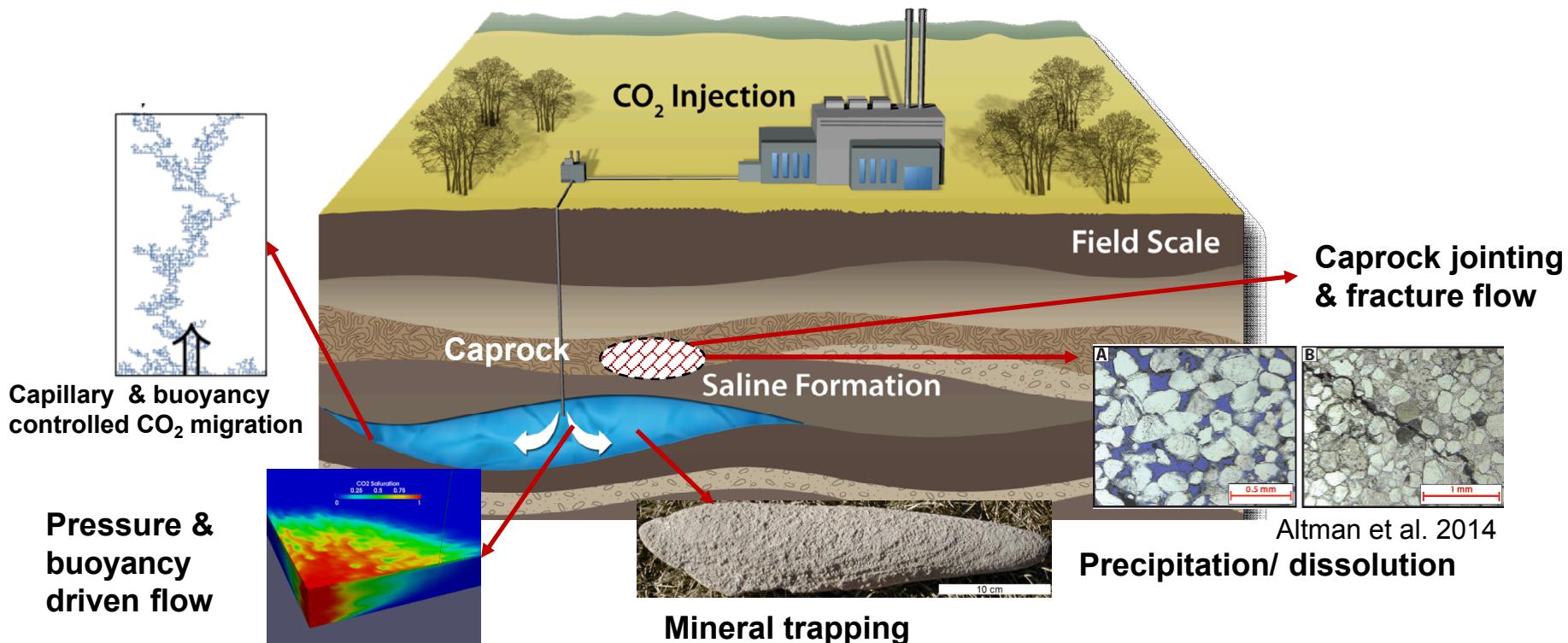


Benchmark: Modeling CO₂ gas flow in a heterogeneous sand architecture

Alec Kucala, Mario Martinez, and Hongkyu Yoon
CFSES Challenge Meeting- Sept 27, 2017

