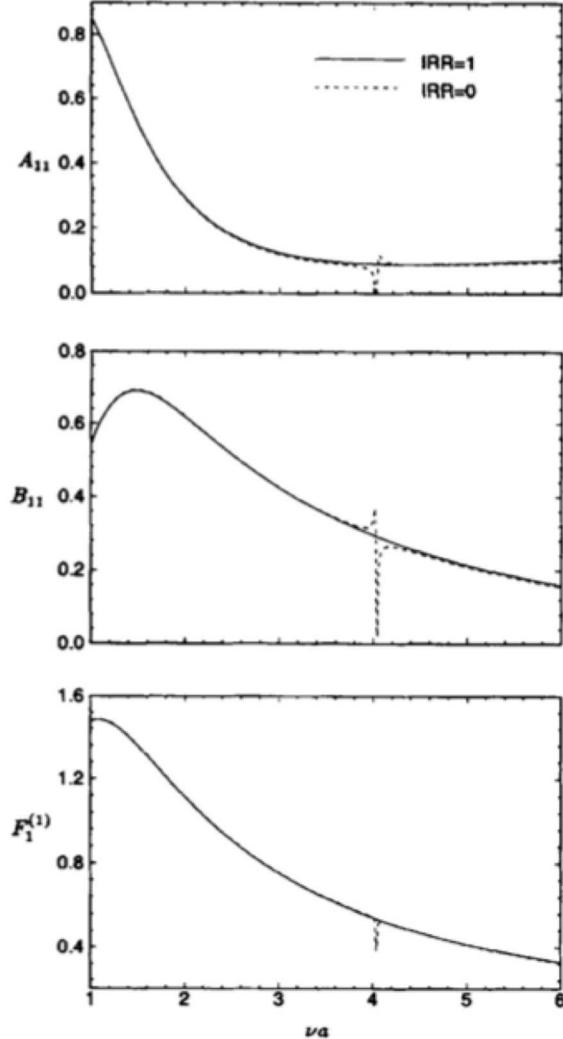
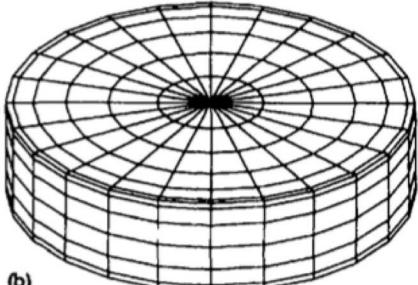
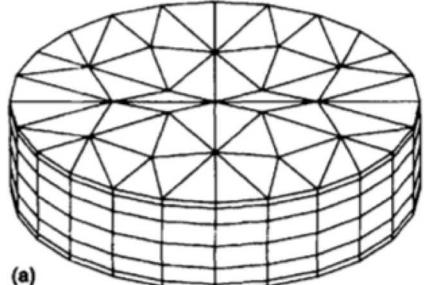
Set  $\varphi_R$  and  $\varphi_S$  to satisfy BVP



# Boundary element model

## - Linear, usage

- Meshing (diminishing returns and dependence on wave length)
- Only mesh the wetted surface below the SWL
- Irregular frequencies
- High order vs low order method





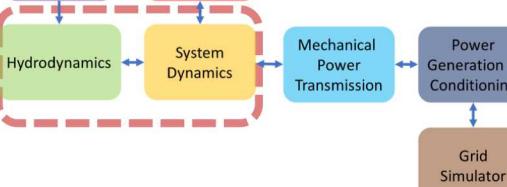
# Linear Hydrodynamic Theory

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Presented by Kelley Ruehl and Ryan Coe

Wave  
Resource

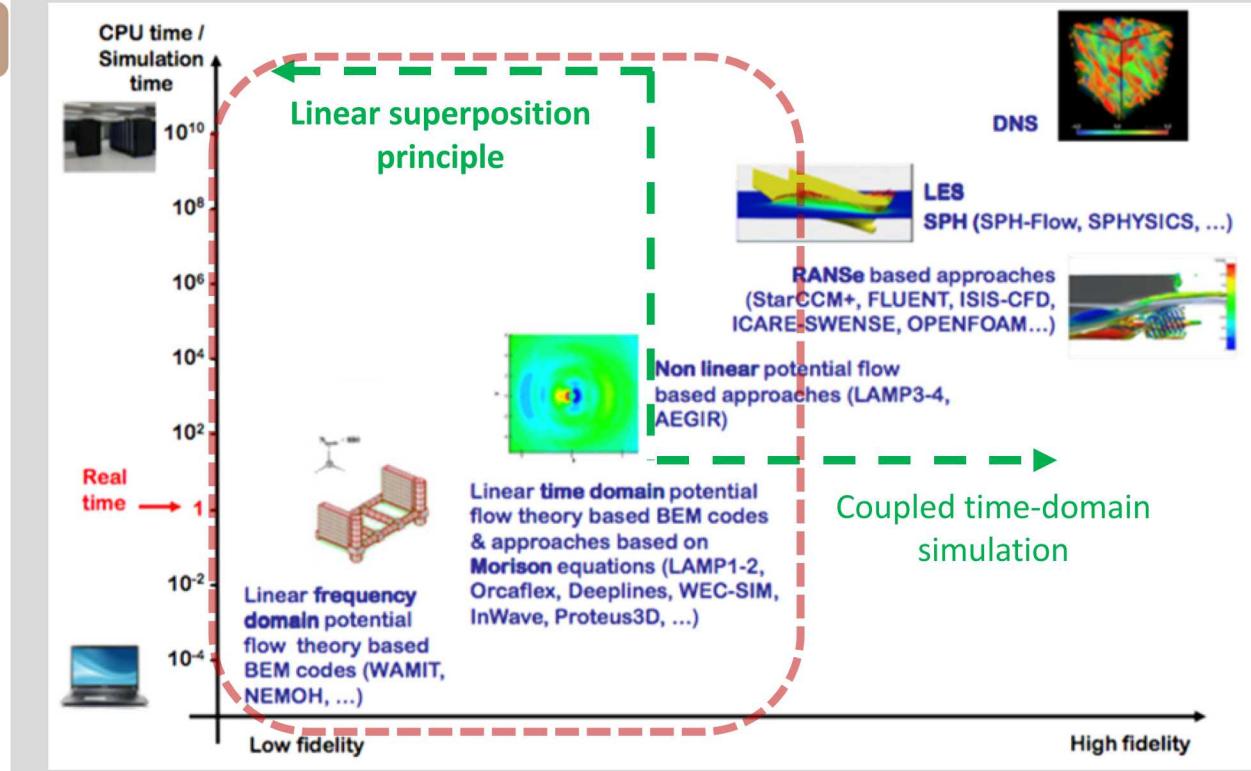
Structural  
Dynamics



## Wave and Floating Body Interaction:

Linear superposition principle  
Vs  
Coupled time-domain  
simulation

# Hydrodynamics and system dynamic model fidelity versus computational time



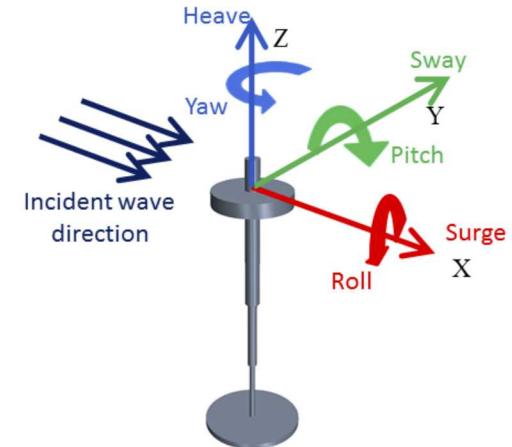
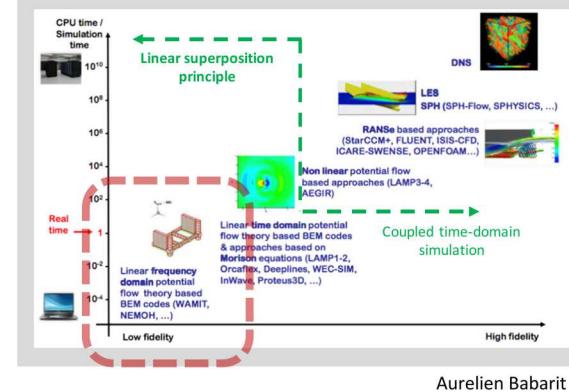
Aurelien Babarit

# WEC Equation of Motion (Frequency-Domain)

$$F_{e,i}(\omega) = \sum_{i=1}^6 X_i(\omega) [-\omega^2(m + A_{ii}) + j\omega(B_{ii} + A_{pto,i}) + k_{ii}]$$

where  $i = 1-6$  for 6DOF

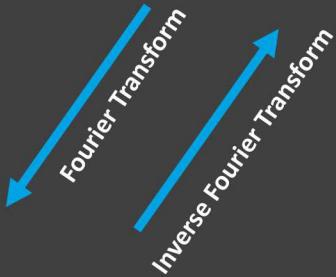
- Hydrodynamics based on BEM solution from Linear Wave Theory (small amplitude motion, inviscid, irrotational flow)
- Linearity assumption, aka linear superposition



# WEC Equation of Motion

## Time-domain

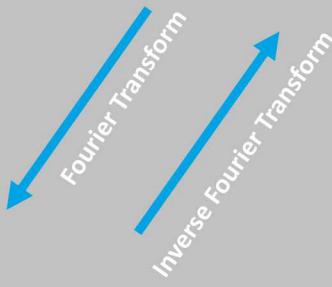
- Hydrodynamics based in linear potential flow, but allows additional of non-linear forcing
- i.e. realistic PTO, real-time control, drag, non-linear hydrostatics, etc



## Frequency-domain

- Linearity assumption, aka linear superposition
- i.e. linear damping for PTO, linear mooring, linear hydrostatics, etc

$$F_{e,i}(t) = (m + A_{\infty,ii})\ddot{X}_i + \int_0^t \dot{X}_i(\tau)k_{r,ii}(t - \tau)d\tau + k_{ii}X_i + F_{pto,i} + B_{v,i}|\dot{X}_i|\dot{X}_i + F_{ext,i}$$



$$F_{e,i}(\omega) = \sum_{i=1}^6 X_i(\omega) [-\omega^2(m + A_{ii}) + j\omega(B_{ii} + A_{pto,i}) + k_{ii}]$$

# WEC Equation of Motion (Time-Domain)

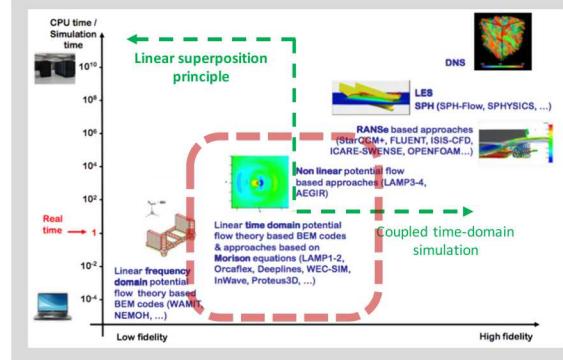
$$F_{e,i}(t) = (m + A_{\infty,ii})\ddot{X}_i + \int_0^t \dot{X}_i(\tau)k_{r,ii}(t - \tau)d\tau + k_{ii}X_i$$

$+ F_{pto,i} + B_{v,i}|\dot{X}_i|\dot{X}_i + F_{ext,i}$

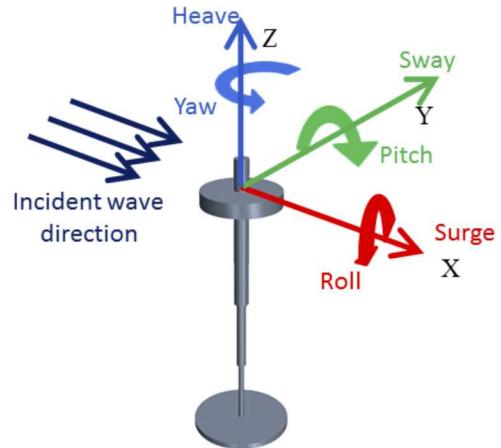
**Non-linearities**

where  $i = 1-6$  for 6DOF

- Hydrodynamics based on BEM solution from Linear Wave Theory (small amplitude motion, inviscid, irrotational flow)
- Quasi-nonlinear, addition of non-linear drag, pto, and external forcing



Aurelien Babarit



# WEC Equation of Motion (Time-Domain)

$$F_{e,i}(t) = (m + A_{\infty,ii})\ddot{X}_i + \int_0^t \dot{X}_i(\tau)k_{r,ii}(t - \tau)d\tau + k_{ii}X_i + F_{pto,i} + B_{v,i}|\dot{X}_i|\dot{X}_i + F_{ext,i}$$

Excitation Force      Added Mass      Radiation Force      Hydrostatic Force      PTO Force      Viscous Drag      External Forcing

- Excitation Force  $F_e(t) = \int_{-\infty}^{\infty} \eta(\tau)f_e(t - \tau)d\tau$

- Radiation Force  $F_r(t) = \int_0^t \dot{x}(\tau)k_r(t - \tau)d\tau$

- Added Mass
- Hydrostatic Force (linear/non-linear)
- PTO Force (linear/non-linear)
- Viscous Damping and Drag (linear/non-linear)
- External Forcing (linear/non-linear mooring, control, end stops, etc)

# Impulse Response Functions (IRFs) in Hydrodynamics

## Radiation Force:

$$F_r(t) = \int_0^t \dot{x}(\tau) k_r(t - \tau) d\tau$$

Radiation IRF

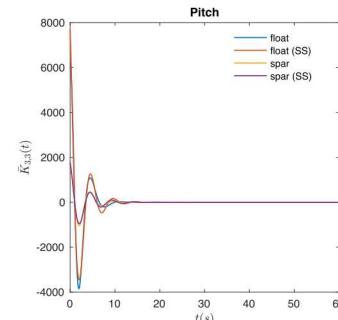
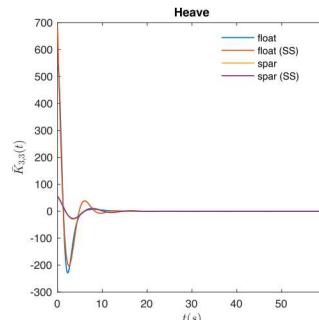
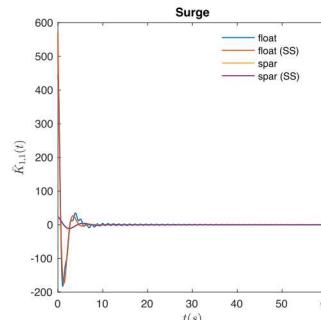
## Radiation IRF:

$$k_r(t) = \frac{2}{\pi} \int_0^{\infty} B(\omega) \cos(\omega t) d\omega$$

Radiation Damping

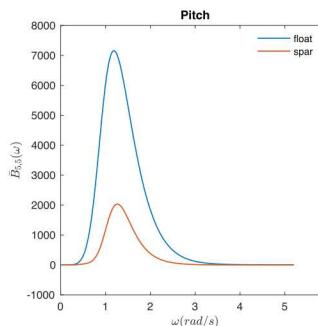
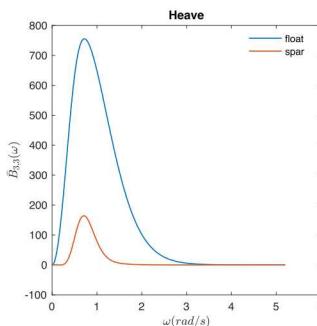
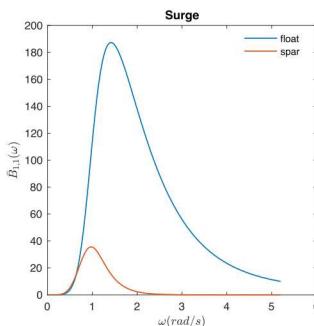
Fourier Transform      Inverse Fourier Transform

Normalized Radiation Impulse Response Functions:  $\tilde{K}_{i,j}(t) = \frac{2}{\pi} \int_0^{\infty} \frac{B_{i,j}(\omega)}{\rho} \cos(\omega t) d\omega$

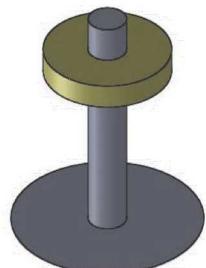


### Notes:

- The IRF should tend towards zero within the specified timeframe. If it does not, attempt to correct this by adjusting the  $\omega$  and  $t$  range and/or step size used in the IRF calculation.
- Only the IRFs for the surge, heave, and pitch DOFs are plotted here. If another DOF is significant to the system, that IRF should also be plotted and verified before proceeding.



Fourier Transform      Inverse Fourier Transform



### Notes:

- $\tilde{B}_{i,j}(\omega)$  should tend towards zero within the specified  $\omega$  range.
- Only  $\tilde{B}_{i,j}(\omega)$  for the surge, heave, and pitch DOFs are plotted here. If another DOF is significant to the system that  $\tilde{B}_{i,j}(\omega)$  should also be plotted and verified before proceeding.

# Impulse Response Functions (IRFs) in Hydrodynamics

$$\text{Normalized Excitation Impulse Response Functions: } \bar{K}_i(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \frac{X_i(\omega, \beta)}{\rho g} e^{i\omega t} d\omega$$

## Excitation Force:

$$F_e(t) = \int_{-\infty}^{\infty} \eta(\tau) f_e(t - \tau) d\tau$$

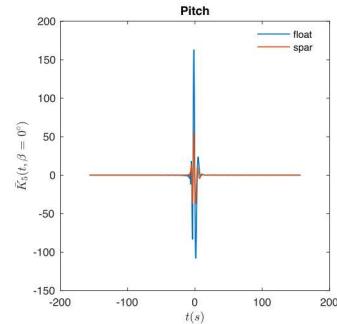
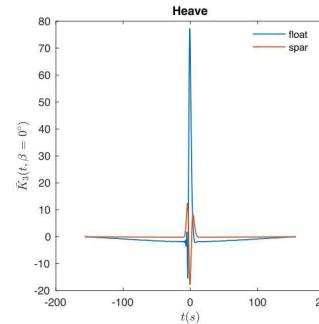
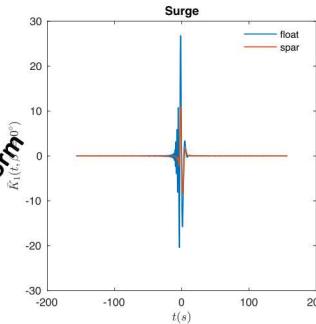
Excitation IRF

## Excitation IRF:

$$k_e(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(i\omega) e^{i\omega t} d\omega$$

Excitation Coefficient

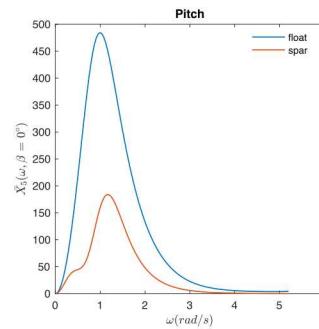
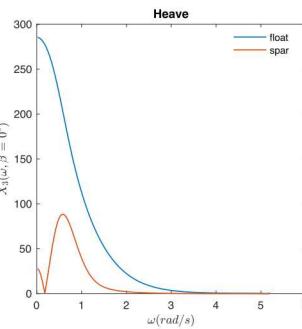
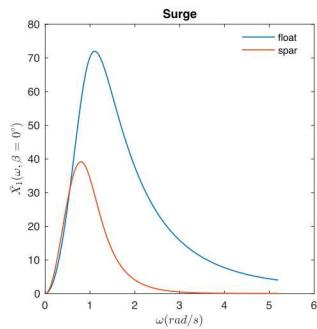
Fourier Transform      Inverse Fourier Transform



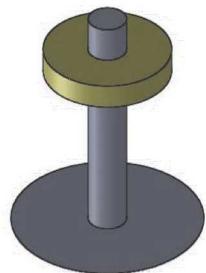
Notes:

- The IRF should tend towards zero within the specified timeframe. If it does not, attempt to correct this by adjusting the  $\omega$  and  $t$  range and/or step size used in the IRF calculation.
- Only the IRFs for the first wave heading, surge, heave, and pitch DOFs are plotted here. If another wave heading or DOF is significant to the system, that IRF should also be plotted and verified before proceeding.

$$\text{Normalized Excitation Force Magnitude: } \bar{X}_i(\omega, \beta) = \frac{X_i(\omega, \beta)}{\rho g}$$



Fourier Transform      Inverse Fourier Transform

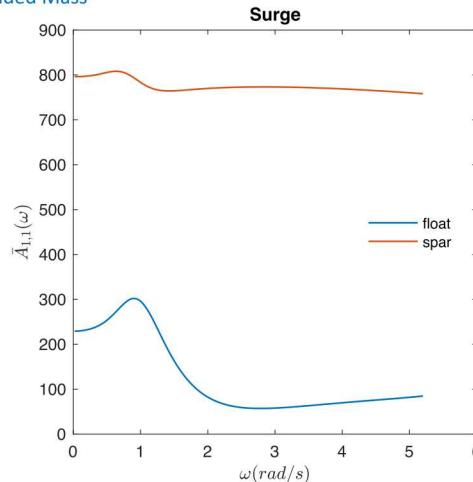


# Impulse Response Functions (IRFs) in Hydrodynamics

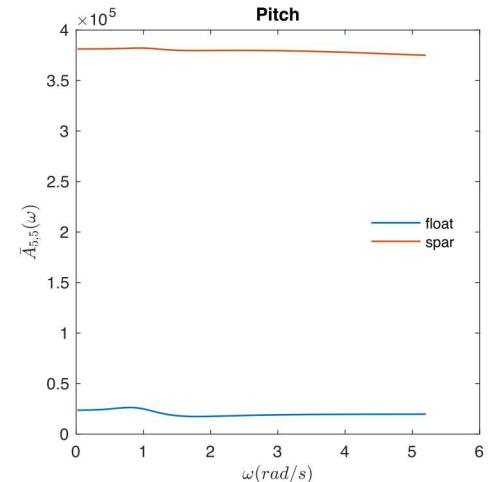
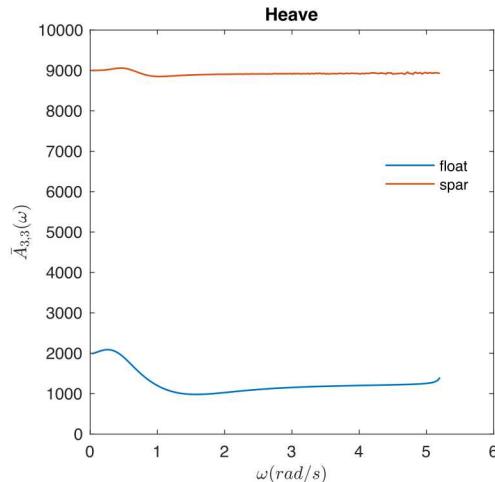
## Infinite Added Mass

$$(m + A_{\infty,ii})\ddot{X}_i$$

Added Mass

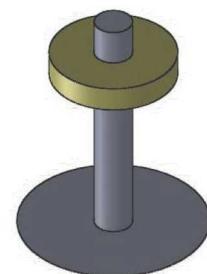


Normalized Added Mass:  $\bar{A}_{i,j}(\omega) = \frac{A_{i,j}(\omega)}{\rho}$



Notes:

- $\bar{A}_{i,j}(\omega)$  should tend towards a constant,  $A_{\infty}$ , within the specified  $\omega$  range.
- Only  $\bar{A}_{i,j}(\omega)$  for the surge, heave, and pitch DOFs are plotted here. If another DOF is significant to the system, that  $\bar{A}_{i,j}(\omega)$  should also be plotted and verified before proceeding.



## 1DOF example

OMAE2018\_shortCourse\_1DofExample.py

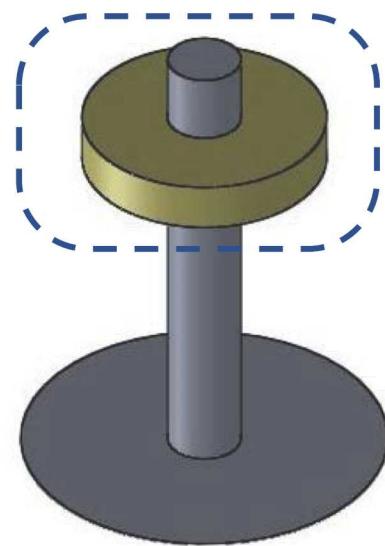
```
95 ax[1].set_xlabel('Period [s]')
96 # Some waves
97
98 w = 2 * np.pi / 10
99 t = np.arange(0, 60, 0.01)
100
101 fig, ax = plt.subplots(nrows=2, sharex=True)
102 ax[0].plot(t, np.real(np.exp(1j * w * t)))
103 ax[1].plot(t, np.real(x(w) * np.exp(1j * w * t)))
104
105 for ai in ax:
106     ai.grid(True)
107 plt.xlim(0, 60)
108 ax[0].set_ylabel('$\eta(t)$')
109 ax[1].set_ylabel('$x(t)$')
110 plt.xlabel('Time [s]')
111
112 # plt.show()
113
114 # Now in the time domain
115
116 rad_A = np.array(f['body1/hydro_coefficients/radiation_damping/state_space/A/components/3_3'].value)
117 rad_B = np.array(f['body1/hydro_coefficients/radiation_damping/state_space/B/components/3_3'].value)
118 rad_C = np.array(f['body1/hydro_coefficients/radiation_damping/state_space/C/components/3_3'].value)
119 rad_D = np.array(f['body1/hydro_coefficients/radiation_damping/state_space/D/components/3_3'].value)
120
121 n = len(rad_B)
122
123 A = np.block([[[-b visc / m, -k / (1 + Ainf/m), -1 * (rad_C) / (1 + Ainf/m)], \
124     [1/m, 0, np.zeros([1, n])], \
125     [rad_B / m, np.zeros([n, 1]), rad_A]]])
126 B = np.block([[1 / (1 + Ainf/m), [0], [np.zeros([n, 1])]]])
127 C = np.zeros([1, n + 2])
128 print A.shape
129 print B.shape
130 print C.shape
131 rad_SS = signal.lti(A, B, C, np.array(0))
132
133 Fet = np.real(Fe(w) * np.exp(1j * w * t))
134
135 tout, yout, xout = signal.lsim(rad_SS, Fet, t)
136 print yout.shape
137 print xout.shape
138 plt.figure()
139 plt.plot(tout, xout[:, 1])
140 plt.grid(True)
141
142 plt.show()
143
```

## 1. Import BEM data

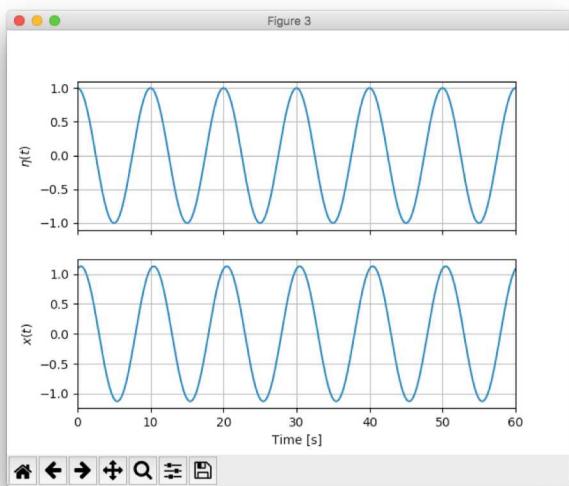
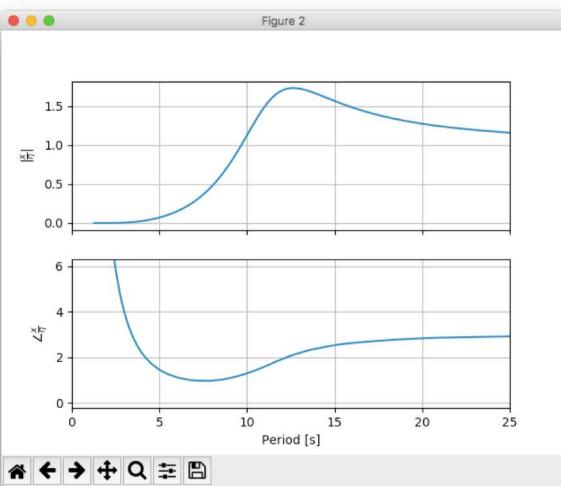
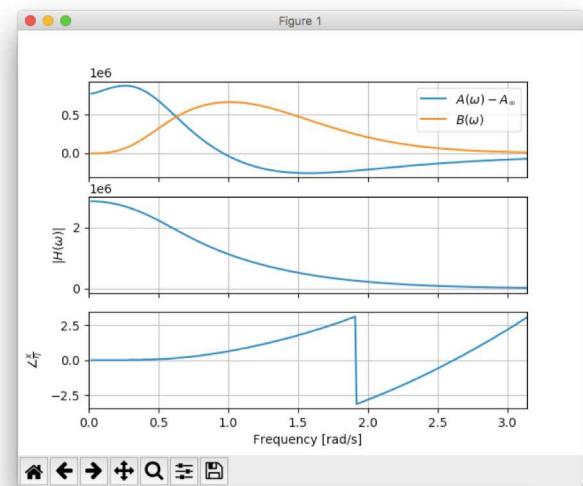
## 2. Check BEM data

### 3. Freq. domain model

## 4. Time domain model



# 1DOF example - FD



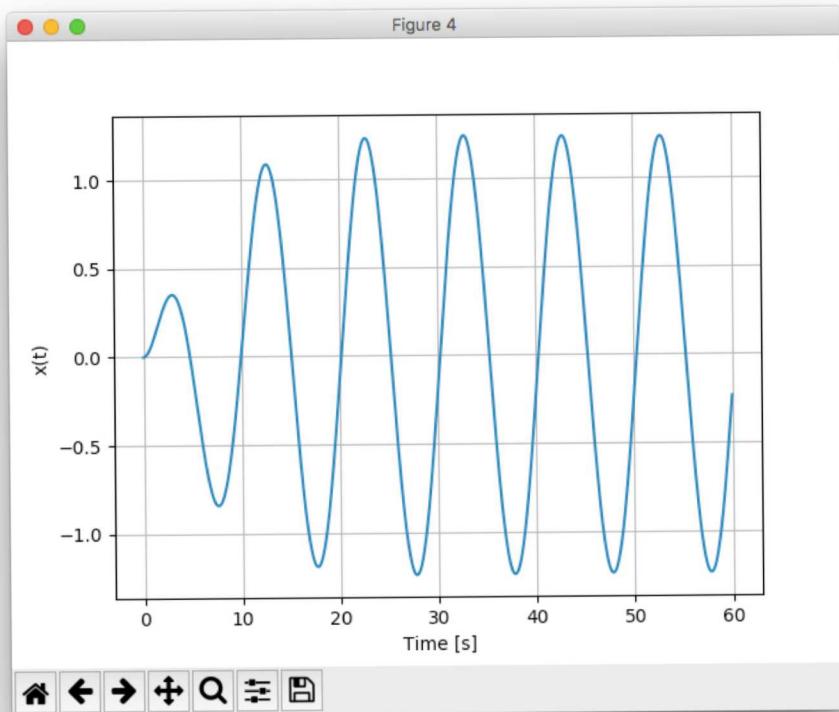
$$Z_i(\omega) = B(\omega) + B_f + i(\omega(M + A(\omega)) - K/\omega)$$

$$\hat{x} = \frac{\hat{F}_e}{\hat{Z}_i}$$

# 1DOF example - TD

$$\begin{aligned}
 \dot{\mathbf{x}}(t) &= \begin{bmatrix} 0 & \frac{-C_b}{1+m_\infty/m_b} & \frac{-\mathbf{C}_r}{1+m_\infty/m_b} \\ 1/m_b & 0 & \mathbf{0}_{1 \times 4} \\ \mathbf{B}_r/m_b & \mathbf{0}_{4 \times 1} & \mathbf{A}_r \end{bmatrix} \mathbf{x}(t) \\
 &+ \begin{bmatrix} \frac{1}{1+m_\infty/m_b} \\ 0 \\ \mathbf{0}_{4 \times 1} \end{bmatrix} F_m(t) + \begin{bmatrix} \frac{1}{1+m_\infty/m_b} \\ 0 \\ \mathbf{0}_{4 \times 1} \end{bmatrix} F_e(t) \\
 &\equiv \mathbf{A} \mathbf{x}(t) + \mathbf{B} F_m(t) + \mathbf{B} F_e(t) \\
 \mathbf{y}(t) &= \mathbf{C} \mathbf{x}(t)
 \end{aligned}$$

$$x_1 = m\dot{\eta}, \quad x_2 = \eta \quad \text{and} \quad [x_3, \dots, x_N]^T = \mathbf{z}$$



# Hydrodynamics Simulation

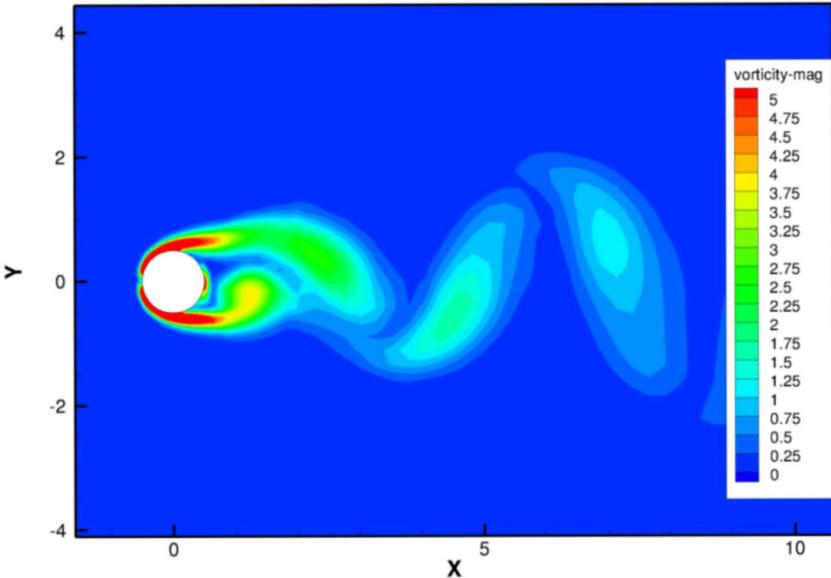
## Viscous flow

Presented by Yi-Hsiang Yu

Continuity:  $\nabla \cdot \vec{v} = 0$

$$\text{Navier-} \underbrace{\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j}}_{\text{substantial derivative}} \text{ Stokes : } \frac{1}{\rho} \frac{\partial \tau_{ij}}{\partial x_j} + \frac{1}{\rho} F_i$$

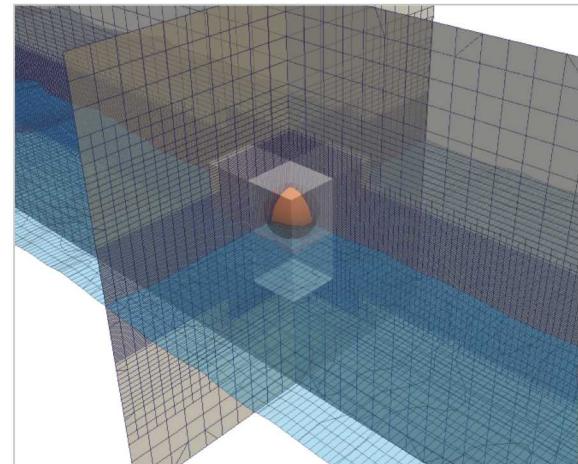
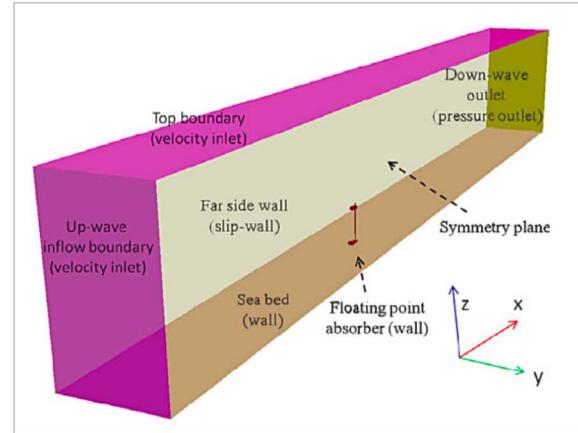
*substantial derivative*  
*(time rate change of cord-sys moving w/ particle)*



# Fundamental CFD

The most fundamental consideration in CFD is how one treats *a continuous fluid in a discretized fashion* on a computer?

