

Compact Model of Resistive Memory Devices for Pulsed Analog and Neuromorphic Applications

John Niroula*, Sapan Agarwal, Robin Jacobs-Gedrim, David Hughart, Alex Hsia, Conrad D. James, Matthew J. Marinella**

Abstract

Resistive switching devices are promising candidates for next generation computer hardware, with the ever increasing need for more efficient, faster computation. These devices show particular promise for use in a neuromorphic accelerator as they can be tuned to multiple resistance states which can be a hardware equivalent to the weights in neuromorphic algorithms. Modeling a ReRAM-based neuromorphic accelerator requires a compact model capable of correctly simulating the small weight update behavior associated with neuromorphic training. Here, we propose an empirically derived general purpose state-conductance model that can accurately capture the nonlinearity of an arbitrary two terminal device to match pulse measurements important for neuromorphic applications.

Hardware Based Deep Learning Overview

Mathematical

$$\begin{bmatrix} V_1 & V_2 & V_3 \end{bmatrix} \begin{bmatrix} W_{1,1} & W_{1,2} & W_{1,3} \\ W_{2,1} & W_{2,2} & W_{2,3} \\ W_{3,1} & W_{3,2} & W_{3,3} \end{bmatrix} = \begin{bmatrix} I_1 & I_2 & I_3 \end{bmatrix}$$

$$I_1 = \sum V_{i,1} W_{i,1} \quad I_2 = \sum V_{i,2} W_{i,2} \quad I_3 = \sum V_{i,3} W_{i,3}$$

Electrical

Physical

- Deep Learning provides solutions but currently requires MWs of power.
- Analog accelerators may offer $\sim 10^5$ times less power
- Matrix vector multiplication is most computationally expensive process

"Let physics do the computation"

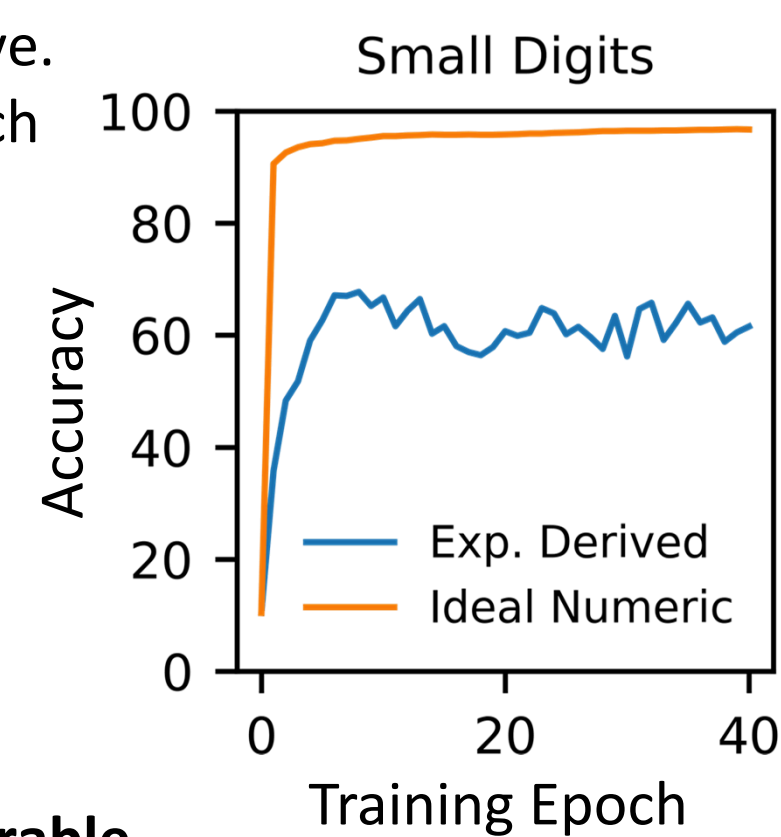
Compact Model Basics

- However we need to be able to model devices for circuit design and simulation
- Model must be accurate, fast, and intuitive.
- Standard state variable modeling approach