CO₂ Flow and Transport Processes during Geological Carbon Storage

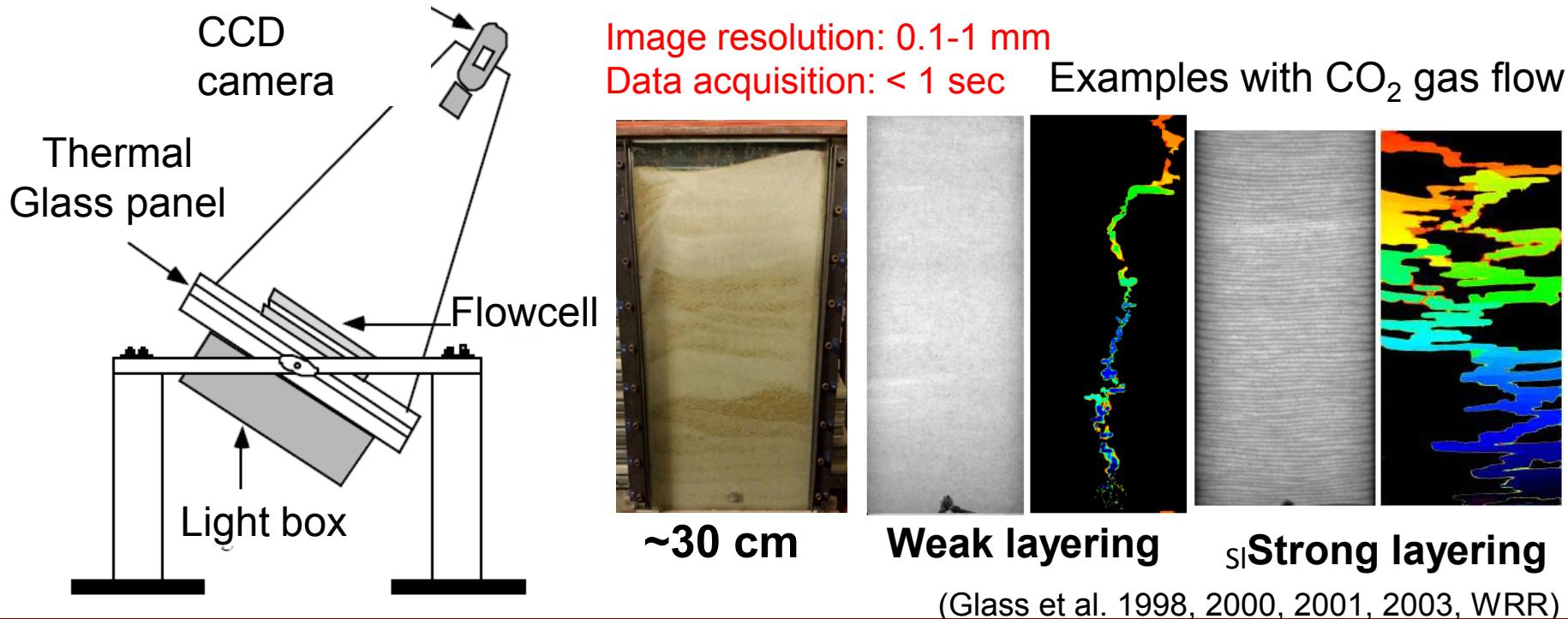


- **Sustaining large storage rates**, of order gigatons of CO₂ per year in the US, for decades without compromising other subsurface resources and without jeopardizing the security with which the CO₂ is stored;
- **Using pore space with unprecedented efficiency**, i.e., placing CO₂ so that it occupies half of the reservoir volume, rather than the typical current estimate of less than five percent;

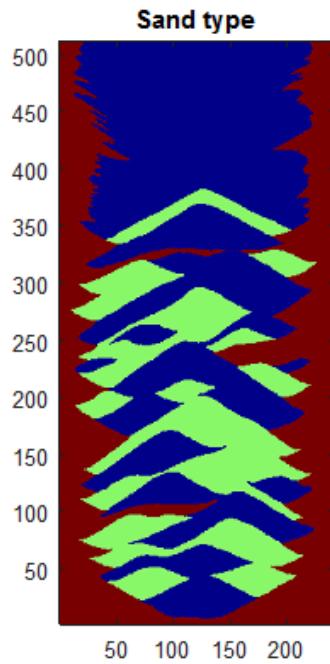
Intermediate scale experiment

1. to understand and quantify the physics of the transition from compact flow to capillary channel flow (coupled with core-scale experiments)
2. to develop new experimental-informed, physics-based models of this transition process, focused on representing cm-scale heterogeneity, with the goal of developing constitutive models suitable for reservoir-scale simulators