- Mesh-based method
  - Finite Difference Method (FDM)
  - Finite Volume Method (FVM)
  - Finite Element Method (FEM): More often used for structure analysis

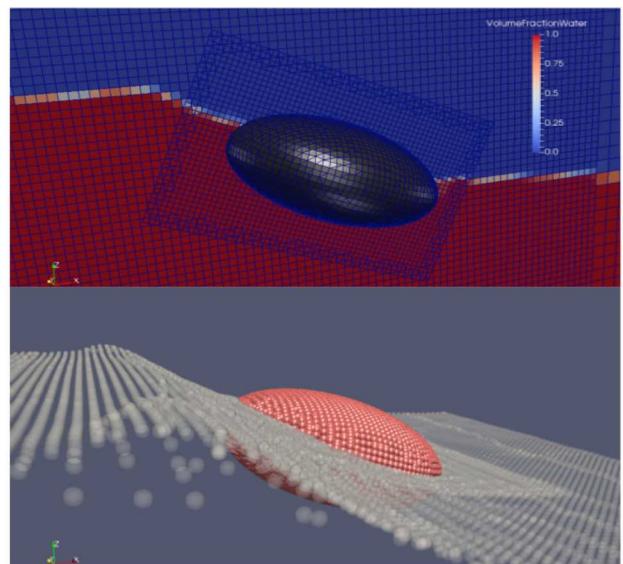
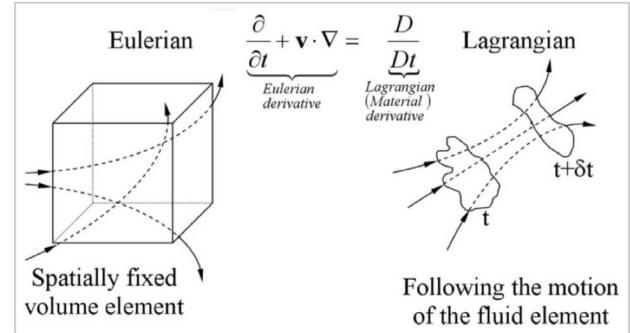


# Fundamental CFD

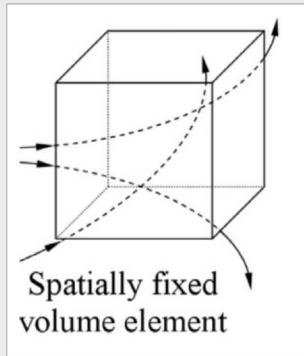
The most fundamental consideration in CFD is how one treats *a continuous fluid in a discretized fashion* on a computer?

- Mesh-free method

Lagrangian (particle-based) method: a mesh free approach that solves the equations of continuity for any continuum media, including both solids and fluids, using a set of particles in which the coordinates move with the particles.



# Finite Volume Method (FVM)



- FVM is the "classical" or standard approach used in commercial software (e.g., ANSYS\_FLUENT, StarCCM+) and open source code (e.g., OpenFOAM).
- FVM discretize the partial differential equations of the N-S equation in the conservative form, which guarantees the conservation of fluxes through a particular control volume.

$$\frac{\partial}{\partial t} \int Q \, dV + \int F \, dA = 0.$$

where  $Q$  is the vector of conserved variables,  $F$  is the vector of fluxes,  $V$  is the cell volume, and  $A$  is the cell surface area.

# Turbulent flow modeling:

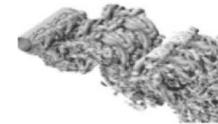
*Turbulence or turbulent flow is a fluid regime characterized by chaotic, random property changes. This includes low momentum diffusion, high momentum convection, and rapid variation of pressure and velocity in space and time.*

*“An ideal model should introduce the minimum amount of complexity while capturing the essence of the relevant physics” (Wilcox, 1993, p. 1)*

DNS



LES



RANS



High

Low

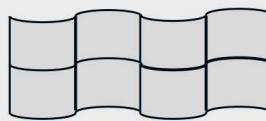
Resolved

Physics

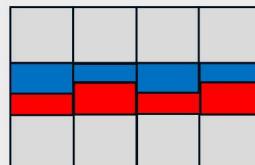
Computational Cost

Modeled

# Modeling of Free-Surface Flows



*3D top view*



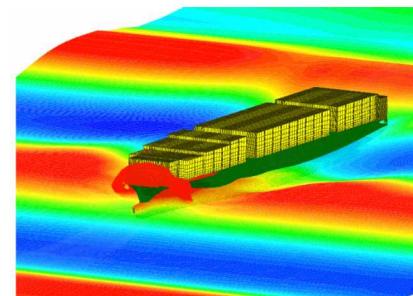
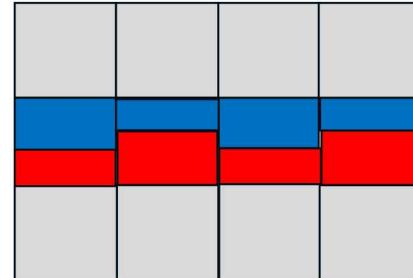
*Side view*

- Free-surface flows are driven by gravity and surface tension
- Majority of hydrodynamic problems do not require a sophisticated model for air (can be modelled as ideal gas)
- FVM are based on either
  - Interface-tracking methods
    - Moving, boundary-fitted grid
  - Interface-capturing methods
    - Fixed grid, volume share dynamics based on transport equation

# Interface-Capturing Method

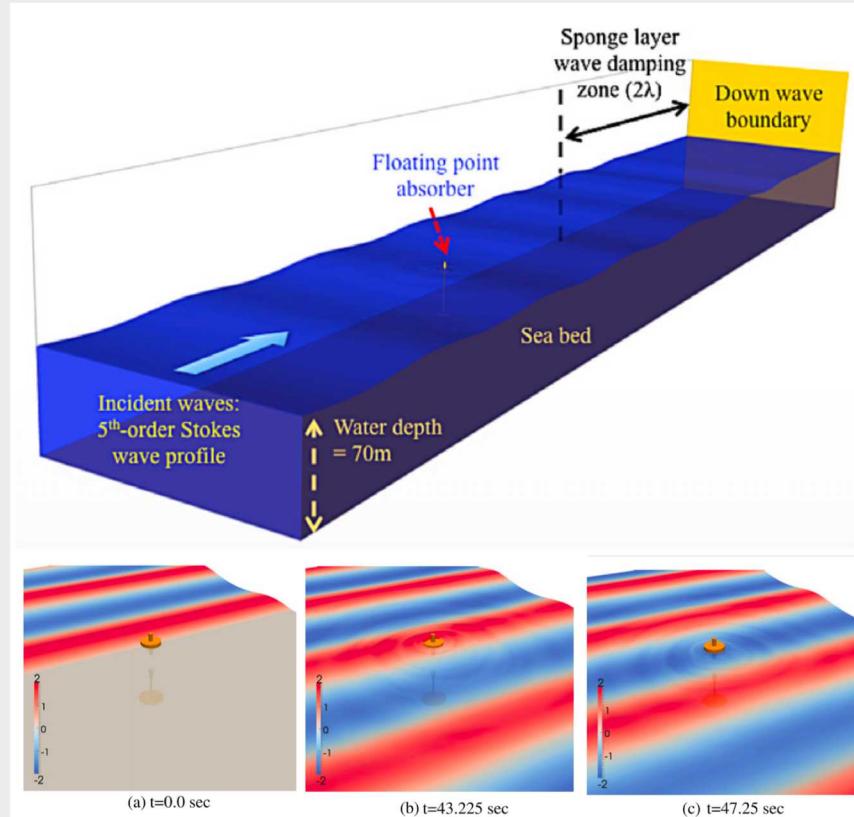
- Suitable for complex geometries, multi-phase flows
- The  $\alpha$ -equation is coupled to the Navier-Stokes equations; thus accounts for **nonlinear and viscous free-surface effects**

$$\frac{\partial}{\partial t} \int_V \alpha \, dV + \int_S \alpha \mathbf{v} \cdot \mathbf{n} \, dS = 0$$



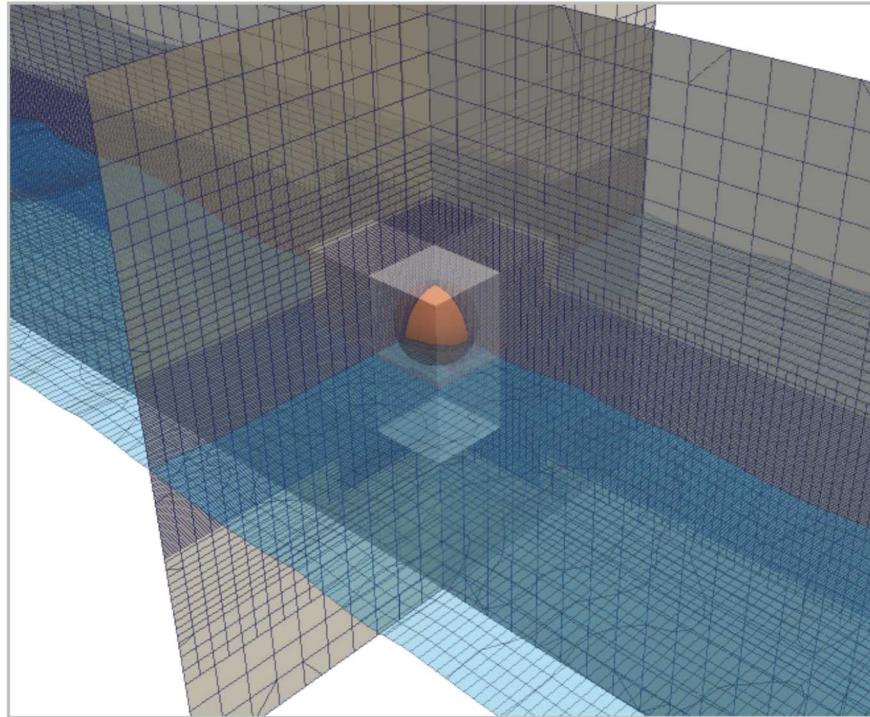
# Numerical Wave Tank

Just like “physical” wave tank, waves are generated on one side and need to be absorbed on the other end.



# Numerical Wave Tank

- Capture wave propagation and the dynamic interaction between waves and the floating body
- Space and temporal resolutions are function of  $H$ ,  $T$  and  $\lambda$
- Like experimental tank test, it is recommended to resolve the space and temporal resolutions that is needed without the present of the device

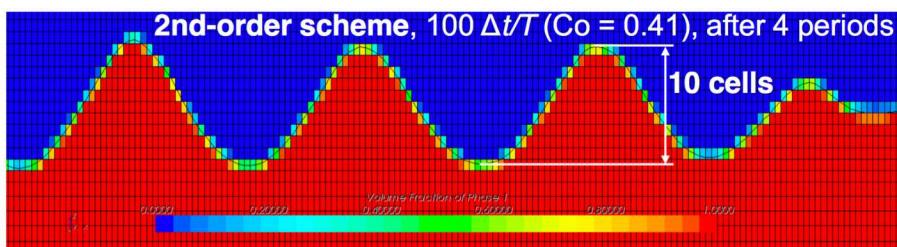
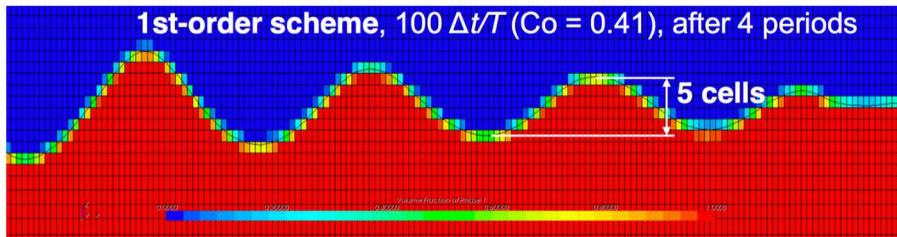


# Numerical Wave Tank

## With Insufficient Resolution

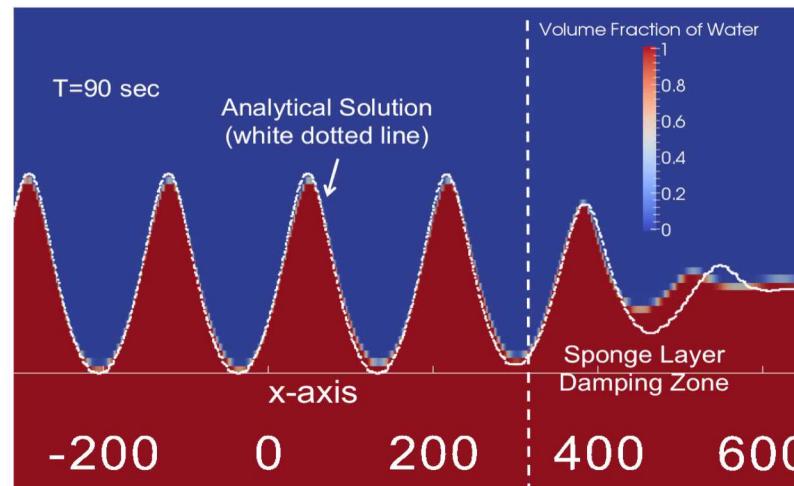
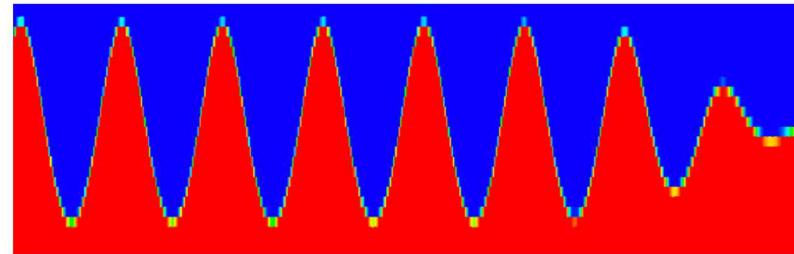
- Induced by numerical damping
- Wave amplitude decays as waves propagate through the domain
- Wave propagation speed will be inaccurate
- Unrealistic wave breaking

Example:  $H=5\text{m}$  and  $T=8\text{sec}$  and wave damping zone was applied over the last 100 m 41 cells per wave length, 11.5 cells per wave height ( $\Delta x = 2.5 \text{ m}$ ,  $\Delta z = 0.5 \text{ m}$ )



# Numerical Wave Tank

- Wave train initialized using Stokes 5th-order theory
- Damping Zone:  $1 \sim 2 \lambda$
- $\Delta z > H/20$ ;  $\Delta x > \lambda/80$
- Second-order time integration scheme
- Higher space and temporal resolutions maybe needed for larger and steeper waves and longer domain/duration cases



Operational Waves



Extreme Waves



# Hydrodynamics Simulation

It is all about using the right tool for what we want to investigate

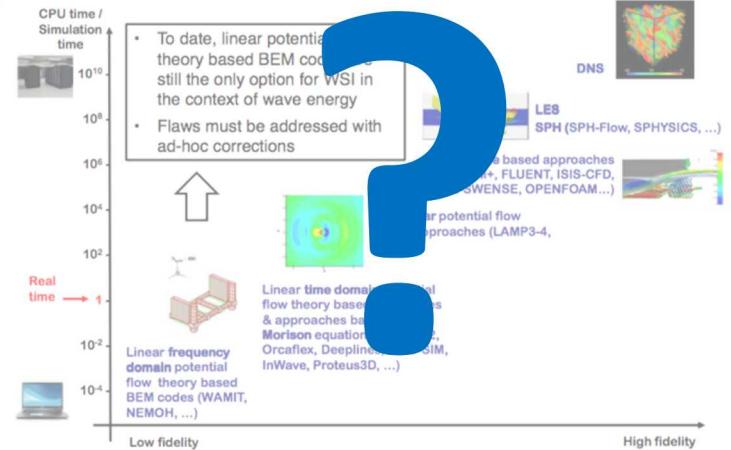
# Hydrodynamics Simulation

## Typically:

- Linear model -> System design and optimization
- High-fidelity model -> Extreme condition modeling and viscous drag coefficient calculation

## However:

- What numerical model to use depends on the complexity of the fundamental physics
- Don't use a sledgehammer to crack a nut



Lunch (12:30 ~ 13:30)

# Agenda

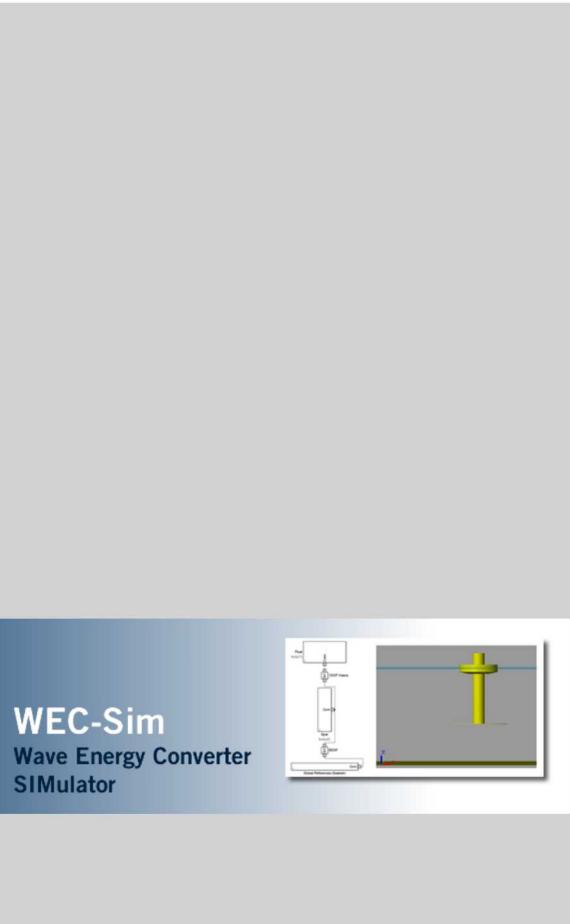
1. Introduction
2. WEC fundamentals
3. Ocean waves
4. Numerical methods
5. Experimental methods
6. WEC control
7. Extreme response and fatigue

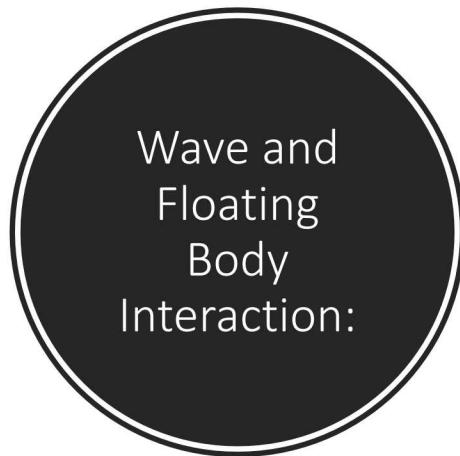
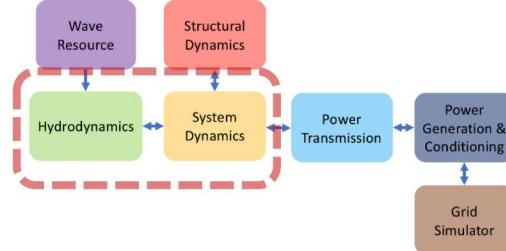
# Numerical Methods

## WEC-Sim

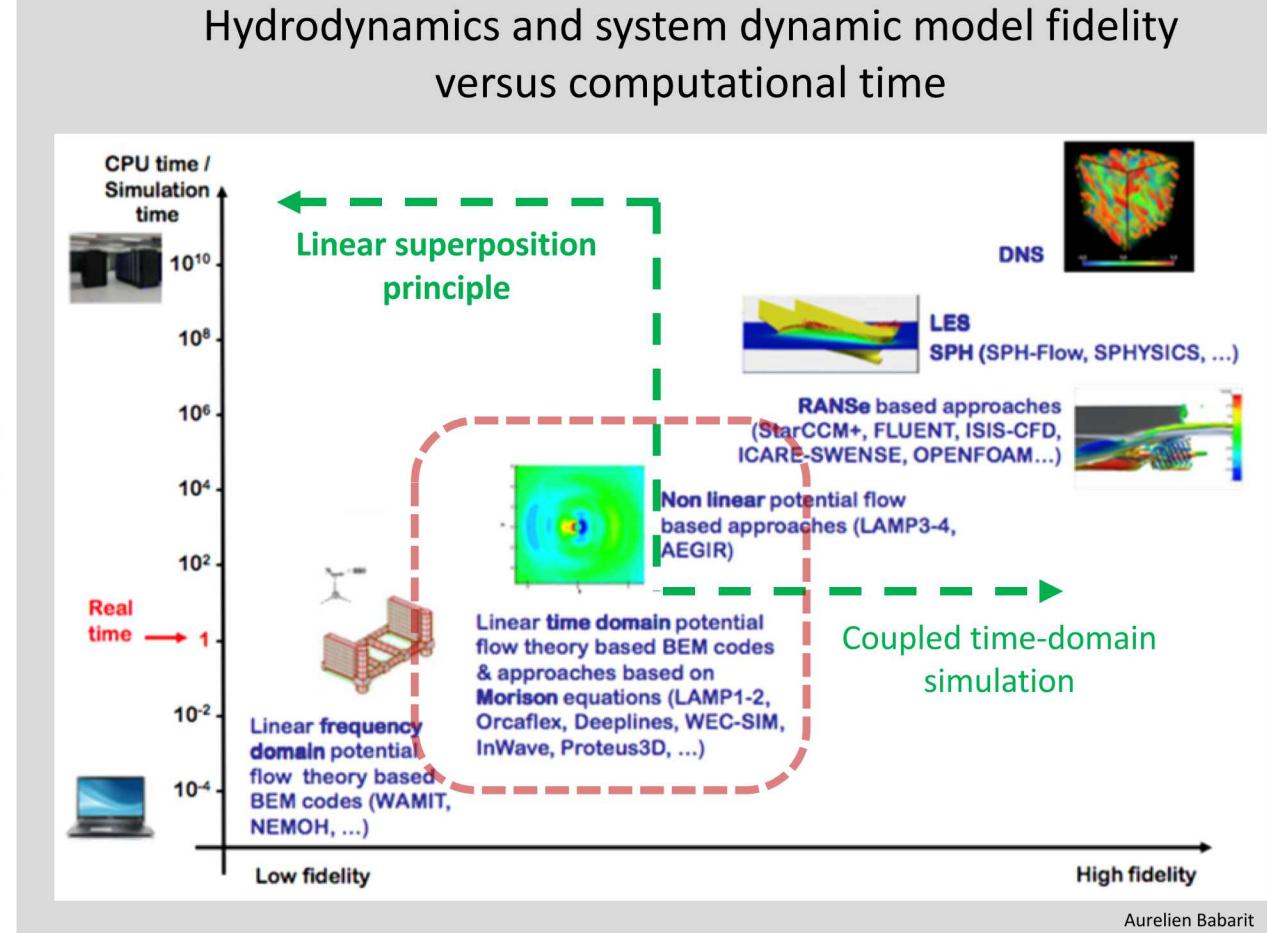
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Presented by Kelley Ruehl and Yi-Hsiang Yu



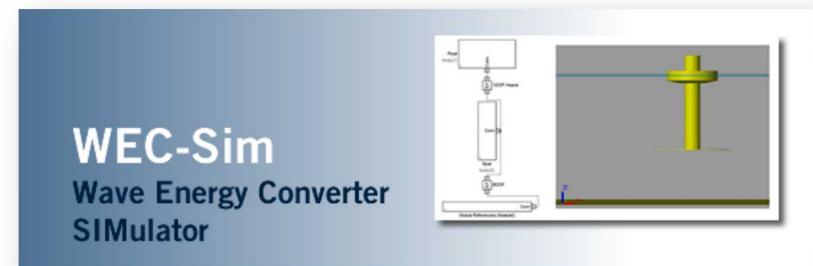


Linear superposition principle  
Vs  
Coupled time-domain simulation



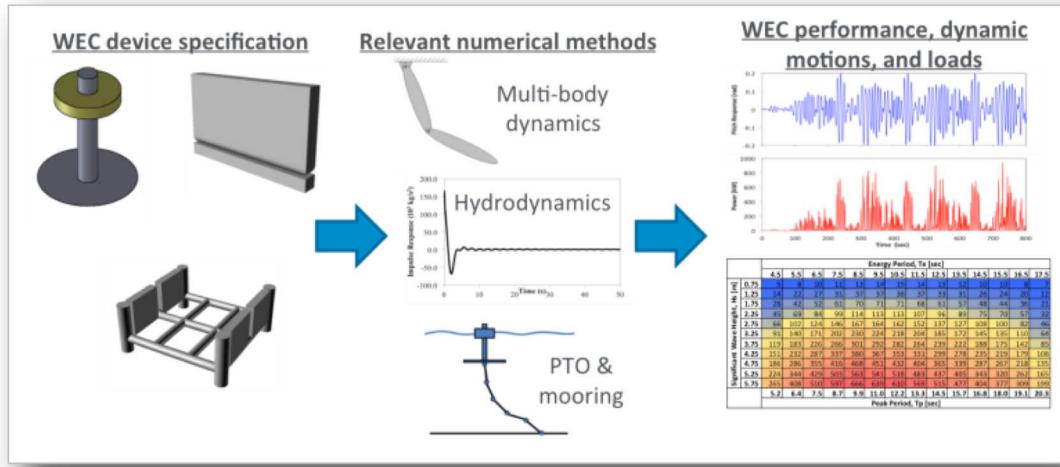
# What is WEC-Sim?

- WEC-Sim (Wave Energy Converter Simulator)
  - Simulates wave energy converter dynamics in operational waves
  - Time-domain rigid body equation of motion solver based on Cummins' formulation
  - Open source code developed in MATLAB/SIMULINK
  - Joint NREL/Sandia project funded by the US Department of Energy
  - First Release: v1.0 in June 2014
  - Current Release: v3.0 in December 2017



# Why use WEC-Sim?

- WEC-Sim has the ability to model the dynamics of devices that are comprised of rigid bodies, power-take-off (PTO) systems, and mooring systems.
- WEC-Sim uses hydrodynamic coefficients derived from frequency-domain boundary element (BEM) simulations to model the relevant hydrodynamics.
- Time-domain simulations are performed by solving the governing WEC equations of motion in 6 degrees-of-freedom.



# WEC-Sim Theory

- Dynamics simulated by solving time-domain equation of motion (Cummins, 1962)

$$m\ddot{x}(t) = f_{hs}(t) + f_{ex}(t) + f_{rad}(t) + f_v(t) + f_{pto}(t) + f_m(t)$$

Hydrostatic restoring force

Wave excitation & diffraction force (from BEM simulations)

Radiation force: added mass and radiation damping (from BEM simulations)

Viscous force

Power take-off force

Mooring force

- Use radiation and diffraction method and calculate the hydrodynamic forces from frequency-domain Boundary Element Method (BEM)

$$f_{rad}(t) = -A_\infty \ddot{X} - \int_0^t K(t-\tau) \dot{X}(\tau) d\tau$$

BEM

$$f_{ex}(t) = \Re \left[ R_f F_X(\omega_r) e^{i(\omega_r t + \phi)} \int_0^\infty \sqrt{2S(\omega_r)} d\omega_r \right]$$

BEM

$$= \int_{-\infty}^{\infty} \eta(\tau) f_e(t-\tau) d\tau$$

BEM

# WEC-Sim Software Requirements

- **CAD** (Computer-aided design), e.g. Rhinoceros, SolidWorks, ANSYS, etc.
- **BEM** (Boundary Element Method), e.g. WAMIT, NEMOH, AQWA
- **WEC-Sim** (Wave Energy Converter Simulator) and **BEMIO** (Boundary Element Method Input/Output)
  - <http://wec-sim.github.io/WEC-Sim/>
  - Requires MATLAB (R2015b), Simulink, Simscape and SimMechanics (Simscape Multibody in 2016a)

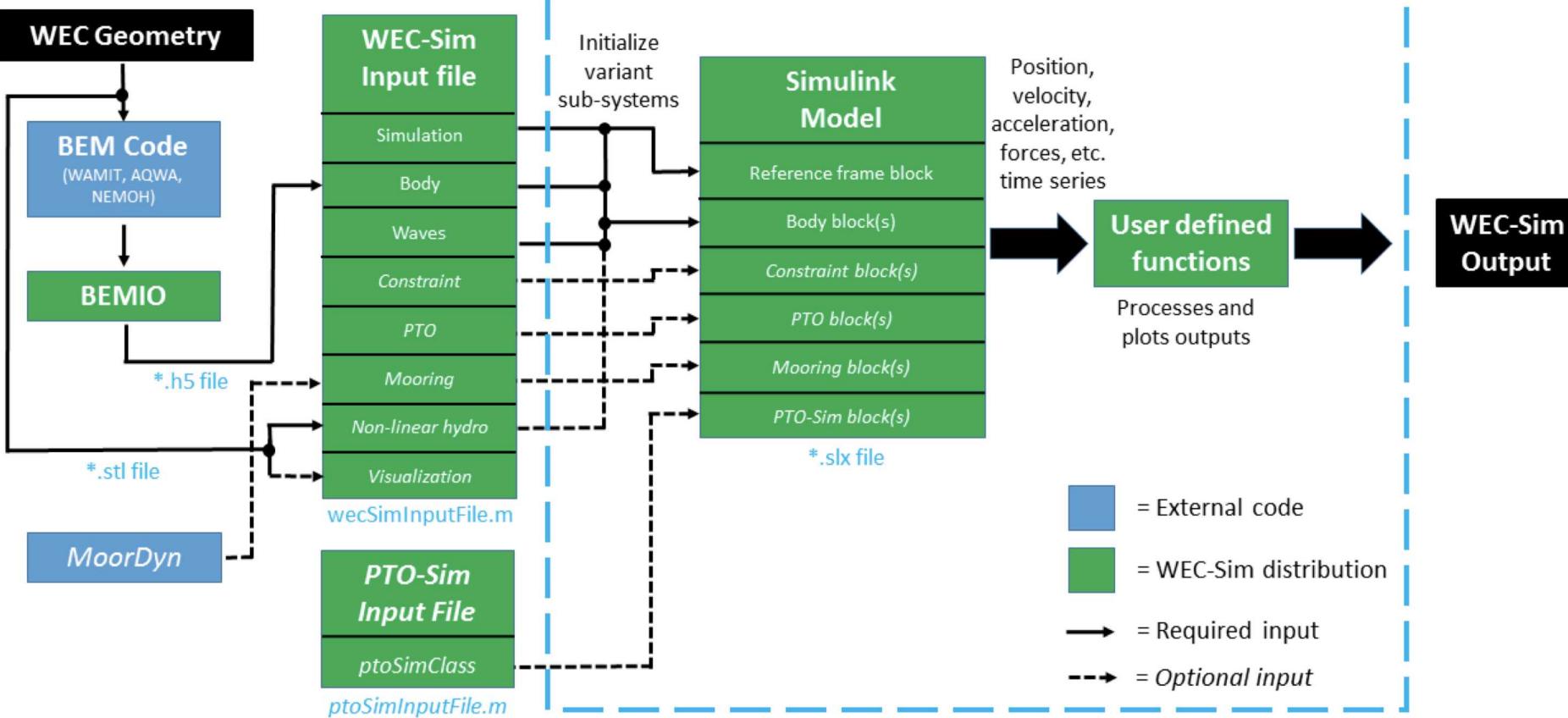


- **ParaView** (Optional)
  - <http://www.paraview.org/>
  - Optional, for additional visualization and analysis capabilities

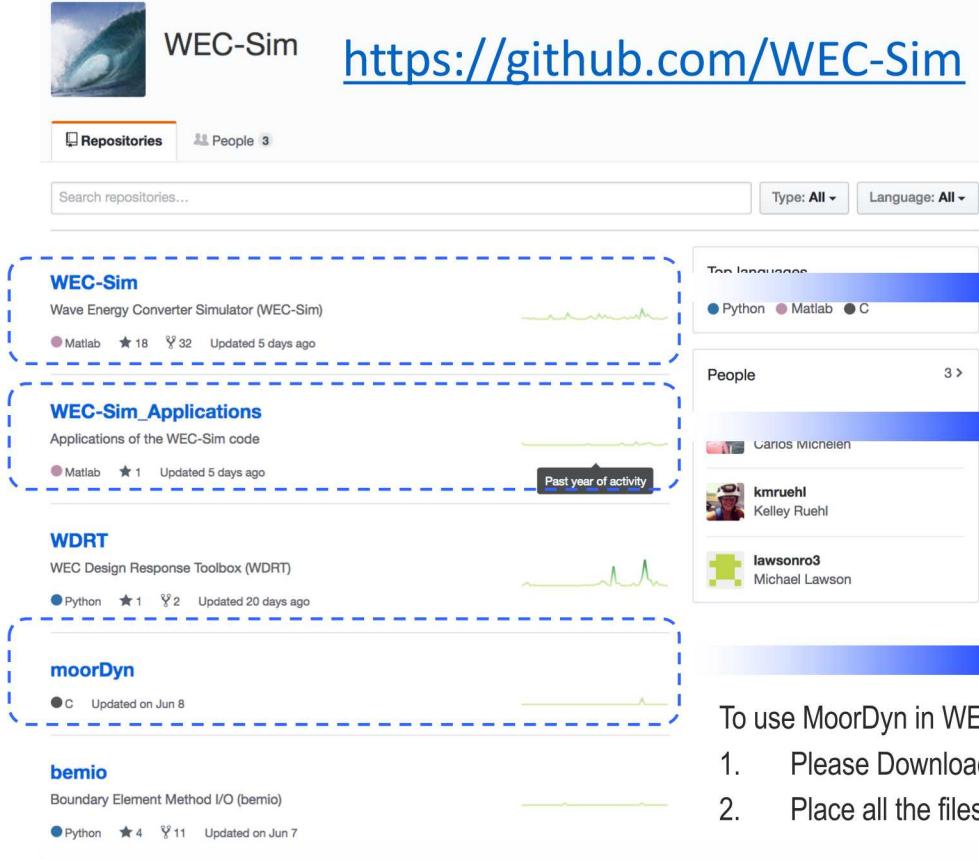


# wecSim.m

Reads input file, runs Simulink model, calls user-defined functions for output processing



# WEC-Sim (GitHub) Repositories



WEC-Sim <https://github.com/WEC-Sim>

Repositories People 3

Search repositories... Type: All Language: All

**WEC-Sim**  
Wave Energy Converter Simulator (WEC-Sim)  
Matlab 18 32 Updated 5 days ago

**WEC-Sim\_Applications**  
Applications of the WEC-Sim code  
Matlab 1 Updated 5 days ago

**WDRT**  
WEC Design Response Toolbox (WDRT)  
Python 1 2 Updated 20 days ago

**moorDyn**  
C Updated on Jun 8

**bemo**  
Boundary Element Method I/O (bemo)  
Python 4 11 Updated on Jun 7

Top languages: Python, Matlab, C

People: 3 >

Carlos Michelen  
kmruehl  
lawsonro3

Past year of activity

WEC-Sim Source Code

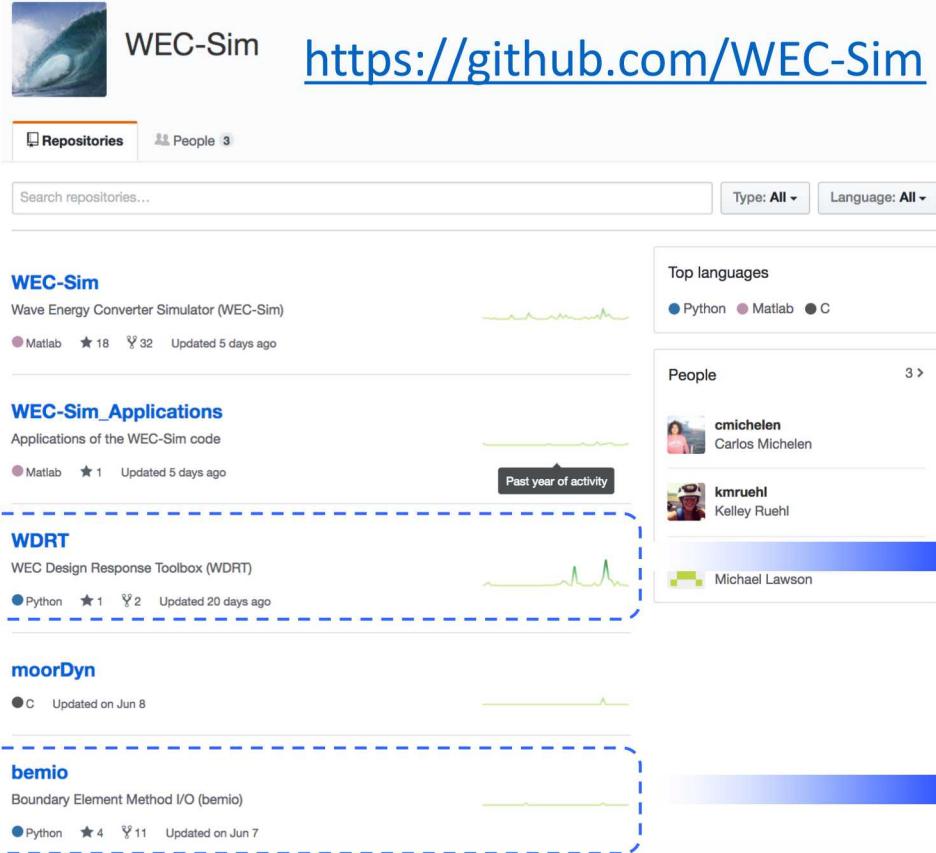
Additional Applications

Complied MoorDyn Library

To use MoorDyn in WEC-Sim,

1. Please Download MoorDyn from the repo <https://github.com/WEC-Sim/moorDyn>
2. Place all the files and folders under WEC-Sim/source/functions/moorDyn folder

# WEC-Sim (GitHub) Repositories



WEC-Sim <https://github.com/WEC-Sim>

WEC-Sim

WEC-Sim

WEC-Sim\_Applications

WDRT

moorDyn

bemio

Top languages

Python Matlab C

People

cmichelen

kmruehl

Michael Lawson

Past year of activity

<http://wec-sim.github.io/WDRT/>

WDRT was developed by Sandia National Laboratories and the National Renewable Energy Laboratory (NREL) to provide extreme response and fatigue analysis tools, specifically for design analysis of ocean structures such as WECs.

