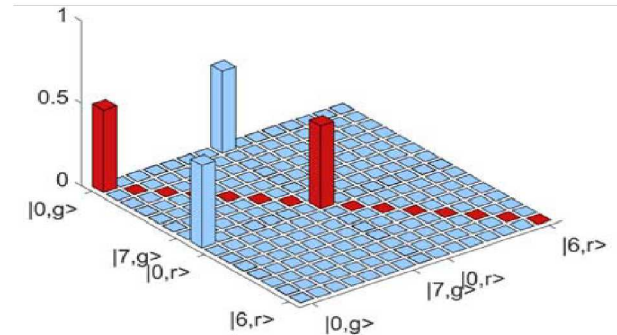
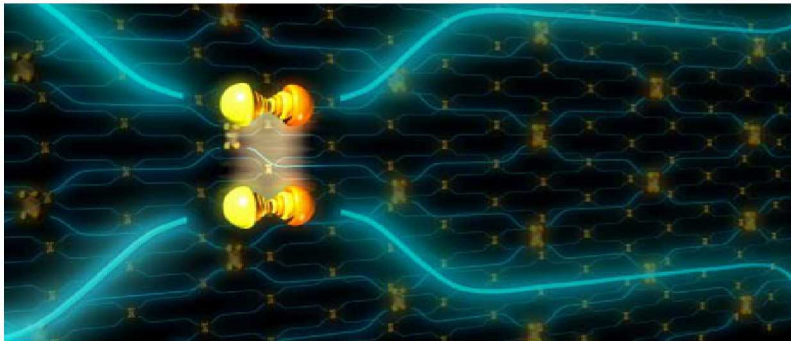


*Exceptional service in the national interest*



# Optical manipulation of neutral atoms for quantum information science

## Team members

- **Grant W. Biedermann**
- Yuan-Yu Jau (Sandia)
- Jongmin Lee (Sandia)
- Ivan Deutsch (UNM)

Michael J. Martin

This work was supported by the Laboratory Directed Research and Development program at Sandia National Laboratories



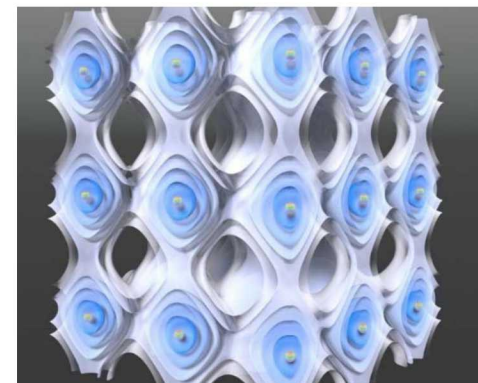
Sandia National Laboratories is a multimission laboratory managed and operated by National Technology & Engineering Solutions of Sandia, LLC, a wholly owned subsidiary of Honeywell International, Inc., for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA0003525.

# Outline

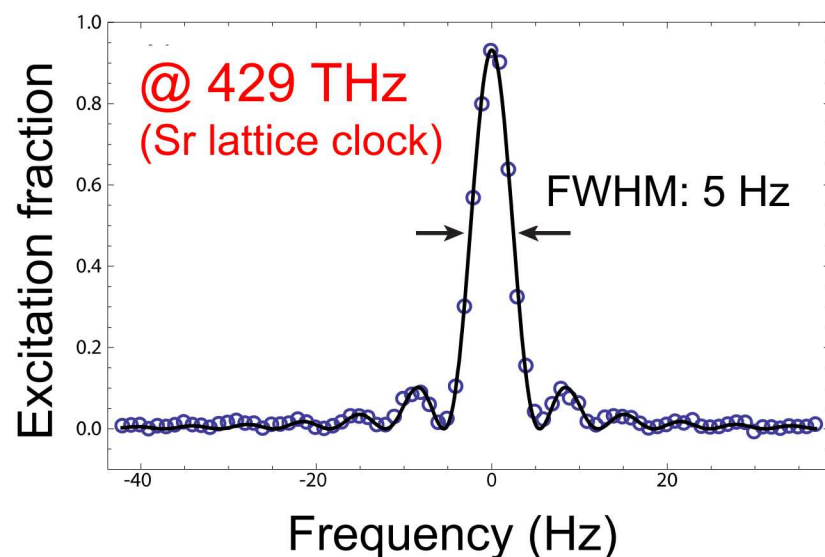
- Introduction to Rydberg atoms and the Sandia Rydberg atom experiment
- Rydberg dressed physics and entangling gates.
- Study of a controlled-phase (CPHASE) gate.
- Holography for trap arrays.

# Neutral atom technology

- Trap, cool, manipulate 1 to  $>10^9$  quantum particles.
- New phases of matter (*e.g.*, BEC).
- Incredibly precise measuring tools (root N).

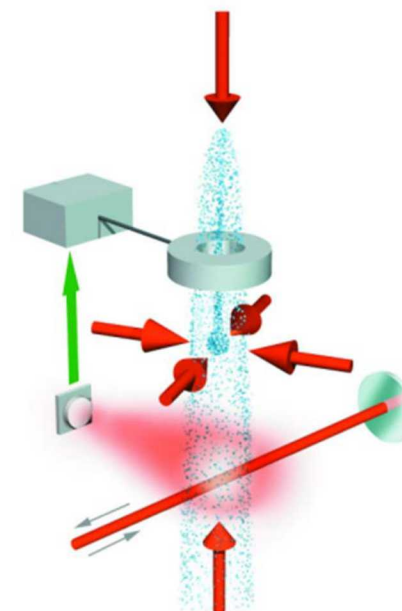


Credit: Brad Baxley, JILA



MJM, PhD Thesis, JILA

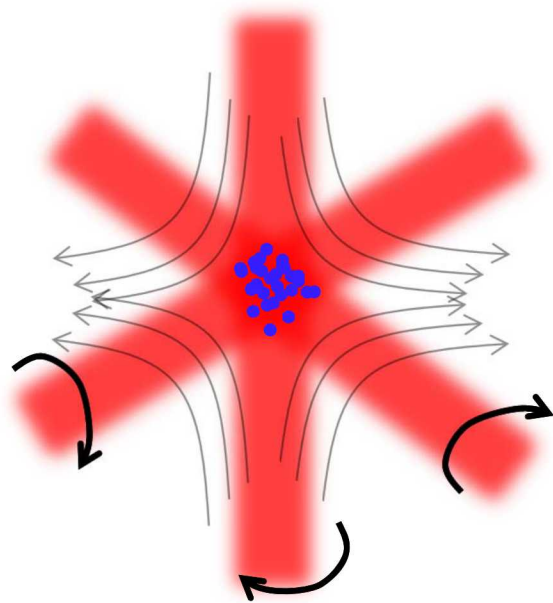
- Timekeeping, gravimetry, magnetometry, etc.



[http://smc.cnes.fr/PHARAO/GP\\_instrument.htm](http://smc.cnes.fr/PHARAO/GP_instrument.htm)

# Neutral atom tools

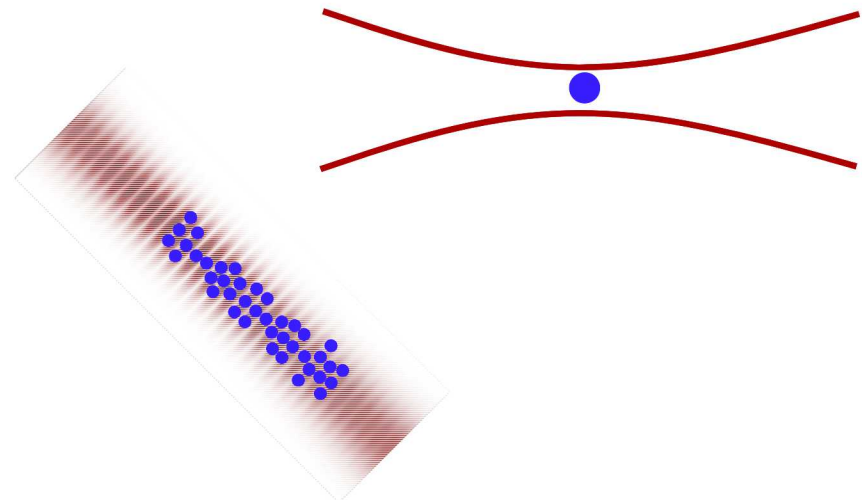
## Magneto-optical trap (MOT)



- Trapping and cooling at the  $\mu\text{K}$  level via scattering laser light


## Optical dipole traps

- Laser induces a polarization in atom that results in conservative trap potential.



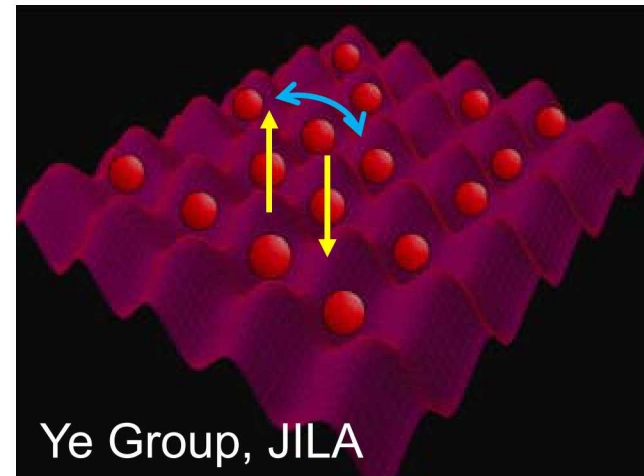
# Interaction between *neutral* atoms

Atom 1      Atom 2


$$U = \frac{4\pi a \hbar^2}{m} \times \bar{n}$$

S-wave cold  
collisions

$$J_{ex} \propto J^2 / U$$



- Interaction between ground state atoms is small  $\sim 100$  Hz
- Thermal energy scales too large (e.g., QSIM)
- Long gate times (e.g., QIP)

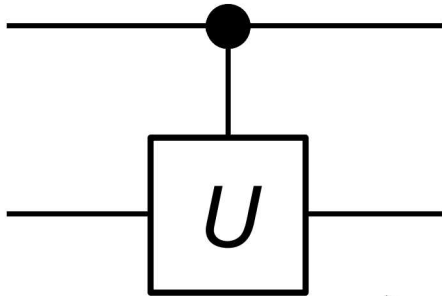
One solution: use Rydberg states

S. Trotzky *et al.*, Science **319**, 295-299 (2008)

I. Bloch, J. Dalibard, and S. Nascimbène, Nat. Phys. **8**, 267-276 (2012)

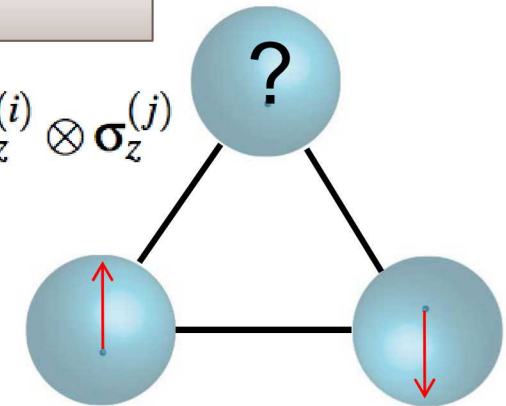
# Applications

Pairwise entangling gates between two neutral atoms



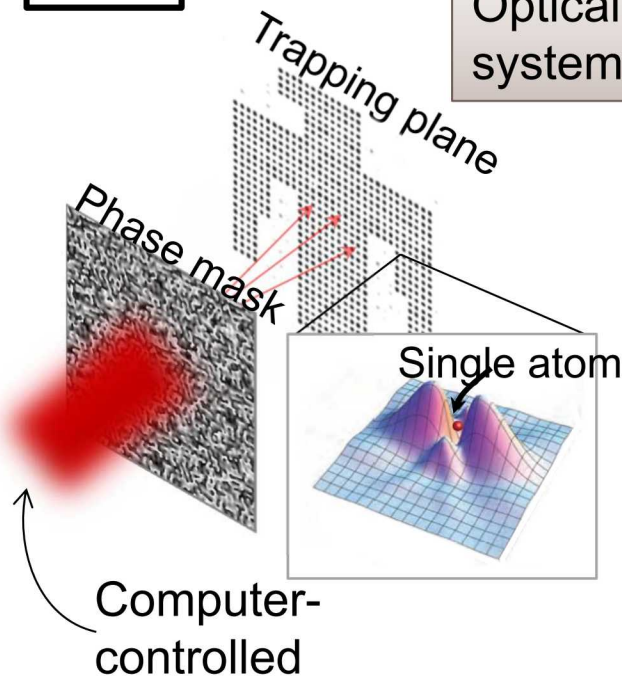
Quantum simulation

$$H_P = \sum_{i=1}^N \tilde{h}_i \sigma_z^{(i)} + \sum_{i,j=1}^N \tilde{J}_{ij} \sigma_z^{(i)} \otimes \sigma_z^{(j)}$$

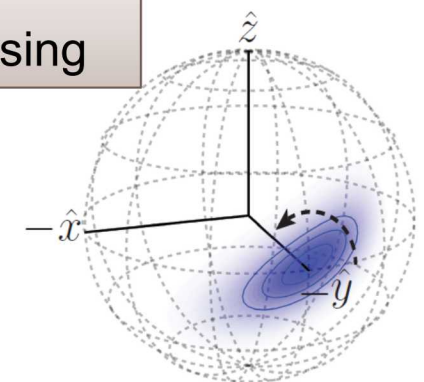


Frustrated magnetism

Optical control of atomic systems

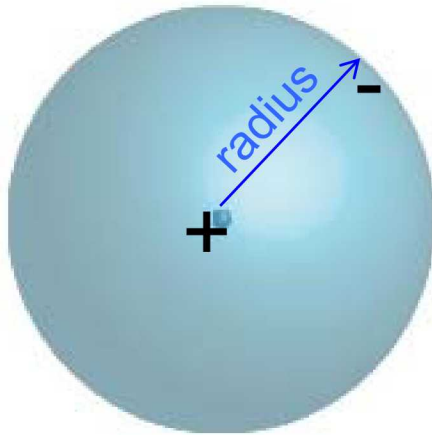


Large-scale/rapid entanglement for sensing

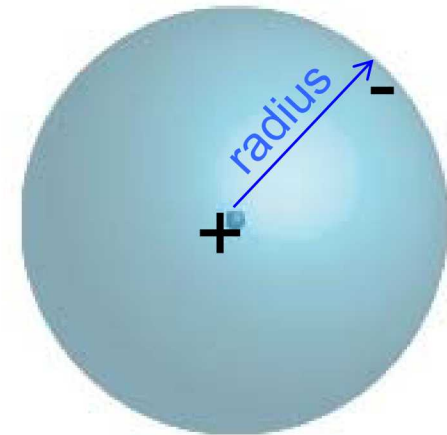


# Interaction between *neutral* atoms

Valence electron  
in Rydberg state



Valence electron  
in Rydberg state



orbital radius  $\propto n^2$

- Excite valence electron to Rydberg state—nearly ionized
- Atom becomes highly polarizable—strong interactions

# Interaction between *neutral* atoms

## Parameter scaling

van der Waals

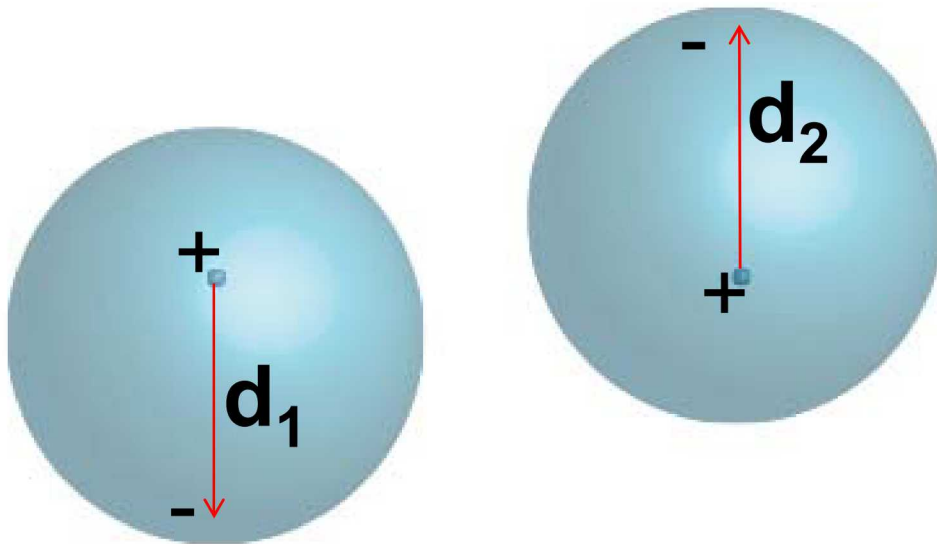
$$U \propto n^{11}$$

Lifetime

$$\tau \propto n^3$$

DC polarizability

$$\alpha(0) \propto n^7$$



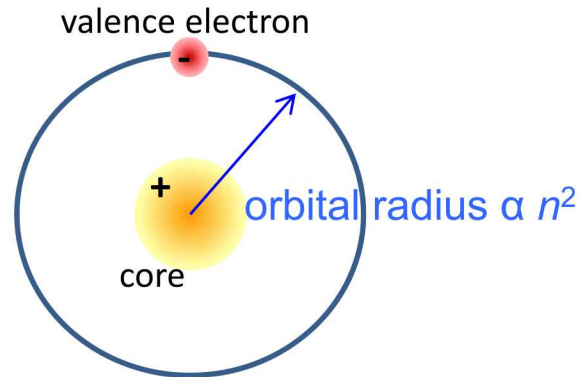
van der Waals interaction

- Even the presence of another atom can cause a massive response  $\gg 10$  MHz
- Induced Electric Dipole-Dipole Interaction  $\propto 1/r^6$