$$I = G(x) \times h(V)$$

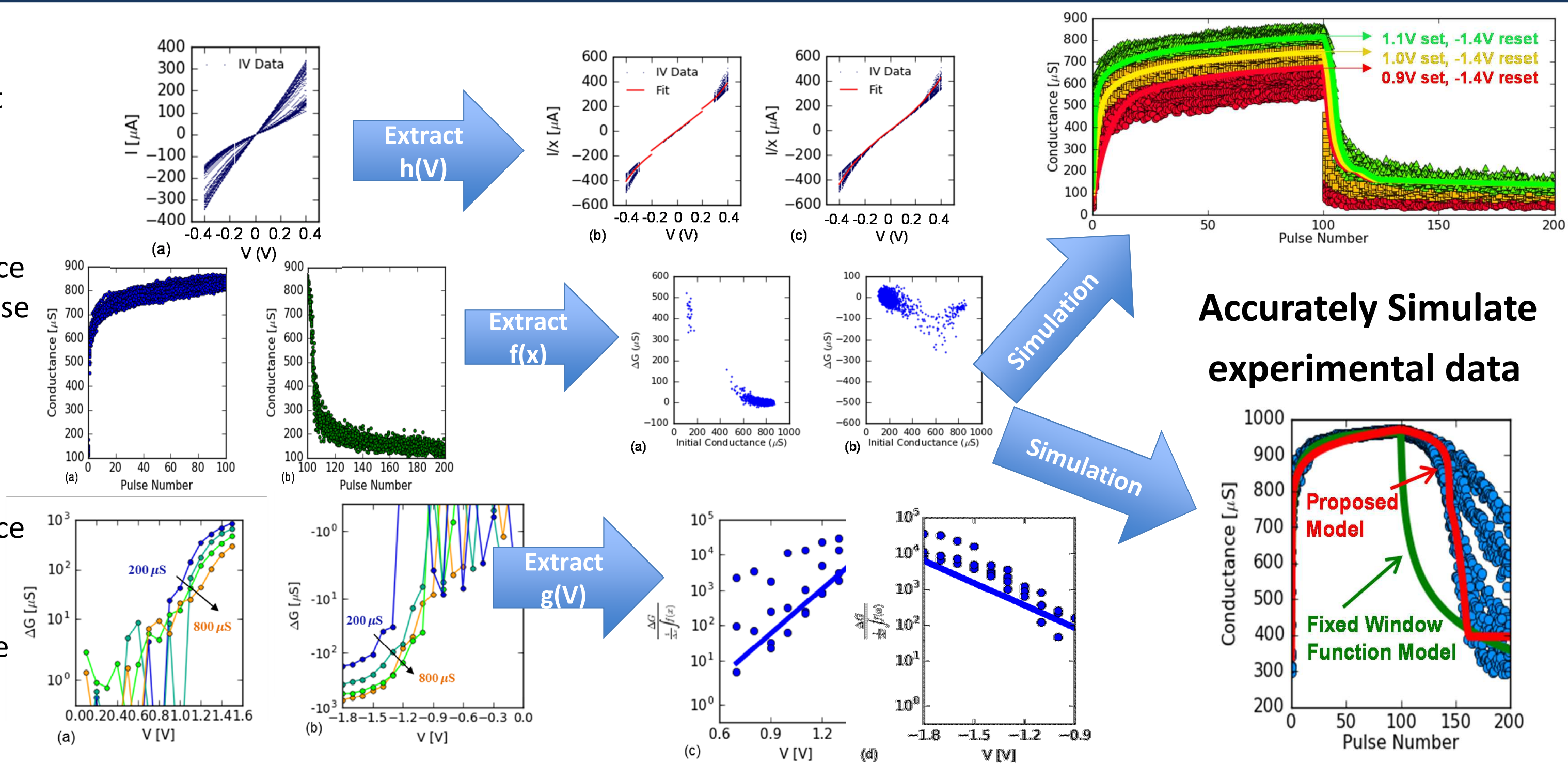
$$\frac{dx}{dt} = C \times f(x) \times g(V)$$

- Where $G(x) = x = \frac{G}{G_{max}}$ is normalized conductance
- This allows us to experimentally obtain $f(x)$ and $g(V)$
- $f(x) \times g(V) = \frac{dx}{dt} \approx \frac{\Delta x}{\Delta t} = \frac{\frac{\Delta G}{G_{max}}}{\Delta t} \leftarrow \text{measurable}$



Parameter Extraction and Model Validation

- Measure static I-V at multiple states, achieved through pulses
- Measure conductance changes through pulse train sequence with fixed voltage pulse height
- Measure conductance change at fixed conductance by varying voltage pulse heights



Conclusion

A compact model that accurately simulates the pulsed conductance changes in a two terminal resistive switching device has been presented. The key improvement of this compared to prior models is the capability to model arbitrary ΔG - G behavior, which is a requirement for correctly modelling training in a neuromorphic accelerator. This model is compatible with any two terminal resistance switching device that has separable static and dynamic equations and is operated in the regime controlled by a single state variable. Parameter extraction on a Sandia Ta/TaO_x ReRAM demonstrates the capability of this model to correctly predict conductance-pulse behavior.

Acknowledgements

The authors would like to acknowledge Michael Van Heukelom and Steven DiGregorio for measurement help and Jim Stevens for device fabrication. This work was supported by Sandia National Laboratories Hardware Acceleration of Adaptive Neural Networks (HAANA) Grand Challenge Laboratory Directed Research and Development (LDRD) project.