**WEC Design Response Toolbox**

**Old Python based BEMIO**

# Documentation

<http://wec-sim.github.io/WEC-Sim/>



The screenshot shows the WEC-Sim documentation website. The left sidebar contains links to 'Getting Started', 'Examples', 'Theory', 'Code Structure', 'Advanced Features', 'Webinars', 'License', 'Publications', 'Release Notes', and 'Contact Us'. The main content area has a header 'Docs » WEC-Sim (Wave Energy Converter SIMulator)' and a 'View page source' link. Below the header is a 3D rendering of a yellow vertical-axis wave energy converter (WEC) in the water, with a schematic diagram of its internal components to its left. The title 'WEC-Sim' is prominently displayed, followed by the subtitle 'Wave Energy Converter SIMulator'. A detailed description of the tool follows, mentioning its development in MATLAB/SIMULINK, its use of Simscape Multibody, and its ability to model rigid bodies, power-take-off systems, and mooring systems. It is noted that simulations are performed in the time-domain using 6 degrees-of-freedom equations of motion. The project is funded by the U.S. Department of Energy's Water Power Technologies Office and is a collaboration between NREL and Sandia National Laboratories.

Docs » WEC-Sim (Wave Energy Converter SIMulator) [View page source](#)

## WEC-Sim

### Wave Energy Converter SIMulator

**WEC-Sim (Wave Energy Converter SIMulator)**

WEC-Sim (Wave Energy Converter SIMulator) is an open-source wave energy converter simulation tool. The code is developed in MATLAB/SIMULINK using the multi-body dynamics solver Simscape Multibody. WEC-Sim has the ability to model devices that are comprised of rigid bodies, power-take-off systems, and mooring systems. Simulations are performed in the time-domain by solving the governing WEC equations of motion in 6 degrees-of-freedom. The WEC-Sim project is funded by the U.S. Department of Energy's Water Power Technologies Office and the code development effort is a collaboration between the National Renewable Energy Laboratory (NREL) and Sandia National Laboratories (Sandia).

# WEC-Sim Forum

<https://github.com/WEC-Sim/WEC-Sim/issues>

WEC-Sim / WEC-Sim

Watch 19 Star 18 Fork 33

Code Issues 2 Pull requests 2 Projects 7 Insights

is:issue is:open Labels Milestones New issue

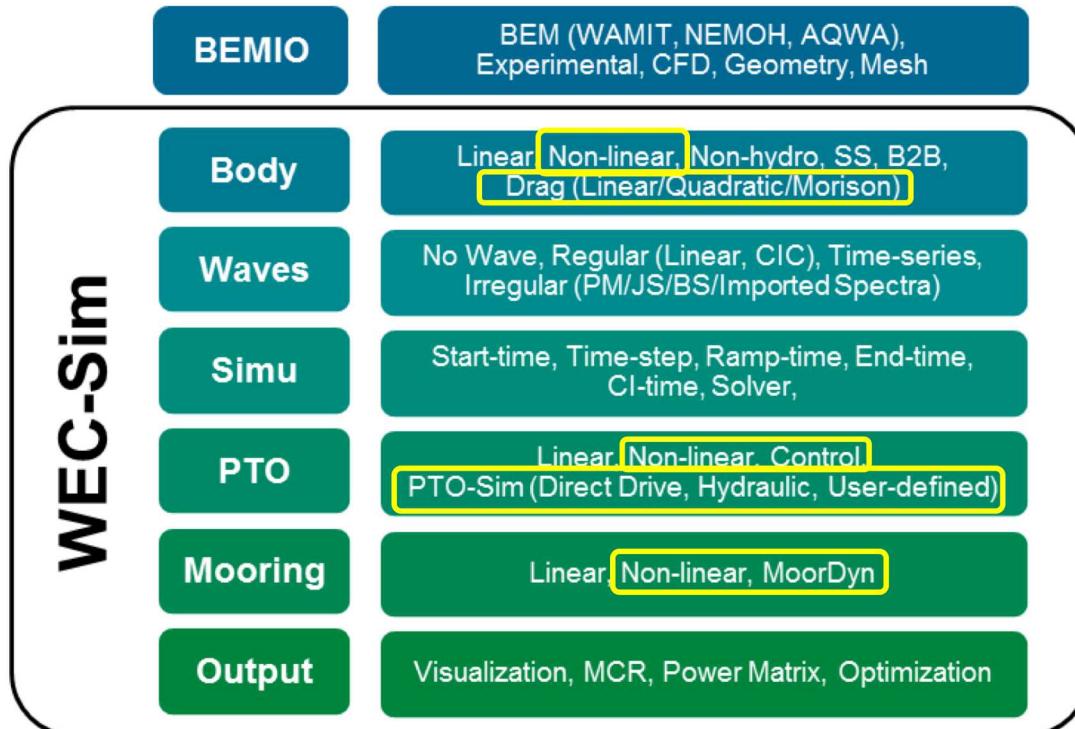
2 Open ✓ 144 Closed Author Labels Projects Milestones Assignee Sort

**ode14x compatibility?** question #191 opened 25 days ago by bradling

**AQWA excitation phase** BEM/bemio bug #186 opened on Jun 22 by kmruehl

💡 ProTip! Bookmark issues and pull requests to revisit later.

# Numerical Assumptions and Nonlinearities



# IEA OES International Code Comparison



## International Energy Agency Ocean Energy Systems Task 10 Wave Energy Converter Modeling Verification and Validation

Fabian Wendt<sup>a</sup>, Yi-Hsiang Yu<sup>a</sup>, Kim Nielsen<sup>a</sup>, Kelley Ruehf<sup>b</sup>, Tim Bunnik<sup>b</sup>, Inanou Touzon<sup>b</sup>, Bo Woo Nam<sup>b</sup>, Jeong Seok Kim<sup>b</sup>, Kyong-Hwan Kim<sup>b</sup>, Carl Van Janssen<sup>b</sup>, Ken-Robert Jakobson<sup>b</sup>, Sarah Crowley<sup>b</sup>, Luis Vega<sup>b</sup>, Krishnakumar Rajagopal<sup>b</sup>, Sumanth Sankar<sup>b</sup>, Debashis Ghosh<sup>b</sup>, Suresh Rambabu<sup>b</sup>, Paul Lamont-Kane<sup>b</sup>, Wanwan Sheng<sup>b</sup>, Roman Costello<sup>b</sup>, Ben Kosch<sup>b</sup>, Sarah Thomas<sup>b</sup>, Pilar Hens<sup>b</sup>, Harry Bingham<sup>b</sup>, Adi Kurniawan<sup>b</sup>, Morten Melhede Kramer<sup>b</sup>, David Oyden<sup>b</sup>, Samuel Girardot<sup>b</sup>, Autenille Babarit<sup>b</sup>, Pierre-Yves Wautheau<sup>b</sup>, Dean Steinke<sup>b</sup>, Andre Roy<sup>b</sup>, Scott Beatty<sup>b</sup>, Paul Schofield<sup>b</sup>, Johan Jansson<sup>a,c,d</sup>, and Johan Hoffman<sup>a</sup>

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<sup>i</sup>WavEC, Portugal, <sup>j</sup>Hawai' Natural Energy Institute, USA, <sup>k</sup>Glosten, USA, <sup>l</sup>Plymouth University, UK

<sup>m</sup>Queen's University Belfast, UK, <sup>n</sup>University College Cork, Ireland, <sup>o</sup>Wave Venture, UK, <sup>p</sup>Floating Power Plant, Denmark

<sup>q</sup>Technical University of Denmark, <sup>r</sup>Aalborg University, Denmark, <sup>s</sup>INNOSEA, France

<sup>t</sup>EC Nantes, France, <sup>u</sup>Dynamic Systems Analysis, Canada

<sup>v</sup>Cascadia Coast Research, Canada, <sup>w</sup>ANSYS, USA, <sup>x</sup>KTH, Sweden, <sup>y</sup>BCAM, Spain

**Abstract**—This is the first joint reference paper for the Ocean Energy Systems (OES) Task 10 Wave Energy Converter Modeling Verification and Validation. The task was established under the IEA OES Technology Network program under the International Energy Agency. OES was founded in 2001 and became a task in 2004. The task was established by the International Energy Laboratory (IEL) in 2015 and approved by the OES Executive Committee in 2016. The kick-off workshop took place in Copenhagen, Denmark, in March 2017. The first phase of the project, Experience from similar offshore wind validation/validation projects (OC3-OC5) conducted within the International Energy Agency (IEA) Offshore Energy Systems (OES) Task 10 is to gain confidence in using numerical models and assessing the accuracy of these codes. This project will eventually help to improve confidence levels in numerical predictions of power production and losses, which are important parameters for the development of reliable and cost-effective WECs.

A total of 25 different organizations from 10 countries participated in the first phase of this project. The participants include universities, research laboratories, commercial software developers, and WEC developers.

The first phase focused on the relatively simple problem of a heaving, spherical body. The motivation behind the selection of this simplistic modeling problem was mitigating potential

### I. INTRODUCTION

Numerical modeling is an important aspect of the design of a wave energy converter (WEC). Designers use different simulation software packages (codes) that predict the response and loads of a WEC during operation and extreme events. These codes are based on different assumptions and numerical models. The kick-off workshop included the International Energy Agency (IEA) Offshore Energy Systems (OES) Task 10 to gain confidence in using numerical models and assessing the accuracy of these codes. This project will eventually help to improve confidence levels in numerical predictions of power production and losses, which are important parameters for the development of reliable and cost-effective WECs.

The first phase focused on the relatively simple problem of a heaving, spherical body. The motivation behind the selection of this simplistic modeling problem was mitigating potential

1

F. Wendt and et al., "International Energy Agency Ocean Energy Systems Task 10 Wave Energy Converter Modeling Verification and Validation," in Proceedings of the 12th European Wave and Tidal Conference, Cork, Ireland, 2017.

## International Energy Agency Ocean Energy Systems Task 10

- This task on WEC modeling verification and validation will internationally assess the accuracy and **establish confidence in the use of numerical models for WECs**.
- WEC-Sim was submitted by labs and also by other institutions
- Phase 1 results presented in EWTEC 2017 publication
- **Currently modeling a new WEC geometry and looking for participants**

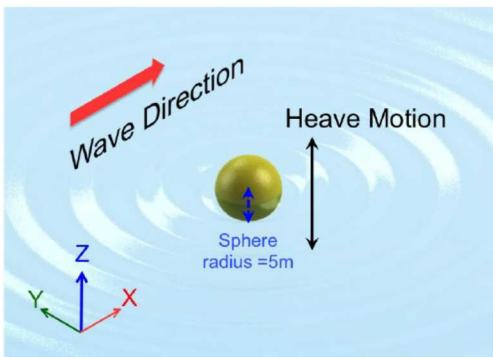


Fig. 1. Illustration of the heaving sphere used in the first phase of the project

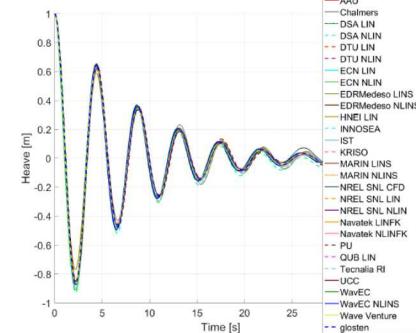


Fig. 3. Free-decay response in heave for the 1.0-m initial displacement.

# WEC Control Competition (WECCCOMP)



- International competition to **maximize WEC benefit-to-cost ratio through innovative control strategies**
- First stage is **implementation of WEC control in a numerical simulation** at model scale using the WEC-Sim code
- Second stage involves **implementation of WEC control in an experimental wave tank**
- This paper details development and validation of a WEC-Sim representation of a 1-20th scale Wavestar model for WECCCOMP.

## AVAILABLE AT

<http://www.eeng.nuim.ie/coer/wec-control-competition-released/>

## ORGANIZED BY



## WECCCOMP Timeline

1st Dec. 2017	Registration opens
1st Sept. 2018	Entry deadline
31st Oct. 2018	Shortlisting complete
15st Nov. 2018	Interactive implementation
31st Jan. 2019	Implementation evaluation
31st Mar. 2019	Final results published



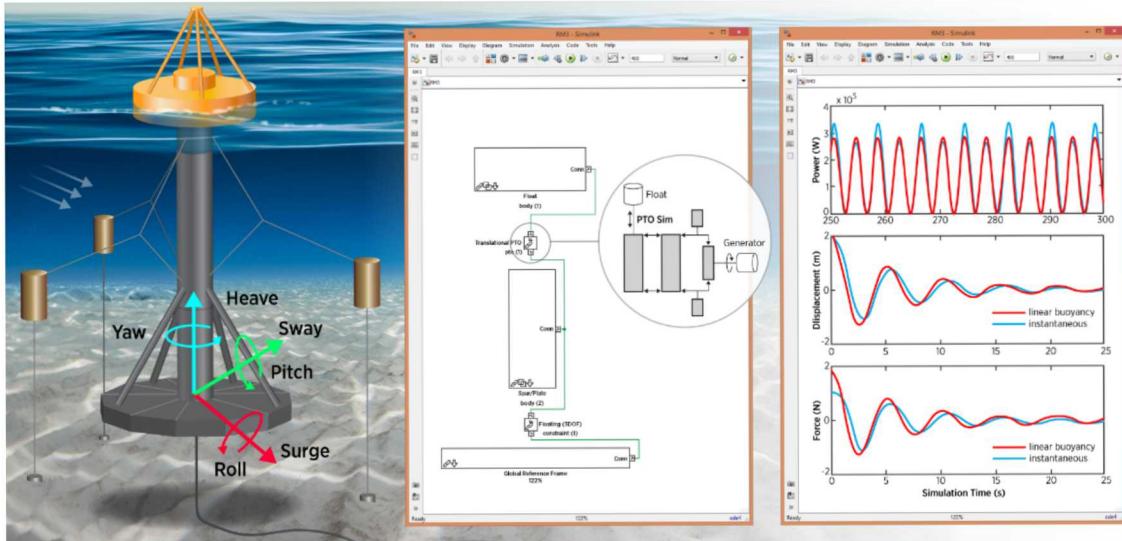
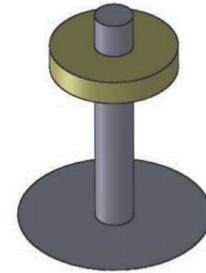
# RM3 Tutorial

- Tutorial available online here:

<https://github.com/WEC-Sim/WEC-Sim/tree/master/tutorials/RM3>

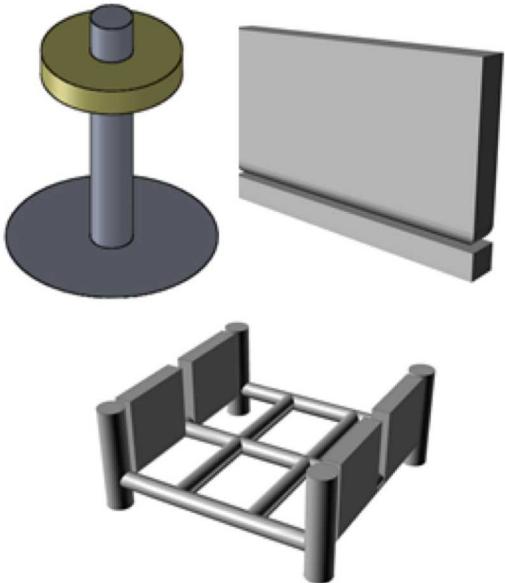
- Details available here:

<http://wec-sim.github.io/WEC-Sim/tutorials.html#two-body-point-absorber-rm3>

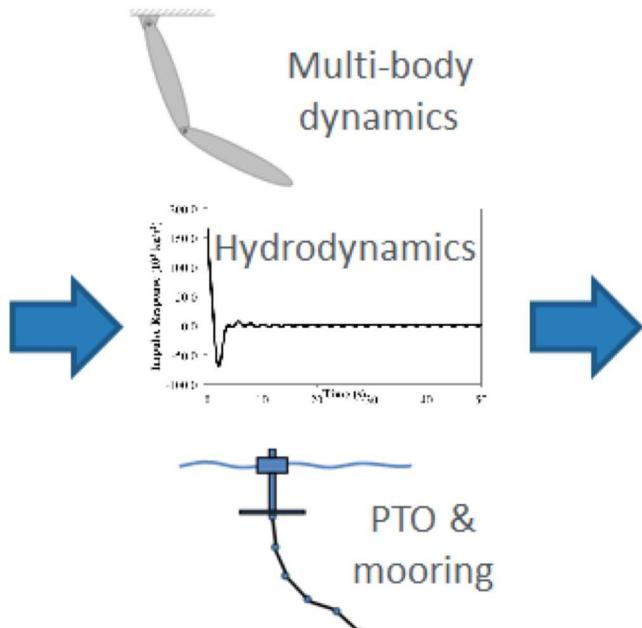


# Analysis and Post-processing

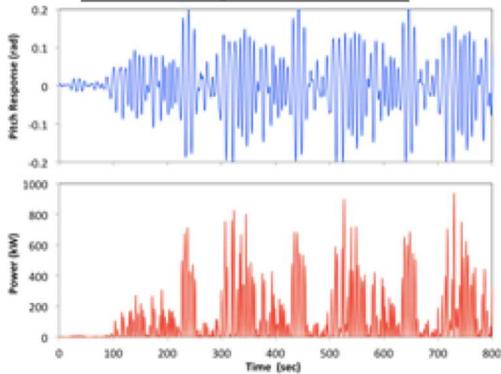
## WEC device specification



## Relevant numerical methods



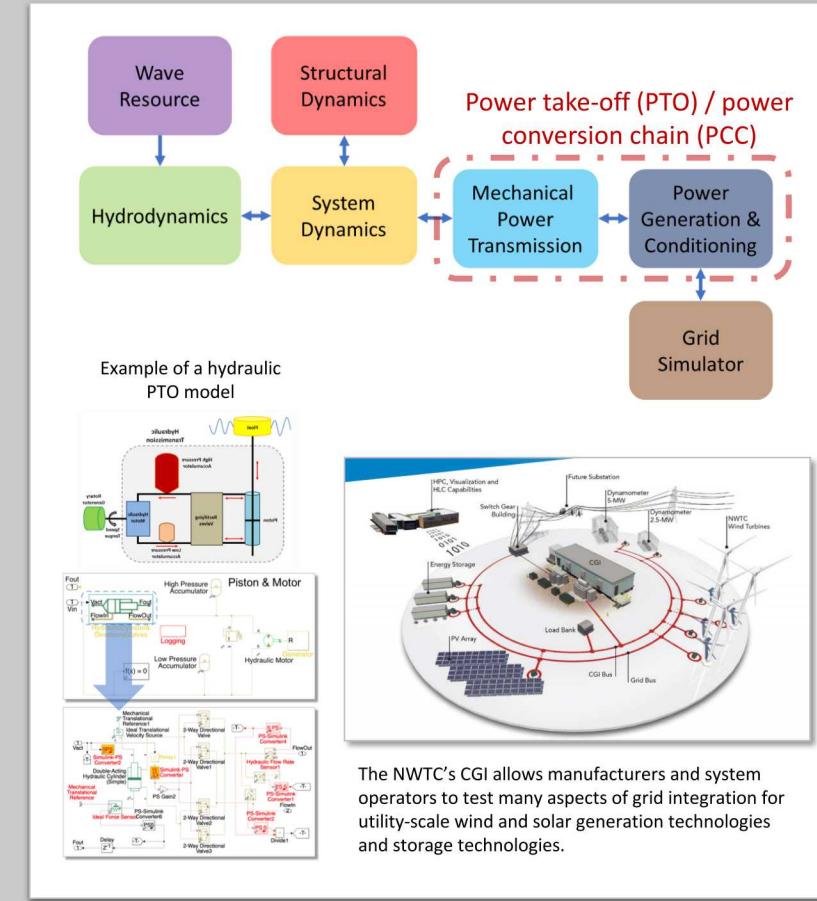
## WEC performance, motions, and loads



Power Matrix (kW) Cd_float=1.4; Cd_plate=4.25 (Based on CFD)													
Energy Period (s)													
	5.7	6.7	7.7	8.7	9.7	10.7	11.7	12.7	13.7	14.7	15.7	16.7	17.7
0.25	0.42	0.71	0.97	1.19	1.36	1.46	1.49	1.45	1.36	1.24	1.11	0.99	0.87
0.75	3.77	6.36	8.75	10.73	12.22	13.14	13.38	13.02	12.21	11.17	10.03	8.91	7.85
1.25	10.51	17.66	24.32	29.80	33.93	36.49	37.17	36.15	33.92	31.02	27.88	24.74	21.80
1.75	21.66	34.79	47.66	58.41	66.55	71.52	72.85	70.86	66.49	60.80	54.62	48.49	42.73
2.25	37.64	62.75	79.03	96.55	110.02	128.13	120.43	117.14	109.92	100.50	90.28	80.16	70.64
2.75	57.95	100.66	121.83	144.23	164.36	176.62	179.90	174.98	164.19	150.13	134.87	119.74	105.52
3.25	85.24	150.37	178.99	204.14	229.54	246.68	251.27	244.40	229.33	209.69	188.37	167.24	147.38
3.75	108.16	209.85	249.53	279.77	306.79	328.42	334.57	325.38	305.32	279.58	250.78	222.66	196.22
4.25	138.93	272.93	332.45	371.07	399.54	421.84	429.68	427.93	402.17	378.59	322.12	285.99	252.04
4.75	173.54	340.92	426.99	477.32	509.63	530.38	536.79	522.05	485.87	447.92	402.37	357.24	314.83
5.25	212.00	416.47	531.26	597.80	654.50	655.75	657.31	637.74	598.43	547.19	491.54	456.41	384.60

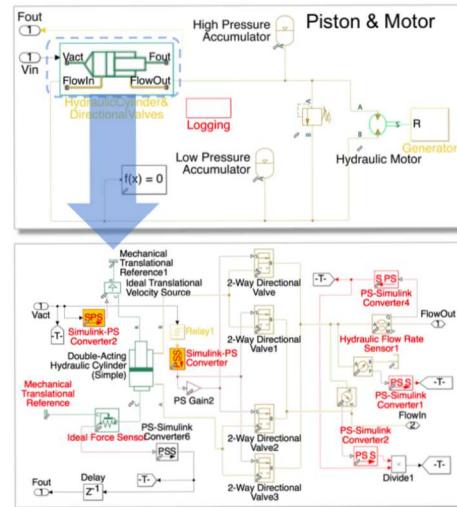
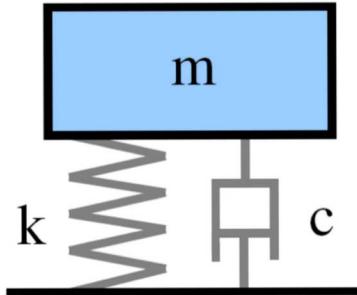
# Wave-To Wire Simulations

- Hydrodynamics simulation (including wave resource characterization) is important but is just half the battle.
- Mechanical power transmission and power electric and management (including grid impact) is the other half, which are essential to system design optimization and would affect the WEC hydrodynamics.
- Ultimately, WEC is a energy conversion system and cost efficiency is important.



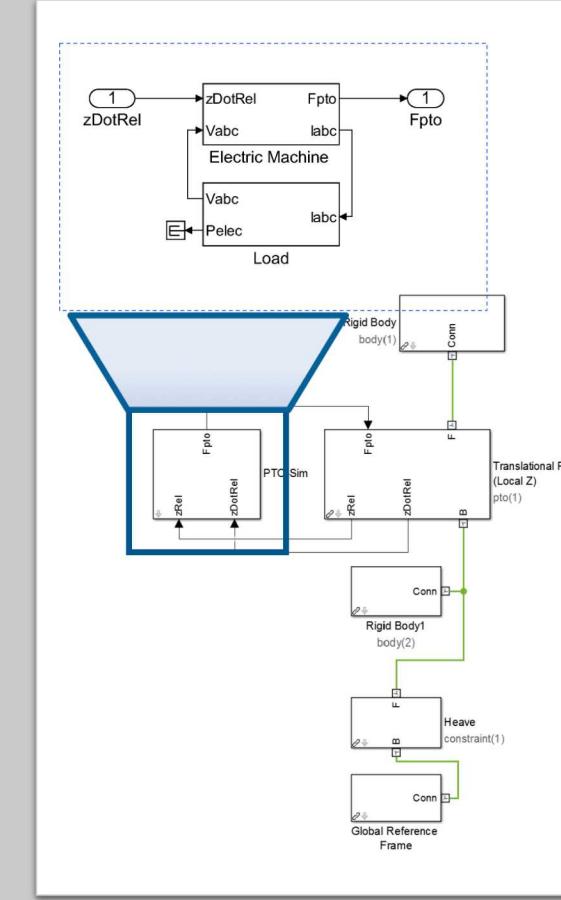
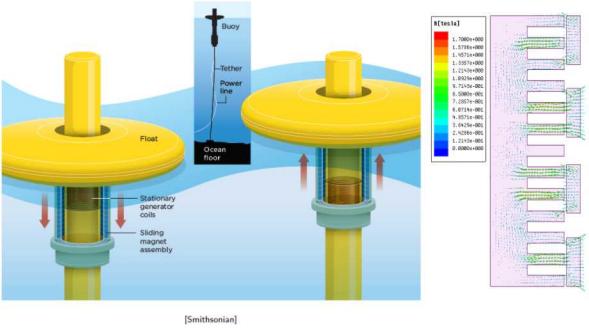
# PTO System Modeling

- Linear spring damper
- Coulomb damping
- Empirical correlation & lookup table
- PTO components simulation

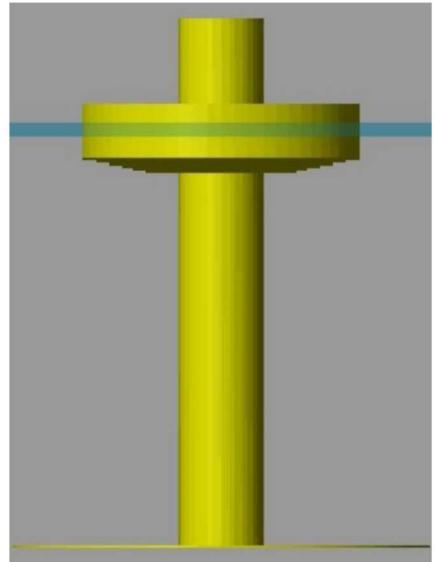


# Case 1: Direct Drive PTO

- OSUL10: Two-body point absorber
- WEC-Sim using PTO-Sim

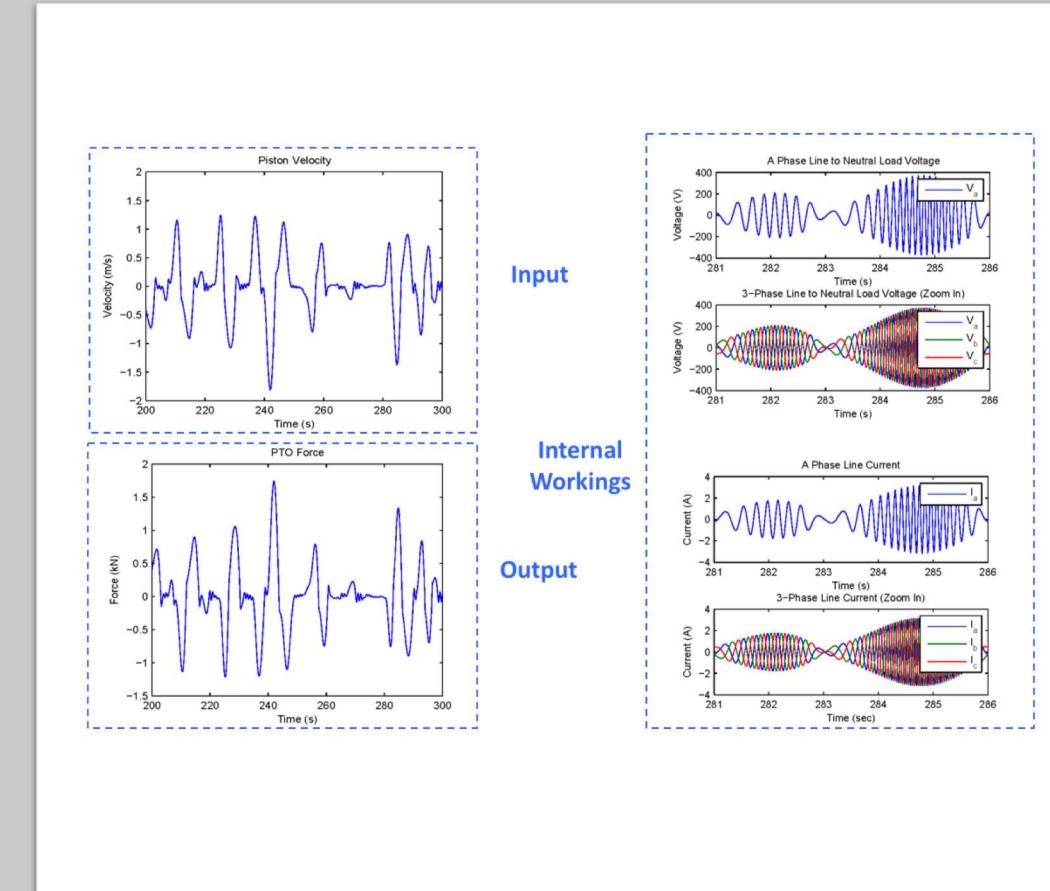
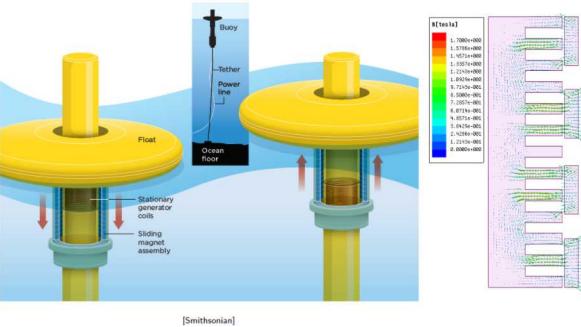


So, R., Simmons, A., Brekken, T., Ruehl, K., and Michelen, C., 2015. "Development of PTO-Sim A power performance module for the open-source wave energy converter code WEC-Sim," *34th International Conference on Ocean, Offshore and Arctic Engineering*.



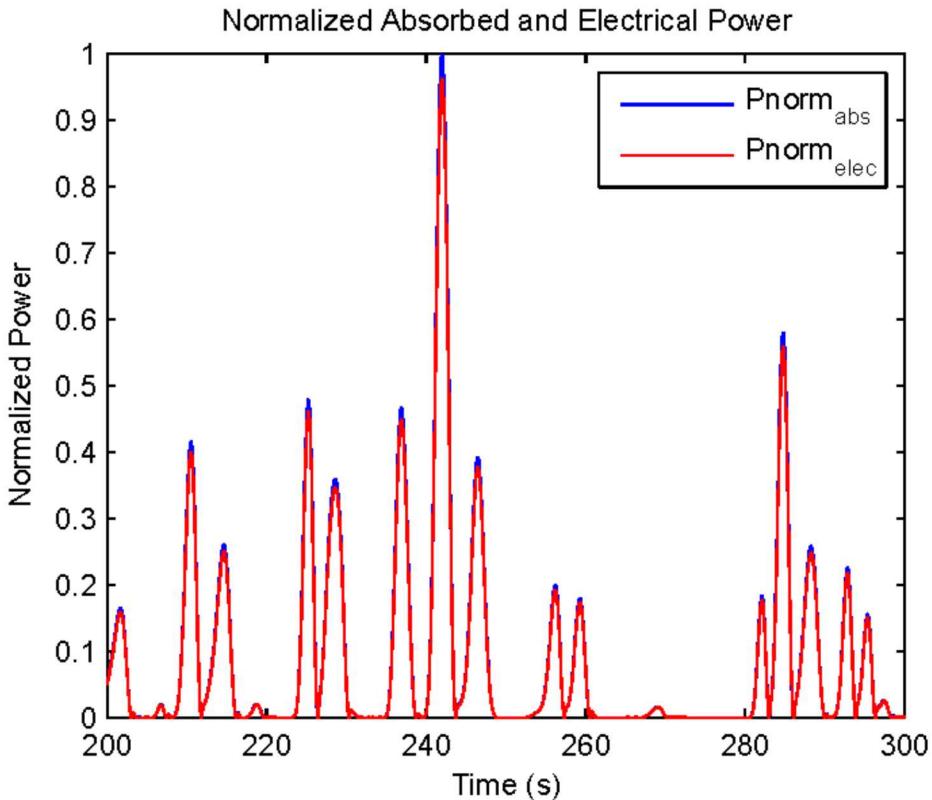
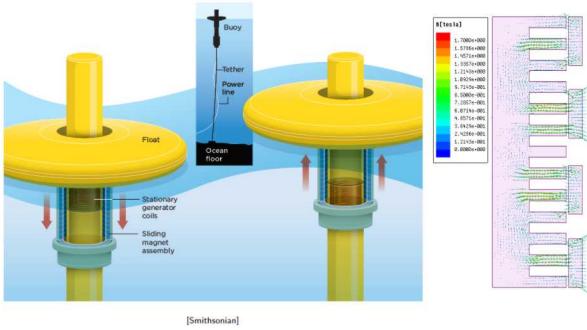
# Case 1: Direct Drive PTO

- OSUL10: Two-body point absorber
- WEC-Sim using PTO-Sim



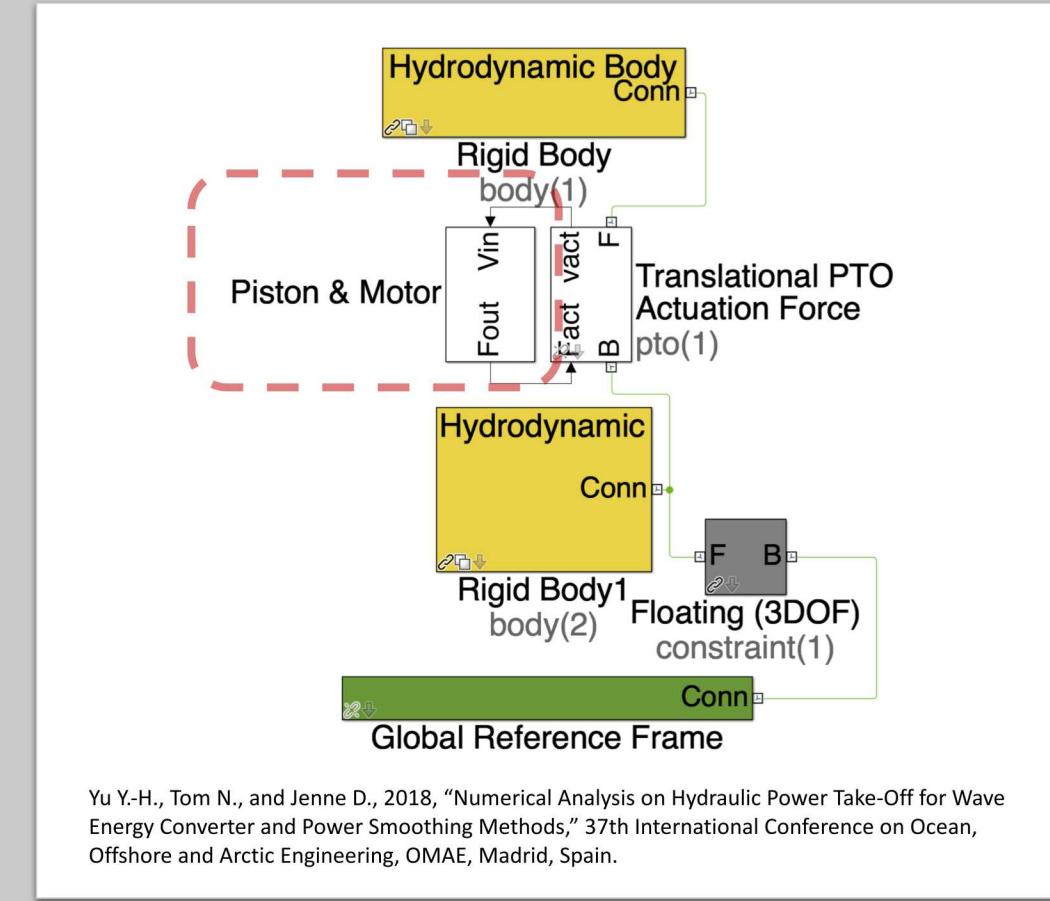
# Case 1: Direct Drive PTO

- OSUL10: Two-body point absorber
- WEC-Sim using PTO-Sim



# Case 2: Hydraulic PTO

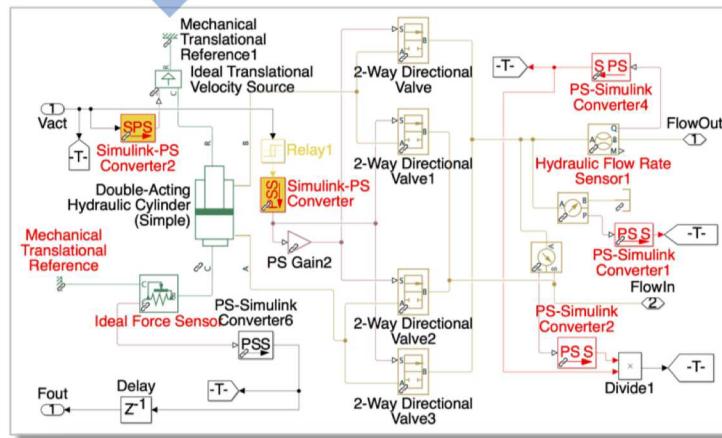
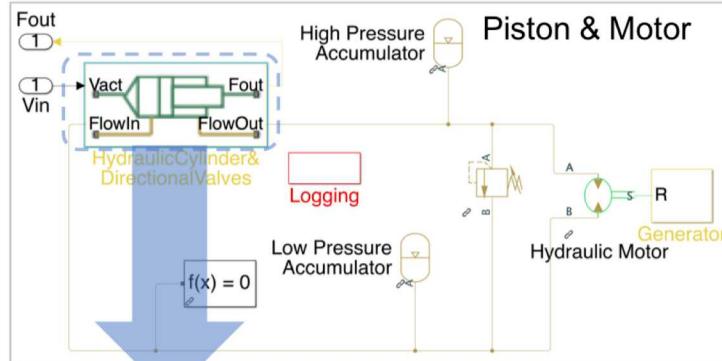
- Reference Model 3: Two-body point absorber
- WEC-Sim + Simscape Fluids



Yu Y.-H., Tom N., and Jenne D., 2018, "Numerical Analysis on Hydraulic Power Take-Off for Wave Energy Converter and Power Smoothing Methods," 37th International Conference on Ocean, Offshore and Arctic Engineering, OMAE, Madrid, Spain.