Entanglement demonstrations

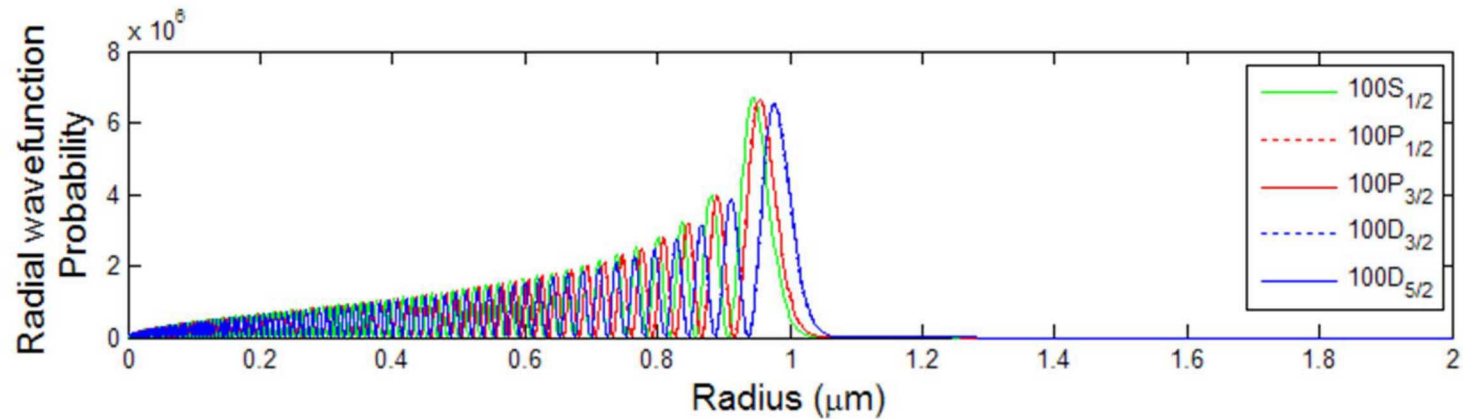
- Madison: Phys. Rev. Lett. 104, 010503 (2010)
- Paris: Phys. Rev. Lett. 104, 010502 (2010)

# Rydberg state mediated interaction

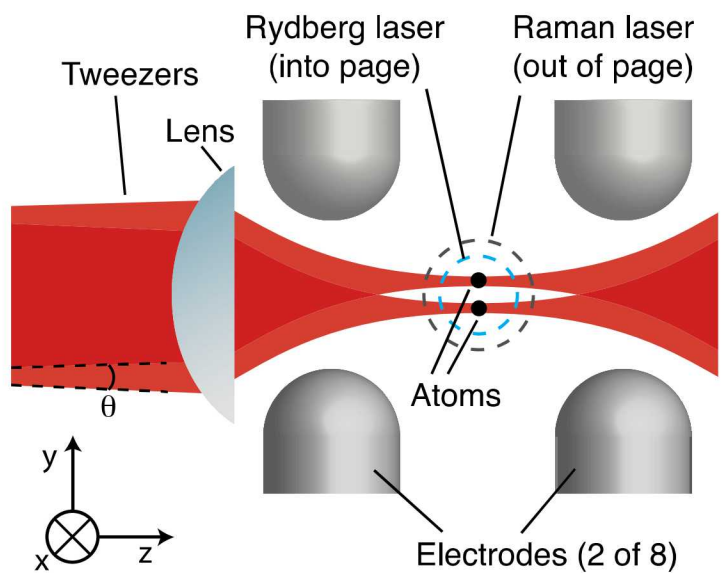
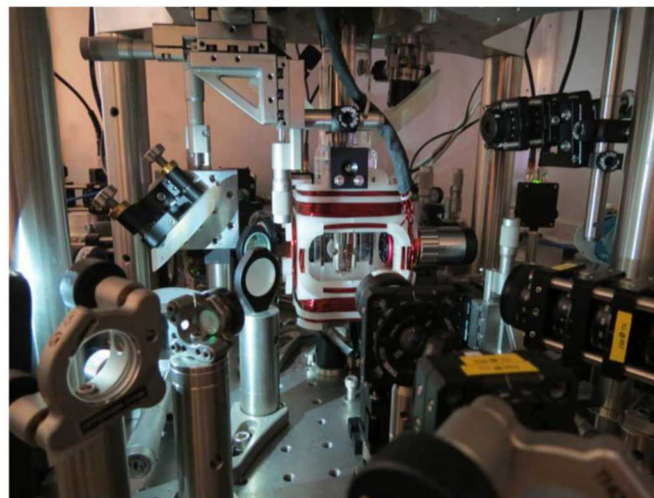
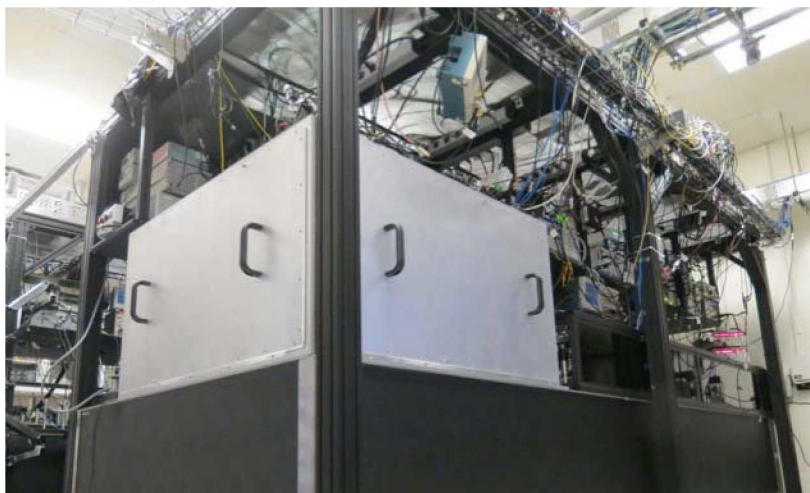


A classical picture of an atom

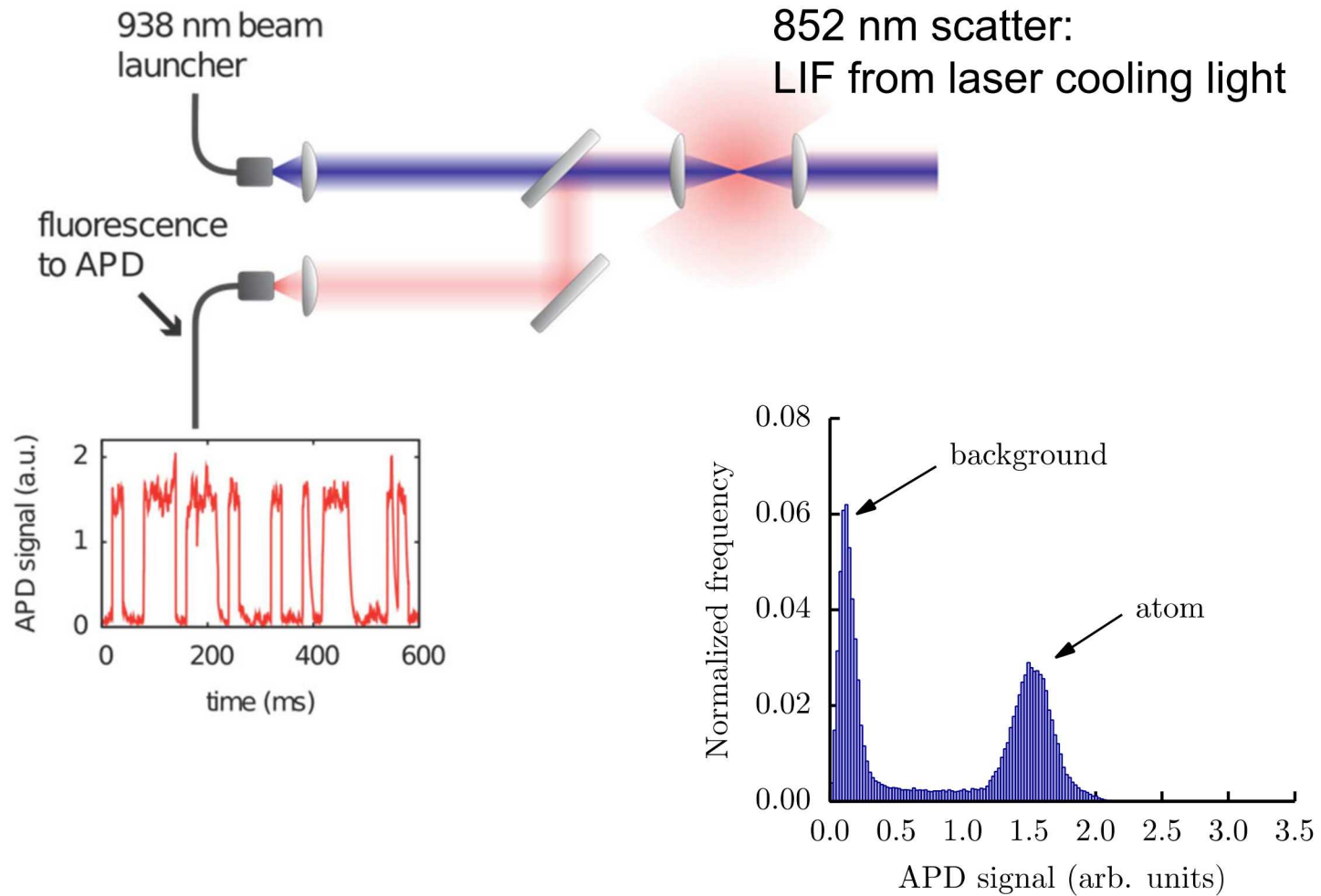
An example of the radial wavefunctions of a Cs atom at  $n = 100$ :



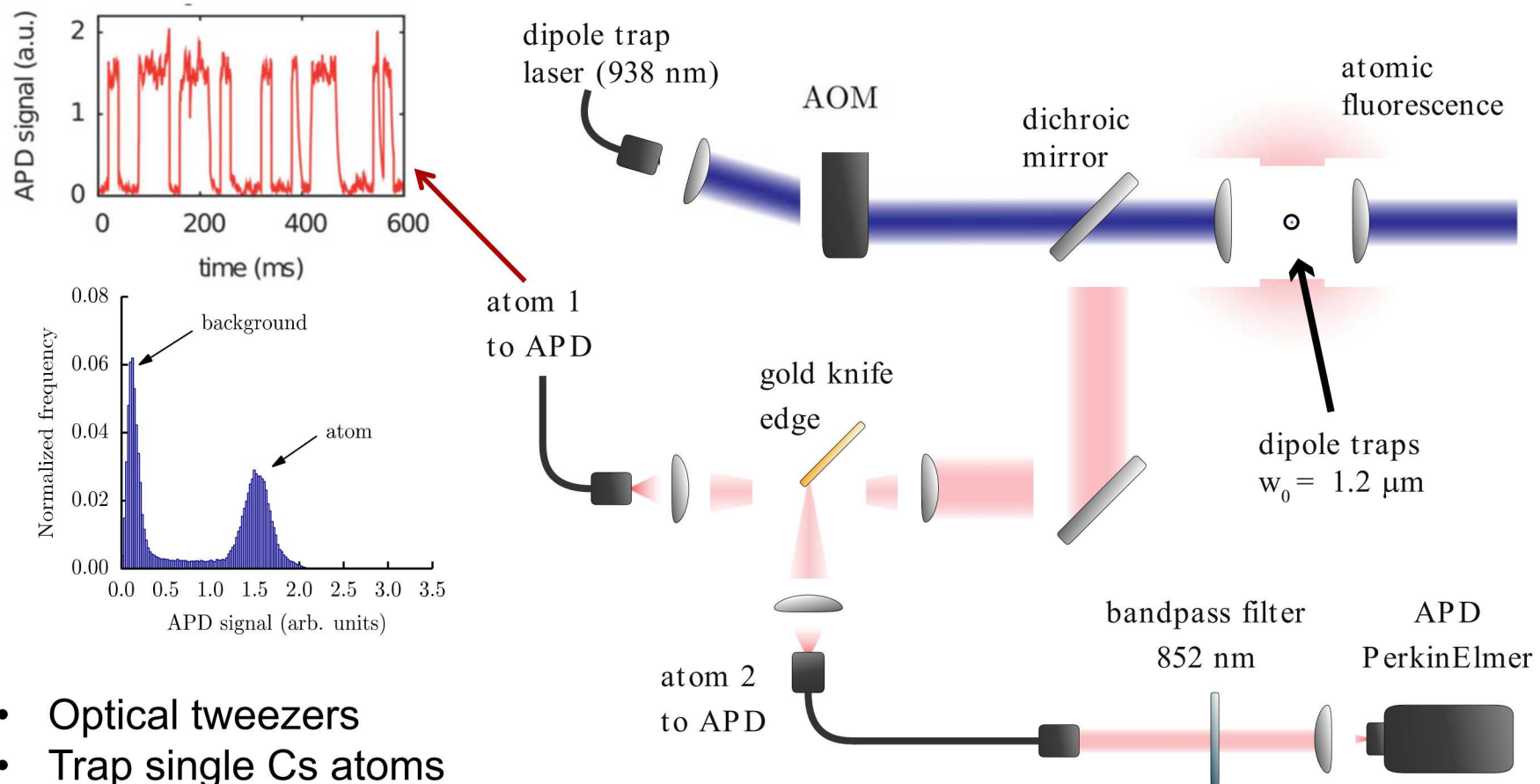
# Apparatus



# Single atom control



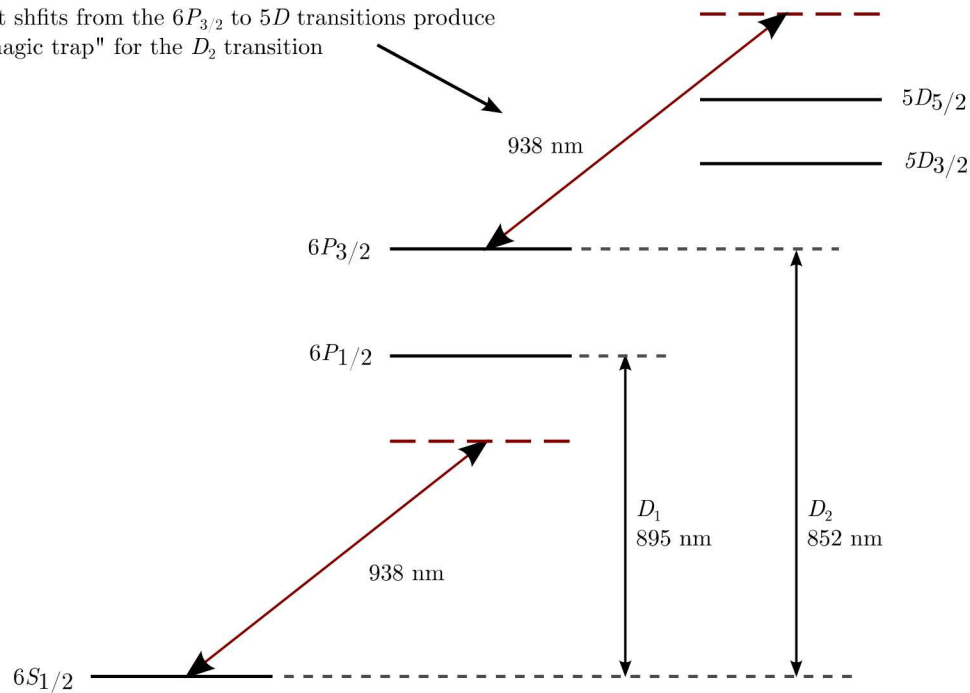
# Single atom control of 2 atoms



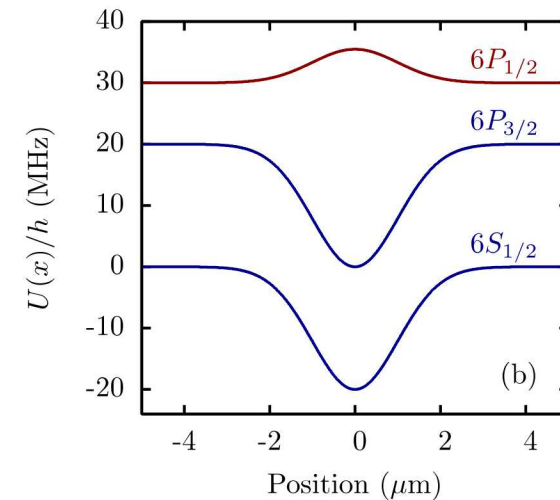
- Optical tweezers
- Trap single Cs atoms
- Laser cooling to load traps
- AOM deflection controls trap position
- Photon counters for detection