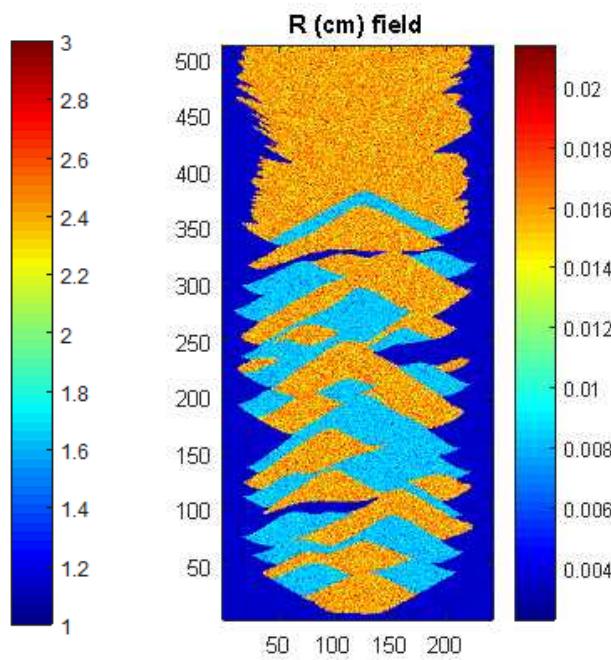
Light transmission system



Overview Bob Glass Experiments



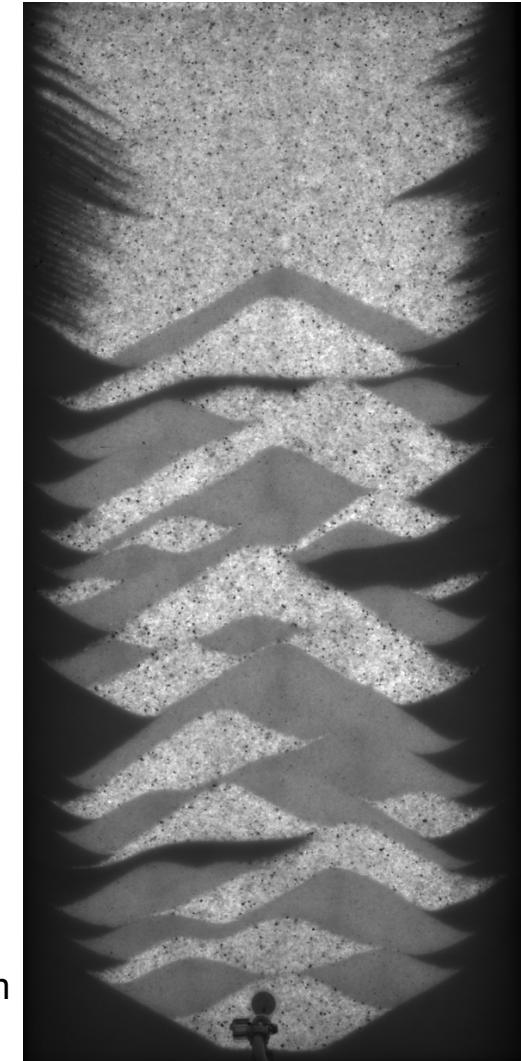
Sand 1: Accusand 12-20
Sand 2: Accusand 30-40
Sand 3: Accusand 50-70



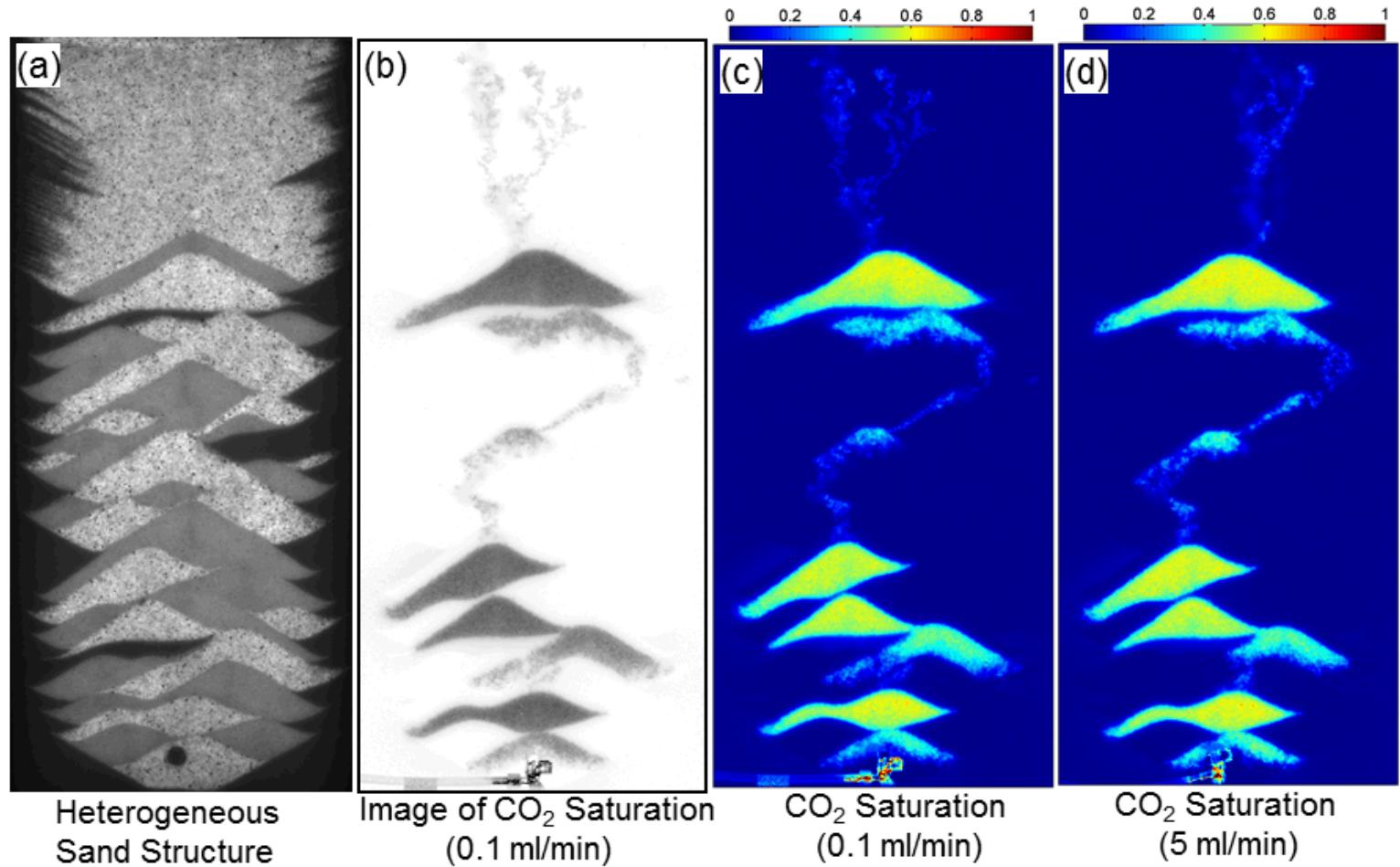
Grid: 240 x 511 ($dx=dy=0.1087\text{cm}$)
Origin: lower left corner in figures

Dimension: 26.088cm x 55.55cm x 1cm
Injection hole: Diameter=11 pixels at (110.5, 35.5) in [240 x 511] grid system
Injection rates: 0.1, 0.5, 1, 2, 5 mL/min

Experimental image



Experimental Data Analysis



(a) Experimental heterogeneous sand structure (26 cm wide, 55.5 cm tall) of Glass et al. showing the fine sand (dark, #50-70), medium sand (gray, #30-40), and coarse sand (light, 12-20) units.