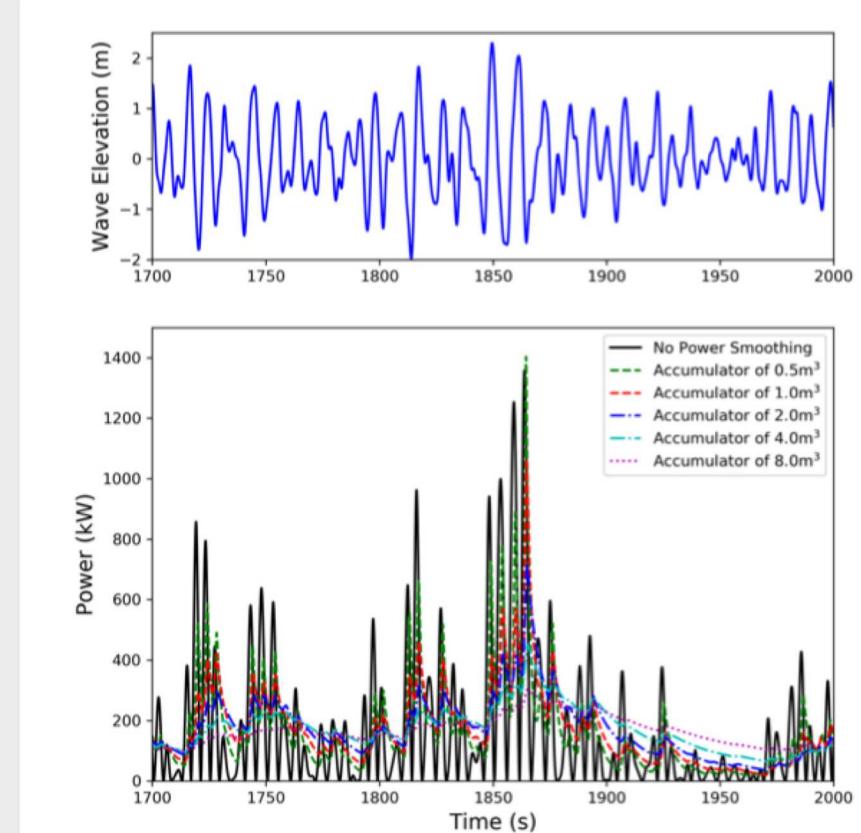
## Case 2: Hydraulic PTO

- Reference Model 3: Two-body point absorber
- WEC-Sim + Simscape Fluids

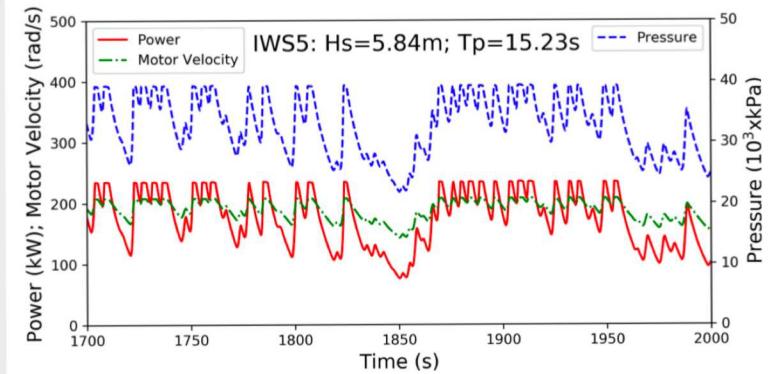
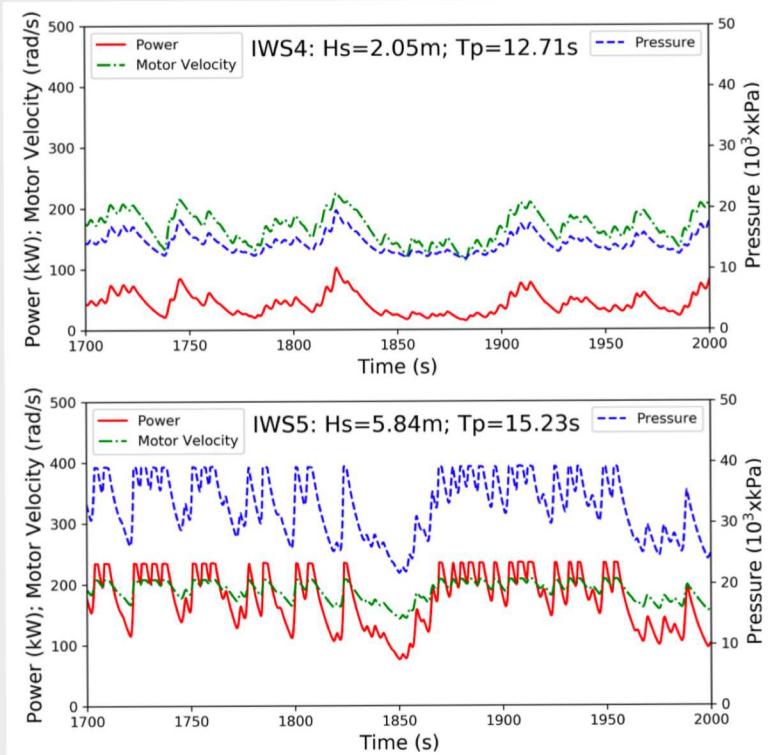
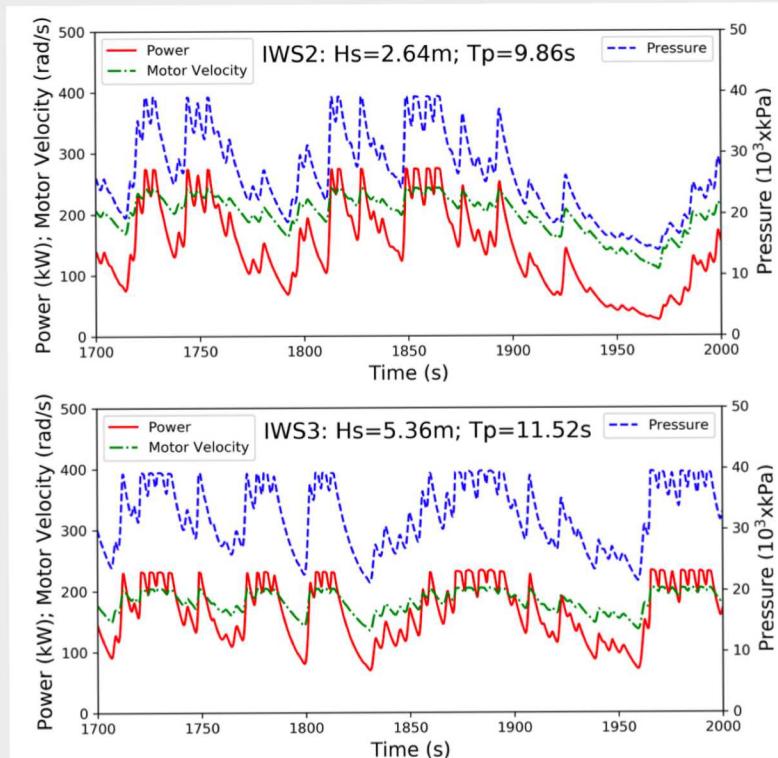


## Case 2: Hydraulic PTO

*The variations of the power output (voltage, frequency, rate of change in power output) can be a problem which must be well understood as it drives additional design considerations for wider power system development.*



## Case 2: Hydraulic PTO

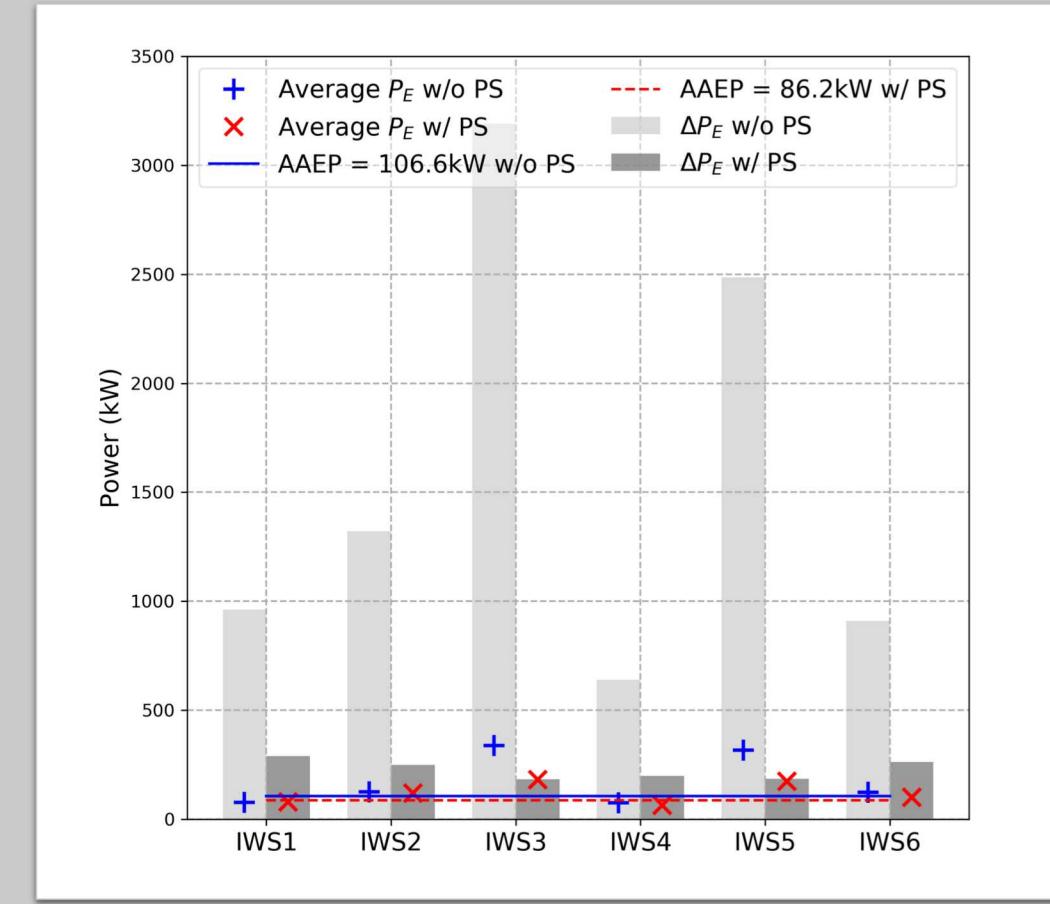


# Case 2: Hydraulic PTO

## Control for Power Smoothing

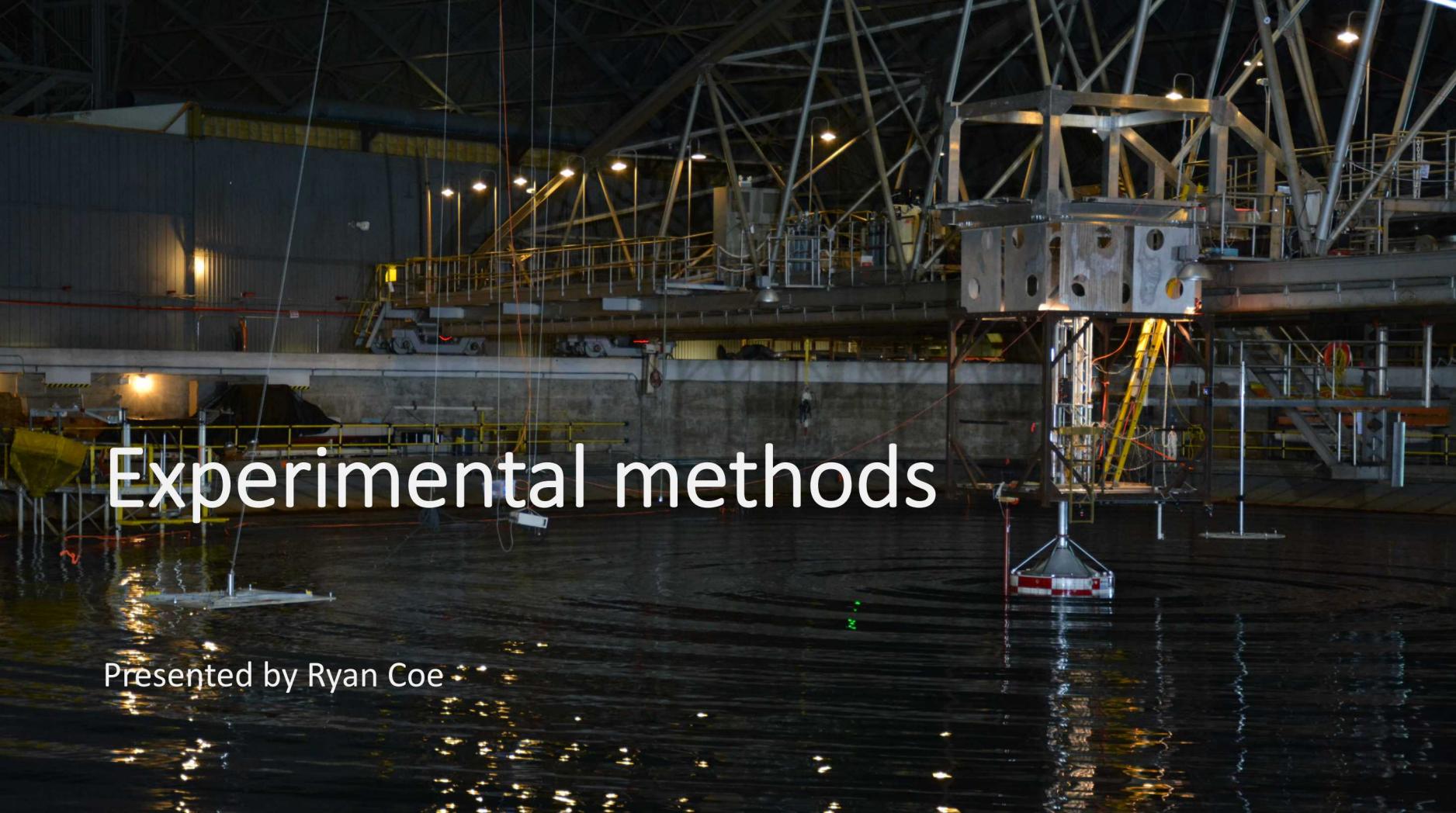
### Wave Energy Prize Sea States

Wave #	Tp (s)	Hs (m)	Weighting
IWS 1	7.31	2.34	0.175
IWS 2	9.86	2.64	0.268
IWS 3	11.52	5.36	0.058
IWS 4	12.71	2.05	0.295
IWS 5	15.23	5.84	0.034
IWS 6	16.50	3.25	0.054



## PTO System Modeling Challenges

- A multi-physics problem
- What level of detail do we want to resolve?
- Numerical stabilities – often required smaller time steps or use different time-step sizes for different physics.



# Experimental methods

Presented by Ryan Coe

# Why System ID?

- Most effective control strategies are model-based
- Control effectiveness is directly dependent on model accuracy
- Numerical methods  
(e.g., boundary element)  
are imperfect
  - Linearized
  - Only tell you about part of the system



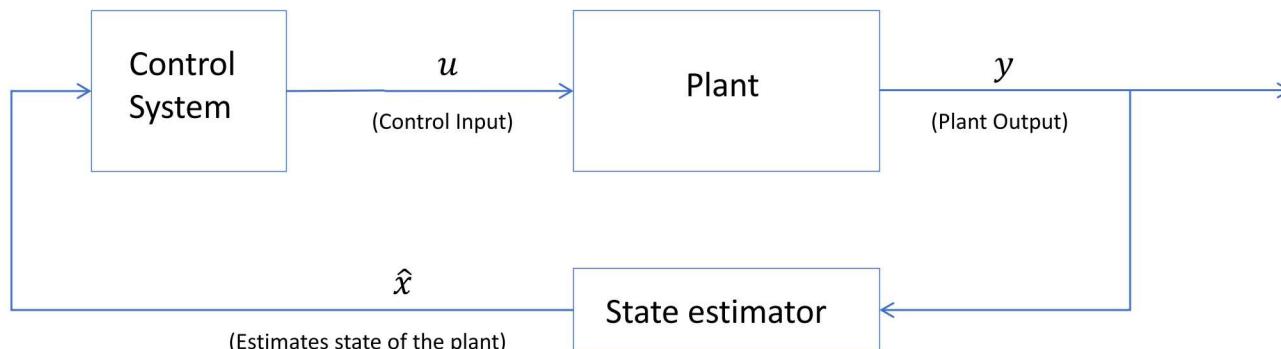
# Control models

## What is the objective?

### Control system design

## Steps

1. Identify available measurements ( $y$ )
2. Study quality of the measurements ( $y$ )  
(e.g. noise)
3. Design state estimator/observer
  - E.g.: Kalman filter and Luenberger observer are model based
4. Design control system
  - Many control algorithms require a model of the plant (e.g. MPC, LQ)



# Types of models

- Many types of models to choose from
- “Correct” model type dictated by intended application(s)

	Time domain	Frequency domain
Parametric	State-space	Transfer function
Non-parametric	Impulse response function	Frequency response function (WAMIT)

# Types of models

Frequency domain models often provide useful insight in system dynamics and assist in analytic tuning

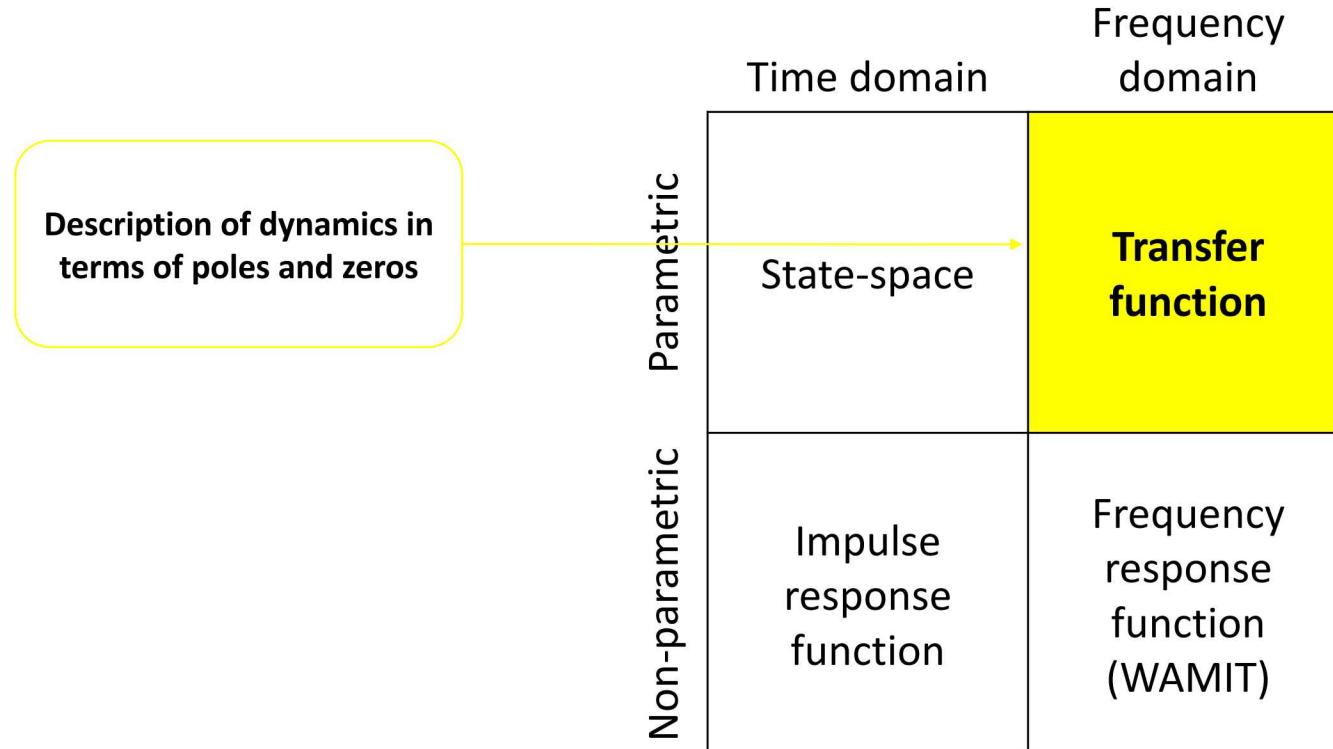
	Time domain	Frequency domain
Parametric	State-space	<b>Transfer function</b>
Non-parametric	Impulse response function	<b>Frequency response function (WAMIT)</b>

# Types of models

	Time domain	Frequency domain
Parametric	State-space	Transfer function
Non-parametric	Impulse response function	Frequency response function (WAMIT)

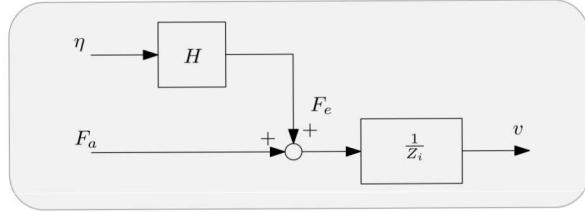
Non-parametric models directly produced by numerical and empirical methods (no fitting necessary)

# Types of models

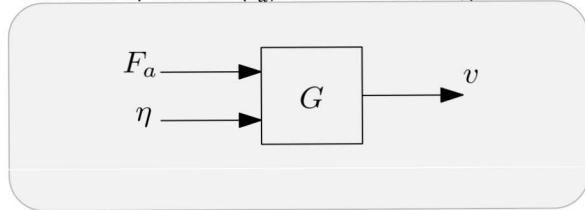


# Types of models

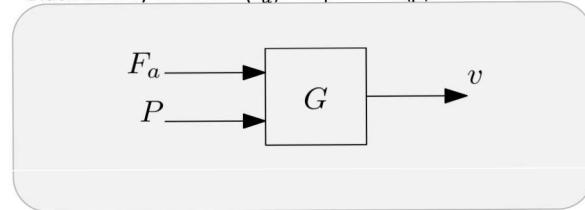
Radiation-diffraction model



Black-box w/ actuator ( $F_a$ ) and wave elevation ( $\eta$ )

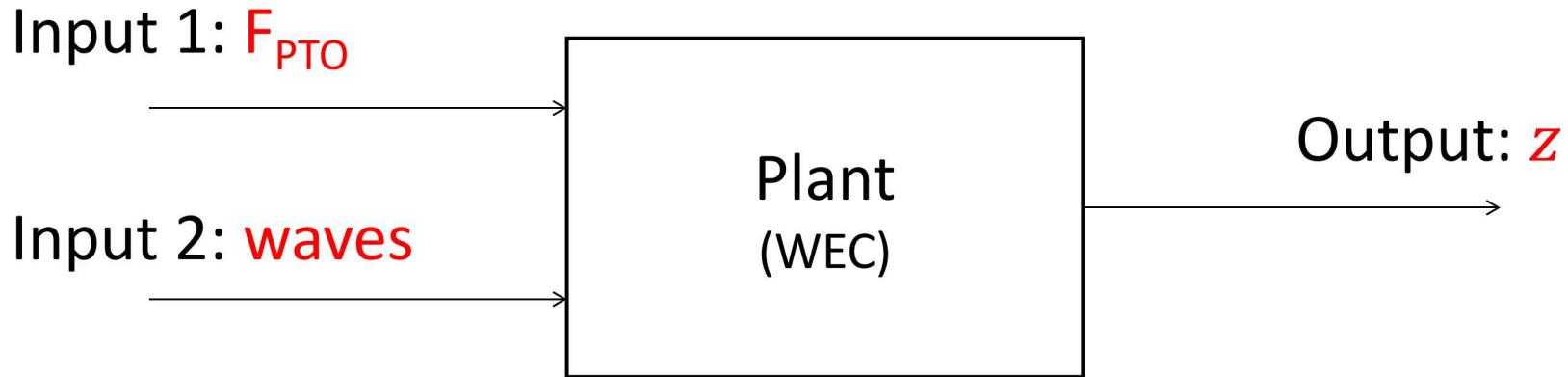


Black-box w/ actuator ( $F_a$ ) and pressure ( $p$ )



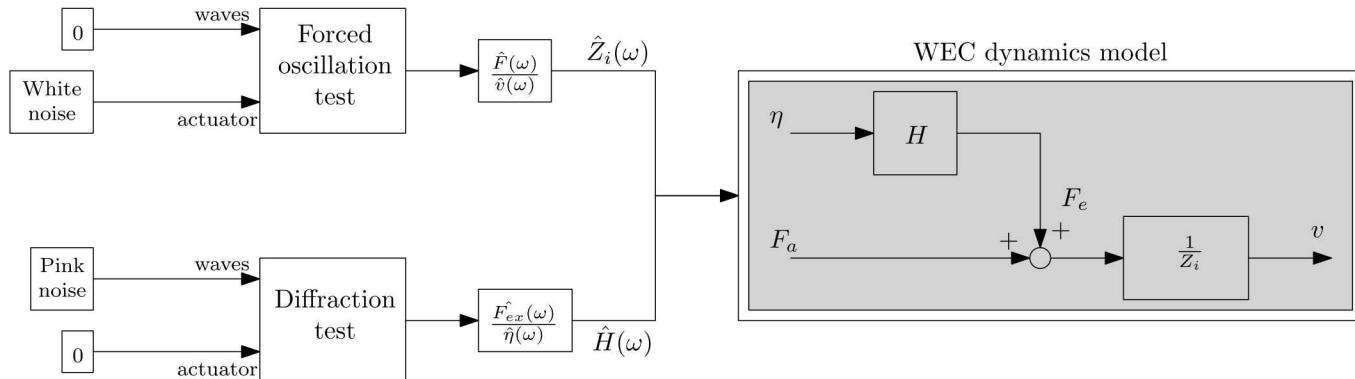
	Time domain	Frequency domain
Parametric	State-space	Transfer function
Non-parametric	Impulse response function	Frequency response function (WAMIT)

# Testing - System identification



Multi Input Single Output (MISO) system

# WEC System Identification



- **Forced oscillation test**
  - Force control
  - Multi-sine input signal (e.g., white noise)
- **Diffraction test**
  - While idealized ocean spectra (e.g. Bretschneider) are acceptable, flatter spectra are more desirable.
  - White (flat) spectra waves have a tendency to break; pink spectra do not

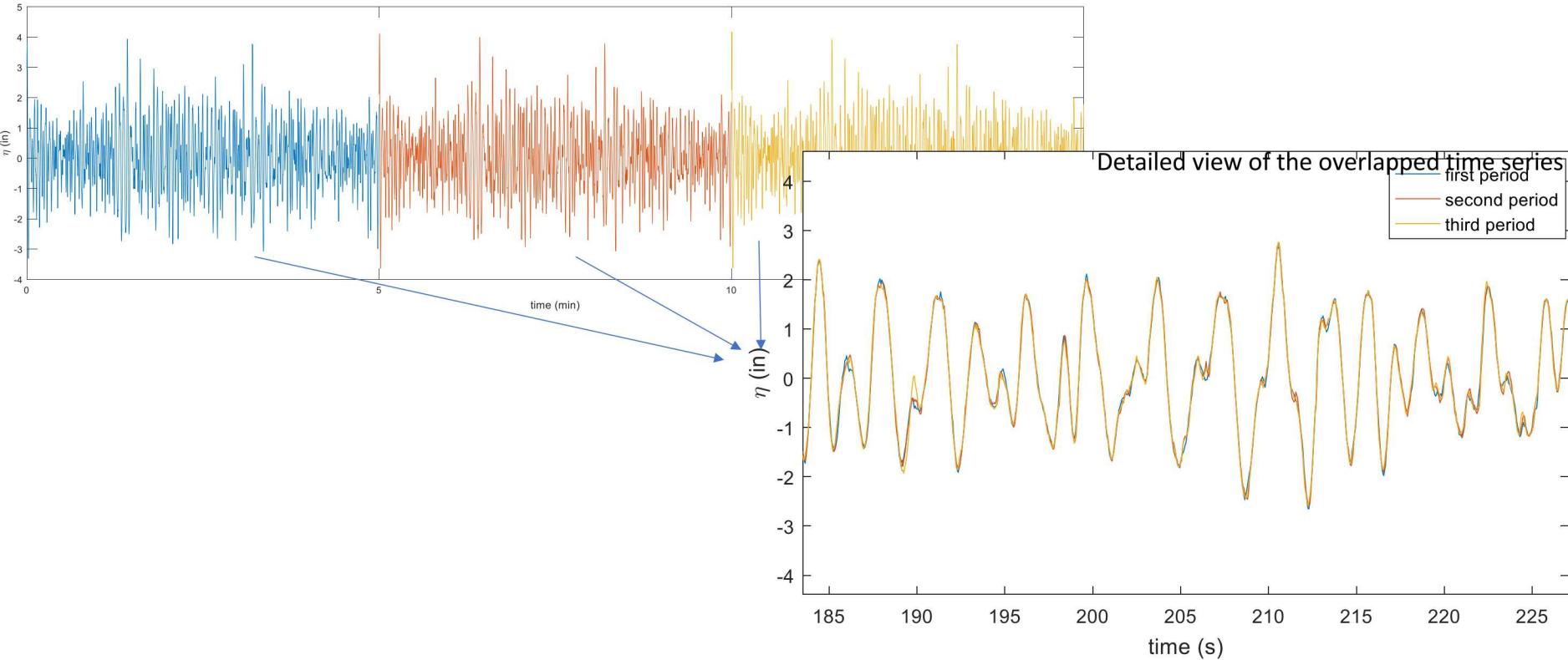
$$\left( B(\omega) + B_f + i \left( \omega (M + A(\omega)) - \frac{K}{\omega} \right) \right) \hat{V} = \hat{H}(\omega) \hat{\eta} + \hat{F}_a$$

*Intrinsic impedance*  $Z_i(\omega) = \frac{\hat{F}_a}{\hat{V}} = B(\omega) + B_f + i(M + A(\omega) - K/\omega)$

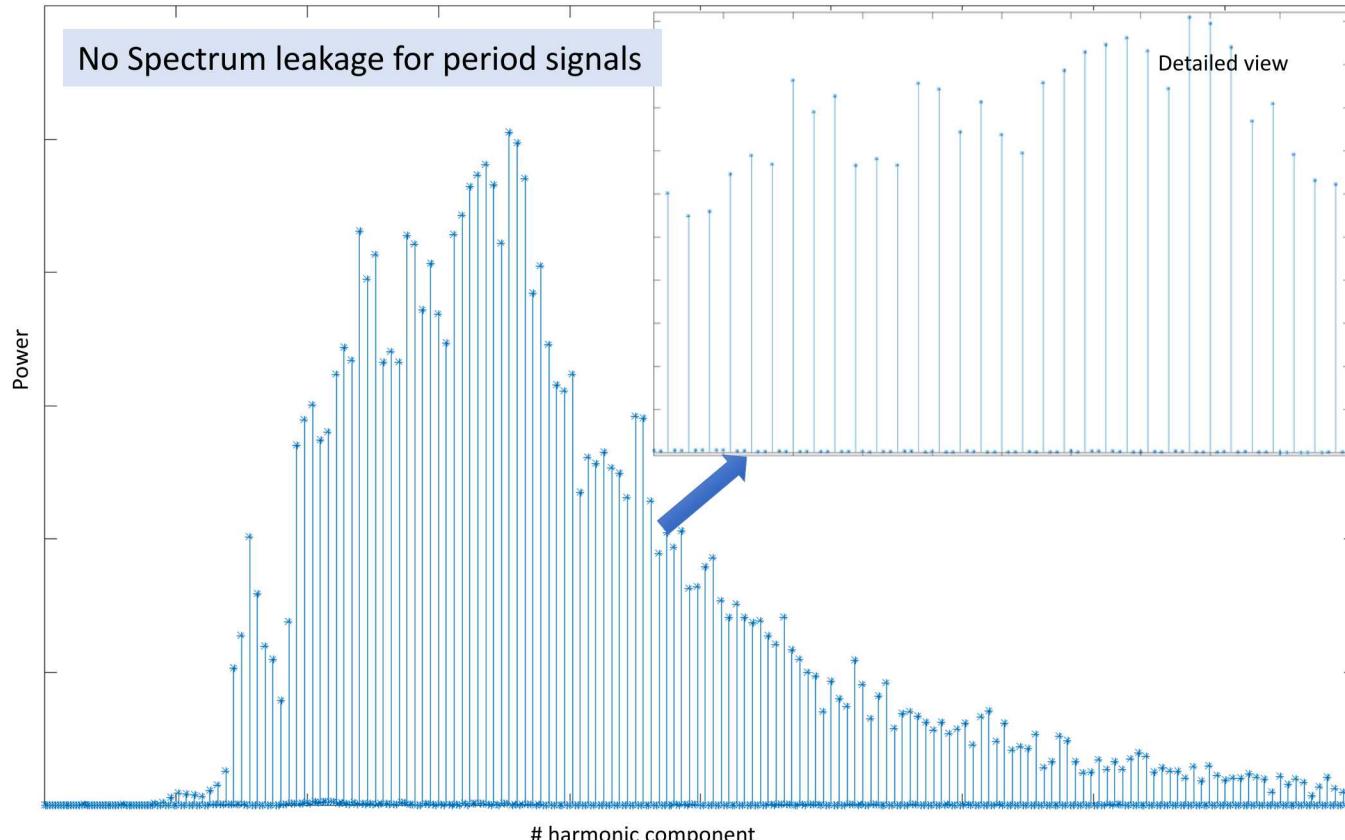
$$\hat{V} = \frac{H(\omega)}{Z_i(\omega)} \hat{\eta} + \frac{1}{Z_i(\omega)} \hat{F}_a.$$

# Testing - Repeating vs non-repeating spectra

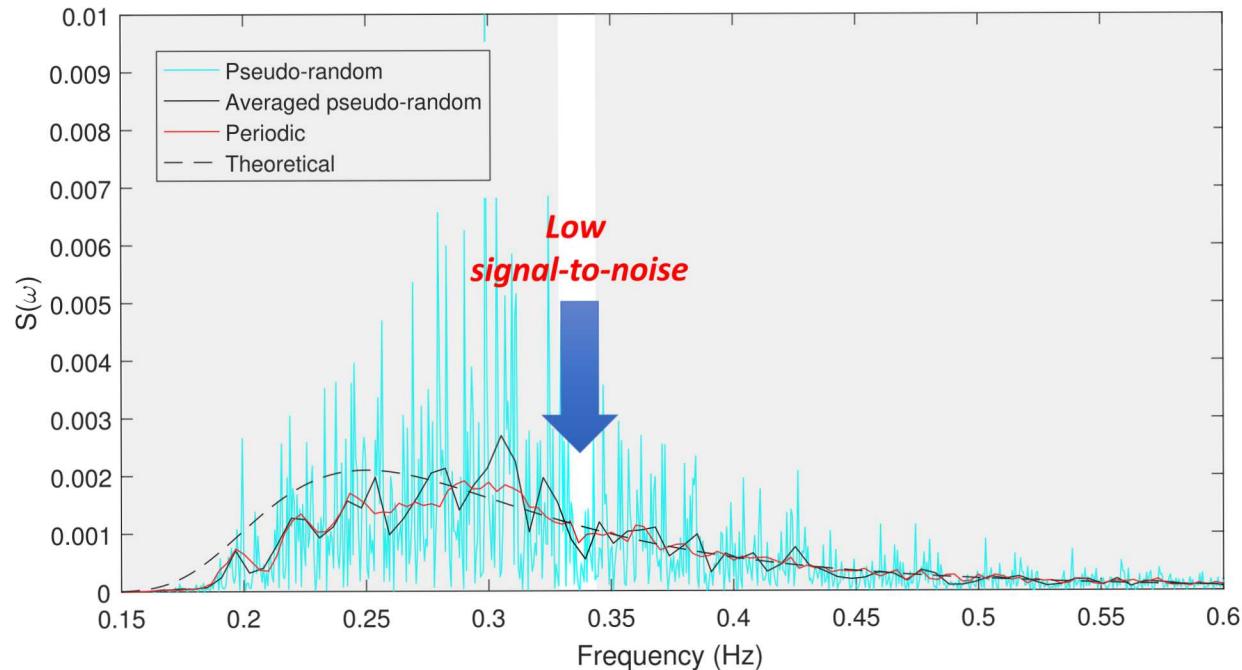
Water surface elevation: Bretschneider spectrum, repeat period  $T_{\text{rep}} = 5\text{ minutes}$



