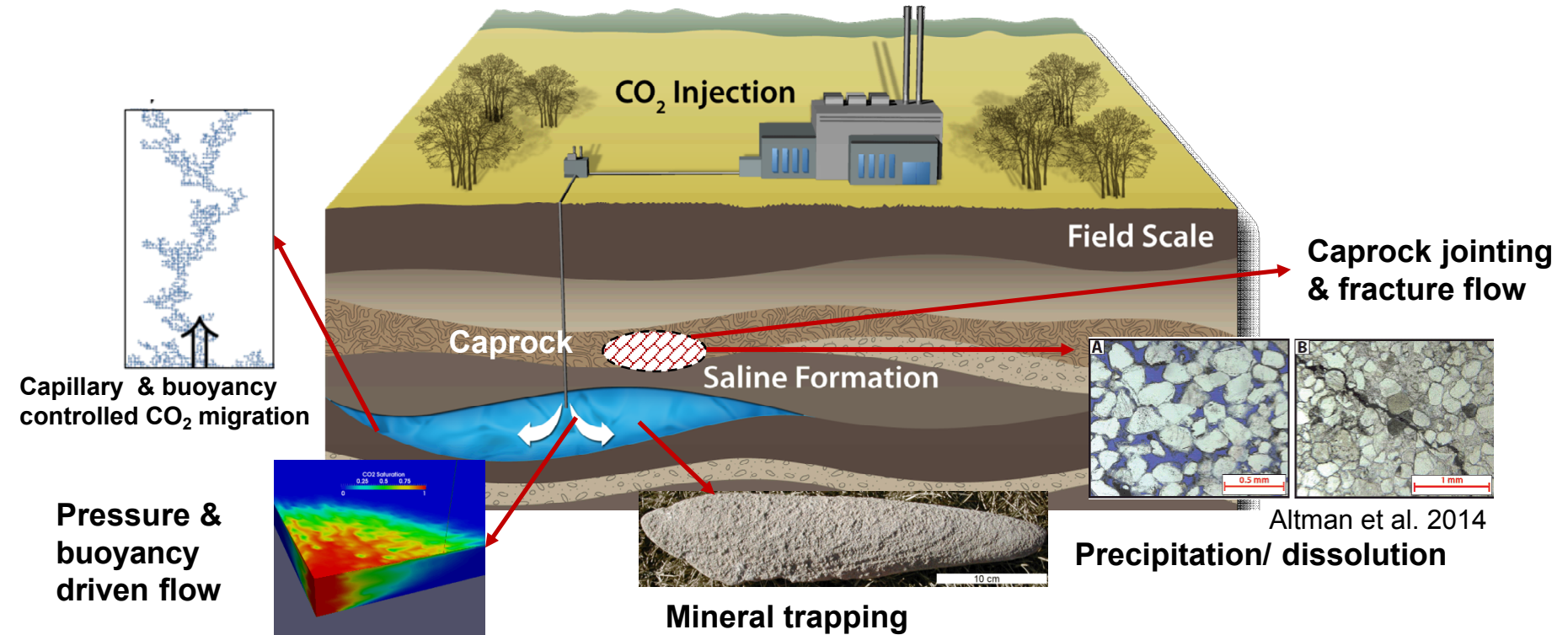


Benchmark: Modeling CO₂ gas flow in a heterogeneous sand architecture

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CO₂ Flow and Transport Processes during Geological Carbon Storage



- **Sustaining large storage rates**, of order gigatons of CO₂ per year in the US, for decades without compromising other subsurface resources and without jeopardizing the security with which the CO₂ is stored;
- **Using pore space with unprecedented efficiency**, i.e., placing CO₂ so that it occupies half of the reservoir volume, rather than the typical current estimate of less than five percent;

Intermediate scale experiment

1. to understand and quantify the physics of the transition from compact flow to capillary channel flow (coupled with core-scale experiments)
2. to develop new experimental-informed, physics-based models of this transition process, focused on representing cm-scale heterogeneity, with the goal of developing constitutive models suitable for reservoir-scale simulators

Light transmission system

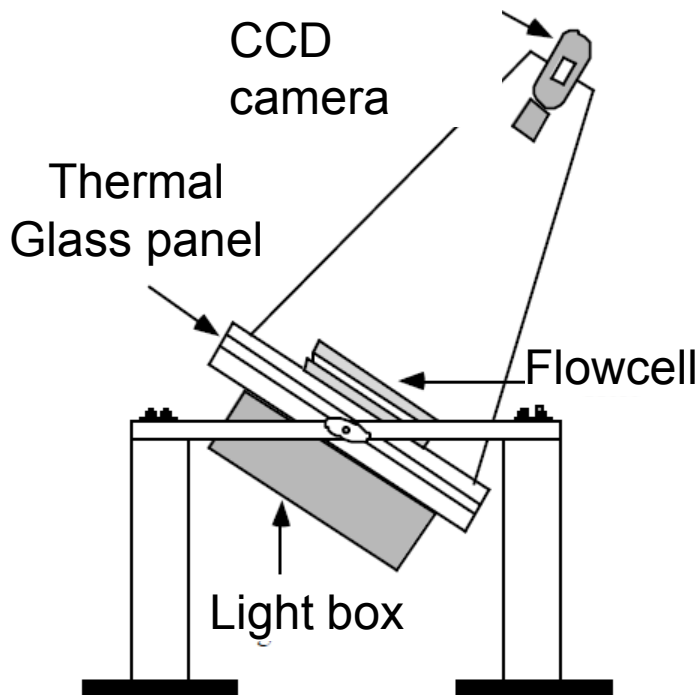
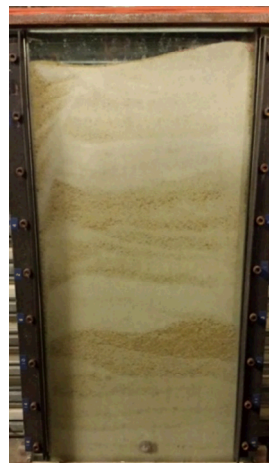