(b) CO_2 saturation image at a CO_2 gas injection rate of 0.1 ml/min.

(c-d) Experimental CO_2 saturations just after CO_2 gas reached the top of the chamber at 0.1 mL/min and 5 ml/min, respectively.

Overview of Model – Aria

- Solve Darcy equations for two-phase immiscible fluid flow using thermal/fluids finite-element code Aria (SNL code)

$$\frac{\partial}{\partial t}(\rho_w \phi(1 - S_n)) = \nabla \cdot \left(\rho_w \frac{k_{rw}}{\mu_w} \mathbf{K} \cdot (\nabla p - \rho_w \mathbf{g}) \right) + Q_w$$

$$\frac{\partial}{\partial t}(\rho_n \phi S_n) = \nabla \cdot \left(\rho_n \frac{k_{rn}}{\mu_n} \mathbf{K} \cdot (\nabla p + \nabla p_c - \rho_n \mathbf{g}) \right) + Q_n$$

$$p_c = p_n - p_w$$

$$S_w + S_n = 1$$

Overview of Model – Aria (cont.)

- Capillary Pressure use van Genuchten function:

$$p_c = p_{c0} (s^{-\frac{1}{\lambda}} - 1)^{\frac{1}{\beta}}$$

$$\lambda = 1 - \frac{1}{\beta} \quad , \quad \beta > 1$$

$$s = (S_w - S_{w,r}) / ((1 - S_{nw,r}) - S_{w,r})$$

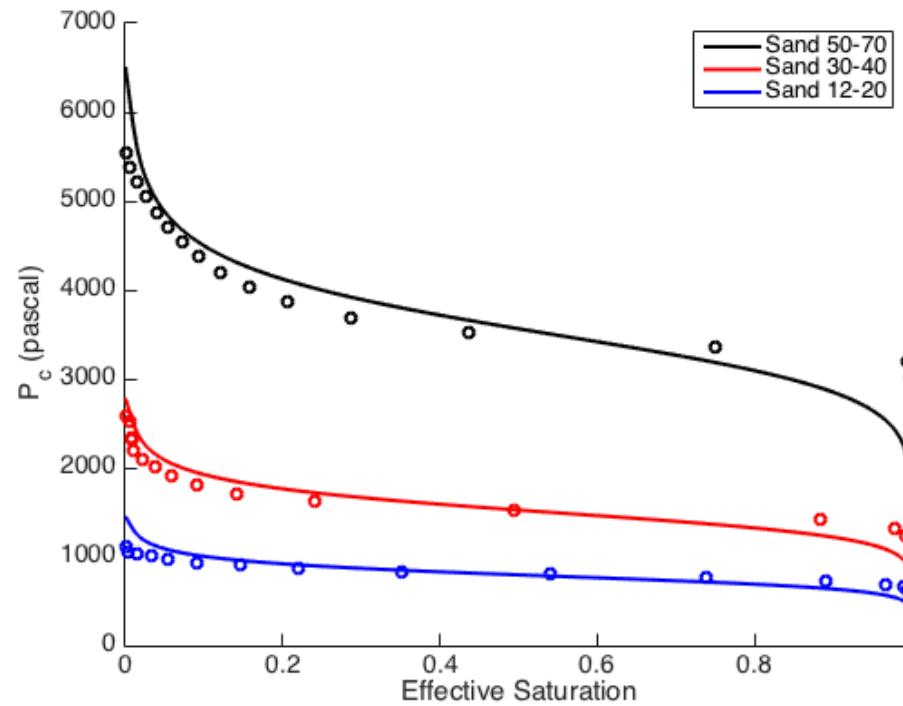
- Relative perm use van Genuchten function:

$$k_{rl} = \sqrt{s} \left[1 - \left(1 - s^{\frac{1}{\lambda}} \right)^{\lambda} \right]^2$$

$$k_{rg} = \sqrt{1 - s} \left[1 - s^{\frac{1}{\lambda}} \right]^{2\lambda}$$

Capillary Pressure Curves

- Fit data to provided capillary pressure curves measured for the three sand-types using van Ganuchten model $\beta = 10$