# Testing - Repeating vs non-repeating spectra



# Benefits of periodic input signals



$$T_r = 2 \text{ hr}, T_{\text{exp}} = 30 \text{ min}$$

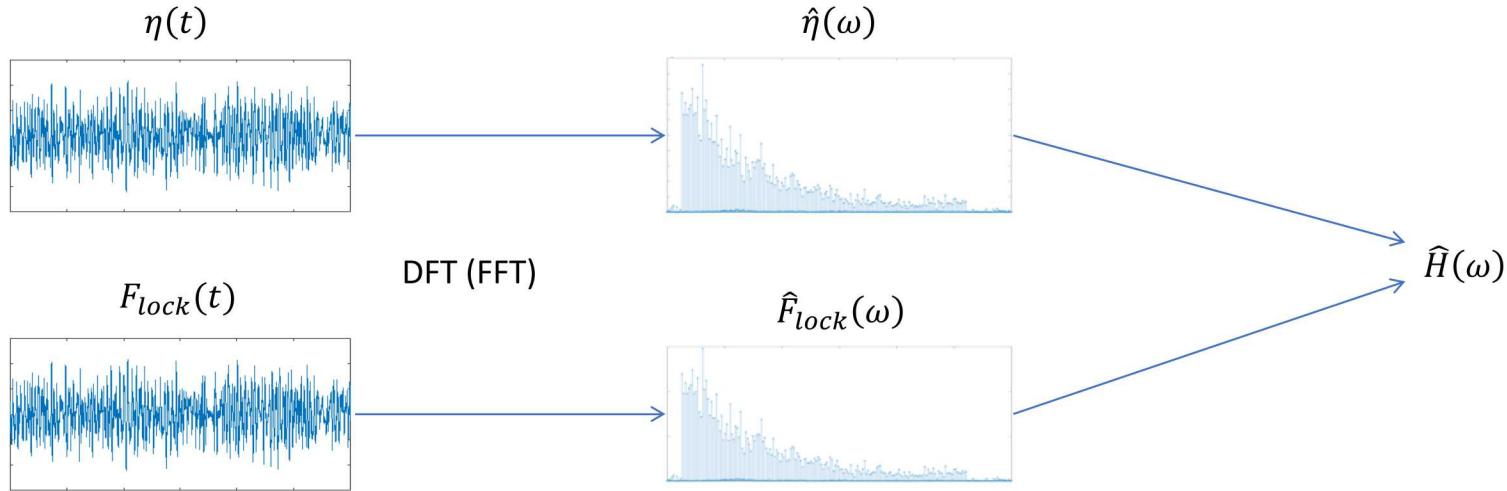
$$T_r = 5 \text{ min}, T_{\text{exp}} = 15 \text{ min}$$

# MASK Basin Testing



# Testing - Excitation FRF

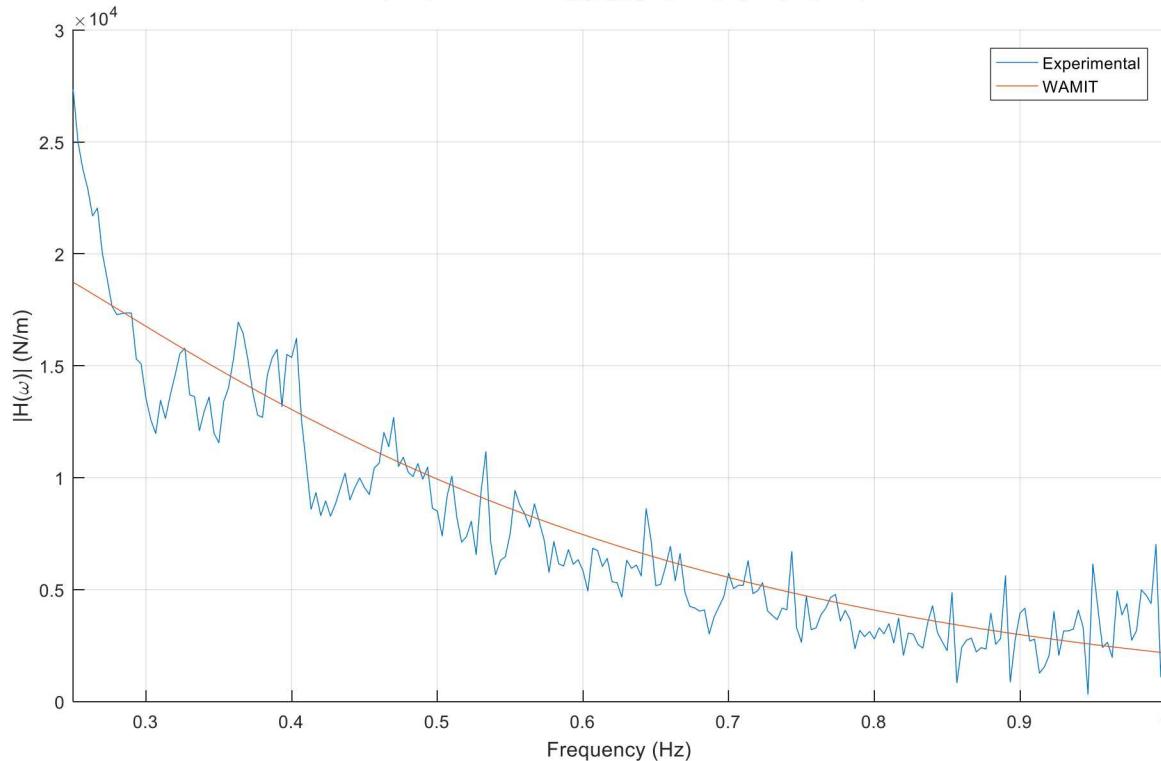
$$\hat{H}(\omega) = \hat{F}_{lock}(\omega)/\hat{\eta}(\omega)$$



$\eta(t), F_{lock}(t)$  trimmed at integer multiple of period

# Testing - Excitation FRF

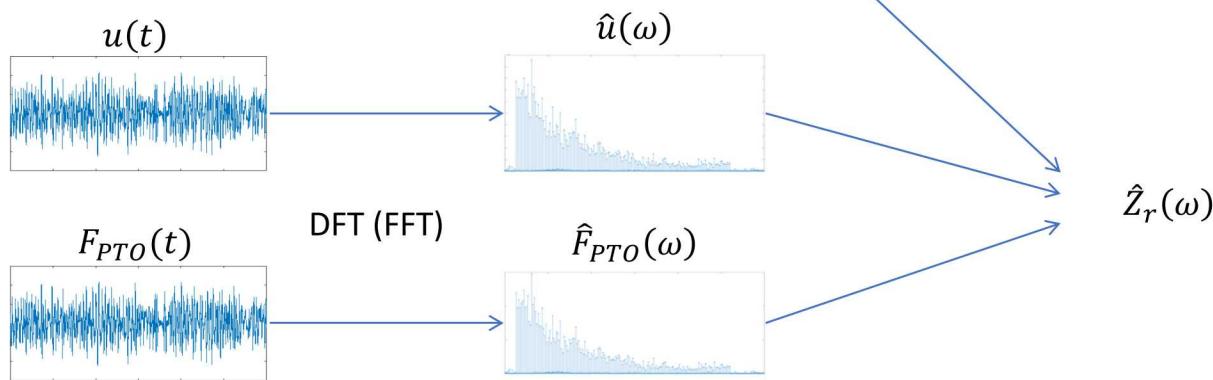
$$\hat{H}(\omega) = \hat{F}_{lock}(\omega)/\hat{\eta}(\omega)$$



# Testing - Radiation FRF

$$\hat{Z}_r(\omega) = \hat{R}(\omega) + i\omega\hat{M}_a(\omega) = \frac{\hat{F}_{PTO}(\omega)}{\hat{u}(\omega)} - B - i\left(\omega M - \frac{K}{\omega}\right)$$

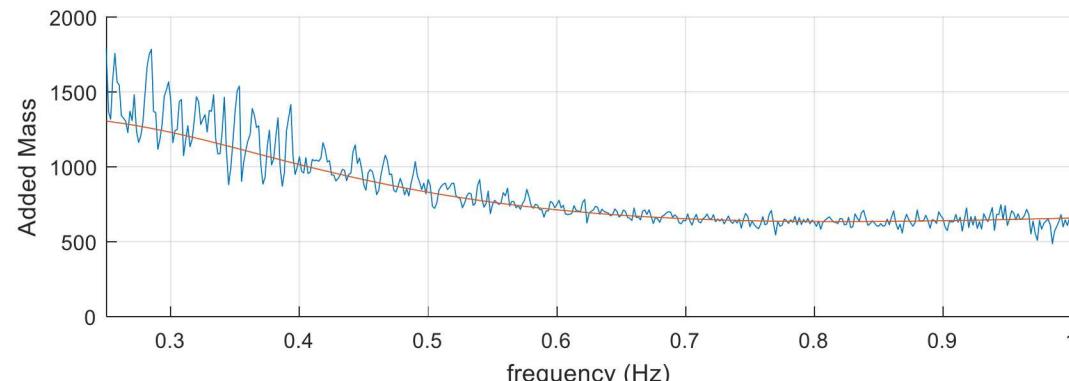
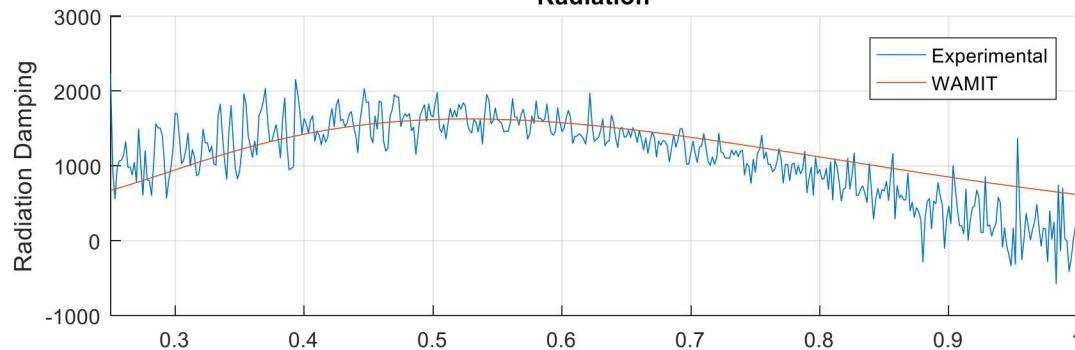
$\hat{R}$  = Radiation damping  
 $\hat{M}_a$  = Added mass  
 $\hat{u}$  = velocity  
 $\hat{F}_{PTO}$  = PTO force  
 $B$  = linear friction/dissipation  
 $M$  = mass  
 $K$  = hydrostatic restoring coeff



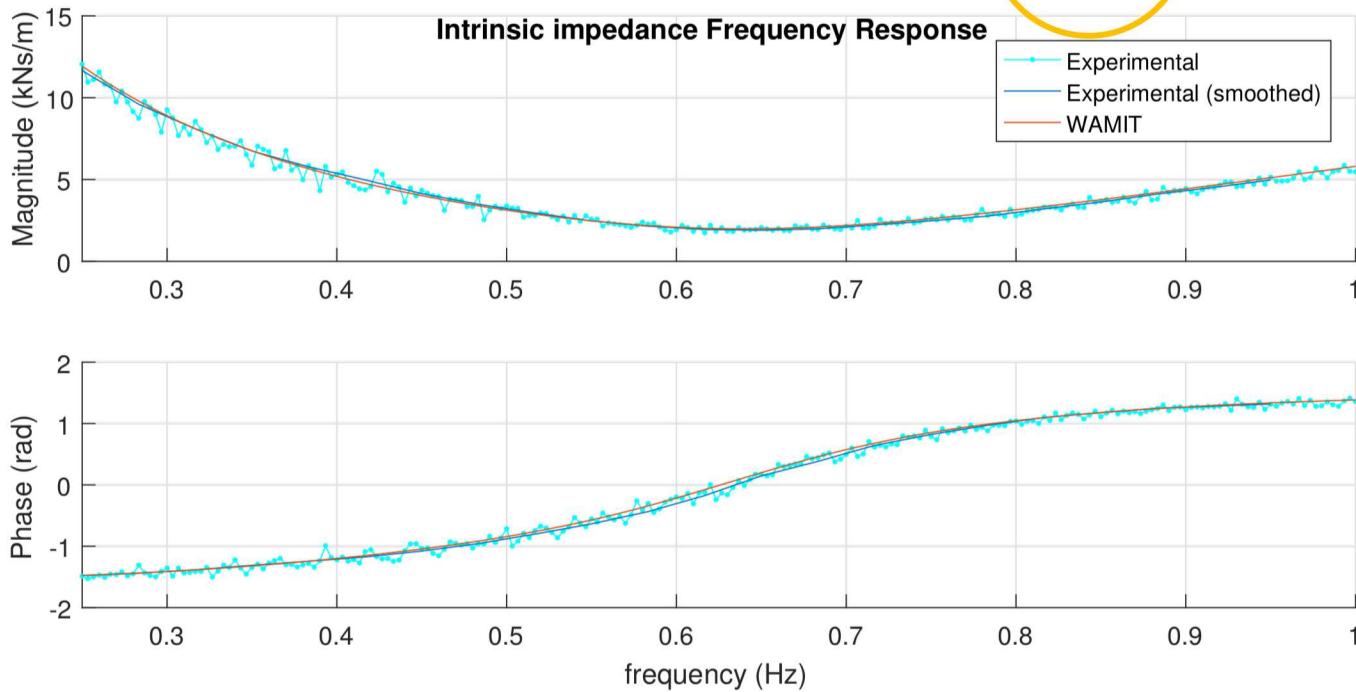
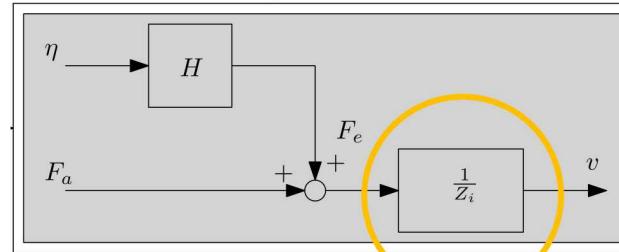
$u(t), F_{PTO}(t)$  trimmed at integer multiple of period

# Testing - Radiation FRF

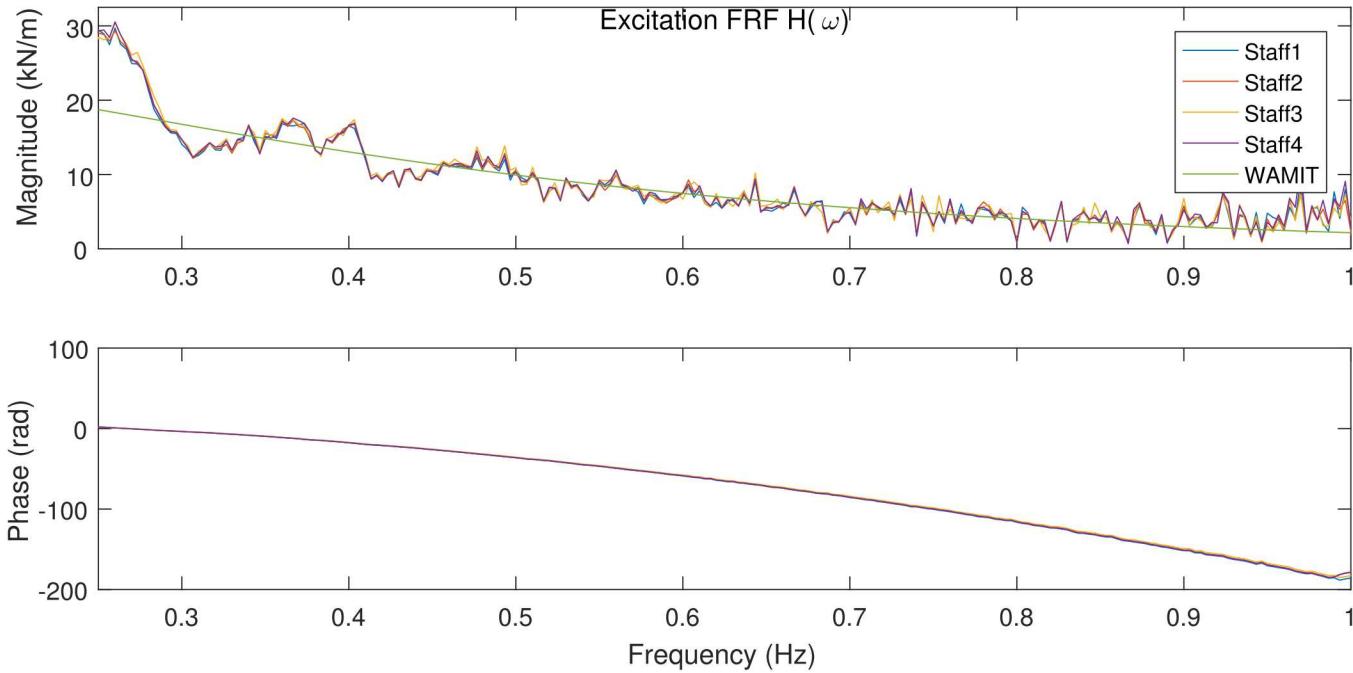
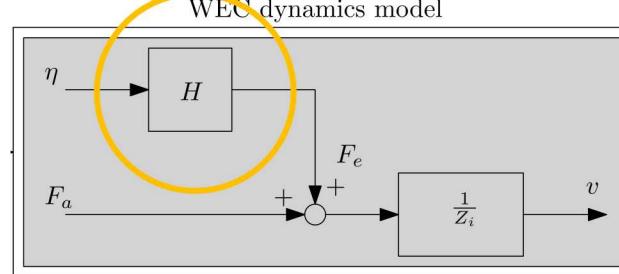
$$\hat{Z}_r(\omega) = \hat{R}(\omega) + i\omega\hat{M}_a(\omega)$$



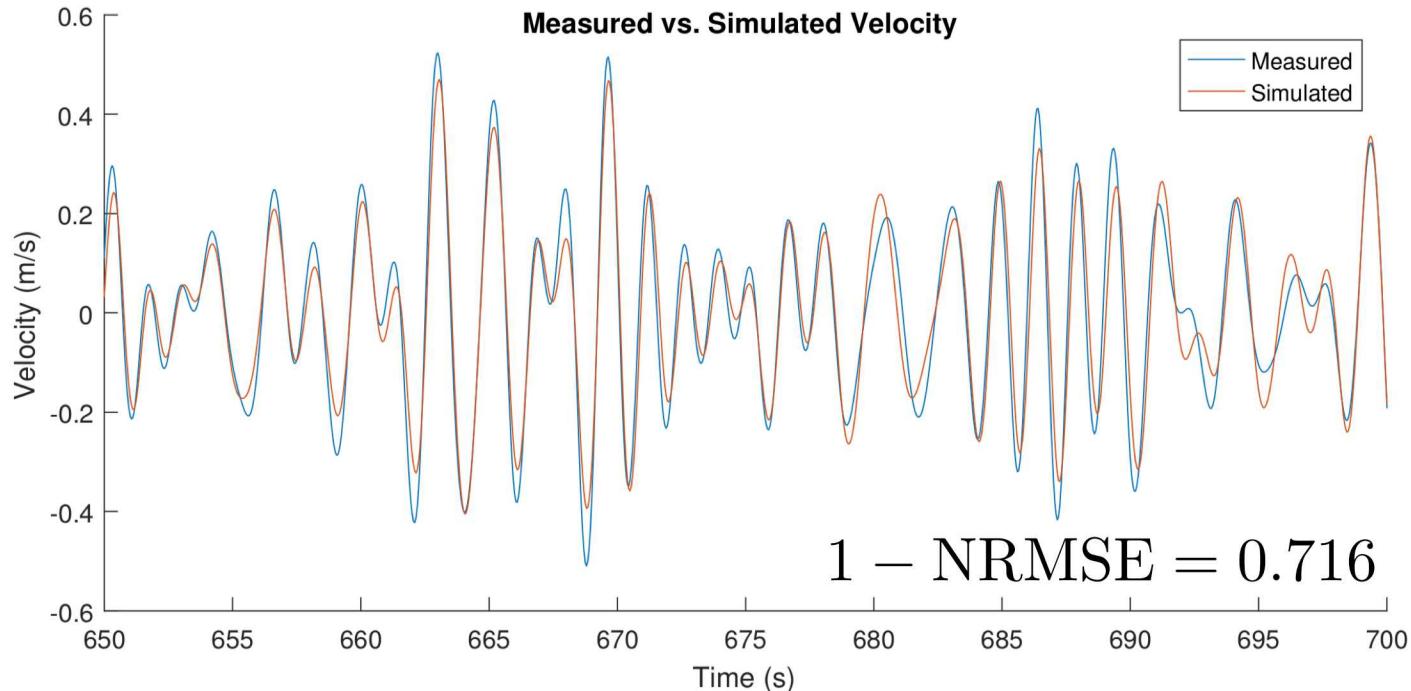
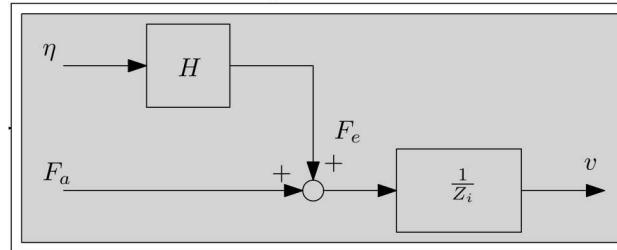
# Model validation



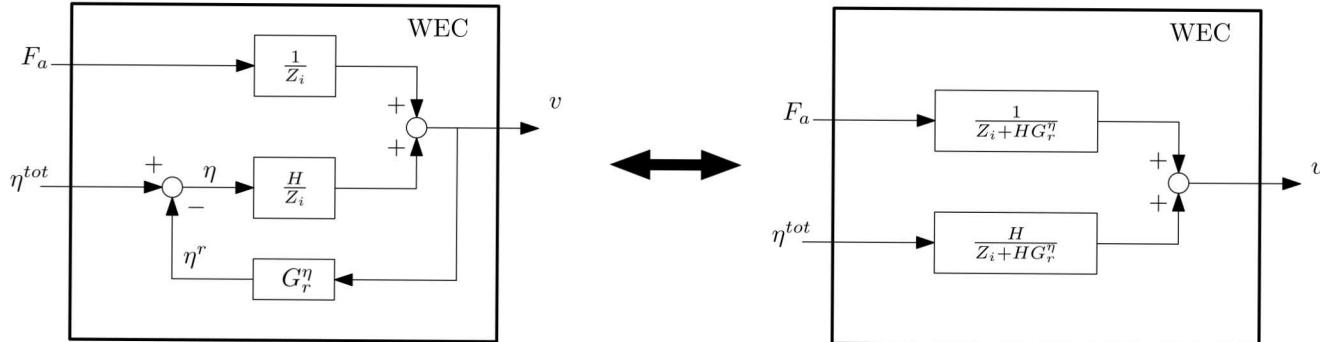
# Model validation



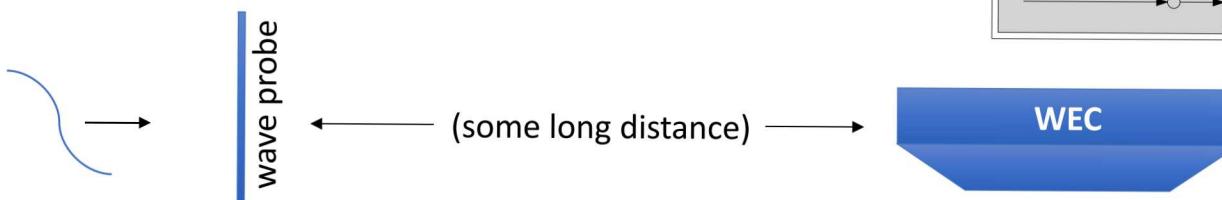
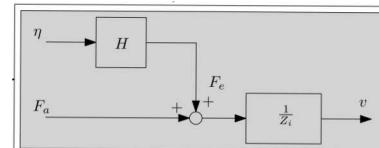
# Model validation



# Multiple-Input Single-Output (MISO)

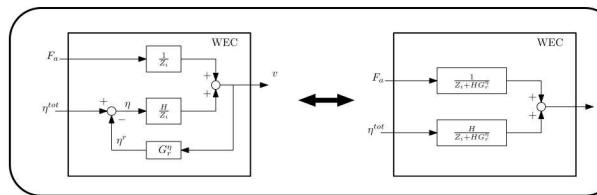


$$v = \underbrace{\frac{1}{Z_i + HG_r^\eta} F_a}_{\text{Actuator (PTO)}} + \underbrace{\frac{H}{Z_i + HG_r^\eta} \eta^{tot}}_{\text{excitation}} \Big|_{G_r^\eta \rightarrow 0} \approx \frac{1}{Z_i} F_a + \frac{H}{Z_i} \eta^{tot}$$

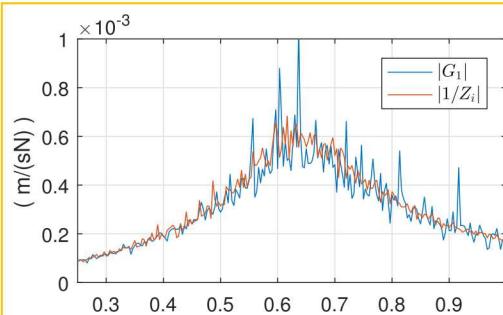


# MISO model

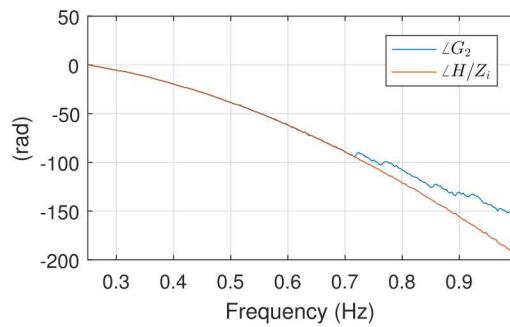
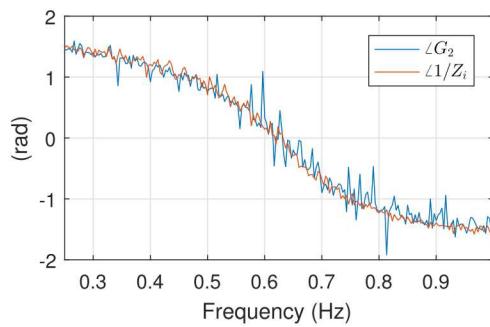
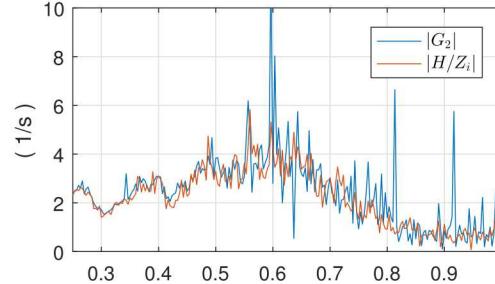
## MISO vs. radiation/diffraction



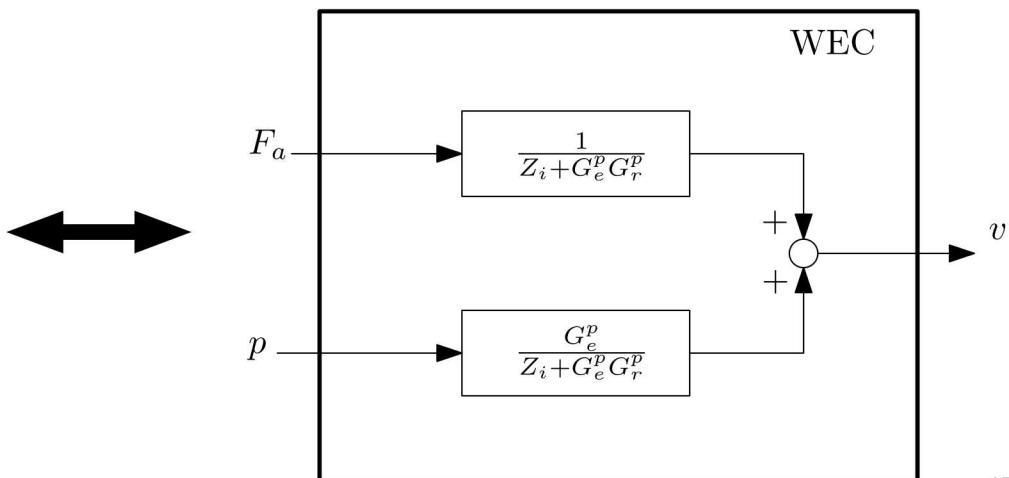
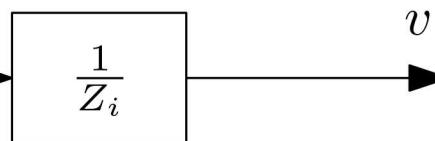
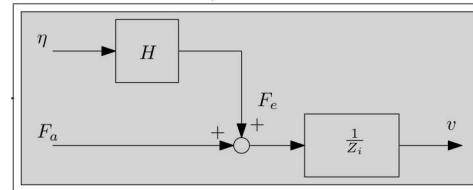
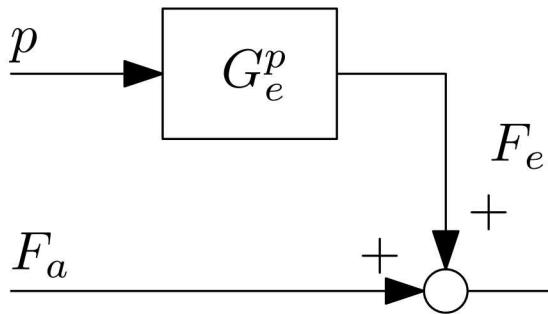
impedance/admittance



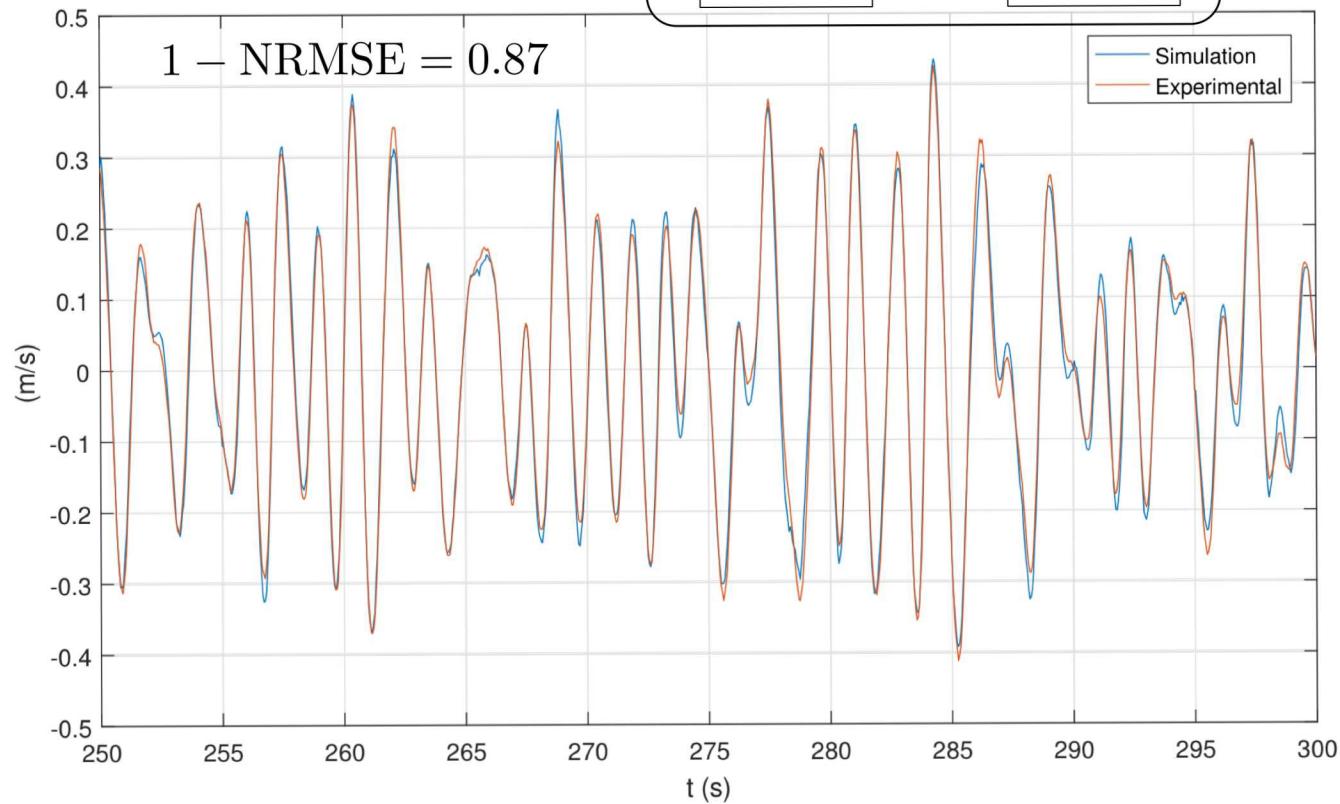
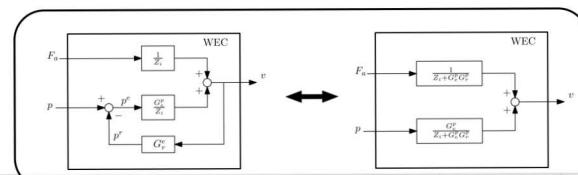
excitation



# Pressure as an input



# MISO pressure



# Modeling: nonlinearities

## NL hydrostatics

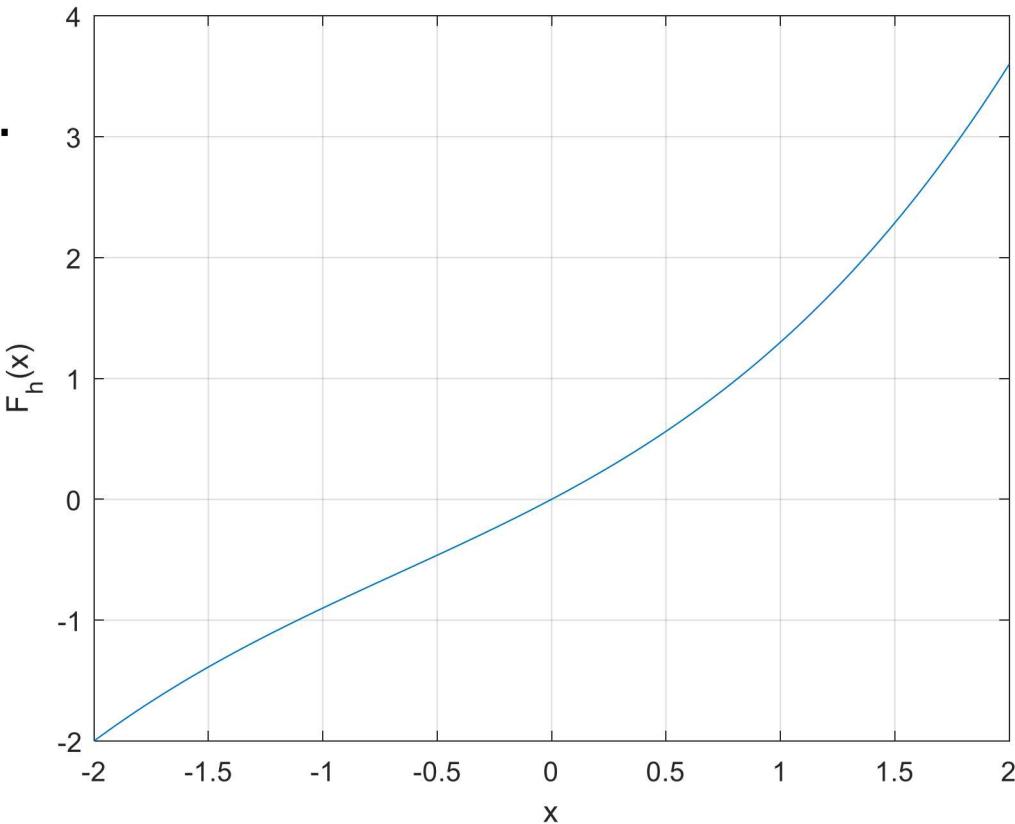
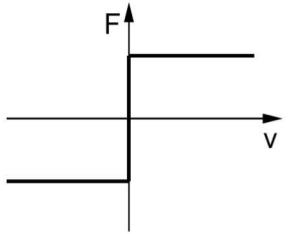
$$F_h(x) = k_1 x + k_2 x^2 + k_3 x^3 \dots$$