Image resolution: 0.1-1 mm

Data acquisition: < 1 sec

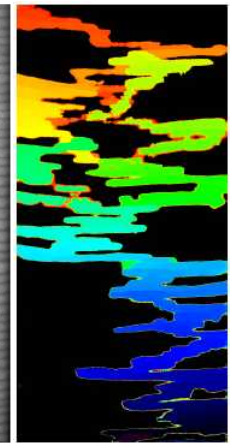
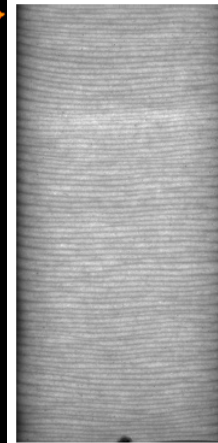
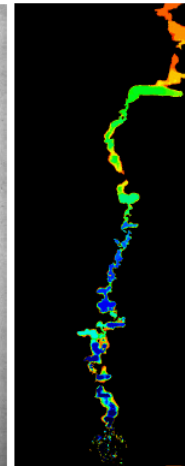
Examples with CO₂ gas flow



~30 cm



Weak layering

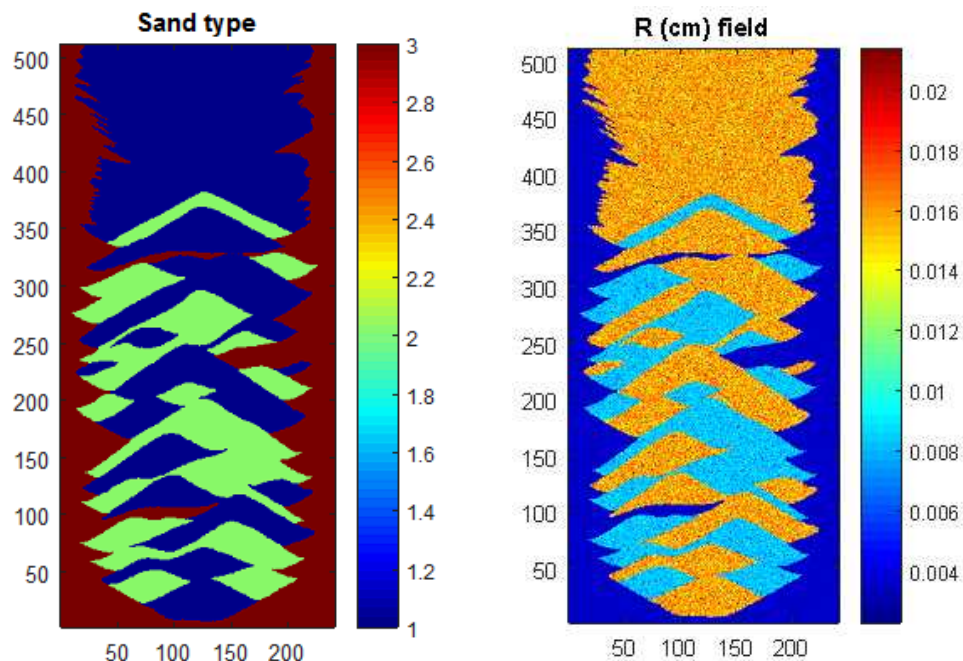


Strong layering

(Glass et al. 1998, 2000, 2001, 2003, WRR)

Overview Bob Glass Experiments

Experimental image



Sand 1: Accusand 12-20

Sand 2: Accusand 30-40

Sand 3: Accusand 50-70

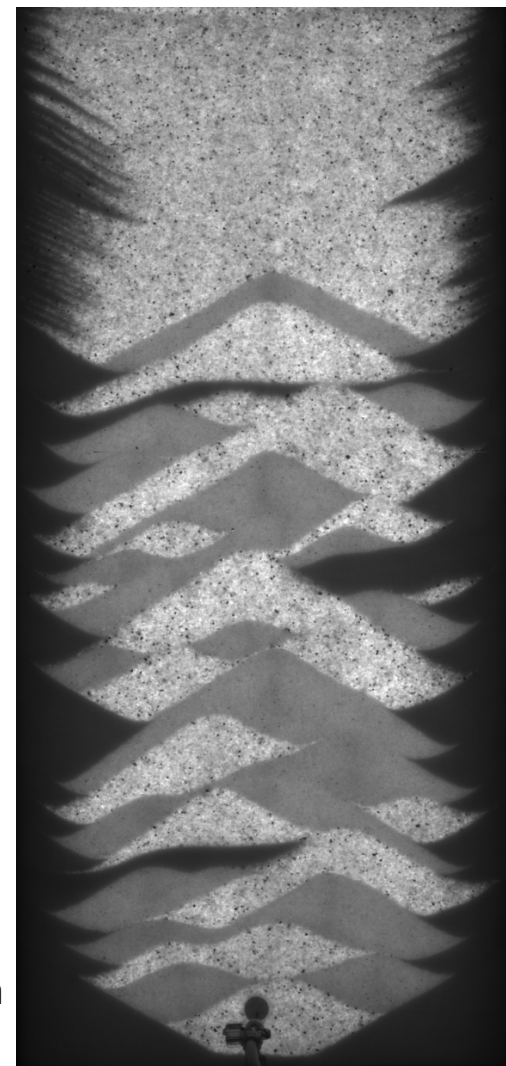
Grid: 240 x 511 (dx=dy=0.1087cm)