# A note about our optical tweezers

Light shifts from the  $6P_{3/2}$  to  $5D$  transitions produce a "magic trap" for the  $D_2$  transition

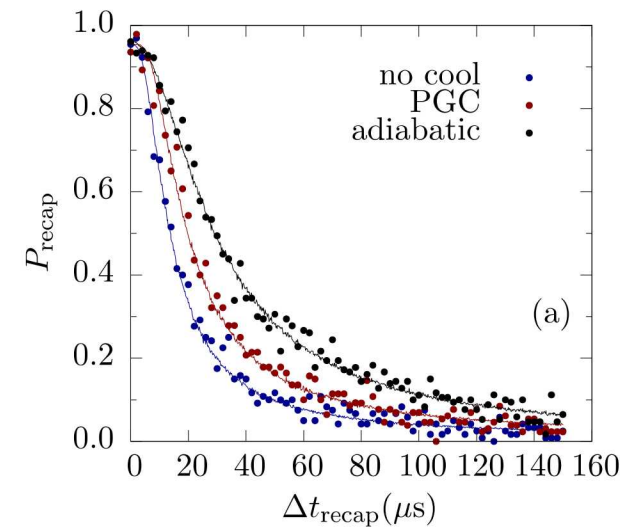
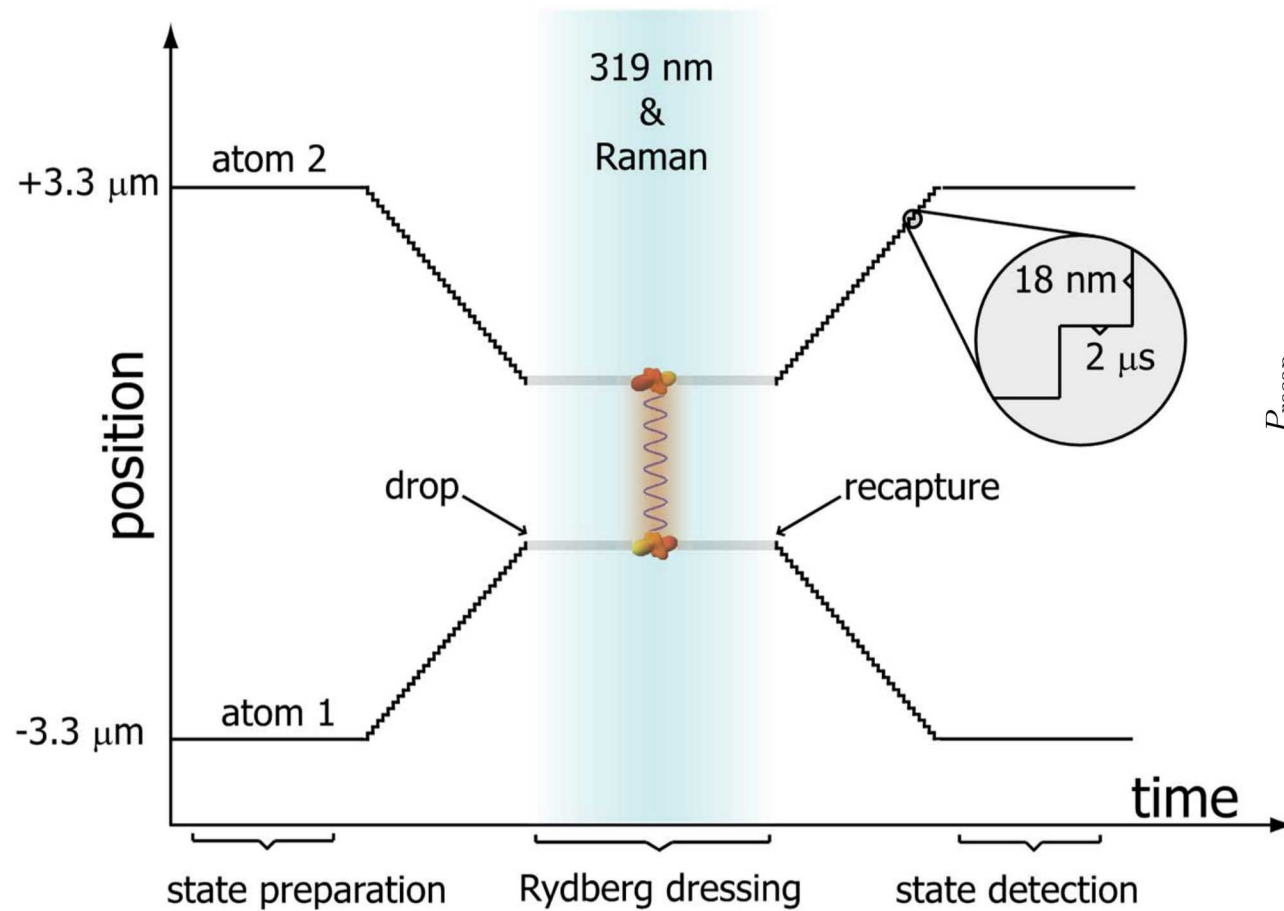


Why 938 nm? It's magic for the cooling transition.



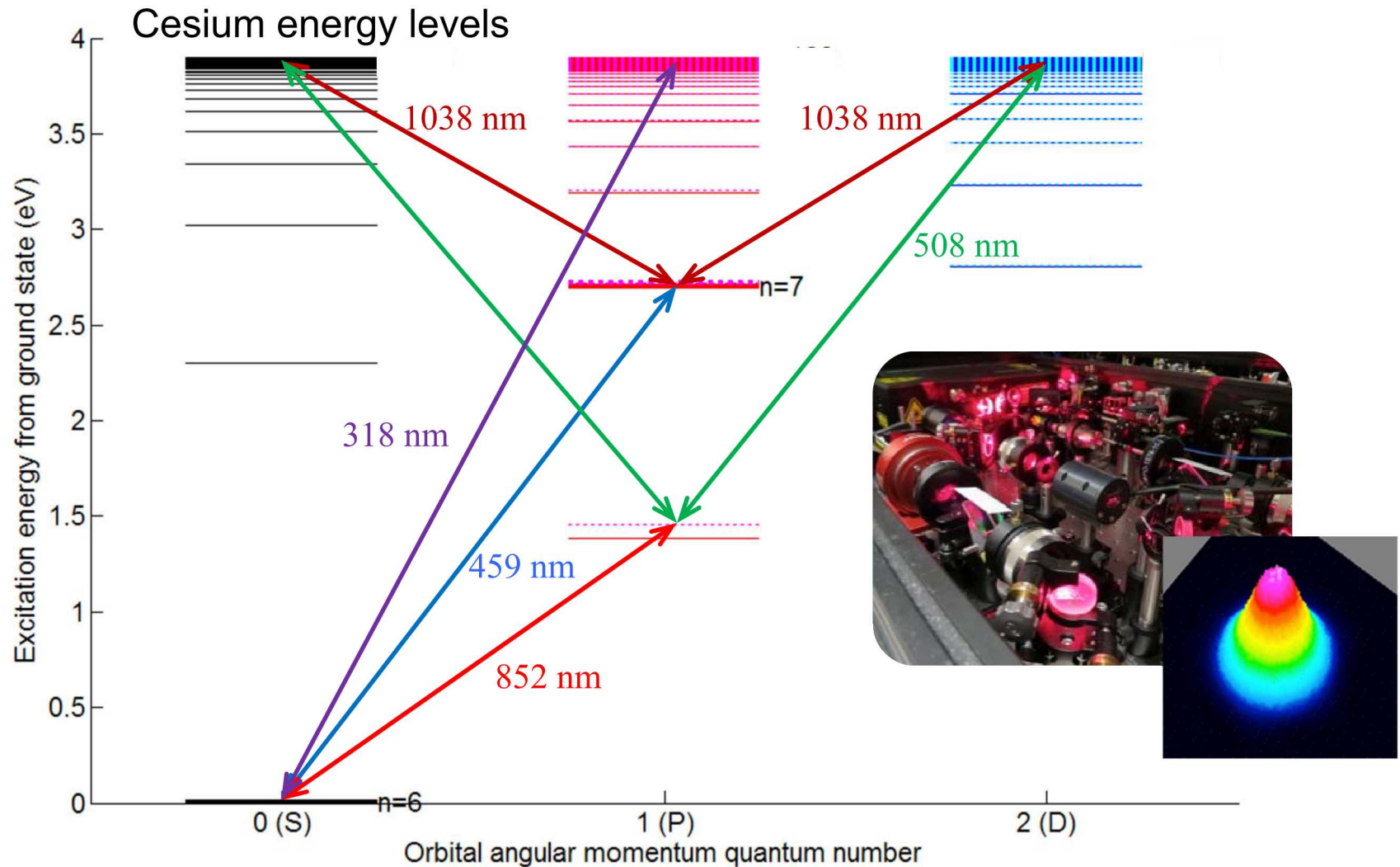
- $\approx 5$  mW, 43 nm red
- focused to  $\approx 1$   $\mu\text{m}$
- gives  $\approx 20$  MHz or  $\approx 1$  mK

# Dynamic atom positioning

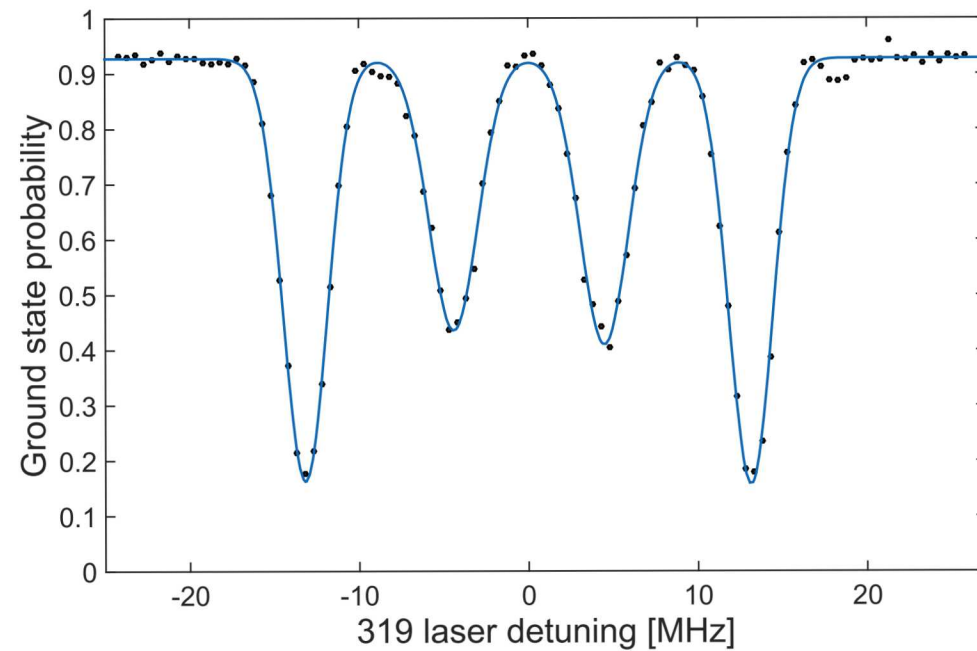
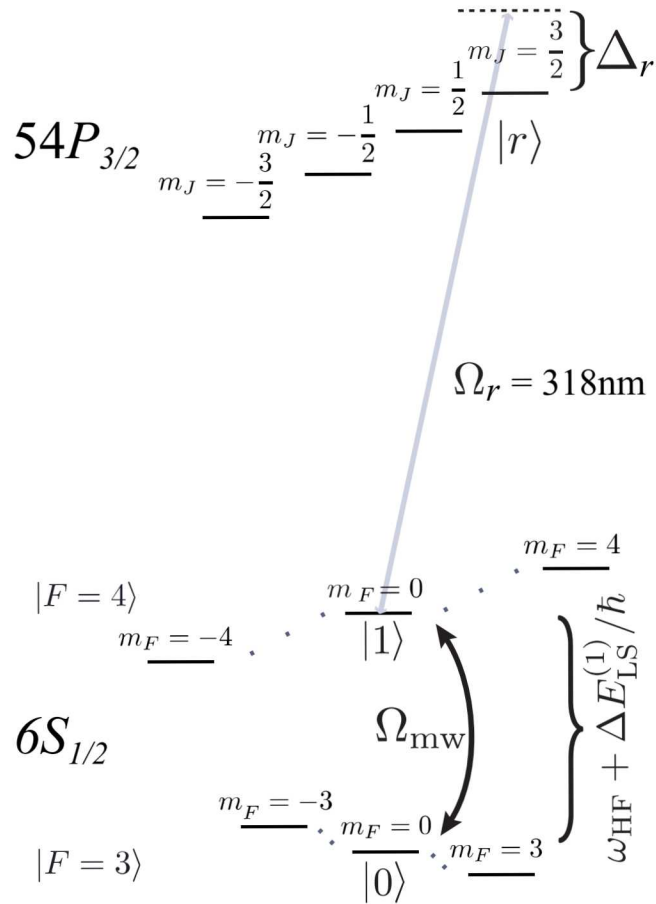


Drop and recapture

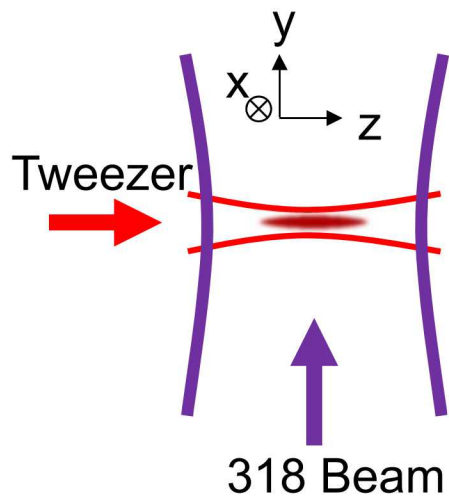
# Rydberg excitation laser



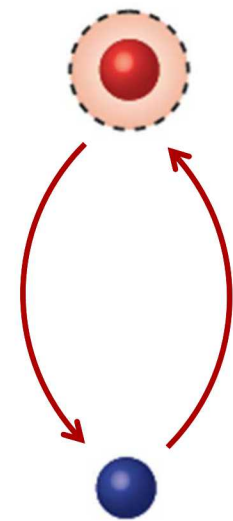
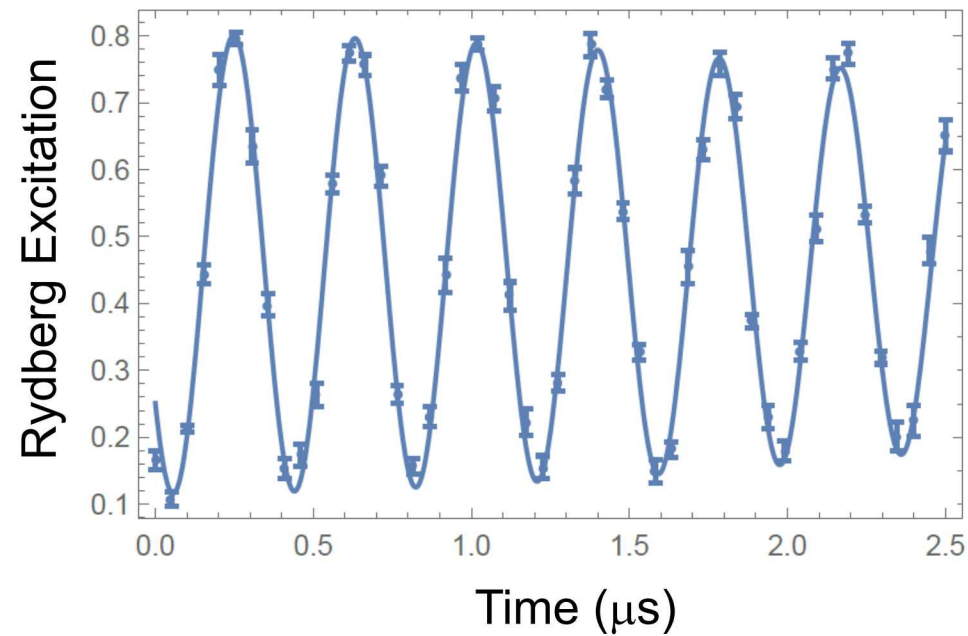
# Rydberg state spectrum