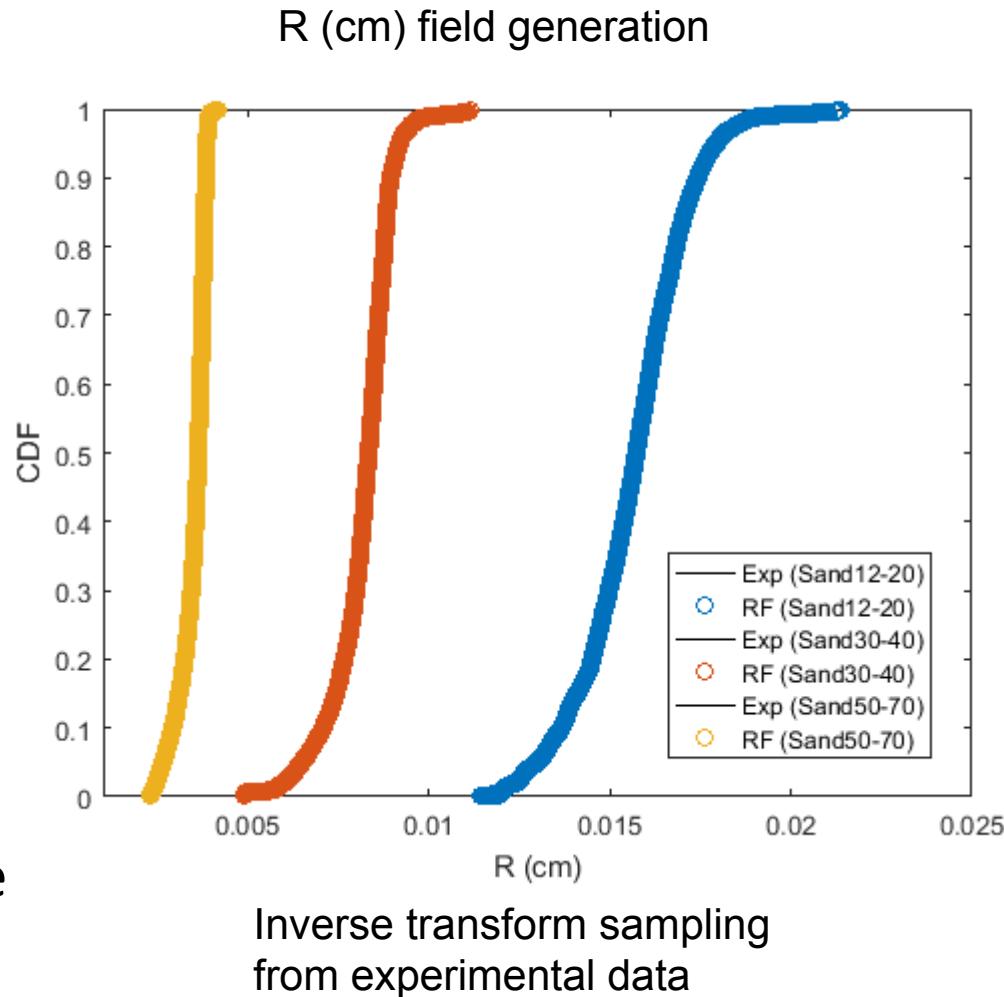


Overview of Model - Permeability

- Take provided radius field (r_p) generated from probability density function.
- Generate single-phase permeability using Carman-Kozeny relationship:

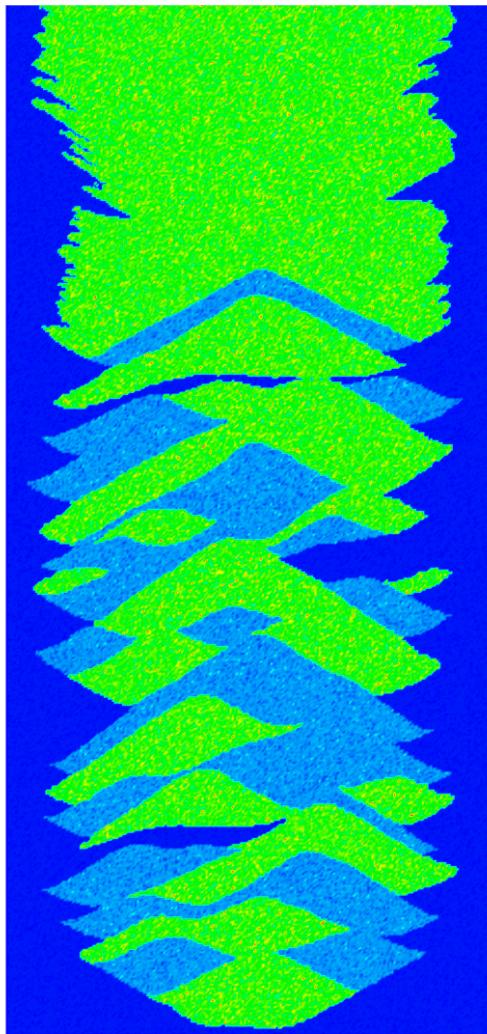
$$\kappa = \frac{a\phi^3 r_p^2}{4(1-\phi)^2}$$