Origin: lower left corner in figures

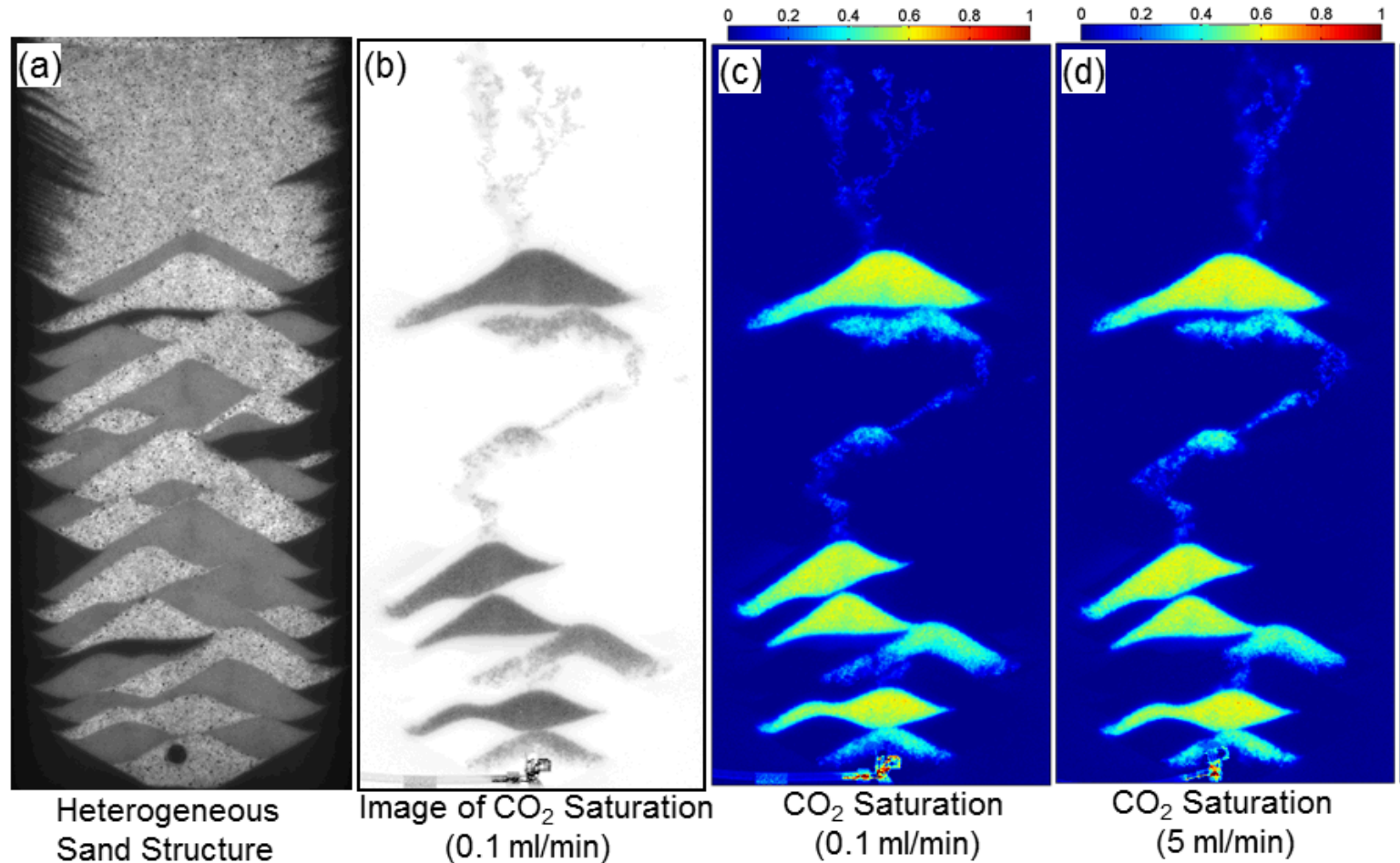
Dimension: 26.088cm x 55.55cm x 1cm

Injection hole: Diameter=11 pixels at (110.5, 35.5) in [240 x 511] grid system

Injection rates: 0.1, 0.5, 1, 2, 5 mL/min



Experimental Data Analysis



- (a) Experimental heterogeneous sand structure (26 cm wide, 55.5 cm tall) of Glass et al. showing the fine sand (dark, #50-70), medium sand (gray, #30-40), and coarse sand (light, 12-20) units.
- (b) CO₂ saturation image at a CO₂ gas injection rate of 0.1 ml/min.
- (c-d) Experimental CO₂ saturations just after CO₂ gas reached the top of the chamber at 0.1 mL/min and 5 ml/min, respectively.