# Direct excitation 318 nm Rydberg Rabi flopping



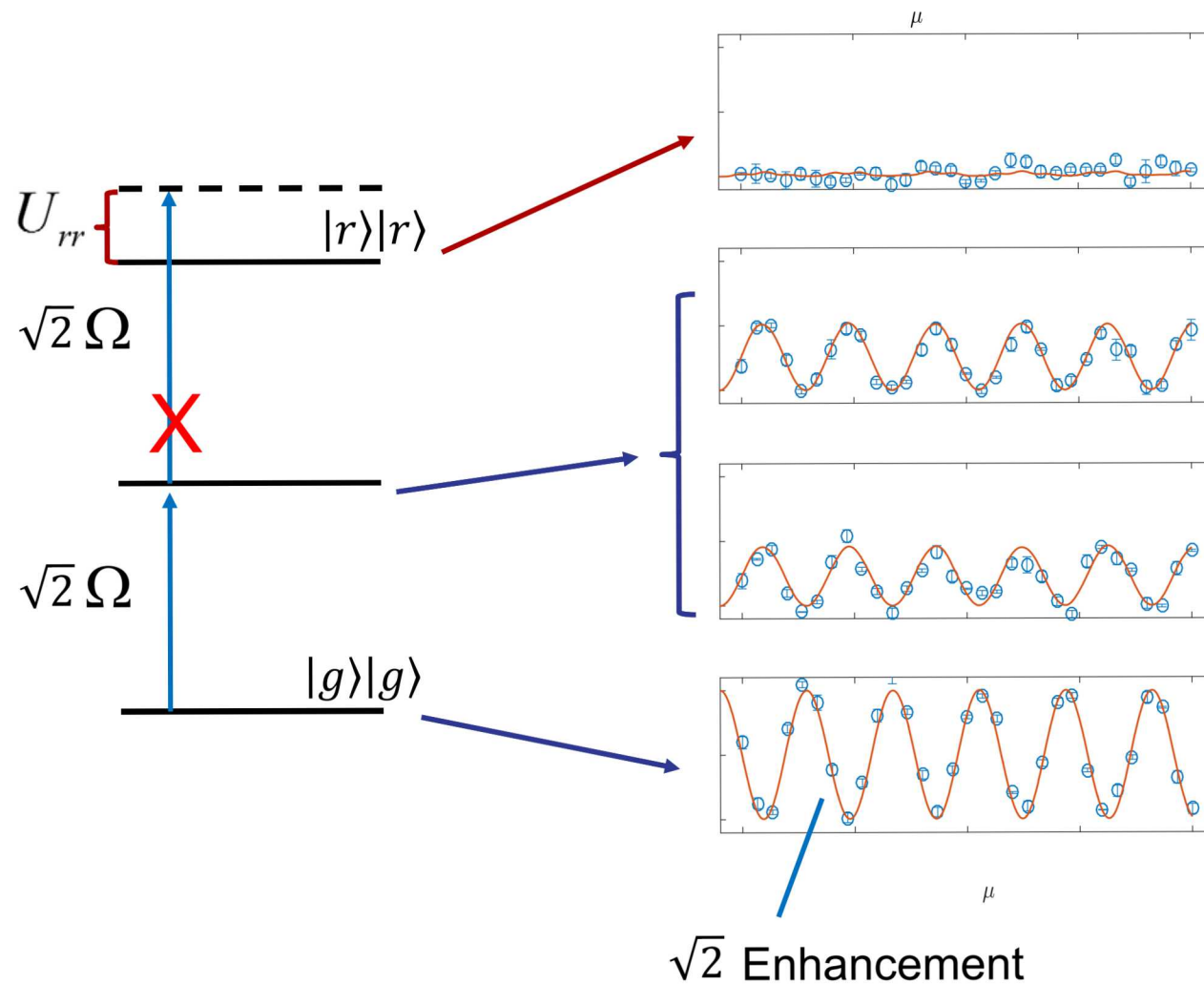
Direct excitation, measured through loss



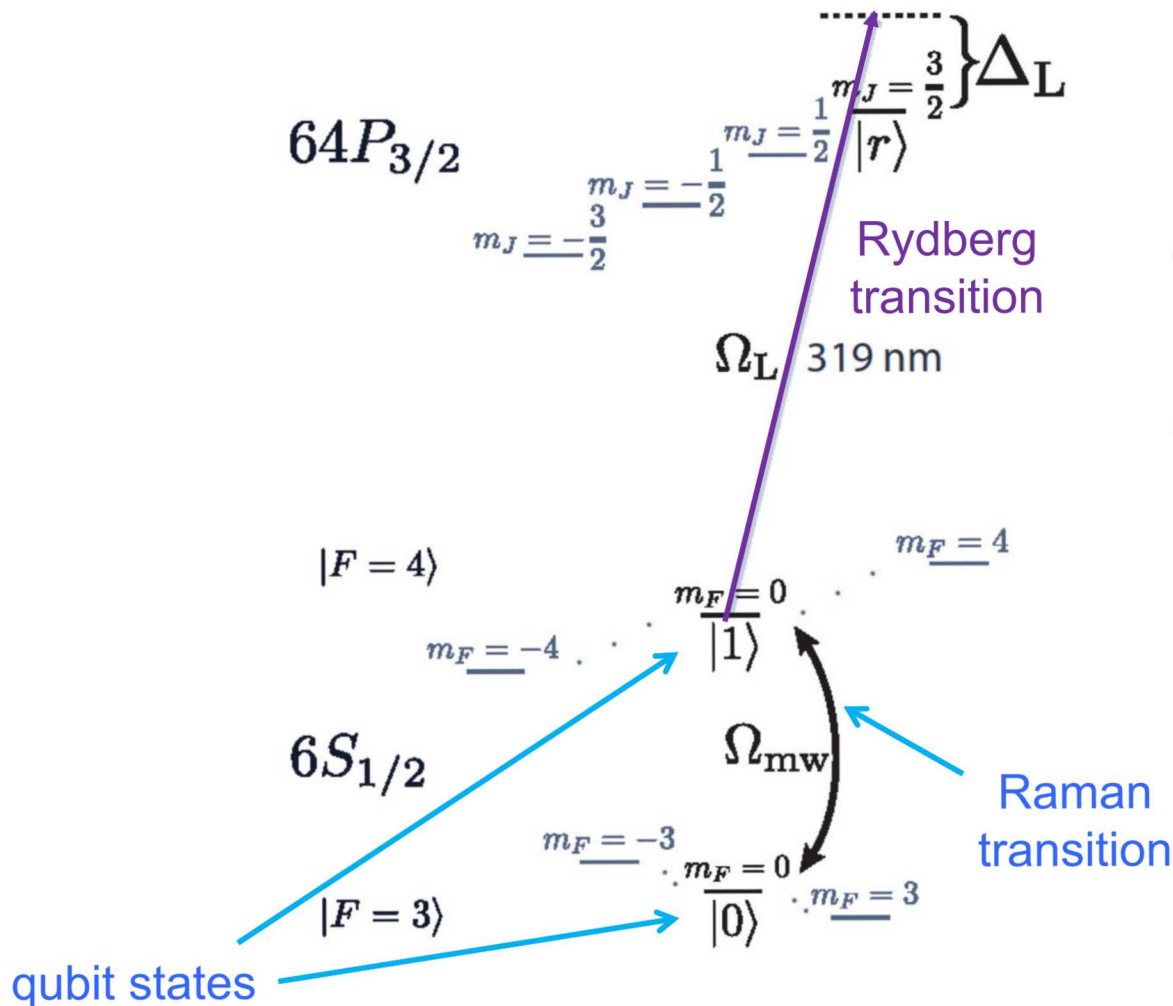


# Two-atom Rydberg blockade

Strong ( $U_{RR} > 6$  MHz)



# Level diagram

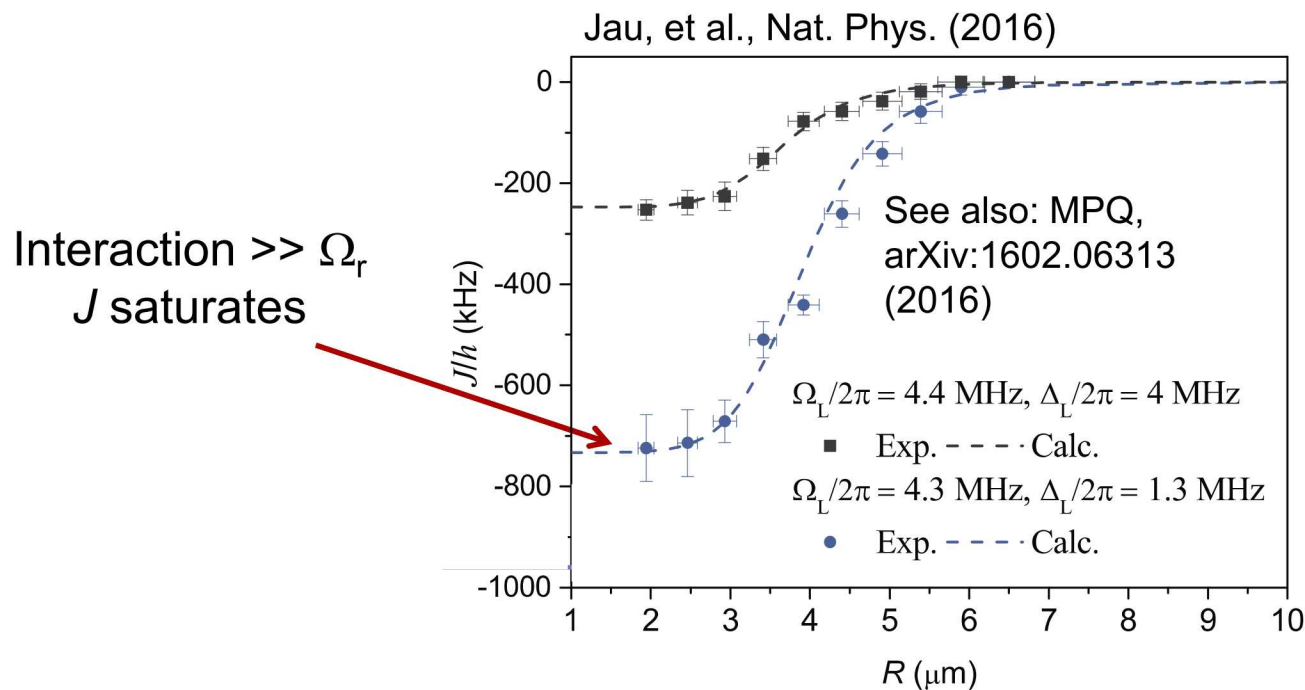


- 1-S scale coherence time. Neutral atoms define the SI second!
- Form the basis of sensors and clocks that utilize measurements of  $\sim 10^6$  atoms.

# Rydberg-dressed interaction

## First measurement

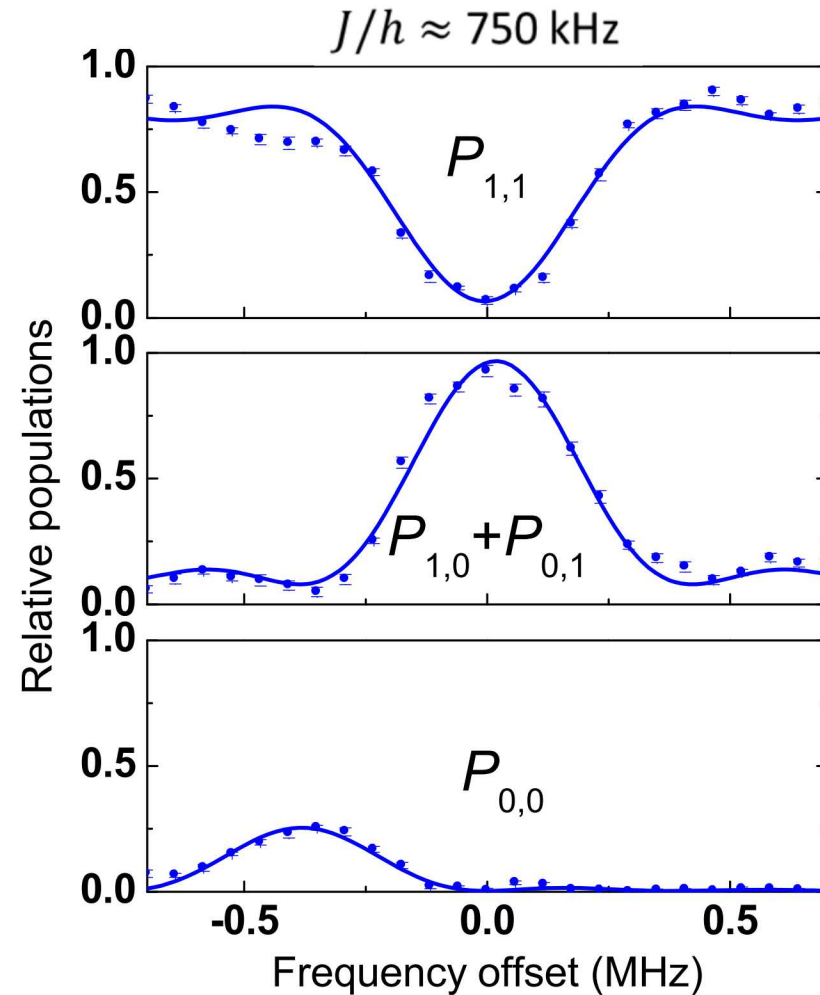
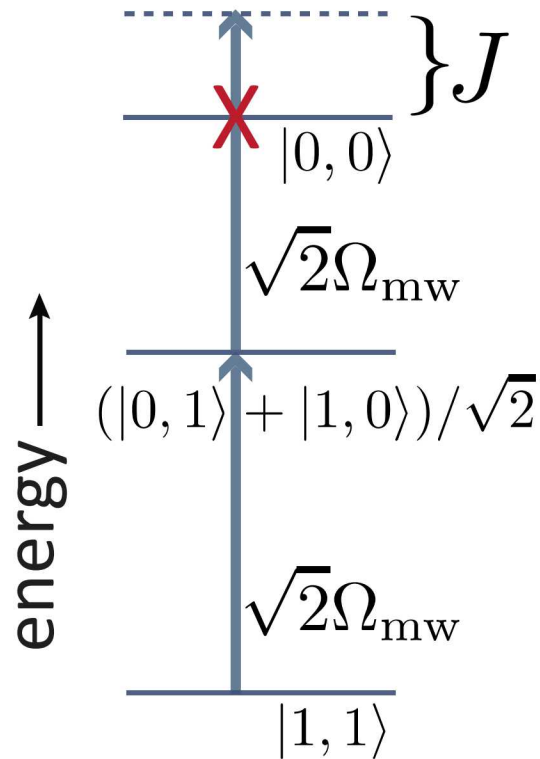
*Smooth and tunable!*