## NL drag

$$F_d(v) = b_1 v + b_2 v|v| + b_3 v^3 \dots$$

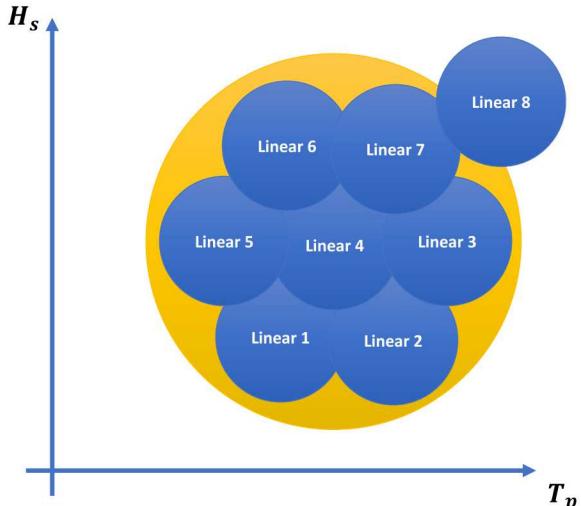
## Saturations

$$F_c(v) = c_1 \text{sign}(v)$$

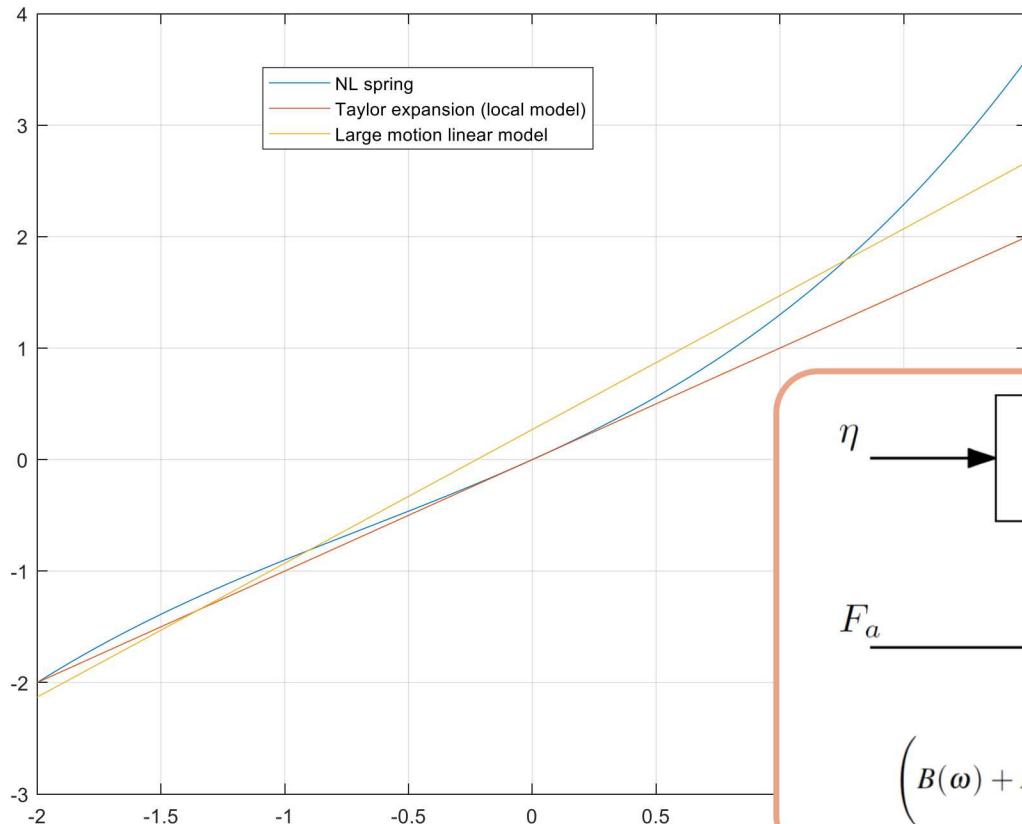


# Linear vs. Nonlinear models

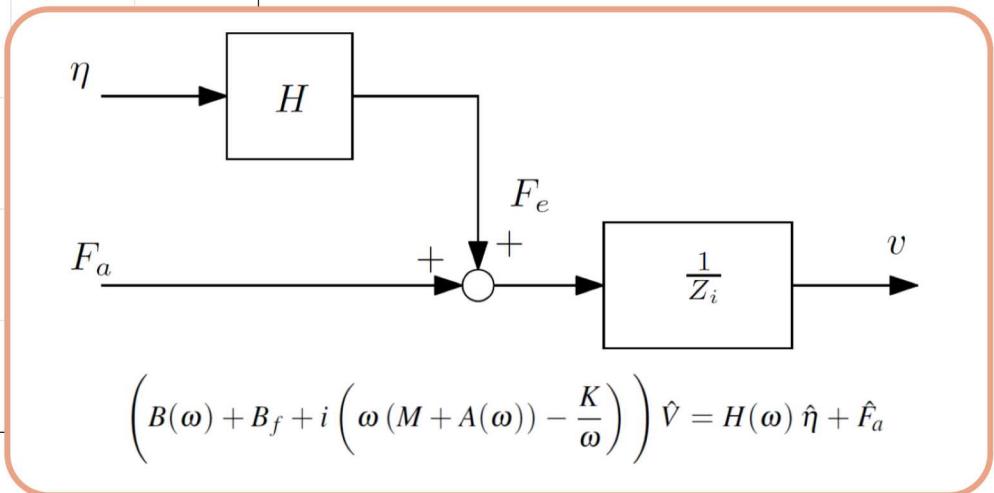
- Non Linear:
  - Pro
    - More accurate description of system dynamics over broader region of operation
    - Better performing control
  - Cons
    - More difficult to identify
    - More difficult for control design
    - May be less “robust” (good interpolators, but may not be good extrapolators)
- Linear
  - Pro
    - Identification is much easier (plenty of tools and theory available)
    - Control design is easier (plenty of tools and theory available)
    - Can have many “local model” and controllers (e.g. Gain scheduling )
  - Cons
    - Local approximation (models are good only around a region of operation)
    - Certain systems cannot be approximated by linear models



# Linearization of non linear models

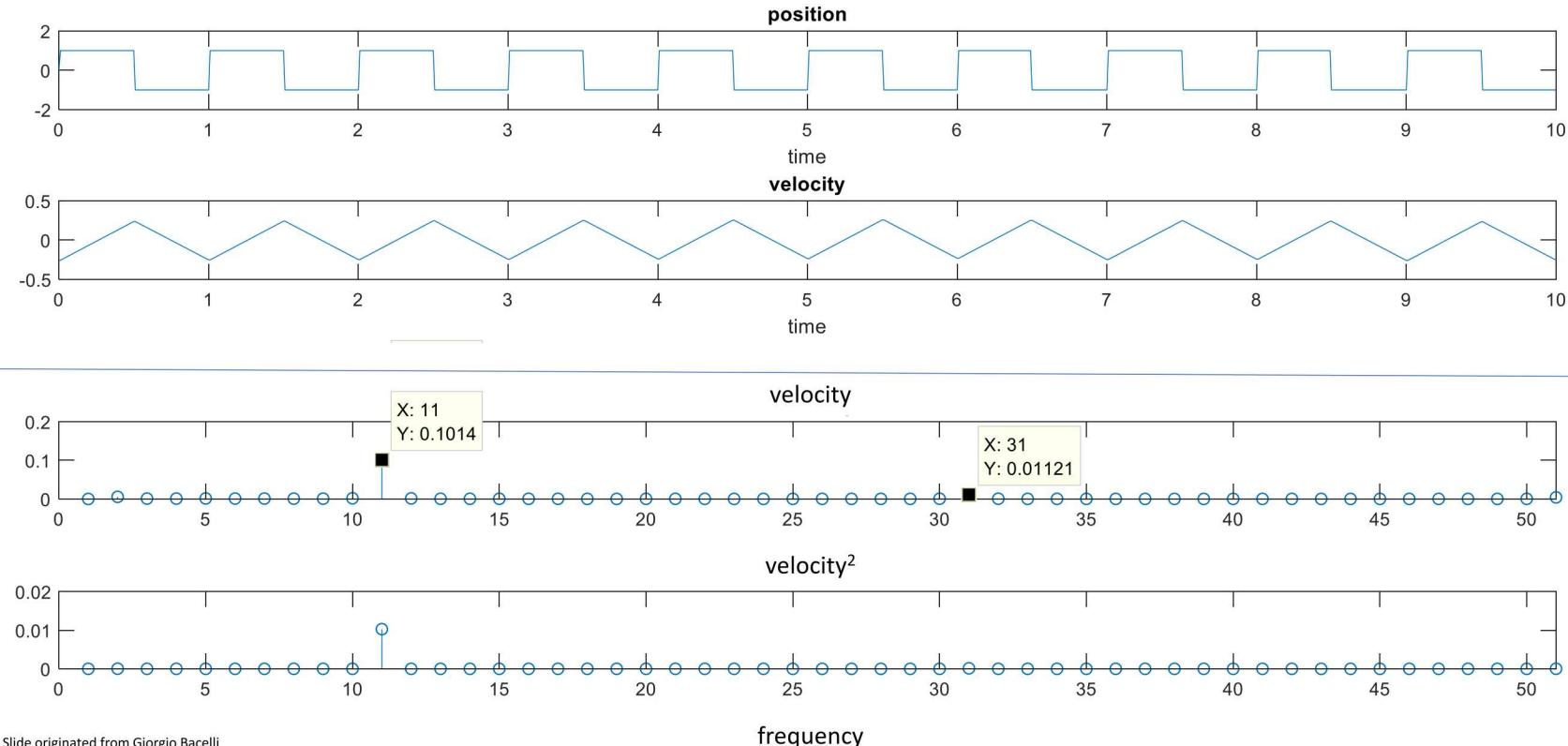


- Large motion linear models vs small motion linear model (Taylor expansion)
- Same structure, but different coefficients

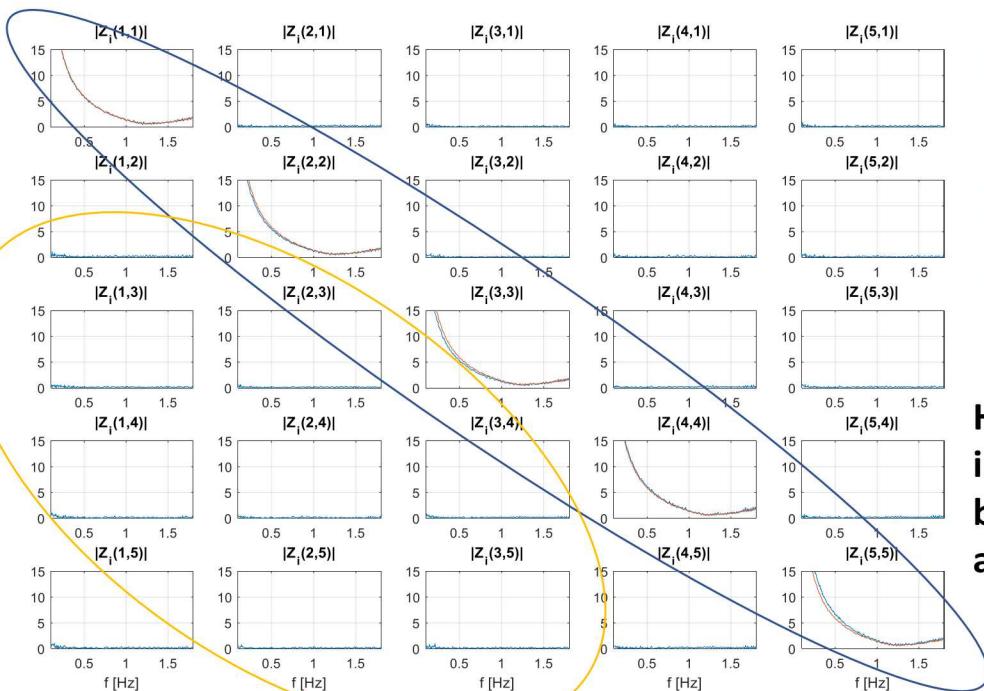


# Nonlinearities

- How important is it to consider nonlinearities?
- Example: Spectral content of square wave (Parseval's identity)



# Array testing



Hydrodynamic interactions between devices are small (<10%)

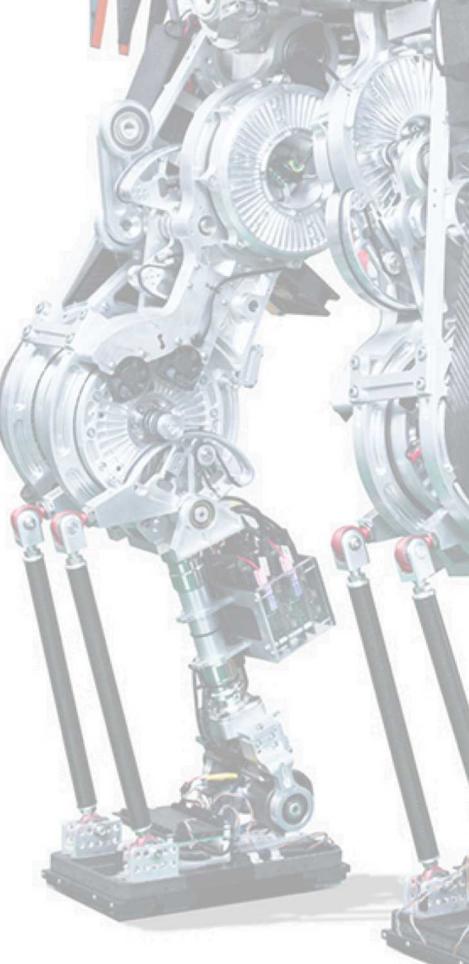


Electrical interaction more important

Coffee Break (15 mins)

# Implementing WEC control

Presented by Ryan Coe



# Dynamical Systems

*"particle or ensemble of particles whose state varies over time and thus obeys differential equations involving time derivatives."*

If linear

Time domain:  
states-space (ODE)

$$\begin{aligned}\dot{\mathbf{x}}(t) &= A\mathbf{x}(t) + B\mathbf{u}(t) \\ \mathbf{y}(t) &= C\mathbf{x}(t) + D\mathbf{u}(t)\end{aligned}$$

Complex domain:  
Transfer function

$$H(s) = \frac{Y(s)}{X(s)}$$



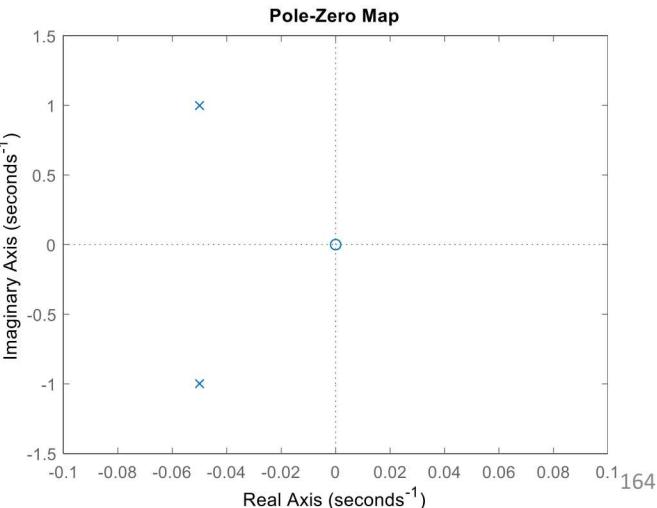
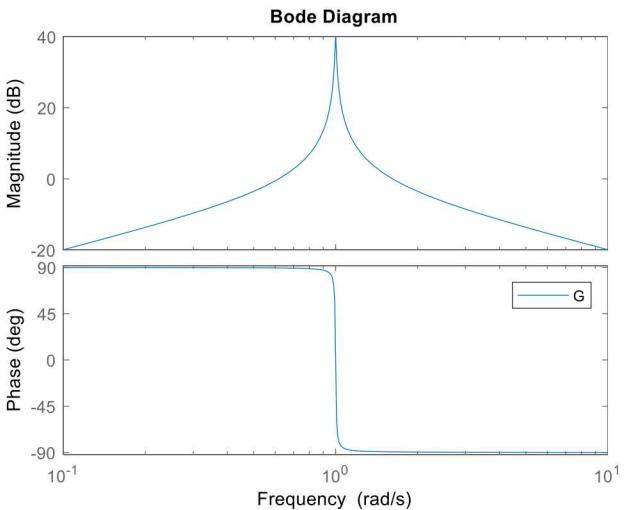
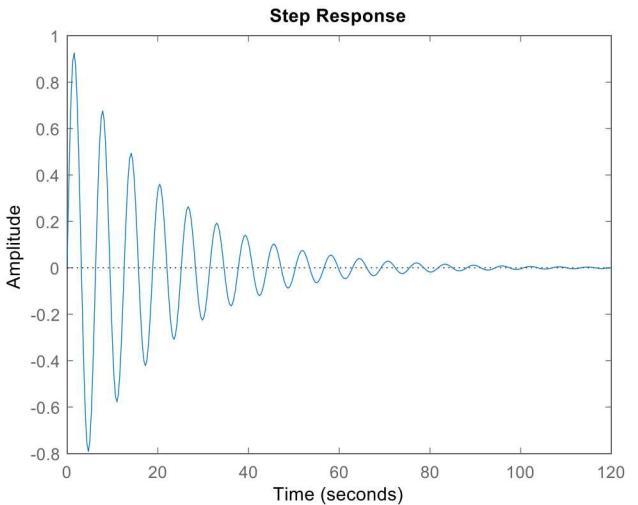
Laplace transform

If  $s = j\omega$   $\rightarrow$  Frequency domain

# Dynamical Systems: analysis

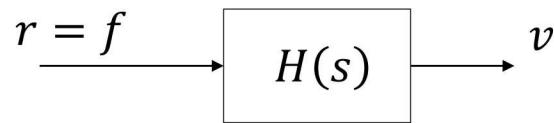
Example: Mass-Spring-Damper

$$H(s) = \frac{v}{f} = \frac{s}{m s^2 + b s + k}$$



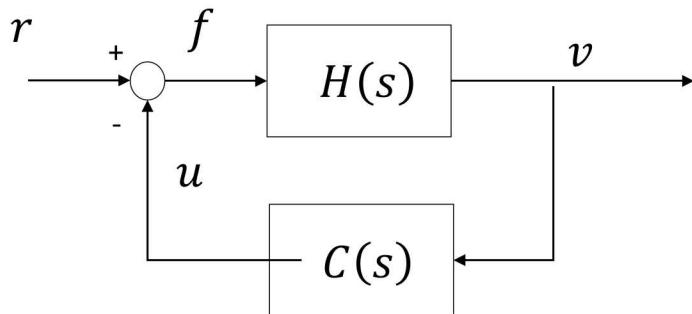
# Control of dynamical system

## *Uncontrolled system*



$$\frac{out}{in} = \frac{v}{r} = \frac{v}{f} = H(s)$$

## *Controlled system*



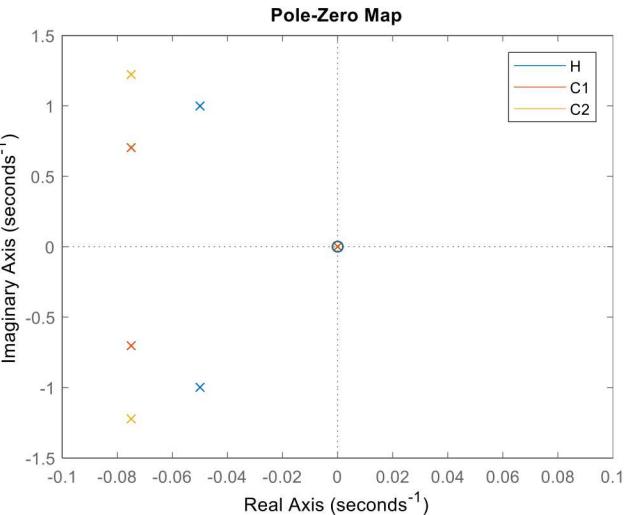
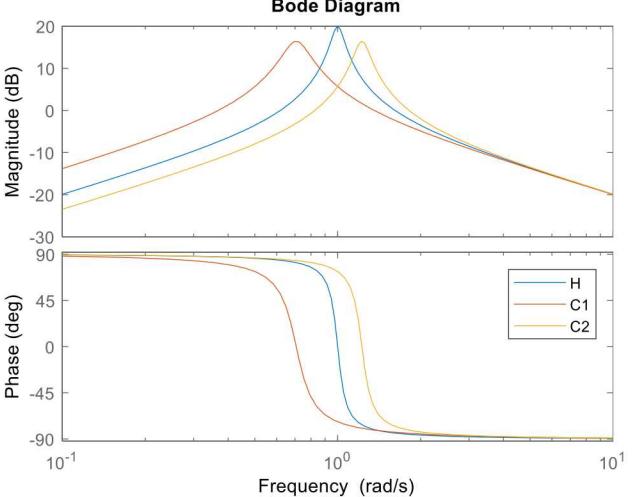
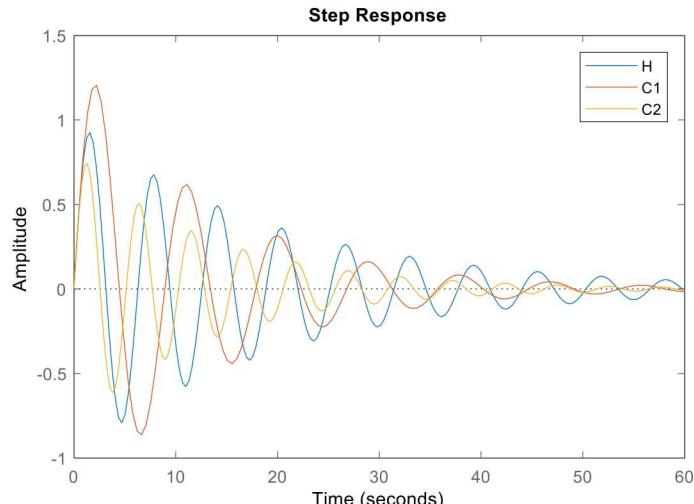
$$\frac{out}{in} = \frac{v}{r} = \frac{v}{f + u} = \frac{H(s)}{1 + H(s)C(s)}$$

# Control of dynamical system

*What happens to the system when it's being controlled?*

$$H(s) = \frac{s}{m s^2 + b s + k} \quad C(s) = K_p + \frac{K_i}{s}$$

$$\frac{H(s)}{1+H(s)C(s)} = \frac{s^2}{s^3 + b_2 s^2 + b_1 + b_0}$$



# Example: importance of linear analysis

Even if the system is nonlinear, linear analysis is still very important

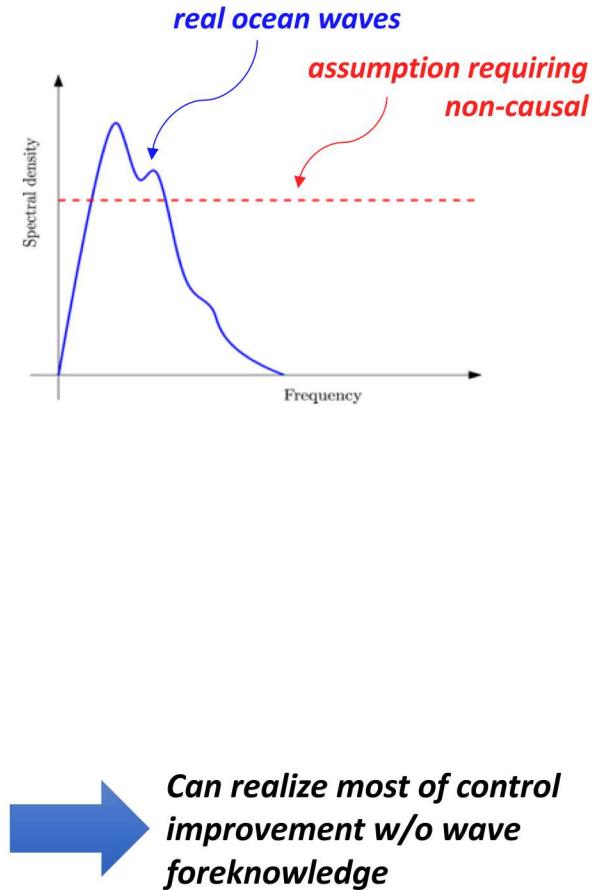
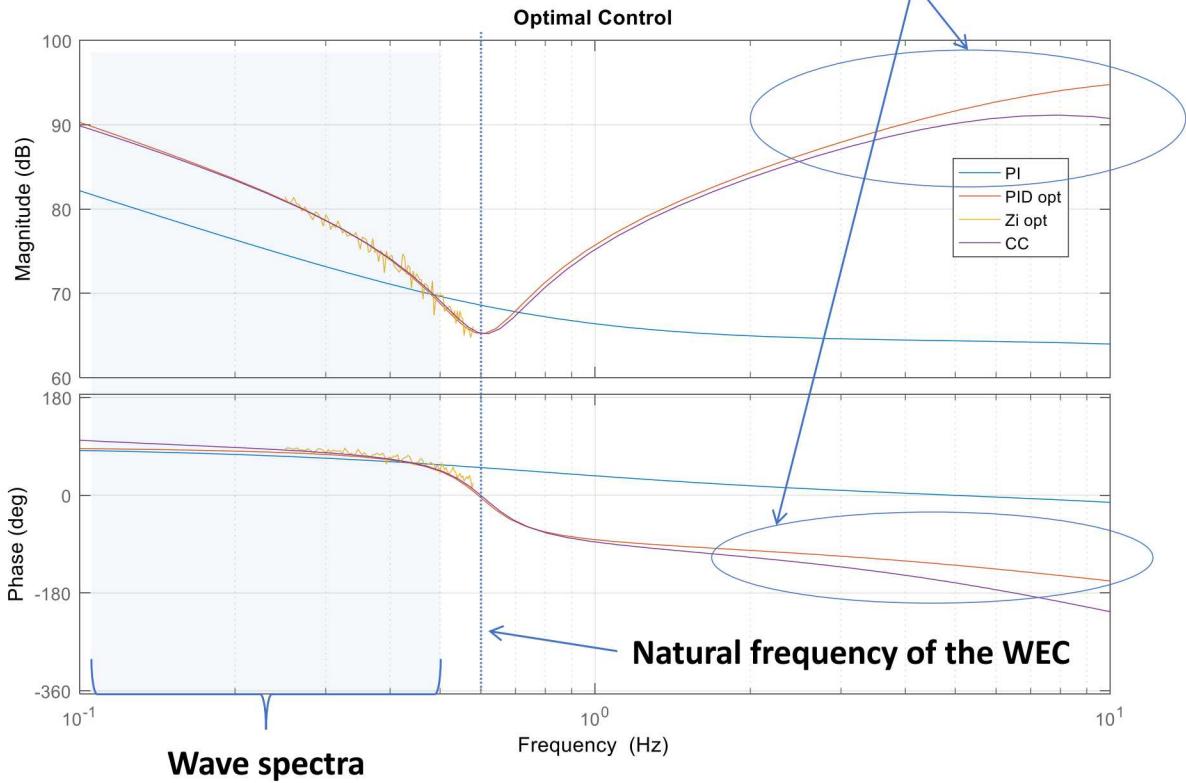


**Figure 6.** NASA X-29 forward-swept-wing aircraft (photo courtesy of NASA).

*“...You see, all of the various control design teams used **modern digging machines** early in the design process. As a result, we were **well insulated from the fundamental difficulties** imposed by the airplane’s violent open-loop instability. ... We discovered only at the last moment that the vehicle was almost too unstable to control with the given hardware.”*

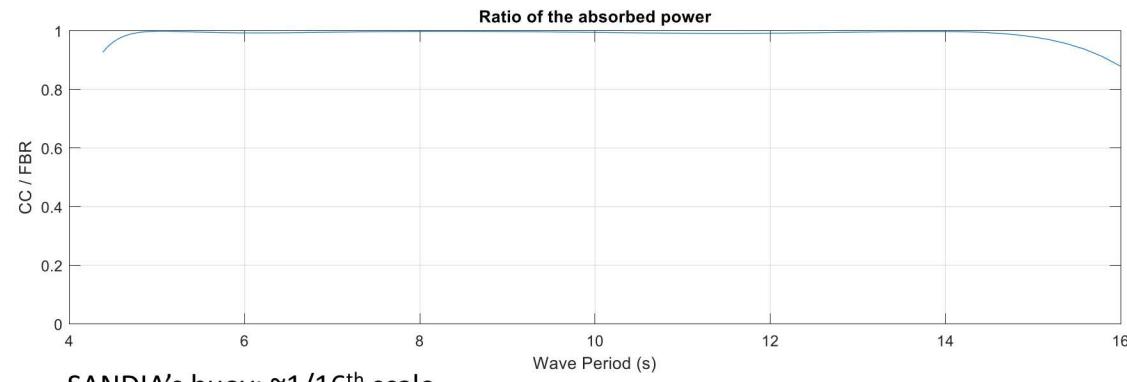
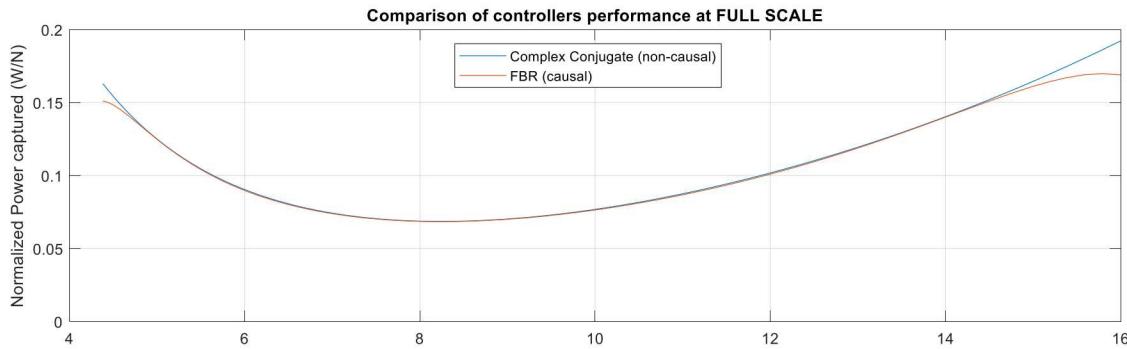
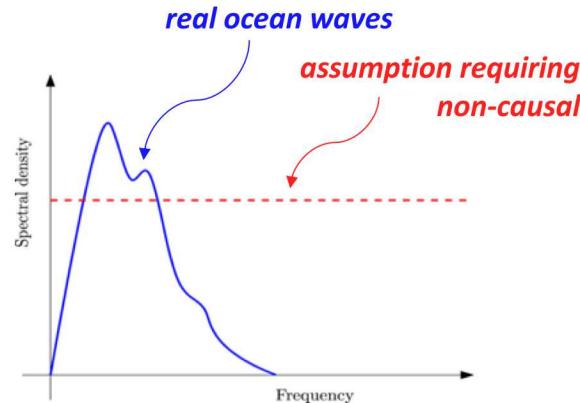
# How essential is wave foreknowledge?

*NON-CAUSALITY shows up in the asymptotic behavior (freq  $\rightarrow \infty$ )*



# How essential is wave foreknowledge?

Let's make some (reasonable) assumption: band limited wave spectra



Real ocean waves are band-limited



Causal FBR Controller is almost as efficient as Non causal CC controller in a limited frequency band (95%-100%)

Can be tuned to different Frequency bands for different scales

# Control design

Modeling

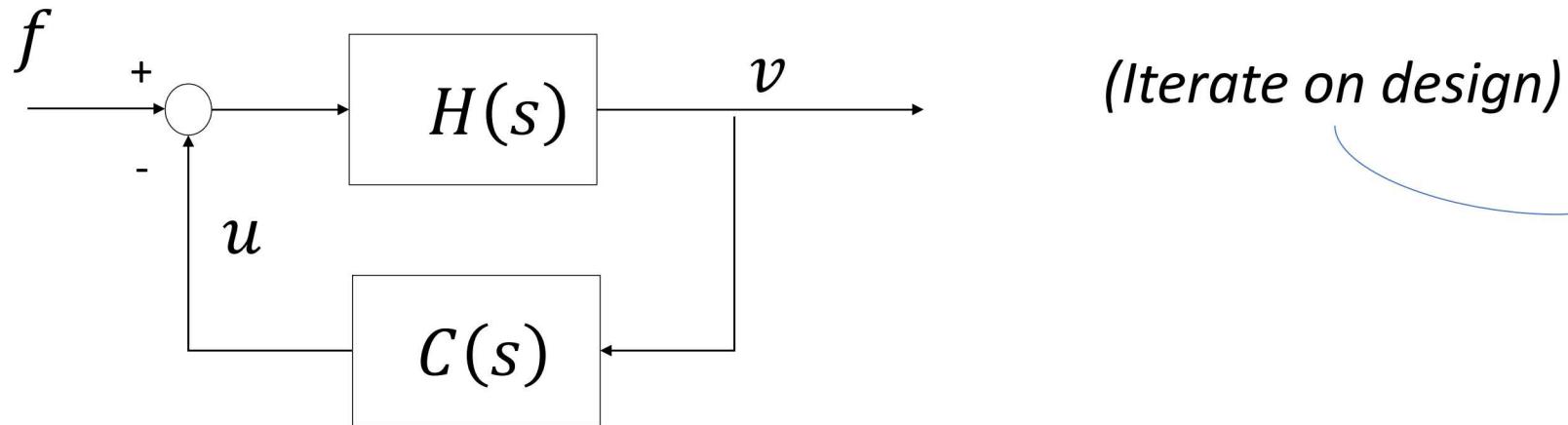
$$H(s)$$

Measurement and Estimation

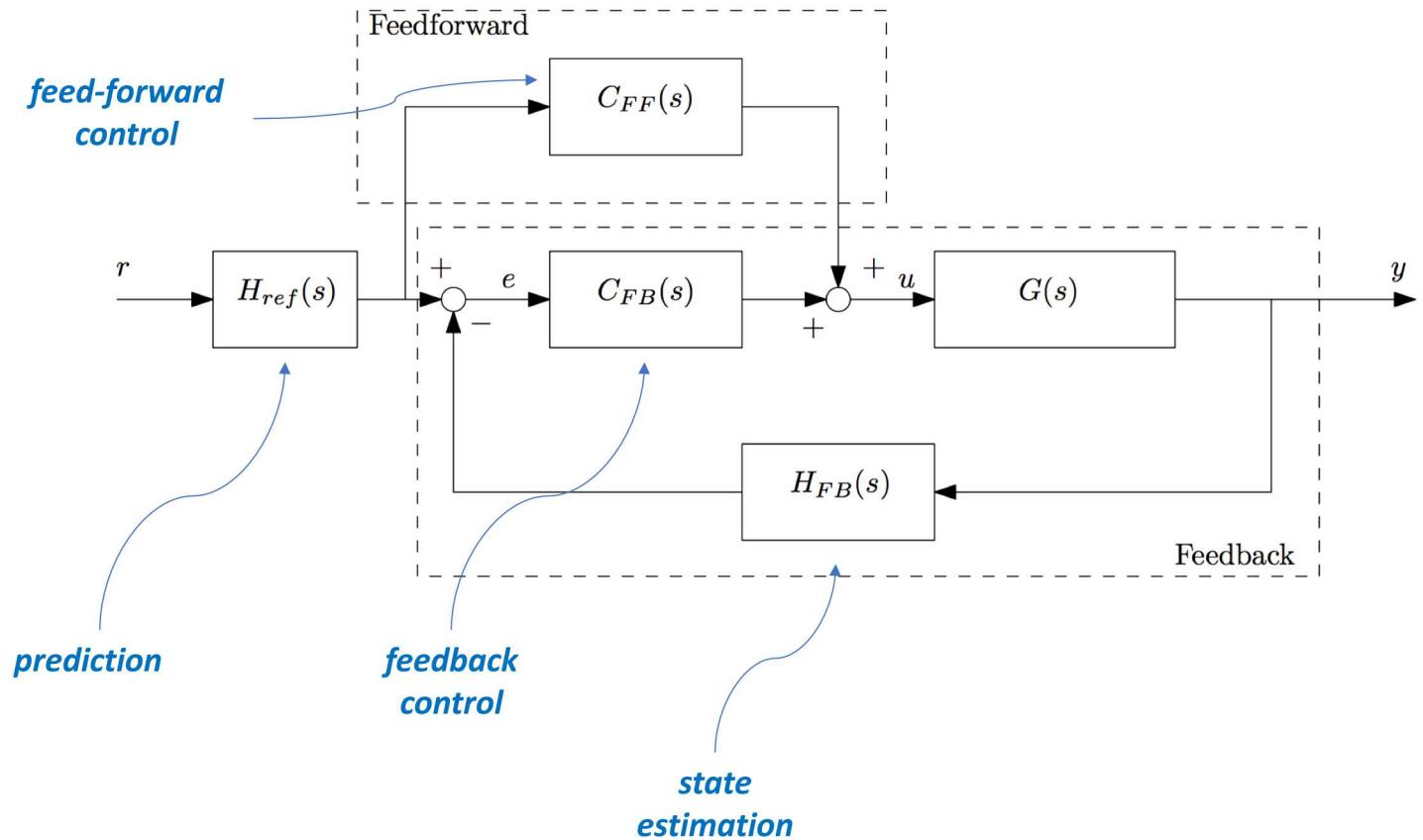
$$\mathcal{V}$$

Controller

$$C(s)$$



# Implementation of control on a numerical model

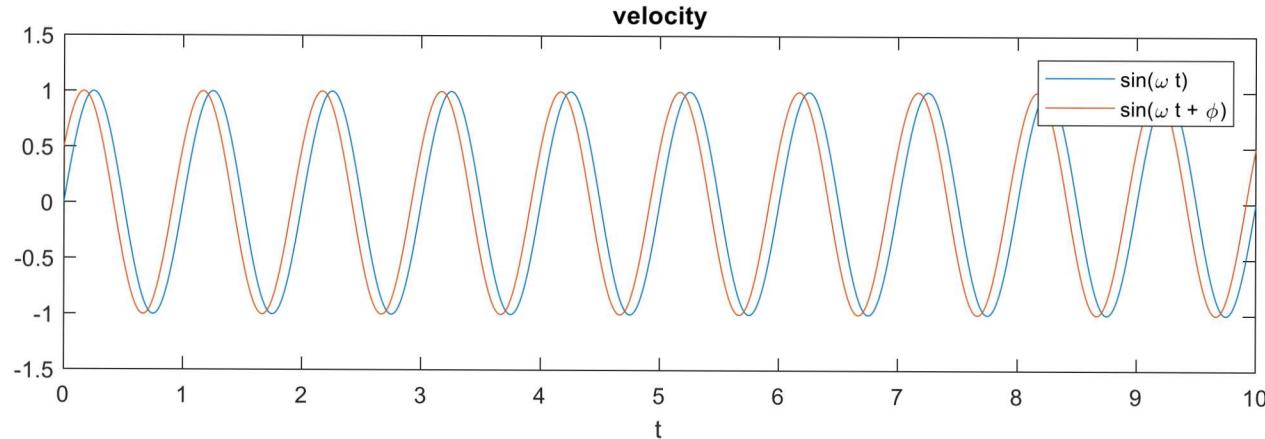


# Implementation of control on hardware

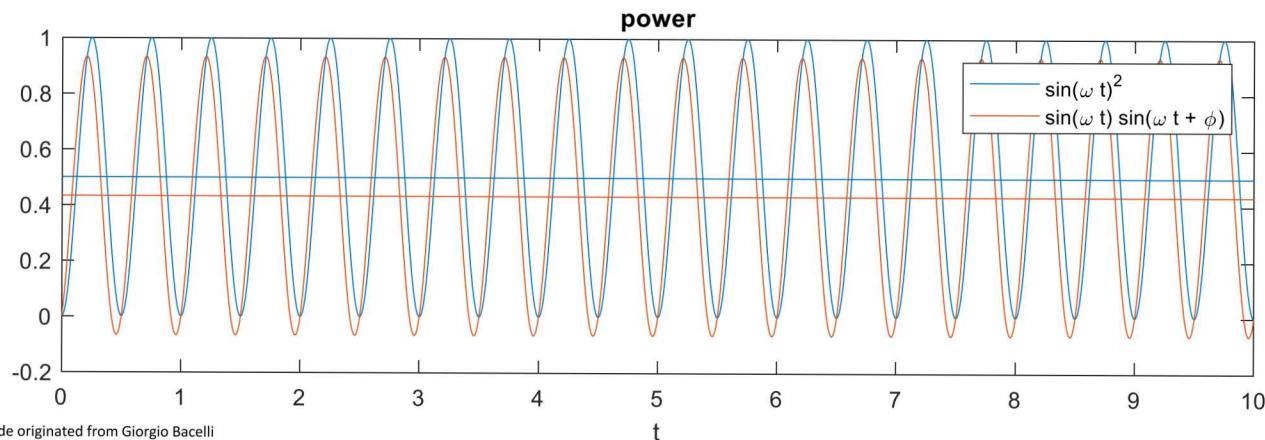
- Key considerations for sensor selection
  - Saturation limits
  - ***Frequency response***
  - Signal type (minimize noise)