Overview of Model – Aria

- Solve Darcy equations for two-phase immiscible fluid flow using thermal/fluids finite-element code Aria (SNL code)

$$\frac{\partial}{\partial t}(\rho_w \phi(1 - S_n)) = \nabla \cdot \left(\rho_w \frac{k_{rw}}{\mu_w} \mathbf{K} \cdot (\nabla p - \rho_w \mathbf{g}) \right) + Q_w$$

$$\frac{\partial}{\partial t}(\rho_n \phi S_n) = \nabla \cdot \left(\rho_n \frac{k_{rn}}{\mu_n} \mathbf{K} \cdot (\nabla p + \nabla p_c - \rho_n \mathbf{g}) \right) + Q_n$$

$$p_c = p_n - p_w$$

$$S_w + S_n = 1$$

Overview of Model – Aria (cont.)

- Capillary Pressure use van Genuchten function:

$$p_c = p_{c0} \left(s^{-\frac{1}{\lambda}} - 1 \right)^{\frac{1}{\beta}}$$

$$\lambda = 1 - \frac{1}{\beta} \quad , \quad \beta > 1$$

$$s = (S_w - S_{w,r}) / ((1 - S_{nw,r}) - S_{w,r})$$

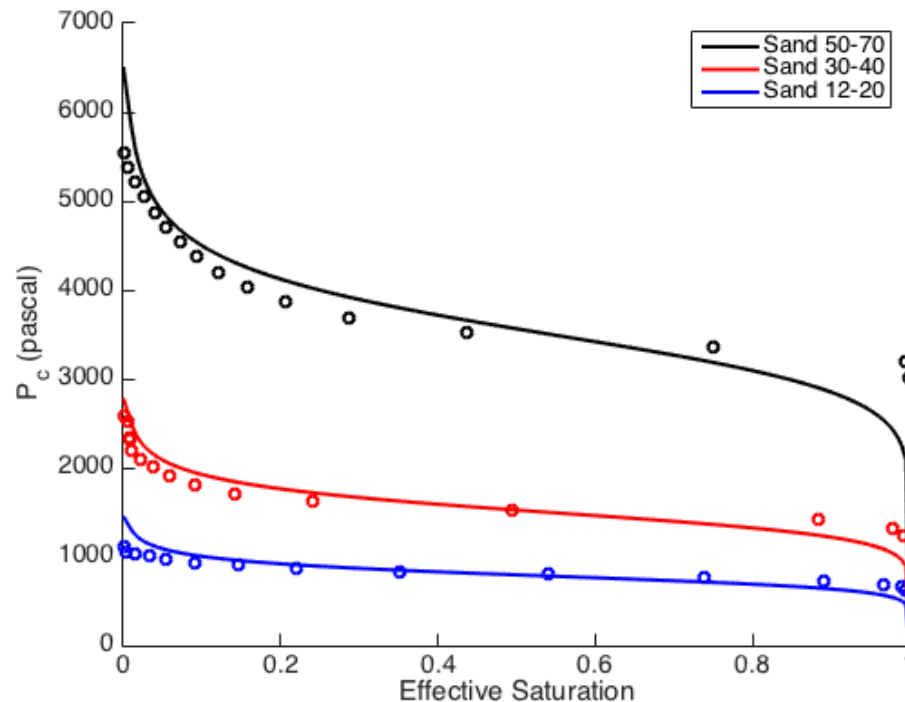
- Relative perm use van Genuchten function:

$$k_{rl} = \sqrt{s} \left[1 - \left(1 - s^{\frac{1}{\lambda}} \right)^{\lambda} \right]^2$$

$$k_{rg} = \sqrt{1 - s} \left[1 - s^{\frac{1}{\lambda}} \right]^{2\lambda}$$

Capillary Pressure Curves

- Fit data to provided capillary pressure curves measured for the three sand-types using van Ganuchten model $\beta = 10$