*Strong interaction*

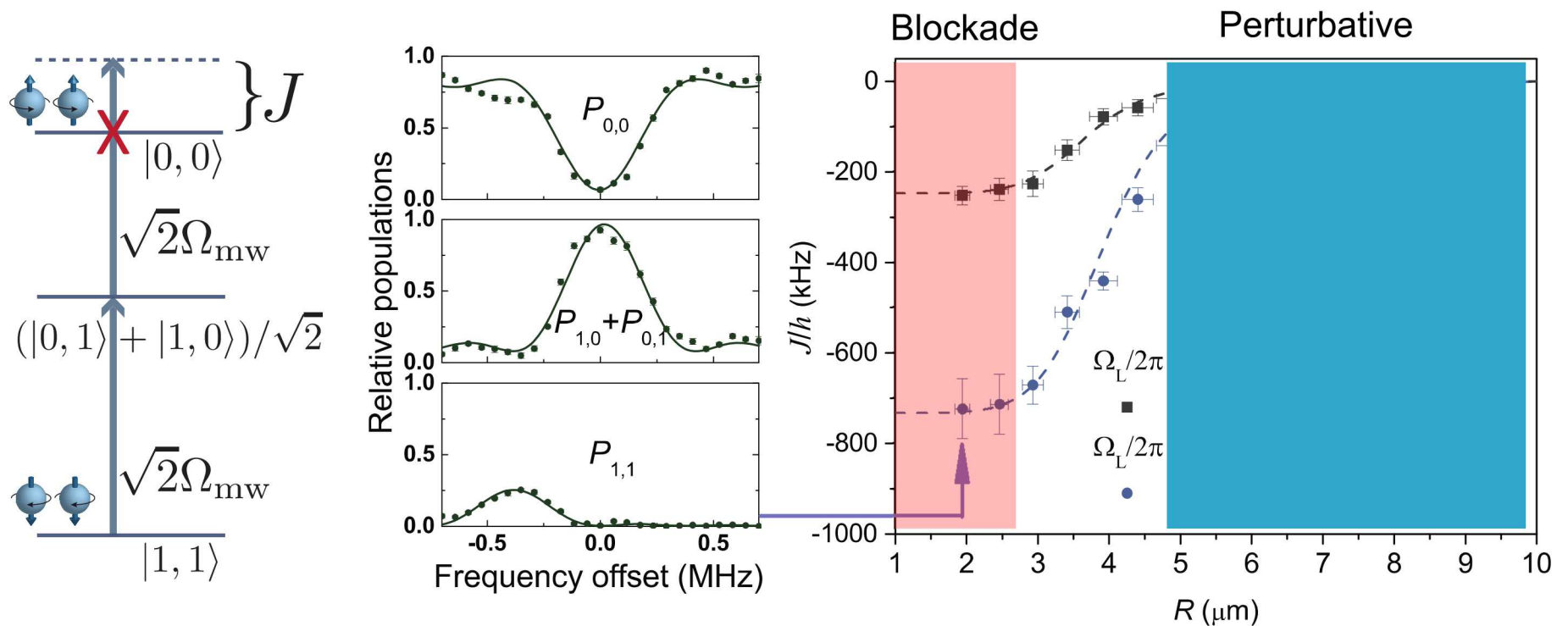
*Can be either  
positive or  
negative*

# Two-qubit microwave resonances



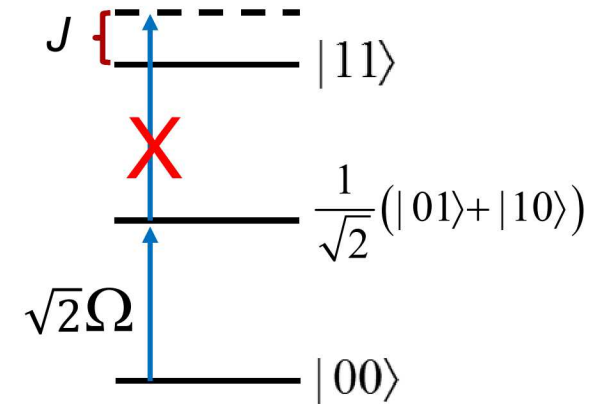
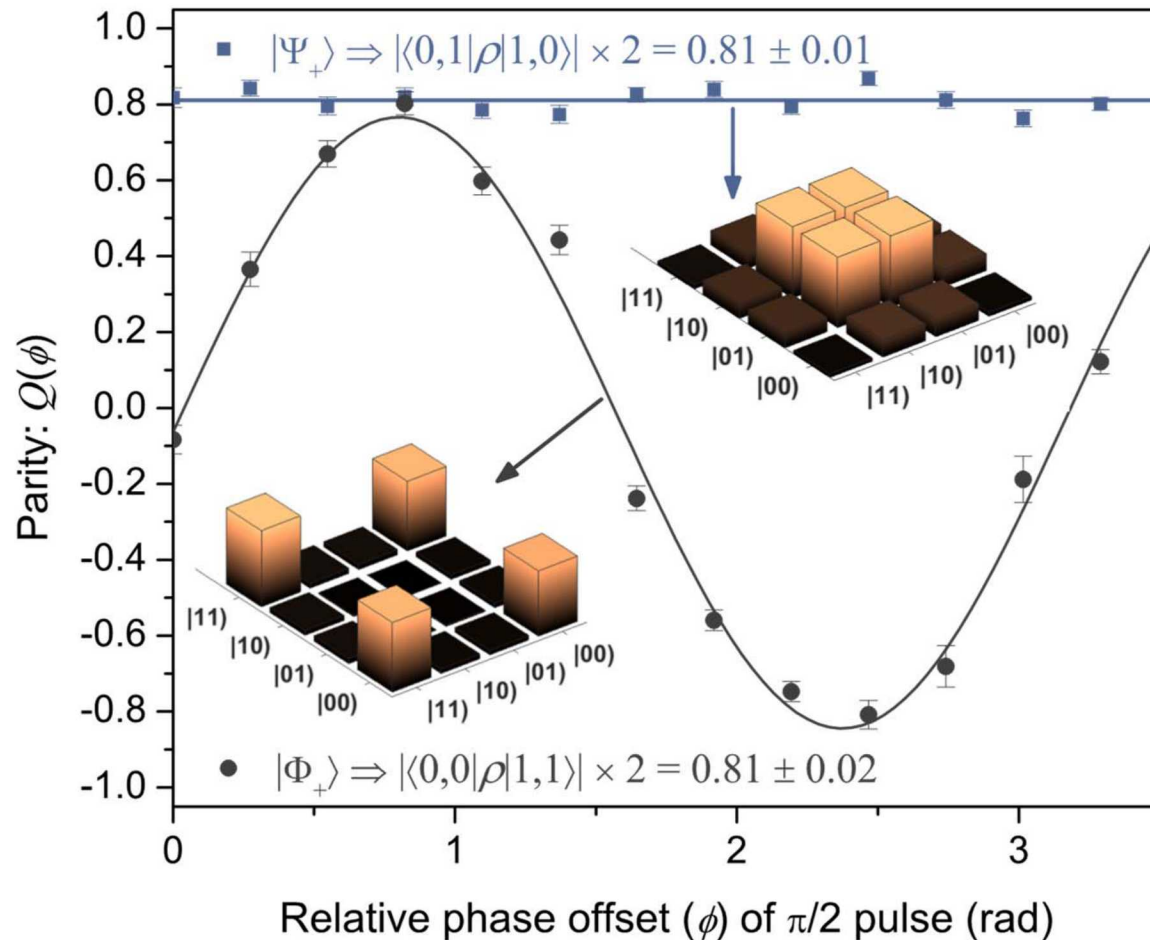
# Observing blockade on hyperfine qubit

Direct measurement of two-qubit interaction strength  $J$  as a function of two-atom separation with different dressing conditions.



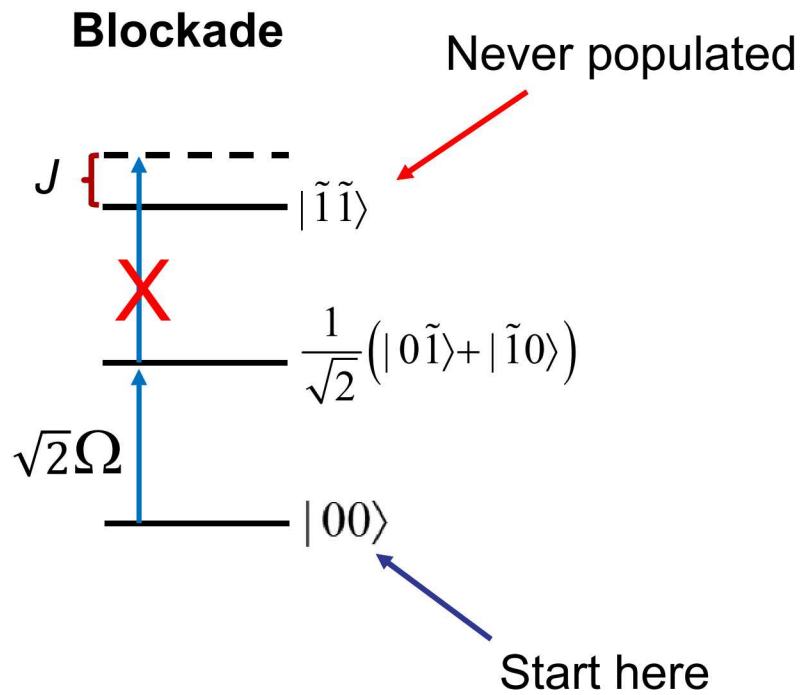
# Spin-flip blockade

Verify the entanglement via parity measurements



1. Prepare Bell state
2. Apply global  $\pi/2$  with given phase
3. Measure parity  $Q$
4. Obtain bound on fidelity = 0.81(2)

# Spin-flip blockade vs. CPHASE



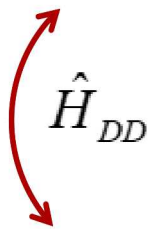
## Controlled Phase (CPHASE)

- Utilize nonlinear Hamiltonian that can be turned on at will:

$$\hat{H}_{DD} = J |\tilde{1}\tilde{1}\rangle\langle\tilde{1}\tilde{1}|$$

- Start in any state you want, e.g.,

$$|\psi_0\rangle = \frac{1}{2}(|0\rangle + |1\rangle) \otimes (|0\rangle + |1\rangle)$$

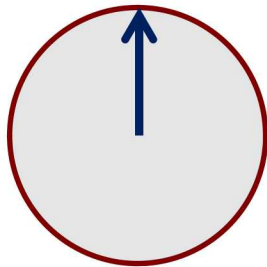
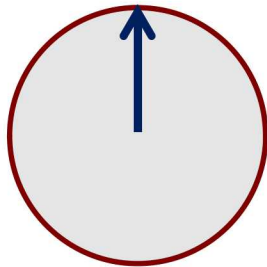


$$\rightarrow \frac{1}{2}(|00\rangle + |10\rangle + |01\rangle + e^{i\phi} |11\rangle)$$

Entangled state!

# Generating Entanglement

Phase:



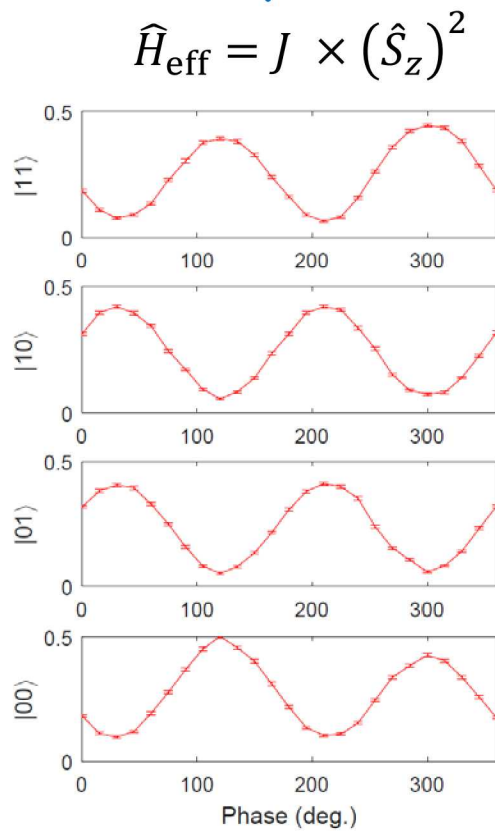
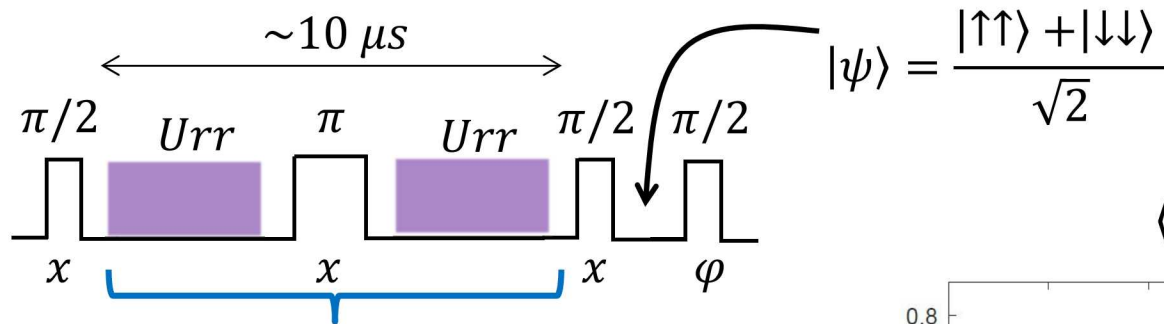
$$\hat{H}_{DD} = J |11\rangle\langle 11|$$

Laser **ON**F

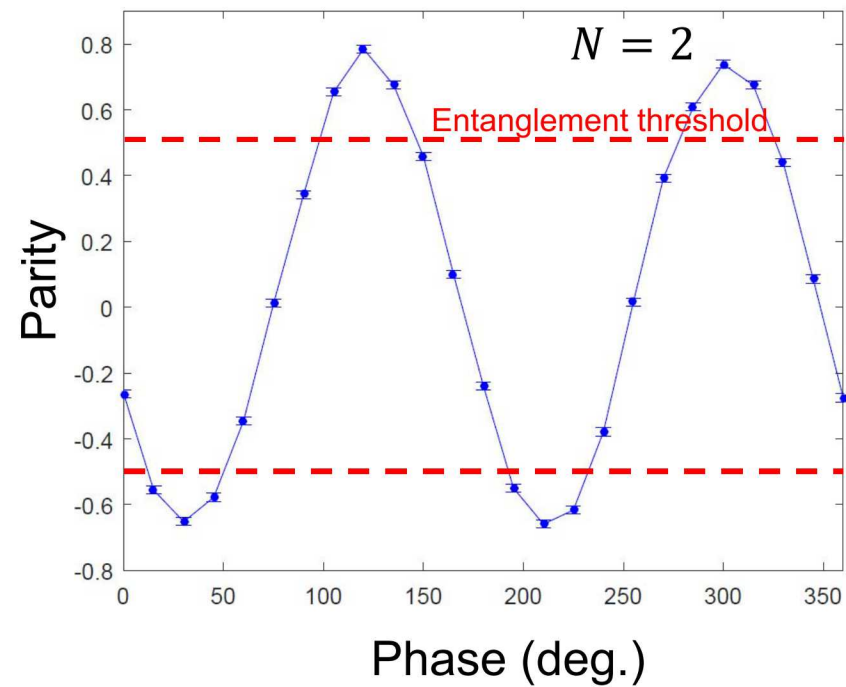
—————  $|11\rangle$

—————  $|01\rangle |10\rangle$   
and  $|00\rangle$

# Dressed CPHASE gate



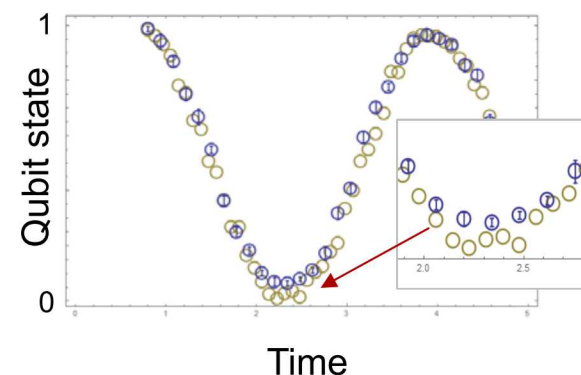
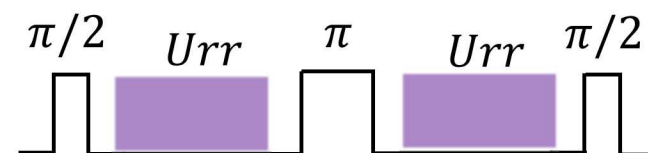
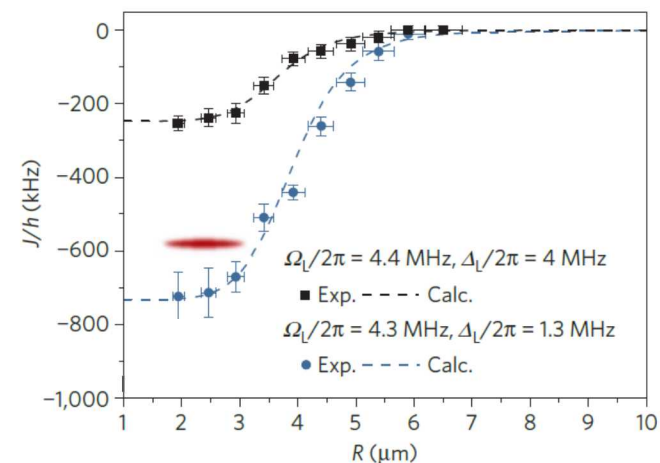
$$\langle \hat{\Pi} \rangle \propto \sin N\phi$$



J. J. Bollinger *et al.*, "Optimal frequency measurements with maximally correlated states." Phys. Rev. A **54**(6) (1996).