- Porosity based on sand-type $\phi \approx 0.35$ for all sands

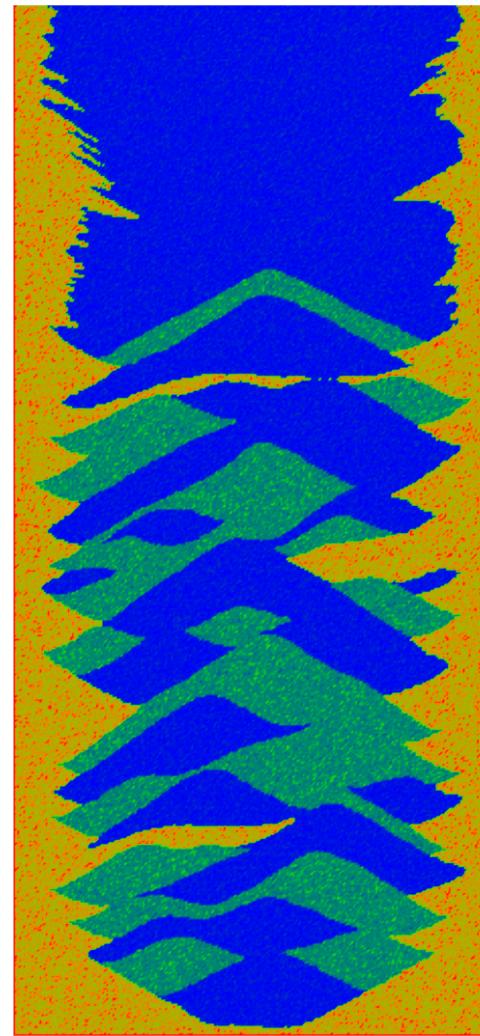


Permeability and Pressure Fields

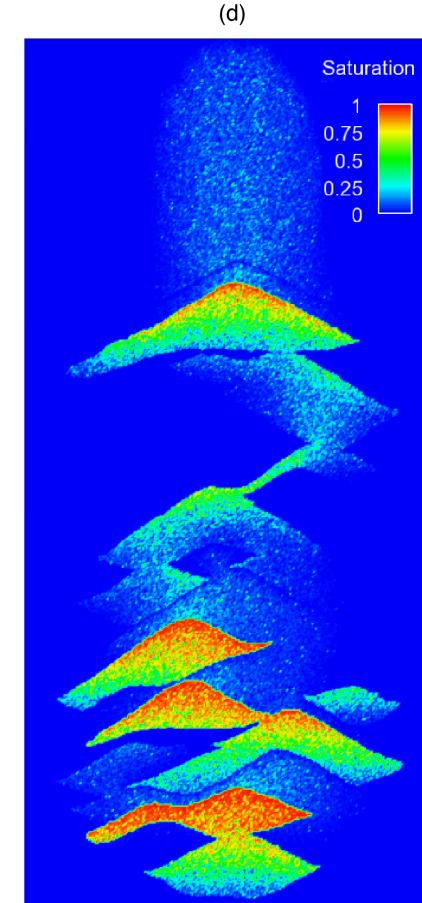
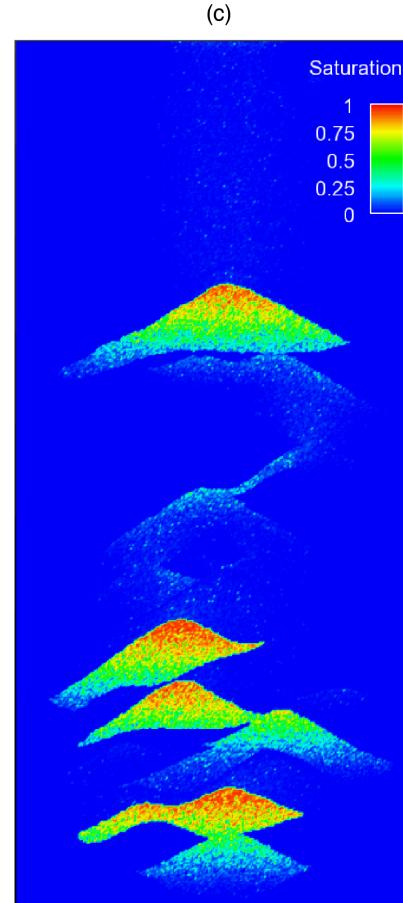
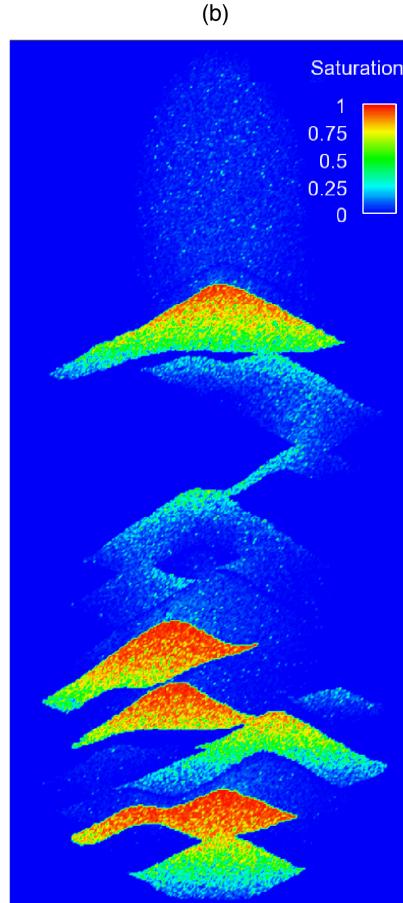
Permeability Field κ



Capillary Pressure Field p_{c0}



Results – Saturation Profiles (Aria)