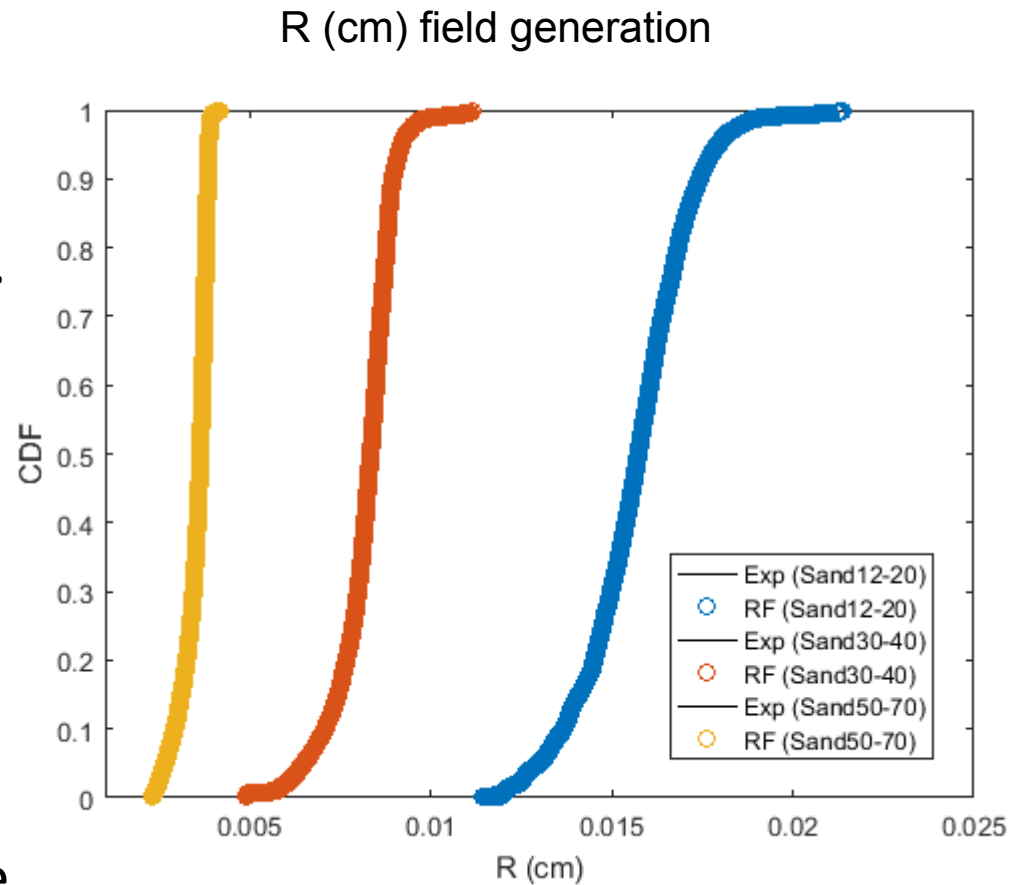


Overview of Model - Permeability

- Take provided radius field (r_p) generated from probability density function.
- Generate single-phase permeability using Carman-Kozeny relationship:

$$\kappa = \frac{a\phi^3 r_p^2}{4(1 - \phi)^2}$$

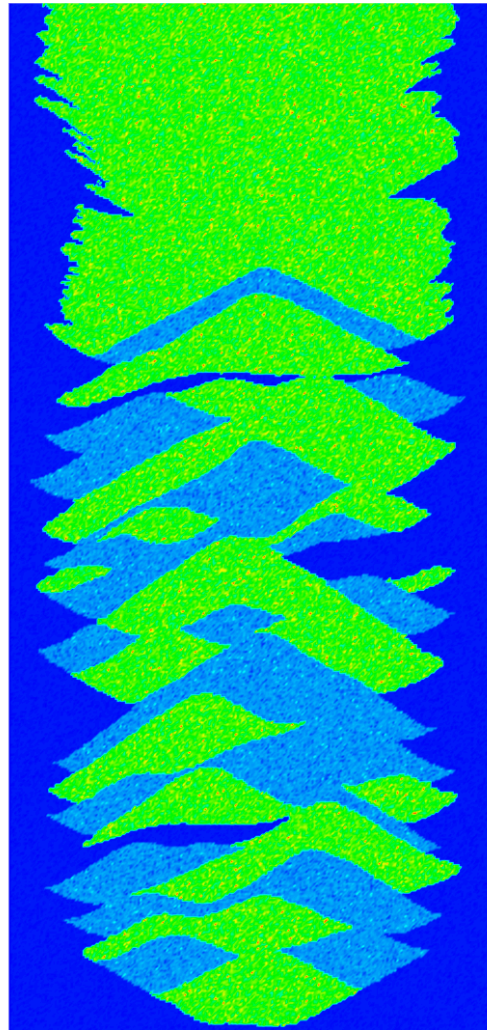
- Porosity based on sand-type
 $\phi \approx 0.35$ for all sands