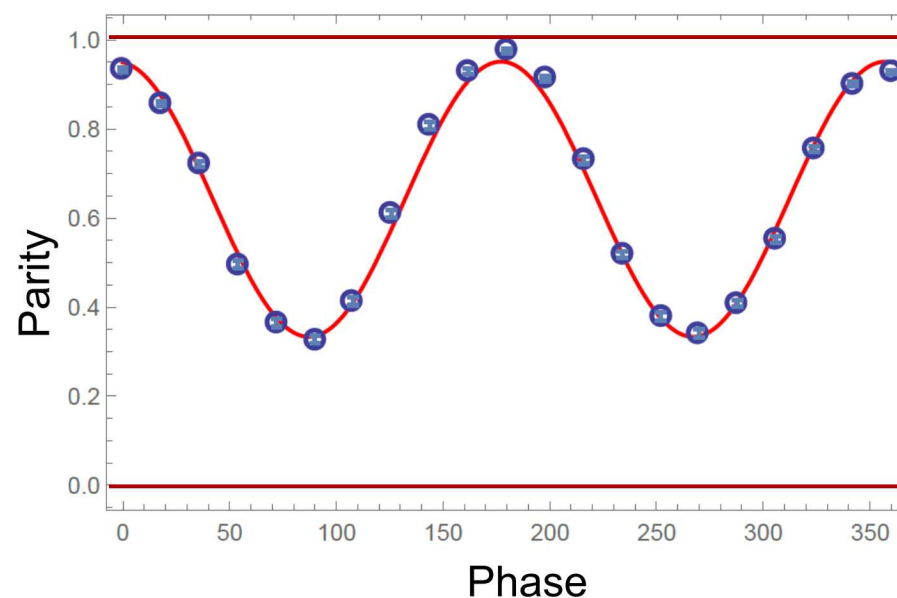
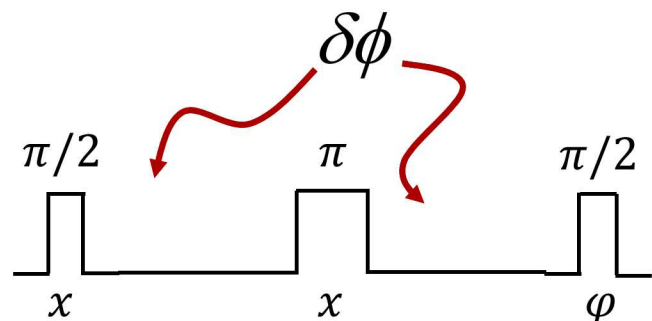
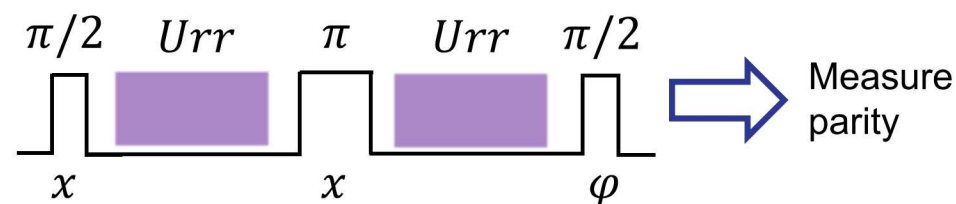
# Potential limitations

- Thermal, shot-to-shot, position spread
  - Measured position spread, currently limiting at the 3% level.
  - “Fine structure” in dressed Rydberg potential still a possible limitation.
- Doppler noise
  - Motion-dependent single-atom light shift.
  - Mitigated by echo to <0.1%
- State purity
  - Implemented extra state purification.
  - >97% purity demonstrated.
- Rydberg laser phase and amplitude noise
  - Characterized for current operating parameters: contributes <1%



# Local oscillator noise

- Sequence to test qubit rotation operations:
- Expect sine wave with peak-to-peak amplitude of 1.
- Measured results consistent with 0.5 rad RMS phase fluctuations:

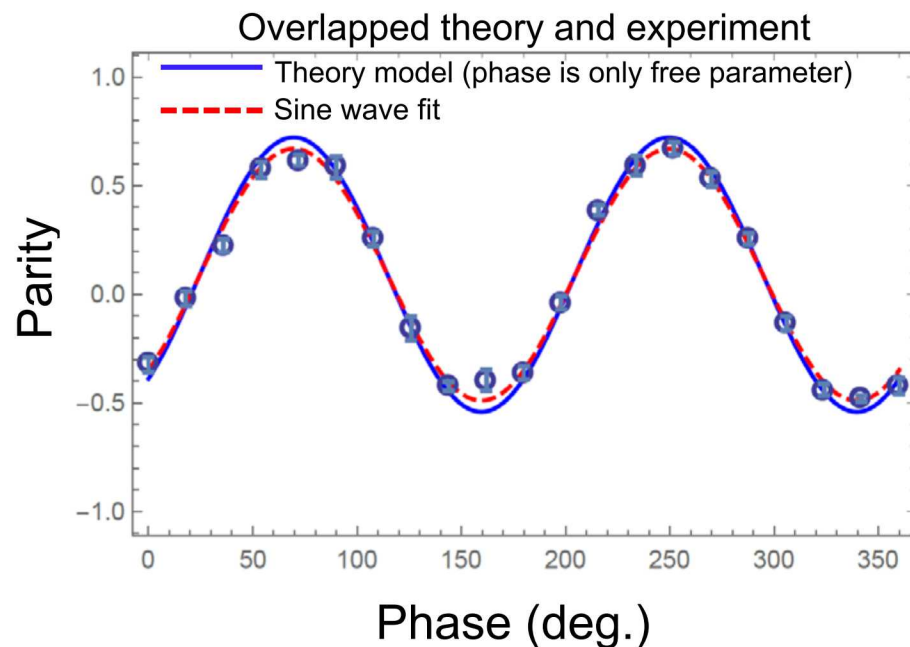


- Potential sources: **Raman Laser linewidth** and **near-resonant amplified spontaneous emission pedestal**.

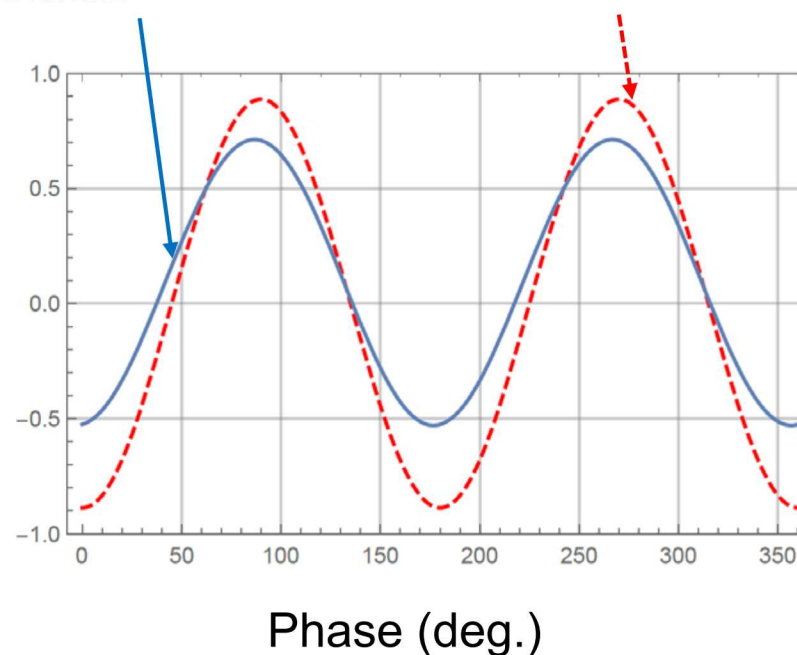
# CPHASE limitations

- Calculated the effect of :
  - Atomic position spread
  - Atomic velocity distribution
  - **Effective local oscillator phase noise**

➔ Theory model with measured noise parameters matches data.

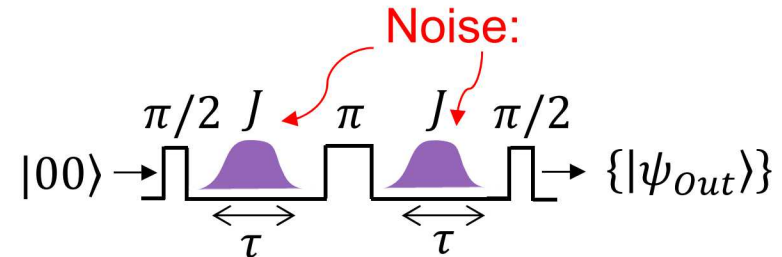


Theory including all noise.



# Error budget for CPHASE gate

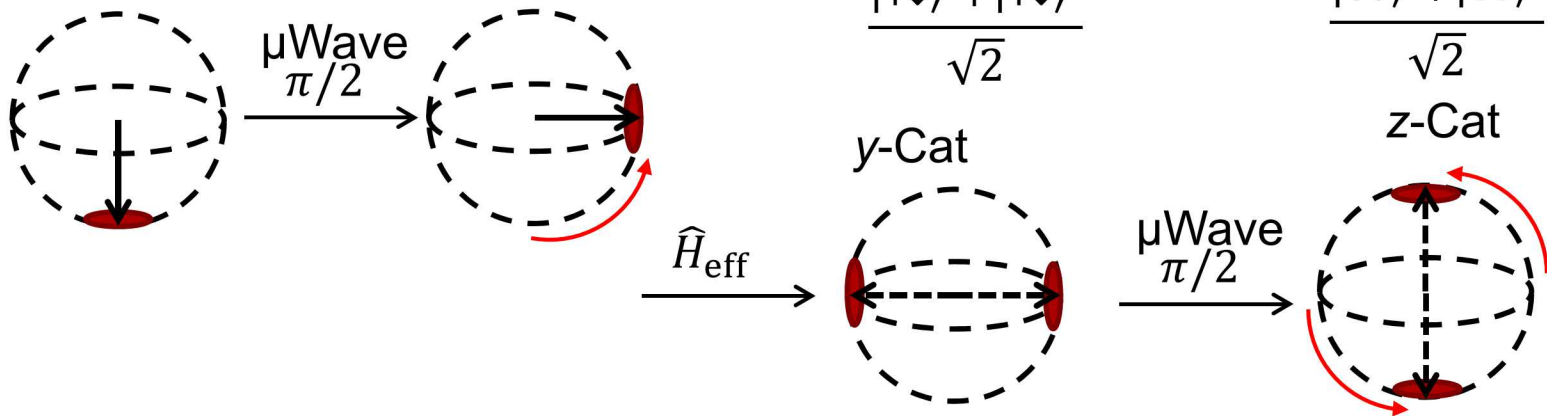
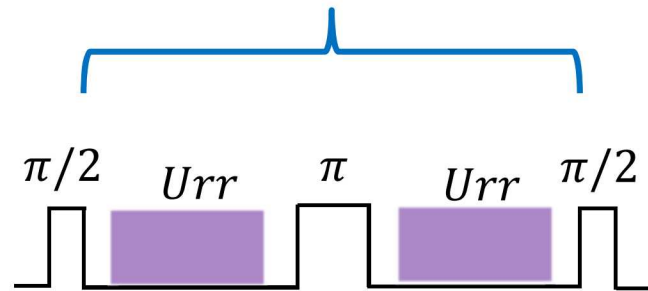
$$\text{Fidelity} = \langle \psi_{tar} | \rho_{out} | \psi_{tar} \rangle$$



Effect	Fidelity reduction	Mitigation
LO noise	10% $\pm$ 0.1%(stat.) $\pm$ 2%(sys.)	Clean Raman laser/ $\mu$ Wave cavity
State purity	<3%	Clean Raman laser/ $\mu$ Wave cavity
Atomic position spread	3% $\pm$ 0.5%	Sideband cooling to ground state
Wave-packet overlap	<0.1%	Sideband cooling to ground state
Atomic velocity spread	<0.1%	Sideband cooling to ground state
318 nm Laser frequency noise	0.2% $\pm$ 0.1%	Pre-stabilized seed lasers, different detuning, dynamical decoupling
Spontaneous emission	0.4% $\pm$ 0.2%	Higher principal quantum #
318 nm laser amplitude noise	<0.1%	Install “noise eater” on laser

# Scaling to $N$ atoms

$$\hat{H}_{\text{eff}} = Urr \times (\hat{S}_z)^2$$



-  $\hat{S}_z$  is the collective  $S_z$  spin operator for the pseudospin  $N/2$  system.

- For  $N$  atoms all within a blockade radius, an  $N$ -atom cat state forms at  $J \times \tau = \pi/2$

(2-atom case)

$$\frac{|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle}{\sqrt{2}}$$

$y$ -Cat

(2-atom case)

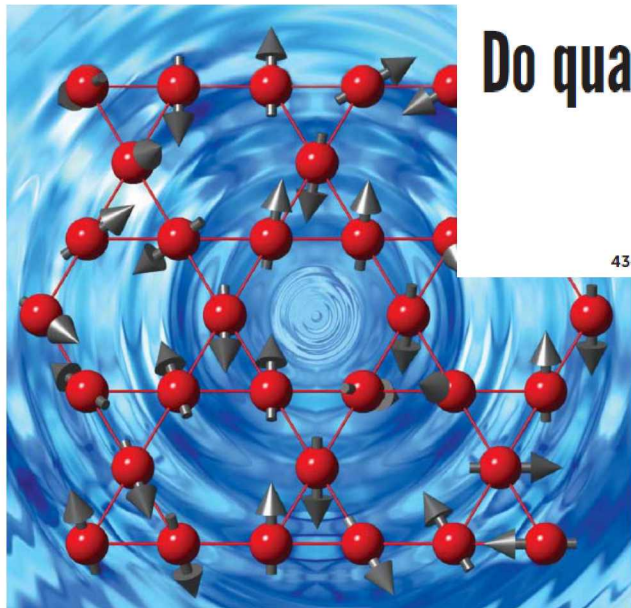
$$\frac{|\uparrow\uparrow\rangle + |\downarrow\downarrow\rangle}{\sqrt{2}}$$

$z$ -Cat

# Scaling to larger systems

## Rydberg physics:

- Enable creation of large-scale entangled states.
- Create geometries that can simulate interesting, physically-relevant, models of quantum magnetism.



## Do quantum spin liquids exist?

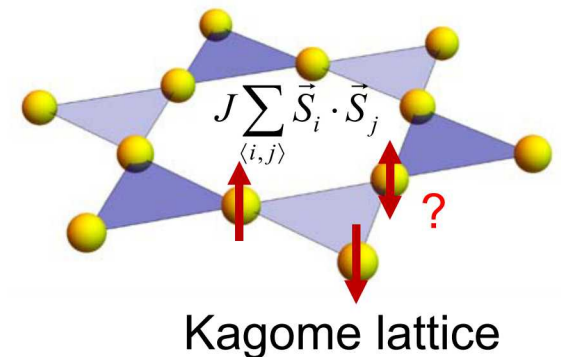
Takashi Imai  
and Young S. Lee

The search for the hypothetical state has been a 43-year-long slog, one whose end may now be in sight.

## Methods for realizing Hamiltonians for quantum magnetism:

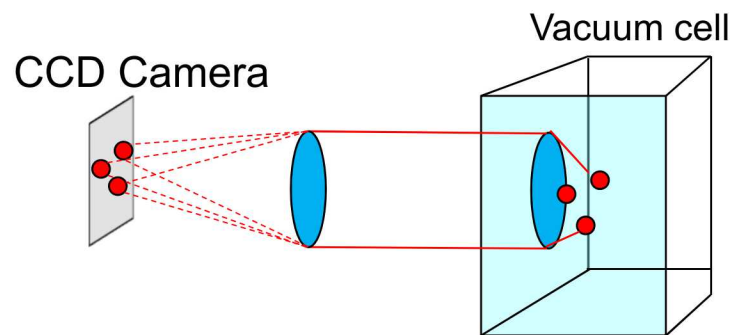
$$\hat{H} = \sum_{\langle ij \rangle} \alpha \hat{S}_x^i \cdot \hat{S}_x^j + \beta \hat{S}_y^i \cdot \hat{S}_y^j + \gamma \hat{S}_z^i \cdot \hat{S}_z^j$$

Glaetzle *et al.*, Phys. Rev. Lett. **114**, 173002 (2015).