Flow Rate = 1.2 mL/min
Break through time = 42.3 min
Break through vol = 50.8 mL

Flow Rate = 1.0 mL/min
Break through time = 46.4 min
Break through vol = 46.4 mL

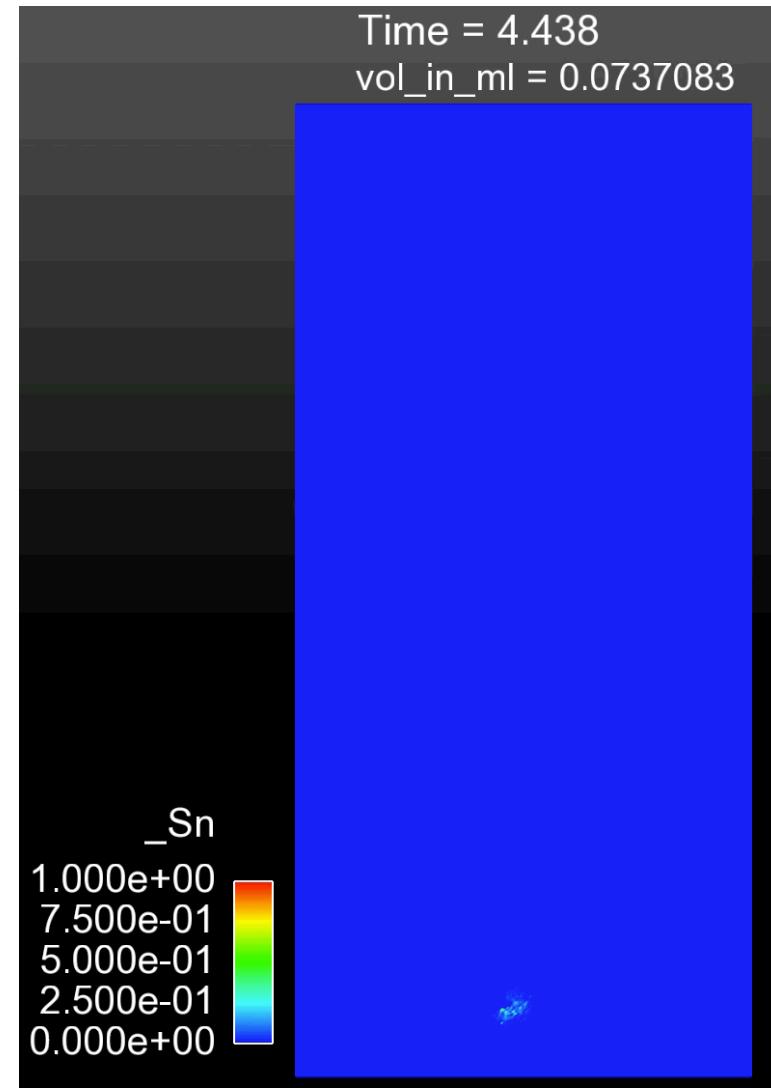
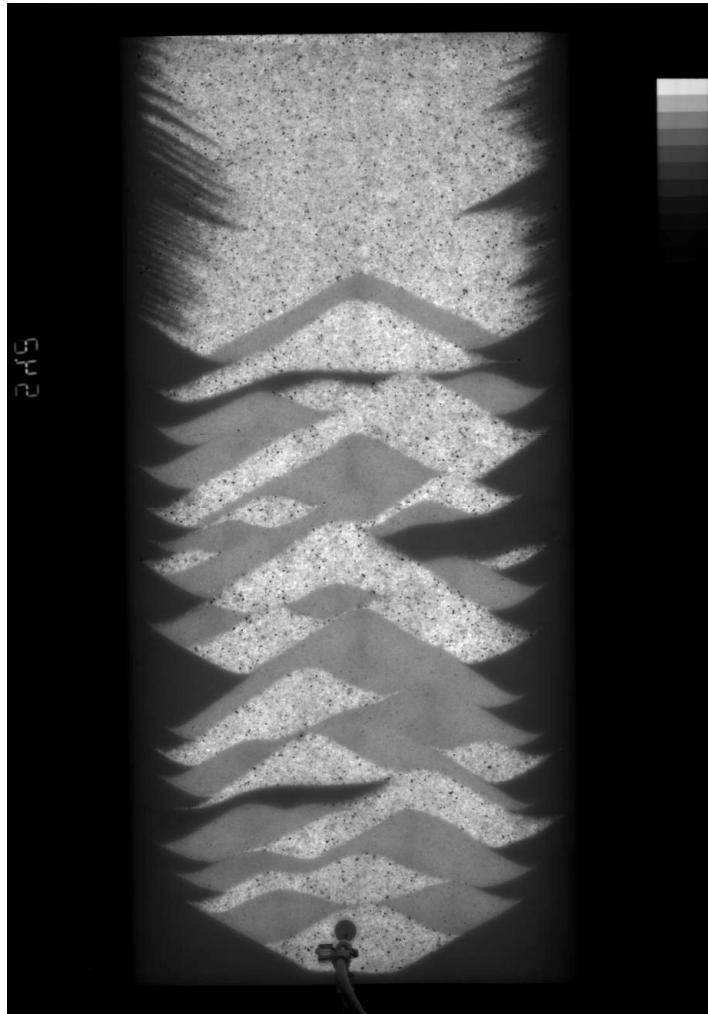
Flow Rate = 0.1 mL/min
Break through time = 296 min
Break through vol = 29.6 mL