Inverse transform sampling
from experimental data

Permeability and Pressure Fields

Permeability Field κ

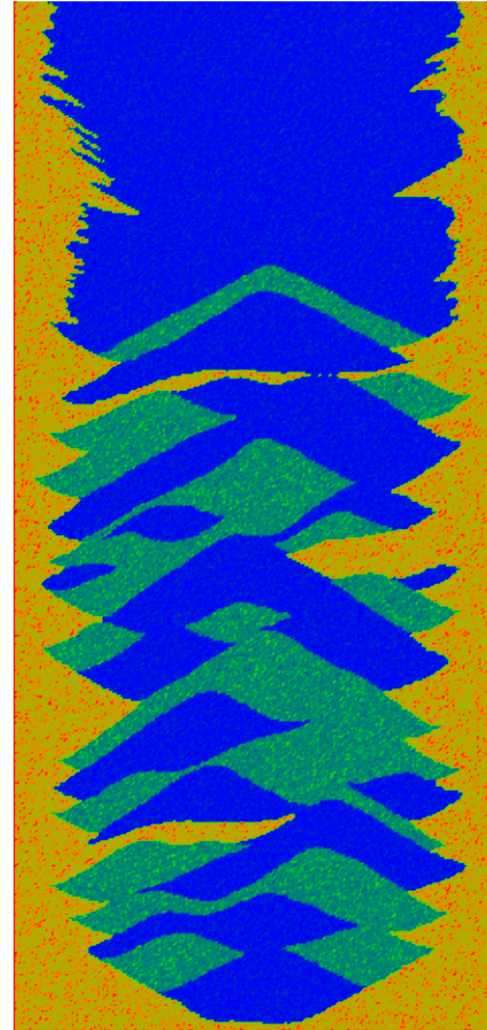


_PERM

5.646e-11
4.238e-11
2.830e-11
1.422e-11
1.453e-13



Capillary Pressure Field p_{c0}

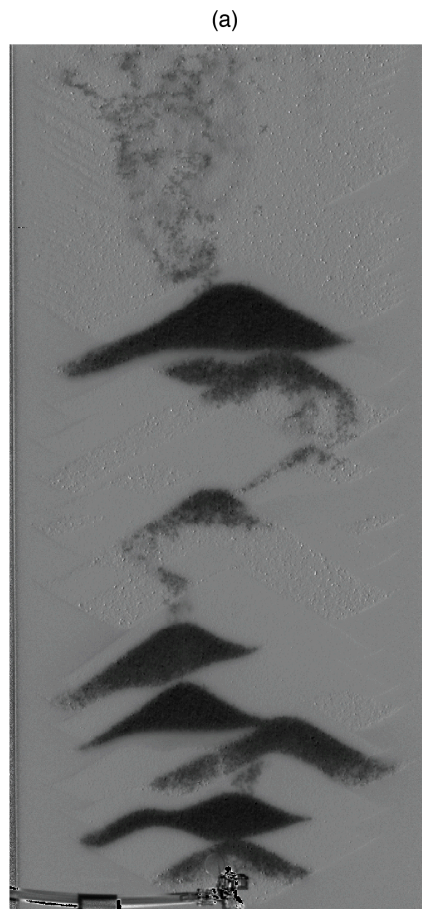


PCREF_VG

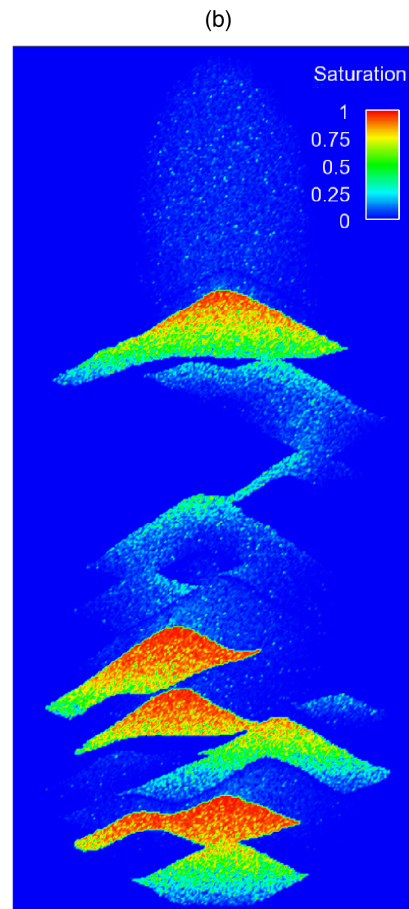
5.897e+03
4.611e+03
3.325e+03
2.039e+03
7.524e+02



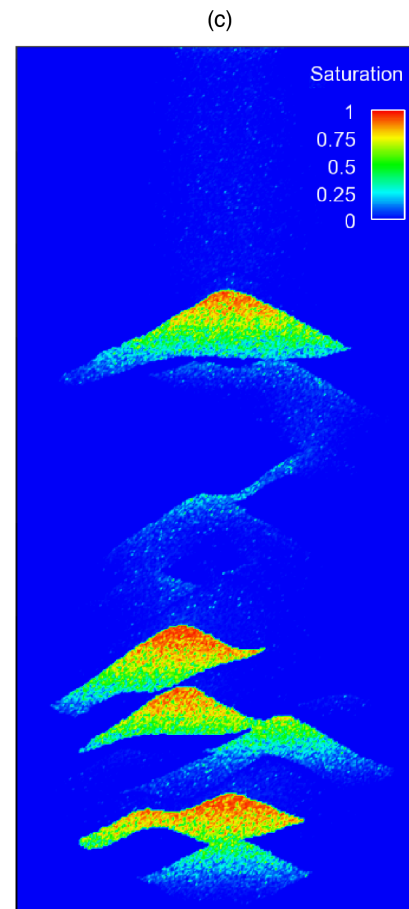
Results – Saturation Profiles (Aria)



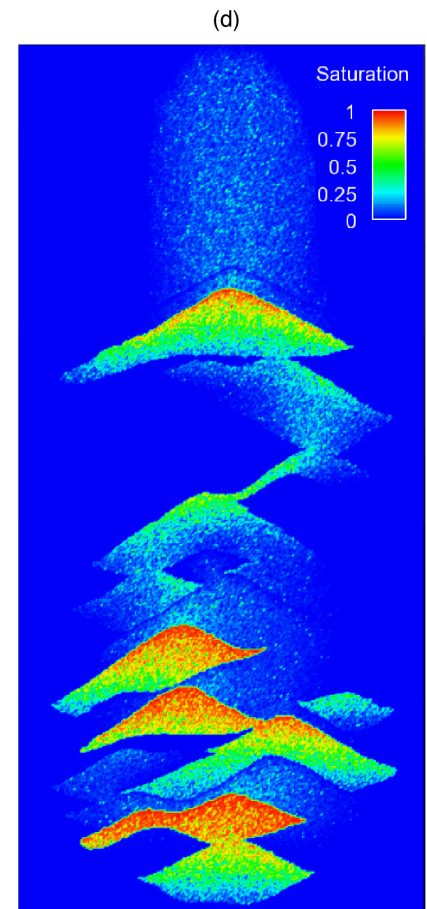
Flow Rate = 1.2 mL/min
Break through time = 42.3 min
Break through vol = 50.8 mL