# Implementation of control on hardware



Oscillating system, phase is important



# Practical aspects – Real-time systems

- What is a real-time (RT) system
  - Hard RT
  - Soft RT
- Very basic example: Calculate velocity from position
  - $v = dx/dt$
  - In RT systems,  $dt$  is constant
  - In Non-RT systems  $dt$  may not be constant -> velocity not calculated accurately

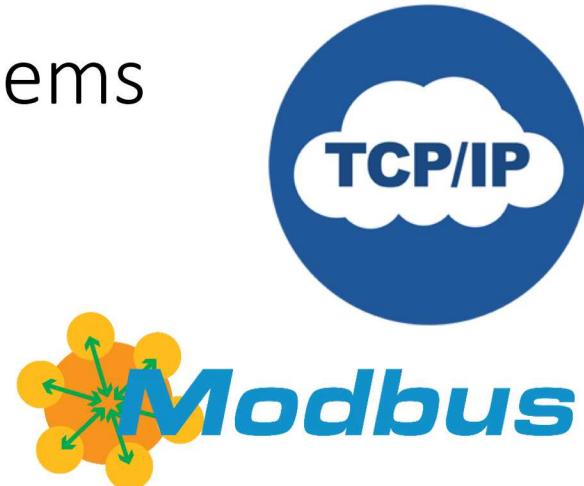
# Practical aspects – Real-time systems

## ***Ethernet is fast, right?***

All of the packets go to all of the nodes, and collisions between data packets are a serious problem

Data can take variable paths and therefore variable times to travel from the sending node to the receiving node

→ Rate of communication is fast, but the time span (the determinism) in which a response is expected is unpredictable



# Practical aspects – DAQ/RT

- Discretization
  - sampling time
- Quantization
  - amplification/signal conditioning
- Filtering
- Communication
  - Bandwidth
  - Synchronization
  - Determinism
- Software
  - Research vs. production



# Practical aspects - PTO design, modeling and control



## Small Scale

Torque tracking for full scale PTO emulation and control

## Large scale

Torque tracking no longer highest priority

Objective is maximize power, and satisfy constraints, therefore we need very good model for control design.

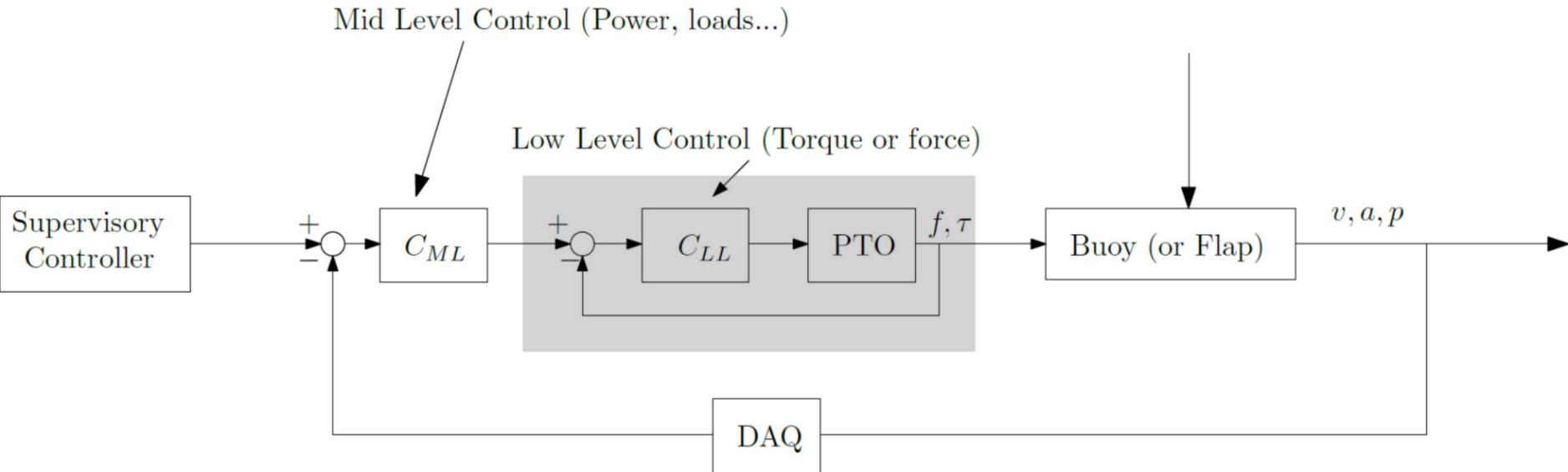
Good model also necessary for device (WEC+PTO+control) optimization



# Design

Need to look at the dynamic of the whole system for design

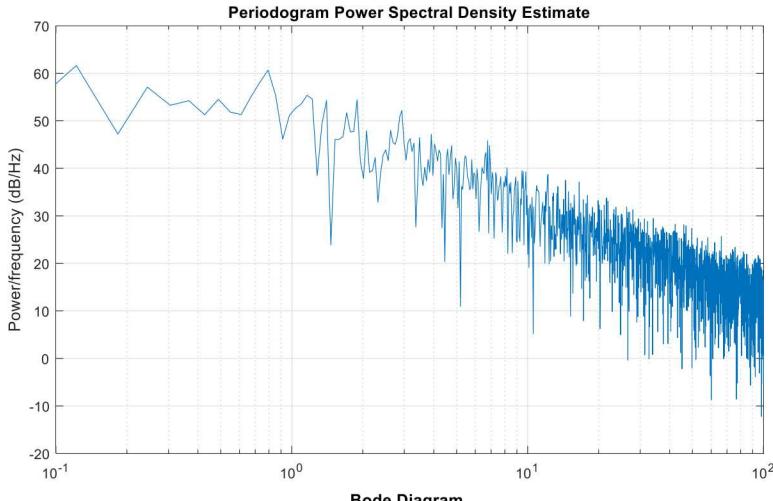
Excitation Force (waves)



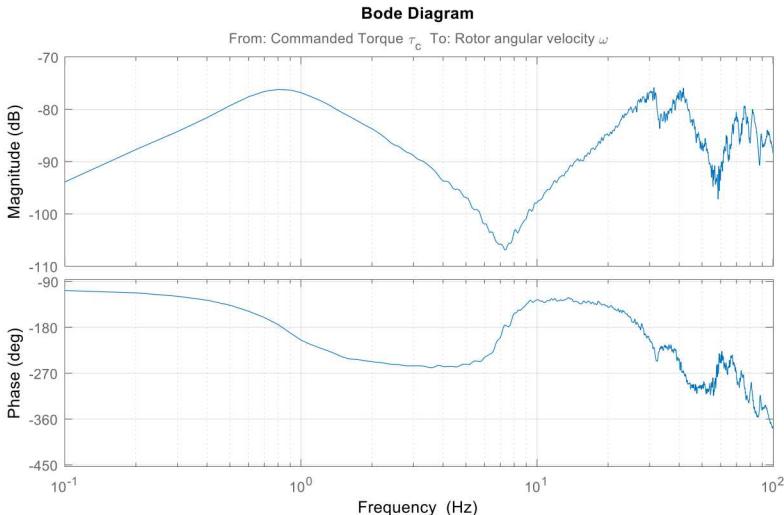
The system needs to be designed as ONE block  
(at least until we have accumulated enough experience to develop good practice)

# Drivetrain model – SID

*Input signal: LPF white noise* 



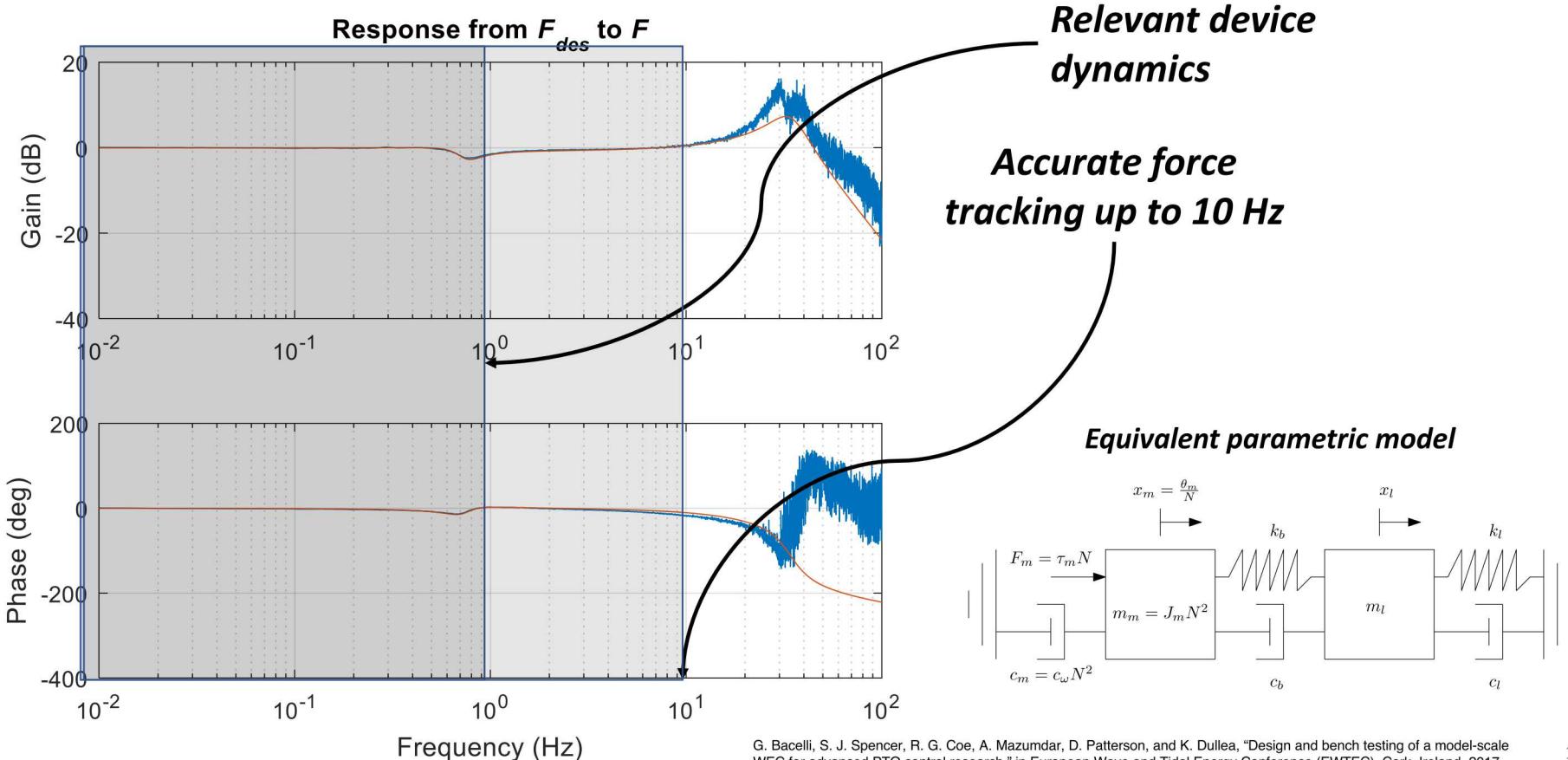
*Response: torque to velocity* 



# Drivetrain model – SID



# Drivetrain model – parametric



# Extreme response & fatigue

Presented by Ryan Coe and Yi-Hsiang Yu

# Extreme Condition Modeling Workshop (May13-14, 2014)



Sandia  
National  
Laboratories

## Extreme Conditions Modeling Workshop Report

R.G. Coe and V.S. Neary  
Sandia National Laboratories

M.J. Lawson, Y. Yu and J. Weber  
National Renewable Energy Laboratory

The Extreme Conditions Modeling Workshop was organized and run by the National Renewable Energy Laboratory and Sandia National Laboratories with funding from the Wind and Water Power Technologies Program within the U.S. Department of Energy's Office of Energy Efficiency and Renewable Energy.

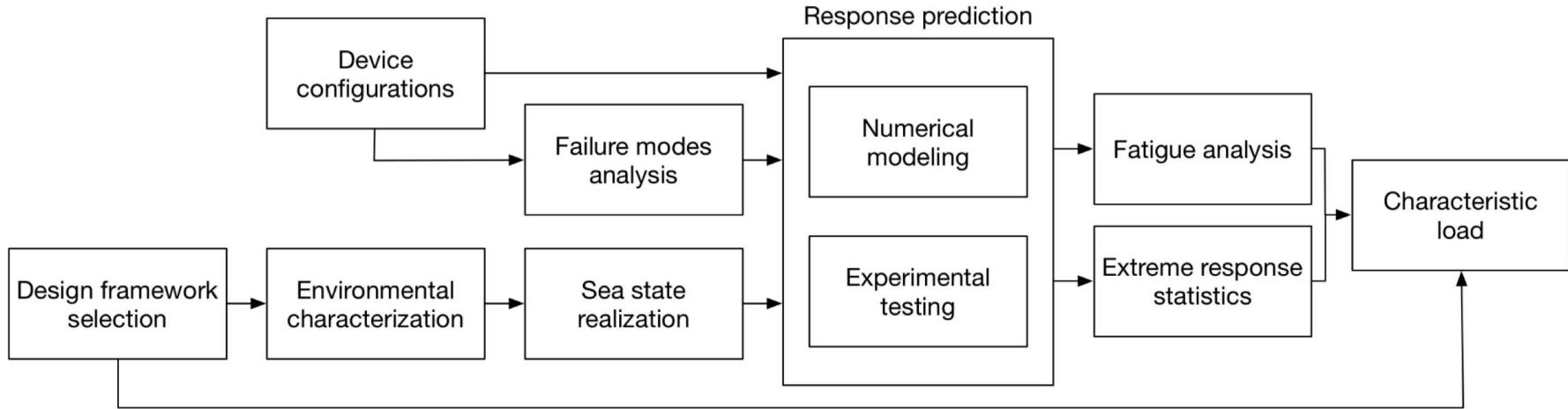
The National Renewable Energy Laboratory is a national laboratory of the U.S. Department of Energy, Office of Energy Efficiency and Renewable Energy, operated by the Alliance for Sustainable Energy, LLC.

Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

Technical Report  
NREL/TP-5000-42305 - SNL/SAND2014-16384R  
July 2014  
Contract No. DE-AC36-08GO28308

- More than 30 U.S. and European WEC experts from industry, academia, and national research institutes attended the workshop.
- WEC Device is designed to maximize its motion and wave-induced load at the dominant sea states, and offshore oil and gas platforms and ships are not.
- Not always the largest wave that causes extreme loads and more often it is a specific wave train (can be at a rated operational sea state).
- Nature of the irregular sea states makes extreme sea state characterization challenging and the prediction of the conditions that cause extreme loads is difficult.
- Move towards a risk-based design methodology

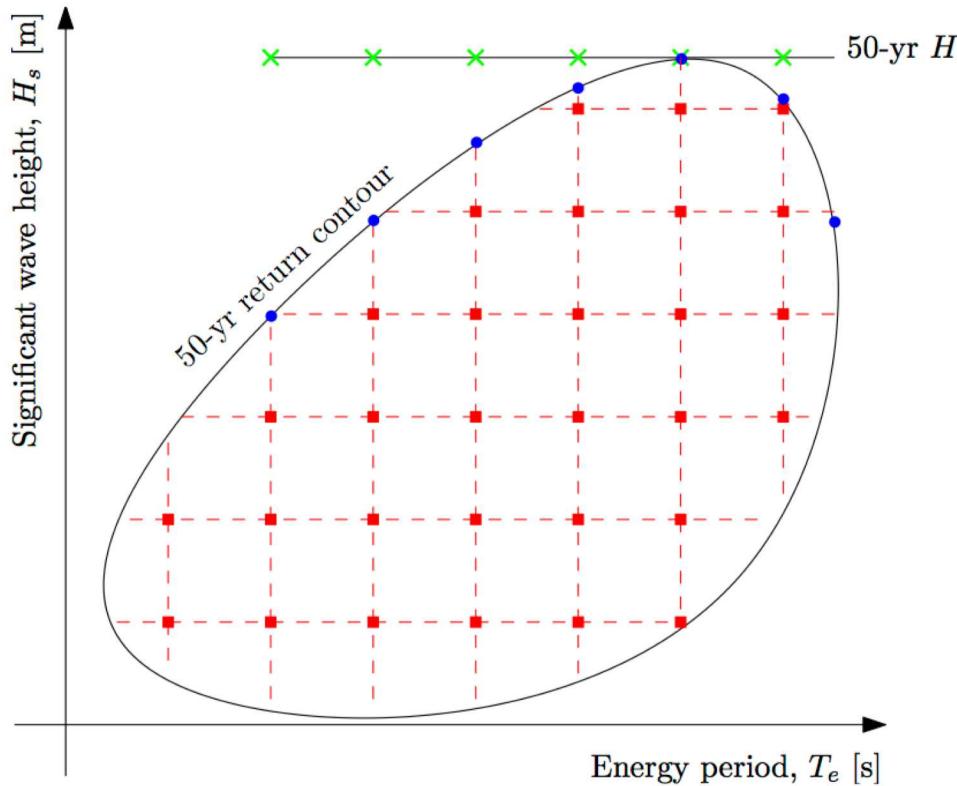
# Generalized design analysis process



# Survival analysis frameworks

***Which conditions will we analyze?***

- One-Dimensional
- Contour
- All-Sea-State

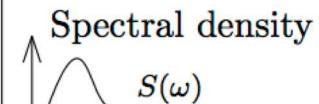


# Design waves

***Need to represent real ocean waves...***

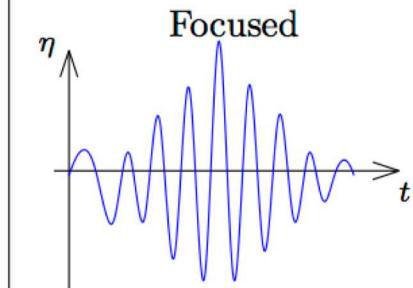
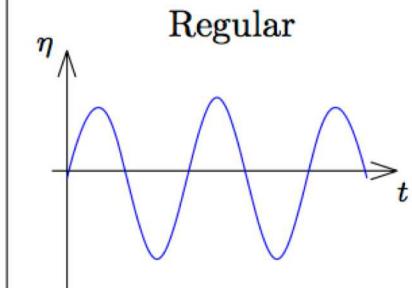
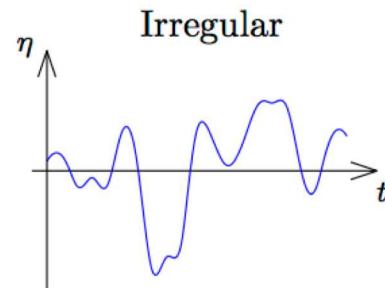
***Irregular sea states are often too long, or cannot be realized by hardware***

$$H_{s,100}, T_{p,100}$$



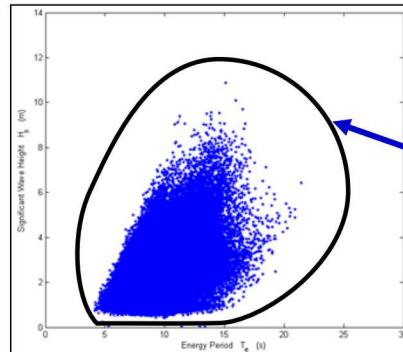
$$a\sqrt{H_{100}} \leq T \leq b\sqrt{H_{100}}$$
$$H_{reg} = 1.9H_s$$

New Wave,  
MLER,  
(other formulations)



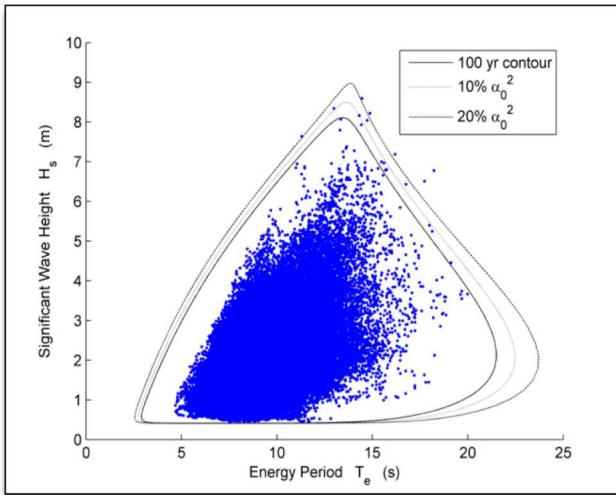
# Using Environmental Contours

- **Sea state contours** seek to determine (1) the characteristics of extreme events and (2) the probability of these events by using short term data ( $\sim 10$  years) to find a contour of variables that describes extreme events related to a given likelihood



Contour defines pairs of variables whose combination is related to an extreme event.

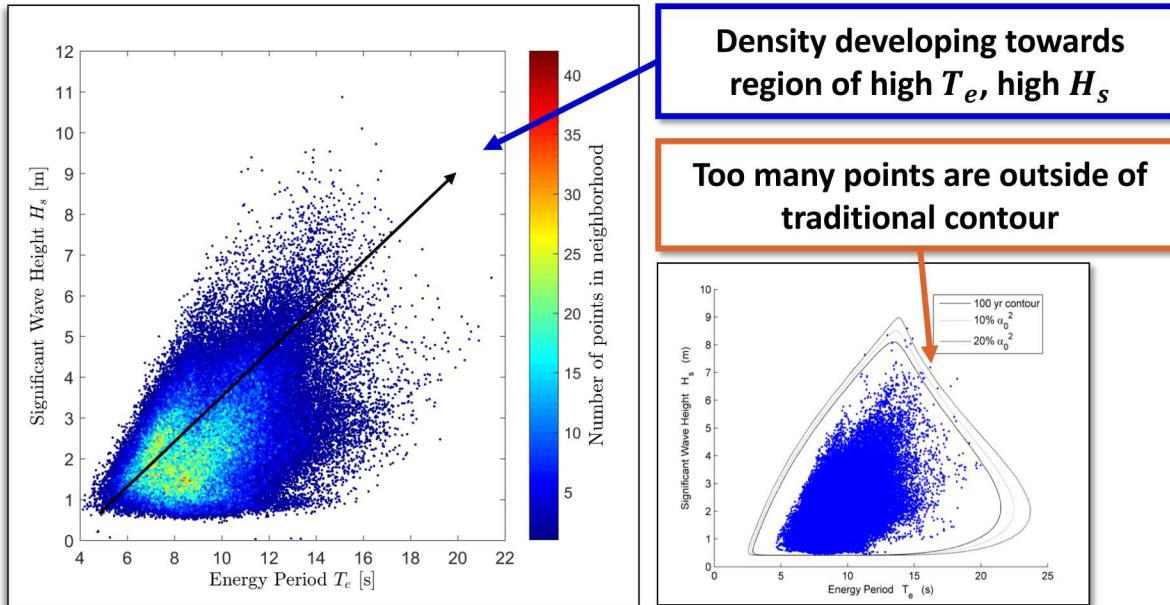
# Contour from Standard of Practice



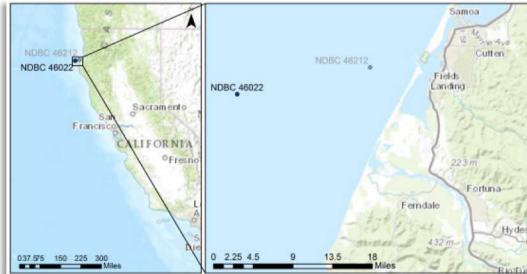
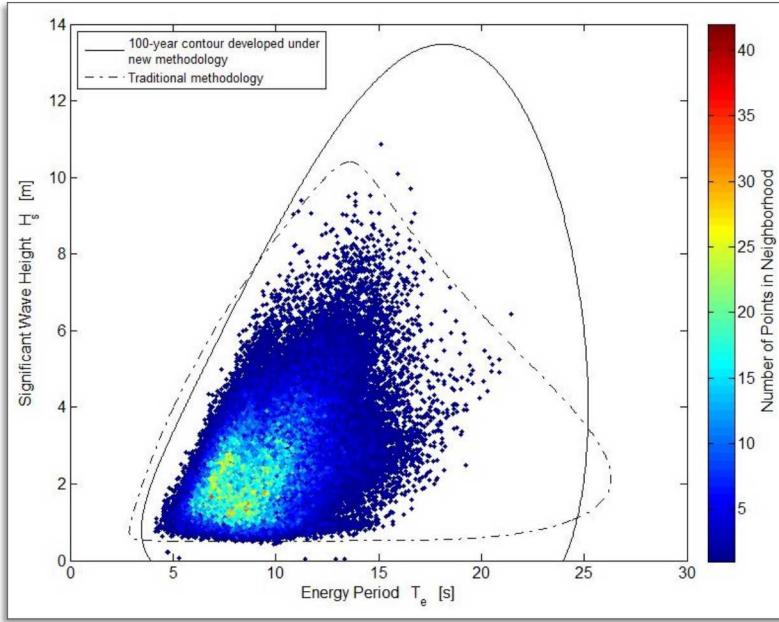
- Environmental contours derived from methodology presented in key papers that are widely cited (Haver and Winterstein, 2008) using **I-FORM** and applied in **design standards** for offshore structures

# Representing Data Density

- **Data trends in empirically calculated density** show that contour shape should include additional regions that parametric joint probabilities do not always capture



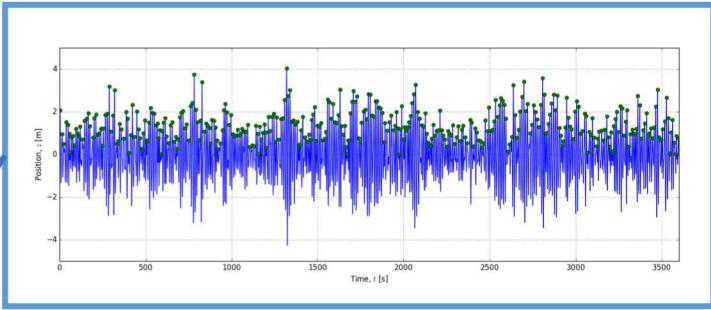
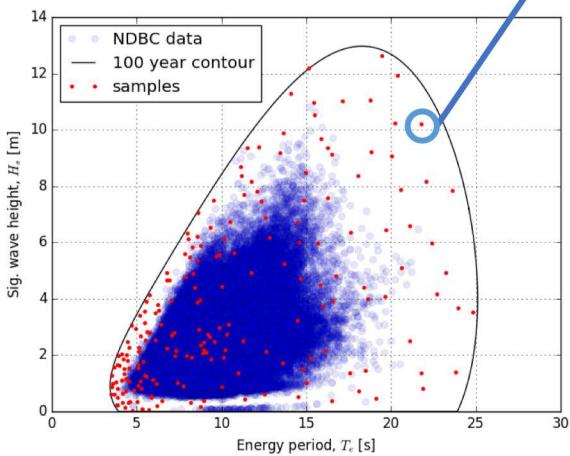
# PCA Contour Results



### *NDBC 46022 – Northern California site location.*

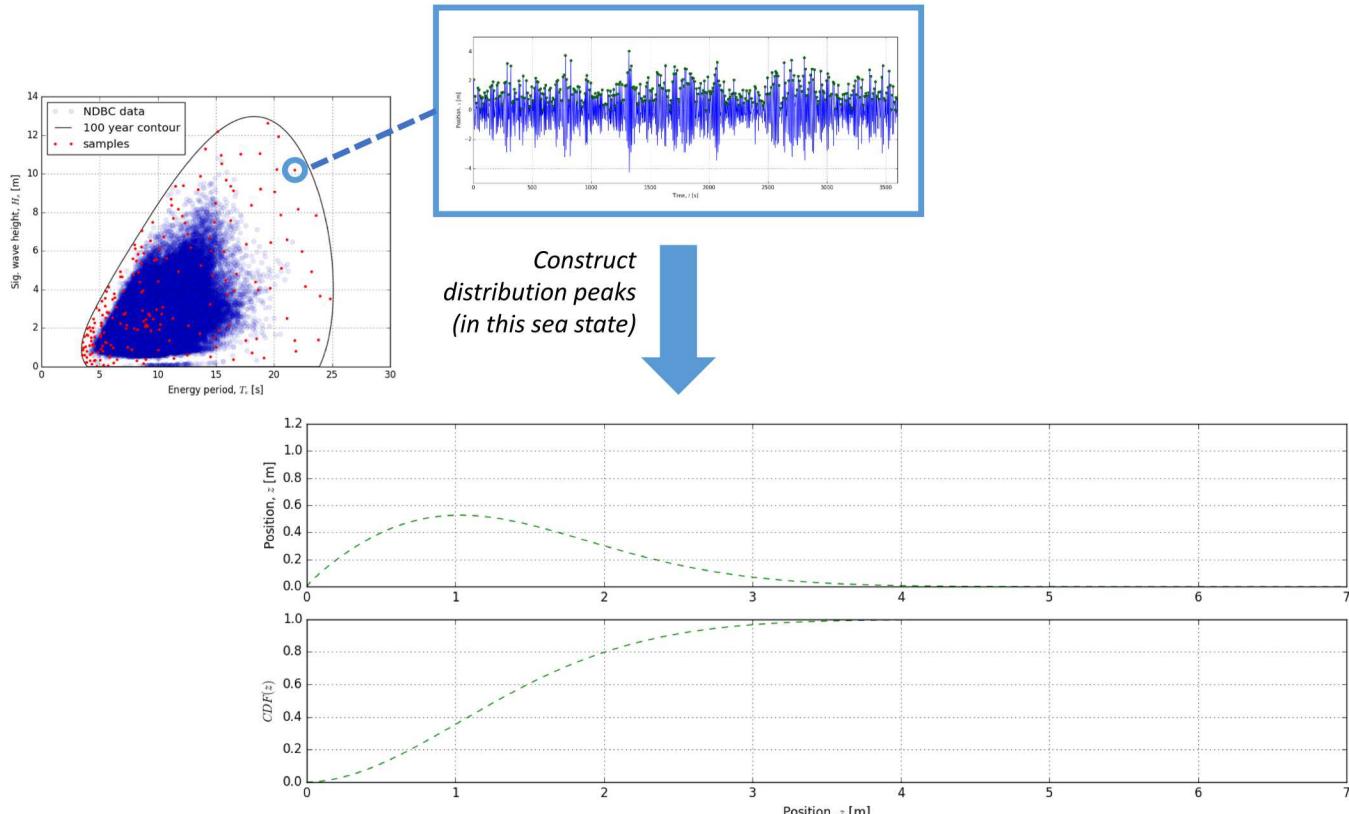
## NDBC 46022 – Northern California

# Design Response Statistics

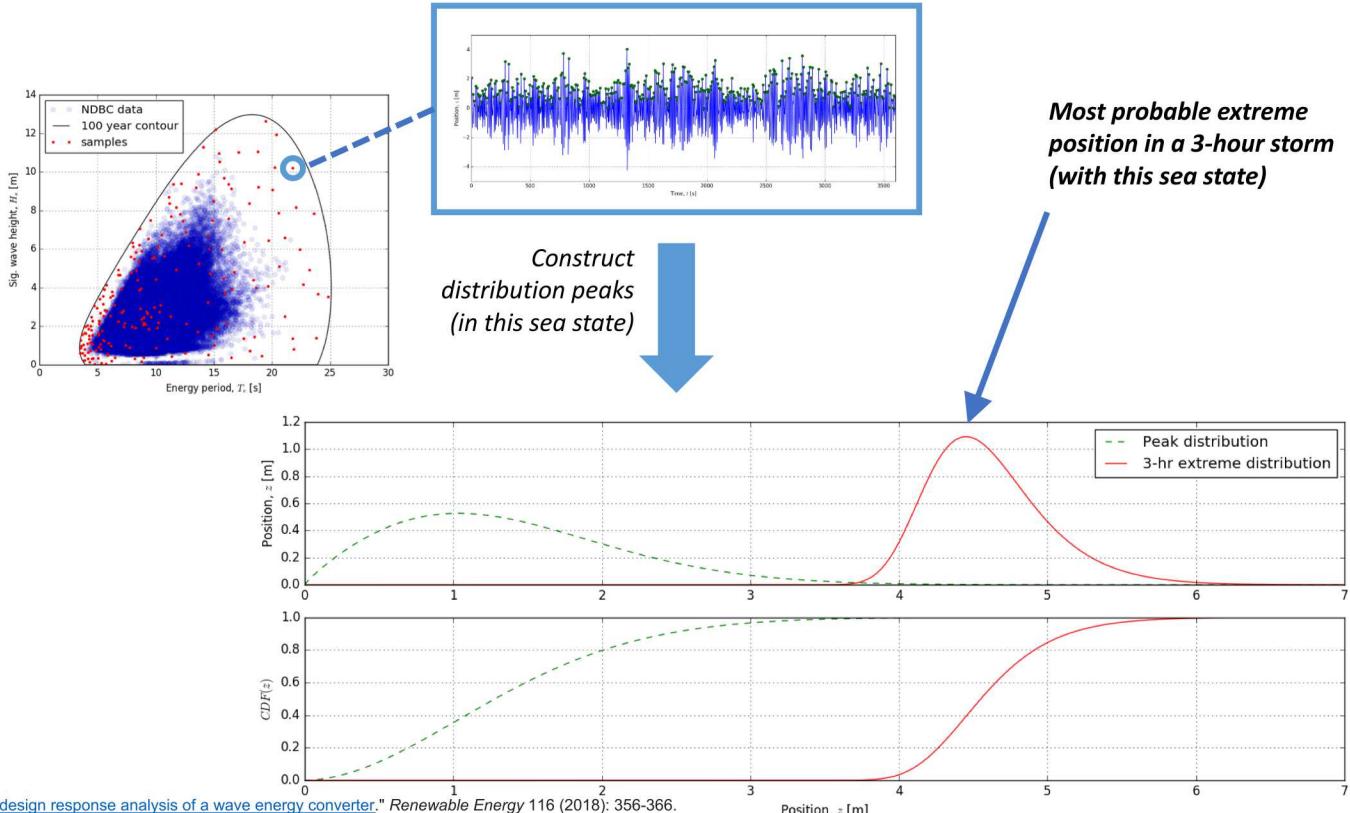


*Need to observe enough peaks in the response of interest to construct a stochastic description*