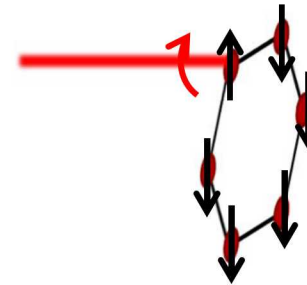
# Technical challenges

## 1. Single-site imaging capabilities with $1\ \mu\text{m}$ -scale resolution.



✓ -Established techniques exist

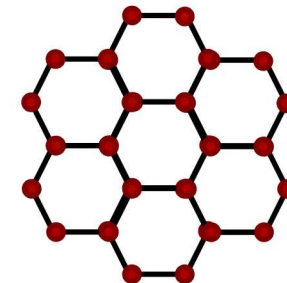
## 2. Single-site addressing



✓ -Established techniques exist

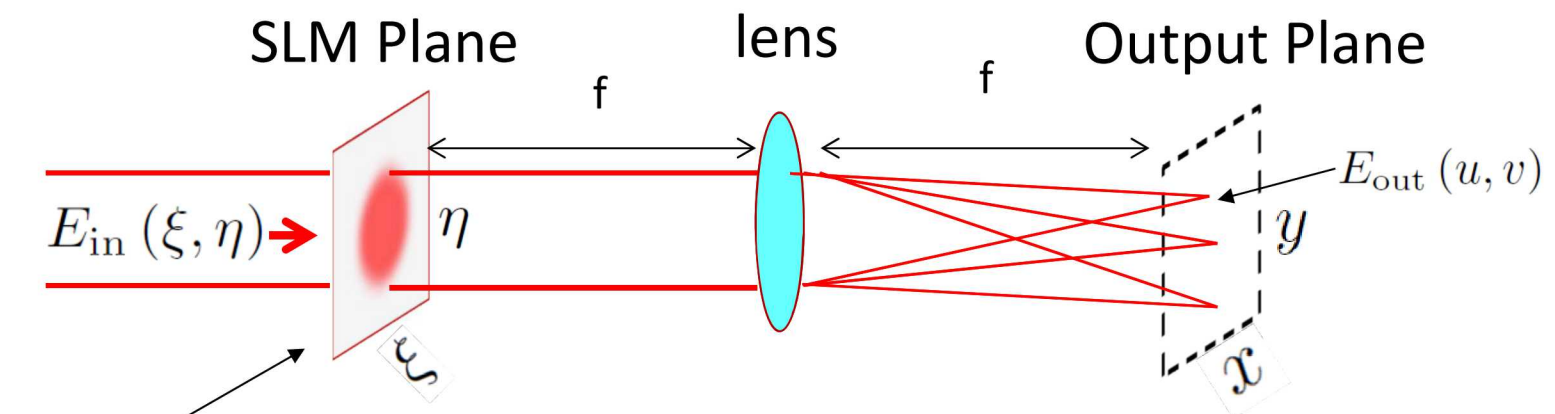
## 3. Reproducible atomic configurations:

- Example: unity filling-factor lattice.
- How to fill complex patterns consistently?



# Background: Physical optics

We utilize the Fourier-Transform properties of a lens in scalar diffraction theory (i.e., treat the electric field as a complex-valued scalar field). Here, the output field is related to the phase-imprinted input field by a scaled Fourier Transform.



$$\mathcal{M}(\xi, \eta) = \exp[i\phi(\xi, \eta)]$$

Phase mask is imprinted on input field

Output field is a scaled Fourier transform of the field in the SLM plane. The SLM plane field is given by the product of the input field and phase mask.

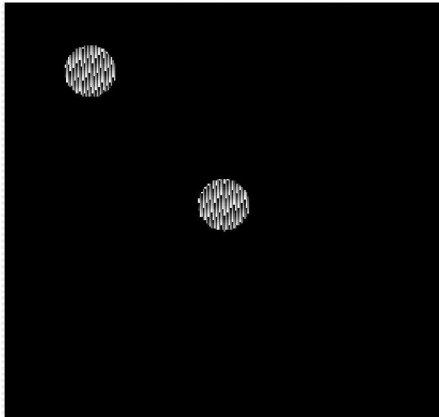
$$E_{\text{out}}(u, v) = \mathcal{F}[E_{\text{in}}(\xi, \eta) \mathcal{M}(\xi, \eta)]$$

Where output coordinates are scaled as:

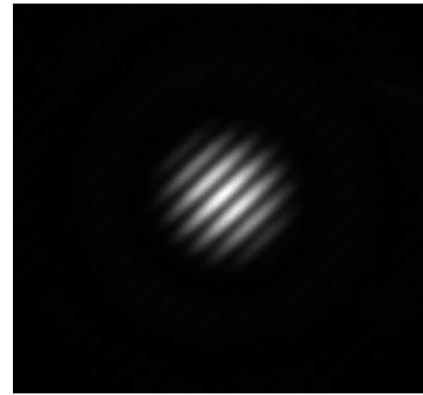
$$v = y/(\lambda f), \quad u = x/(\lambda f)$$

# Control of point source interference for measuring local phase

Phase mask

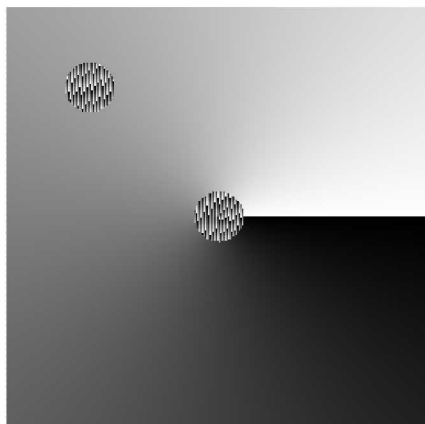


$\mathcal{F}$

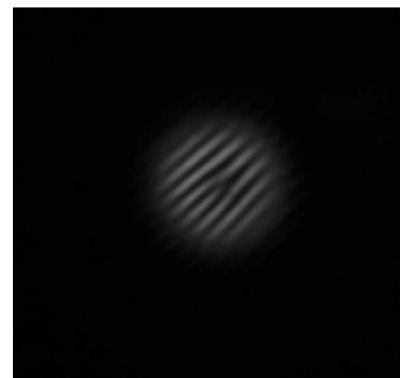


Two sources in the Fourier plane (right) diffract and interfere in the image plane (left).

Phase mask



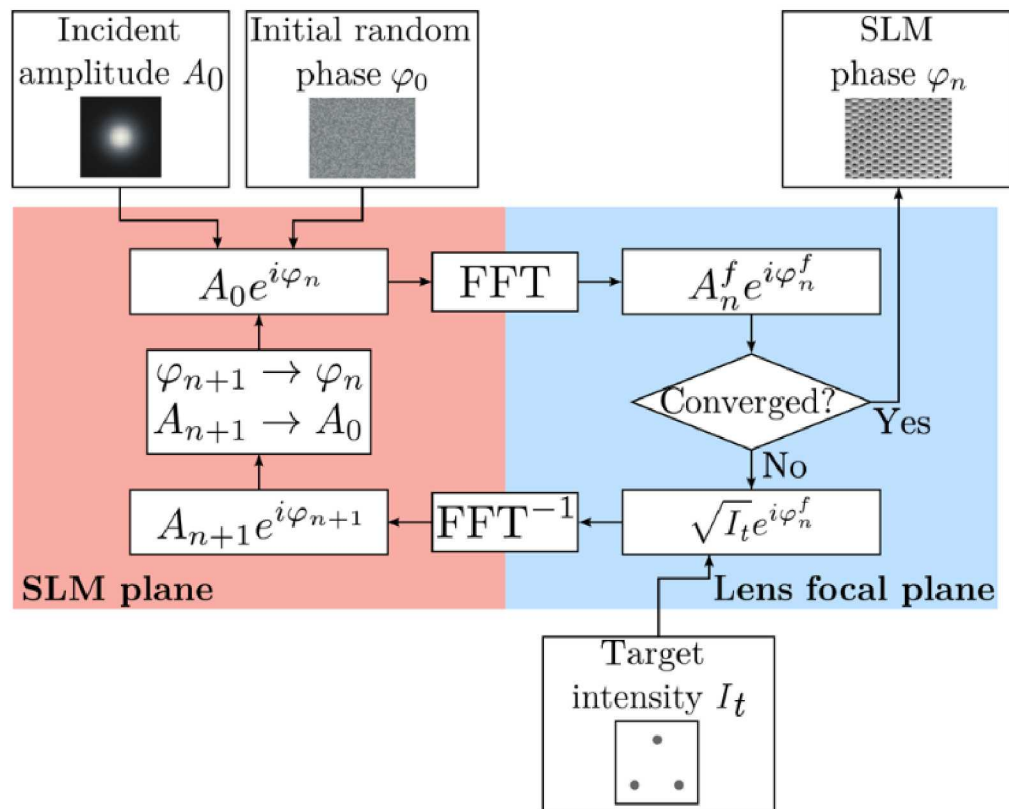
$\mathcal{F}$



As above, but now the spot in the middle contains a phase singularity.

# Background: Computing holograms

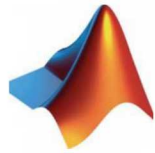
## Gerchberg-Saxton loop



- An arbitrary complex field is completely defined by its Fourier Transform, which includes both amplitude and phase.
- The Gerchberg-Saxton (GS) algorithm attempts to find a phase-only pattern that Fourier Transforms into a desired intensity pattern.
- The GS algorithm iterates between the Fourier (SLM plane) and the image plane (Lens focal plane).
- Before iterating to the Fourier plane, the field amplitude is replaced with the desired amplitude (phase is kept).
- Before iterating back to the image plane, the amplitude is replaced by the input field amplitude.

**Image from:** F. Nogrette, *et al.*, "Single-Atom Trapping in Holographic 2D Arrays of Microtraps with Arbitrary Geometries," *Phys. Rev. X* **4**, 021034 (2014).

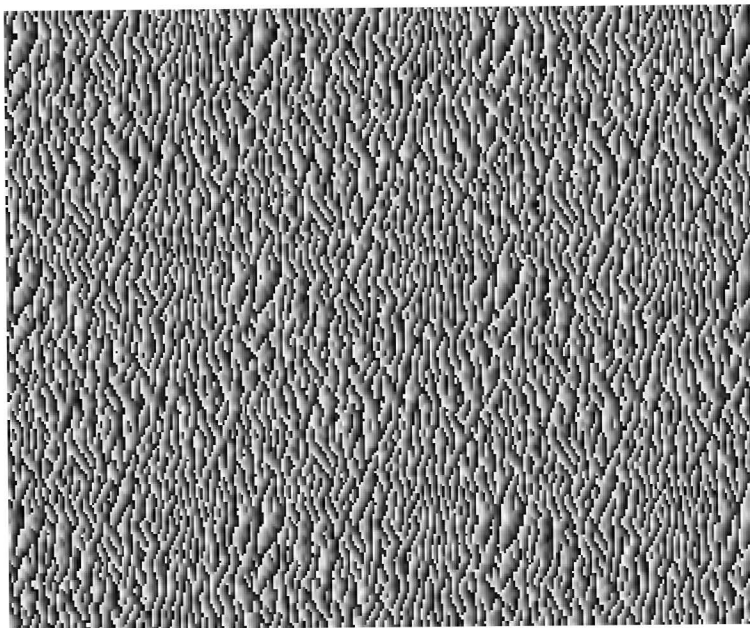
# Generation and control of >500 of individual traps



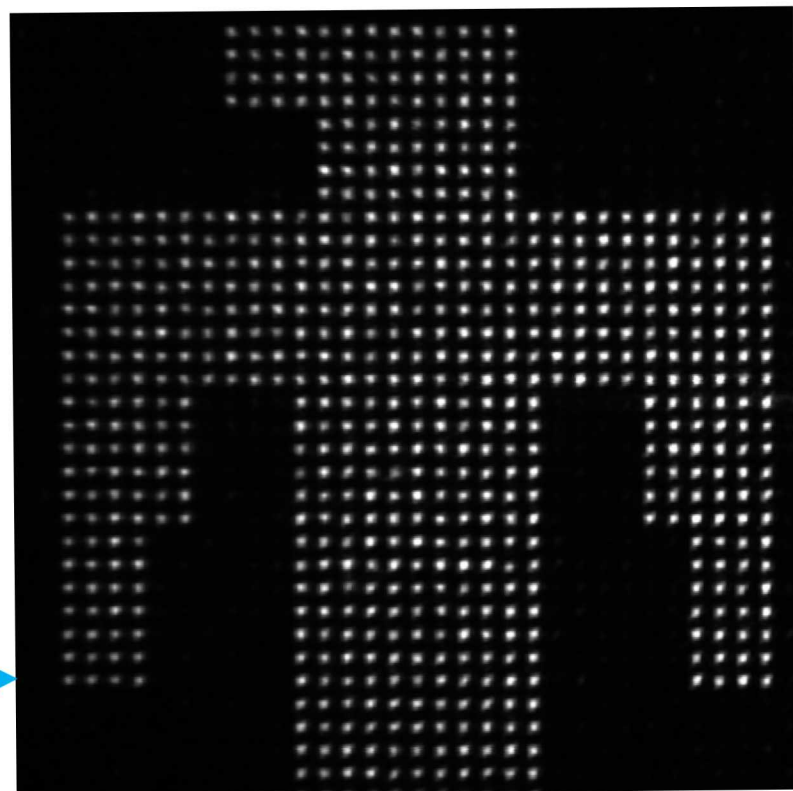
MATLAB code deploys Gerchberg-Saxton algorithm  
With GPU compute acceleration  
(~50 Hz hologram calculation)



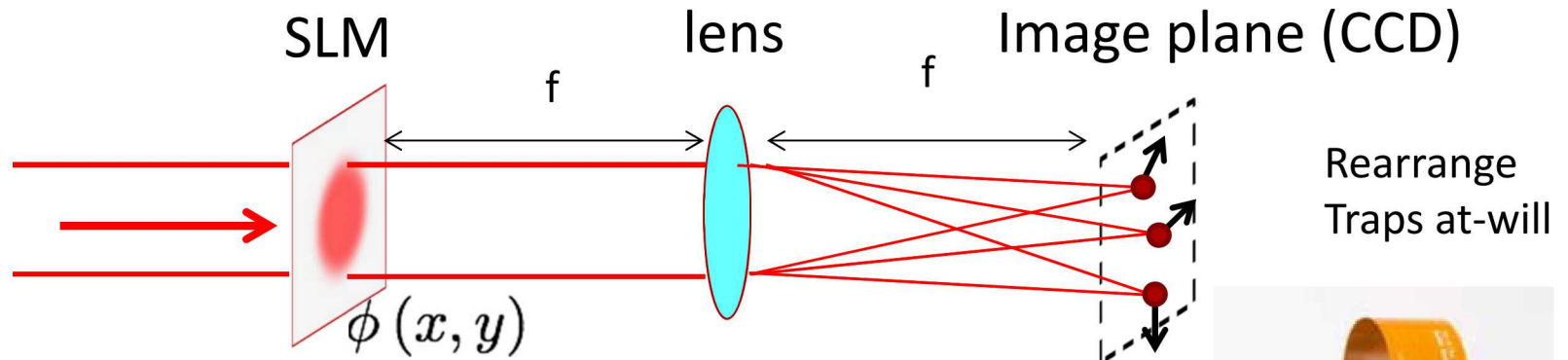
Phase to SLM



Intensity profile (measured)



# Generating dynamical traps for deterministic loading and manipulation.



1. Minimize trap distortion as frames advance through tailored algorithms.
2. Compute SLM “movie”, comprising ~100 frames with as little dead time as possible using parallel computation.
3. Verify that trap motion will not cause trap loss via measurement of trap intensity fluctuations.

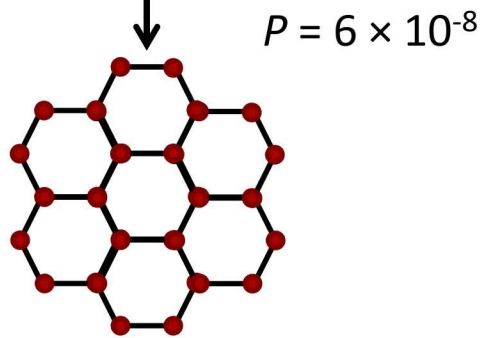
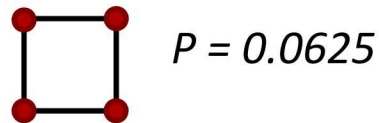
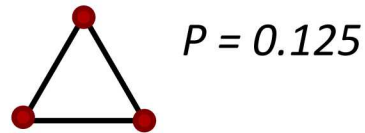


# Deterministic loading

## Without dynamic control

Probability of perfect loading scales exponentially with atom number

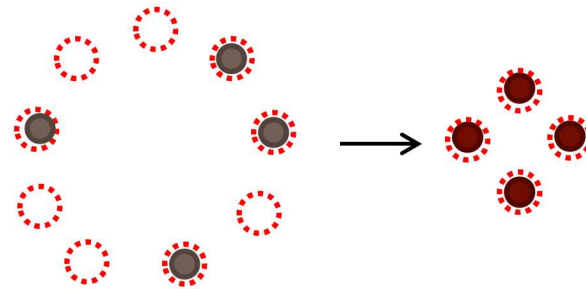
1 second



1 month

## With dynamic control

*e.g.*, Attempt to load 9 traps, reconfigure to a desired pattern with four atoms.