Flow Rate = 1.0 mL/min
Break through time = 46.4 min
Break through vol = 46.4 mL



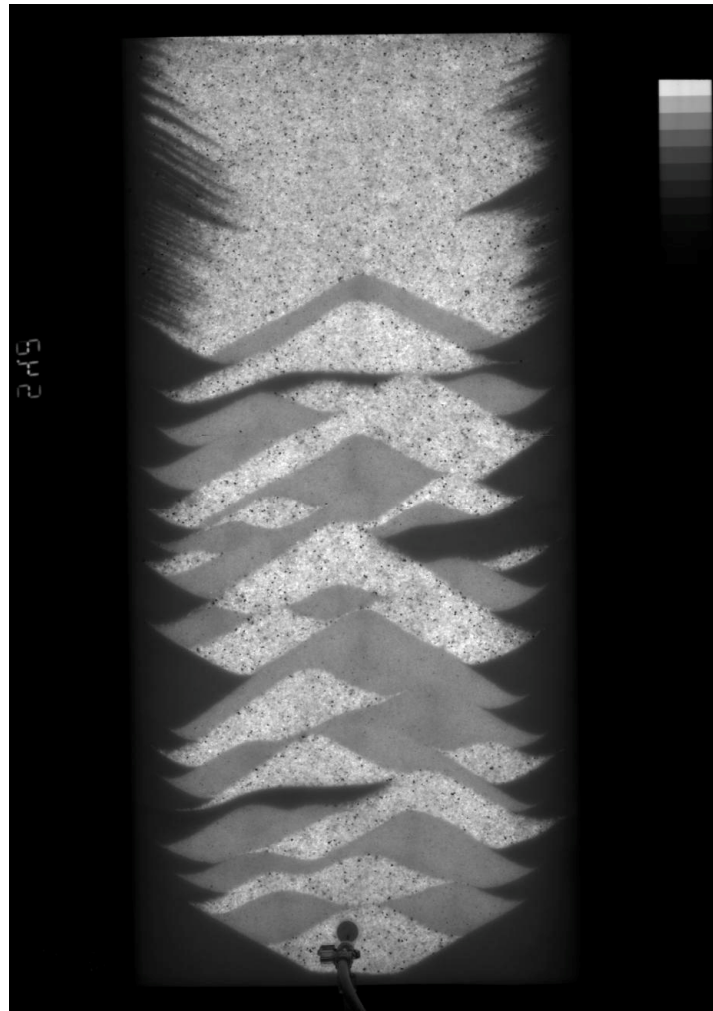
Flow Rate = 0.1 mL/min
Break through time = 296 min
Break through vol = 29.6 mL



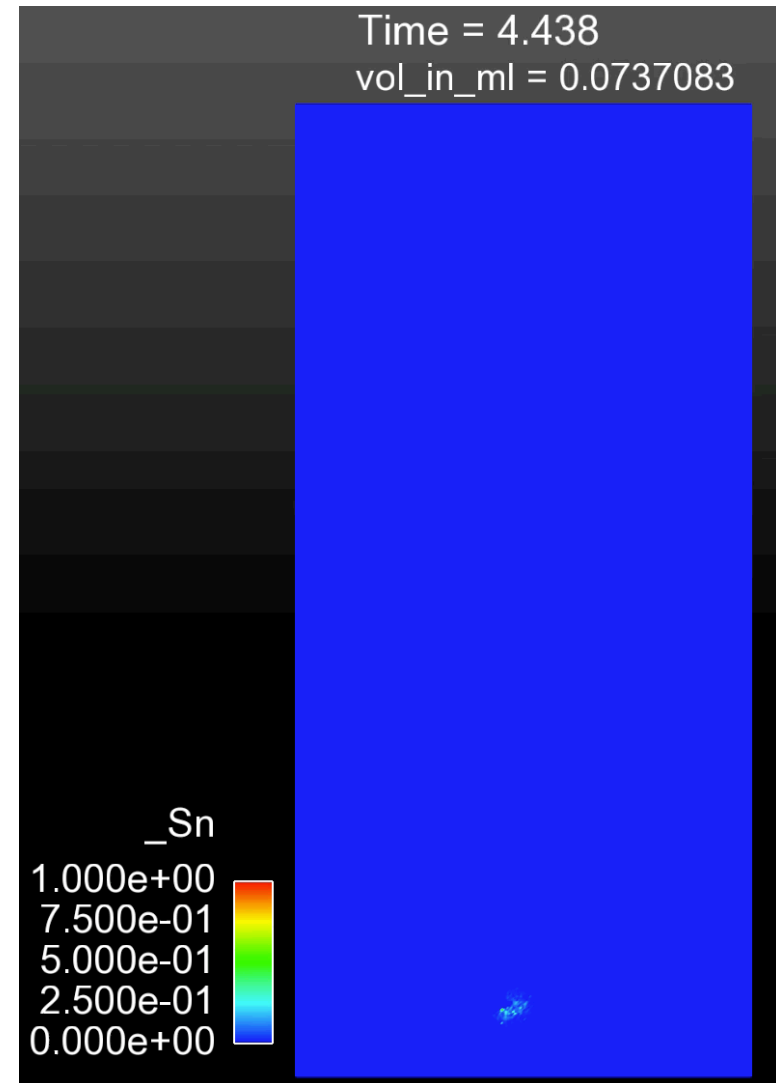
Flow Rate = 5.0 mL/min
Break through time = 10.1 min
Break through vol = 50.5 mL

Results – Saturation Profiles (cont.)