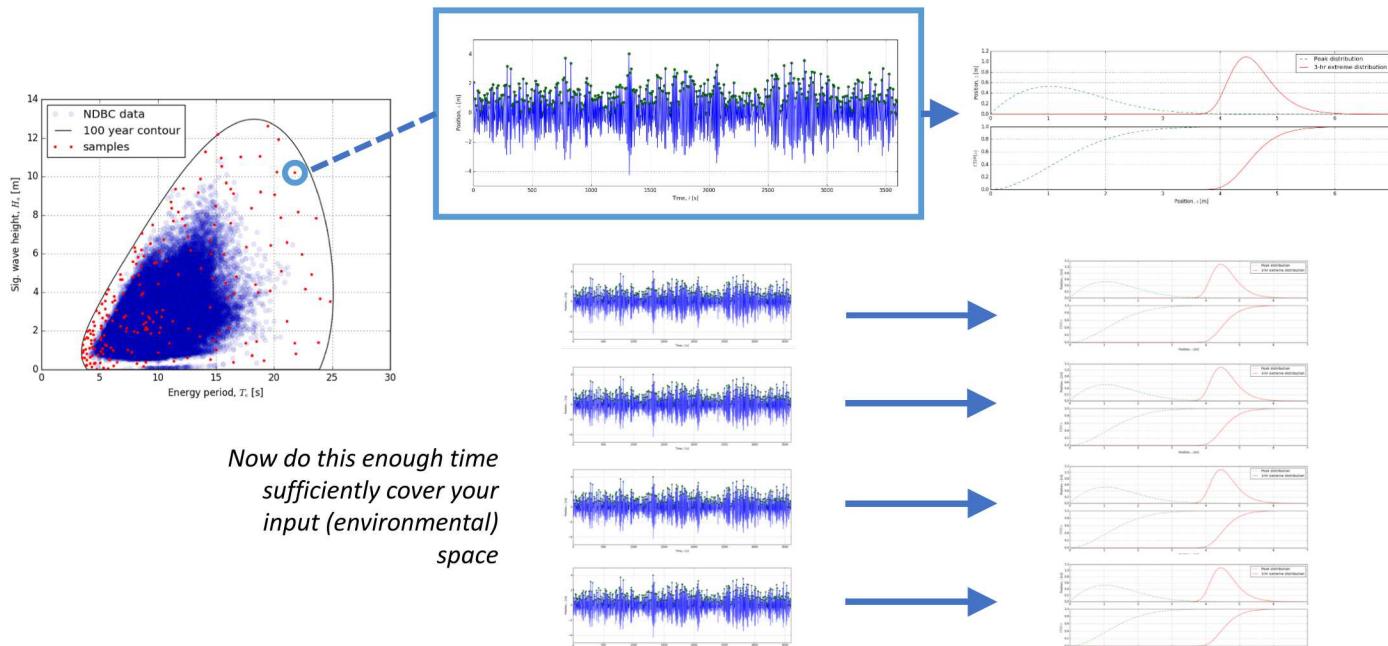
# Design Response Statistics



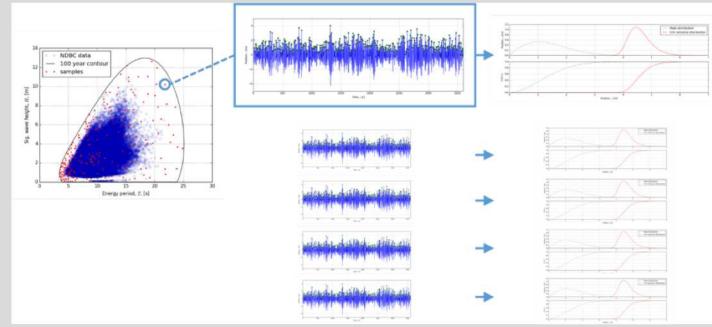
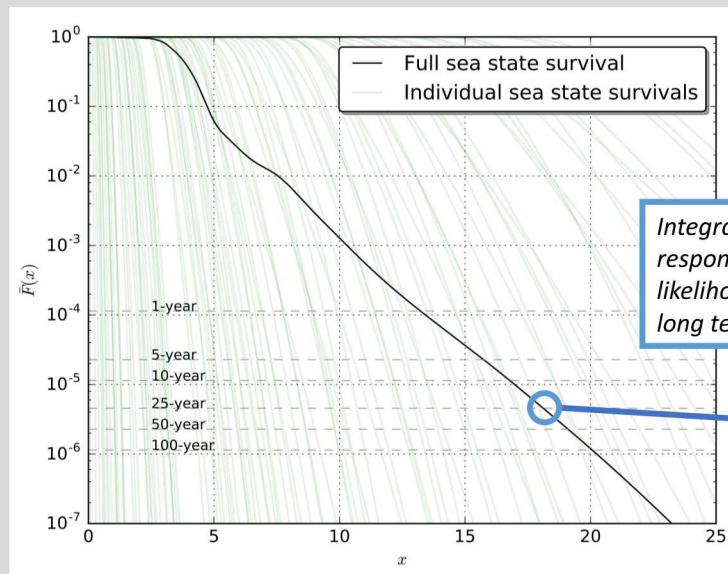
# Design Response Statistics



# Design Response Statistics



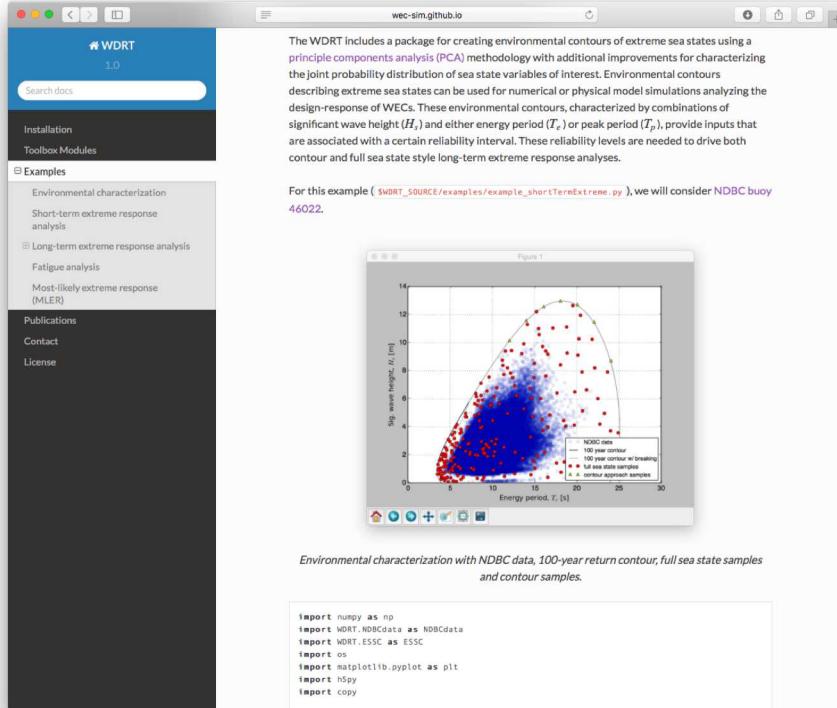
# Design Response Statistics All-Sea-State Approach



*Integrating the short-term extreme responses (and weighting based on the likelihood of each sea state) gives the long term response*

*In a 25-year deployment at this location, we expect this device to see a max displacement of ~18 m*

# WEC Design Response Toolbox (WDRT)



<http://wec-sim.github.io/WDRT>

- Environmental Characterization
- Short-term Extreme Response
- Long-term Extreme Response
- Most-likely Extreme Response (MLER)
- Fatigue Loads
- Structural Loads

# Design Response Statistics

## Case Study: All-Sea-State Approach

- Reference Model 3 (Gen 1)
  - 1:100 scale version
  - $H = 3, 9, 15 \text{ m}$

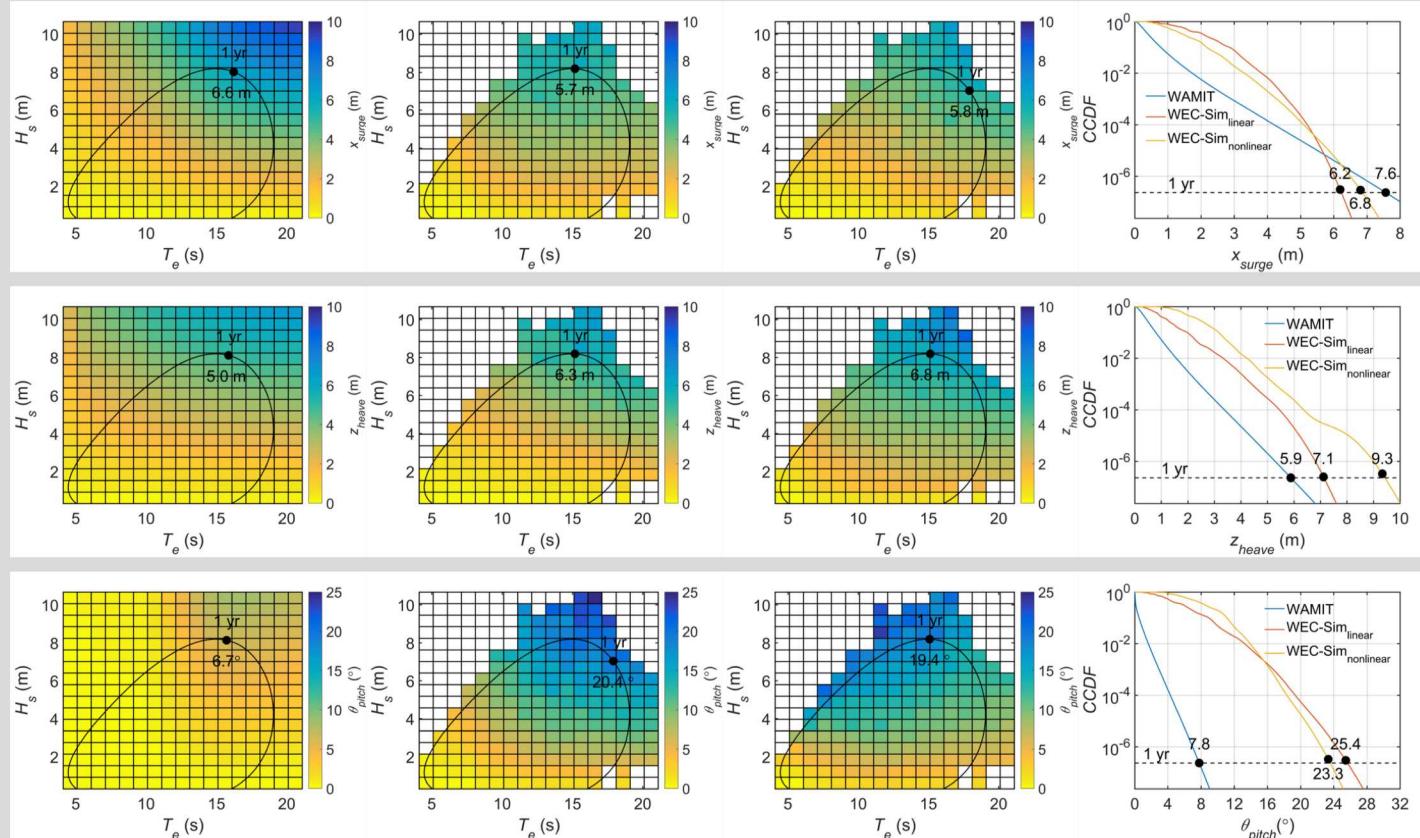
Property	Value	Units
$m$	0.313	$kg$
$I_x$	$8.89 \times 10^{-3}$	$kg \cdot m^2$
$I_y$	$8.89 \times 10^{-3}$	$kg \cdot m^2$
$z_{cg}$	-0.214	$m$
$z_{mooring,top}$	-0.051	$m$
$z_{mooring,bottom}$	-0.213	$m$
$k_{mooring}/8$	0.7	$N/m$



Yu, Y.-H., Lawson, M., Li, Y., Previsic, M., Epler, J., and Lou, J., 2015, Experimental Wave Tank Test for Reference Model 3 Floating-Point Absorber Wave Energy Converter Project, NREL/TP-5000-62951.

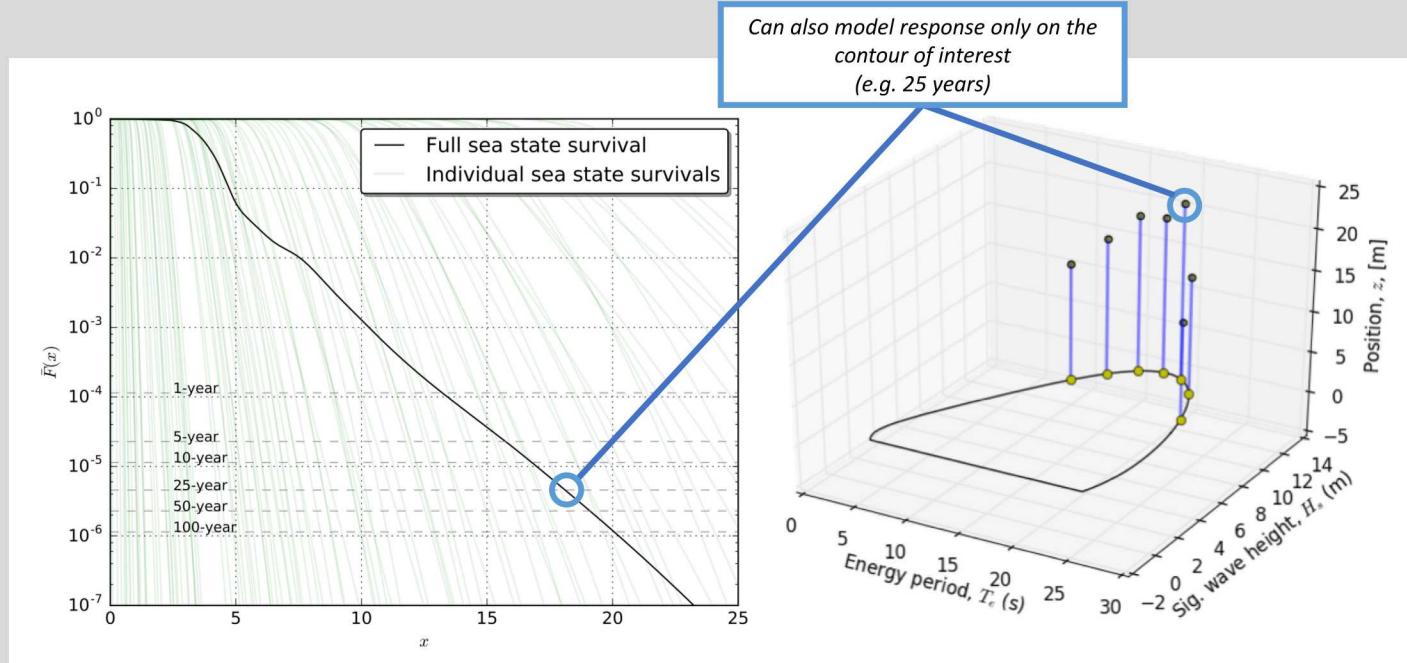
# Results and Discussion

van Rij J., Yu Y.-H., and Coe R. G., 2018, "Design Load Analysis for Wave Energy Converters," 37th International Conference on Ocean, Offshore and Arctic Engineering, OMAE, Madrid, Spain.

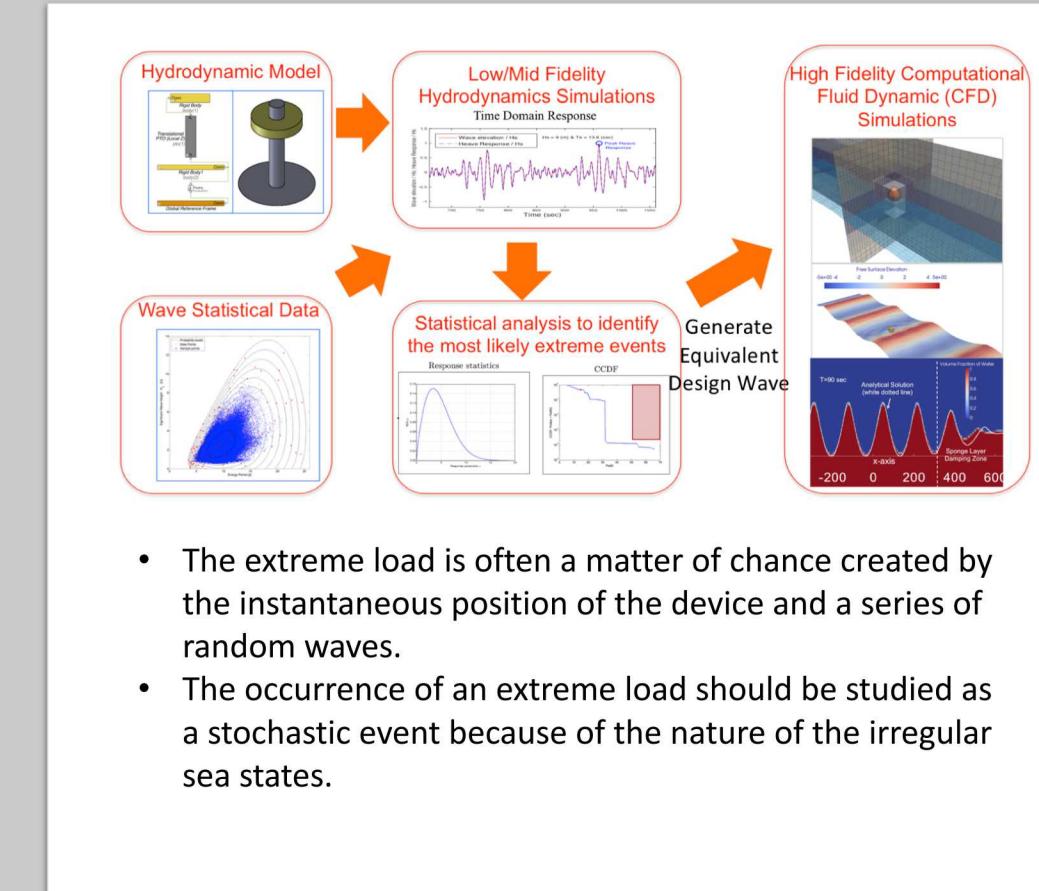
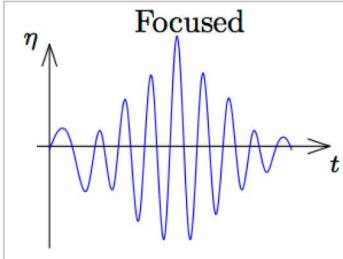
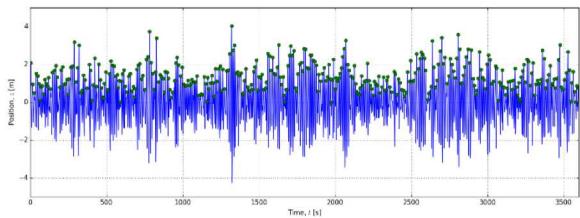


# Design Response Statistics

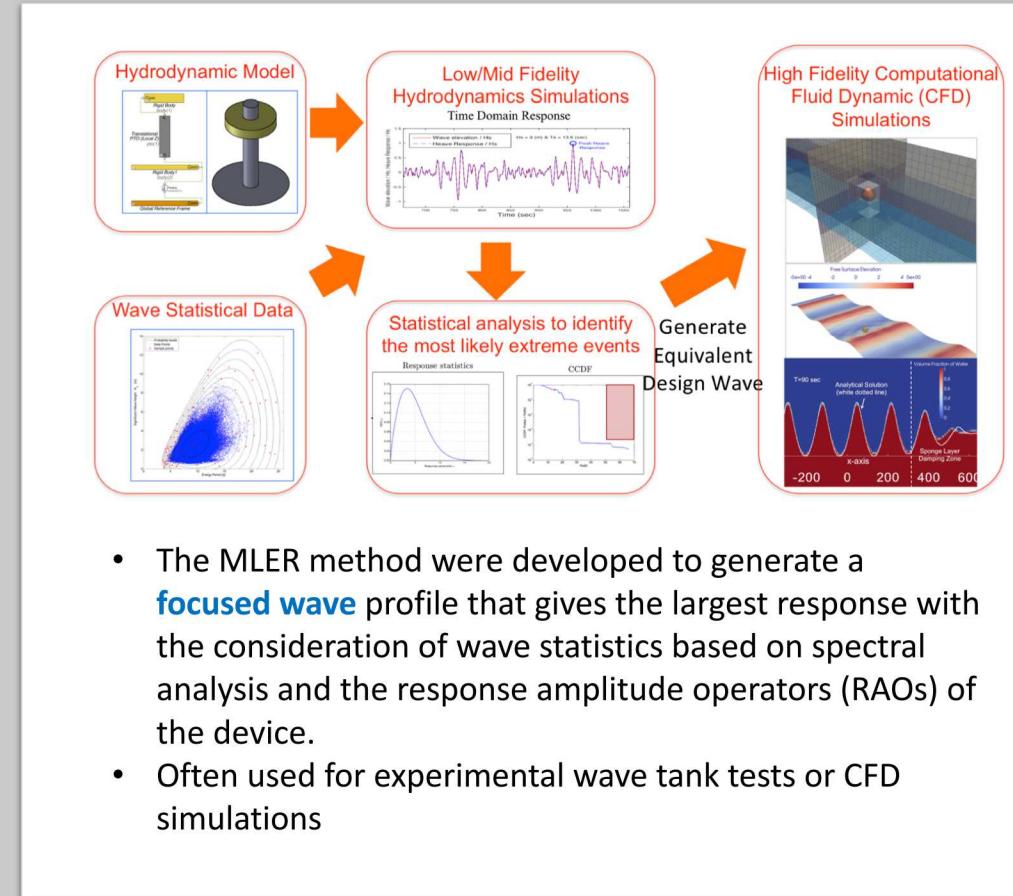
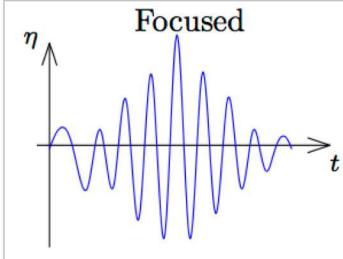
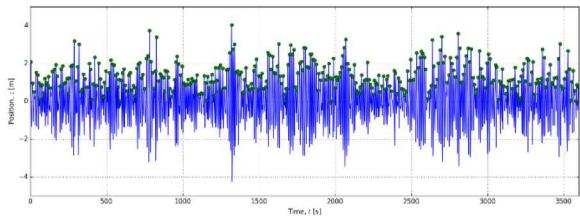
## Contour Approach



# Most-Likely Extreme Response



# Most-Likely Extreme Response



- The MLER method were developed to generate a **focused wave** profile that gives the largest response with the consideration of wave statistics based on spectral analysis and the response amplitude operators (RAOs) of the device.
- Often used for experimental wave tank tests or CFD simulations

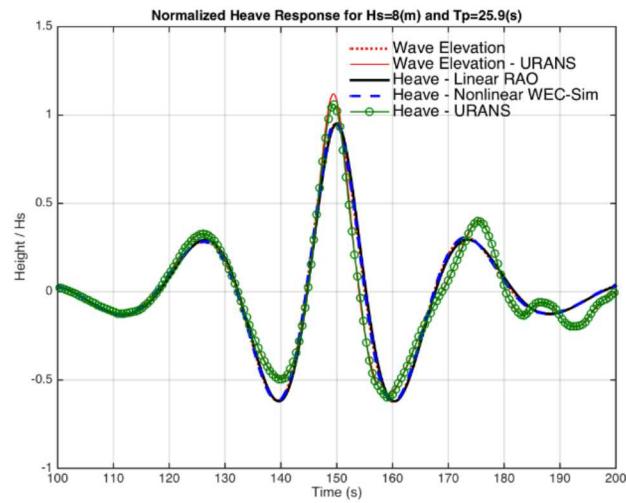
# Most-Likely Extreme Response

Construct an ensemble of design wave profiles

$$\eta = \sum_{n=1}^N A_n [V_n \cos(\omega_n t) - W_n \sin(\omega_n t)],$$

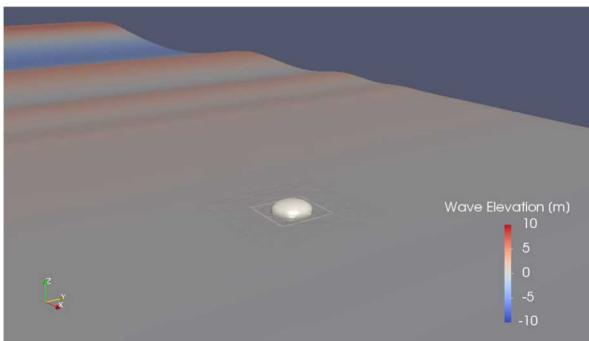
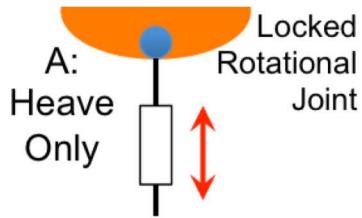
$A_n$ : Wave spectrum

$V_n$  and  $W_n$ : Independent standard normal random variables

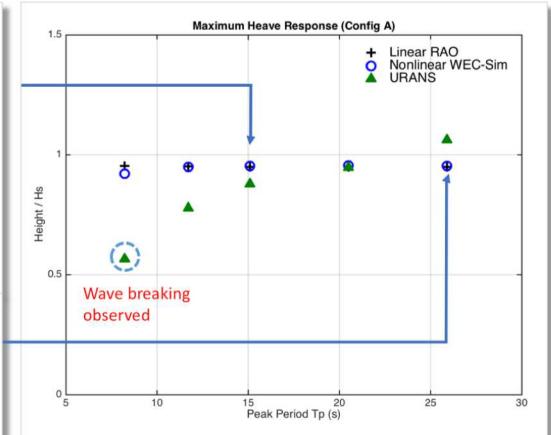
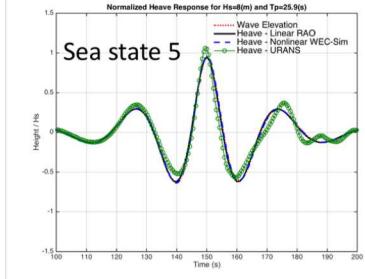
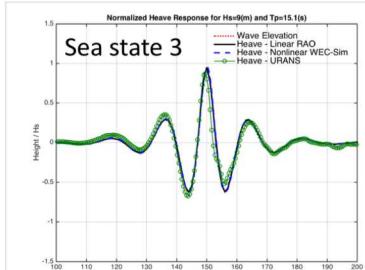


- Dietz, J. S., 2004. "Application of Conditional Waves as Critical Wave Episodes for Extreme Loads on Marine Structures". PhD thesis, Technical University of Denmark.
- Drummen, I., Wu, M., and Moan, T., 2009. "Numerical and experimental investigations into the application of response conditioned waves for long-term nonlinear analyses," *Marine Structures*, 22(3), Jul, pp. 576–593.
- Quon E., Platt A., Yu Y., and Lawson M., 2016, "Application of the Most Likely Extreme Response Method for Wave Energy Converters," *OMAE 2016*, Busan, South Korea.

# Most-Likely Extreme Response

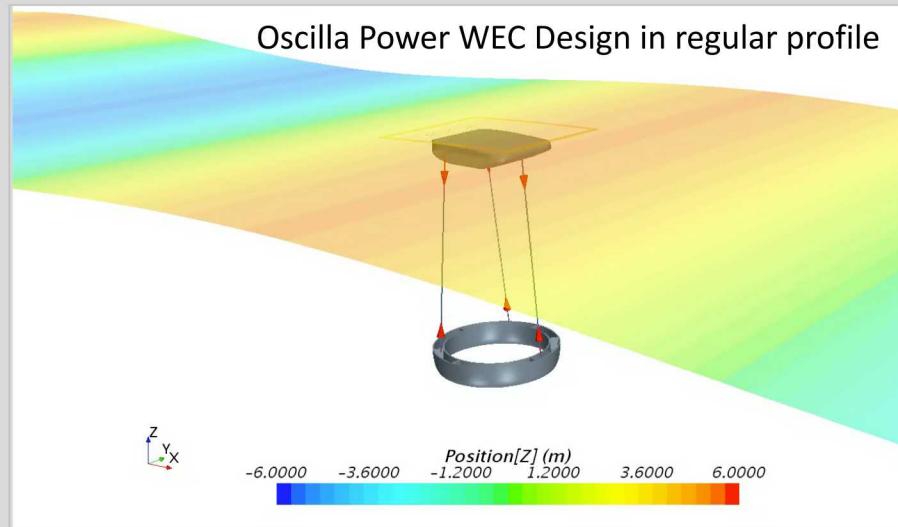
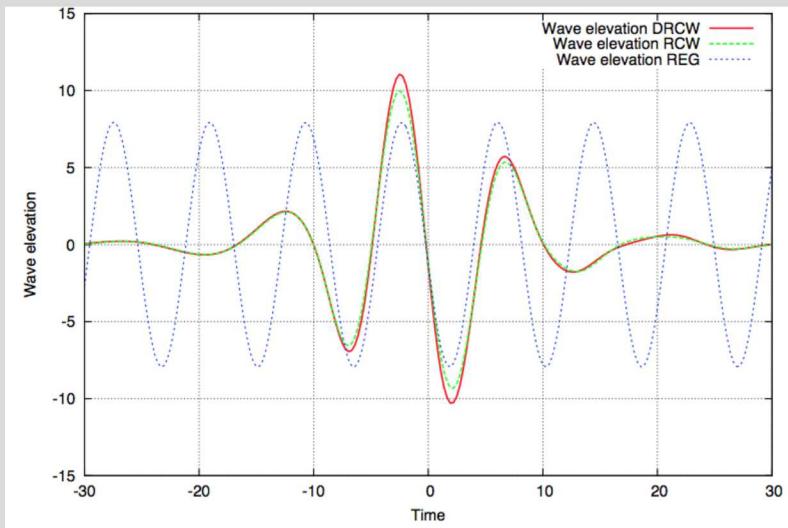


## Case Study



Quon E., Platt A., Yu Y., and Lawson M., 2016,  
"Application of the Most Likely Extreme  
Response Method for Wave Energy  
Converters," OMAE 2016, Busan, South Korea.

# Other Response conditioned wave profiles

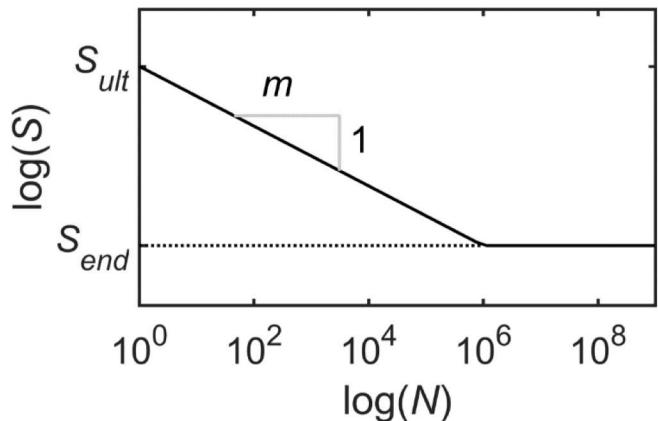


de Hauteclocque G., Derbanne Q., and El-gharbaoui A., 2012, "Comparison of Different Equivalent Design Waves with Spectral Analysis," 31st International Conference on Ocean, Offshore and Arctic Engineering, OMAE, ed., OMAE, Rio de Janeiro, Brazil.

Ryan G. Coe, Chris C. Chartrand, Eliot W. Quon, Brian J. Rosenberg, Yi-Hsiang Yu, Jennifer van Rij, Tim R. Mundon, 2012, "CFD survival analysis of a two-body wave energy converter" (in preparation).

# Fatigue Analysis

- In addition to extreme loads, a WEC must also be able to structurally withstand fatigue loading for its design life.
- Fatigue loads are time varying loads which cause cumulative damage to structural components and eventually lead to structural failure.
- Usually, a component's fatigue strength/life is reported in terms of an S-N curve. The S-N curve, which is typically obtained empirically, gives the number of load cycles  $N$  to failure at constant load amplitude  $S$ .



# Fatigue Analysis

- WEC loads, however, are highly variable and by no means of constant amplitude. The most common method used to predict the cumulative damage of variable loading is the Palmgren-Miner rule.
- The total damage equivalent load,  $S_N$ , is obtained with a linear summation of the distributed load ranges, obtained via the rainflow counting method.

$$S_N = \left( \sum \frac{S_i^m n_i}{N} \right)^{\frac{1}{m}}$$

# Fatigue Analysis

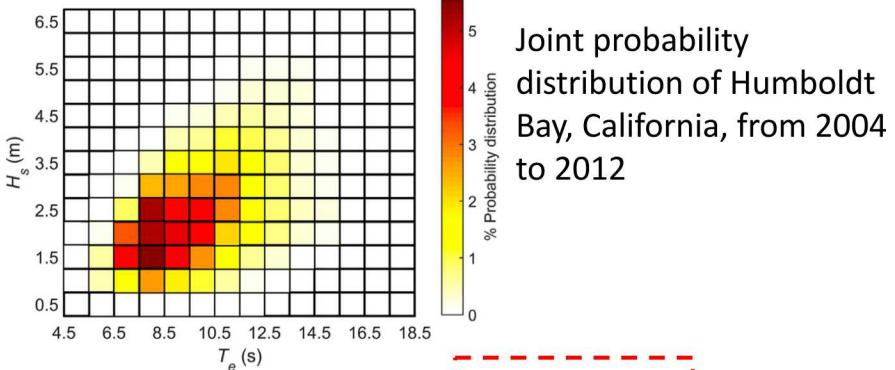
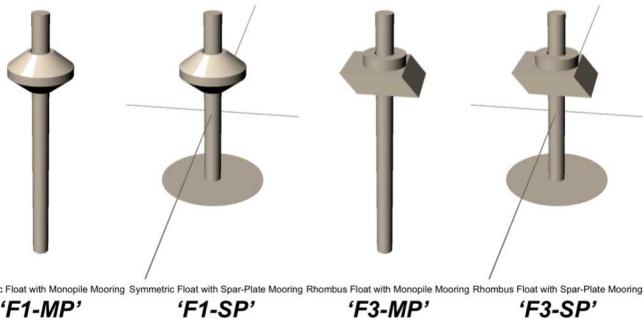
The intended use of the fatigue analysis here is as an early design stage WEC fatigue load estimator. The required inputs are:

- A force or stress history, which may be obtained either experimentally or via simulation. Pertinent loads may include, power-take-off (PTO) loads, mooring loads, bending moments, etc.
- The  $S_N$  curve slope,  $m$ , which is likely unknown with any accuracy in the early stages of design, but as an initial estimate, the following ranges may be used:  $m \approx 3-4$  for welded steel,  $m \approx 6-8$  for cast iron, and  $m \approx 9-12$  for composites.
- And,  $N$ , the number of cycles expected in the WEC's design life, which is up to the user to ascertain given a specified design life and environmental characterization.

$$S_N = \left( \sum \frac{S_i^m n_i}{N} \right)^{\frac{1}{m}}$$

# Fatigue Analysis: Case Study

- Innovative buoy design for OPT



	$\frac{P_{avg}^{1yr}}{W_{disp}}$	$\frac{P_{avg}^{1yr}}{F_{eq}^{1yr}}$	$\frac{P_{avg}^{1yr}}{F_{float}}$
	$kW$ $MN$	$kW$ $MN$	$kW$ $MN$
<i>F1-MP (0°)</i>	<b>8.23</b>	<b>161.65</b>	<b>40.21</b>
<i>F3-MP (0°)</i>	<b>7.80</b>	<b>169.52</b>	<b>31.76</b>
<i>F3-MP (30°)</i>	<b>7.51</b>	<b>164.64</b>	<b>30.09</b>
<i>F1-SP (0°)</i>	<b>9.13</b>	<b>137.15</b>	<b>44.23</b>
<i>F3-SP (0°)</i>	<b>7.12</b>	<b>147.81</b>	<b>36.47</b>
<i>F3-SP (30°)</i>	<b>7.03</b>	<b>141.71</b>	<b>39.21</b>

Power to fatigue load ratio



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This work was also supported by the U.S. Department of Energy under Contract No. DE-AC13-08GO28308 with the National Renewable Energy Laboratory.

The views expressed in the article do not necessarily represent the views of the U.S. Department of Energy or the United States Government.

# Thank you!

The authors would like to thank Ratanak So, Nathan Tom, Jennifer van Rij, Giorgio Bacelli, and Sam Kanner for the use of slides and graphics

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