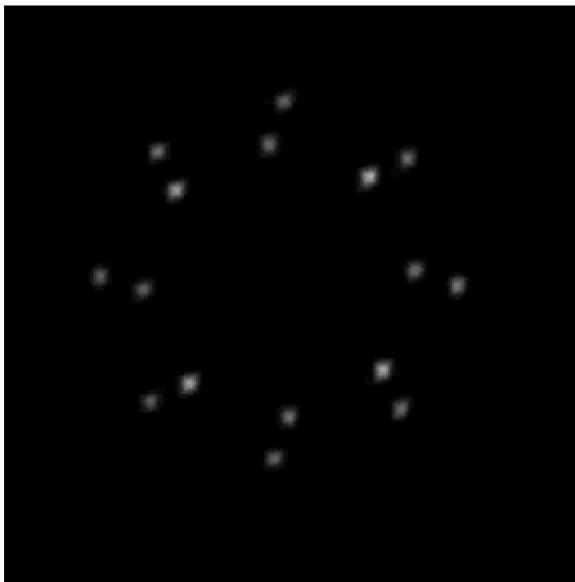
## Scale to larger arrays

See:

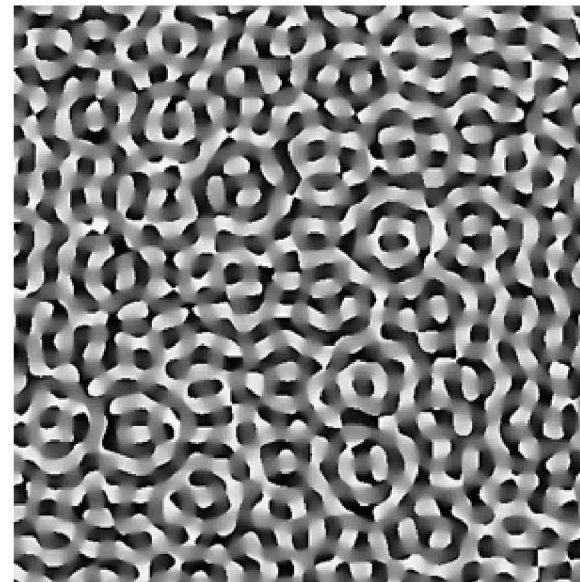
W. Lee et al., Phys. Rev. A **95**, 053424 (2017)

# Dynamic control of hologram-generated traps (movie disabled)

30 fps, real time



Phase hologram

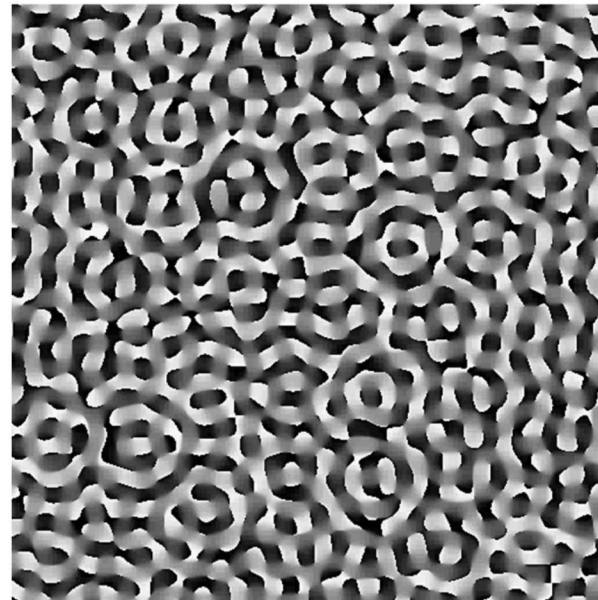


# Dynamic control of hologram-generated traps

30 fps, real time

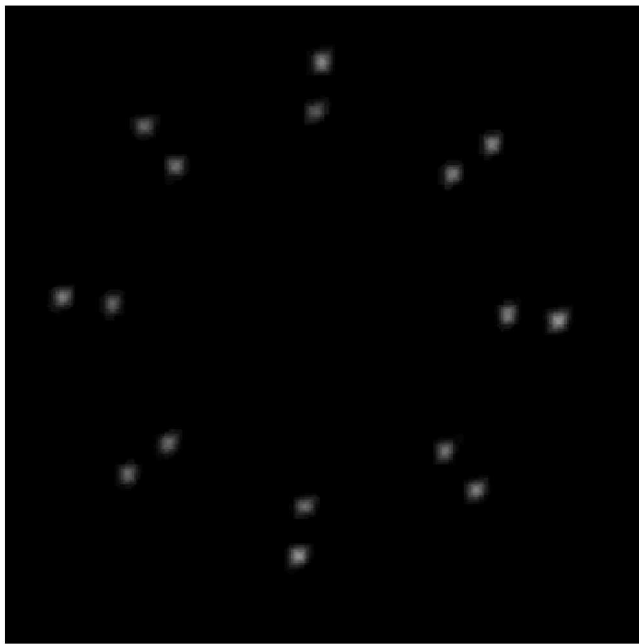


Phase hologram



# Dynamic control of hologram-generated traps (movie disabled)

500 fps played at 30 fps



-Optimize techniques for calculating hologram with as little phase discontinuity between frames as possible.

# Dynamic control of hologram-generated traps

500 fps played at 30 fps



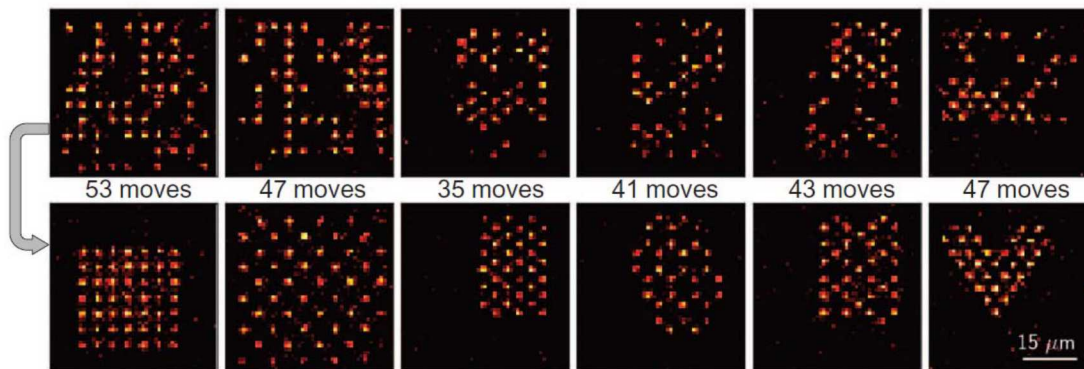
-Optimize techniques for calculating hologram with as little phase discontinuity between frames as possible.

# Defect-free neutral atom arrays

## Lukin group, Harvard<sup>1</sup>

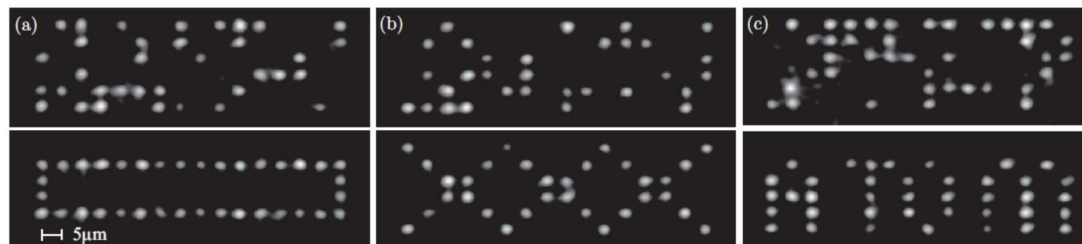


## Browaeys group, Institut d'Optique (France)<sup>2</sup>



- There has been a revolution in creating defect free, controllable arrays of neutral atoms.
- 1D and 2D arrays demonstrated.
- This capability makes scaling to a many qubit simulator a reality.

## Ahn Group, KAIST (South Korea)<sup>3</sup>

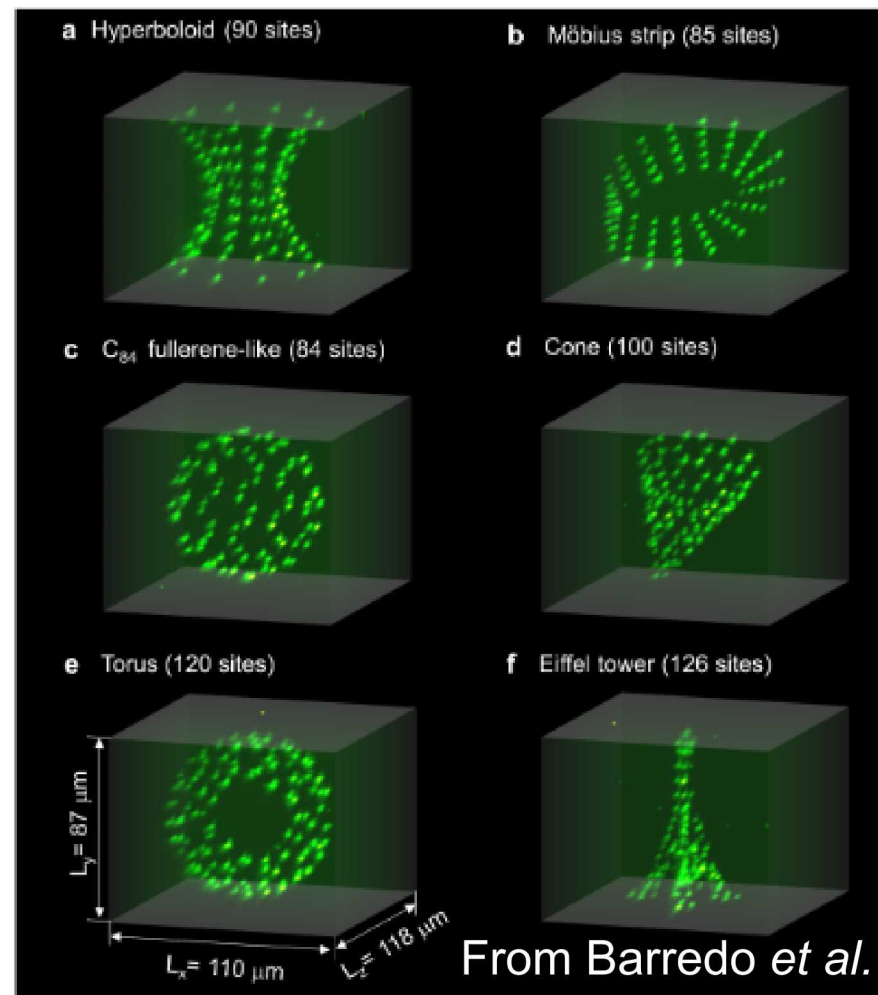


1. M. Endres et al., Science 354, 1024 (2016)
2. D. Barredo et al., Science 354, 1021 (2016)
3. W. Lee et al., Phys. Rev. A **95**, 053424 (2017)

# Defect-free neutral atom arrays

## Now in 3D

- 3D Gerchberg-Saxton algorithms allows 3D control of trap sites.
- Opens the door to studying complex quantum systems with neutral atoms.

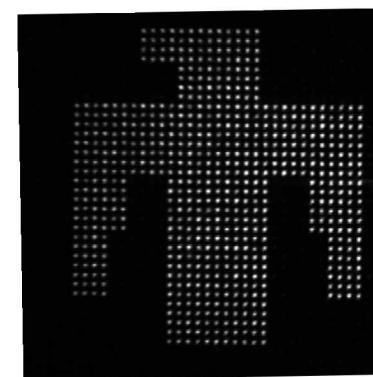
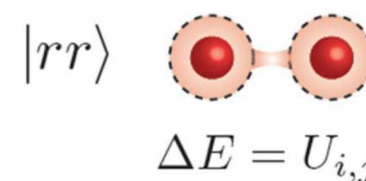


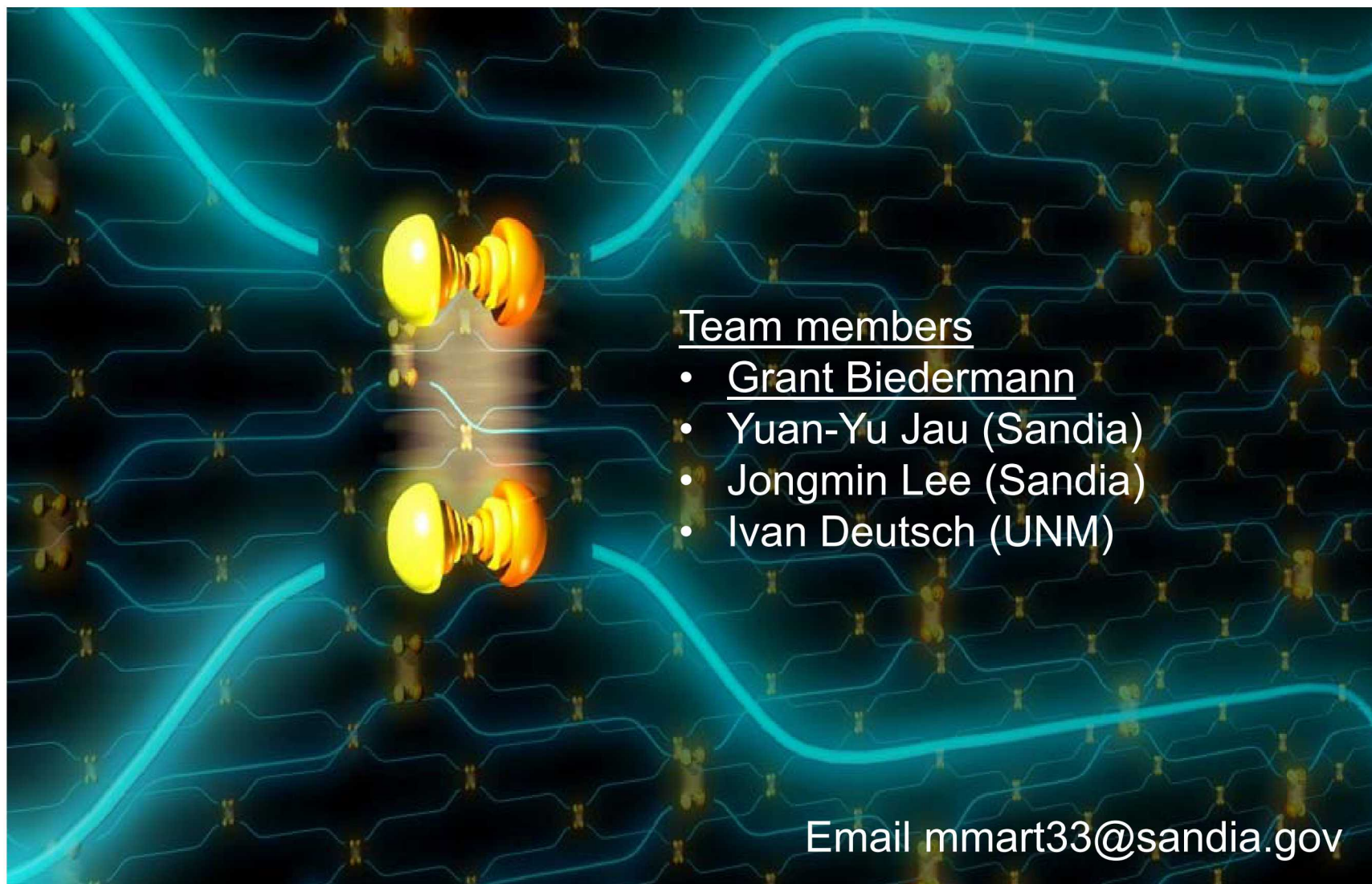
D. Barredo, V. Lienhard, S. de Léséleuc, T. Lahaye, A. Browaeys, “Synthetic three-dimensional atomic structures assembled atom by atom”, arXiv:1712.02727 (2017).

# Concluding remarks

- Optical systems are enabling big advances in atomic physics!
- Single-photon Rydberg dressing opens up possibilities for large-scale entanglement via both quantum control direct Hamiltonian evolution, and quantum simulation.
- Protocols demonstrated at SNL show that high-quality entanglement between neutral atoms is not far off.

Strongly interacting





Team members

- Grant Biedermann
- Yuan-Yu Jau (Sandia)
- Jongmin Lee (Sandia)
- Ivan Deutsch (UNM)

Email [mmart33@sandia.gov](mailto:mmart33@sandia.gov)