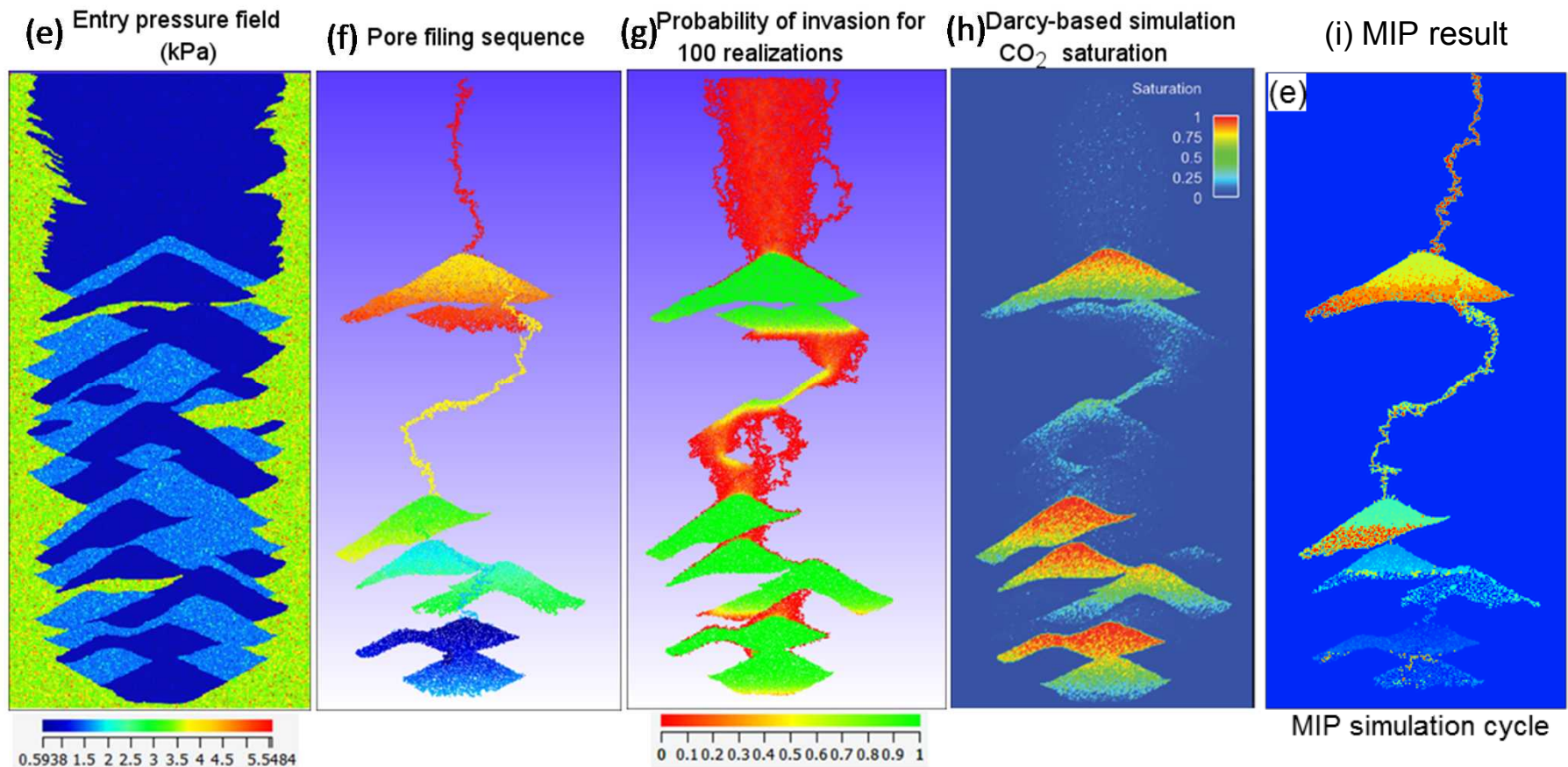
Experiment



Simulation (Aria)



Results – IP Simulations



(e) Entry pressure (kPa) field for invasion percolation models corresponding to sand packing architecture shown in (a). A total of 100 realizations are employed. (f) Invasion (pore filling) percolation result in one realization. Cool and hot colors are early and late filling order, respectively. (g) Probability of invasion per each pixel for 100 realizations. (h) CO₂ saturation based on Darcy-based continuum model in the random field domain in (e), (i) Modified invasion percolation cycle with cold color for early and warm color for late filling cycles.

Summary & Conclusions

- Modeled the heterogeneous sandbox experiments of Bob Glass
 - Darcy Flow
 - Aria
 - PFLOTTRAN
 - Invasion Percolation (IP)
- Good agreement with experiment
 - Breakthrough times
 - Saturation profiles
 - Plume at top of sandbox