Flow Rate = 5.0 mL/min
Break through time = 10.1 min
Break through vol = 50.5 mL

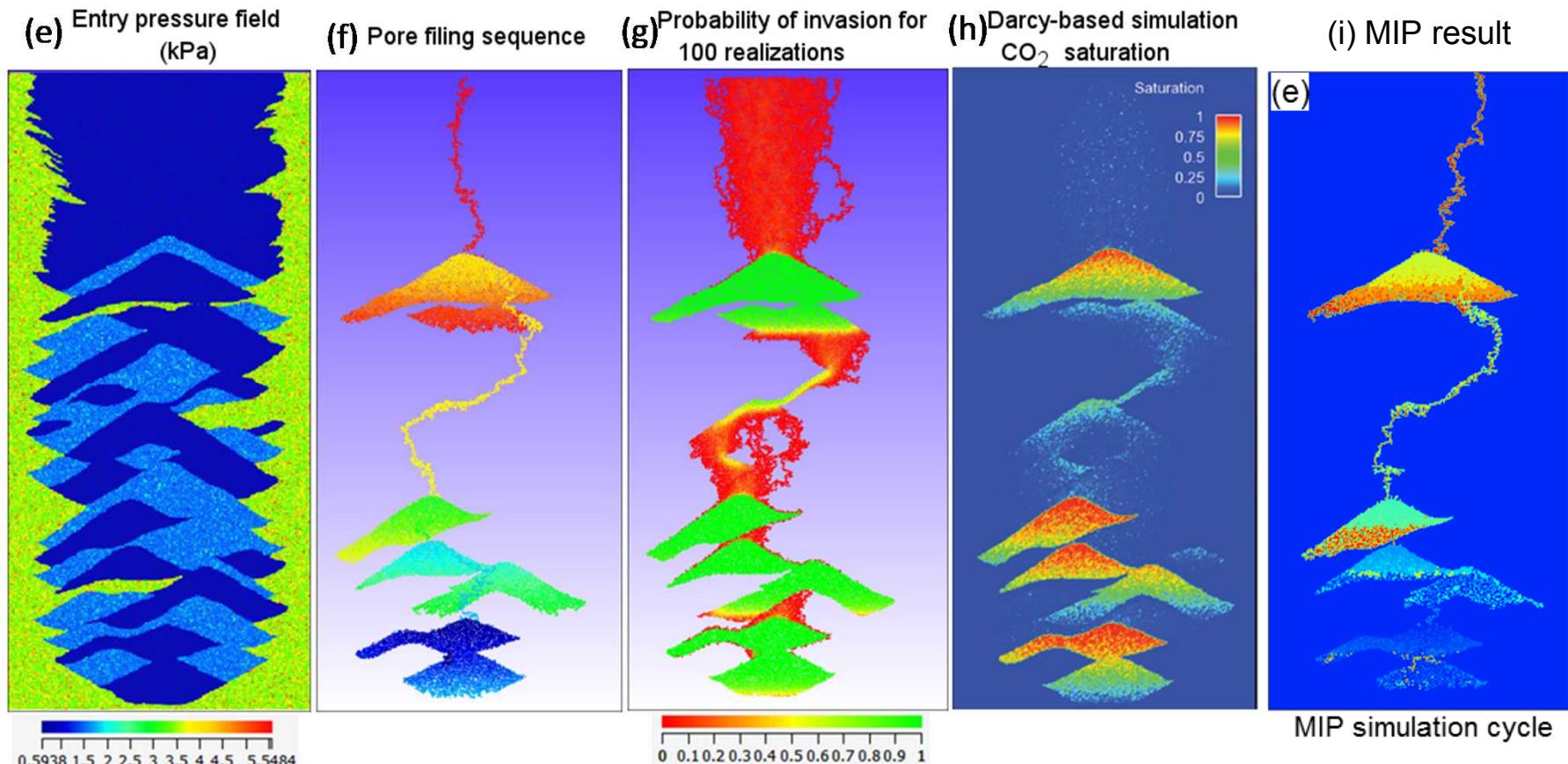
Results – Saturation Profiles (cont.)

Simulation (Aria)

Experiment



Results – IP Simulations



(e) Entry pressure (kPa) field for invasion percolation models corresponding to sand packing architecture shown in (a). A total of 100 realizations are employed. (f) Invasion (pore filling) percolation result in one realization. Cool and hot colors are early and late filling order, respectively. (g) Probability of invasion per each pixel for 100 realizations. (h) CO_2 saturation based on Darcy-based continuum model in the random field domain in (e), (i) Modified invasion percolation cycle with cold color for early and warm color for late filling cycles.

Summary & Conclusions

- Modeled the heterogeneous sandbox experiments of Bob Glass
 - Darcy Flow
 - Aria
 - PFLOTRAN
 - Invasion Percolation (IP)
- Good agreement with experiment
 - Breakthrough times
 - Saturation profiles
 - Plume at top of sandbox